



UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
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INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS  
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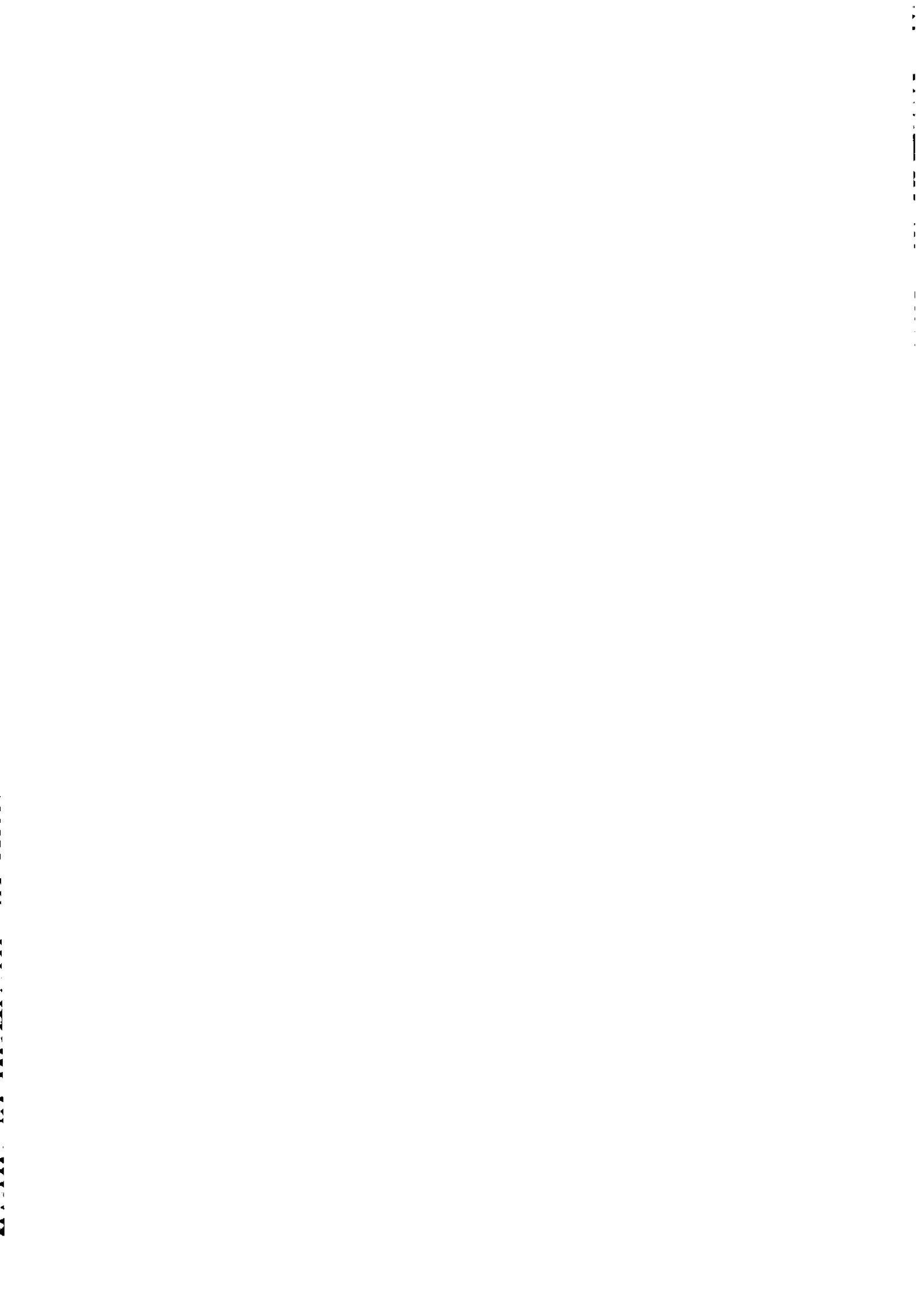
## WINTER COLLEGE ON OPTICS

9 - 27 February 1998

### *Confocal Scanning Microscopy*

**T. Wilson**

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# Confocal Scanning Microscopy

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# Confocal Scanning Microscopy

This short course is divided into three lectures.

(i) Introduction to confocal microscopy

In this lecture the confocal optical system is introduced and the origins of the resolution enhancement and the optical sectioning or depth discrimination property are explained. The consequences of this unique imaging mode are illustrated with many examples.

(ii) Imaging modes in Confocal microscopy

The three-dimensional imaging of the confocal microscope arises because of the use of a point, pinhole, detector. The image formation becomes more versatile if optical fibres rather than pinholes are used to detect the image signal. In this way differential amplitude and differential phase contrast images may be obtained in addition to the confocal image. Finally, various interference and optoelectronic implementations will be described.

(iii) Real time Confocal microscopy with white light

The most common configuration of confocal microscope uses a laser as light source and does not usually form an image in real time. These drawbacks may be alleviated to some extent by constructing a number of parallel confocal systems which image adjacent parts of the object. This is the basis of the tandem scanning or Nipkow disc based microscopes which permit real time imaging with white light sources. However these systems are light inefficient and so three relatively new approaches will be discussed. They are based on the use of microlens arrays and aperture correlation techniques.

# Books on Confocal Microscopy

T. Wilson and C.J.R. Sheppard. Theory and Practice of Confocal Microscopy, Academic Press, 1984. A little dated now but contains the basic optical theory.

T. Wilson (Editor). Confocal Microscop, Academic Press, 1990. A multi-author volume covering many aspects and applications of confocal microscopy.

J.B. Pawley (Editor). Handbook of Biological Confocal Microscopy, Plenum, 1995. A multi-author volume concentrating on biological applications. The book also has details of many commercially available systems.

Min Gu. Principles of three-dimensional imaging in confocal microscopes, World Scientific, 1996. An extremely thorough theoretical discussion based on the use of the three dimensional transfer function approach.

T.R. Corle and G.S. Kino. Confocal Scanning Optical Microscopy and Related Imaging Systems, Academic Press, 1996. A useful book concentrating on the non-biological aspects and applications of confocal microscopy.

These are the main book references. The main source of journal articles is probably the following:

Applied Optics  
Optics Letters  
Journal of Optical Society of America  
Optics Communications  
Journal of Modern Optics  
Journal of Microscopy  
Bioimaging  
Scanning

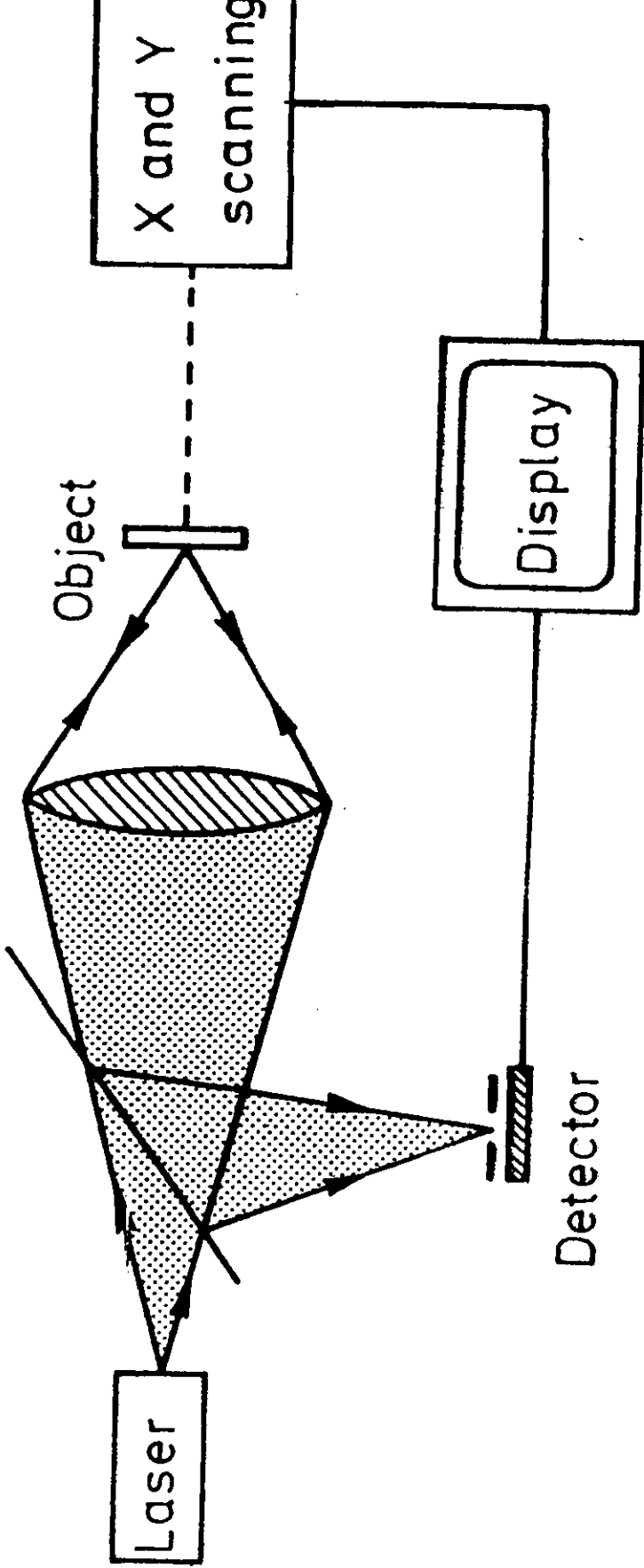
# Confocal Microscopy

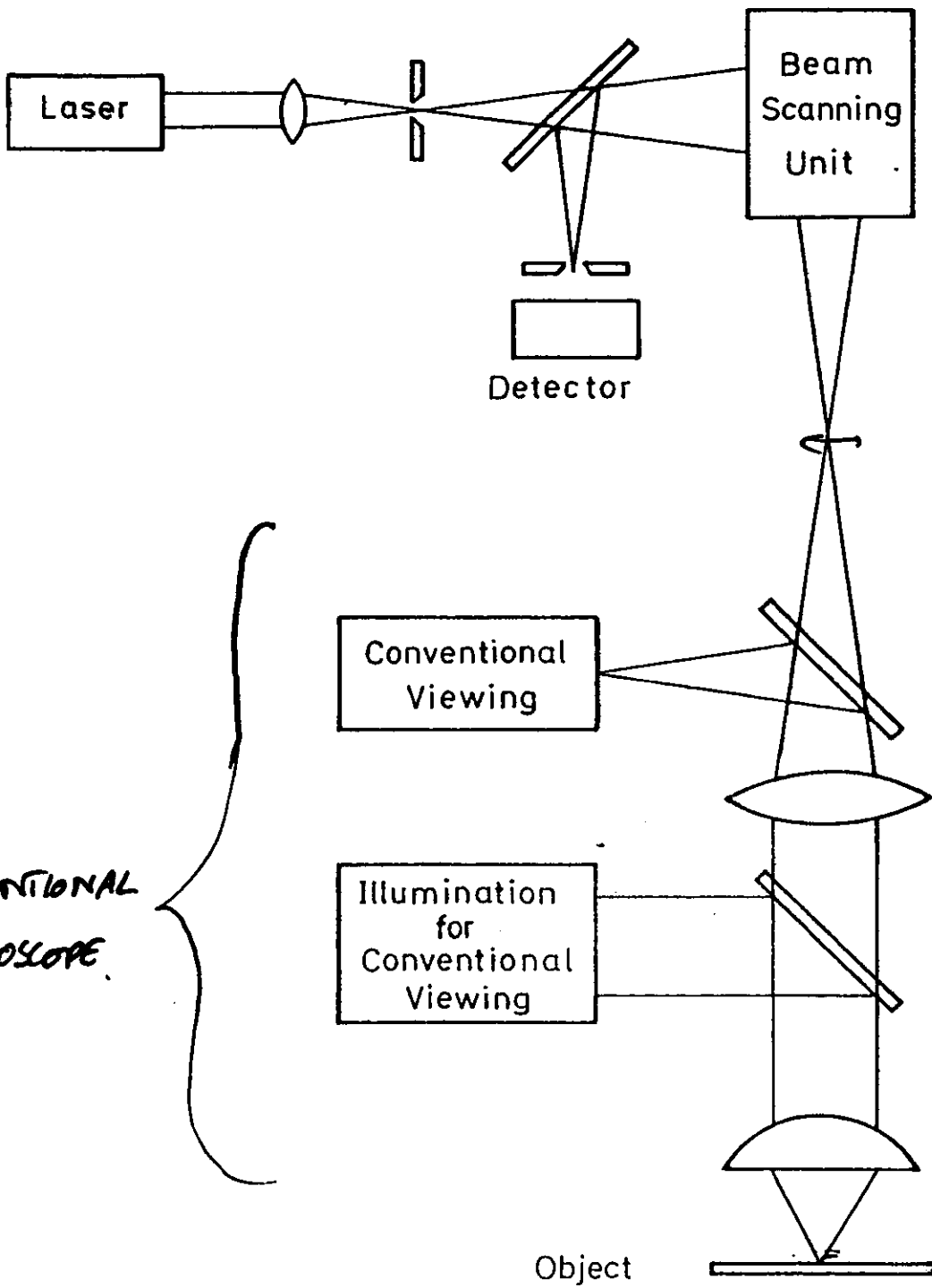
- Implementations
- Lateral Resolution
- Axial Resolution



"3-D" imaging

Examples.



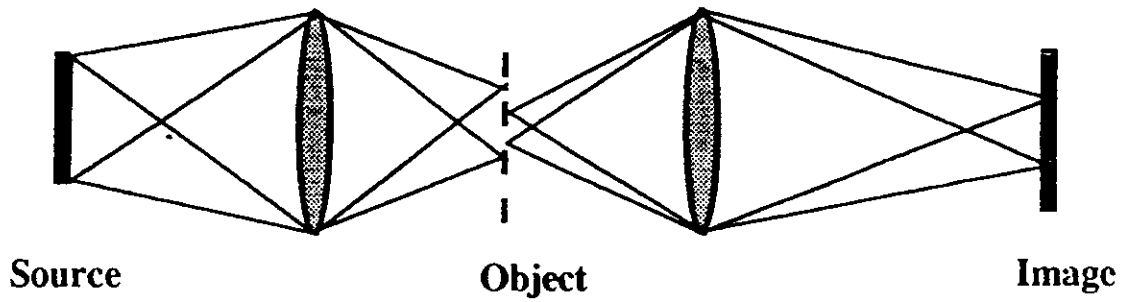


CONVENTIONAL  
MICROSCOPE

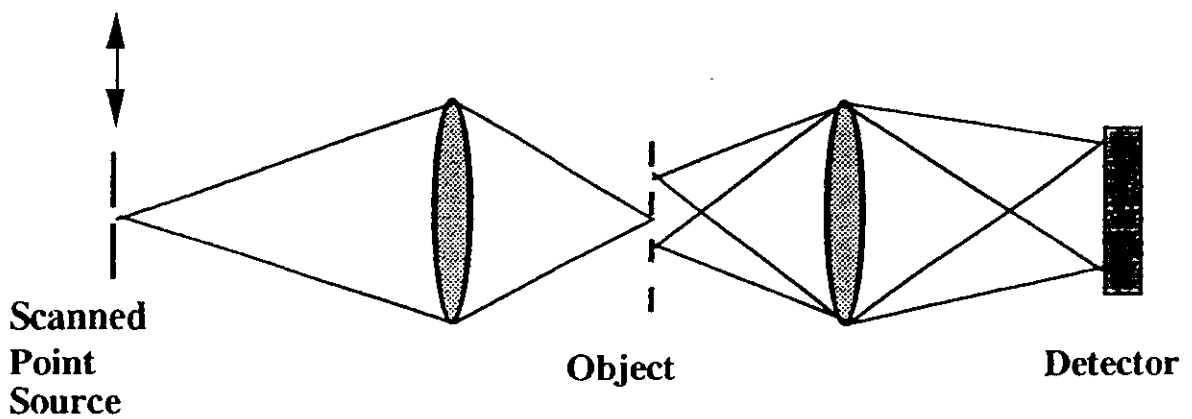
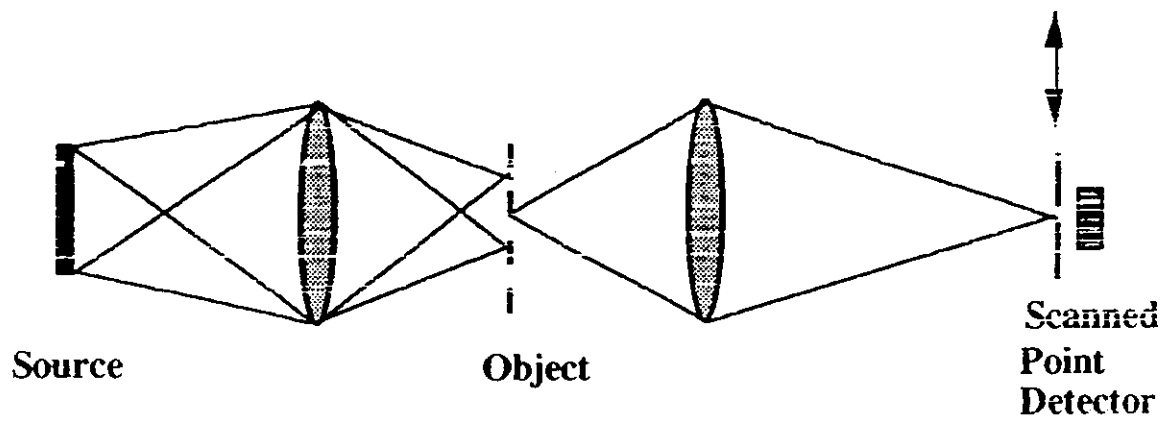
Object



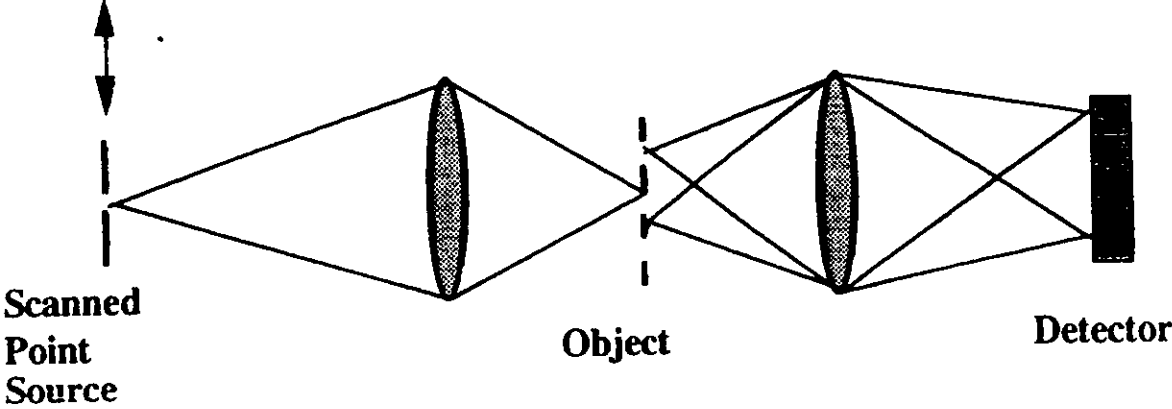
## Conventional Microscope



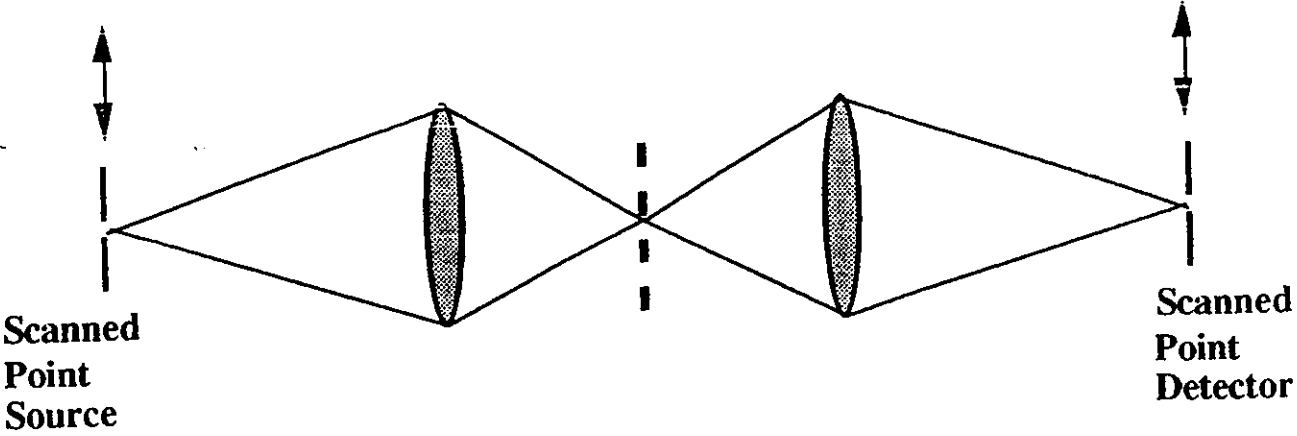
## Scanning Microscope



# Scanning Microscope



# Confocal Microscope



# Confocal Imaging

①. Coherent optical system

$$I = |h_1 h_2 \otimes t|^2$$

↑  
correlation

$h$  is point spread function (amplitude) of lens

$$L \approx \mathcal{F}\{P\}$$

Ex point object

$$I = |h_1 h_2|^2 = \left( \frac{2J_1(v)}{v} \right)^4$$

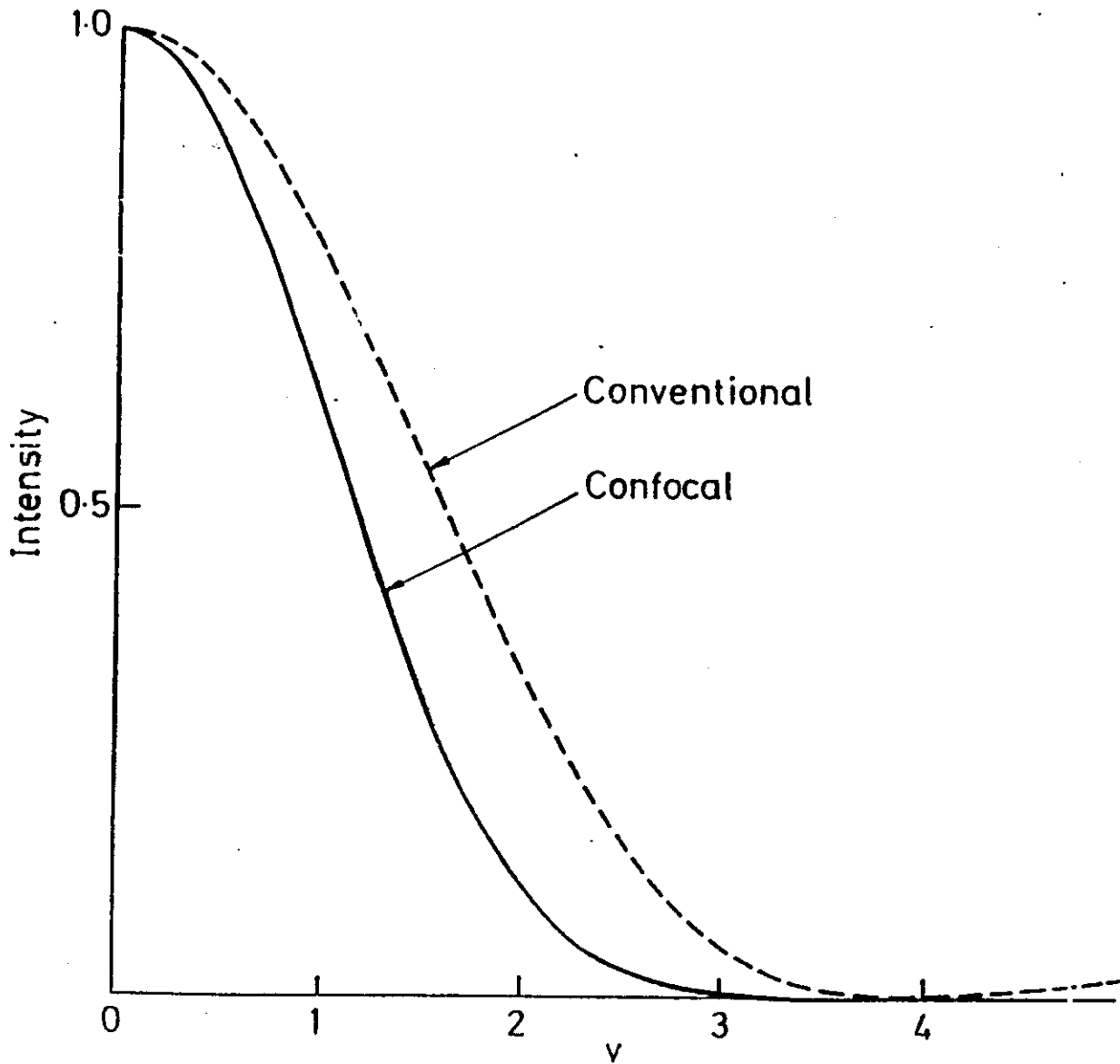
conventional

$$I = |h_1|^2 = \left( \frac{2J_1(v)}{v} \right)^2$$

$$v = \frac{2\pi}{\lambda} \cdot r \cdot \sin \alpha$$

↑  
N.A. of lens

Image of a Point Object - Confocal.  
Conventional.



# Point Detector - Coherent Optical System

$$I = |h_1 h_2 \otimes t|^2$$

Point Object

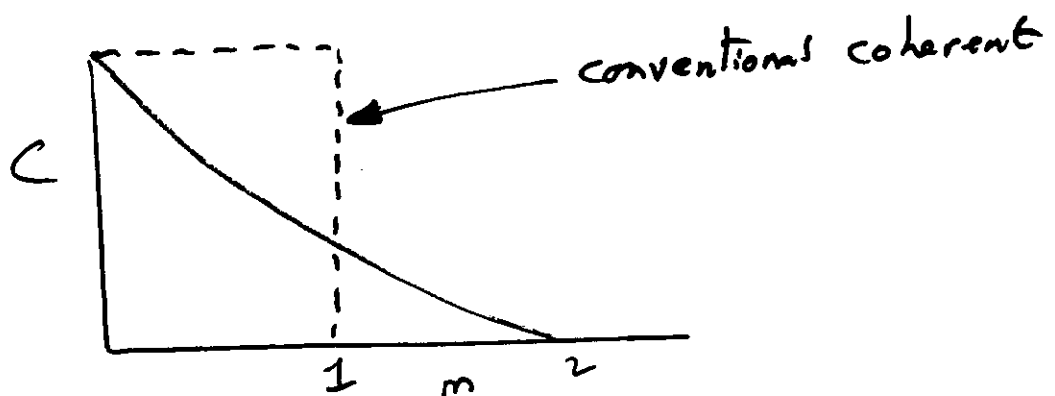
$$I = \left[ \frac{2 J_1(v)}{v} \right]^4$$

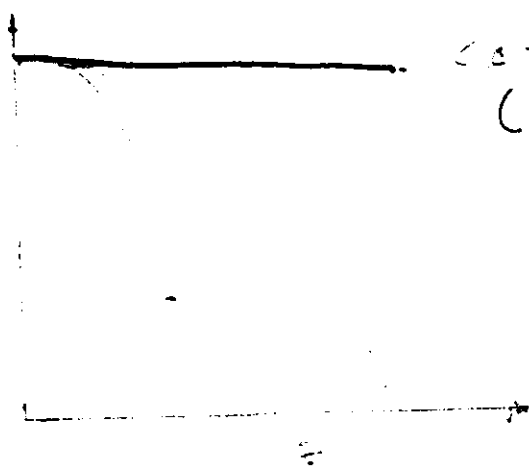
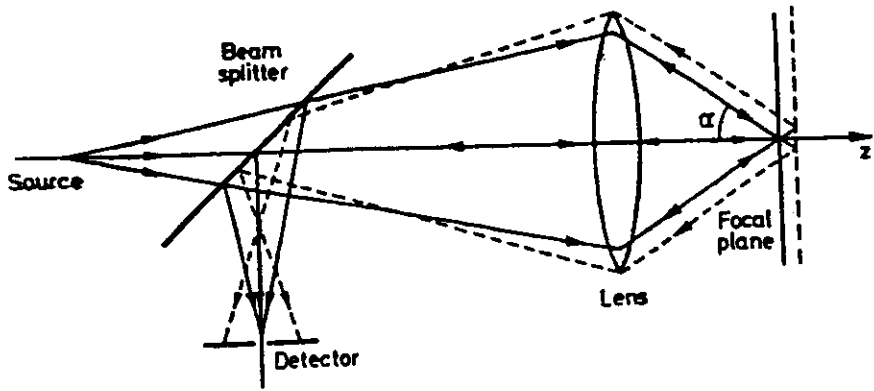
compare conventional microscope

$$\left[ \frac{2 J_1(v)}{v} \right]^2$$

Transfer function

$$C(m, n) = P_1 \otimes P_2$$

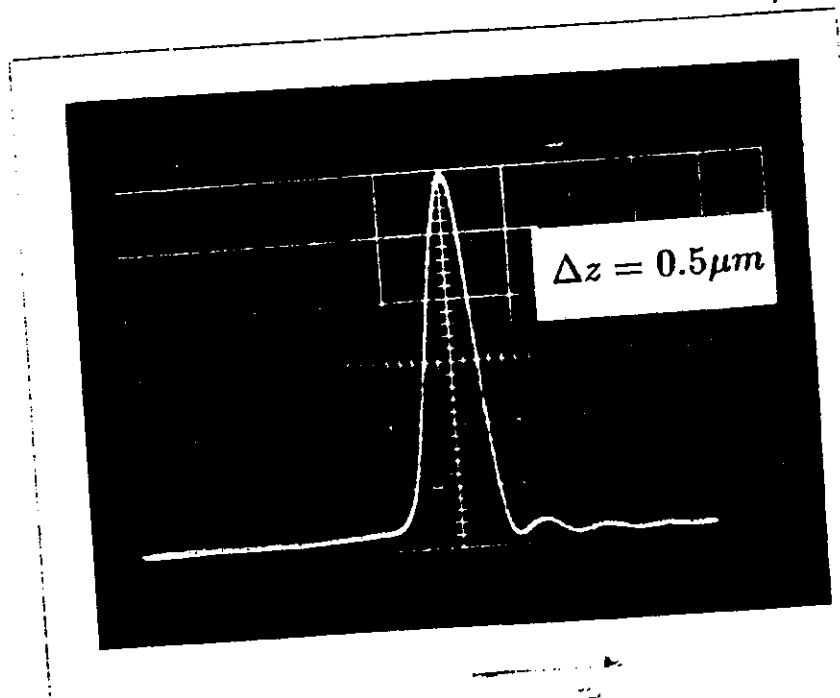




convention!  
(no pinhole)

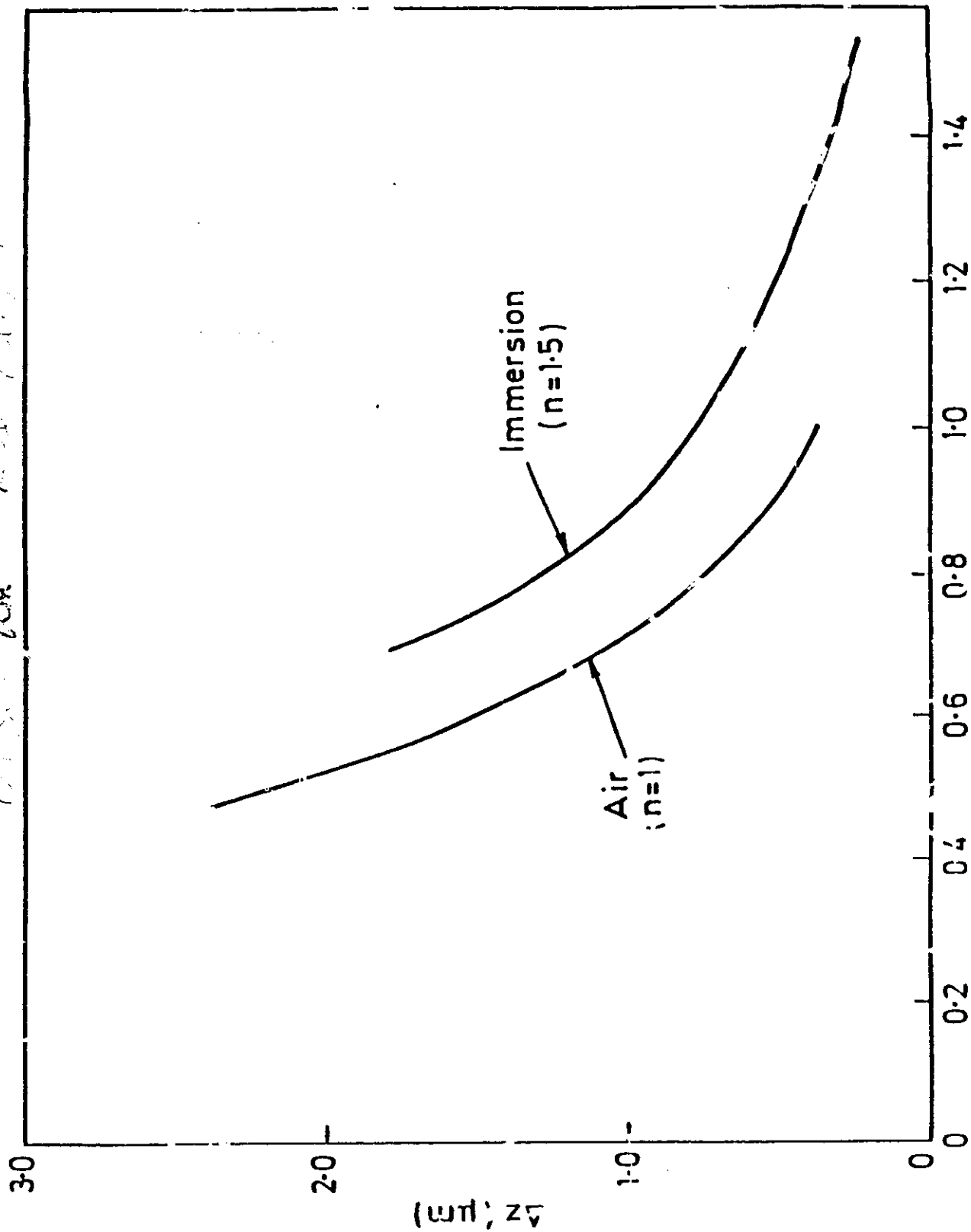
is possibility of through-focus series of images  
use plane reflector as metric of sectioning.

$V(z)$



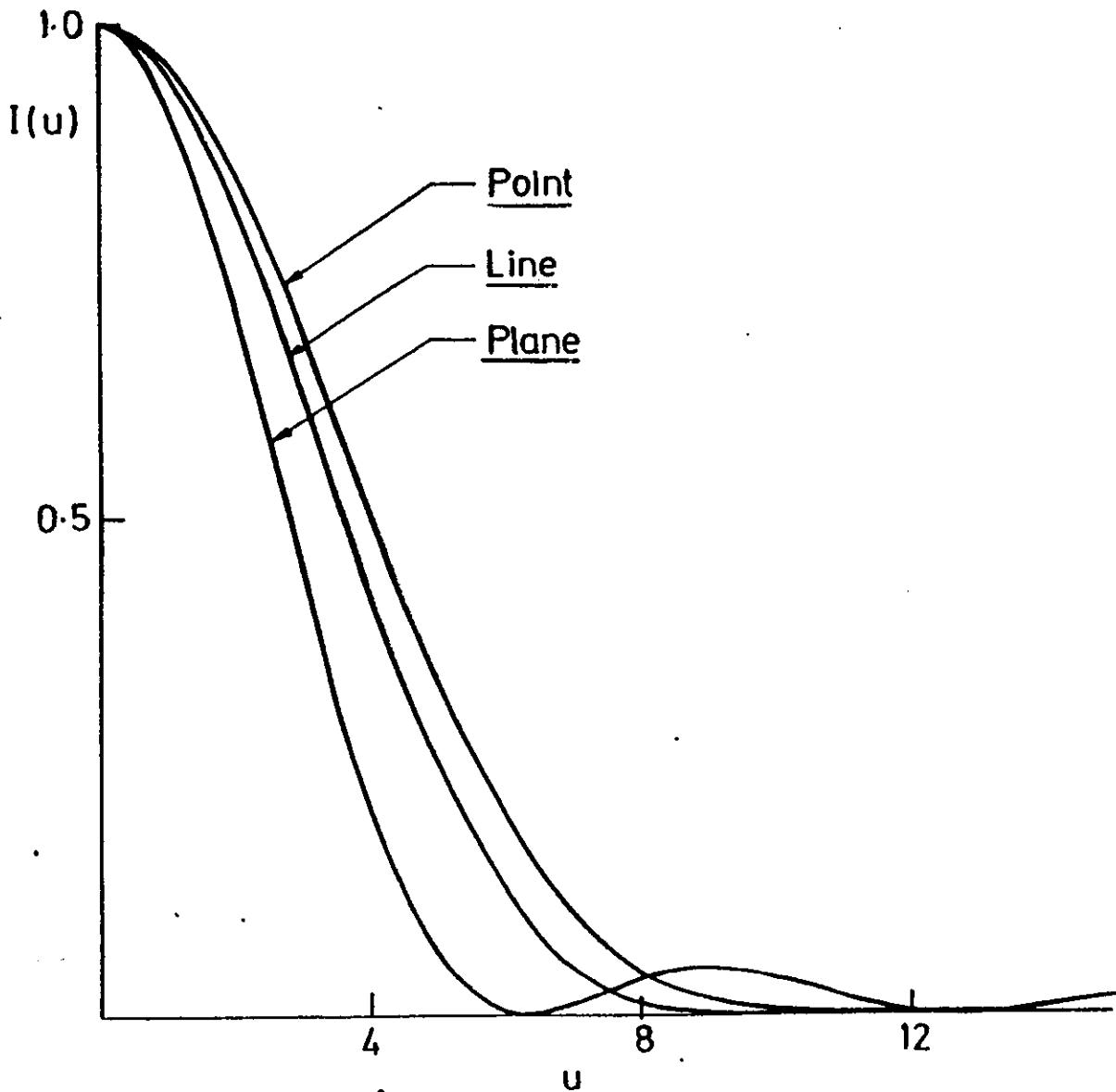
...  
...

0.033 um  $R_{eff} = 1.0$



N.A.

# Sectioning Strength – object dependent.



$$u \sim z$$

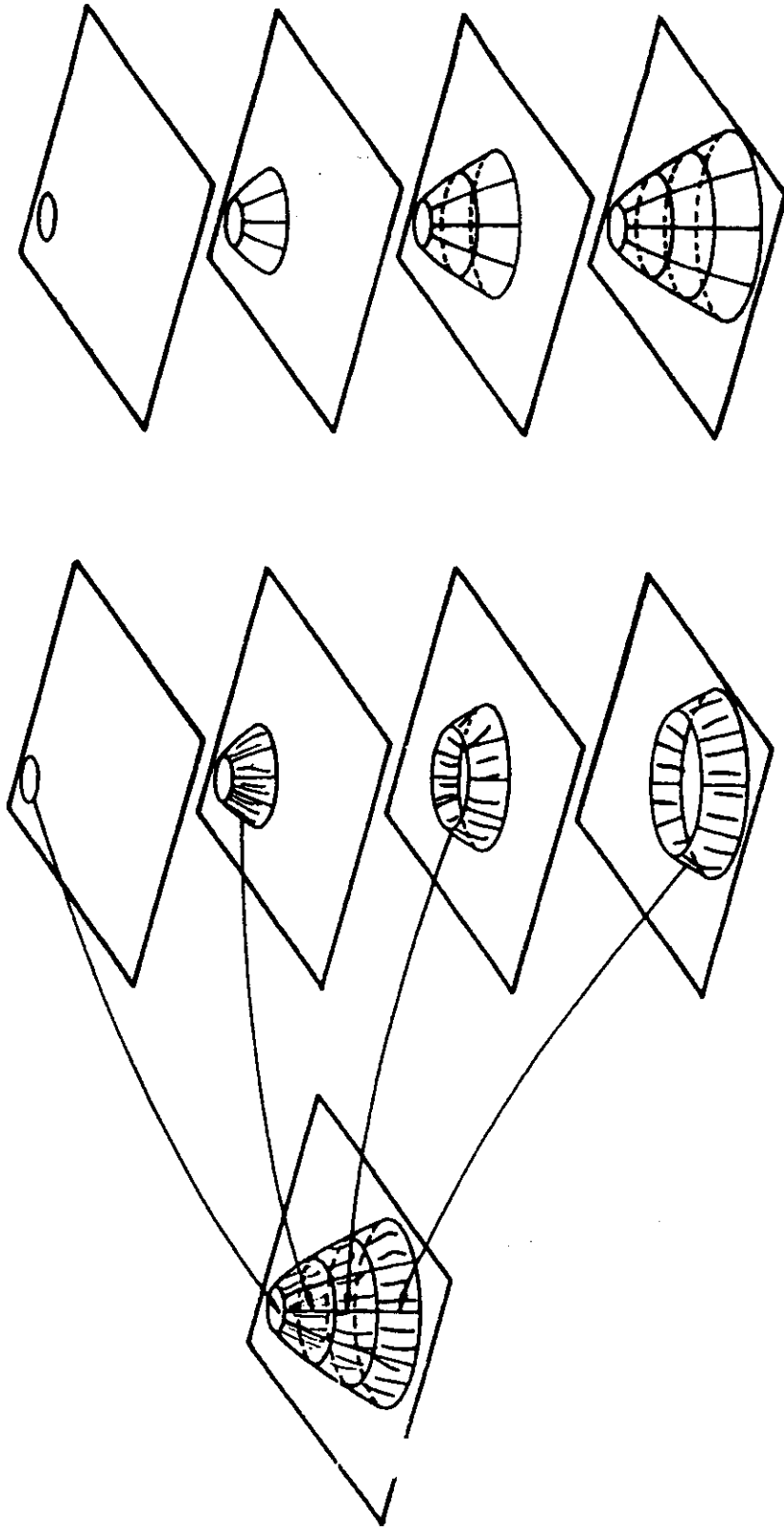
plane

$$I(u) = \left( \frac{\sin \frac{u}{2}}{\frac{u}{2}} \right)^2$$

$$\left[ u = \frac{8\pi}{\lambda} \cdot z \cdot \sin^2 \frac{\alpha}{2} \right]$$



"Optical sections"



Focus position

Extended focus  
(SUM ALL OPTICAL  
SECTIONS)

## LIMITS OF RESOLUTION

### LATERAL RESOLUTION (Full width half maximum) (confocal)

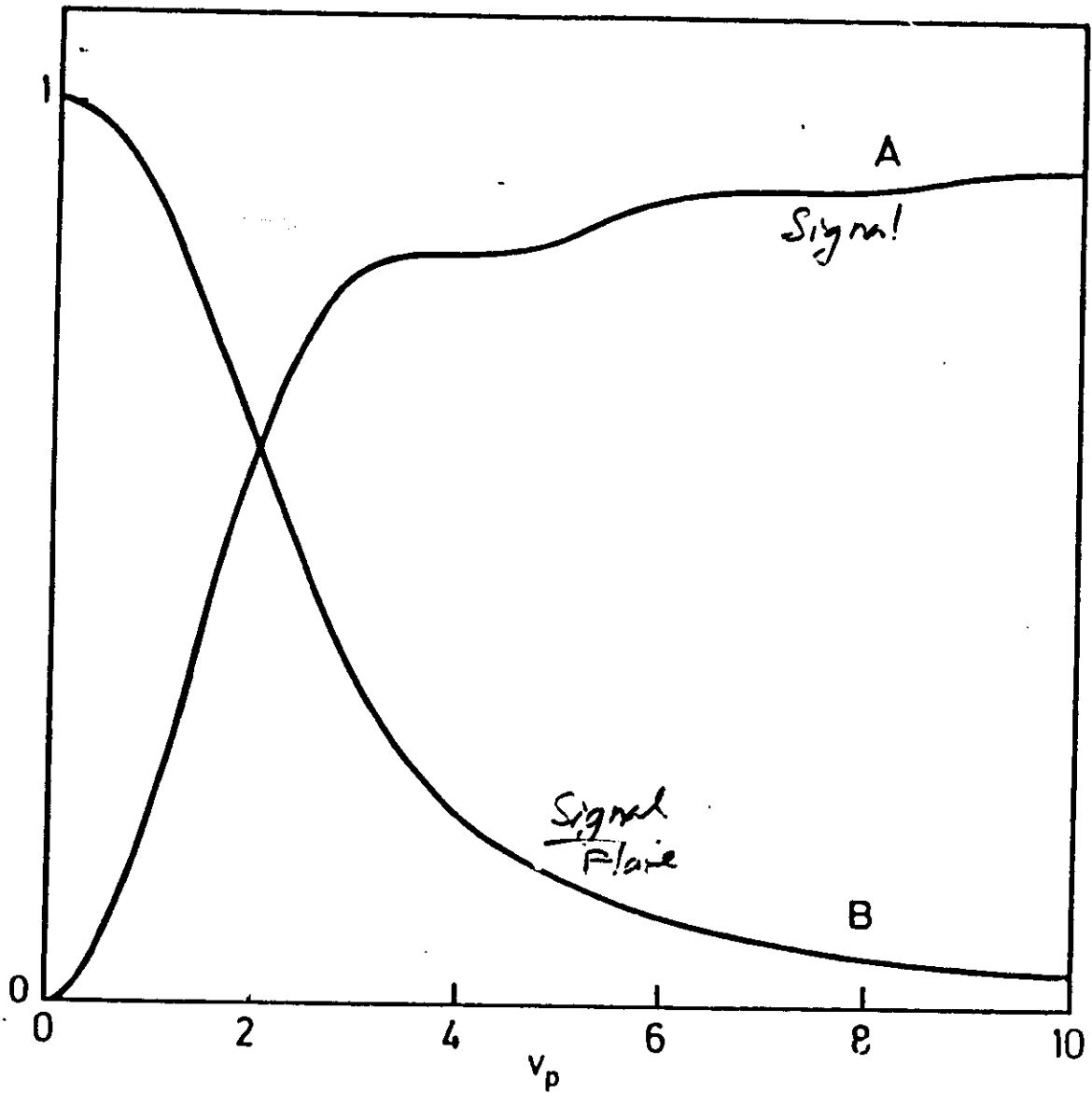
	<u>Wavelength</u>	
NA	<u>442 nm</u>	<u>193 nm</u>
.95	.20	.09 $\mu\text{m}$
1.4 (immersion)	.14 $\mu\text{m}$	.06 $\mu\text{m}$

### DEPTH RESOLUTION (FWHM) (Confocal)

	<u>Wavelength</u>	
NA	<u>442 nm</u>	<u>193 nm</u>
.95	.34 $\mu\text{m}$	.15 $\mu\text{m}$
1.4 (immersion)	.23 $\mu\text{m}$	.10 $\mu\text{m}$

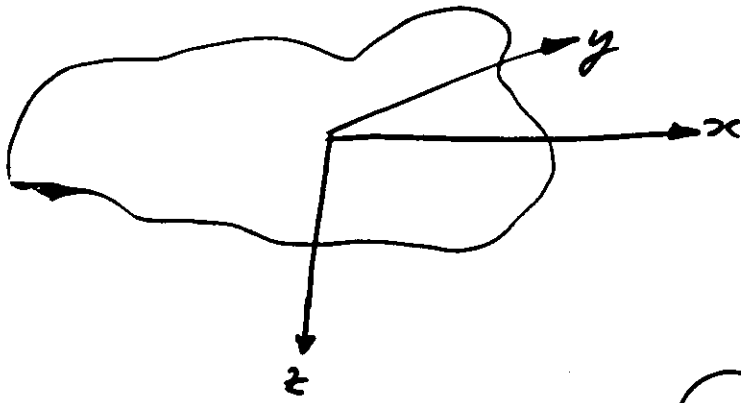
N.B. Depth sensitivity is better than 1  $\text{\AA}$  (interference methods)

# Flare and Scatter



$$v_p = \frac{2.5}{r} r_p \approx 8.5$$

Pinhole rejects light from everywhere but the object.



choose by "focus"

Confocal section  $I(x, y, z)$  (x-z image)

sectioning stronger than depth of focus.

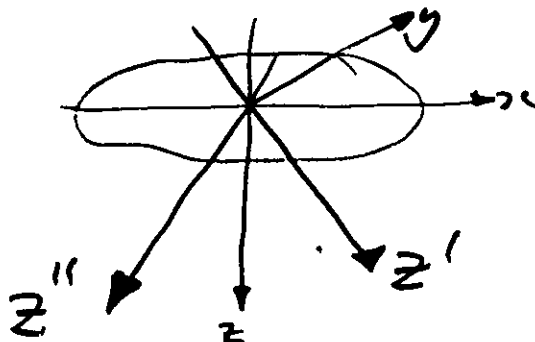
Extended focus  $I_{EF}(x, y) = \int_{-\infty}^{+\infty} I(x, y, z) dz$

introduce axial scan

Auto focus  $I_{AF}(x, y) = I_{max}(x, y)$

Profile  $z_{max}$  corresponding to  $I_{max}(x, y)$

stereo stack sections at angles to give L.H. and R.H. view

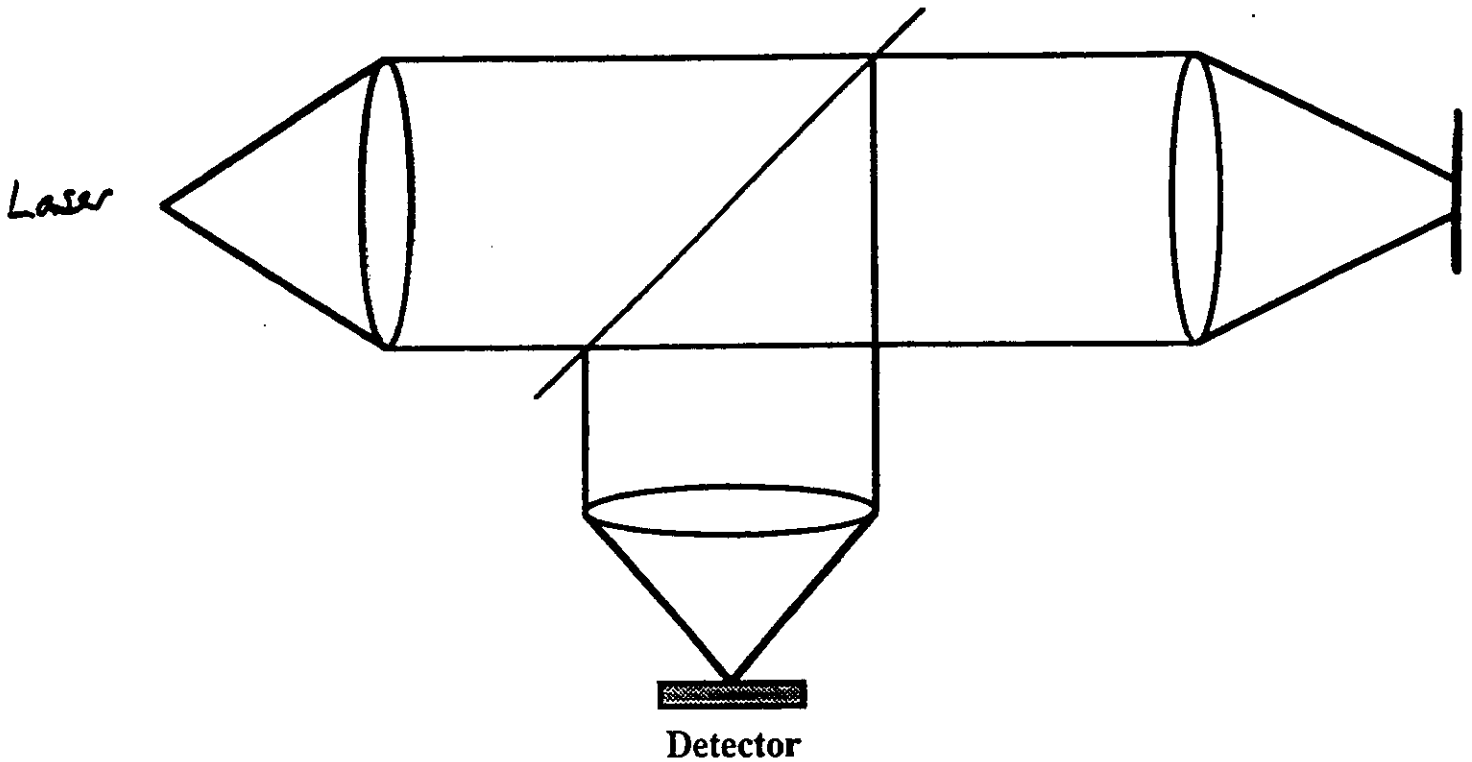


# Confocal Microscopy

## Coherent Detection

- Optical fibres
  - single mode
  - two mode
- Interference microscopy
- Laser Feedback microscopy

# Coherent Detection



## Incoherent Detector

$$I = \int |U|^2 dS$$

## Coherent Detector

$$I = \left| \int U dS \right|^2$$

Examples:

Mimic optically

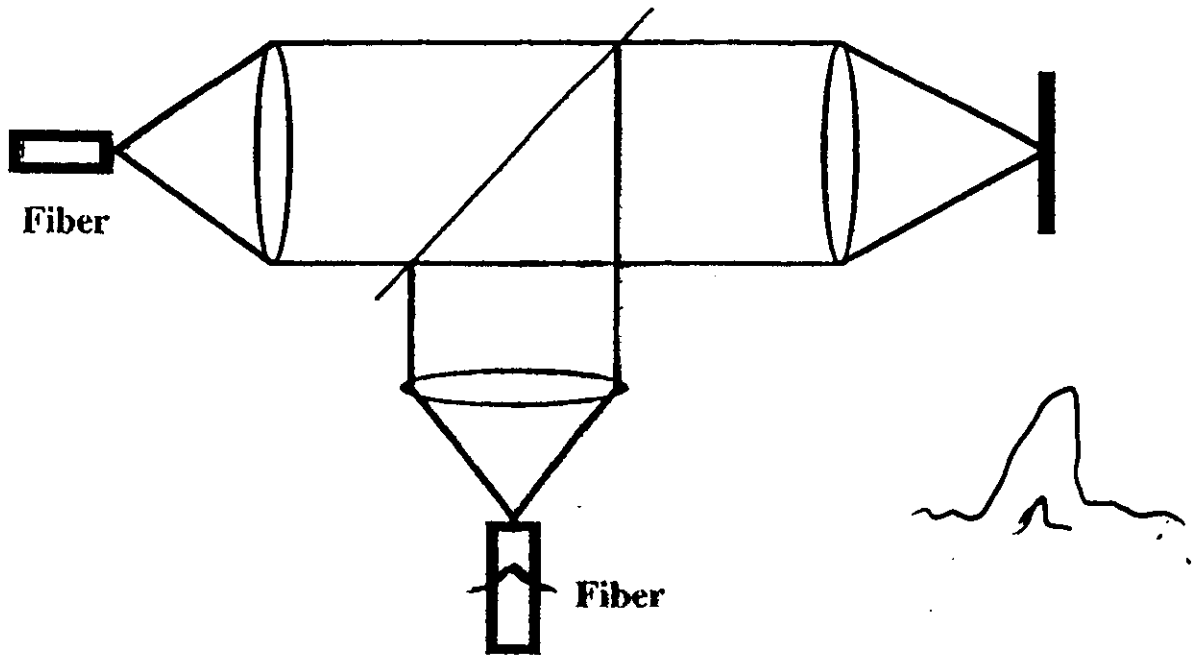
Single mode optical fibre

Multi-mode optical fibres

Differential imaging

# Optical Fiber Detection

Replace pinhole with fiber



Monomode fiber -- confocal

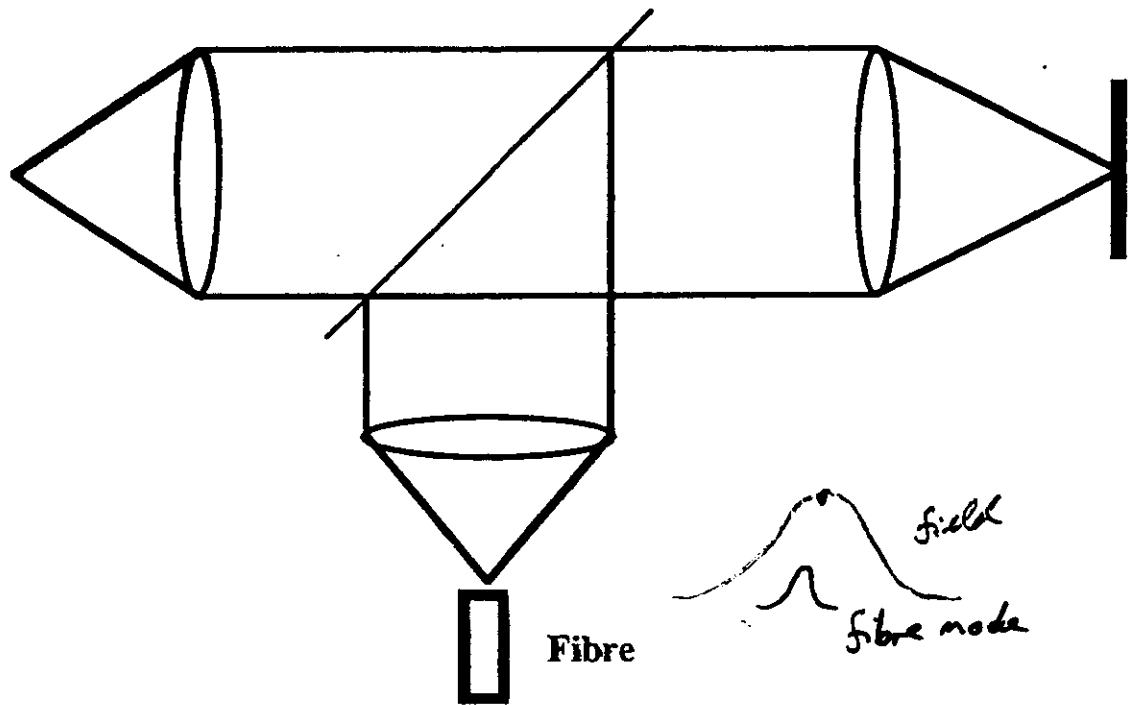
Two - mode fiber -- field amplitude and

differential amplitude detected

Confocal and differential contrast

Height Contrast

# Coherent Detection -- Optical Fibres.



If field at fibre tip is  $U$  then modes are excited as

$$a_i = \int U e_i dS$$

If one mode only excited we detect

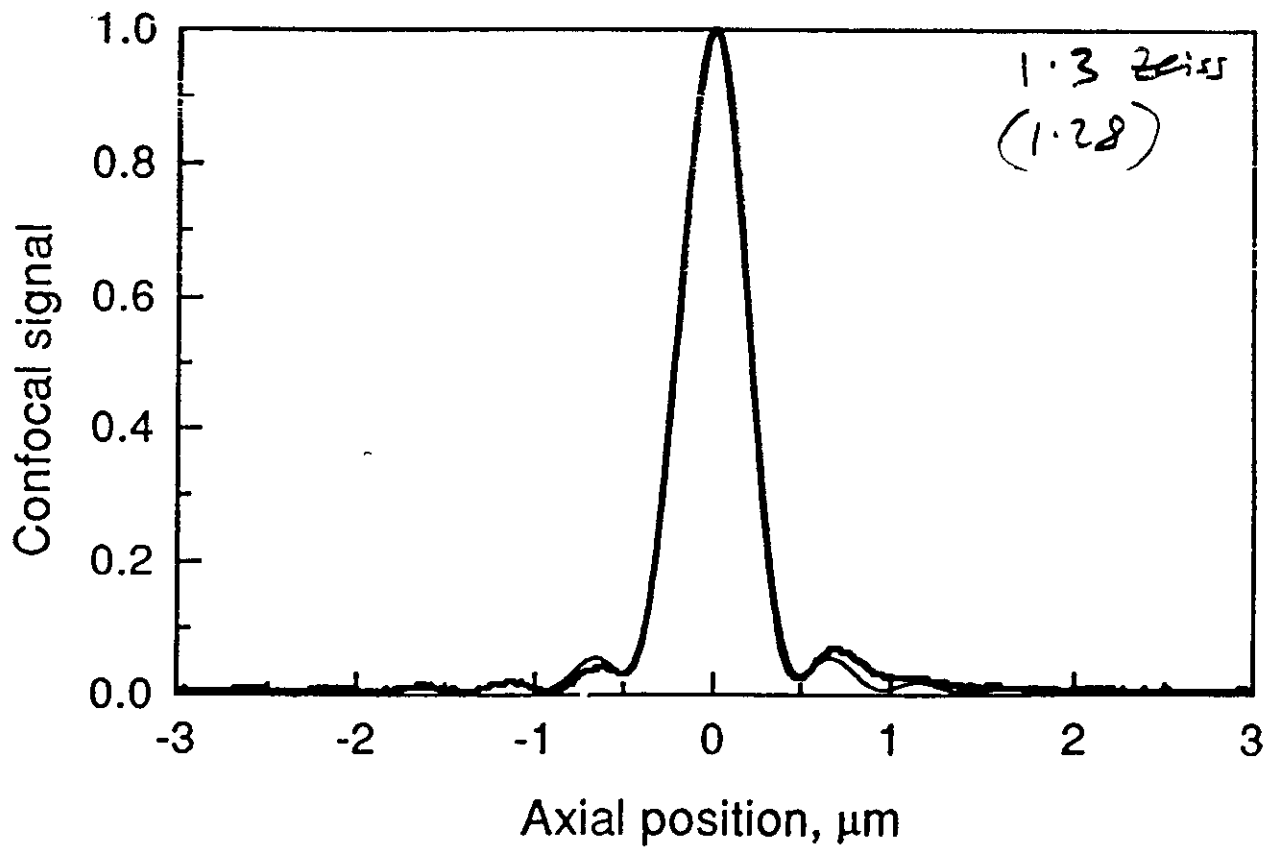
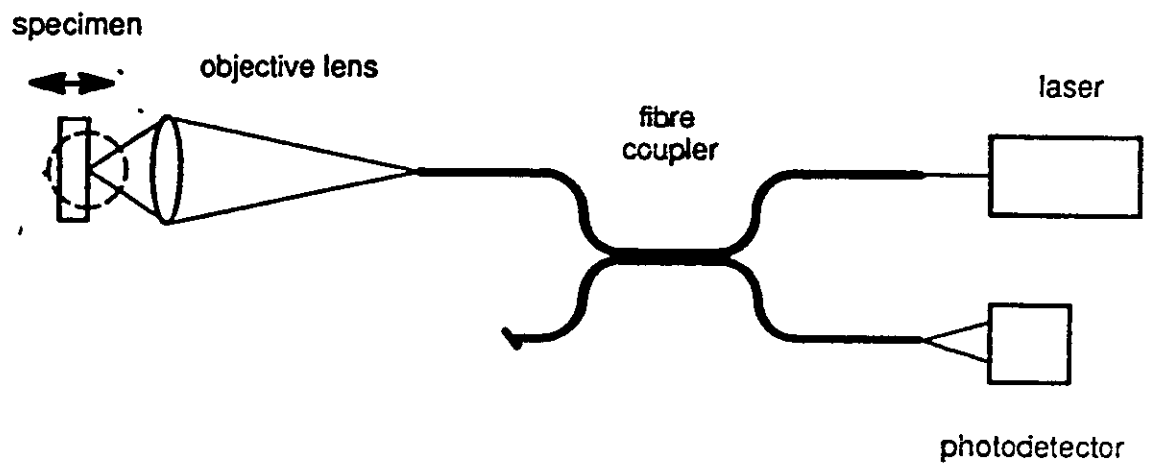
where

$$\underline{|a_1|^2}$$

$$\underline{a_1 = h h_{\text{eff}} \otimes t}$$

$$\underline{h_{\text{eff}} = h \otimes e_1} \quad \boxed{P_{\text{eff}} = P E_1}$$





# Two mode fiber detection

Mode 1 'detects' field

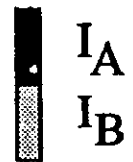
$$a_1 \underline{e}_1 \exp -j\beta_1 l$$

Mode 2 'detects' differential of field

$$a_2 \underline{e}_2 \exp -j\beta_2 l$$

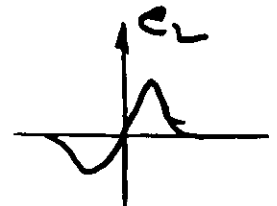
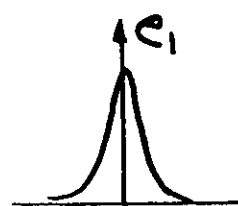
$$U_{\text{fiber}} = a_1 \underline{e}_1 \exp -j\beta_1 l + a_2 \underline{e}_2 \exp -j\beta_2 l$$

phase difference is tunable by varying fiber length



eigenmode  $e_1$  is an even function

eigenmode  $e_2$  is an odd function



$$\underline{I_+ + I_- = |a_1|^2 + |a_2|^2}$$

$$\underline{I_+ - I_- = 2 \operatorname{Re}\{a_1 a_2^* \exp -j\Delta\beta l\}}$$

$$a_2 \sim \frac{da_1}{dx}$$

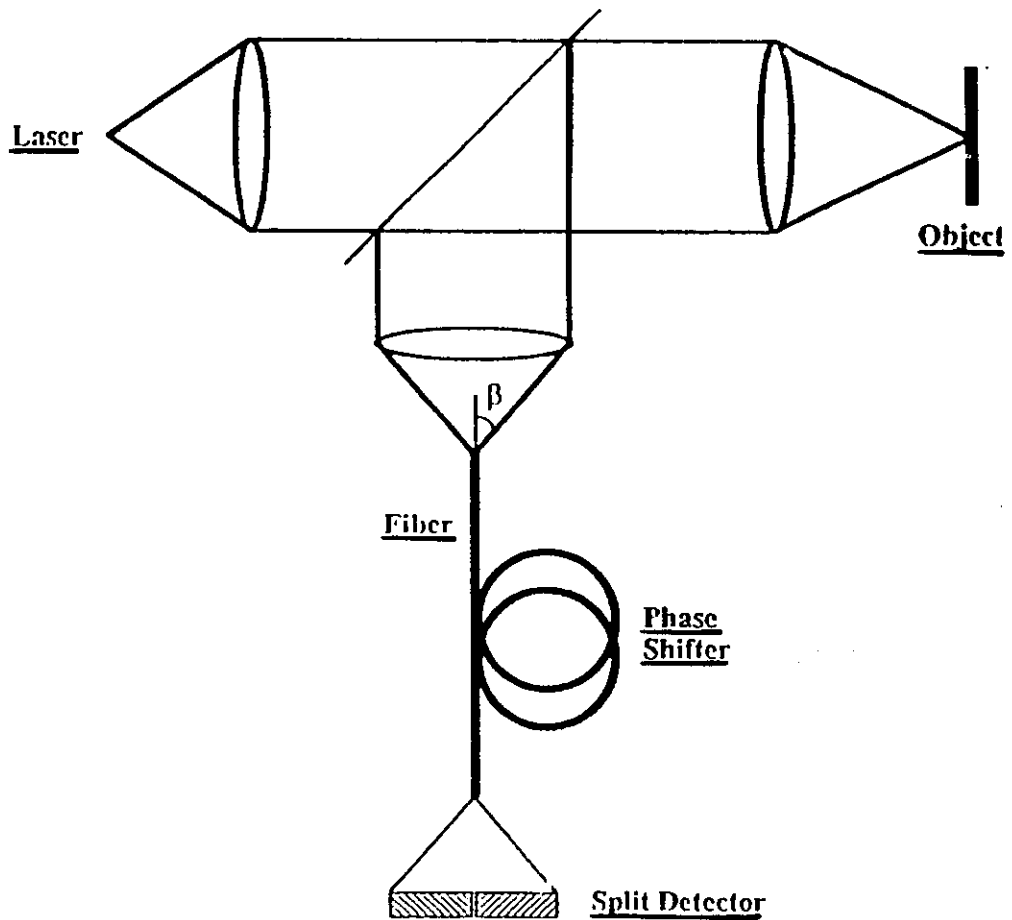
and let

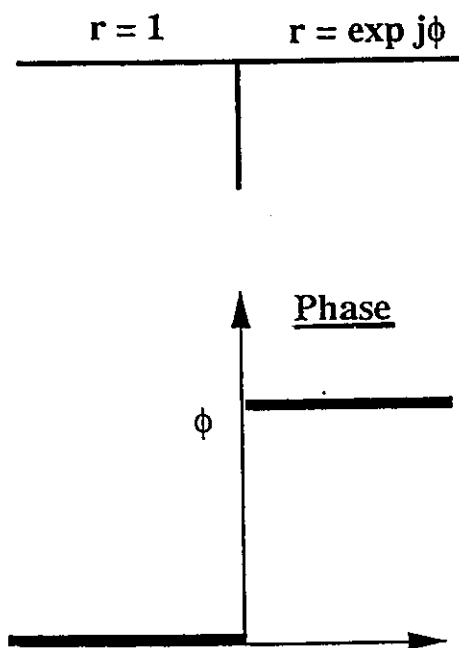
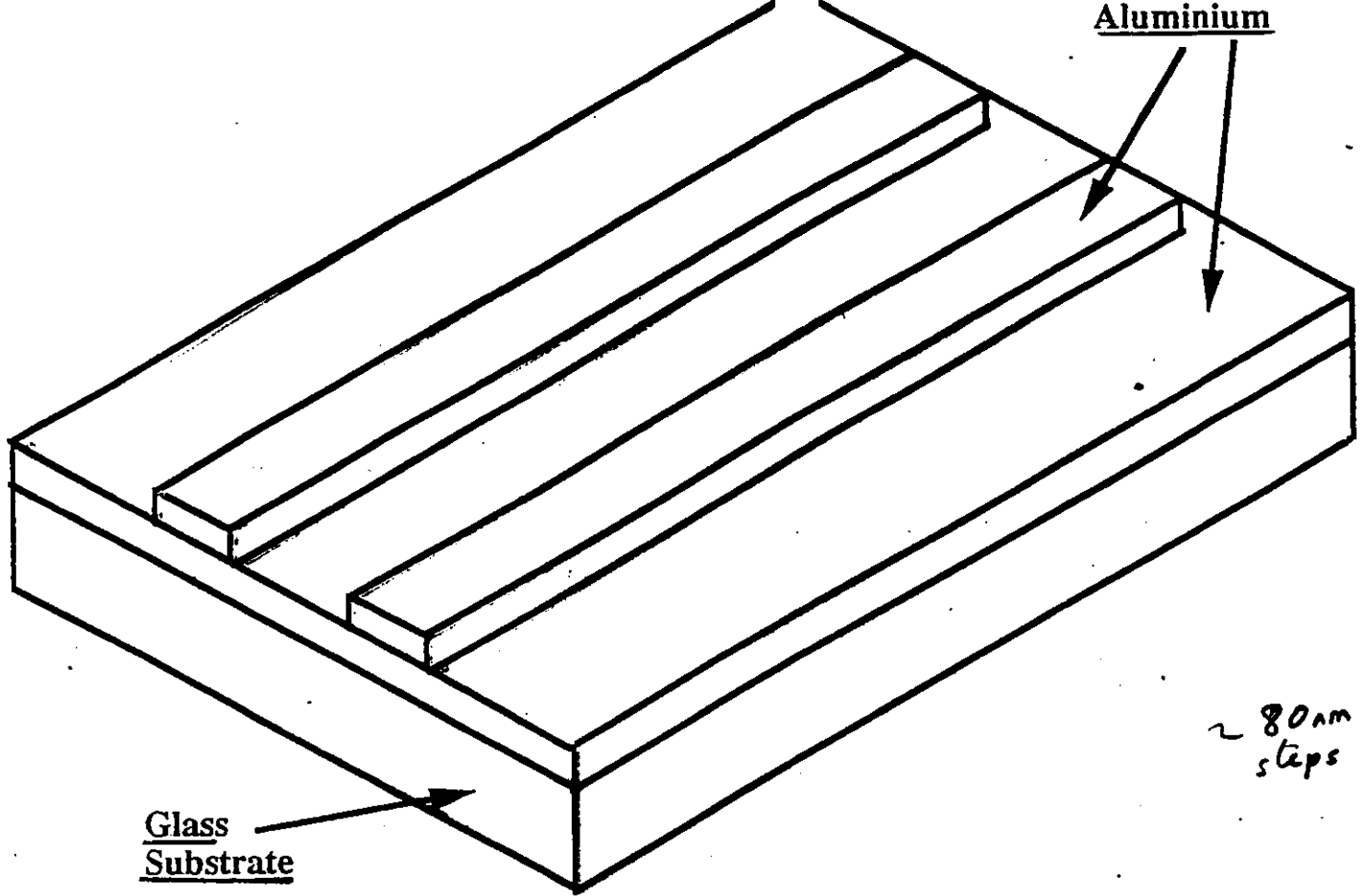
$$a_1 = b \exp j\phi$$

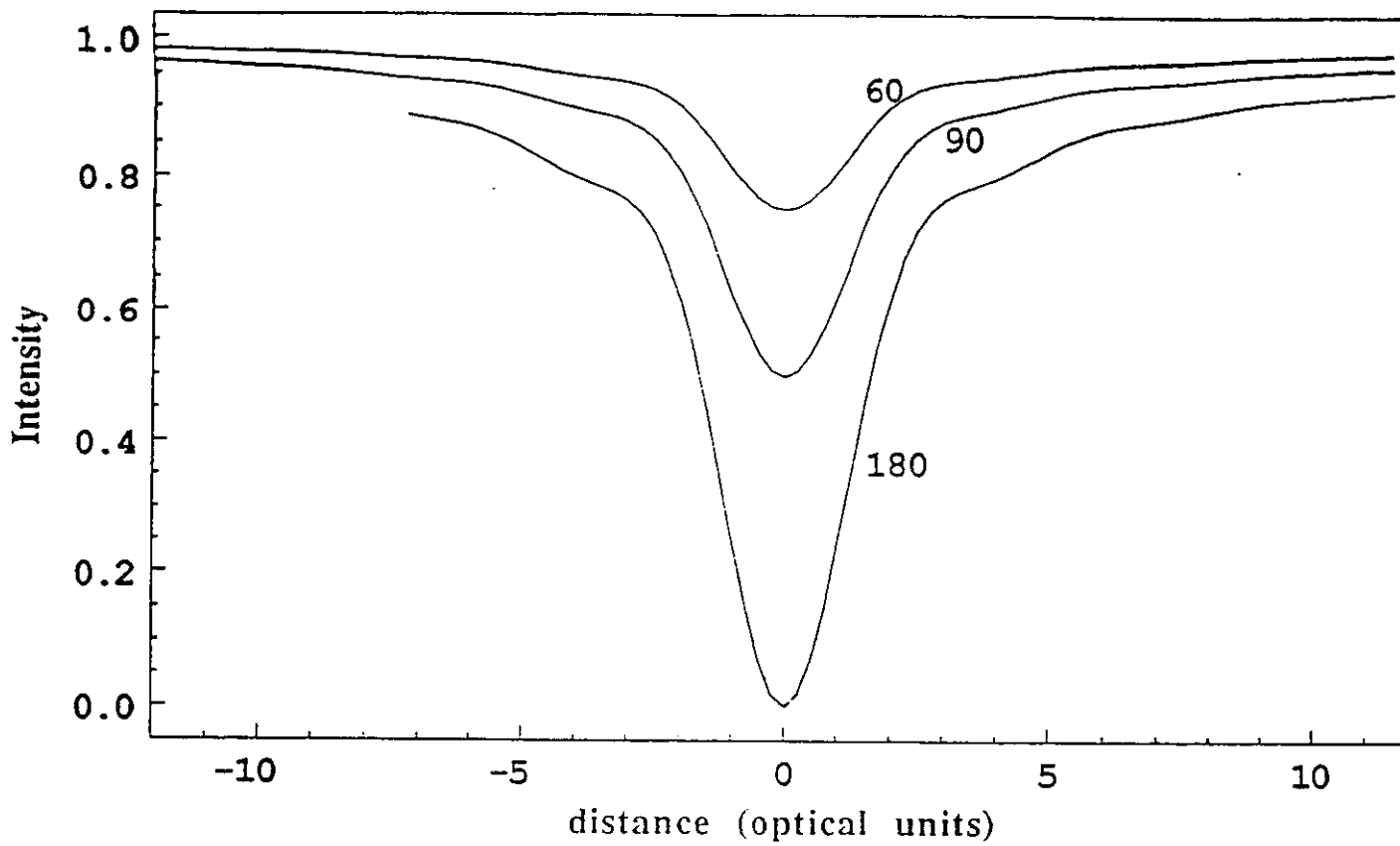
$$I_+ - I_- = \frac{db^2}{dx} \sin(\Delta\beta l) + 2 b^2 \frac{d\phi}{dx} \cos(\Delta\beta l)$$

Differential  
amplitude  
contrast

Differential  
phase  
contrast

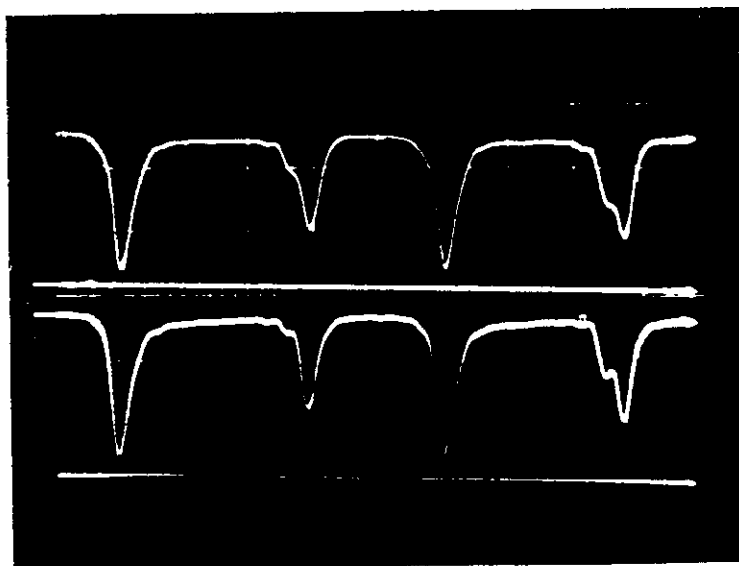


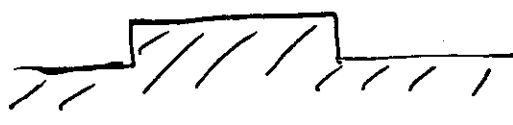
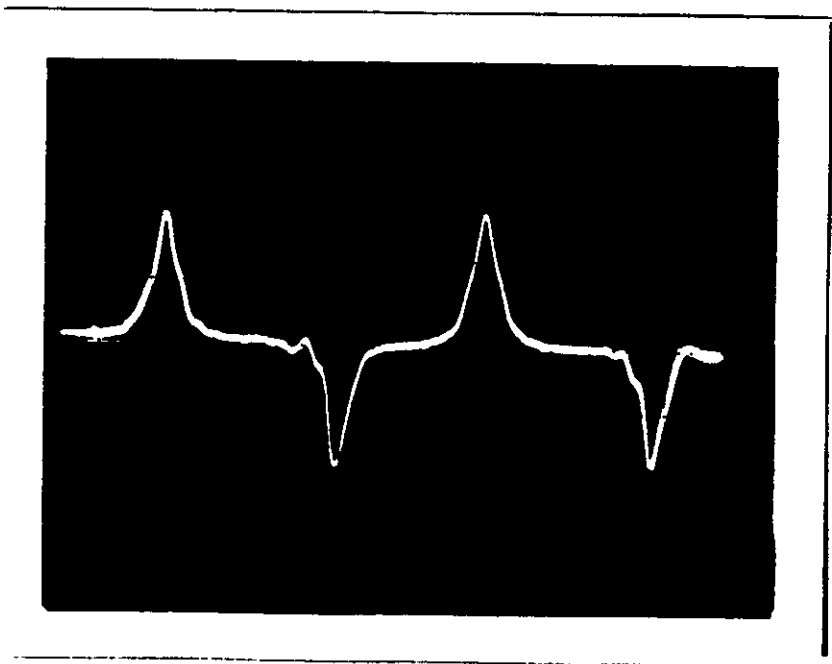
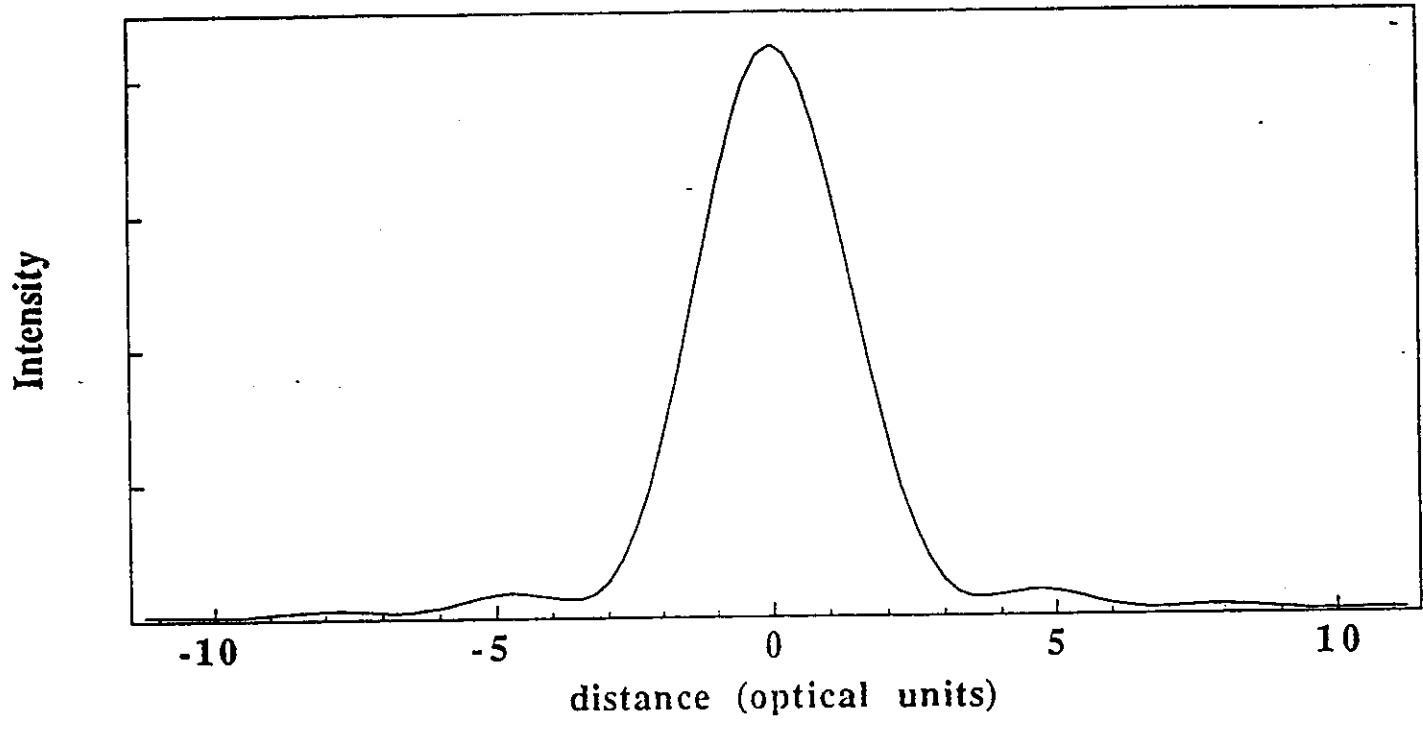


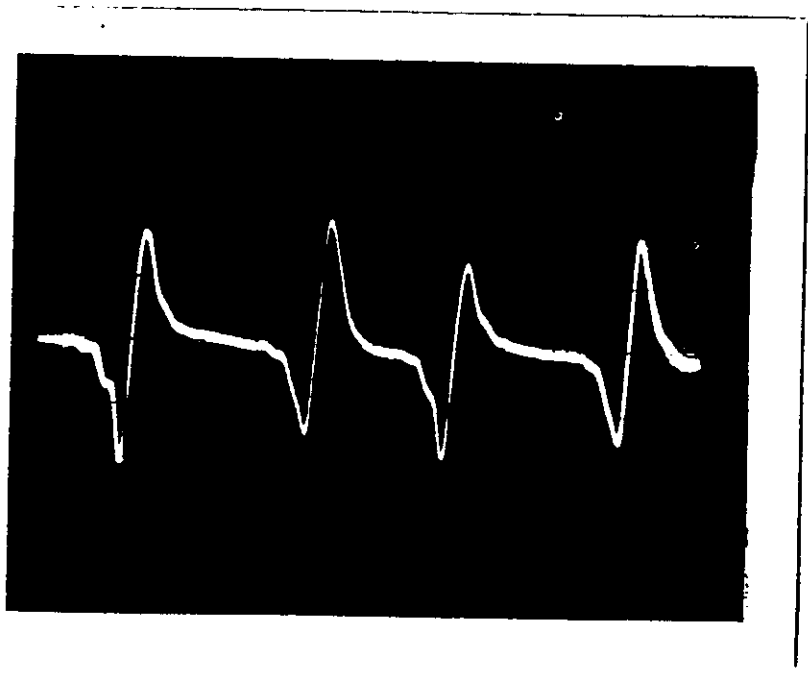
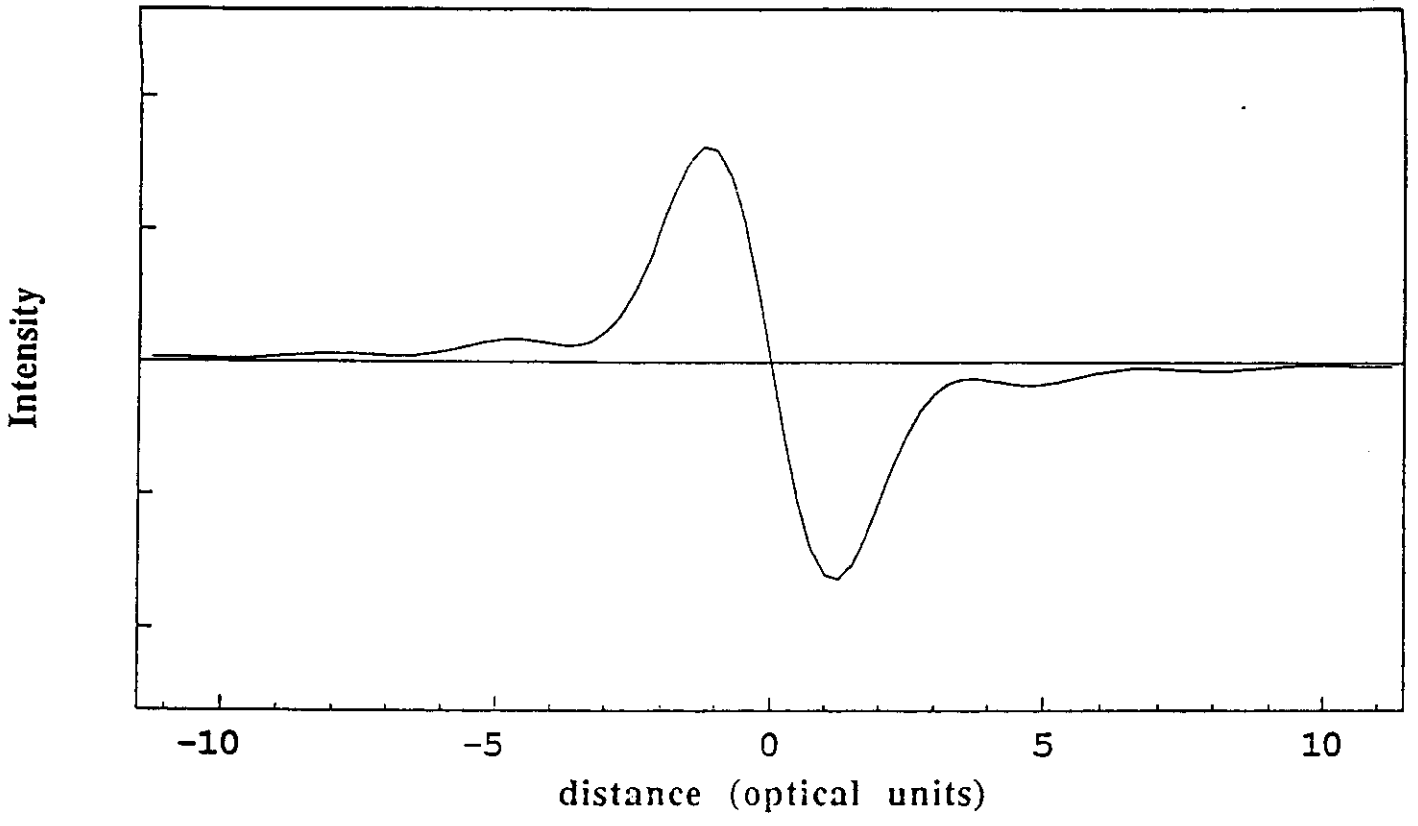


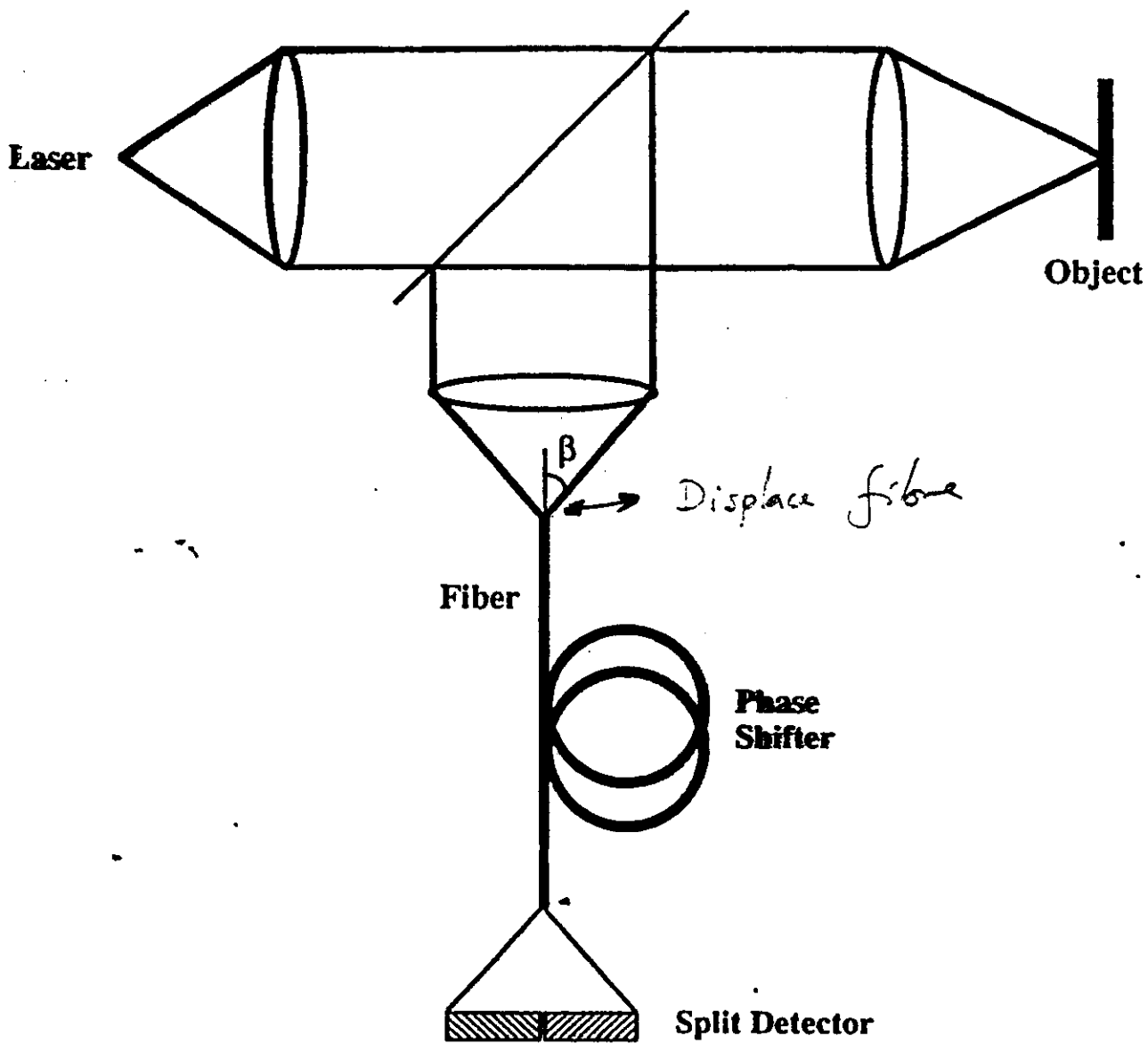
Fibre.

pinhole  
confocal.





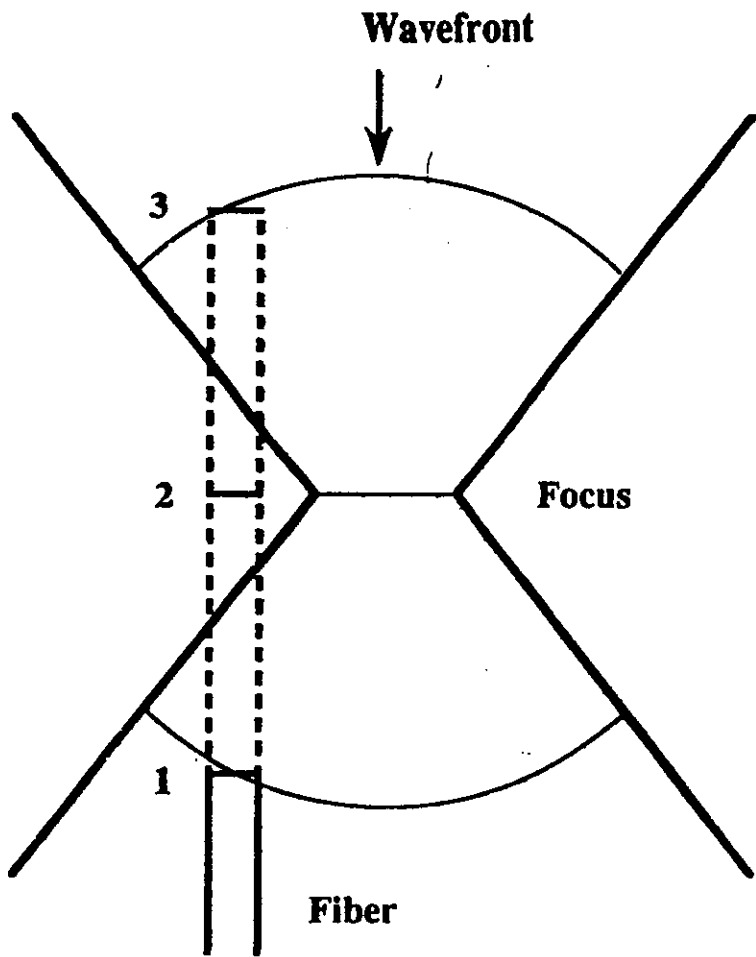




work in diff phase mode

? Axial Response





DPC

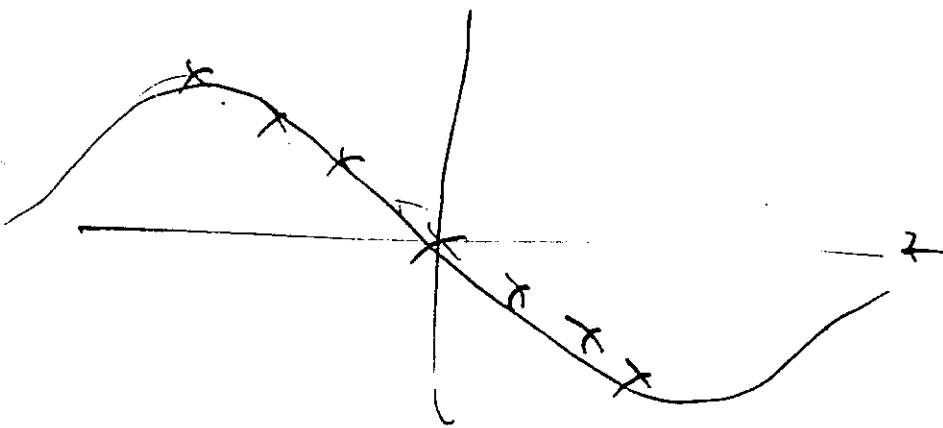
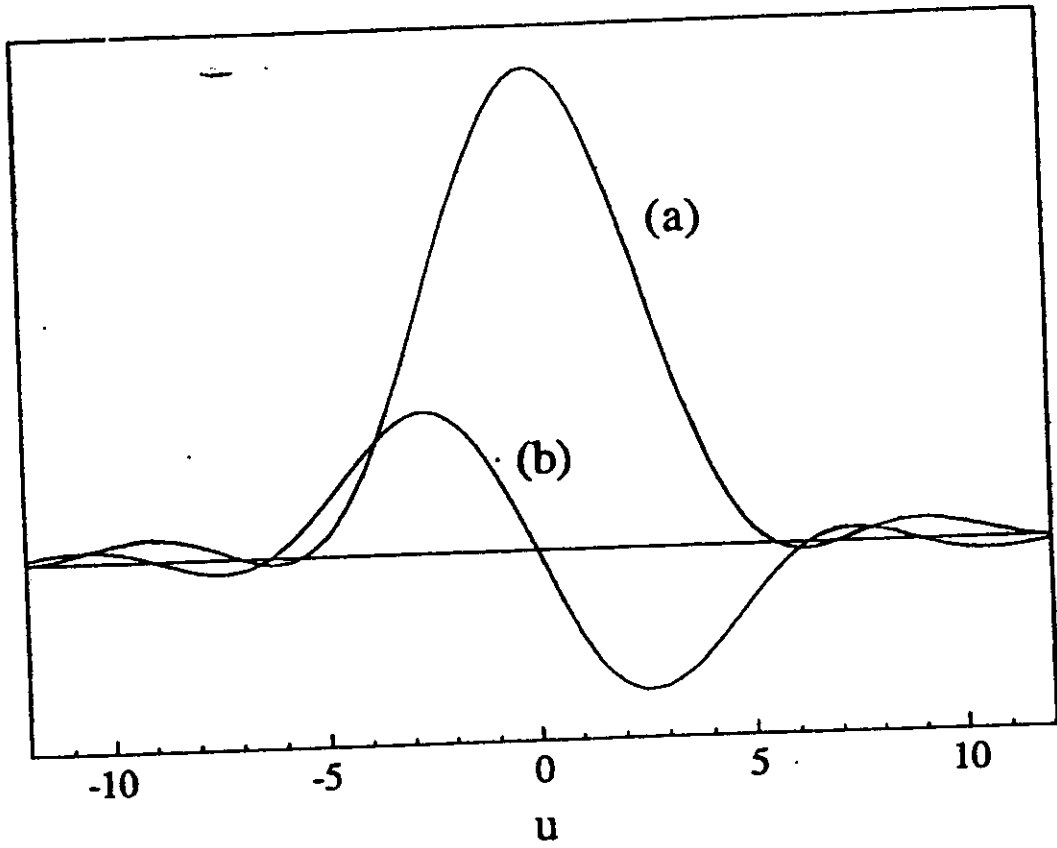
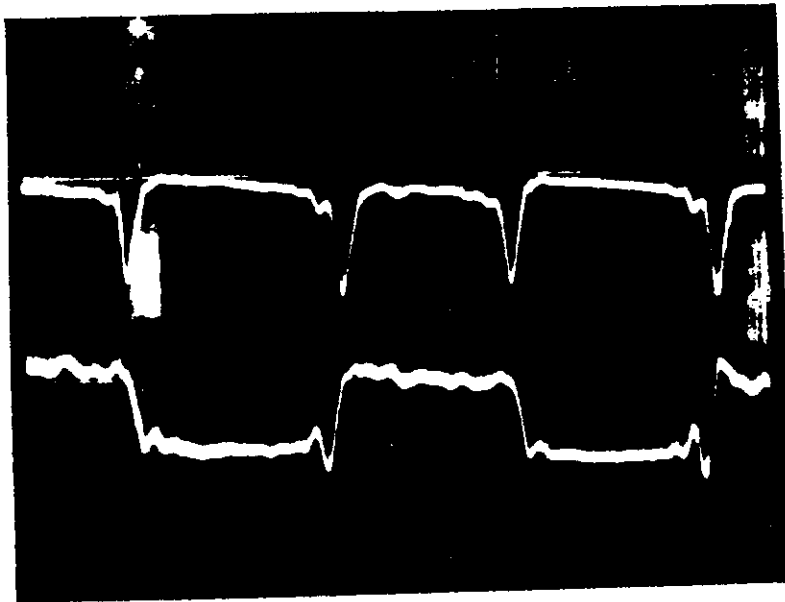
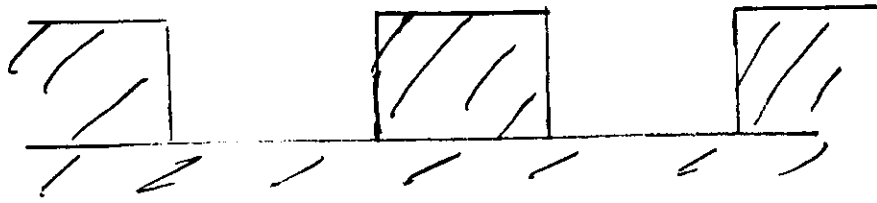


Fig. 2

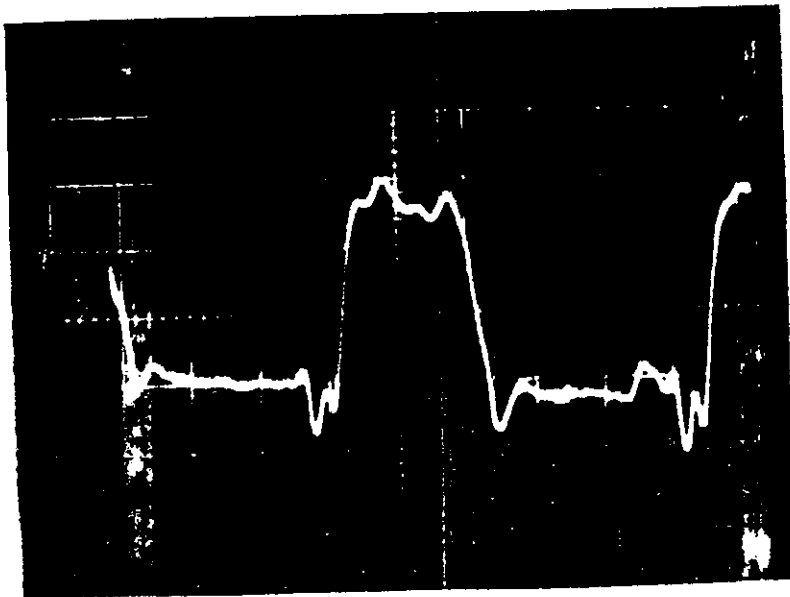
Axial Response - displacement





← confocal

← uncalibrated height

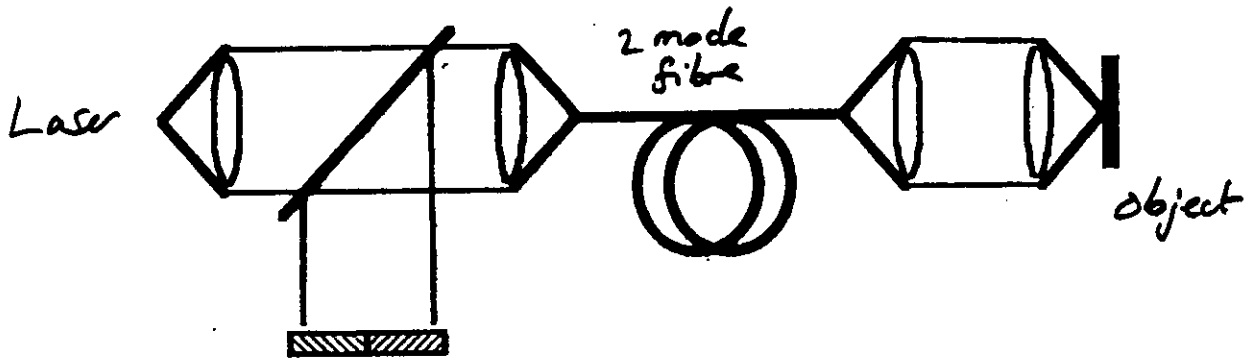


Calibrated height  
using feedback

0.1  $\mu\text{m}$   $\updownarrow$

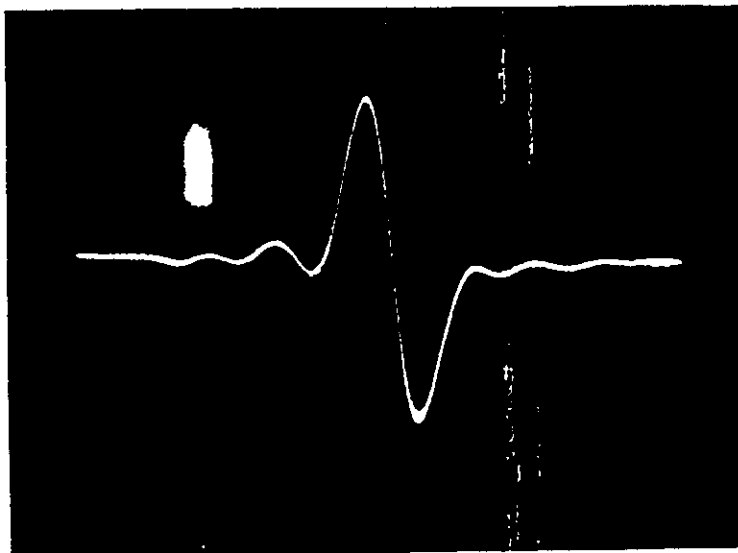
# Reciprocal Imaging

Launch and detect BOTH modes

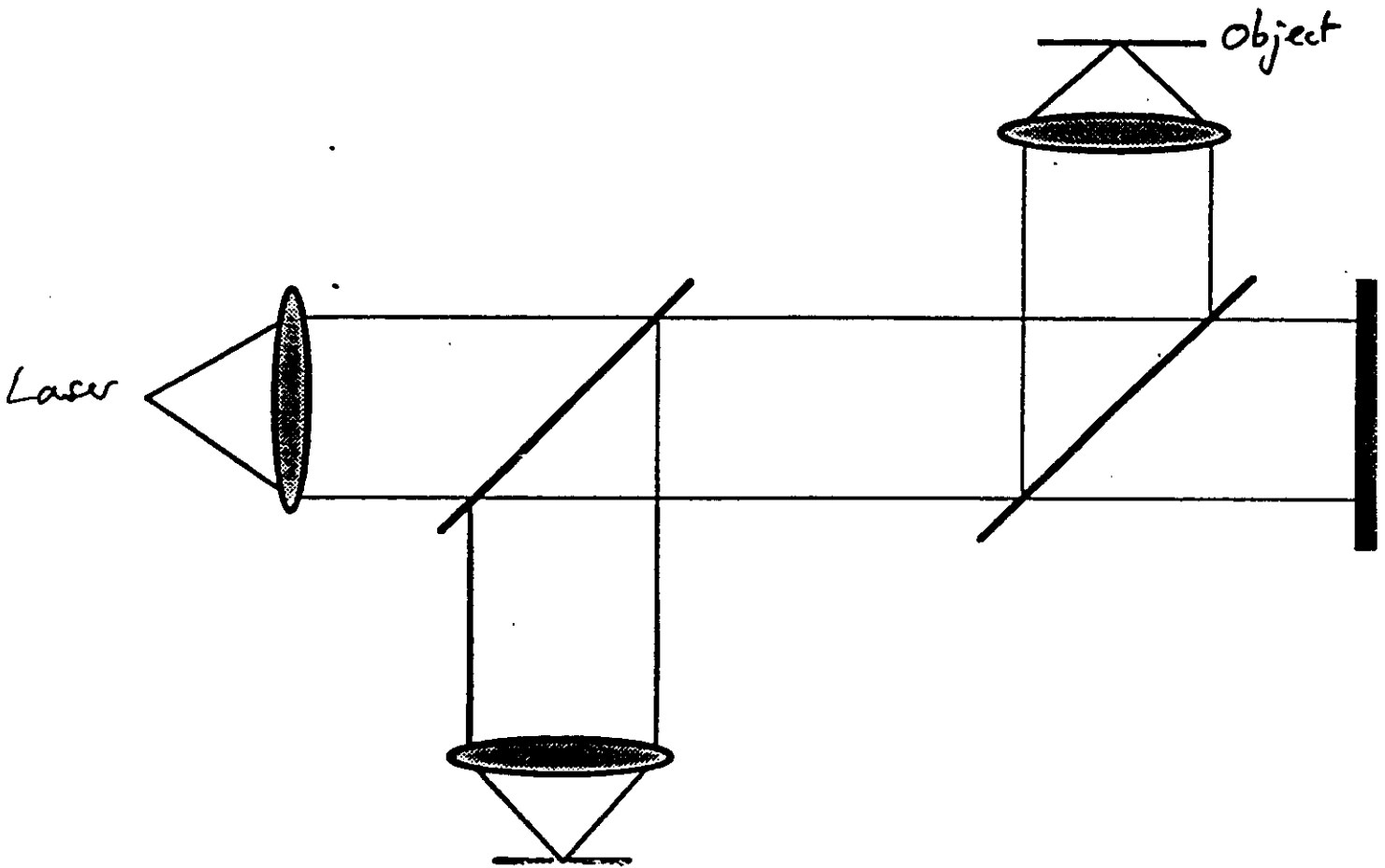


Differential axial scan

Profilometry without lateral shift



# Interference Imaging



$$I = |U + r|^2$$

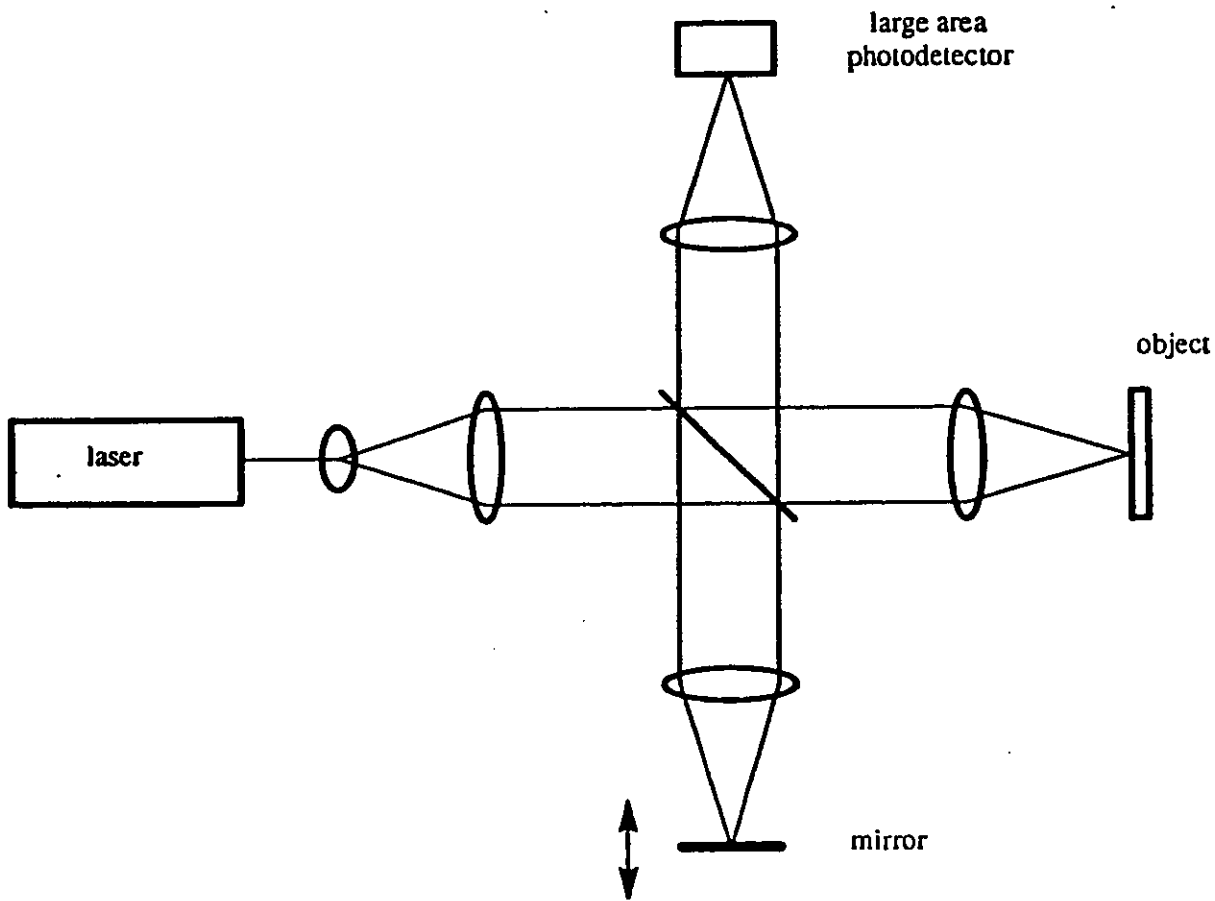
$$= |U|^2 + |r|^2 + 2\text{Re}\{r^* U\}$$

Confocal  
Image

Constant  
Reference

Interference term  
image

↑  
≡ conf & confocal



## Modulation Schemes

### Phase Modulation

$$\underline{\phi = \phi_0 \cos\omega t}$$

$$I = |r + U \exp j \phi(t)|^2$$

$$= r^2 + |U|^2 + 2r [\text{Re}\{U\} \underline{\cos(\phi_0 \cos\omega t)} - \text{Im}\{U\} \underline{\sin(\phi_0 \cos\omega t)}]$$

### Recall

$$\underline{\cos(\phi_0 \cos\omega t)} = J_0(\phi_0) - \underline{2J_2(\phi_0) \cos 2\omega t} + 2J_4(\phi_0) \cos 4\omega t + \dots$$

$$\underline{\sin(\phi_0 \cos\omega t)} = \underline{2J_1(\phi_0) \cos\omega t} - 2J_3(\phi_0) \cos 3\omega t + \dots$$

### Synchronously demodulate (lock-in)

(i) cos $\omega t$

$$\underline{I_1 \sim \text{Re}\{U\} J_1(\phi_0)}$$

(ii) cos $2\omega t$

$$\underline{I_2 \sim \text{Im}\{U\} J_2(\phi_0)}$$

### Quadrature Interference term images

$$\underline{\text{Confocal} \sim \alpha I_1^2 + \beta I_2^2}$$

# DEMODULATED SIGNALS

$$\underline{I_1 \sim \operatorname{Re} \{U\} J_1(\varnothing_0)}$$

$$\underline{I_2 \sim \operatorname{Im} \{U\} J_2(\varnothing_0)}$$

## Dither

frequency

180 kHz

amplitude

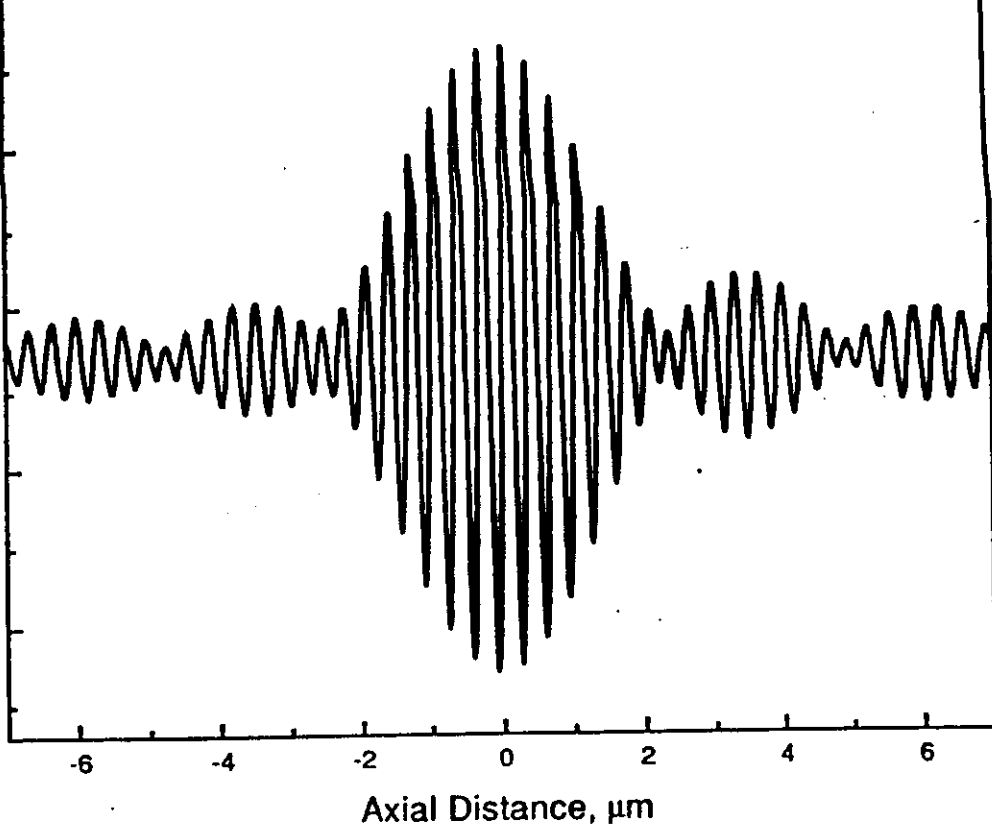
$J_1(\varnothing_0) \approx J_2(\varnothing_0)$

## Axial Response

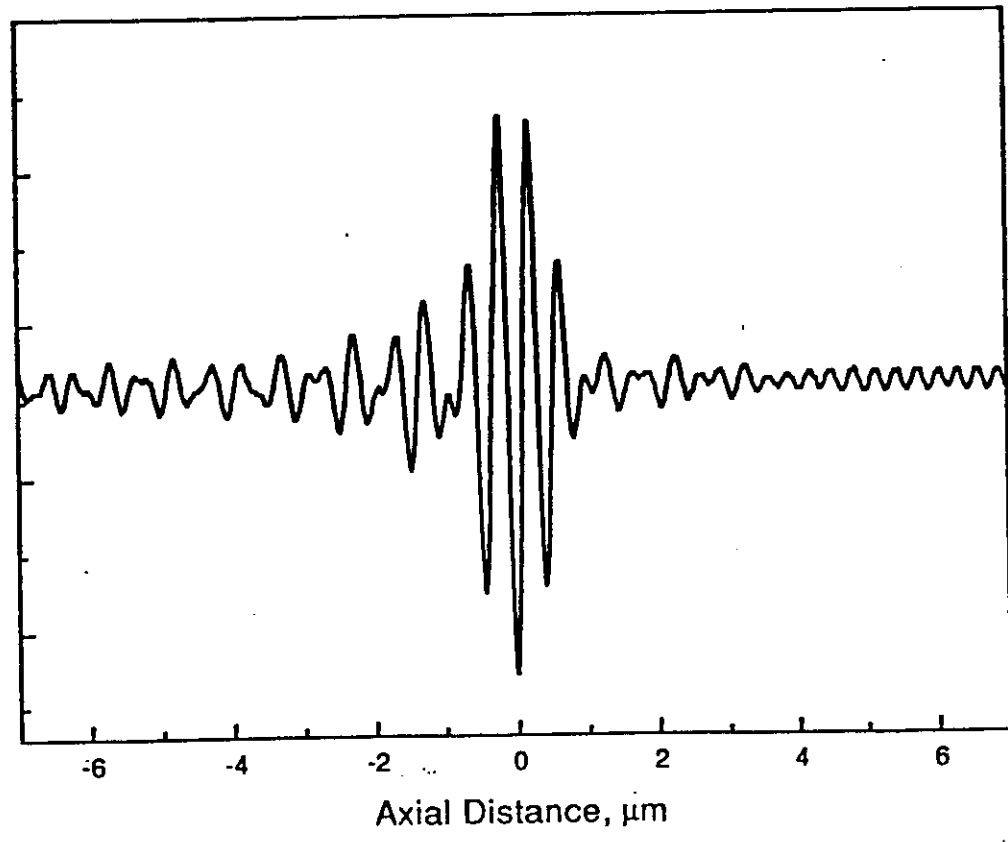
$$\underline{I_1 = \operatorname{sinc}(u/2) \sin(2kz \cos^2 \alpha/2)}$$

$$\underline{I_2 \approx \operatorname{sinc}(u/2) \cos(2kz \cos^2 \alpha/2)}$$





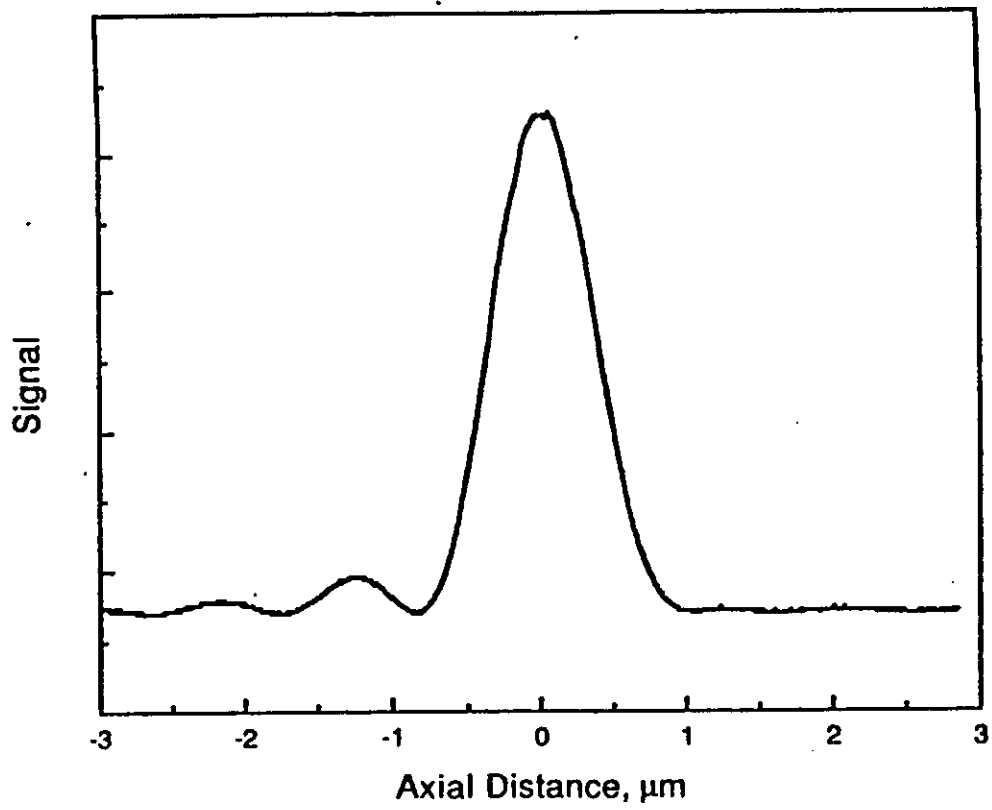
NA = 0.5



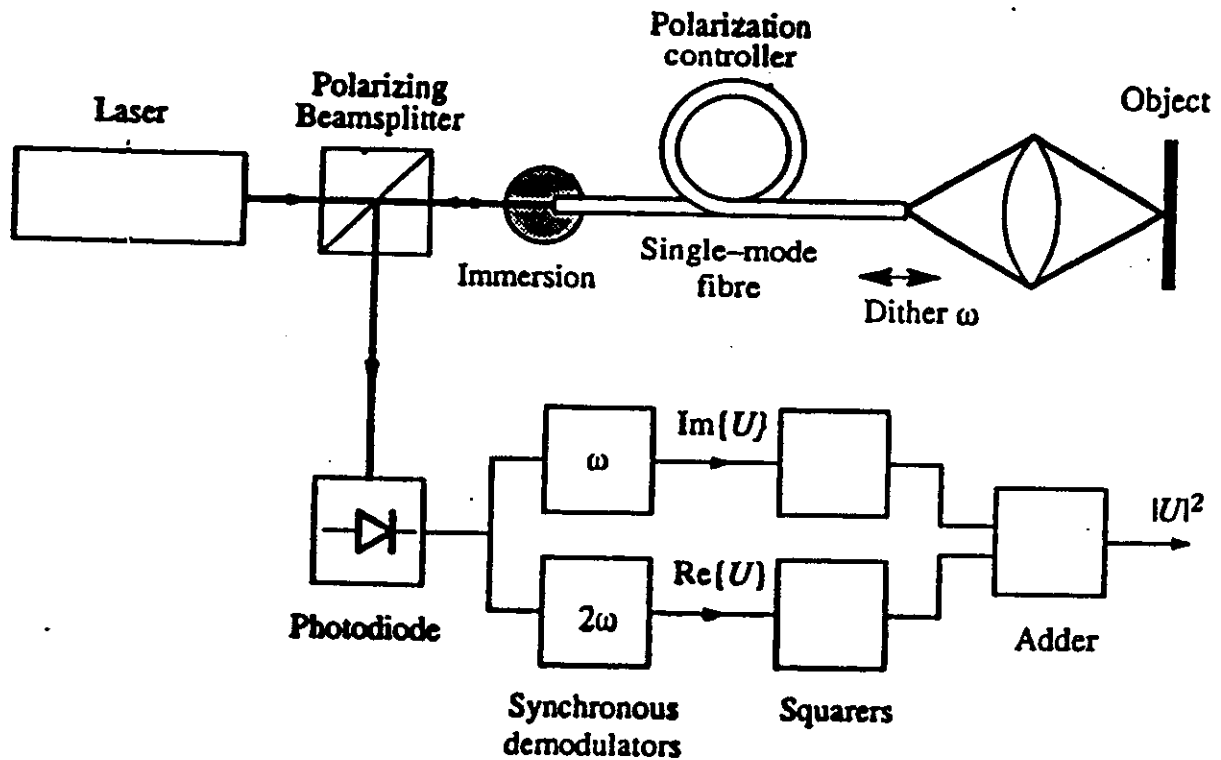
NA = 0.8

Intensity vs. Axial Distance

0.8 NA



# Interference System

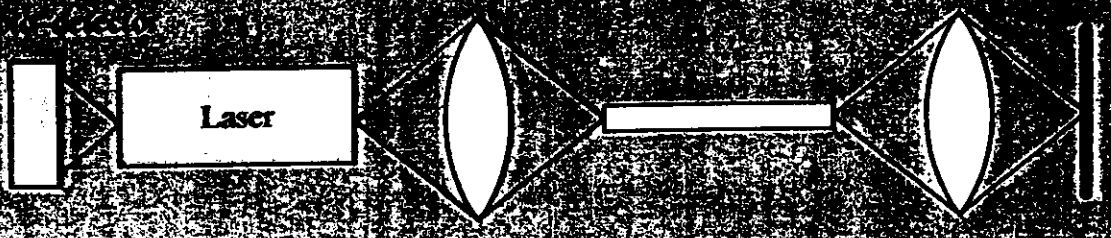


## Axial Response

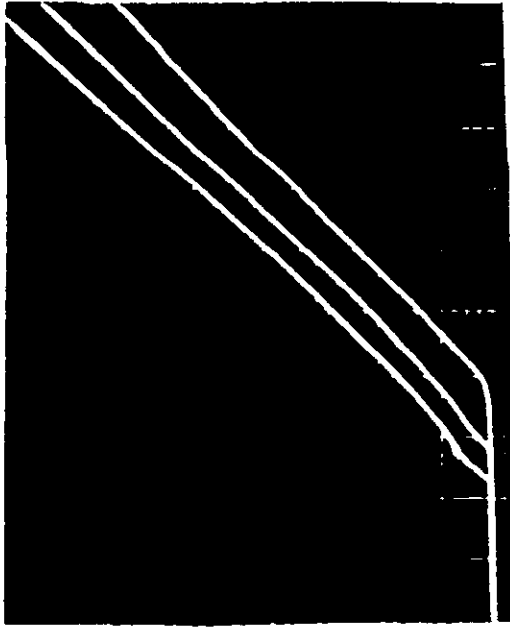
$$\text{Im} \{U\} \approx \text{sinc} \left( \frac{u}{2} \right) \sin \left( 2kz \cos^2 \frac{\alpha}{2} \right)$$

$$\text{Re}\{U\} \approx \text{sinc} \left( \frac{u}{2} \right) \cos \left( kz \cos^2 \frac{\alpha}{2} \right)$$

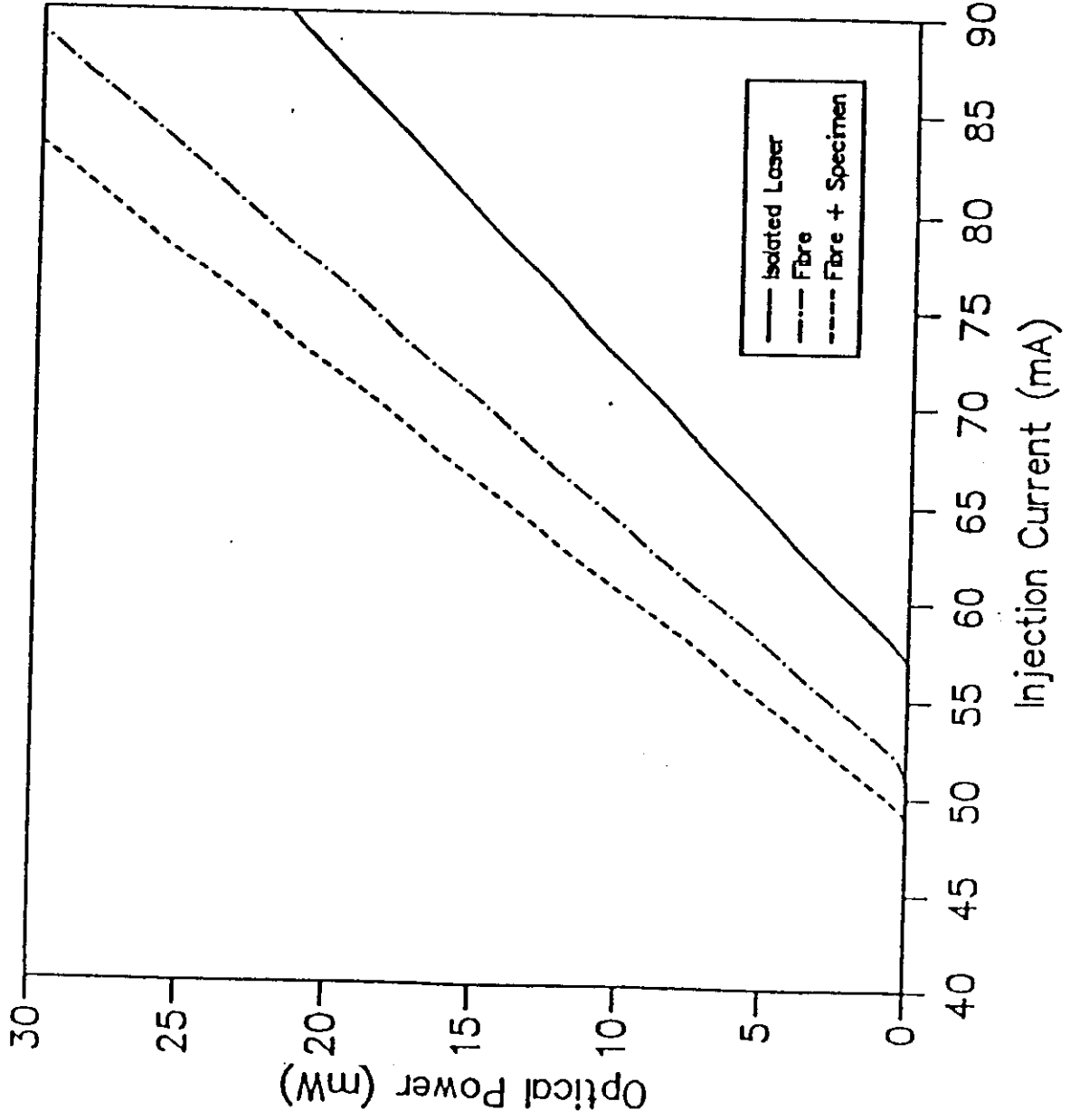
# OPTICS OF THE LASER CONCENTRATION



# Experimental Results



# Theoretical Power vs Current



$$\text{Optical Power [mw]} = S_1(1-r^2) \times$$

$$\frac{S_2 L \text{ Current [mA]} + \ln(r(r + c(1-r^2))) - 1}{(1 + r/(r+c(1-r^2))) \{1 - r/(r+c(1-r^2))\}}$$

$S_1, S_2$  : Scaling Factors.

$$S_1 = 33.95, S_2 = 128.89$$

L : Active Length of Laser. L = 0.3mm

c : Coupling Coefficient of laser to fibre.

$$c = 0.80$$

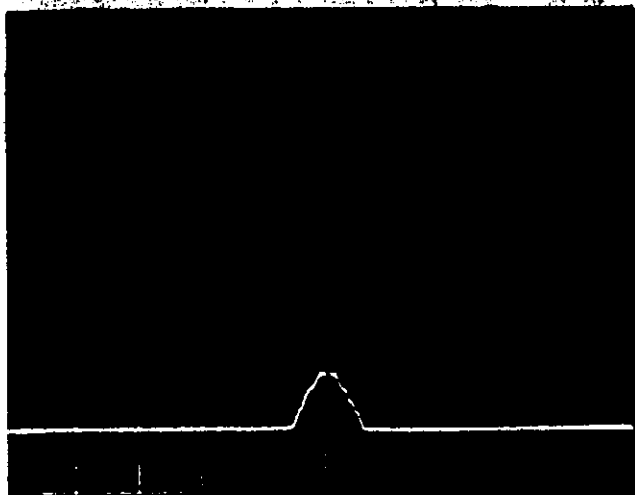
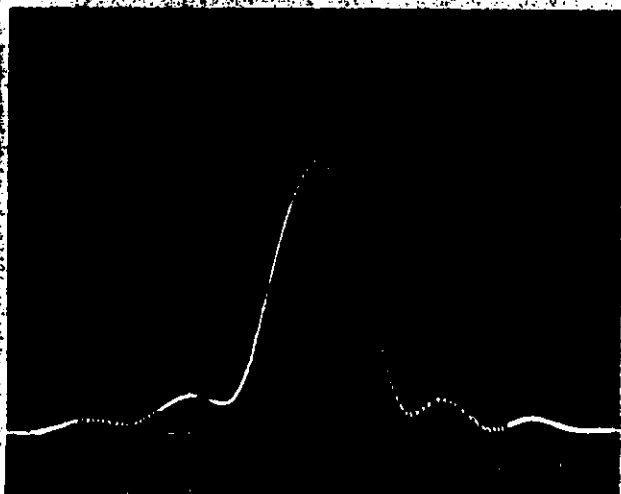
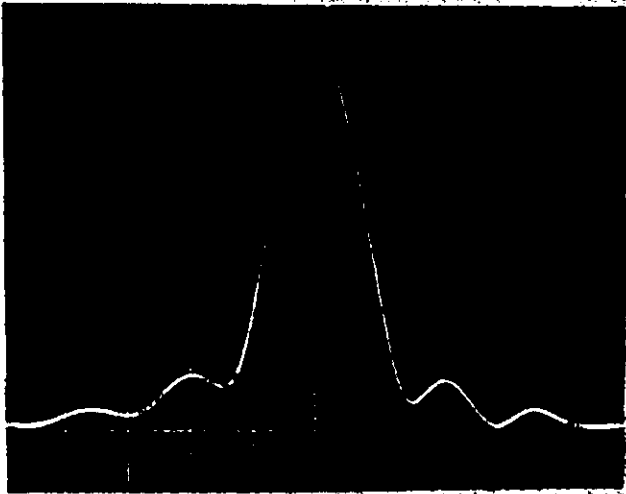
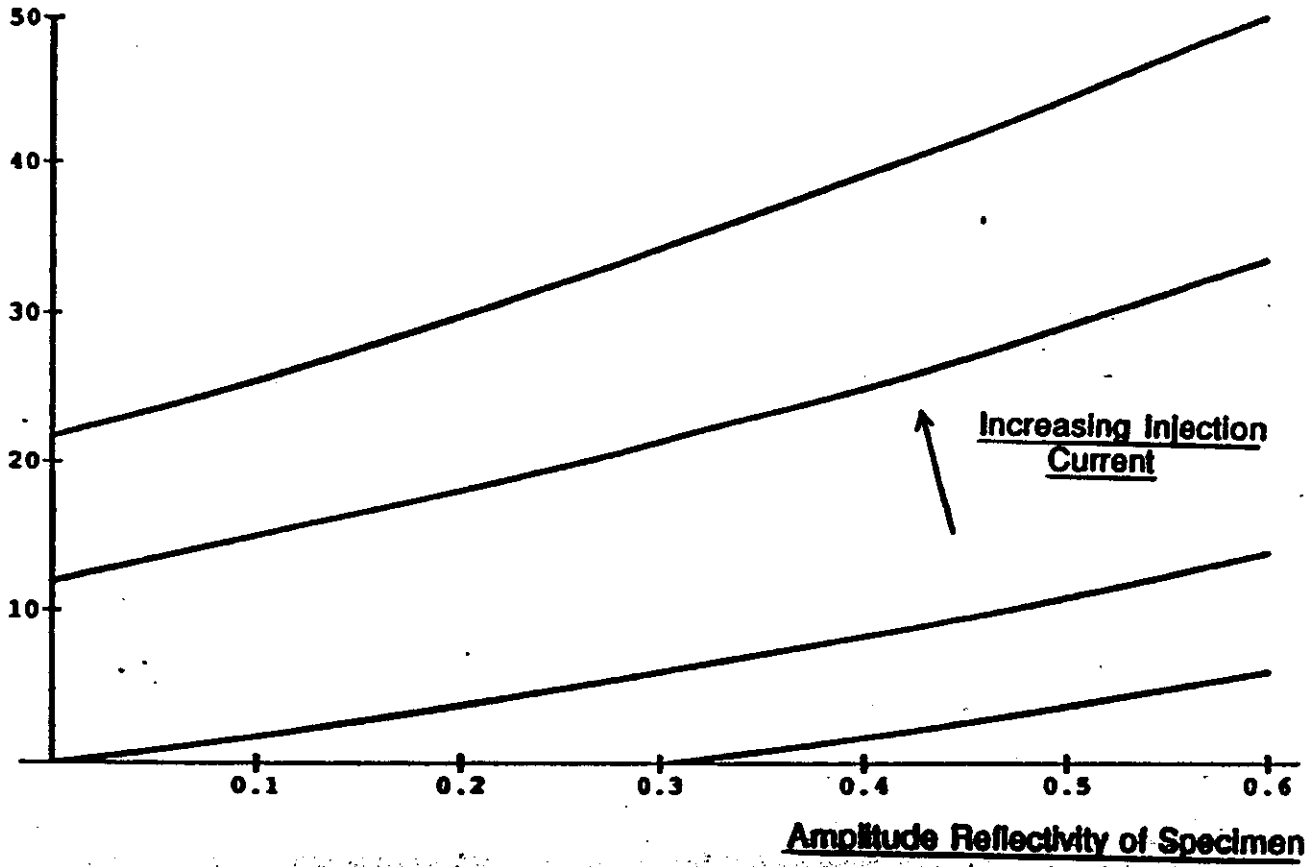
r : Amplitude Reflectivity of "Isolated Laser"

$$\text{Mirror. } r = 0.5477$$

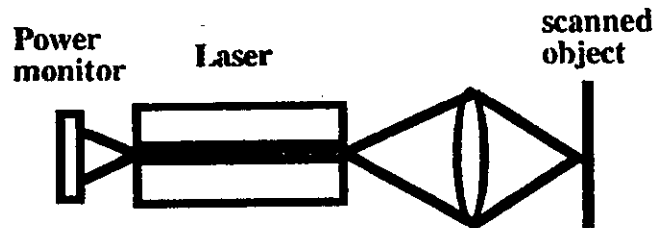
t : Amplitude Reflectivity of Specimen.

$$t = 0.317, 0.200, 0.00 \text{ (from left to right)}$$

**Power Detected  
by Monitor (mW)**



# Laser detection

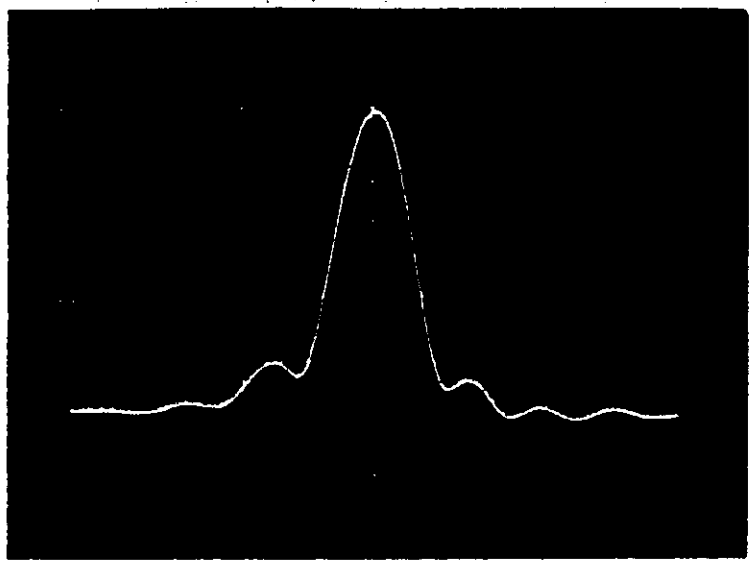


Laser mode acts as spatial filter

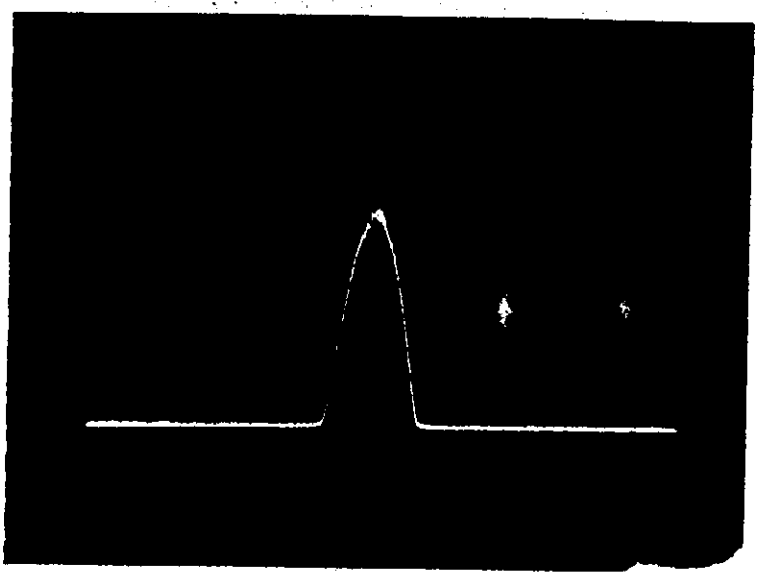
He-Ne laser gives  $\Delta I \sim \text{Re}\{s\}$

Semiconductor laser gives  $\Delta I \sim |s|$

181

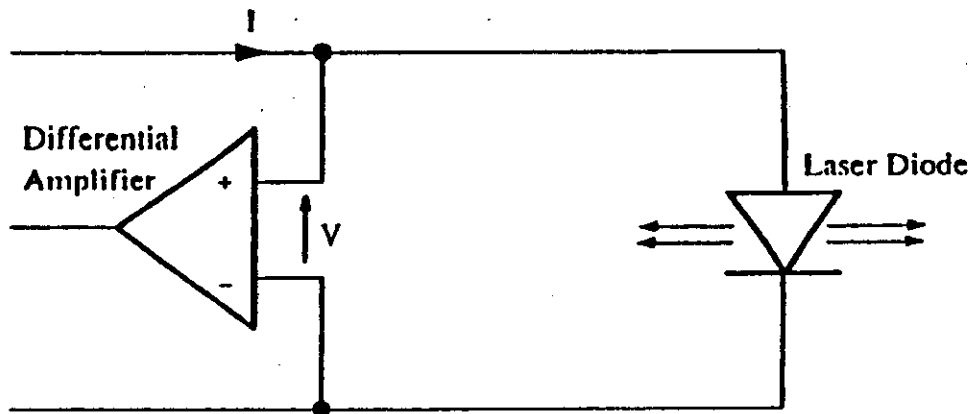
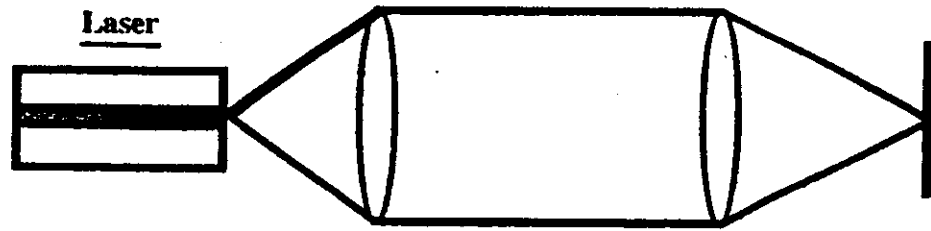


below  
threshold





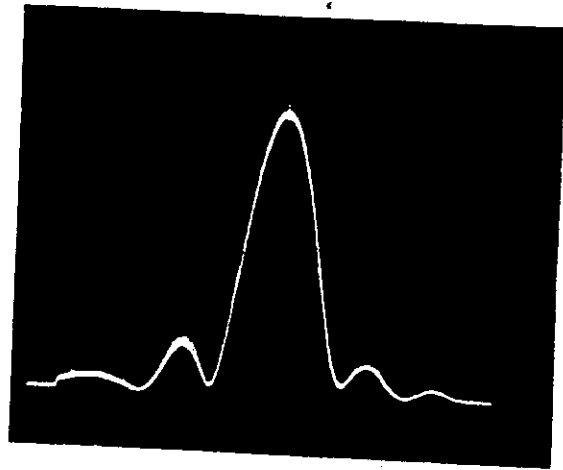
# Semiconductor laser confocal microscope



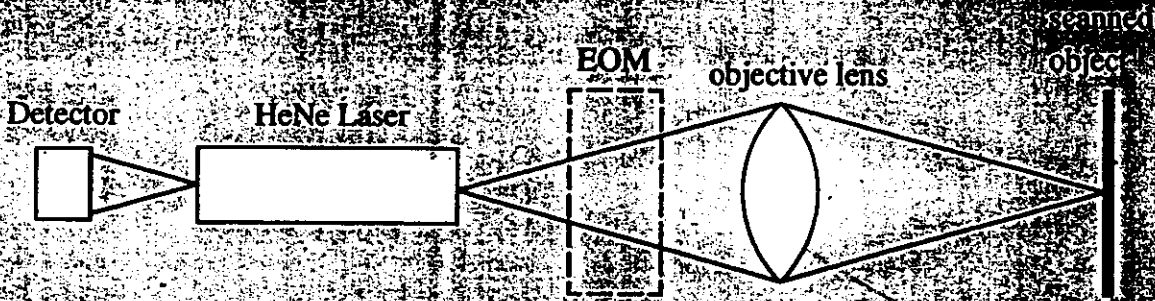
Perturbation on junction voltage

constant injection current

# Axial Response



# PROFILOMETRY



$$I = \cos \left[ \phi + 2kz \cos \left( \frac{\alpha}{2} \right) \right] \operatorname{sinc} \left( \frac{V}{2} \right)$$

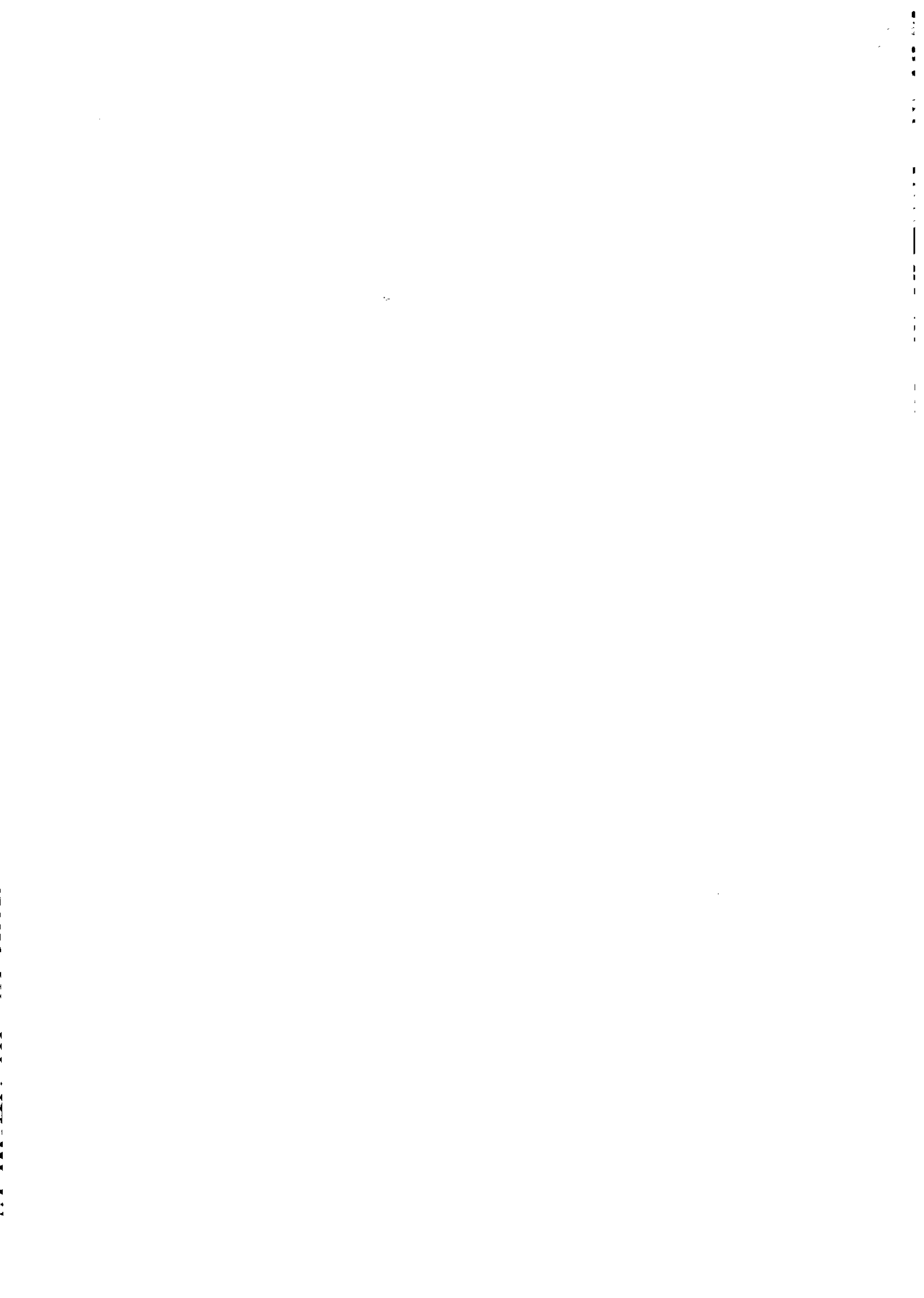
Feedback control of  $\phi \Rightarrow$  Surface profiles ( $z$ )

(i) dc feedback

(ii) Modulation feedback  $\phi = \phi_0 + \phi_1 \cos \omega t + \phi_2$

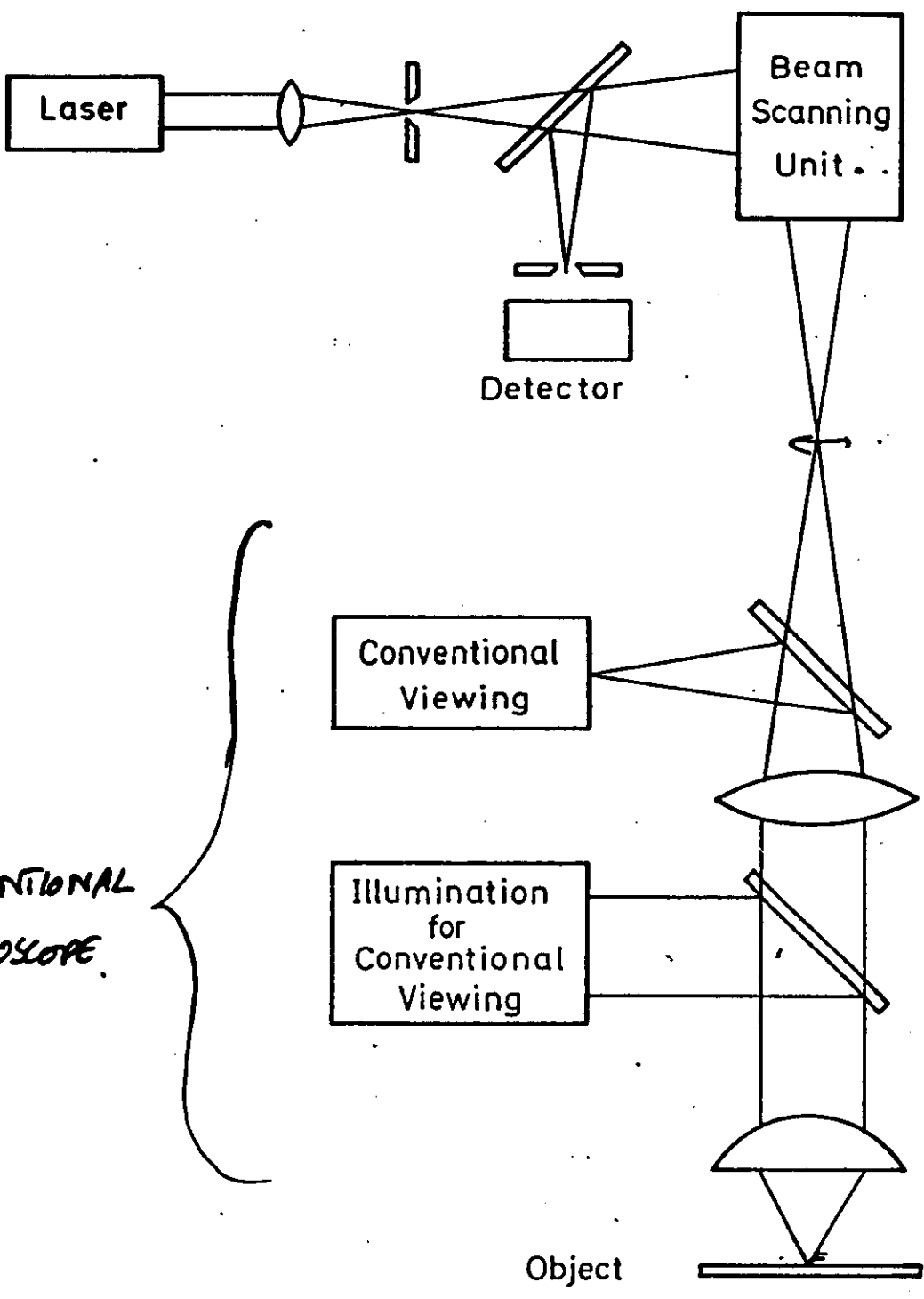
Lock-In:  $\phi_2 \propto$  surface height

$\Rightarrow$  Confocal Image



# Confocal Microscopy with White Light.

- Tandem Scanning
- Aperture Correlation (SCAM)
- Grid Illumination.  
(Structured Light)



CONVENTIONAL  
MICROSCOPE

Object

## Some drawbacks

### **Lasers**

**brightness**

**limited wavelength choice**

***usually* not real-time**

**pinhole alignment problems**

**need to scan**

## Some goals

**Easy to align**

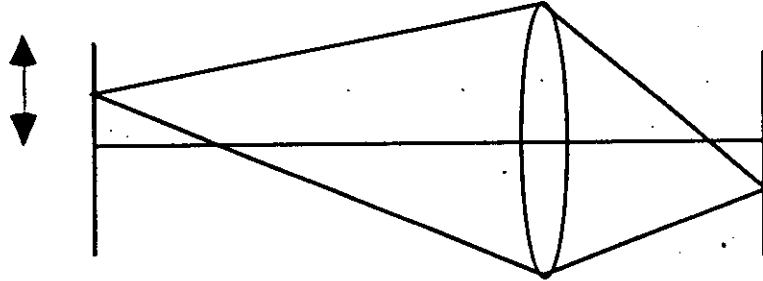
**No scanning**

**real-time**

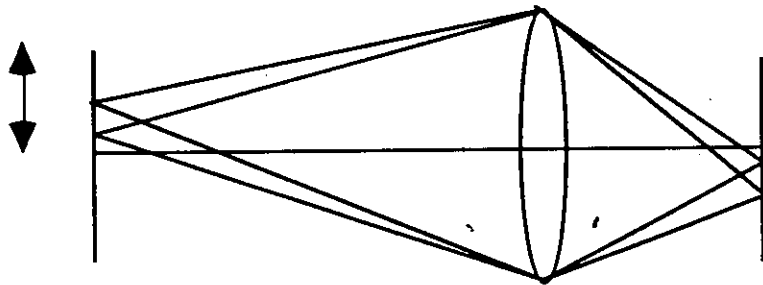
**no laser**

# The Principle

- **Single point systems**



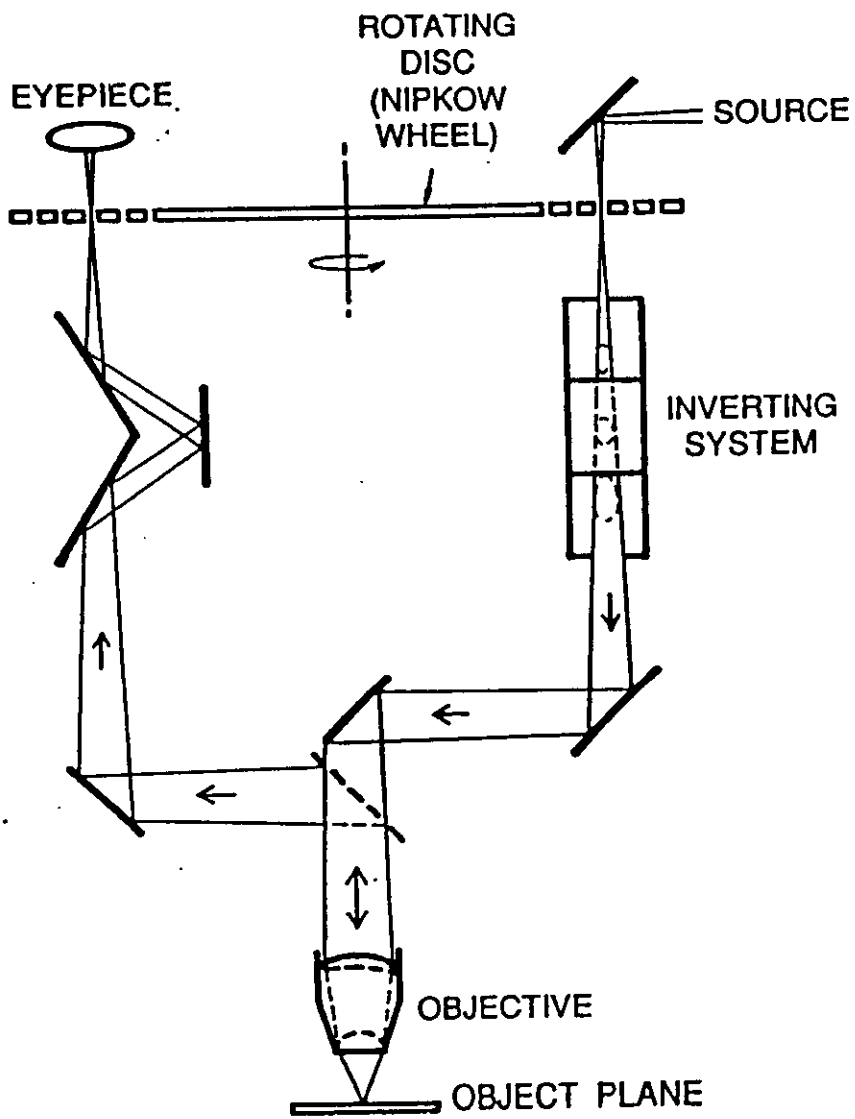
- **Two point systems**

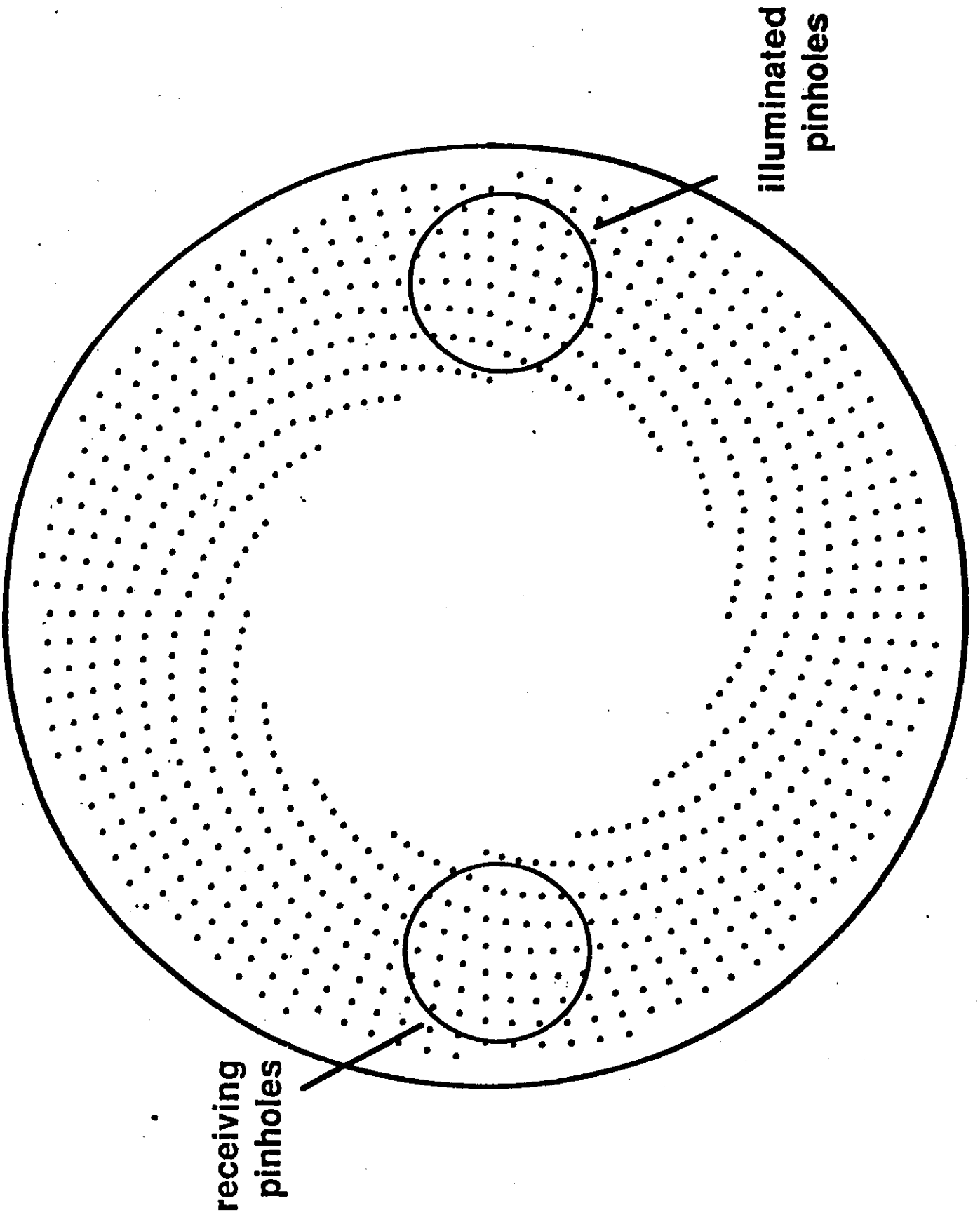


- **Multiple point systems -- TSM**

**space pinholes far apart -- cross talk**

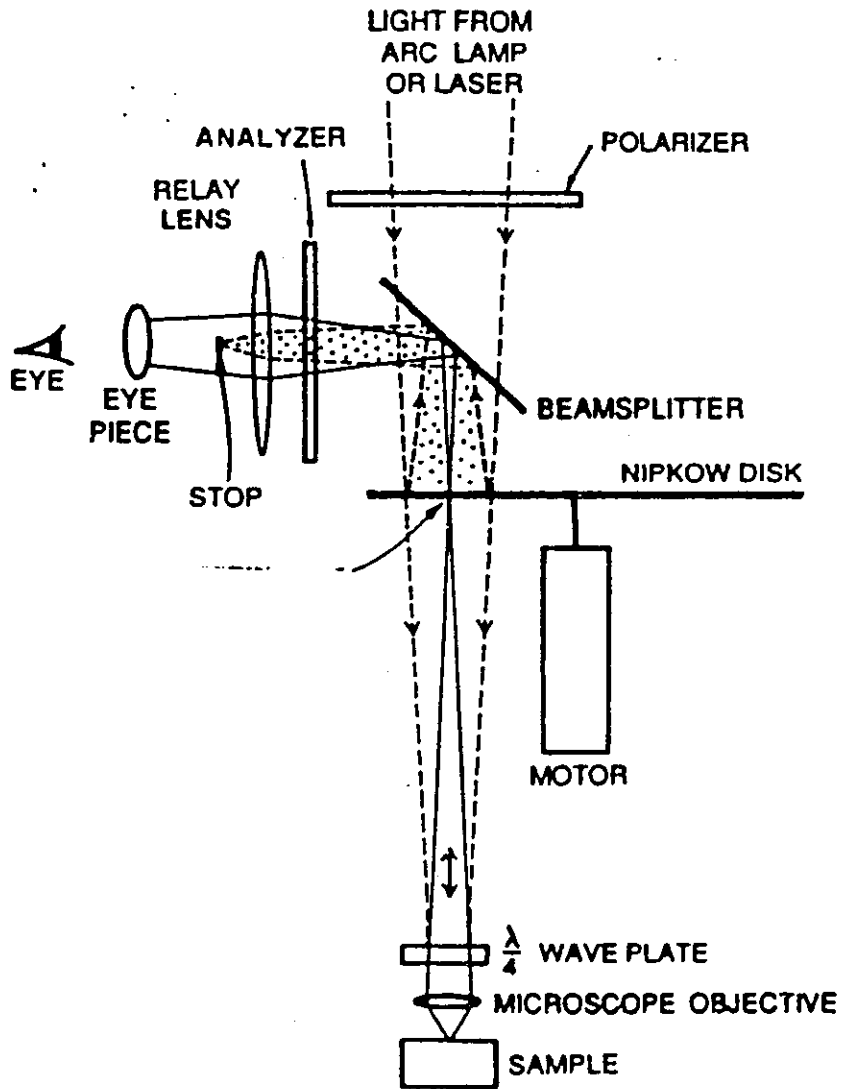






polarised light  
black disc  
stop  
Tilt disc - not shown

GORDON KINO



*filt (maybe)*

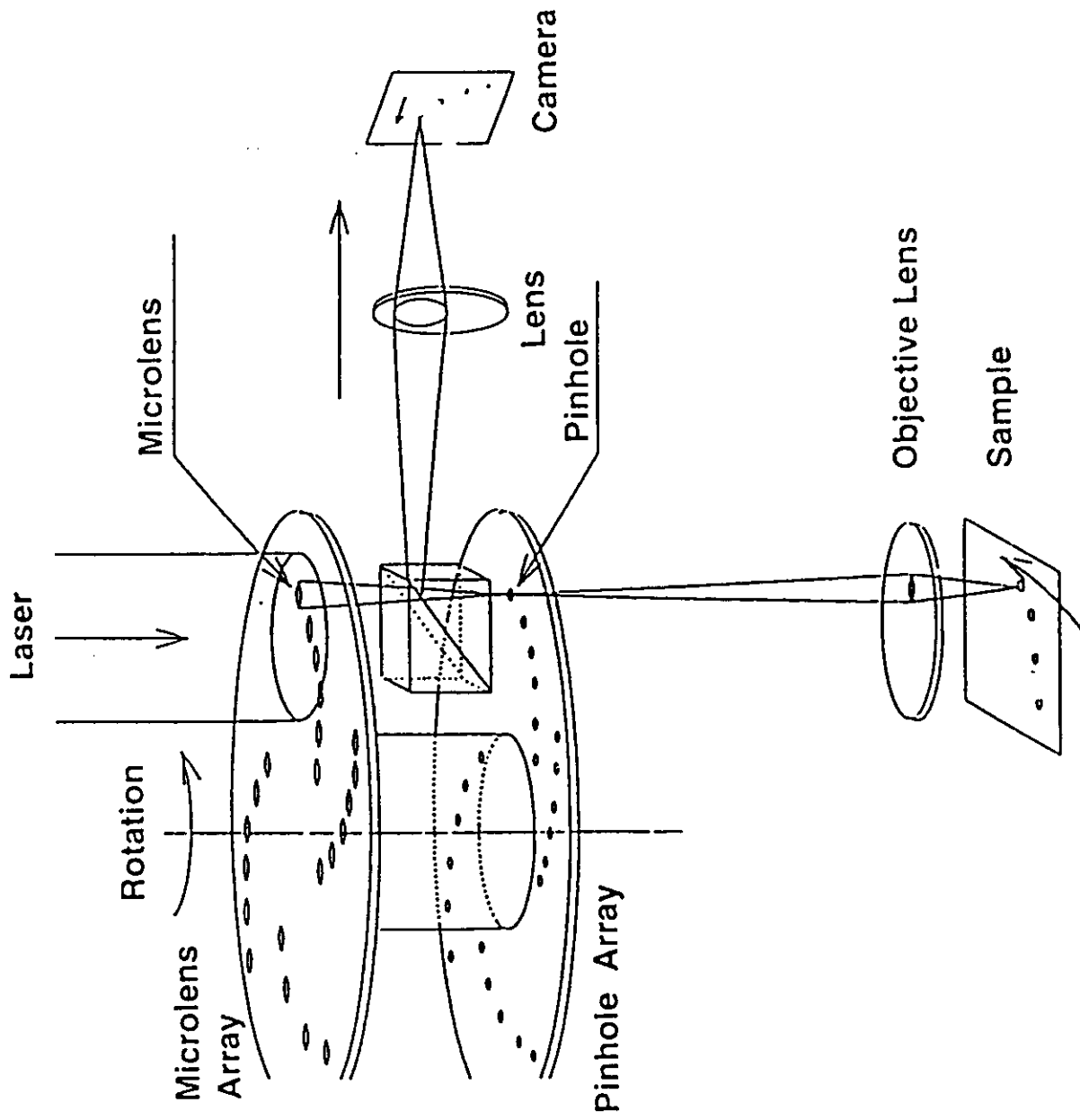


FIG.1. Overview of CSU10

# Confocal Microscopes

- **Single point systems**

**Lasers**

**brightness**

**limited wavelength choice**

***usually* not real-time**

- **Multiple point systems**

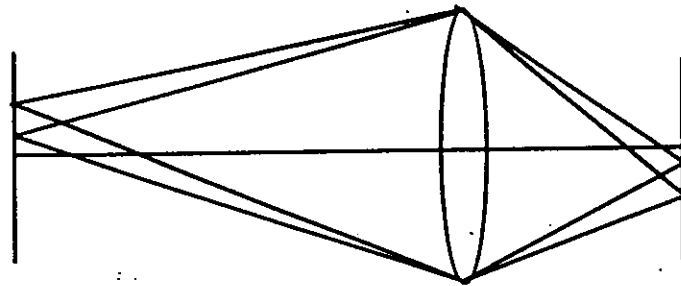
**Arc lamps can be used**

**wide wavelength choice**

**real-time**

**low light budget**

## Aperture Correlation



aperture  
mask

- Place pixels close together
- Programmable SLM as aperture mask
- Use time sequential pixel transmission,  $b_i(t)$ .
- Choose  $b_i(t)$  such that

$$\langle b_i(t)b_j(t) \rangle = \begin{cases} 1 & i = j \\ 0 & i \neq j \end{cases}$$

i.e. no cross talk between pixels

- Also need  $\langle b_i(t) \rangle = 0$

## Correlation Sequences

- Choose  $b_i(t)$  such that

$$\langle b_i(t)b_j(t) \rangle = \delta_{ij}$$

i.e. zero cross correlation between pixels

- (i) Independent random binary sequences +1, -1
- (ii) Complementary time shifted Golay sequences

Both require negative intensities!

### Solution

Add constant dc offset to  $b_i(t)$ .

Pixel transmission  $(b_i(t) + 1)/2$  i.e. 0 or 1

### Result

Composite confocal and conventional image

## **System implementation**

- **Code apertures -- obtain composite image**
- **Obtain conventional image**
- **Subtract to obtain confocal image**

## **Implementation**

- **Spatial light modulators**

**intensity or polarisation modulation of pixels**

- **Spinning aperture discs**

**impress correlation codes lithographically**

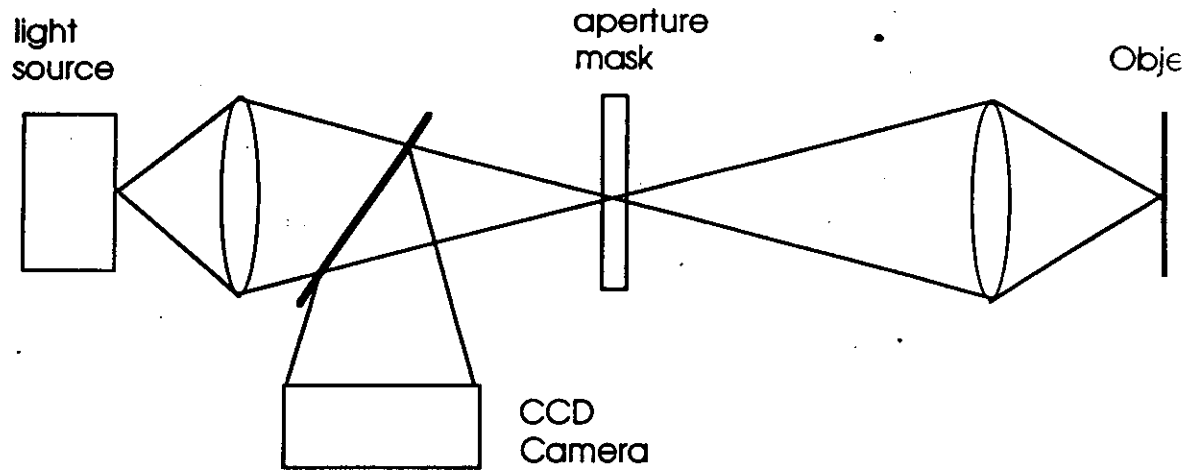
**spin disc to achieve correlation**

**use blank sector to obtain conventional image**

**real time subtraction**



# The System

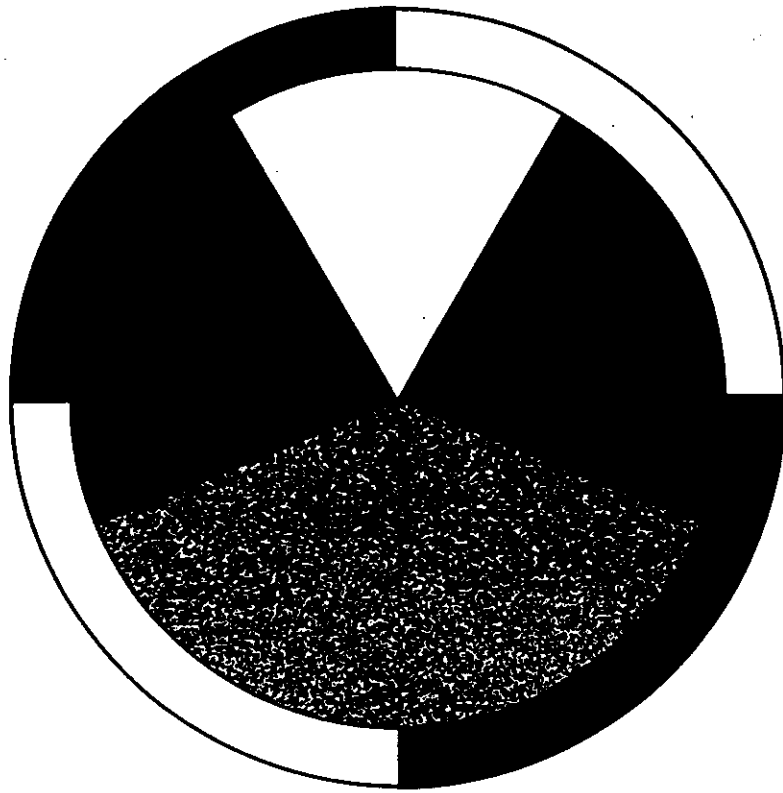


**Aperture Disc -- 80  $\mu\text{m}$  pixels on 80  $\mu\text{m}$  pitch  
random sequence  
equal black and white**

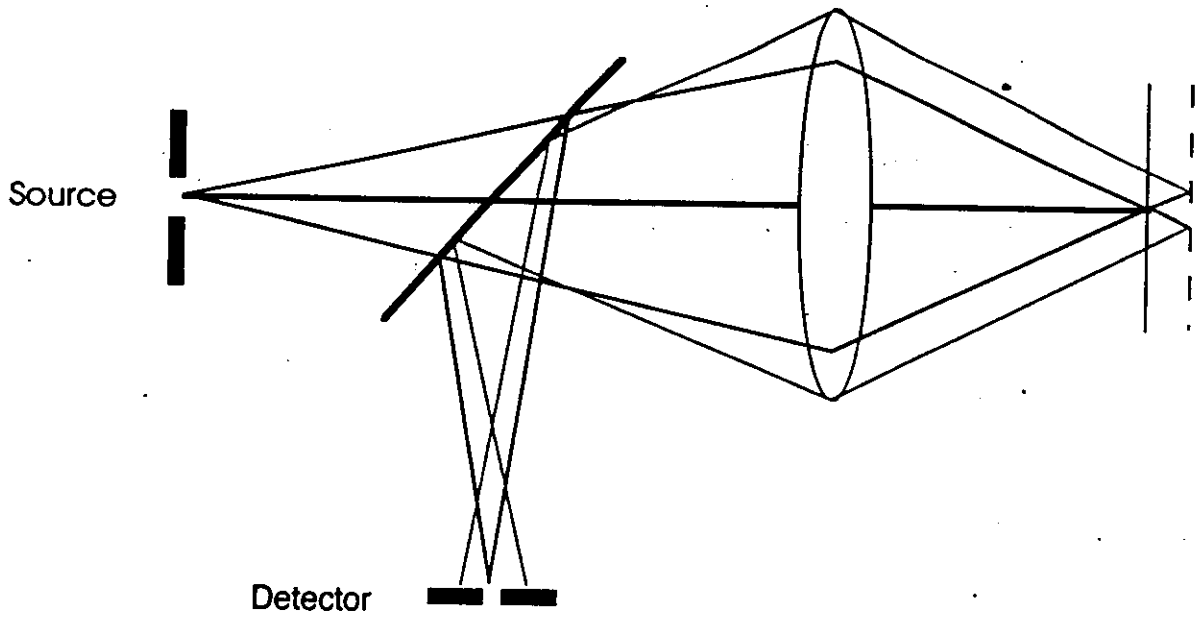
**Camera -- simple CCTV CCD camera**

**Light source -- incandescent projector bulb**

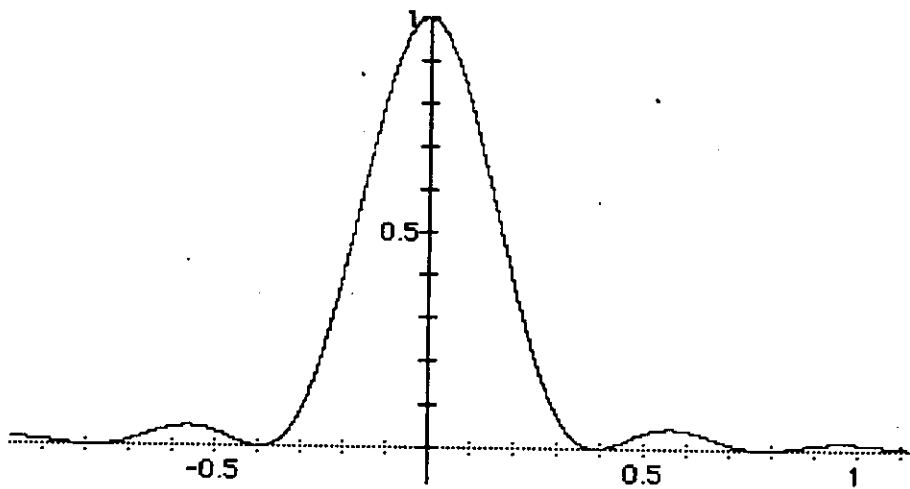
**Image speed -- 17 confocal frames/second**

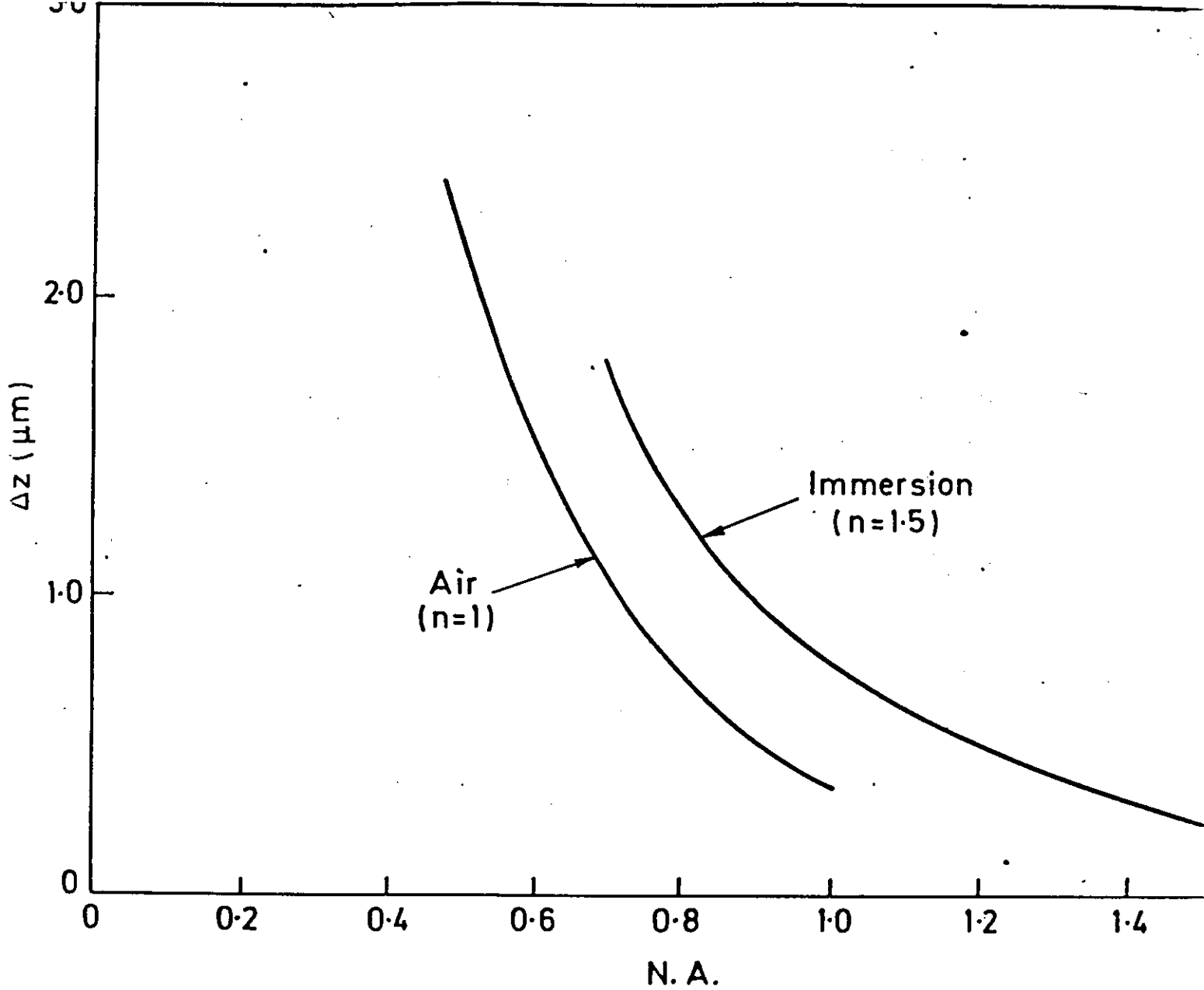


# Optical sectioning



- **Scan plane reflector through focus**



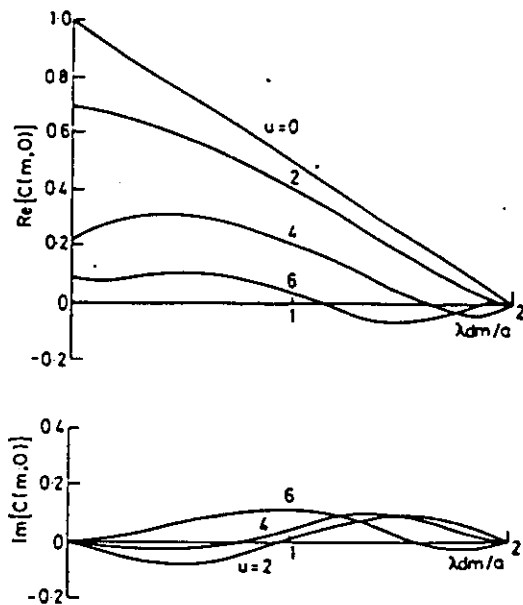


(11)

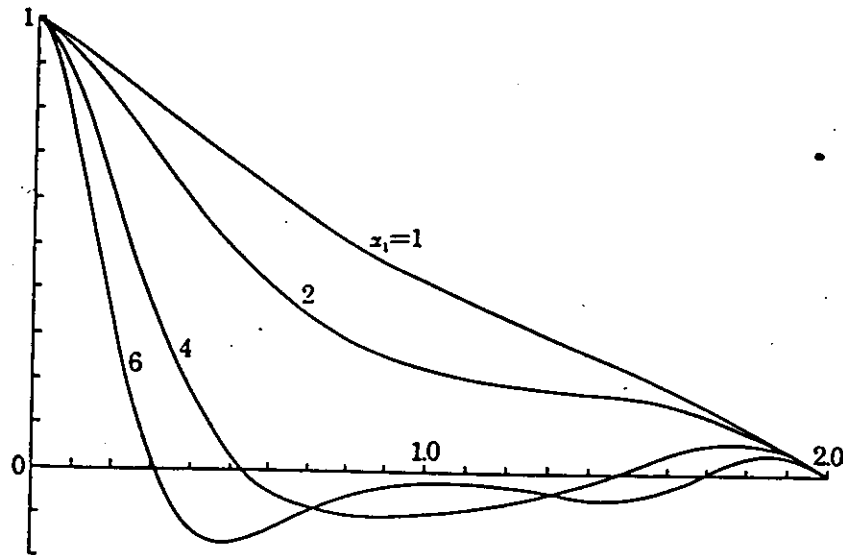
# Optical Sectioning

- Require all spatial frequencies to attenuate with defocus.
- Confocal -- yes
- Conventional -- no
- Weak object transfer function reflection

## Confocal



## Conventional



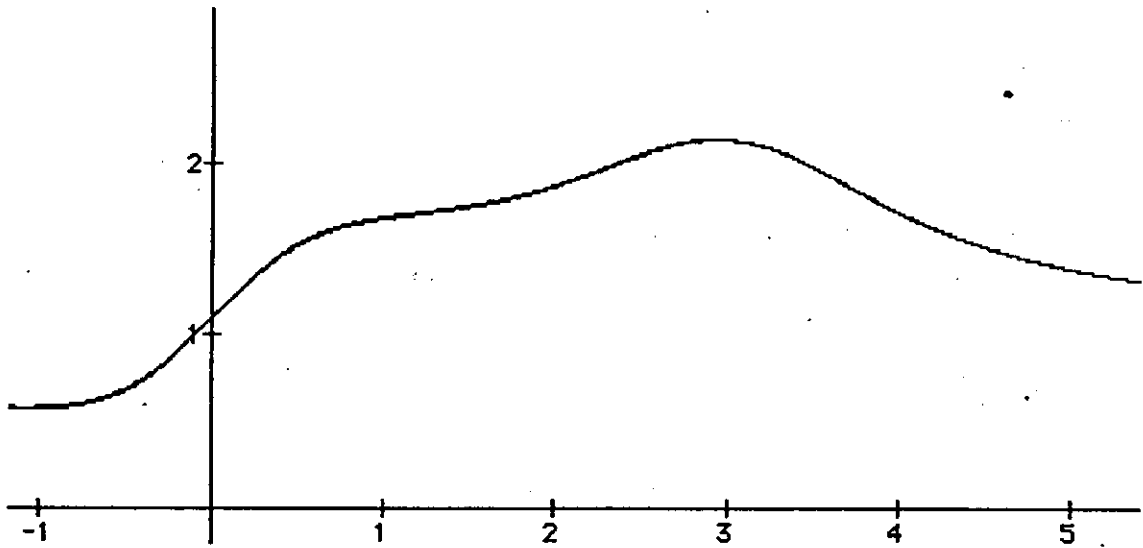
- **Non-zero spatial frequencies do attenuate with defocus.**

so

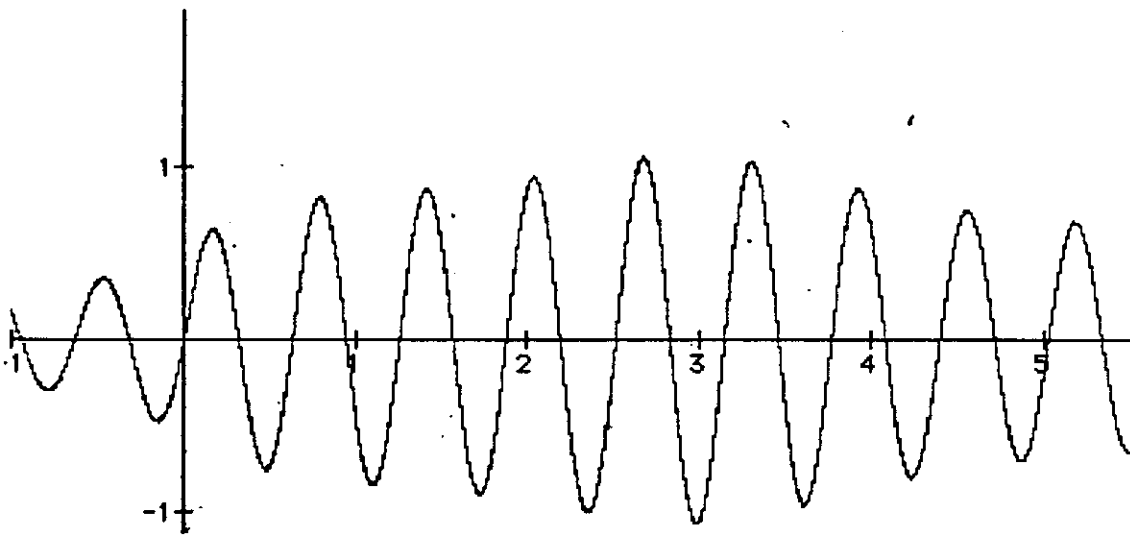
- **illuminate object with a single spatial frequency -- fringe pattern.**
- **obtain optically sectioned image but with fringe pattern super-imposed.**
- **remove fringe pattern**
- **optically sectioned image**

# Example

## Actual image signal



## Image with fringes



## Fringe Removal?

## Implementation

- Introduce 1 D grating into illumination path

$$S = 1 + \cos(2\pi v x)$$

- Image  $I = I_0 + I_{sf}$

$I_0$  is a conventional image.

$I_{sf}$  is the sectioning image with fringes.

## Fringe removal

- Design of suitably matched detector array to sample at fringe maxima (followed by  $\pm 1$  multiplication).
- Very stringent alignment -- impractical.
- Mathematical technique using three images.
- Fast, simple, no alignment problems



## Fringe removal

- **1 D grating in illumination path**

$$S = 1 + \cos\{2\pi\nu(x + \phi)\}$$

$\phi$  represents a shift in the grating position

- **Image crudely**

$$I = I_0 + I_s \cos\{2\pi\nu(x + \phi)\}$$

$I_s$  is the desired sectioning image.

Take three images.

$I_1$  corresponding to  $\phi=0$

$I_2$  corresponding to  $\phi=120$

$I_3$  corresponding to  $\phi=240$

Calculate

$$I_s = \sqrt{(I_1 - I_2)^2 + (I_1 - I_3)^2 + (I_2 - I_3)^2}$$

$$I_0 = I_1 + I_2 + I_3$$

## Fringe Removal

$$I_s = \sqrt{(I_1 - I_2)^2 + (I_1 - I_3)^2 + (I_2 - I_3)^2}$$

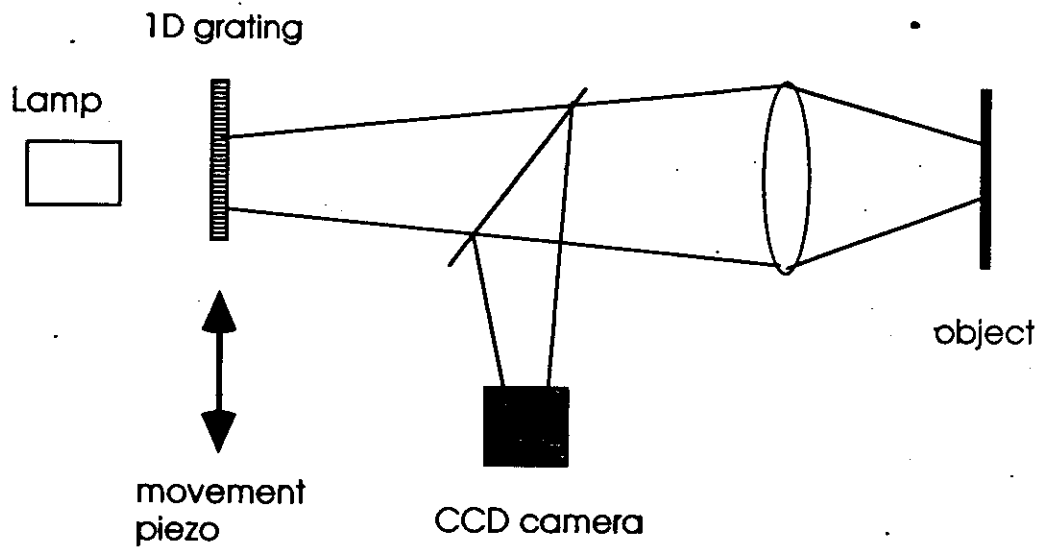
- **Computationally intense**
- **$I_1, I_2,$  and  $I_3$  all from 8 bit, say, camera**
- **Fixed number of values**
- **Look-up table -- real time imaging.**

Full theory gives

$$I = \left| \iint C(m, p) T(m) T^*(p) \exp - j(m - p)x dm dp \right|$$

- **partially coherent**
- **axial response to plane mirror --  $|C(0,0)|$**

# Implementation



- **standard microscope illumination**
- **piezo-driven 25  $\mu\text{m}$  pitch grating**
- **light efficient**
- **real-time imaging**
- **easily and cheaply implemented in conventional microscope**

