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**IX TRIESTE WORKSHOP ON  
OPEN PROBLEMS IN  
STRONGLY CORRELATED SYSTEMS**

***14 - 25 July 1997***

**RECENT RESULTS ON THE  
LAYERED PEROVSKITE  $Sr_2RuO_4$**

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**These are preliminary lecture notes, intended only for distribution to participants.**

# Recent results on the layered perovskite $\text{Sr}_2\text{RuO}_4$

Talk by Andy Mackenzie

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Collaborators

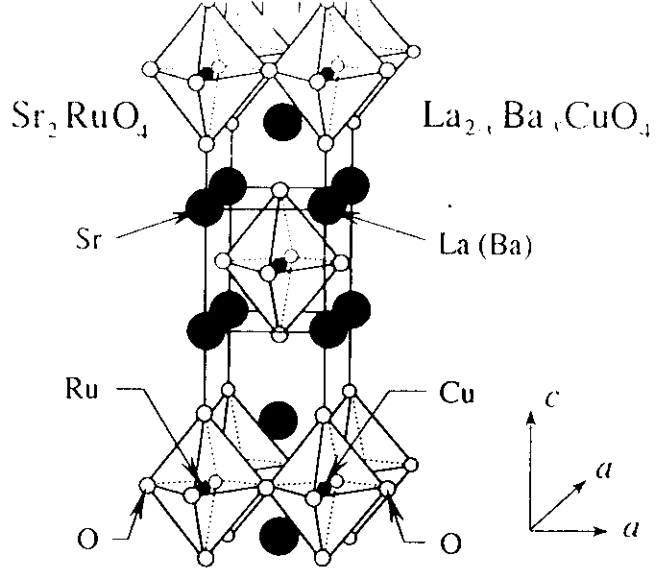
S.R. Julian, N.E. Hussey, A.J. Diver, G.J. McMullan,  
A.W. Tyler and G.G. Lonzarich  
*University of Cambridge*

Y. Maeno, S. Nishizaki, S. Ikeda  
*University of Kyoto, Japan*

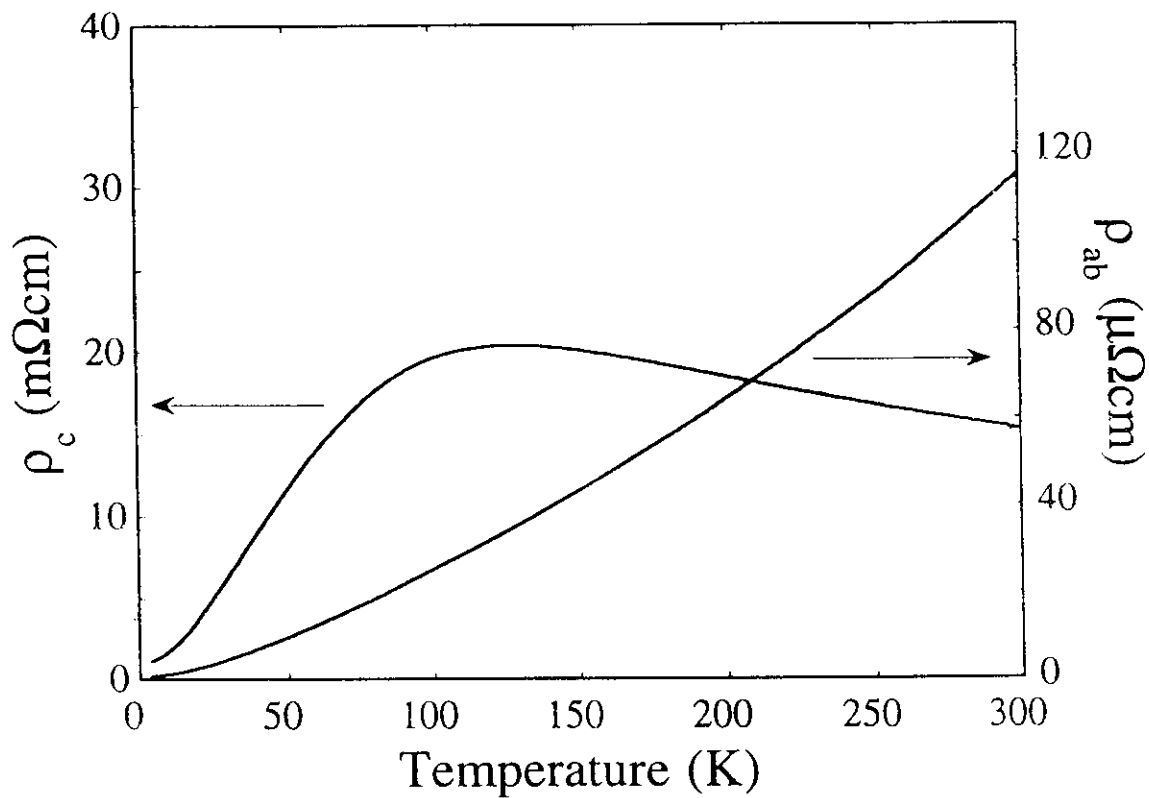
K. Yoshida, T. Fujita  
*University of Hiroshima, Japan*

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1. Introduction to  $\text{Sr}_2\text{RuO}_4$ .
2. Observation and interpretation of quantum oscillations.
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4. Open questions about superconductivity.
5. Open questions about normal state transport.
6. Summary.



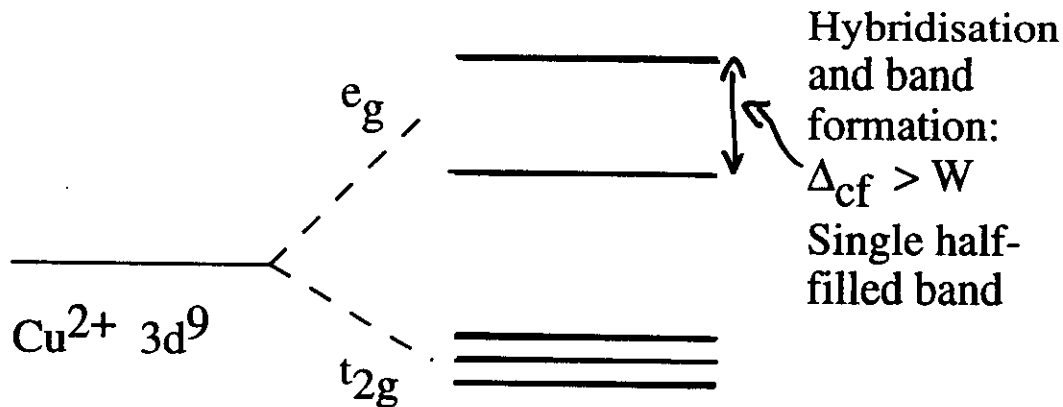
*F. Lichtenberg et al., Appl. Phys. Letts. 60, 1138 (1992)*



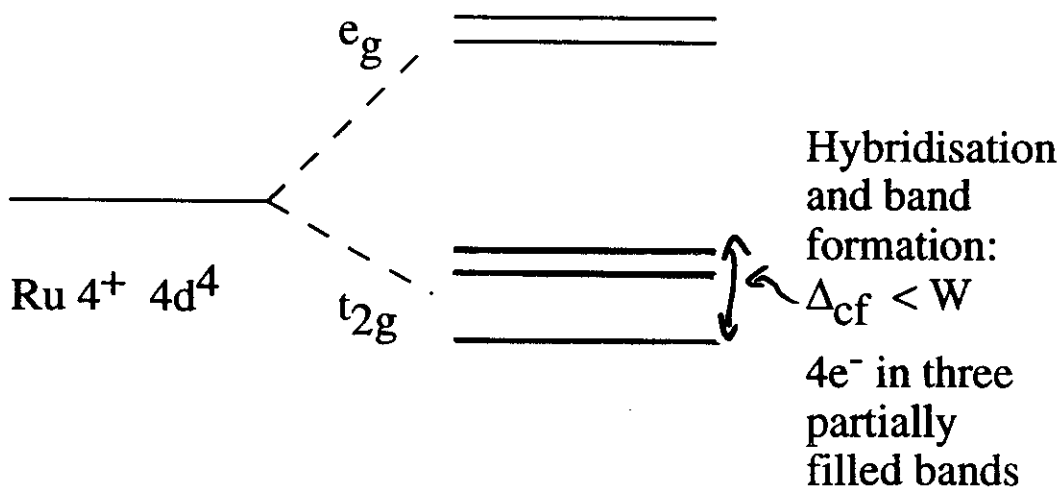
Most people only became interested after the discovery of superconductivity with  $T_c \sim 1\text{K}$  (Maeno et al., Nature 372, 532 [1994]).

Electronic structure is significantly different from that of the cuprates, since the relevant orbitals are 4d's rather than 3d's.

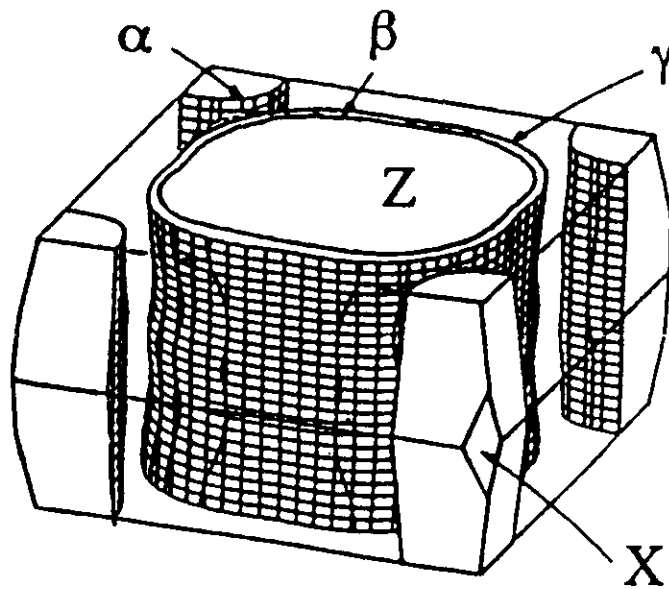
Cuprate in the presence of a crystal field:



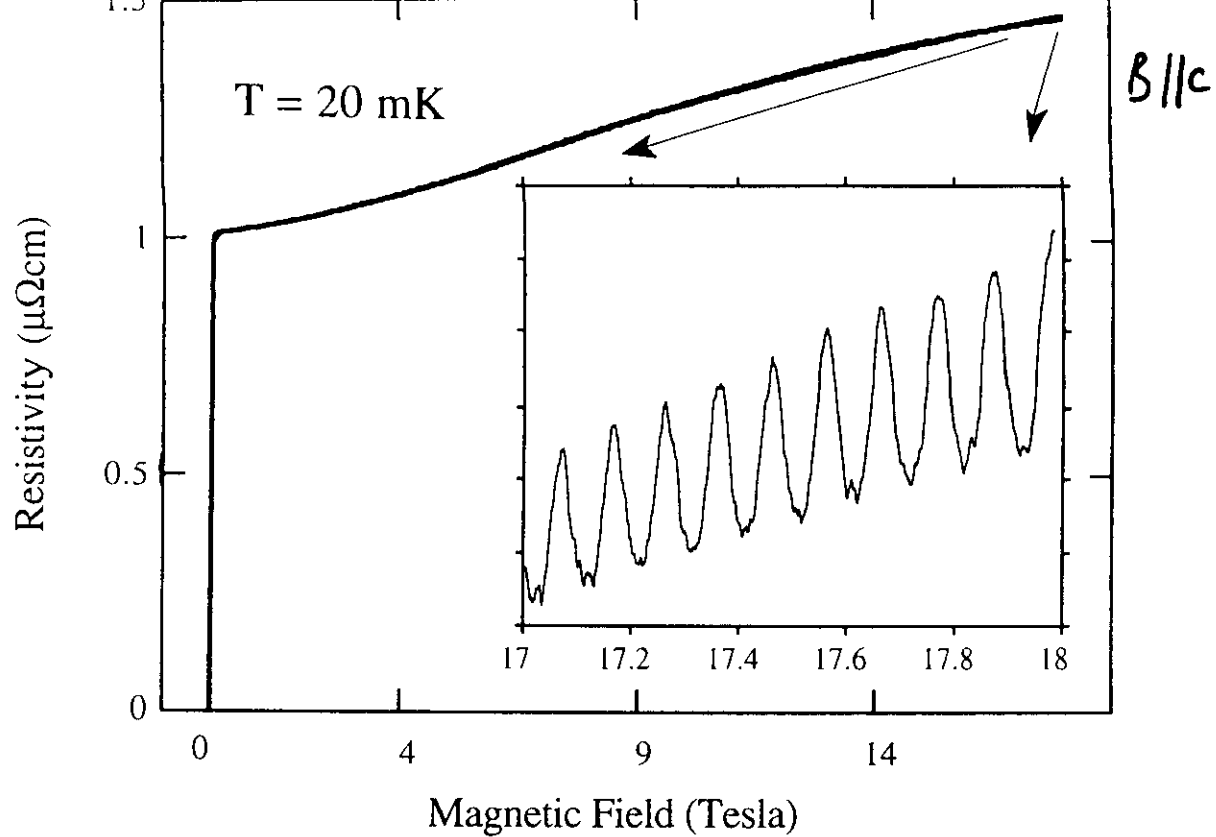
Ruthenate in the presence of a crystal field:



Results of actual band structure calculations for  $\text{Sr}_2\text{RuO}_4$ :



*Figure based on a calculation by G.J. McMullan, M.P. Ray and R.J. Needs. Previous published band calculations: T. Oguchi, Phys. Rev. B 51, 1385 (1995); D.J. Singh, Phys. Rev. B 52, 1358 (1995). All are in qualitative agreement.*



Oscillations come from quantisation of cyclotron motion of charge carriers in a magnetic field  $\mathbf{B}$ .

Fermi liquid theory makes specific predictions of the temperature and field dependence of the oscillations, which can be analysed to give the quasiparticle masses and mean free paths respectively.

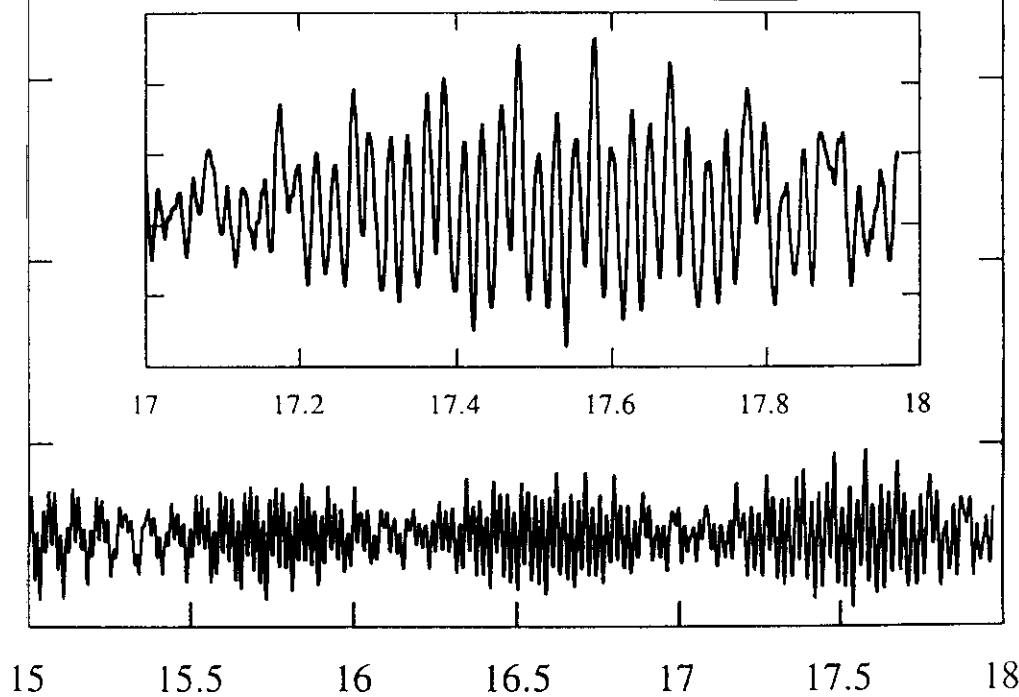
Observation is difficult-requires low temperatures, high magnetic fields and clean samples.

T = 20 mK

Sample dimensions:  
0.3x0.2x0.1 mm<sup>3</sup>

B//c

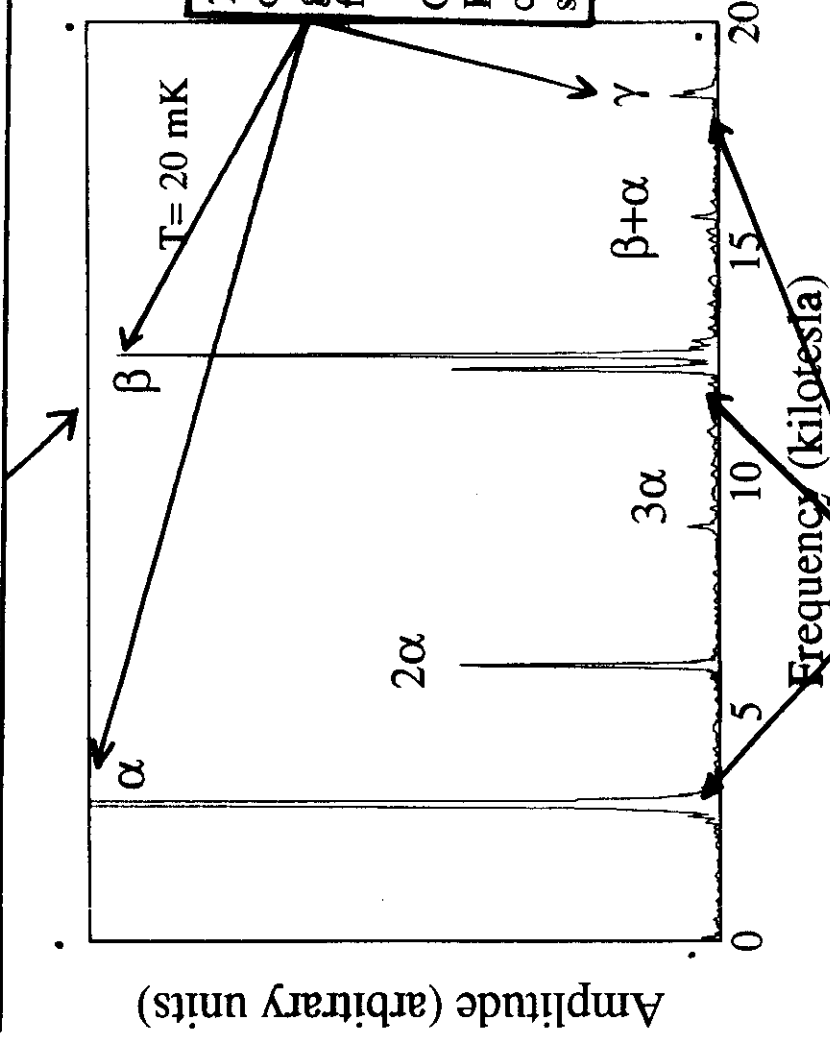
Susceptibility (arb. units)



Magnetic Field (Tesla)



Splitting of fundamental peaks, resolved by studying the oscillations over a wide field range, gives information about the small 3D dispersion. We can measure the average transfer integral  $t_{\perp}$  for each FS sheet.

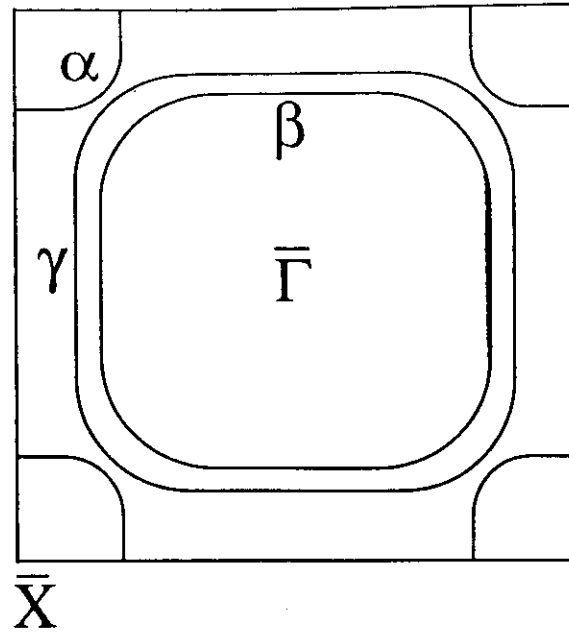


Temperature dependence of amplitude of each component gives cyclotron effective mass for each FS sheet.

Good agreement with Lifshitz-Kosevich formula (not shown) confirms Fermi Liquid ground state.

Frequencies of fundamental components give topological information via Onsager relation:  $A_{\text{ext}} = 2\pi e F / \hbar$

Angular dependence confirms essentially 2D nature of FS.



	$\alpha$	$\beta$	$\gamma$
Freq F (kT)	3.05	12.7	18.5
Band calc.	3.4	13.4	17.6
Avg. $k_F$ ( $\text{\AA}^{-1}$ )	0.302	0.621	0.750
Band calc.	0.319	0.638	0.732
Cyc. mass ( $m_e$ )	3.4	7.5	14.6
Band calc.	1.1	2.0	2.9
Mass enhancement	3.1	3.8	5.0

*Experiment and explicit comparison with in-house band calculation: A.P. Mackenzie, S.R. Julian, A.J. Diver, G.J. McMullan, M.P. Ray, G.G. Lonzarich, Y. Maeno, S. Nishizaki and T. Fujita, Phys. Rev. Lett. 76, 3786 (1996). Previous published band calculations: T. Oguchi, Phys. Rev. B 51, 1385 (1995); D.J. Singh, Phys. Rev. B 52, 1358 (1995).*

We have a detailed, sheet specific knowledge of the low energy excitations which determine the physical properties of the material, and can perform successful quantitative calculations of all independently measured low temperature properties.

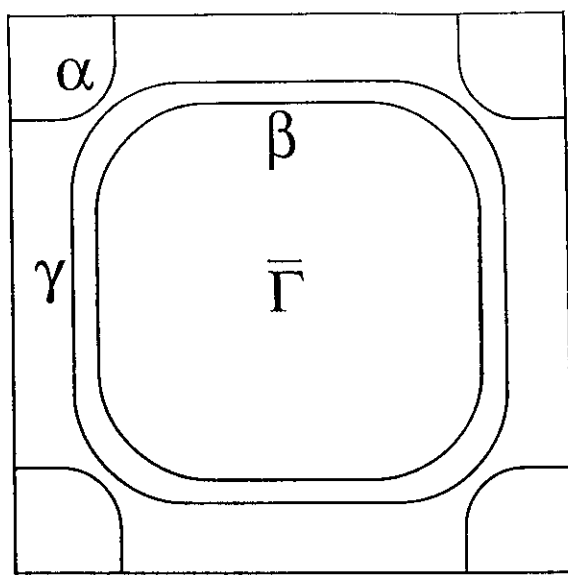
Electronic specific heat  $\gamma = 39 \text{ mJ/molK}^2$   
(Y. Maeno et al., Nature 372, 532 [1994])

Hall coefficient  $R_H = -1.1 \times 10^{-9} \text{ m}^3/\text{C}$   
(A.P. Mackenzie et al., Phys. Rev. B 54, 7425 [1996])

Superconducting upper critical field  $H_{c2}(0) \approx 400 \text{ Oe}$   
(K. Yoshida et al., Physica C 263, 519 [1996])  
A.P. Mackenzie et al., Physica C 263, 510 [1996])

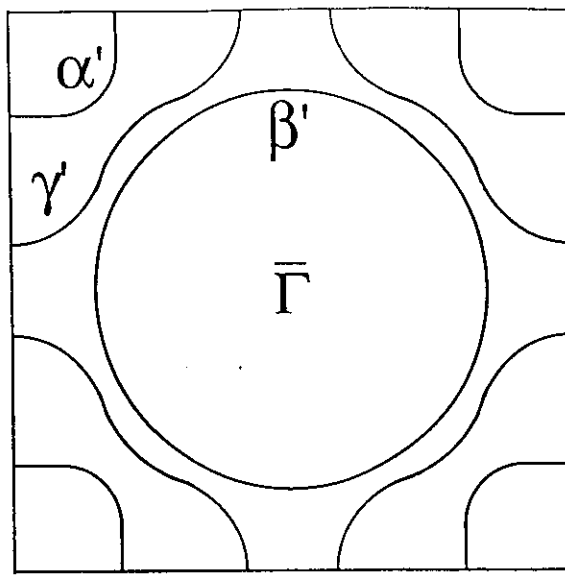
$\text{Sr}_2\text{RuO}_4$  is a Pauli paramagnet with a temperature independent susceptibility of approximately  $10^{-3} \text{ emu/mol}$  up to 700K.  
(Y. Maeno et al., to appear in J. Phys. Soc. Jpn. [1997]).

All in all,  $\text{Sr}_2\text{RuO}_4$  is one of the best understood correlated metals in condensed matter physics. Ten years ago, it was impossible to imagine a ternary oxide in such a role.



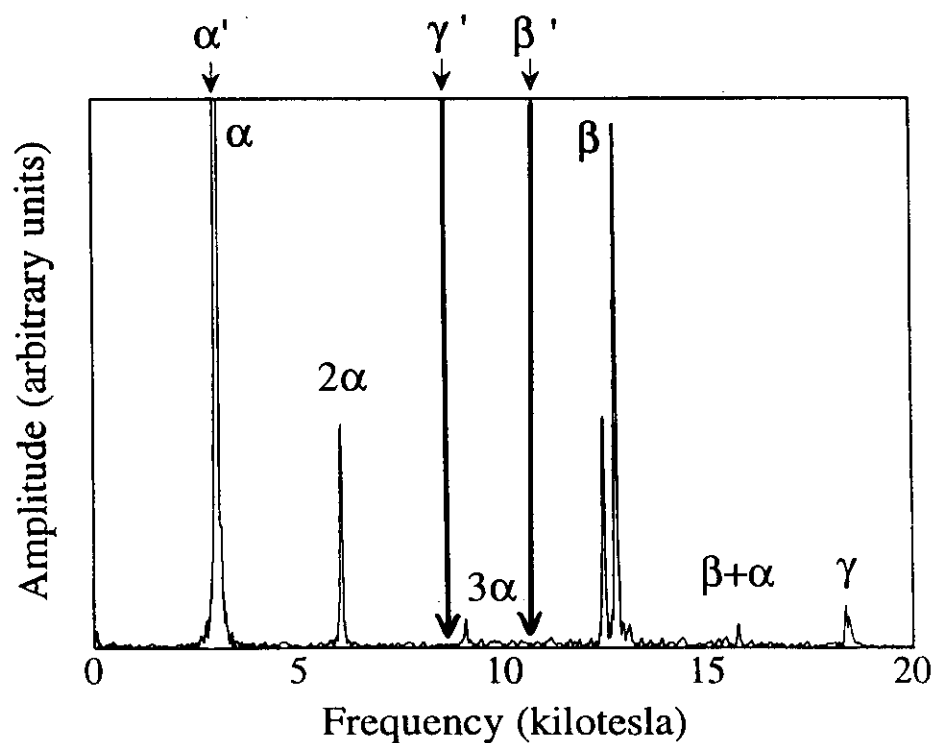
$\bar{X}$

dHvA / LDA Fermi surface



$\bar{X}$

ARPES Fermi surface



**dHvA:** A.P. Mackenzie, S.R. Julian, A.J. Diver, G.J. McMullan, M.P. Ray, G.G. Lonzarich, Y. Maeno, S. Nishizaki and T. Fujita, *Phys. Rev. Lett.* **76**, 3786 (1996); A.P. Mackenzie, S.R. Julian, G.G. Lonzarich, Y. Maeno and T. Fujita, *Phys. Rev. Lett.* **78**, 2271 (1997).

**ARPES:** T. Yokoya et al., *Phys. Rev. Lett.* **76**, 3009 (1996); *Phys. Rev. Lett.* **78**, 2272 (1997); D.H. Lu et al., *Phys. Rev. Lett.* **76**, 4585 (1996).

## Superconductivity of $\text{Sr}_2\text{RuO}_4$

Immediately after discovery -  $T_c \sim 1\text{K}$  is unspectacular after the cuprates, and so probably conventional (phononic?) mechanism.

After quasiparticle parameters known from quantum oscillations, it was noticed that they are very similar to those of  $^3\text{He}$ , a p-wave superfluid. (*T.M. Rice and M. Sigrist, J. Phys.: Cond. Matt. 7, L643 [1995]*).

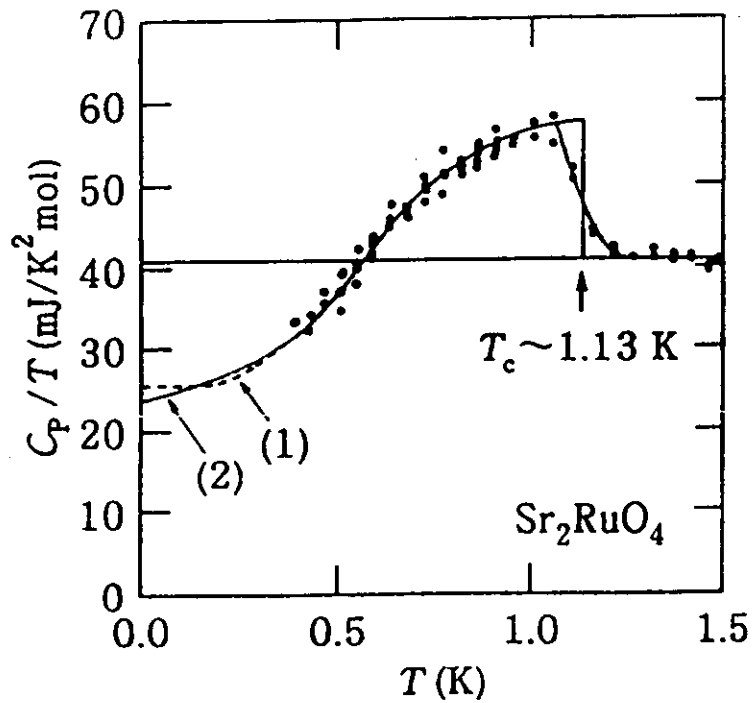
Their suggestion - could  $\text{Sr}_2\text{RuO}_4$  be a p-wave superconductor?

Other circumstantial evidence - related compounds such as the cubic perovskite  $\text{SrRuO}_3$  are ferromagnetic

- if the  $\text{Ru}^{4+}$  ion is present in an insulating layered perovskite (e.g. at dilute concentrations in  $\text{Sr}_2\text{IrO}_4$ , or in the hypothetical insulating form of  $\text{Sr}_2\text{RuO}_4$ ) it exists in the  $S=1$  state due to Hund's rule coupling.

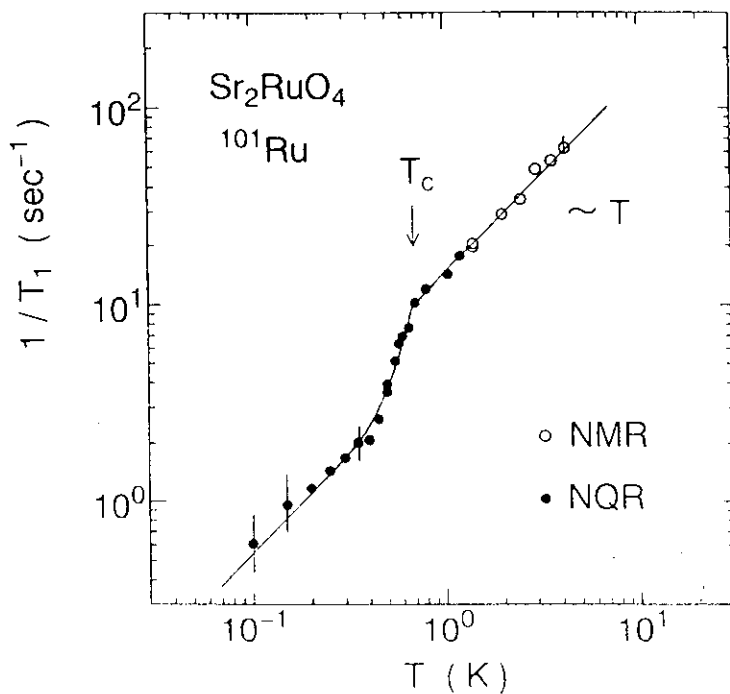
It is not so crazy to consider the possibility of triplet pairing in  $\text{Sr}_2\text{RuO}_4$ .

## Evidence for something unusual



### Specific heat

*Y. Maeno et al.,  
J. Low Temp. Phys. 105,  
1577 (1997).*



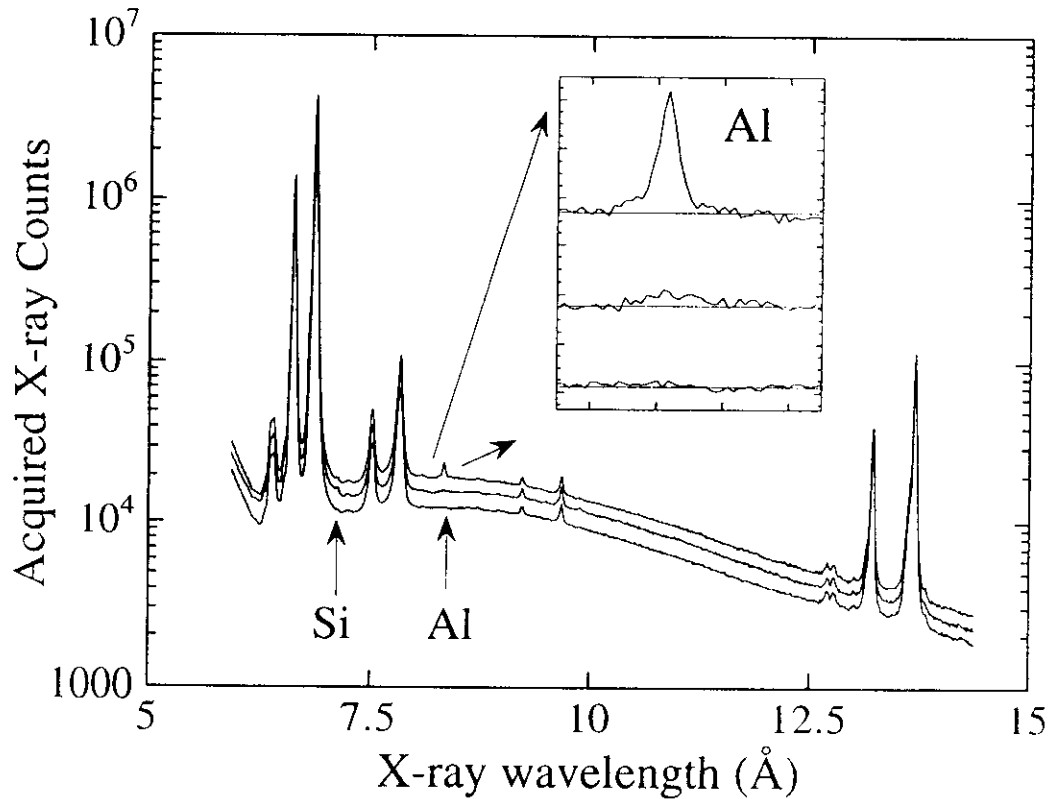
### NMR / NQR into the superconducting state

*K. Ishida, Y. Kitaoka et al.,  
to appear in Phys. Rev. B.*

Known to be a strong growth batch dependence of  $T_c$ .

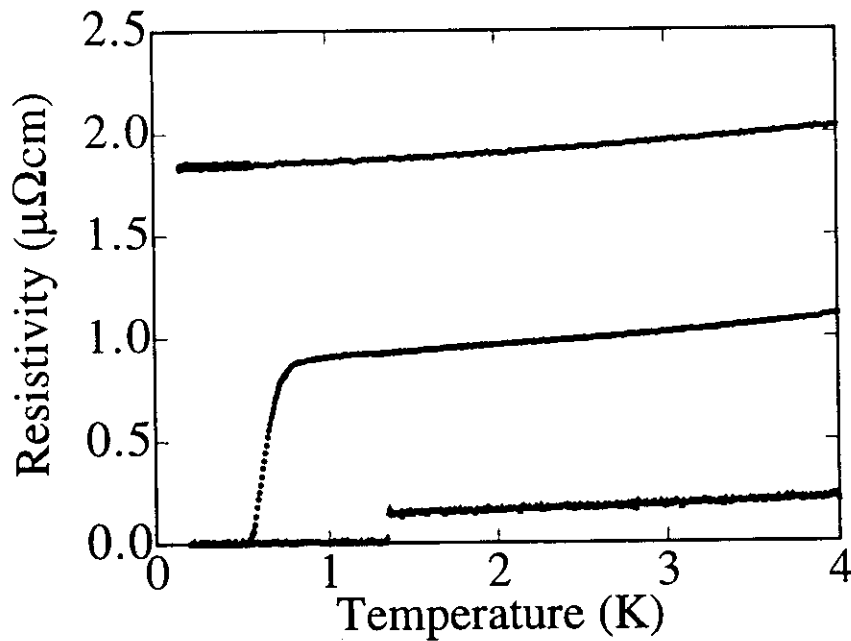
Could this be due to impurities? We have performed a stoichiometric analysis for every element between Na and Bi. Sensitivity is good - detection limits are between 25ppm and 50ppm depending on the element.

A typical scan over part of the x-ray wavelength range for samples with different  $T_c$ :

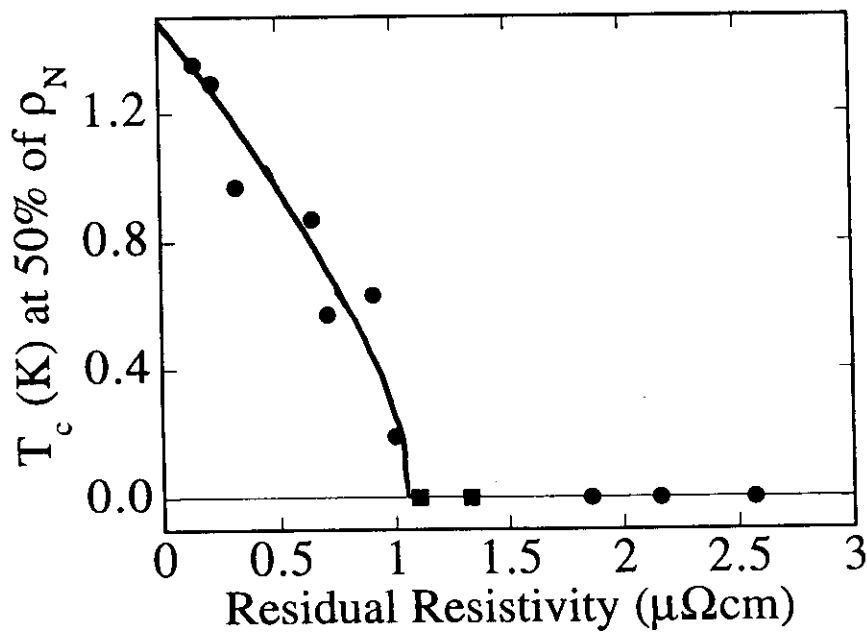


Only impurities detected are Al, Si, Ca and Ba. All of these are thought to be non-magnetic.

The effect of residual resistivity on superconductivity is spectacular:



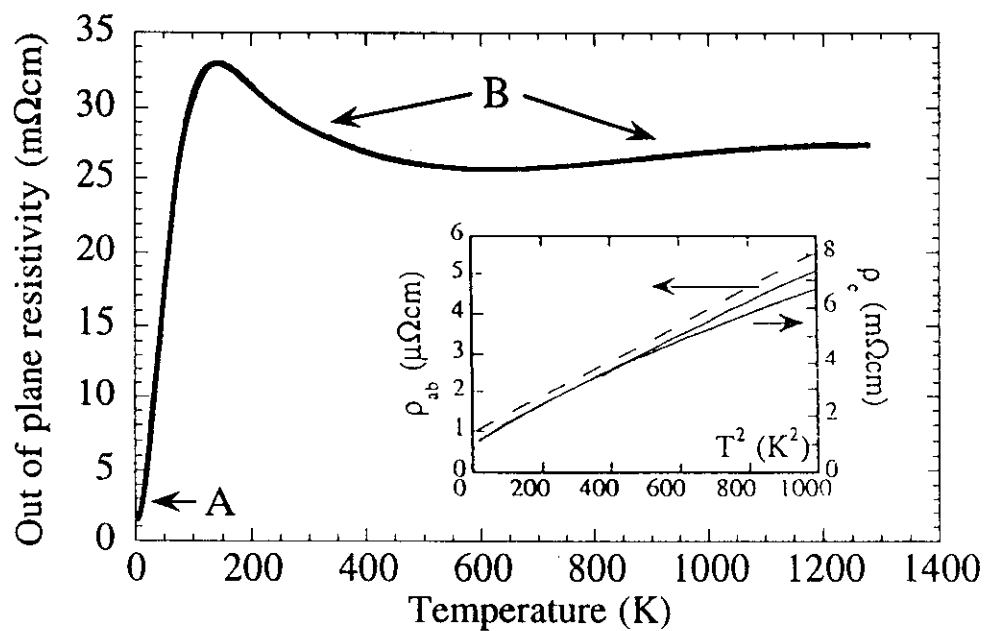
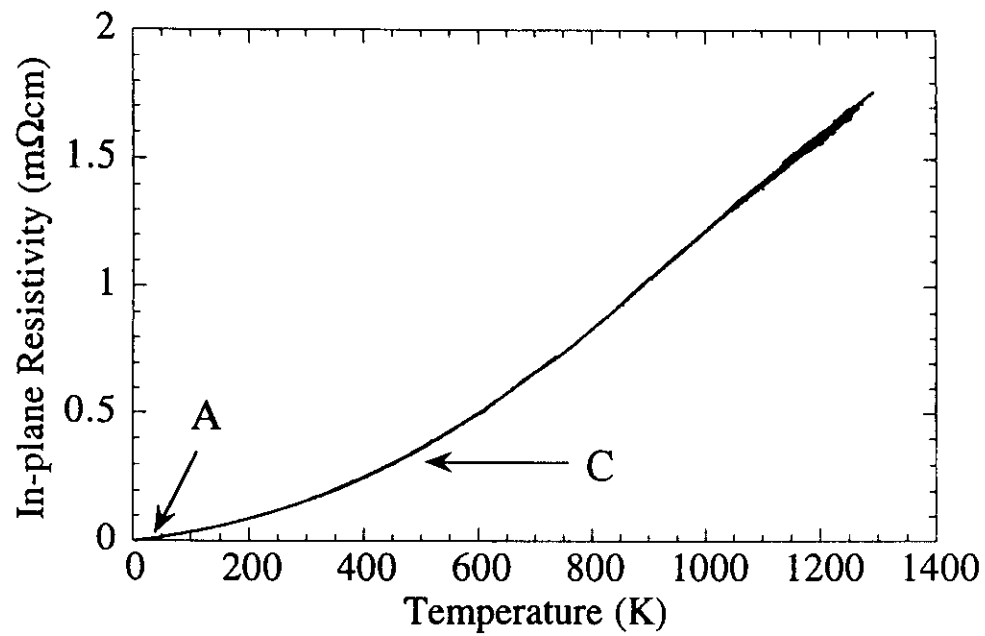
A.P. Mackenzie,  
R.K.W. Haselwimmer,  
A.W. Tyler,  
G.G. Lonzarich,  
Y. Mori, S. Nishizaki  
and Y. Maeno, preprint



Open question: Is Sr<sub>2</sub>RuO<sub>4</sub> p- or d-wave? New measurements of specific heat on the best samples should help to resolve issue.



Open questions posed by transport properties:



A.W. Tyler, A.P. Mackenzie, K. Yoshida, S. Ikeda, S. Nishizaki, Y. Maeno and T. Fujita (unpublished).

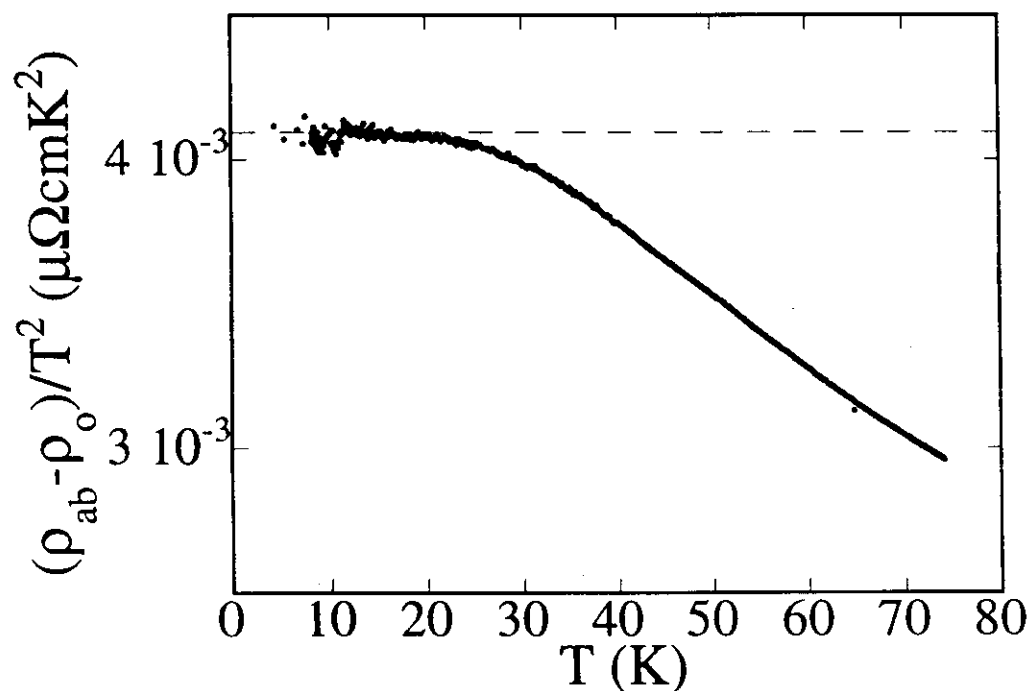
A: What is the origin of the loss of  $T^2$  resistivity in all directions at  $T \approx 20\text{K}$ ?

Most "conventional" viewpoint - some scale principally relevant to in-plane physics causes a change in  $\rho_{ab}$ , and  $\rho_c$  also changes because  $\text{Sr}_2\text{RuO}_4$  is a three dimensional Fermi liquid at low temperatures.

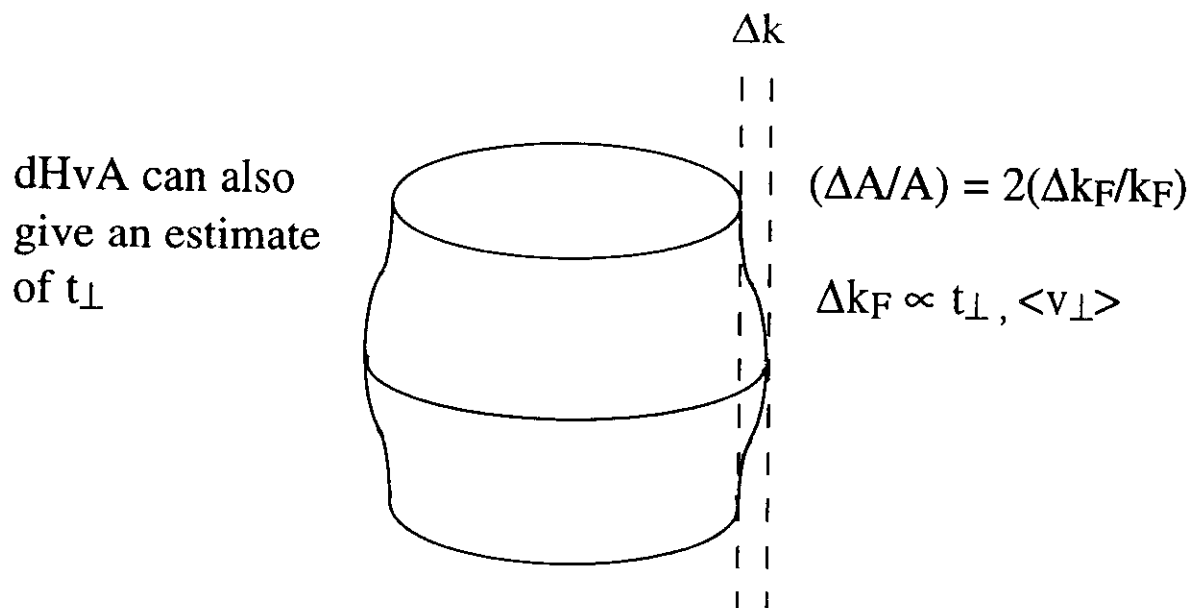
Note: a)  $T_F \sim 1700\text{K}$ .

b) It cannot be an additive scattering mechanism.

c) The change is not simply due to higher powers of temperature, but is a fairly well-defined crossover:



There is one scale which makes a crossover in this region of temperature, which is coherent band formation in the c-direction.



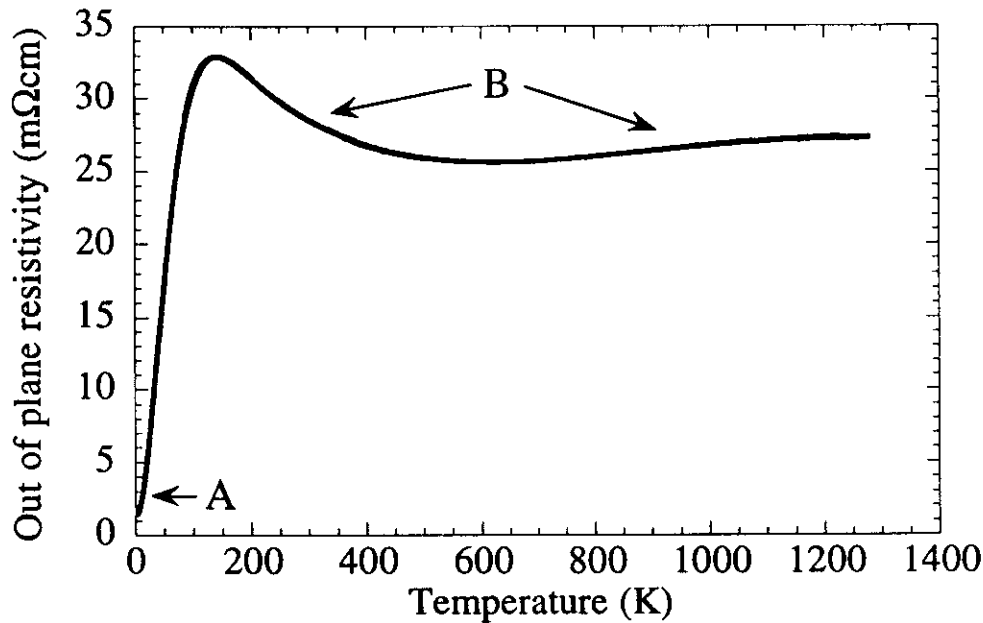
	$\alpha$	$\beta$	$\gamma$
$t_{\perp}$ (meV)	0.1	1.3	0.2

Condition for coherence:  $\tau_{mf} > \tau_{hop}$

We can estimate  $\tau_{mf}$  from  $\rho_{ab}$ , since in-plane motion and scattering dominate in a very anisotropic material.  $\tau_{hop}$  perpendicular to the planes can be estimated from  $\hbar/t_{\perp}$ .

The  $\beta$  sheet dominates, and is coherent at  $T=0$ . Increasing  $T$  decreases  $\tau_{mf}$ , and violates the coherence condition at  $T \approx 20K$ .

Question B: How do we view the high temperature c-axis resistivity?



The very high temperature part is clearly completely incoherent. The rise in  $\rho_c$  above 600K cannot be easily interpreted until data for compressibility, thermal expansion and the pressure dependence of  $\rho_c$  are available.

The maximum at 130K may just be the result of a competition between incoherence at high T and the completely coherent behaviour at low T.

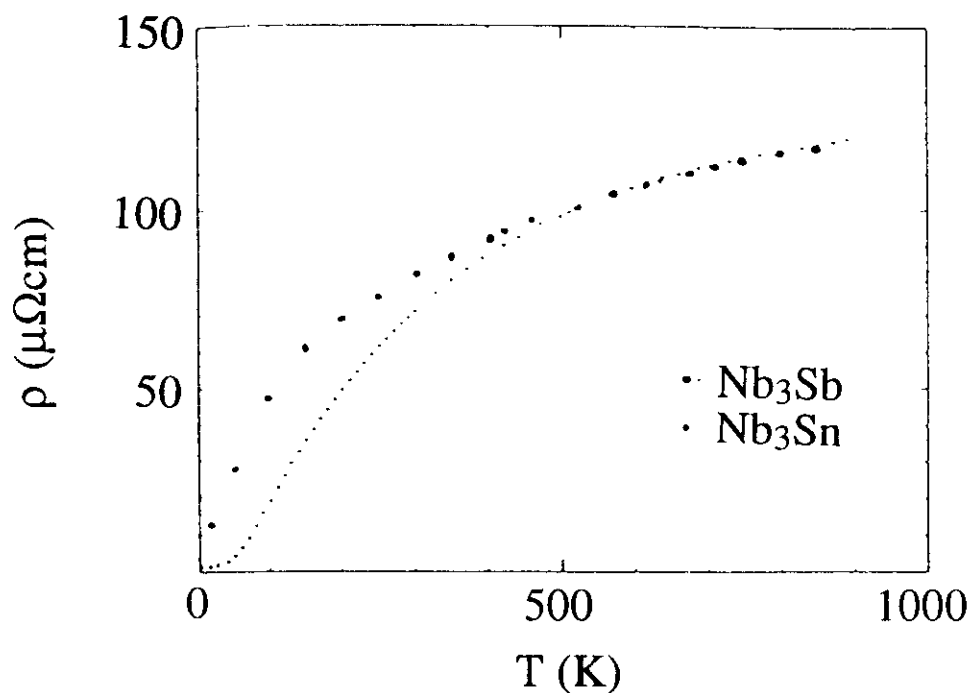
MR data (*Hussey et al., unpublished*) give evidence for competing positive and negative terms above 60K.

Optical conductivity (*Katsufuji, Kasai and Tokura, Phys. Rev. Letts. 76, 126 [1996]*) is also consistent with a coherence - incoherence crossover between 15K and 130K.

Question C: What is the significance of the Mott-Ioffe-Regel limit to high temperature transport?

The Mott-Ioffe-Regel limit is a statement formulated for  $T=0$  about a limiting value to metallic resistivity. It is expressed in terms of the mean free path  $\ell$ , and has various forms, e.g.  $k_F \ell = 1$ ,  $k_F \ell = 2\pi$ ,  $\ell = a$ .

Some kind of high temperature resistivity saturation appears to be observed in many metals, e.g. the A15 compounds, at values which are consistent with the range given above:

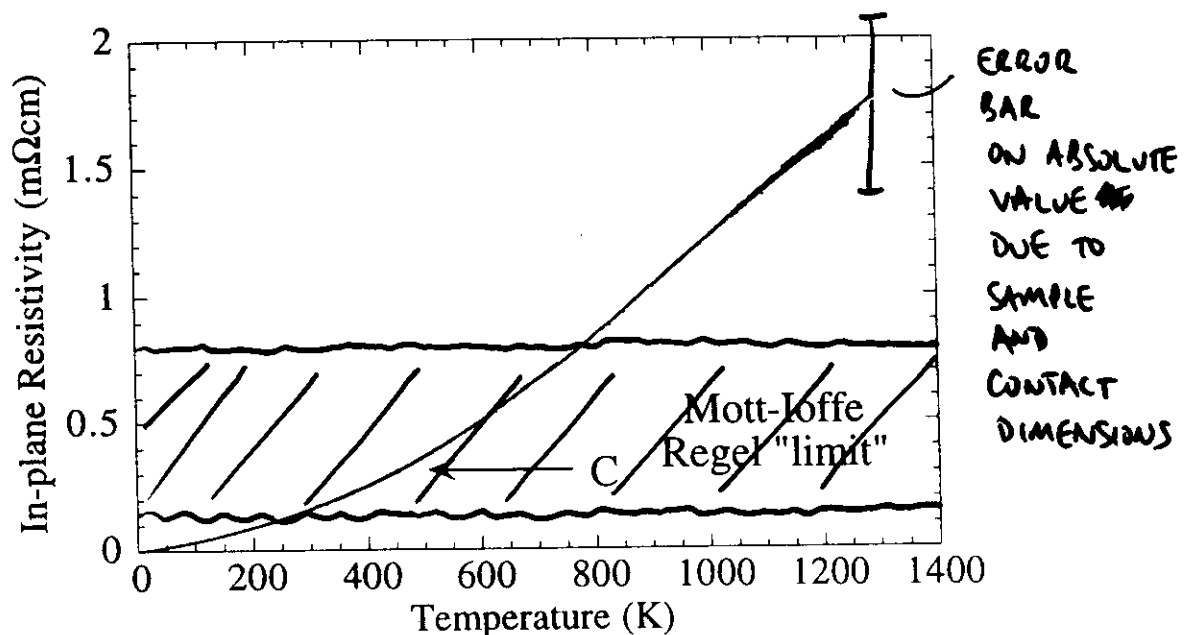


Fisk and Webb, Phys. Rev. Lett. 36, 1084 (1976).

These observations have led to the high temperature MIRL being quite widely accepted.

However, resistivity saturation is not observed in a number of interesting cases, e.g. high  $T_c$  cuprates, some organic metals,  $\text{SrRuO}_3$  and doped  $\text{C}_{60}$ . It has been suggested that in these "bad metals", an anomalous high temperature conduction mechanism exists which may even extend to low temperatures below the MIRL (Emery and Kivelson, Phys. Rev. Letts. 74, 3253 [1995]).

No sign of resistivity saturation is observed in  $\text{Sr}_2\text{RuO}_4$ , which by the above reasoning is a "bad metal" at high temperatures, although it is clearly a very good metal at low temperatures.



Does this indicate a crossover to a different conduction mechanism at high temperatures, or is the MIRL not, in fact, applicable in this regime?

## Summary

$\text{Sr}_2\text{RuO}_4$  is a mass enhanced Fermi liquid at low temperatures, and its quasiparticle spectrum is understood in some detail.

The superconductivity is not s-wave;  $T_c$  has an extremely strong dependence on residual resistivity. Whether it is p-wave or d-wave is still an open question.

Although the normal state is understood at low temperatures, there are plenty of interesting questions about the observed behaviour at high temperatures ( $T > 1\text{K!}$ ). Understanding some of these is likely to aid understanding of the cuprates.

