

the  
**abdus salam**  
international centre for theoretical physics

SMR/1270-29

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## **SCHOOL ON SYNCHROTRON RADIATION**

**6 November – 8 December 2000**

*Miramare - Trieste, Italy*

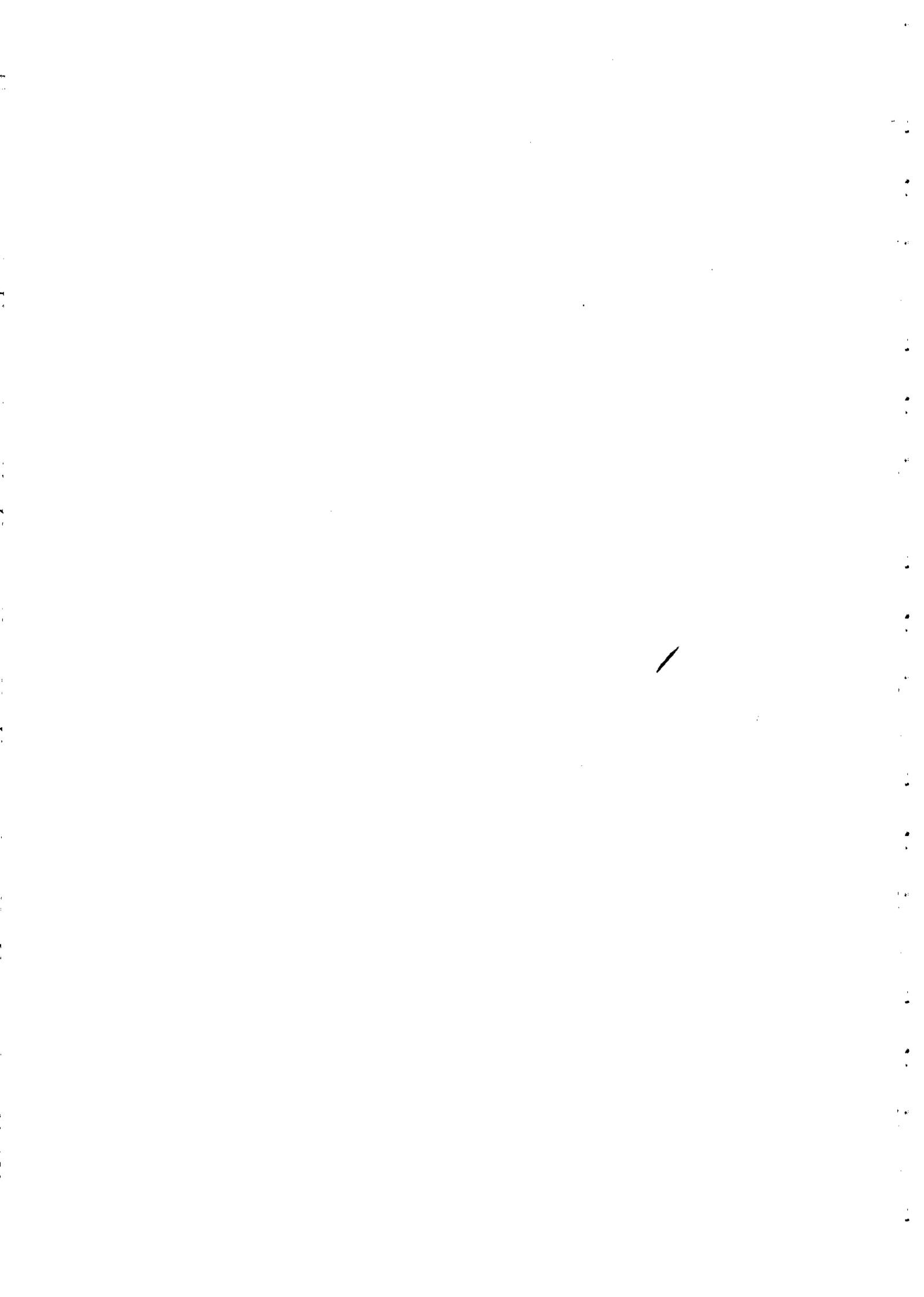
*Supported in part by the Italian Ministry of Foreign Affairs  
in connection with the SESEME project*

*Co-sponsors: Sincrotrone Trieste,  
Società Italiana di Luce di Sincrotrone (SILS)  
and the Arab Fund for Economic and Social Development*

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*Angle-Resolved Photoemission from One- and  
Two-Dimensional Systems - Surface States*

Juerg Osterwalder  
Universitaet Zuerich-Irchel  
Zurich, Switzerland



Lecture at the School on Synchrotron Radiation, ICTP Trieste, Nov. 29-Dec. 4 2000

## Photoemission from Valence Bands Fermi Surface Mapping

Jürg Osterwalder, Physik-Institut, Universität Zürich  
Winterthurerstr. 190, CH-8057 Zürich, Switzerland – [osterwal@physik.unizh.ch](mailto:osterwal@physik.unizh.ch)  
<http://www.physik.unizh.ch/groups/grouposterwalder/>

### Lecture 1

*Angle-Resolved Photoemission from One- and Two-Dimensional Systems – Surface states*

- 1) Electronic Bandstructure in 1-3 Dimensions
- 2) Photoemission from a Periodic Potential
- 3) The Three-Step Model
- 4) A 1D Example:  $p(2 \times 1)$  O – Cu(110) -> Band Mapping
- 5) A 2D Example: The Shockley Surface State on Cu(111)
- 6) A Few Words about Surface States in General
- 7) Surface States and Nanostructures

### Lecture 2

*Angle-Resolved Photoemission from Three-Dimensional Systems – Including Magnetism*

- 1) A Few Words about the Fermi Surface in General
- 2) Fermi Surface Mapping
- 3) Free Electron Final States
- 4) Mapping Final States in GaAs
- 5) Examples: Cu, Al
- 6) Itinerant Ferromagnetism: The Fermi Surface of Nickel

### Lecture 3

*Spin- and Angle-Resolved Photoemission / Manybody Effects*

- 1) Spin-Resolved Photoemission
- 2) A Complete Photoemission Experiment in the Construction Phase
- 3) Fermi Surfaces in Multilayers
- 4) Thickness-Dependent Fermi Surface in Co Films on Cu(111)
- 5) Manybody Effects in Solids: Theoretical Concepts – Spectral Functions
- 6) Example: Valence Photoemission in Nickel

#### **Lecture 4**

##### *Photoemission Intensities and Line Widths*

- 1) Exploiting Photon Polarization Effects
- 2) Ultraviolet Photoelectron Diffraction: Cu as an Example
- 3) Diffraction versus Dispersion in Fermi Surface Mapping: K/Si(001)
- 4) Interpretation of Line Widths in Valence Photoemission
- 5) Momentum Distribution Curves
- 6) Example: Dispersion Curves from Ni(001)

#### **Lecture 5**

##### *X-Ray Excited Valence Photoemission – Highest Resolution Photoemission*

- 1) Determination of Partial Densities of States
- 2) Examples for Elemental Metals: Pt, Al
- 3) Application to a Binary System: AuCu<sub>3</sub>
- 4) Highest Resolution Photoemission
- 5) Application to Superconductivity
- 6) Quantum Well States

#### **Lecture 6**

##### *Exploring the Limits of X-Ray Photoelectron Diffraction*

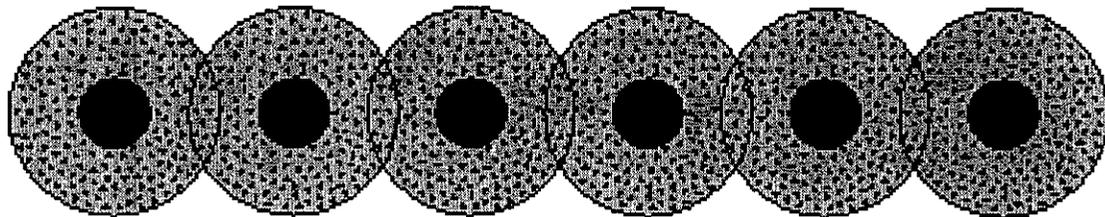
- 1) Surface Structure Problems Solved by XPD
- 2) Simple Structure Identification by Fingerprinting
- 3) Orientation of Large Molecules: C<sub>60</sub>
- 4) Orientation and Conformation of Large Molecules: Chiral 7-Helicene
- 5) Monolayer Film Structure: Hexagonal Boron Nitride (h-BN)
- 6) Monolayer Film to Substrate Registry: again h-BN
- 7) Application to Catalysis: Determining Bonding Sites of Single Atoms
- 8) Application to Catalysis: Finding Subsurface Species (O/Rh(111))

#### **Further Reading (Photoemission from Valence Bands):**

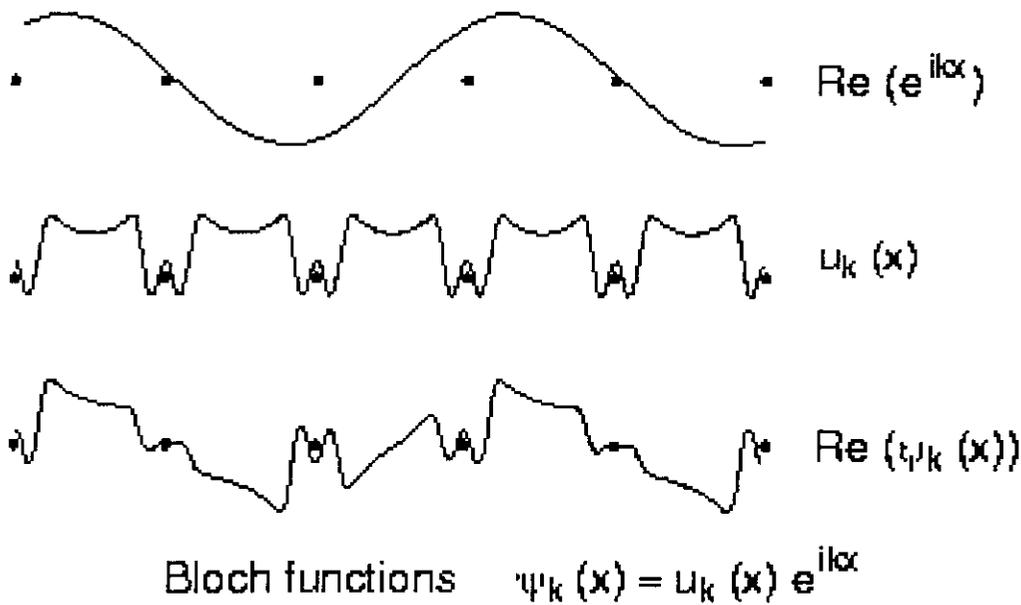
- 1) S. Hüfner, *Photoelectron Spectroscopy* (Springer, Berlin 1995)
- 2) E. W. Plummer and W. Eberhardt, *Adv. Chem. Phys.* 49 (1982) 533
- 3) S. D. Kevan (ed.), *Angle-Resolved Photoemission – Theory and Current Applications* (Elsevier, Amsterdam 1992)

# Electronic Bandstructure in 1 Dimension

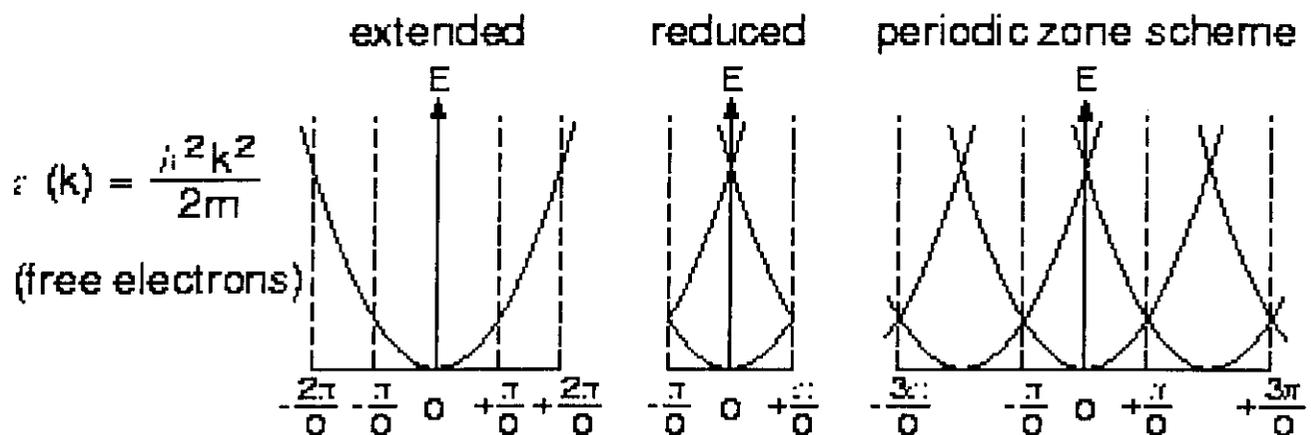
chain of atoms:



wave functions:

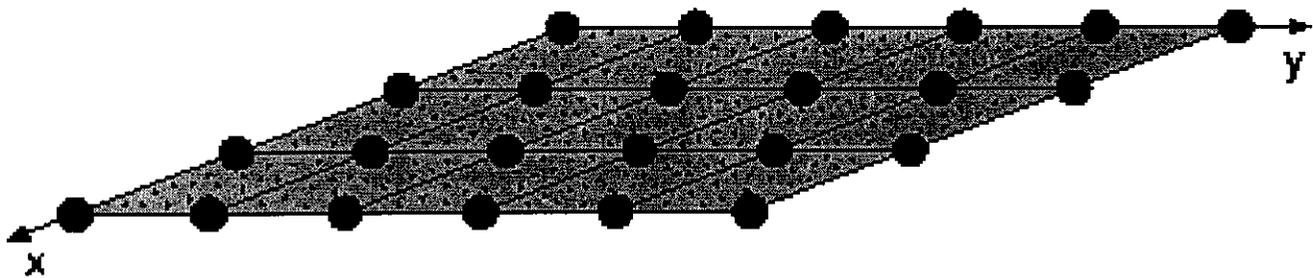


dispersion relation (reciprocal space):

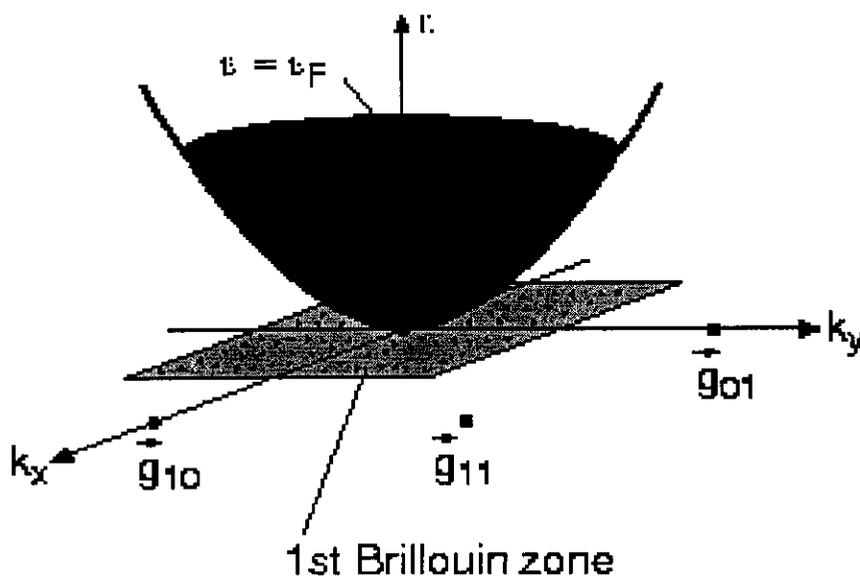


# Electronic Structure in 2 Dimensions

(Plane of atoms)

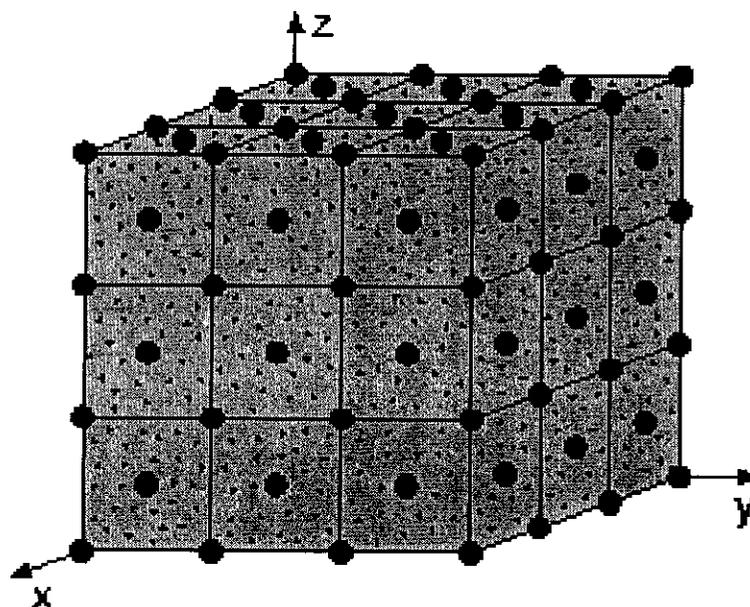


dispersion relation

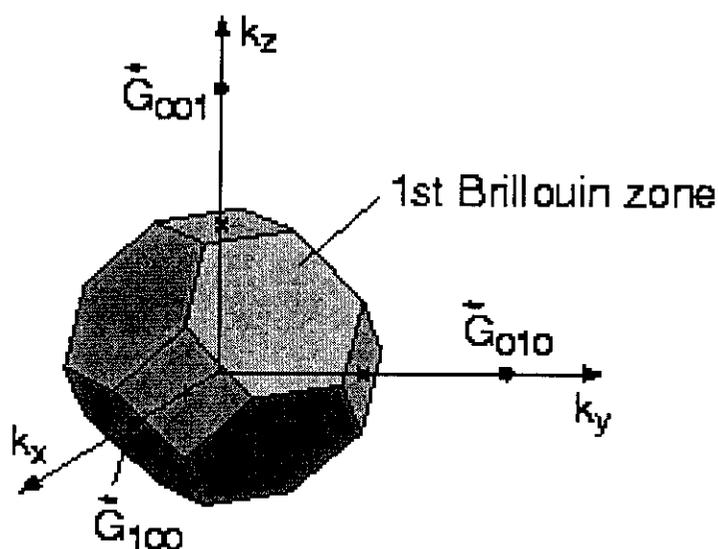


# Electronic Structure in 3 Dimensions

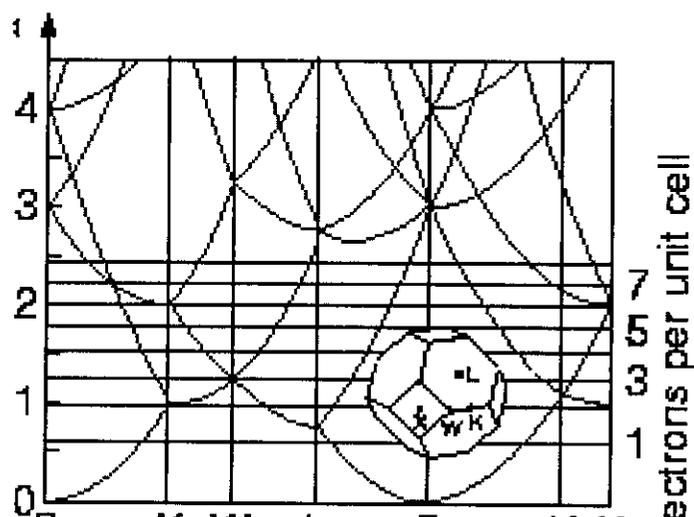
real space:  
(face-centered cubic lattice)



reciprocal space:

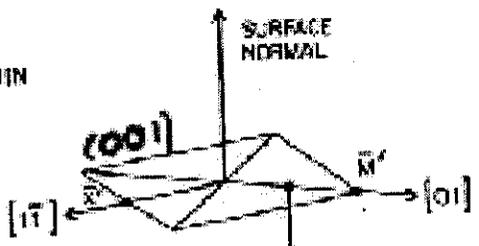


dispersion relation:



2D

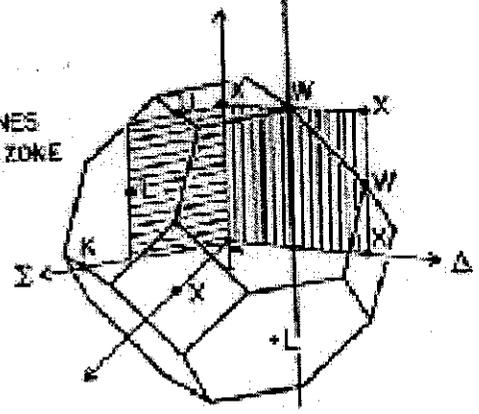
SURFACE BRILLOUIN ZONE



fcc

3D

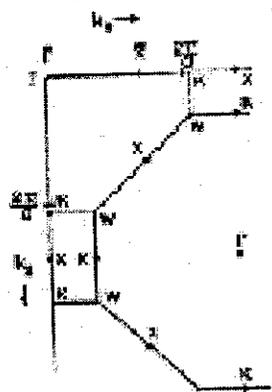
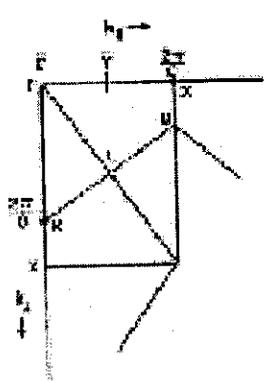
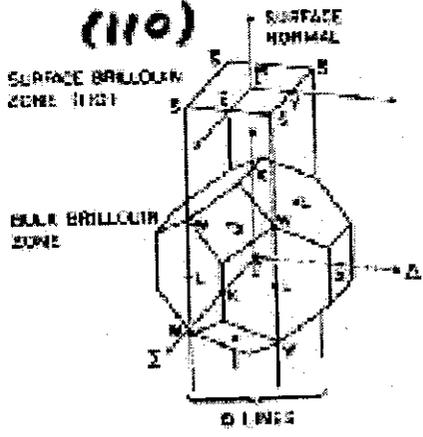
PROJECTION PLANES  
BULK BRILLOUIN ZONE



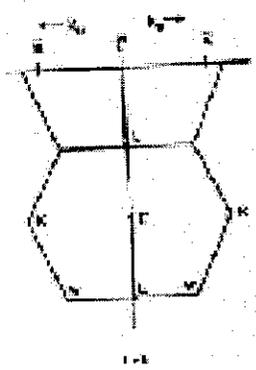
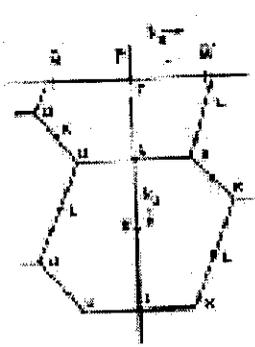
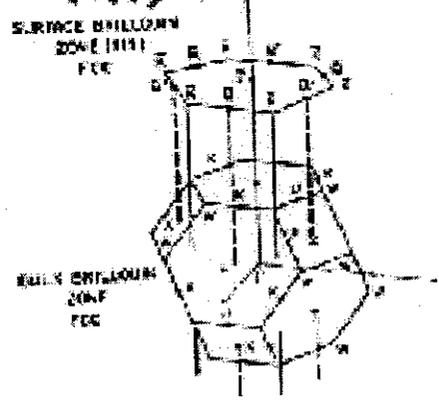
E. W. PLUMMER AND W. IBERHARDT

Adv. Chem. Phys. #9, 535 (1962)

(110)



(111)



## Photoemission of a free electron

	Energy	Momentum
free electron	$E(\vec{k}) = \frac{\hbar^2 k^2}{2m}$	$\hbar \vec{k}$
photon ( $h\nu$ )	$E(\vec{k}) = \hbar \omega = \hbar c  \vec{k} $	$\hbar \vec{k}$

wave numbers  $k$

$$e^- : k = 0.51 \sqrt{E[\text{eV}]} \text{ \AA}^{-1}$$

$$h\nu : k = 0.51 \cdot E[\text{eV}] \cdot 10^{-3} \text{ \AA}^{-1}$$

Photoemission:



Conservation Laws:

$$E_1 + h\nu = E_2$$

$$\vec{k}_1 + \vec{k}_{h\nu} = \vec{k}_2$$

... cannot be simultaneously fulfilled!  
 $\rightarrow$  process forbidden

Atoms, Molecules: Recoil

Solids: Recoil (= reciprocal lattice vector)

# Photoemission from a Periodic Potential

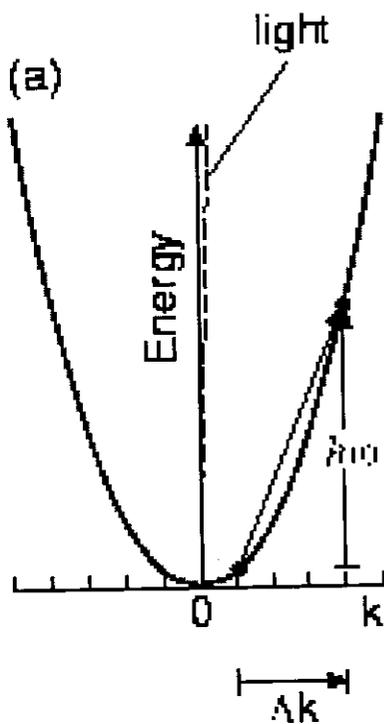
## Conservation Laws:

$$\epsilon_i(\vec{k}_i) + h\nu = \epsilon_f(\vec{k}_f)$$

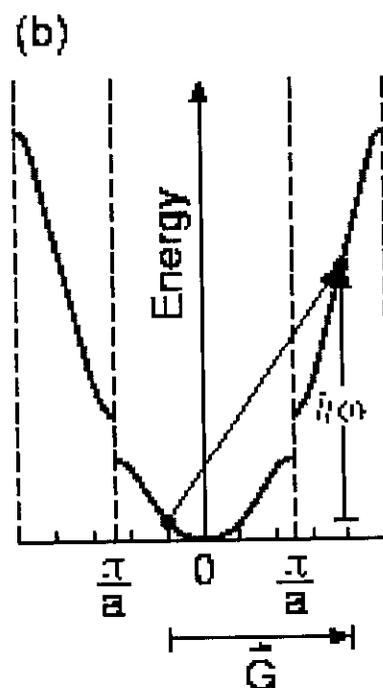
$$\vec{k}_i + \vec{k}_{ph} + \vec{G} + \vec{g} = \vec{k}_f$$

$\approx 0$

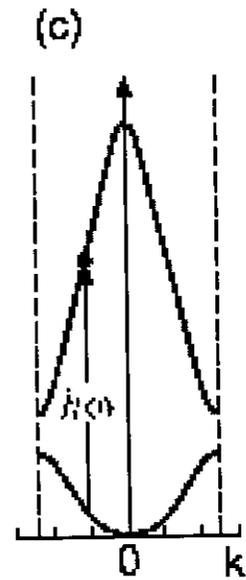
reconstructed  
surface



free electron



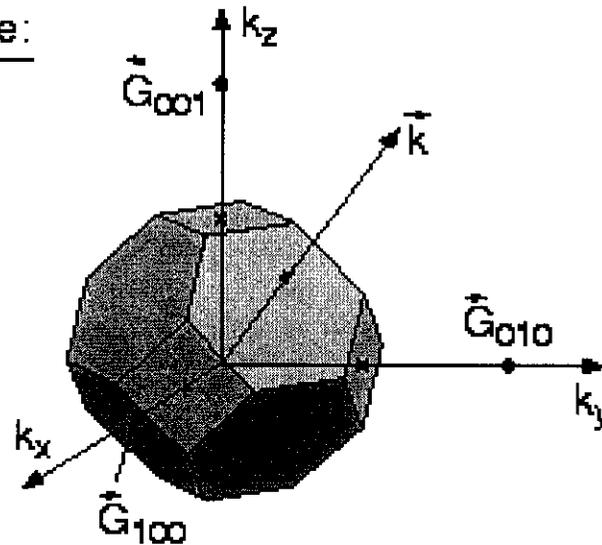
extend zone  
periodic potential



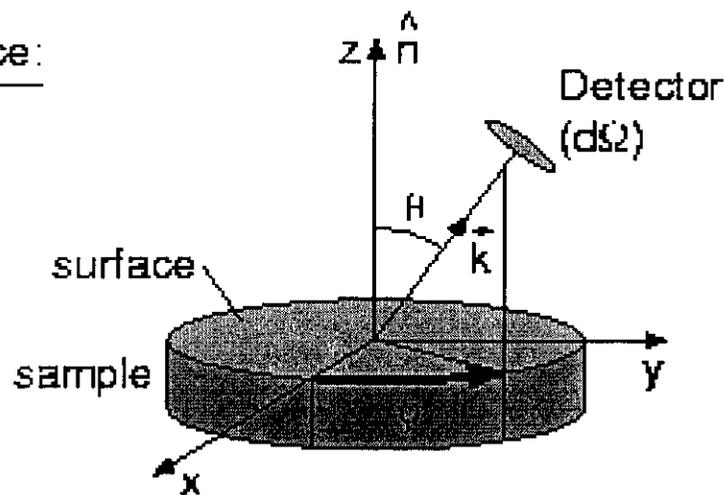
reduced zone  
periodic potential

## Measurement of the Photoelectron Momentum

reciprocal space:



real space:



direction:  $\hat{k} = \theta, \phi$  (watch for refraction)

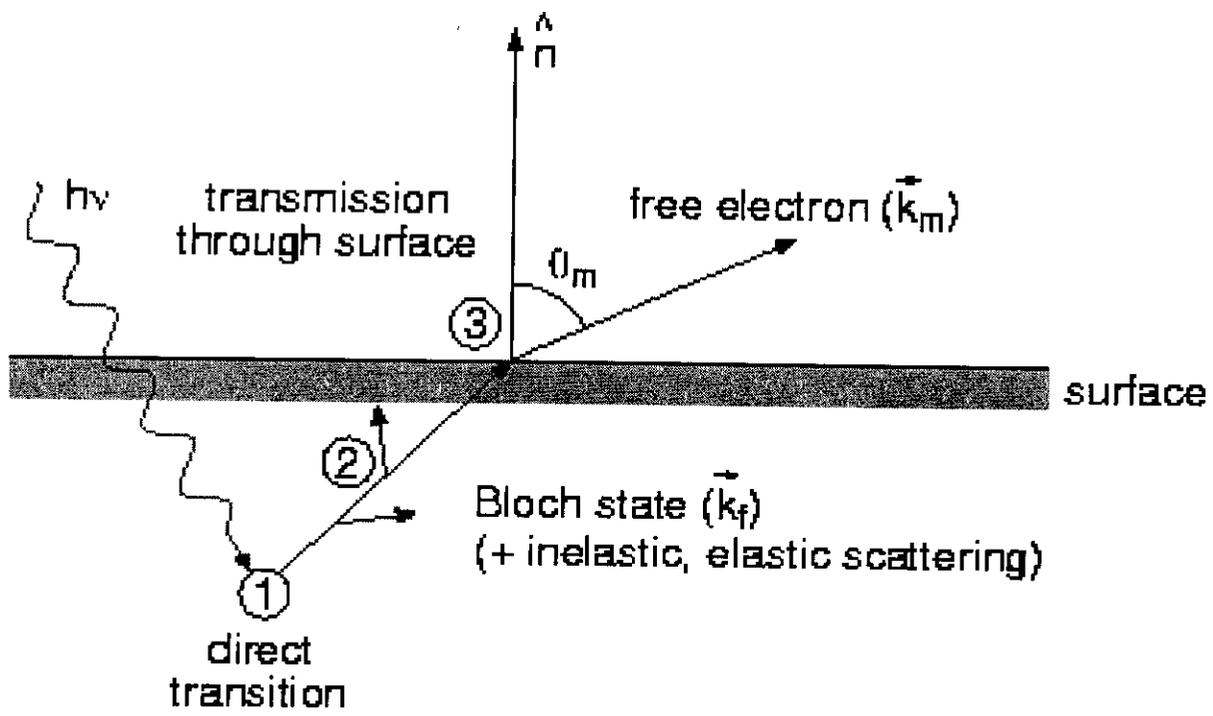
magnitude: from  $\epsilon_f(\vec{k})$  ( $\epsilon_f$  is measured)

Problem:  $\epsilon_f(\vec{k})$  usually not known

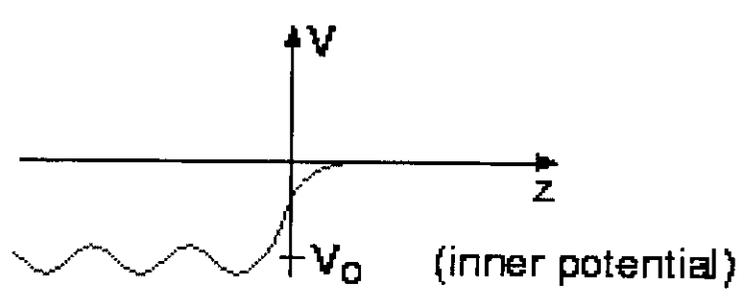
Solution: free electron final state

$$\epsilon_f(k) = \frac{\hbar^2 k^2}{2m}$$

# The 3-Step Model

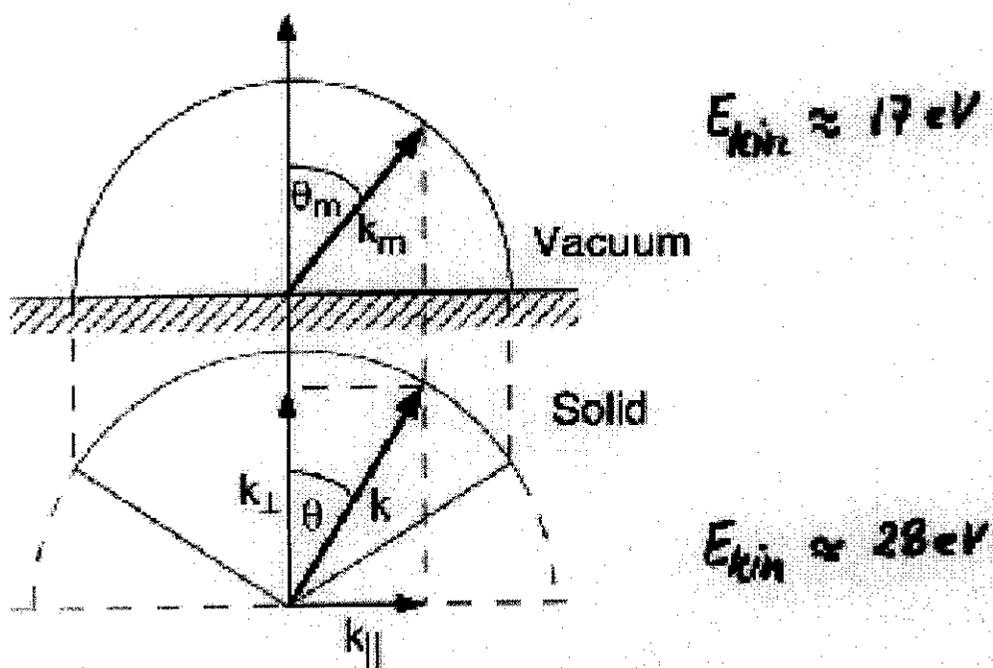


- ① Photoexcitation
- ② Propagation to surface
- ③ surface potential step  $\rightarrow$  Refraction



periodicity within surface  $\rightarrow \vec{k}_{f\parallel} = \vec{k}_{m\parallel}$   
 surface potential step  $\rightarrow \vec{k}_{f\perp} > \vec{k}_{m\perp}$

## Refraction at the Surface Potential Step



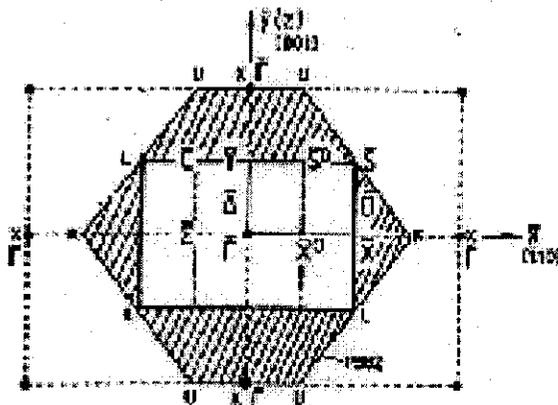
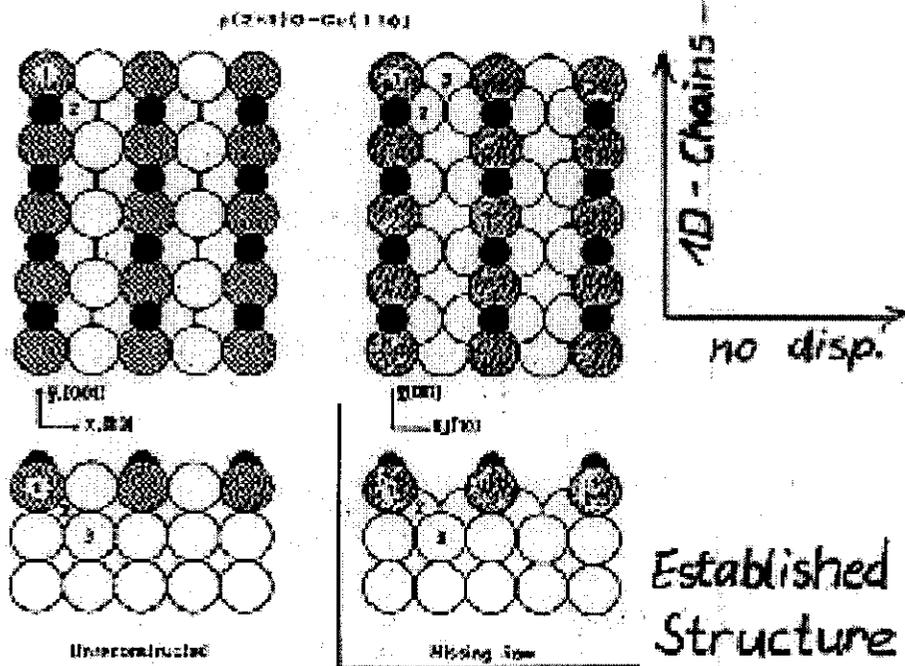
$$\sin \theta = \sin \theta_m \sqrt{\frac{h\nu - \Phi}{h\nu - \Phi + V_0}}$$

$\Phi$ : work function

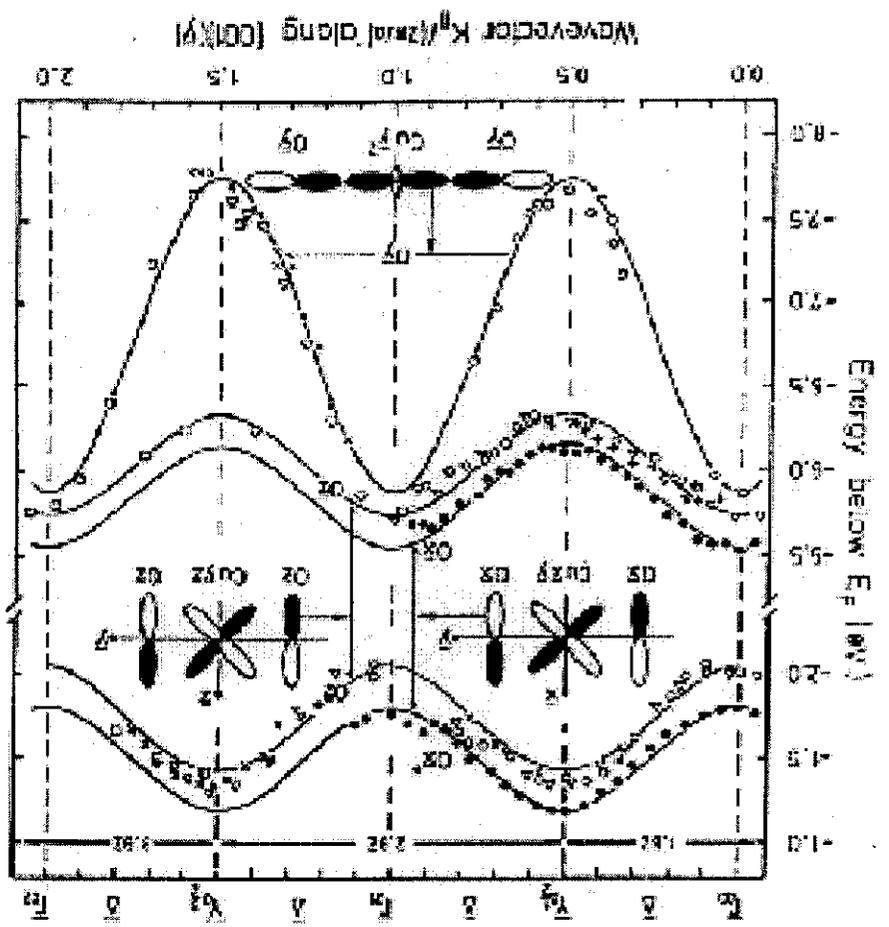
$V_0$ : inner potential

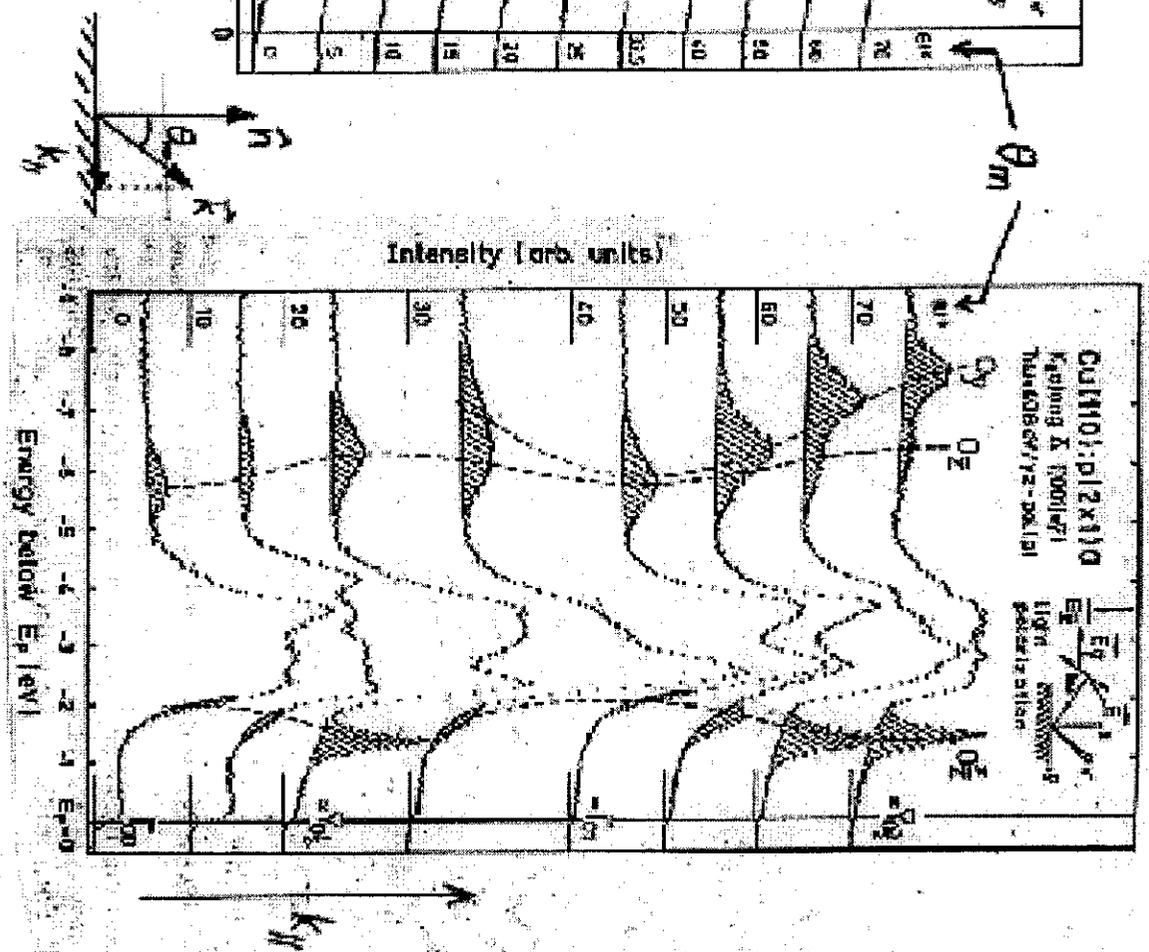
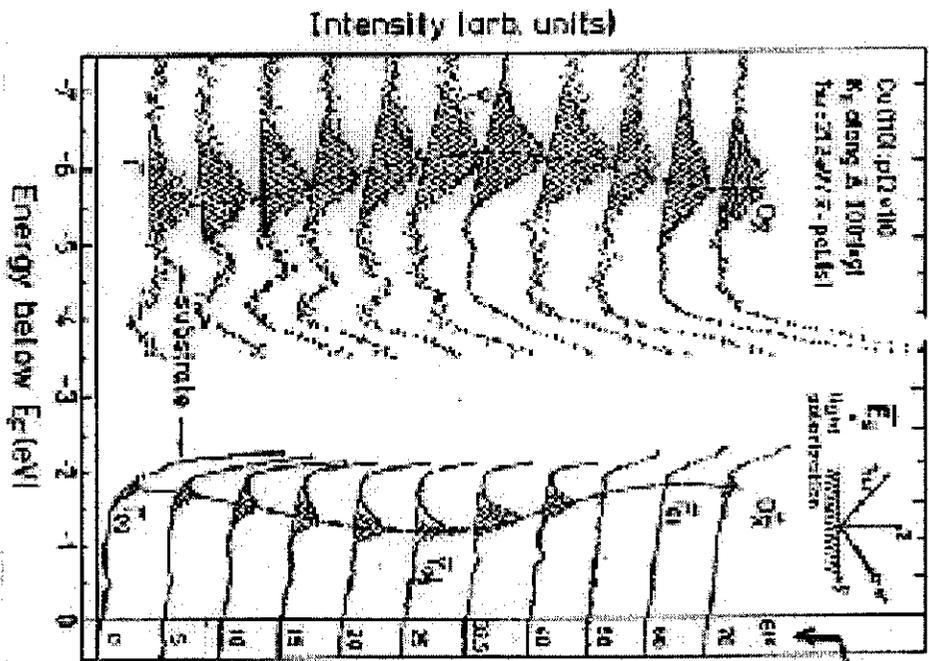
# A One-Dimensional Example:

$p(2 \times 1) O - Cu(110)$

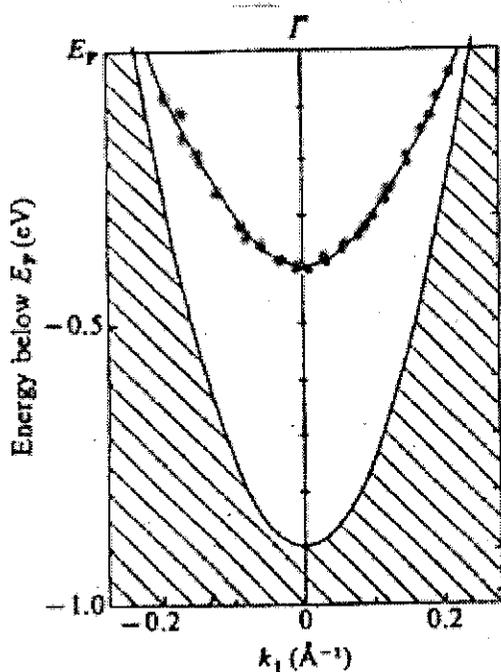
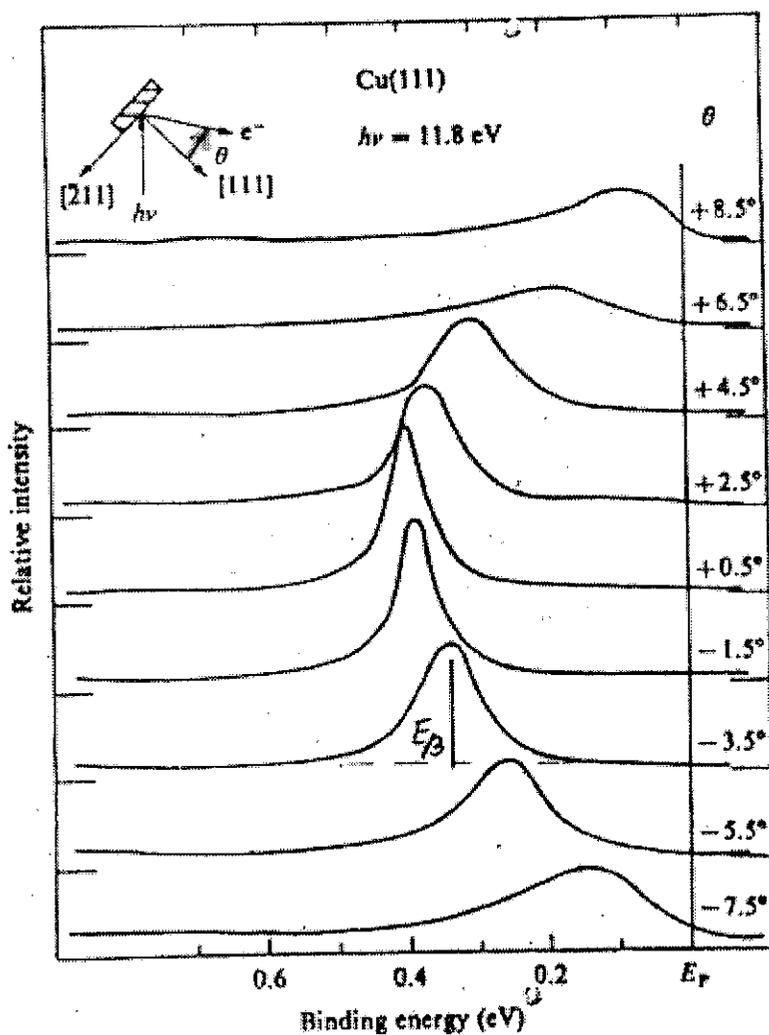


fcc [110] surface Brillouin zone (SBZ)



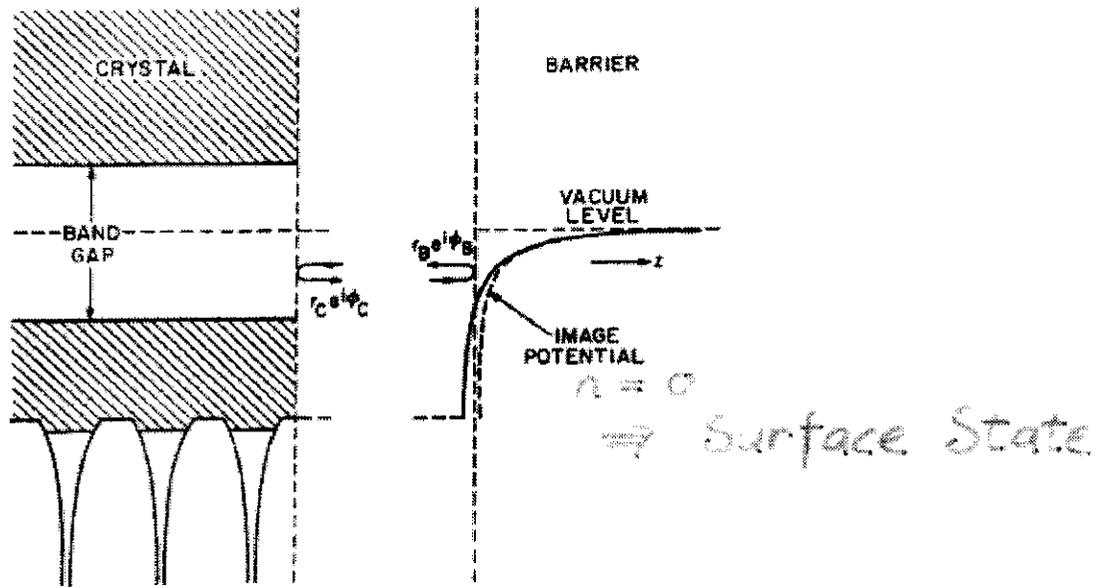


# A 2D Example: Shockley Surface State on Cu(111)

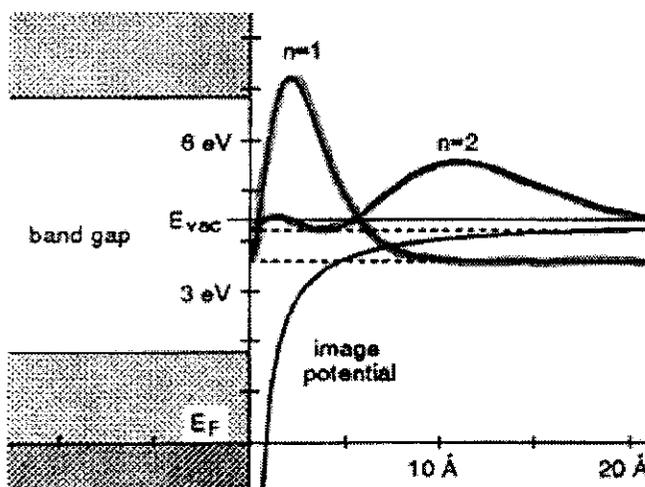
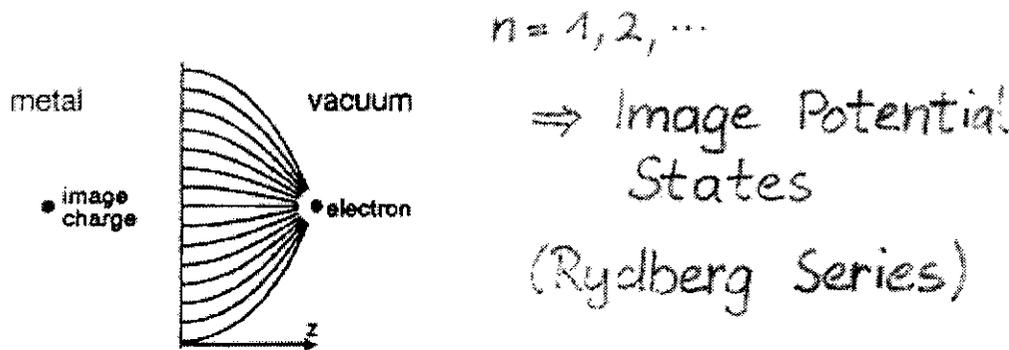


S.D. Kevan et al.  
 PRB 12 ('87) 5809

# Surface States

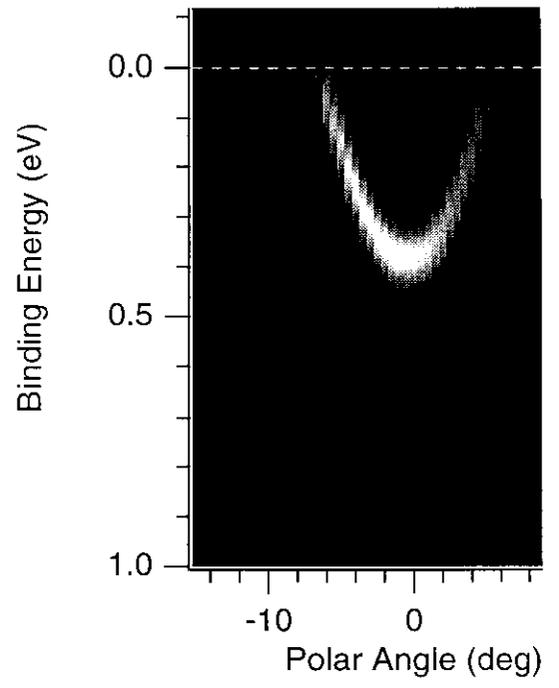
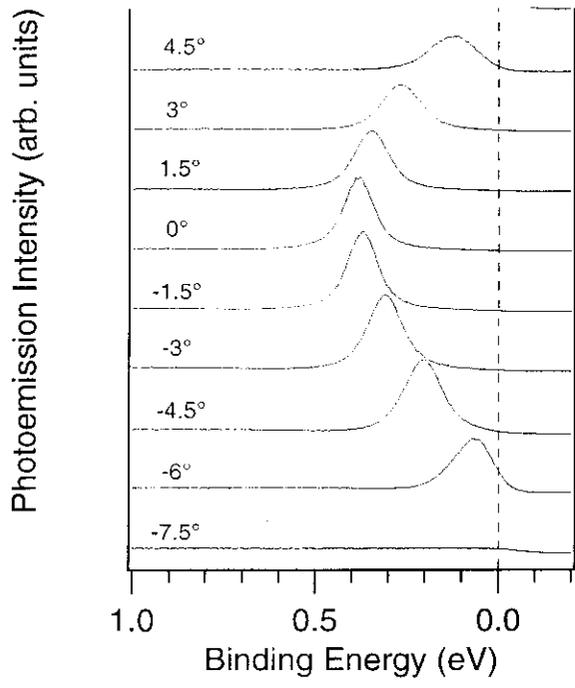


from N. V. Smith, PRB 32, 3549 (1985)



T. Fauster,  
Appl. Phys. n.  
59 (1994) 639

Fig. 1. Top: The electric field of an electron in front of a metal surface can be described by the concept of an image charge. Bottom: The corresponding attractive image potential leads to a series of bound states if the electron cannot penetrate into the metal along certain directions due to a band gap. For the lowest two states the square of the wave function is shown.



... in  $k_{//}$

occupation numbers re

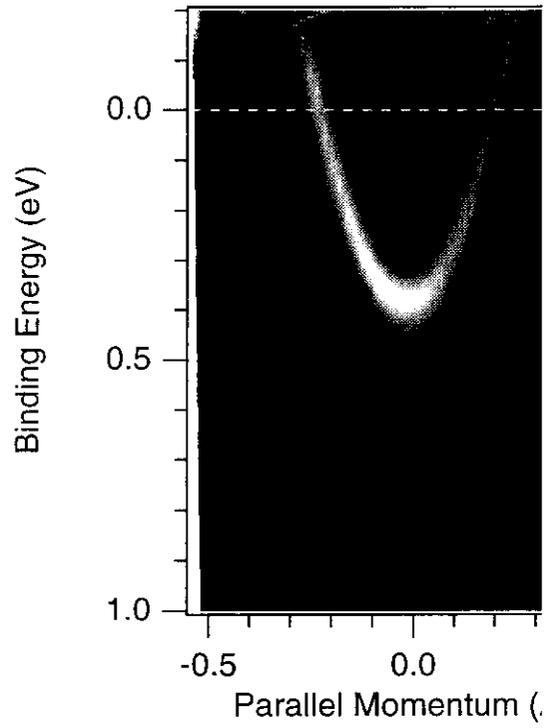
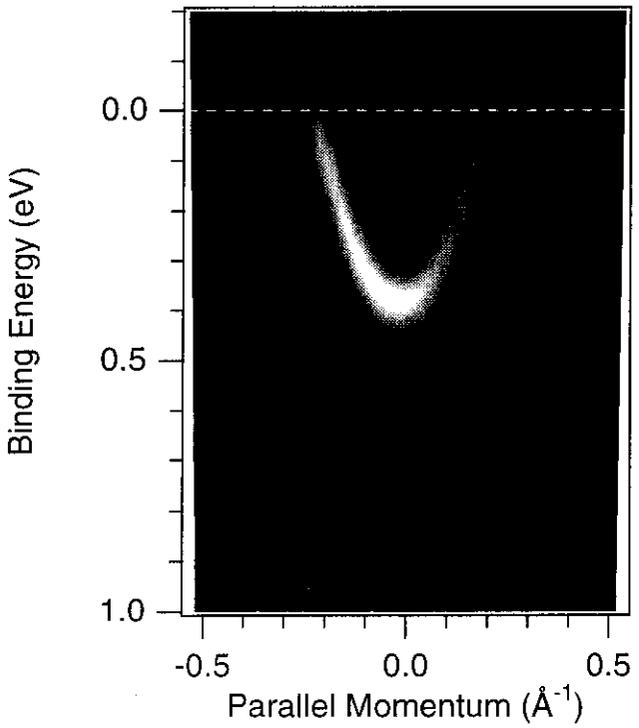
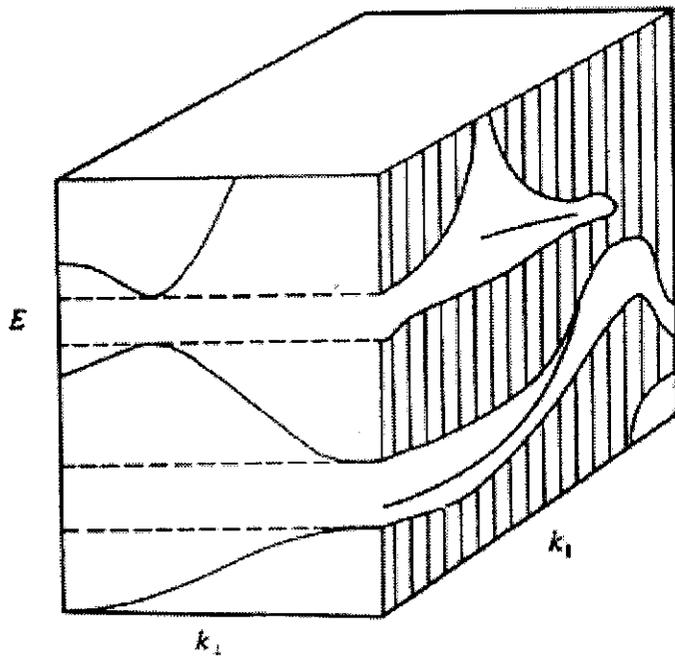


Fig. 4.15. Projected bulk band structure at the surface of a metal. The dispersion of two possible surface state bands is indicated.



Where do surface states exist?

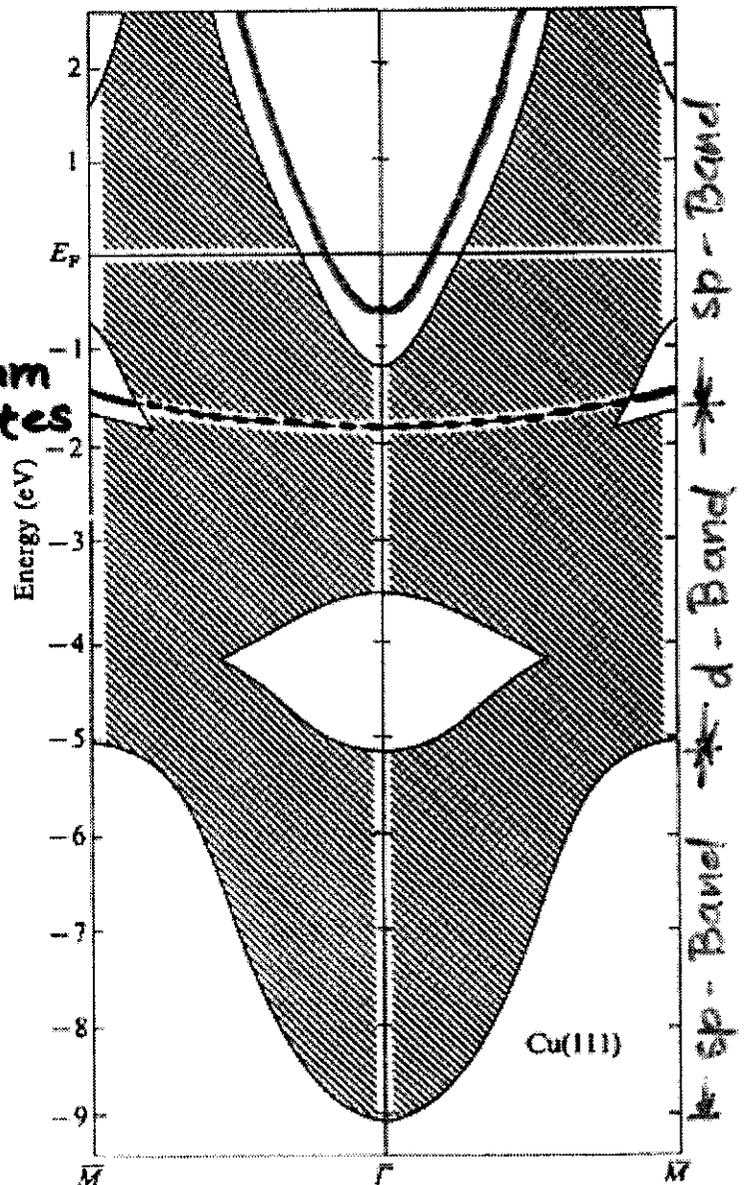
Shockley St.

Experimental identification:

- "crud" test
- no dispersion in  $k_{\perp}$  ( $\rightarrow$  S.R.)

Fig. 4.17. Surface states (dashed curves) and bulk projected bands at a Cu(111) surface according to a six-layer surface band structure calculation (Encoda, Bylander & Kleinman, 1983).

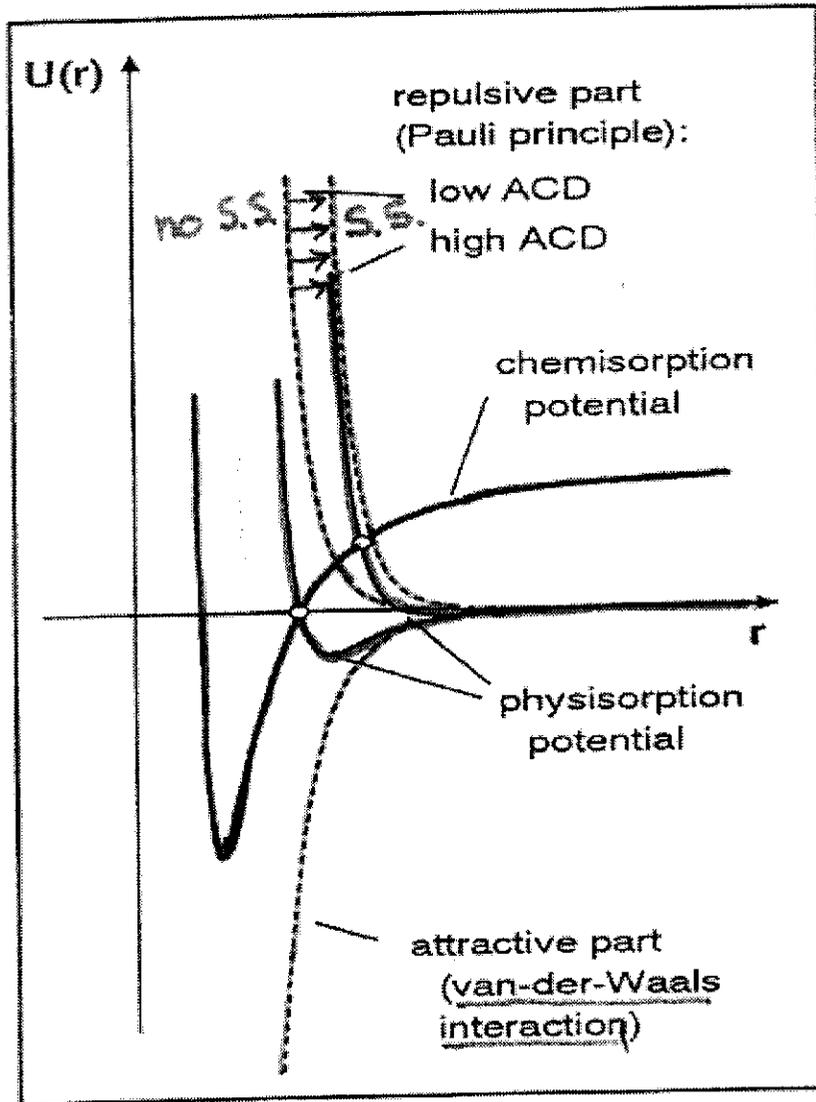
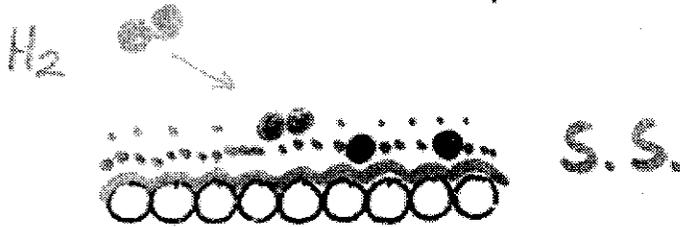
Tamm States



aus Zangwill

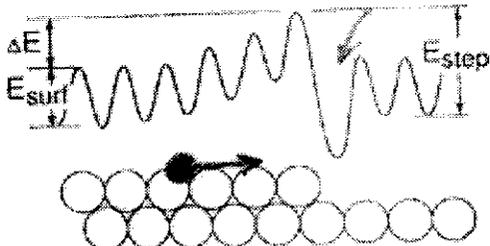
# Importance of Surface States

→ dissociative chemisorption



→ surface diffusion

Schwöbl barrier



... reduced by S.S.

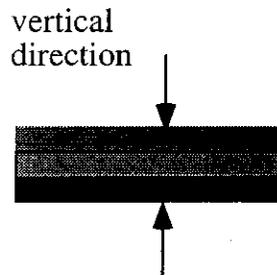
E. Bertel et al.  
Appl. Phys. A 63  
(1996) 523

Memmel, Bertel, PRL 75 ('95) 485.

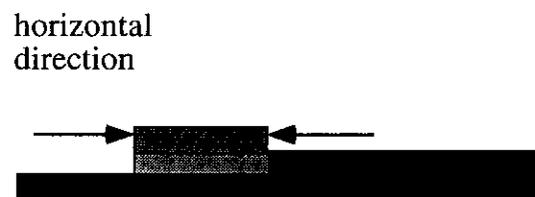
FIG. 1 Schematic representation of the diffusion potential at a step.

# Surface States and Nanostructures

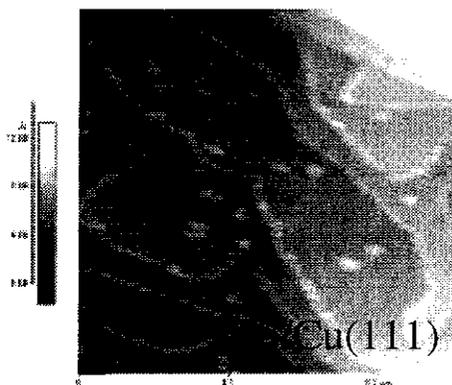
2D Electron Gas:	GaAs/AlGaAs	met. surf. state
electron concentrations	$\sim 10^{11} \text{cm}^{-2}$	$\sim 10^{15} \text{cm}^{-2}$ Al(001) $\sim 10^{14} \text{cm}^{-2}$ Cu(111)
Fermi wave length	$\sim 40 \text{ nm}$	$\sim 0.7 \text{ nm}$ Al(001) $\sim 3 \text{ nm}$ Cu(111)
phase coherence length	$\sim 50 \mu\text{m}$ (4K)	$\sim 1000 \text{ nm}$ (4K) $\sim 10 \text{ nm}$ (300K) ... can be lower
	mesoscopic physics	nanostructures !
	Quantum Size Effects	



no problem  
(e.g. surface states)



challenge !



steps,  
step decoration,  
self assembly, ...

# Quantum Mirages

... hand-made  
nanostructures !

... viewed by the  
Kondo effect

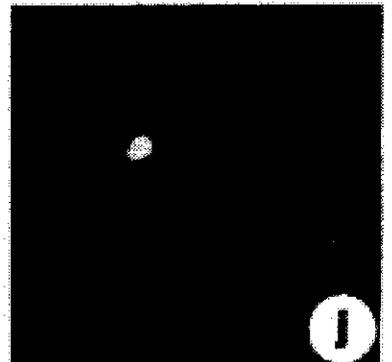
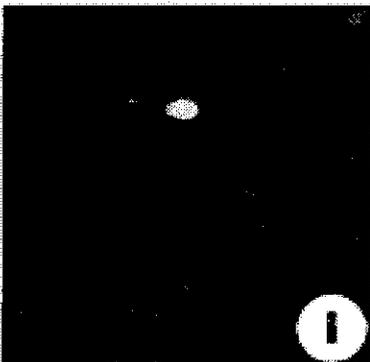
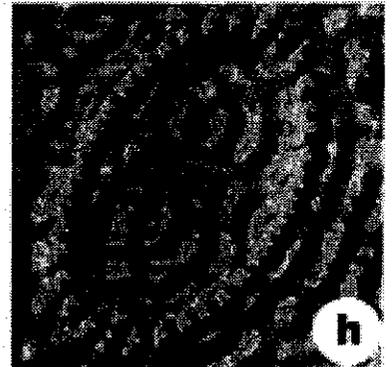
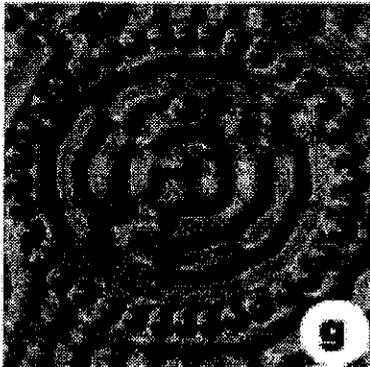
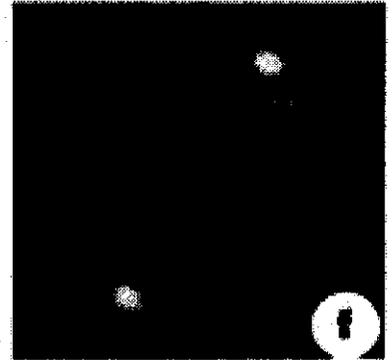
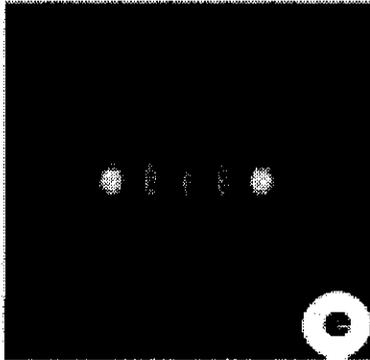
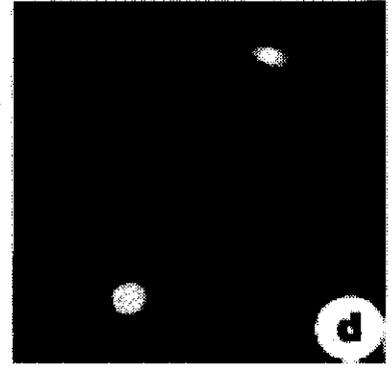
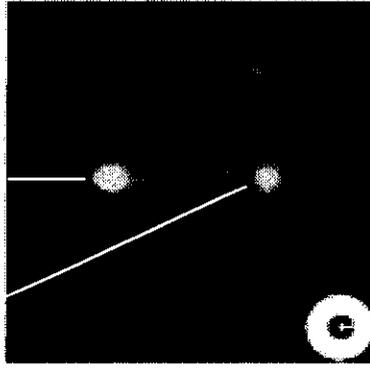
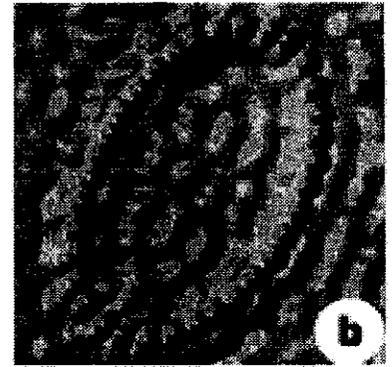
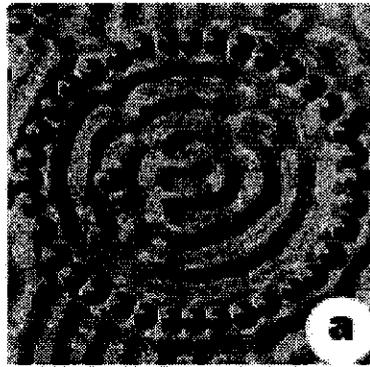
Atom

"Mirage"

Calculated  
Eigenmodes

... put atom off the  
focal point :

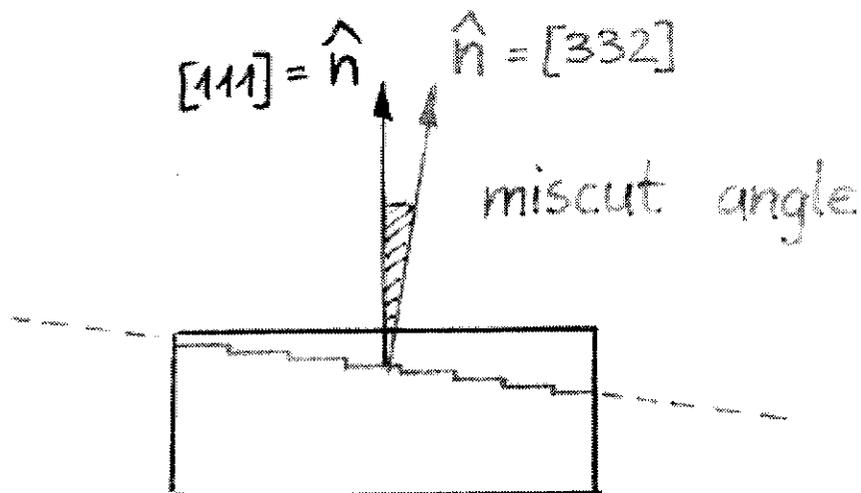
... no mirage !



H. C. Manoharan, C. P. Lutz,  
D. M. Eigler,  
Nature 403 (2000) 512

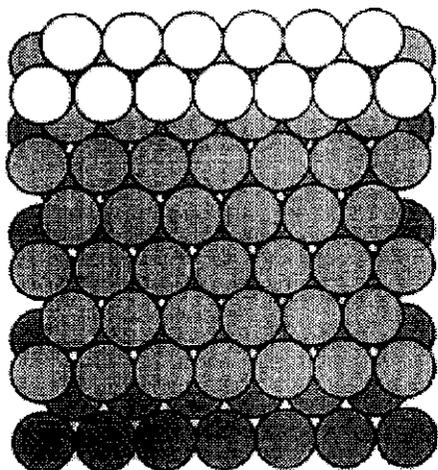
# Surface State on Stepped Cu Surfaces

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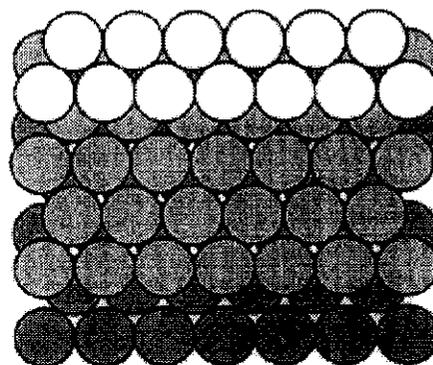


→ Interaction Steps  $\rightleftharpoons$  Surf. State  
... → chem. Reactivity?

**Cu(332)**  
(10° miscut, 12Å terraces)

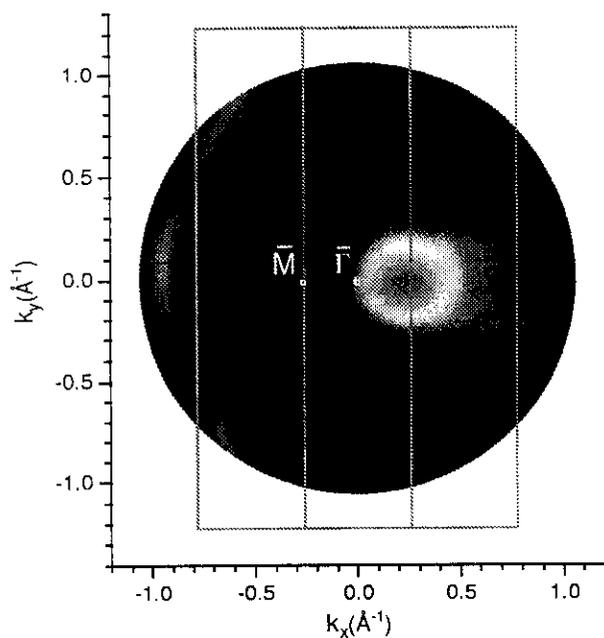


**Cu(221)**  
(15.8° miscut, 7.7Å terraces)



# 1D Shockley Surface State Resonance on Cu(332)

Fermi Surface Map



Dispersion Plots

