



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION



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SMR/107 - 20

WORKSHOP ON PATTERN RECOGNITION AND ANALYSIS OF SEISMICITY

(5 - 16 December 1983)

FRACTURE DYNAMICS

Modeling the Earthquake Source

L. KNOPOFF

These are preliminary lecture notes, intended only for distribution to participants.
Missing copies are available from Room 230.

FRACTURE DYNAMICS

MODELING the EARTHQUAKE SOURCE

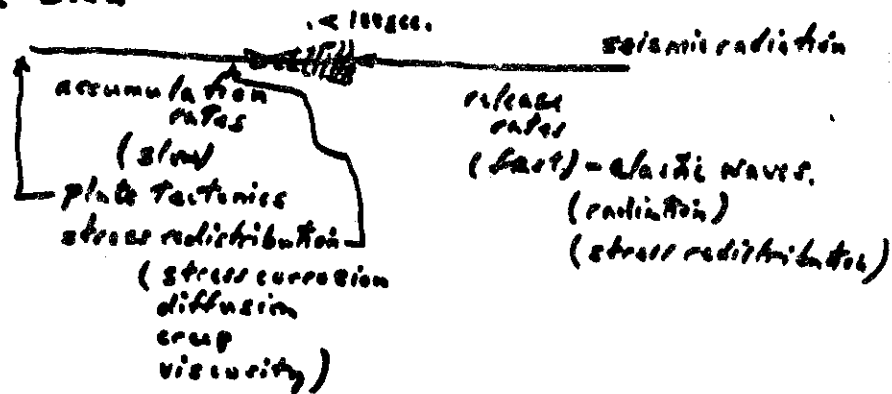
Eqs. ARE rapid release of stored potential energy: Containment

Types of conservative systems (for our purposes)
elastic, magnetic, electric, gravitational
atomic

for shallow earthquakes \rightarrow elastic

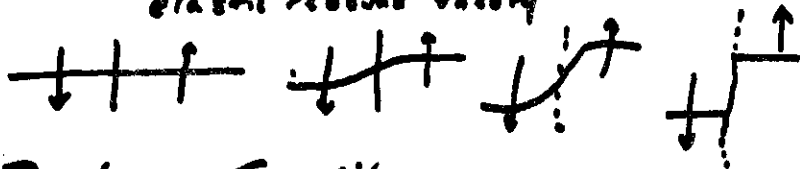
deep earthquakes \rightarrow elastic?, atomic?

Time Scale



Critical Point: Fracture criteria

elastic rebound theory

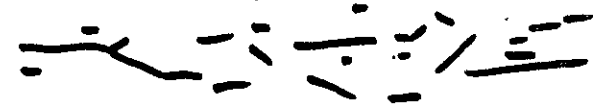


Prestress, Causality

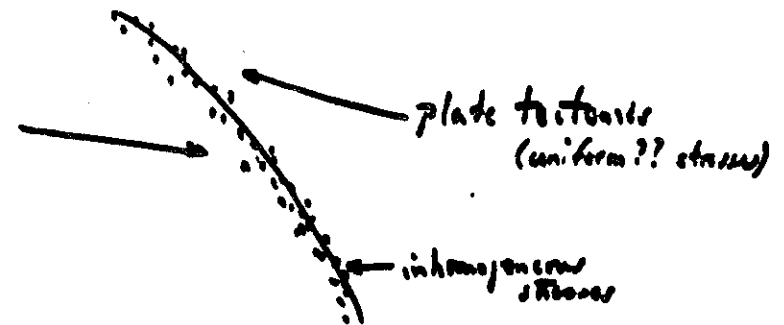
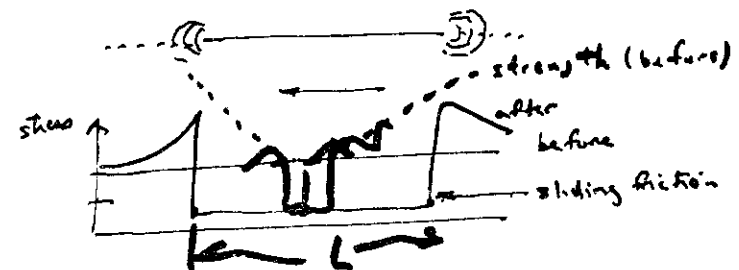
Geometry of fracture

Pre-existing fracture surfaces
re-arrangement
crushing

Self-similarity



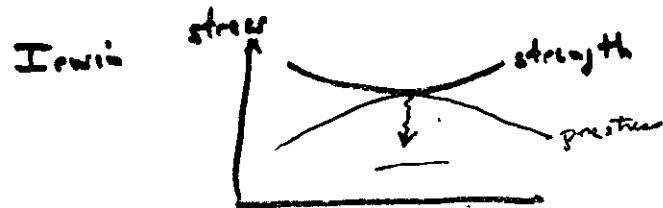
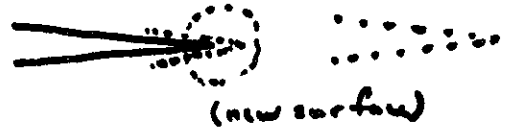
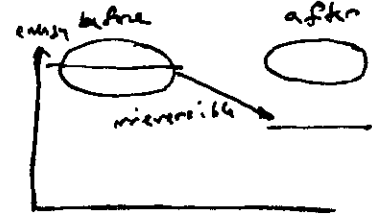
Stress redistribution



Stat. Form energy balance

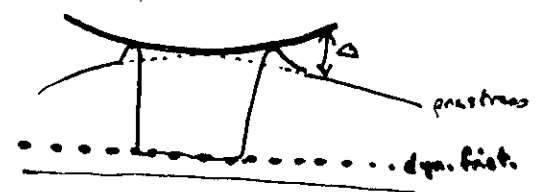
Prestress energy \rightarrow radiation
frictional sliding
redistribution

Fracture criteria
Griffith



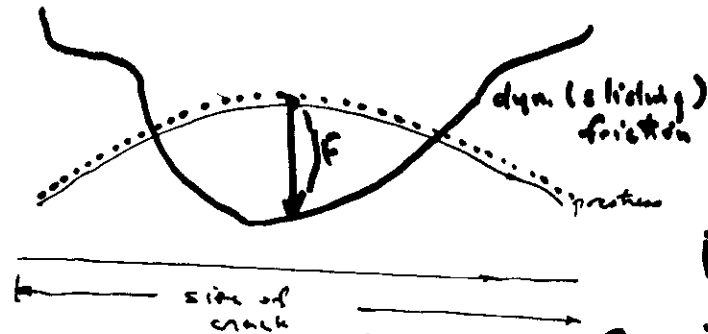
Compatible?

What stops a crack?



rate of expansion \rightarrow self-regulating
(by barrier Δ)

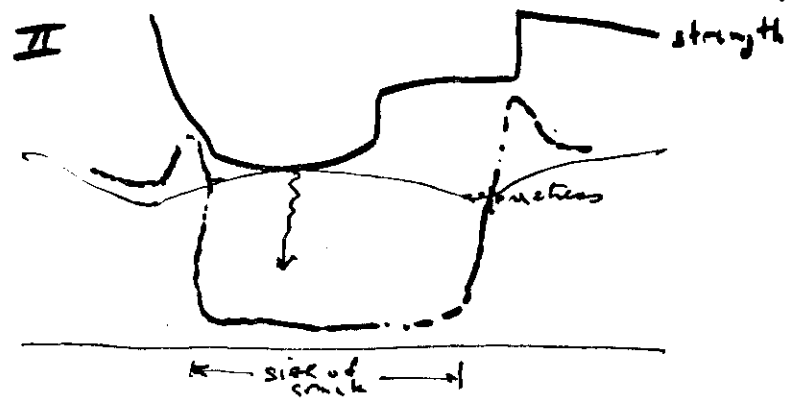
I



$$F = ma$$

Burridge
& Holliday
Geophys. J.
R.A.S.
1972 \pm 1

II



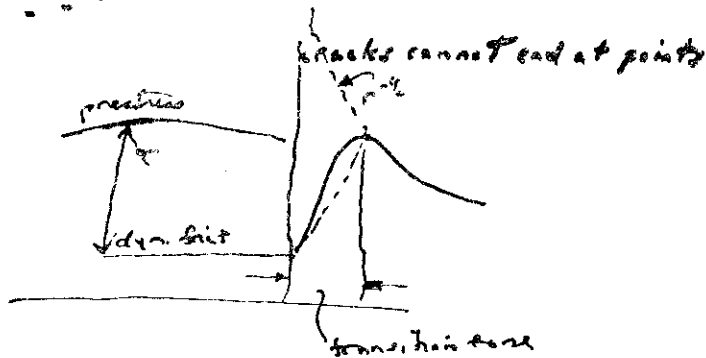
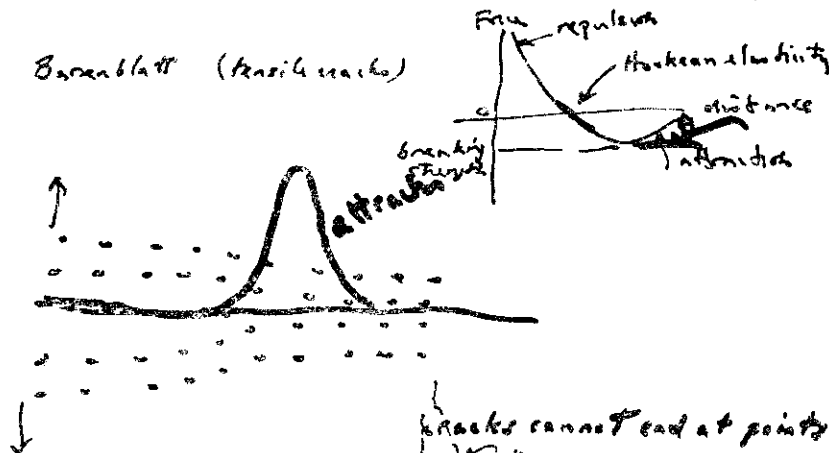
III-5

Mathematics → plane fractures: 1-D
2-D

cracks (dynamically) end at a point (1D, 2D)

singularities cracks cannot
 $\sigma \sim r^{-1/2}$ end at points

Barenblatt (tensile cracks)

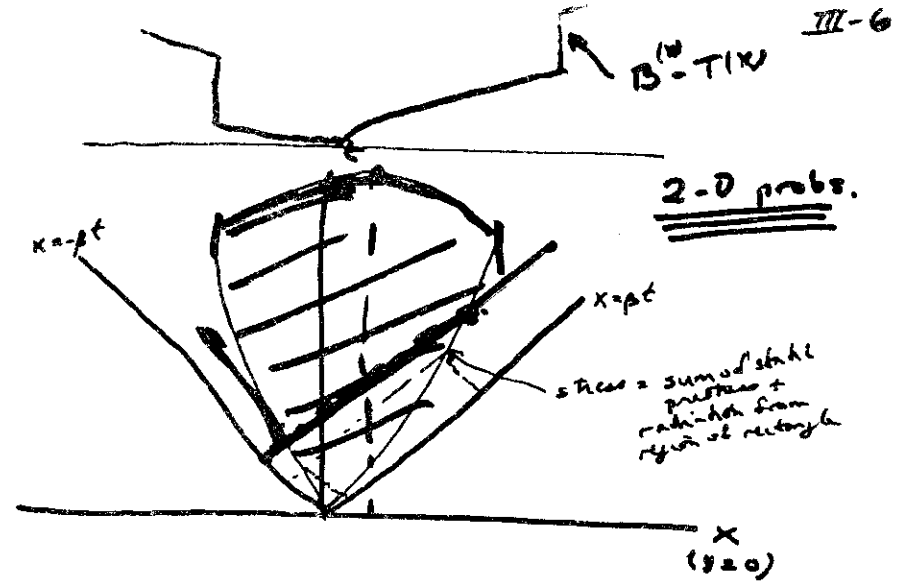


Dynamic/
crack problems - non-linear

$$\sigma \sim K r^{-1/2}$$

$$= \frac{K I}{r^{1/2}}$$

K is the intensity factor



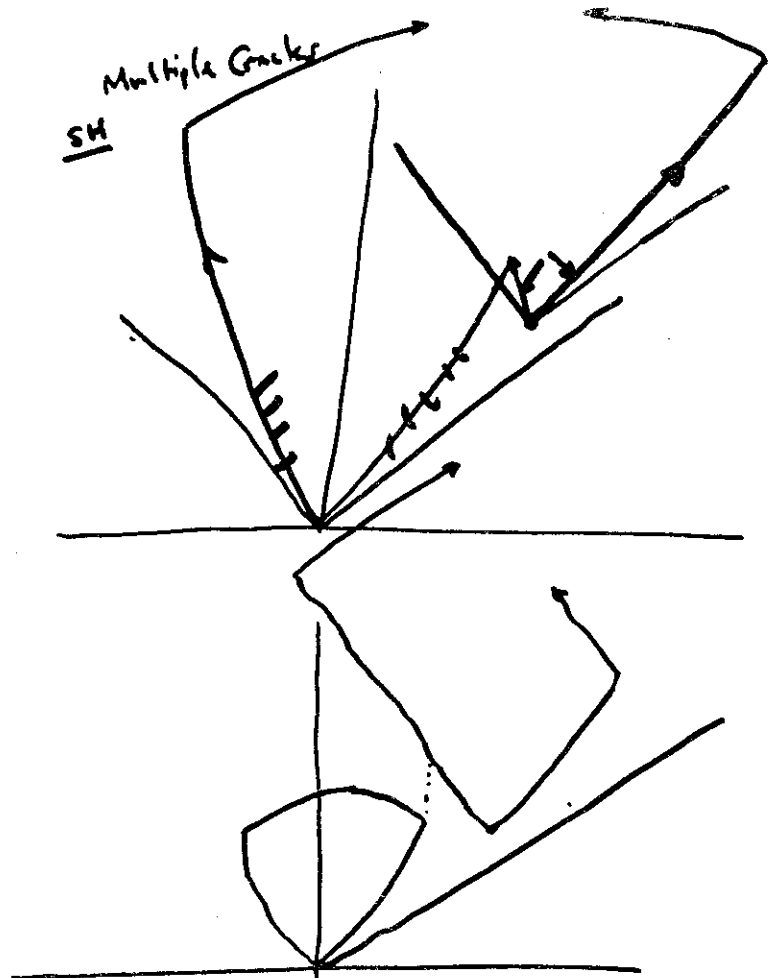
types of motion:

I SH: u_z

If we know $u_0(x, y=0, t)$ we can
calculate motion $u(x, y, t)$.

We can also solve
II SV: u_x, u_y

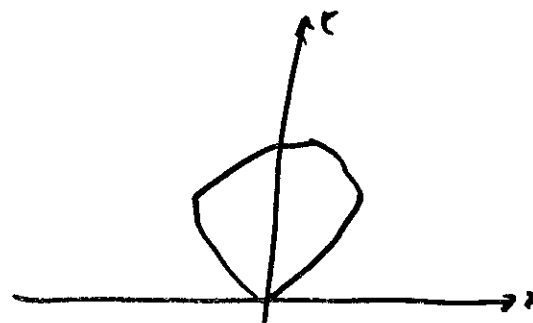
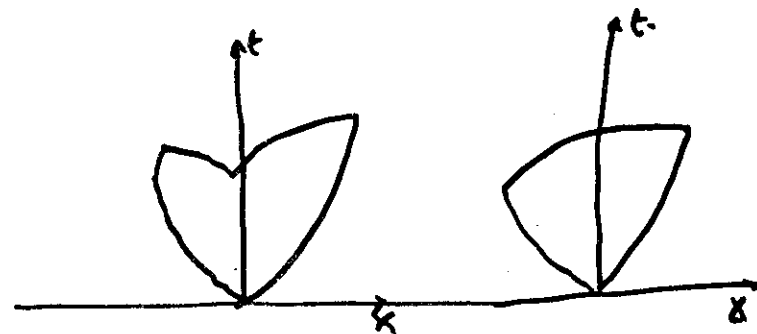
III-6



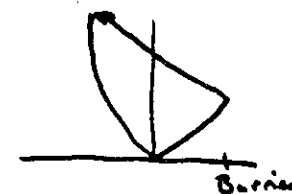
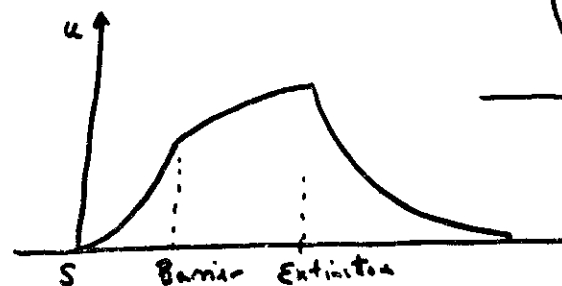
III-7

storing phases

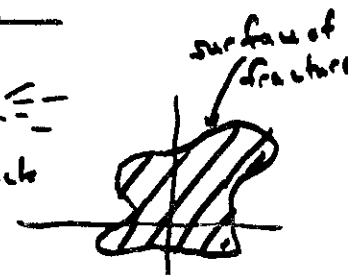
III-8-



seismogram



(Hasel: General 3-D plane crack
Stochastic model of
Crack



Fracture Dynamics

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