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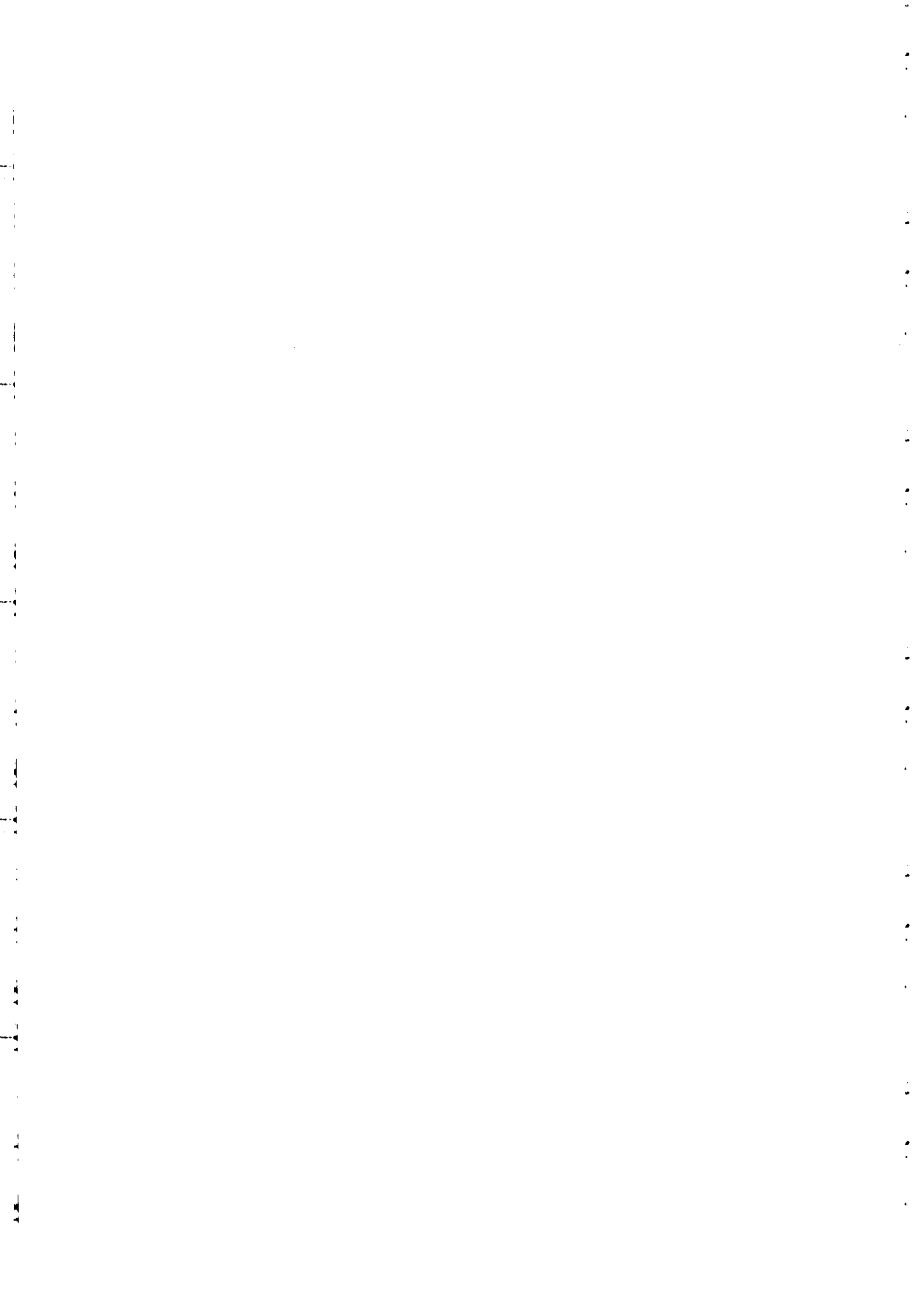
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**"Measurements of Nonlinearities in Silicon Nanoclusters  
& Telecommunication Fibers" - I**

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*Please note: These are preliminary notes intended for internal distribution only.*



# **Measurement of Nonlinearities in Silicon Nanoclusters and Telecommunication Fibers I**

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# Nonlinear Optics

$$\begin{aligned} P = & X^{(1)} \bullet E && \{\text{linear optics; } n = (1 + 4\pi X^{(1)})^{1/2} = \epsilon^{1/2}\} \\ & + X^{(2)} \bullet EE && \{\text{second harmonic generation,} \\ & && \text{sum, difference frequency generation,} \\ & && \text{Pockels effect, } \dots\} \\ & + X^{(3)} \bullet EEE && \{\text{third harmonic generation,} \\ & && \text{nonlinear index of refraction,} \\ & && \text{Raman scattering,} \\ & && \text{two photon absorption, } \dots\} \\ & + \dots \end{aligned}$$

# Optical Nonlinearities

- Optical nonlinearities limit the amount of power transmitted through a fiber and can cause noise and crosstalk in lightwave systems. A long-haul transmission system (10,000-km) would require 250 erbium-doped fiber amplifiers (EDFAs) for a typical repeater spacing of 40-km. EDFAs are typically 15-25 meters in length. A technique to measure  $n_2$  ( $n = n_0 + n_2 I$ ) in *short lengths* ( $< 25\text{-m}$ ) of fiber would be extremely useful in predicting system performance.
- Silicon nanoclusters, with enhanced third order nonlinearities ( $\chi^{(3)}$  (esu)) may prove to be a new and novel nonlinear element for all-optical switching. Due to the extremely small nonlinearity of silica fiber ( $\chi^{(3)}$  (esu)  $\approx 9 \times 10^{-14}$ ), a fiber nonlinear optical loop mirror (NOLM) has to be on the order of 10-km long to achieve the necessary  $\pi$ -phase shift for ~~high-speed~~ **all optical** switching. Nonlinearities as large as ( $\chi^{(3)}$  (esu)  $\approx 10^{-4}$ ) **have been** measured in silicon nanoclusters.

# Nonlinear Optical Properties of Silicon Nanoclusters Made by Laser Ablation And Ion Implantation

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# Introduction

- Previous experiments with ns pulses indicated large nonlinearity in laser ablated Si nanoclusters (NC)  $\chi \sim 10^{-13}$  esu  
(S. Vijayalakshmi, and H. Grebel) *Silica fiber*  
 $\lambda = 532\text{nm}; \chi_{\text{Re}}^{(3)} \sim 10^{-4}$  esu;  $\lambda = 355\text{ nm}; \chi_{\text{Re}}^{(3)} \sim 10^{-5}$  esu
- Current investigations of ultrashort pulses ( $\lambda = 375\text{nm}, 532\text{ nm}, 790\text{ nm}$ ) are consistent with ns results.
- Large nonlinearity may be due to a quantum size effect arising from close-packed nanocrystallites of silicon within micron-sized droplets--a "cooperative" phenomena
- Si ion implantation  $\rightarrow$  uniform size distribution  
 $\rightarrow$  nonlinear response dominated by nonlinear absorption ( $\chi_{\text{Im}}^{(3)}$ )
- Potential as an optical switch for Si based integrated optoelectronic systems.

## Laser Ablated Si NC

## Ion Implanted Si NC

- Pulses from a KrF excimer laser ( $\lambda=248$  nm,  $\tau_p=8$  ns,  $P=3$ W) are focused onto a Si wafer ( $\langle 100 \rangle$ , n-type,  $10^{16}$  cm $^{-3}$ )
- Clusters from silicon are deposited onto a quartz substrate 3 cm away.
- Resultant film made of micron-size droplets (2-3  $\mu$ m)
- Within the droplets, close-packed Si NC with a size distribution: 3-50 nm
- Due to directional nature of plume, samples possessed three regions with varying film thickness: 100nm, 200nm and 400nm
- Si NC formed by Si (400keV) implanted into fused silica followed by annealing (1100° C) in flowing Ar + 4% H $_2$
- Implantation dose of  $6 \times 10^{17}$  cm $^{-2}$  with a peak excess Si concentration of  $2 \times 10^{22}$  cm $^{-3}$
- Cluster mean diameter: 5-6 nm
- Film thickness: 300 nm

*Ion implanted Si sample provided by*

*C.W. White*

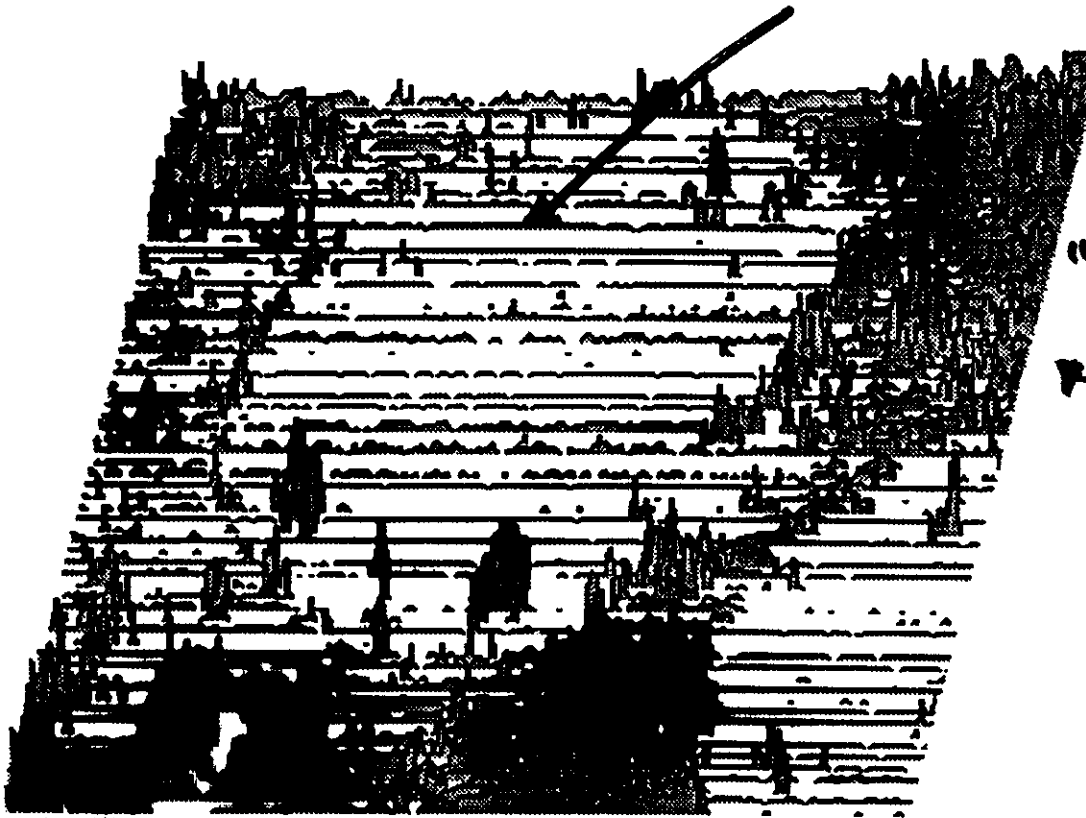
*Solid State Division, Oak Ridge*

*National Laboratory*



# Laser Scanning Microscopy

laser ablated region

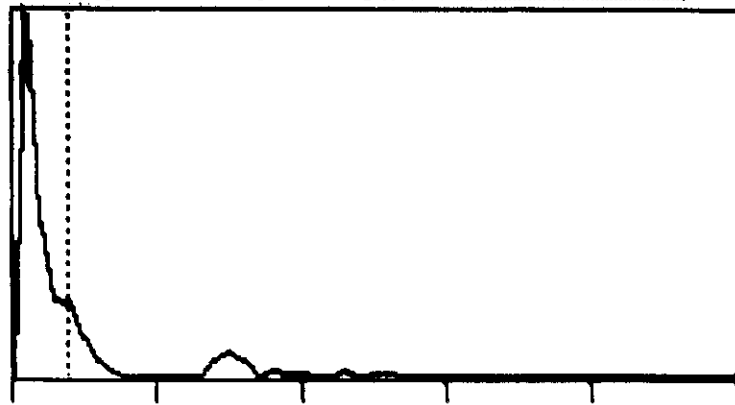


"Nano-Dust"

2  $\mu\text{m}$

20  $\mu\text{m}$

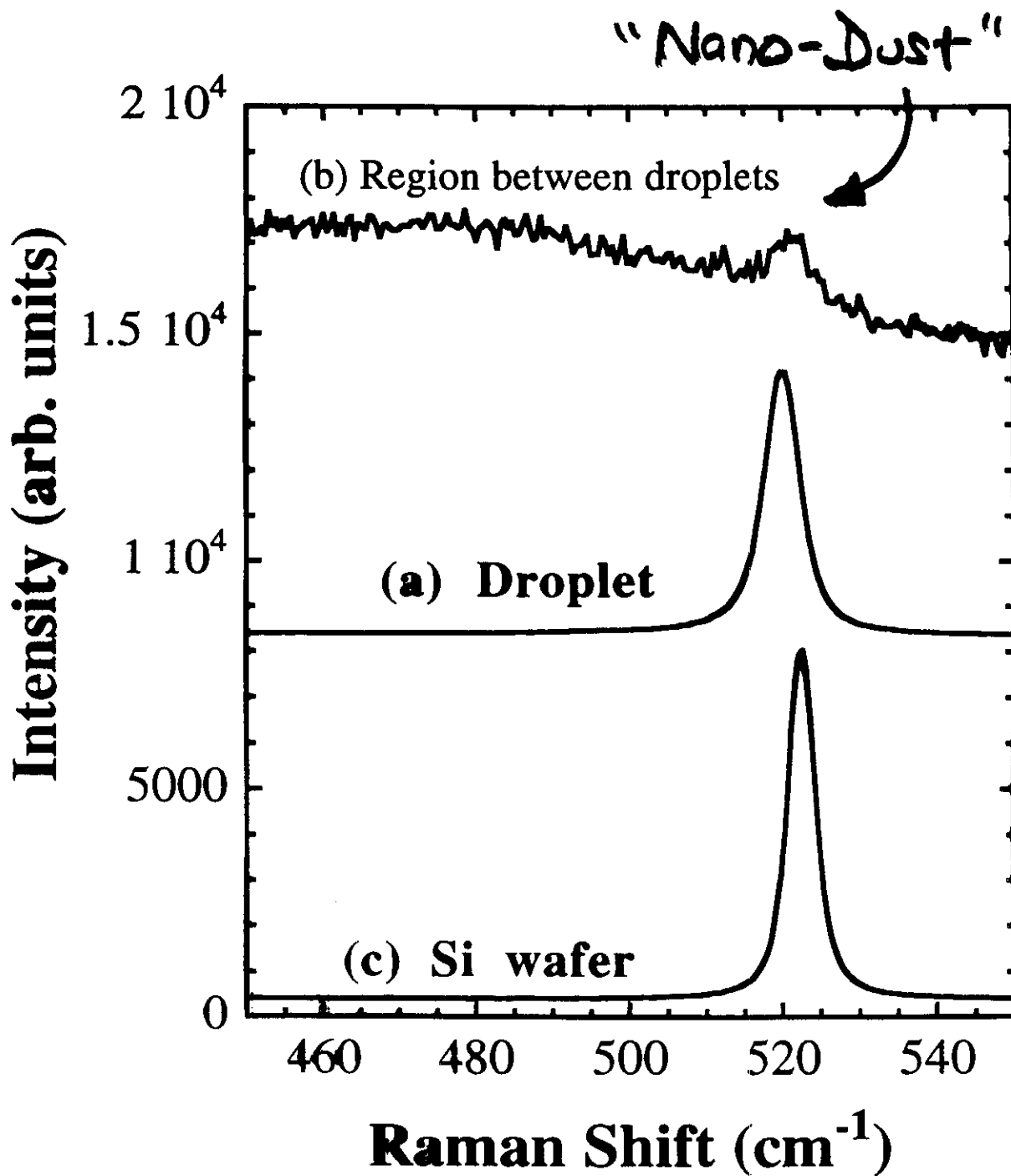
z : x = 9.92



0  $\mu\text{m}$

2  $\mu\text{m}$

# Micro-Raman Spectra - Laser Ablated



# Nonlinear Optical Materials

$$n = n_0 + n_2 I(r,t) = n_0 + \Delta n(r,t)$$

$$\alpha = \alpha_0 + \beta I(r,t) = \alpha_0 + \Delta \alpha(r,t)$$

$$n_2 \sim \chi_{Re}^{(3)}$$

$$\beta \sim \chi_{Im}^{(3)}$$

$$\Delta \phi(t) = \frac{2\pi}{\lambda} \Delta n(t) l_{eff} ; l_{eff} = \frac{1 - e^{-\alpha L}}{\alpha}$$

$$I(r) = I_0 e^{-2r^2/r_0^2}$$

Gaussian spatial profile

$$\text{Rayleigh range } z_0 = \frac{\pi r_0^2}{\lambda} = \frac{\pi \omega_0^2}{\lambda}$$

$\omega_0 \equiv$  beam waist

$$f^{-1} = L \left. \frac{\partial^2 \Delta n}{\partial r^2} \right|_{r=0}$$

Nonlinear lens

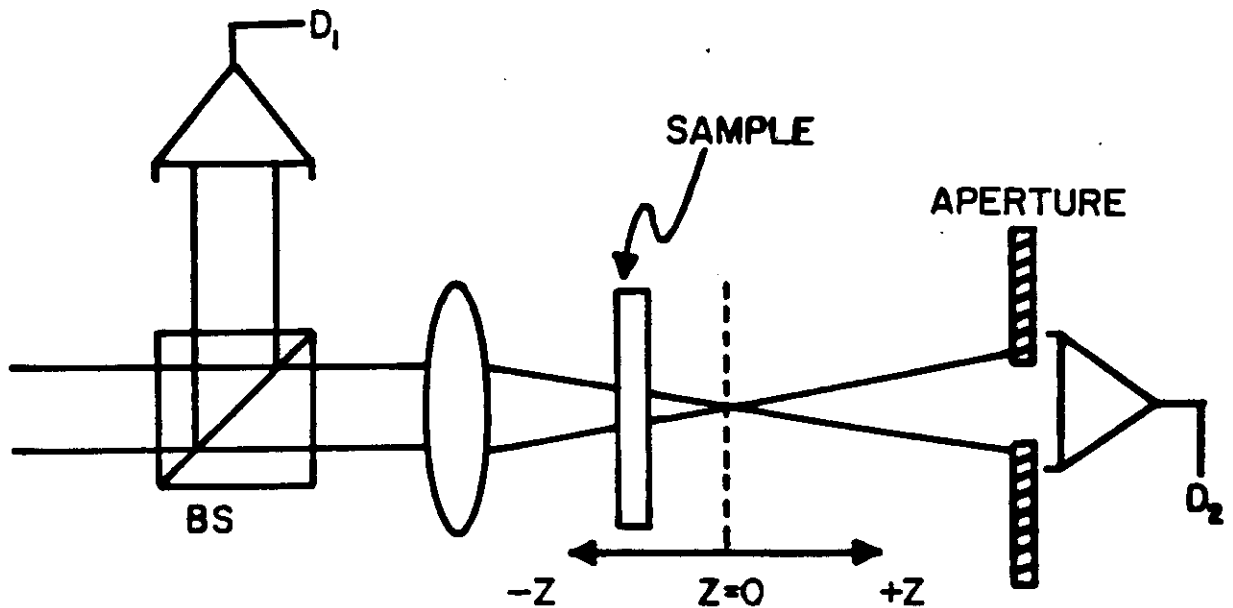
$$f = \frac{r_0^2 c \epsilon_0 n_0}{n_2 I_0 L}$$

of focal length  $f$

The thin nonlinear material ( $L \ll z_0$ ) acts similar to thin concave ( $n_2 > 0$ ) and convex ( $n_2 < 0$ ) lenses for paraxial rays.

# Z-SCAN

(Mansoor Sheik-Bahae, Eric Van Stryland  
et al., 1990)

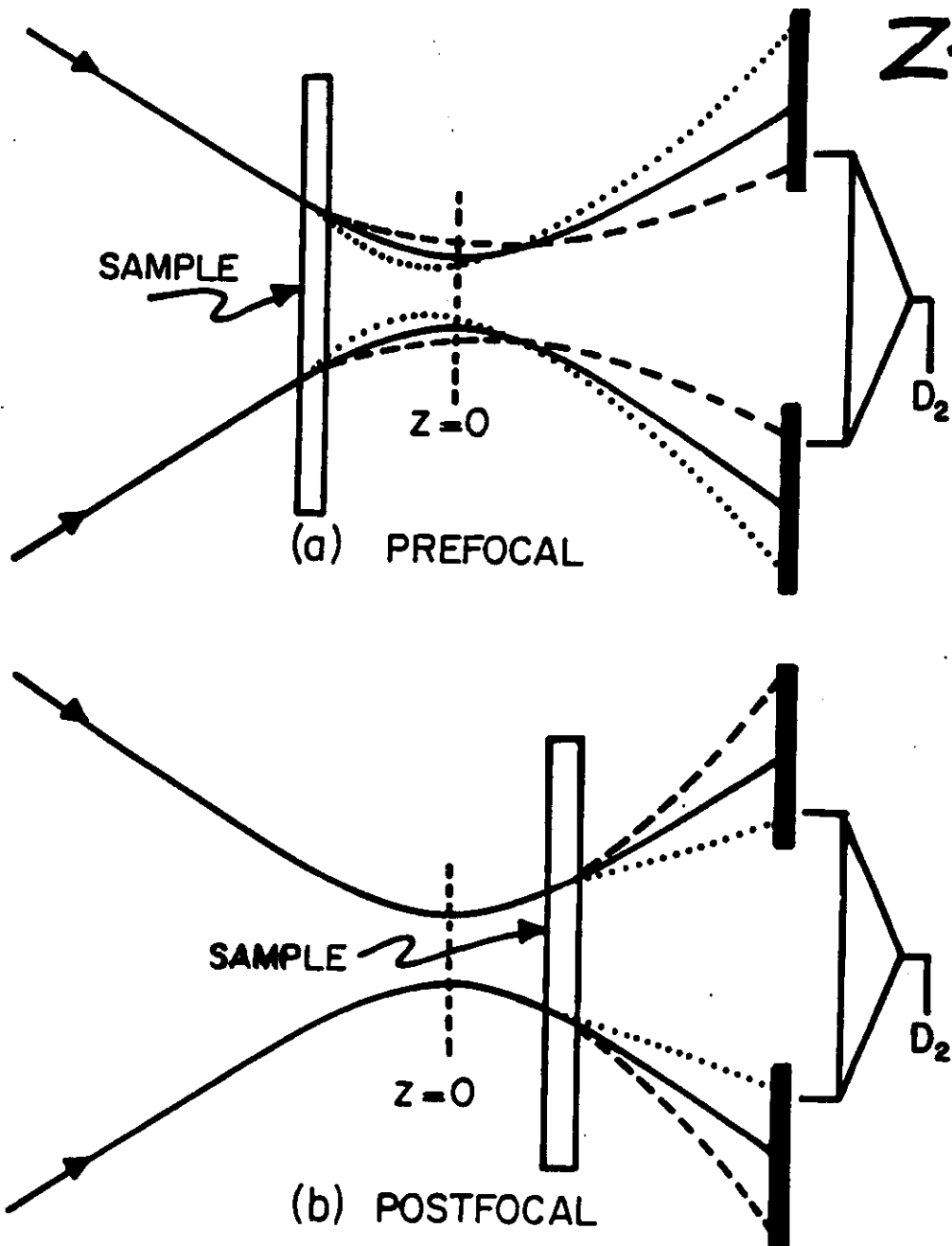


**FIGURE 13.8** Experimental setup for the z-scan measurement. The transmission through the thin sample and aperture is determined by the ratio of the energy measured by detector  $D_2$  to that measured by detector  $D_1$ ,  $T = D_2/D_1$ .

# Z-SCAN

A technique that uses a thin material ( $L \ll Z_0$ ) to determine the sign and magnitude of the index change ( $\Delta n = n_2 I$ ) and the magnitude of the nonlinear absorption ( $\Delta \alpha = \beta I$ ). A small aperture is placed on-axis in front of a detector in the far field. For an incident laser beam, the normalized transmittance is measured at different positions along the  $z$  direction while the sample is translated symmetrically through the focused beam waist. If  $n_2 > 0$  and the sample is positioned before the focus, the nonlinear medium will focus the beam earlier and to a smaller waist (dotted line Prefocal). Since the waist is made smaller the beam expands more rapidly owing to diffraction; remains collimated over a shorter distance in the near field; and diverges at a larger beam angle in the far field, which reduces the irradiance at detector  $D_2$ . When the sample passes into the postfocal position the positive self-lensing of the nonlinear material tends to reduce the beam divergence (dotted line Postfocal), which results in increased irradiance at detector  $D_2$ . If  $n_2 < 0$  and the sample is placed in the prefocal region, the beam waist at the focus will be increased and the focus will be closer to the aperture (dashed line Prefocal). As a result, more radiation will pass through the aperture, producing an increased signal on the detector. When the material passes into the postfocal region the negative lensing effect of the material will spread the already diverging rays even more (dashed line Postfocal) so that the irradiance will be significantly decreased at the detector.

# Z-SCAN



**FIGURE 13.9** Nonlinear refraction: (a) prefocal ( $z < 0$ ) diffraction, (b) postfocal ( $z > 0$ ) diffraction. The solid line in both figures is linear (low-intensity) diffraction. The dotted line shows  $n_2 > 0$  and the dashed line corresponds to  $n_2 < 0$ .

.....  $n_2 > 0$   
-----  $n_2 < 0$

# Z-SCAN (closed)

Time averaged apertured on-axis transmission

$$T = 1 + \frac{4\Delta\phi x}{(x^2 + 1)(x^2 + 9)}$$

$$x = z/z_0 ; z_0 = \frac{\pi \omega_0^2}{\lambda}$$

$$n(I) = n_0 + \delta I = n_0 + n_2 I$$

$$\delta = \frac{\Delta\phi \lambda}{2\pi I_0 L_{\text{eff}}}$$

$$\chi_{\text{Re}}^{(3)} = 2n_0^3 \epsilon_0 c \delta$$

$$n_2 (\text{esu}) = \frac{c n_0}{40\pi} \delta \left( \frac{\text{cm}^2}{\text{W}} \right)$$

# Closed aperture Z-scan

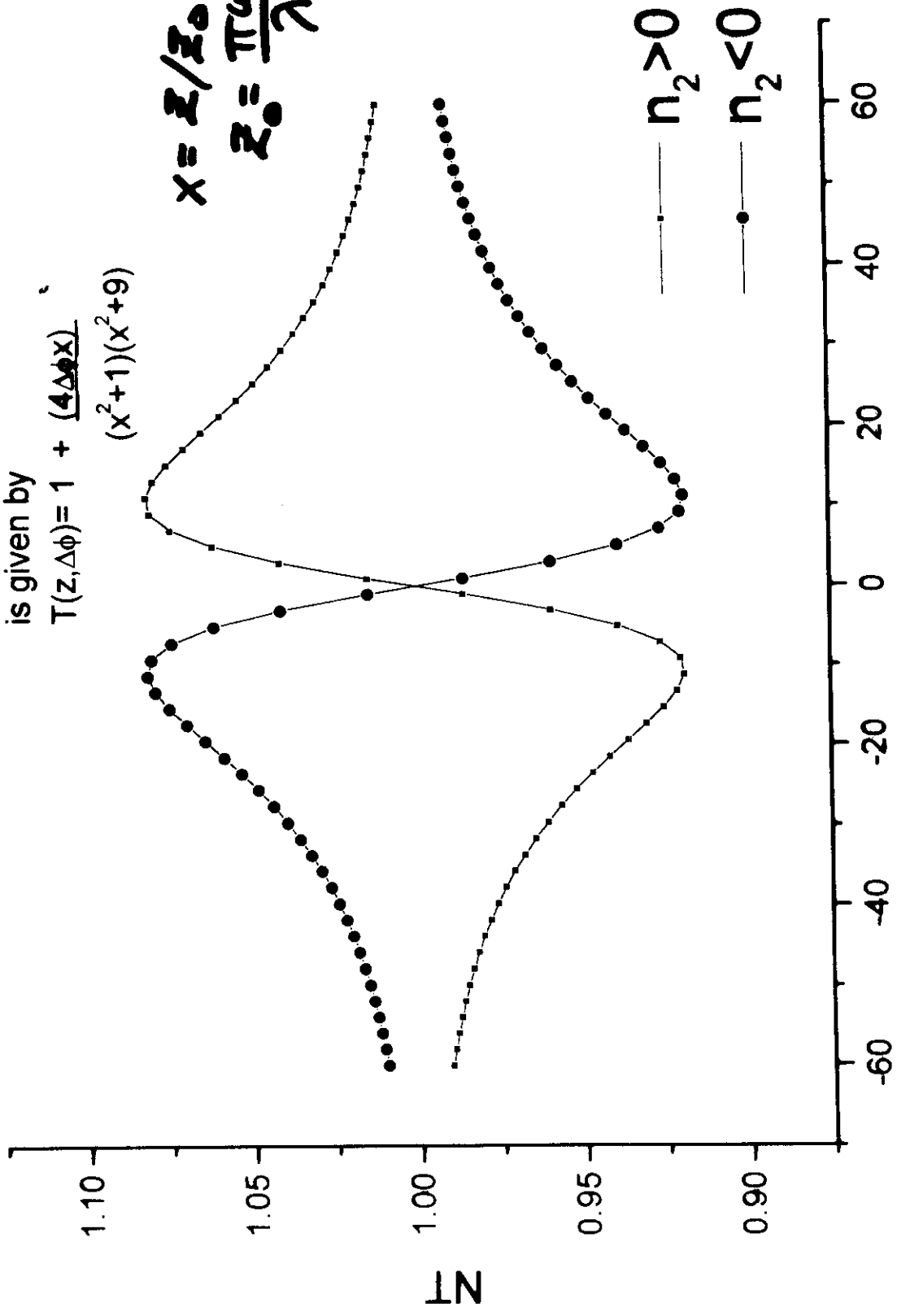
The normalized transmission

is given by

$$T(z, \Delta\phi) = 1 + \frac{(4\Delta\phi x)}{(x^2 + 1)(x^2 + 9)}$$

$$x = z/z_0$$

$$z_0 = \frac{\pi \omega_0^2}{\lambda}$$



Z(mm) fig.4



# Z-SCAN (open)

Open apertured transmission  
- sensitive to nonlinear  
absorption only

$$T = 1 - \frac{\beta I_0 L_{\text{eff}}}{2\sqrt{2}(1+x^2)}$$

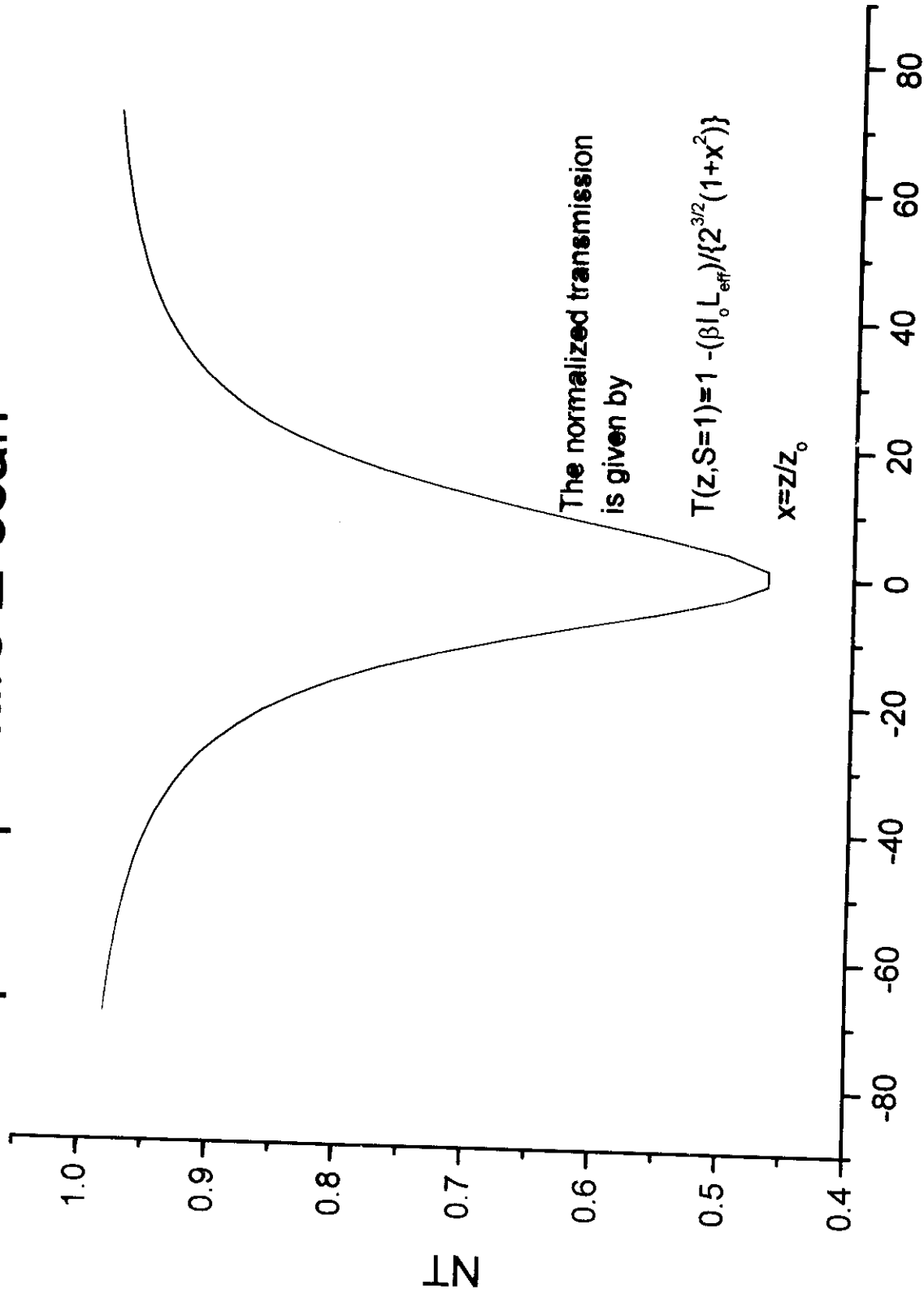
$$x = z/z_0 ; z_0 = \frac{\pi \omega^2}{\lambda}$$

$$\alpha = \alpha_0 + \beta I$$

$$\chi_{\text{Im}}^{(3)} = \frac{n_0^3 \epsilon_0 c^2}{\omega} \beta$$

$$\omega = 2\pi \nu$$

# Open aperture Z-scan



Z (mm) fig.2

# Z-SCAN

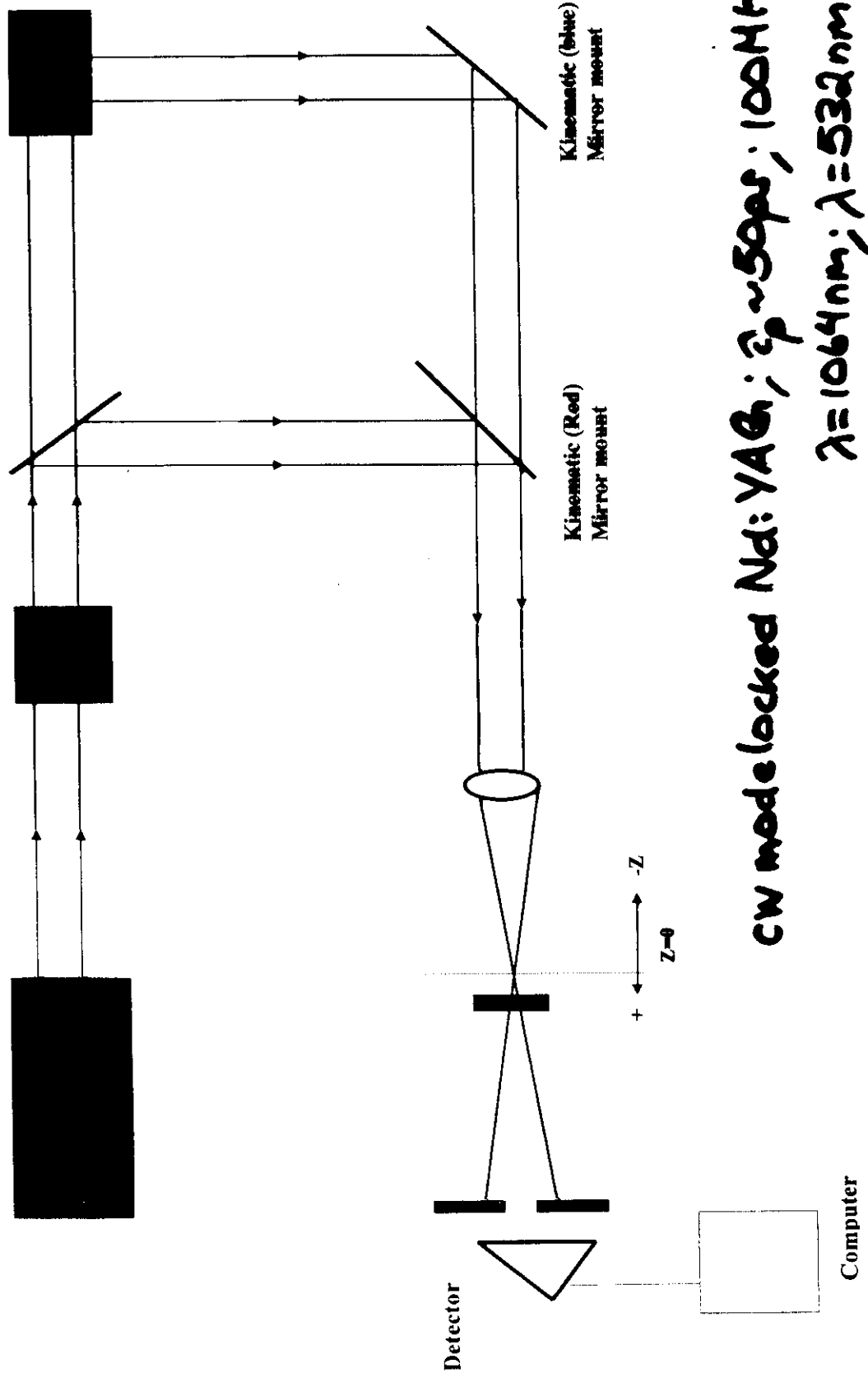
(M. Sheik-bahae et al., 1990)

- Sample is scanned about the focal length of a lens and transmission detected as a function of distance from the focal point.
- Sample acts as a thin lens and either self-focuses or defocuses the beam
- Nonlinear refraction estimated by measuring farfield output with an apertured detector and nonlinear absorption without the aperture.
- In the presence of nonlinear absorption: normalized closed aperture is divided by open aperture to retrieve  $n_2$ .

**Ti:sapphire Laser**  
 $\lambda : 7-1 \mu\text{m}, \tau_p \sim 100 \text{ fs}$

**Pulse selector**  
**Rep. rate: 4KHz-82 MHz**

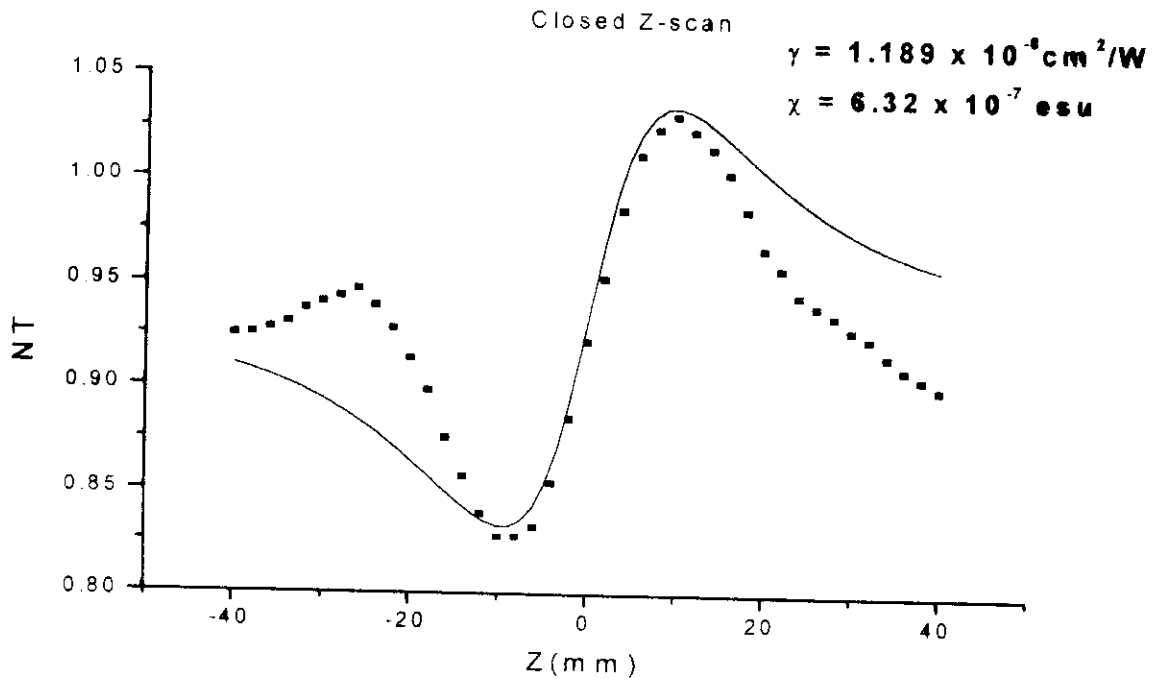
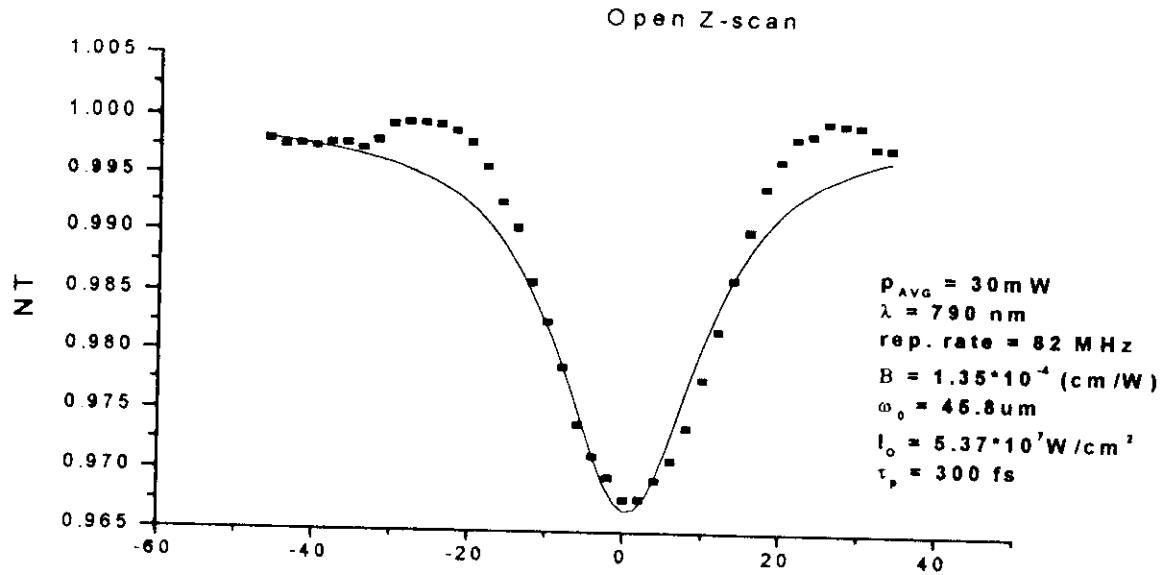
**Doubler & Tripler**  
 $\lambda : 230-532 \text{ nm}$



**CW mode locked Nd:YAG;  $\tau_p \sim 50 \text{ ps}, 100 \text{ MHz}$**   
 **$\lambda = 1064 \text{ nm}; \lambda = 532 \text{ nm}$**

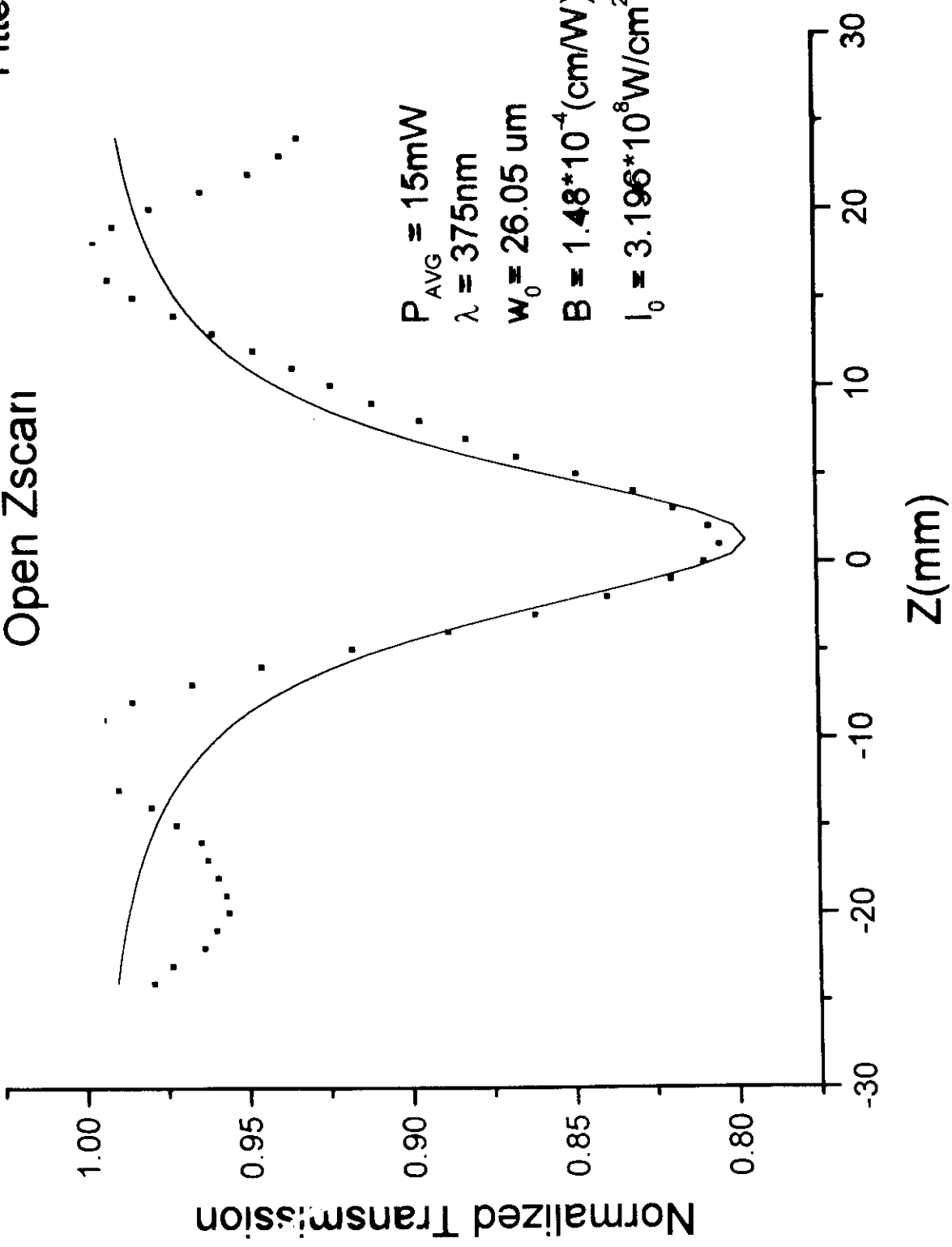
*Experimental setup for the Z-scan measurement (fig.1)*

# Laser Ablated Si NC

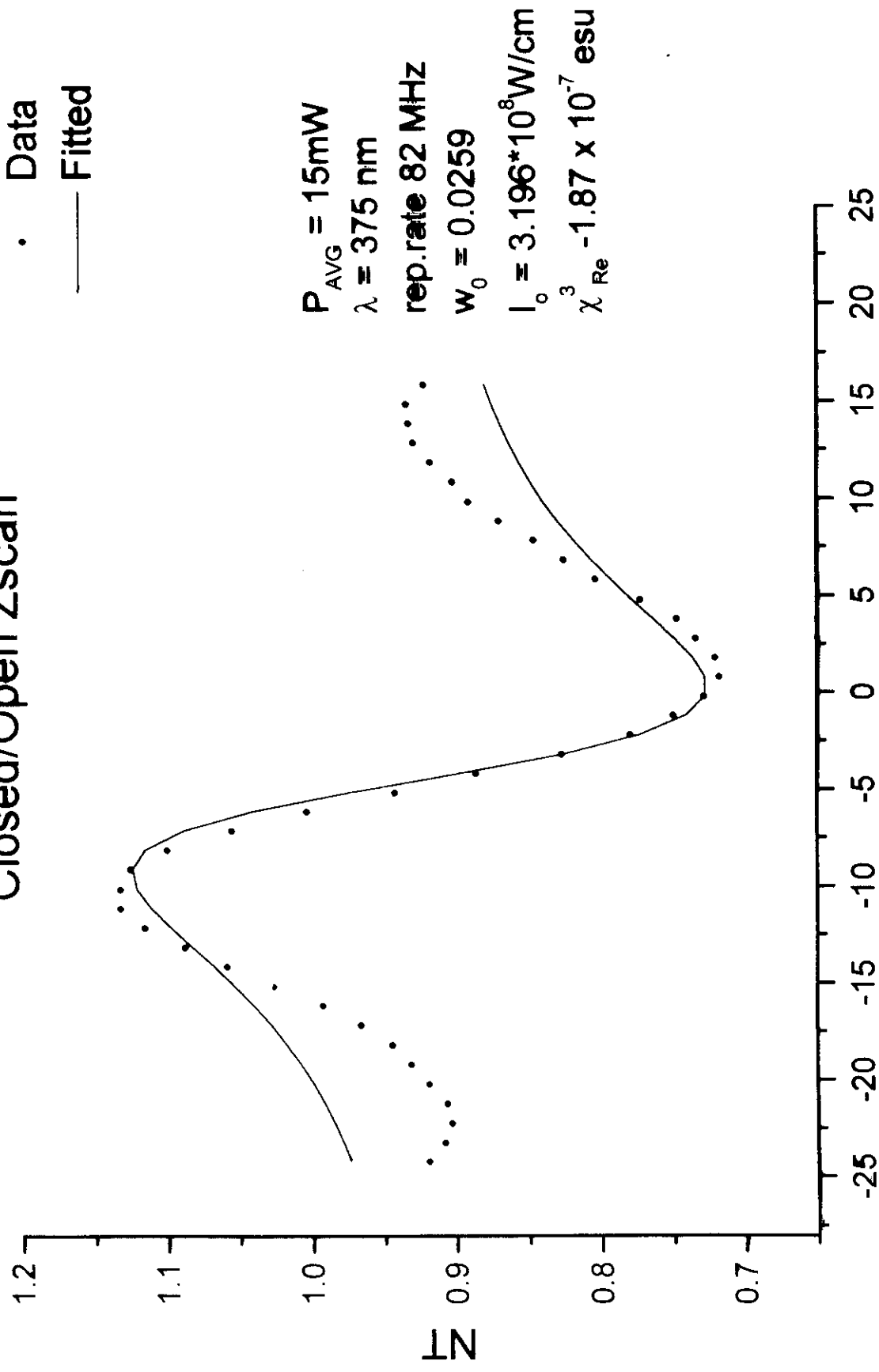


# Laser Ablated Si NC Open Zscan

DATA  
Fitted



# Laser Ablated Si NC Closed/Open Zscan



Z(mm) fig.4

**Z-scan measurements of Si nanoclusters prepared  
by laser ablation**

**Table 1**

**cw-modelocked Ti-Sapphire laser**

$\lambda(\text{nm})$	Rep. rate	$\tau_p$	$\beta(\text{cm/W})$	$\chi^{(3)}(\text{esu})$	$I_0 (\text{W/cm}^2)$
<b>790</b>	<b>82 MHz</b>	<b>250 fs</b>	$1.35 \times 10^{-4}$	$6.32 \times 10^{-7}$	$5.37 \times 10^7$
<b>375</b>	<b>82 MHz</b>	<b>100 fs</b>	$1.48 \times 10^{-5}$	$-1.87 \times 10^{-7}$	$3.2 \times 10^8$
<b>375</b>	<b>82 MHz</b>	<b>100 fs</b>	$6.07 \times 10^{-4}$	$-7.64 \times 10^{-7}$	$1.062 \times 10^8$

**cw-modelocked and frequency doubled Nd:YAG laser**

$\lambda(\text{nm})$	Rep. rate	$\tau_p$	$\chi^{(3)}(\text{esu})$	$I_0(\text{W/cm}^2)$
<b>532 nm</b>	<b>100 MHz</b>	<b>50 ps</b>	$6 \times 10^{-4}$	$5.1 \times 10^4$
<b>532 nm</b>	<b>1 MHz</b>	<b>50 ps</b>	$4 \times 10^{-4}$	$1.9 \times 10^5$

**Second & third harmonics of a pulsed Q-switched Nd:YAG Laser**

(Vijayalakshmi and Grebel)

$\lambda(\text{nm})$	Rep. rate	$\tau_p$	$\chi^{(3)}(\text{esu})$	$I_0(\text{W/cm}^2)$	$\tau^*$
<b>532</b>	<b>10 Hz</b>	<b>8 ns</b>	$10^{-3}$	$3 \times 10^4$	$3.5 \pm .5 \text{ ns}$
<b>355</b>	<b>10 Hz</b>	<b>8 ns</b>	$2.28 \times 10^{-5}$	$5 \times 10^5$	$143 \pm 20 \text{ ns}$

\*Limited by laser  
pulse width

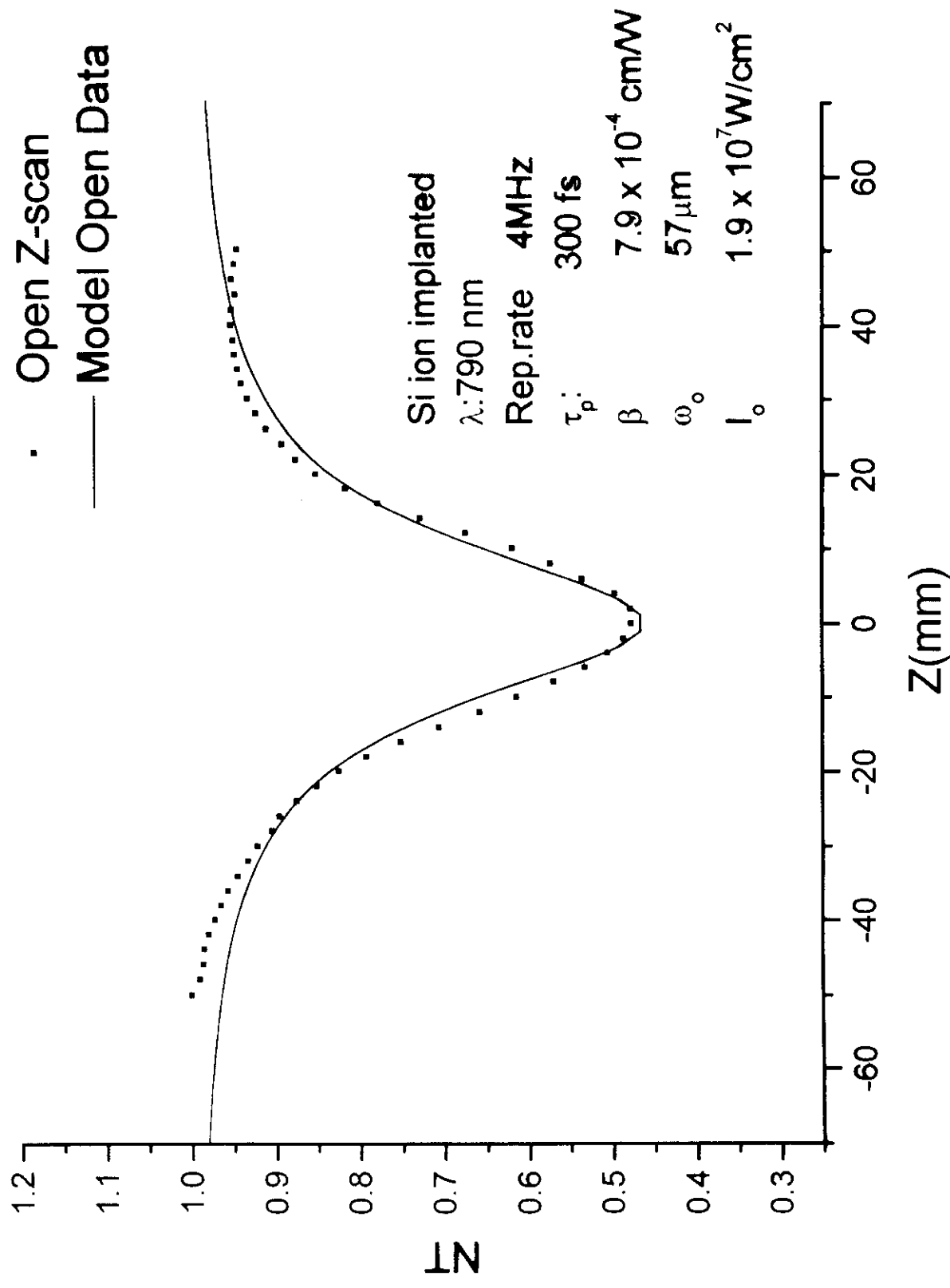
**Porous Silicon :**  $\chi_{\text{Re}}^{(3)} \approx 10^{-9} \text{ esu}$  (Henari et. al, 1995)

**Silica Fiber:**  $\chi_{\text{Re}}^{(3)} \approx 9 \times 10^{-14} \text{ esu}$

Lalanne, Johnson et al.



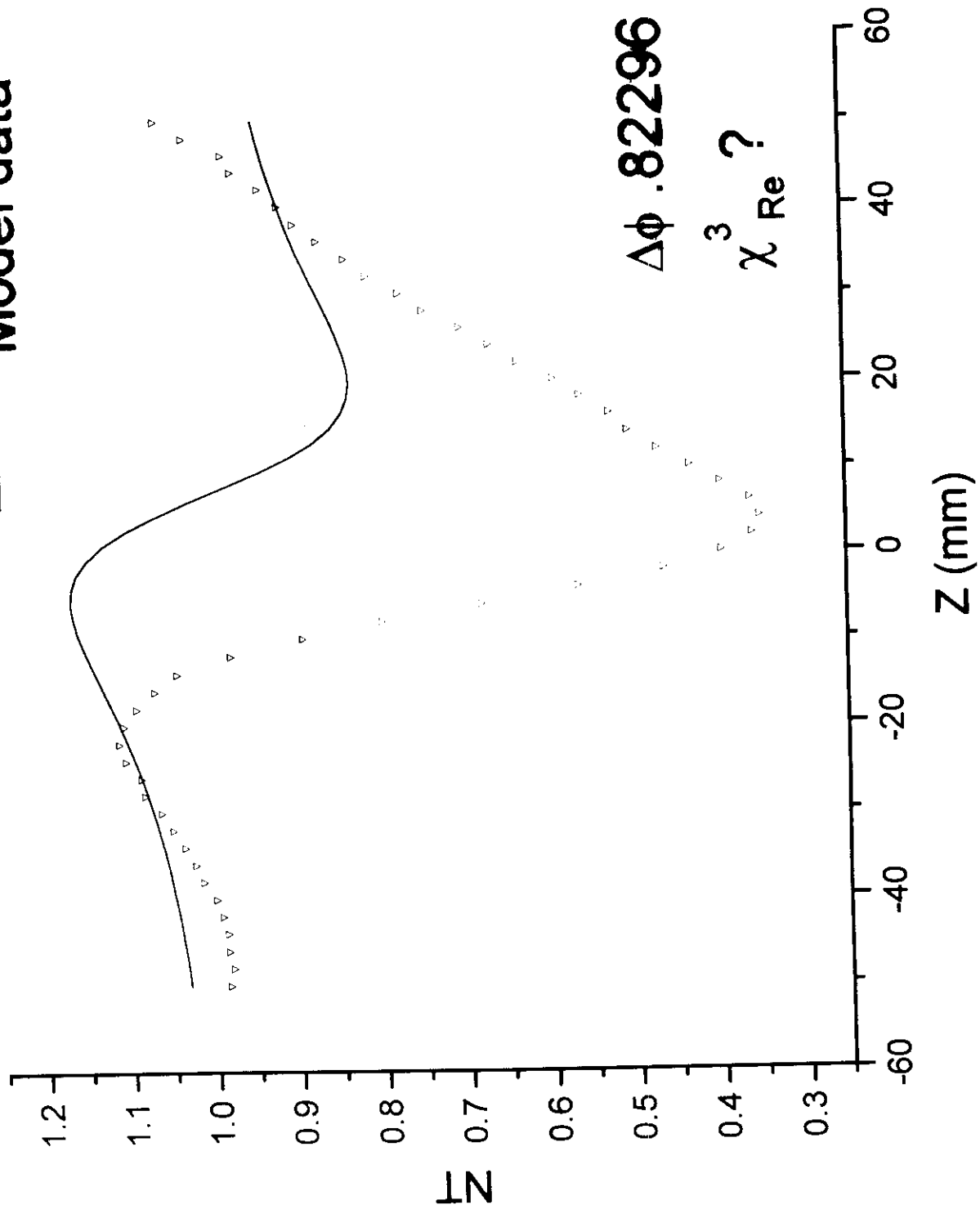
# Si ion implanted sample



# Si ion implanted sample

Closed/Open Z-scan

— Model data

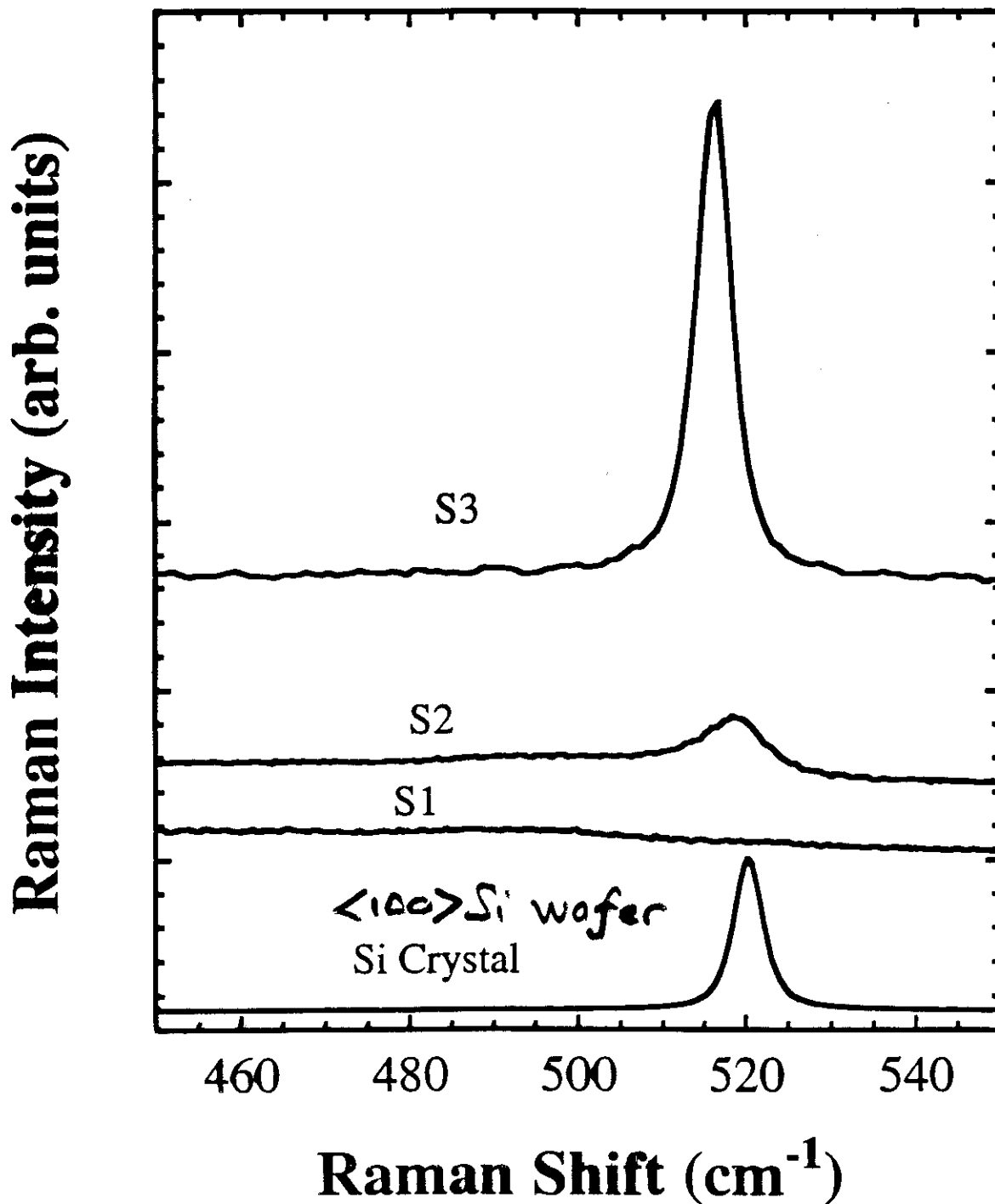


# Micro-Raman Spectra

S1:  $1.5 \times 10^{17} \text{ cm}^{-2}$ ; Si-NC  $\sim 3-4 \text{ nm}$

S2:  $6 \times 10^{17} \text{ cm}^{-2}$ ; Si-NC  $\sim 5-6 \text{ nm}$

S3: laser ablated; Si-NC  $\sim 15 \text{ nm}$



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## Conclusions (Laser Ablated)

- Large nonlinearity arises from close-packed nanocrystallites of silicon within the micron-sized droplets -- a “cooperative” or “collective” phenomena.
- Thermal contributions to  $\chi^{(3)}_{\text{Re}}$  appears to be small @ 532 nm  
( $\tau_p$  50 ps) 100 MHz :  $\chi_{\text{Re}}^{(3)} = 6 \times 10^{-4} \text{esu}$   
1 MHz :  $\chi_{\text{Re}}^{(3)} = 4 \times 10^{-4} \text{esu}$
- Consistent with the ns result (532 nm, 355nm) ultrashort pulse excitation results in a peak in  $\chi_{\text{Re}}$  at 532 nm and a nearly 3 order of magnitude drop at 375 nm and 790 nm  
→ resonance?

- 
- Underlying Physics is still not well understood
  - Future experiment:  
Time resolve the nonlinearity for both the laser ablated and ion implanted Si NC

# Conclusions (Ion Implanted)

- Z-scan data shows a large  $\beta$  which is attributed to 2-photon absorption.
- Nonlinearity is dominated by absorption, unable to extract information about  $\chi^{(3)}_{\text{Re}}$
- Thermal contributions to  $\chi^{(3)}_{\text{Im}}$  decrease as a function of repetition rate.

@790 nm

Rep. rate	$\beta$	$I_0$
82 MHz	$2.193 \times 10^{-3} \text{ cm/W}$	$4 \times 10^6 \text{ W/cm}^2$
4 MHz	$6.18 \times 10^{-4} \text{ cm/W}$	$8.12 \times 10^6 \text{ W/cm}^2$
.8 MHz	$3.26 \times 10^{-4} \text{ cm/W}$	$2 \times 10^7 \text{ W/cm}^2$

Apparent larger thermal contribution to the nonlinearity than the laser ablated Si NC

# Future Experiments

- Efforts to time resolve the nonlinearity have been hampered by low pulse energies (pJ) – 50 kHz Ti:sapphire regenerative amplifier ( $\mu\text{J}$ ) on order.
- Time-resolved two-color Z-scan measures nondegenerate nonlinear absorption ( $\beta$ ) and nonlinear refraction ( $n_2$ ) – time resolve separately the sign and the magnitude of  $\beta$  and  $n_2$  at frequency  $\omega_{\text{probe}}$  that are due to the presence of a strong excitation at frequency  $\omega_{\text{exc}}$ .
- For high-speed optical switching a fast electronic nonlinearity is needed over a slow thermal nonlinearity and thus time-resolved nonlinearity measurements. Another approach – use fs pulses ( $\lambda=1550 \text{ nm}$ ) to generate a third harmonic signal ( $\lambda=517 \text{ nm}$ ) – a third harmonic signal can only result from an electronic nonlinearity.