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**Joint INFM - the Abdus Salam ICTP School on  
"Magnetic Properties of Condensed Matter Investigated by Neutron  
Scattering and Synchrotron Radiation Techniques"**

**1 - 11 February 2000**

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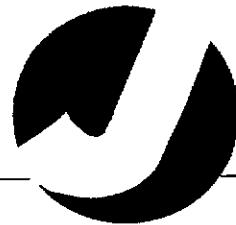
***PHOTOEMISSION FROM MAGNETIC SYSTEMS***

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***These are preliminary lecture notes, intended only for distribution to participants.***



## **Photoemission from Magnetic Systems**

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Forschungszentrum Jülich

### **I. Photoemission and Bandstructure**

Basic Aspects of the Method

Bandstructure of Magnetic Materials

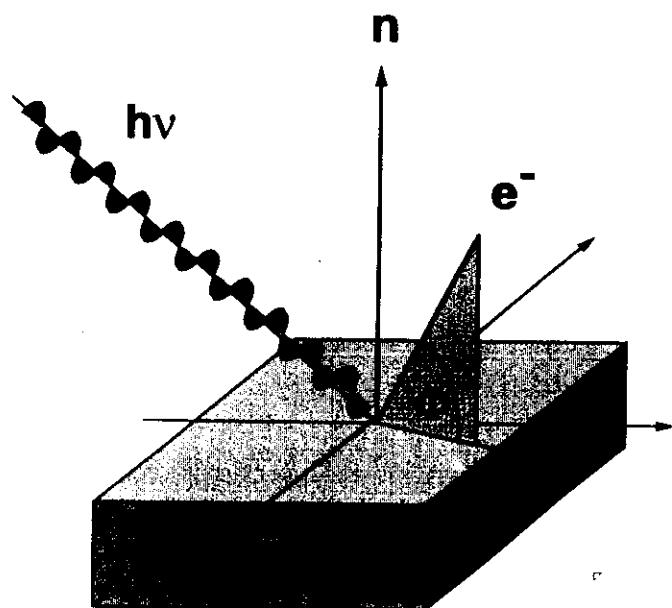
### **II. Electronic Structure and Magnetism**

Finite temperature effects

Finite size effects in low-dimensional structures

**Trieste, 11-2-2000**

# Photoemission



photon in ==> electron out

# Photoemission

**Einstein (1905) :**  
**Theory of the photoelectric effect**

A photon is absorbed in the photoemission process. It transfers its energy, momentum, and angular momentum to an electron, which is excited

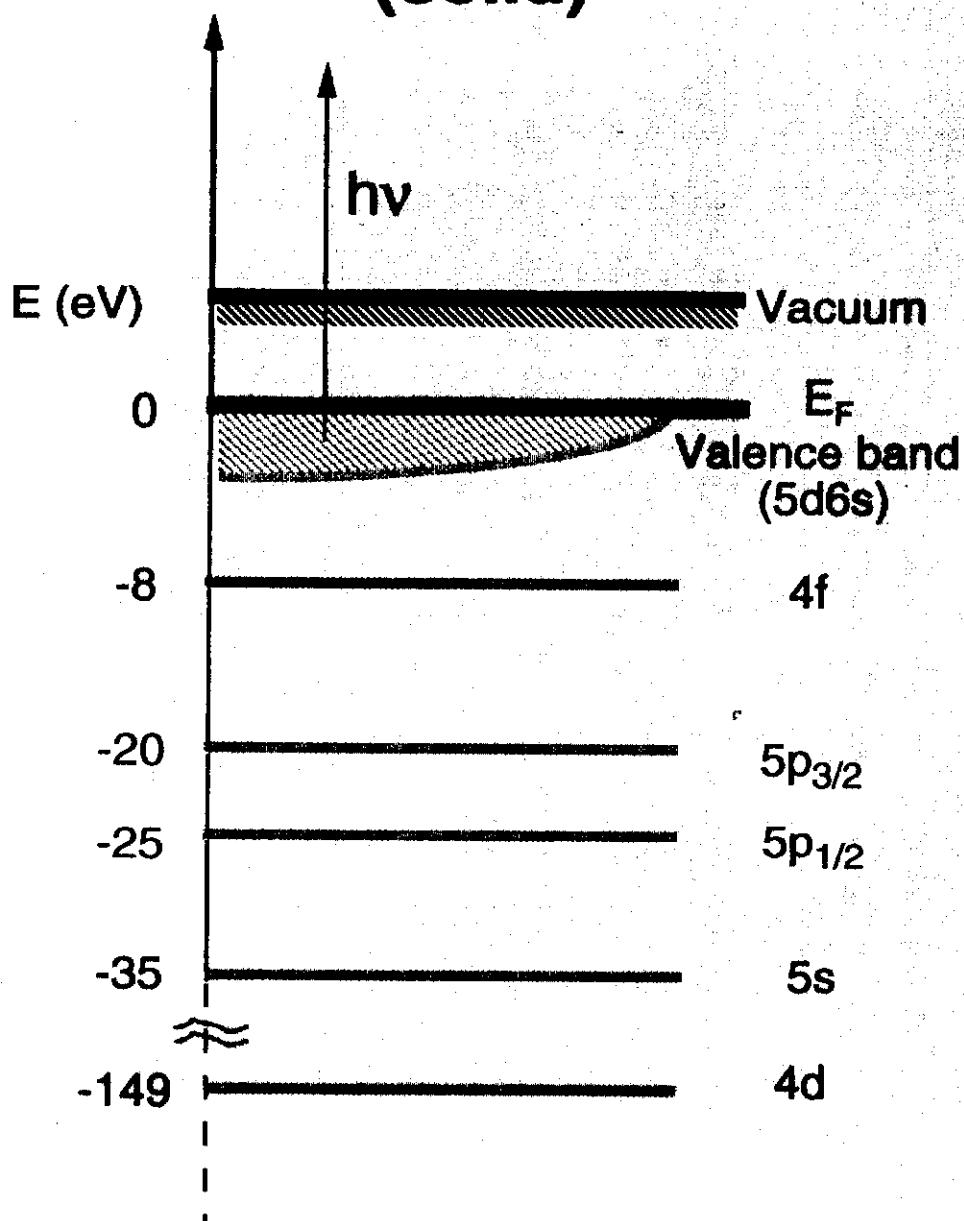
The energy of the excited (emitted) electron is proportional to the energy (wavelenght) of the photon

The number of the emitted electrons is proportional to the intensity of the incoming photons

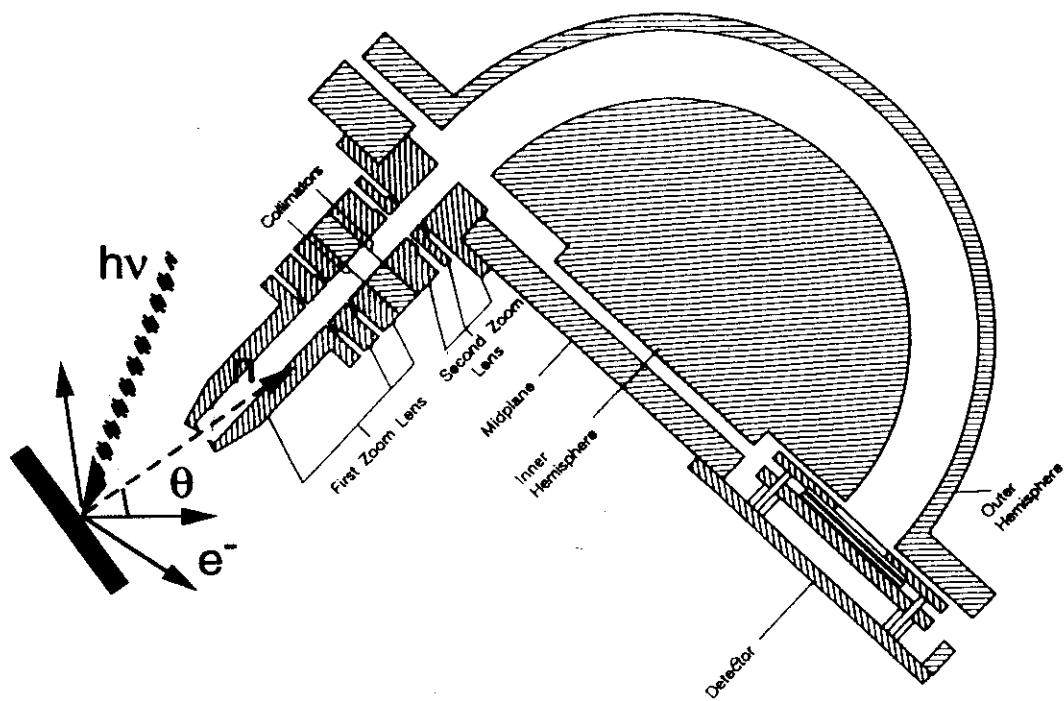
**Energy conservation :**

$$E_f = E_i + h\nu$$

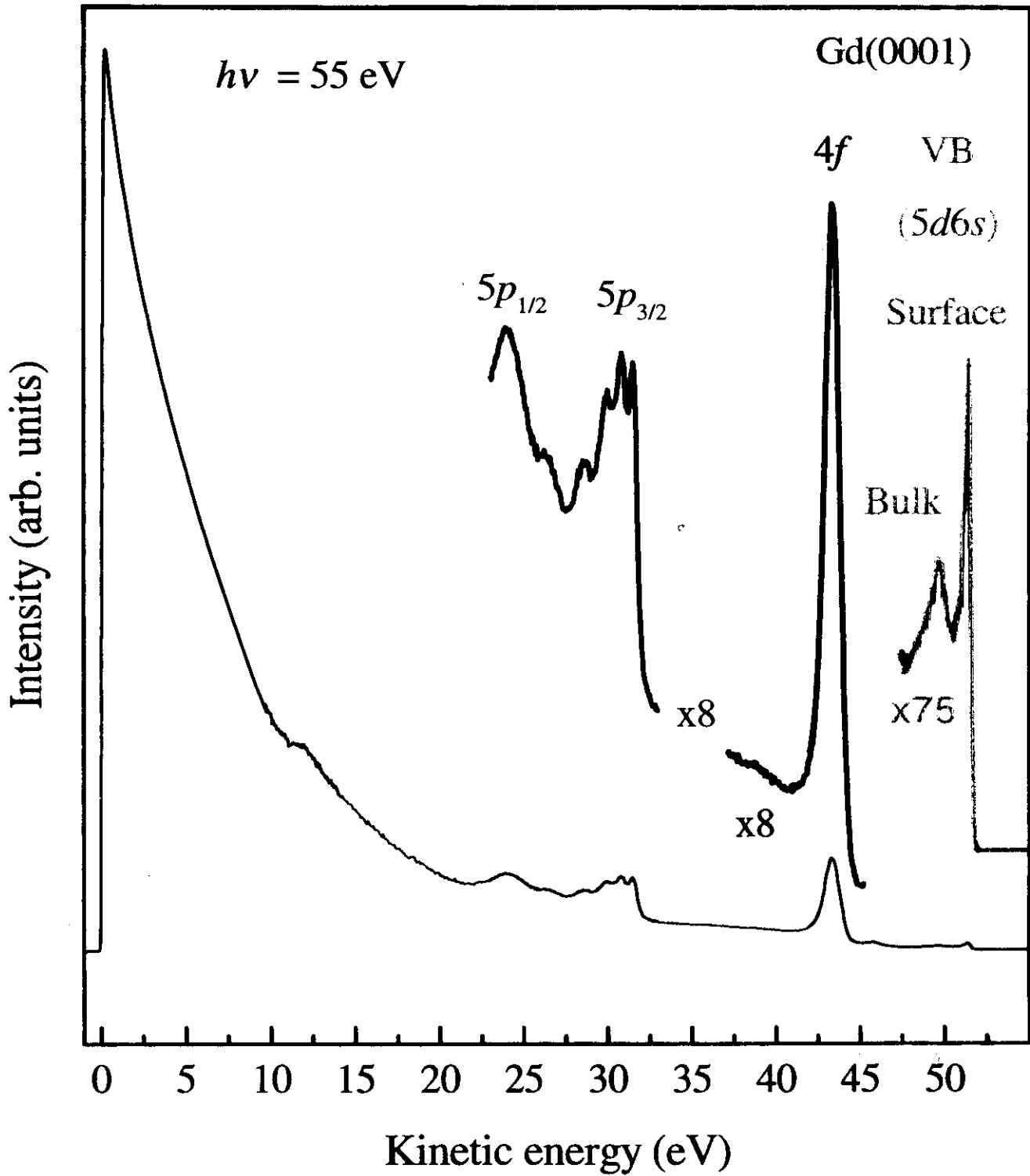
# Energy levels of Gd (solid)



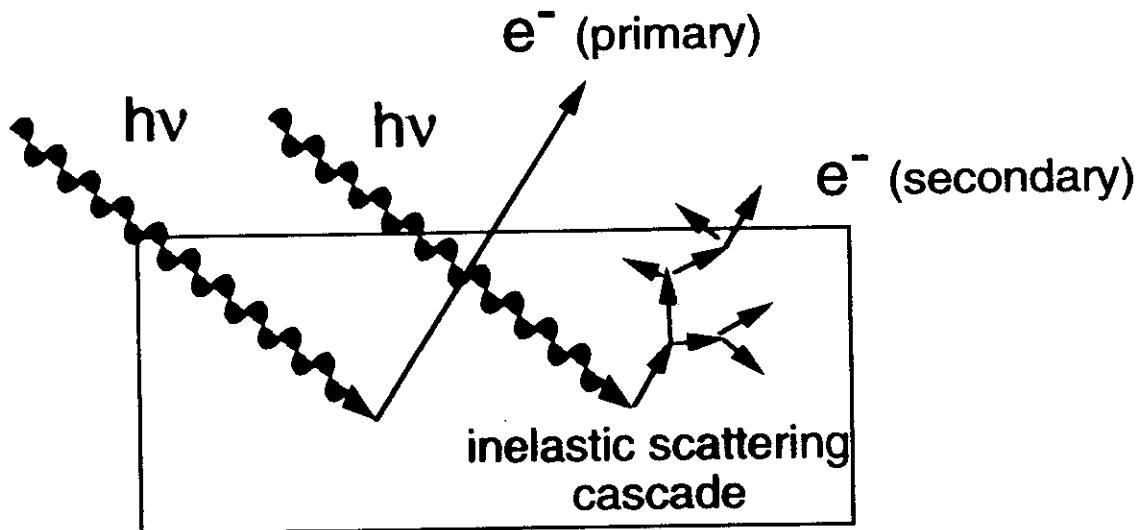
# Electron Energy Analyzer



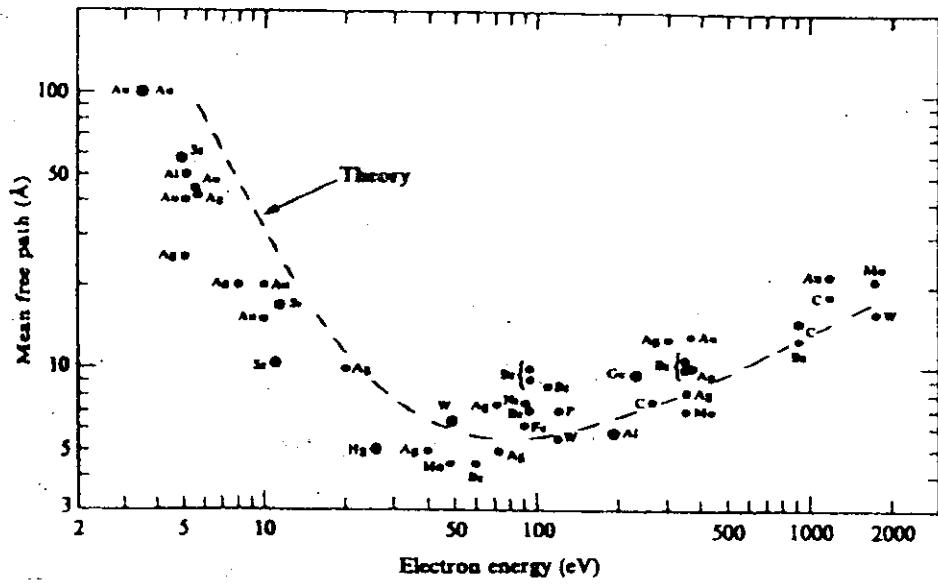
measure photoelectron  $E_{\text{kin}}$  and emission angle ( $\theta$ )



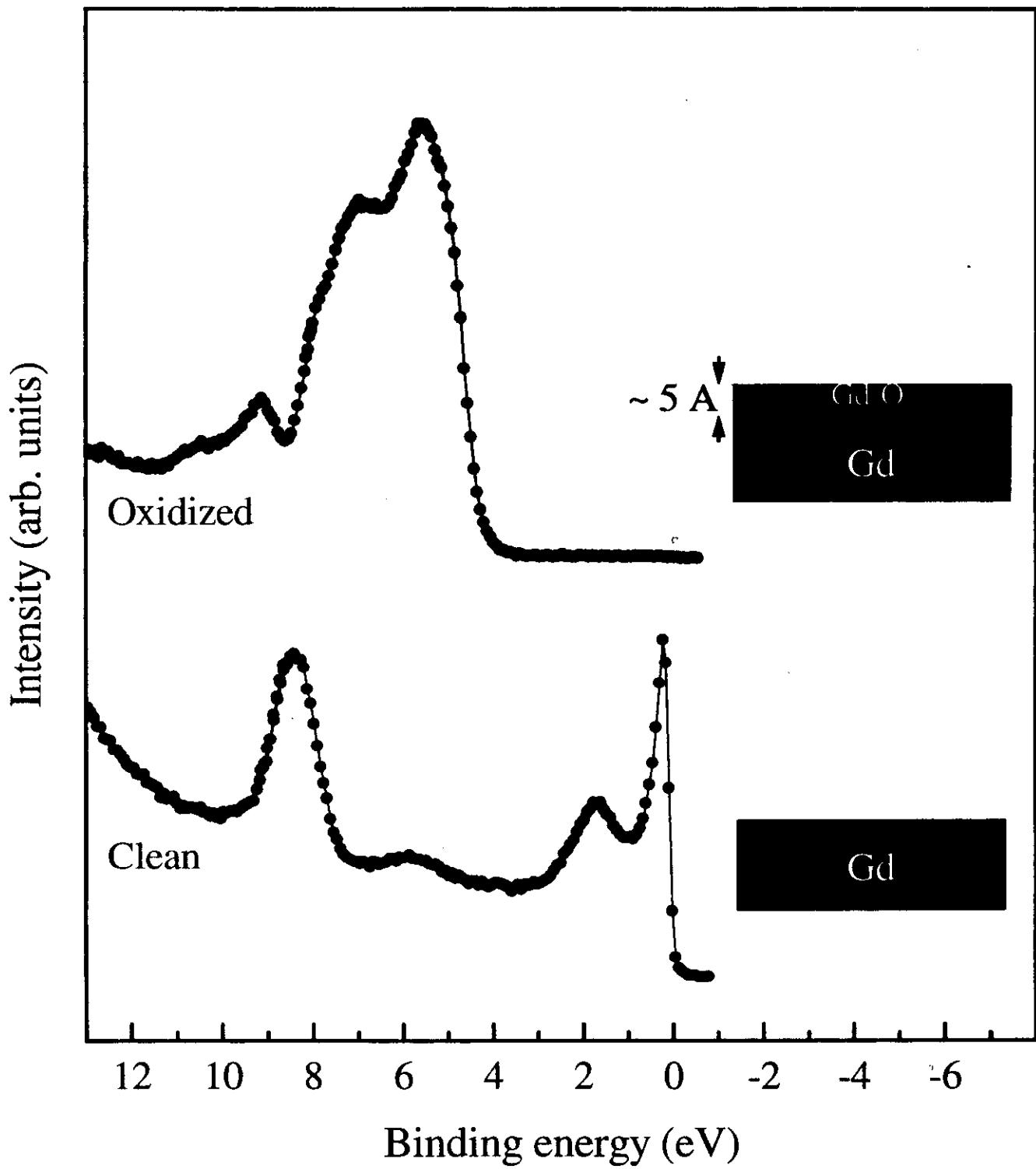
# Inelastic scattering and electron mean free path



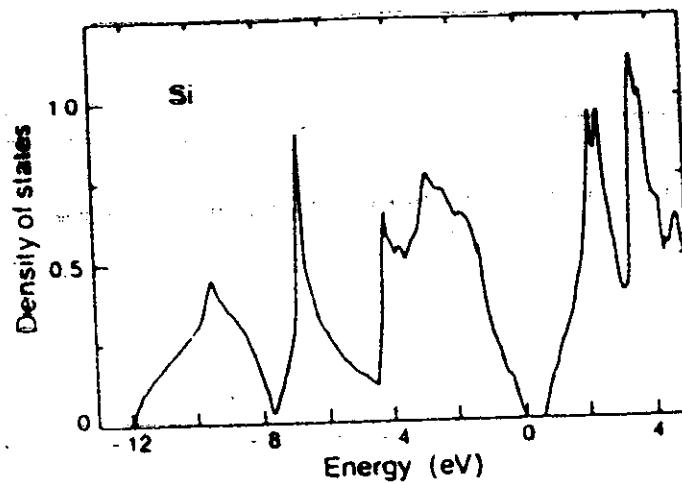
## Electron mean free path



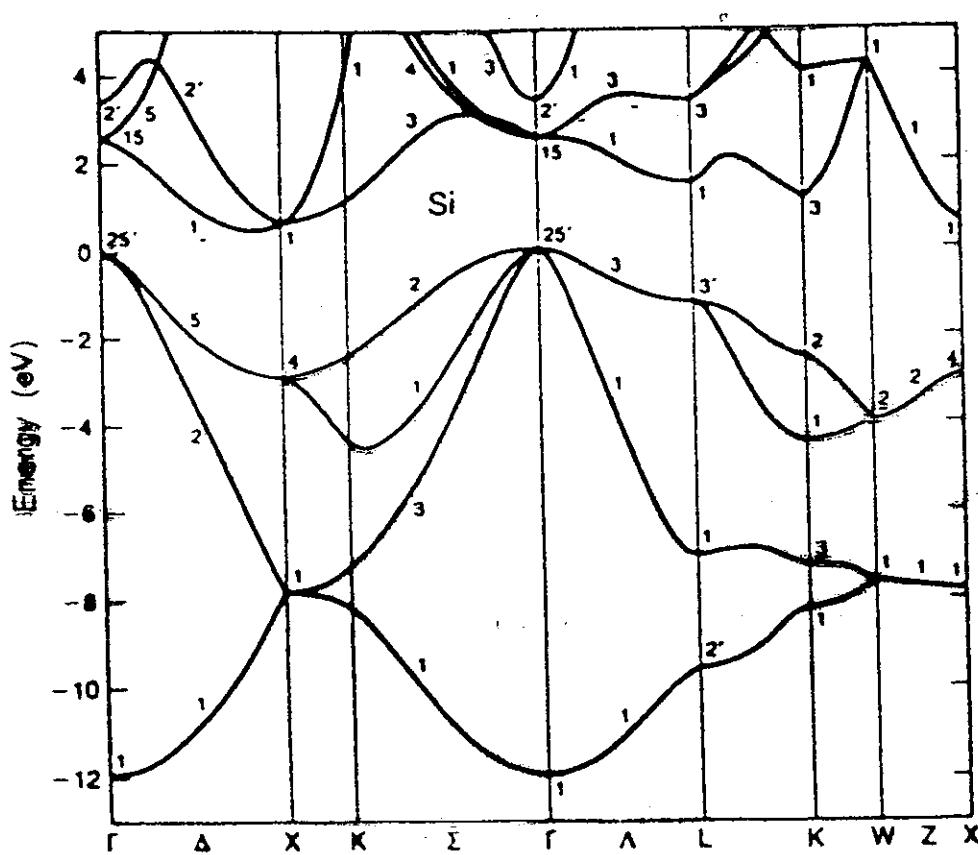
# Surface sensitivity



# Density of States



# Bandstructure: $E = E(k)$



## Transition rates, Matrix elements

“Fermi Golden Rule“

$$W \propto \langle f | H' | i \rangle^2 \delta(E_f - E_i - h\nu)$$

$$H' = \frac{e}{2mc} (\mathbf{A} \cdot \mathbf{P} + \mathbf{P} \cdot \mathbf{A}) + \frac{e^2}{2mc^2} |\mathbf{A}|^2 - e\Phi$$

$$[\mathbf{A}, \mathbf{P}] = -i\hbar \nabla \mathbf{A}$$

$$W \propto \left| \langle f | 2\mathbf{A} \cdot \mathbf{P} - i\hbar \bar{\nabla} \cdot \mathbf{A} | i \rangle \right|^2 \delta(E_f - E_i - h\nu)$$

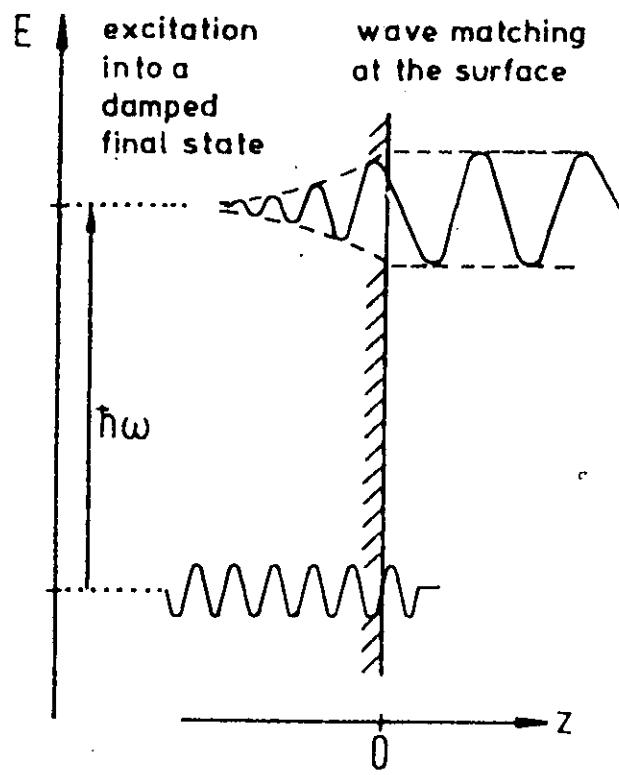
$$\text{with } \bar{\nabla} \cdot \mathbf{A} = 0$$

$$W \propto \left| \langle f | \mathbf{A} \cdot \mathbf{P} | i \rangle \right|^2 \delta(E_f - E_i - h\nu)$$

Dipole Matrix Element

$$\langle f | \mathbf{A} \cdot \mathbf{P} | i \rangle$$

# One Step Model

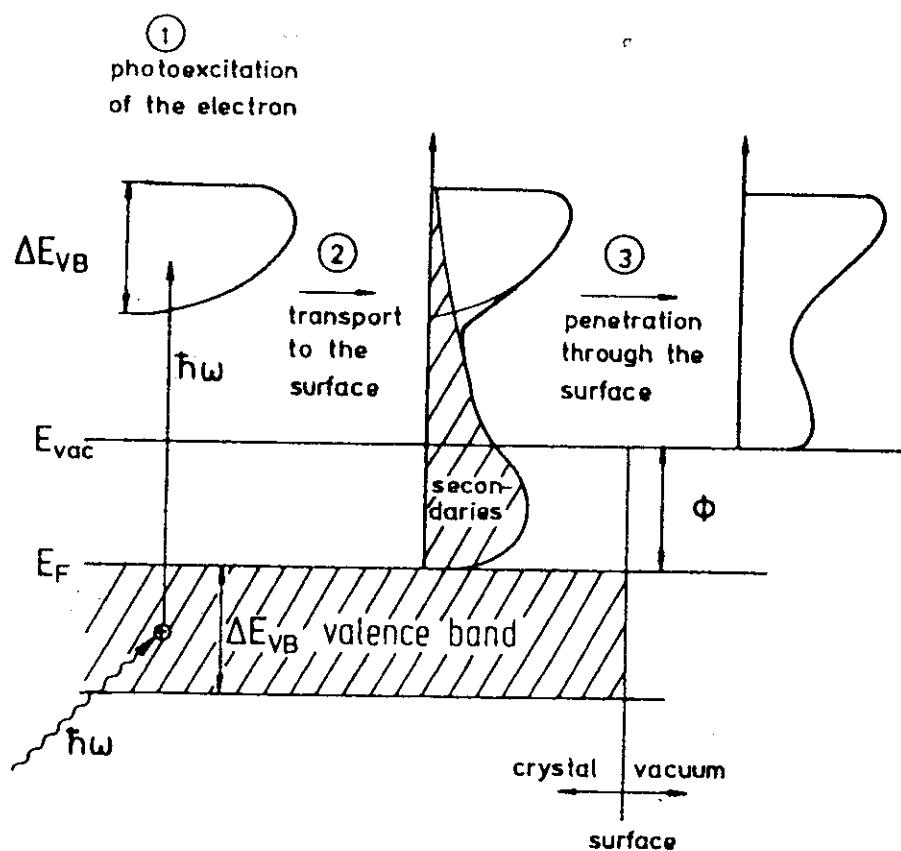


$|i\rangle$  Bloch state in solid

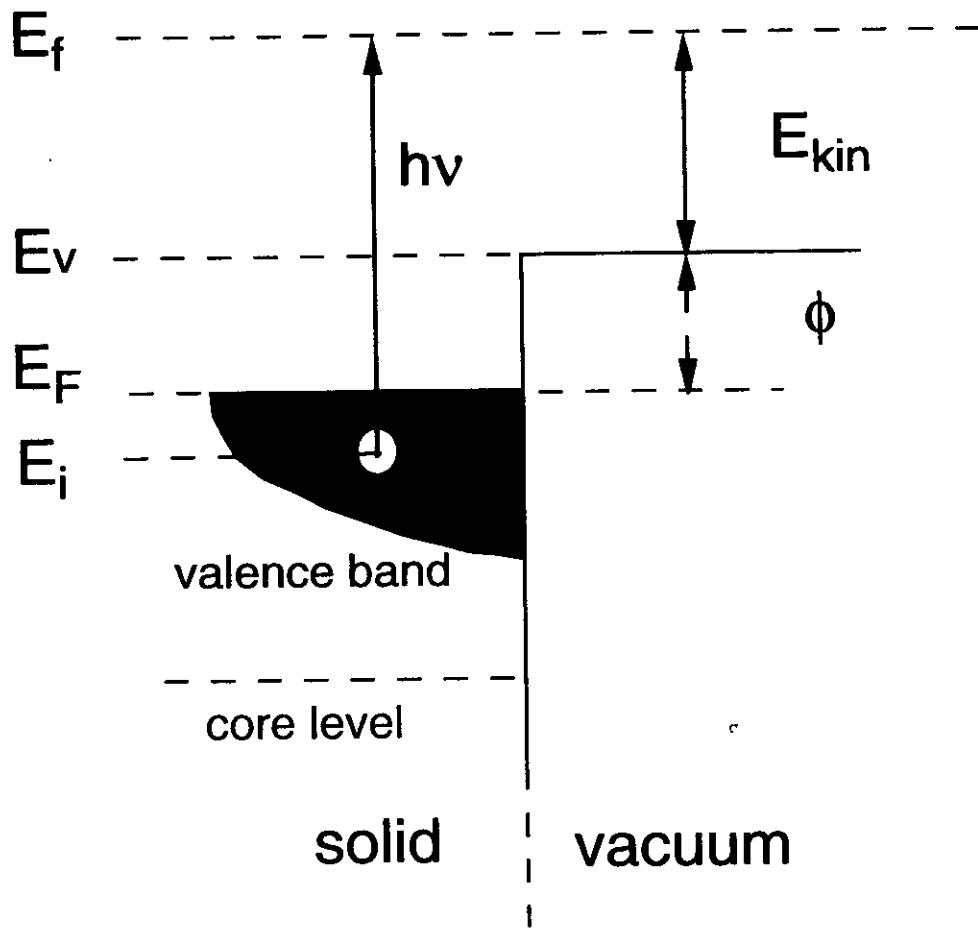
$|f\rangle$  freely propagating wave in vacuum

# The Three Step Model

- 1) photoexcitation
- 2) transport to the surface
- 3) escape into vacuum



# Energy Conservation

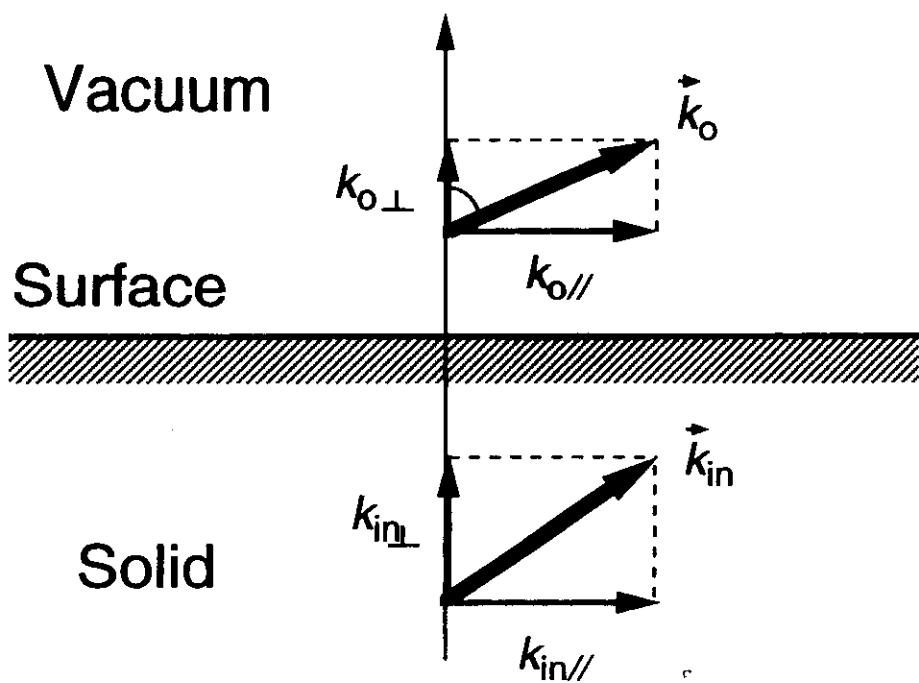


$$E_f = E_i + h\nu$$

$$E_{kin} = h\nu - E_B - \phi$$

$$E_B = E_F - E_i$$

## Momentum Conservation

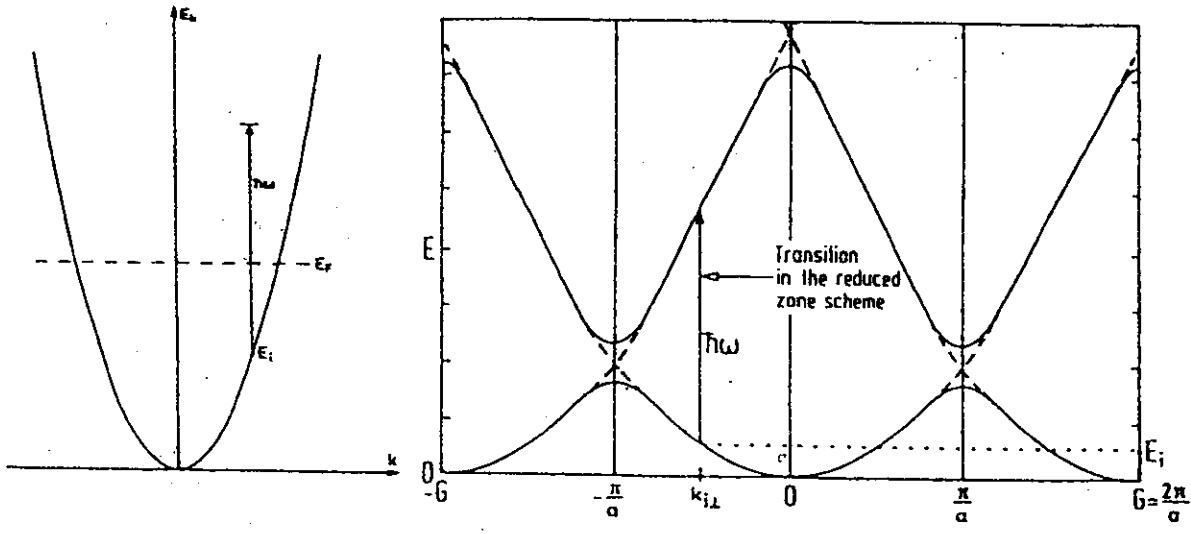


Periodic crystal structure :

$$k_{in//} = k_{o//}$$

$$k_{o//} = \frac{1}{\hbar} \sqrt{2 m E_{kin}} \sin \theta$$

# Momentum Conservation : Direct Transitions

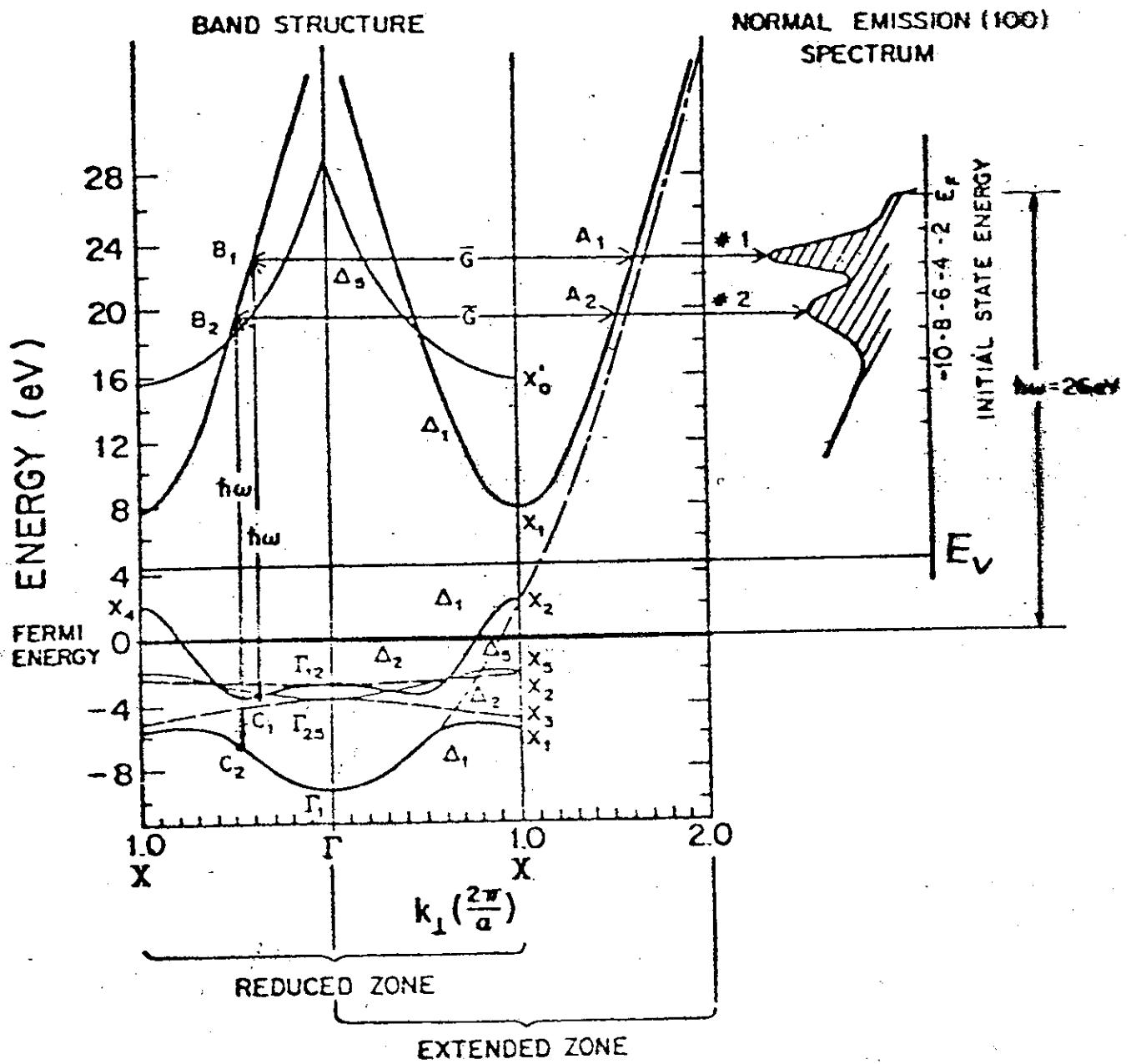


free electron

nearly free electron in a solid

$$\mathbf{k}_f = \mathbf{k}_i \pm \vec{\mathbf{G}}$$

# Direct Transitions in Solids



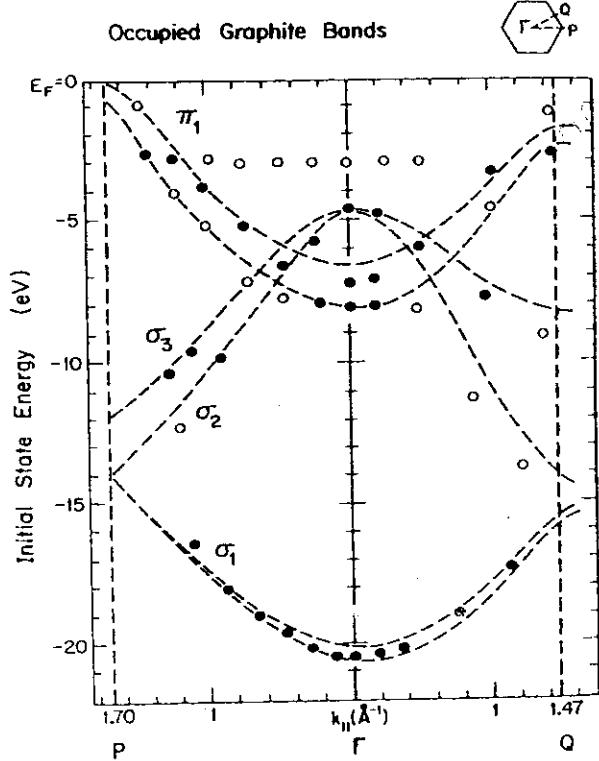
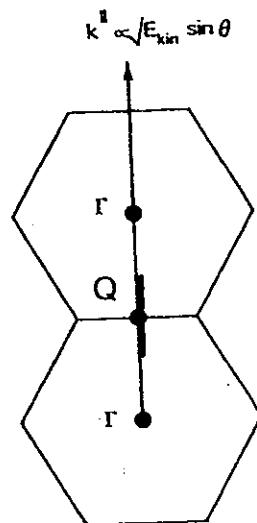
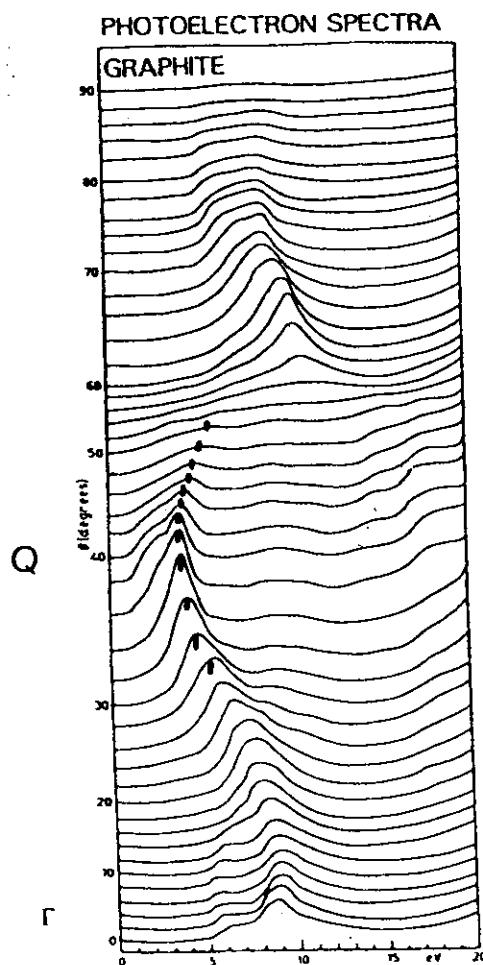
$$\mathbf{k}_f = \mathbf{k}_i + \vec{\mathbf{G}}$$

## Two-dimensional states: $E = E(k_{\parallel})$

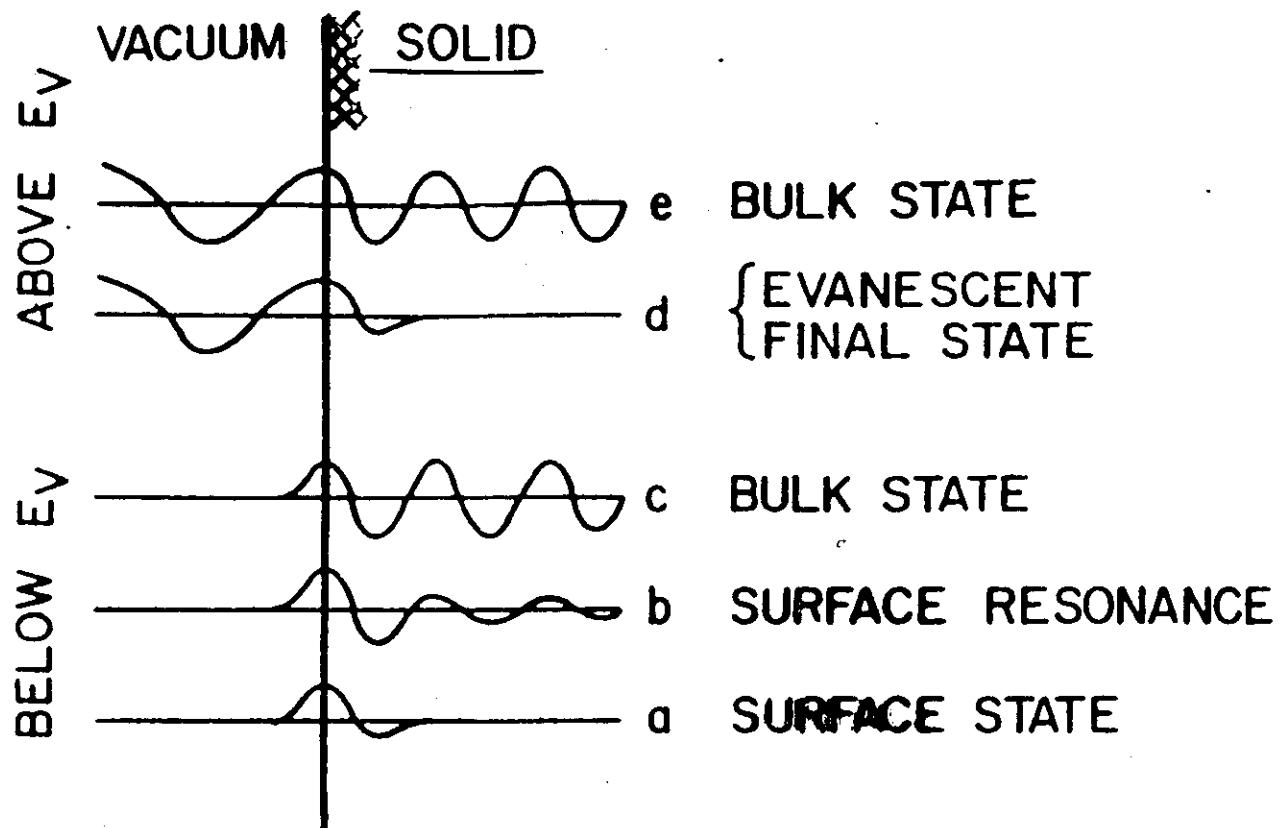
electrons confined in 2-D:

layered materials  
surfaces  
surface adsorbates  
thin films

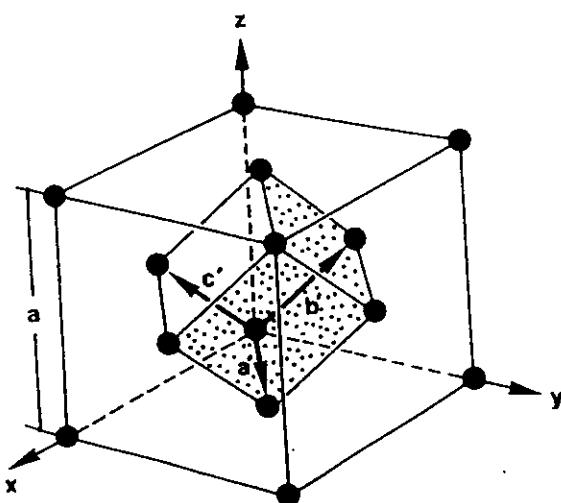
$$k_{in//} = k_{o//} = \frac{1}{\hbar} \sqrt{2mE_{kin} \sin \theta}$$



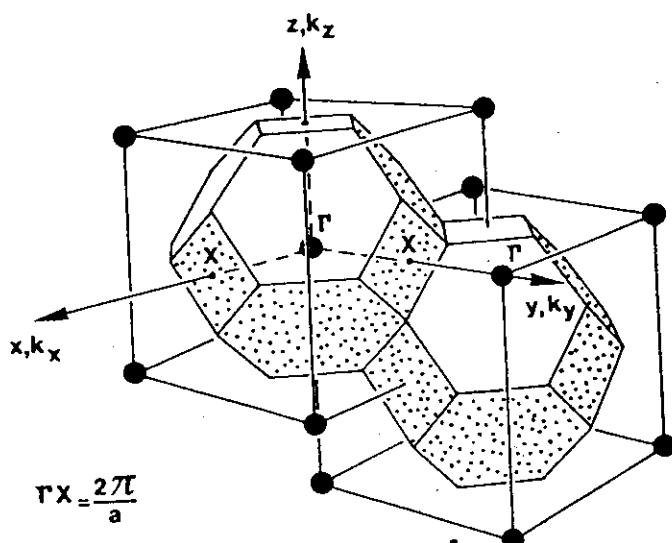
## WAVE FUNCTIONS AT THE SURFACE



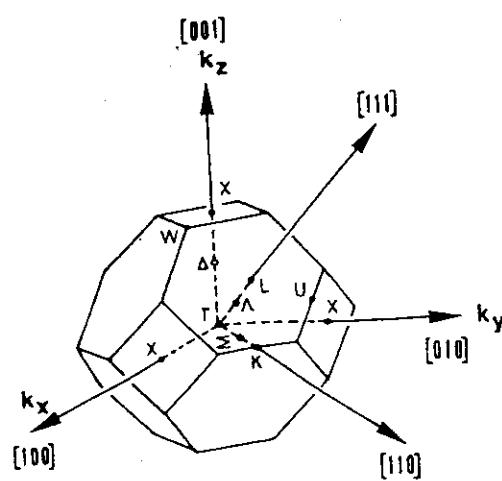
# Face Centered Cubic Structure



Real Space

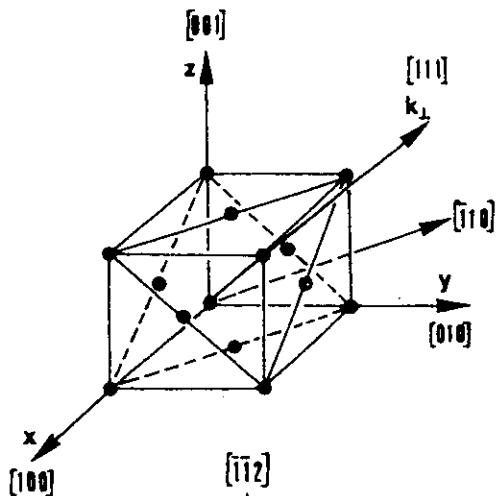


Reciprocal Space  
(and Brillouin Zone)

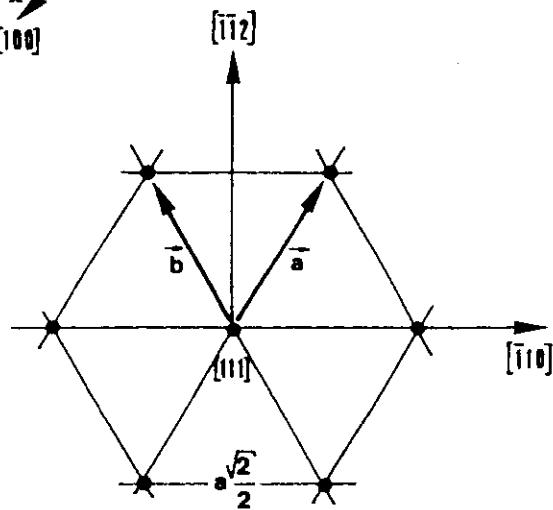


1st Brillouin Zone  
(and high symmetry directions)

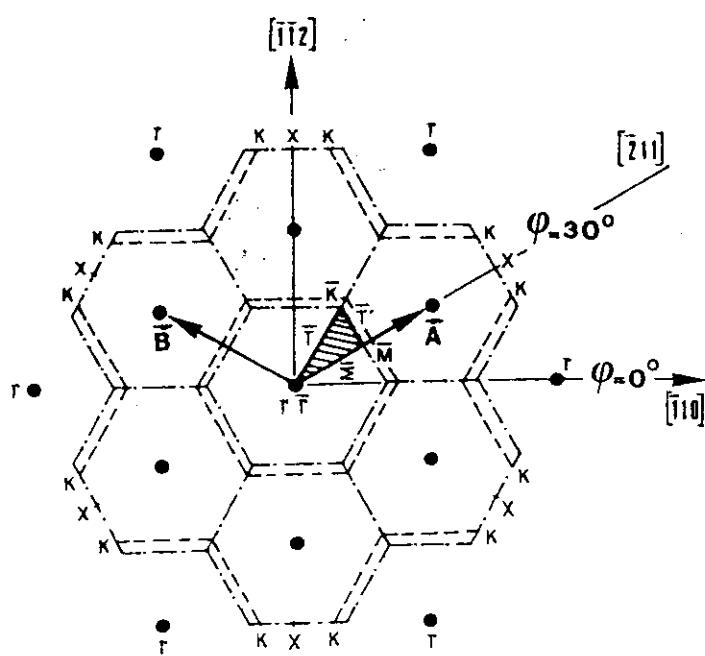
# Face Centered Cubic Structure



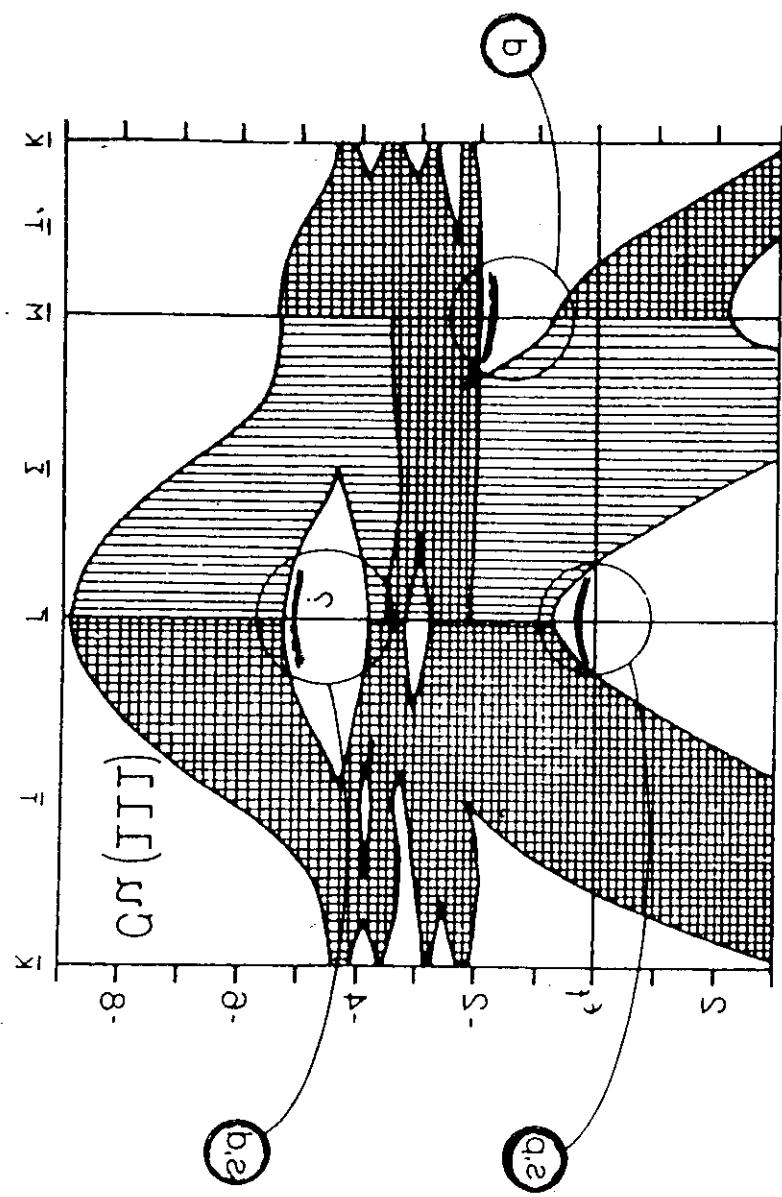
Real Space  
(111) Face



(111) Surface

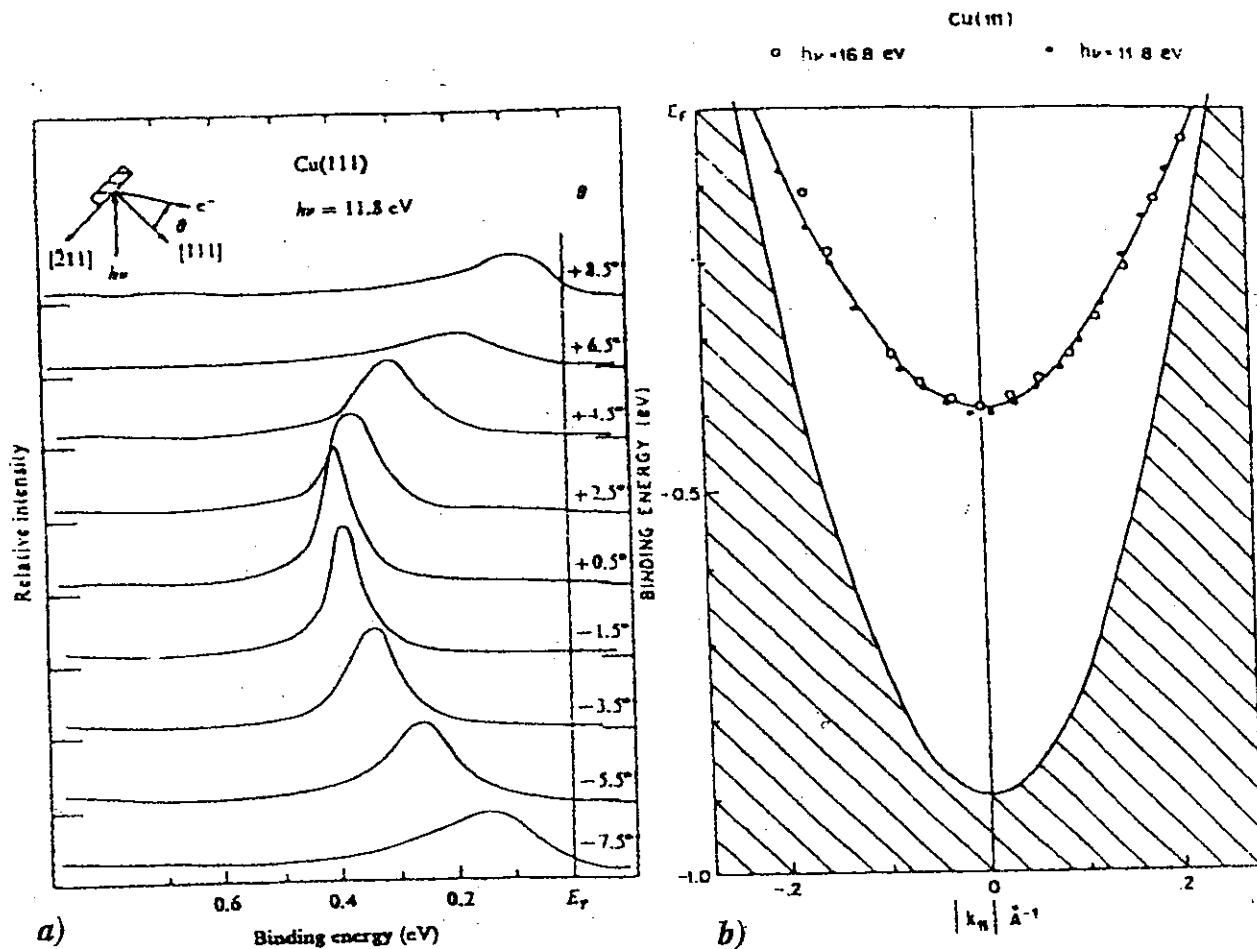


Reciprocal  
Surface Lattice  
*1st Surface  
Brilloiinn Zone*



(v) ELETTRONI IDRAZANE

# Cu(111): Surface State Band

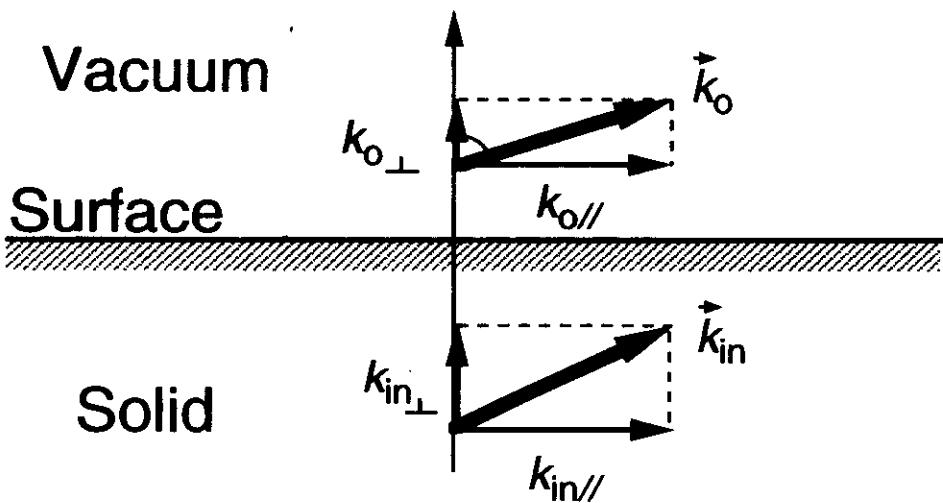


$$k_{\text{in}/\parallel} = k_{0/\parallel} = \frac{1}{\hbar} \sqrt{2m E_{\text{kin}}} \sin \theta$$

# PHYSICS TODAY

NOVEMBER 1993

# 3-D System: $E = E(\vec{k})$

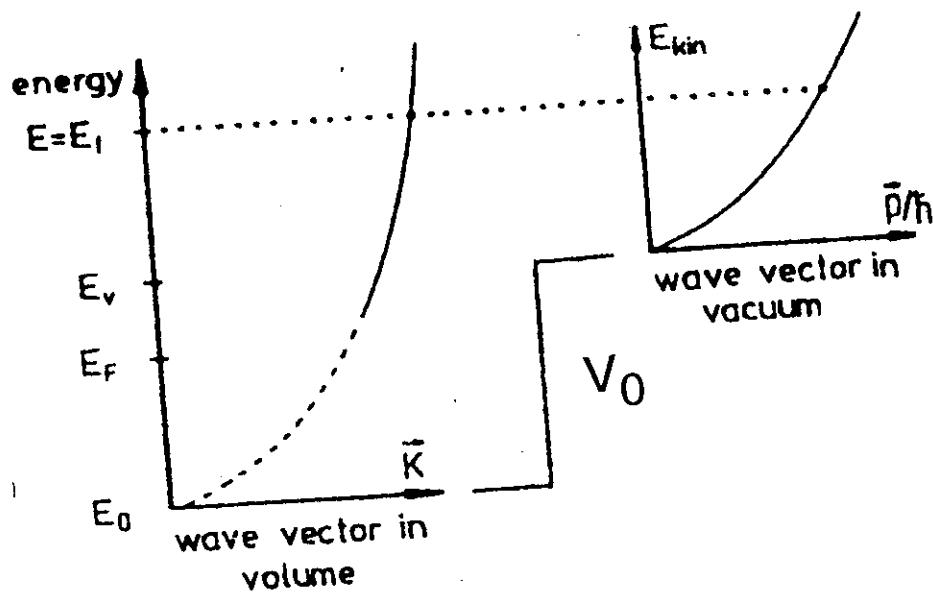


$$k_{in//} = k_{o//} = \frac{1}{\hbar} \sqrt{2 m E_{kin}} \sin \theta$$

$$k_{in\perp} \neq k_{o\perp} = \frac{1}{\hbar} \sqrt{2 m E_{kin}} \cos \theta$$

how to determine  $k_{i\perp}$ ?

## Free electron final states



$$E_{\text{kin}} = \frac{\hbar^2}{2m} (k_{0\parallel}^2 + k_{0\perp}^2) = \frac{\hbar^2}{2m} (k_{\text{in}\parallel}^2 + k_{\text{in}\perp}^2) - V_0$$

substituting :

$$k_{0\parallel} = k_{\text{in}\parallel} \quad k_{0\perp} = \frac{1}{\hbar} \sqrt{2m E_{\text{kin}} \cos \theta}$$



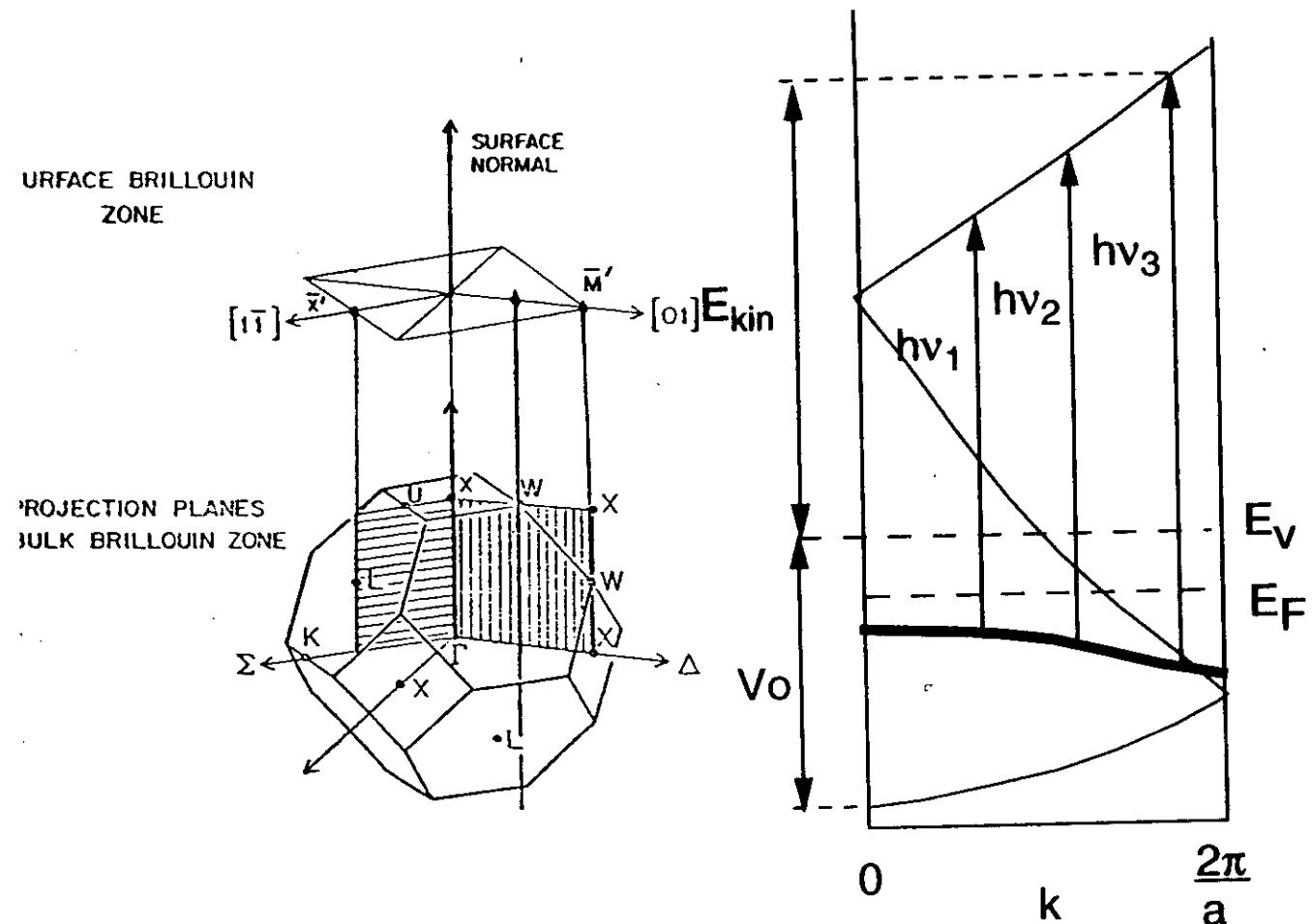
$$k_{\text{in}\perp} = \sqrt{k_{0\perp}^2 + \frac{2mV_0}{\hbar^2}}$$

$$= \frac{\sqrt{2m}}{\hbar^2} \sqrt{E_{\text{kin}} \cos^2 \theta + V_0}$$

- 25 -

# Band Mapping

Example : normal emission



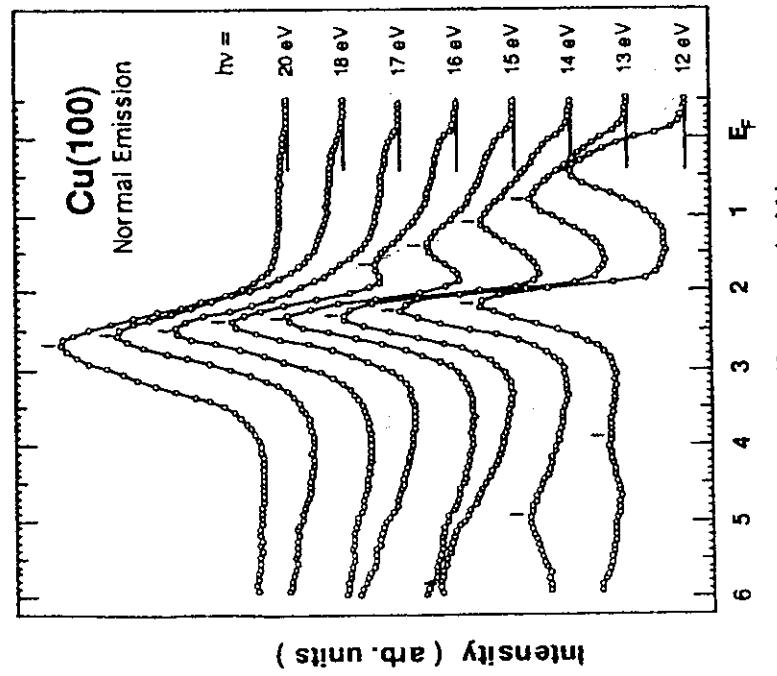
$$k_{0//} = k_{in//} = 0$$

$$k_{in\perp} = \frac{\sqrt{2m}}{\hbar^2} \sqrt{E_{kin} + V_0} \quad (\pm \vec{G})$$

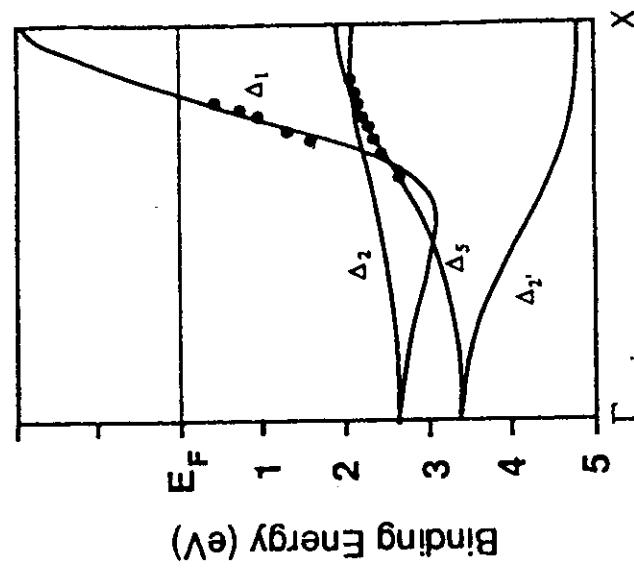
$$\frac{\sqrt{2m}}{\hbar^2} \sqrt{E_i + h\nu - \phi + V_0} \quad (\pm \vec{G})$$

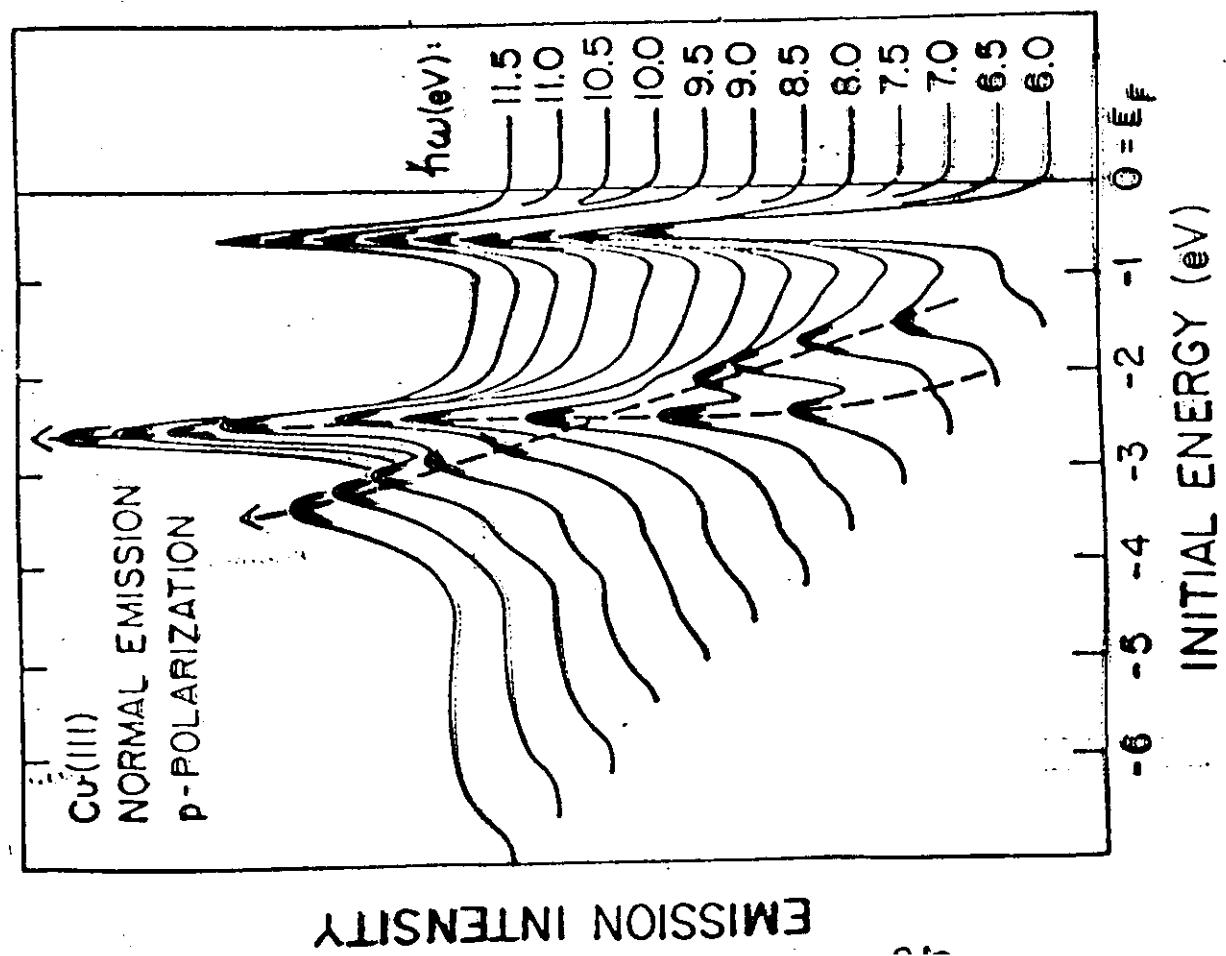
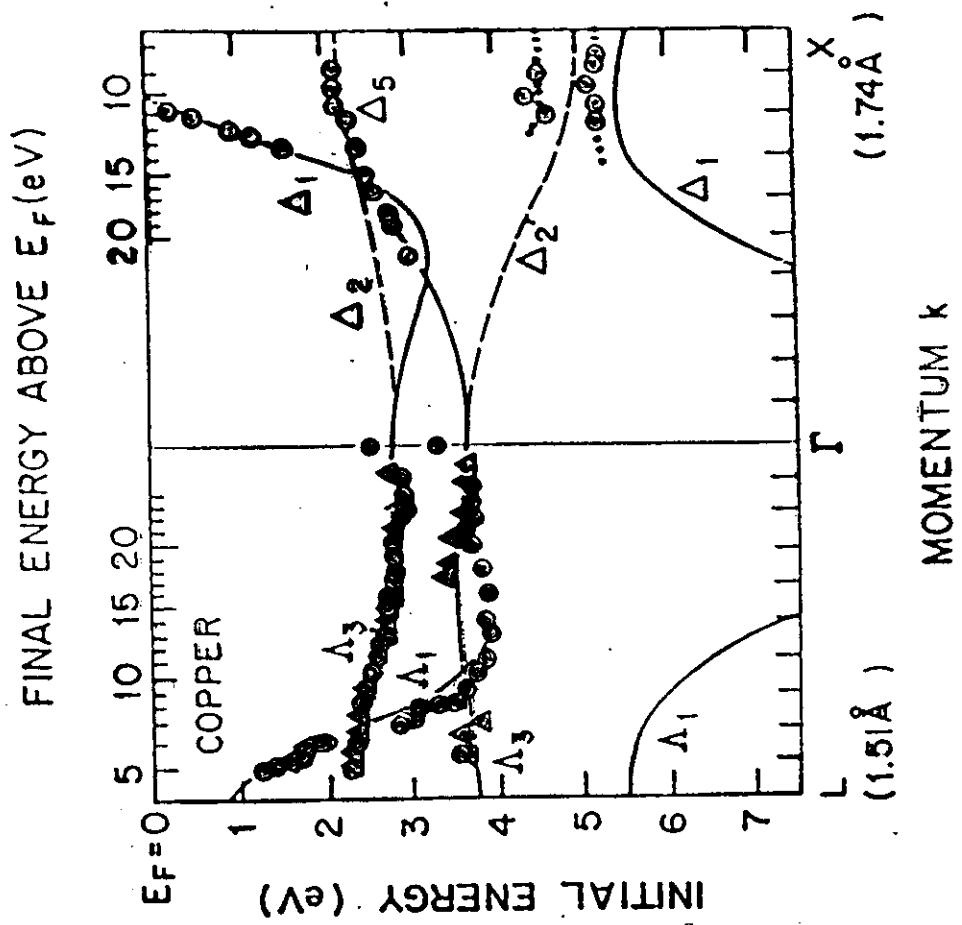
# Photoemission from Cu (100)

Spectra vs. Photon Energy



Band dispersion.



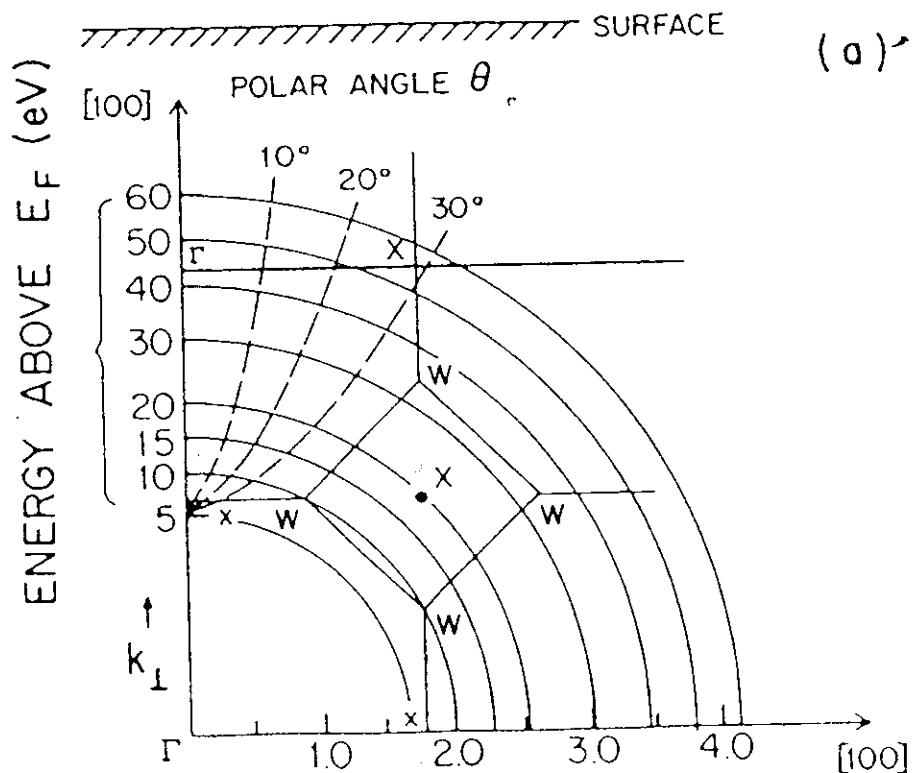


# Band Mapping

The general case : off-normal emission

$$k_{in//} = k_{0//} = \frac{\sqrt{2m}}{\hbar^2} \sqrt{E_{kin} \sin^2 \theta}$$

$$k_{in\perp} = \frac{\sqrt{2m}}{\hbar^2} \sqrt{E_{kin} \cos^2 \theta + V_0}$$



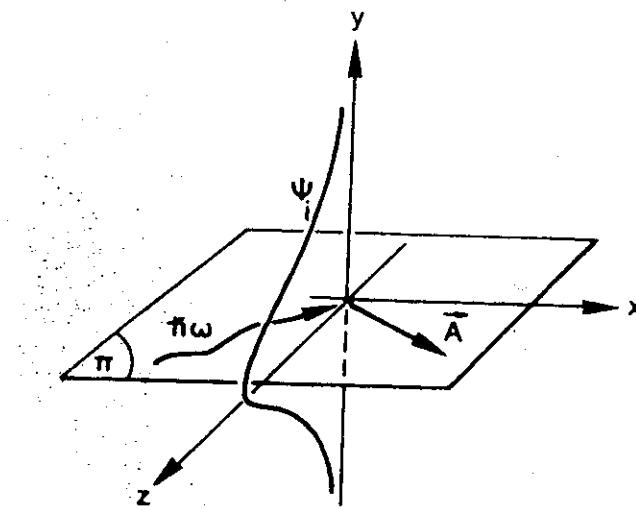
$$k_{11} (\text{\AA}^{-1})$$

Free electron final state : circles     $E = \frac{\hbar^2}{2m} (k_{in//}^2 + k_{in\perp}^2)$

# Symmetry selection rules

$$\langle f | \mathbf{A} \cdot \mathbf{P} | i \rangle$$

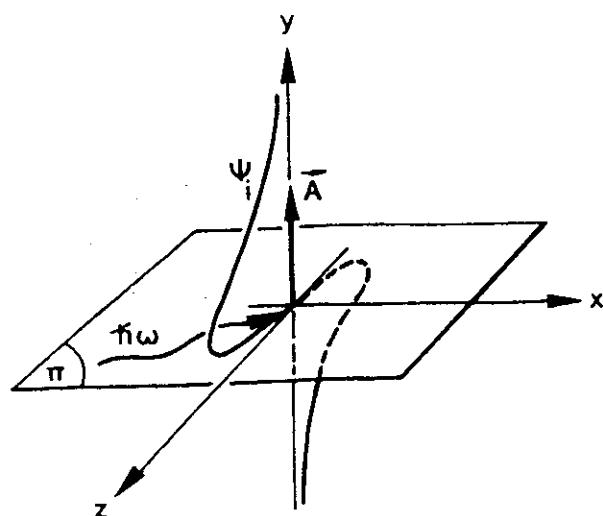
Emission in a mirror plane :  $\langle f | \equiv g$   
 (detector in mirror plane)  $| i \rangle \equiv g$



$$\mathbf{A} \parallel \pi$$

$$\mathbf{A} \cdot \mathbf{P} \equiv g$$

$$| i \rangle \equiv g$$

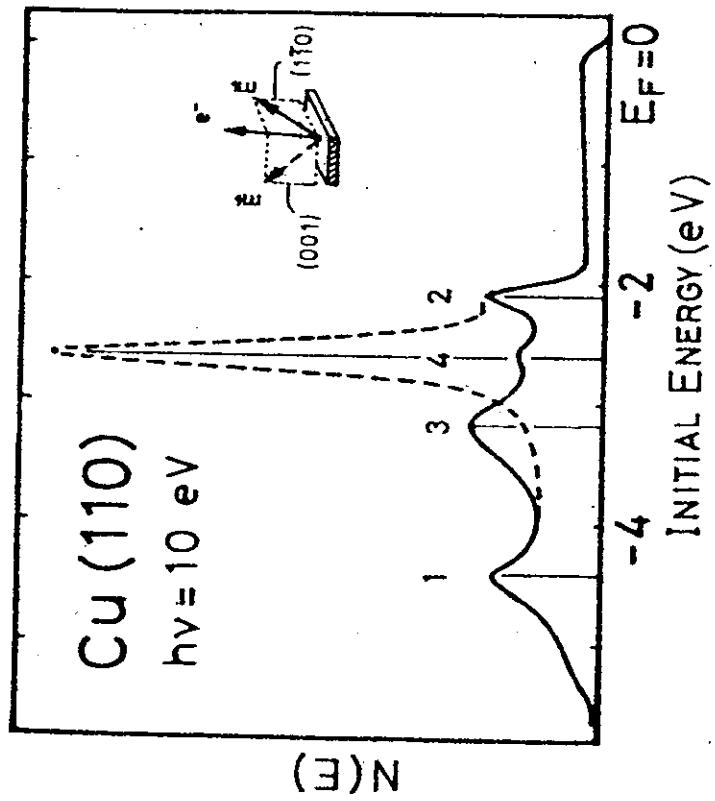


$$\mathbf{A} \perp \pi$$

$$\mathbf{A} \cdot \mathbf{P} \equiv u$$

$$| i \rangle \equiv u$$

POLARIZATION SELECTION RULES

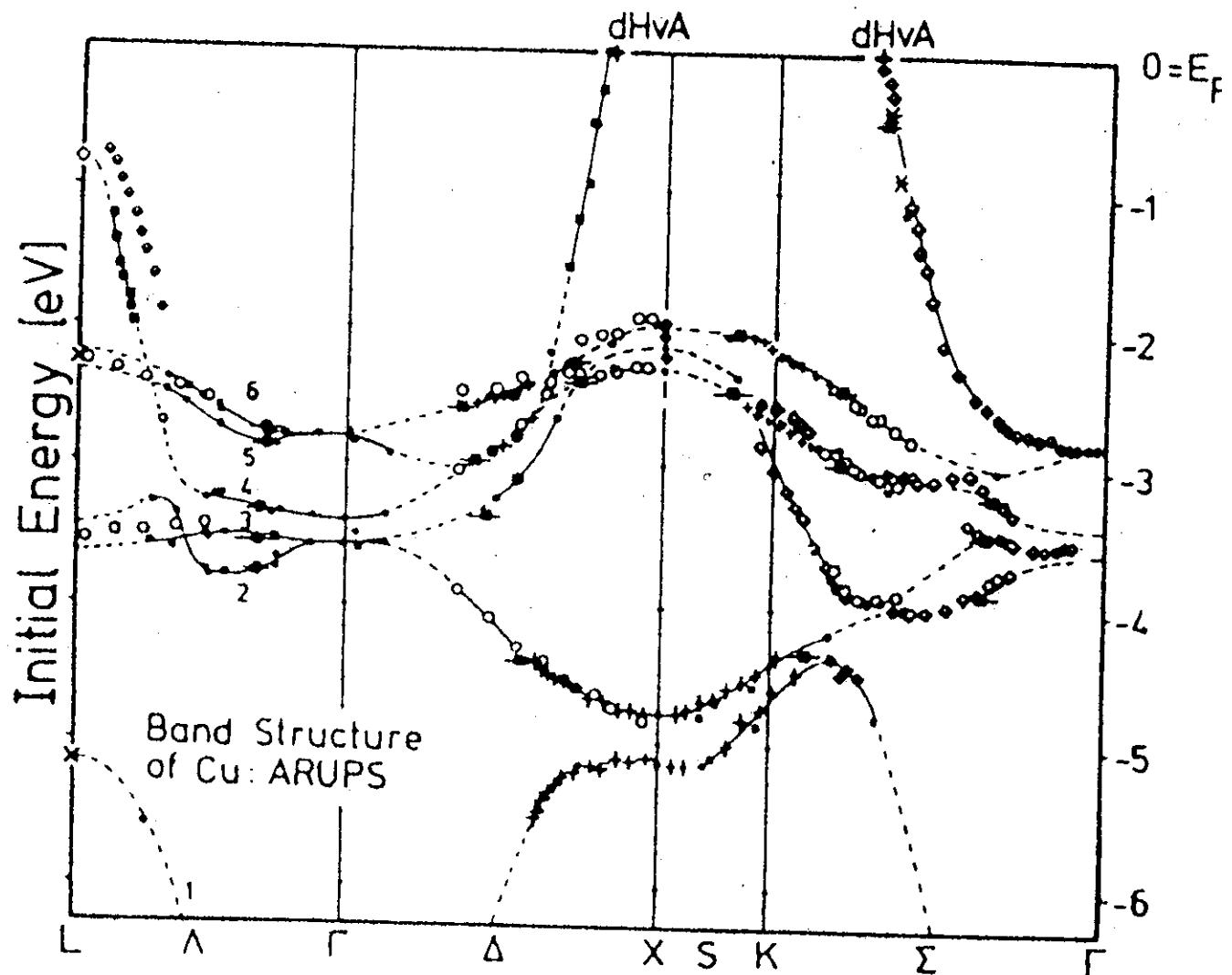


Kristall- Koordinaten Achsen  
fläche      irreduzierbare  
            Darstellungen

Symmetrie des  
Anfangszustandes

	$A  x$	$A  y$	$A  z$
(001)	$<100>$	$<010>$	$<001>$
(110)	$<001>$	$<110>$	$<110>$
(111)	$<110>$	$<112>$	$<111>$

# Cu Bandstructure

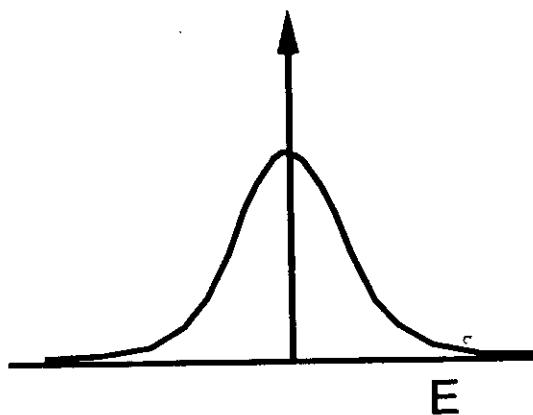


## Beyond the single particle picture

electron and hole lifetime

e.g. Lifetimebroadening of the „initial state“ :

$$\delta(E_f - E_i - h\nu) \longrightarrow \frac{1}{\pi} \frac{\Gamma_i}{(E_f - E_i - h\nu)^2 + \Gamma_i^2}$$



+ hole screening (Coulomb interaction)

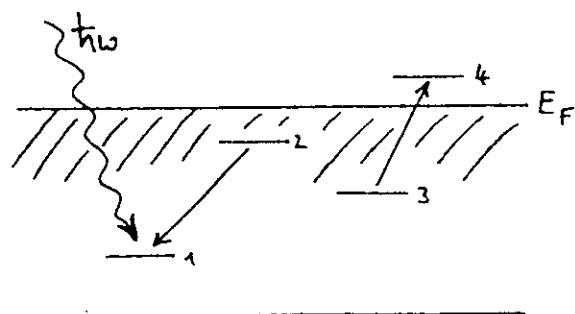
In general : Spectral distribution of the hole state  $A_i(E_f - h\nu)$

$$A_i(E) = \frac{1}{\pi} \frac{\text{Im } \Sigma_i(E)}{(E - E_i - \text{Re } \Sigma_i(E))^2 + (\text{Im } \Sigma_i(E))^2}$$

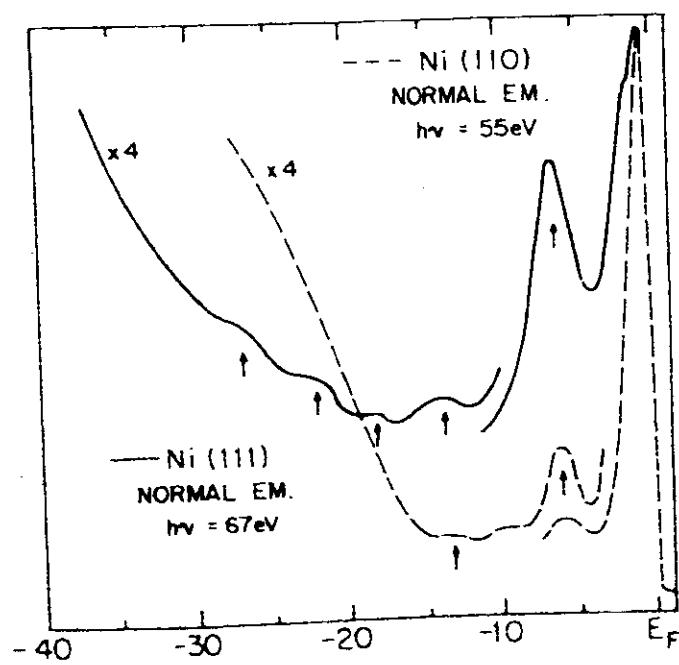
with complex self energy  $\Sigma_i(E)$

Photoemission measures the excitation spectrum !

## Many-body excitations

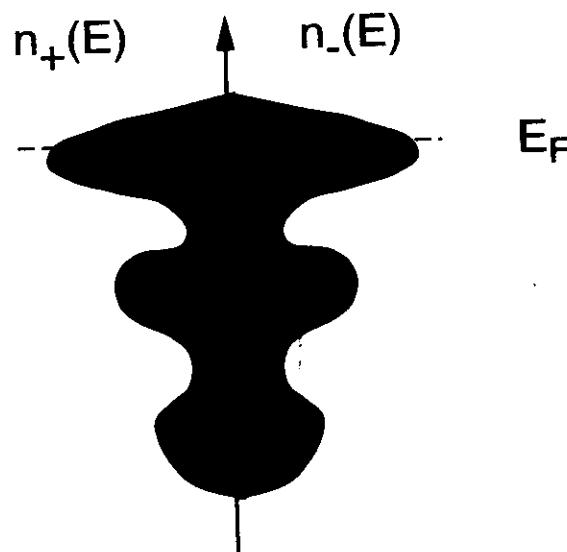


“Satellites” in Ni photoemission spectra



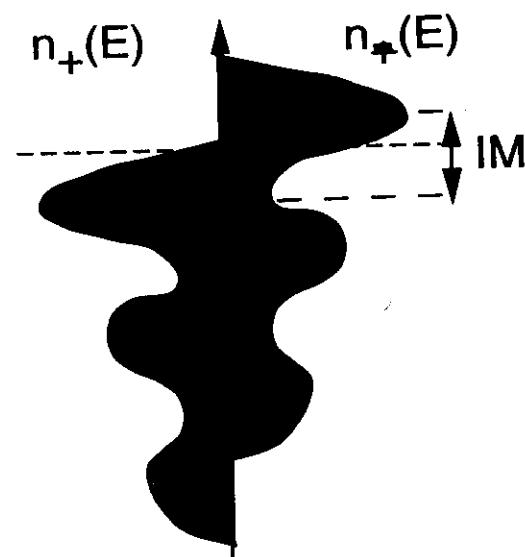
# Stoner Model - Ferromagnetic Electronic Structure

PARAMAGNETIC DOS



$$n_+(E) = n_-(E) = 0.5 n_o(E)$$

FERROMAGNETIC DOS



$$n_{\pm}(E) = n_o(E \pm 0.5 IM)$$

I exchange integral

M local moment

$$M = \int \{ n_+(E) - n_-(E) \} dE$$

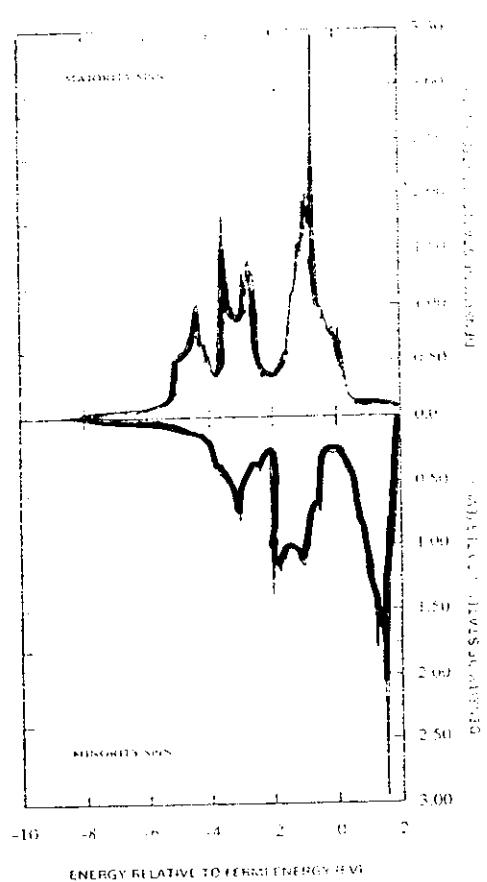
# FERROMAGNETIC METALS

## SPIN DEPENDENT DENSITY OF STATES

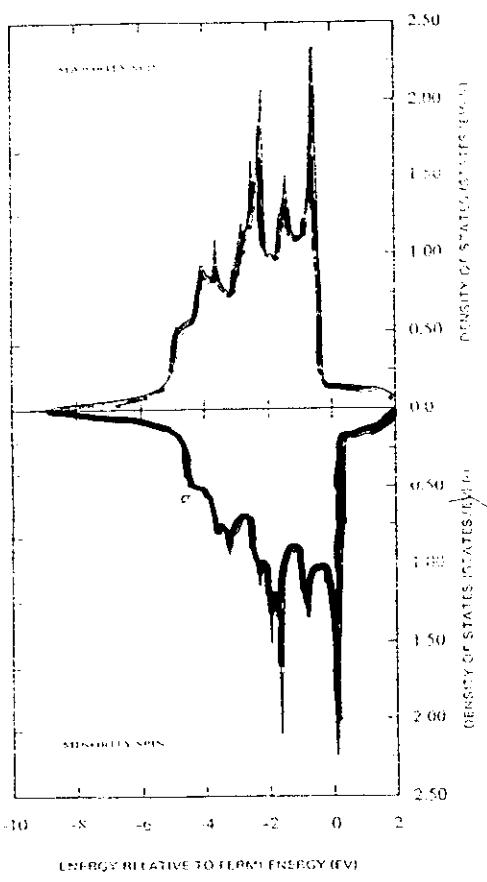
Fe

Ni

Spin-up



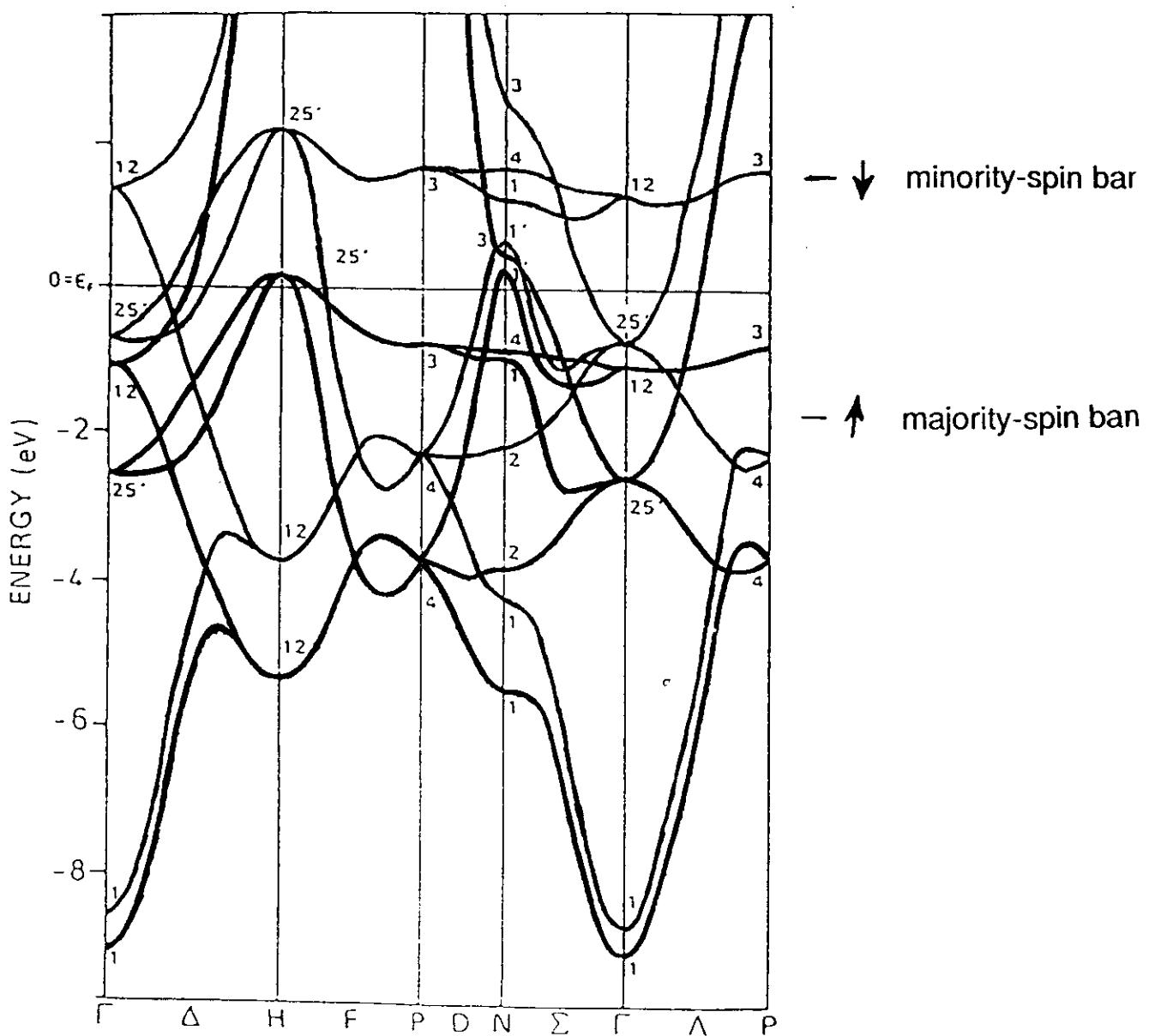
Spin-down



Magnetic Moments [  $\mu_B$  / atom ]

	Fe	Co	Ni
Theory	2.15	1.56	0.59 (spin)
Exp.	2.12	1.57	0.55 (spin)
" (spin+orb.)	2.22	1.71	0.61 (tot.)

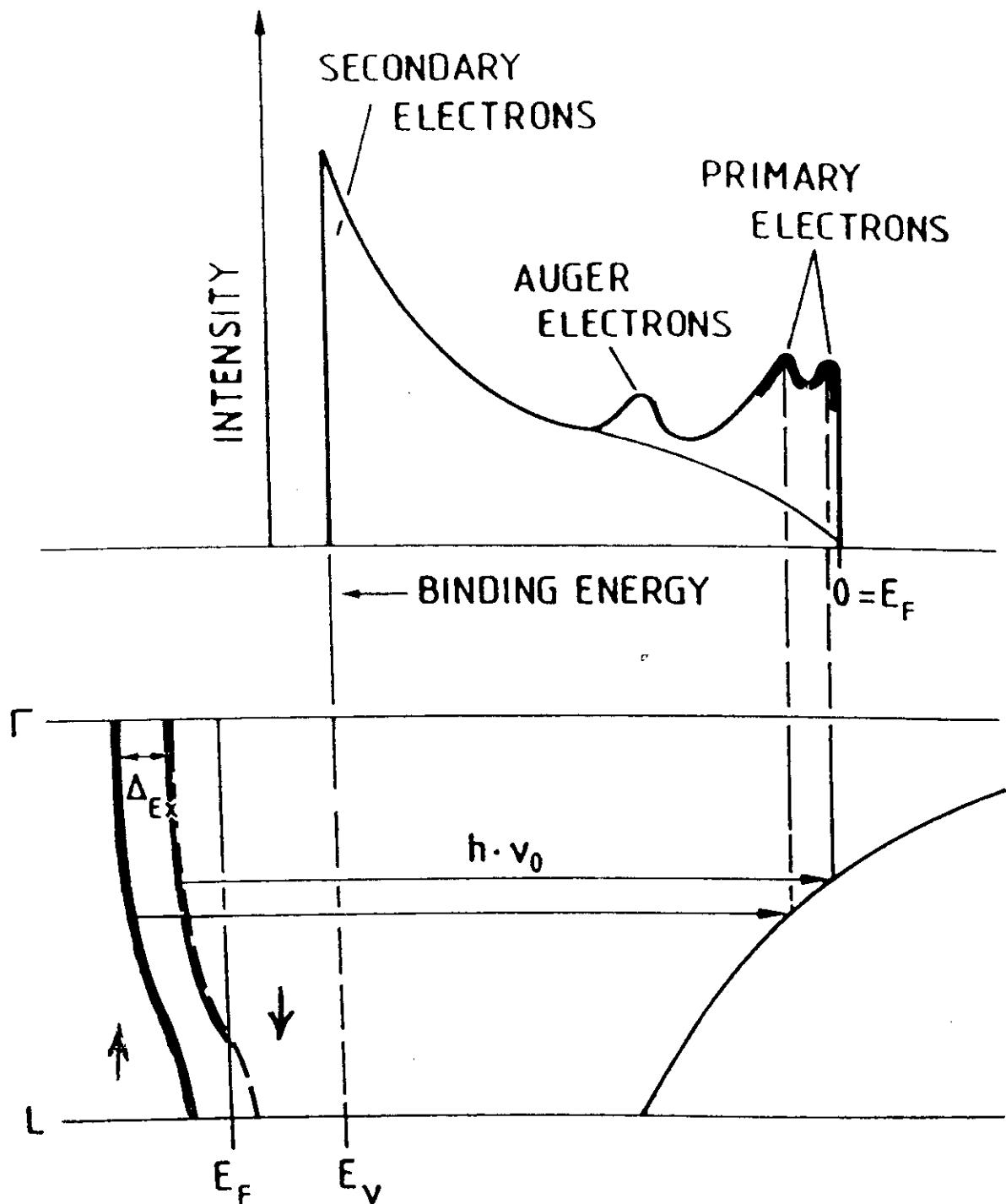
## Fe Band Structure



Calculated bandstructure along high symmetry directions. Hathaway et al PRB 31, 7601 (1985)

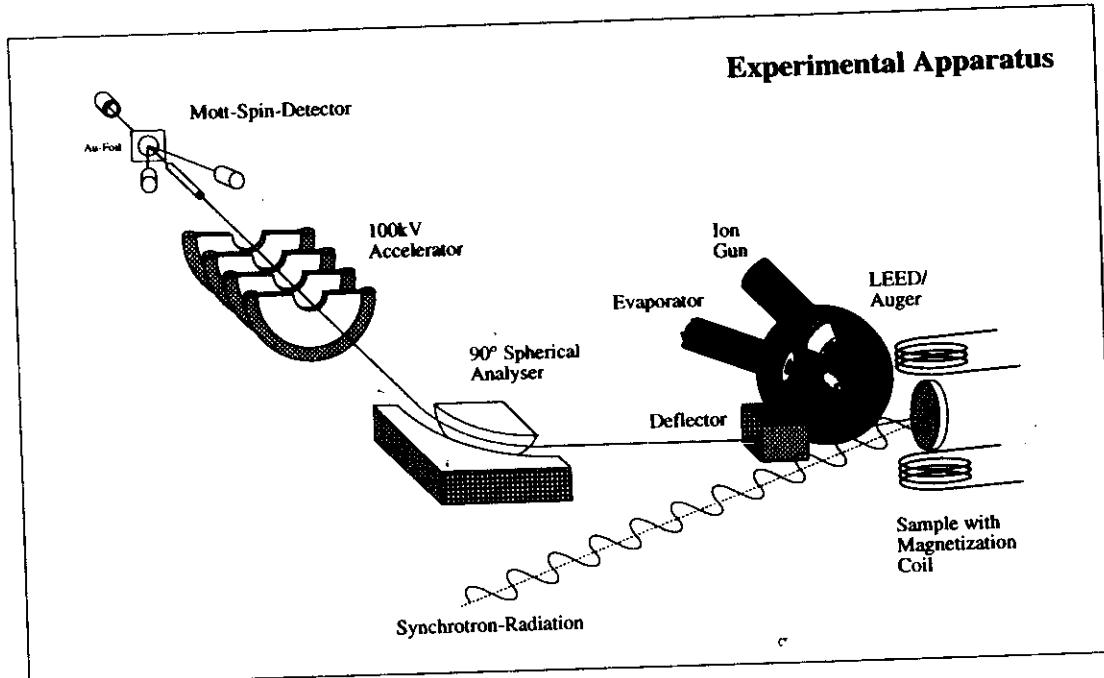
$$E = E(\vec{k}, \bar{\sigma})$$

# Photoelectron Spectroscopy: Principles



{ kinetic energy    ---> binding energy  
 { emission angle    ---> k vector  
 polarization    ---> spin

# Spin- and Angle-Resolved Photoemission



MEASURE :

$E_k$  (kinetic energy)

$\vec{p}$  (momentum)

$\vec{P}$  (polarization)

outside

TO OBTAIN :

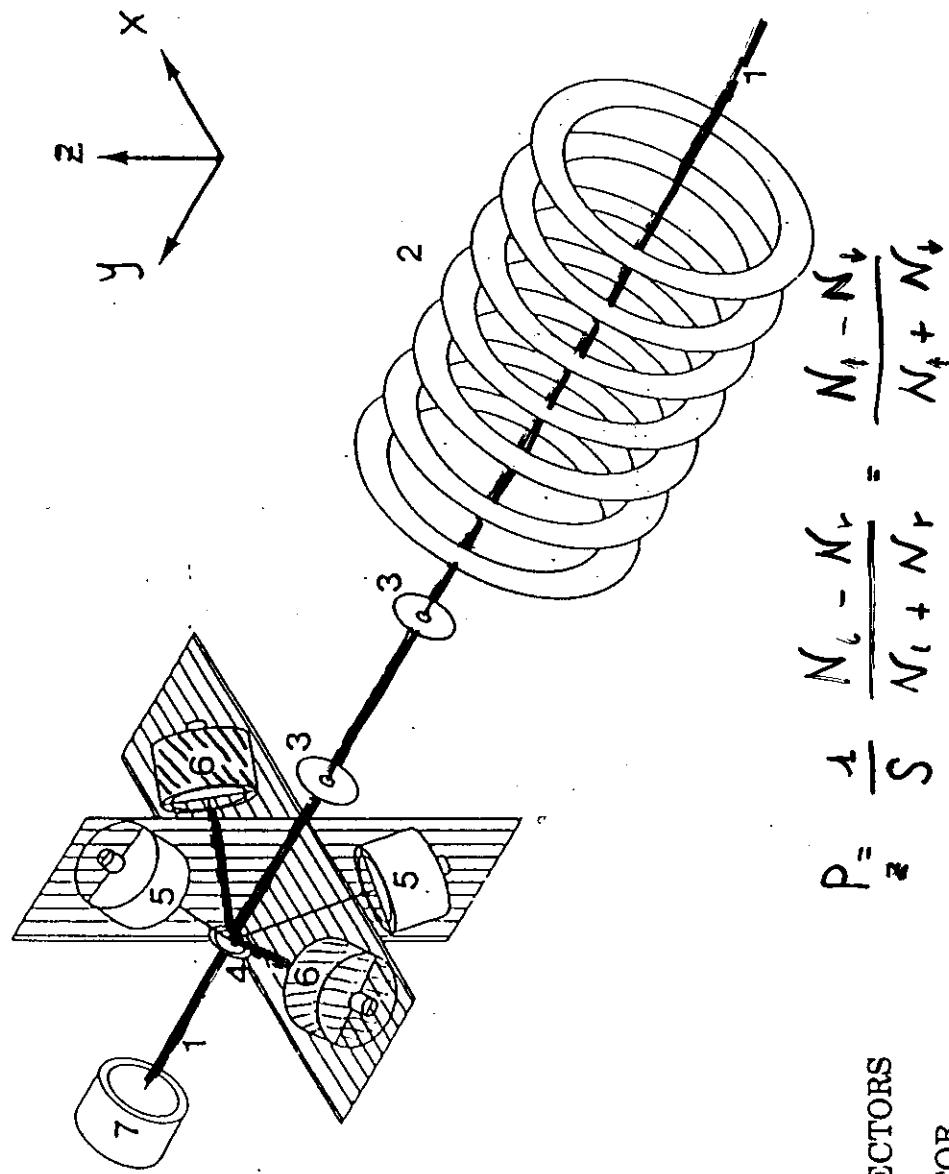
$E_B$  (binding energy)

$\vec{k}_\parallel$  (wave vector)

$\vec{\sigma}$  (spin)

inside

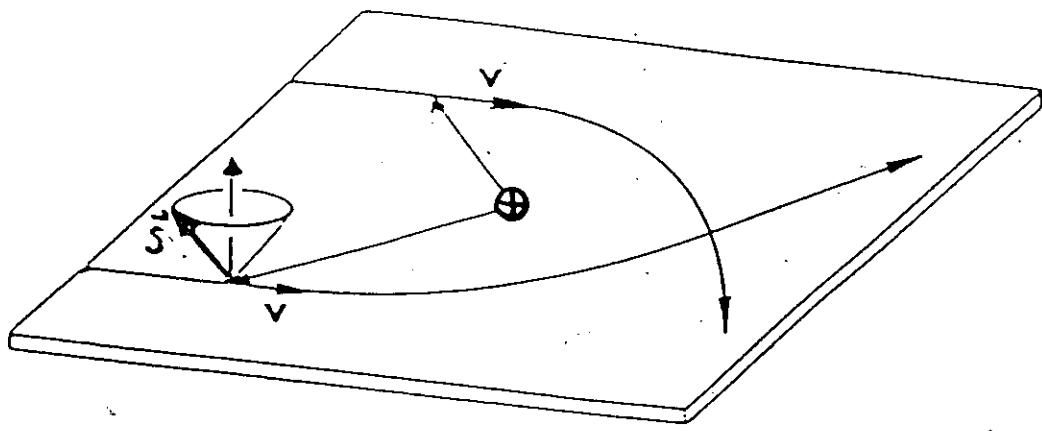
## MOTT DETECTOR



- 1) INCOMING ELECTRON BEAM
- 2) ACCELERATOR (30- 100 KeV)
- 3) COLLIMATOR
- 4) Au TARGET
- 5-6) BACKSCATTERED ELECTRON DETECTORS
- 7) TRANSMITTED ELECTRON DETECTOR

$$\frac{P}{S} = \frac{1}{S} \frac{N_t - N_r}{N_t + N_r} = \frac{N_t - N_r}{N_t + N_r}$$

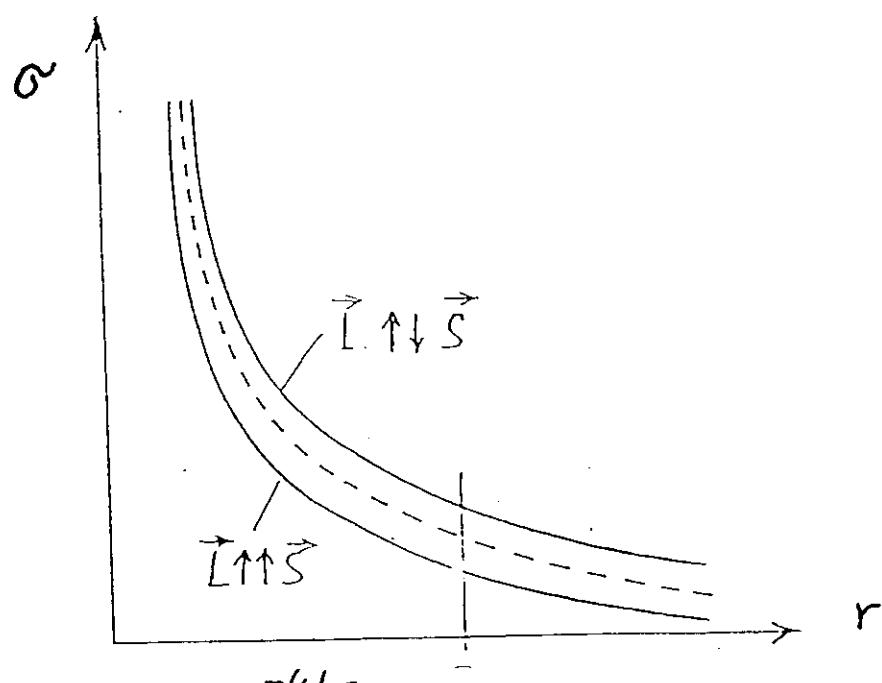
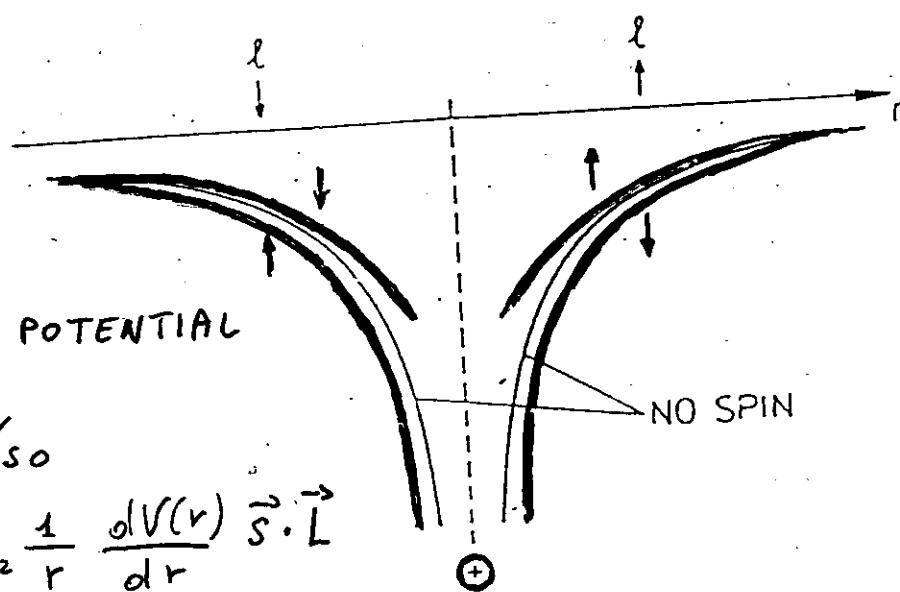
$$M = S^2 \left( \frac{N_t + N_r}{N_t - N_r} \right) \approx 10^{-4}$$



SCATTERING POTENTIAL

$$V = V_0 + V_{SO}$$

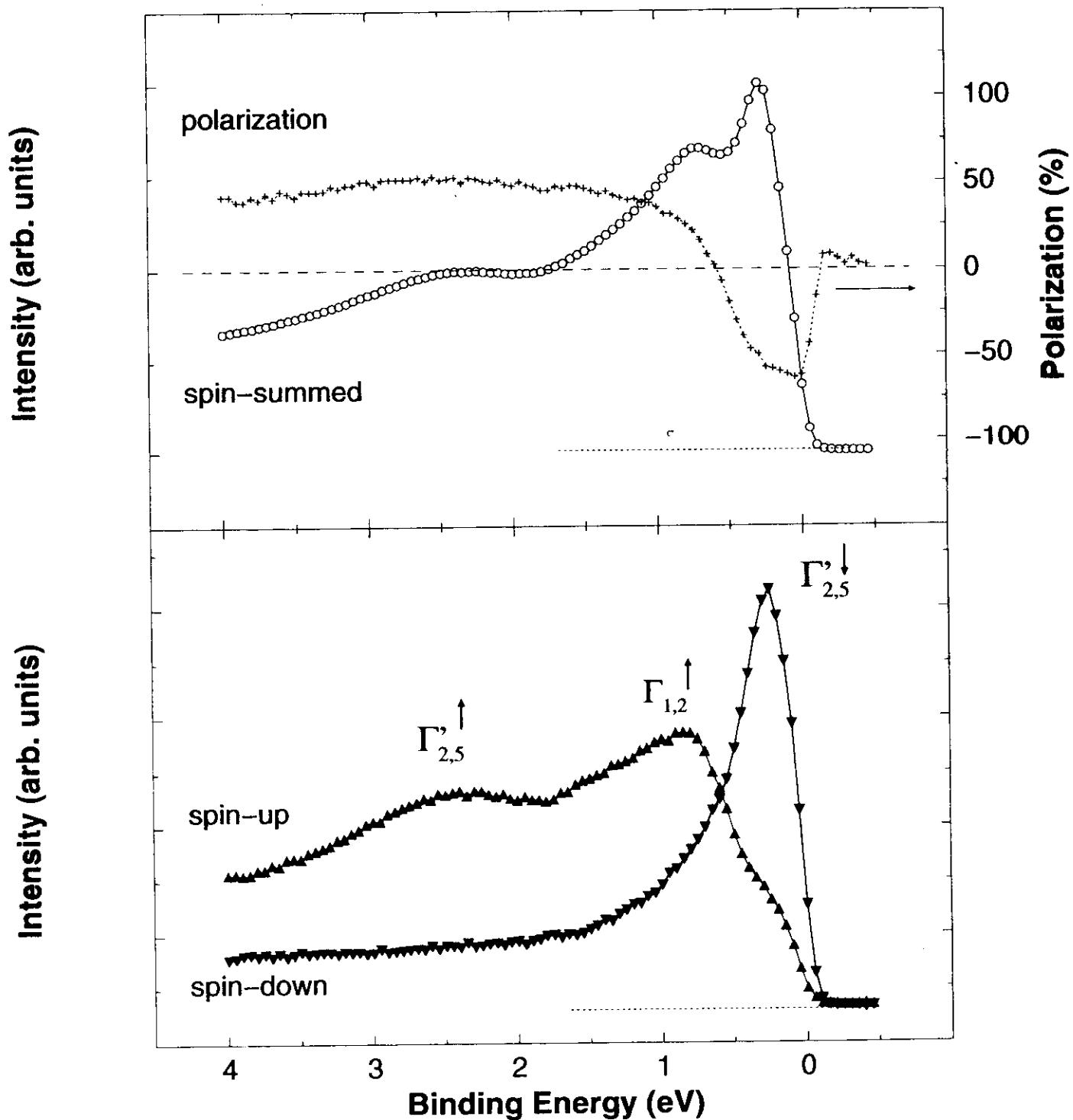
$$V_{SO} = \frac{1}{2m^2c^2} \frac{1}{r} \frac{dV(r)}{dr} \vec{s} \cdot \vec{l}$$



## **Fe(110)**

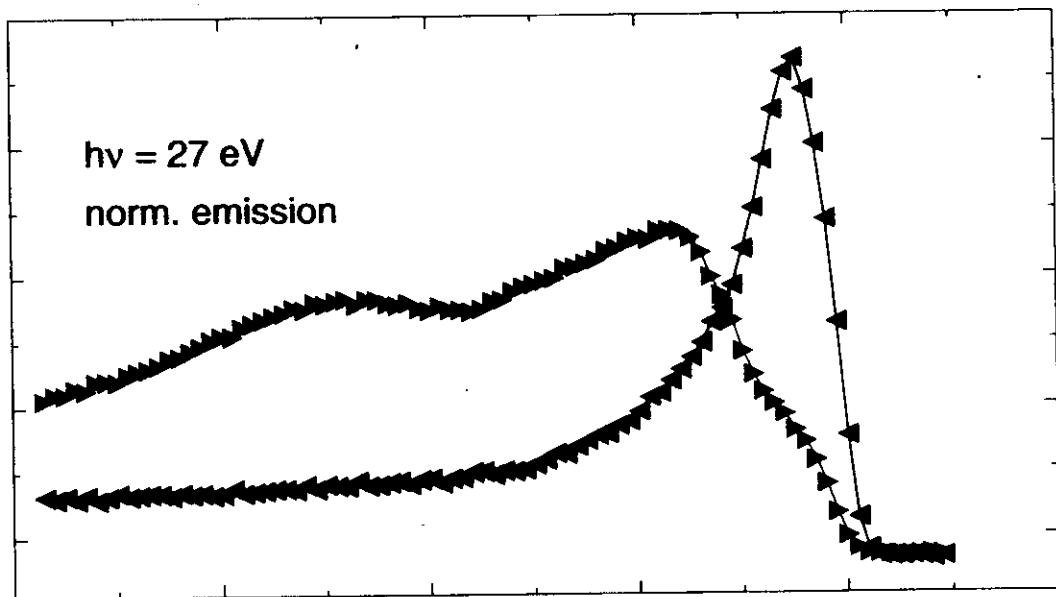
$\hbar\nu = 27 \text{ eV}$  ( $k_{\perp} (E_F) = 0$ )

*norm. emission* ( $k_{||} = 0$ )

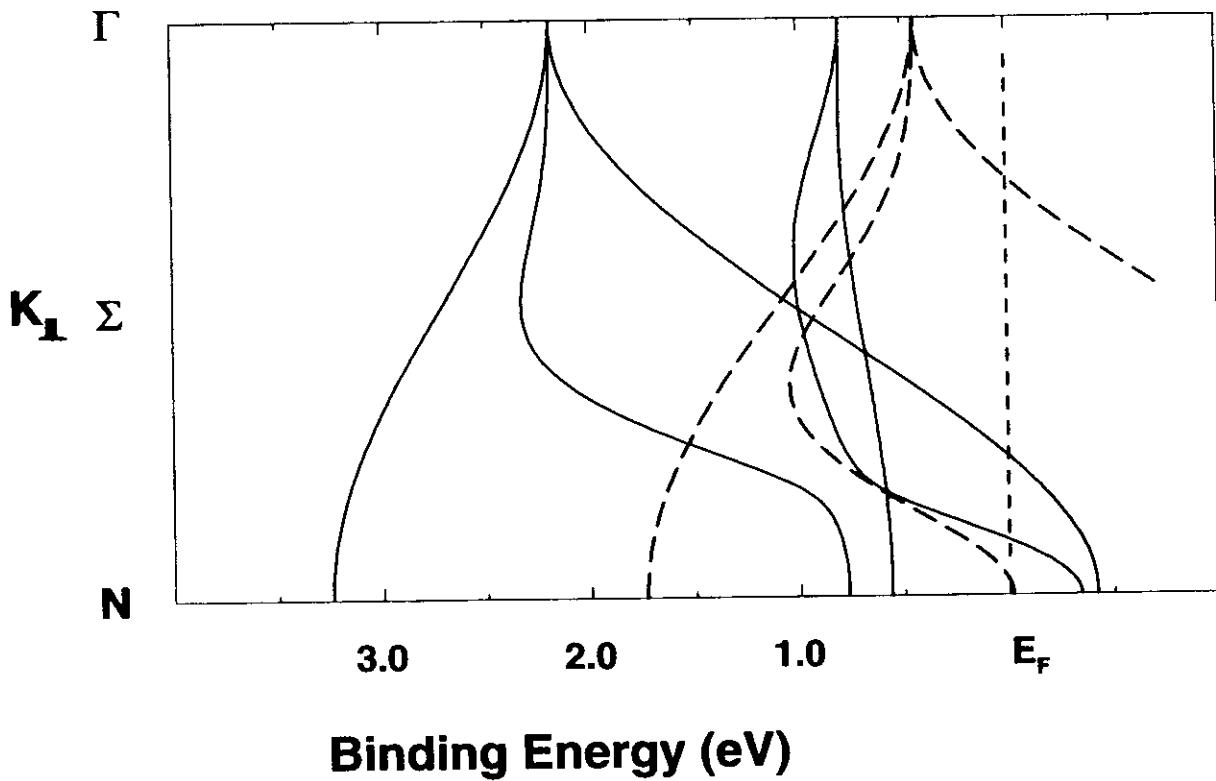


**Fe(110) –  $\vec{M} \parallel [1\bar{1}0]$**

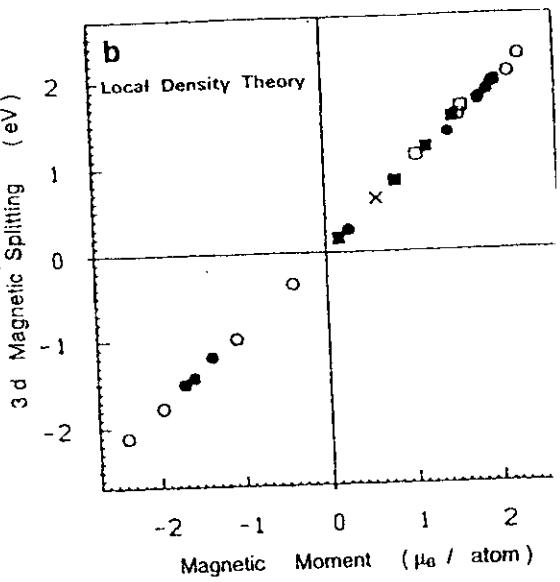
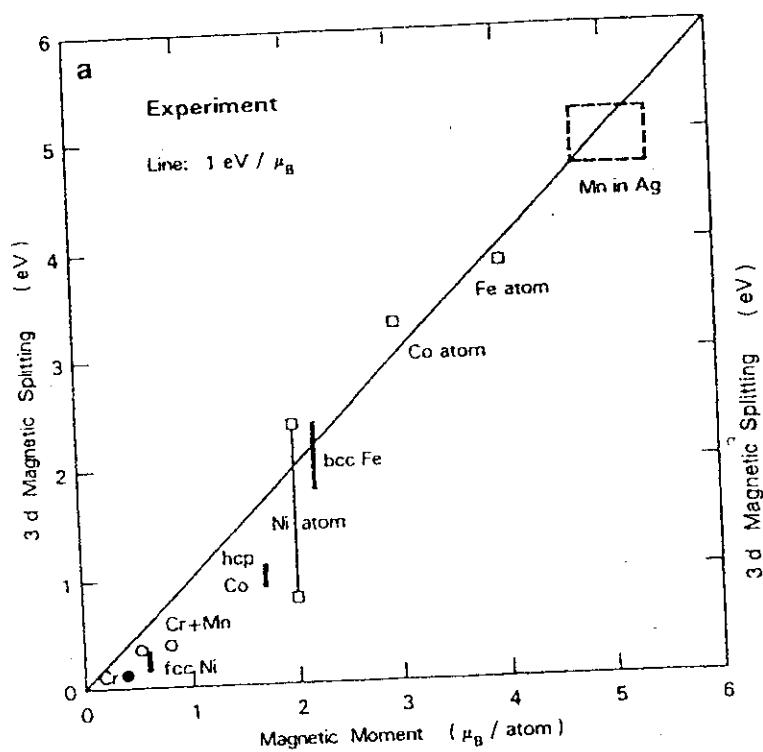
Intensity (arb. units)



$\Gamma_{2,5}$        $\Gamma_{1,2}$        $\Gamma_{2,5}$

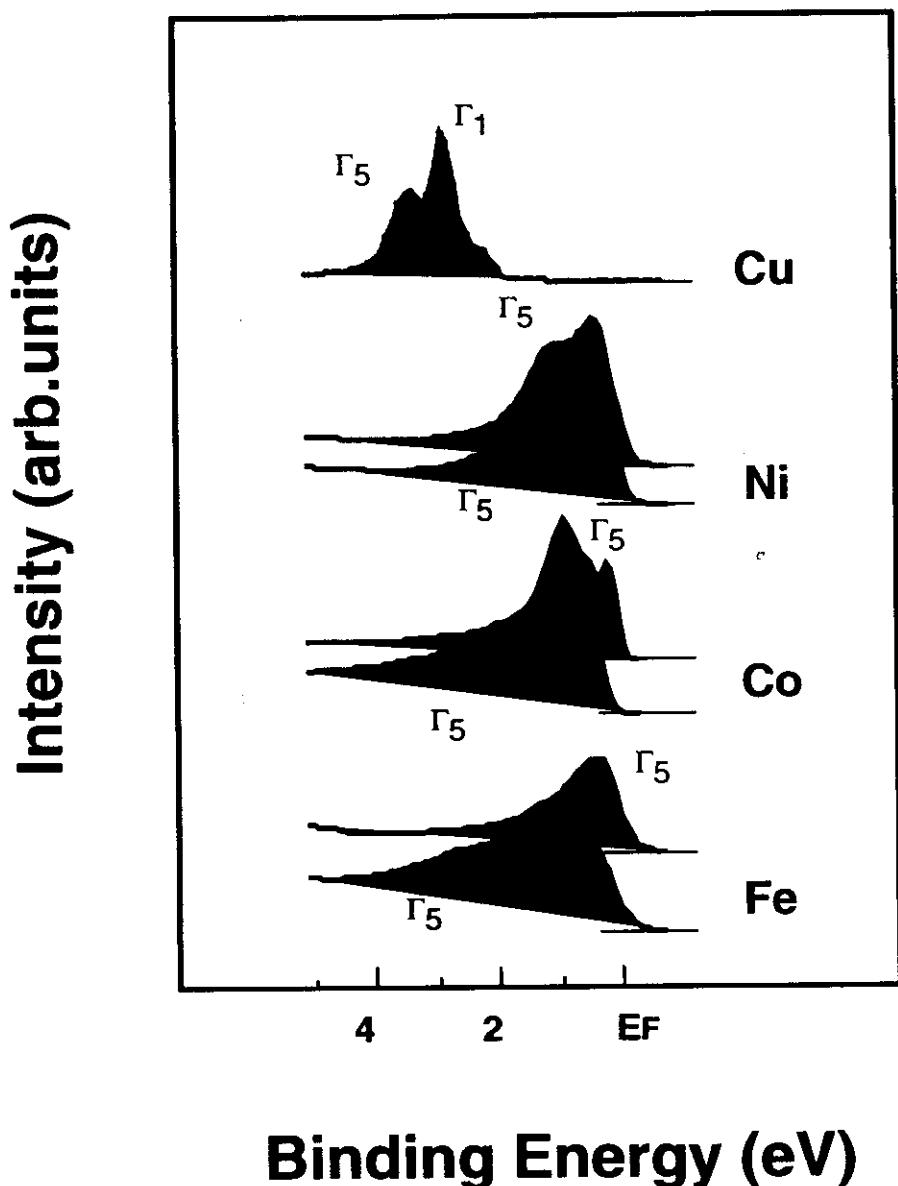


Magnetic Exchange Splitting  $\delta E_{\text{ex}}$   
versus Magnetic Moment



# Epitaxial fcc Films

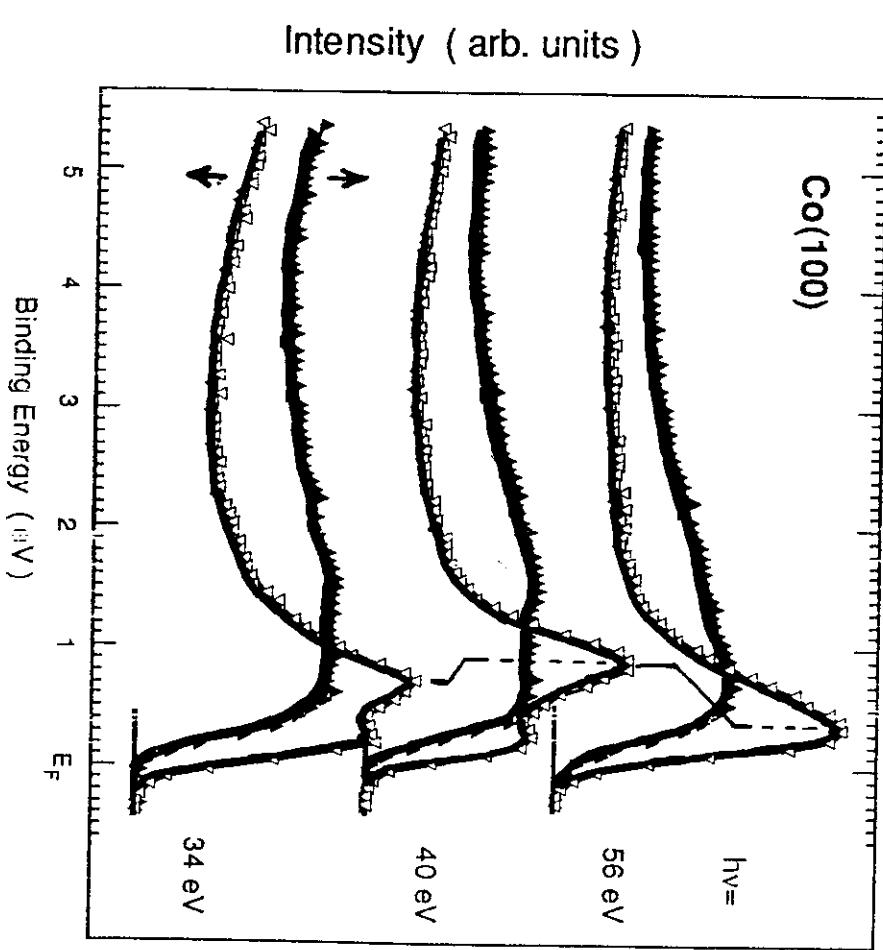
## Spin-Resolved Photoemission



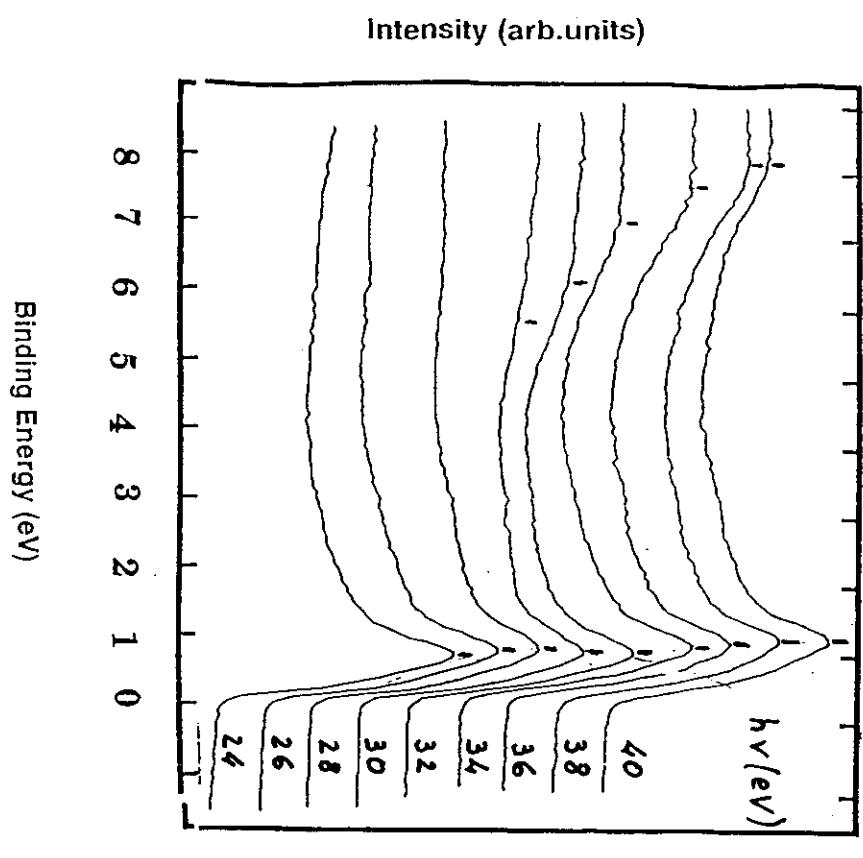
## Band Mapping of Magnetic States

Fcc Co (100)

### Spin Resolved

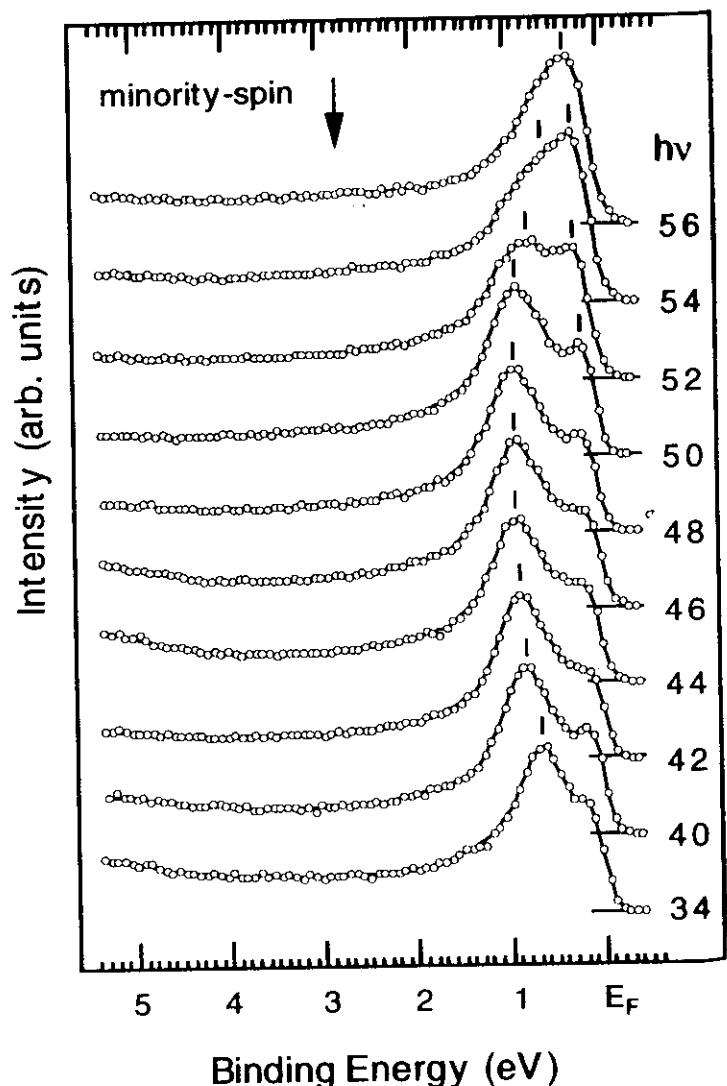


### Spin Integrated



# fcc-Co: bandstructure

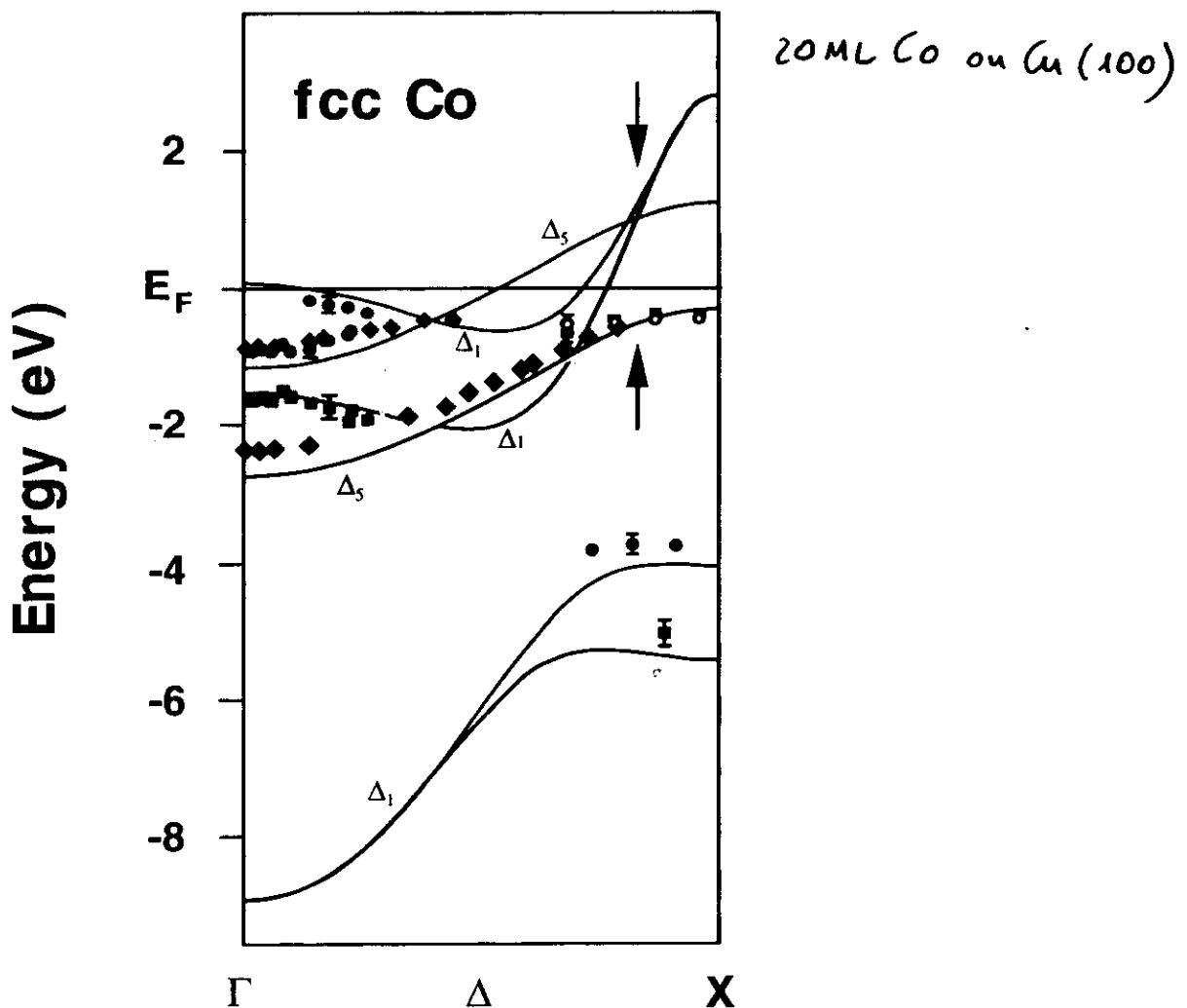
Minority-Spin Emission Only



$$E = E(k_{\perp}, \sigma_{\downarrow})$$

$k_{\perp}$  along  $\Gamma$ -X

# Fcc Co -Bandstructure



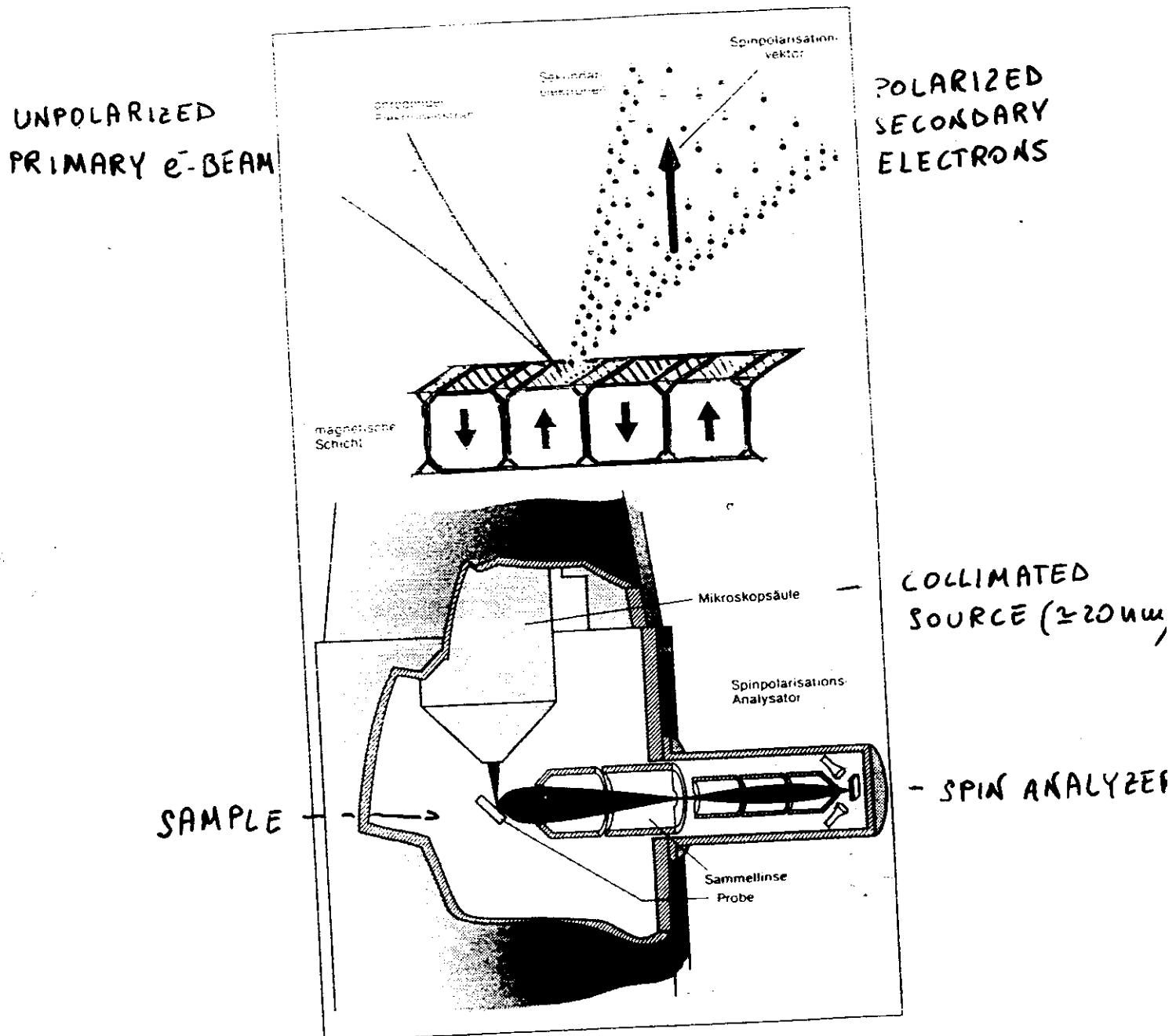
Experiment (symbols) vs.theory (lines)

Band disperion  $E=E(k,\sigma)$

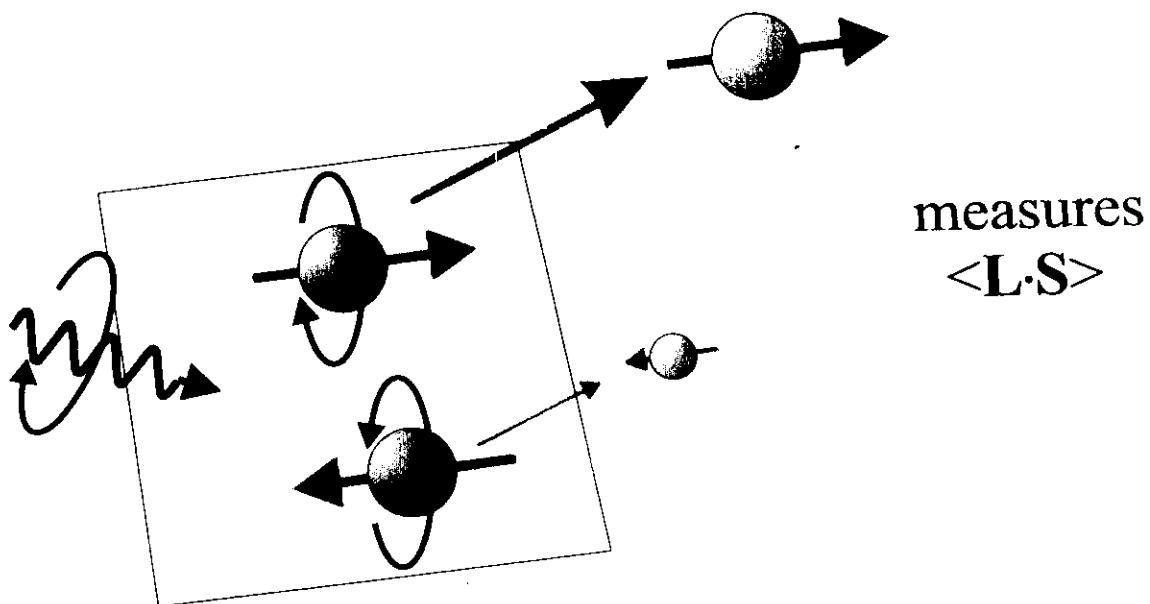
Exp.: R.Kläsges, PhD thesis, Köln (98)

Th: P.Bruno, Europhys. Lett. 23, 615 (93)

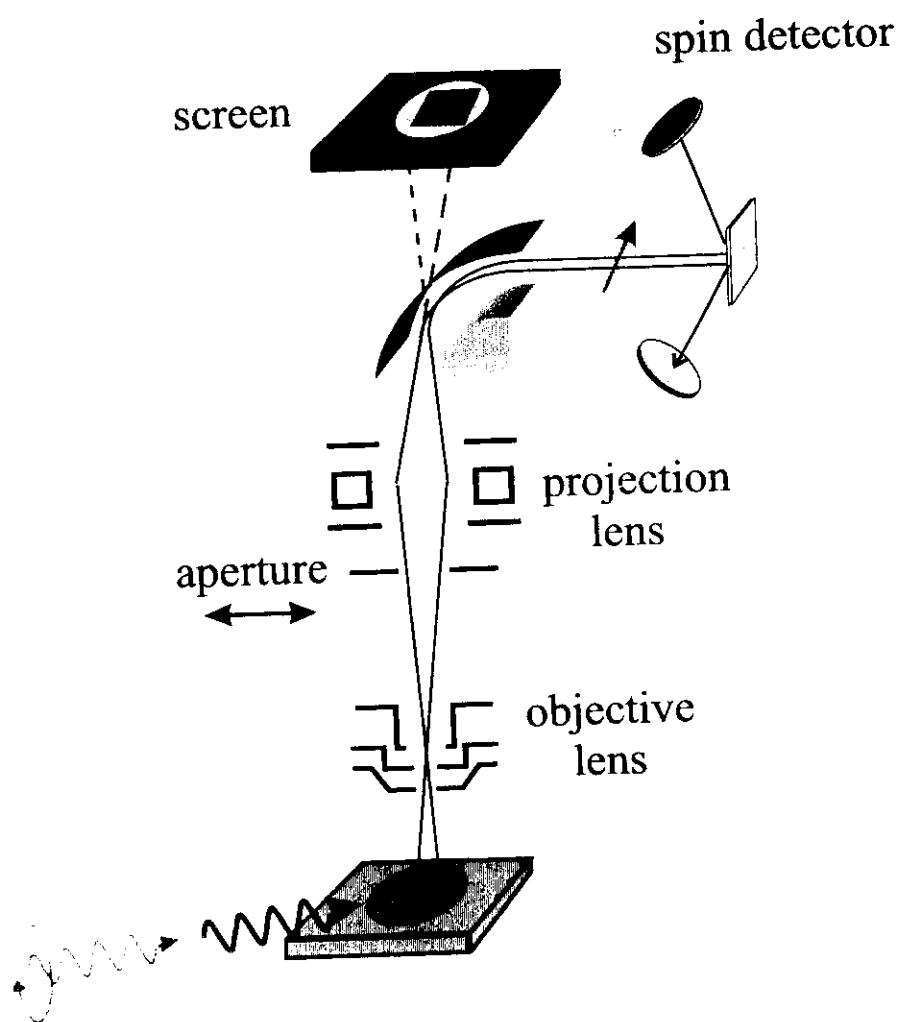
# SCANNING ELECTRON MICROSCOPY OF POLARIZED ELECTRONS



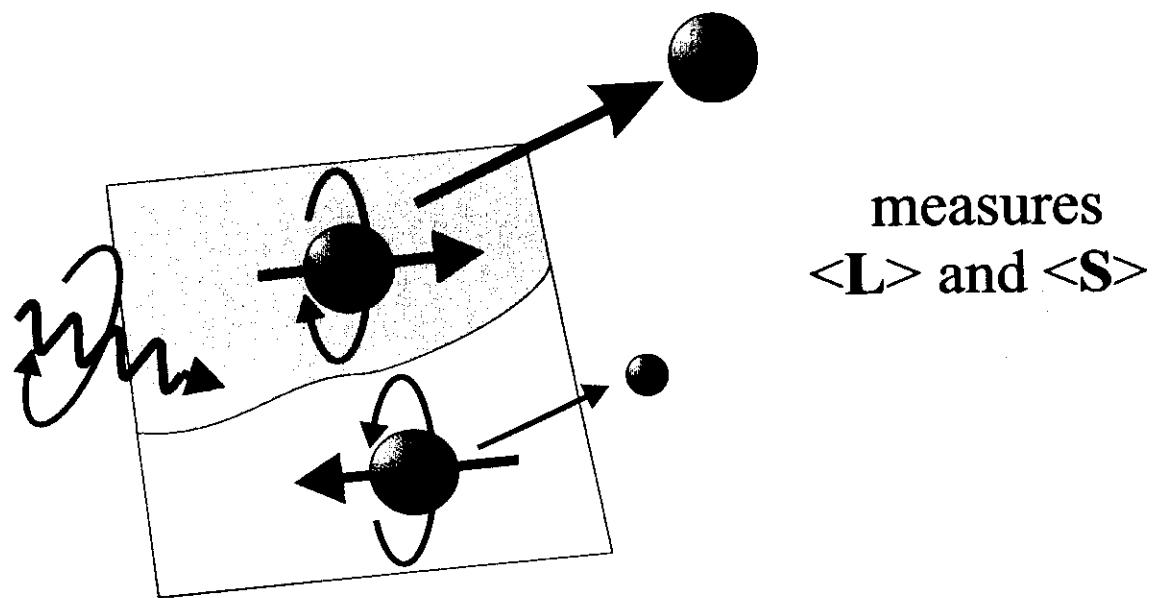
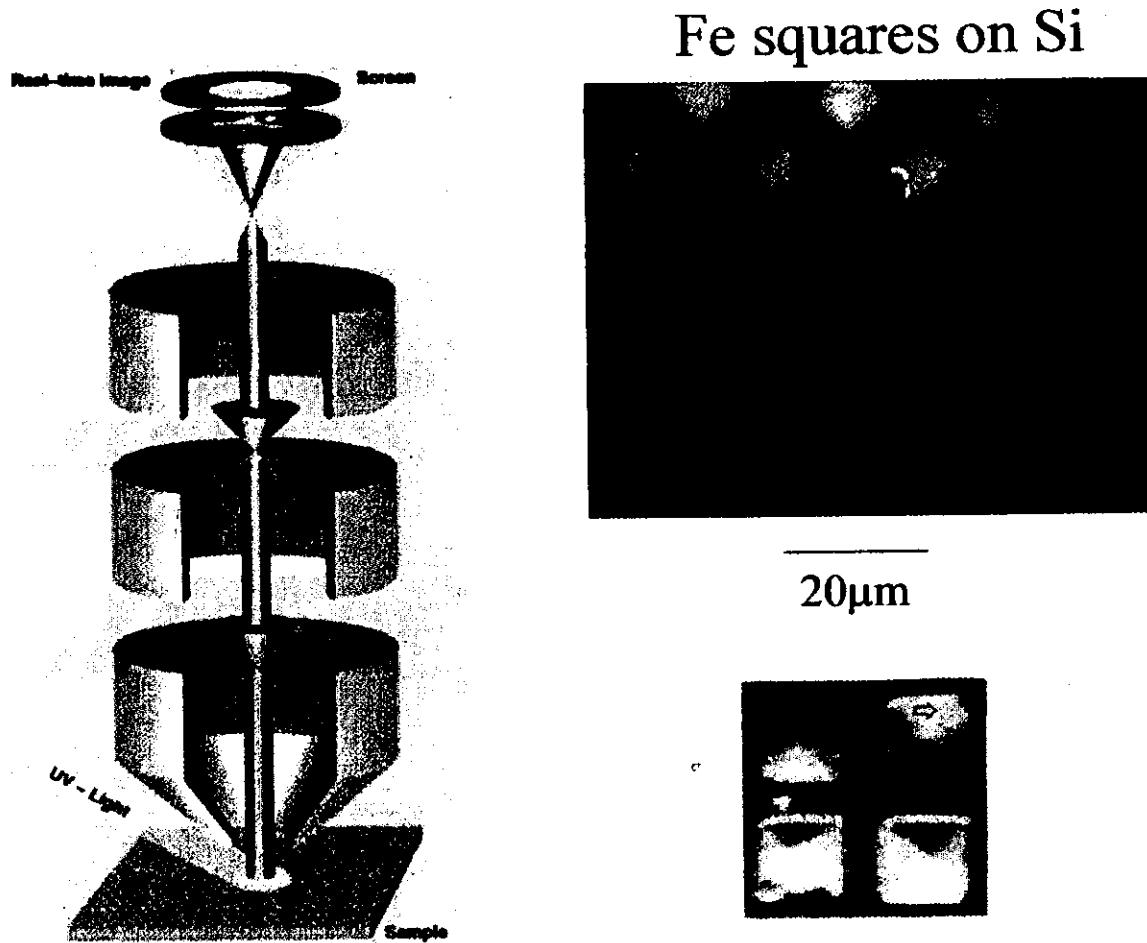
$$P \approx \frac{n_B}{n_V} n_B \text{ Bohr magnetons (per atom)} \\ n_V \text{ valence electrons (per atom)}$$



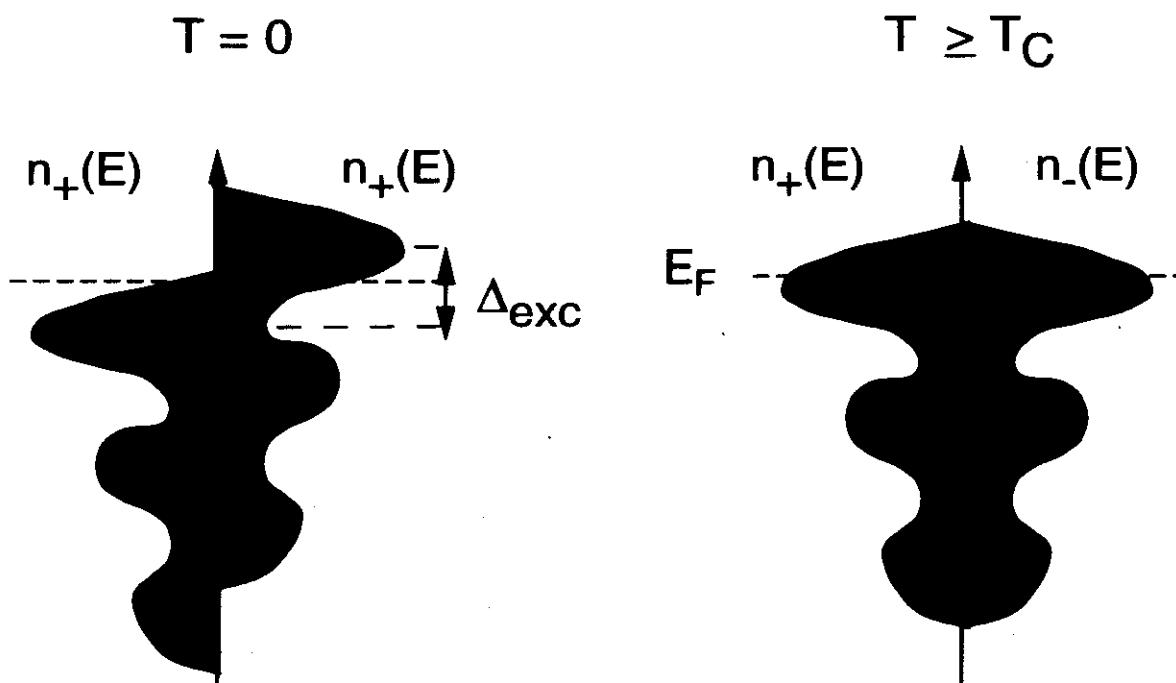
spin-polarized PEEM



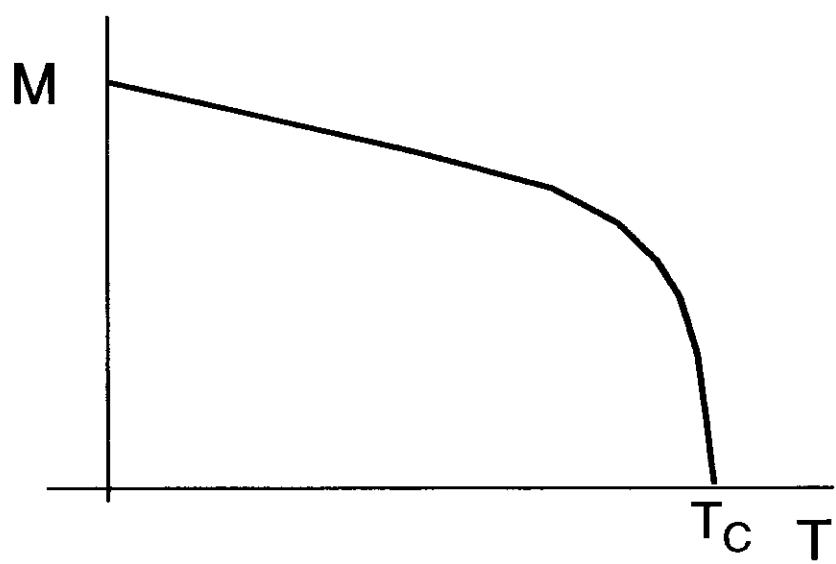
# Photo Emission Electron Microscopy



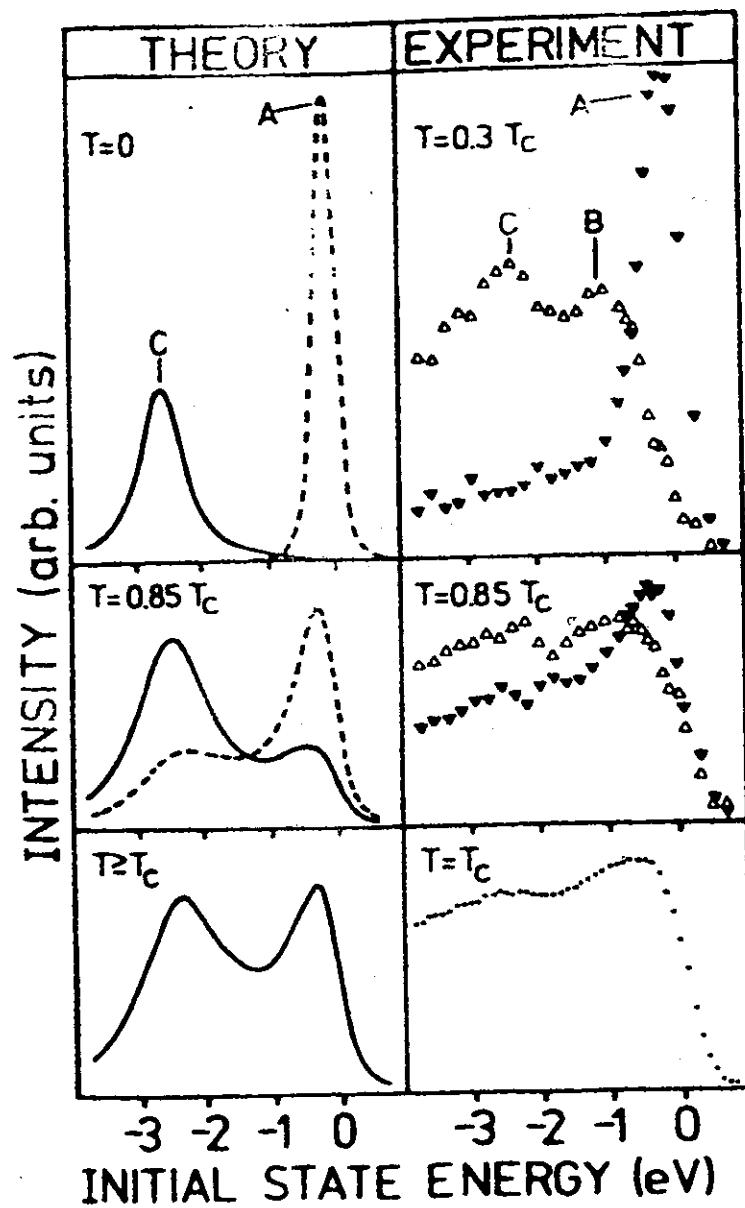
# Stoner Model - Ferromagnetic Electronic Structure



$$\Delta_{\text{exc}} \propto M$$



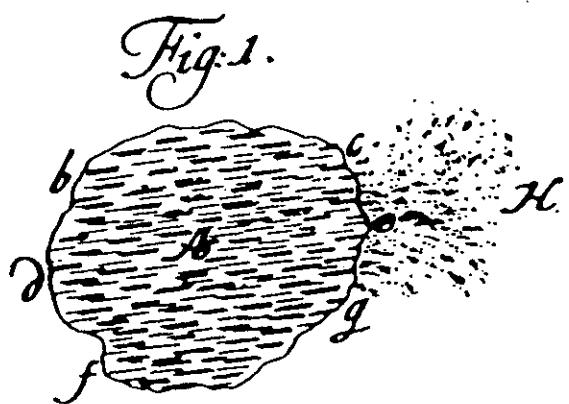
# Fe: Temperature dependence



The exchange-splitting does not vanish  
approaching  $T_c$

# Order - Disorder

Magnetized Fe  
(e.g.  $T < T_c$ )

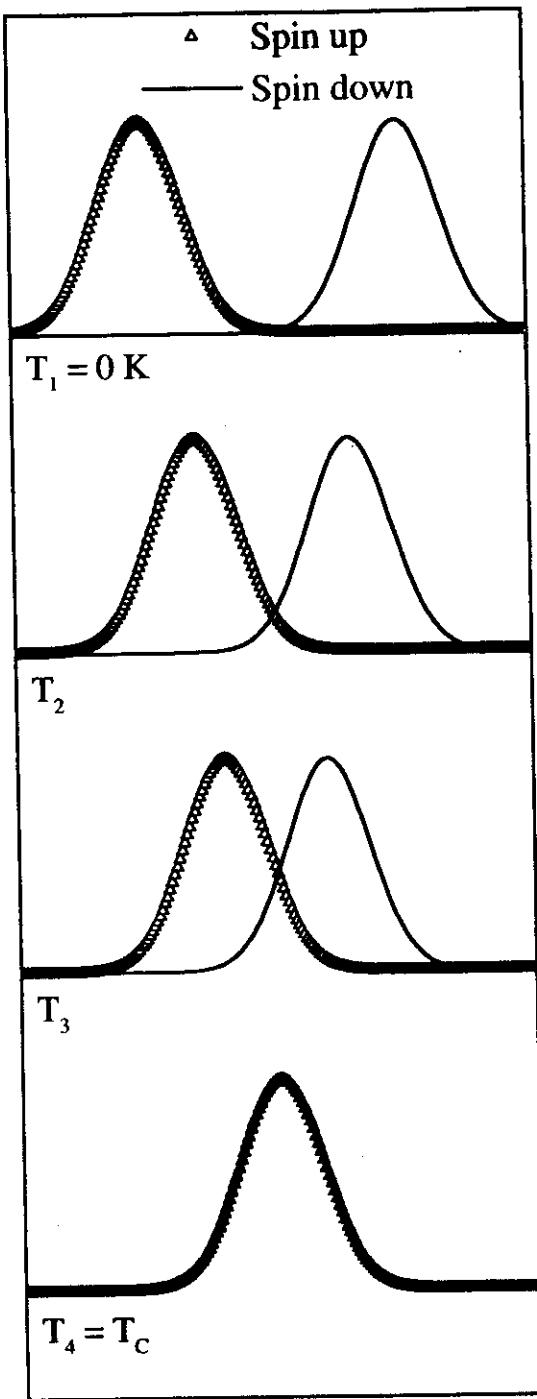


Non-Magnetized Fe  
(e.g.  $T \geq T_c$ )



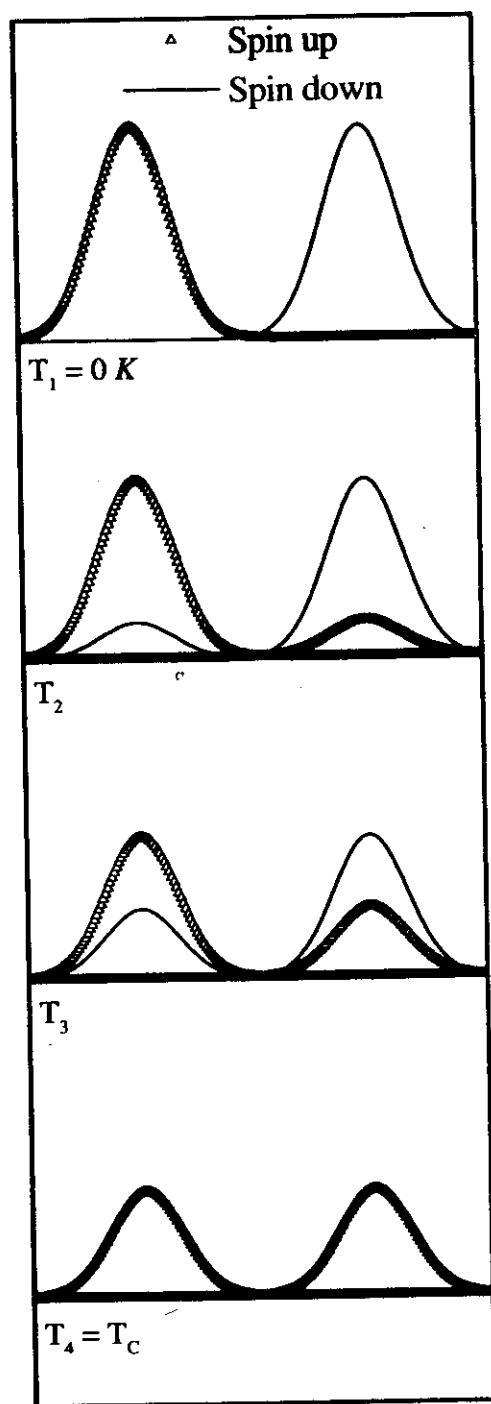
*E.Swedenborg, Principia rerum naturalium (1734)*

## Stoner model



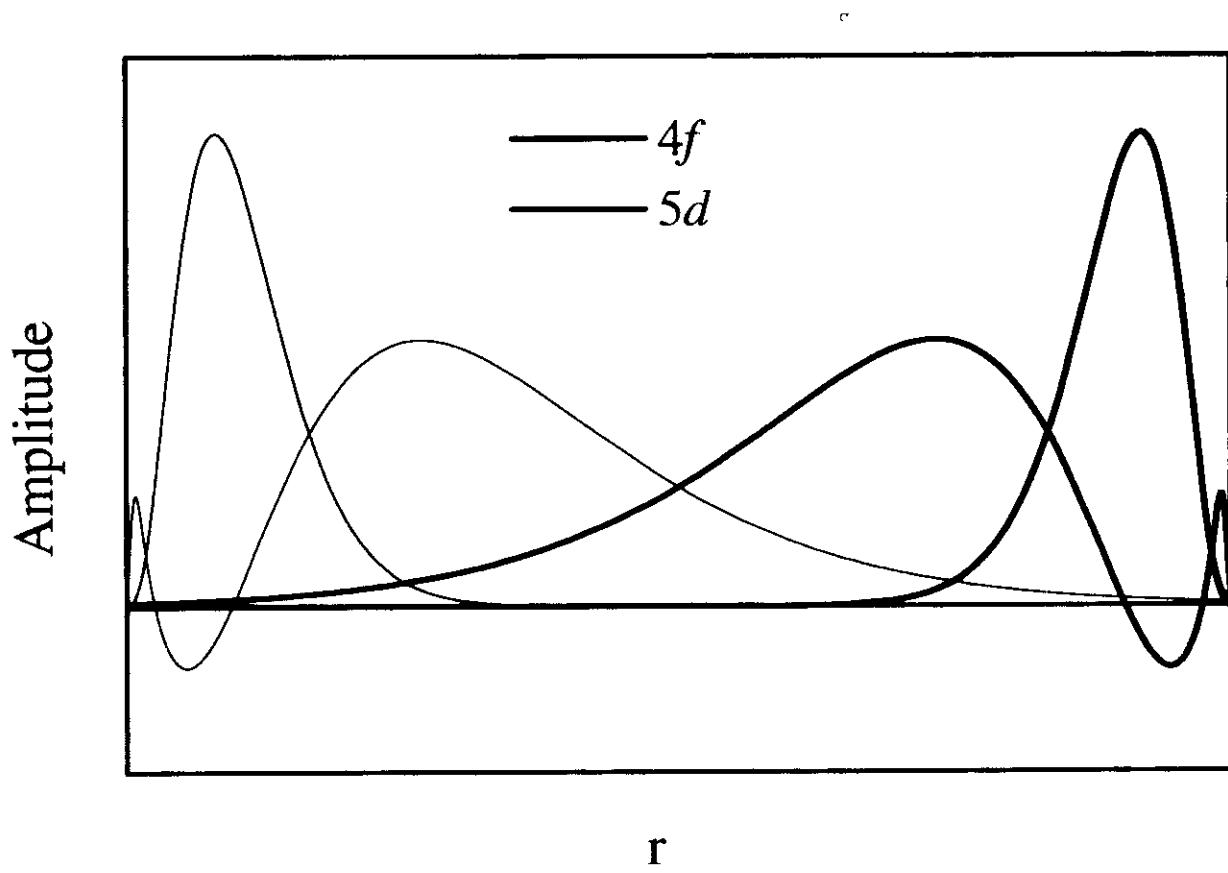
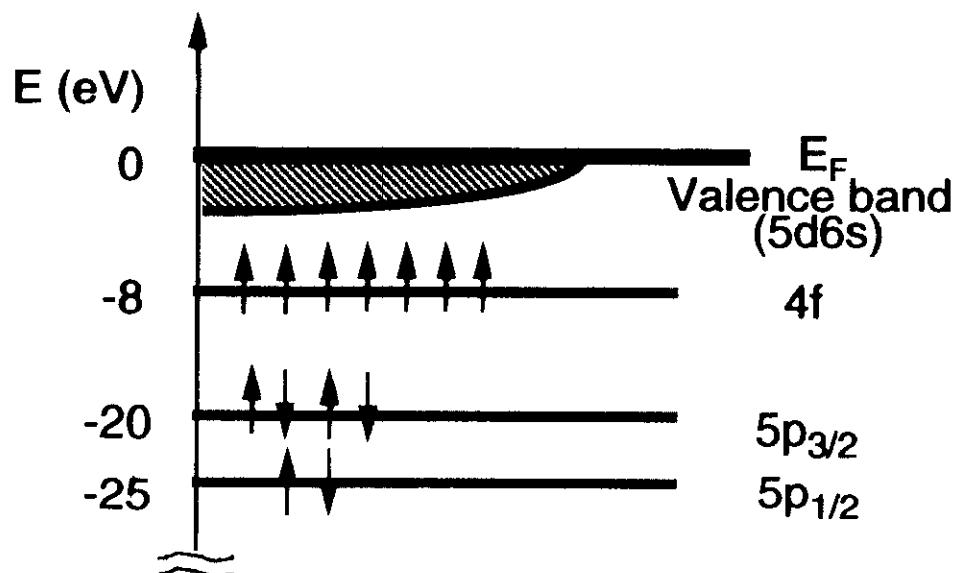
Binding energy

## Spin mixing

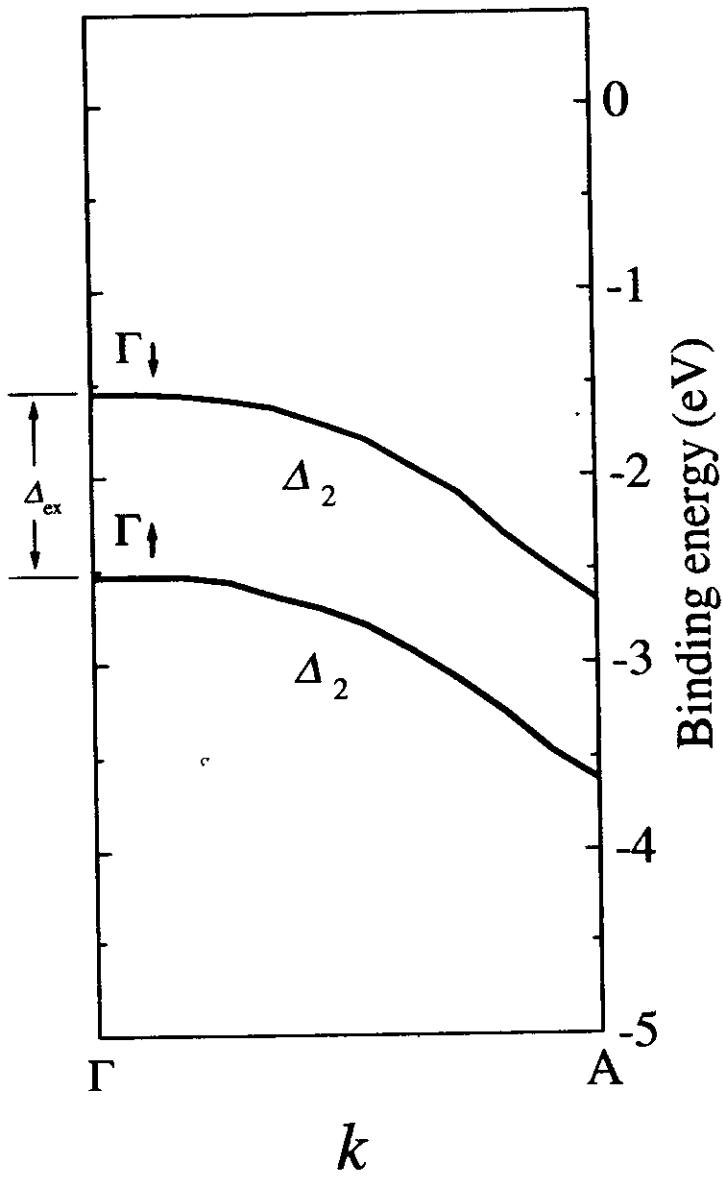
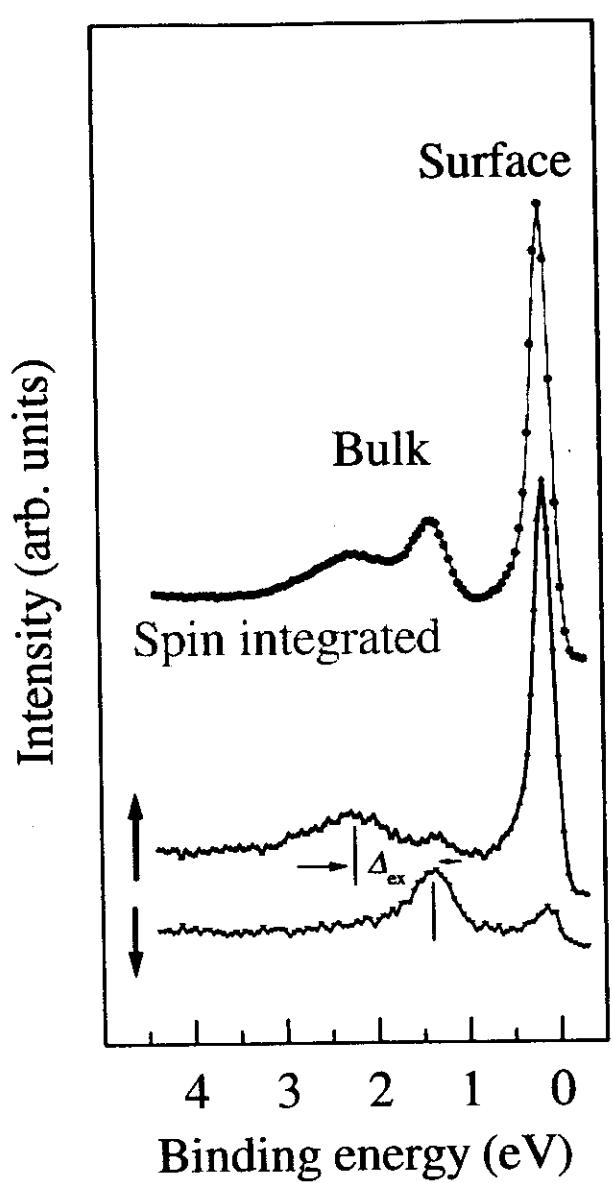


Binding energy

## Energy levels of Gd



## Gd : Valence band



Gd(0001)

Angular dependence

$\theta = +9,5^\circ$

$\theta = +7,5^\circ$

$\theta = +3,5^\circ$

surface state

exchange-splitted

$S_{\downarrow} \times$  state

$\theta = -0,5^\circ$

spin up

— spin down

$\theta = +23,5^\circ$

$\theta = +19,5^\circ$

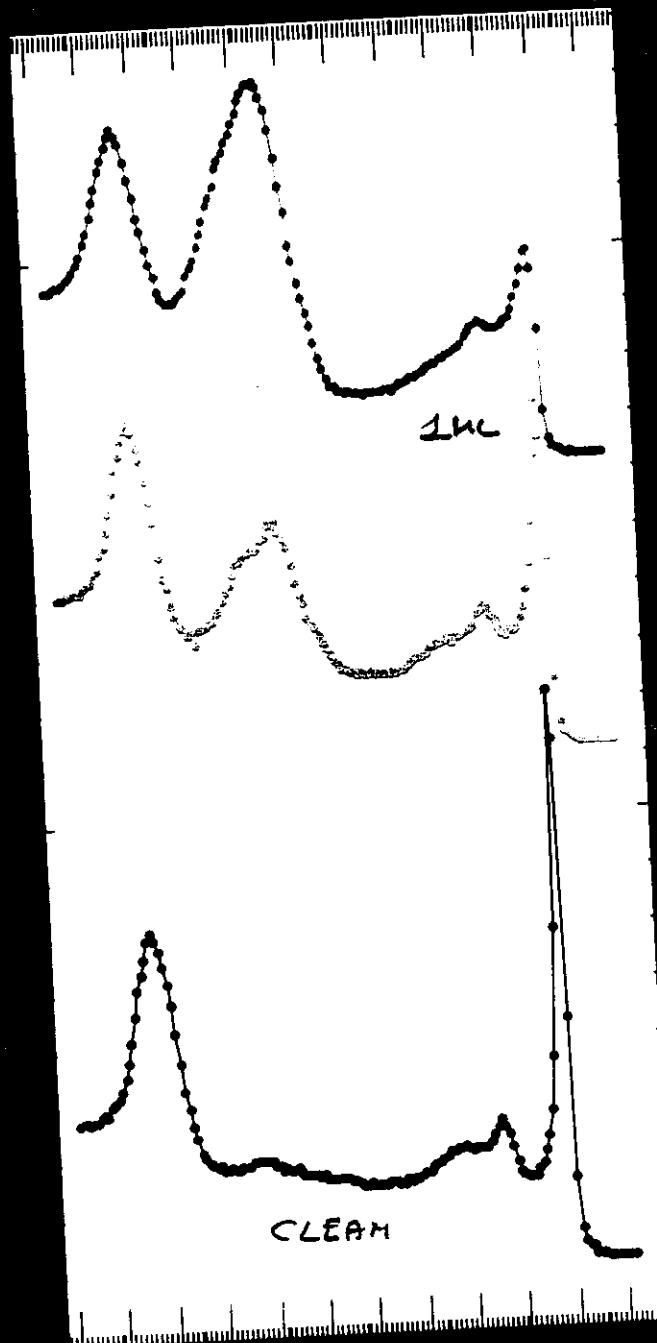
$\theta = +15,5^\circ$

$\theta = +13,5^\circ$

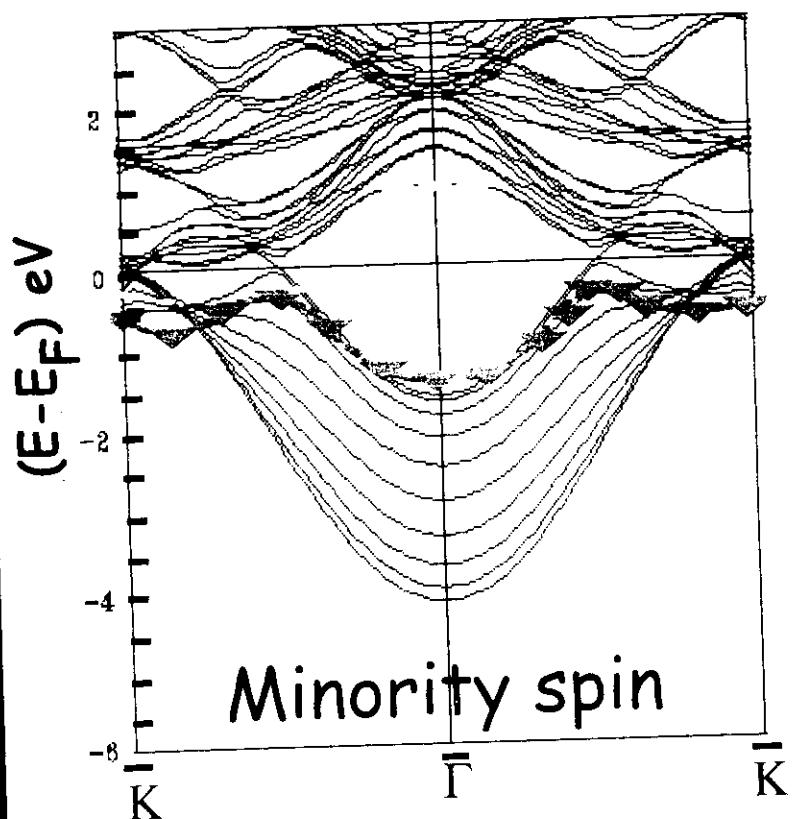
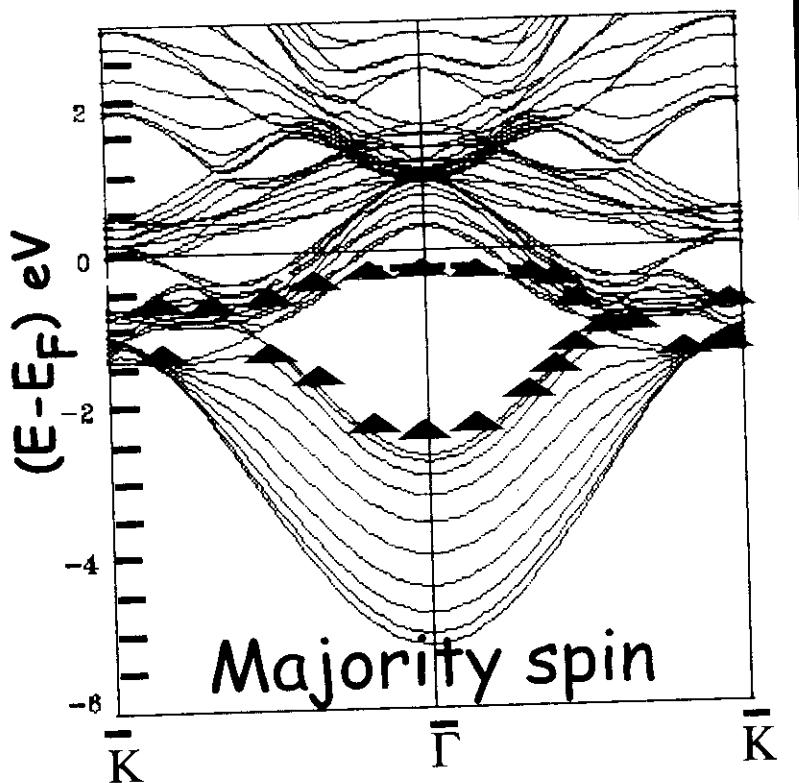
$\theta = +11,5^\circ$

1  $E_F$

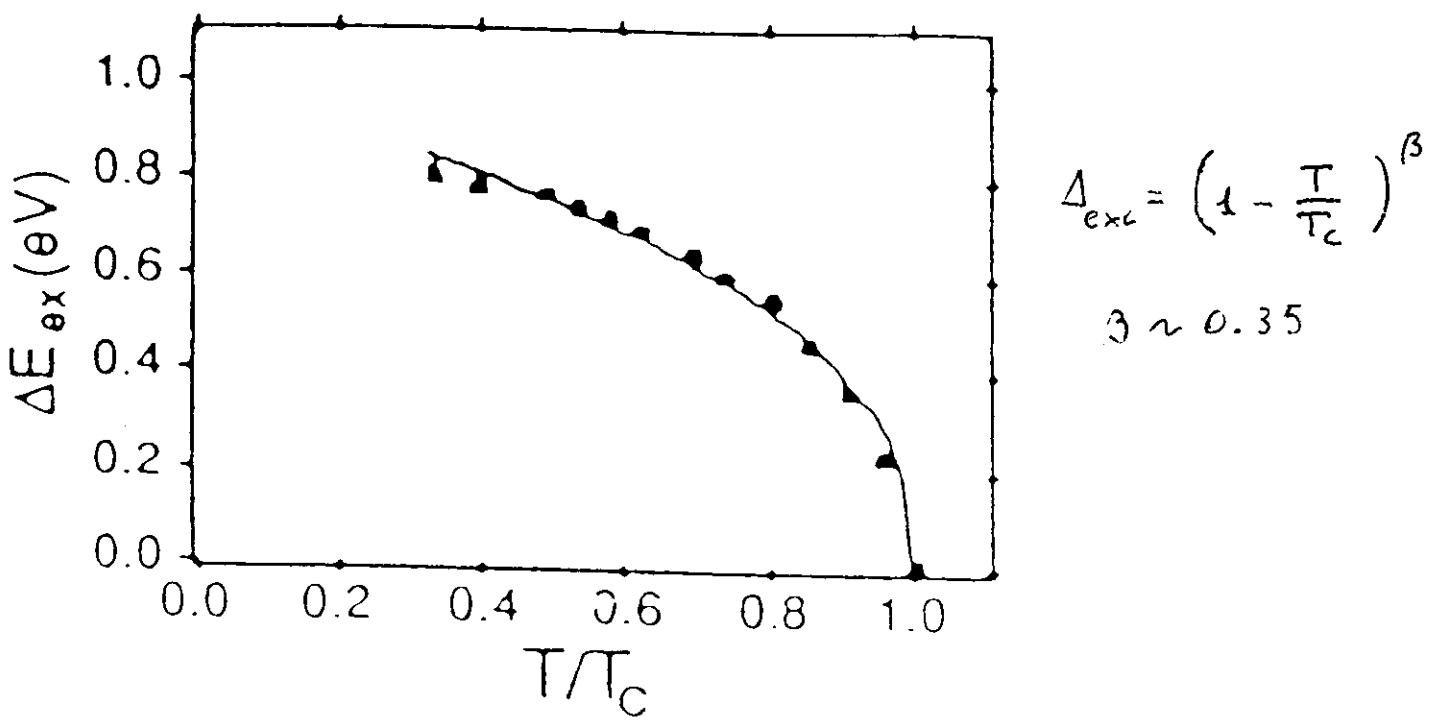
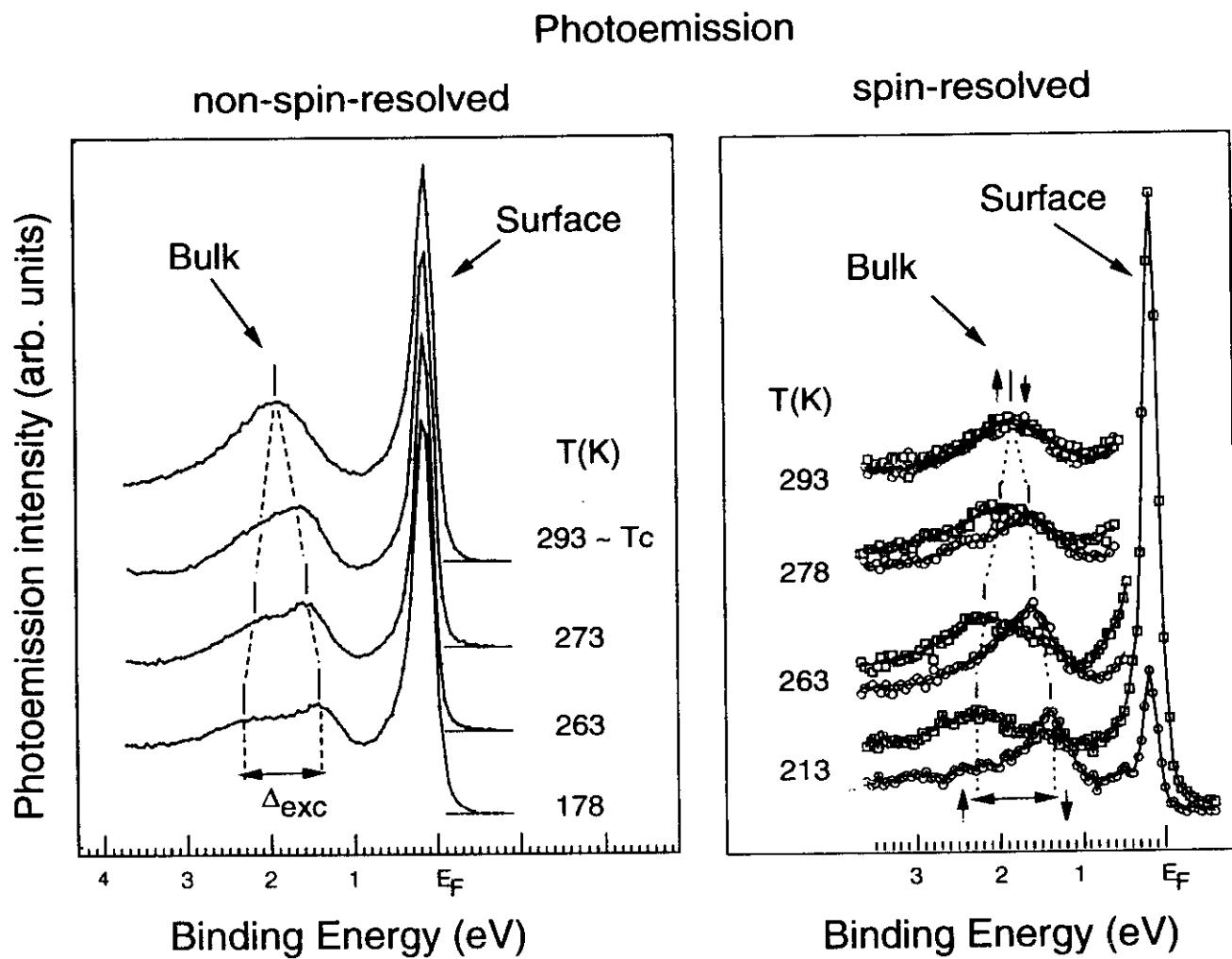
# Oxygen Exposure



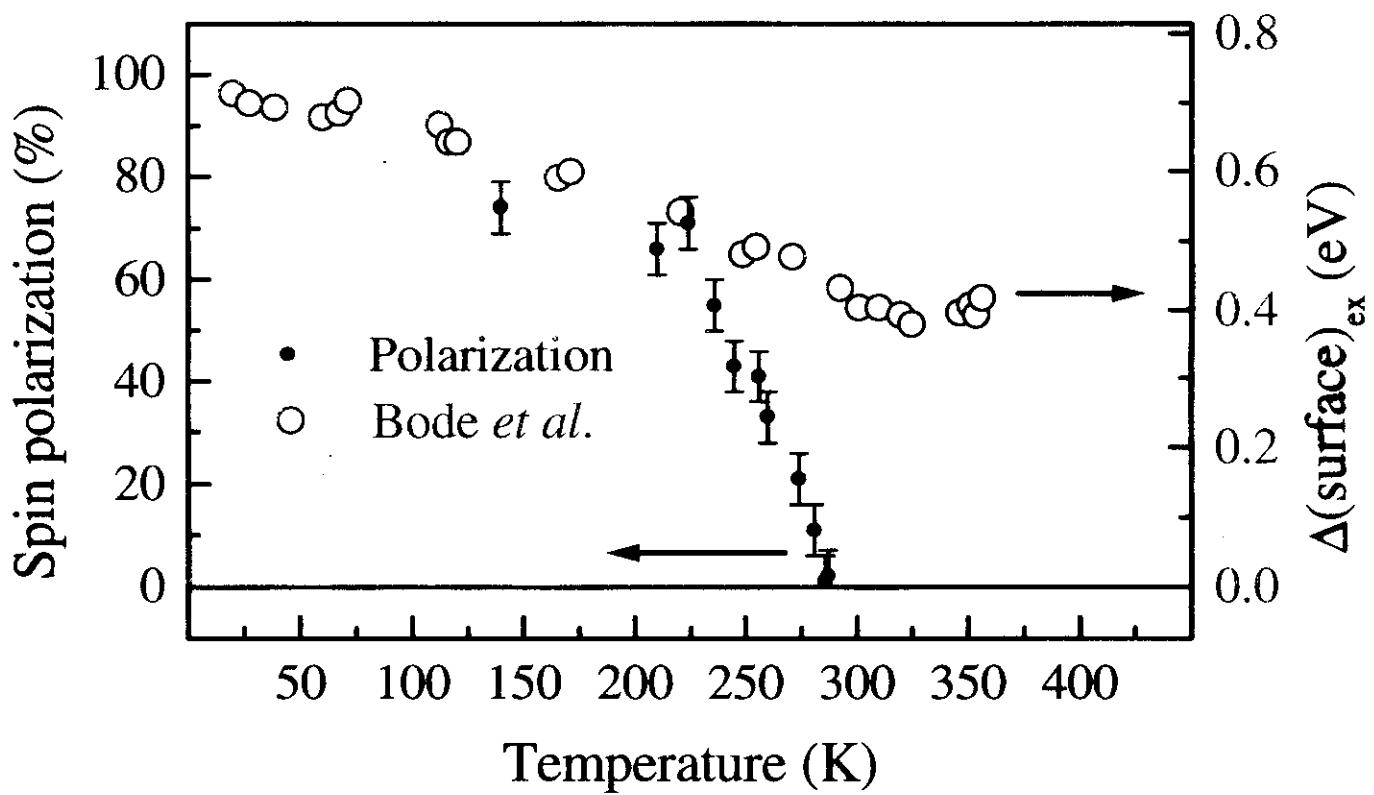
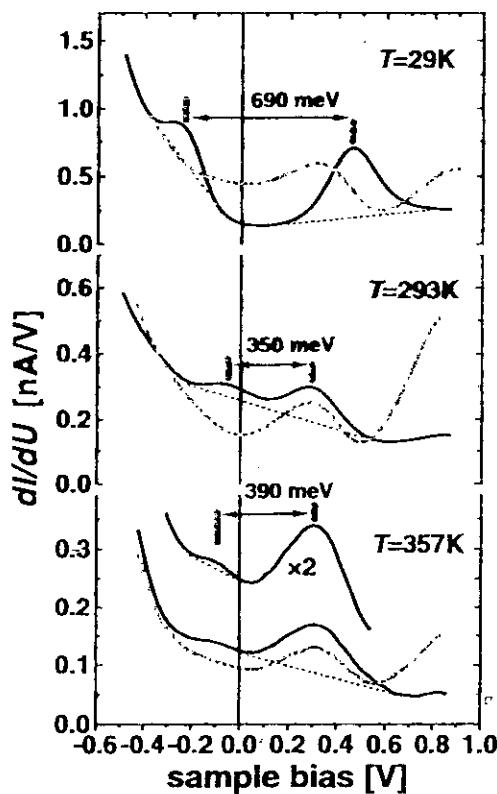
The measured variation of the binding energy as a function of the K value is compared with new L S D A calculations (coloured triangles represent experimental data).



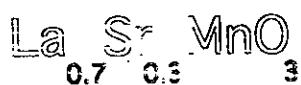
# Exchange splitting in Gd bands



## Tunneling spectra measured on Gd(0001) surface



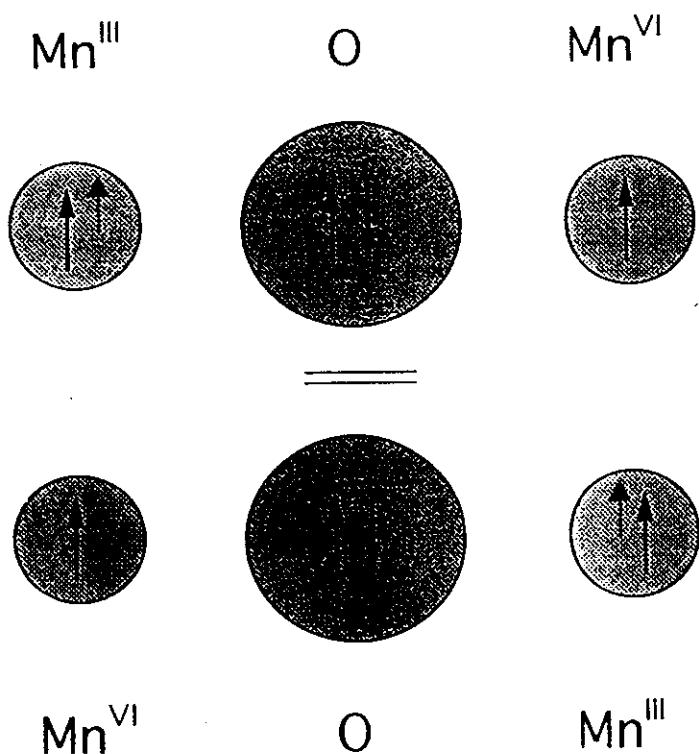
# Epitaxial thin film of



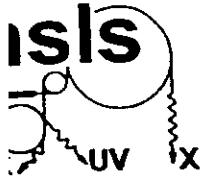
perovskite structure from the parent  $\text{LaMnO}_3$   
ferromagnetic/paramagnetic      } phase transitions  
metal/insulator  
colossal magnetoresistance

## *Double Exchange mechanism*

(Zener, Phys. Rev. 82, 403 (9151))



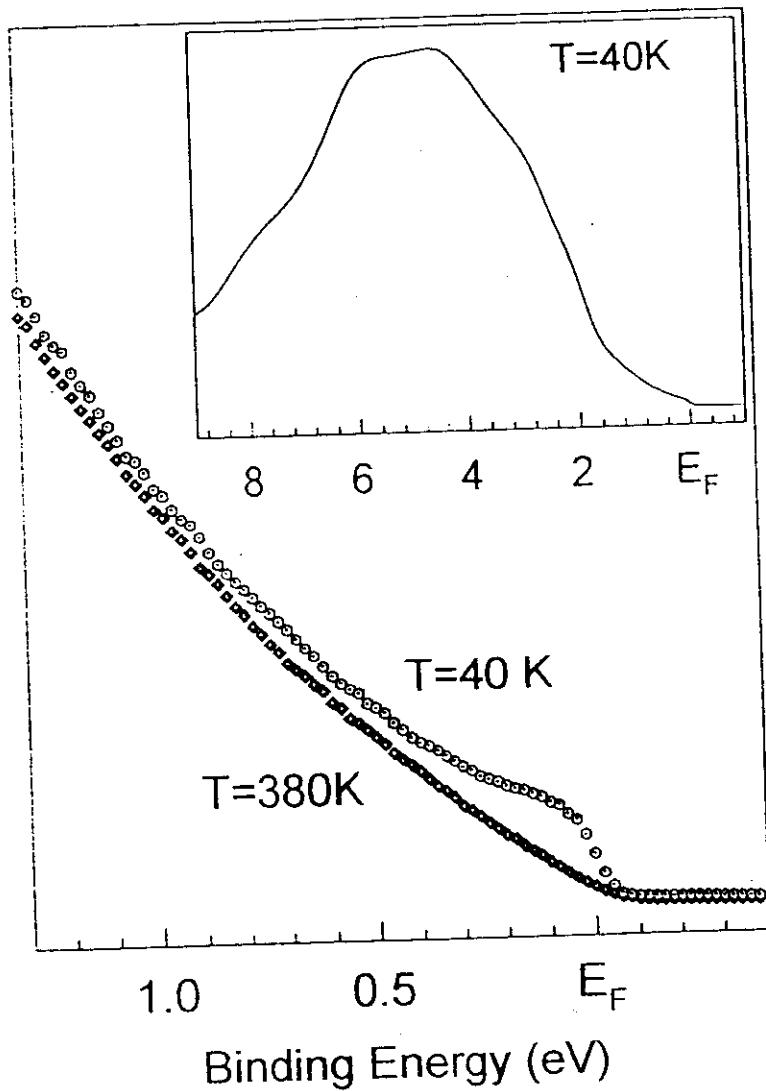
The linear combination lowers the total energy.  
It implies the contemporary occurrence of:  
a) metallicity  
b) ferromagnetic order



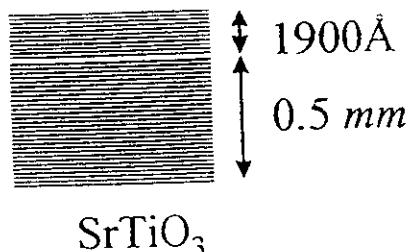
# Photoemission Study of $La_{0.7}Sr_{0.3}MnO_3$ Thin Film

1900Å  $La_{0.7}Sr_{0.3}MnO_3$  on  $SrTiO_3$

Intensity (Arbitrary Units)



$La_{0.7}Sr_{0.7}MnO_3$

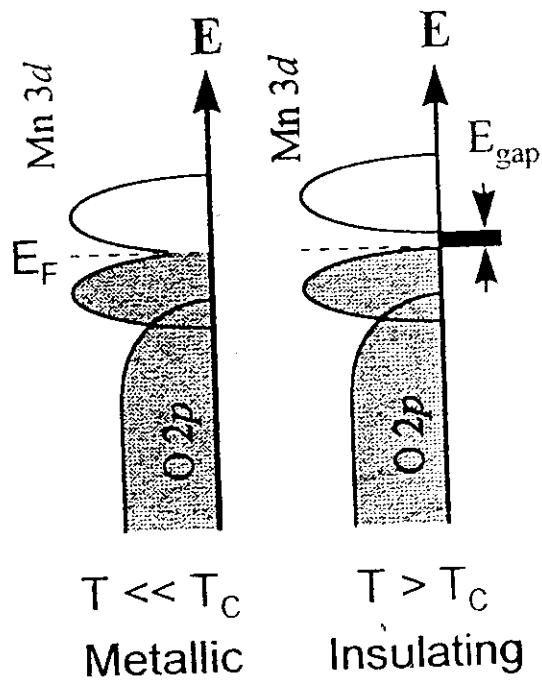


$SrTiO_3$

$T_C = 350\text{ K}$

$h\nu = 40\text{ eV}$

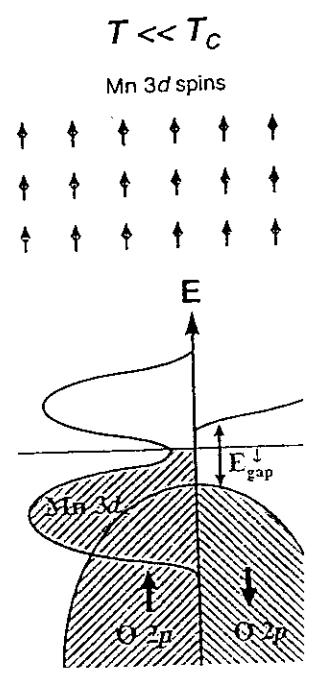
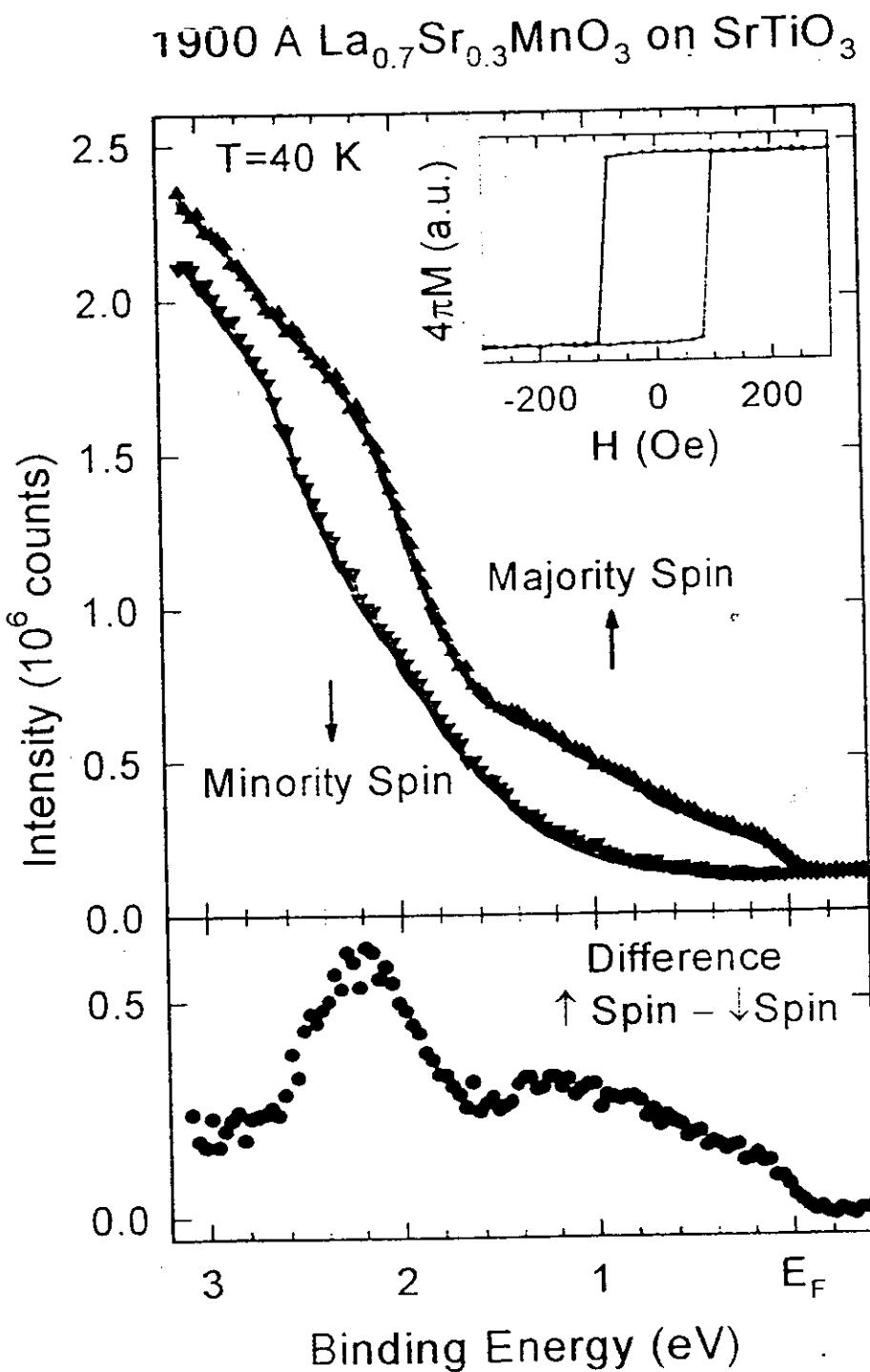
$\Delta E = 0.12\text{ eV}$



## Metal-Insulator Transition !!

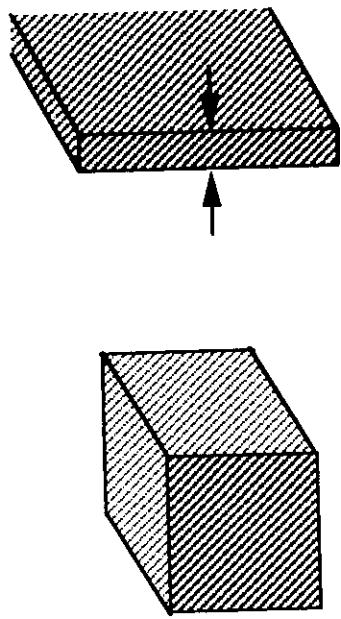
National Synchrotron Light Source ■ Brookhaven National Laboratory

# Spin resolved photoemission spectra

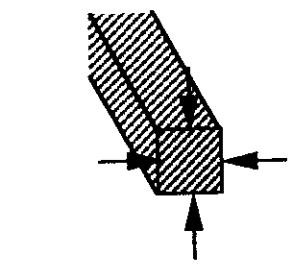
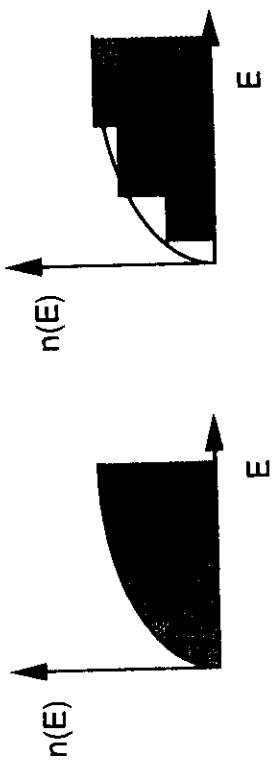


J.H. Park, E. Vescovo et al., Nature

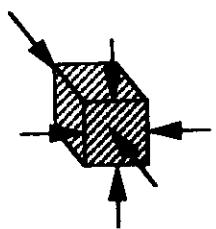
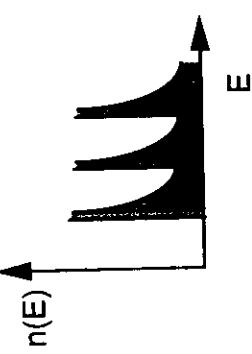
# Electron confinement and density of states



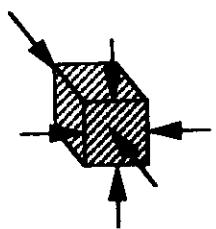
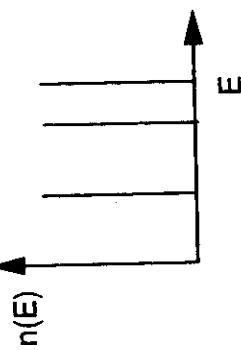
Bulk



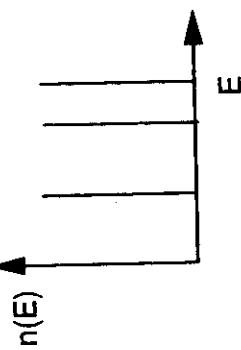
Quantum Film



Quantum Wire

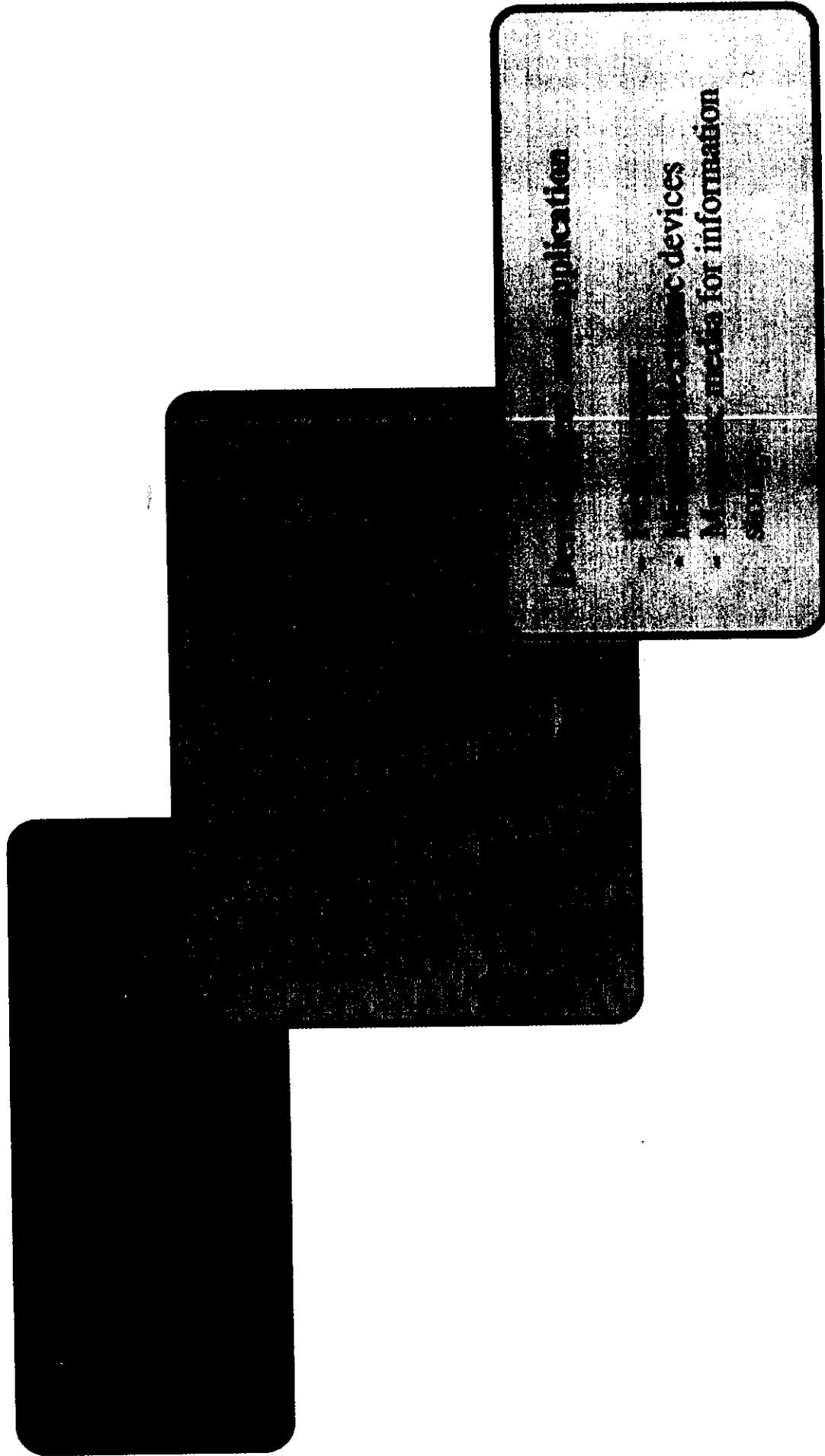


Quantum Box



Quantum Box

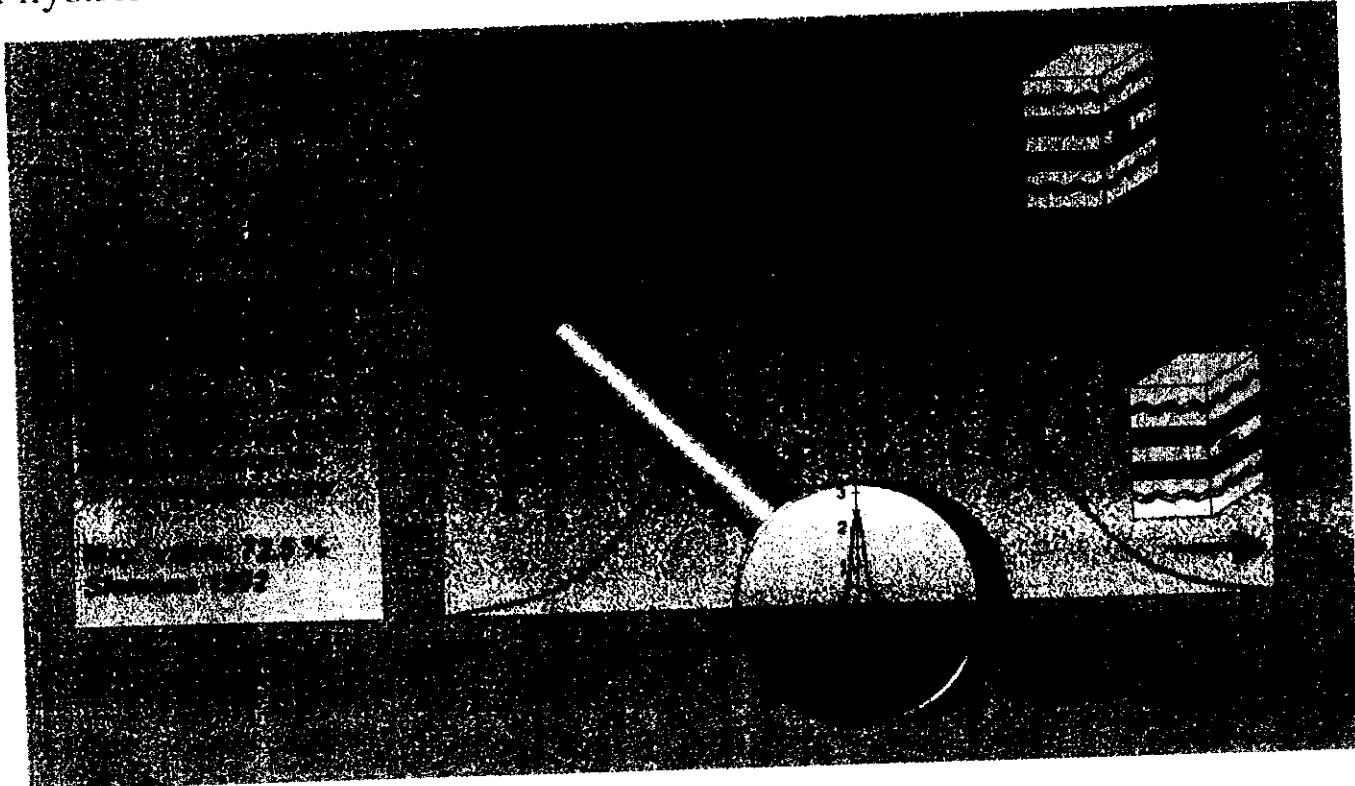
# MAGNETIC NANOSTRUCTURES



# Giant Magnetoresistance Effect

## Publications

M.N. Baibich, J.M. Broto, A. Fert, F. NguyenVanDan, F. Petroff,  
P. Etienne, G. Creuzet, A. Friederich, J. Chazelas  
Phys. Rev. Lett. 61, 2472 (1988)  
G. Binasch, P. Grünberg, F. Saurenbach, W. Zinn  
Phys. Rev. B39, 4828 (1989)



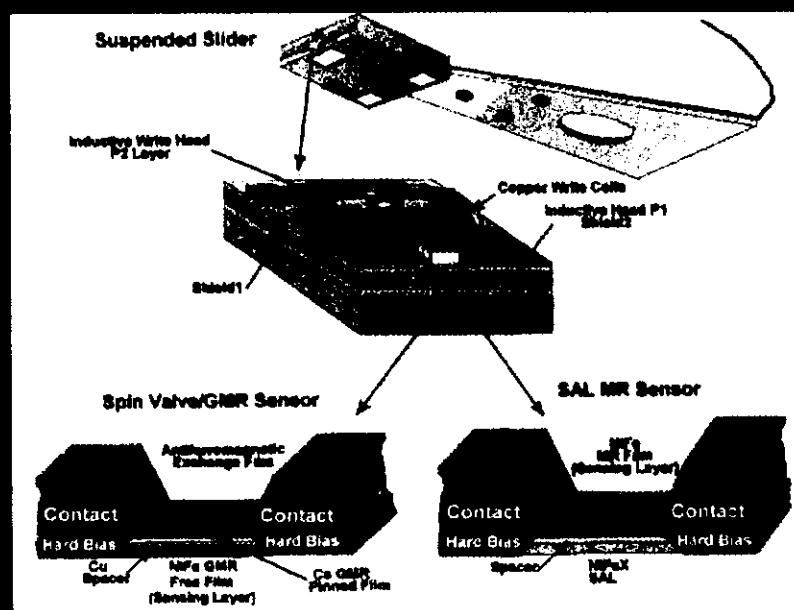
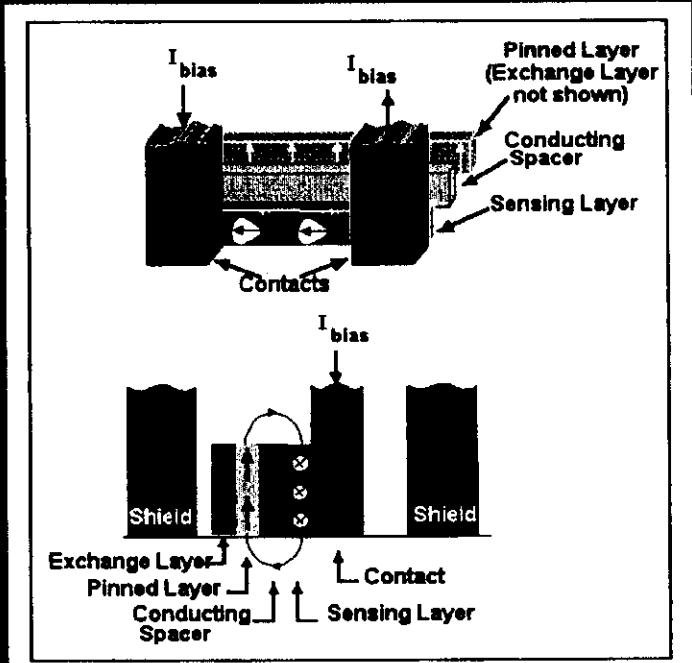
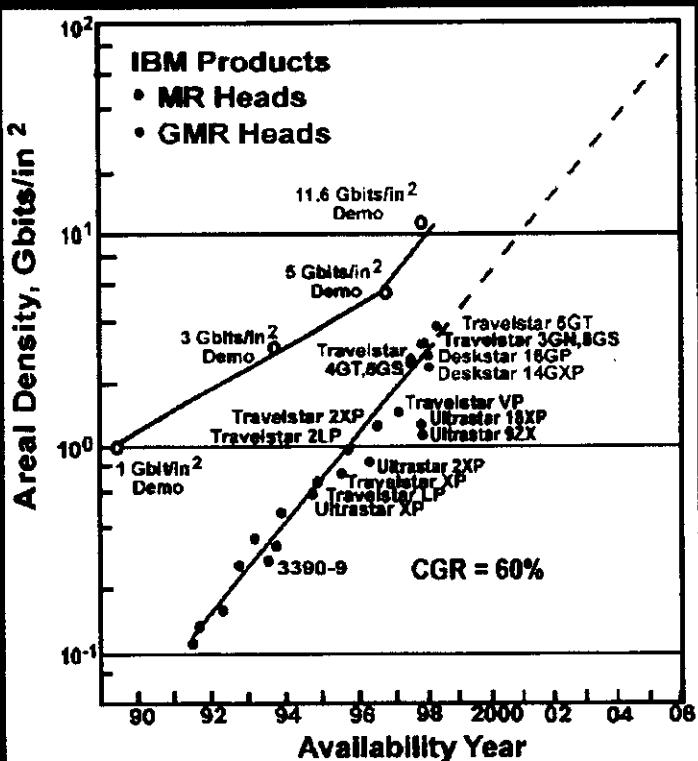
## Patent (U.S. No. 4949039)

P. Grünberg IFF, Forschungszentrum Jülich  
Magnetic Field Sensor with Ferromagnetic thin layers  
having magnetically antiparallel polarized components

## License agreements

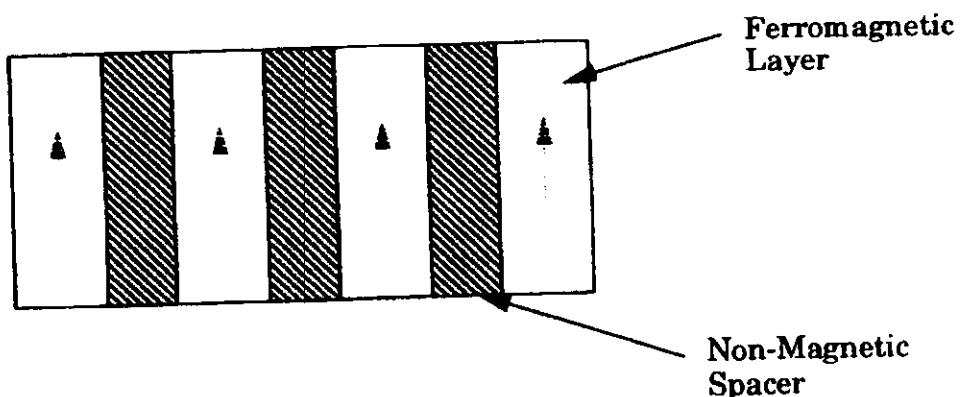
IBM Corp	1995	Fujitsu	1997	Read Rite Corp	1998
Yamaha	1996	Hitachi	1997		
TDK Corp	1996	Siemens	1997		
Silmag	1996	Seagate	1997		
		Matsushita	1997		

# GMR Readout Head Technology

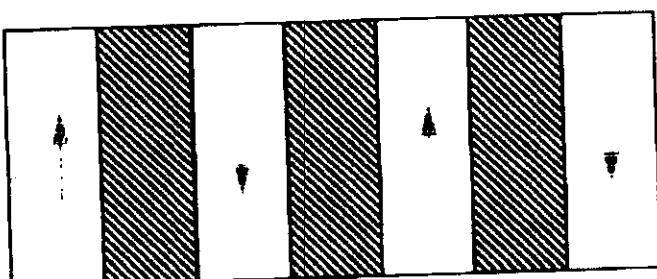


## Exchange Coupling Through Non-Magnetic Layers

**Ferromagnetic Coupling  
(FM)**



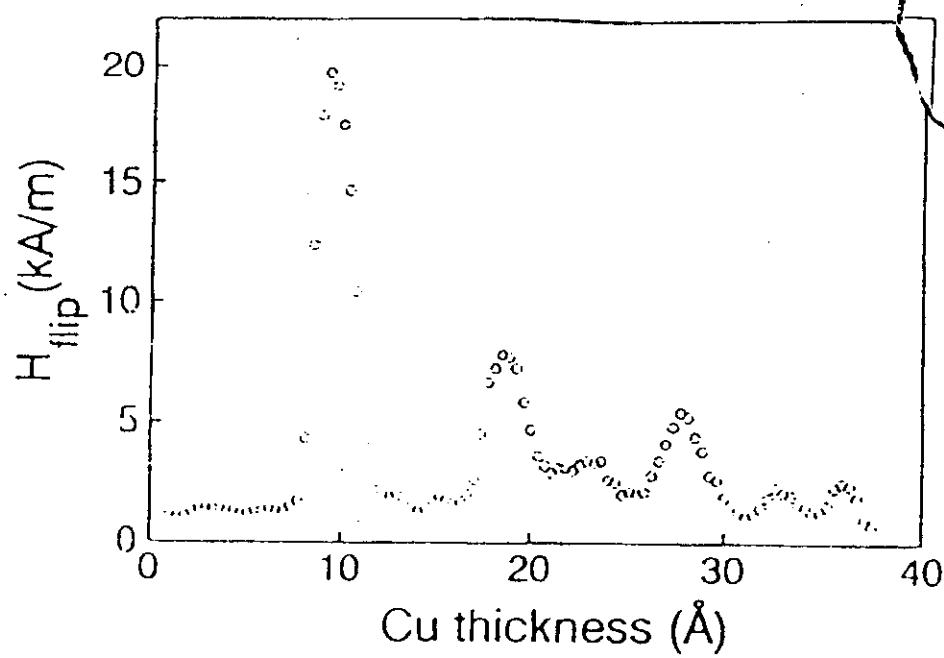
**Antiferromagnetic Coupling  
(AF)**



- The sign of the coupling depends on the thickness of the non-magnetic spacer
- It oscillates periodically between AF and FM

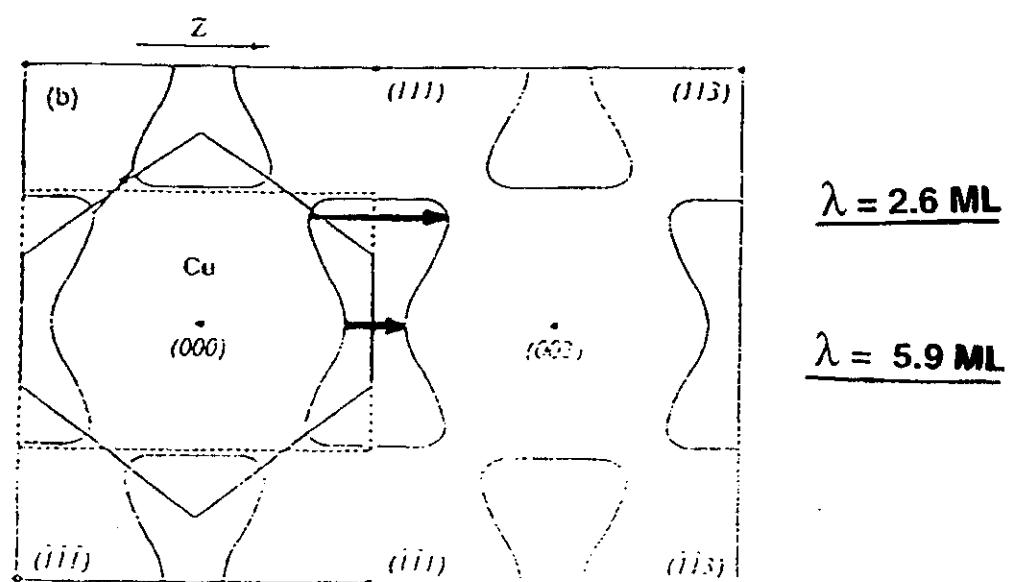


## Oscillatory Coupling of Co layers separated by Cu (100)



Bloemen et al., PRL 68, 2688 (1994)

## Cu Fermi Surface-RKKY coupling scheme

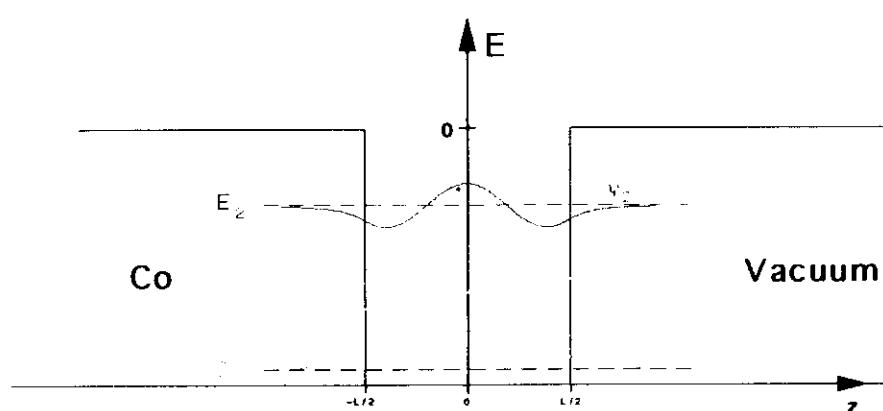
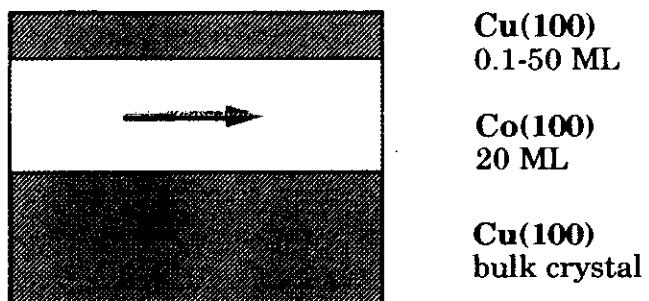


Bruno and Chappert, PRL 67, 1602 (1991); 67, 2592 (1991)



# Quantum Well States in Cu on Co(100)

## EPITAXIAL Cu LAYERS ON Co(100)

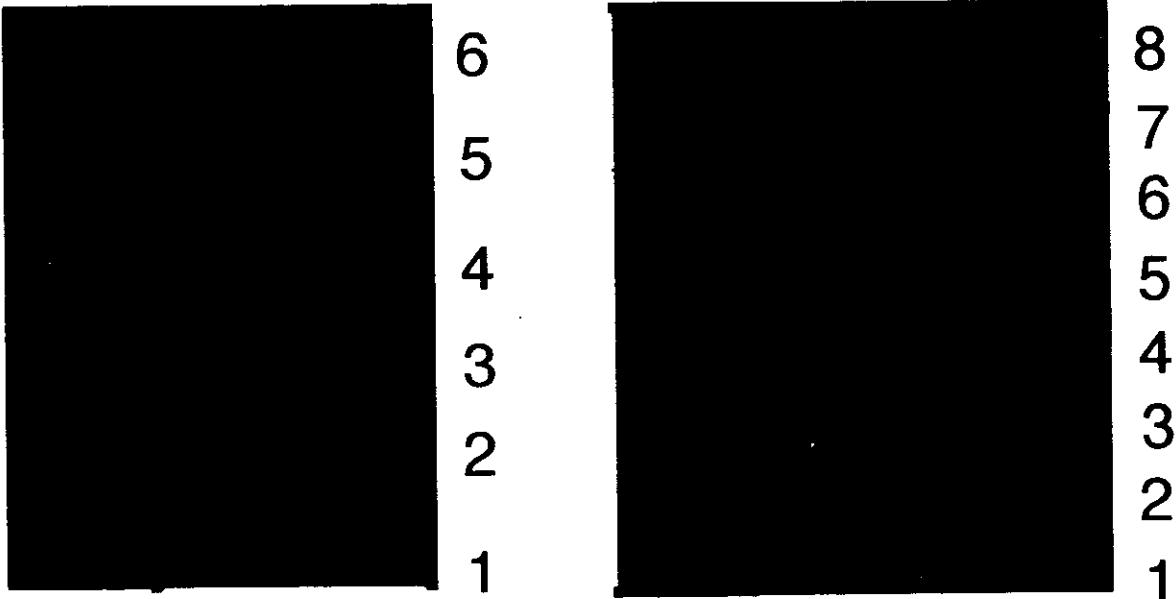


Discretization of  $k_{\perp}$  in thin films  $\rightarrow$  2D - Quantum Well States

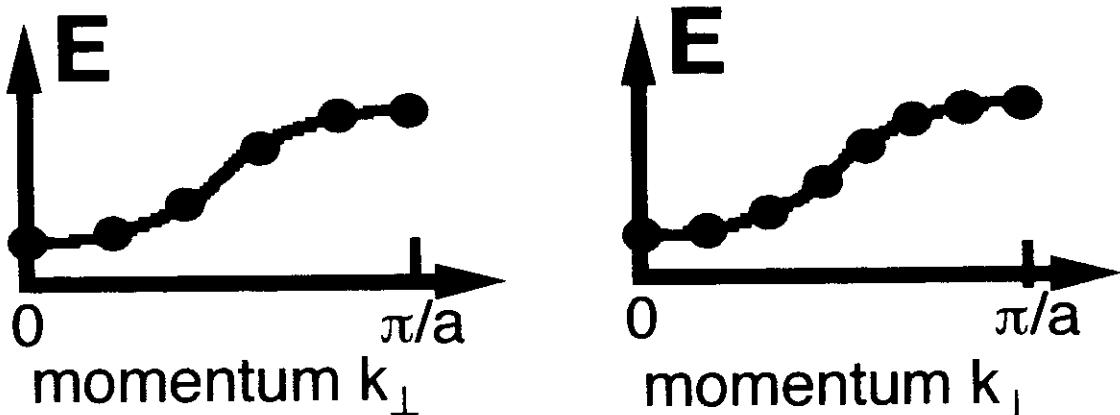
J. Ortega and F.J.Himpsel, PRL 69,844(92); Garrison et al, PRL71,2801(93),  
Carbone et al, PRL71,2805(93)

# Quantum Well States

## Real Space

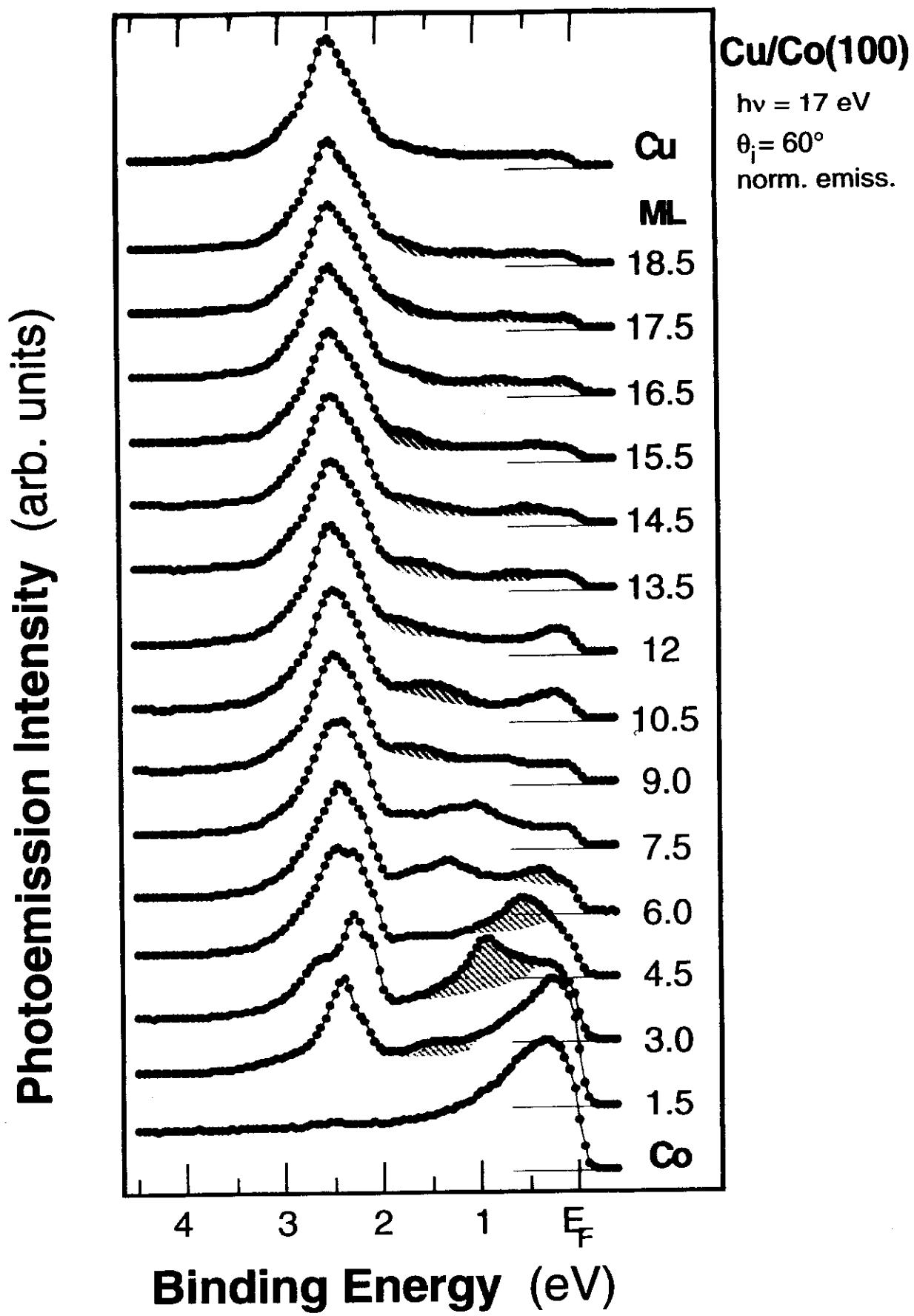


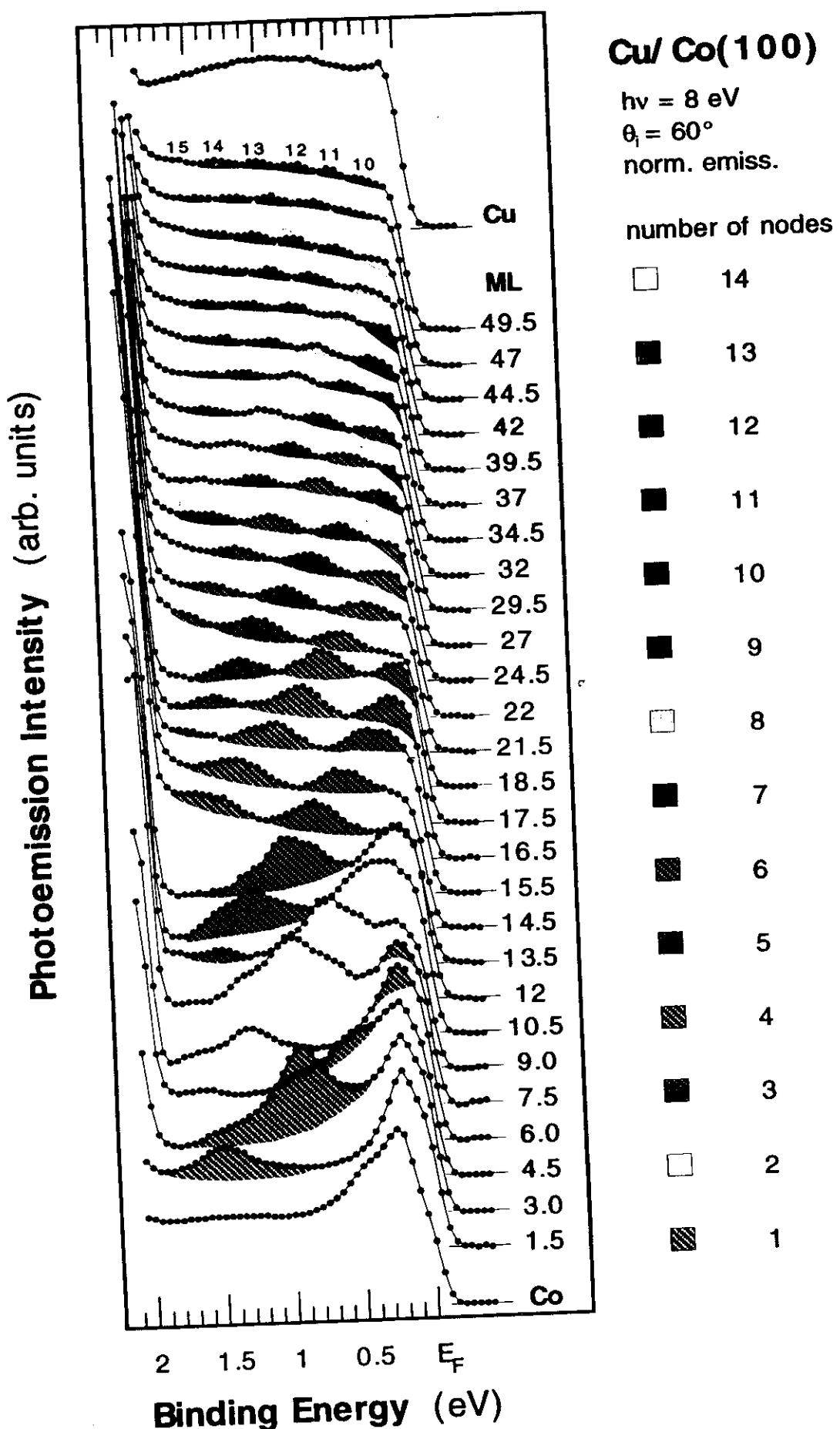
## Reciprocal Space



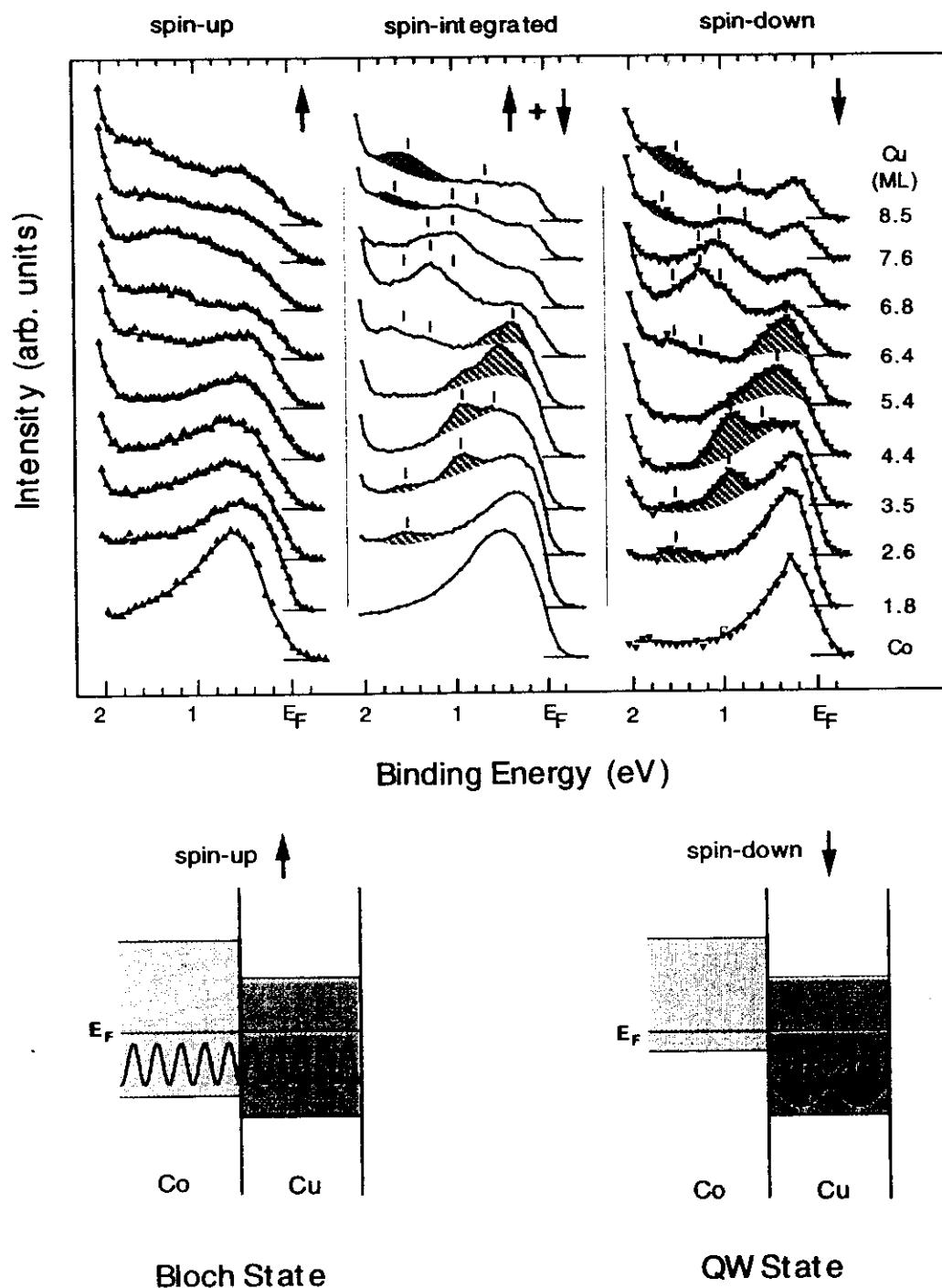
## Reflectivity Boundary Conditions

IFF-EE 94



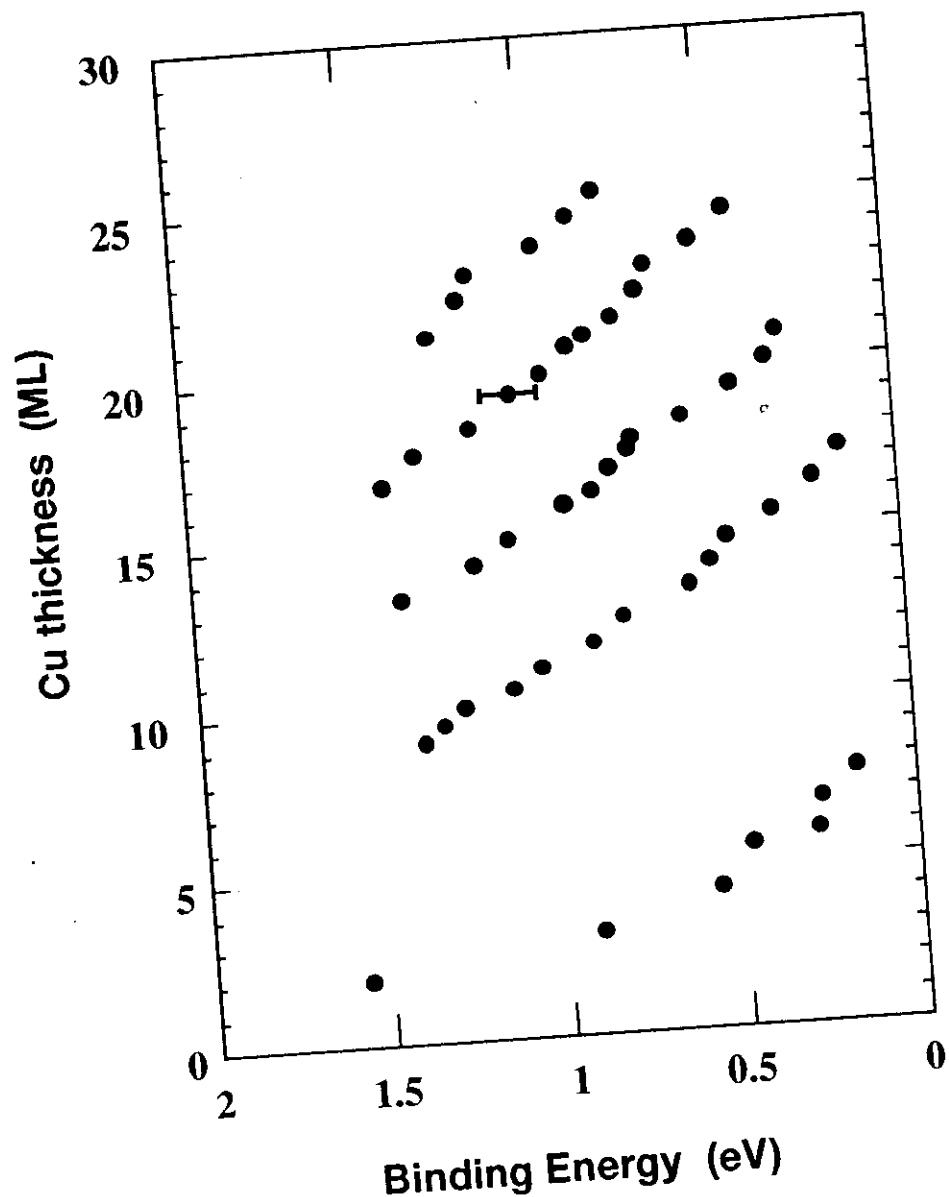


## Spin polarisation of QW States in Cu/Co(100)



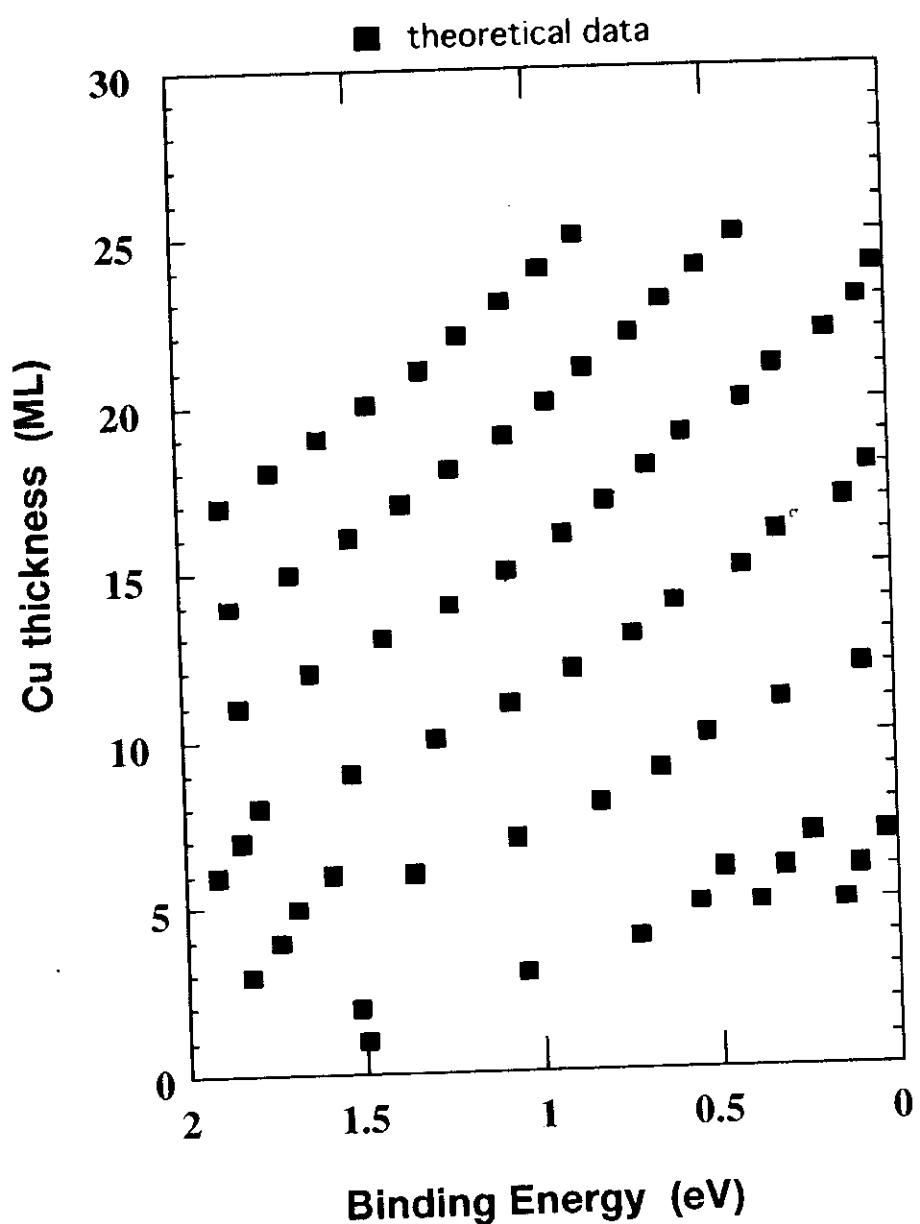
## Cu / Co(100)

● experimental data

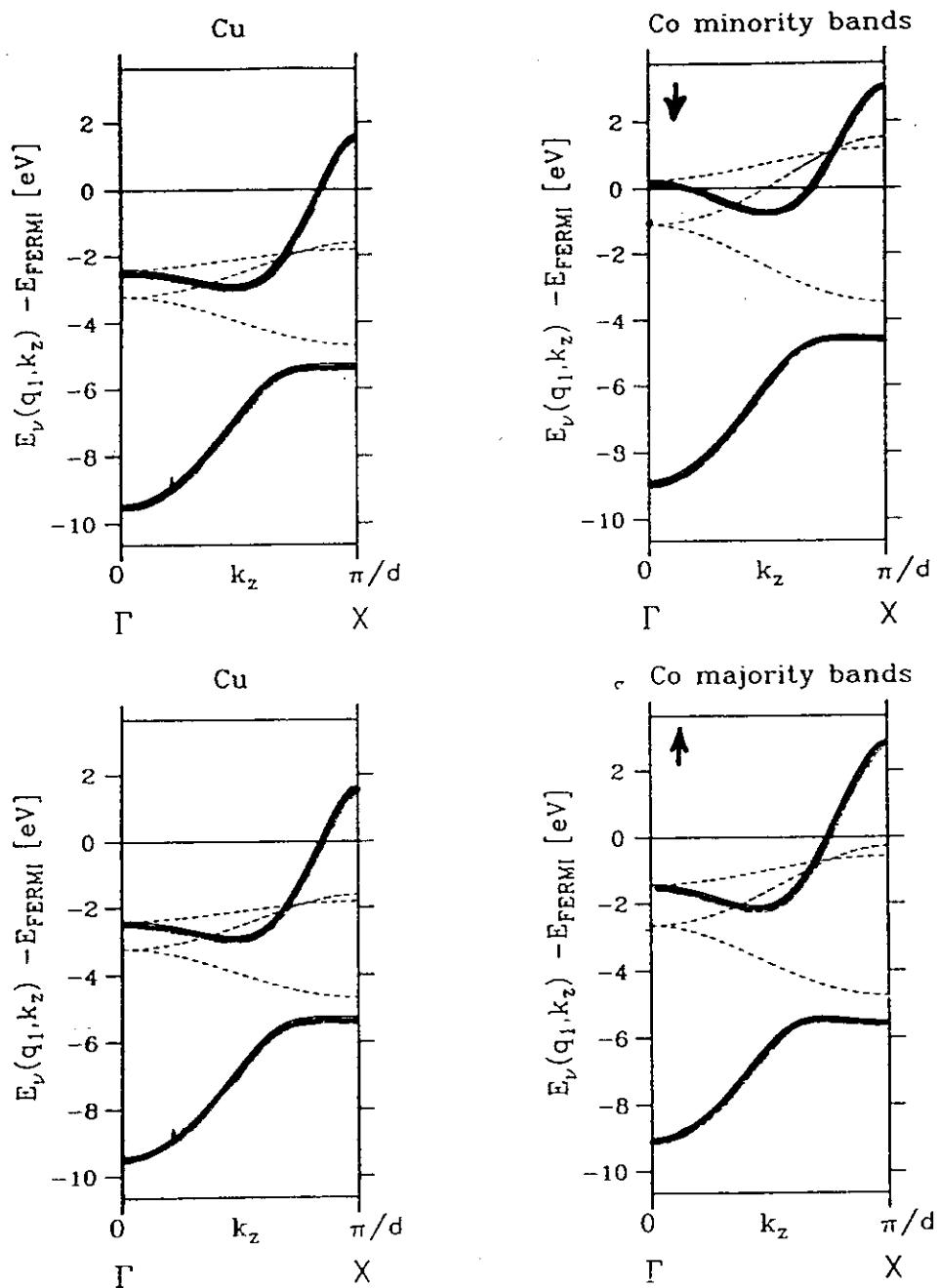


# Theory vs. Experiment

## Cu / Co(100)



# BAND STRUCTURE AT $\bar{\Gamma}$



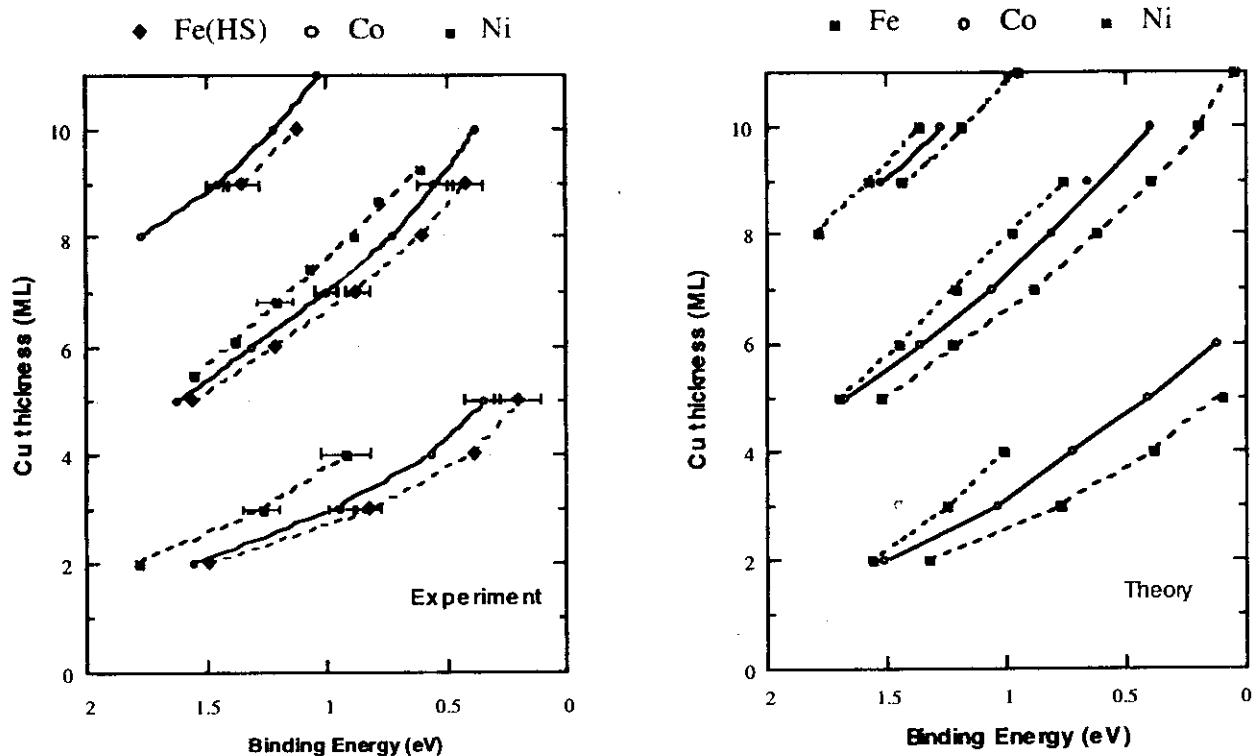
Interface reflectivity is spin dependent:

Minority-spin =====> strong reflection =====> QW

Majority-spin =====> weak reflection =====> Bloch states

# Experiment and Theory

## Cu films on Fe(100), Co(100), Ni(100)

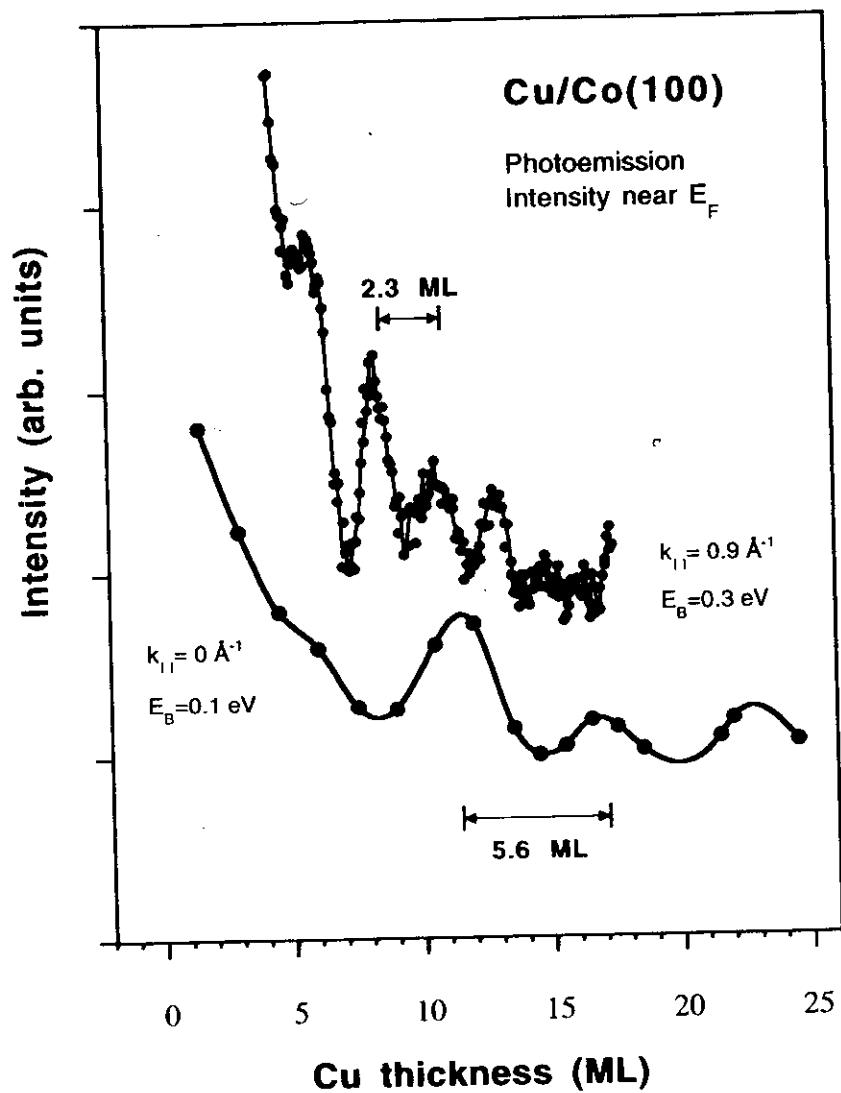


Binding energy of spin-down quantum well states → Phase shift in the interface reflection

$$2kd + \Phi_i + \Phi_v = 2n\pi$$

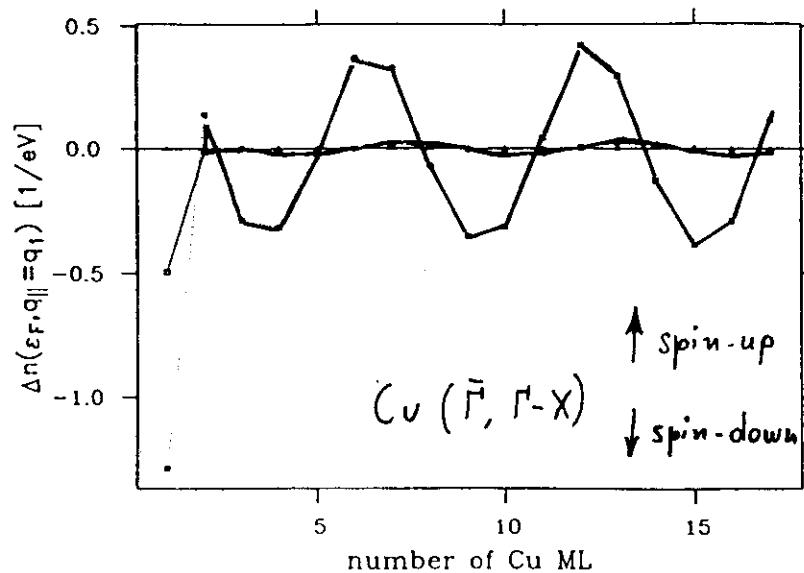
R. Kläsges et al. (1998)

## Long- and short-period oscillation near $E_F$ in Cu/Co(100)



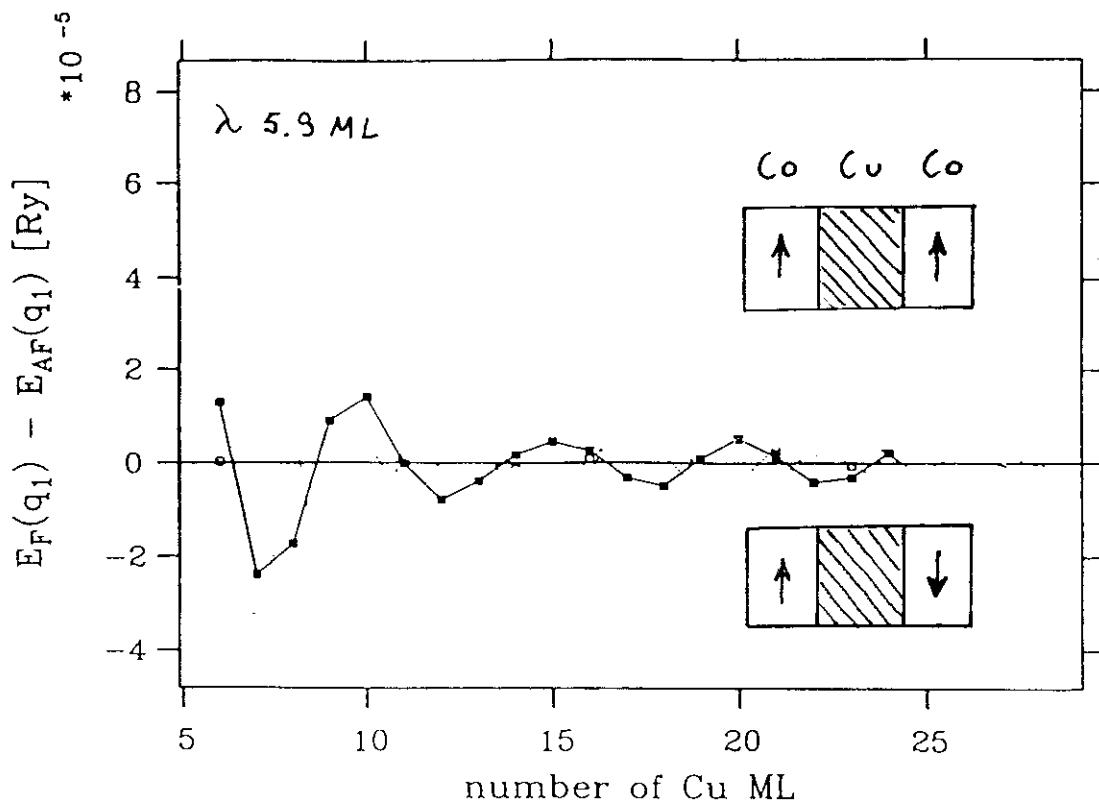
## THEORY

### Change of the Partial Density of States at $E_F$



### Exchange Coupling

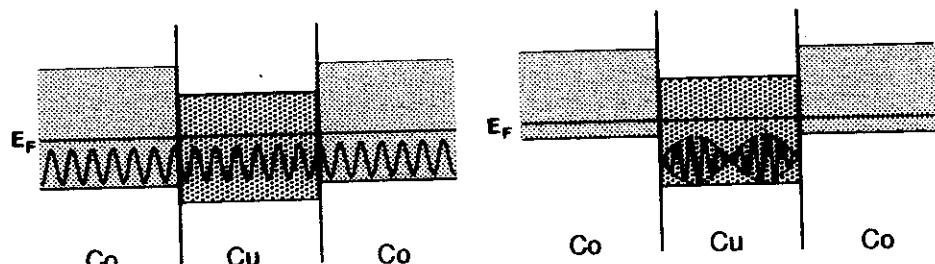
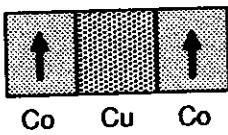
$11\text{ Co} / n\text{ Cu} / 11\text{ Co}$



## **Spin- Polarized QW States**

# Oscillatory Exchange Coupling

### **Parallel Coupling:**



### **Antiparallel Coupling:**

