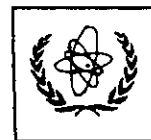




UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL ATOMIC ENERGY AGENCY
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
I.C.T.P., P.O. BOX 586, 34100 TRIESTE, ITALY, CABLE: CENTRATOM TRIESTE



SMR.1065 - 19

COLLEGE ON SOIL PHYSICS **14 - 30 APRIL 1998**

"Erosion Models"

Donald M. GABRIELS
University of Ghent
Laboratory of Soil Physics
Department of Soil Management & Soil Care
Faculty of Agriculture & Applied Biological Sciences
Coupure Links 653
B-9000 Ghent
BELGIUM

These are preliminary lecture notes, intended only for distribution to participants

MODELANSWERSAreal Non-Point Source Watershed
Environment Response Simulation

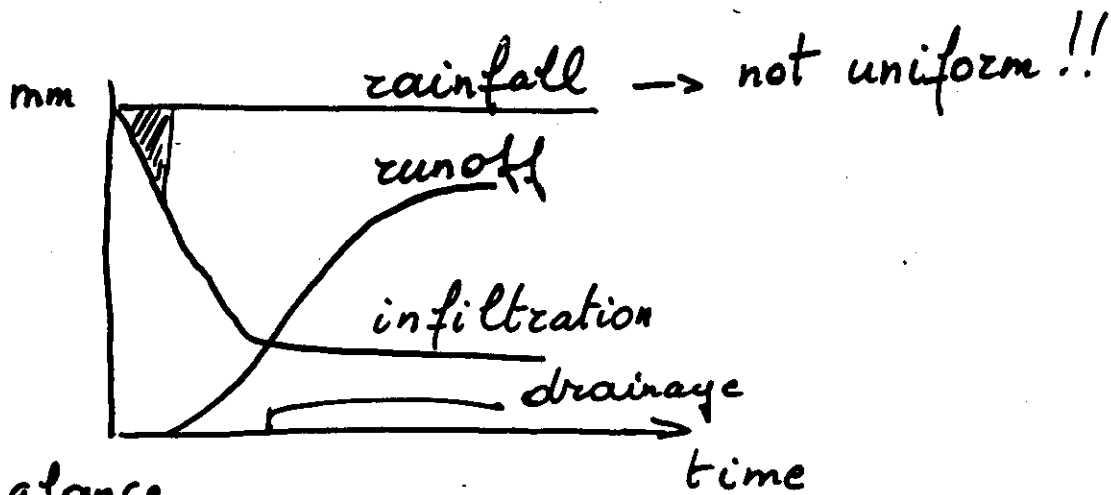
→ Agricultural Watersheds
consists of

- 1) Hydrological model
- 2) Sediment Detachment/Transport model
- 3) components to describe movement of water
 - overland flow
 - channel flow
 - subsurface flow

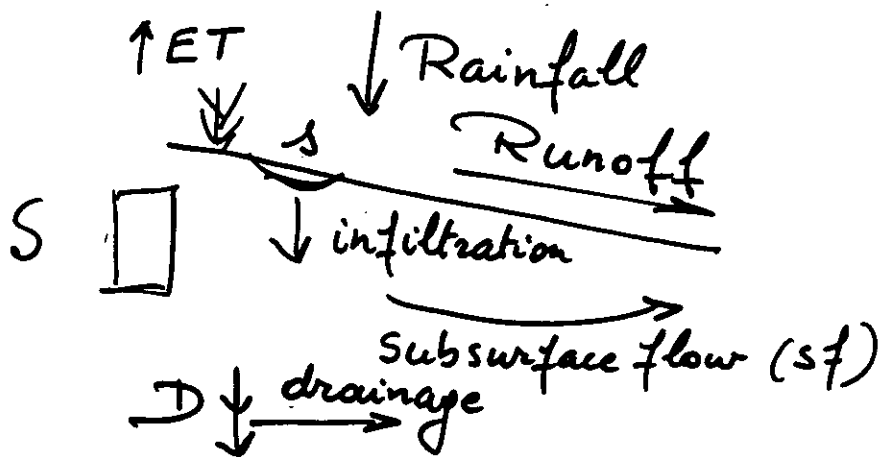
→ event oriented $\neq$ long term

1) Hydrology model

2



Balance.

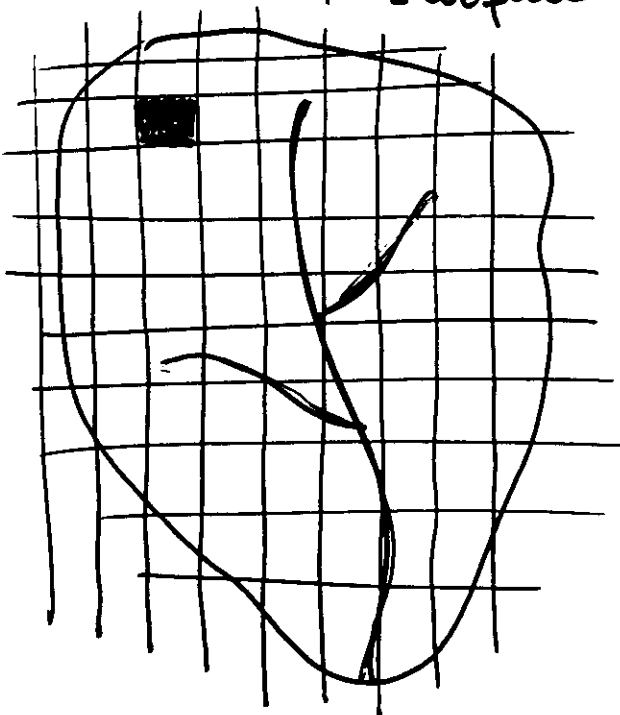
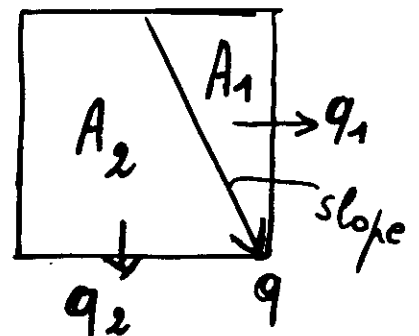


$$\text{Rainfall} = \text{infiltration (I)} + \text{runoff (r)} + \text{soil storage (S)} + \text{drainage D} + \text{subsurface flow (sf)} + \text{surface storage} + \text{ET}$$

$$\text{Input} - \text{Output} = \frac{dS}{dt}$$

$$q_1 = \left(\frac{A_1}{A_1 + A_2} \right) q$$

$$q_2 = \left(\frac{A_2}{A_1 + A_2} \right) q$$



Infiltration $f = f_c + A \left(\frac{S-F}{T_p} \right)^P$

f : infiltration rate at a particular time
 f_c : final or steady state infiltration rate

A : difference between maximum and steady state rates

S : storage potential of soil
 (total porosity - antecedent moisture content)

F : total volume of water infiltrated

T_p : total porosity within the control depth

P : coefficient related to decrease infiltration
 increase soil moisture

Subsurface drainage

- drainage? when soil water content > field capacity

- when soil is saturated then the subsurface drainage = steady state infiltration rate (k_s)

$$SDR = f_c \left(1 - \frac{PVOL}{SWC} \right)^b$$

f_c : steady infiltration rate

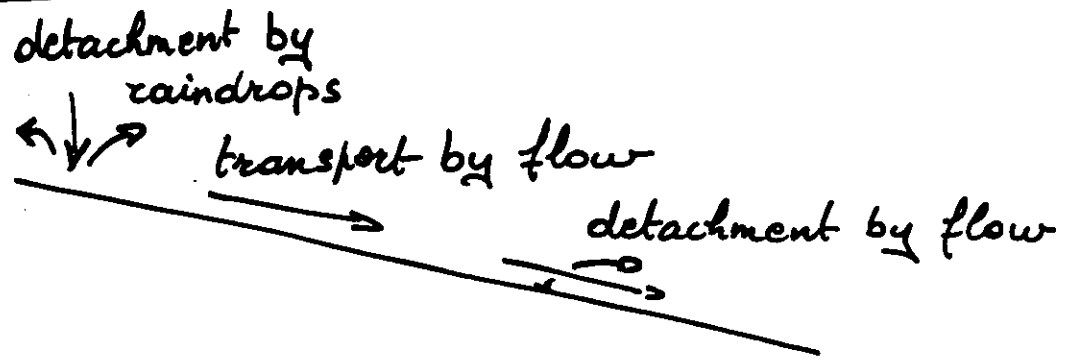
$PVOL$: unsaturated pore volume
 (tot. porosity - soil moisture content)

SWC : volume of gravit. water
 (tot. porosity - field capacity)

b : drainage coefficient

Flow in CHANNELS ?? Manning's equation,
 $\frac{\text{flow depth}}{\text{flow rate}}$

2) Erosion model



Sediment movement in flow

$$\frac{dG_F}{dx} = R_{DT} + D_F$$

G_F : rate of sediment movement in flow
(weight per unit width per unit time)

x : distance along flow surface

R_{DT} : rainfall detachment rate
(weight per unit area per unit time)

D_F : flow detachment rate
(weight per unit area per unit time)

DETACHMENT OF SOIL PARTICLES by RAIN DROP IMPACT

5

$$\boxed{D_R = 0.027 C K A_I I^2}$$

where: D_R = rainfall impact detachment rate
kg/min

C : cropping factor

K : soil erodibility factor

A_I : area increment (m^2)

I : rainfall intensity (mm/min)

or (splash erosion rate) W_s ($kg/m^2/h$)

$$W_s = 0.182 K_r K_h C_m \left[2.96 (\sin \theta)^{0.79} + 0.56 \right] \times \left[(1-p) I^{ex} + p C_n I_x^{ex} \right]$$

where: K_r : erodibility factor for splash
 K_h : water depth correction factor
 C_m : crop mulch factor
 θ : slope gradient
 p : fraction of area covered by canopy
 C_n : crop canopy factor
 I : rainfall intensity (cm/hr)
 I_x : excess rainfall intensity

$$K_h = a \cdot e^{-h/D_{50}}$$

h : water depth (cm)

D_{50} : median drop
diameter of raindrops

DETACHMENT OF SOIL PARTICLES BY OVERLAND FLOW

6

$$D_F = 0.018 C K A_I S Q$$

where D_F : overland flow detachment rate
kg/min

S : slope steepness

Q : flow rate per unit width (m^2/min)

or FLOW EROSION RATE W_F ($kg/m^2/h$)

$$W_F = 11.02 K_f C_f \tau^{cx}$$

τ : bed shear stress (N/m^2)

$\tau = \gamma h S$ γ : specific gravity of water

S : slope gradient

h : water depth

K_f : flow erodibility factor K (USLE??)
depends on soil erosion

C_f : crop factor

EROSION in CHANNELS E_{CH} ($kg/m^2/h$)

$$E_{CH} = 11.02 c K_f C_f \tau^{cx}$$

c : correction factor for rill channels gullies

TRANSPORT CAPACITY of FLOW

$TF = 146 (S Q^{1/2})$ for $Q < 0.046 m^2/min$

$TF = 14600 (S Q^2)$ for $Q > 0.046 m^2/min$

TF : transport capacity of flow ($kg/min/m$)

Q : flow rate per unit width m^2/min

S : slope (m/m)

Sediment concentration/streampower relationships

$$W = \rho g S D_w V_w$$

$$W = \rho g S OVF_w$$

W : streampower of overland flow ($J/s.m^2$)

S : slope

D_w : water depth

V_w : flow velocity

OVF_w : Volumetric water flux of overland flow
 $m^3/s.m$ (m^2/s)

Bagnold sediment transport/streampower relationships

$$\frac{i_b}{(W - W_0)} = \left[\frac{(W - W_0)}{W_0} \right]^{1/2} \left(\frac{Y}{D} \right)^{-2/3}$$

i_b : sediment transport rate

W : streampower of runoff

W_0 : threshold streampower

Y/D : flow depth to grain size

Kirkby's sediment transport

$$G = Q^2 S$$

$$G = CP Q^2 \sin S 10^{-3}$$

G : transport capacity of overland flow

Q : overland flow discharge

CP : cover-practice factor.