



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION



INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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WINTER COLLEGE ON LASERS, ATOMIC AND MOLECULAR PHYSICS

(24 January - 25 March 1983)

CARS Spectroscopy

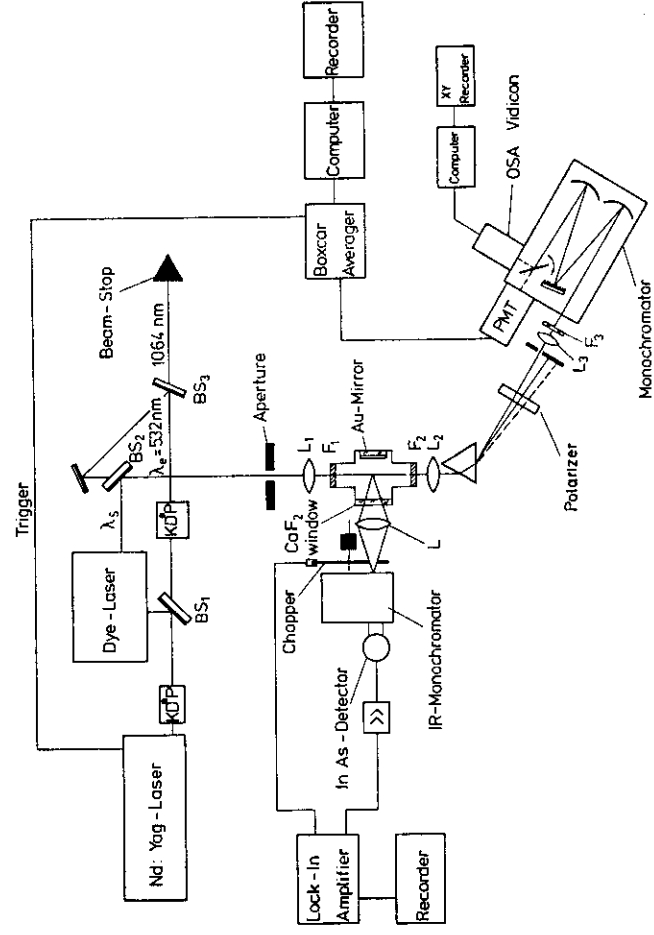
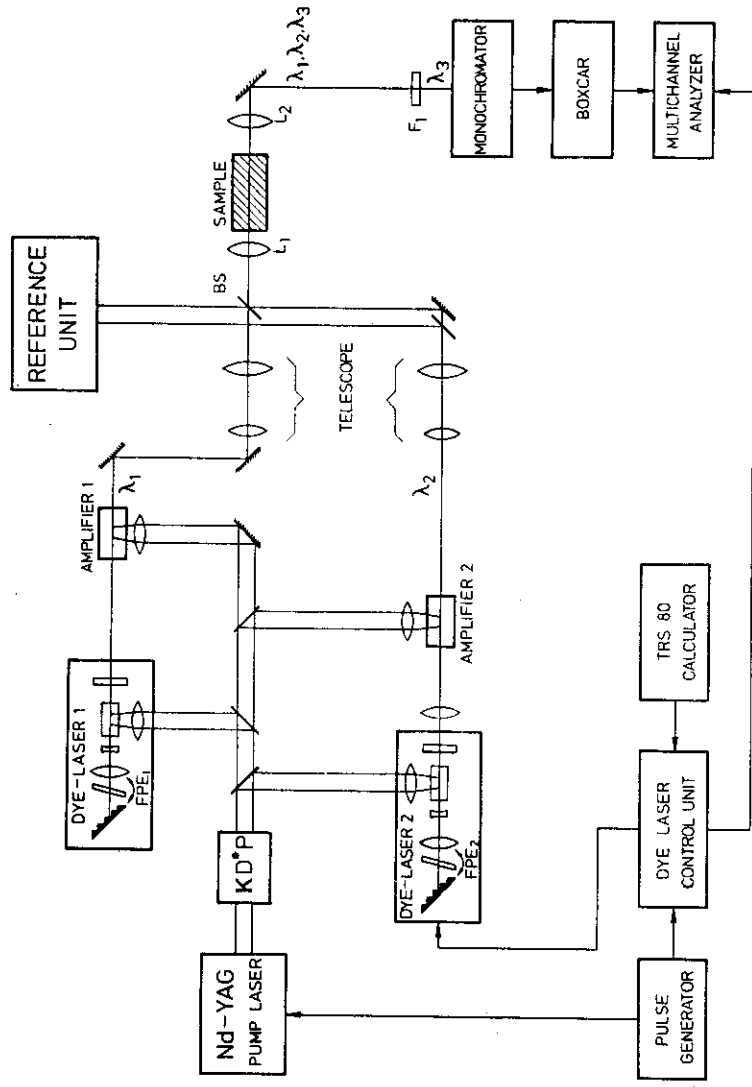
Part II

- a) Lasers for CARS
- b) Electronic Enhancement of CARS-Spectra

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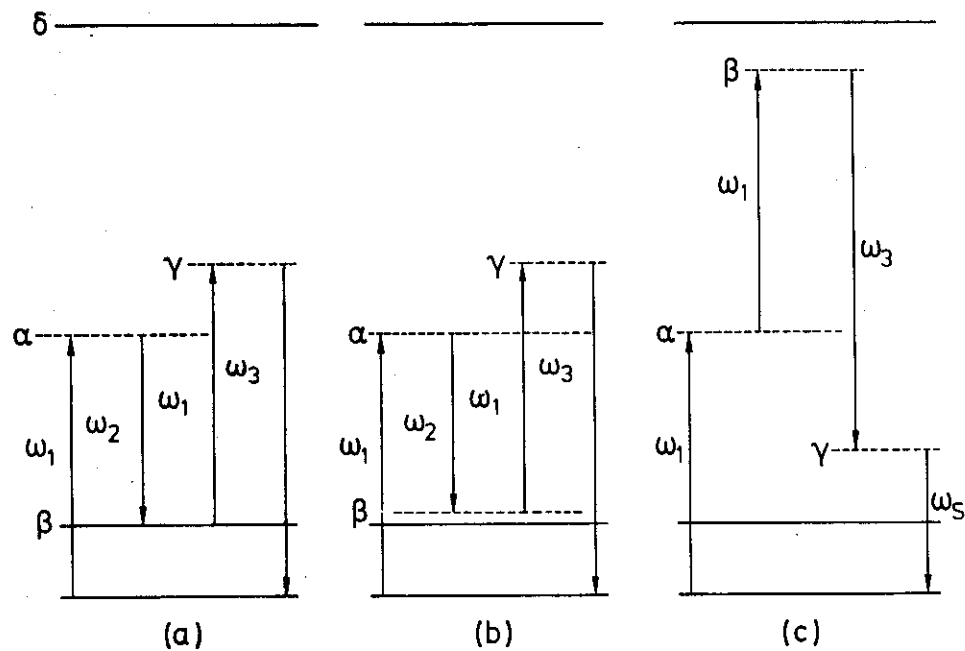
These are preliminary lecture notes, intended only for distribution to participants
Missing or extra copies are available from Room 230.



III/1)

III/2)

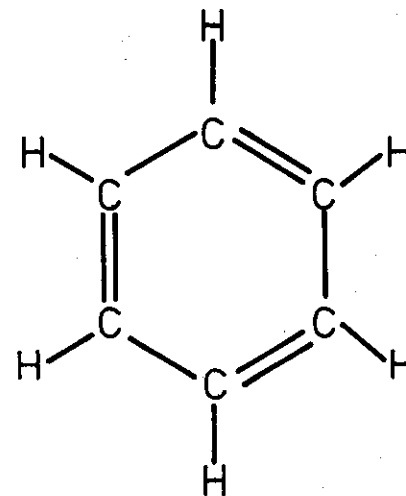
4



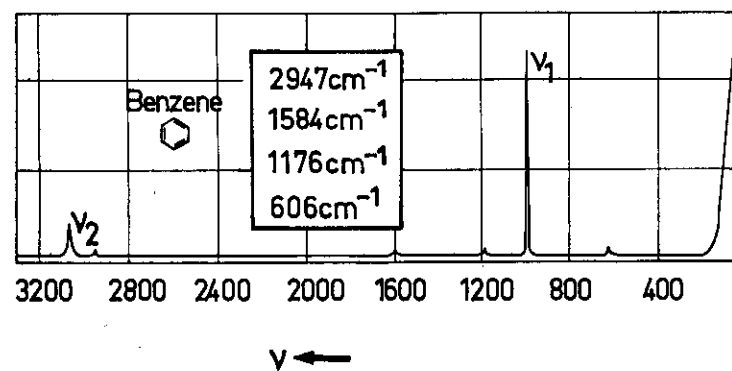
CARS-Type
Experiments

2-Photon-Type
Experiments

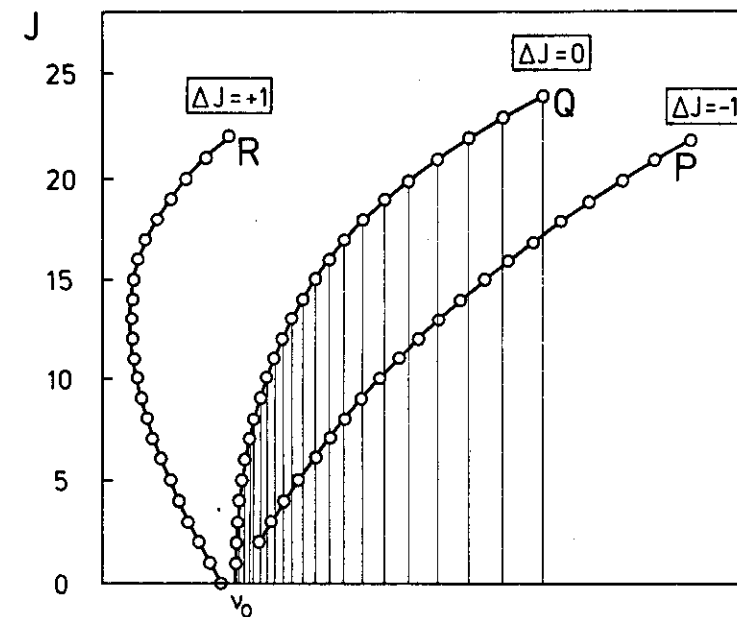
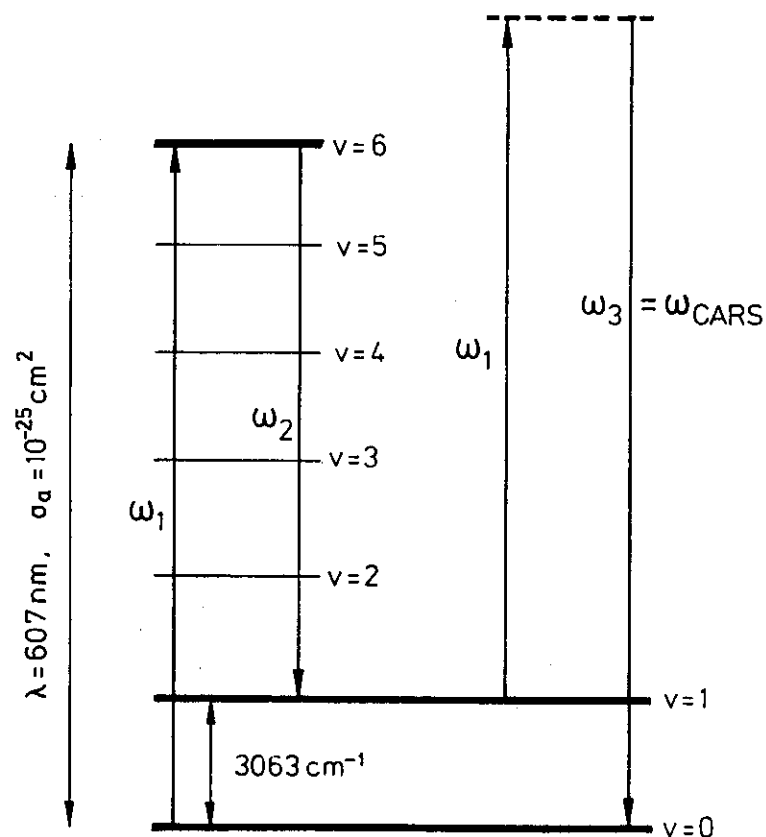
Benzene:
 ν_1 - mode
 ν_2 - mode



$$\nu_1 = 992 \text{ cm}^{-1} ; \quad \nu_2 = 3063 \text{ cm}^{-1}$$



607nm Resonance



Fortrat — Diagramm

III/4

7

IV/1

5

R.T. Lynch et al. Opt Comm. 16 (1976), 372

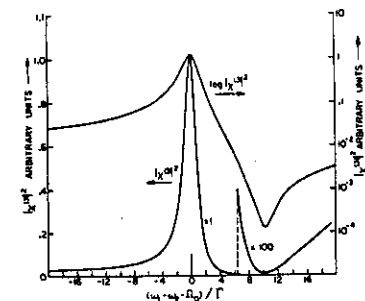
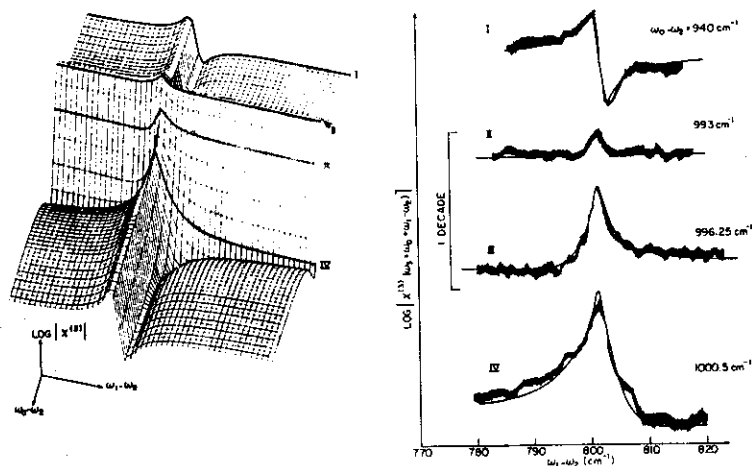


Fig. 7.4. The CARS line shape of (7.60) for $N(\omega_{pp})^2/4\hbar\Omega_p\Omega_s = 10^4$ on linear and logarithmic scales. This plot corresponds to the frequency dispersion of $|\chi^{(3)}|^2$. The deep minimum occurs when the non-resonant background is cancelled by the real part of the resonant Raman susceptibility

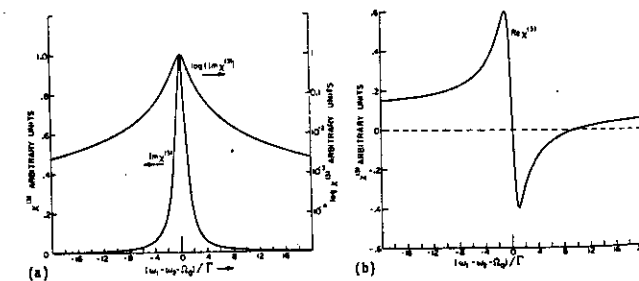


Fig. 7.5a, b. The real and imaginary parts of the Lorentzian resonance responsible for the CARS line shape in Fig. 7.4. Part (a) shows $\text{Im}(\chi^{(3)})$ on linear and logarithmic scales while (b) gives $\text{Re}(\chi^{(3)})$

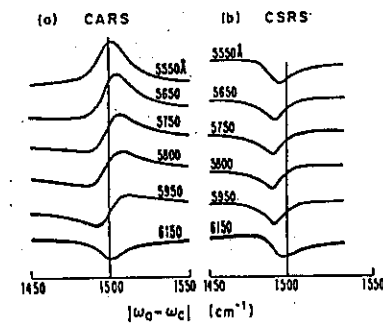
$$\chi^{(3)}(\omega_3 = \omega_0 + \omega_1 - \omega_2) = \chi_{NR}^{(3)} + \frac{A_M}{\Omega_M - \Omega_a - i\Gamma_M} + \frac{A_{M'}}{\Omega_M - \Omega_b - i\Gamma_{M'}}$$

$$\Omega_M = 992 \text{ cm}^{-1} \text{ (benzene)}$$

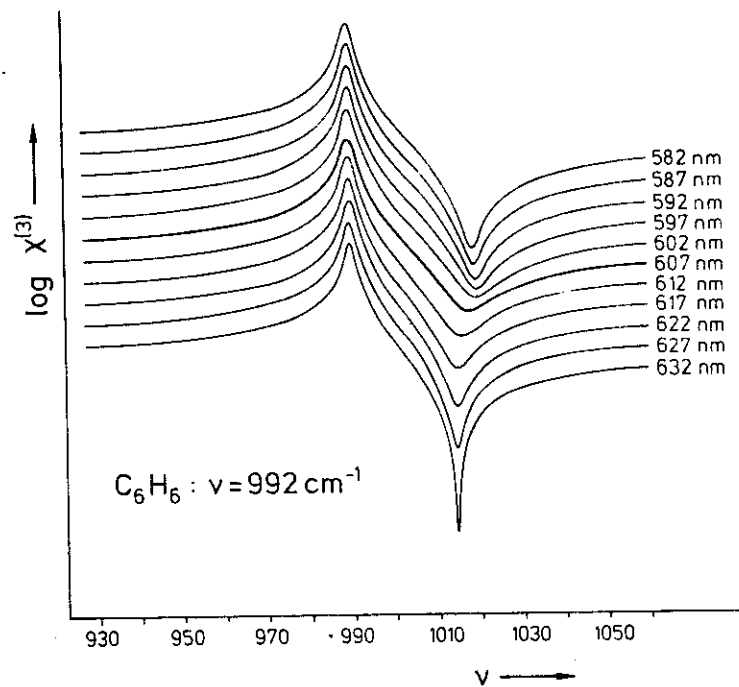
$$\Omega_M = 801 \text{ cm}^{-1} \text{ (cyclohexane)}$$

$$\Omega_a = \omega_0 - \omega_2$$

$$\Omega_b = \omega_1 - \omega_2$$



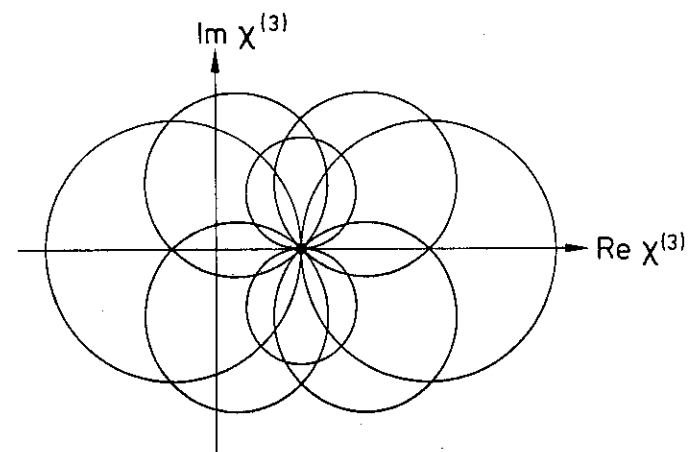
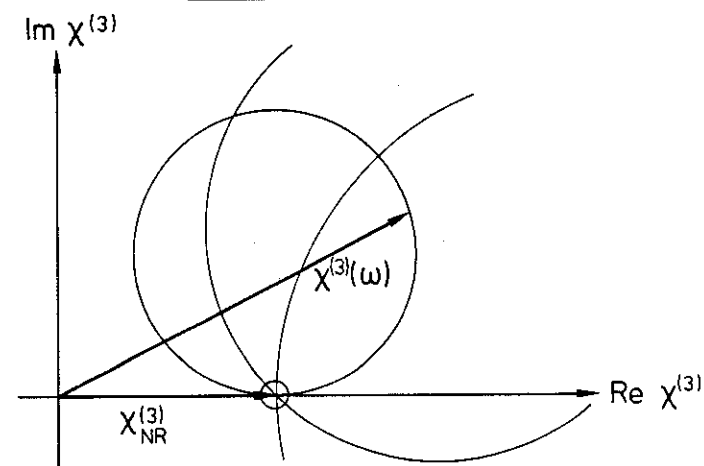
$\frac{\bar{\nu}}{2}$

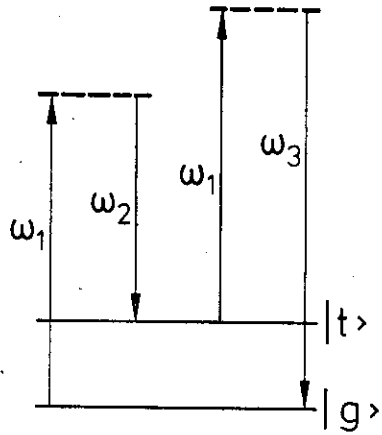


$$\chi^{(3)} = A \cdot \bar{\chi}^{(3)} + B \cdot \bar{\bar{\chi}}^{(3)}$$

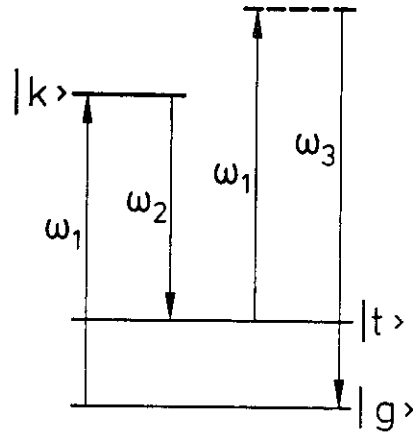
$(B \approx 0,02 A)$

$\chi^{(3)}$ -Geometrie

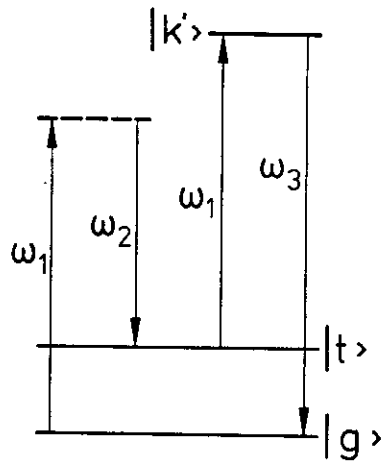




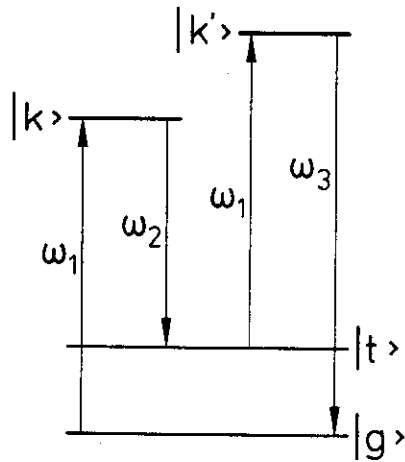
CARS



$$\omega_1 \equiv \omega_e^{kg}$$



$$\omega_3 \equiv \omega_e^{k'g}$$



$$\omega_1 \equiv \omega_e^{kg} \quad \omega_3 \equiv \omega_e^{k'g}$$

Theoretical Approach:
Perturbation Theory

$$\frac{\delta \rho}{\delta t} = -\frac{i}{\hbar} [H_0 + V, \rho] + \left. \frac{\delta \rho}{\delta t} \right|_{\text{damp}}$$

$$V = -\vec{\mu} \cdot \vec{E}(t)$$

$$P_{NL}^{(3)}(\omega_a, t) = N \sum_{m,n} \rho_{nm}^{(3)} \vec{\mu}_{mn}$$

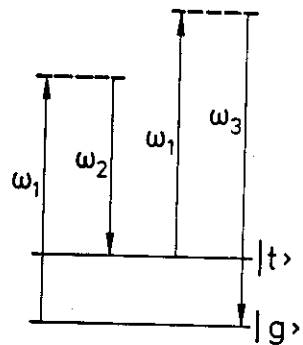
$$\rho_{nm}^{(3)} \sim [V(t)]^3 \text{ in } \omega_a$$

$$P_{NL}^{(3)}(\omega_a, t) = \chi^{(3)}(\omega_a) \cdot E_L^2 \cdot E_S^*$$

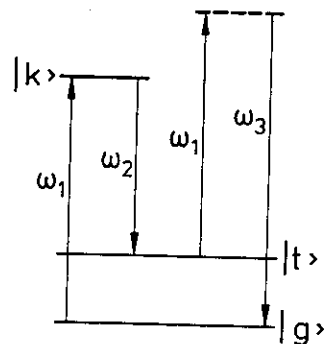
$$\times \exp \{ i(2k_L - k_S)z - \dots \} + c.c$$

$$\chi^{(3)}(\omega_a) \equiv \chi_{NR}^{(3)} + \sum_{a,b} \chi_R^{ab}$$

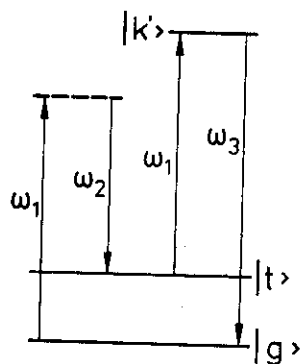
$\bar{V}/1$



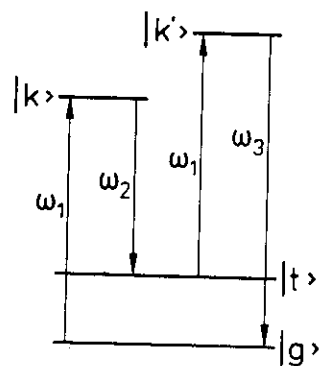
CARS



$$\omega_1 = \omega_e^{kg}$$



$$\omega_3 = \omega_e^{k'g}$$



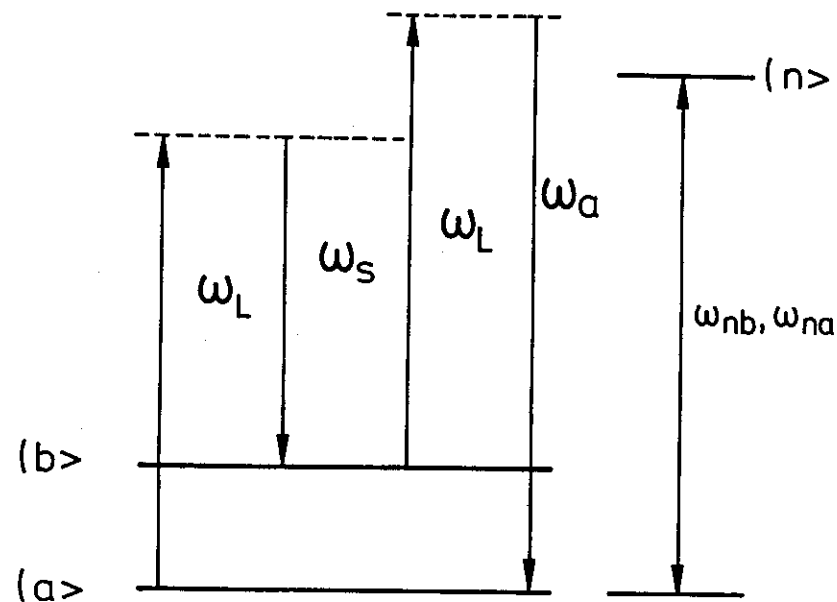
$$\omega_1 = \omega_e^{kg} \quad \omega_3 = \omega_e^{k'g}$$

(13)

$\bar{V}/2$

(1)

- 1 -



$$\chi_{\Sigma}^{(3)}(\omega_a) = \tilde{\chi}_{NR} + N \cdot \chi^{(3)}(\omega_a)$$

$$\chi^{(3)}(\omega_a) = \chi_{NR} + \sum_{a,b} \chi_R^{ab}$$

1/3

- 2 -

$$\begin{aligned} \chi_R^{ab} &= \frac{1}{3! \hbar^3} \frac{1}{\omega_{ba} - (\omega_L - \omega_S) - i\Gamma_{ba}} \\ &\times \left\{ \sum_{n'} \left(\frac{P_{an'} P_{n'b}}{\omega_{n'a} - \omega_a - i\Gamma_{n'a}} + \frac{P_{an'} P_{n'b}}{\omega_{n'b} + \omega_a + i\Gamma_{n'b}} \right) \right. \\ &\times \sum_n \left(\rho_{aa}^{(0)} - \rho_{nn}^{(0)} \right) \left(\frac{P_{bn} P_{na}}{\omega_{na} + \omega_S - i\Gamma_{na}} + \frac{P_{bn} P_{na}}{\omega_{na} - \omega_L - i\Gamma_{na}} \right) \\ &- \sum_{n'} \left(\frac{P_{an'} P_{n'b}}{\omega_{n'a} - \omega_a - i\Gamma_{n'a}} + \frac{P_{an'} P_{n'b}}{\omega_{n'b} + \omega_a + i\Gamma_{n'b}} \right) \\ &\times \sum_n \left(\rho_{bb}^{(0)} - \rho_{nn}^{(0)} \right) \left(\frac{P_{bn} P_{na}}{\omega_{nb} - \omega_S + i\Gamma_{nb}} + \frac{P_{bn} P_{na}}{\omega_{nb} + \omega_L + i\Gamma_{nb}} \right) \Bigg\} \end{aligned}$$

1/4

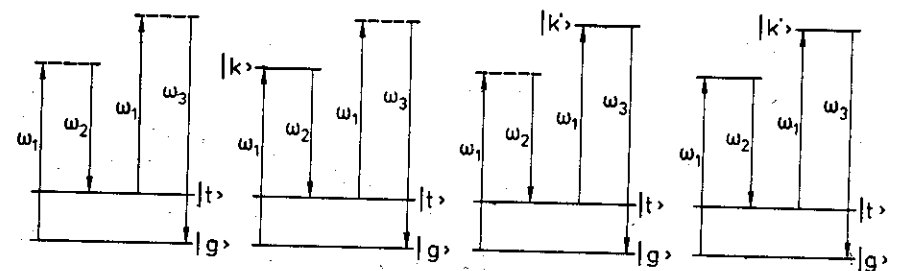
- 3 -

$$\begin{aligned} \chi_R^{ab} &= \frac{1}{3! \hbar^3} \frac{1}{\omega_{ba} - (\omega_L - \omega_S) - i\Gamma_{ba}} \times \\ &\times \left\{ \frac{\tilde{\tilde{\chi}}_e}{(\omega_{na} - \omega_a - i\Gamma_{na})(\omega_{na} - \omega_L - i\Gamma_{na})} + \tilde{\chi}_e^{(3)} \right\} \end{aligned}$$

$$\left| \frac{\tilde{\tilde{\chi}}_e}{\Delta\omega - i\Gamma_{na}} \right| \gtrless \tilde{\chi}_e^{(3)}$$

$$\chi^{(3)} [\text{esu}] = \left| \frac{\chi_{\Sigma}^{(3)}}{\Gamma_{ba}} \right|$$

$$C_6 H_6: \left| \chi_{\Sigma}^{(3)} / \Gamma_{ba} \right| \gg \chi_{NR}^{(3)}$$



CARS

$$\omega_1 = \omega_e^{kg}$$

$$\omega_3 = \omega_e^{k'g}$$

$$\omega_1 = \omega_e^{kg} \quad \omega_3 = \omega_e^{k'g}$$

