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SECOND SUMMER COLLEGE IN BIOPHYSICS

30 July - 7 September 1984

Dynamics of Conformational Fluctuations in DNA from Hydrogen Exchange Rate Measurements.

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## LECTURE 1.

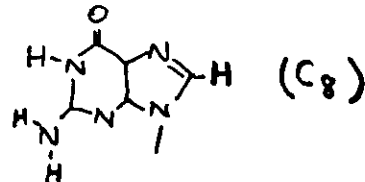
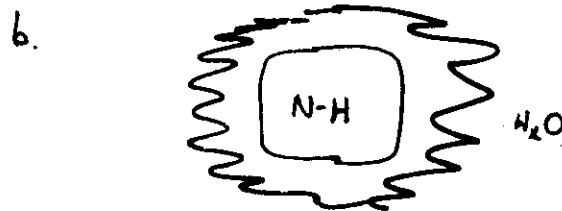
## INTRODUCTION TO EXCHANGE: CHEMICAL ASPECTS

A. GENERAL BACKGROUND.1. DNA IS A FLEXIBLE MOLECULE. Some indications:a. NMR relaxation of  $^1\text{H}$   $^{13}\text{C}$   $^3\text{P}$  indicates rapid motions (nsec) in backbone + bases.b. Time resolved decay of fluorescence anisotropy of bound dyes (ethidium) or spinlabelled molecules points to nsec relaxation processesc. Hydrodynamics: flexing in torsion / bending exists.

2. DYNAMICS MAY MEDIATE ACCESS TO H-BONDS IN INTERIOR OF DNA AND RNA.

a. RNA polymerases act as melting protein in forming open complex (initiation of transcription).b. Nucleases may require opening of duplex to cut.c. Opening reactions can mediate drug binding in principle.

②

B. EXCHANGE REACTIONS. MONITOR ACCESSIBILITY OF INTERIOR DOMAIN IN PROTEINS + NUCLEIC ACIDS, TO SOLVENT OR IONS.1. N-H and O-H protons occur frequently in biopolymers; they can exchange with solvent protons in general.a. Peptide bonds: 
$$-\text{C}(=\text{O})-\text{N}-$$
b. Nucleobases:  (C8) \* Some C-H are exchanged [Varshavsky, Schimmel]2. AS index of interior vs. exterior, exchange reactions are least perturbative chemically.a. Thus,  $\text{N-H} \leftrightarrow \text{N-D}$  is minimal substitution  
 $\text{N}^3\text{-H}$ Native structure generally retards exchange reactions

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3. In nucleic acids exchange reactions detect an "open state" with novel properties.

a. Exchange in principle can occur via direct penetration of interior by solvent.

b. Alternatively, exchange requires opening = breakage of H-bonds.

c. In the last case, the state that is responsible for exchange is not necessarily denatured.



Native (Intermediates) Denatured

d. Exploring these issues requires rate measurements at different I, pH, .... in order to provide a means of distinguishing cases. This is not easy or straightforward!

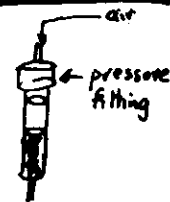
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C. RATES OF HYDROGEN EXCHANGE ARE MEASURED BY ISOTOPIC SUBSTITUTION OR DIRECTLY IN NMR

1.  $BH-H$  EXCHANGE BY GEL EXCLUSION OR ABSORPTION CHROMATOGRAPHY.

- a. Principle:
- (1) Molecule is equilibrated in  $^3H_2O$  labelled  $H_2O$  (radioactive!)
  - (2) At time  $t=0$ , labelled molecule is separated from solvent.
  - (3) At time  $t (> 10^4)$ , macromolecule ~~is~~ separated from solvent is counted ( $\rightarrow$  CPM) and Concentration determined (e.g. IR,  $A_{260}$ , P, N)
  - (4) Profile of H / molecule (or base pair, etc) is constructed from doing this at many times  $t$ .
- Each time point  $\leftarrow$  one column run!

b. Gel exclusion:



Gel sieves macromolecules from solvent

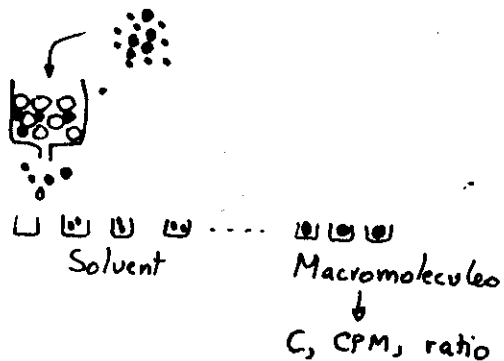
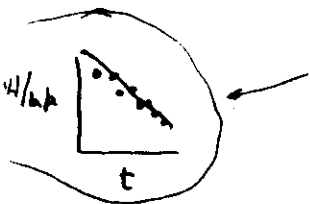


Macro molecule fractions

Solvent fractions

$C$ , CPM, ratio

### c. Absorption



### d. Drawbacks

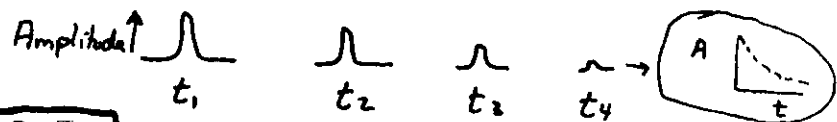
Slow  $> 10^4$  sec.

Tedious

Not selective unless coupled with mass spectroscopy

## 2. $^2\text{H}$ - $^1\text{H}$ EXCHANGE BY STOPPED FLOW OR DIRECT MEASUREMENT OF $[^2\text{H}]$ as $f(t)$ .

a. **Slow exchange**:  $t=0$  dissolve or dilute sample in  $\text{H}_2\text{O}$  ( $\text{D}_2\text{O}$ ) detect a proton say:



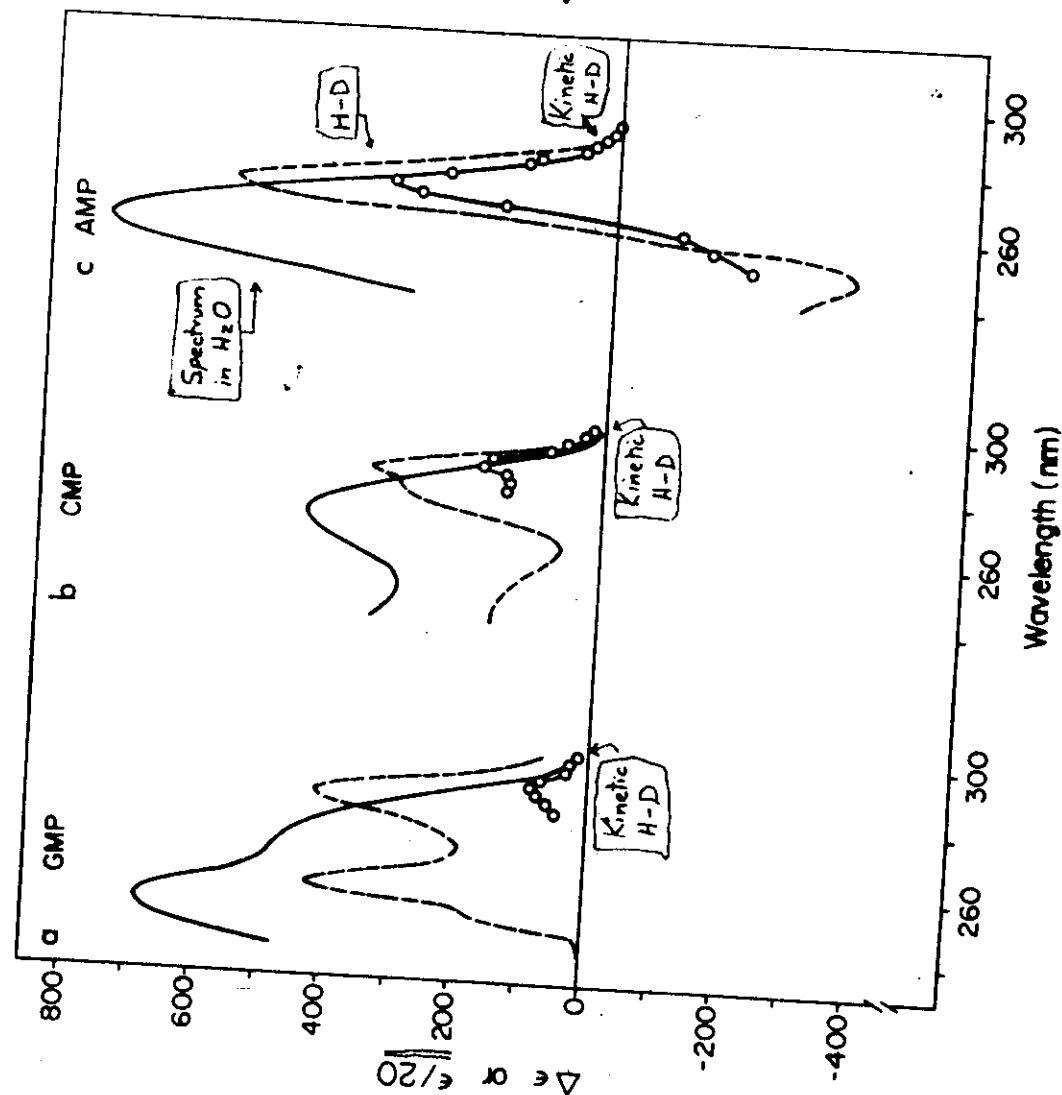
**Signal** can be  $^1\text{H}$  resonance, ( $^{15}\text{N}$ ), IR or Raman band.

This is the basis for HX work in most proteins (BPTI)

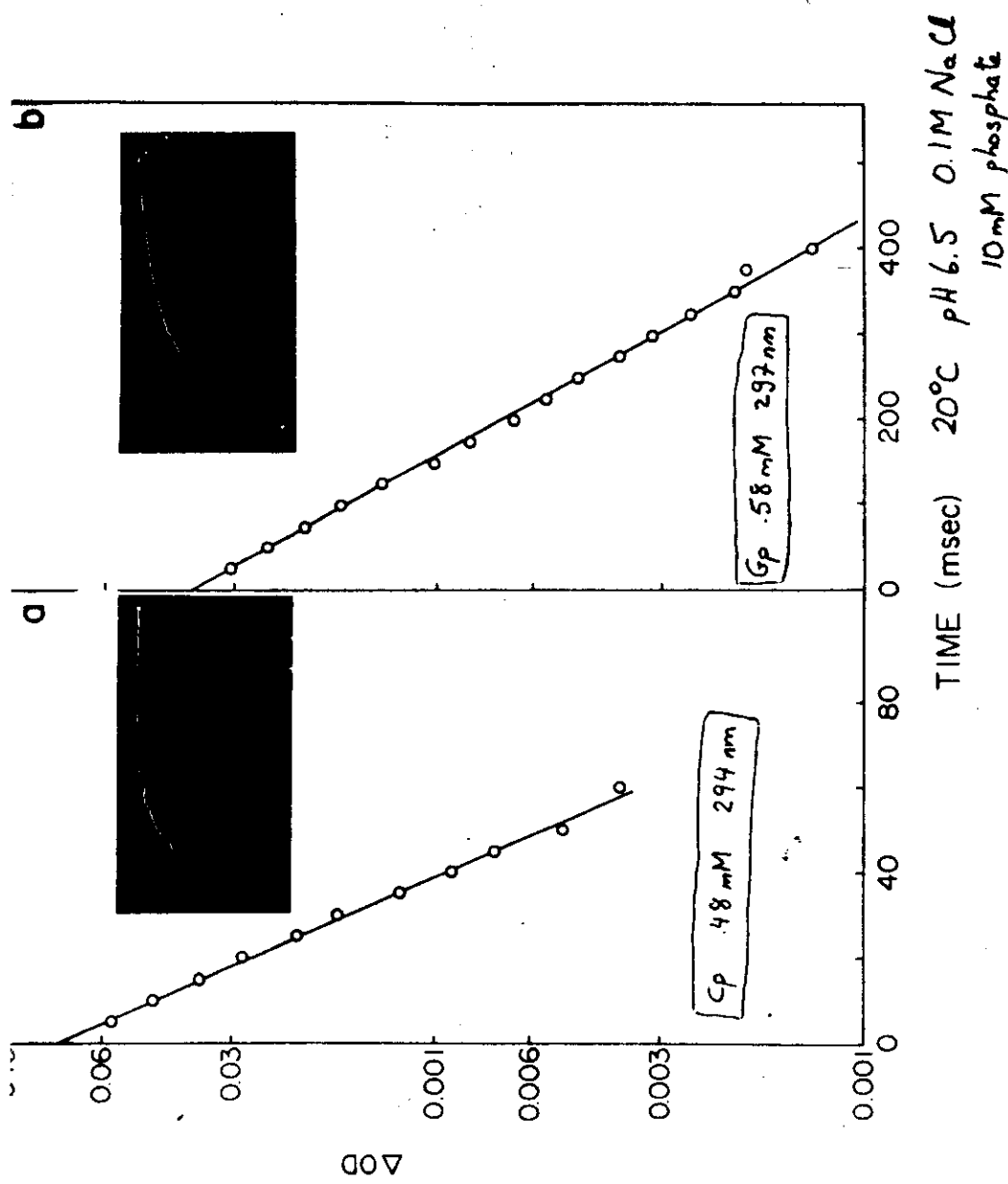
b. **Bases** exchange too fast generally (not proteins!)

Absorbance or fluorescence of a chromophore often depends on H vs. D substitution. Zero point vibrational  $\Delta E \rightarrow$  difference in electronic signal.

D. Cross (1975) reported this for adenine derivatives



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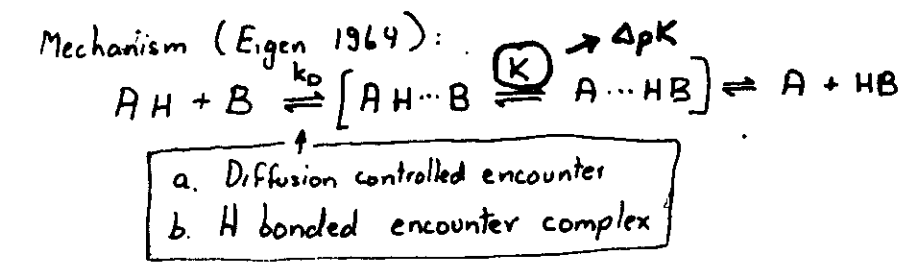
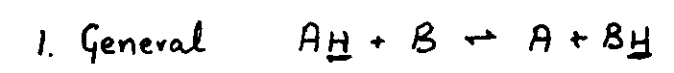


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2c.  $^1\text{H} - ^1\text{H}$  rates can be measured in NMR. Oligonucleotides  

 See Hilbert's Lecture

# D. PROTON TRANSFERS IN FREE BASES.



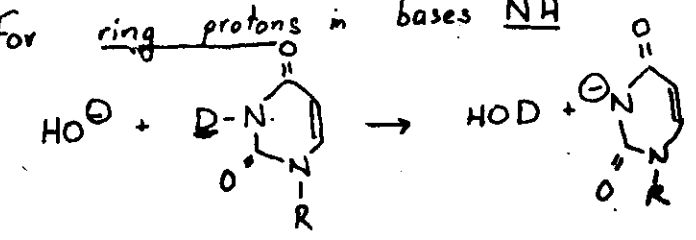
Rapid equilibrium in complex is controlled by  $K = 10^{\Delta pK}$   $\Delta pK = pK_{\text{acc}} - pK_{\text{donor}}$

So if B is stronger base, every collision succeeds, rates approach  $k_d$  ( $\sim 10^{10} \text{ M}^{-1} \text{ s}^{-1}$ )

If not, only a fraction of encounters succeed because equilibrium in complex lies to left.

$$k_{\text{ex}} = \frac{k_d [\text{B}] K}{1 + K} ; K = 10^{\Delta pK}$$

2. For ring protons in bases NH



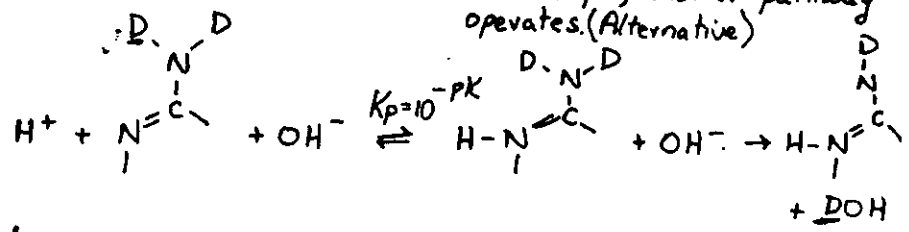
$$\Delta pK = pK_{OH^-} - pK_{ring\ NH}$$

$$\sim 15.7 - (9.5/10) \gg 0$$

∴ Diffusion controlled.

3.  $NH_2$  protons more complex because  $pK$  is very high ( $\sim 19$ ).  
 $K \sim 10^{-3}$

At high pH, this still works.  
 At low pH, another pathway operates. (Alternative)



In addition, direct catalysis by  $H_2O$  itself can operate, as a third alternative.

At any pH

$$\therefore k_{ex} = I + II + III$$

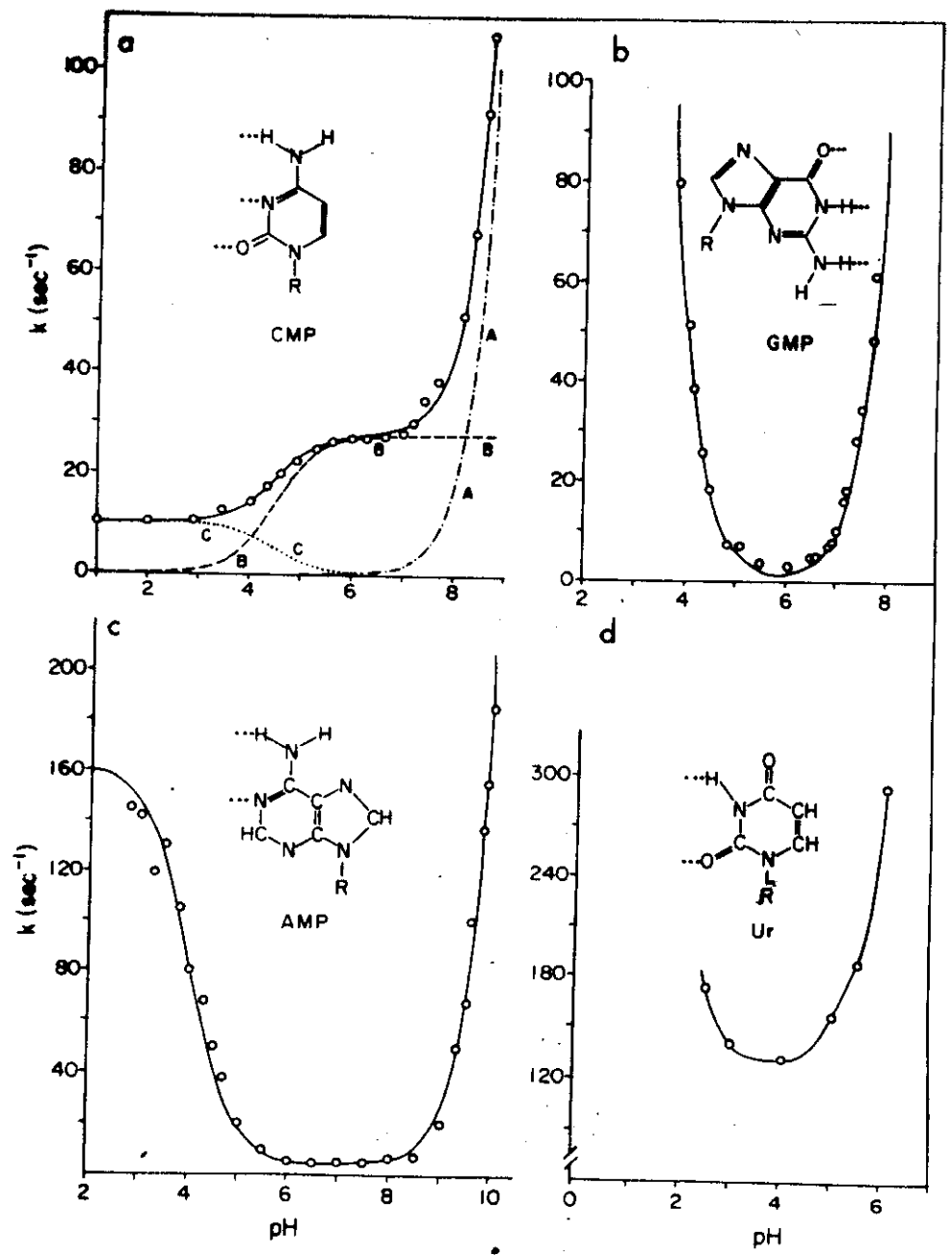
$$k_I = \frac{k_{unprot.} (OH^-) K}{1 + K}$$

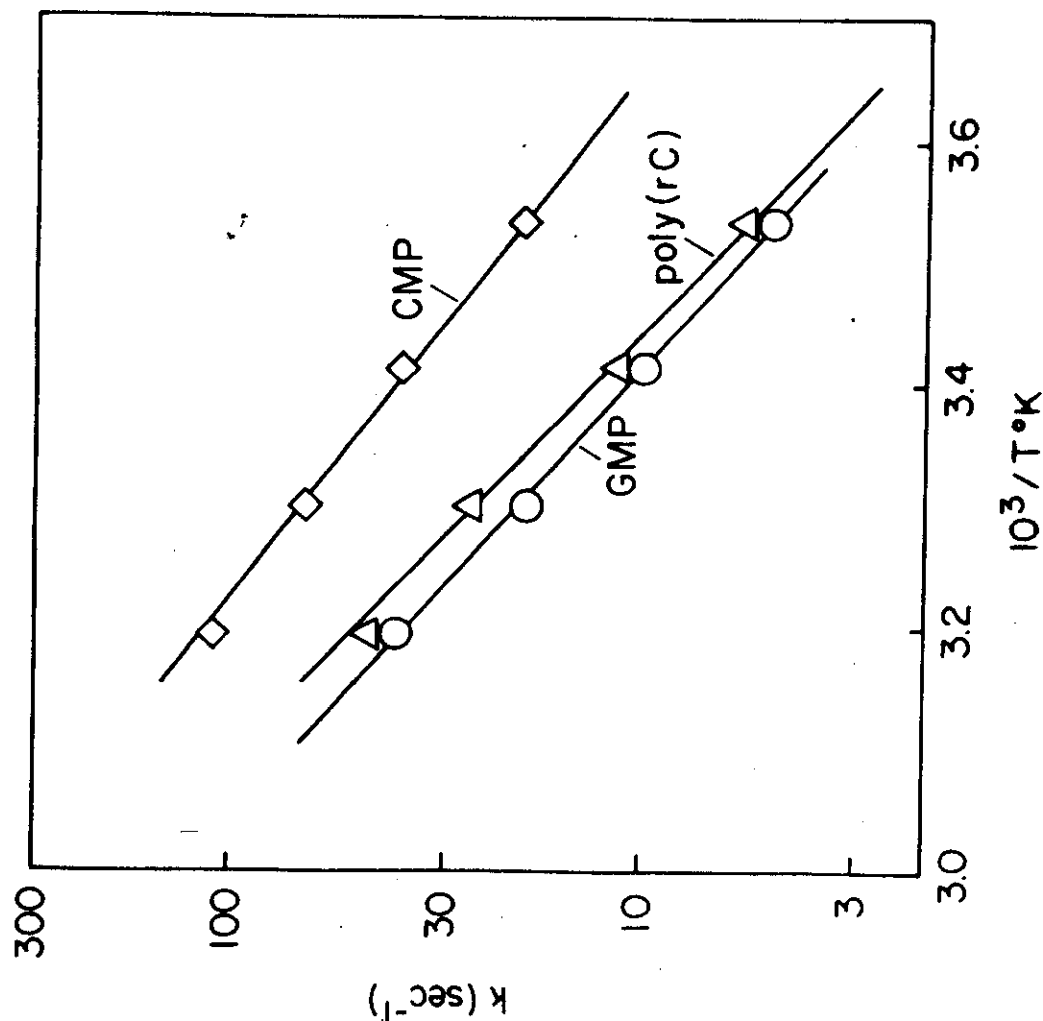
$$k_{III} = k^{H_2O} (H_2O) \cdot \frac{(H^+) K_p}{1 + (H^+) K_p}$$

$$k_{II} = \frac{k^{prot} (OH^-) (H^+) K_p}{1 + (H^+) K_p}$$

Data at different pH (next page) give:

	$pK_a$	$k_{OH}^{unp.}$	$k_{OH}^{prot}$	$k_{H_2O}^{prot} \{ M^{-1} s^{-1} \}$
$C_p$	4.5	$1.6 \cdot 10^7$	$8.8 \cdot 10^{10}$	.2
$G_p$	2.4	$9 \cdot 10^7$	-	40
$A_p$	4.0	$9 \cdot 10^7$	$19.8 \cdot 10^{10}$	3





#### 4. OTHER BASES THAN $\text{OH}^-$ ?

a. Ring protons sensitive to concentration of base added (imidazole Tris etc). Effect  $\propto pK$ .

b. Amino protons respond to concentration of catalyst acid form:

$$k_{ex} = k_{base} (\text{Base}) \frac{(\text{H}^+) K_p}{1 + (\text{H}^+) K_p}$$

small

Above pH 5:

$$\approx k_{base} (\text{Base}) (\text{H}^+) K_p$$

$(\text{BH}^+) K_a$

$$k_{ex} = k_{base} K_p K_a [\text{BH}^+]$$

$$= (\text{constant}) =$$

E. Examples of exchange data from nucleic acid polymers: DNA, tRNA, rA-rU, rI-rC. (Data from  $^2\text{H}$ - $^1\text{H}$  column method)  $0^\circ\text{C}$ . slow reaction.

1. DNA: several rates
2. tRNA: folding in  $\text{Mg}^{2+}$  produces new H-bonds.  
NMR: ring N-H downfield / amino's nearer  $\text{H}_2\text{O}$ , aromatic.  
 $\therefore$  Harder to resolve.
3. rA-rU: Detect only 2 H/b.p. Originally these
4. rI-rC: were assigned as Watson-Crick H-bonds  
protons; but they turn out to be the A-NH.
5. dG-dC: All 5 N-H show up at  $0^\circ\text{C}$ .

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Some Points:

1. G-C  $\rightarrow$  5H/b.p. at  $t=0$ , extrapolated
2. A-U  $\rightarrow$  2H/b.p. but rAU gives 3.

$$\therefore \text{DNA (50\% GC)} \rightarrow \frac{1}{2}(5+3) = \boxed{4}$$

3. Cloverleaf structure in tRNA alone  $\rightarrow \boxed{100}$  (fmet)

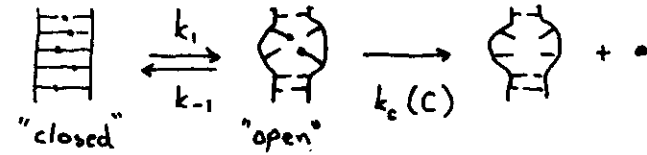
More protons than this / molecule occur.  
Recently applied to SS, other species.

4. Note that exchange rate is a property characteristic of a polynucleotide. rG:rC exchanges slowly compared to dG:dC, for example.

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## F STRUCTURALLY LIMITED EXCHANGE.

Consider the model in which H-bond breakage necessarily precedes exchange.



$$k_{ex} = k_c(c) (\text{open})$$

$$\frac{d}{dt} (\text{open}) = k_1(\text{closed}) - k_{-1}(\text{open}) - k_c(c)(\text{open})$$

Steady state:  $(\text{open}) = \frac{k_1}{k_{-1} + k_c(c)}$

$$\boxed{k_{ex} = \frac{k_1 k_c(c)}{k_{-1} + k_c(c)}}$$

← Similar to Michaelis-Menten eqn.

Simple limiting cases:

(I)  $k_c(c) \gg k_{-1}$  : transfer rate higher than structural closing

$$\boxed{k_{ex} = k_1}$$

(II)  $k_c(c) \ll k_{-1}$  open/close repeatedly before exchange

$$k_{ex} = \frac{k_1}{k_{-1}} \cdot k_c(c) = \boxed{K_{eq} k_c(c)}$$

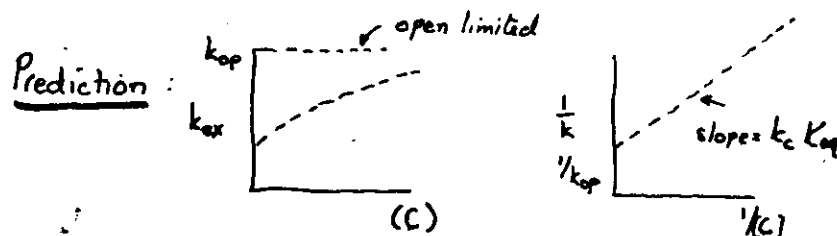
opening equilibrium constant



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Note Reciprocal Plot (Lineweaver):

$$\frac{1}{k_{ex}} = \frac{1}{k_{op}} + \frac{1}{k_c K_{eq}} \left( \frac{1}{C} \right)$$



## 6. CASE OF POLY(A). POLY(U)

Ref: C. Mandal et al.  
J. Mol. Biology  
135 391 (1979)

1. CHEMISTRY 3H / b.p. :  $U N_3 H$   
 $A N H_2$

Expect : $6 < pH < 8$	Rate	Response to base catalyst Tris, e.g.
$U N_3 H$	Fast	$\propto (B)$
$A N H_2$	Slow	$\propto (BH^+)$

2. OBSERVE Two rates : Fast; Slow

Fast : no response to base  
Slow : responds to base,  $\propto (BH^+)$ !

Detailed catalysis slows slow  $\rightarrow$  fast with catalysis.

Conclude:

$U N_3 H$  (?)  
 $A N H$

Comparison numbers:

$rA \cdot rU$ end base unpair	+1.1	+7.1	+20	calorimetry
$rA \cdot rU$ , int base loopout	+1.5-4	+6-9	+13-17	(Fink + Crothers 1976) (Lomant + Fresco 1975)

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3. WHAT IS OPENING PROCESS?

a. Fluctuation must break H-bond for  $A N H_2$  in W.C. pair, otherwise no encounter complex can form.

b. Same step seems to allow  $U N H$  to exchange; its chemistry is faster — hence it appears open-limited.

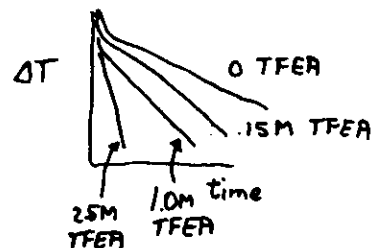
c. Under maximum catalysis  $A N H_2$  (both) accelerate only to F rate, not faster.

d. Open state can be defined energetically, as well as kinetically.  
 $\Delta H_F^+ = +15 \text{ kcal/mole}$  (mole opening).  
 $\Delta H_S^+ = +17.6 \text{ kcal/mole}$   
( $\Delta H_{AMP}^+ = 12$ ;  $\Delta H_{PA}^+ = 14$ ).

e. Calculation of  $K_{eq}$  from reciprocal plot yields  $K = .05$  (polyA ref) at 20°C.

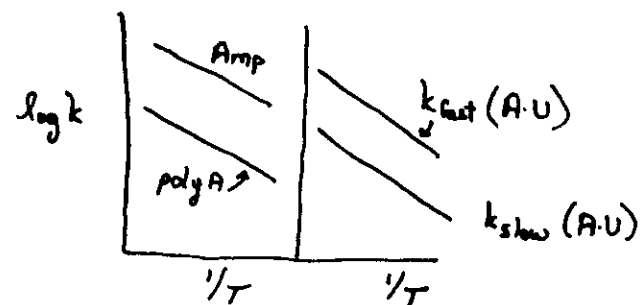
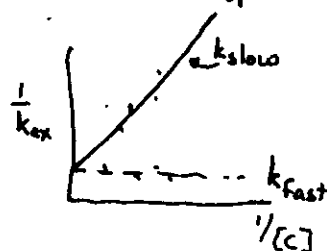
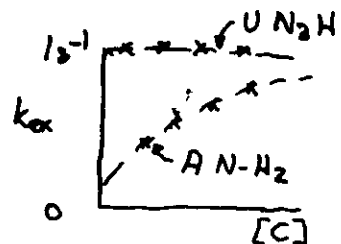
	$\Delta G_{25}^\circ$	$\Delta H_{25}^\circ$	$\Delta S^\circ \text{ e.u.}$	
$rA \cdot rU$	+1.8	+4	7	polyA
	+2.4	+6	12	Amp

# Data on poly(rA) poly(rU)



Catalysis of exchange in poly(rA)  
poly(rU) by trifluoroethylamine  
pH 6.2 20°C 1M NaCl.

Rates obey reciprocal eqn. for  
open limited process:



N.B. ALL rates are insensitive to salt (0.01-1M).

TABLE I

Kinetic and Thermodynamic Parameters of Hydrogen Exchange and Base Pair  
Opening<sup>a</sup>

Property	poly (rA):poly (rU)	poly (rI):poly (rC)
$k_{ex}$ (fast phase), $\text{sec}^{-1}$ at 20 C	1.1	12
$k_{ex}$ (slow phase), $\text{sec}^{-1}$ at 20 C	0.14	0.13
<u>Polynucleotide standard</u>		
$K_{op}$ at 20°C	0.05	0.01
$\Delta H^\circ$ , kcal/mole	3.8	3.7
$\Delta S^\circ$ , cal/mole-°K	6.7	3.3
$T_m$ , °C	290	840
<u>Mononucleotide standard</u>		
$K_{op}$ at 20°C	0.02	0.004
$\Delta H^\circ$ , kcal/mole	6.1	6.3
$\Delta S^\circ$ , cal/mole-°K	12	2.5
$T_m$ , °C	240	360

<sup>a</sup>Kinetic measurements were performed in 100mM NaCl, 10mM  $\text{NaH}_2\text{PO}_4$ , pH 7.0.

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H. Does the HX open state relate to equilibrium premelting?

Small extent of change may be detectable spectroscopically. Obvious approach:

follow T dependence of A260 CD Raman or IR bands, verify if same  $\Delta H^\circ$  as HX open state.

1. Two state analysis for  $\Delta H^\circ$ :



At temp T

$$\ln K_{eq} = \ln \frac{(\alpha_A - \alpha)}{(\alpha - \alpha_B)}$$

$$= \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{RT}$$

$\alpha$  = any parameter sensitive to A/B diff.

$\alpha_A$  = value of  $\alpha$  for 100% A state

$\alpha_B$  = " " " " " B state

$$\ln \left( \frac{\alpha_A - \alpha_i}{\alpha_i - \alpha_B} \right) = \frac{\Delta H^\circ}{R} \left( \frac{1}{T_m} - \frac{1}{T_i} \right) \quad i=1, \dots, N_{obs}$$

Strategy

Trial  $\Delta H^\circ$   $T_m$

↓

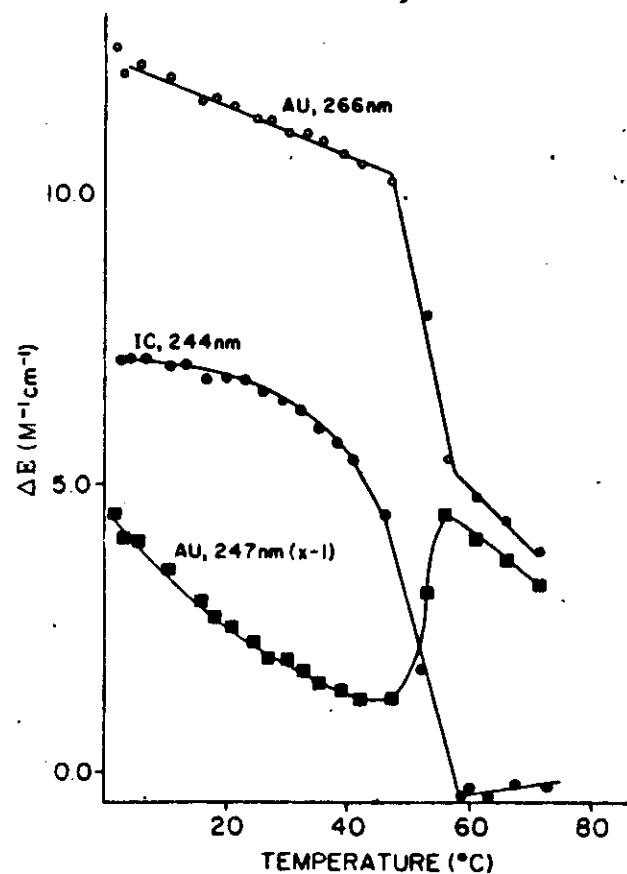
Calculate  $\alpha_A$   $\alpha_B$  K

↓

$$\text{minimize } S = \sum_i (\alpha_i^{calc} - \alpha_i)$$

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Preisler Fig. 10.



Preisler Fig. 12

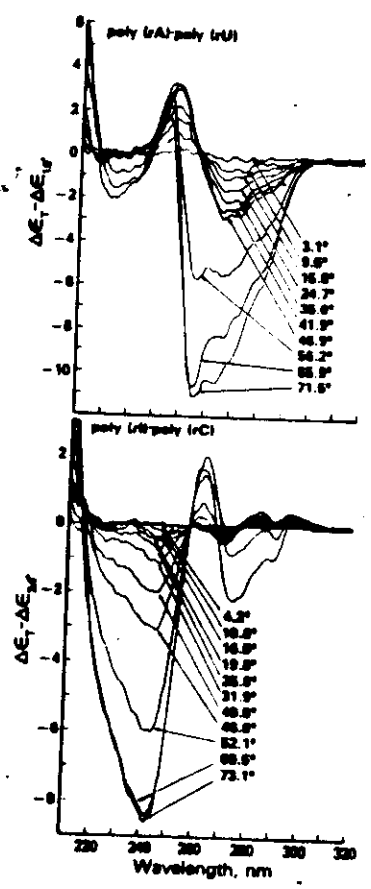


TABLE V  
Calculated Enthalpies of Premelting Transitions

Technique	Number of Data Sets	H <sup>c</sup> , kcal/mole
poly (rA) : poly (rU)		
HX	1	3.8 <sup>a</sup> 6.1 <sup>b</sup> 5.5 <sup>c</sup>
IR	5	16 25 22 17 9.4 (Average) 18 ± 5.4
CD	2	9.4 6.3 (Average) 7.9
poly (rI) : poly (rC)		
HX	1	3.7 <sup>a</sup> 6.3 <sup>a</sup> 4.3 <sup>c</sup>
IR	5	39 14 8.9 17 7.0 (Average) 17 ± 11
CD	2	14 14 (Average) 14

<sup>a</sup>From van't Hoff plot based on equation (1); polynucleotide standard.  
<sup>b</sup>From van't Hoff plot based on equation (1); mononucleotide standard.  
<sup>c</sup>From program 1; polynucleotide standard.