

INTERNATIONAL ATOMIC ENERGY AGENCY
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SMR/107 - 22

WORKSHOP ON PATTERN RECOGNITION AND ANALYSIS OF SEISMICITY

(5 - 16 December 1983)

PHYSICAL CAUSES OF AFTERSHOCKS

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These are preliminary lecture notes, intended only for distribution to participants.
Missing copies are available from Room 230.

IV Aftershocks

Time scale — minutes (or less) to years

Rate $n \sim 1/2$ Omori (1892)

→). Possibility of very long time aftershocks
- Intraplate seismicity

Triggered by main earthquake
stress relaxation or stress of fault is important

if Diffusive processes may be dissipative

Processes in time interval between shock diffusive

Processes at times of aftershocks are elastic

Example of stress relaxation/diffusion in laboratory

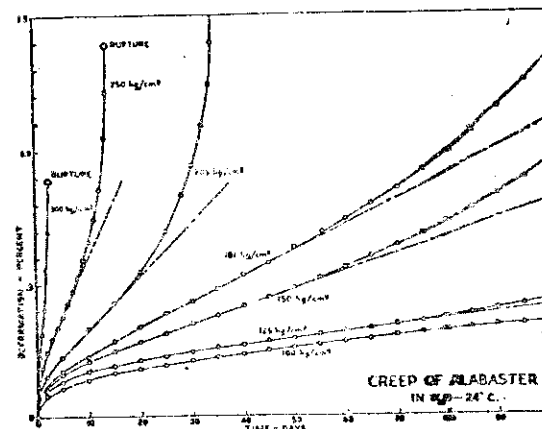
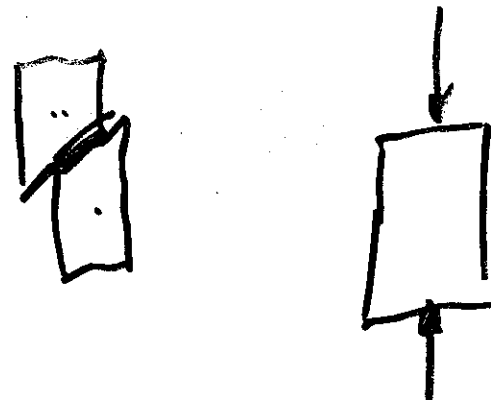
Processes in rocks accelerated because of water

Rate of accel. enough why not
fast enough

$$t_f = t_0 e^{-E/kT}$$



Time taken
recrystallization



$$t_f = t_0 e^{-E/kT} \quad E = \sigma V$$

a large number of
references:

Glasses: Preston et al., Nature 156, 1946
J. App. Phys. 17, 1946

Metals: Zhurkov, Int. J. Fract. Mech. 1, 1965

Rock: Griggs, Bull. G.S.A. 51, 1940

Plastics, Ionic Solids: Zhurkov, loc. cit.

Natals: Cherepanov, Mech. of Brittle Fract. (McGraw-Hill 1979)

TABLE 1.—Properties of alabaster in wet creep tests at different stresses
(Gypsum in each experiment subject to constant load, in the presence of its own saturated aqueous solution, at 70°C, $\epsilon_0 = \epsilon_\infty = 0$)

Compressive stress ($\sigma_1 = \sigma_2$ in kg/cm ²)	Steady-state velocity (millionths per day) v_s	Deformation before fracture (per cent) δ	Duration of test (to fracture) (days) t_f	Equivalent viscosity (poises) $\eta \times 10^{10}$
300	2000	1.89	2.45	.42
250	440	1.39	13.58	1.60
205	219*	2.5*	48*	2.64
181	100	3.0	133	5.11
165	77.0	3.8	285	0.04
150	68.5	>1.05	>110	0.36
125	24.5	3.8	308	14.4
103	7.0	>2.7	>520	41.0 (1)
	2.6	>6.1	71900	42.2

* Average of three duplicate tests.

Properties of same gypsum when dry:
Strength (short-time) = 520 kg/cm²
Deformation before fracture = 35% (primarily elastic)
Equivalent viscosity = $> 5 \times 10^{10}$ at 420 kg/cm²

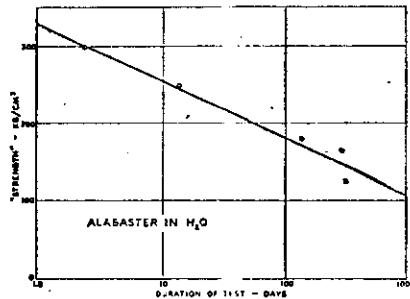


FIGURE 10.—Strength of alabaster as a function of duration of test
Data from experiments of Figure 8.

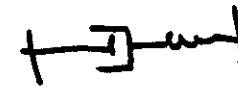
Viscosity? Viscoelasticity?

Seismological evidence for creep

1. Afterslip before & after earthquakes
2. Silent earthquakes
3. Aftershock swarms (no clusters).

Linear viscoelasticity

Maxwell body



runs away under
static load

Kelvin body



ind. resistance
inf. atten. at
omega
(but real h.f. & minima v.g.)

Std viscoel.
solid



$$\tau = \mu \epsilon + \eta \dot{\epsilon}$$

Consider a pre-existing crack in

- 1) a uniform stress field and
- 2) the medium has the properties of a standard viscoelastic body

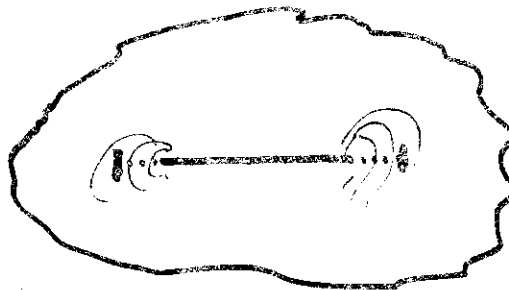
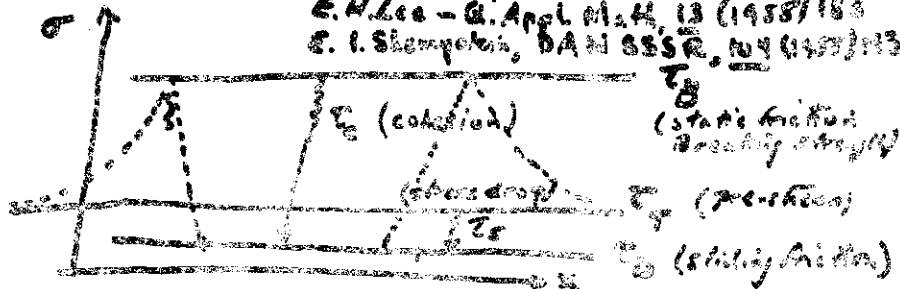
We separate the problem into two regimes

a) quasistatic

b) seismic

correspondence principle

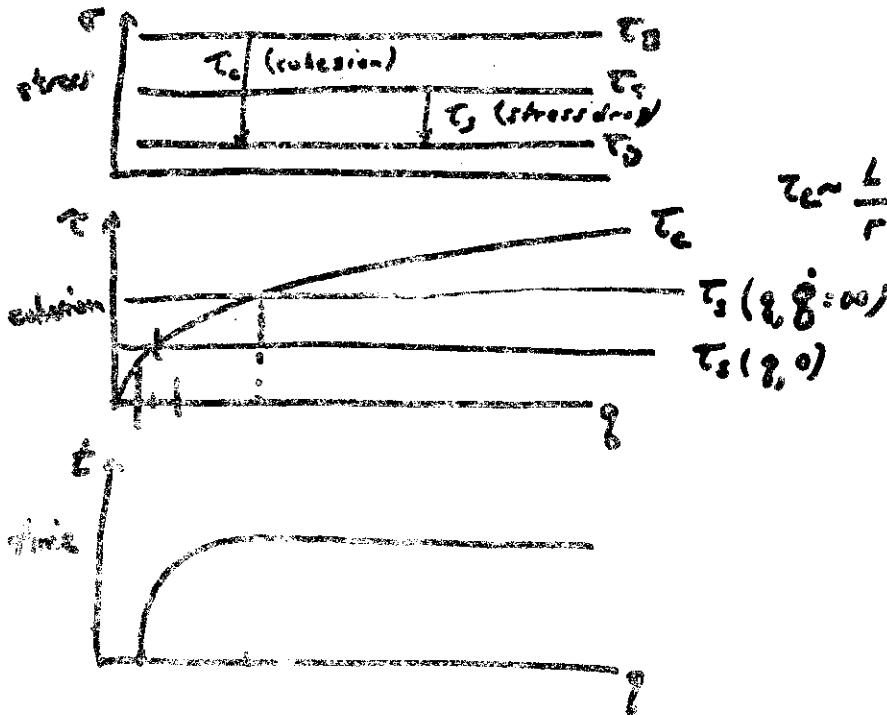
E.H. Lee - Q. Appl. Math. 13 (1955) 183
S. I. Shampygin, DAN SSSR, 124 (1957) 113



2-D

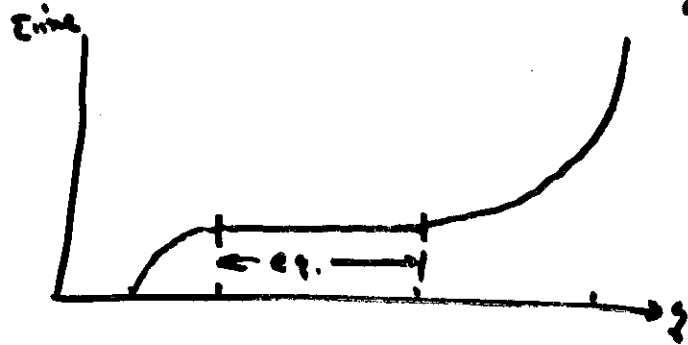
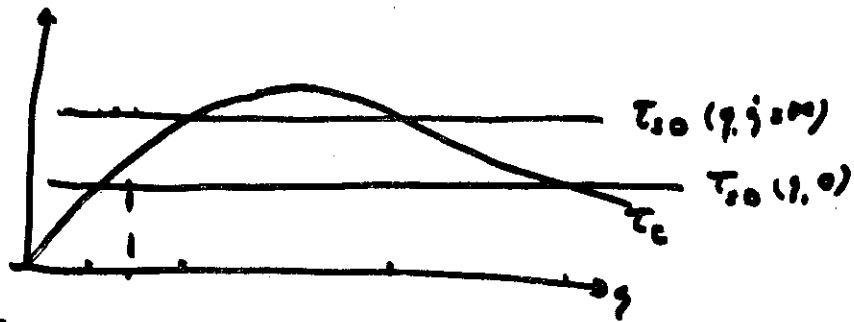
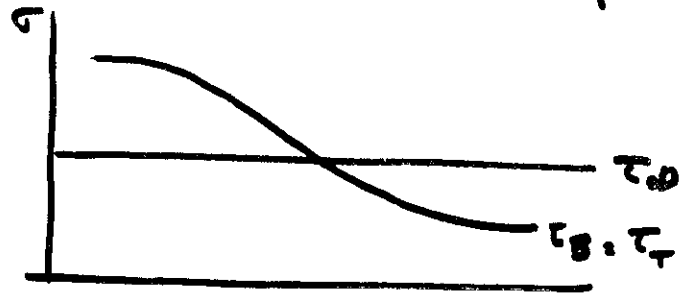
$$v \propto \sqrt{\frac{K}{\rho}}$$

This crack will undergo accelerated extension quasistatically for a finite time; when its velocity of extension reaches velocity comparable to $\beta = v_s$, it starts to radiate seismic waves. This crack never stops.

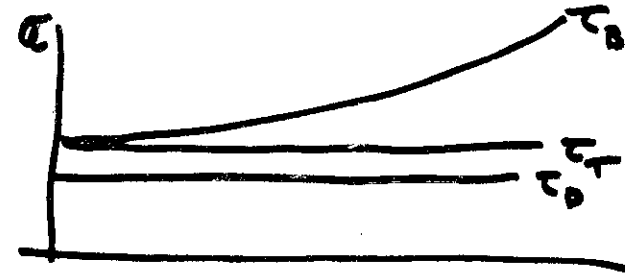


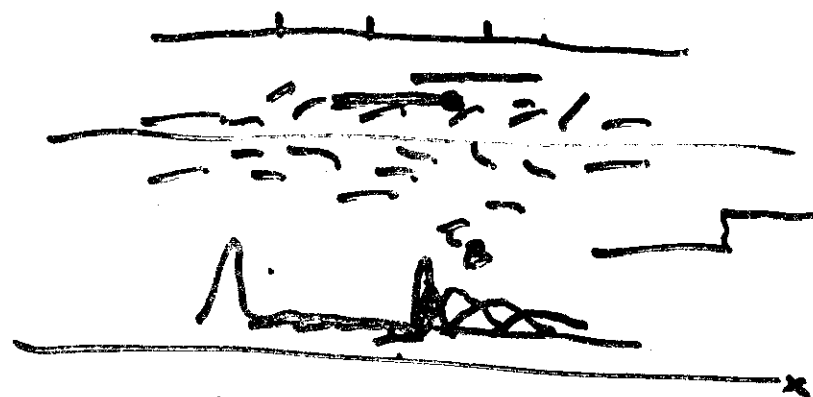
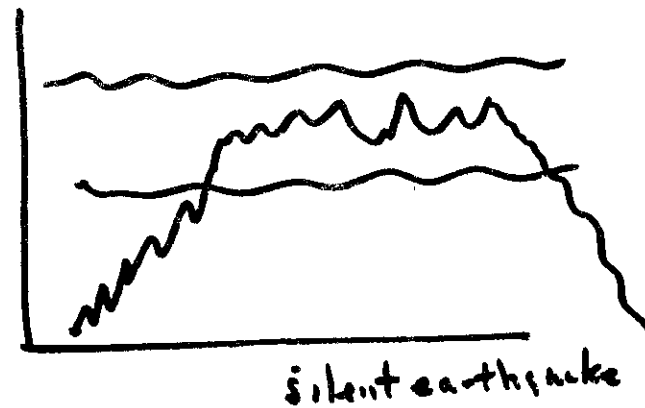
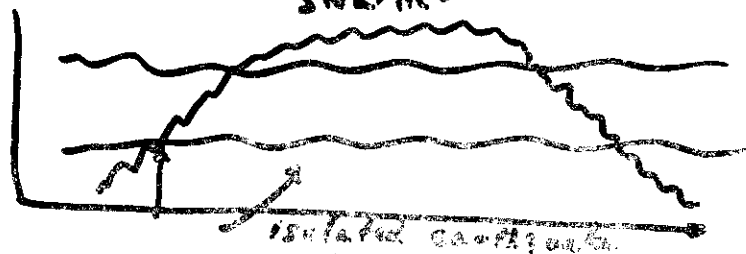
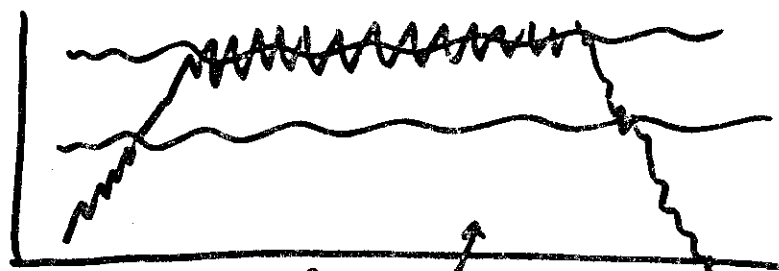
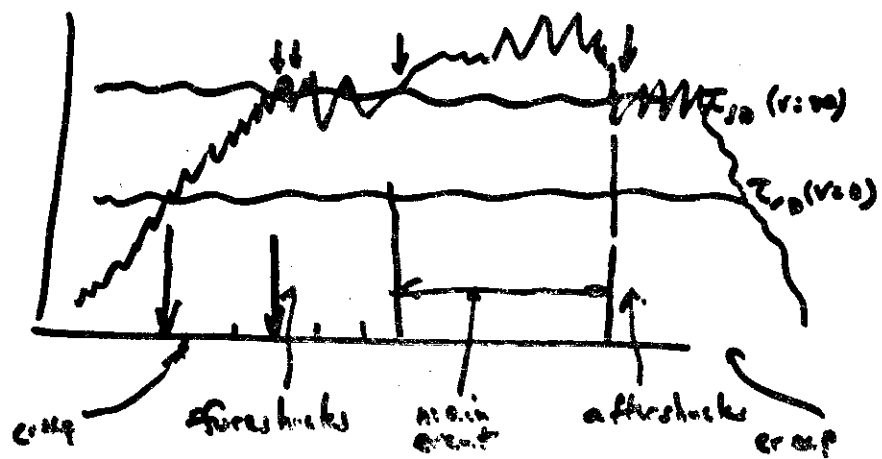
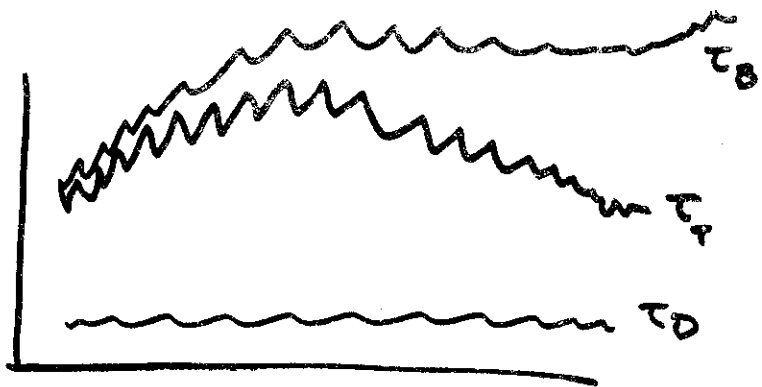
$$\tau_c \sim \frac{L^2 \tau_s^2}{\rho h}$$

reversal of stress drop
~~as method of stopping a crack~~ as method of stopping a crack



Elevated breaking strength as method of
 stopping a crack





References Aftershocks

Experimental: See text

Fracture Dynamics: See Lecture III

T. Yamashita, J. Phys. Earth, 28 (1980) 309

T. Yamashita, J. Phys. Earth, 29 (1981) 283

Y. T. Chen and L. Knopoff: 1. Static shear crack with a zone of slip weakening.

2. Quasistatic extension of a shear crack with
a zone of slip-weakening in a viscoelastic medium.

3. Simulation of earthquake sequences.

All three of these are "in preparation"