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**IX TRIESTE WORKSHOP ON
OPEN PROBLEMS IN
STRONGLY CORRELATED SYSTEMS**

14 - 25 July 1997

**NEW EXPERIMENTS AND KEY ISSUES IN
COLOSSAL MAGNETORESISTANCE**

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These are preliminary lecture notes, intended only for distribution to participants.

COLOSSAL MAGNETORESISTANCE OXIDES

1. Introduction
 2. Theoretical ideas
 3. Unusual metallic state
 - 4 The paramagnet
 - 5 charge ordering and related phenomena.
-

1. Introduction :-

A. La Mn O_3 is an insulator

[Both above and below the
Neel temperature $\sim 150 \text{ K}$]
Mott insulator

$\text{La}_{1-x} \text{Sr}_x \text{Mn O}_3$ is a metal

for $0.18 \leq x \leq 0.4(?)$ and at low temperature.

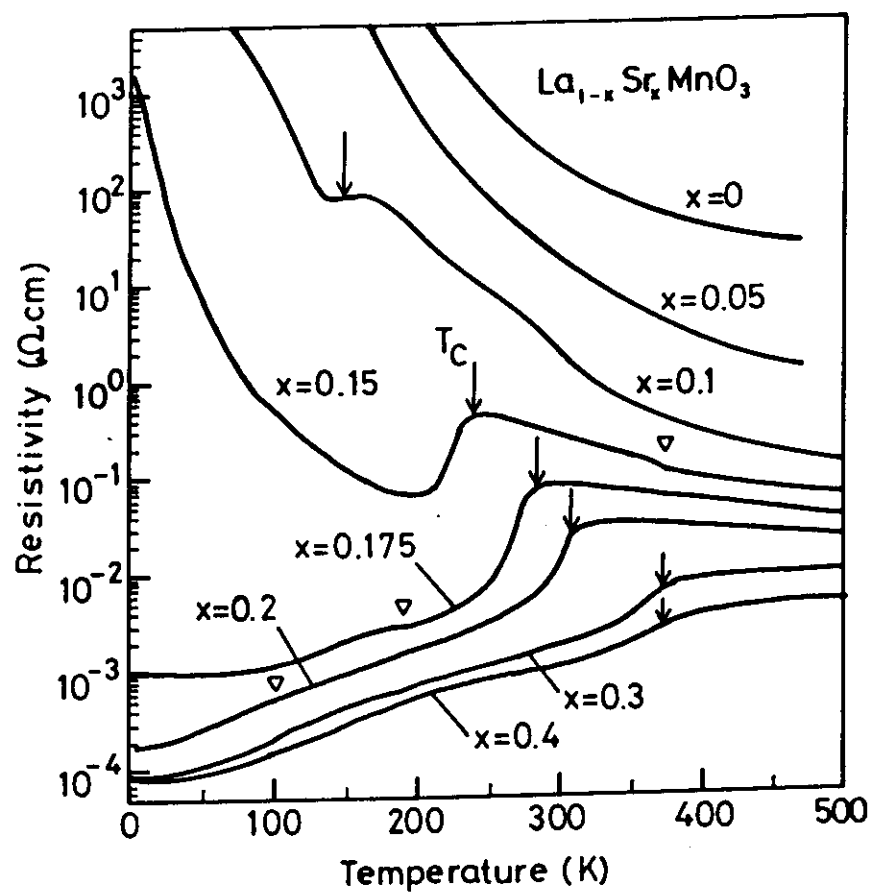
Paramagnetic
(bad metal? insulator?) $\rightarrow$ Ferromagnetic metal
 $T_0 \sim 300 \text{ K}$.

The family $\text{Re}_{1-x} \text{A}_x \text{Mn O}_3$

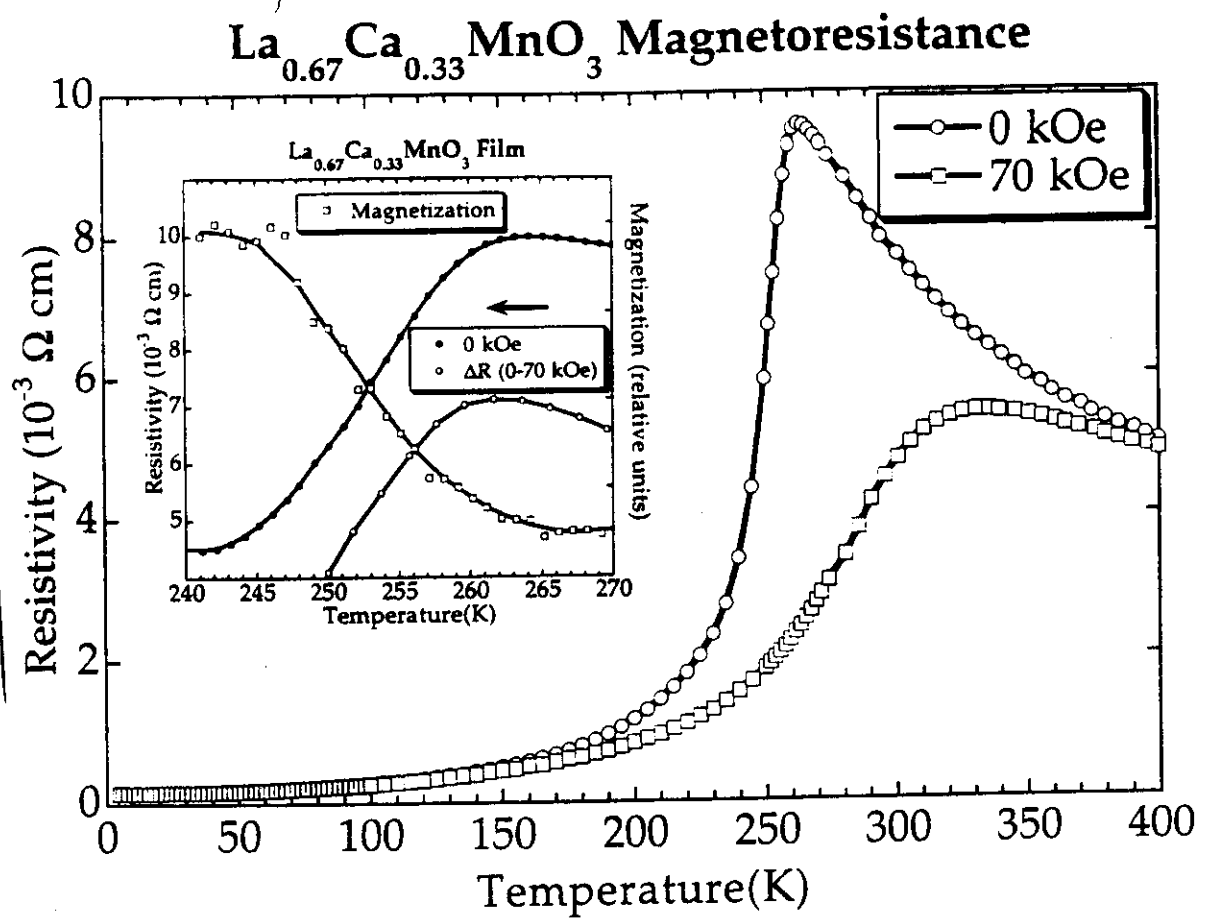
is home to a variety of phenomena

- a) metal insulator transitions (as T increase)
- B) colossal magnetoresistance [and other forms of hypersensitivity to magnetic fields, strain, current]
- x) charge ordering / melting

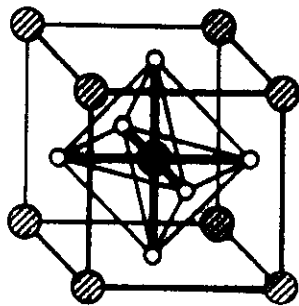
many of which are poorly understood, unusual and spectacular.



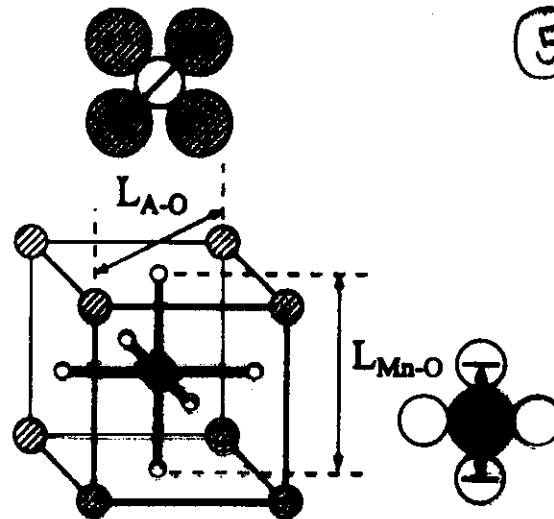
Urushibara . . . Tokura



Snyder... Geballe



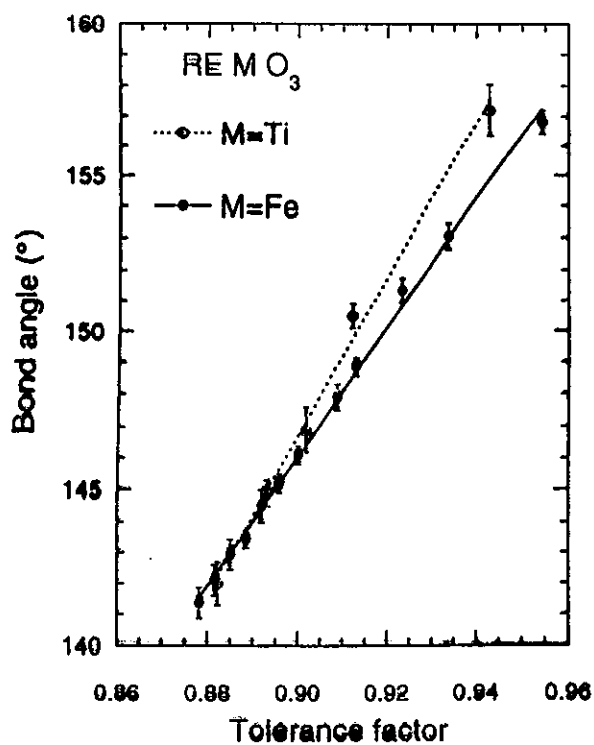
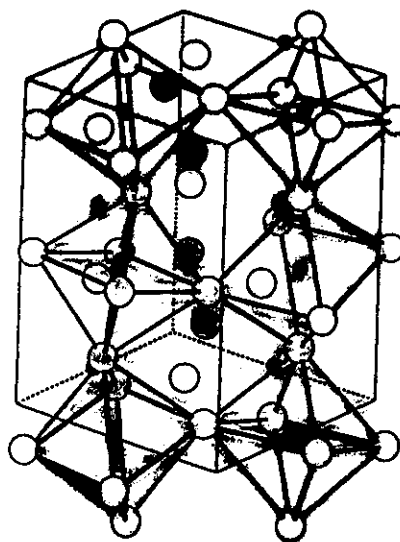
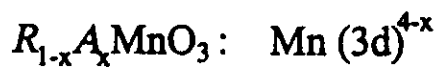
(hatched circle) A-site ions:
 R^{3+} : La, Y, Nd, Pr, Sm, ...
 A^{2+} : Sr, Ba, Ca, Pb, ...
 (solid black circle) Mn
 (open circle) O



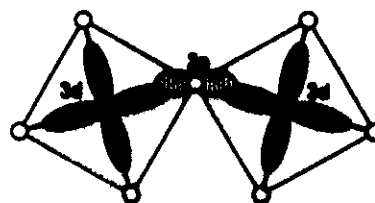
tolerance factor

$$t = \frac{L_{A-O}}{\sqrt{2}L_{Mn-O}}$$

Carrier Doping



Tilting of octahedra reduces electron hopping.



$$t_{dd} \propto (\cos\theta)^2$$

Bandwidth control

Fig. 66

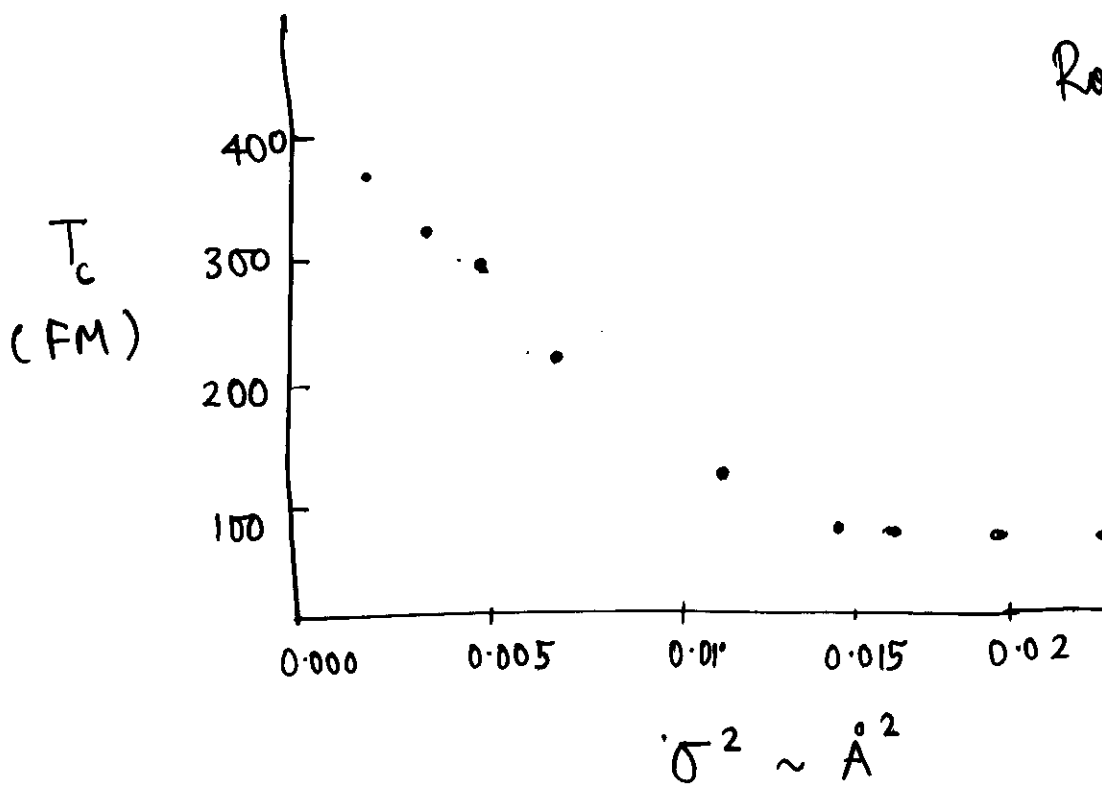
Ionic radii :-

La^{3+}	~ 1.22	Ca^{2+}	~ 1.18
$(\text{Pr}, \text{Nd})^{3+}$	~ 1.145	Sr^{2+}	~ 1.31
Sm^{3+}	~ 1.13	Ba^{2+}	~ 1.47

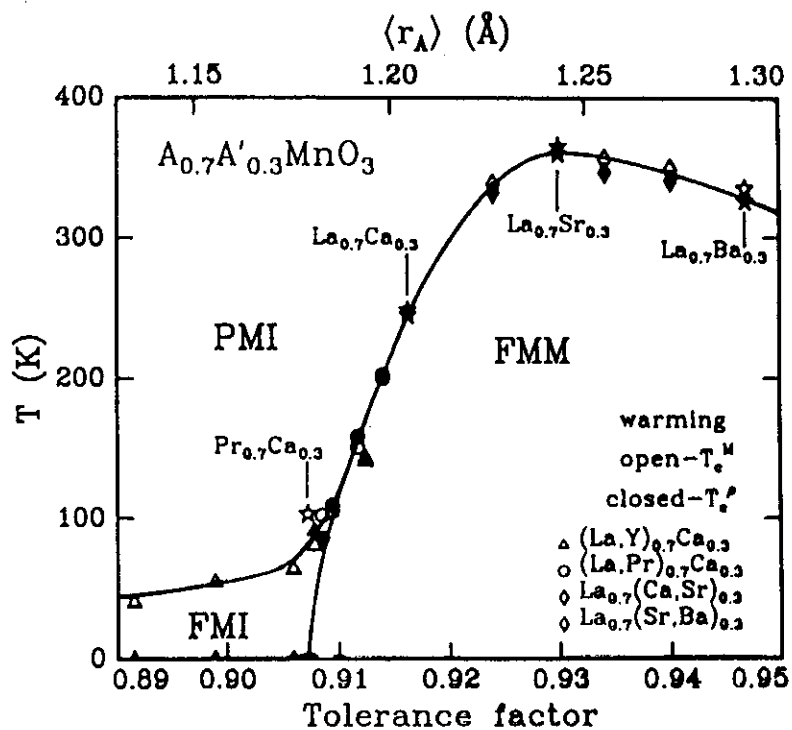
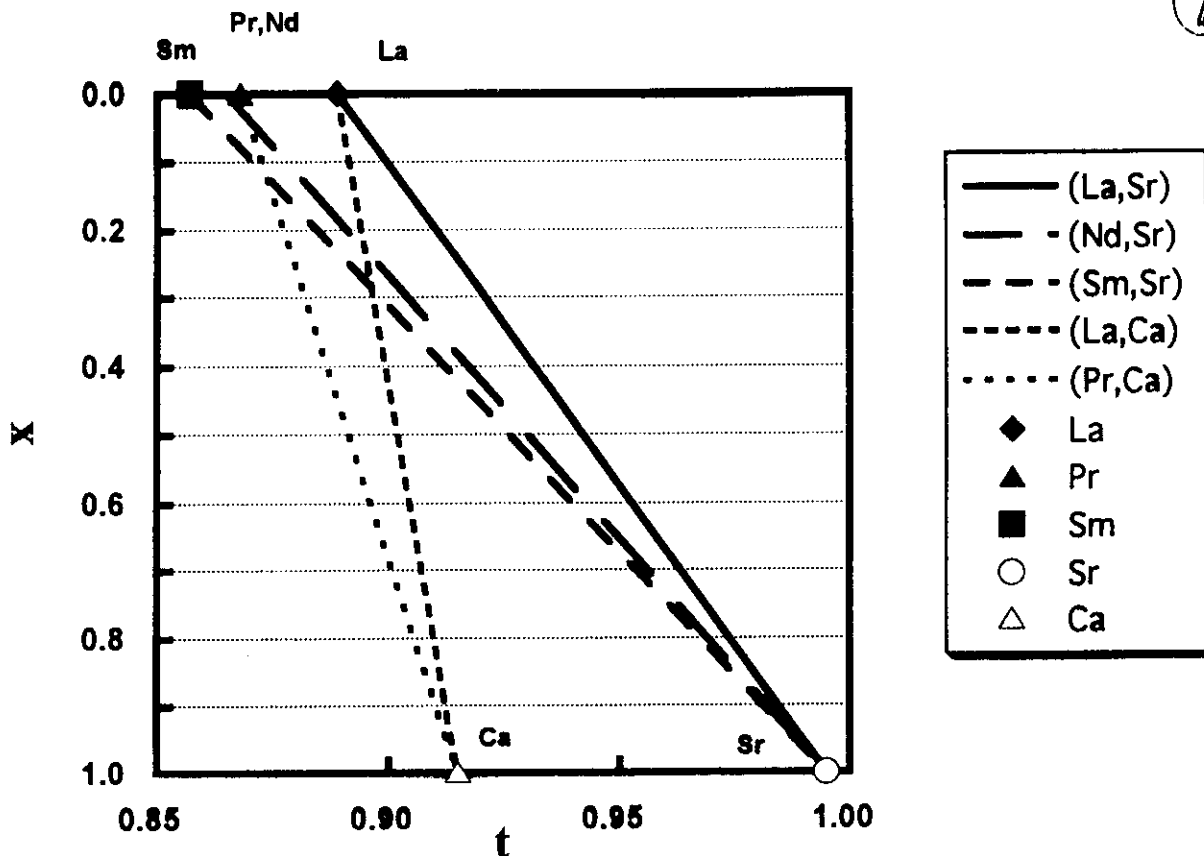
Ideal size $\approx 1.30 \text{ \AA}$

$\langle \delta_A \rangle$ or tolerance factor often used to organize information.

Useful, but not always.

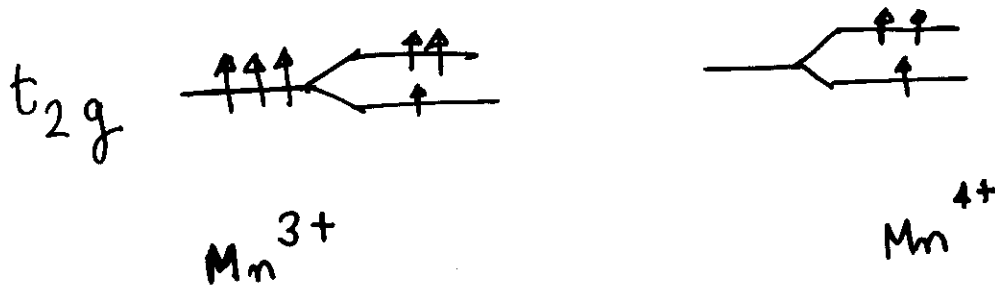
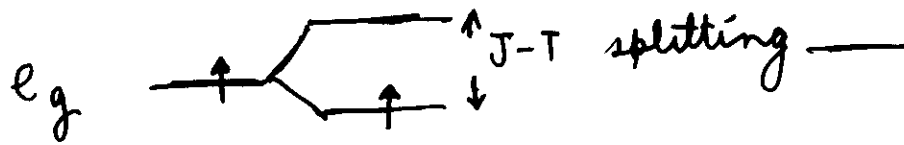


Rodriguez-Martinez
&
Attfield



"Lattice effect"

Hwang et al.



(i) Strong Hund's rule coupling.
[Zener, Anderson and Hasegawa, de Gennes].

$$H = - \sum_{\langle lm \rangle} (t_{lm} c_l^\dagger c_m + \text{h.c.})$$

$$c_l = \cos\left(\frac{\theta_l}{2}\right) c_{l\uparrow} + i \sin\left(\frac{\theta_l}{2}\right) e^{i\phi_l} c_{l\downarrow}$$

$\begin{matrix} \nearrow (\theta_l, \phi_l) \\ l \\ \nwarrow (\theta_m, \phi_m) \\ m \end{matrix}$

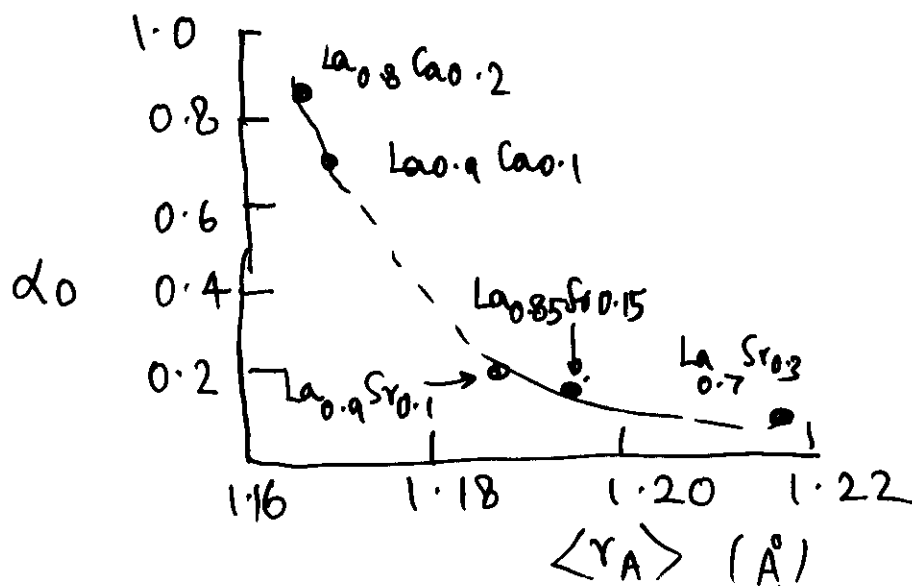
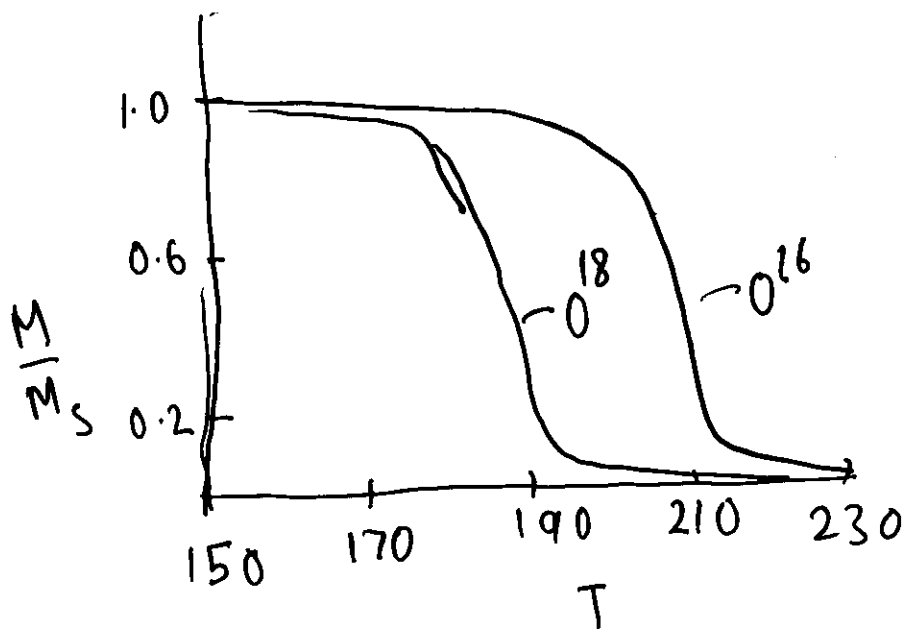
$$t_{lm} = \cos\left(\frac{\theta_l}{2}\right) \cos\left(\frac{\theta_m}{2}\right) + \sin\left(\frac{\theta_l}{2}\right) \sin\left(\frac{\theta_m}{2}\right) e^{i(\phi_l - \phi_m)}$$

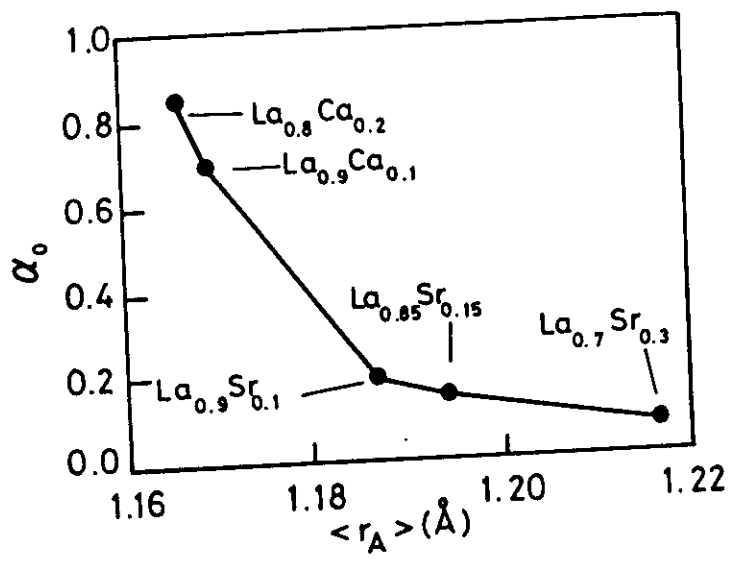
$$(U = \infty, J_H = \infty).$$

Strong electron lattice effects

24
86

- (i) Mn - O radial distribution
- (ii) Debye - Waller factor
- (iii) Isotope effect on T_c .





(9)

$$H_{J-T} = g \sum_{l, a, \alpha} \vec{r}_l \cdot \vec{c}_{la\alpha}^\dagger \vec{e}^{ab} c_{lb\alpha}$$

a, b orbitals
 α electron spin
 $\vec{r}_l$ lattice displacement

Other interactions between spins?

Mn^{4+} limit :- Ferromagnetic

Mn^{3+} limit :- Antiferromagnetic
(in some detail)

Models explored so far :-

$$H = H_{Kondo}^F \quad (\text{Furukawa})$$

$$H_{Kondo}^F = - \sum_{\langle ij \rangle} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} - \sum_i J_H \vec{S}_i \cdot \vec{S}_i$$

$$H = H_{Kondo}^F + H_{J-T} + H_{ph}$$

$d = \infty$
 [In dynamical mean field theory. $\Sigma_i(\omega)$, m_i , r_i]

(10)

coherent metal. $\rightarrow$ incoherent metal
 (ferromagnetic) (paramagnetic).

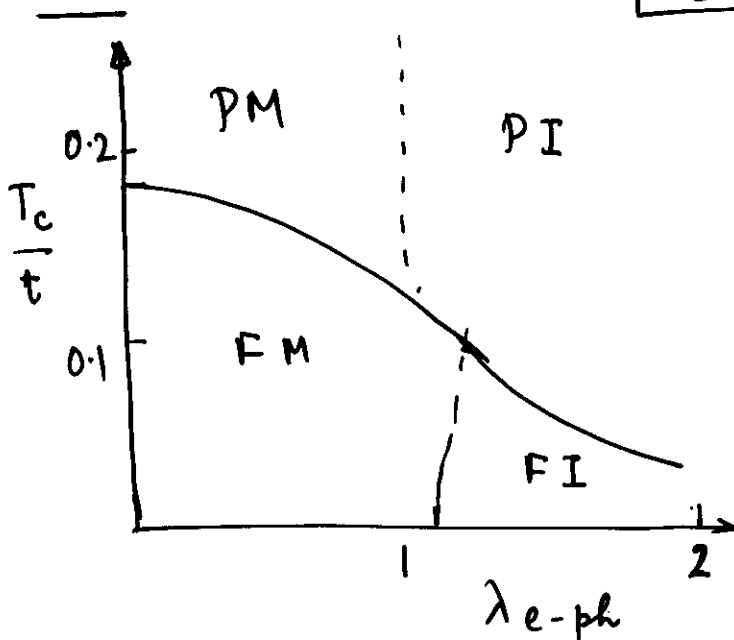
$$\rho(T) \Rightarrow \rho\left(\frac{M}{M_S}\right)$$

and similar scaling relations.

Realistic T_c ($\ll xW$).

Spin wave spectrum

$n_e = 1$ per site



Insulator due
 to J-T distortion,
 and local, bound
 (trapped) electron
 for large λ_{e-ph}
 $\lambda_{e-ph} \sim (J/t)$.

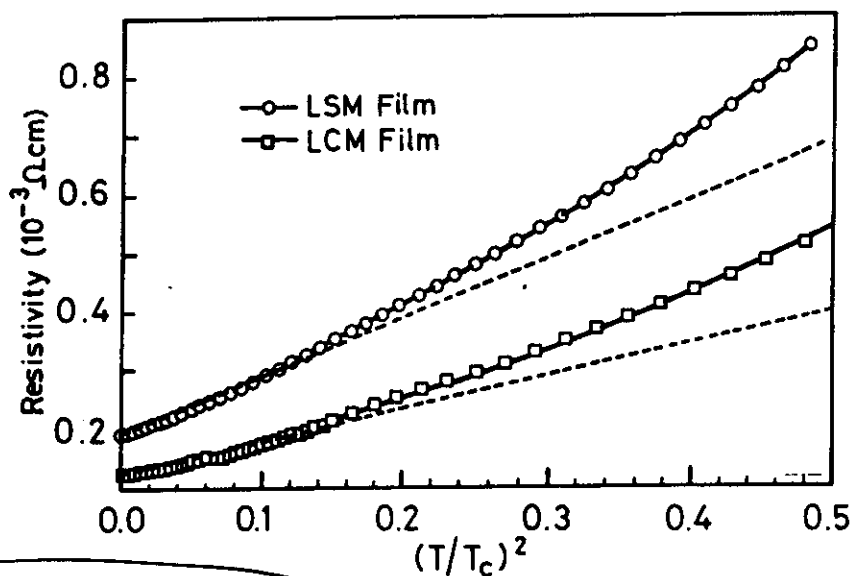
Much milder effects away from
 $n_e = 1$.

Broad features
 $\approx$ similar to
 experiment.

(α) Low Temperature Resistivity : STATE (11)

$$\rho(T) \approx \rho(0) + A T^2 \quad T \ll T_c$$

$\swarrow$
very large

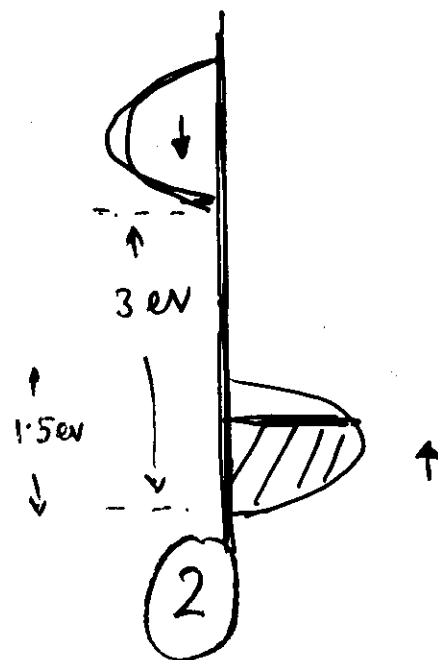


Snyder & Geballe

No low energy spin flip excitations



$$\Delta\rho \sim T^{9/2}$$



(β) Strong violation of Mott $\sigma_{\min}(P_{\max})$

(i) $\rho_{\max}^{\text{metal}} \sim 2 \text{ m}\Omega \text{ cm}$

[Geometrical, i.e. related to $\lambda_{\text{de Broglie}} \sim r_{\text{interatomic}}$]

Generally well obeyed, except for quantum effects at low T and near critical disorder.

(ii) Exponentially large $\rho(T=0)$,

$$\rho \sim \rho_0 \exp\left(\frac{\lambda \delta M}{M_s}\right) \quad ?$$

$T < T_c$.

(iii) Polaronic band narrowing?

a) $\rho_{\max}$ indep. of bandwidth.

$$\sigma \sim e^2 \langle \vec{v} \rangle^2 \frac{\rho(\epsilon_F)}{t} \left(\frac{1}{r}\right) \quad \text{bandwidth } t$$

$$\sim \frac{e^2}{a^3} (a t)^2 \left(\frac{1}{t}\right) \left(\frac{1}{t}\right) \quad \left[\sigma_{\min} \sim \frac{e^2}{ka} \right]$$

(b) classical $\rightarrow$ quantum

(13)

$$\sigma \sim \left(\frac{p_{\text{hopping}}}{k_B T} \right) \quad p_{\text{hopping}} \sim t_{\text{eff}} \quad k_B T \gg t_{\text{eff}}$$

$$\sim \frac{p_{\text{hopping}}}{t_{\text{eff}}} \sim \left(\frac{e^2}{\hbar a} \right)$$

$$k_B T \ll t_{\text{eff}}$$

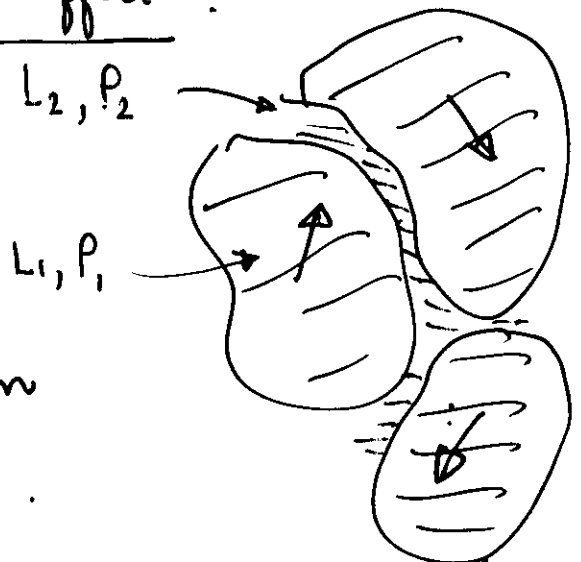
No signs of our being in
classical regime or of such a
low T crossover.

Maheśh
Raychaudhuri
Rao

(iv) Grain boundary effect?

$$\rho \approx \rho_1 + \left(\frac{L_2}{L_1} \right) \rho_2$$

(Crude effective medium
picture, $L_2 \ll L_1$).



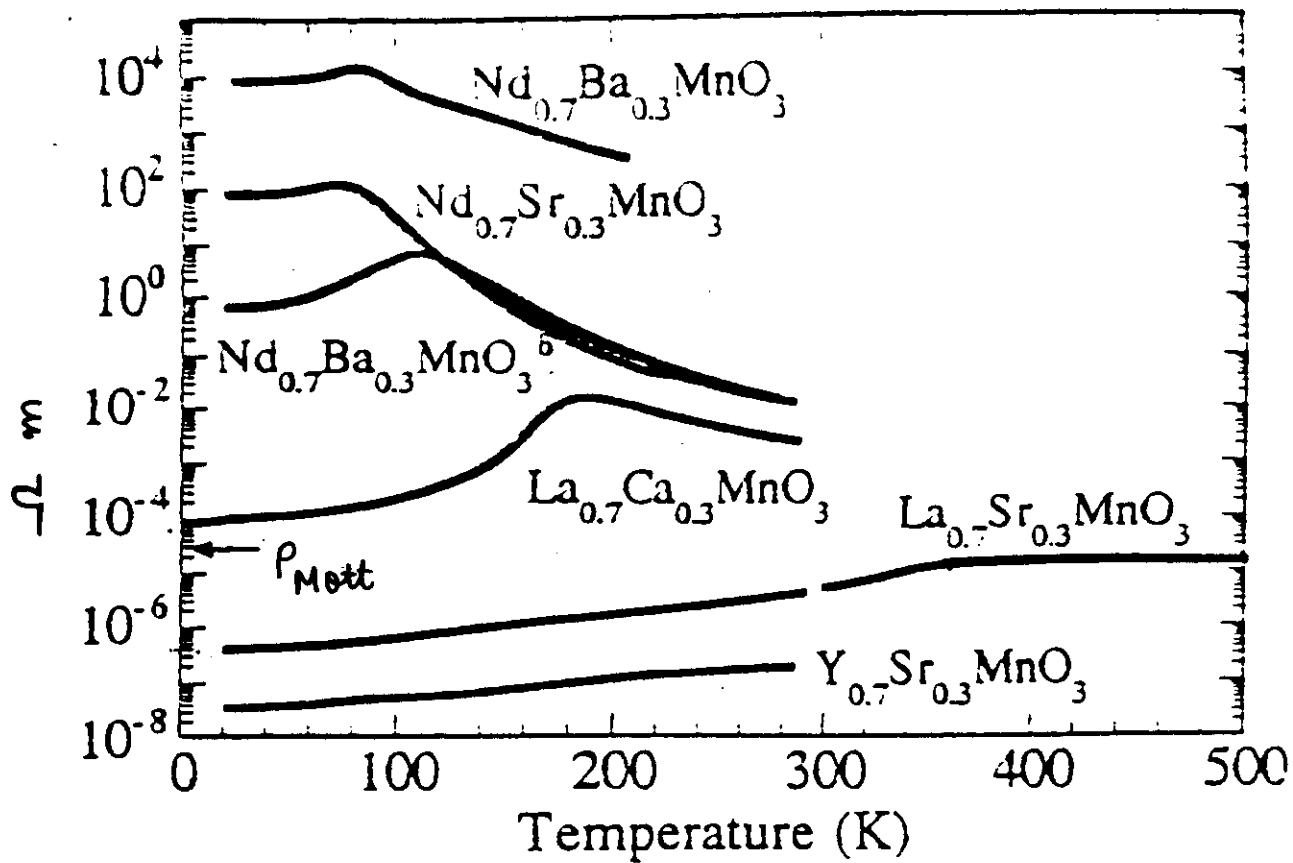
Fits above model.

L_1	ρ
24 μm	$10^{-2} \Omega \text{ cm}$
3	$2 \times 10^{-1} \Omega \text{ cm}$
0.2	$3 \times 10^2 \Omega \text{ cm}$

$$L_2^* \rho_2 \approx 6 \times 10^{-5} \Omega \text{ cm}^2$$

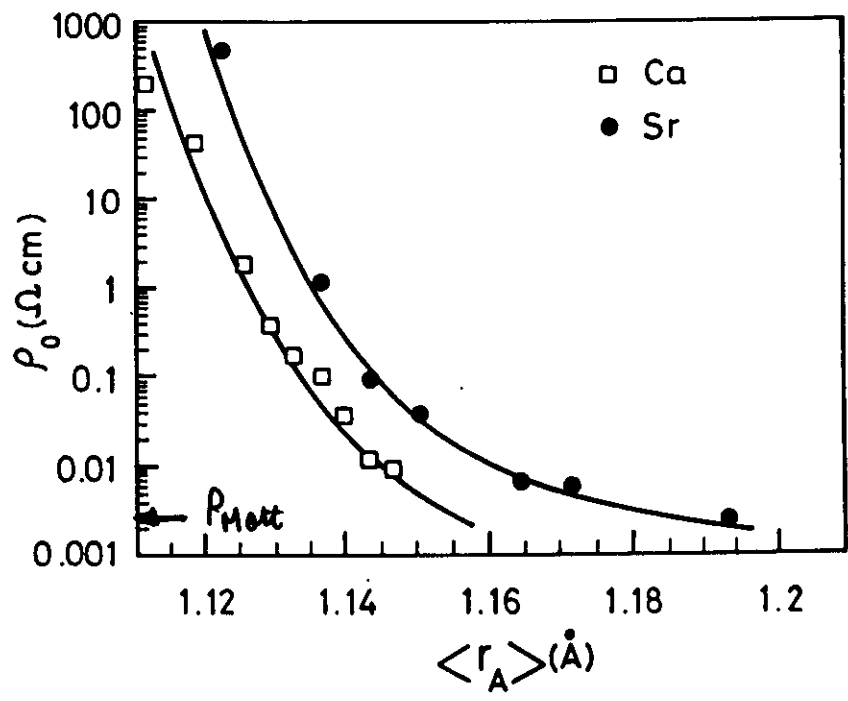
$$L_2 \approx 10 \text{ \AA}$$

$$R_2 \approx 10^5 (h/e^2) !$$



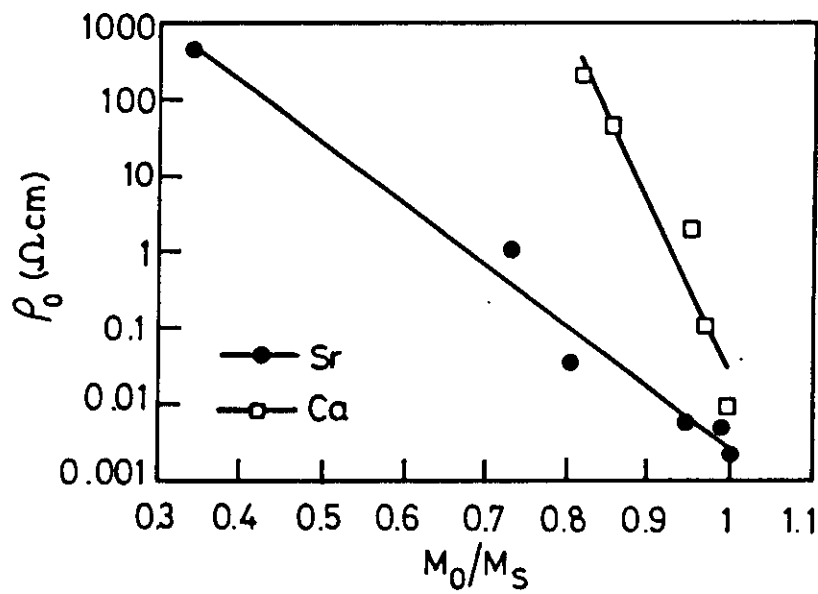
2. Temperature dependence of the resistivity of $x\text{B}^{2+}_x\text{MnO}_3$ thin films (b denotes a polycrystalline ic).

Coey et al



Garcia - Munoz et al

$\langle r_A \rangle$



$$\rho_0 = \rho_{\text{Mett}} \exp \left[\lambda \frac{\delta M}{M_S} \right]$$

$$\rho_{\text{Mett}} \simeq 2 \text{ m}\Omega\text{cm}$$

$$\lambda \simeq 18 \text{ for Sr}$$

$$\lambda \simeq 71 \text{ for Ca}$$

(6)

Garcia-Munoz et al

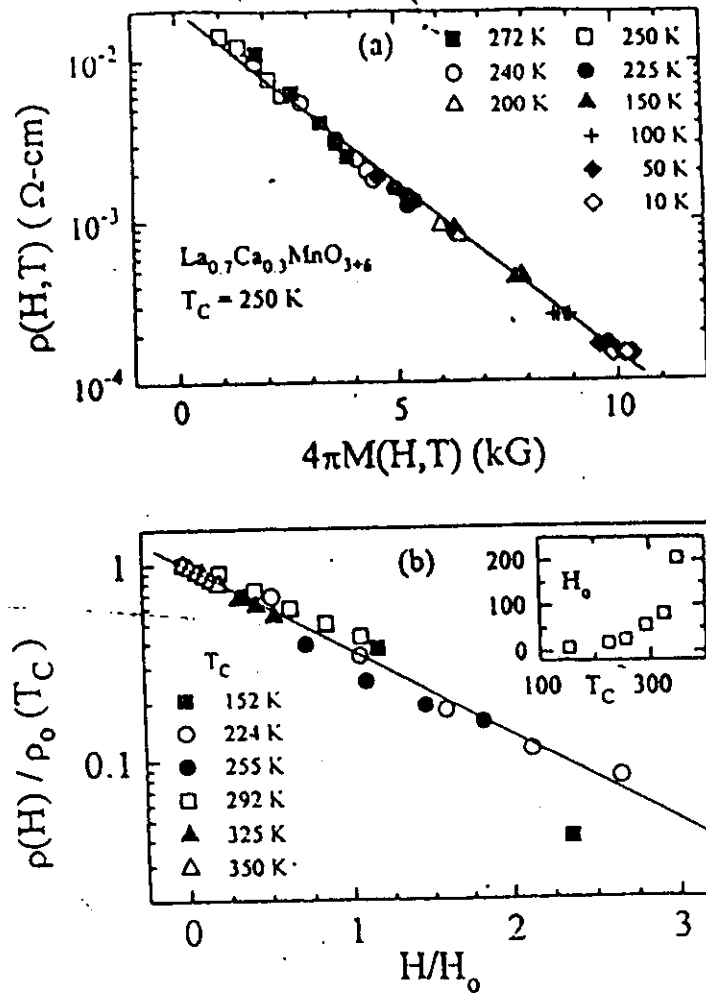


FIG. 4. (a) $\rho(H, T)$ vs. $M(H, T)$ for sample 3. At each T , points are included at $H = 10, 20, 30, 40$, and 50 kOe. The solid line is a least-squares fit to the data. (b) Normalized magnetoresistance at T_c plotted vs. H/H_0 for samples 1-6; the scaling parameter H_0 (in kOe) is plotted against sample T_c in the inset.

Hurdley et al

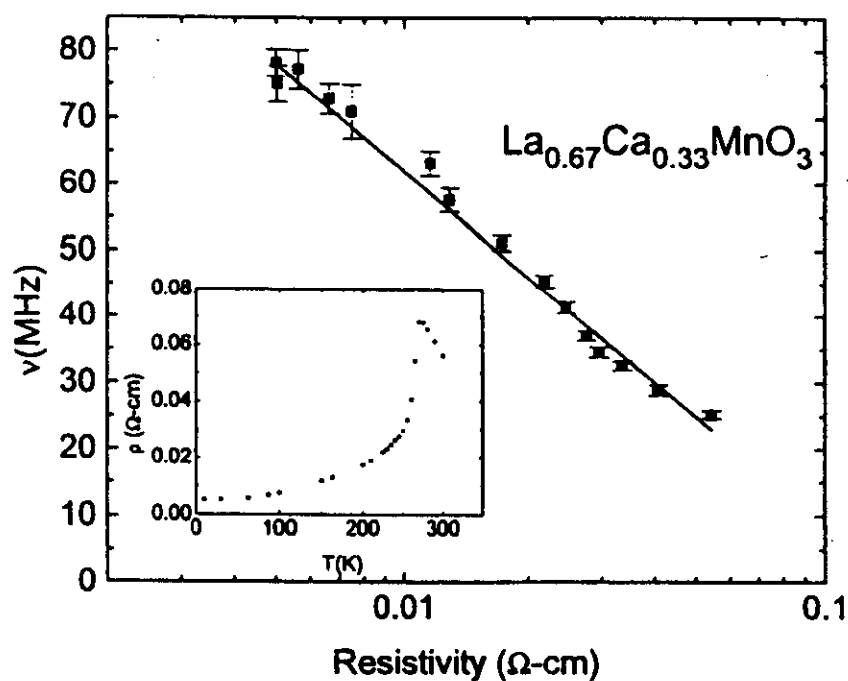


FIG. 2. Temperature dependence of $\nu_\mu(T)$ vs resistivity on a log scale. The solid line is a least squares fit showing $\nu_\mu(T) \propto -\ln[\rho(T)]$. The inset shows resistivity vs temperature.

Heffner; Uemura . . .

(8) Optical conductivity

19

$n_{\text{eff}} \sim 0.14 n$
 m^* enhanced?

γ (electronic heat capacity)
 shows no sign of it

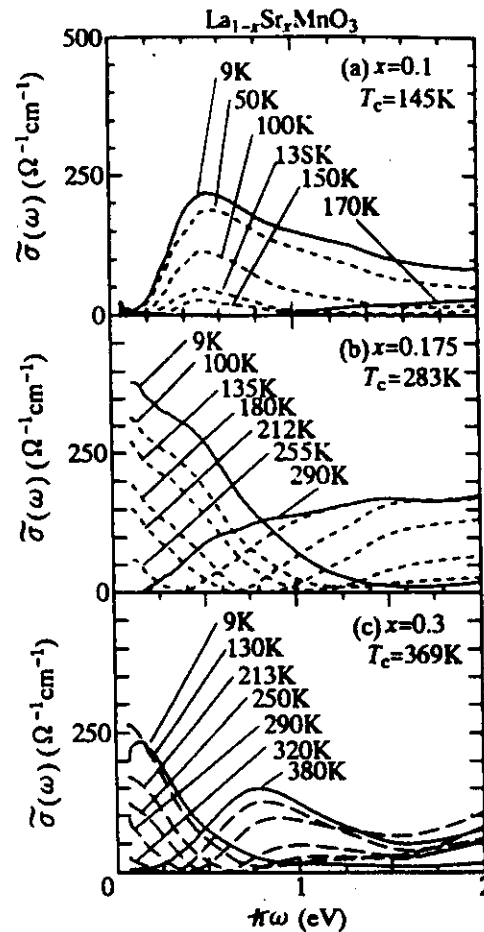
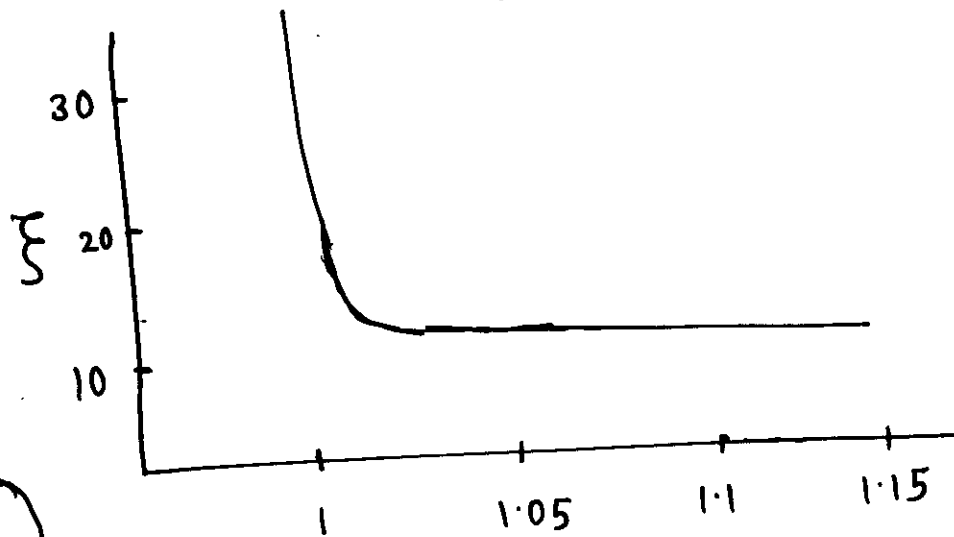


FIG. 6. Reduced optical conductivity spectra which are derived by subtracting the temperature independent part (the hatched curves in Fig. 5) at various temperatures in $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$: (a) $x=0.1$, (b) $x=0.175$, and (c) $x=0.3$. The far-infrared region dominated by the optical phonons is omitted to avoid complexity.

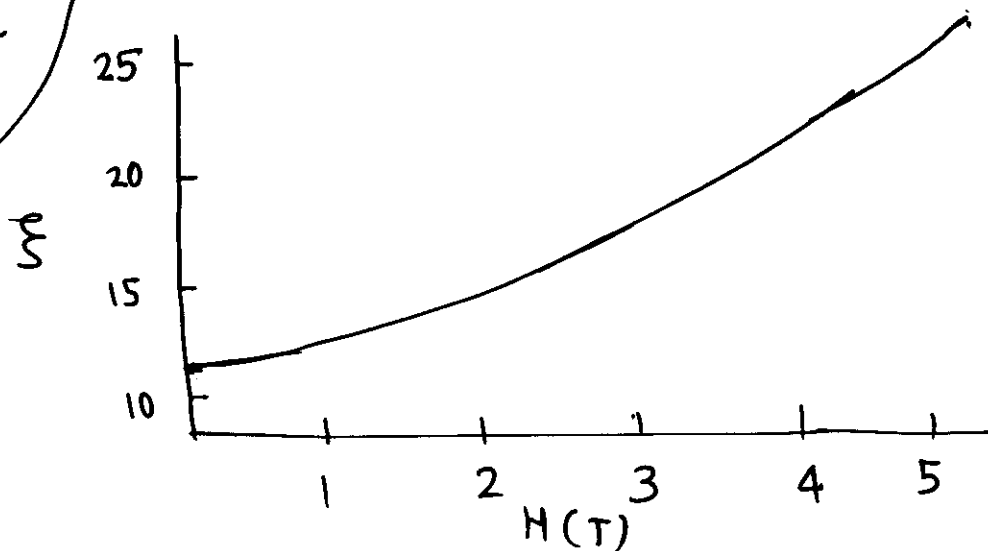
Okamoto, ~ Tokura

(iv) Behaviour near and above T_c :- (20)

1. Considerable short range order
SANS with $\xi_{\text{mag}} \approx 12 \text{ \AA}$
 $T \approx 1.2 T_c$



de Teresa
Ibarra
et al



ξ_{mag} increases rapidly with field.

2. Carriers localize above T_c

$$\left(\frac{\mu_0 H \rho_{xx}}{\rho_{Hall}} \right) \sim \mu \quad \text{mobility}$$

Use this to find n_e .

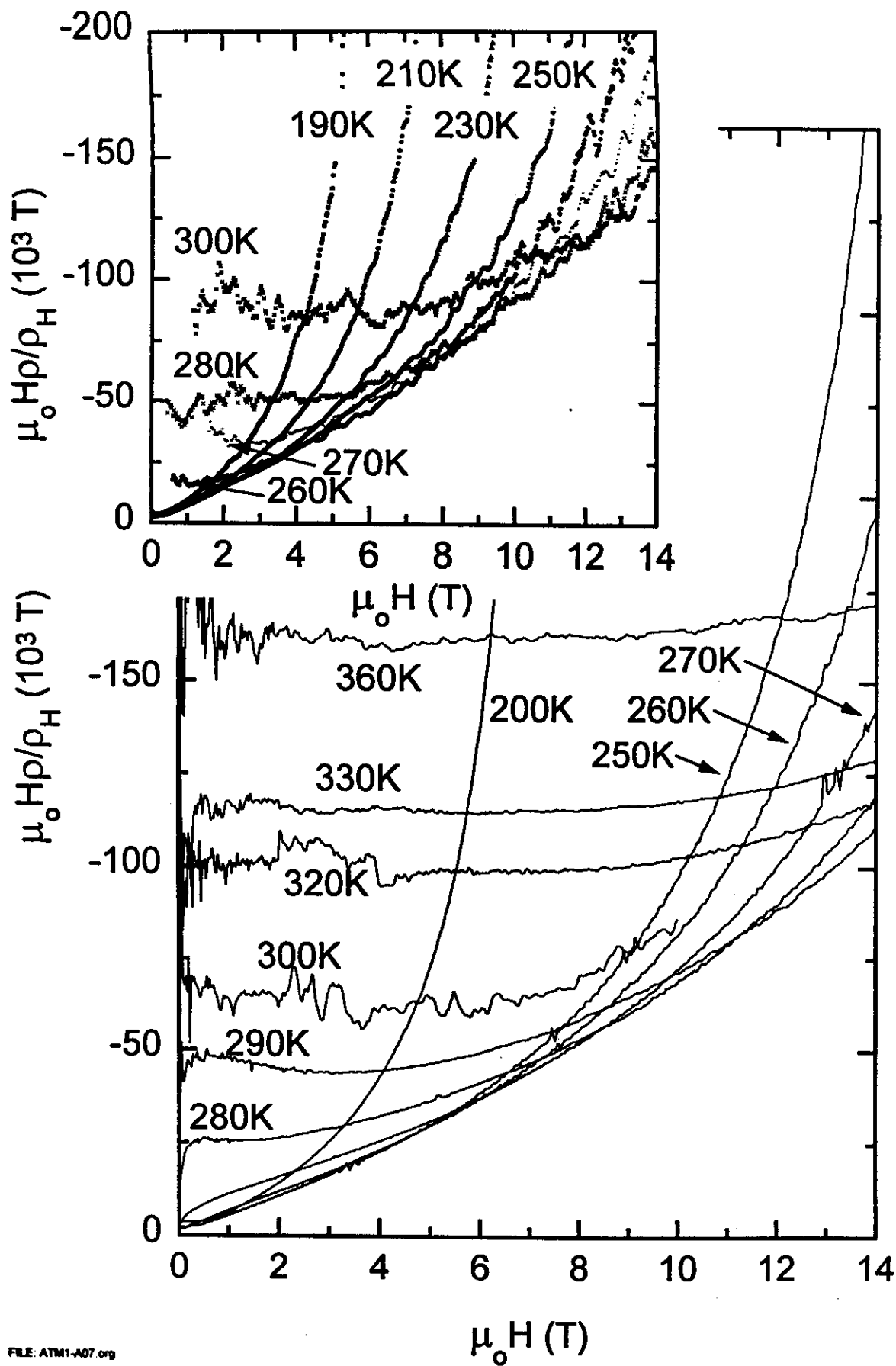
(i) mobility weakly field dependent
at low H

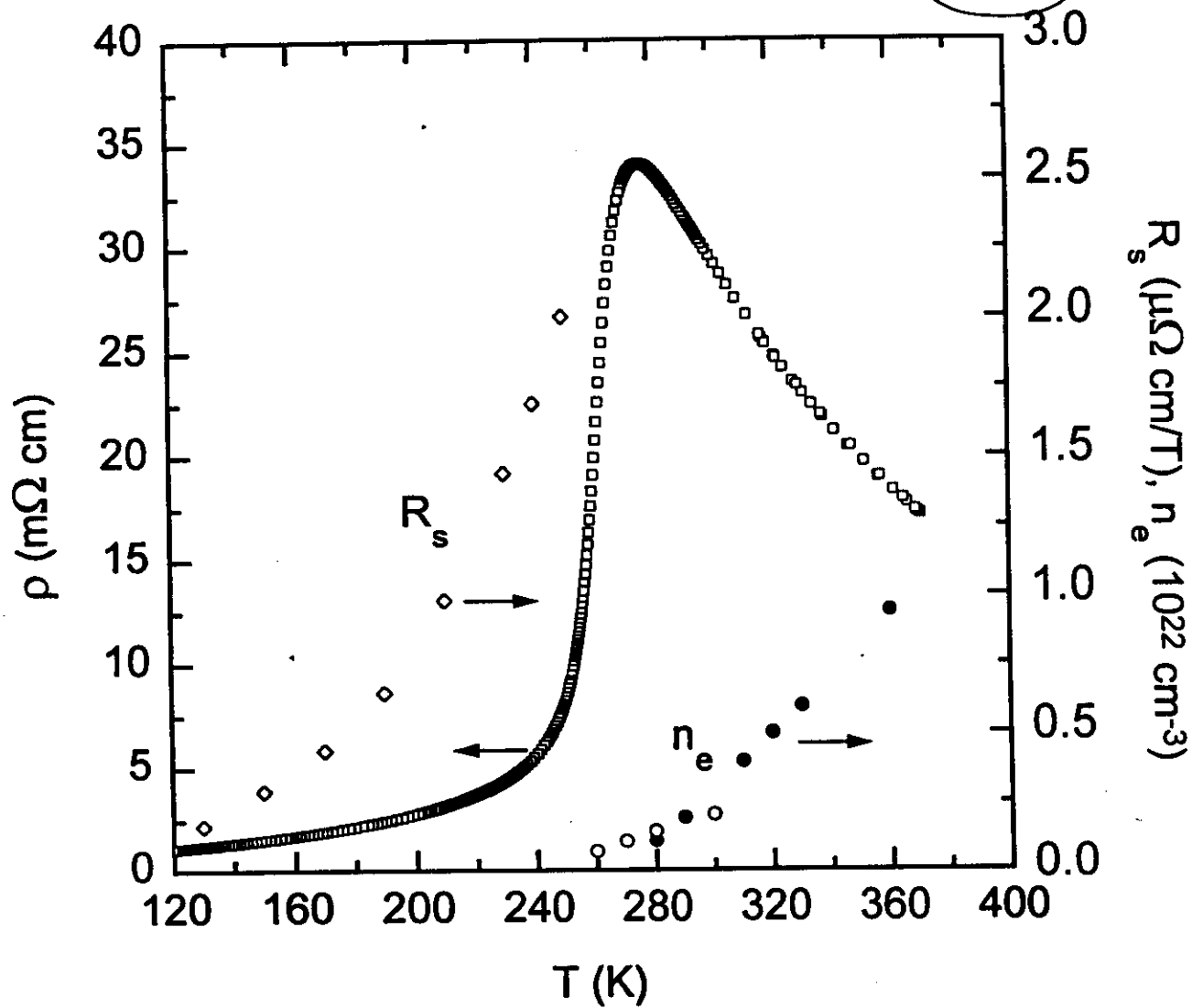
(ii) n_e strongly T dependent.

Analysis complicated due to

Anomalous Hall Effect ($\propto M$)

strong ^{and magnetic} field dependence of
 ρ_{xy} , ρ_{xx} . . .





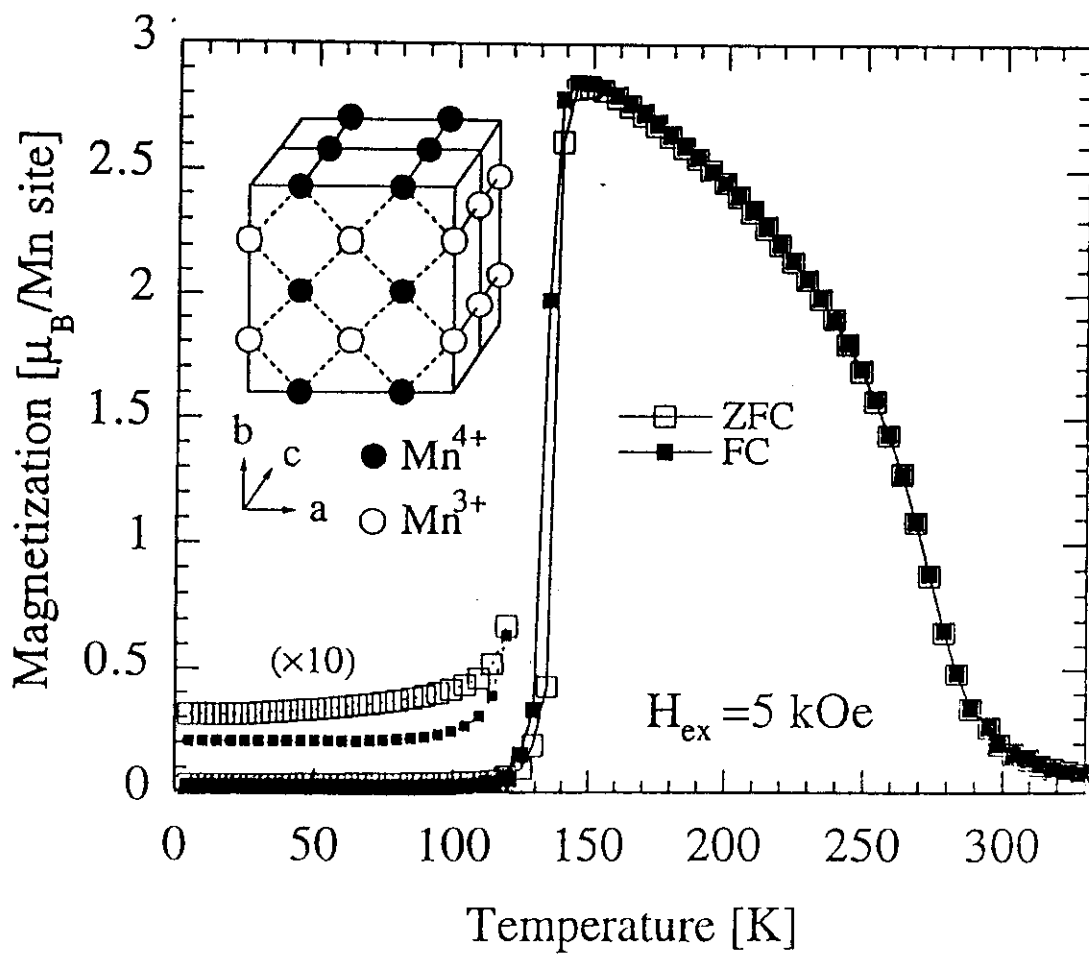
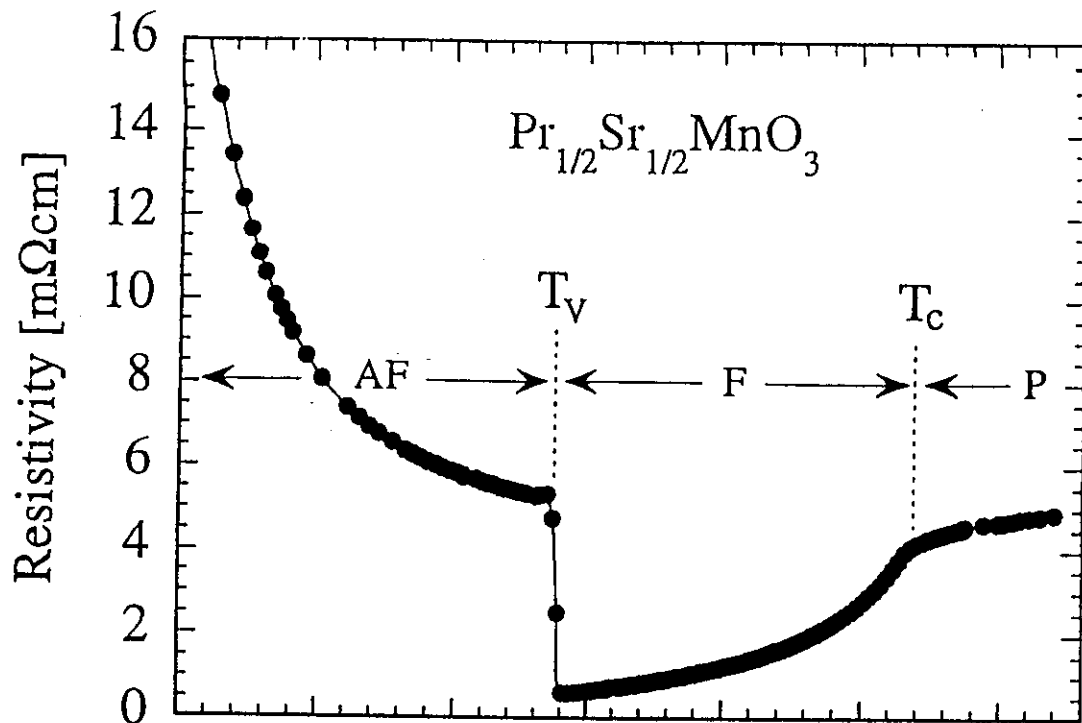
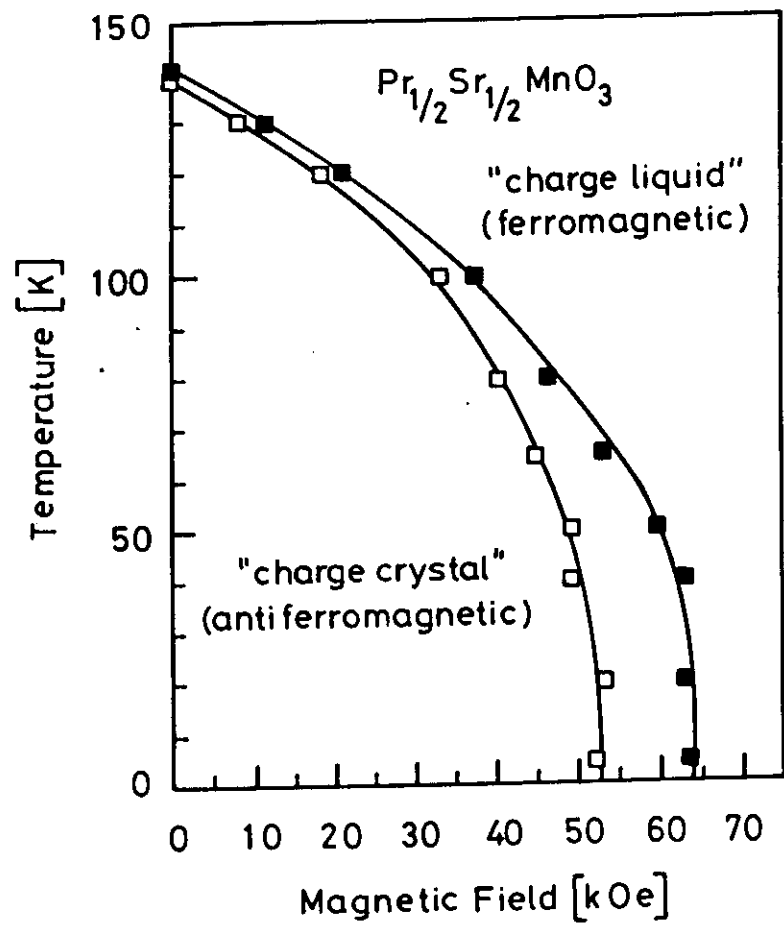


Figure 1. Y. Tomioka et al.

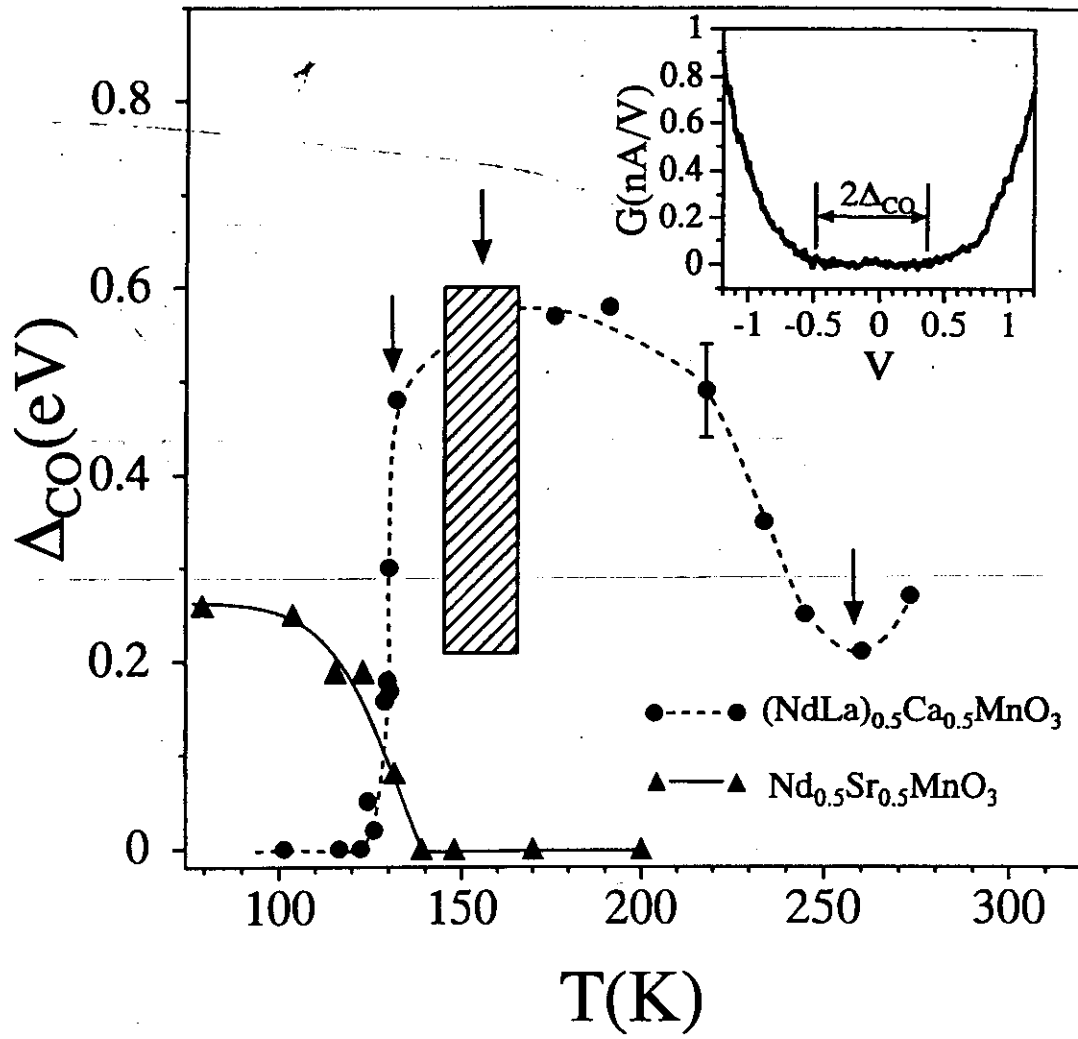
(25)

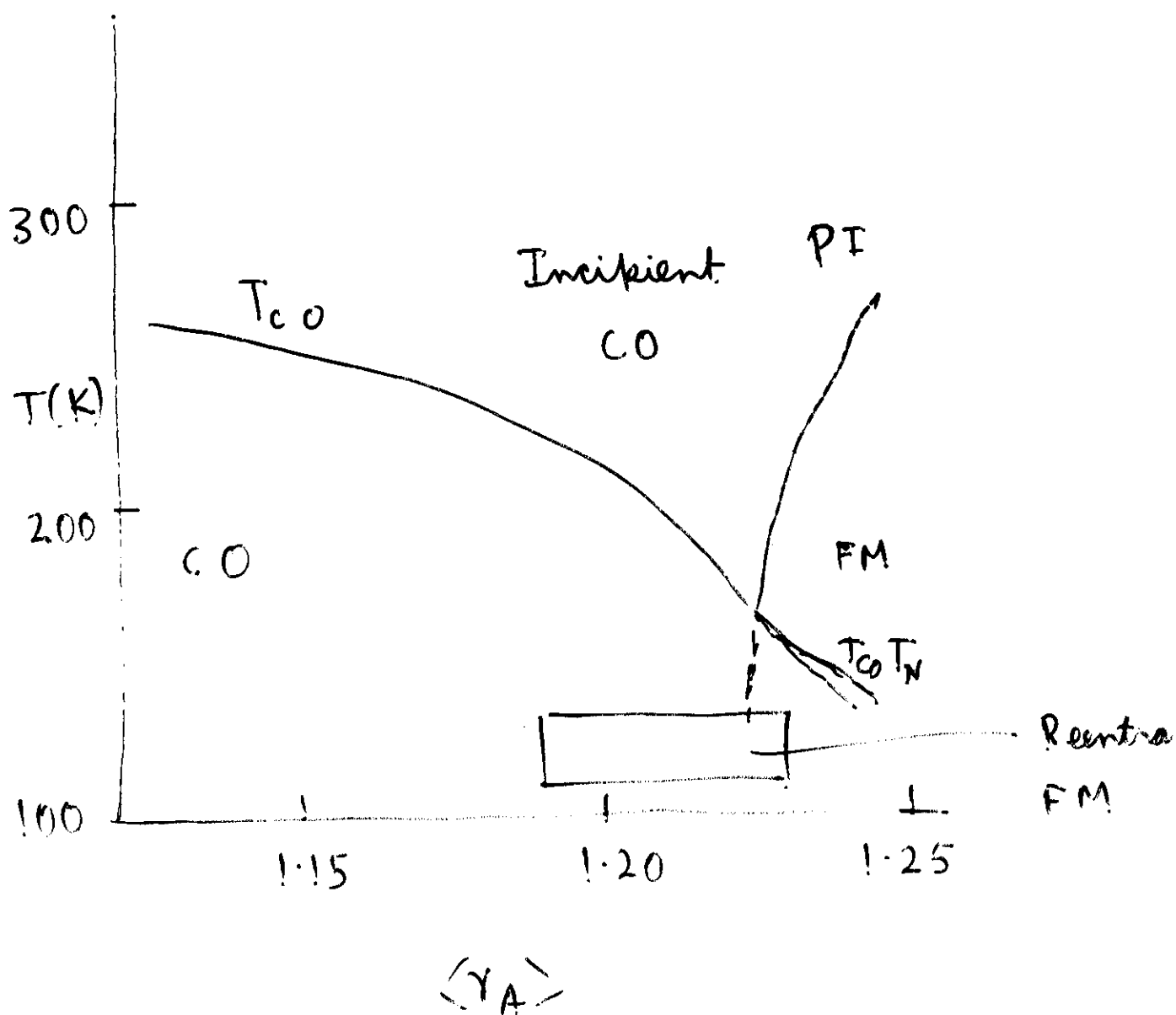
Tokura
et al



$$\begin{aligned} 5 \text{ Tesla} &\approx 5 \times 3.5 \times \frac{2}{3} \\ &\approx 12 \text{ K} \end{aligned}$$

(9)





Conclusion :-

(30)

- (i) The ingredients are known
(basic interactions)
but we don't fully know
how to cook
(put them together so as
to describe what is seen).
- (ii). There is a very effective
(exponentially effective ?)
localizing mechanism
that is poorly understood.
- (iii) Because of (i) and
competing interactions,
rich variety of phases.

