

SUMMER SCHOOL ON ASTROPARTICLE PHYSICS AND COSMOLOGY

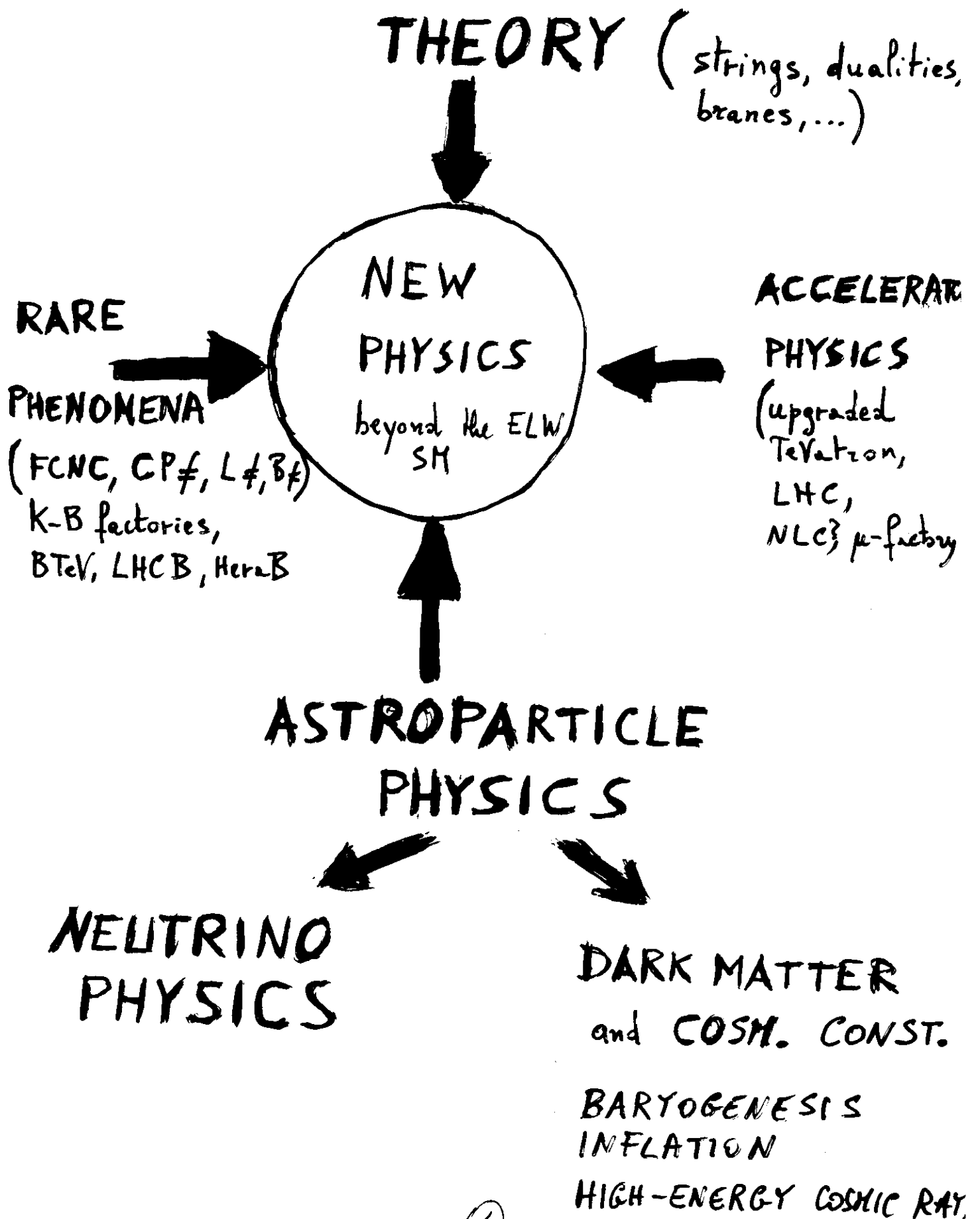
12 - 30 June 2000

DARK MATTER AND PARTICLE PHYSICS

Lectures I and II

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Please note: These are preliminary notes intended for internal distribution only.



THE STANDARD MODEL OF PARTICLE PHYS.

ELECTROWEAK SM $\rightarrow$ Glashow - Weinberg - Salam SI
 INTERACTIONS (GWS)

STRONG INTERACTIONS $\rightarrow$ QCD

GWS and QCD are GAUGE THEORIES

↓
Local Symmetry

$$GWS \text{ SM} \rightarrow SU(2)_L \times U(1)_Y$$
$$QCD \rightarrow SU(3)_c$$

[global symm. : ex. $\bar{\psi} (\not{\partial} - m) \psi$
invariant under $\psi(x) \rightarrow e^{i\alpha} \psi(x)$
the phase α is the same $\forall x$

Local symm. is ask for invariance under

$$\psi(x) \rightarrow e^{i\alpha(x)} \psi(x)$$

α depends on x

$$\bar{\psi}(\partial - m)\psi \Rightarrow \bar{\psi}(\cancel{\partial} - m)\psi$$

↳ covariant derivative

$$\partial_\mu \rightarrow \partial_\mu - ie A_\mu \xrightarrow{(2)} \text{vector compensating field}$$

$SU(2)_L \rightarrow 3$ vector (gauge) fields, $W_\mu^1, W_\mu^2, W_\mu^3$

$U(1)_Y \rightarrow 1$ " " " B_μ

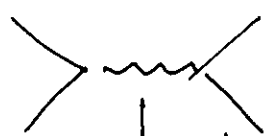
$SU(3)_C \rightarrow 8$ " " " λ_μ^a $a=1, \dots, 8$

(vector (gauge) fields in the adjoint representation)

Exact Gauge Symmetries $\begin{cases} \rightarrow \text{Renormalizable } \text{😊} \\ \rightarrow \text{Massless gauge bosons } \text{😞} \end{cases}$

weak interactions
need massive vector bosons

Feynman $\times$ ← point-like interactions


↓ intermediate vector boson

How to break a gauge theory without
spoiling its renormalizability?

⇓

SPONTANEOUS BREAKING OF
GAUGE SYMM. $\Rightarrow$ HIGGS MECHANISM

explicit breaking : add $M^2 W_\mu W^\mu$
spoils renormaliz.

spontaneous breaking:

L invariant, vacuum is not invariant

(ex. : $\mathcal{L} = \partial_\mu \varphi \partial_\mu \varphi^* + V(\varphi)$)

$$V(\varphi) = -\mu^2 |\varphi|^2 + \lambda |\varphi|^4$$

spont. break. of a global symm : Goldstone bosons

$G \rightarrow G'$ # Goldst. bosons = # of generators in G/G'

spont. break. of a gauge theory:

Goldst. bosons "eaten up" by the gauge bosons (they become their longitudinal comp.)

$\Rightarrow$ Higgs mechanism

$$SU(2)_L \otimes U(1)_Y \Rightarrow U(1)_{em}$$

Higgs doublet H

$$\Rightarrow \langle H \rangle = \begin{pmatrix} 0 \\ v \end{pmatrix}$$

$$\mathcal{L} = \partial_\mu H \partial_\mu H^\dagger + \mu^2 H H^\dagger - \lambda (H H^\dagger)^2$$

W^+, W^-, Z^0 massive
 γ massless

FERMION MASSES

Lot. group $SU(2) \times SU(2)$

2-comp. Weyl spinor $\chi \left(\frac{1}{2}, 0 \right) \xrightarrow{\text{conj. same 2 comp}} \bar{\chi} \left(0, \frac{1}{2} \right)$

$\eta \left(0, \frac{1}{2} \right) \quad \bar{\eta} \left(\frac{1}{2}, 0 \right)$

Given the two 2-comp. Weyl spinors χ and η , what are the possible fermion mass terms?

1) $\chi^\alpha \chi^\beta \epsilon_{\alpha\beta}$ ($\alpha, \beta = 1, 2$ $SU(2)$ indices)
 $\eta^{\dot{\alpha}} \eta^{\dot{\beta}} \epsilon_{\dot{\alpha}\dot{\beta}}$ There are terms involve only 2 components

$\Rightarrow$ MAJORANA MASS TERMS
 obtained coupling a spinor with itself

2) $\chi^\alpha \bar{\eta}^\beta \epsilon_{\alpha\beta}$ DIRAC MASS TERMS
 $\bar{\chi}^{\dot{\alpha}} \eta^{\dot{\beta}} \epsilon_{\dot{\alpha}\dot{\beta}}$ $2+2=4$ components
 $\nwarrow$ bilinears formed
 with two independent spinors

FERMION MASSES IN SM

MAJORANA MASSES IMPOSSIBLE FOR
EL. CHARGED FERMIONS ($\chi\chi$ carries
 $Q \neq 0$ if χ is charged) since $U(1)_Q$ is
an exact symmetry

only candidate for Major. mass: neutrino

$\underbrace{\nu^\alpha \nu^\beta}_{\substack{\downarrow \\ T_3 = +1}} \epsilon_{\alpha\beta}$ but ν carries $T_3 = +\frac{1}{2}$

$\rightarrow SU(2)$ forbids this term

DIRAC MASSES:

ex. $\bar{u}_L u_R$ $Q=0$ so $U(1)_Q$ does not
forbid these terms

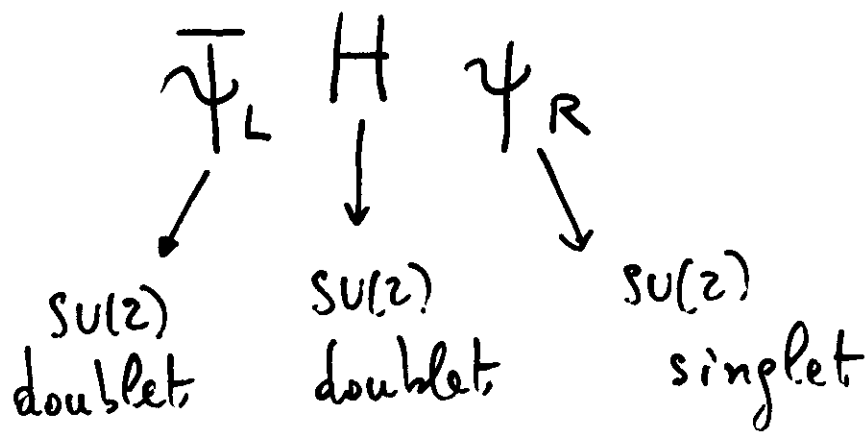
BUT $\downarrow$ in $SU(2)$ doublet $\rightarrow$ in $SU(2)$ triplet
 $SU(2)$ forbids all the fermionic mass terms

$\Rightarrow$ GAUGE INVARIANCE $SU(2)_C \times U(1)_Q$ FORBIDS

BOTH MAJOR. AND $\odot$ DIRAC MASSES IN $\mathcal{L}$

HENCE NO DIRECT FERMION MASS TERM CAN BE ADDED TO $\mathcal{L}_{SM}$

SINCE $SU(2) \times U(1)$ prevents the appearance of $m_f \Rightarrow$ MAKE m_f appear after spontaneous breaking of $SU(2) \times U(1)$



spont. breaking $\langle H^0 \rangle \neq 0 \Rightarrow m \bar{\Psi}_L \Psi_R$

$$\mathcal{L}_{\text{YUKAWA}} = h_U \bar{Q}_L H U_R + h_D \bar{Q}_L \tilde{H} d_R + h_L \bar{L}_L \tilde{H} e_R + \text{h.c.}$$

$$\tilde{H} = i \tau_2 H^* \quad H = \begin{pmatrix} H^0 \\ H^- \end{pmatrix}; \quad \tilde{H} = \begin{pmatrix} H^+ \\ -H^{0*} \end{pmatrix}$$

N.B.: NEUTRINOS ⁽⁴⁾ MASSLESS

NEUTRINO MASS

8

S.M. : ν_L ~~no~~ ν_R why? only ψ $SU(2)_L$ doublet in the scalar sector

Majorana mass : $\rightarrow$ ENLARGEMENT OF THE HIGGS SECTOR

$\nu_L \nu_L$ transforms as the $T_3 = +1$ of an $SU(2)_L$ triplet

$\rightarrow$ gauge invar. requires $\Delta \equiv SU(2)_L$ scalar triplet

$\nu_L \nu_L \Delta \rightarrow SU(2)_L$ singlet
 $\downarrow$ after S.S.B. $\langle \Delta \rangle$

Alternatively: $\nu_L \nu_L \psi \psi$ non-renorm. term. from some fundam. th.

Dirac mass : $m \bar{\nu}_L \nu_R$ $\rightarrow$ ENLARGEMENT OF THE FERMION SECTOR
 requires $(\nu^c)_L$ or ν_R

$\Rightarrow$ in SM ν is rigorously massless!
 at any order in perturbation theory

$$L \neq \quad \nu_L \nu_L \rightarrow \text{triplet}$$

$$\nu \nu \underbrace{\phi \phi}_{\text{triplet}} \Rightarrow \text{dim. } 5$$

$$\frac{1}{M}$$

$$m_\nu \sim e^2 G_F^{-1} / M$$

(if ϕ not elem $\phi \sim \langle \psi \bar{\psi} \rangle$ $\text{dim } \frac{3}{2} \times 6 = 9$)

$$m_\nu \sim e^4 G_F^{-3} / M^5$$

$$L_e, L_\mu, L_\tau \neq : \quad \mu \rightarrow e \gamma$$

$$\underbrace{(\bar{\ell}_{\mu L} \phi \delta_{\mu\nu} \ell_{\nu R})}_{\text{dim } 6} B^{\mu\nu}$$

$$\pi^0 \rightarrow \mu^- e^+, K^0 \rightarrow \mu^- e^+$$

$$\ell'^+ \rightarrow \mu^- e^+ \dots$$

$$\underbrace{(\bar{\ell}_{\mu L} \gamma_\alpha \ell_{\nu L}) (\bar{q}_L \gamma^\alpha q_L)}_{\text{dim } 6}$$

$$(\text{BR}(\mu \rightarrow e \gamma) < 10^{-11}_{\text{exp}})$$

SM

$SU(2) \times U(1)$

GAUGE GROUP
SPONTANEOUSLY
BROKEN GAUGE THEOR.

MATTER

RADIATION

fermions { quarks
leptons

scalars { Higgs

gauge vector

bosons

(messengers of the interaction)

$$\begin{pmatrix} u \\ d \end{pmatrix}_L \xrightarrow{Q=2/3} u_R \quad d_R \quad \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L \quad e_R$$

$$\begin{pmatrix} c \\ s \end{pmatrix}_L \xrightarrow{Q=-1/3} c_R \quad s_R \quad \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L \quad \mu_R$$

$$\begin{pmatrix} t \\ b \end{pmatrix}_L \quad t_R \quad b_R \quad \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L \quad \tau_R$$

$SU(2)$
doublet

$SU(2)$ singlet

$$Q = T_3 + Y$$

$$m_\nu = 0$$

$$\textcircled{H} = \begin{pmatrix} H^0 \\ H^- \end{pmatrix} \text{ higgs doublet}$$

→ ONLY MISSING ACTOR OF THE PLAY (10)

$$W^+ W^- W^0$$

$$U(1)$$

$$B^0$$

$$SU(3)_c$$

$$g^a \quad a=1, \dots, 8$$

gluons

$$\text{after SSB: } SU(2) \times U(1)_r$$

$$\downarrow$$

$$W^+ W^- Z^0, \gamma, g^a$$

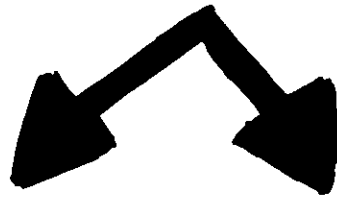
$$g^a$$

PARTICLE PHYSICS TESTS OF THE SM

- PRECISION TESTS → some observables tested at LEP with % precision without any appreciable deviation from the SM expectation
 ↓
 ANY NEW PHYSICS MUST "REPRODUCE EXACTLY" THE SM AT 100 GeV
- ANOMALIES → R_b , 4-jet events, ... (gone)
 HEZA anomalous event at high q^2 (gone)
 $e^+e^- \gamma \gamma$ " CDF event (no other events in the new run)
- RARE PROCESSES → flavour changing neutral current (FCNC) phenomena, CP violation
 (highly suppressed or forbidden in the SM)
 ex. $K-\bar{K}$, $B-\bar{B}$ mixings, $b \rightarrow s \gamma$
 BR ($\mu \rightarrow e \gamma$), d_n^e , ...
 places where new physics BSM can compete fairly with SM
 all results compatible with SM expectations

➡ **NO** INDICATION OF NEW PHYSICS BEYOND THE SM FROM EXP. PARTICLE PHYSICS

1. WHY PHYSICS BEYOND THE SM



EXPERIMENTAL NEEDS

→ PARTICLE PHYSICS

→ PARTICLE + ASTRO
PHYSICS

→ PARTICLE PHYSICS
+
COSMOLOGY

THEORETICAL NEEDS

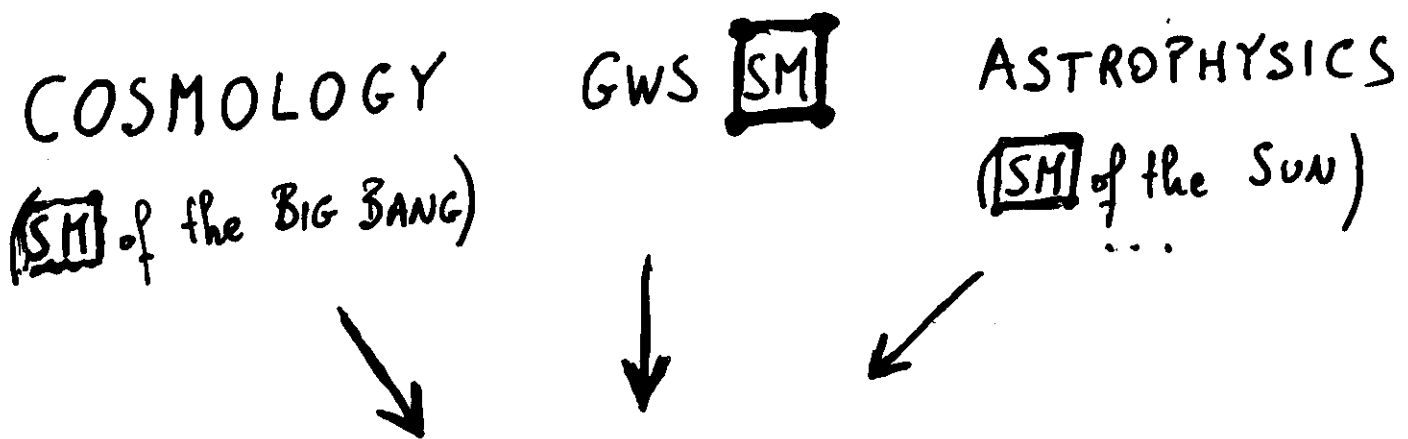
→ INTRINSIC INCONSISTENCY
OF THE MODEL

→ SHORTCOMINGS
(FAILURES TO ANSWER
SOME QUESTIONS WE
CONSIDER FUNDAMENTAL)

→ FINE-TUNINGS

ASTROPARTICLE HINTS

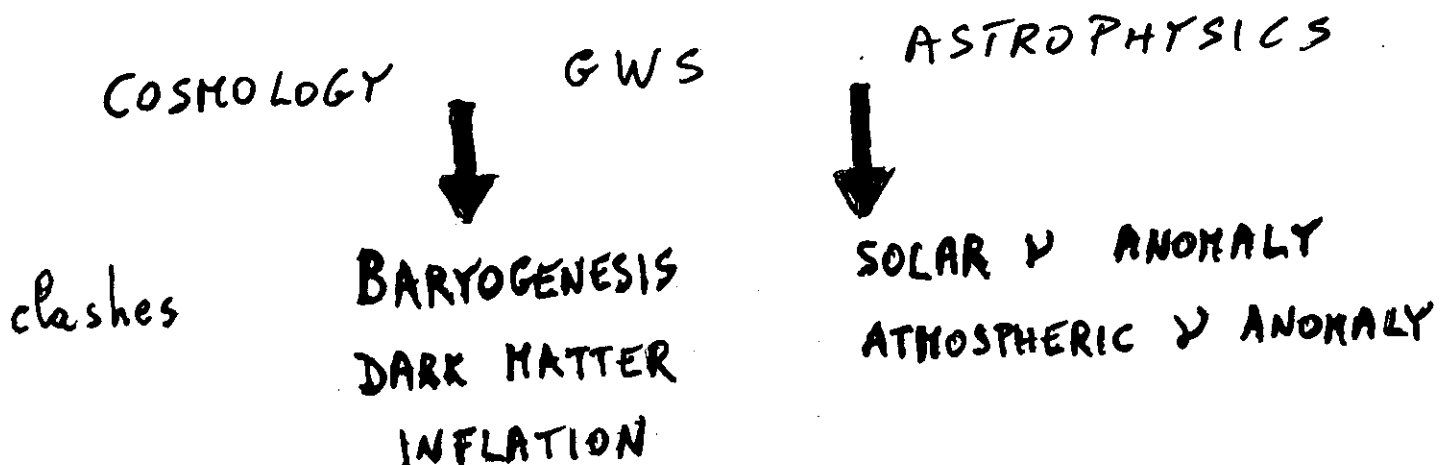
OF PHYSICS BEYOND THE SM



MANY EXAMPLES OF MUTUAL SUPPORT

(ex. # neutrino species from nucleosynthesis and LEP)

BUT ALSO CLASHES POINTING (hopefully)
TO NEW PHYSICS BEYOND THE GWS SM



BARYOGENESIS

- No evidence of antimatter within the solar system
- $\bar{p}$'s in cosmic rays $\rightarrow$ in agreement with production as secondaries in collisions
- if in cluster of galaxies certain galaxies were of matter and others of antimatter $\Rightarrow$ the γ flux produced by $p\bar{p}$ annihilations in the cluster would exceed the observed γ flux
- if $n_b = n_{\bar{b}}$ and they are not separated well before they decouple we would be left with $(n_b - n_{\bar{b}})/n_\gamma$ several orders of magnitude smaller than $n_b/n_\gamma \sim 10^{-10}$
- if b and $\bar{b}$ are separated earlier $\rightarrow$ domains of b and $\bar{b}$ are too small today to explain separations larger than the supercluster size

$\rightarrow$ ONLY MATTER IS PRESENT

$\rightarrow$ HOW TO PRODUCE DYNAMICALLY A Baryon-Antibaryon ASYMM. STARTING FROM A SYMMETRIC SITUATION

SACKAROV'S
CONDITIONS FOR
BARYOGENESIS

$B \neq$ INTERACTIONS
 $C, CP \neq$ INTERACTIONS
OUT OF EQUILIBRIUM

in SM :

$B \neq \rightarrow$ although B number is
conserved at any order
in perturbation theory
NON-PERTURB. QUANTUM EFFECTS
VIOLATE B

$CP \neq \rightarrow$ NOT ENOUGH to produce $n_B/n_\gamma \sim 10^{-11}$

out of equilibrium $\rightarrow$ NO 1st ORDER
PHASE TRANS.
demand⁺ that $\Delta B \rightarrow$ NOT ACHIEVED
which is produced
is no longer
erased
 m_H TOO LARGE

$\Rightarrow$ ALTHOUGH $B \neq$ INTERACTIONS OF THE SM
MAY ERASE A PREVIOUSLY GENERATED ΔB
THEY ARE **NOT** ABLE TO PRODUCE
A MATTER-ANTIMATTER ASYMMETRY

THE DM PROBLEM

$$\Omega = \rho/\rho_c \quad \rho_c = \frac{3H^2}{8\pi G_N} \approx 10^{-29} \text{ g/cm}^3; \quad H = h \text{ } 100 \text{ km/s Mpc}$$

$$0.4 < h < 0.9$$

$$\hookrightarrow '98 \quad h = 0.65 \pm 0.15$$

* $\boxed{\Omega \geq 0.1}$ galactic rotation curves

* $\boxed{\Omega \geq 0.3 - 0.4}$ clusters and superclusters

* $\boxed{\Omega_{\text{LUMINOUS}} < 0.01}$ total luminous mass density

* $0.01 \leq \Omega_{\text{baryons}} h^2 \leq 0.015$

from nucleosynthesis

↓

$$\boxed{0.01 < \Omega_{\text{baryons}} < 0.1}$$

↙
 $\exists$ baryonic DM
 (Machos...)

↘
 $\exists$ NON-BARYONIC DM

* $\boxed{\Omega = 1}$ favoured by $\left\{ \begin{array}{l} \text{INFLATION} \\ \text{"NATURALNESS" arguments} \end{array} \right. + \text{CMB data}$

* $\boxed{\Omega h^2 \leq 1}$ ($\tau_{\text{univ}} > 10^{10} \text{ yrs.}$)

$$\Omega_{\text{THEORISTS}} = 1 \quad !$$

$$\left(\frac{\dot{R}}{R}\right)^2 \equiv H^2 = \frac{8\pi G_N}{3} \rho - \frac{k}{R^2}$$

$$\Omega \equiv \rho/\rho_c \quad H^2 = \frac{8\pi G_N}{3} \rho_c$$

$$\Omega(t) = \frac{1}{1 - \frac{k/R^2}{\frac{8\pi G_N}{3} \rho}}$$

$\rho \propto R^{-4}$ radiation-dominated Univ.

$\rho \propto R^{-3}$ matter - " "

to have $\Omega = O(1)$ today one must impose

$$|\Omega - 1| < 10^{-60} \text{ at } t_{\text{reanch}} \sim 10^{-43} \text{ s.}$$

IF INFLATION IS PRESENT $\Rightarrow \Omega \approx 1$ predicted
 during inflation $H = \text{const} \Rightarrow R = R_0 e^{Ht}$ (in a "natural way")
 k/R^2 negligible $\Rightarrow \Omega \approx 1$

$$\Omega_0 = \Omega_M + \Omega?$$

BEST DETERMINATION
FROM ANISOTROPY OF
CBR

0.4 ± 0.1
(baryon fraction
method.)

at last scattering Baryons coupled to γ : B fall into DM
potential wells $\rightarrow \gamma$ pressure acts as a restoring force

$\rightarrow$ gravity-driven acoustic oscillations

$\rightarrow$ Fourier modes with $k \sim \ell \frac{H_0}{2}$

$\rightarrow$ SERIES OF ACOUSTIC PEAKS STARTING AT $\ell \sim 200$

POSITION OF THE FIRST PEAK $\ell \approx \frac{200}{\sqrt{\Omega_0}}$

↓

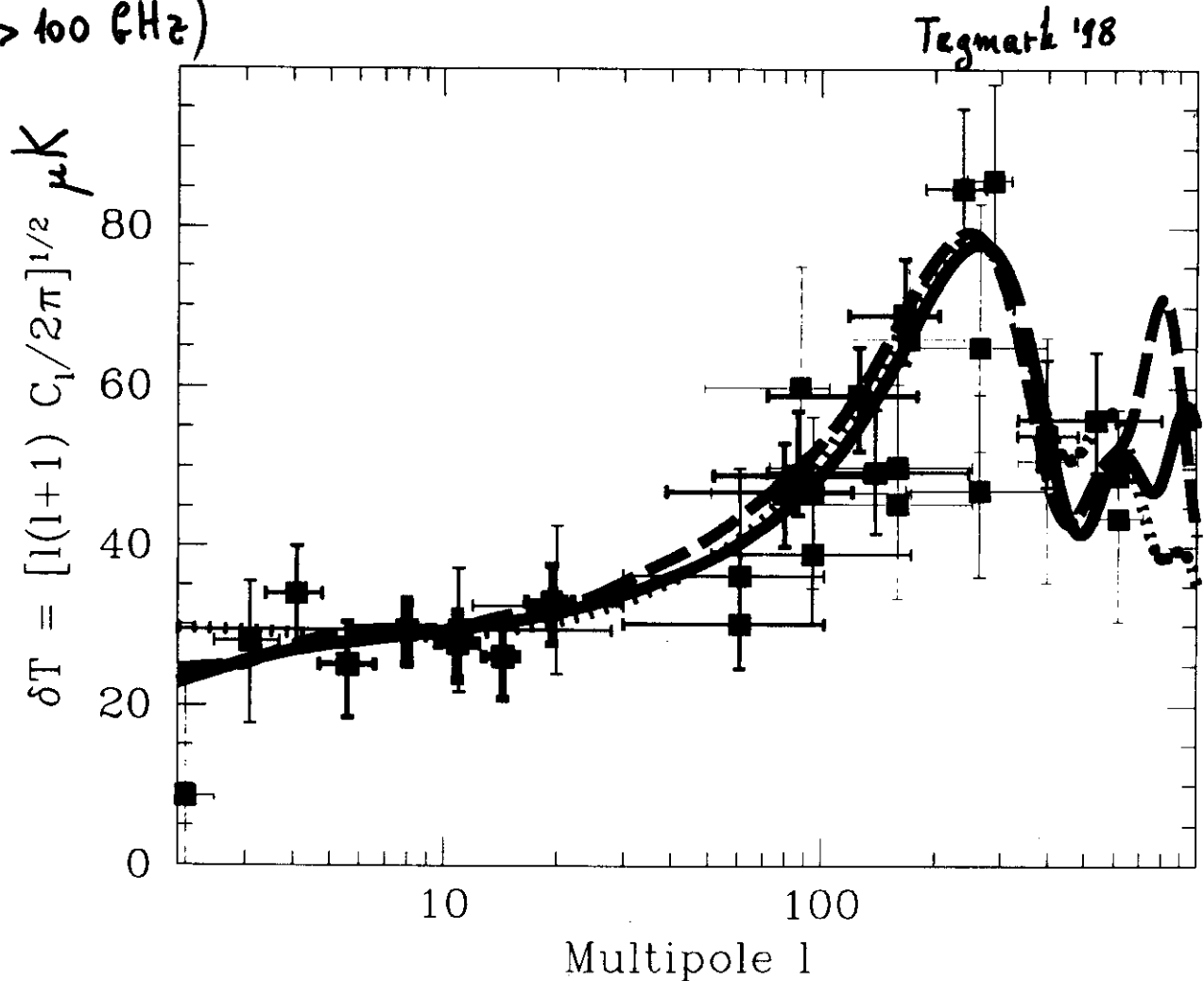
$$\text{CBR} \rightarrow \Omega_0 = 1 \pm 0.2$$

Lineweaver (198)

$\rightarrow$ pre-Boor

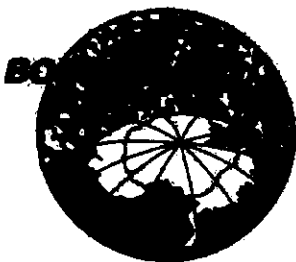
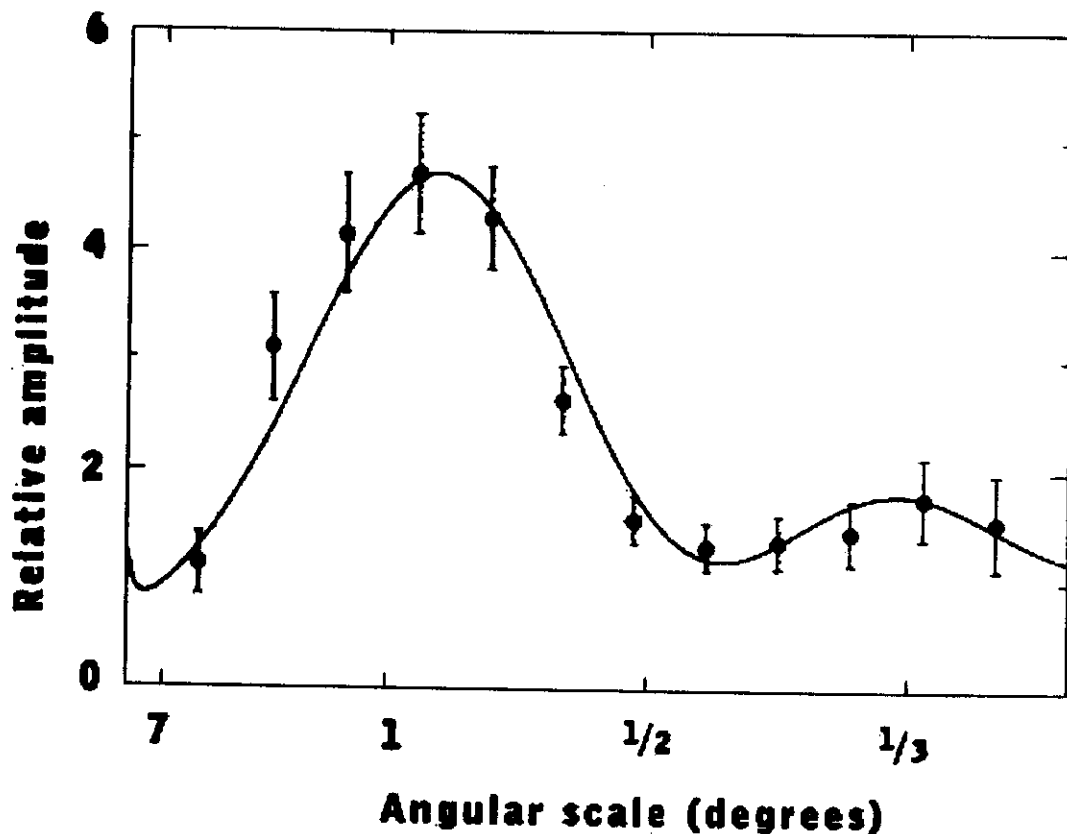
position of the 1st peak is insensitive to the
composition of Ω_M and Ω_b , only to their sum $\odot$

COBE MOST PRECISE COVERS MULTIPOLE $l \sim 2-20$
 OTHER MEASUREMENTS FROM BALLOON-BORNE,
 ANTARCTICA-BASED, GROUND-BASED EXPTS.
 USING LOW-FREQUENCY ($f < 100$ GHz) and HIGH-FREQUENCY
 ($f > 100$ GHz)



SATELLITES { MAP (NASA) late 2000
 PLANCK (ESA) 2007

resolution ~ 30 times better than COBE ($\sim 0.1^\circ$)
 map entire CBR sky
 (2)



The Spectrum of Primordial Sound. The temperature variations in early universe seen in the BOOMERANG images are due to sound waves in the primordial plasma. The angular spectrum of these images shown here, reveals the characteristic size of the structures that dominate the image. A peak in this spectrum at scales of ~ 1 degree, as is seen here in the BOOMERANG data, indicates that the Universe is nearly spatially flat. The data can be well fit by cosmological models that contain non-baryonic matter in addition to normal, baryonic matter. One such model is indicated by the solid blue curve. A generic feature of such models is the presence of a harmonic series of additional peaks beyond the fundamental peak at ~ 1 degree. The relative height of the second peak at $\sim 1/2$ degree on the sky varies with the balance of matter in the Universe contained in normal or baryonic matter and non-baryonic matter.

$$l_{\text{peak}} = (197 \pm 6) \quad (1\sigma \text{ error})$$

FROM OBSERVATIONS

$$\Omega_M \sim 0.4$$

$$\Omega_0 = \Omega_M + \Omega_\Lambda \approx 1$$

$\exists$ of DARK, EXOTIC FORM OF ENERGY SMOOTHLY DISTRIBUTED (UNCLUSTERED)

$$\Omega_\Lambda \neq 0 \text{ with } \Omega_\Lambda \sim 0.6$$

IS IT POSSIBLE TO TEST IT ?

→ main signature :

ACCELERATING (instead of de-accelerating) UNIVERSE

try to measure q_0

$$R_{\text{curv}}^2 = \frac{H_0^{-2}}{\Omega_0 - 1}$$

$$q_0 \equiv -\frac{(\ddot{R}/R)_0}{H_0^2} = \frac{1}{2}\Omega_0 + \frac{3}{2}\Omega_i w_i$$

(21) $P_i = w_i \rho_i$ ($w_i = 0$ baryons; $w_i = -1$ cosm. cons; $w_i = 1/3$ rad)

Einstein eq. for an isotropic and homogeneous Universe

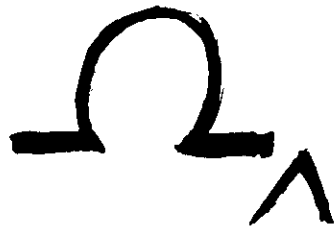


$$H^2 = \left(\frac{\dot{R}}{R} \right)^2 = \frac{8\pi G_N}{3} - \frac{k}{R^2}$$

expansion rate $\swarrow$ $\searrow$ cosmic scale factor $\nearrow$ signature of the 3-curvature

$$\frac{\ddot{R}}{R} = -\frac{4\pi G}{3} (\rho_{\text{matter}} - 2\rho_{\Lambda})$$


$\rightarrow$ for $\rho_{\Lambda} > \frac{1}{2} \rho_{\text{matter}}$ the expansion of the Universe ACCELERATES!



TO AVOID INTERFERING WITH STRUCTURE FORMATION
(UNIVERSE MUST HAVE BEEN MATTER DOMINATED FROM
THE EPOCH OF MATTER-RADIATION EQUALITY UNTIL VERY
RECENTLY) $\Rightarrow$ Λ form of energy must be
less important in the past than it is today

eq. of state: $p_\Lambda = w_\Lambda \rho_\Lambda \Rightarrow \rho_\Lambda \propto R^{-n}$
 $n = 3(1 + w_\Lambda)$
 $\searrow$ UNIV. SCALE FACTOR

to be less important in the past $\Rightarrow n < 3$, i.e. $w_n < 0$

ex.: cosmological const. $w_\Lambda = -1$

bonus: $H_0 \uparrow$ with $w \downarrow \Rightarrow$ older Univ. for a given h_0
(no "age crisis")

$$q_0 = \frac{1}{2} \Omega_{\text{M}} - \Omega_{\Lambda} \sim -0.4 \quad (\text{from obs. values of } \Omega_{\text{M}} \text{ and } \omega_0)$$

EVIDENCE FOR THIS "SMOKING GUN" FROM SNe Ia

MEASURING q_0

Expansion of the Universe is just a conformal scaling up of all distances:

$$v = H_0 d \quad (\text{Hubble law})$$

$\Rightarrow$ if the distances and velocities to distant galaxies were all measured at the present then they would obey $v = H_0 d$

but we see distant galaxies at an earlier time

and so $\left\{ \begin{array}{l} \Rightarrow \text{if the expansion is SLOWING their velocity} \\ \text{should be ABOVE the Hubble-law prediction} \\ \Rightarrow \text{if the expansion is SPEEDING UP their velocity} \\ \text{should fall BELOW the Hubble-law prediction} \end{array} \right.$

magnitude-redshift Hubble diagram
for ~ 50 SNe Ia out to z of nearly 1



this is what was found by the
two groups $\left\{ \begin{array}{l} \text{SUPERNOVA COSMOLOGY PROJECT} \\ \text{HIGH-Z SUPERNOVA SEARCH} \end{array} \right.$

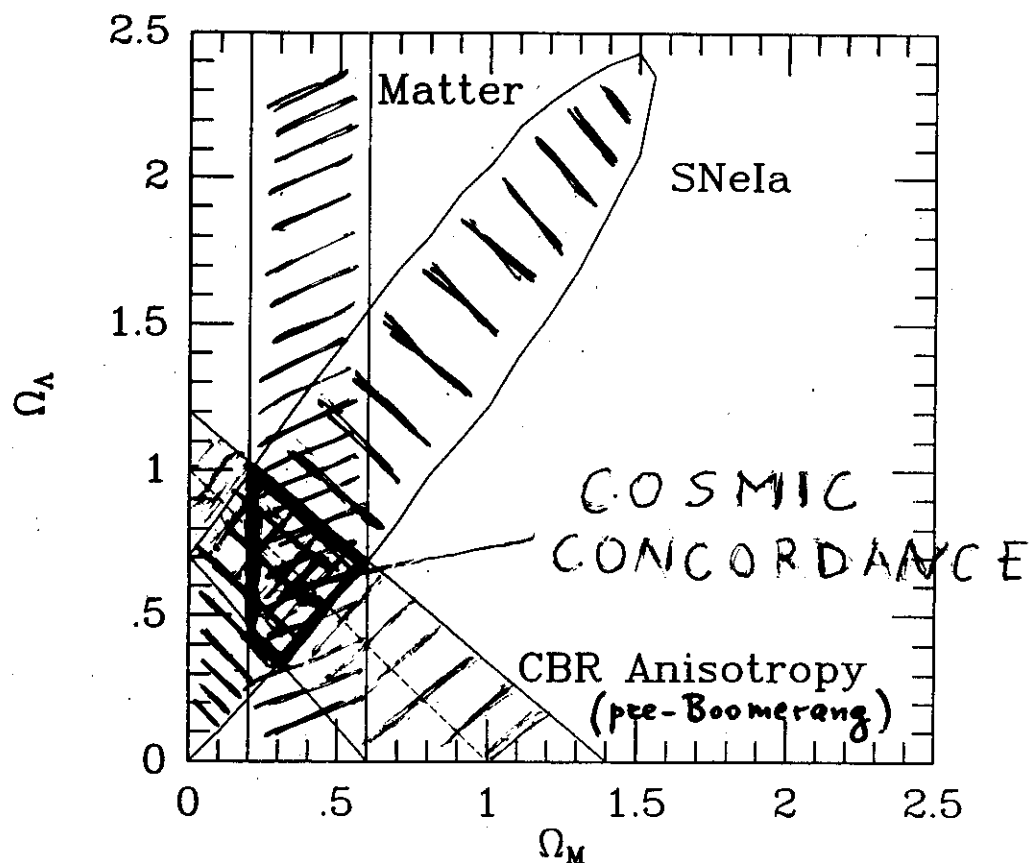
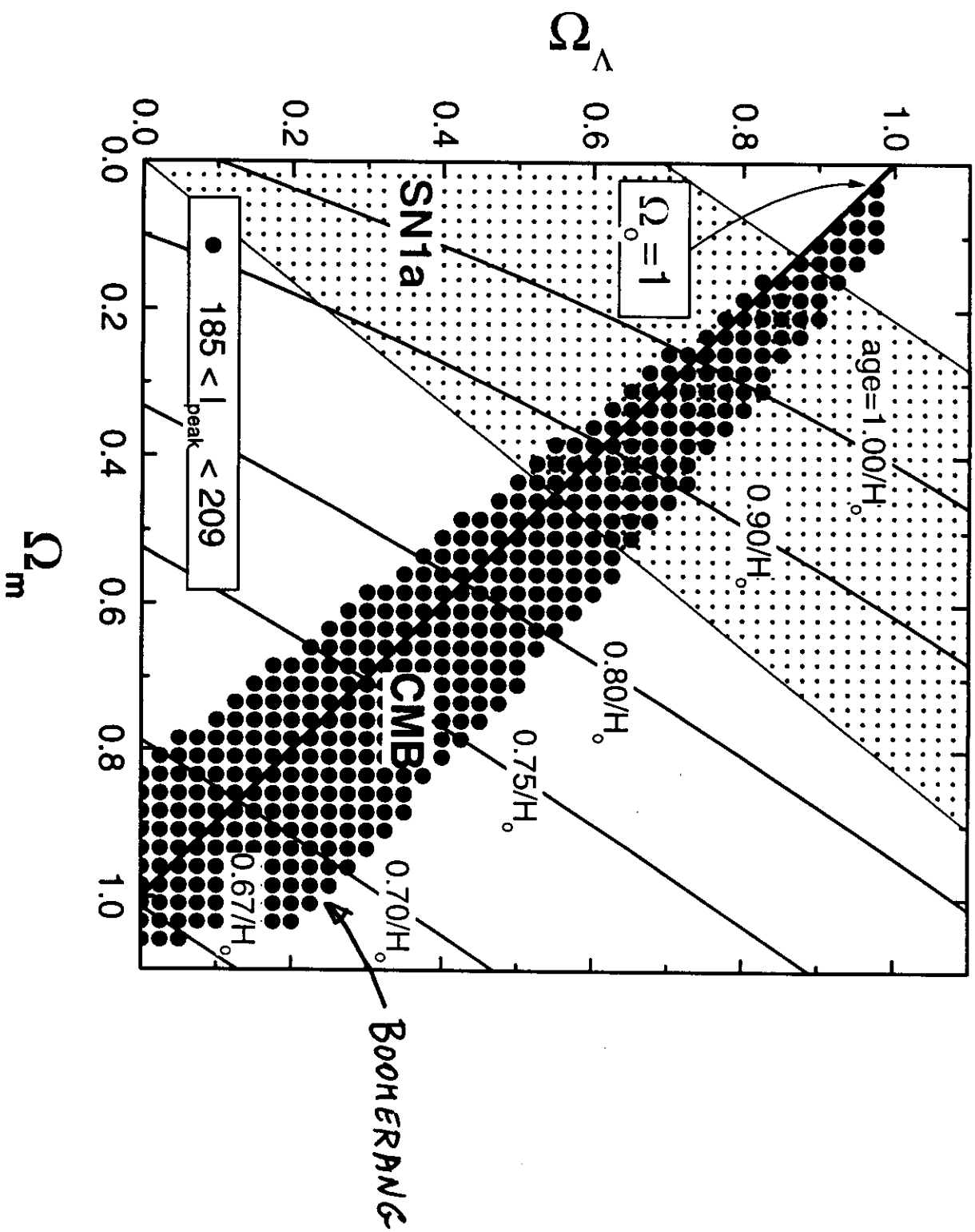


Figure 6. Constraints to Ω_M and Ω_Λ from CMB anisotropy, SNeIa, and measurements of clustered matter. Lines of constant Ω_0 are diagonal, with a flat Universe shown by the broken line. The concordance region is shown in bold: $\Omega_M \sim 1/3$, $\Omega_\Lambda \sim 2/3$, and $\Omega_0 \sim 1$. (Particle physicists who rotate the figure by 90° will recognize the similarity to the convergence of the gauge coupling constants.)

CONCORDANCE REGION

$$\Omega_M \approx \frac{1}{3} \quad \Omega_\Lambda \approx \frac{2}{3}$$



WHAT IS THE DM MADE OF ?

Ω
 $\swarrow$ Ω_{MATTER} at least 0.3
 $\searrow$ Ω_{Λ} Λ cosm. const.

SM : relies $\nearrow \Omega_{\gamma h^2 = 2.48 \times 10^{-5}$ with $w_{\gamma} = 0$ $\Omega_{\gamma} = \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} \Omega_{\gamma}$
 $\nwarrow \gamma, \nu, \text{ baryons}$ $\Omega_{\text{SM}} < 0.1$
 $\Omega_{\text{B}} < 0.1$



NON-BARYONIC DM CALLS FOR NEW PHYSICS BEYOND SM

DM RELIC PARTICLES

THERMAL $\swarrow$ NON-THERMAL
 (ex. axions)
 $\swarrow$ $\searrow$
 ex: $m_{\nu} \sim 10 \text{ eV}$ $T_{\text{decoupl}}^{\nu} \sim \text{MeV}$ **HOT** **COLD** ex: $m_{\chi^0} \sim 100 \text{ GeV}$
 $m \ll T_{\text{decoupl}}$ $m \gg T_{\text{decoupl}}$ $T_{\text{decoupl}}^{\chi^0} \sim 20 \text{ GeV}$
 relativistic at non relativistic when galaxies
 time structure formation starts start forming
 (24)

STANDARD MODEL AND DARK MATTER

SM: ONLY RELICS FROM THE EARLY UNIVERSE

$$\gamma \rightarrow \text{CBR} \quad T_\gamma \sim 2.7 \text{ K}$$

$$\nu \rightarrow \text{CB} \nu \quad \text{slightly less than} \\ m_\nu = 0 \quad \gamma \text{ CBR} - \text{a bit colder than } \gamma$$

$$\text{BARYONS} \rightarrow \Omega_B < 10\%$$

→ IN SM NO EXPLANATION FOR

$$\Omega_{NB} > 10\% \\ \Downarrow$$

NEED MASSIVE NON-BARYONIC DM

ex: new physics may provide a mass to neutrinos

→ ALSO IN SM NO SCALAR PARTICLE
GIVING RISE TO INFLATION

→ PROBLEM FOR THE BIRTH OF INITIAL $\delta\rho/\rho$ FLUCTUAT.

STRUCTURE FORMATION

DM

AMOUNT AND
NATURE OF
THE MATERIAL
IN THE UNIVERSE

$$\Omega_i = \rho_i / \rho_{crit}$$

COLD, HOT, WARM

SEED OF DENSITY
FLUCTUATIONS

INITIAL SPECTRUM
OF ρ FLUCTUATIONS

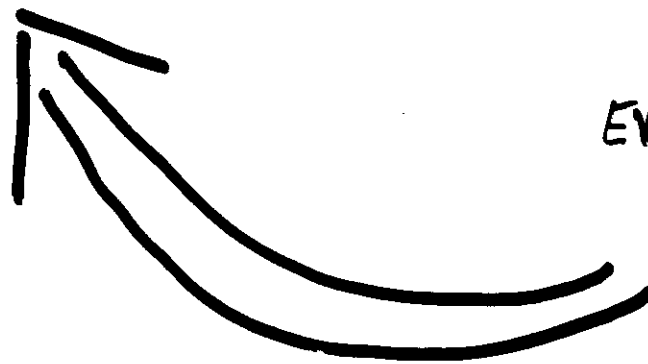


INFLATION OR
TOPOLOGICAL DEFEC

SCALE INVAR.
FLUCTUATION
SPECTRUM



EVOLUTION
UNDER GRAVITY



EXP. INPUT: COBE, GALAXY DISTRIBUTIONS, PECULIAR VELOC.

TH. INPUT: GROWTH OF $\delta\rho/\rho$ (dependence on the nature of DM)

THEORETICAL REAPPRAISAL OF THE SM

a) intrinsic inconsistencies

ex: Fermi theory

→ four-fermion contact interaction

~~X~~ $\sigma \sim G^2 s \rightarrow$ violation of unitarity

~~X~~ uncontrollable explosion of ultraviolet divergence
(non-renormalizability)

⇒ WE ARE NOT FORCED TO GO BEYOND THE SM
BY THIS KIND OF INCONSISTENCIES

b) Questions that we think a fundamental theory should answer, but which do not find any satisfactory answer in the SM

• NO TRUE UNIFICATION

$(G_F, e \leftrightarrow g_1, g_2 ; \quad g_1, g_2, g_3 ;$

classically no explanation for charge quantization (why $|Q_d| = |Q_e|/3$?)

⑦ → ANOM. CANCELL. (including gauge-grav. anom.) charge quantization

- gravity absent
- apart from g_1, g_2, g_3

⇒ LARGE NUMBER OF FREE PARAMETERS

Fermion spectrum { why and how many fermion families
fermion masses
within the same generation
(m_t/m_b ?) or between two
different generations (m_μ/m_e ?)

Fermion mixing ⇒ parameters of the
CKM matrix

Arbitrariness in the scalar (higgs) sector { how many and in which representations
 μ, λ param. in the scalar potential

c) FINE-TUNINGS ⇒ look at the SM as a low-en. effective theory ⇒

OUT OF THE THREE CLASSES OF
THEORETICAL ARGUMENTS

PUSHING US BEYOND THE SM

- FLAVOUR PROBLEM
(fermion masses and mixings)
- UNIFICATION OF FUNDAMENTAL INTER.
(including gravity)
- GAUGE HIERARCHY PROBLEM

ONLY THE HIERARCHY ISSUE
CALLS FOR NEW PHYSICS
AT A SCALE CLOSE TO
THE ELW. SCALE

1. THE STANDARD MODEL : A CRITICAL REAPPRAISAL



- SPONT. BROKEN GAUGE THEORY
↓
RENORMALIZABILITY
- EXTRAORDINARY EXPER. SUCCESS

- "UNIFICATION" OF ELM. + WEAK

- GH, FCNC SUPPRESSION
- $CP \neq$
- B and L automatic conservation at the perturbative level
- economy in the Higgs sector (1 doublet $\rightarrow$ M_u, M_d, m_e)



① - LACK OF "TRUE" UNIFICATION

- a) no Q quantization
- b) elm-weak $G_F, e \Rightarrow g, g'$
- c) g_s, g, g' far apart
- d) no gravity

② FLAVOUR PROBLEM

- a) # of families
- b) fermion masses
- c) ν mass
- d) CKM parameters

③ SCALAR PROBLEM

- a) arbitrariness in the scalar sector
- b) gauge hierarchy (G_F, M_{Pl})

HOW WEAK and STRONG CAN MERGE TOGETHER

RGE:

Georgi, Quinn, Weinberg

$$\frac{d\alpha_i}{d\ln q^2} = b_i \alpha_i^2 + O(\alpha_i^3)$$

$$b_i = -\frac{1}{4\pi} \left[\frac{11}{3} C_2(G_i) - \sum_f \frac{4}{3} T(R)_f + \text{scal. contrib.} \right]$$

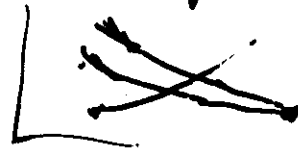
$C_2(G_i)$ = eigenvalue of the Casimir oper. of G_i

$$T(R) = \frac{d(R) C_2(R)}{r}$$

r # generators

$C_2(R)$ Casimir
for reps. R

$SL(N) : T(N) = \frac{1}{2}$



$$\begin{cases} b_3 = -(4\pi)^{-1} \left[\frac{11}{3} \times 3 - \frac{4}{3} n_{\text{gener}} \right] \\ b_2 = -(4\pi)^{-1} \left[\frac{11}{3} \times 2 - \frac{4}{3} n_{\text{gener}} \right] \\ b_1 = -(4\pi)^{-1} \left[0 - 20/9 n_{\text{gener}} \right] \end{cases}$$

3 equations

Inputs: α_{em}, α_3 (at low energy)

Unknowns: M_X scale at which $\alpha_1 = \alpha_2 = \alpha_3$
 α_G common value of $\alpha_1, \alpha_2, \alpha_3$ at M_X

$\sin^2 \theta_w$ (from α_1, α_2
 input α_{em}
 unknown $\sin^2 \theta$)

$\Rightarrow$ IT IS POSSIBLE TO

PREDICT a LOW EN.

(testable) fundamental
 quantity !

(exercise: solve the 3 eqs.)

$$M_X \sim 10^{15} \text{ GeV}$$

$$\sin^2 \theta_w \sim 0.2 \quad \uparrow \text{further de}$$

approximations:

1) RGE at 1 loop (today available at 2 loops)

2) **STEP APPROXIMATION** ~~mon~~
 (neglecting of threshold effects
 → important when q^2 approaches M_X)

→ **GUT SCENARIO** ~~mon~~

$E > M_X$	$E \sim M_X$	$M_W < E < M_X$	$E \sim M_W$
$G \rightarrow \underbrace{SU(3) \times SU(2) \times U(1)}_{3 \times 2 \times 1}$	$G \rightarrow 3 \times 2 \times 1$	$3 \times 2 \times 1$	$3 \times 2 \times 1$ ↓ $3 \times 1 \times 1$

GENERAL CONSEQUENCES OF A GUT SCHEME

- * Q QUANTIZATION (Q generator of G)
- * PREDICTION OF $\sin^2 \theta_w$
- * POSSIBLE FERMION MASS RELATIONS
(f in a repres. of G)
- * POSSIBLE B and L NON CONSERVATION
(q and l in the same repres. of G)
- * LARGE VALUE OF M_X
 $M_X \sim 10^{15} \text{ GeV}$
 $\rightarrow \text{dim } 6 \Rightarrow \text{CLOSE TO EXP. LIMIT}$
operators responsible for proton decay

$$\sin^2 \theta_w$$

$$e = g \sin \theta_w \Rightarrow \sin^2 \theta_w = \frac{e^2}{g^2}$$

correctly normalized Q : $\hat{Q}$

$$\text{Tr } \hat{Q}^2 = \text{Tr } \hat{T}_3^2 \quad \text{Tr } \hat{T}_3^2 / 5 = 1/2$$

$$Q \rightarrow \begin{pmatrix} 1/3 & 1/3 & 1/3 \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \end{pmatrix} \quad \text{Tr } Q^2 = 4/3 \quad \hat{Q} = \sqrt{\frac{3}{8}} Q$$

$$\hat{T}_3 = T \rightarrow \hat{g}_2 = g_2$$

$$\hat{e} \hat{Q} = e Q \Rightarrow \hat{e} = \sqrt{\frac{8}{3}} e$$

$$\sin^2 \theta_w = \frac{e^2}{g^2} = \frac{3}{8} \frac{\hat{e}^2}{\hat{g}_2^2} = \frac{3}{8} \text{ at } M_U \text{ where } \hat{e} = \hat{g}_2 = g_m$$

$\sin^2 \theta_w$ is running $\Rightarrow$ renormalization of $\sin^2 \theta_w$ from M_U to M_w

$$\Rightarrow \sin^2 \theta_w^{\text{th}}(M_2) = 0.214^{+0.004}_{-0.003}$$

problem for GUT's

$$\Rightarrow \sin^2 \theta_w^{\text{exp}} = 0.23155 \pm 0.00019$$

+ proton decay problem in minimal (SU(5)) GUT
 $\tau_{\text{SU(5)}}^p \lesssim 10^{32} \text{ yrs}$ $\tau_{\text{exp}}^p > 10^{33} \text{ yrs}$

Courtesy of prof. Nishikawa

Summary of Nucleon Decay Searches

mode	exposure (kt·yr)	ϵB_m (%) ^m	observed event	B.G.	τ/B limit (10 ³² yrs)
$p \rightarrow e^+ + \pi^0$	52	44	0	0.2	33
$p \rightarrow \mu^+ + \pi^0$	52	35	0	0.1	27
$p \rightarrow e^+ + \eta$	45	17	0	0.3	11
$p \rightarrow \mu^+ + \eta$	45	12	0	0	7.8
$n \rightarrow \bar{\nu} + \eta$	45	21	5	9	5.6
$p \rightarrow \bar{\nu} + K^+$	33				7.3
$K^+ \rightarrow \nu \mu^+$ (spectrum)		40	—	—	3.3
prompt $\gamma + \mu^+$		4.4	0	0.4	2.1
$K^+ \rightarrow \pi^+ \pi^0$		6.5	0	0.7	3.1
$n \rightarrow \bar{\nu} + K^0$	52				1.8
$K^0 \rightarrow \pi^0 \pi^0$					
2-ring		3.2	9	8.0	0.64
3-ring		4.9	9	9.5	1.1
4-ring		1.7	1	3.3	0.84
$K^0 \rightarrow \pi^+ \pi^-$		4.1	4	1.6	0.89
$p \rightarrow e^+ + K^0$	52	10.9	1	1.53	6.1
$p \rightarrow \mu^+ + K^0$	52				10
$K^0 \rightarrow \pi^0 \pi^0$		6.1	0	0.7	4.6
$K^0 \rightarrow \pi^+ \pi^-$					
2-ring		5.0	0	1.8	3.8
3-ring		3.1	0	0.4	2.4

SEEKING PHYSICS BEYOND THE SM

SM $\rightarrow$ EFFECTIVE FIELD THEORY
VALID UP TO THE CUTOFF
SCALE Λ

SM field content: ϕ ψ $F_{\mu\nu}$
scalar fermion gauge fields

$B, L (L_e, L_\mu, L_\tau)$
automatically
conserved

No TREE LEVEL
FCNC, GIM
suppression

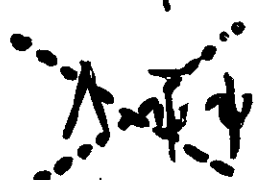
RENO. OPERATORS

NON-RENO. OPER.

$B, L \neq$
GIM NOT EFFECTIVE

Λ^4

$\Lambda^2 \phi^2$



$(\bar{\psi} \psi)^2, \bar{\psi} \psi \phi^2, \phi^4$

$\bar{\psi} \psi \phi \phi$

$\bar{\psi} \psi \psi \psi$

$\phi^6 / \Lambda^2 \dots$

dim 0 $\rightarrow$ cosm. const.

dim 2 $\rightarrow$ scalar mass

dim 3 $\rightarrow$ fermion mass
(forbidden by
chirality)

dim 4 $\rightarrow$ only by dependence
on Λ

dim 5, 6, ...
 $\rightarrow$ expansion
in Λ^{-n}

$\Lambda \gg \text{FERMI SCALE}$



SUPPRESSION OF
OPER. OF DIM > 4

$B \neq, L \neq, FCNC$ UNDER
CONTROL

PROBLEM: $a \Lambda^2 \phi^2$

need a extremely tiny

GAUGE HIERARCHY PROBLEM

$m_{\text{HIGGS}} > 130 \text{ GeV}$

→ SCALARS TEND TO GET
THE LARGEST AVAILABLE
MASS SCALE IN THE THEORY

$\Lambda \sim \text{FERMI SCALE}$



NO PROBLEM
WITH

$a \Lambda^2 \phi^2$
↳ of $O(1)$

PROBLEM:

POTENTIALLY
LARGE

$B \neq, L \neq, FCNC$



CANDIDATE
MSSM

$m_{\text{HIGGS}} < 130 \text{ GeV}$

WHAT IF $\Lambda \gg M_W$?

GOOD POINT: ALL NON-RENDORM. OPER.

(creating troubles for p -decay,
FCNC, ...) ARE LARGELY SUPPRESSED
BY Λ^{-n}

BAD POINT (HIERARCHY PROBLEM)

$$m_H^2 \Rightarrow \Lambda^2 \gg v^2$$

$\hookrightarrow$ VEV which breaks $SU(2) \times U(1)$

but from $V = +\mu^2 \varphi \varphi^\dagger + \lambda (\varphi \varphi^\dagger)^2$

$$\Rightarrow v = \sqrt{-\frac{\mu^2}{2\lambda}} \quad m_{H_0}^2 \Rightarrow \lambda v^2$$

$$m_H^2 \sim \underbrace{\lambda v^2}_{\sim \Lambda^2} + \sum_i a_i \Lambda^2 \quad \sum_i a_i \sim \frac{v^2}{\Lambda^2}$$

FINE TUNING

NEED AN INCREDIBLE CONSPIRACY
OF LOW- AND HIGH-ENERGY PHYSICS

HOW TO DEAL WITH THE SCALAR MASS PROBLEM

GET RID OF THEM

FORCE THEM TO RESPECT $m_H^2 \sim G_F^{-1}$

CONSTRUCTION OF
GAUGE THEORIES
WITHOUT (ELEMENTARY)
SCALARS



ex. $SU(2)_L \times U(1)$ without ϕ
 $\langle \bar{U}_L U_R \rangle \langle \bar{d}_L d_R \rangle \neq 0$
 break $SU(2) \times U(1)$
 scale $\sim f_\pi$ $\begin{cases} M_W \sim f_\pi \\ \pi \text{ eaten up by } W \end{cases}$



try scaled up version
of QCD with
 $\langle \bar{U}_L U_R \rangle \Rightarrow f_\pi \sim 10^3 f_\pi$

"INDUCED"
PROTECTION
ON SCALAR MASSES

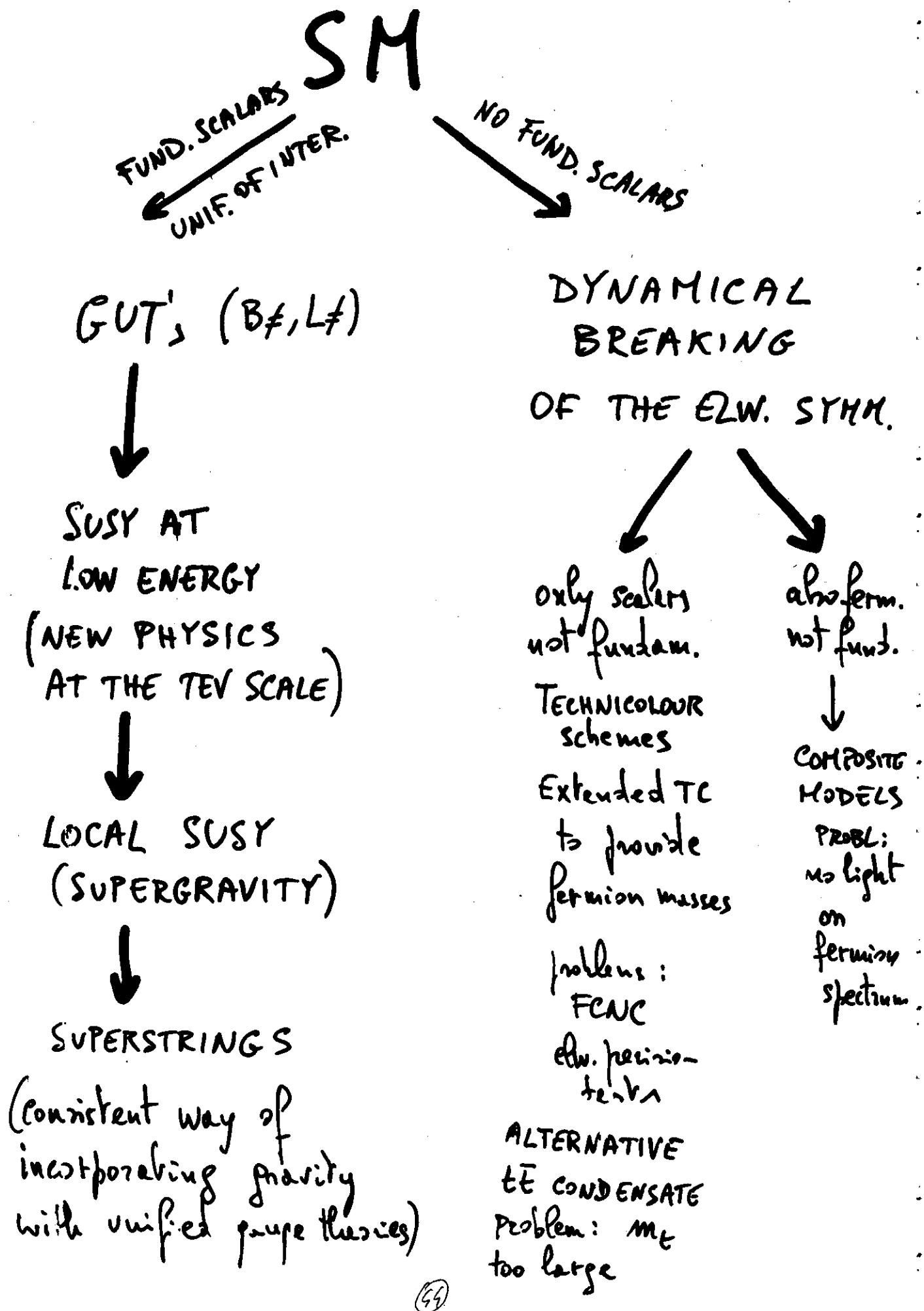


m_ϕ^2 not protected

m_ψ protected



put $\begin{pmatrix} \phi \\ \psi \end{pmatrix}$ in a
multiplet of a symm.
as long as this
symm. is unbroken
 $m_\phi = m_\psi$
 $\Rightarrow$ if this symm.
broken $\sim M_W$
 $m_\phi - m_\psi \leq O(M_W)$

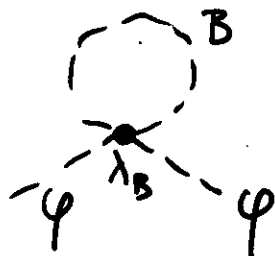
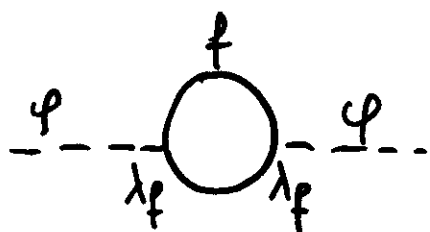


• HIERARCHY PROBLEM

$\Rightarrow$ SUSY HAS TO BE BROKEN

AT A SCALE CLOSE
TO 1 TeV

$m_\varphi^2 \propto \Lambda^2 \rightarrow$ scale of susy breaking



$$\delta m_\varphi^2 \sim \frac{\lambda_B - \lambda_f^2}{16\pi^2} \Lambda^2$$

$$\Rightarrow |m_B^2 - m_f^2|^{1/2} \sim \frac{1}{\sqrt{G_F}}$$

$\begin{pmatrix} B \\ F \end{pmatrix}$ in SUSY multiplet

2. WHAT IS SUSY

84

The simplest graded Lie algebra which is a symmetry of an S -matrix consistent with a relativistic quantum field theory involves the generators of the Poincaré group (even part of the algebra) as well as two anticommuting spinor generators of supersymmetry

$$[P^m, P^n] = 0$$

$$\boxed{\{Q^\alpha, \bar{Q}_{\dot{\alpha}}\} = 2 \sigma^\mu_{\alpha\dot{\alpha}} P_\mu} \quad \leftarrow$$

$$\{Q_\alpha, Q_\beta\} = \{\bar{Q}_{\dot{\alpha}}, \bar{Q}_{\dot{\beta}}\} = 0$$

$$[Q_\alpha, P^m] = [\bar{Q}_{\dot{\alpha}}, P^m] = 0$$

$$[M^{mn}, P^q] = -i (P^m \eta^{nq} - P^n \eta^{mq})$$

$$[M^{mn}, M^{qr}] = i (\eta^{mq} M^{nr} - \eta^{mr} M^{nq} + \eta^{nr} M^{mq} - \eta^{nq} M^{mr})$$

$$\boxed{[M^{mn}, Q_\alpha] = -i \sigma^{mn \beta}_\alpha Q_\beta} \quad \leftarrow Q \text{ rotates as a spinor}$$

$$[M^{mn}, \bar{Q}^{\dot{\alpha}}] = -i \bar{\sigma}^{mn \dot{\alpha}}_{\dot{\beta}} \bar{Q}^{\dot{\beta}}$$

$$\sigma^{mn \beta}_\alpha = \frac{1}{4} [\sigma^m_{\alpha\dot{\alpha}} \bar{\sigma}^{n\dot{\alpha}\beta} - \sigma^n_{\alpha\dot{\alpha}} \bar{\sigma}^{m\dot{\alpha}\beta}]$$

$$\bar{\sigma}^{mn \dot{\alpha}}_{\dot{\beta}} = \frac{1}{4} [\bar{\sigma}^{m\dot{\alpha}\alpha} \sigma^n_{\alpha\beta} - \bar{\sigma}^{n\dot{\alpha}\alpha} \sigma^m_{\alpha\beta}]$$

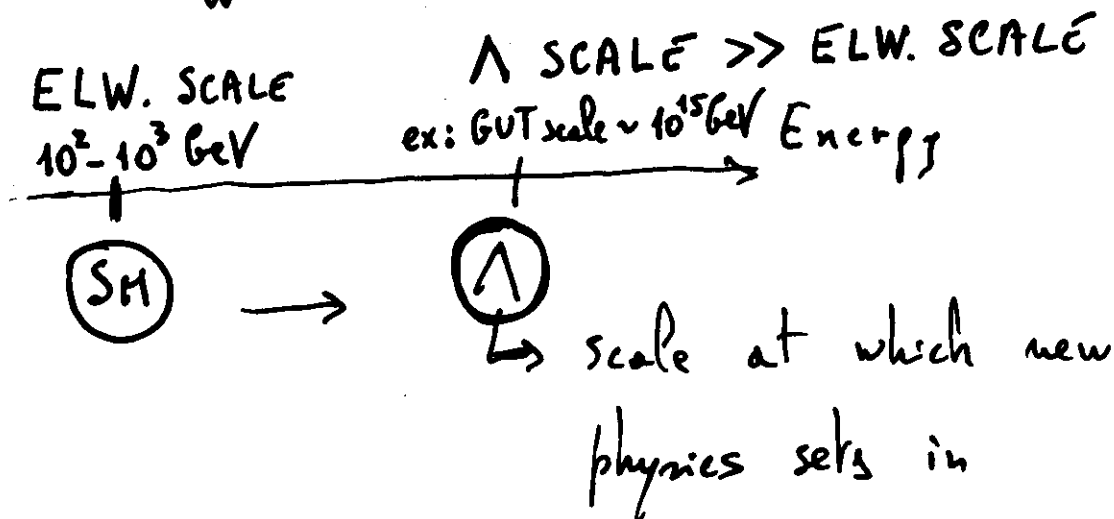
spinor representation of generators of the Lorentz group).

$Q_\alpha, \bar{Q}^{\dot{\alpha}}$ are generators of SUSY transf. and form the grading representation of the Poincaré algebra.

SUSY EXTENSION OF THE SM

$$V = -\mu^2 H^2 + \lambda H^4$$

$\mu \rightarrow M_W$



$\Rightarrow \Lambda^2 H^2$ no symm. protection

fermion masses
gauge boson masses

ELW. SYMM. BREAKING

m_f, m_W CANNOT JUMP TO Λ

$H \leftrightarrow \psi \rightarrow$ mass protected
SUSY

new symm.:
changing the spin of particles in its reps.

SUSY: good symm. down to the elw. scale

LOW ENERGY SUSY $\Rightarrow m_{\text{s-particles}} \leq O(1 \text{ TeV})$

THE SUPERSYMMETRIC STANDARD MODEL

Particle content

VECTOR	MULTIPLETS
$J=1$ g (gluon)	$J=1/2$ $\tilde{g}$ (gluinos)
$W^\pm, W^3$	$\tilde{W}^\pm, \tilde{W}^3$ (winos)
B	$\tilde{B}$ (bino)

CHIRAL	MULTIPLETS
$J=1/2$ q_L, q_R (quarks)	$J=0$ $\tilde{q}_L, \tilde{q}_R$ (squarks)
l_L, l_R (leptons)	$\tilde{l}_L, \tilde{l}_R$ (sleptons)
$\tilde{H}_1, \tilde{H}_2$	H_1, H_2 (higgses) ↳ 2 higgs doublets

BARYON AND LEPTON NUMBER IN SM and SUSY

SM $\Rightarrow$ B and L are AUTOMATIC SYMMETRIES: it is IMPOSSIBLE to write a renormalizable ($\dim \leq 4$) operator invariant under $SU(3) \times SU(2) \times U(1)$ which violates B or L

SUSY $\Rightarrow$ B and L are **NOT** AUTOMATIC SYMMETRIES

$$W \supset \lambda'' u^c d^c d^c \Big|_{\alpha\beta} \Rightarrow B \neq 0$$

$$\lambda L L e^c \Big|_{\alpha\beta} \Rightarrow L \neq 0$$

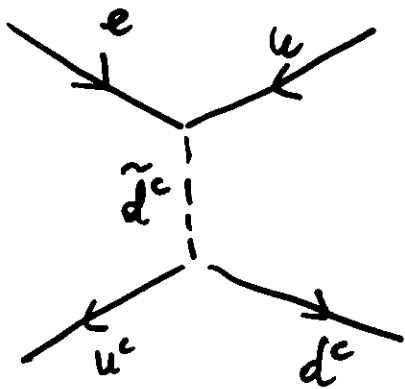
$$\lambda' L Q d^c \Big|_{\alpha\beta} \Rightarrow L \neq 0$$

dim 4 operators violating either B or L

if both λ'' and λ (or λ') terms
are present p -decay is very fast

ex.: $L Q d^c /_{\theta\theta} \Rightarrow e u \tilde{d}^c$

$$u^c d^c d^c /_{\theta\theta} \Rightarrow u^c d^c \tilde{d}^c$$

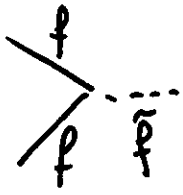


$$p \rightarrow e^+ + X$$

$$m_{\tilde{d}^c} \leq O(1 \text{ TeV})$$

$\Rightarrow$ NEED TO IMPOSE AN
ADDITIONAL SYMMETRY
TO FORBID EITHER $B \neq$
OR $L \neq$ OPERATORS IN W
OR ALL B and $L \neq$ OPERATORS

R PARITY



all $\lambda, \lambda', \lambda''$ dangerous
vertices involve two (ordinary) fermions
and one (supersymmetric) fermion

impose a multiplicative discrete symm.

such that $R(\text{ordinary particles}) = 1$

and $R(\text{susy particles}) = -1$

$\Rightarrow$ forbidden

Gauge $\otimes$ $N=1$ susy $\otimes$ R parity $\rightarrow$ W conserves
B AND L

R PARITY $\rightarrow$ {
- superparticles can be produced
or annihilated only in pairs
- the lightest susy particle (LSP)
IS ABSOLUTELY STABLE
(52)

IMPLICATIONS OF R-PARITY



SUSY PARTICLES CAN BE
CREATED OR DESTROYED
ONLY IN PAIRS

THE LIGHTEST
SUSY PARTICLE (LSP)
IS ABSOLUTELY
STABLE
(relic candidate)

