

**Winter College on Optics and Photonics
7 - 25 February 2000**

1218-1

"Fiber Optics: An Introduction"

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FIBER OPTICS

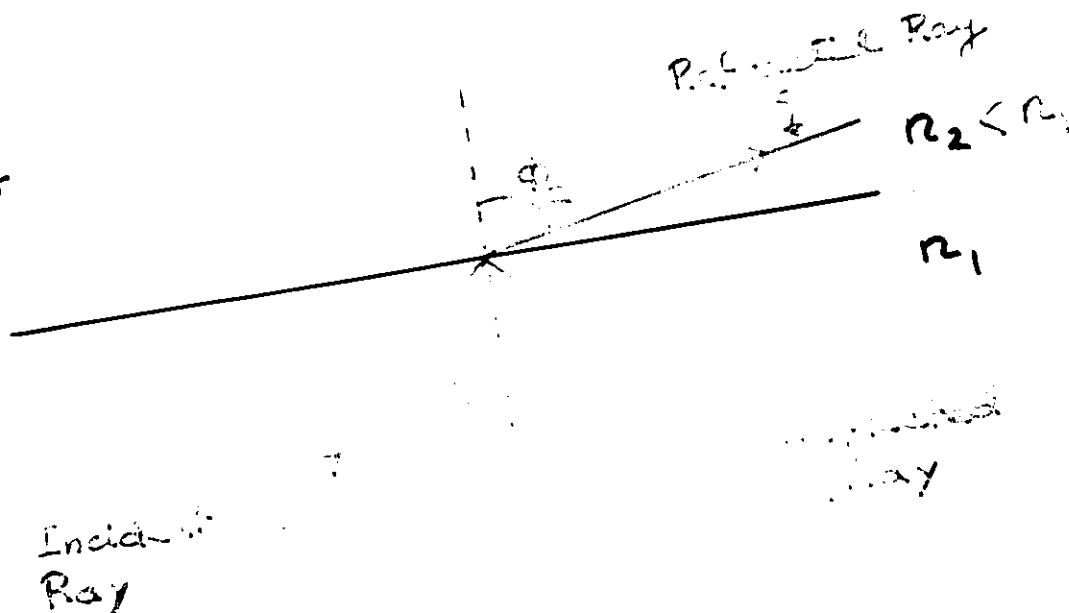
An Introduction

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Light Frequencies ($\sim 10^{14}$ Hz) - much

- Radio wave

$$n = \frac{c}{v}$$

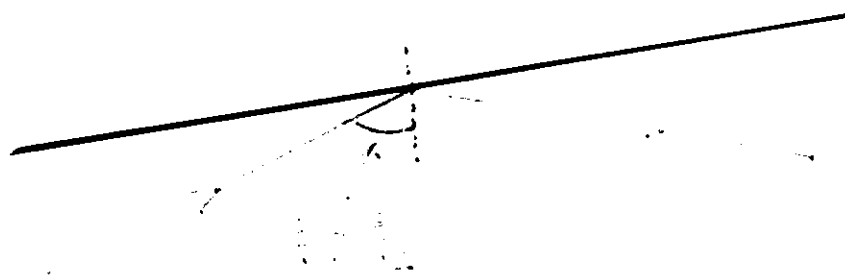


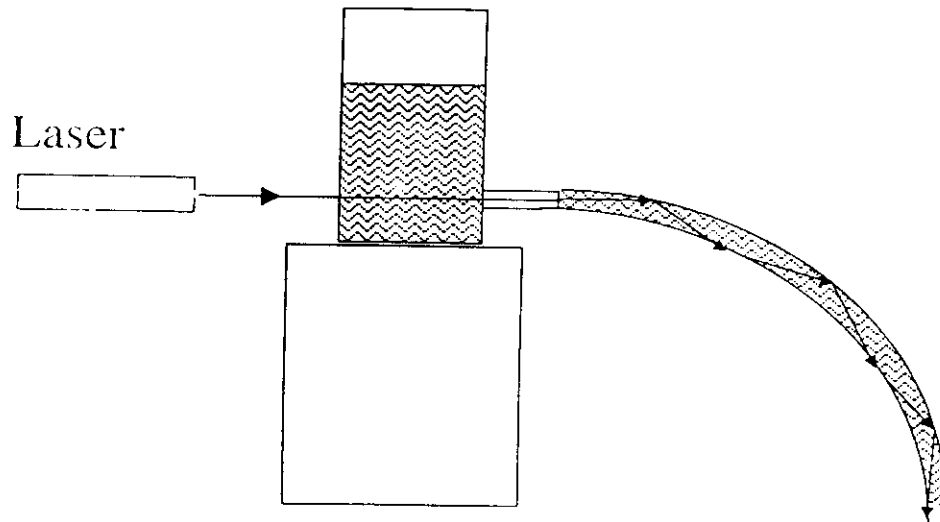
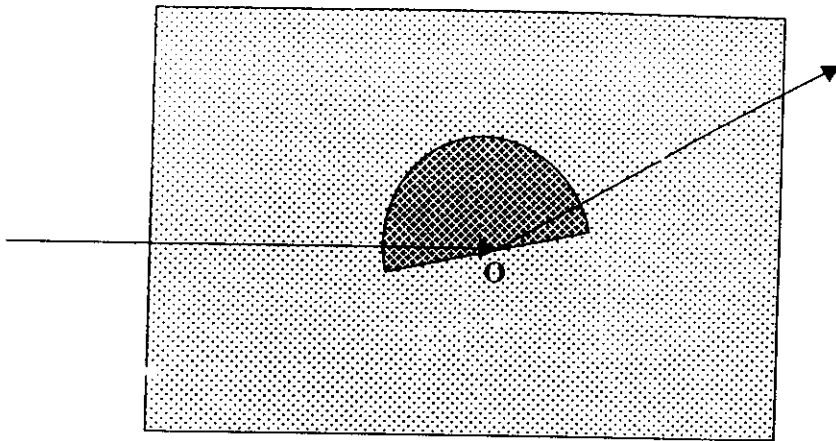
Snell's Law: $n_1 \sin \phi_1 = n_2 \sin \phi_2$

If $n_2 < n_1$

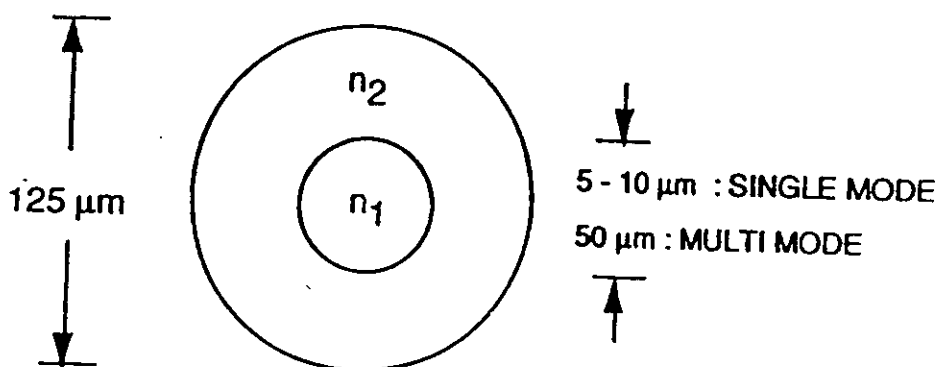
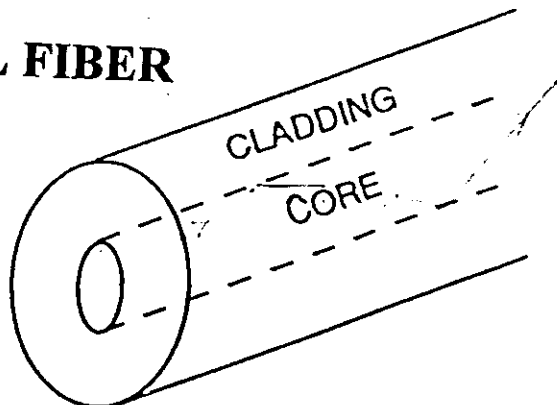
then $\phi_2 > \phi_1$

When $\phi_2 = 90^\circ$, $\phi_1 = \phi_c = \sin^{-1}\left(\frac{n_2}{n_1}\right)$

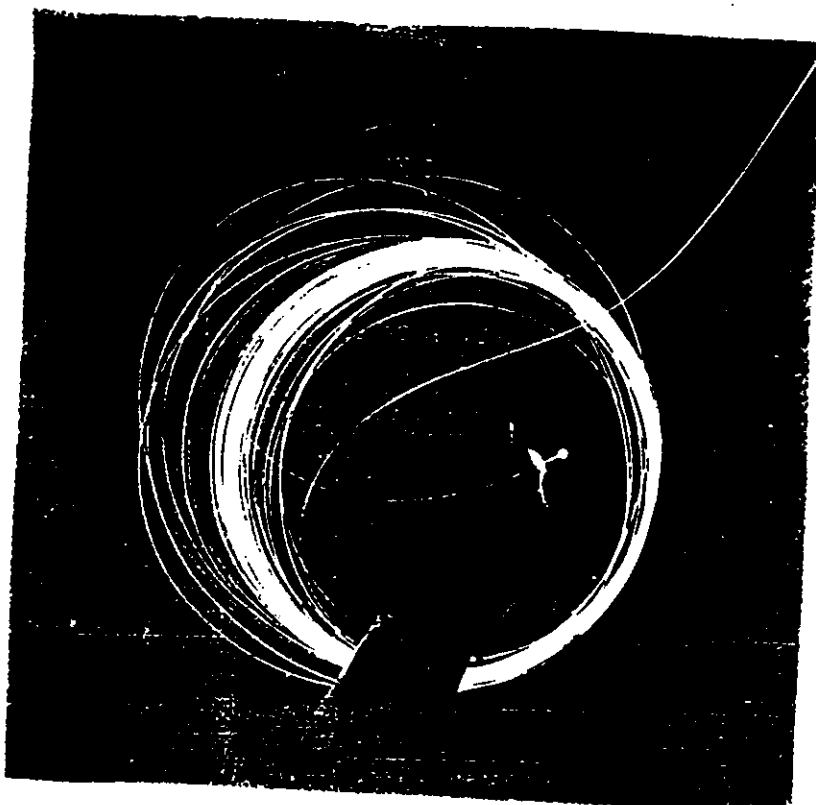




OPTICAL FIBER



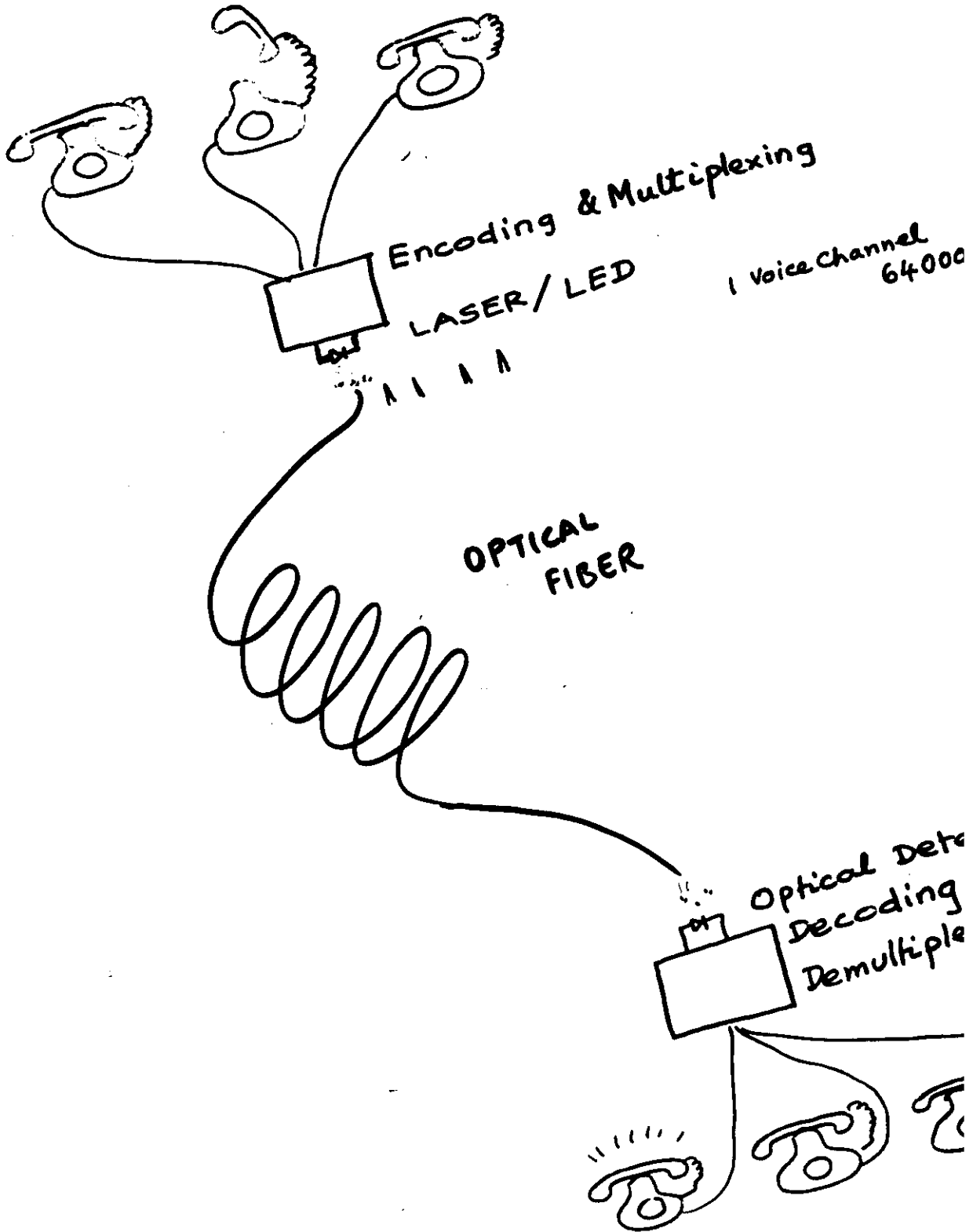
MATERIAL : DOPED SILICA



I-6

2 Gbits \leftrightarrow 68.5 kHz
 \Rightarrow 2M voice channel $\times 10$

I-6



Typical bit rates required

Service

Bit requirement

Telephone circuit

64×10^3 bits/s

1000 words of text

60×10^3 bits

20 Volume encyclopaedia

3×10^8 bits

Standard TV

100×10^6 bits/s

1.2×10^9 bits/s

A typical SMF can carry

1 Gbit/s for 40 km
without any repeater

To transmit 1 voice channel

\Rightarrow 64000 bits/s

Thus one fiber can carry

$$\frac{10^9}{64000} \approx 15,000 \quad \text{voice channels for 40 km}$$

To transmit 1 TV channel

\Rightarrow 100 Mbits/s

Thus one fiber can carry

$$\frac{10^9}{100 \times 10^6} \approx 10 \quad \text{TV channels for 40 km}$$

ADVANTAGES

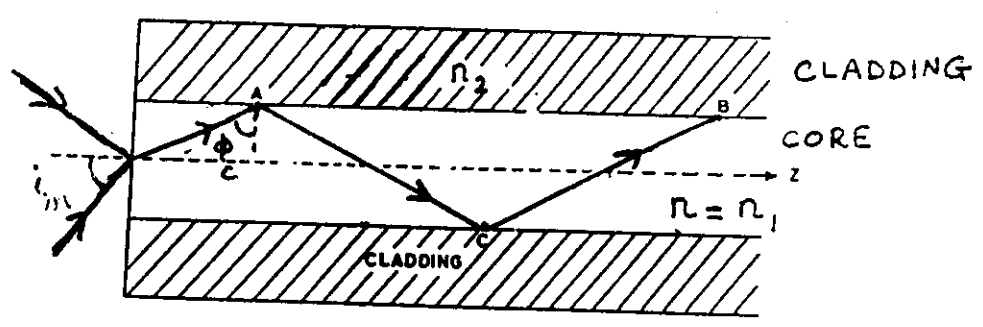
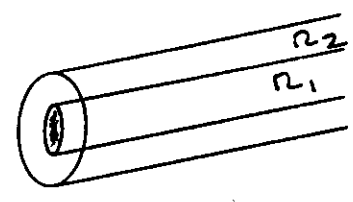
- # Very large information carrying capacity:
 - 10 GBits / Sec over 9000 Km
 - = 1.4 Billion voice channels. kilometer
- # Very low loss
 - * Large repeater spacing
 - * With optical amplifiers 10,000 km repeater spacing possible
- # Light weight and low volume
- # Very little cross talk and secure
- # Little electromagnetic interference .
- .
- .

Two important characteristics of any digital communication system

LOSS

PULSE BROADENING

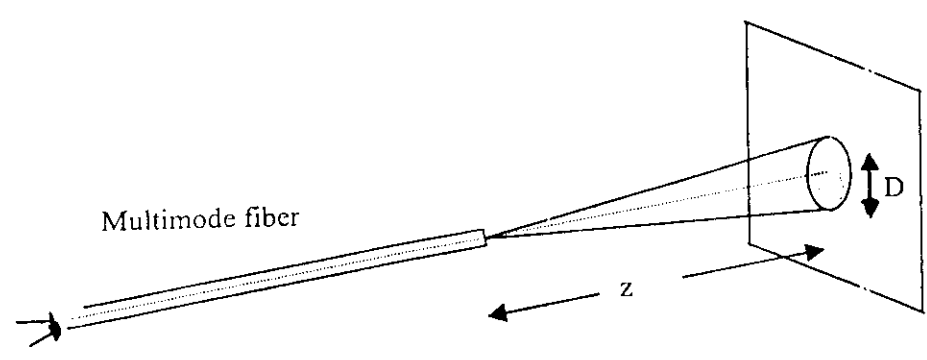
Numerical Aperture: NA

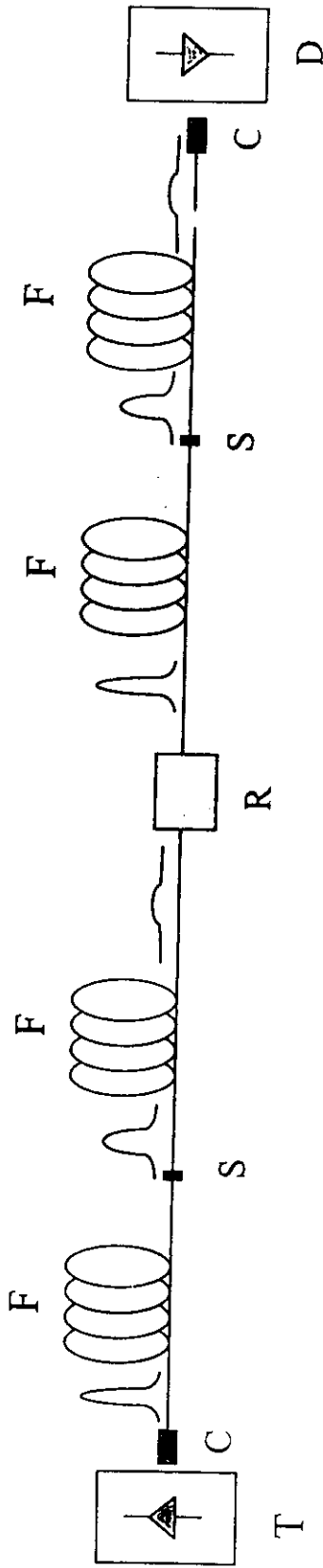


$$NA = \sin i_m = \sqrt{n_1^2 - n_2^2}$$

$$n_1 = 1.48 ; n_2 = 1.46$$

$$\Rightarrow NA = 0.24 \quad \& \quad i_m \approx 14^\circ$$



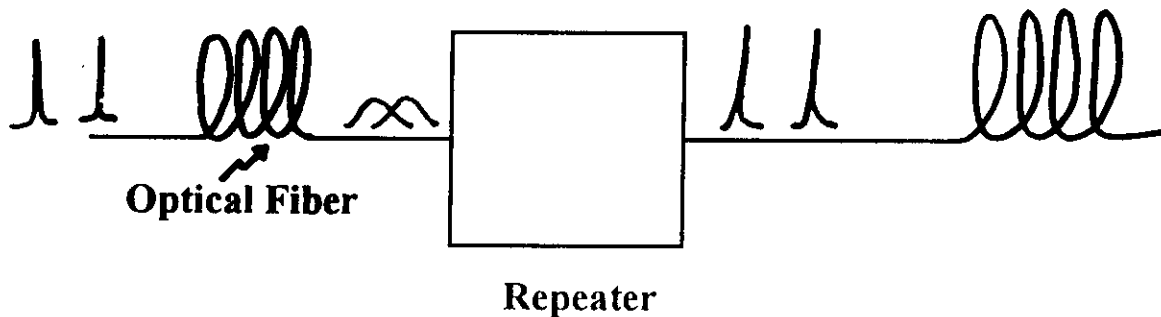


- T Transmitter
- C Connector
- F Fiber
- S Splice
- R Repeater
- D Detector

- Optical fibers have revolutionized the field of communication
- More than 80 million kilometers of fibers world wide carrying traffic
- Two important characteristics of any digital communication system

1. **LOSS**

2. **PULSE BROADENING**



To reduce cost

Repeater spacing should be large

⇒

Attenuation should be small

&

Pulse Broadening should be small

Loss of power in decibels

$$\alpha = 10 \log_{10} \frac{P_1}{P_2}$$

P_1 : input power
 P_2 : output power

$$\text{If } P_2 = \frac{1}{2} P_1$$

$$\Rightarrow \alpha = 10 \log 2 \approx 3 \text{ dB}$$

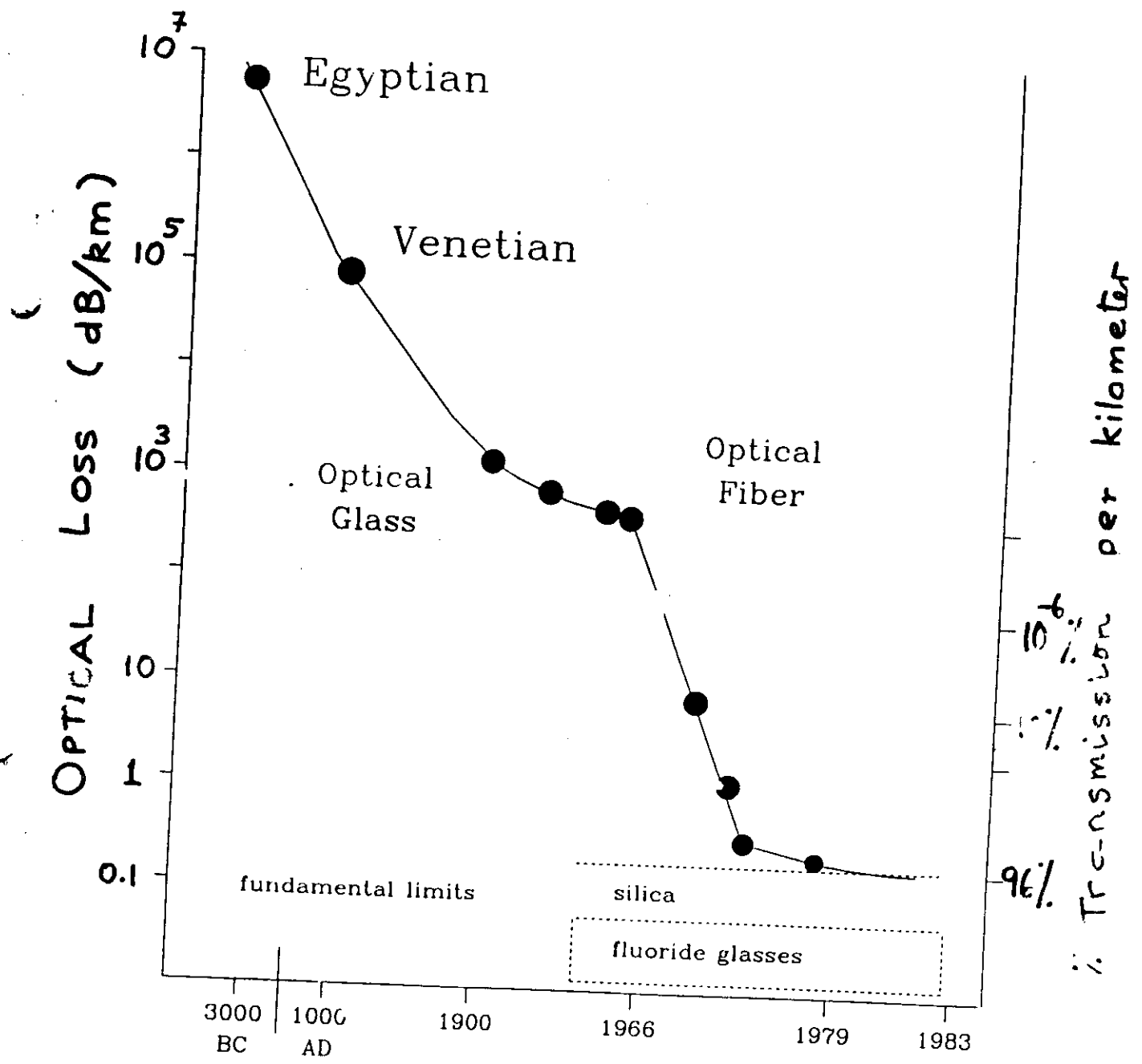
$\Rightarrow 3 \text{ dB loss} \equiv 50\% \text{ Power loss}$

$$\text{If } P_2 = \frac{1}{1000} P_1$$

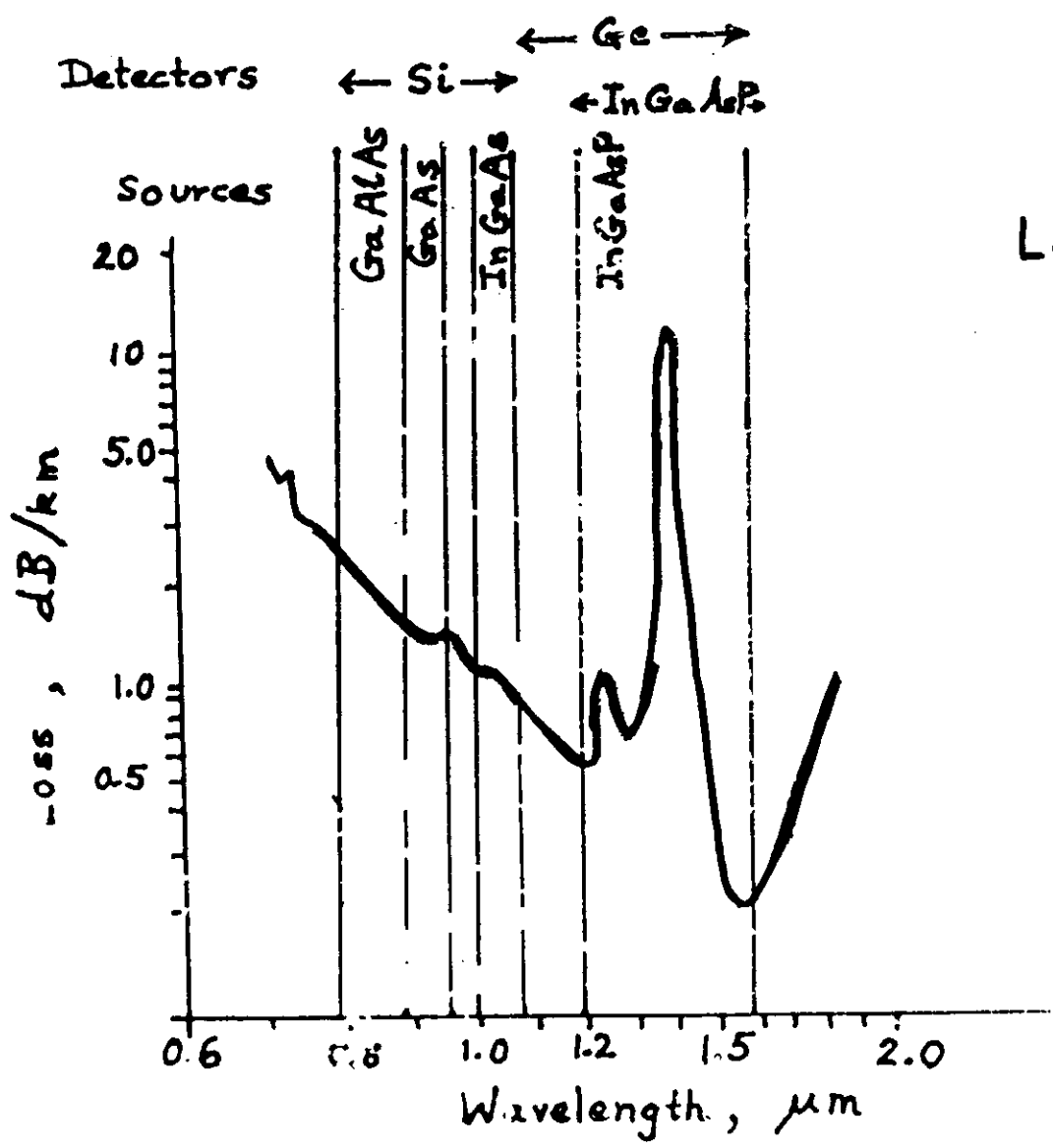
$$\Rightarrow \alpha = 10 \log 1000 = 30 \text{ dB}$$

Thus

30 dB loss \equiv Power loss by a factor of 1000



3 dB \Leftrightarrow 50% power loss



$$\text{Loss (dB)} = 10 \log \frac{P_{in}}{P_{out}}$$

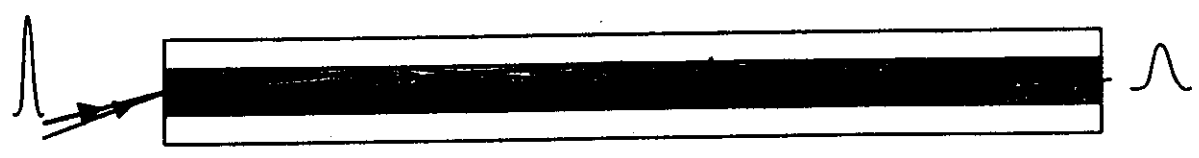
0.2 dB/km \Leftrightarrow 96% transmission in 1 km

Why Glass Fibers ?

Glass is a remarkable material which has been use for at least 9000 years. The three most important properties of glass are:

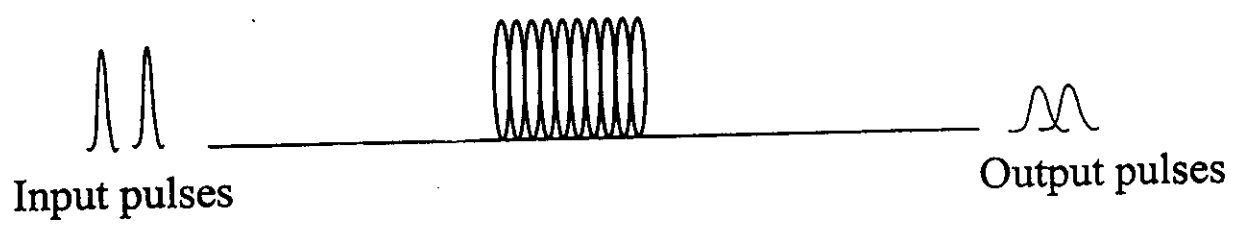
1. Glass does not solidify at a discrete freezing temperature but gradually becomes stiffer and stiffer and eventually becomes hard. In the transition region it can be easily drawn into a thin fiber.
2. Highly pure silica is characterized with extremely low light transmission loss. Today, in most commercially available silica fibers, 96% of the power gets transmitted after propagating through 1 km of optical fiber.
3. The third most remarkable property is the intrinsic strength of glass. Its strength is about $2,000,000 \text{ lb/in}^2$ so that a glass fiber of the type used in the telephone network and having a diameter of about $125 \mu\text{m}$ can support a load of about 40 lb.

• What is pulse dispersion ?



The two rays of light propagating in the fiber take different times to reach the other end

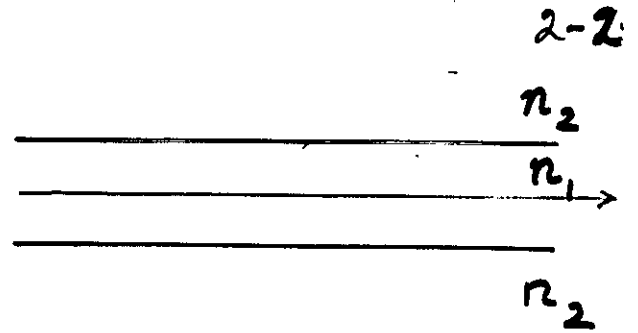
PULSE DISPERSION



Larger pulse dispersion → Smaller possible bit rate

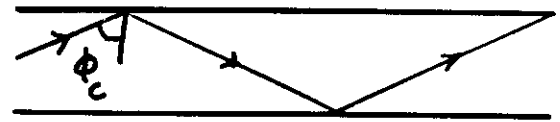
$$\tau_{\min} = \frac{L}{c/n_1}$$

$$= \frac{n_1 L}{c}$$



$$\tau_{\max} = \frac{L/\sin\phi_c}{c/n_1}$$

$$= \frac{n_1^2 L}{c n_2}$$



$$\sin\phi_c = \frac{n_2}{n_1}$$

Pulse dispersion

$$\Delta\tau = \tau_{\max} - \tau_{\min}$$

$$= \frac{n_1 L}{c} \left[\frac{n_1 - n_2}{n_2} \right]$$

$$\Delta = \frac{n_1 - n_2}{n_2} \approx 0.01 ; n_1 \approx 1.5 ; L = 1 \text{ km}$$

$$c = 3 \times 10^8 \text{ m/s}$$

$$\Rightarrow \Delta\tau \approx 50 \text{ ns/km}$$

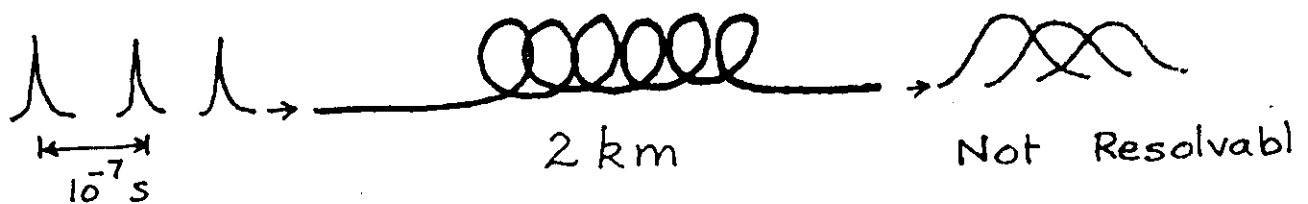
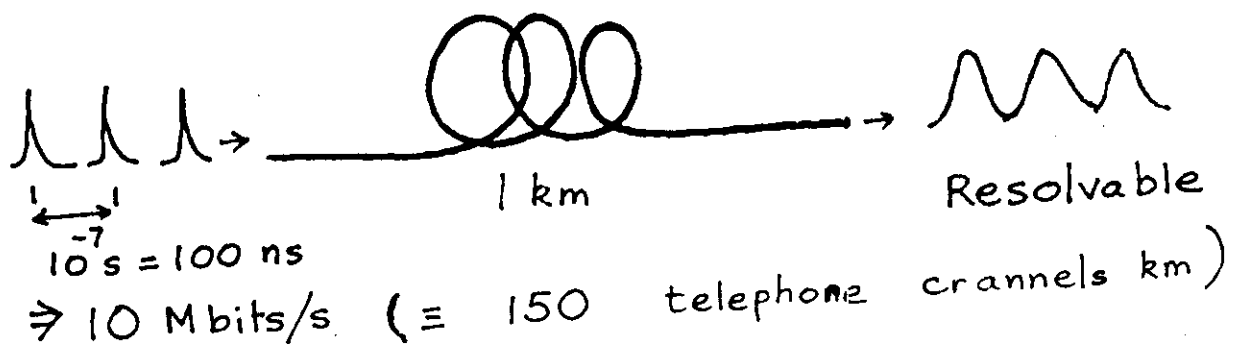
Intermodal Dispersion

Pulse Dispersion $\Delta\tau = \frac{L}{c} n_1 \left(\frac{n_1 - n_2}{n_2} \right)$

Typical Values

$$n_1 = 1.46, \quad \Delta = \frac{n_1 - n_2}{n_2} \approx 0.01, \quad L = 1 \text{ km}$$

$$\Rightarrow \Delta\tau = 50 \text{ ns/km}$$

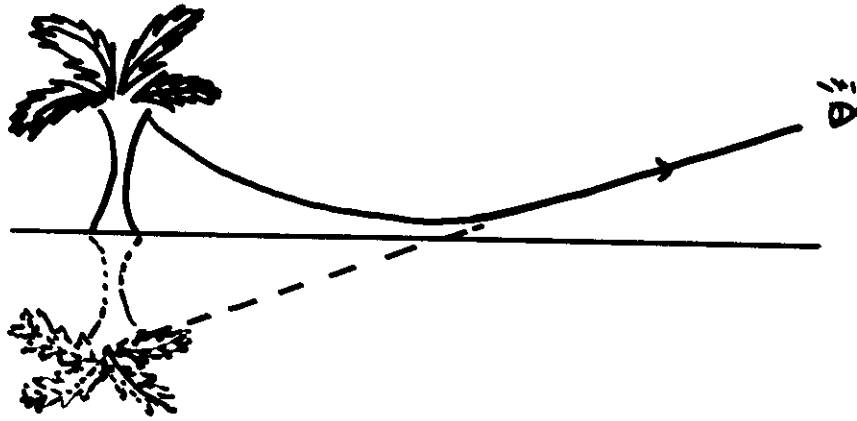


For large information carrying capacity, one must reduce pulse dispersion

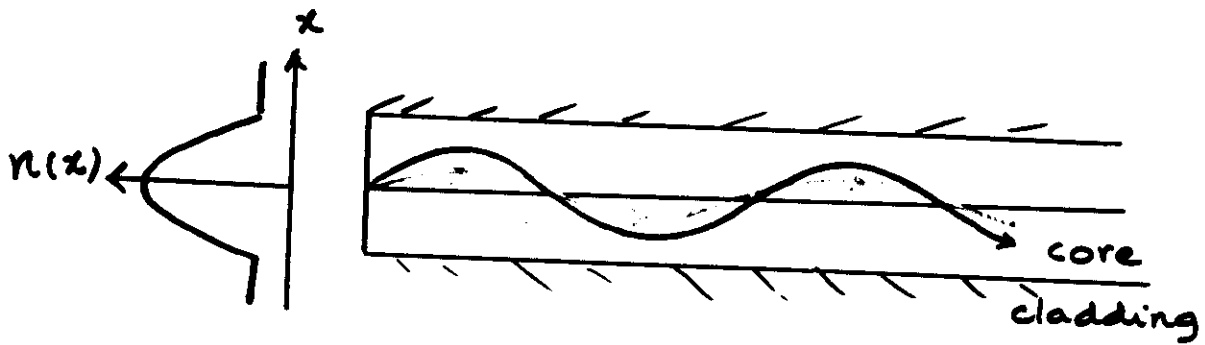
Two alternative solutions:

- (a) GRADED INDEX (Multimode) Fibers
- (b) SINGLE MODE Fibers

Graded index medium



Graded index fiber



Greater path lengths almost compensated by an increased velocity of propagation

⇒ Less pulse dispersion

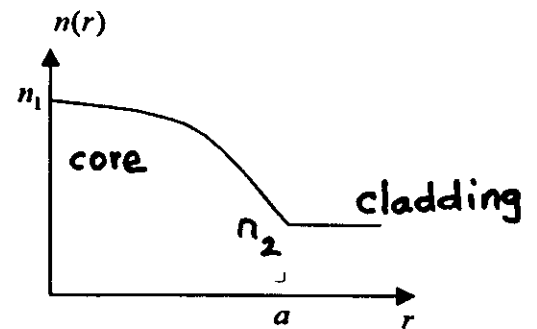
reduction by almost a factor of 1000 as compared to step index fibers

Optimum profile ⇒ Nearly parabolic

Parabolic Index Fiber

$$n^2(r) = n_1^2 \left[1 - 2\Delta \left(\frac{r}{a} \right)^2 \right] \quad 0 < r < a$$

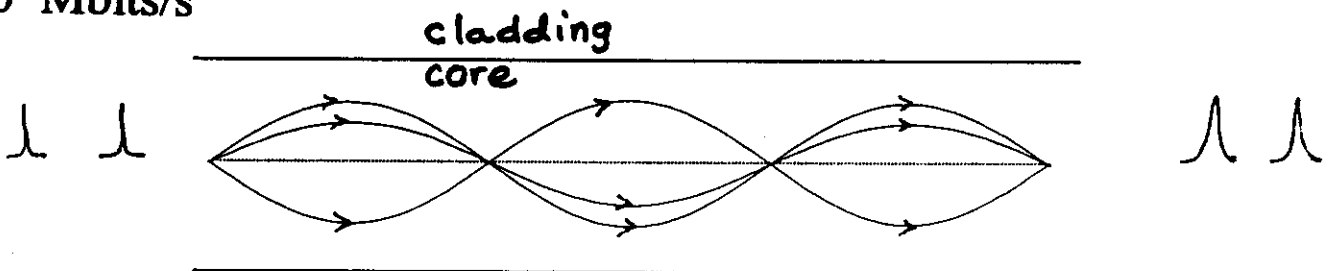
$$= n_2^2 = n_1^2 (1 - 2\Delta) \quad r > a$$



Intermodal dispersion : $(\Delta\tau)_i = \frac{n_1 L}{2c} \Delta^2$

$$n_2 \approx 1.5, L = 1 \text{ km}, \Delta \approx 0.01 \Rightarrow (\Delta\tau)_i \approx \frac{1}{4} \text{ ns/km}$$

50 Mbits/s



Pulses will remain resolvable even after about 10 km length of the fiber.

Greater path length is compensated by greater average velocity leading to smaller pulse broadening.

Figure B.3 shows a typical refractive index profile, obtained by Pearson *et al.* (1969), in a 30 mole% Li_2O , 15 mole% Al_2O_3 , 55 mole% SiO_2 glass rod of 1.90 mm diameter, during an ion exchange in a 50 mole% NaNO_3 , 50 mole% LiNO_3 fused salt bath at 470°C for 50 hr. As can be seen from the figure, the refractive index profile is very nearly parabolic. The refractive index at the axis of the rod is approximately 1.539.

The details of the experimental procedure can be found at many places; see, for example, Kitano *et al.* (1970) and Pearson *et al.* (1969).

B.2. The New SELFOC Fibers

The manufacturing process of the SELFOC fibers as discussed in Sec. B.1 is not only time consuming but it also cannot be used for continuous fabrication of fibers. In a recent paper Koizumi *et al.* (1974) have reported the fabrication of SELFOC fibers by a single continuous process, which makes mass production feasible. Further, the refractive index gradient (i.e., the value of a_2) is so large that even if the fiber is bent randomly the

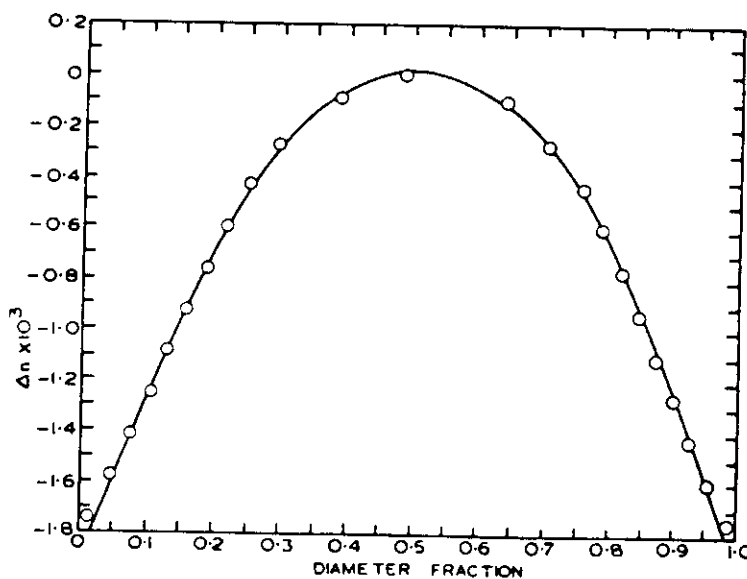


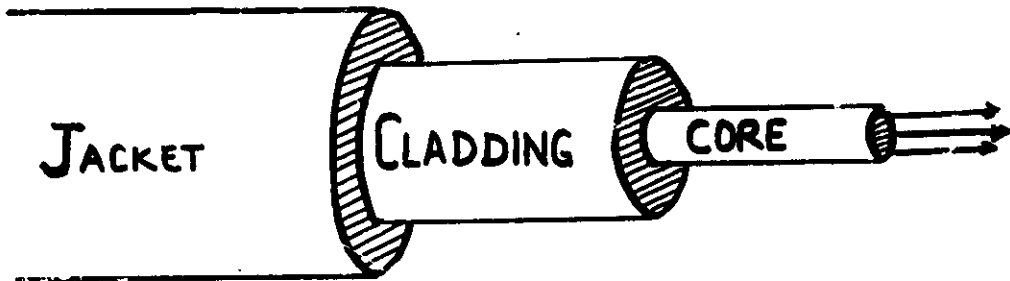
Fig. B.3. Measured refractive index profile of an ion-exchanged rod, normalized to a maximum of zero. The solid line is a parabola fitted to the experimental points by the least-squares method (after Pearson *et al.*, 1969; reprinted by permission).

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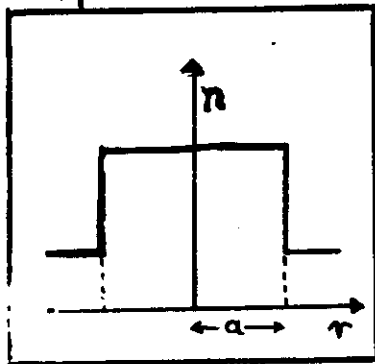
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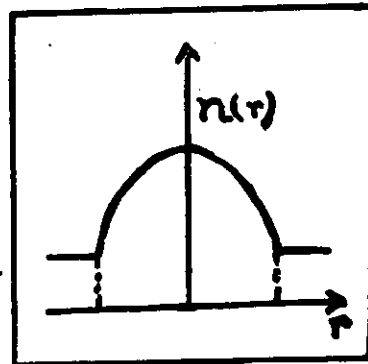
OPTICAL FIBERS



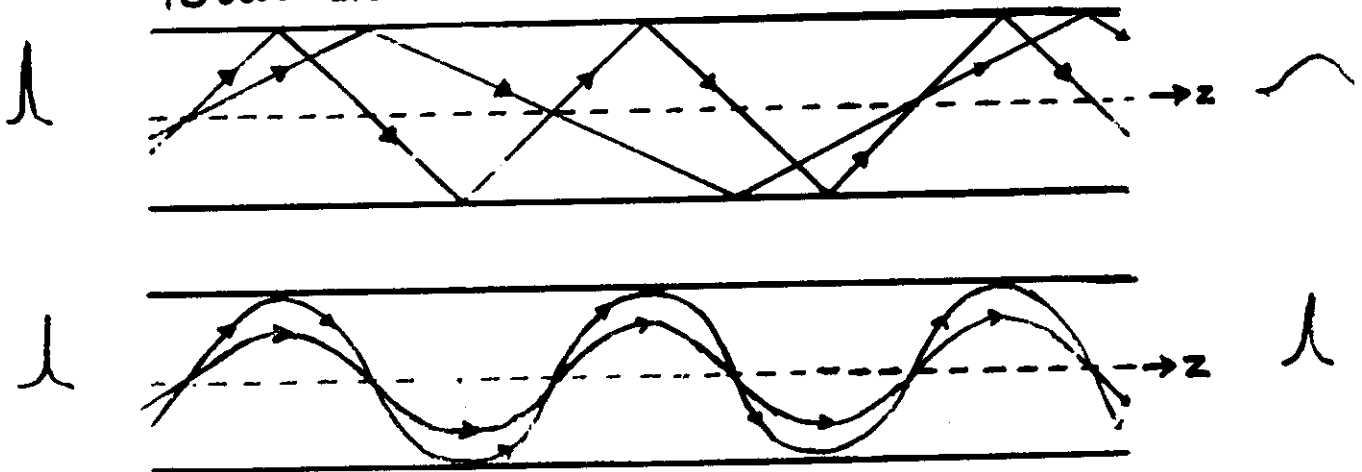
Step Profile



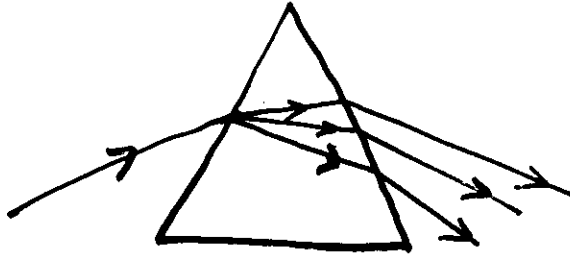
Graded Profile



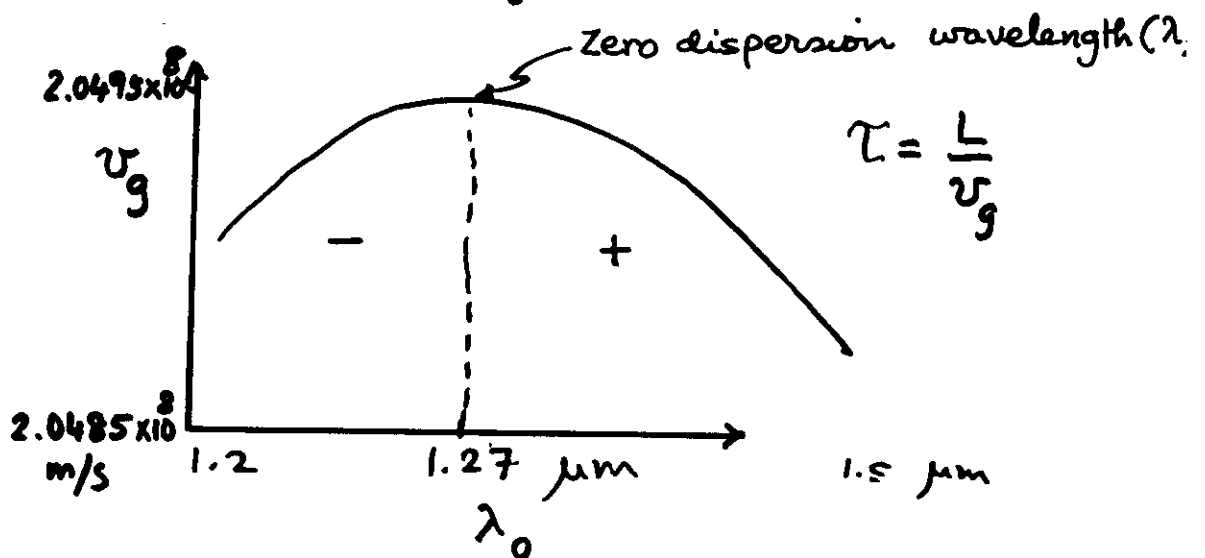
Total Internal Reflections



Material Dispersion [$n(\lambda)$]



Finite spectral width of
a source $\Delta\lambda_0$



$$\Delta\tau_m = -\frac{\lambda_0}{c} \frac{d^2n}{d\lambda_0^2} L \Delta\lambda_0$$

$$c \approx 3 \times 10^8 \text{ m/s}$$

Material Dispersion

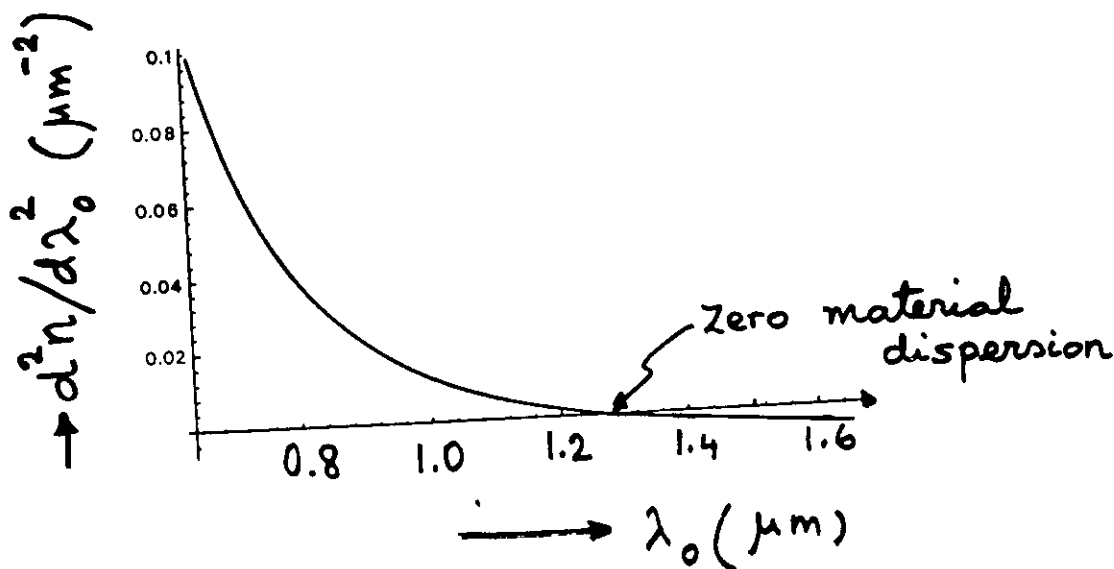
Plane Wave: $\Psi = A e^{i(\omega t - kz)}$

$$k(\omega) = \frac{\omega}{c} n(\omega) \quad ; \quad \omega = \frac{2\pi c}{\lambda_0}$$

$$\frac{1}{v_g} = \frac{dk}{d\omega} = \frac{1}{c} \left[n(\omega) + \omega \frac{dn}{d\omega} \right]$$

$$\tau = \frac{L}{v_g} = \frac{L}{c} \left[n(\lambda_0) - \lambda_0 \frac{dn}{d\lambda_0} \right]$$

$$(\Delta\tau)_m \frac{d\tau}{d\lambda_0} \Delta\lambda_0 = - \frac{\lambda_0 L}{c} \frac{d^2 n}{d\lambda_0^2} \Delta\lambda_0$$



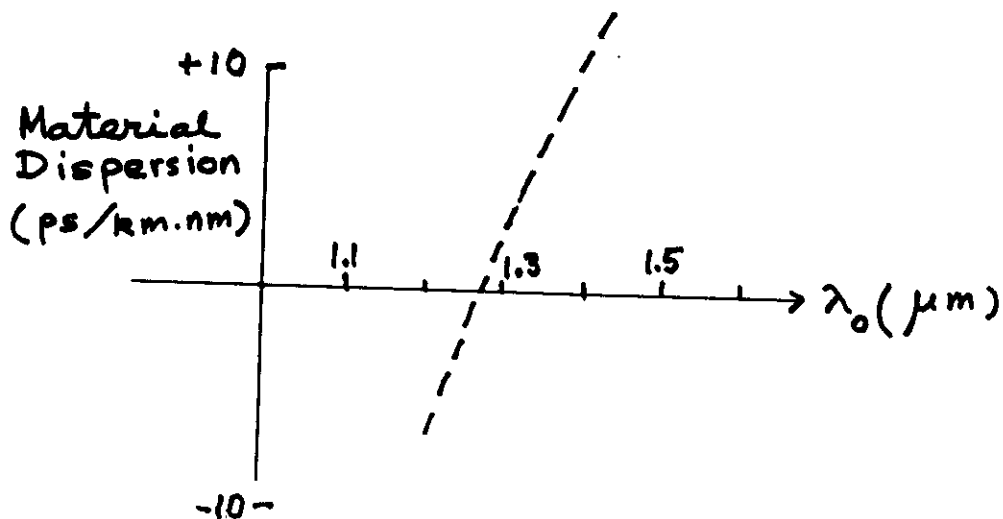
$$\Delta\tau_m = -\frac{\lambda_0 L}{c} \frac{d^2 n}{d\lambda_0^2} \Delta\lambda_0$$

Material Dispersion parameter

$$D_m \equiv \frac{\Delta\tau_m}{L \Delta\lambda_0} = -\frac{1}{\lambda_0 c} \left(\lambda_0^2 \frac{d^2 n}{d\lambda_0^2} \right)$$

$$\approx -\frac{10^4}{3\lambda_0} \left(\lambda_0^2 \frac{d^2 n}{d\lambda_0^2} \right) \text{ ps/km.nm}$$

(λ_0 is measured in μm)



For pure silica

$$D_m \sim -84.2 \text{ ps/km.nm} \quad (\lambda_0 \approx 0.850 \mu\text{m})$$

$$\sim +2.4 \text{ ps/km.nm} \quad (\lambda_0 \approx 1.3 \mu\text{m})$$

$$\sim +21.5 \text{ ps/km.nm} \quad (\lambda_0 \approx 1.55 \mu\text{m})$$

I Generation Optical Communication Systems (~ 1977)

Parabolic Index Multimode Fibers $\Delta\tau_i \gtrsim \frac{1}{4}$ ns/km

LED's at $0.85 \mu\text{m}$ ($\Delta\lambda_0 \approx 25$ nm) Loss ~ 3 dB/km

$$\Delta\tau_m \approx 84 \text{ ps/km.nm} \times 25 \text{ nm} \approx 2.1 \text{ ns/km}$$

Bit rate ~ 45 Mbits/s \Rightarrow Repeater Spacing ~ 10 km

II Generation Optical Communication Systems (~ 1981)

Parabolic Index Multimode Fibers $\Delta\tau_i \sim \frac{1}{4}$ ns/km

LED's at $1.3 \mu\text{m}$ ($\Delta\lambda_0 \approx 25$ nm) Loss ~ 1 dB/km

$$\Delta\tau_m \approx 2.4 \text{ ps/km.nm} \times 25 \text{ nm} \approx 0.06 \text{ ns/km}$$

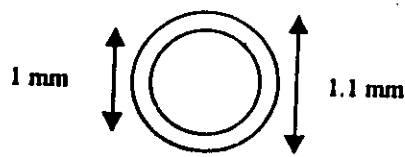
Bit rate ~ 45 Mbits/s \Rightarrow Repeater Spacing ~ 30 km

Table 13.1. Typical characteristics of fiber optic communication systems at different stages

Generation	Date	Bit rate	Type of fiber	Loss (dB/km)	Repeater spacing (km)
I (0.8-0.9 μm)	1977	~45 Mbit/s	Multimode (graded index)	~3	~10
II (1.3 μm)	1981	~45 Mbit/s	Multimode (graded index)	~1	~30
III (1.3 μm)	At present	~2.5 Gb/s	Single mode	≤0.5	~40
IV (1.55 μm)	At present	≥10 Gb/s	Single mode	<0.3	≥100

Note: Futuristic system: WDM, solitons. Infrared fibers ($\lambda_0 > 2 \mu\text{m}$); extremely low loss ($< 10^{-2}$ dB/km); \Rightarrow repeater spacing > 1000 km.

Plastic Optical Fibers (POF)



$$n_1 = 1.49 \text{ (PMMA)}$$

$$n_2 = 1.40 \text{ Polymethyl Methacrylate}$$

$$NA = \sqrt{1.49^2 - 1.40^2} \approx 0.51$$

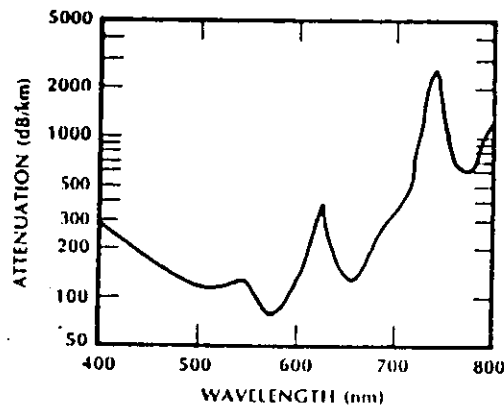
$$\Rightarrow i_m \approx 31^\circ \text{ (very large NA)}$$

Easy splicing/alignment

Low loss windows at

570 nm, 650 nm & 780 nm

At 650 nm : Loss ≈ 110 dB/km



POF's are expected to provide low cost solution to short distance communications (LAN's)

GI POF \rightarrow \sim few hundred Mbits/s

Schrodinger equation solutions

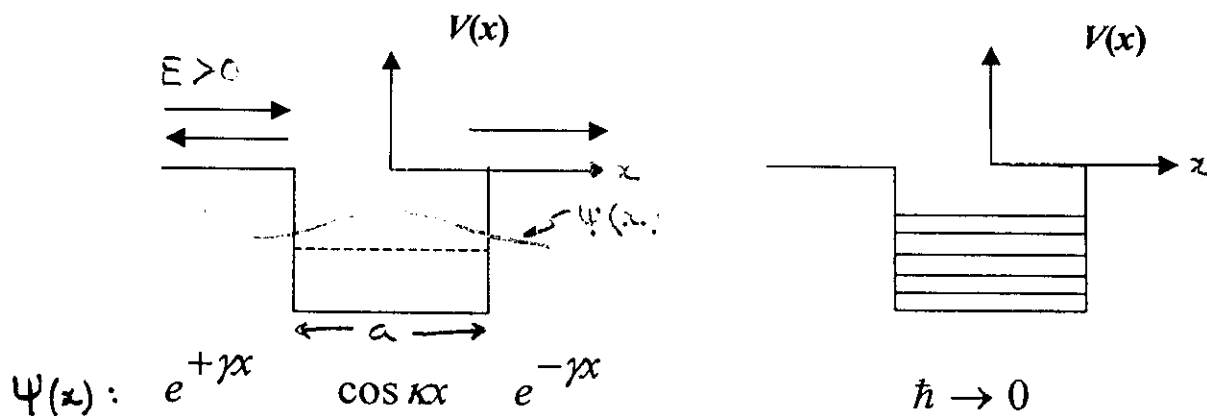
$$V = V(x)$$

$$\Psi(x,t) = \psi(x)e^{-iEt/\hbar} \quad \text{stationary states}$$

$$\frac{d^2\psi}{dx^2} + \frac{2\mu}{\hbar^2}[E - V(x)]\psi(x) = 0$$

$$V(x) = -V_0 \quad |x| < a/2$$

$$= 0 \quad |x| > a/2$$



For $\sqrt{\frac{2\mu V_0 a^2}{\hbar^2}} < \pi$ only one bound state

In general,

$-V_0 < E < 0$ finite number of bound states

$E > 0$ continuum scattering states

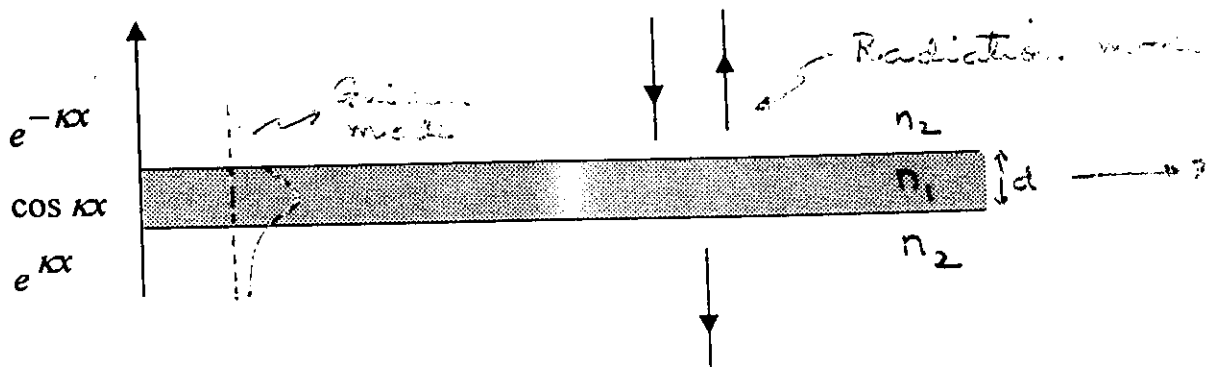
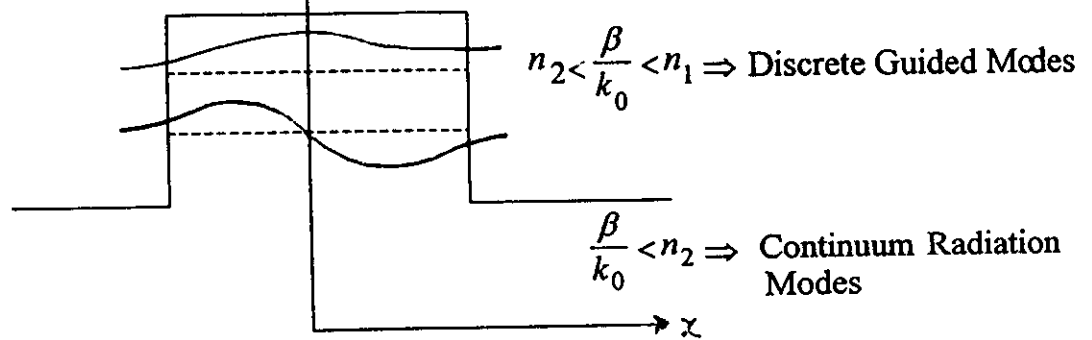
$$n = n(x) \Rightarrow E_y = \psi(x) e^{i(\omega t - \beta z)} \quad (\text{TE modes})$$

$$\frac{d^2\psi}{dx^2} + [k_0^2 n^2(x) - \beta^2] \psi(x) = 0 \quad k_c = \frac{2\pi}{\lambda_0} = \frac{\omega}{c}$$

$$n(x) = n_1; |x| < d/2$$

$$= n_2; |x| > d/2$$

$$\frac{\beta}{k_0} = n_{\text{eff}}$$



$$n_1 = 1.50, \quad n_2 = 1.48, \quad d = 3.9 \mu\text{m}$$

$$\text{For } \lambda_0 = 1 \mu\text{m}; \quad \frac{\beta}{k_0} \approx 1.497 \quad (\text{symm TE modes})$$

$$\frac{\beta}{k_0} \approx 1.488 \quad (\text{antisymm TE modes})$$

Field in the core

$$E_y = A \cos \kappa x e^{i(\omega t - \beta z)}$$

$$= 2 A e^{i(\omega t - \beta z + \kappa x)} + 2 A e^{i(\omega t - \beta z - \kappa x)}$$

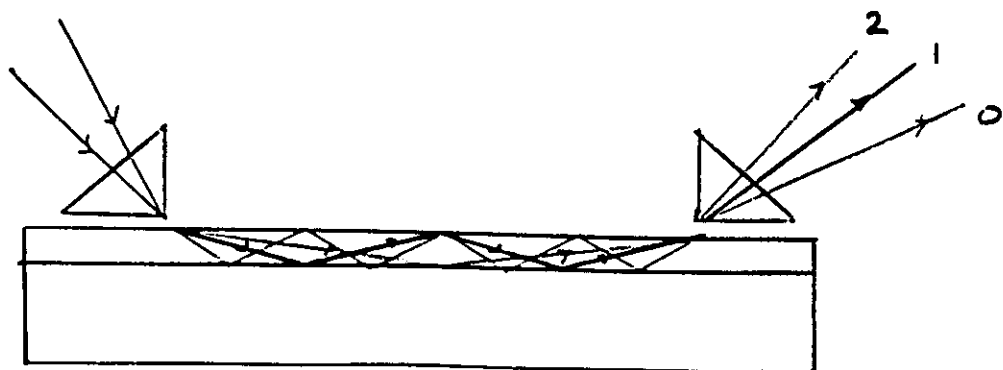
$$\text{Plane Wave: } e^{i(\omega t - \mathbf{k} \cdot \mathbf{r})} = e^{i(\omega t - k_x x - k_y y - k_z z)}$$

$$k_x = \mp \kappa \quad ; \quad k_y = 0 \quad ; \quad k_z = \beta$$

$$\cos \theta = \frac{k_z}{k} = \frac{\beta}{k_0 n_1} \Rightarrow \theta \approx 3.6^\circ \quad (\text{symm TE mode})$$

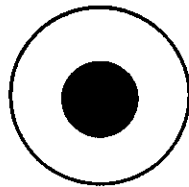
$$\approx 7.1^\circ \quad (\text{Antisymm TE mode})$$

Prism film coupling experiment



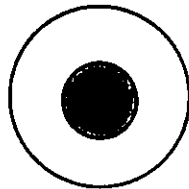
Fiber Types

Step Index
Multimode



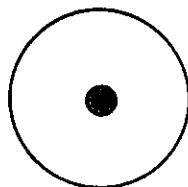
Core dia.: 100 - 200 μm
Cladding dia.: 140 - 240 μm
NA: 0.2 - 0.5

Graded Index
Multimode



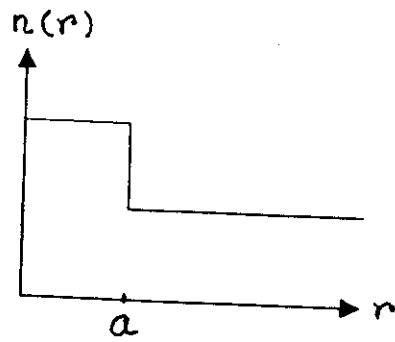
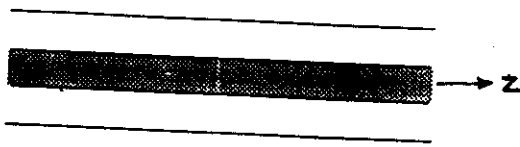
Core dia.: 50 - 85 μm
Cladding dia.: 125 μm
NA: 0.2

Singlemode



Core dia.: 9 μm
Cladding dia.: 125 μm

Step Index Fiber



$$n = n_1 \quad 0 < r < a$$

$$= n_2 \quad r > a$$

$$E(r, \phi, z, t) = R(r) \begin{cases} \cos l\phi \\ \sin l\phi \end{cases} e^{i(\omega t - \beta z)} \quad \text{LP}_{lm} \text{ modes}$$

$$\beta = \beta_{em}$$

$$R(r) = A J_l \left(U \frac{r}{a} \right) \quad 0 < r < a$$

$$= B K_l \left(W \frac{r}{a} \right) \quad r > a$$

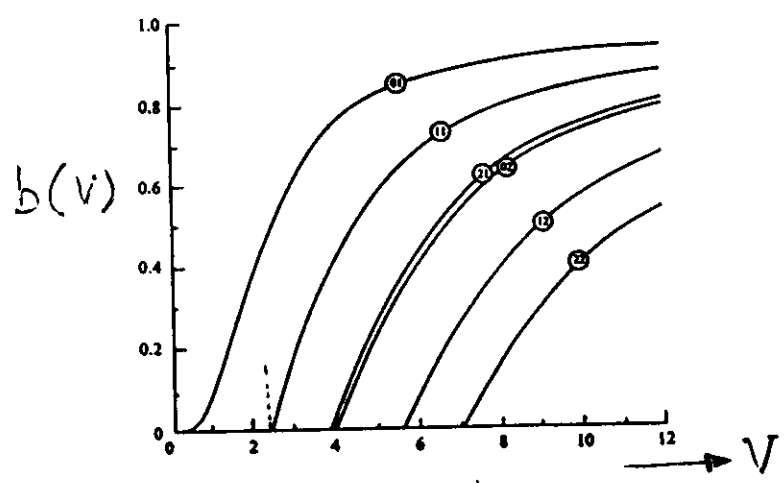
$$U \equiv V \sqrt{1-b} \quad ; \quad W \equiv V \sqrt{b}$$

$$V = \frac{2\pi}{\lambda_0} a \sqrt{n_1^2 - n_2^2} \quad b \approx \frac{\frac{\beta}{k_0} - n_2}{n_1 - n_2}$$

$$U \frac{J'_l(U)}{J_l(U)} = W \frac{K'_l(W)}{W}$$

$$\Rightarrow b = b(V)$$

$$b = b(V) ; \quad 0 < b < 1 \quad (n_2 < \frac{\beta}{k_0} < n_1)$$



$$V = \frac{2\pi}{\lambda_0} a \sqrt{n_1^2 - n_2^2} < 2.4048 \quad \text{SMF}$$

For the fundamental mode

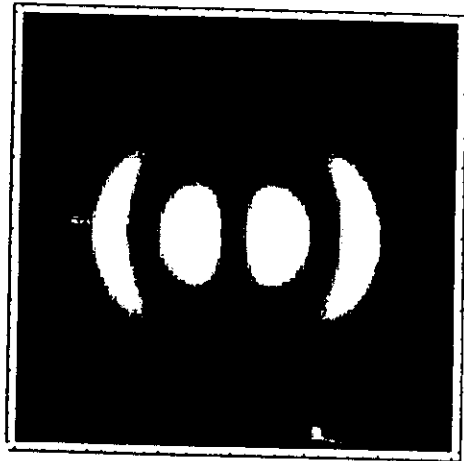
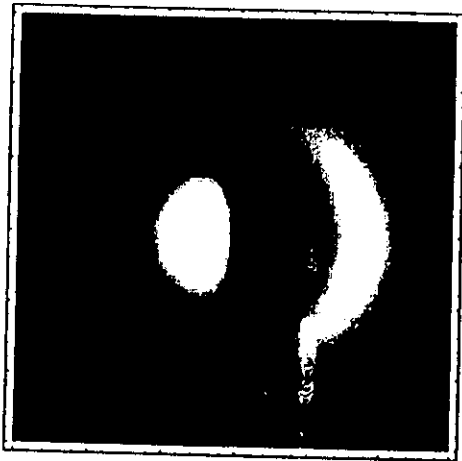
$$b(V) \approx \left[1.1428 - \frac{0.996}{V} \right]^2 ; \quad 1.5 \leq V \leq 2.5$$

$$b \approx \frac{\frac{\beta}{k_0} - n_2}{n_1 - n_2} \Rightarrow \beta = \frac{\omega}{c} [n_2 + b(V)(n_1 - n_2)]$$

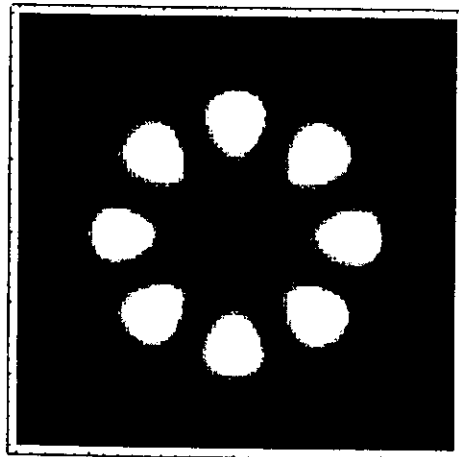
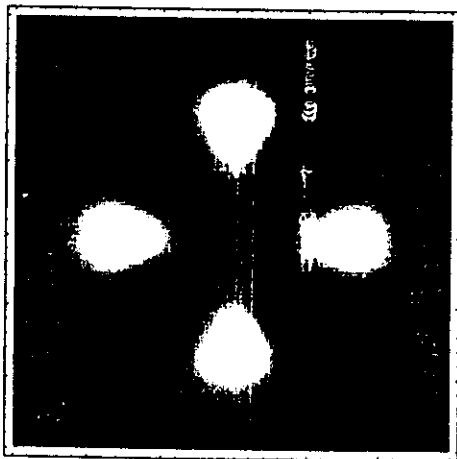
$$b = b(V) \Rightarrow \frac{d^2 \beta}{d\omega^2} \neq 0$$

$$(\Delta\tau)_w \approx -\frac{L}{c} (n_1 - n_2) \left(\frac{\Delta\lambda_0}{\lambda_0} \right) \left(V \frac{d^2 (bV)}{dV^2} \right)$$

LP₁₂



LP₄₁



SINGLE MODE FIBERS

SIF : $V = \frac{2\pi}{\lambda_0} a n_2 \sqrt{2\Delta} < 2.4048$

$$\Delta \approx \frac{n_1 - n_2}{n_2}$$

Example: $a \approx 4.8 \mu\text{m}$, $n_2 \approx 1.45$, $\Delta \approx 0.002$
 $\lambda_0 > 1.15 \mu\text{m} = \lambda_c$



Fundamental Mode:

$$E \approx A e^{-r^2/w^2} e^{i(\omega t - \beta z)}$$

Phase Factor

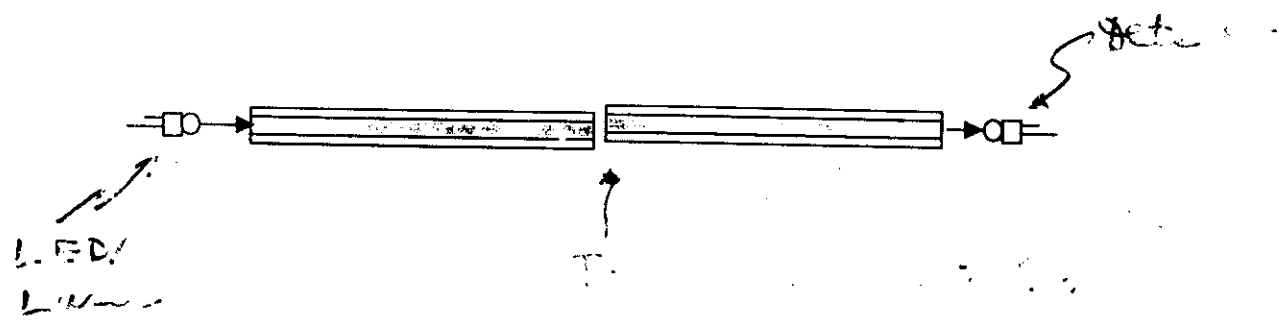
$$\frac{w}{a} \approx 0.65 + \frac{1.619}{V^{3/2}} + \frac{2.879}{V^6}; 0.8 \leq V \leq 2.5$$

Example : $a \approx 4.8 \mu\text{m}$, $n_2 \approx 1.45$, $\Delta \approx 0.002$

$$\lambda_0 = 1.1 \mu\text{m} \Rightarrow w \approx 4.4 \mu\text{m}$$

$$\lambda_0 = 1.3 \mu\text{m} \Rightarrow w \approx 5.0 \mu\text{m}$$

Splice loss at joints



$$\alpha(\text{dB}) \approx 4.34 \left(\frac{u}{w}\right)^2$$

$$w \approx 5 \mu\text{m}$$

For $\alpha < 0.1 \text{ dB}$

$$u < 0.76 \mu\text{m}$$

MODE

PLANE WAVE

$$E = \psi(r) e^{i(\omega t - \beta z)}$$

$$E = E_0 e^{i[\omega t - k(\omega)z]}$$

$$\beta(\omega) = \frac{\omega}{c} n_{\text{eff}}$$

$$k(\omega) = \frac{\omega}{c} n(\omega)$$

$$\frac{1}{v_g} = \frac{d\beta}{d\omega}$$

$$\frac{1}{v_g} = \frac{dk}{d\omega}$$

$$b = \frac{\beta/k_0 - n_2}{n_1 - n_2} \Rightarrow \beta = \frac{\omega}{c} \underbrace{[n_2 + (n_1 - n_2)b(V)]}_{n_{\text{eff}}}$$

$$V = \frac{\omega}{c} a \sqrt{n_1^2 - n_2^2}$$

$$\frac{1}{v_g} = \frac{d\beta}{d\omega} = \frac{n_2}{c} + \frac{n_1 - n_2}{c} \frac{d}{dV}(Vb)$$

Waveguide Dispersion

$$\tau = \frac{L}{v_g} \Rightarrow \Delta\tau_w = L \frac{d}{d\lambda_0} \left(\frac{1}{v_g} \right) \Delta\lambda_0 \approx -\frac{L}{c} n_2 \Delta \left[V \frac{d^2}{dV^2}(bV) \right] \frac{\Delta\lambda_0}{\lambda_0}$$

$$D_w = \frac{\Delta\tau_w}{L \Delta\lambda_0} \approx -\frac{n_2 \Delta}{3\lambda_0} \times 10^4 \left[V \frac{d^2}{dV^2}(bV) \right] \quad \text{ps/km.nm}$$

(λ_0 in micrometers)

$$D_w \approx -\frac{n_2 \Delta}{3\lambda_0} \times 10^4 \left[V \frac{d^2}{dV^2} (bV) \right] \text{ ps/km.nm}$$

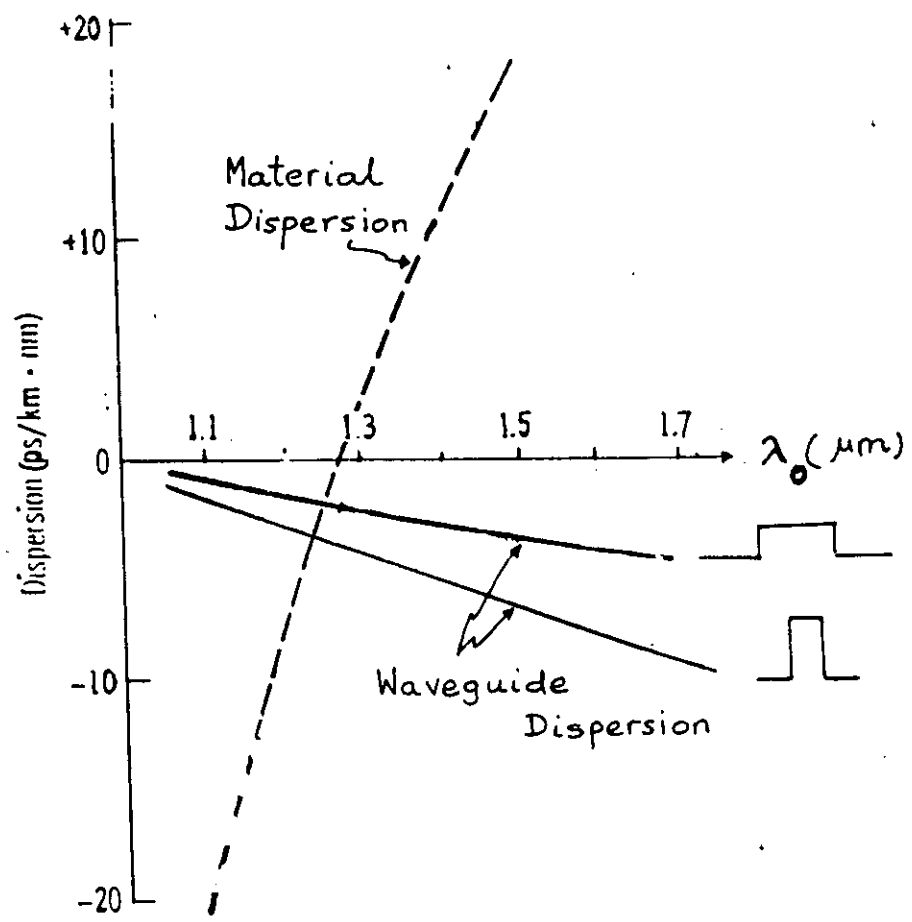
$$b(V) \approx \left(A - \frac{B}{V} \right)^2 ; 1.5 \lesssim V \lesssim 2.5$$

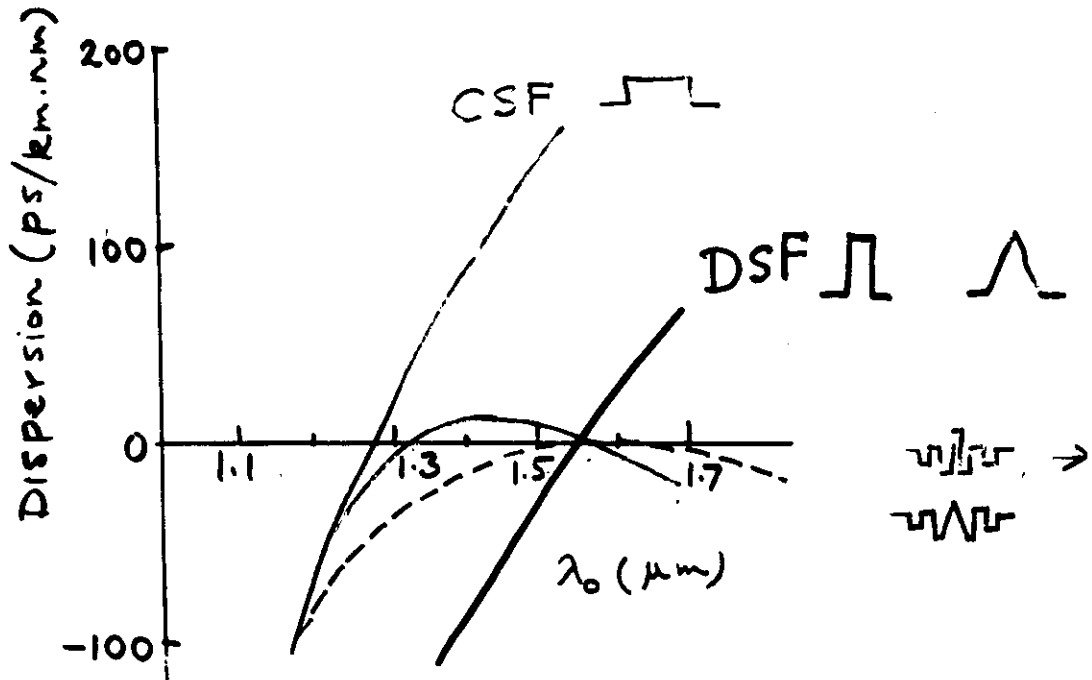
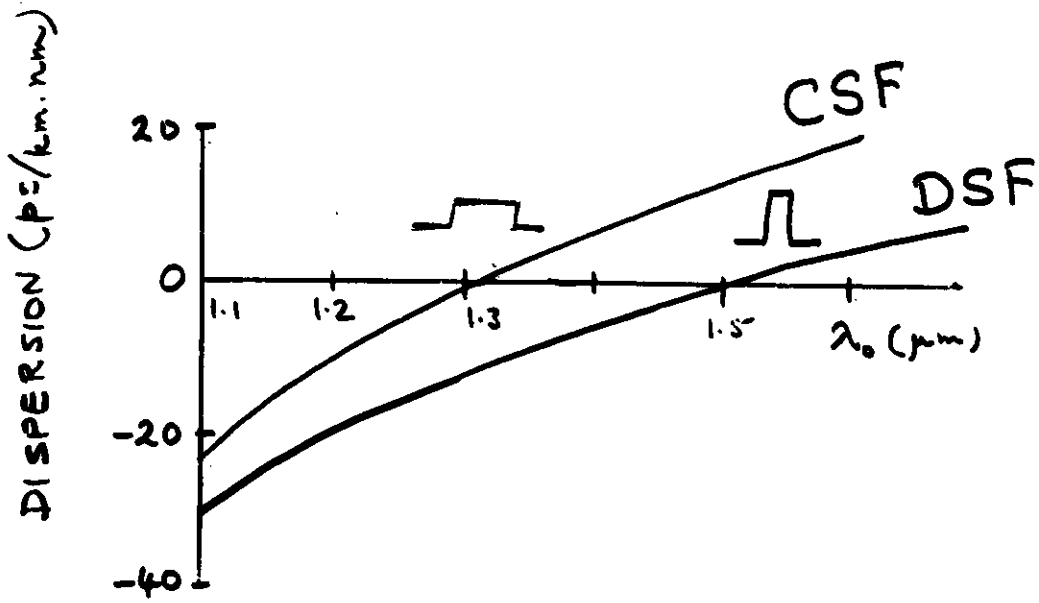
$$\Rightarrow V \frac{d^2}{dV^2} (bV) \approx \frac{2B^2}{V^2} ; \left[V \approx \frac{2\pi}{\lambda_0} a n_2 \sqrt{2\Delta} \right]$$

$$\approx \frac{\lambda_0^2}{2\pi^2 a^2 n_2 (2\Delta)} \quad (V \approx 1.9)$$

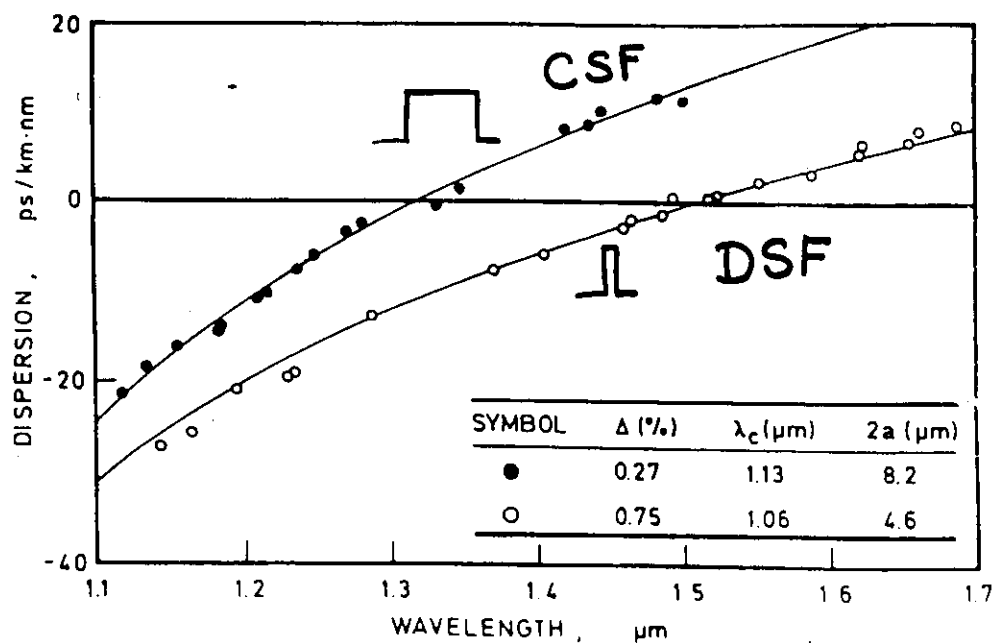
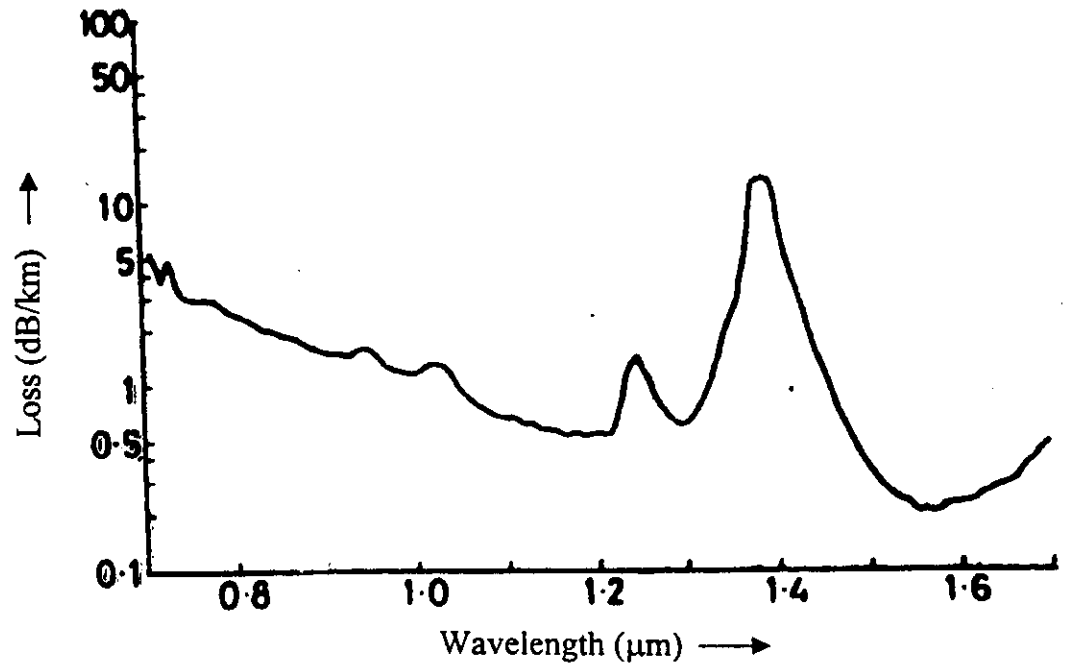
$$D_w \approx -\frac{\lambda_0}{12\pi^2 a^2} \times 10^4 \text{ ps/km.nm}$$

$$a \approx 4 \mu\text{m} \quad , \quad \lambda_0 \approx 1.3 \mu\text{m} \quad \Rightarrow \quad D_w \approx -7 \text{ ps/km.nm}$$



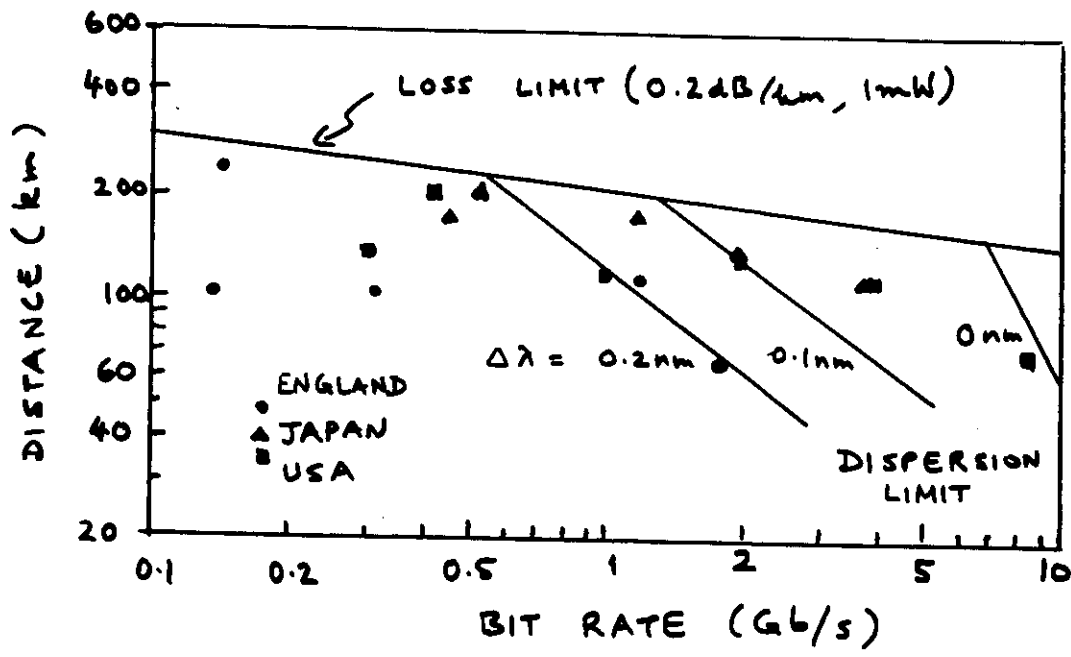


- DISPERSION SHIFTED
- } DISPERSION FLATTENED



Ref: Miya et al., Electron. Letts., 15 (1979) 106

Ref: Kimura, in *Optical Fiber Transmission* (Ed. K. Noda)
North Holland, Amsterdam, 1986

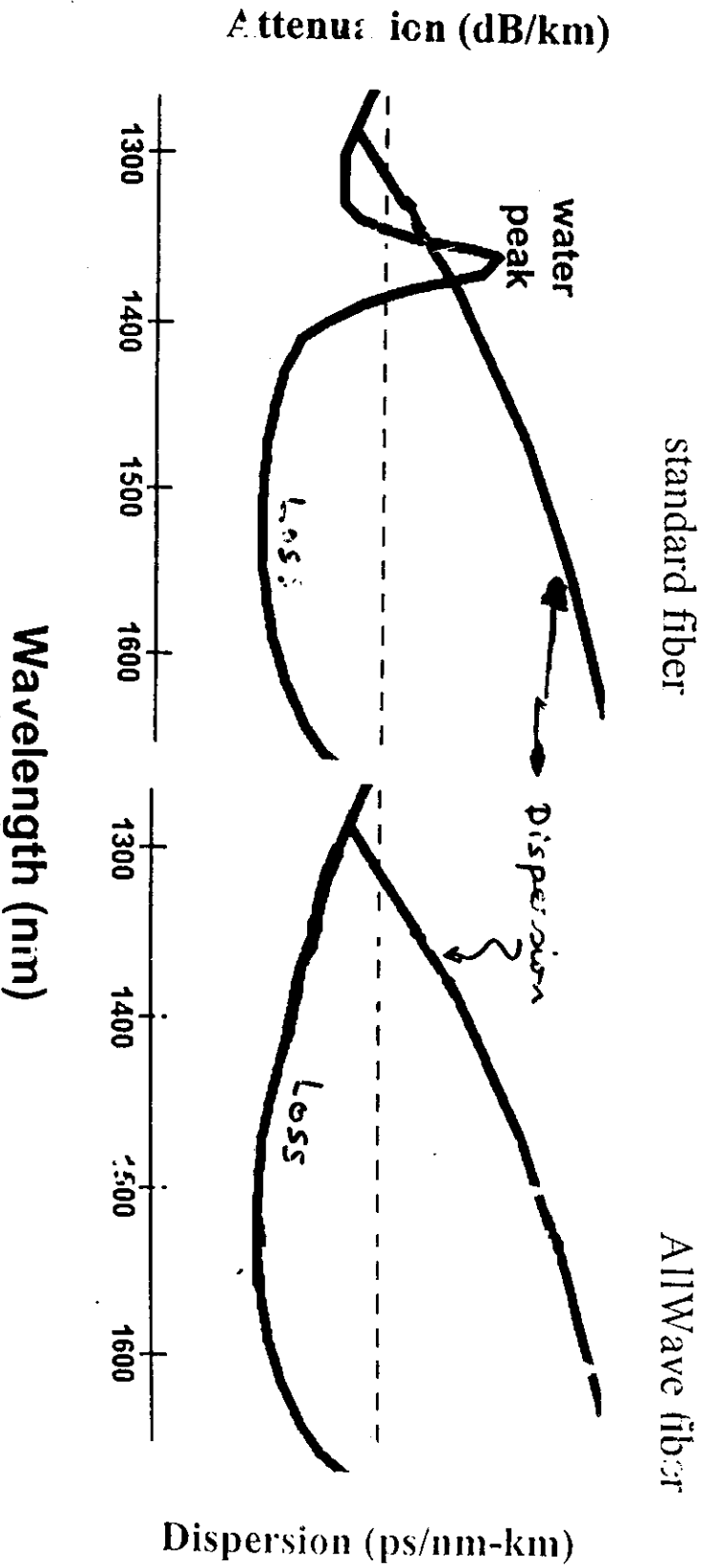


Long distance (>100 km) transmission at ultra high (>10 Gb/s) data rates requires

DISPERSION SHIFTED FIBERS

AllWave™ Fiber

Eliminates Water Peak to Open the 5th Operating Window



Propagation of a pulse

We first consider superposition of plane waves

$$\Psi(z, t) = \int A(\omega) e^{i[\omega t - k(\omega)z]} d\omega \quad ; \quad k(\omega) = \frac{\omega}{c} n(\omega)$$

$$\Psi(z = 0, t) = \int A(\omega) e^{i\omega t} d\omega$$

$$A(\omega) = \frac{1}{2\pi} \int \Psi(z = 0, t) e^{-i\omega t} dt$$

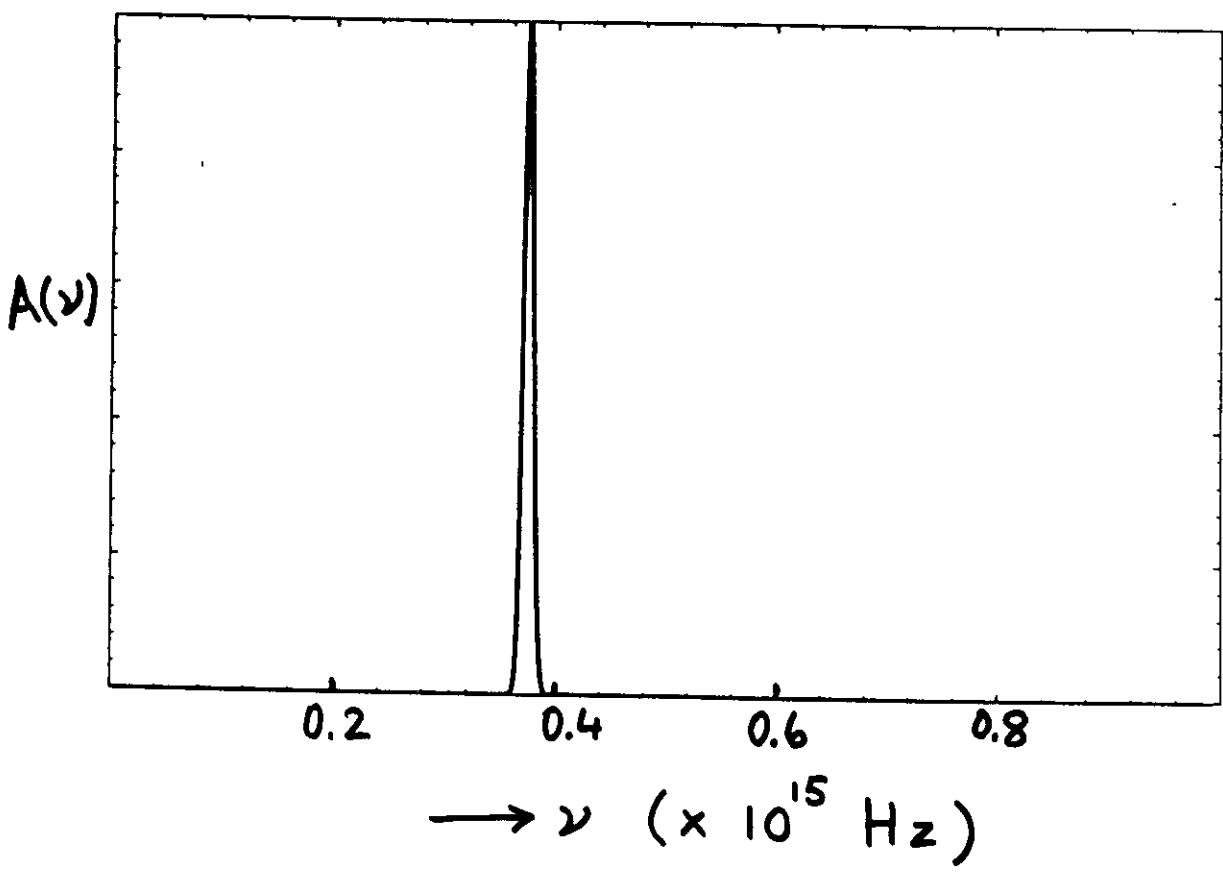
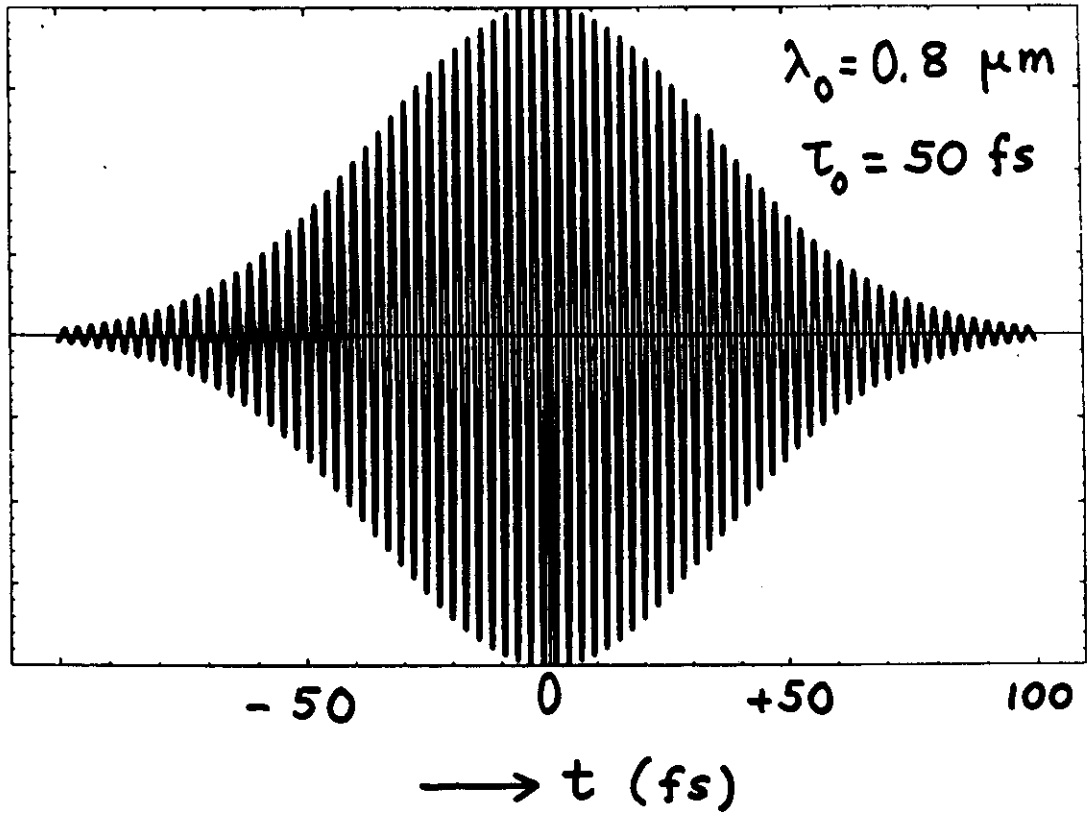
(Frequency spectrum)

Example: Gaussian Pulse

$$\Psi(z = 0, t) = C e^{-t^2 / \tau_0^2} e^{i\omega_0 t}$$

$$A(\omega) = \frac{C\tau_0}{2\sqrt{\pi}} \exp\left[-\frac{(\omega - \omega_0)^2 \tau_0^2}{4}\right]$$

Gaussian Pulse



$$\Psi(z, t) \approx \int_{\omega_0 - \frac{1}{2}\Delta\omega}^{\omega_0 + \frac{1}{2}\Delta\omega} A(\omega) e^{i[\omega t - k(\omega)z]} d\omega$$

$$k(\omega) \approx k(\omega_0) + \left. \frac{dk}{d\omega} \right|_{\omega_0} (\omega - \omega_0) + \left. \frac{1}{2} \frac{d^2k}{d\omega^2} \right|_{\omega_0} (\omega - \omega_0)^2$$

$$\approx k(\omega_0) + \frac{1}{v_g} \Omega + \frac{1}{2} \alpha \Omega^2$$

where $\Omega \equiv \omega - \omega_0$

$$\frac{1}{v_g} \equiv \left. \frac{dk}{d\omega} \right|_{\omega=\omega_0} \quad \& \quad \alpha \equiv \left. \frac{d^2k}{d\omega^2} \right|_{\omega=\omega_0} = \frac{\lambda_0^3}{2\pi c^2} \frac{d^2 n}{d\lambda_0^2}$$

$$\omega t = (\omega_0 + \Omega)t = \omega_0 t + \Omega t$$

Thus

$$\Psi(z, t) \approx e^{i[\omega_0 t - k(\omega_0)z]} \int d\Omega A(\Omega) e^{i[\Omega(t - \frac{z}{v_g}) + \frac{1}{2} \alpha z \Omega^2]}$$

Phase Factor

Envelope Function

Gaussian Pulse : $A(\Omega) = \frac{c\tau_0}{2\sqrt{\pi}} \exp\left[-\frac{1}{4} \tau_0^2 \Omega^2\right]$

$$\Psi(z, t) = \frac{C}{[\tau(z)/\tau_0]^{1/2}} \exp\left[-\frac{(t - \frac{z}{v_g})^2}{\tau^2(z)}\right] e^{i\Phi(z, t)}$$

$$\Phi(z, t) = \omega_0 t + \kappa\left(t - \frac{z}{v_g}\right)^2 - \frac{1}{2} \tan^{-1}\left(\frac{2\alpha z}{\tau_0^2}\right) - k_0 z$$

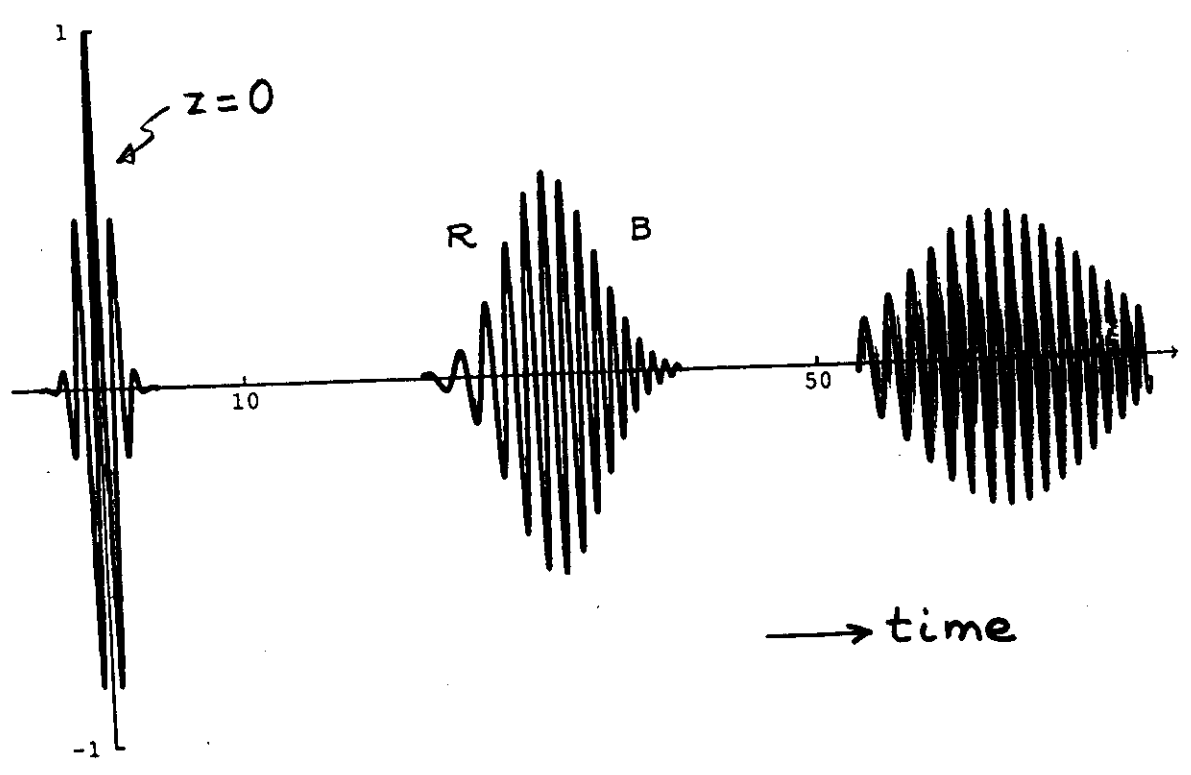
$$\omega(t) = \frac{\partial\Phi}{\partial t} = \omega_0 + 2\kappa\left(t - \frac{z}{v_g}\right) \quad ; \quad \kappa = \frac{2\alpha z}{\tau^2(z)}$$

$$\tau(z) = \tau_0 \left[1 + \frac{4\alpha^2 z^2}{\tau_0^4}\right]^{1/2}$$

If $d^2 n / d\lambda_0^2 > 0 \Rightarrow \kappa > 0$ (Positive Chirp)

For $t < \frac{z}{v_g}$ (Leading edge), $\omega(t) < \omega_0$ (red shifted)

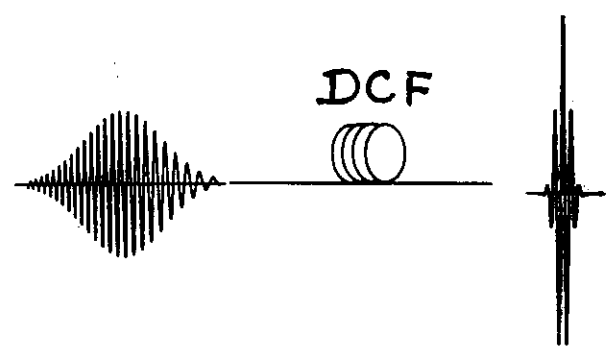
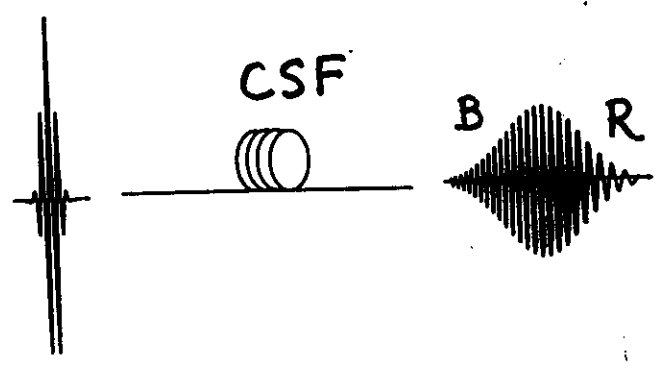
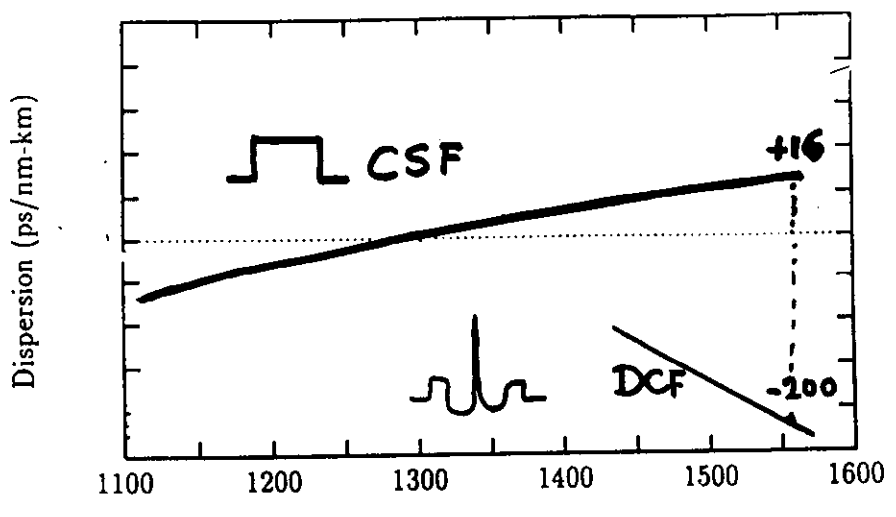
For $t > \frac{z}{v_g}$ (Trailing edge), $\omega(t) > \omega_0$ (blue shifted)



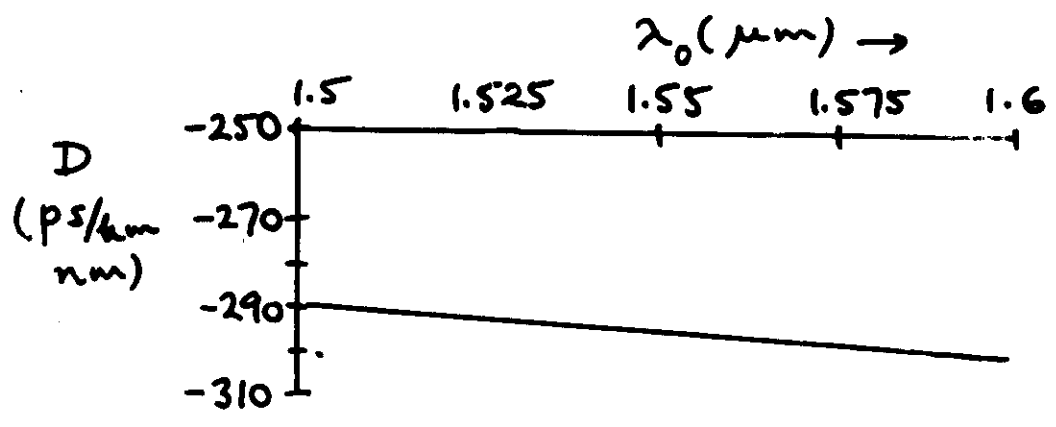
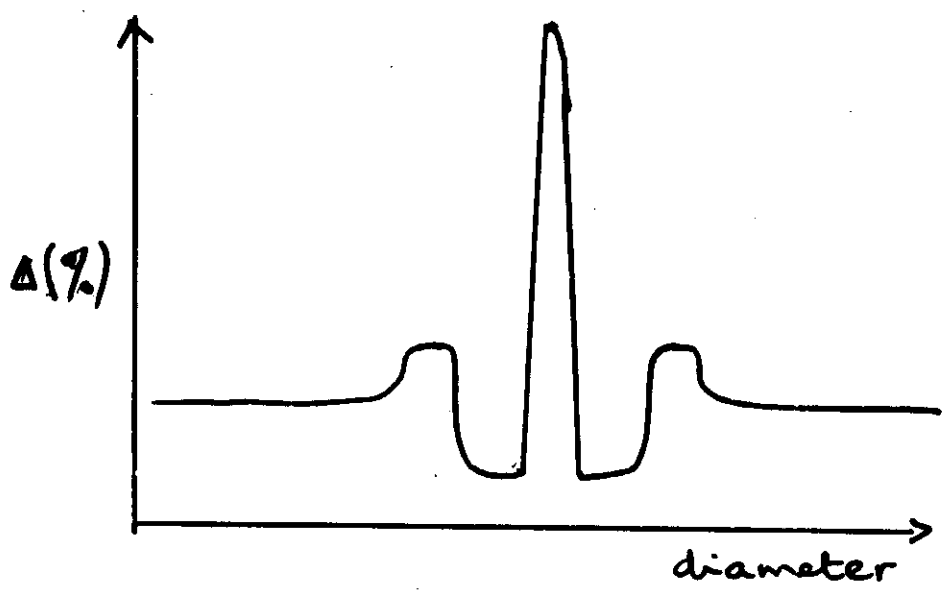
Dispersion Compensation

- More than 70 million km of CSF (with $\lambda_z \sim 1310$ nm) already laid (currently operating at $\lambda_0 \sim 1310$ nm)
- However, the fiber has lowest loss at 1550 nm; also efficient amplifiers operate around 1550 nm
- The CSF's have $D \sim 16$ ps/km-nm at $\lambda_0 \sim 1550$ nm
- How to use existing CSF's at 1550 nm?
 - Through Dispersion Compensation

76
46



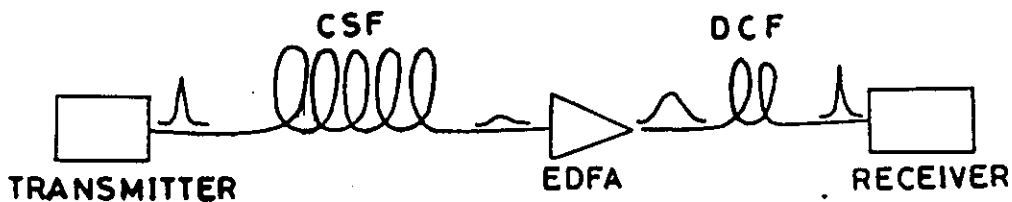
Dispersion Compensating Fiber



Attenuation \sim 0.7 dB/km

Dispersion \sim -293 ps/km.nm
(1550 nm)

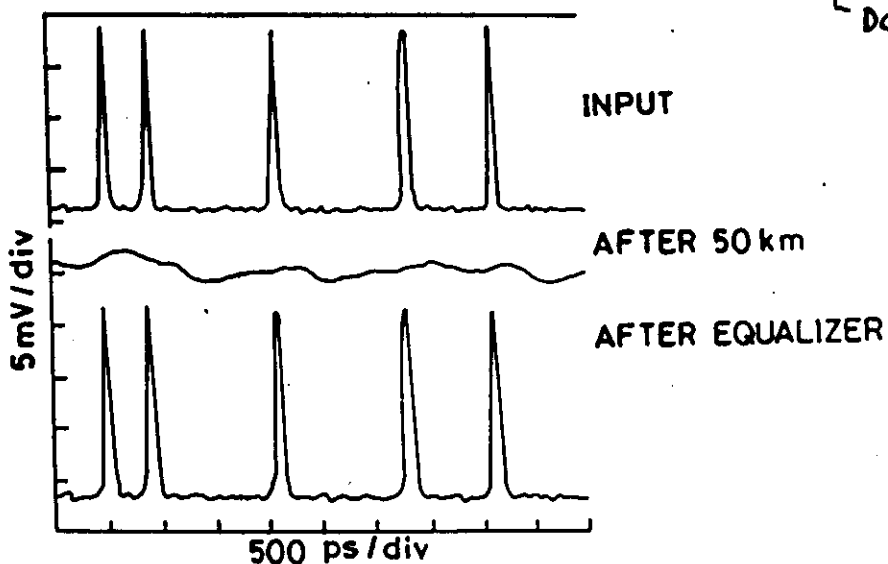
Ref: Hawtof et al. OFC 1996, Post
Deadline paper PDG



(a)

$$D_{DCF} \approx -548 \text{ ps/km.nm}$$

$$L_{DCF} \approx 1.44 \text{ km}$$



(a) A Schematic of dispersion compensation scheme in a conventional single mode fiber (CSF) system operating at 1550 nm using a dispersion compensatory fiber (DCF). EDFA is an erbium doped fiber amplifier. (b) A typical result showing the performance of a dispersion compensator for 2.5 Gb/s bit pattern [Poole et al, JLT, 12, 1746 (1994)].

7-9
4-9

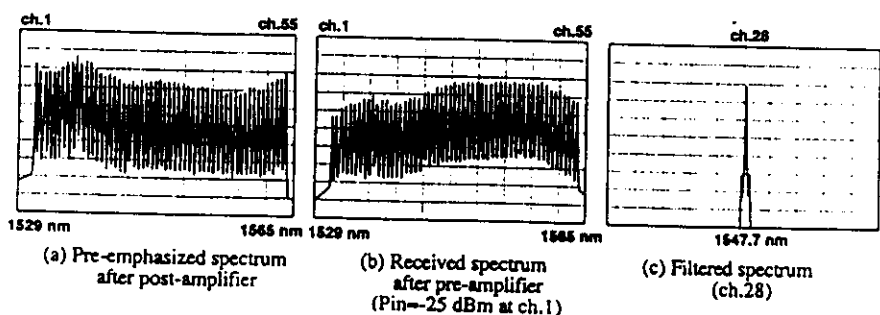
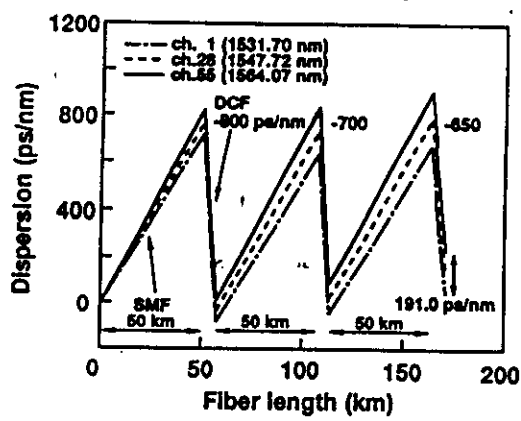
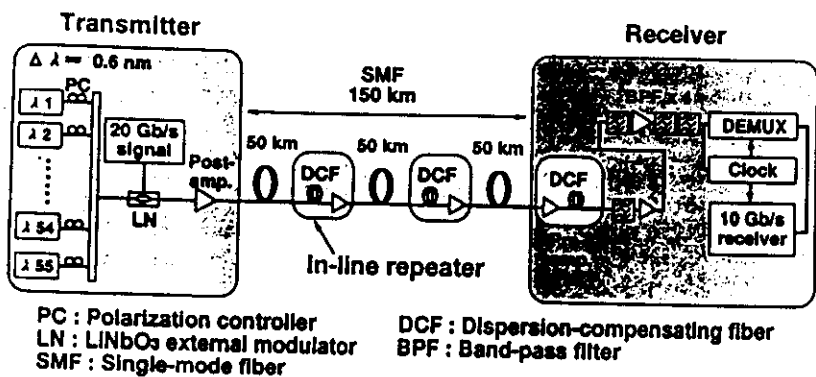
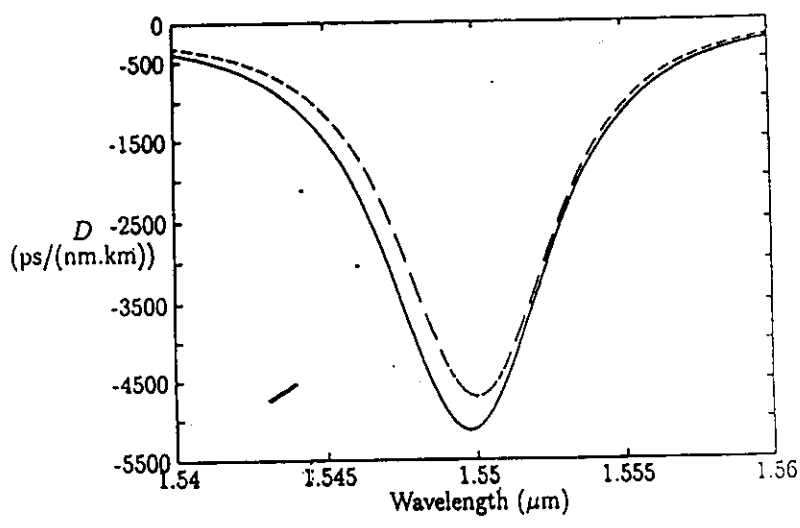
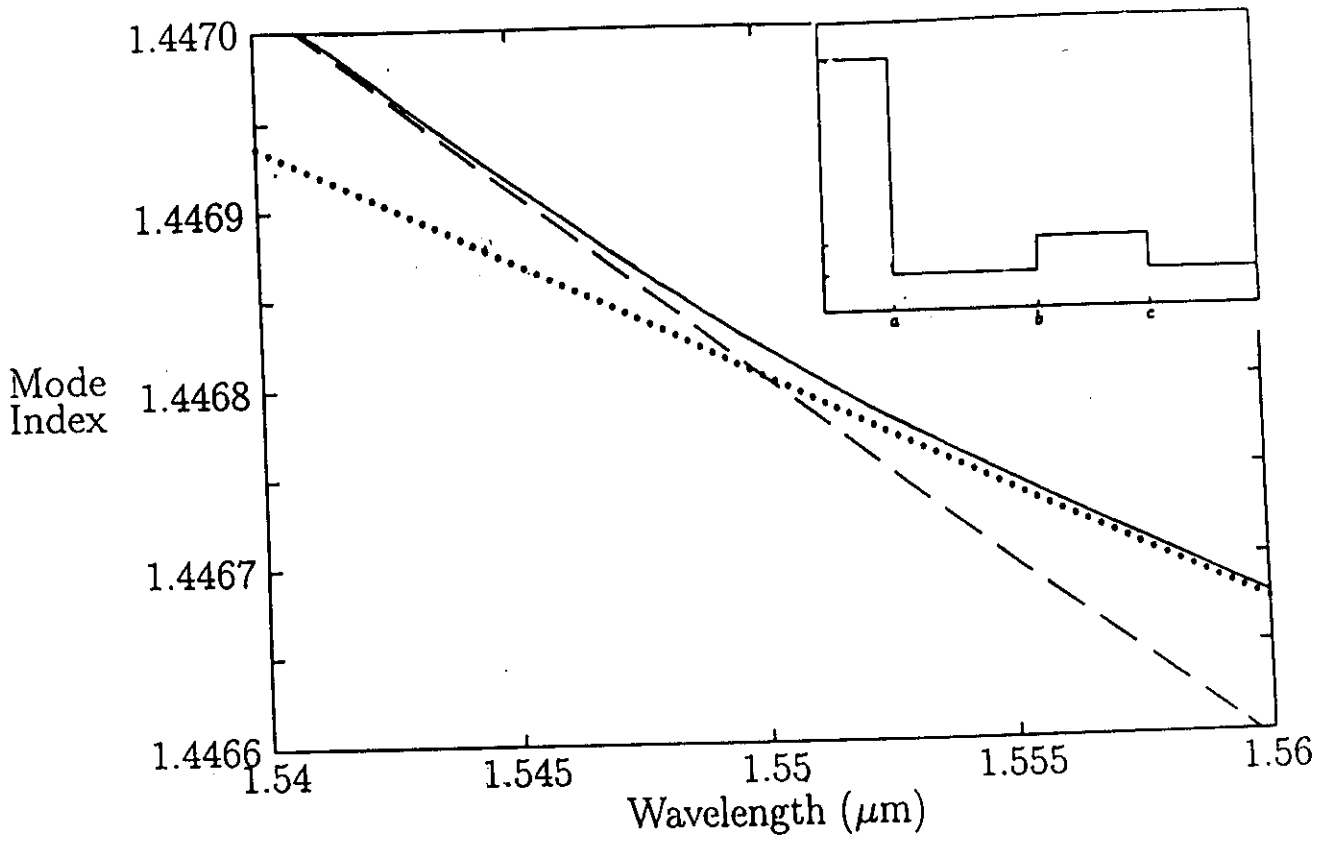


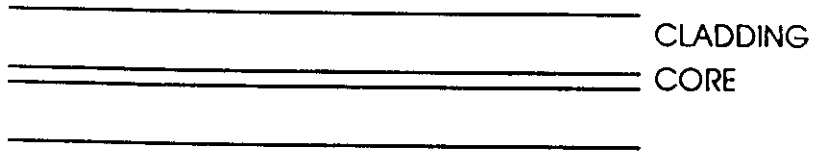
Figure 8: a) Experimental setup for 55 wavelength WDM transmission. b) The corresponding dispersion map. c) 55 wavelength spectra (H:3.6 nm/div, V: 5dB/div, Res: 0.1 nm) [adapted from Ref. 9].

Capacity : $55 \times 20 \text{ Gb/s} = 1.1 \text{ Terabits/s}$ over 150 km

1 Tbit/s = sending contents of 1000 copies of a 30 volume encyclopedia in 1 s



Variation of the mode index and D with wavelength for the refractive index profile of the dual-core DCF shown in the inset [Thyagarajan, Varshney, Palai, Ghatak and Goyal, " A novel design of a dispersion compensating fiber", IEEE Photonics Tech. Letts. 8, November 1996].



10 mW laser beam

$$A_{\text{eff}} \approx 50 (\mu\text{m})^2$$

$$\Rightarrow I \approx 20,000 \text{ W/cm}^2$$

With very low input optical powers (~ 10 mW) one can generate very high intensity levels ($\sim 20 \text{ kW/cm}^2$) over very long interaction lengths ($\sim 100 \text{ km}$)

Non linear effects are relatively easy to observe using guided wave optics.

Self Phase Modulation (SPM)

$$\Psi = e^{i[\omega_0 t - kz]} \quad ; \quad k(\omega_0) = k_0 n(\omega_0) \quad [k_0 = \frac{\omega_0}{c}]$$

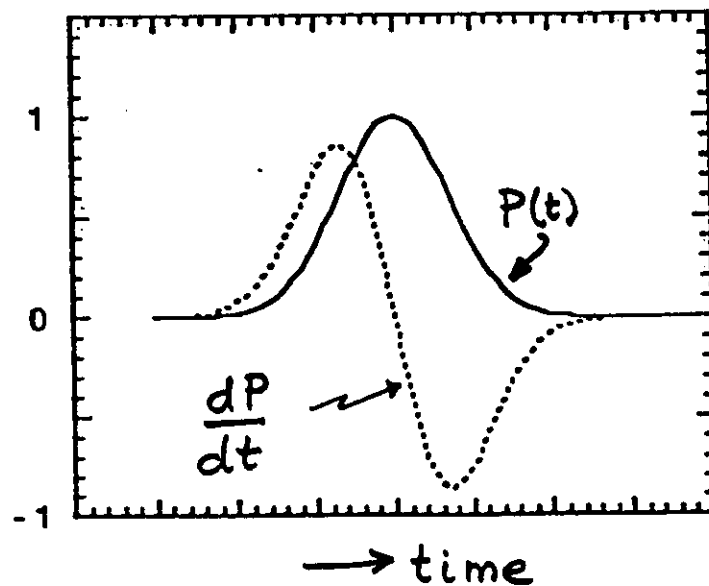
$$n = n_0 + n_2 I = n_0 + n_2 \frac{P}{A_{\text{eff}}}$$

$$\Psi = \psi(r) e^{i(\omega_0 t - \beta z)} = \psi(r) e^{i\phi}$$

$$\phi = \omega_0 t - \beta z \quad ; \quad \beta / k_0 = n_{\text{eff}} = (n_{\text{eff}})_0 + n_2 \frac{P}{A_{\text{eff}}}$$

$$\phi = \omega_0 t - \beta_0 z - k_0 n_2 z \frac{P(t)}{A_{\text{eff}}}$$

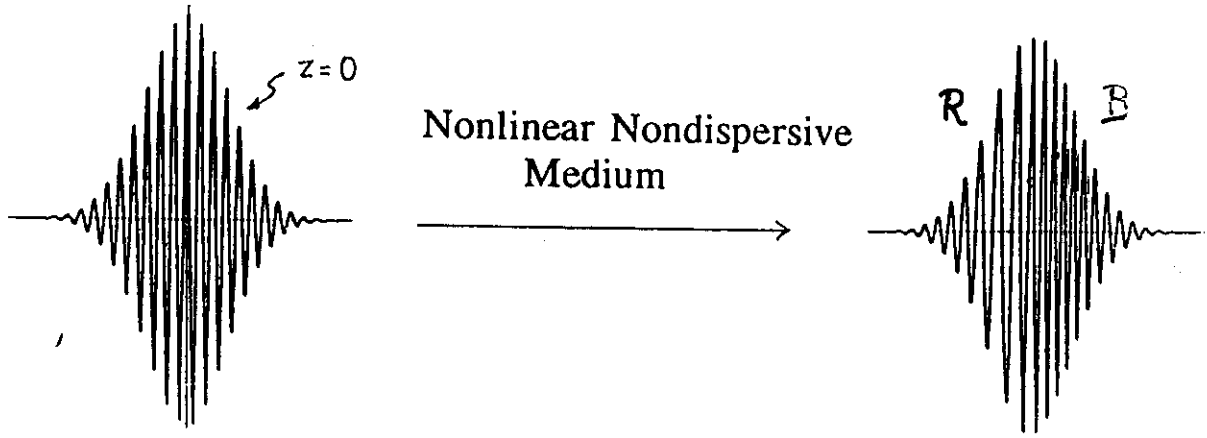
$$\omega(t) = \frac{d\phi}{dt} = \omega_0 - k_0 n_2 z \frac{1}{A_{\text{eff}}} \frac{dP}{dt}$$



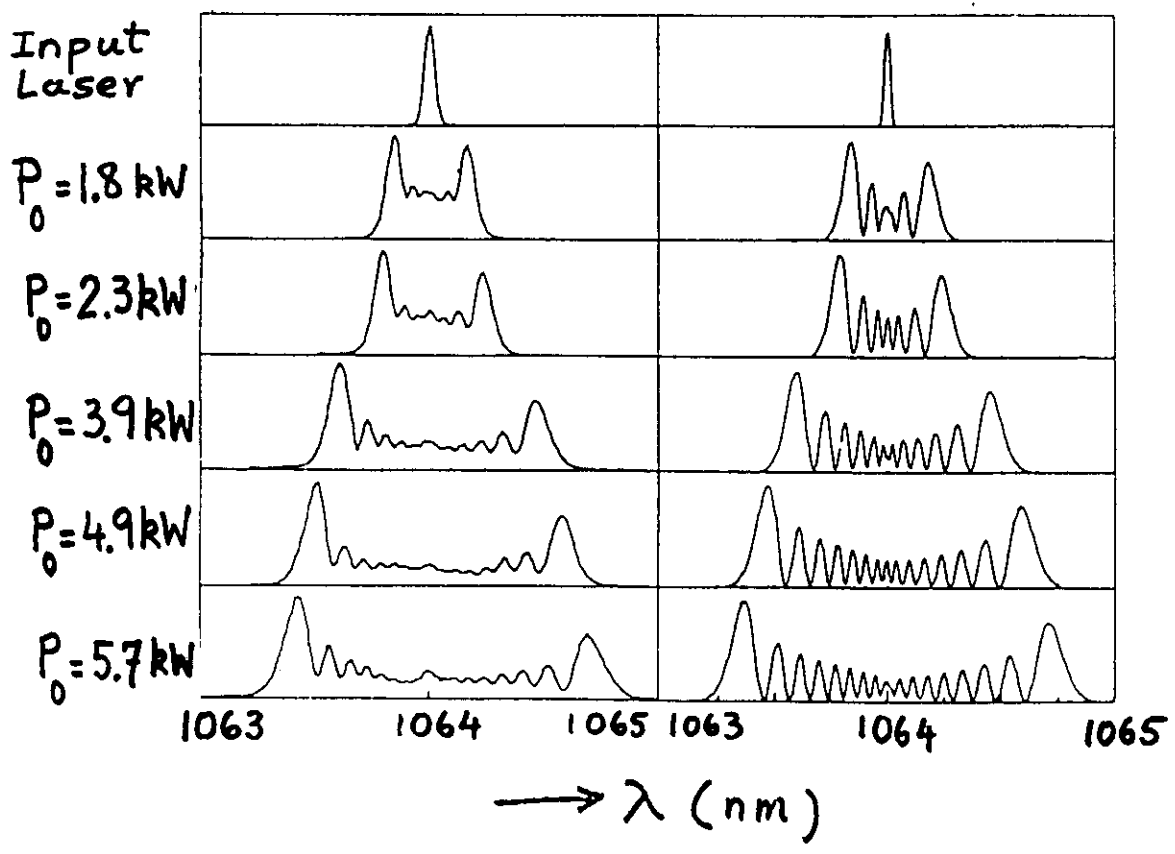
Self Phase Modulation (SPM)

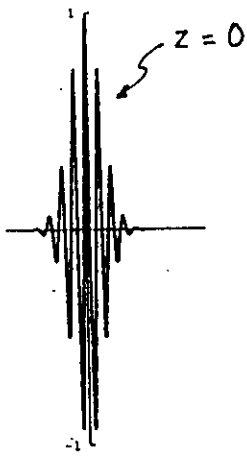
$$P(z,t) = P_0 e^{-\frac{2(t - \frac{z}{v_g})^2}{\tau_0^2}}$$

$$\omega(t) = \omega_0 + \frac{4k_0 n_2 z P_0}{A_{\text{eff}} \tau_0^2} (t - \frac{z}{v_g}) e^{-\frac{2(t - \frac{z}{v_g})^2}{\tau_0^2}}$$

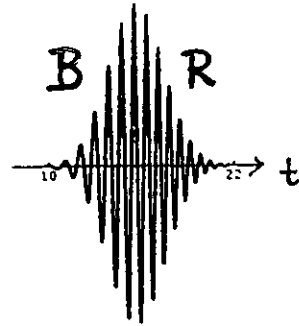
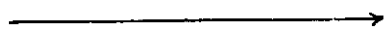


Chirping but no temporal broadening. New frequencies are generated.

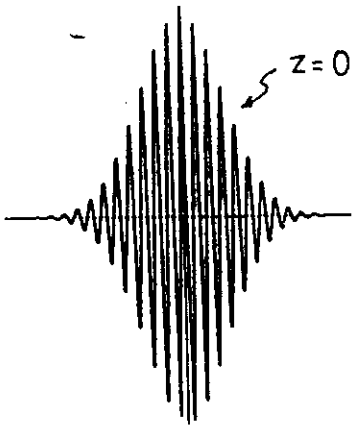




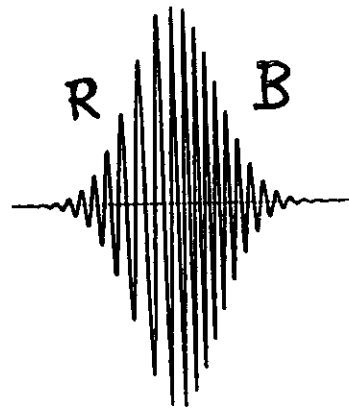
Linear Dispersive Medium



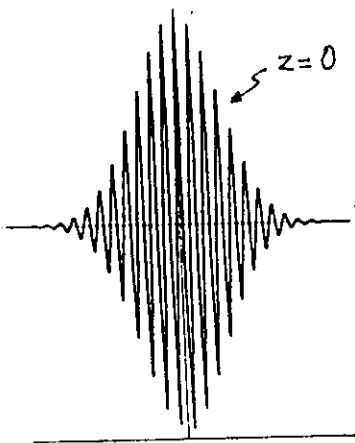
Temporal Broadening & Chirping



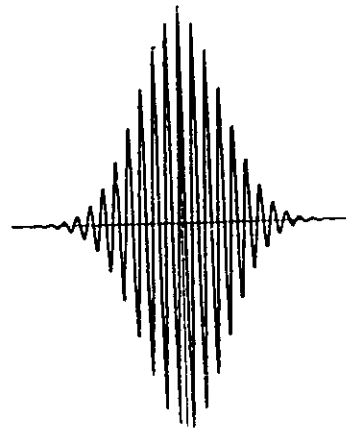
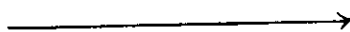
Nonlinear Nondispersive Medium



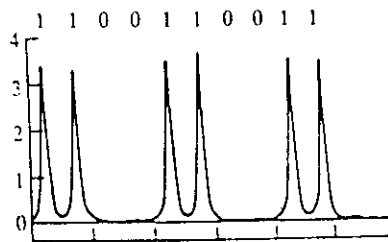
Chirping but no temporal broadening. New frequencies are generated.



Nonlinear Dispersive Medium



SOLITON



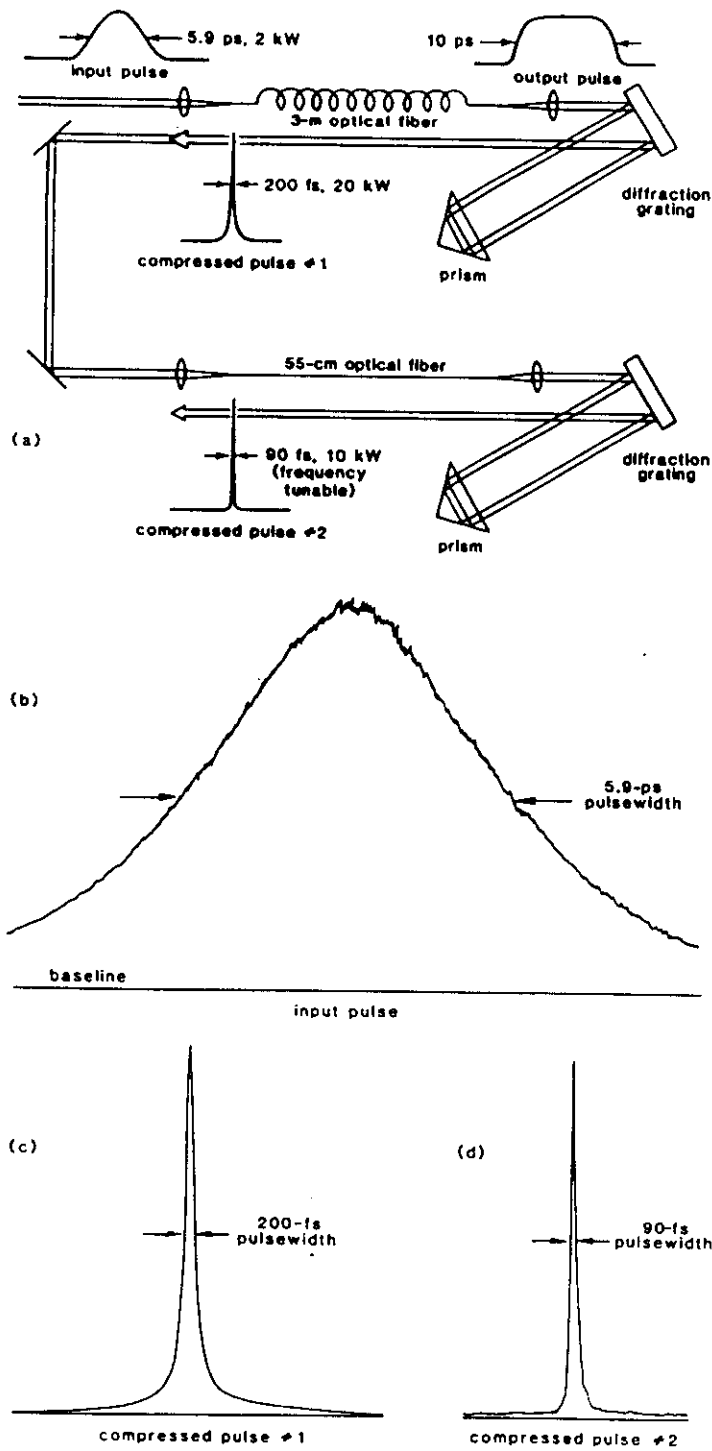


Fig. 16.8: Experimental arrangement for achieving pulse compression. With this arrangement an input pulse of 5.9 ps was compressed to 90 fs using spectral broadening through SPM in the optical fiber and pulse compression using a grating-prism arrangement. [After Nikolaus and Grischowsky (1983).]

$$\omega_{rel}(t) = \omega_0 + \frac{4k_0 n_2 z}{\tau_0^2} \left(t - \frac{z}{v_g}\right) \frac{P}{A_{eff}}$$

$$\omega_d(t) = \omega_0 + \frac{2\sigma}{(1+\sigma^2)\tau_0^2} \left(t - \frac{z}{v_g}\right)$$

$$\sigma = \frac{2z}{\tau_0^2} \alpha ; \quad \alpha = \frac{\lambda_0^3}{2\pi c^2} \frac{d^2 n}{d\lambda_0^2}$$

$$\frac{4k_0 n_2 z}{\tau_0^2} \cdot \frac{P}{A_{eff}} = - \frac{2\sigma}{\tau_0^2} \quad \sigma \ll 1$$

$$\Rightarrow P = \frac{\lambda_0^3 A_{eff}}{4\pi^2 c n_2 \tau_0^2} D$$

$$D = - \frac{\lambda_0}{c} \frac{d^2 n}{d\lambda_0^2}$$

Nonlinear Schrödinger Equation

$$E(z, t) = \underbrace{e^{i[\omega_0 t - k(\omega_0) z]}}_{\text{Phase term}} \underbrace{f(z, t)}_{\text{Envelope term}}$$

$$-i \left(\frac{\partial f}{\partial z} + \frac{1}{v_g} \frac{\partial f}{\partial t} \right) - \frac{1}{2} \alpha \frac{\partial^2 f}{\partial t^2} + \Gamma |f|^2 f = 0$$

$$\frac{1}{v_g} = k' = \left. \frac{dk}{d\omega} \right|_{\omega=\omega_0}$$

$$\alpha = k'' = \left. \frac{d^2 k}{d\omega^2} \right|_{\omega=\omega_0}$$

$$\Gamma = \frac{1}{2} \omega_0 \epsilon_0 n_0 n_2$$

Moving Frame

$$T = t - \frac{z}{v_g}; \quad z = z$$

In the moving frame

$$-i \frac{\partial f}{\partial z} - \frac{1}{2} \alpha \frac{\partial^2 f}{\partial T^2} + \Gamma |f|^2 f = 0$$

$$-i \frac{\partial f}{\partial z} - \frac{1}{2} \alpha \frac{\partial^2 f}{\partial T^2} + \Gamma |f|^2 f = 0 \quad T = t - \frac{z}{v_g}$$

Propagation in absence of dispersion and non-linearity ($\alpha = 0, \Gamma = 0$)

$$\frac{\partial f(z, T)}{\partial z} = 0$$

$$\Rightarrow f = f_0(T) = f_0 \left(t - \frac{z}{v_g} \right)$$

Propagation in presence of dispersion only ($\Gamma = 0$)

$$-i \frac{\partial f(z, T)}{\partial z} - \frac{1}{2} \alpha \frac{\partial^2 f(z, T)}{\partial T^2} = 0$$

$$f(z, T) = \int A(\Omega) e^{i(\Omega T - \frac{1}{2} \alpha \Omega^2 z)} d\Omega$$

Propagation in presence of nonlinearity

$$-i \frac{\partial f(z, T)}{\partial z} + \Gamma |f|^2 f(z, T) = 0$$

$$\frac{\partial |f|^2}{\partial z} = 0$$

$$|f|^2 = F(T) = F\left(t - \frac{z}{v_g}\right)$$

$$f(z, T) = f_0(T) e^{-i\phi(z, T)}$$

$$E(z, T) = f_0\left(t - \frac{z}{v_g}\right) e^{i\left\{\omega_0 t - \Gamma |f_0(t - \frac{z}{v_g})|^2 z - k(\omega_0) z\right\}}$$

In presence of dispersion and nonlinearity we get the soliton solution

$$f(z, T) = E_0 \operatorname{sech}\left[\gamma\left(t - \frac{z}{v_g}\right)\right] e^{-igz}$$

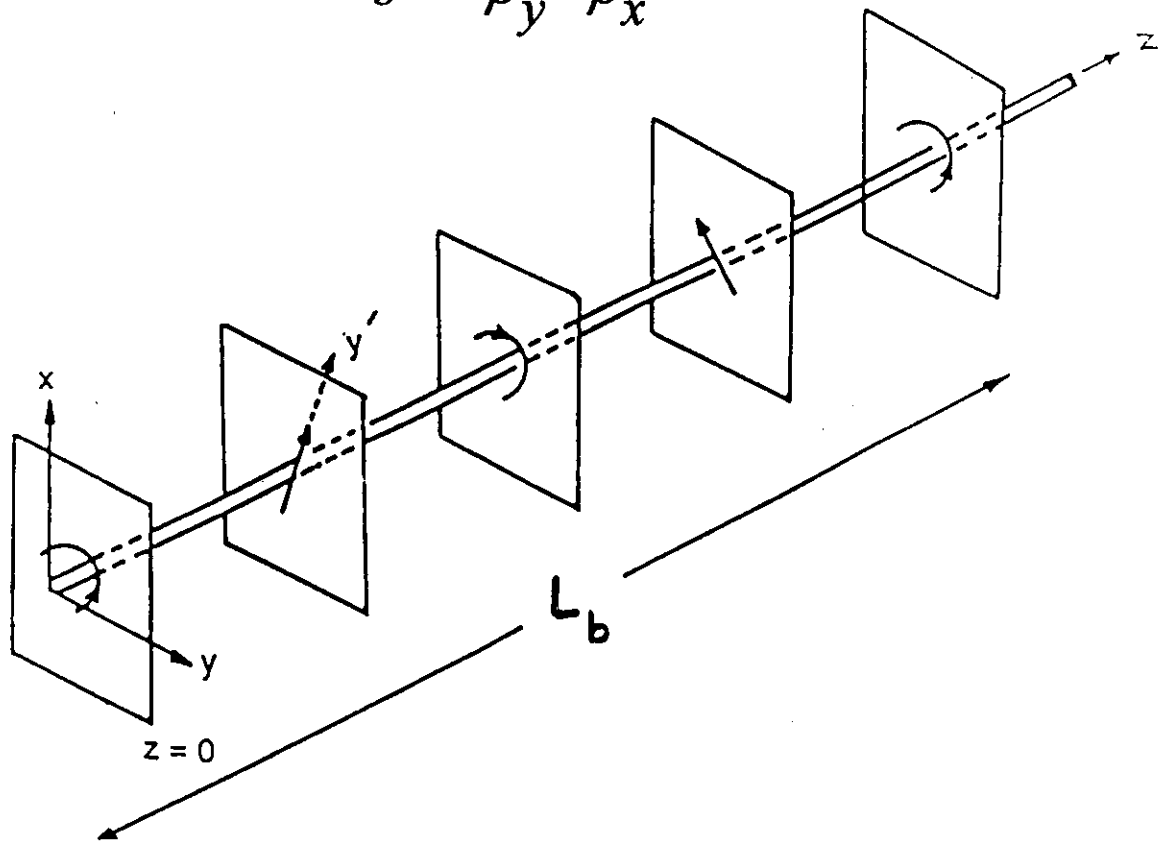
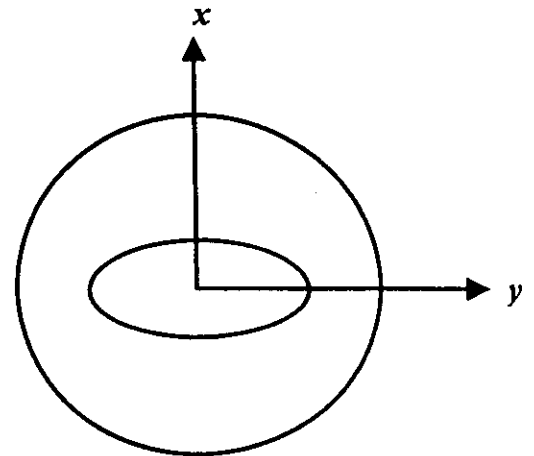
$$g = -\frac{1}{2} \alpha \gamma^2 = \frac{1}{2} \Gamma E_0^2$$

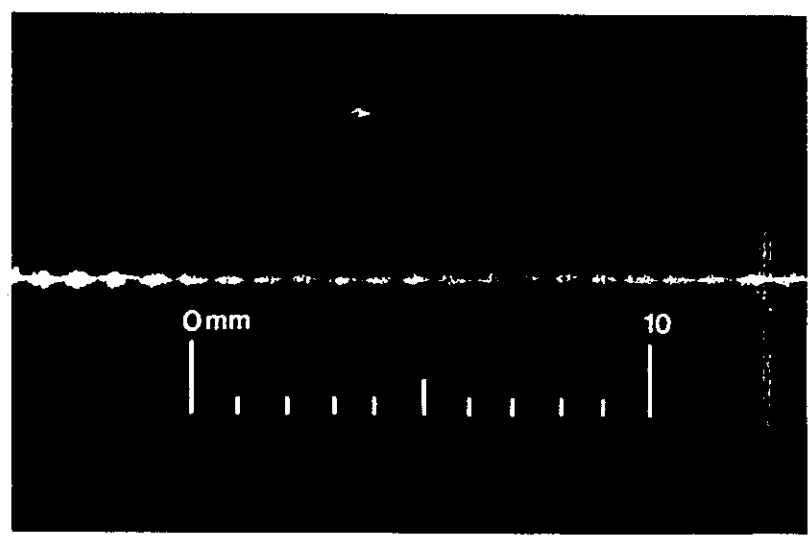
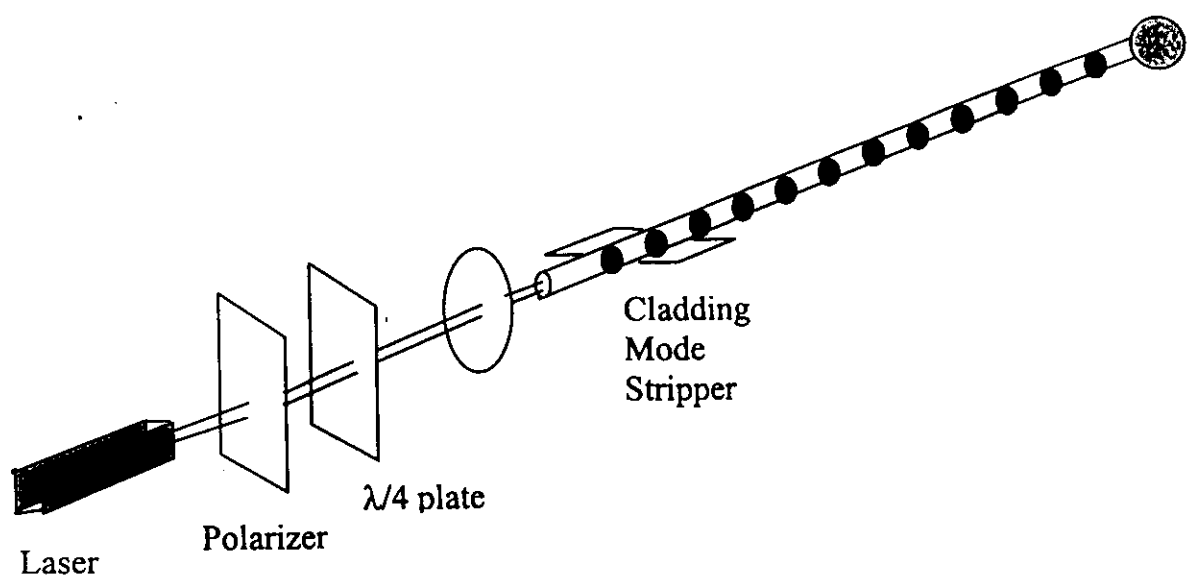
Elliptic core fiber

$$\mathbf{E} = \hat{\mathbf{x}} \psi(x,y) \cos(\omega t - \beta_x z)$$

$$\mathbf{E} = \hat{\mathbf{y}} \psi(x,y) \cos(\omega t - \beta_y z)$$

$$\text{Beat Length } L_b = \frac{2\pi}{\beta_y - \beta_x} \approx \text{few mm}$$





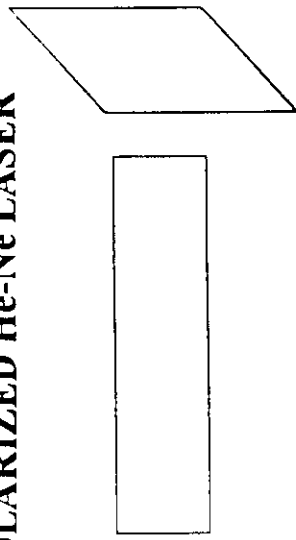
Pure silica

$$\epsilon = \begin{pmatrix} \epsilon_1 & 0 & 0 \\ 0 & \epsilon_1 & 0 \\ 0 & 0 & \epsilon_1 \end{pmatrix}; \quad \epsilon_1 \approx 2.25$$

When a polarized beam propagates through silica along \vec{B} , then

$$\epsilon = \begin{pmatrix} \epsilon_1 & \epsilon' & 0 \\ -\epsilon' & \epsilon_1 & 0 \\ 0 & 0 & \epsilon_1 \end{pmatrix}; \quad \epsilon' \approx 10^{-7} \text{ i per kO of applied magnetic field.}$$

POLARIZED He-Ne LASER



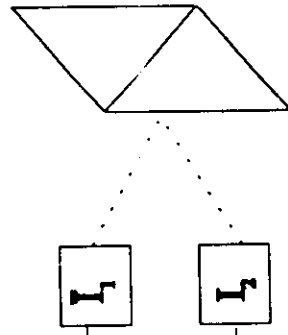
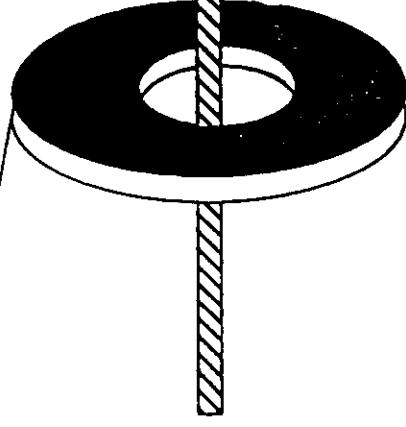
HALF-WAVE PLATE

M.O. 20X

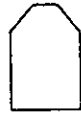


S.M. FIBER

CURRENT
CARRYING
CONDUCTOR



M.O. 20X



POL. CONTROLLER



WOLLASTON PRISM

$$\frac{I_1 - I_2}{I_1 + I_2}$$



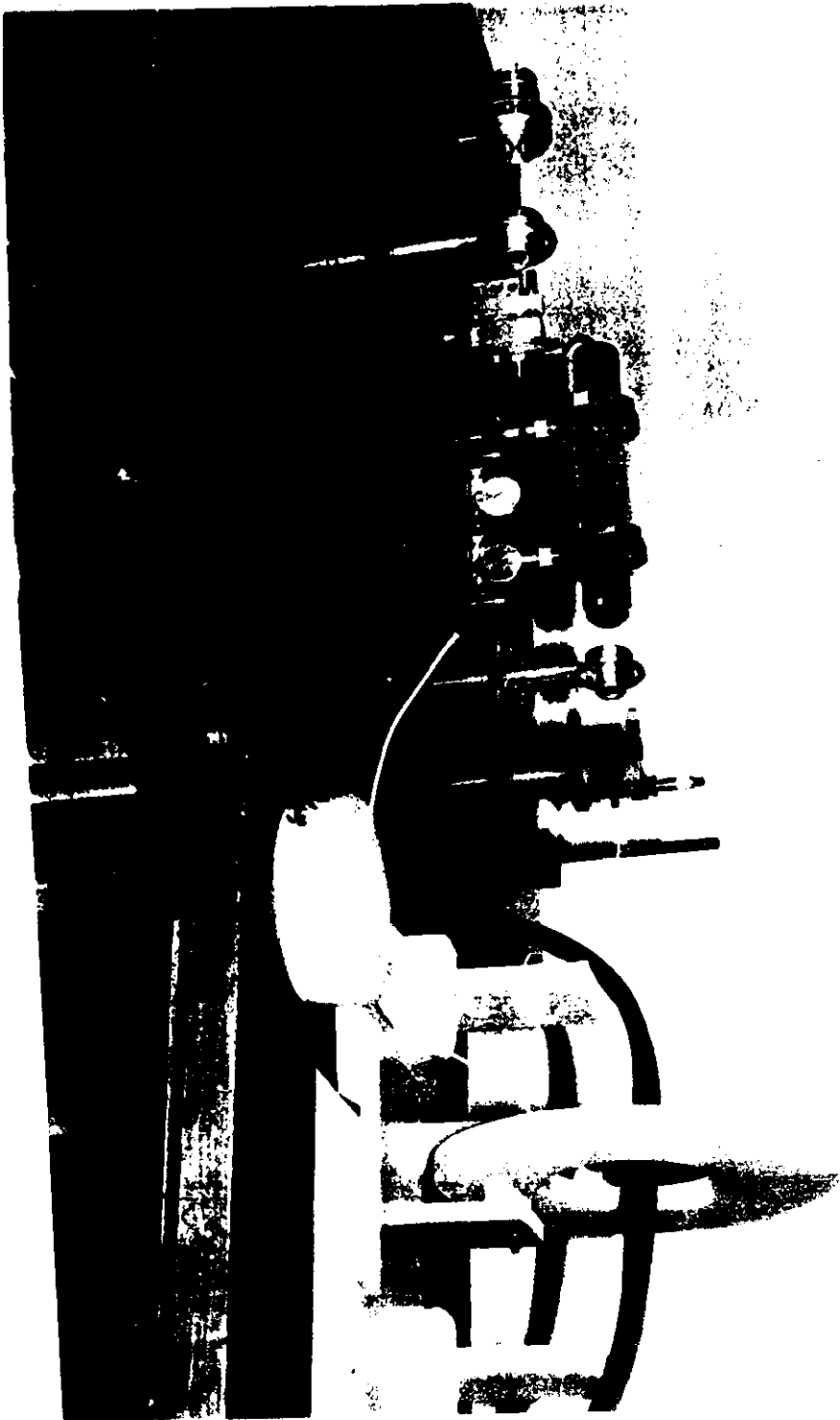
C.R.O. OUTPUT

FIBER OPTIC CURRENT SENSOR

5-4

AP

FIBER - OPTIC CURRENT SENSOR



POLARIZATION MAINTAINING FIBERS

Most fiber optic systems rely upon detection of optical pulses in a photodetector that is independent of optical polarization or phase. However, applications in

Polarimetric & Interferometric sensors, coherent optical communications systems require that the

SOP (state of polarization) be maintained for distances ranging from ~ 100 meters (for sensor applications) to ~ 100 km (for coherent communication systems).

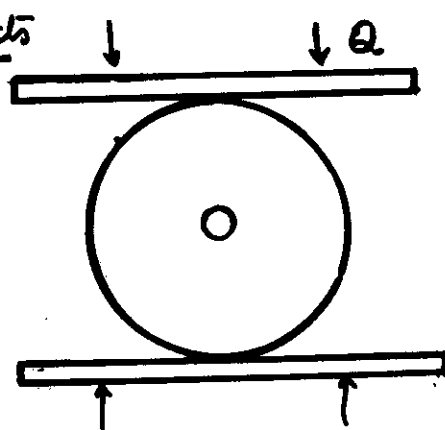
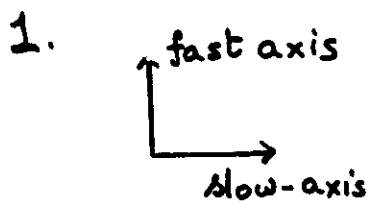
High Birefringent Fibers

β_x very different from β_y

⇒ coupling between x and y polarized modes due to perturbations is almost negligible

⇒ SOP is (almost) maintained in the fiber

External Birefringence effects



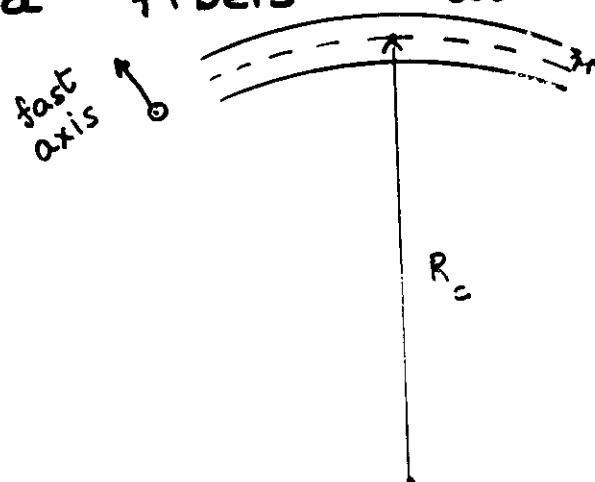
Force Q acting between parallel jaws.

$$\beta_{\text{slow}} - \beta_{\text{fast}} \approx \text{const.} \cdot \frac{Q}{l}$$

$$\text{const.} \approx 1 \text{ rad/N}$$

All numerical values correspond to silica fibers at 6328 \AA

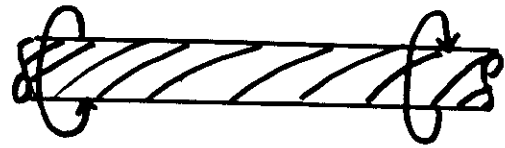
2.



$$\beta_{\text{slow}} - \beta_{\text{fast}} \approx \text{const.} \cdot \left(\frac{1}{R}\right)$$

$$\text{const.} \approx 4.9 \times 10^6 \text{ rad/}$$

3. Circular Birefringence due to ⁵⁻¹⁸ Elastic Twist

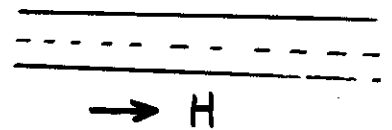
⇒ Modes are  circularly polarized
(≡ Optical Activity)

$$\beta_{\text{slow}} - \beta_{\text{fast}} \approx \text{const.} \cdot \tau$$

τ : twist in rad/m
const. $\approx 0.13 - 0.16$

4. Circular Birefringence due to axial magnetic field (FARADAY EFFECT)

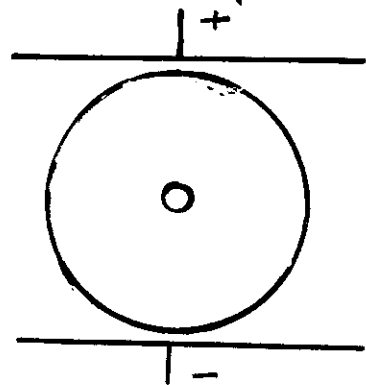
$$\beta_{\text{slow}} - \beta_{\text{fast}} \approx \text{const.} \cdot H$$



5. Linear Birefringence by application of a transverse electric field (Electro-optic Kerr Effect)

$$\beta_{\text{slow}} - \beta_{\text{fast}} \approx \text{const.} \cdot E^2$$

const $\approx 6 \times 10^{-16} \text{ m/V}^2$



Ref: R. Ulrich in Fiber Optic Rotation Sensors (Eds: Ezekiel & Arditty) Springer-Verlag (1982) & references therein

40 lecture course on FIBER OPTICS

Basic characteristics of the optical fiber

Numerical Aperture and attenuation; Pulse dispersion in step index and graded index optical fibers: ray analysis

Material dispersion

Modes of optical waveguides

Single mode fibers

The Gaussian approximation for the fundamental mode & loss calculations at fiber joints; far field pattern

Interplay of waveguide & material dispersion

Conventional single mode fibers, Dispersion shifted fibers & Dispersion compensating fibers, Non-zero dispersion shifted fibers, Dispersion management

Design of a fiber optic communication system

Special Topics

Nonlinear effects in Fibers

Self Phase Modulation, Soliton Propagation

Erbium doped fiber amplifiers

Fiber optic devices

directional couplers, fiber polarizers

Fiber gratings

Fiber optic sensors