

AUTUMN COLLEGE ON PLASMA PHYSICS

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Absorption Physics of High-Frequency Fast Magnetosonic Waves

J. MENARD

Princeton University
Plasma Physics Laboratory
Princeton, U.S.A.

These are preliminary lecture notes, intended only for distribution to participants.

Absorption Physics of High-Frequency Fast Magnetosonic Waves

Presented by J. Menard

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ICTP

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Fast Wave Review (cold plasma)

Assume $\mathbf{E} = \mathbf{E}_0 e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)}$, define $\mathbf{n} = c\mathbf{k}/\omega$, \Rightarrow wave eqn. is $\mathbf{n} \times \mathbf{n} \times \mathbf{E} + \mathbf{K} \cdot \mathbf{E} = 0$

$$\mathbf{K} = 1 + \Sigma \chi_s \quad \chi_s = i\sigma_s / \omega \epsilon_0 \quad \mathbf{J}_s = \sigma_s \cdot \mathbf{E}$$

where σ_s is determined from the linearized equations of motion in a strong magnetic field B_z

$$\mathbf{K} = \begin{bmatrix} S & iD & 0 \\ -iD & S & 0 \\ 0 & 0 & P \end{bmatrix} \quad \begin{array}{l} S: \text{ Vacuum } + \perp \text{ polarization current} \\ D: \mathbf{E} \times \mathbf{B} \text{ drift induced current} \\ P: \text{ Vacuum } + \parallel \text{ polarization current} \end{array}$$

$$\text{Solve for } n_{\perp}^2 = n_{\perp}^2(n_{\parallel}, \mathbf{r}) \Rightarrow n_{\perp}^2 = \frac{(n_{\parallel}^2 - R)(n_{\parallel}^2 - L)}{(S - n_{\parallel}^2)} \quad L, S < 0 \text{ near edge} \Rightarrow$$

$$S = (R + L)/2 \quad D = (R - L)/2$$

$$\text{wave is evanescent until } R > n_{\parallel}^2, \text{ then } \omega^2 \approx k_{\perp}^2 v_A^2 (1 + c^2 k_{\parallel}^2 / \omega_{pi}^2)$$

$$v_A \approx c \Omega_i / \omega_{pi}$$

Motivation for Studying High-Frequency (High-Harmonic) Fast Waves

- Fast waves with frequencies near the ion cyclotron fundamental are routinely used to resonantly heat ions in present fusion experiments.
- Auxiliary current drive and current profile control are important for improving several fusion concepts (Tokamak, ST, RFP)
 - Fast waves well above the cyclotron fundamental can:
 - preferentially heat electrons
 - drive toroidal current
- In particular, next-generation spherical tokamaks will require strong auxiliary heating and current drive to test stability limits and confinement trends
- Wave inverse damping length $1/L_{\text{damp}} \propto \beta_e / v_A \propto \boxed{(\omega_{pe}/\Omega_e)^3 T_e}$ for fixed $\omega/k_{\parallel} v_{Te}$
 - Standard tokamaks have $\omega_{pe}/\Omega_e \approx 1$
 - Spherical tokamaks have $\omega_{pe}/\Omega_e > 5 \Rightarrow$ very strong damping, off-axis CD
- High-harmonic $\Rightarrow \omega = 15\text{-}30 \times \Omega_{ci}$
 - Weaker ion damping per ion-cyclotron harmonic resonance
 - Weaker IBW mode conversion per resonance
 - Natural fit to present low-field ST experiments (NSTX will use TFTR hardware)

Dielectric Tensor Elements

Working in the limit $\Omega_i < \omega \ll |\Omega_e|$ and neglecting ion and electron finite Larmor radius (FLR) effects, the lowest order dielectric tensor elements are:

$$K_{xxc} = 1 + \frac{\omega_{pe}^2}{\Omega_e^2} - \sum_i \frac{\omega_{pi}^2}{\omega^2 - \Omega_i^2} \quad (1)$$

$$K_{xyc} = -\frac{\omega_{pe}^2}{\Omega_e \omega} + \sum_i \frac{\Omega_i}{\omega} \frac{\omega_{pi}^2}{\omega^2 - \Omega_i^2} \quad (2)$$

$$K_{yyc} = K_{xxc} + n_\perp^2 \delta_m \quad (3)$$

$$K_{xzc} = -n_\perp n_\parallel \delta \quad (4)$$

$$K_{yz} = n_\perp \delta_X K_{zze} \quad (5)$$

$$K_{zz} \approx K_{zze} = -\frac{\omega_{pe}^2}{k_\parallel^2 V_{Te}^2} Z'_0\left(\frac{\omega}{k_\parallel V_{Te}}\right) \quad (6)$$

$$\delta_m = \frac{\omega_{pe}^2}{\Omega_e^2} \frac{V_{Te}^2}{c^2} \frac{\omega}{k_\parallel V_{Te}} Z_0\left(\frac{\omega}{k_\parallel V_{Te}}\right) \quad (7)$$

$$\delta = \sum_s \left(\frac{V_T}{c}\right)^2 \frac{\omega^2 \omega_p^2}{(\omega^2 - \Omega^2)^2} \quad (8)$$

$$\delta_X = \left(\frac{V_T}{c}\right)^2 \frac{\omega}{2\Omega_e} n_\parallel \quad (9)$$

Here δ_m is the magnetic pumping (MP) term, δ is small, δ_x represents the cross (X) terms from K_{yz} and K_{zy} , K_{zze} gives the electron Landau damping (ELD), and “c” and “e” indicate cold and (thermal) electron, respectively. Cyclotron frequencies carry the sign of the particle species charge.

Wave Dispersion Relation

The dispersion relation is obtained from the determinant equation:

$$\det \begin{bmatrix} K_{xxc} - n_{\parallel}^2 & -iK_{xyc} & n_{\perp}n_{\parallel}(1 - \delta) \\ iK_{xyc} & K_{xxc} - n_{\parallel}^2 - n_{\perp}^2(1 - \delta_m) & in_{\perp}\delta_x K_{zze} \\ n_{\perp}n_{\parallel}(1 - \delta) & -in_{\perp}\delta_x K_{zze} & K_{zz} - n_{\perp}^2 \end{bmatrix} = 0 \quad (10)$$

The resulting dispersion relation, $g=0$, is quadratic in n_{\perp}^2 :

$$g(n_{\perp r}, n_{\perp i}, n_{\parallel r}) \equiv an_{\perp}^4 + bn_{\perp}^2 + c = 0 \quad (11)$$

The coefficients in the quadratic equation are:

$$a = [\eta - n_{\parallel}^2(1 - \delta)^2](1 - \delta_m) \quad (12)$$

$$b = -K_{xyc}^2 - 2K_{xyc}n_{\parallel}\delta_x(1 - \delta)K_{zze} + \eta^2 - \eta[n_{\parallel}^2(1 - \delta)^2 + K_{zze}(1 - \delta_m) + \delta_x^2 K_{zze}^2] \quad (13)$$

$$c = [K_{xyc}^2 - \eta^2]K_{zze} \quad (14)$$

$$\eta = n_{\parallel}^2 - K_{xxc} \quad (15)$$

Treatment of Complex Roots

Keeping g stationary along the power flow (ray) trajectory \Rightarrow

$$\frac{d\vec{r}}{dt} = -\frac{\partial g / \partial \vec{k}}{\partial g / \partial \omega} \quad \frac{d\vec{k}}{dt} = +\frac{\partial g / \partial \vec{r}}{\partial g / \partial \omega} \quad \frac{d\omega}{dt} = -\frac{\partial g / \partial t}{\partial g / \partial \omega}$$

Problem: Power flow velocity (usually taken to be $d\vec{r}/dt$) should be real-valued, but g is generally complex when damping is strong.

Partial solution: expand k_{\perp} about $k_{\perp r}$ to derive real-valued dispersion relation:

$$G(\vec{r}, t, k_{\perp r}, k_{\parallel}, \omega) = g_r + g_i \frac{\partial g_i / \partial k_{\perp r}}{\partial g_r / \partial k_{\perp r}} = 0$$

Interestingly, finding the root of this dispersion relation is equivalent to minimizing the modulus of g , i.e solving $\frac{\partial}{\partial k_{\perp r}} |g(\vec{r}, t, k_{\perp r}, k_{\parallel})|^2 = 0$.

This methodology also yields the imaginary part of $k_{\perp} = k_{\perp i} = \frac{-g_i}{\partial g_r / \partial k_{\perp r}}$

Ray Tracing Equations

The ray-tracing equations in cylindrical coordinates become:

$$\begin{aligned}\frac{1}{c} \frac{dR}{dt} &= \left[\frac{v_{g\perp}}{c} \left(\frac{k_R - k_{\parallel} \frac{B_R}{B}}{k_{\perp r}} \right) + \frac{v_{g\parallel}}{c} \frac{B_R}{B} \right] \\ \frac{1}{c} \frac{Rd\phi}{dt} &= \left[\frac{v_{g\perp}}{c} \left(\frac{k_{\phi} - k_{\parallel} \frac{B_{\phi}}{B}}{k_{\perp r}} \right) + \frac{v_{g\parallel}}{c} \frac{B_{\phi}}{B} \right] \\ \frac{1}{c} \frac{dZ}{dt} &= \left[\frac{v_{g\perp}}{c} \left(\frac{k_Z - k_{\parallel} \frac{B_Z}{B}}{k_{\perp r}} \right) + \frac{v_{g\parallel}}{c} \frac{B_Z}{B} \right]\end{aligned}$$

where

$$v_{g\perp} = -\frac{\partial G / \partial k_{\perp r}}{\partial G / \partial \omega} \quad v_{g\parallel} = -\frac{\partial G / \partial k_{\parallel}}{\partial G / \partial \omega} \quad k_{\phi} = \frac{n_{\phi}}{R}$$

Current drive efficiency η_{CD}

For good review, see J. Wright, Ph.D. Thesis, Princeton (1998)

$$\begin{aligned} \partial f_e / \partial t &= C_{\text{collision}}(f_e) + C_{\text{wave}}(f_e) = 0 \text{ in steady state } \Rightarrow \\ C_{\text{collision}}(f_e) &= -C_{\text{wave}}(f_e) = -\partial / \partial \mathbf{v} \cdot \mathbf{D}_{ql} \cdot \partial f_e / \partial \mathbf{v} = \partial / \partial \mathbf{v} \cdot \Gamma_{ql} \end{aligned}$$

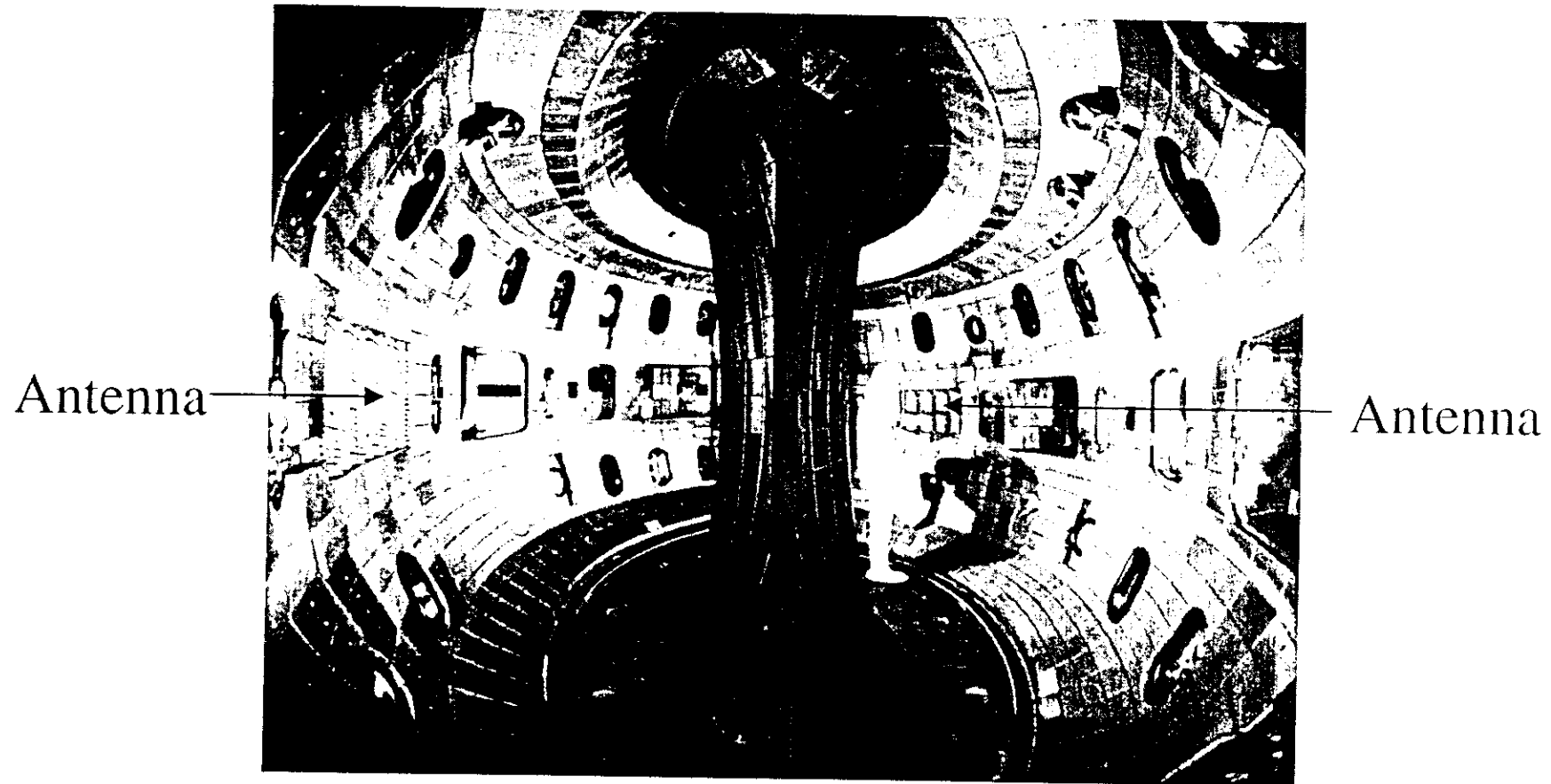
Linearize $C_{\text{collision}}$ and generate Green's function $g(\mathbf{v}, \mathbf{v}') \Rightarrow$
formal solution $f_e(\mathbf{v}) = \int d^3 \mathbf{v}' g(\mathbf{v}, \mathbf{v}') \partial / \partial \mathbf{v}' \cdot \Gamma_{ql}(\mathbf{v}')$

$$\begin{aligned} \chi &= \int d^3 \mathbf{v} q v_{\parallel} g(\mathbf{v}, \mathbf{v}') & \varepsilon &= \int d^3 \mathbf{v} m v^2 / 2 g(\mathbf{v}, \mathbf{v}') \\ J_{\parallel} &= \int d^3 \mathbf{v} q v_{\parallel} f_e & P &= \int d^3 \mathbf{v} m v^2 / 2 f_e \\ \eta_{CD} &= J_{\parallel} / P = \int d^3 \mathbf{v} \Gamma_{ql} \cdot \partial \chi / \partial \mathbf{v} / \int d^3 \mathbf{v} \Gamma_{ql} \cdot \partial \varepsilon / \partial \mathbf{v} \quad (\text{after } \int \text{ by parts}) \end{aligned}$$

$\mathbf{D}_{ql} = D_0 \delta(\omega - k_{\parallel} v_{\parallel}) \mathbf{e}_{\parallel} \mathbf{e}_{\parallel} (2 - x^2)^2 \quad x = v_{\perp} / (T_e / m_e)^{0.5}$ for near-Maxwellian
and Fast Wave dispersion relation (Ehst and Karney, Nucl. Fusion **31**, 1991)

$\eta_{FW} \propto T_e / (n_e \ln \Lambda) * f(Z_i, \varepsilon, \dots)$
where f is a function of ion charge, particle trapping, ...

Most high frequency fast wave experiments have been performed in DIII-D using frequencies $\omega_{\text{RF}}/\Omega_{\text{D}} \approx 4\text{-}7$



The following DIII-D data is reproduced from the review article:

Recent progress in ICRF physics, by M. Porkolab, et al.

Plasma Phys. Control. Fusion **40** (1998) A35-A52

Measured central driven current density
is generally in good agreement with theory

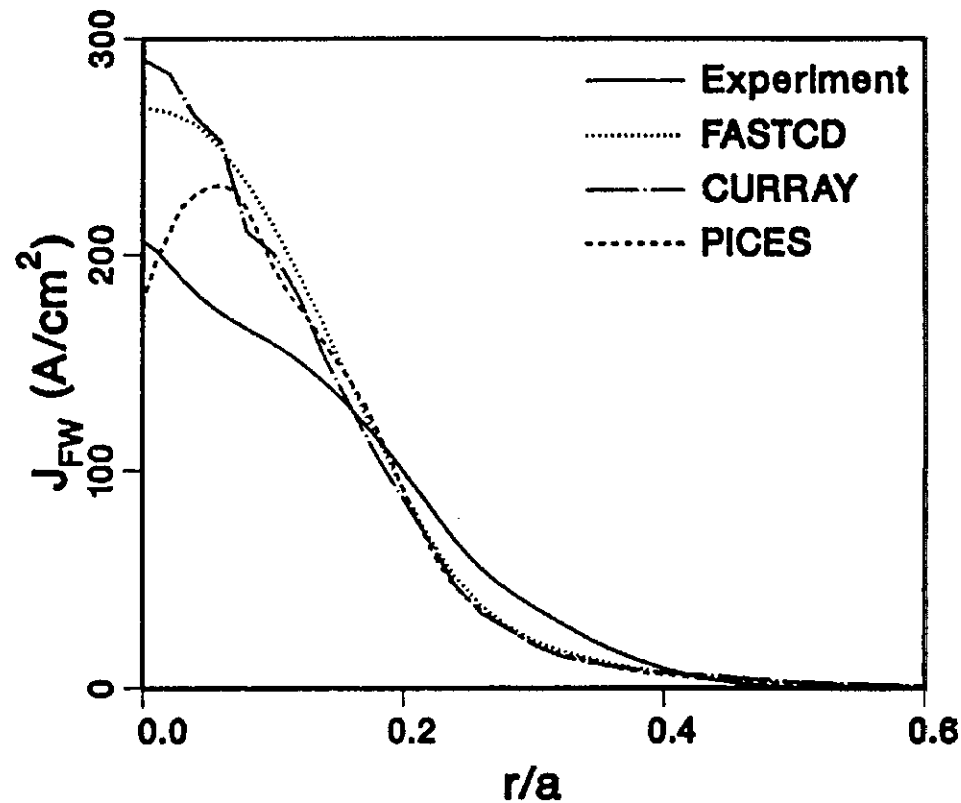


Figure 10. Radial profile of the non-inductive current density driven by FWs in DIII-D together with theoretical profiles ($B_r = 2.1$ T, $\bar{n} = 2.1 \times 10^{19} \text{ m}^{-3}$, $P_{fw} = 2.1$ MW).

Current drive efficiency scales linearly with T_e

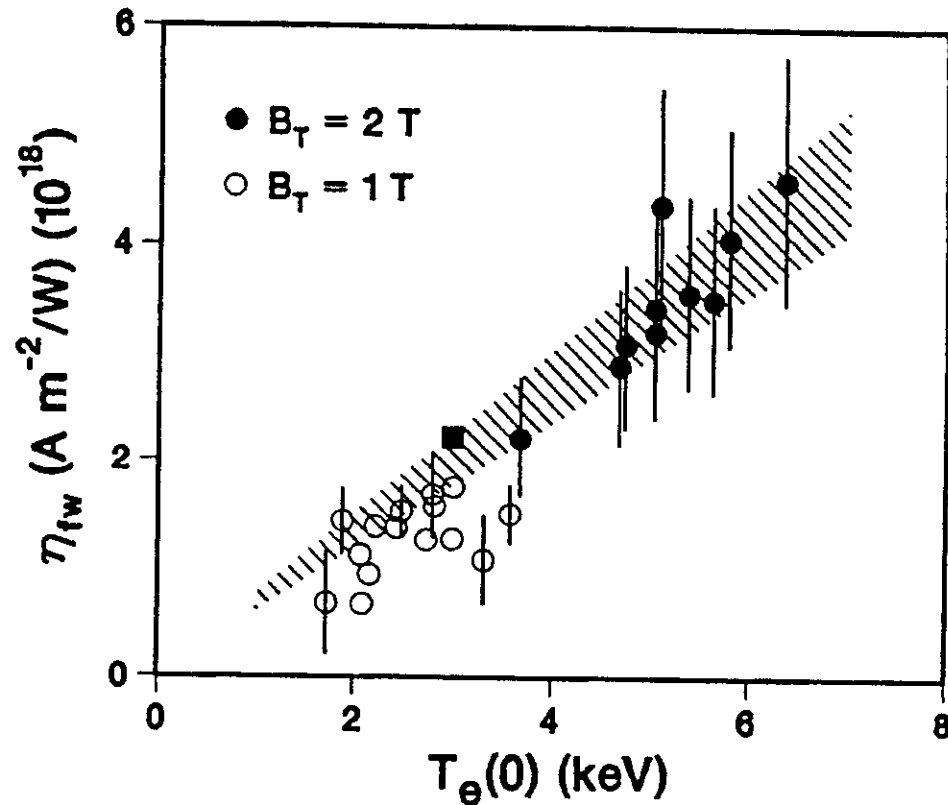


Figure 11. Experimental FWCD efficiency as a function of central electron temperature in DIII-D. The shaded band indicates the predictions from the CURRAY ray tracing code. The solid square represents data from Tore Supra [28].

Fast ion stored energy increases near resonances

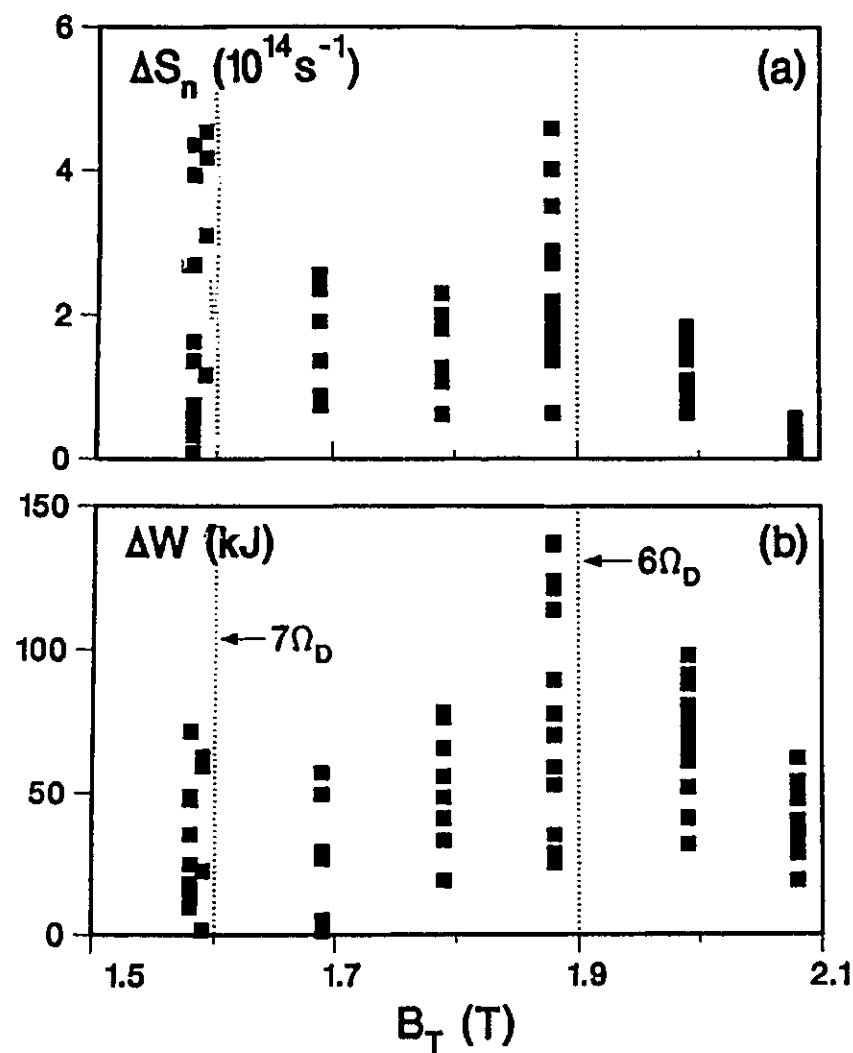


Figure 12. Toroidal magnetic field dependence of the (a) anomalous neutron rate and (b) anomalous fast-ion stored energy ($P_{NI} \approx 3.7$ MW, $P_{fw} \approx 2.3$ MW).

Ion absorption can significantly
reduce effective current drive efficiency

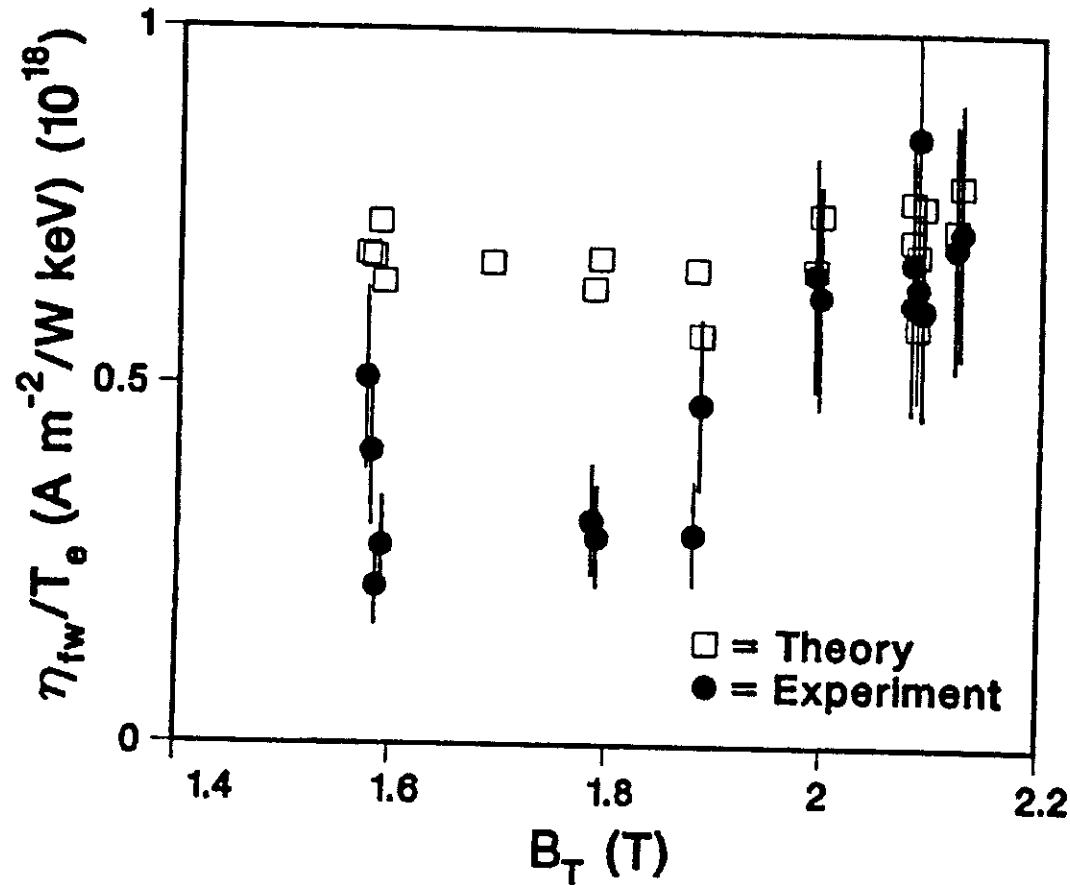


Figure 13. Toroidal magnetic field dependence of the FWCD efficiency normalized to the central electron temperature.

High edge density (H-mode) can lead to anomalous edge wave absorption \Rightarrow reduced FWCD

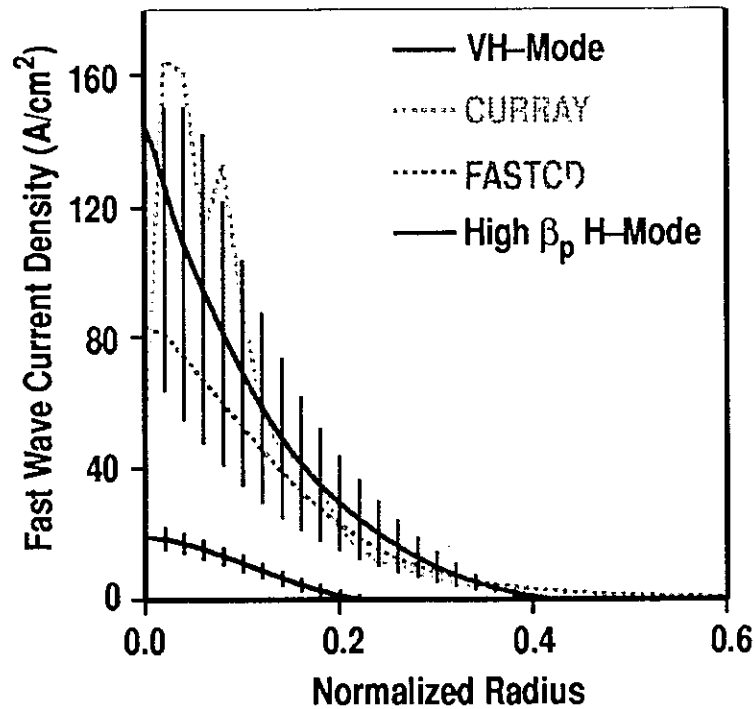


Fig. 1. Radial profile of experimental and theoretical FWCD.

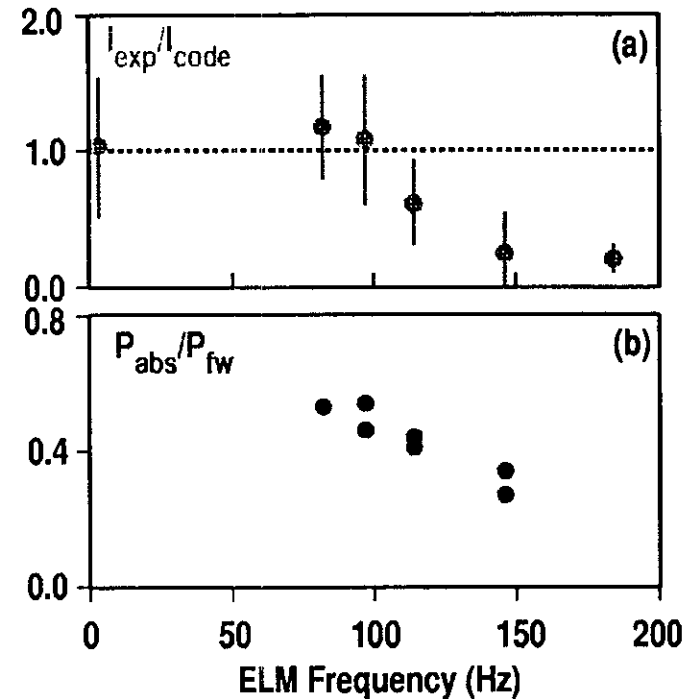


Fig. 2. Dependence on ELM frequency of (a) experimental FWCD, normalized to the theoretical value, and (b) fraction of FWCD power absorbed by electrons.

Data reproduced from:

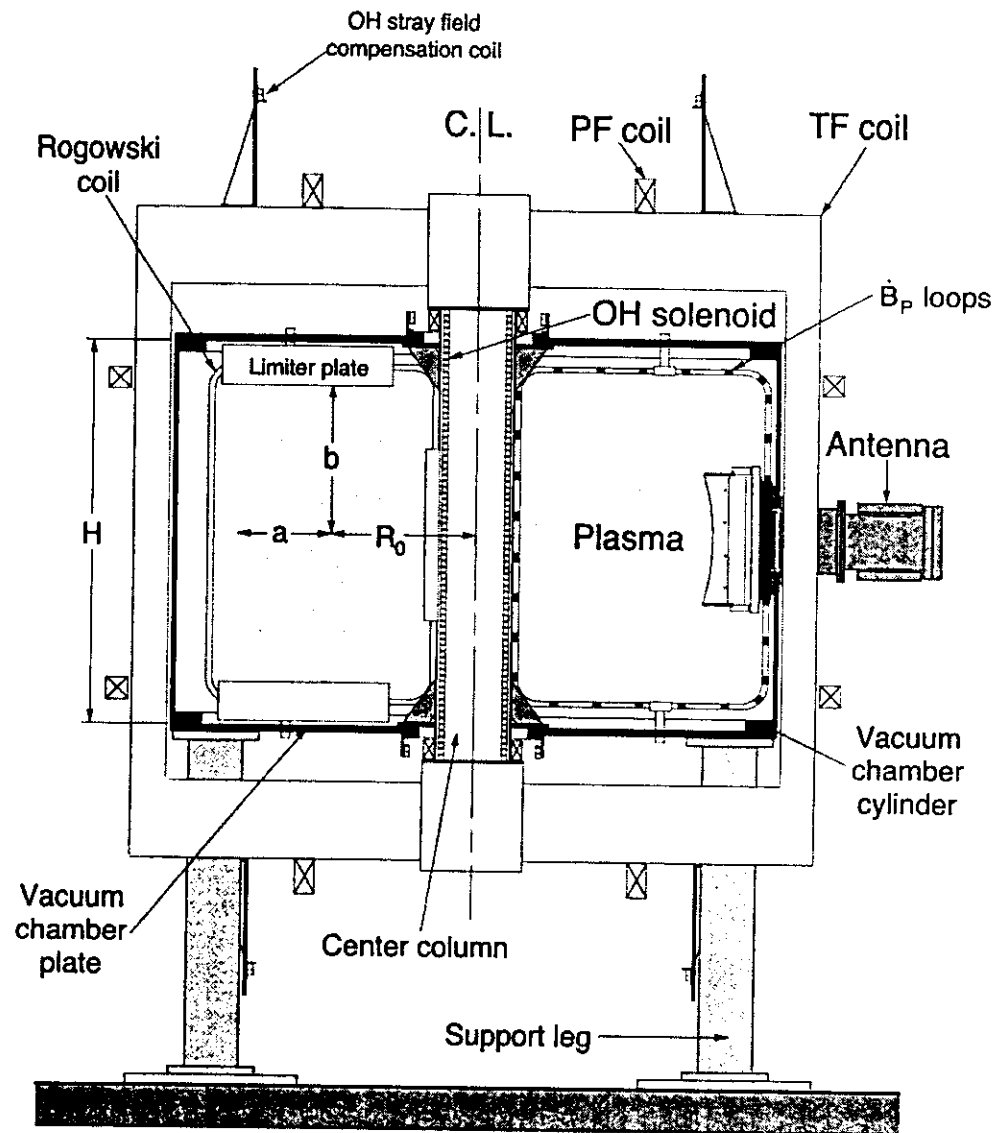
DIII-D TECHNICAL BULLETIN

Number 6 June 10, 1999

A23064

Fast Wave Current Drive in H-Mode Plasmas
C.C. Petty, GA

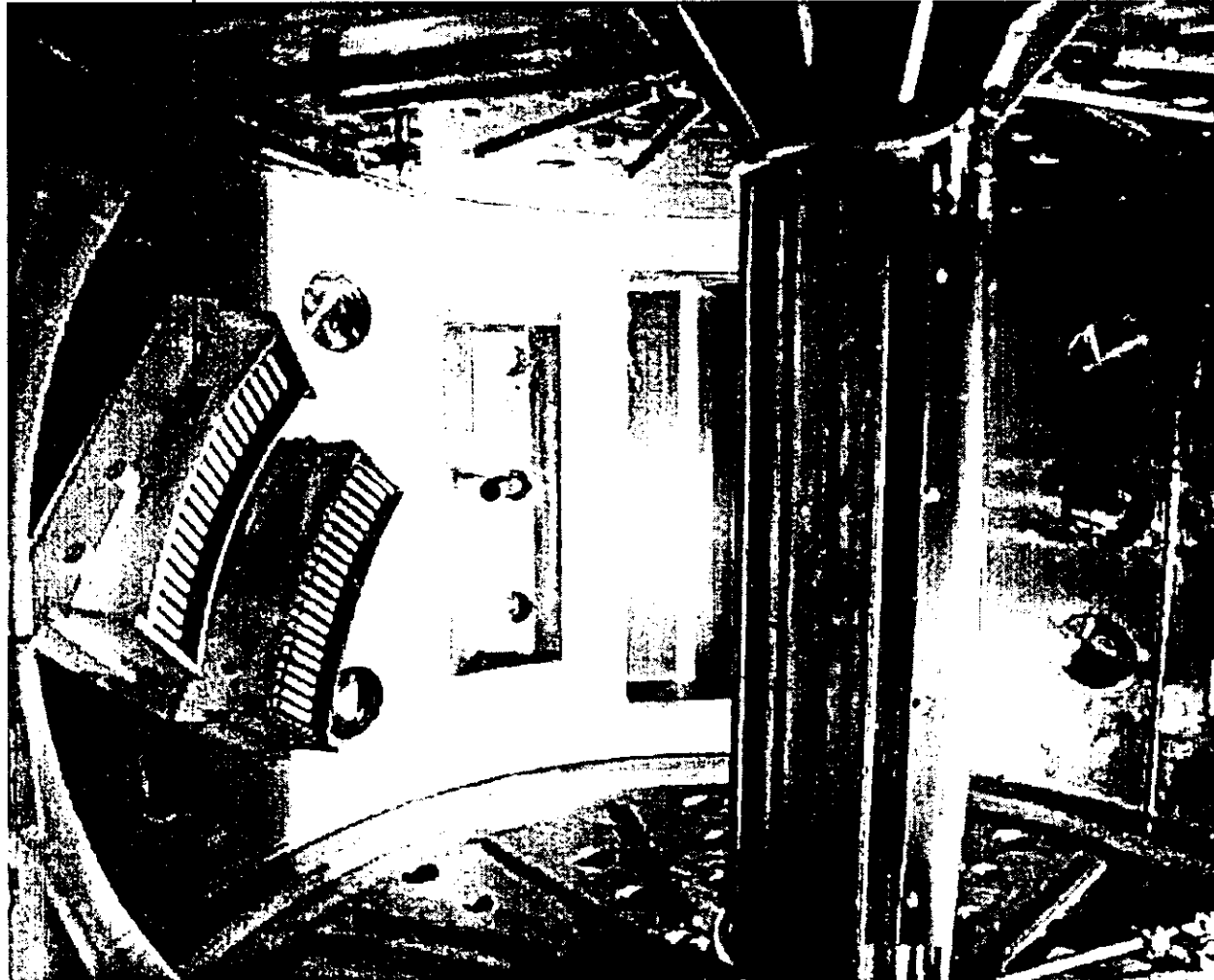
The CDX-U device at PPPL has studied high-frequency fast wave heating in a spherical tokamak geometry



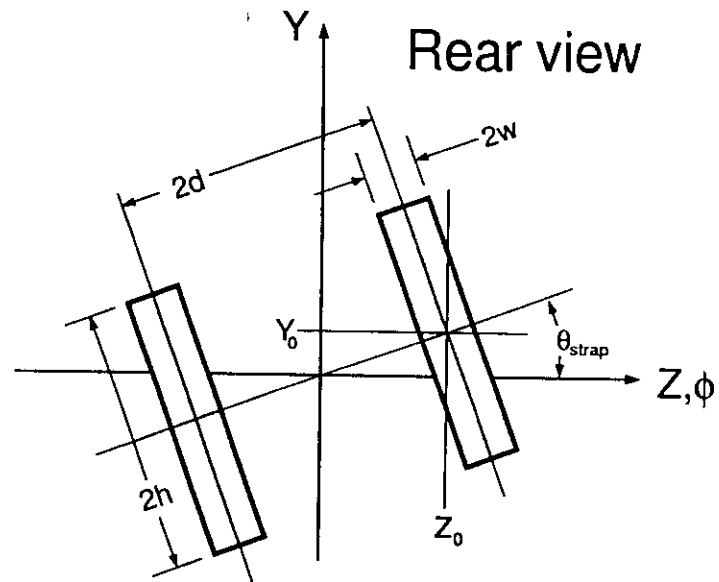
Question:

Does the large poloidal field in an ST complicate coupling to the fast wave?

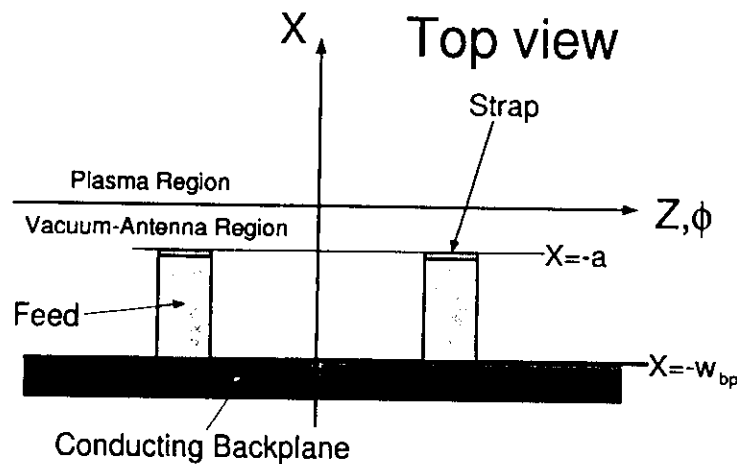
The rotatable fast wave antenna inside CDX-U is used to study FW coupling and heating physics



Simplest possible model for computing fast wave radiation resistance (excitation efficiency)



Antenna Model



Wave equations for fast wave fields in sheared-cylindrical plasma:

$$E_{\perp} = \rho \hat{E}_{\perp}$$

$$\rho = \sqrt{\frac{\Sigma}{x\sigma}}$$

$$\Sigma = n_{\perp}^2 + n_{\parallel}^2 - S$$

$$n_{\perp} = \alpha_f n_y - \beta_f n_z$$

$$\alpha_f = \cos \theta_f$$

$$cB_{\perp} = -\frac{\omega_0}{\omega} n_{\parallel} E_x$$

$$E_x = \frac{-i}{\Sigma} \left[n_{\perp} \frac{d}{dx} E_{\perp} + D E_{\perp} \right]$$

$$E_y = \alpha_f E_{\perp} + \beta_f E_{\parallel}$$

$$cB_y = \alpha_f cB_{\perp} + \beta_f cB_{\parallel}$$

$$n_z = \frac{n}{x}$$

$$0 = \frac{d^2}{dx^2} \hat{E}_{\perp} + \Phi_{FW} \hat{E}_{\perp}$$

$$\Phi_{FW} = -\Sigma + \frac{D^2}{\sigma}$$

$$\sigma = \Sigma - n_{\perp}^2$$

$$n_{\parallel} = \alpha_f n_z + \beta_f n_y$$

$$\beta_f = \sin \theta_f$$

$$cB_{\parallel} = \frac{\omega_0}{\omega} \left[n_{\perp} E_x + i \frac{d}{dx} E_{\perp} \right]$$

$$cB_x = \frac{\omega_0}{\omega} n_{\parallel} E_{\perp}$$

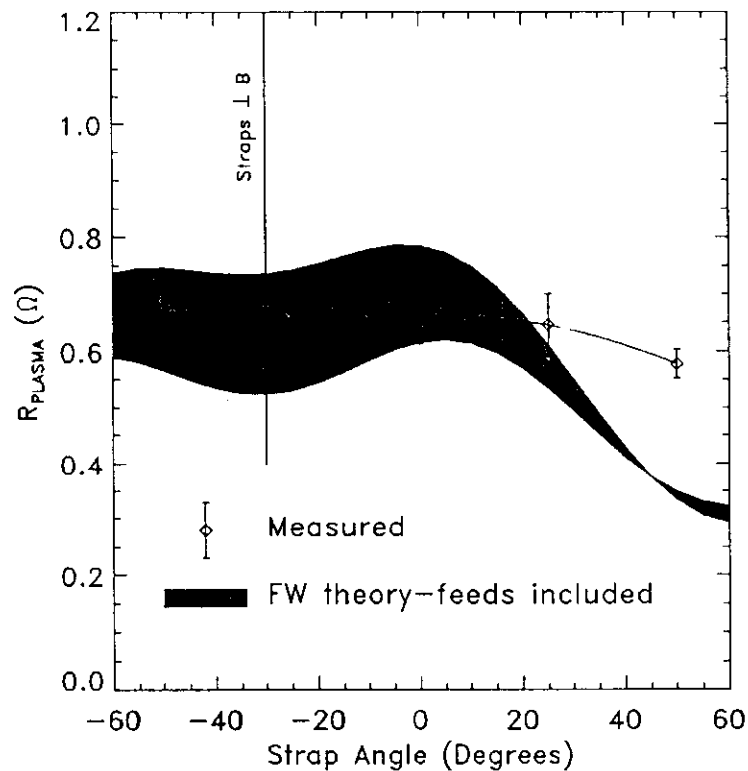
$$E_{\phi} = \alpha_f E_{\parallel} - \beta_f E_{\perp}$$

$$cB_{\phi} = \alpha_f cB_{\parallel} - \beta_f cB_{\perp}$$

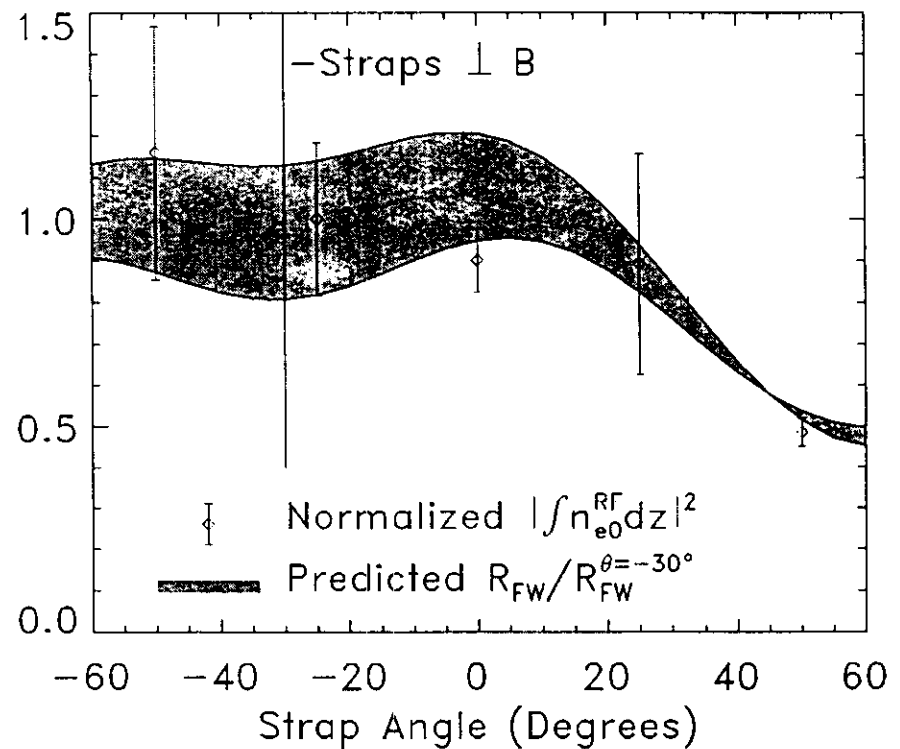
$$E_{\parallel} = \frac{n_{\parallel} \left[ix \frac{d}{dx} \left(\frac{E_x}{x} \right) - n_{\perp} E_{\perp} \right]}{P - n_{\perp}^2}$$

The simple CDX-U antenna can be treated accurately with an analytic model

Measured radiation resistance agrees with model for non-parallel straps



Core wave energy density drops when straps become parallel to B



In CDX-U, a peaked heating profile is predicted, but a broad heating profile is typically measured

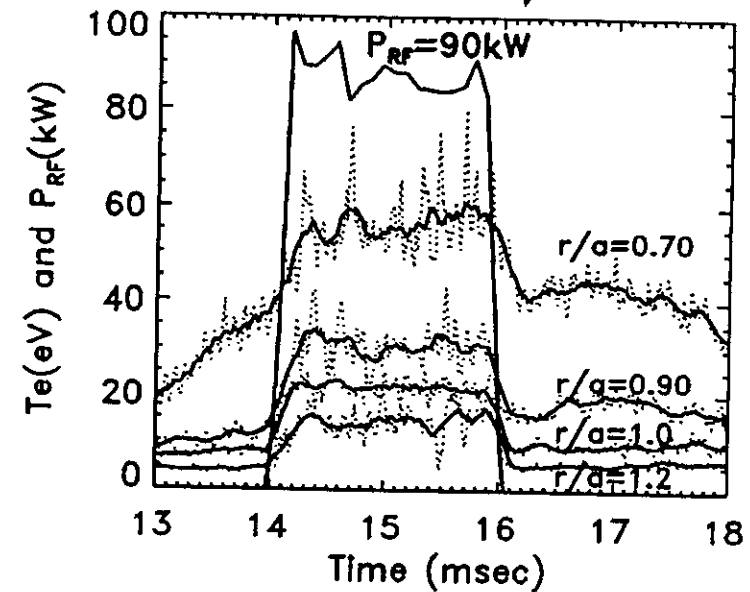
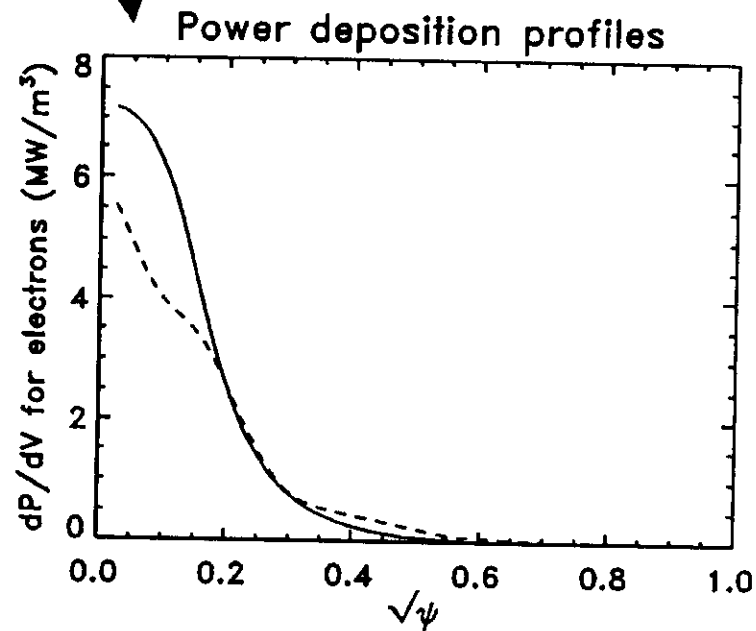


FIG. 6. Predicted power deposition profiles for electron heating in CDX-U computed using hot-electron ray tracing (solid line) and the TORIC full-wave code (dashed line) for an rf input power of 100 kW.

Spectroscopy data shows strong core heating for some discharges (input power may be marginal)

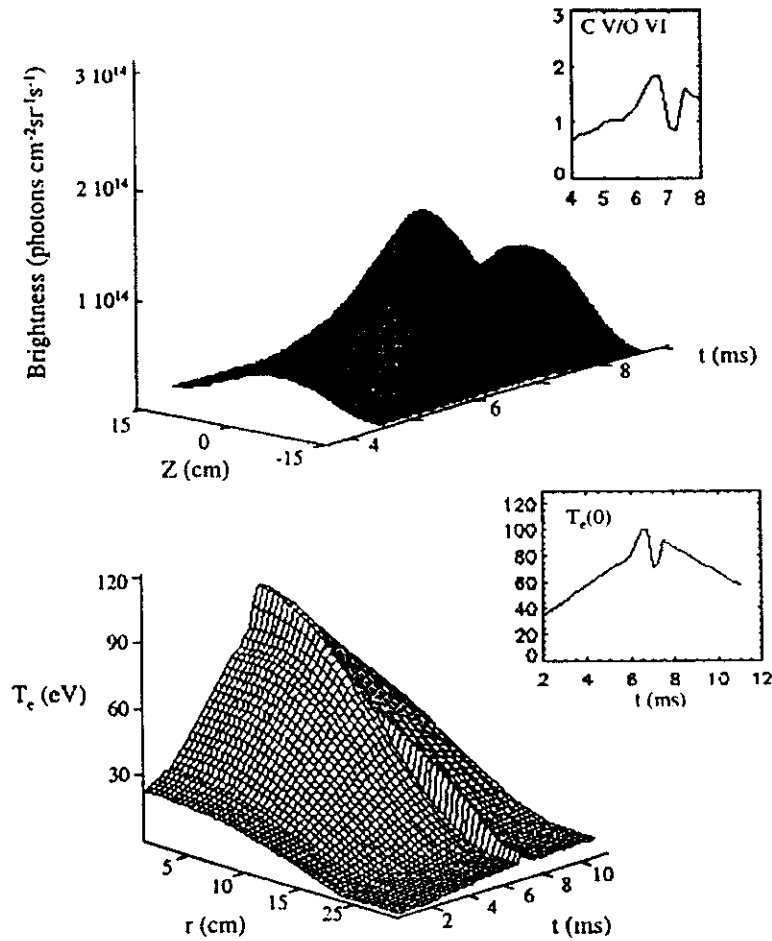


Figure 4. Computed spectroscopic signals and the temperature distribution for the ohmic discharge.

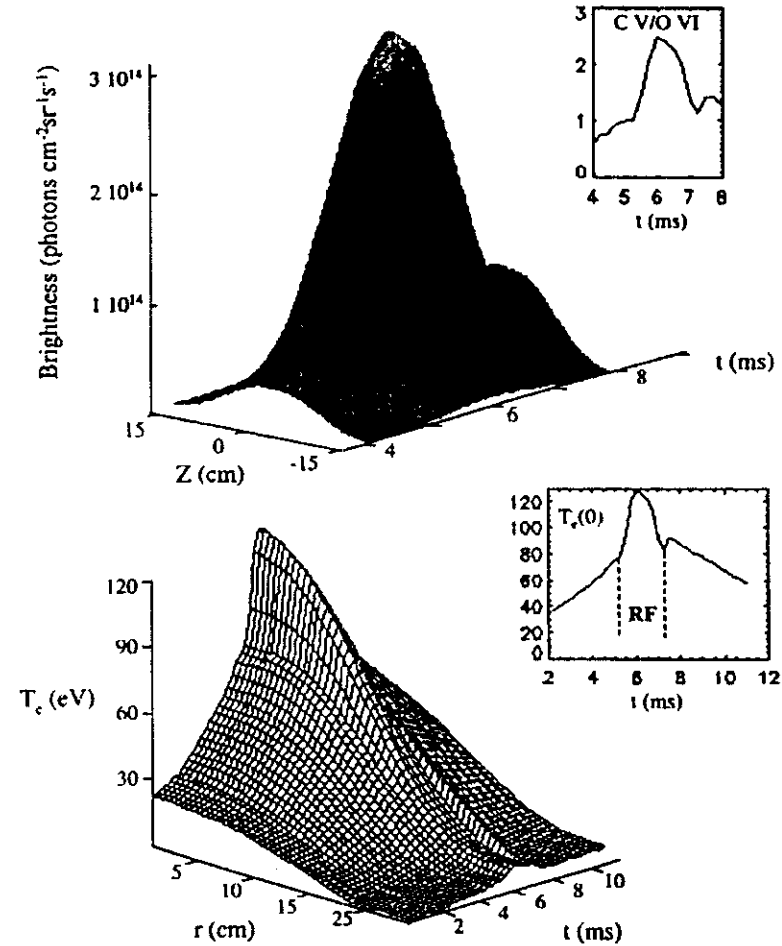
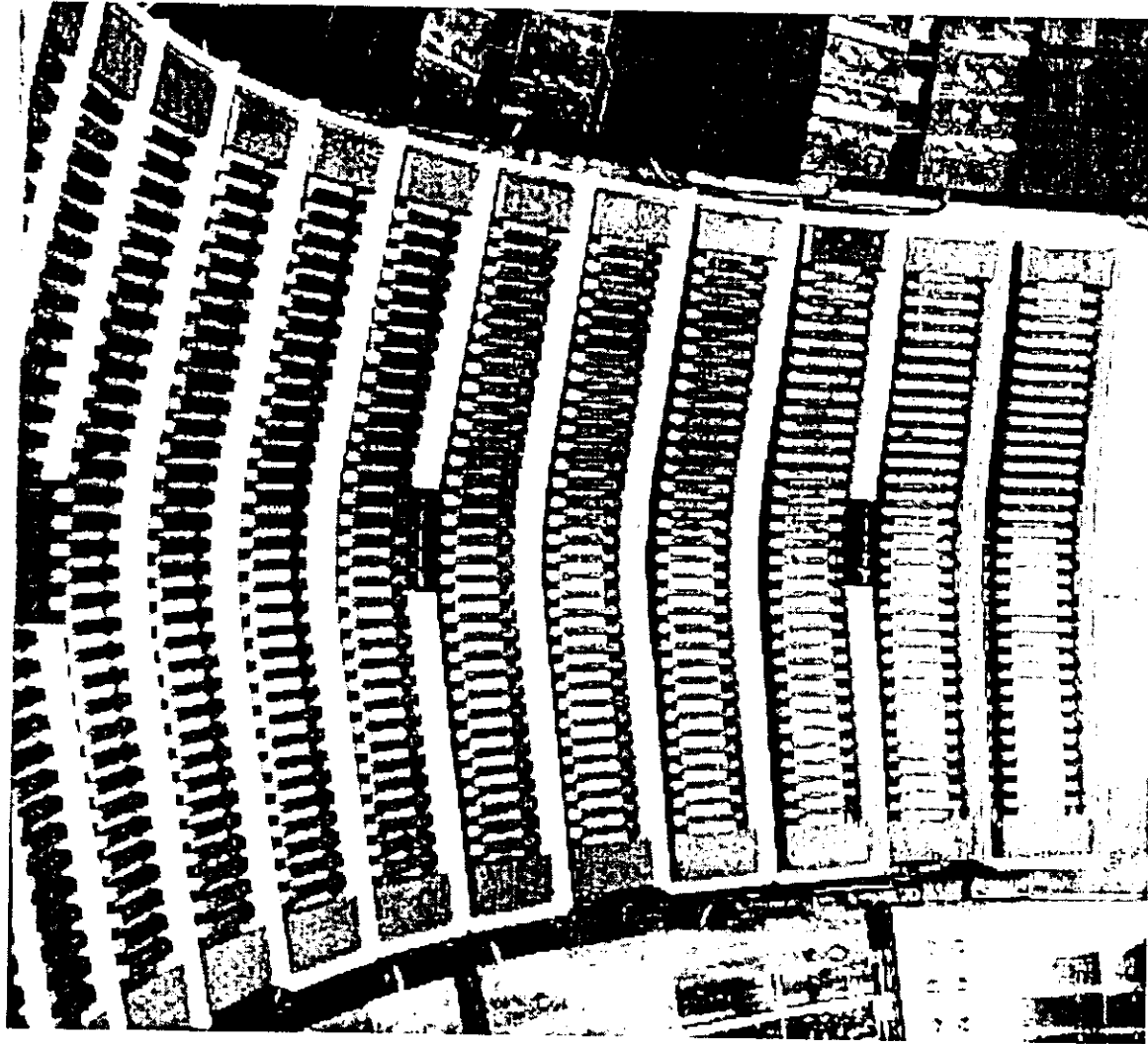


Figure 5. Computed signals and the estimated temperature evolution for the RF discharge.

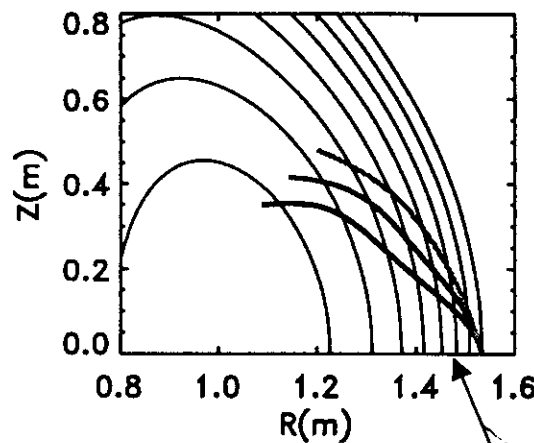
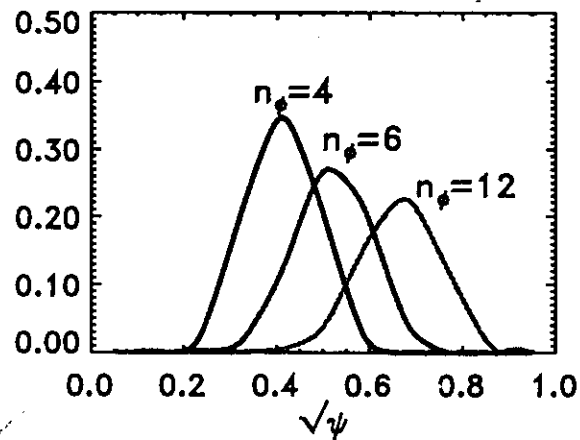
12 Strap HHFW Antenna Inside NSTX



2D equilibrium effects are important in HHFW modeling

Large B_p in ST causes large poloidally directed wave power flow

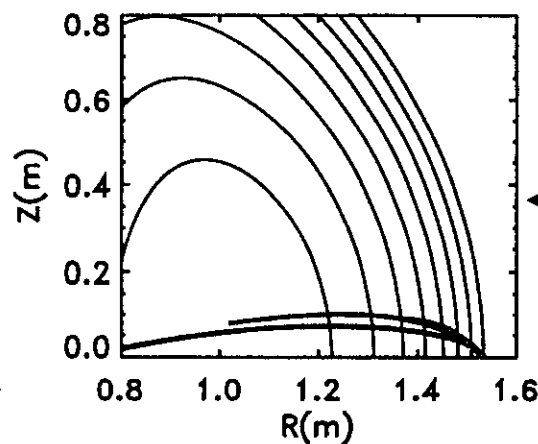
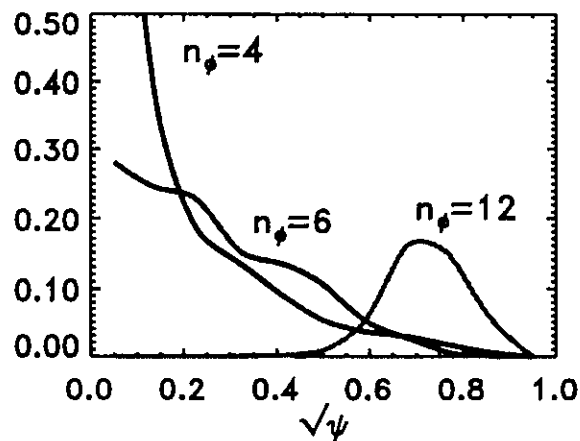
(Strong $n_{||}$ upshift further enhances damping)



← Cold ion ray tracing at $\beta = 30\%$ in NSTX

$$\frac{1}{c} \frac{dZ}{dt} = \left[\frac{v_{g\perp}}{c} \left(\frac{k_z - k_{||} \frac{B_z}{B}}{k_{\perp r}} \right) + \frac{v_{g||}}{c} \frac{B_z}{B} \right]$$

Power deposition profiles



← Same, but B_p reduced 90%

Ion-Cyclotron Damping Modeling Issues:

- For $B = 0.3$ Tesla and $k_{\perp} = 200 \text{ m}^{-1}$, $k_{\perp} \rho_D = 1$ at $T_D = 55 \text{ eV}$
- At $T_D = 1500 \text{ eV}$, $\lambda_D \equiv \frac{(k_{\perp} \rho_D)^2}{2} \approx 14 \Rightarrow$ codes which expand in small λ_D should be used with some caution
- And, resonances are at high harmonic number (15-20)

One plausible solution:

Satisfy full hot plasma dispersion relation along cold-ion ray trajectories using cold-ion $n_{\parallel} \Rightarrow$ exact \vec{E} polarization and damping (within WKB approximation) but approximate deposition profiles.

Motivation:

Non-negligible ion damping \Rightarrow

- Reduced current drive
- Ion tail formation
- Possible fast ion losses

Dielectric Tensor Elements for Hot Plasma

$$K_{xx} = 1 + \frac{\omega_{pe}^2}{\omega_{ce}^2} + \sum_s \frac{\omega_{ps}^2}{\omega^2} \sum_n \xi_{0,s} Z(\xi_{n,s}) n^2 \frac{W_n(\lambda_s)}{\lambda_s}$$

$$K_{xy} = -K_{yx} = i \frac{\omega_{pe}^2}{\omega \omega_{ce}} + i \sum_s \frac{\omega_{ps}^2}{\omega^2} \sum_n \xi_{0,s} Z(\xi_{n,s}) n W'_n(\lambda_s)$$

$$K_{yy} = K_{xx} - 2 \lambda_e \frac{\omega_{pe}^2}{\omega^2} \xi_{0,e} Z(\xi_{0,e}) W'_0(\lambda_e)$$

$$- 2 \sum_s \lambda_s \frac{\omega_{ps}^2}{\omega^2} \sum_n \xi_{0,s} Z(\xi_{n,s}) W'_n(\lambda_s)$$

$$K_{zz} = 1 + \frac{\omega_{pe}^2}{\omega^2} 2 \xi_{0,e}^2 (1 + \xi_{0,e} Z(\xi_{0,e})) - \sum_s \frac{\omega_{ps}^2}{\omega^2}$$

$$K_{yz} = -K_{zy} = +i \frac{k_{\perp}}{k_{\parallel}} \frac{\omega_{pe}^2}{\omega^2} \frac{\omega}{\omega_{ce}} (1 + \xi_{0,e} Z(\xi_{0,e})) - i \frac{k_{\perp}}{k_{\parallel}} \sum_s \frac{\omega_{ps}^2}{\omega^2} \frac{\omega}{\omega_{cs}} \sum_n (1 + \xi_{n,s} Z(\xi_{n,s})) W'_n(\lambda_s)$$

$$K_{xz} = K_{zx} = \frac{k_{\perp}}{k_{\parallel}} \sum_s \frac{\omega_{ps}^2}{\omega^2} \frac{\omega}{\omega_{cs}} \sum_n (1 + \xi_{n,s} Z(\xi_{n,s})) n \frac{W_n(\lambda_s)}{\lambda_s}$$

- Complex $k_{\perp} \Rightarrow$ need complex Bessel functions
- Need 50-100 harmonics in sum
- Need complex root-finder capable of distinguishing between FW and ion-Bernstein branches near resonances at low n_{\parallel}

Wave Power Absorption in WKB Approximation

Vlasov equation \Rightarrow

$$\left\langle \frac{\partial}{\partial t} \int \frac{m_s v^2}{2} f_{2s} d^3v \right\rangle + \left\langle \nabla \cdot \int \frac{m_s v^2}{2} \vec{v} f_{2s} d^3v \right\rangle \stackrel{\text{Time average}}{=} \left\langle \vec{E}_1 \cdot \vec{J}_{1s} \right\rangle$$

(The equivalence of these terms is assumed)

$$\frac{\partial}{\partial t} W_{ps} + -2\vec{k}_{\perp i} \cdot \vec{T}_{\perp s} = \frac{1}{2} \omega \epsilon_0 \vec{E}^* \cdot \vec{\epsilon}_{As} \cdot \vec{E}$$

Field amplitude

$$\frac{\partial P_s}{\partial V} = \frac{1}{2} \omega \epsilon_0 \left[\vec{E}^* \cdot \vec{\epsilon}_{As} \cdot \vec{E} - n_{\perp i} \vec{E}^* \cdot \frac{\partial \vec{\epsilon}_{Hs}}{\partial n_{\perp r}} \cdot \vec{E} \right]$$

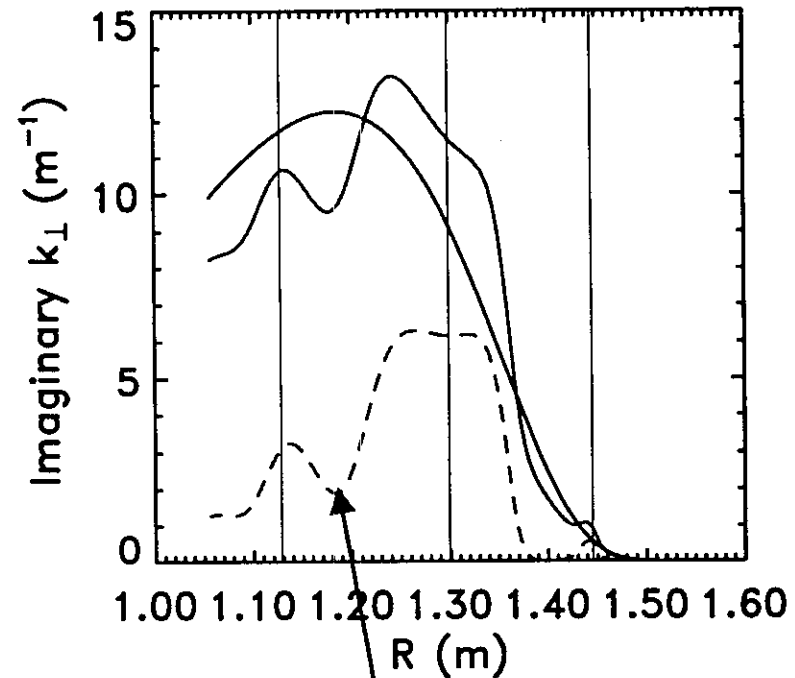
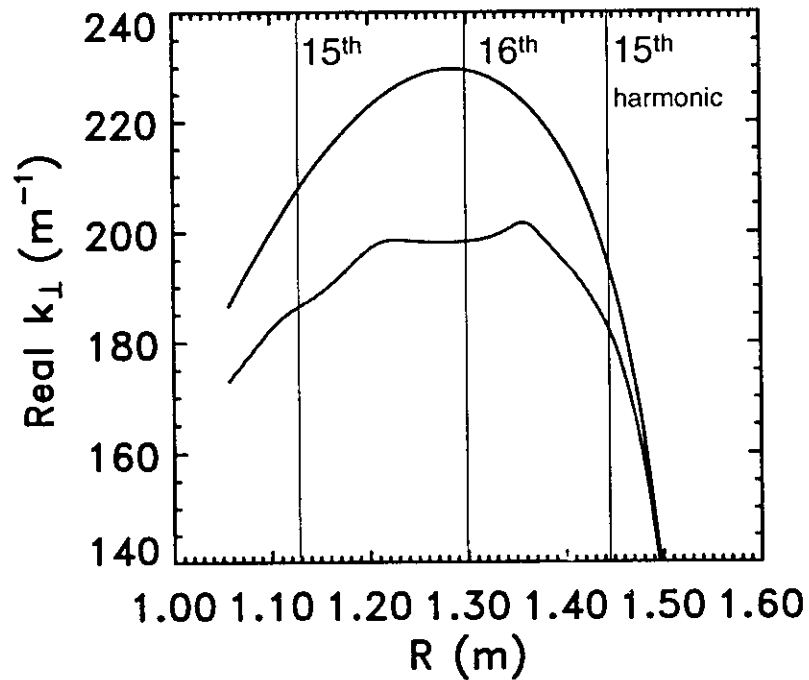
↑
Volumetric power absorption for species s

↑
Full hot plasma $\vec{\epsilon}$ and \vec{E} evaluated with complex \vec{k}

Effect of T_D on wave-number

Finite ion temperature reduces $k_{\perp r}$

Average magnitude of $k_{\perp i}$ similar, but split between species



$$n_{\phi} = 12, f = 30 \text{ MHz}$$

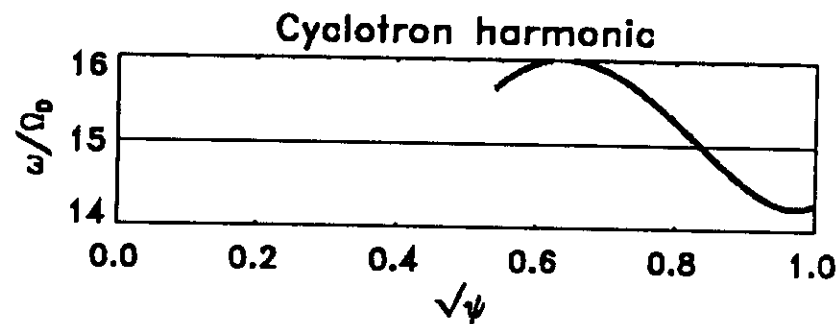
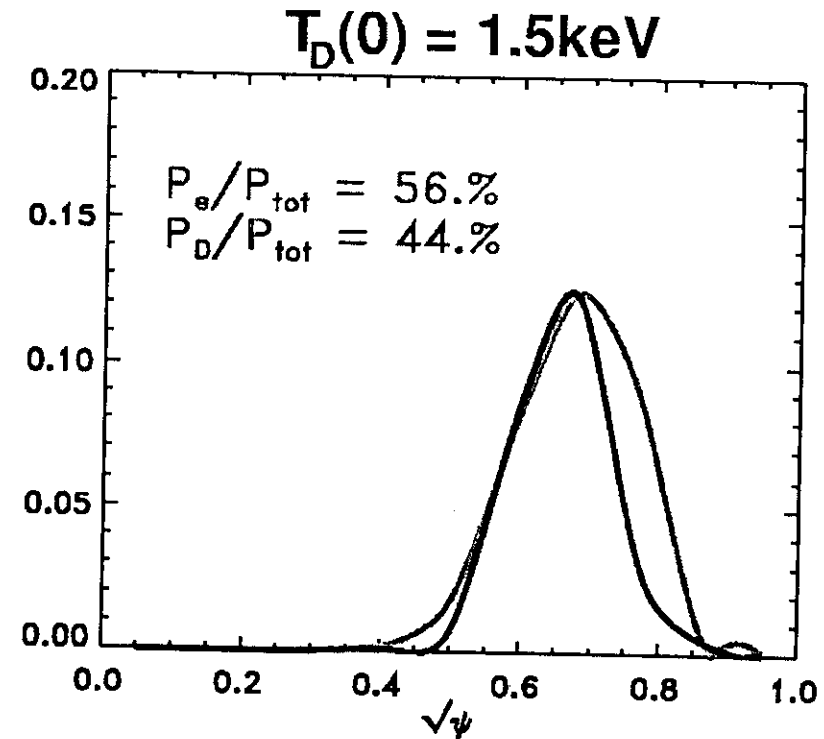
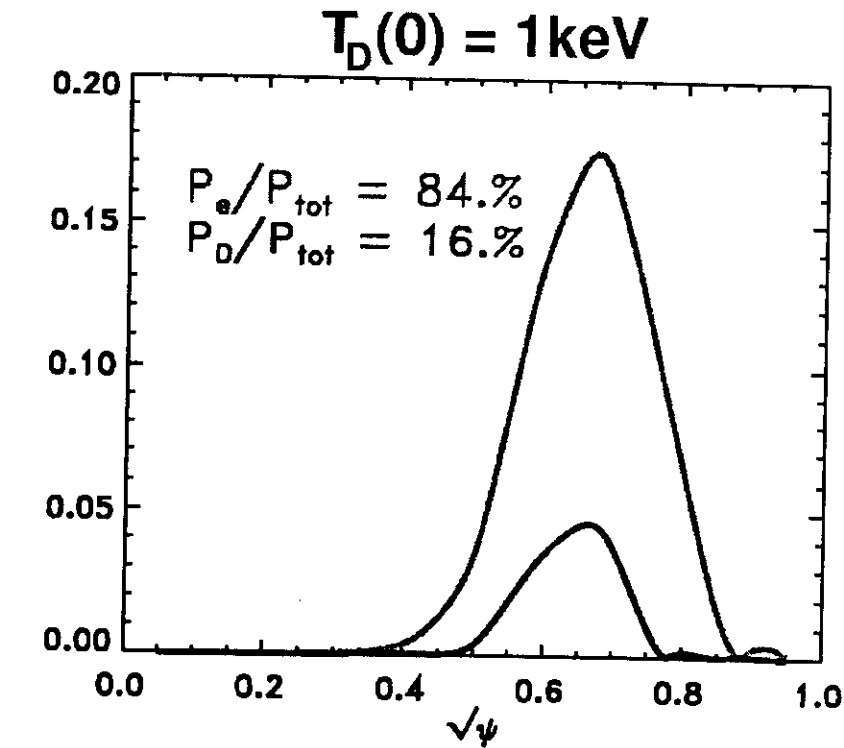
$$T_D(0) = 150 \text{ eV}$$

$$T_D(0) = 1500 \text{ eV}$$

$$T_e(0) = 1500 \text{ eV}$$

Deuterium contribution

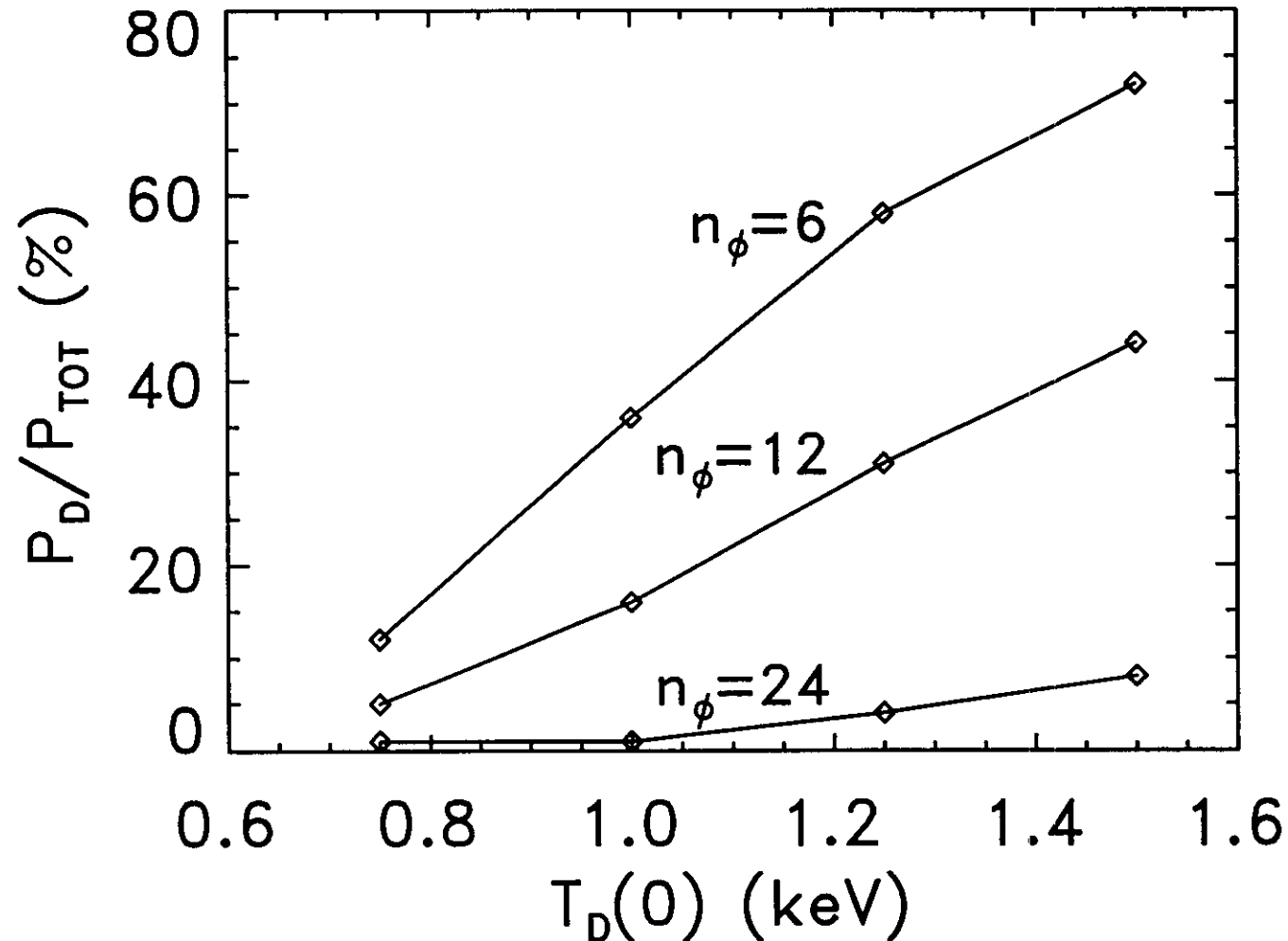
Bulk ion absorption competes with electron damping for temperatures above 1keV



$n_\phi = 12$ (90° phasing)
for both cases

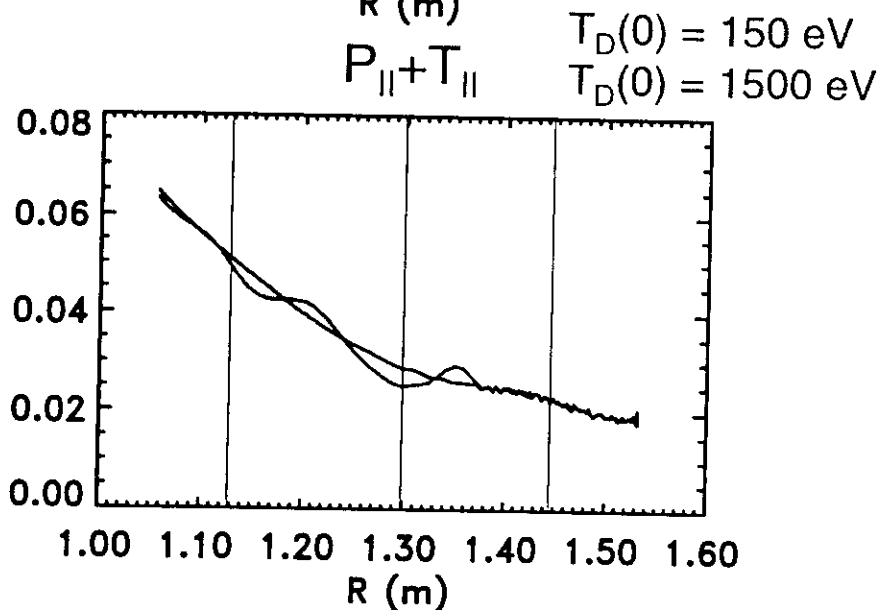
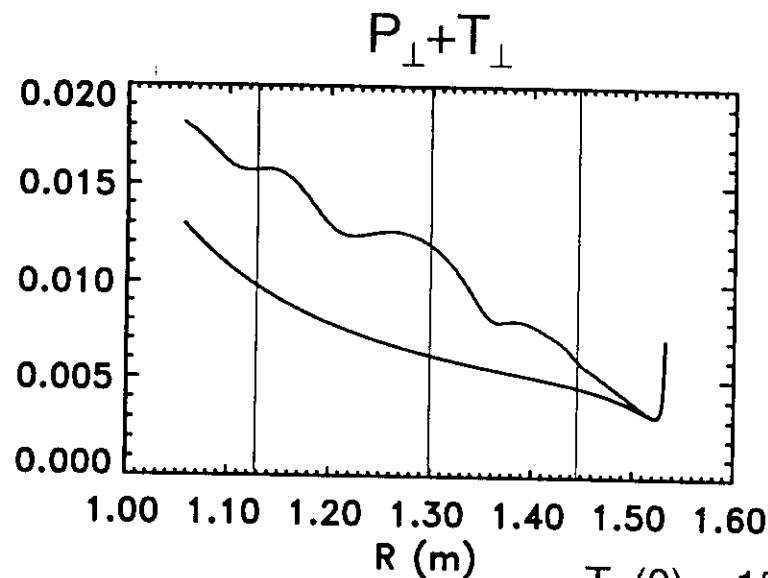
$T_e(0) = 1.5\text{keV}$

Deuterium ion absorption shows strong launched toroidal mode number (n_ϕ) dependence

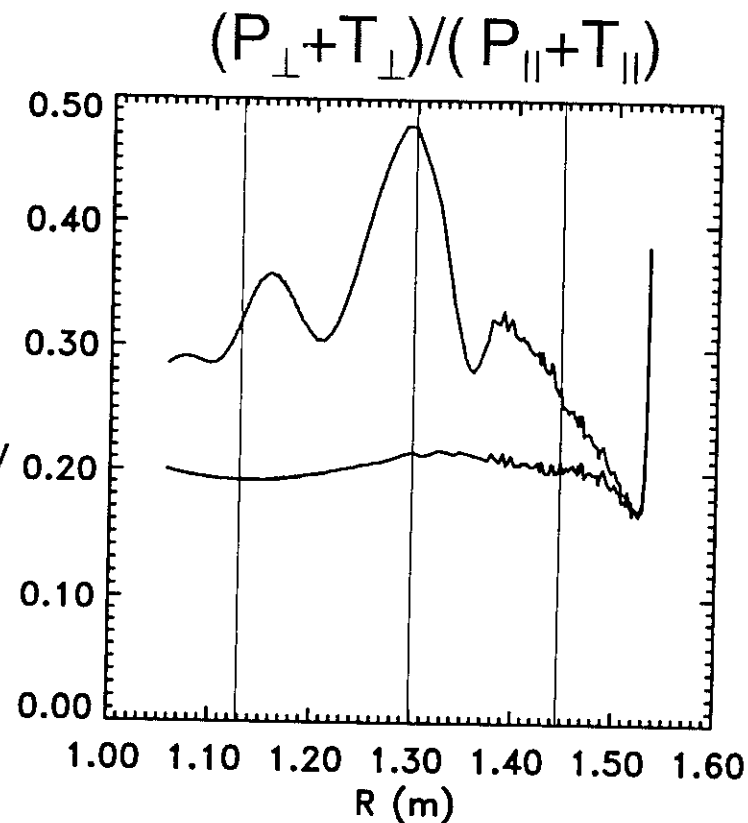


Lower phase velocity broadens and weakens the ion resonances

Use of hot electron - cold ion ray trajectory may be inaccurate at high ion temperature



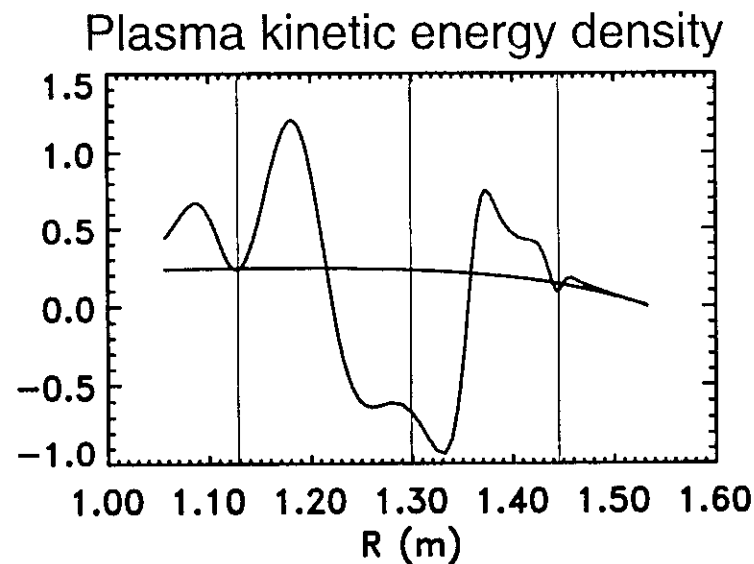
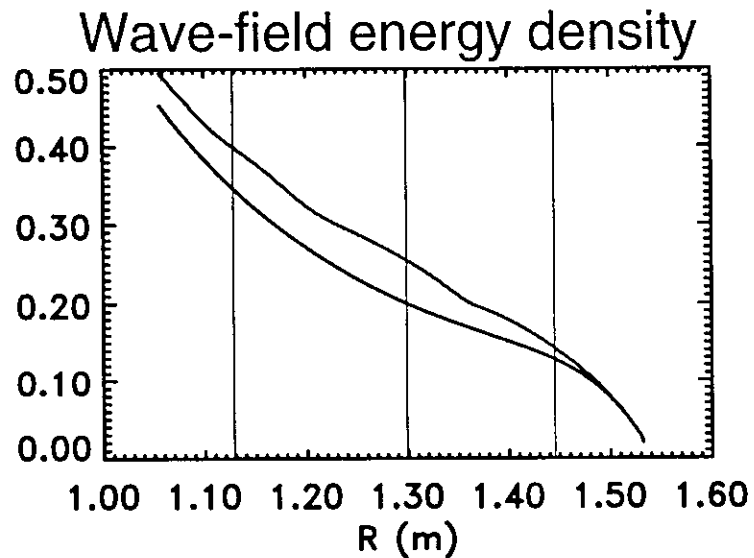
Ion perpendicular kinetic flux changes energy propagation direction



$$n_{\phi} = 12, f = 30 \text{ MHz}$$

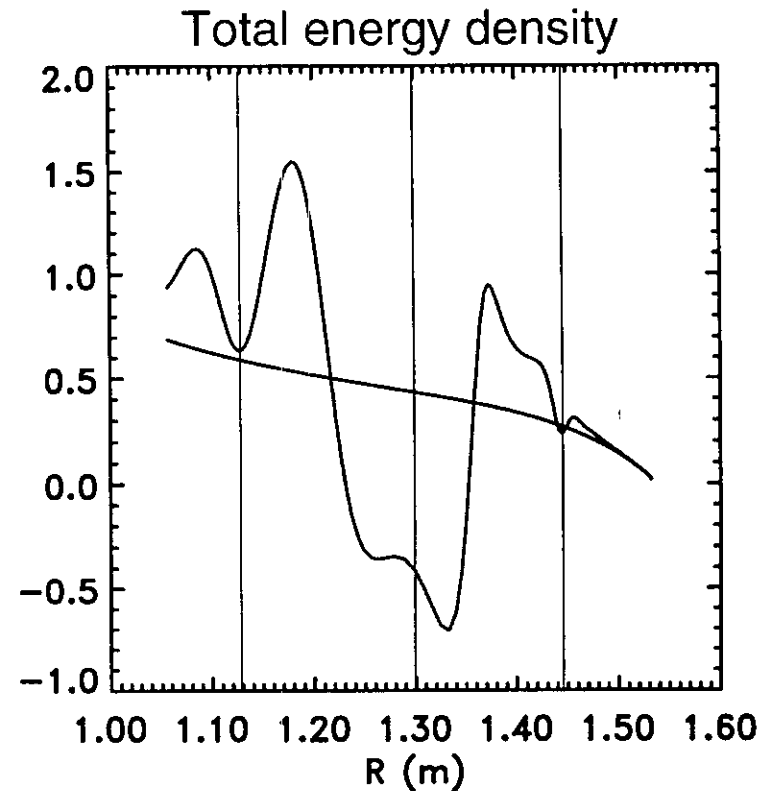
Fluxes normalized to $|E| = 1 \text{ V/m}$

Standard “definition” of perturbed plasma kinetic energy density can become negative with hot ions



Equation for perturbed plasma kinetic energy density (which can become negative):

$$W_{ps} = \frac{1}{4} \epsilon_0 \vec{E} \cdot \frac{\partial}{\partial \omega} (\omega \vec{\chi}_{Hs}) \cdot \vec{E}$$



$T_D(0) = 150 \text{ eV}$
 $T_D(0) = 1500 \text{ eV}$

$n_\phi = 12, f=30\text{MHz}$

Fluxes normalized to $\vec{E} = 10\text{kV/m}$

Negative energy density near cyclotron harmonics \Rightarrow
oscillatory group velocity \Rightarrow

**Hot ion ray tracing on a strongly
complex dispersion relation is ill-posed**

Possible solution: re-normalize power flux \Rightarrow

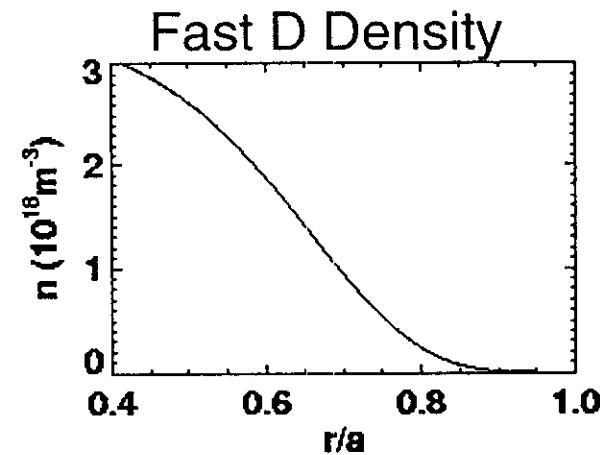
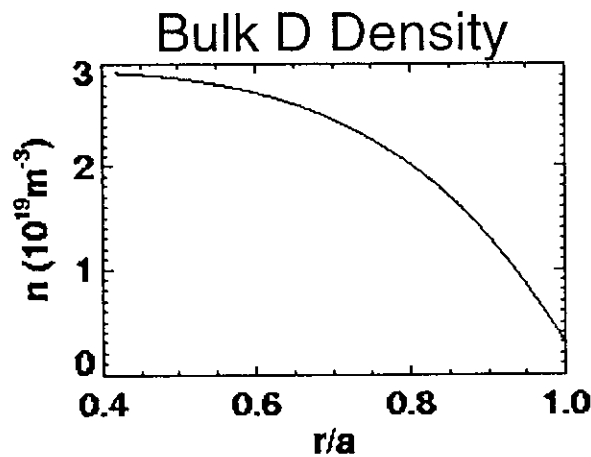
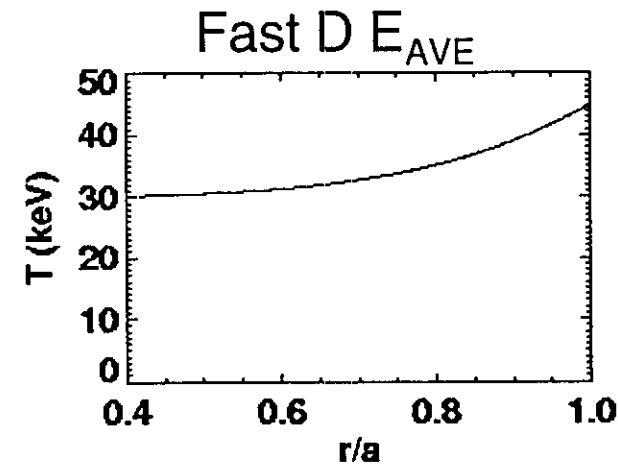
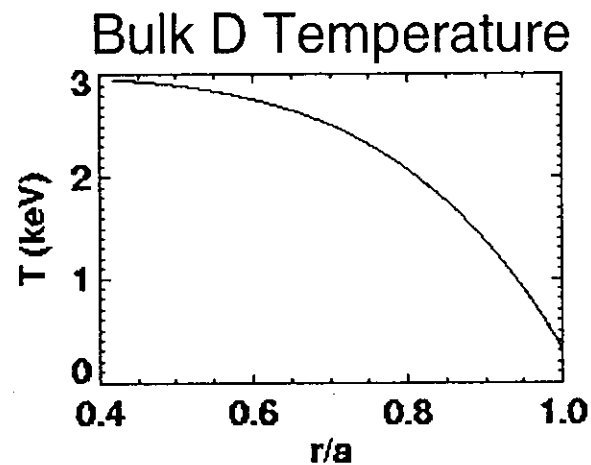
$$\langle \vec{P} \rangle + \sum_s \left\langle \int \frac{m_s v^2}{2} \vec{v} f_{2s} d^3v \right\rangle$$

Ray-trace using $\frac{\langle \vec{P} \rangle + \sum_s \left\langle \int \frac{m_s v^2}{2} \vec{v} f_{2s} d^3v \right\rangle}{\langle W_{\text{field}} \rangle + \sum_s \left\langle \int \frac{m_s v^2}{2} f_{2s} d^3v \right\rangle}$ as group velocity

In other words, compute the power flow velocity explicitly from the RF perturbed distribution function, fields, and Poynting flux

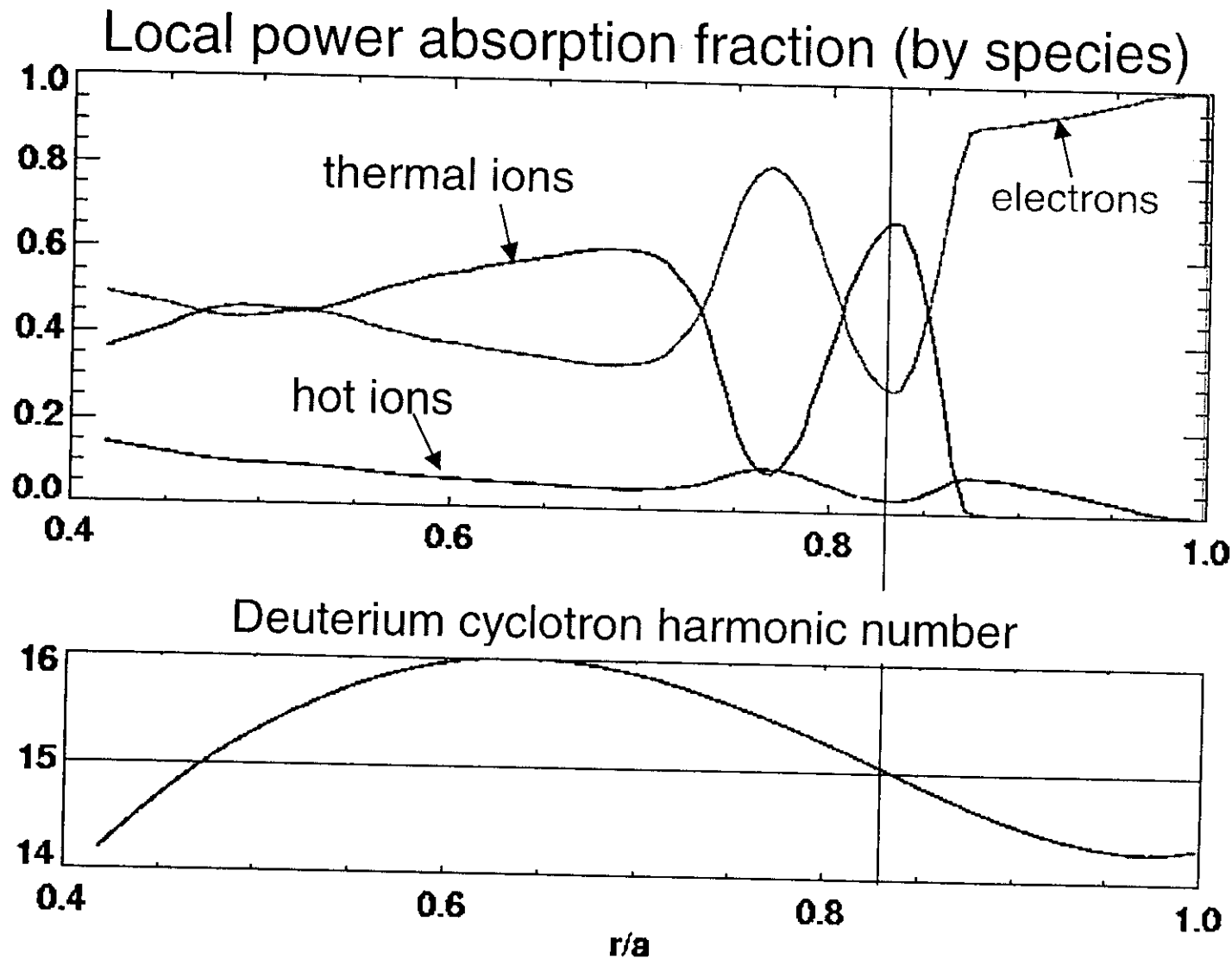
What about interactions with beam ions?

Treat NBI fast ions as hot thermal species using approximate profiles from $\beta=40\%$ TRANSP run



$$T_e(0) = 2.5\text{keV}, E_{\text{BEAM}} = 80\text{keV}, P_{\text{BEAM}} = 5\text{MW}$$

NBI ions absorb < 5% of incident HHFW power



$$T_e(0) = 2.5\text{keV}, \quad n_\phi = 12, \quad P_D/P_{\text{TOT}} \approx 50\%$$

Summary

- DIII-D has shown that high frequency fast waves can be used to heat electrons and drive current on-axis in accordance with theory.
- CDX-U has shown efficient fast wave coupling in an ST.
- Controllable off-axis power deposition and current drive is predicted for high-harmonic fast waves in NSTX.
- At high ion β , ion absorption becomes competitive with electron absorption, and should be strongly dependent on launched toroidal mode number.

Summary (continued)

- Cold ion ray trajectories are potentially inaccurate because of the large ion kinetic flux at high ion β .
- Ray-tracing theory with hot thermal ions breaks down at high ion β is not (necessarily) because of mode conversion to IBW waves, but because of problems in computing the perturbed particle kinetic energy density from the dispersion relation near cyclotron harmonics.
- Re-normalization of the total power flux may remove this difficulty.
- Unlike DIII-D, absorption on NBI generated fast ions in an ST is predicted to be small \Leftrightarrow fast ion β is small and wave phase velocity too slow to damp on fast ions.

