

Strangeness and Spin in hadronic and e.m. interaction

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LNS CERN Saclay

- 1) Strangeness content of the nucleon
- 2) hypernuclear states $\left\{ \begin{array}{l} \text{potential} \\ \text{decay} \\ \text{Y-N int.} \end{array} \right.$
- 3) Strange resonances
- 4) Hyperon polarisation

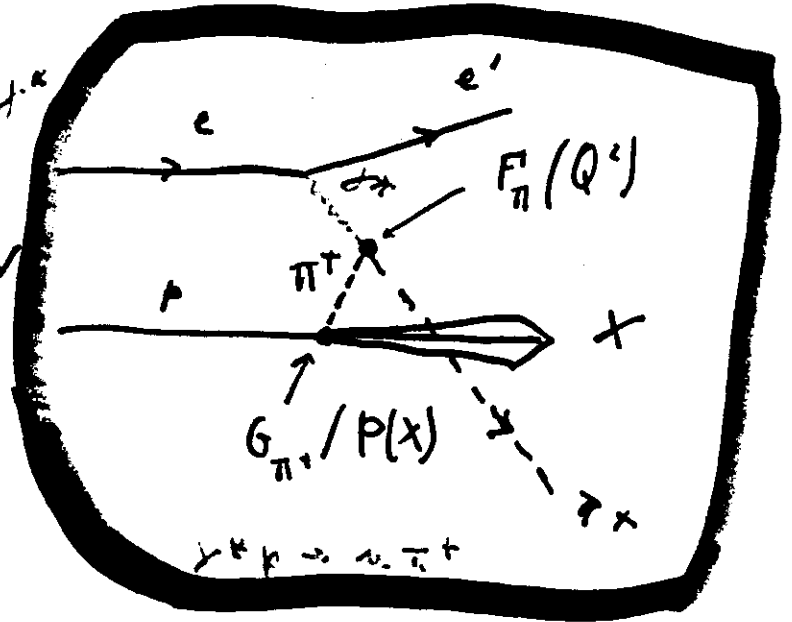
Quasi-elastic scattering on virtual π K

$$q^{*2} = (e - e')^2 = -Q^2 = \text{s.g. mass } q^{*2}$$

$$\nu = E - E' = \text{en. loss of } e$$

$$s = (q^{*2} + p)^2 = W^2 = \text{s.g. mass } q^{*2} N$$

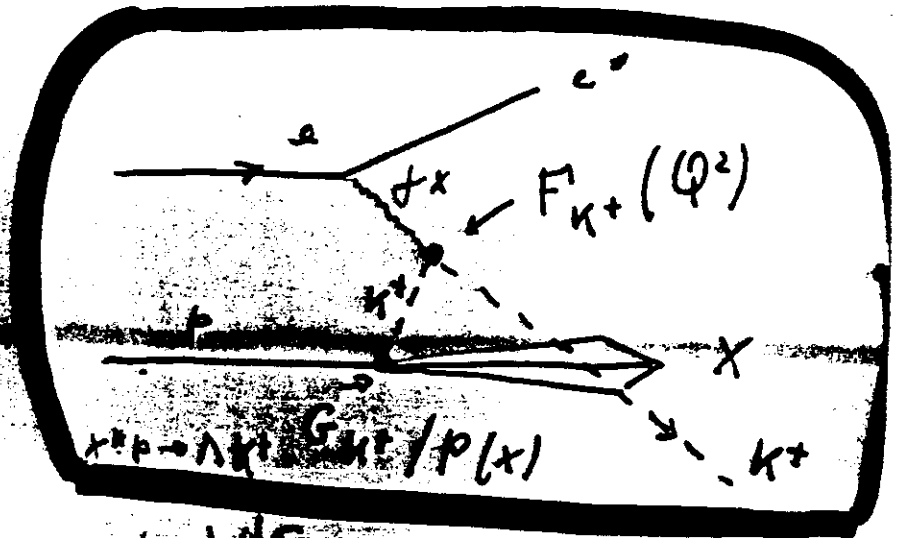
$$t = (q^{*2} - \pi)^2 = \text{s.g. mom. onto } N$$



$$Q^2 \leq 1 \text{ GeV}$$

$$\nu \geq 2.2 \text{ GeV}$$

$$W \geq 2.1 \text{ GeV}$$

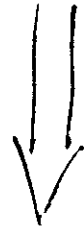


$$2\pi \frac{d^2\sigma}{dt dQ^2} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \epsilon \cos(2\theta) \frac{d\sigma_P}{dt} + \sqrt{2\epsilon(\epsilon+1)} \cos\theta \frac{d\sigma_I}{dE}$$

- $\sigma_T \rightarrow$ unpolarized transverse photons $\frac{1}{2}(\sigma_{11} + \sigma_{-1-1})$
- $\sigma_L \rightarrow$ longitudinal polarized photons σ_{00} $\lambda=0$
- $\sigma_P \rightarrow$ transverse linearly polarized photons $\frac{1}{2}(\sigma_{11} - \sigma_{-1-1})$ $\lambda=1$
- $\sigma_I \rightarrow$ interference transverse-longitudinal polar. phot. σ_{10}

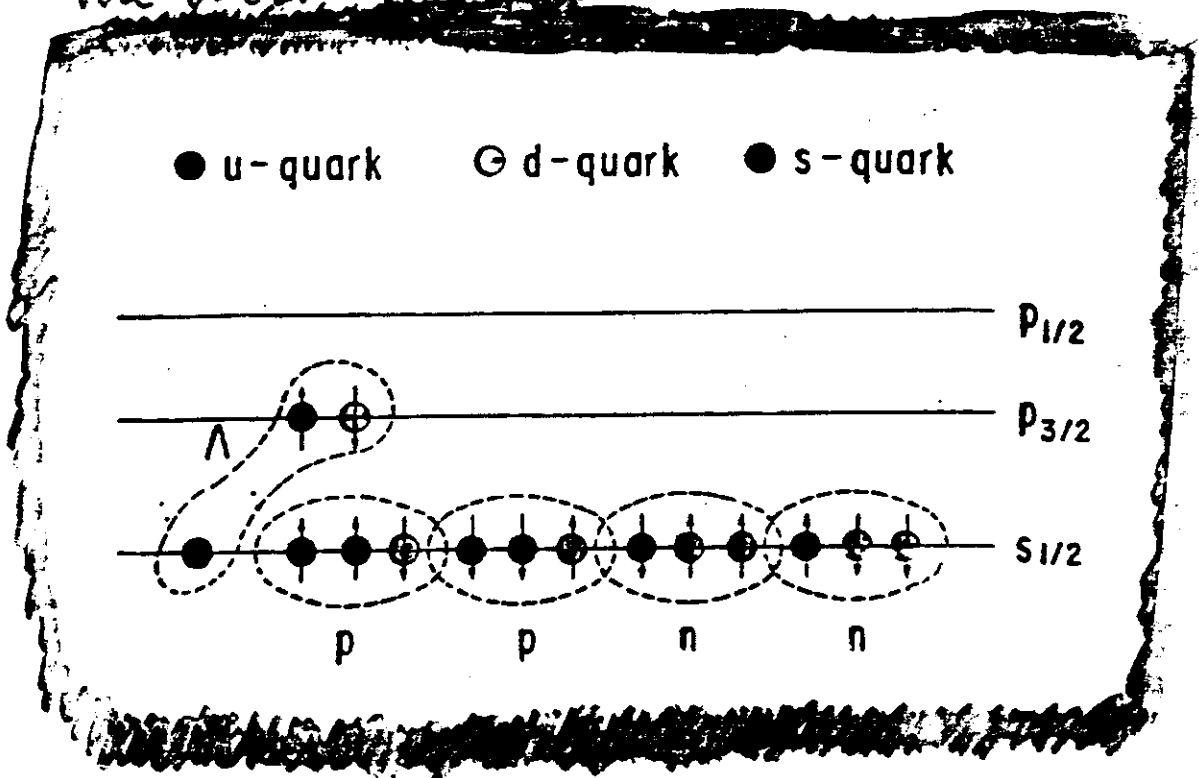
$$\frac{d^2\sigma_L(ep \rightarrow e'\pi^+X)}{d\pi dQ^2} = G_{\pi^+}/p(x) \quad 2\pi \frac{d\sigma_{01}(e\pi^+ \rightarrow e'\pi)}{dQ^2}$$

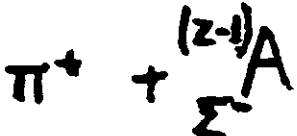
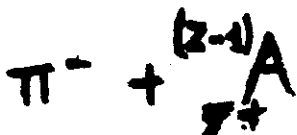
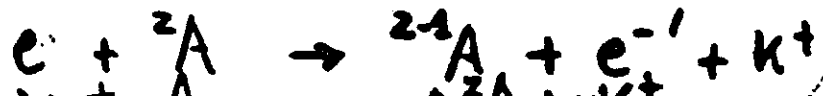
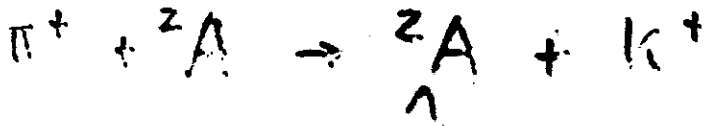
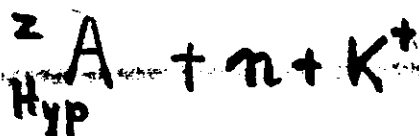
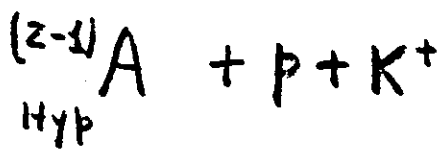
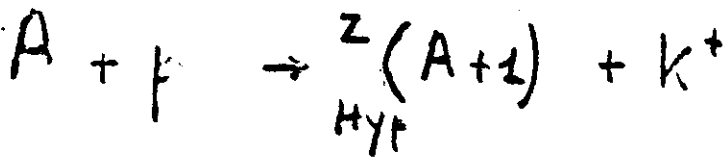
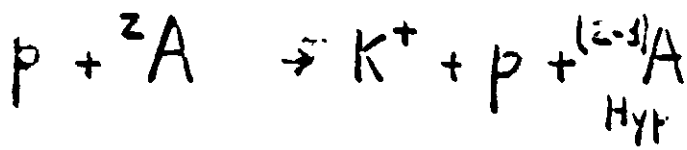
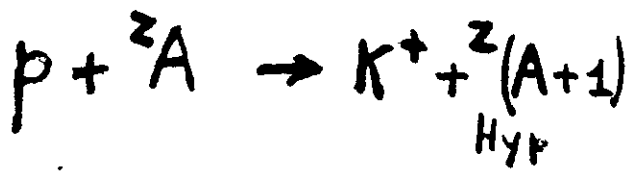
$$\frac{d\sigma}{d\Omega} \text{ Hyp-stats} \sim N_{\text{eff}} \frac{d\sigma}{d\Omega_d} |F(q)|^2$$



Hypernuclei

- 1) Test nuclear model
- 2) hyperon nucleon interaction at low momenta
- 3) Different behaviour of a baryon when free or embedded in nuclear matter





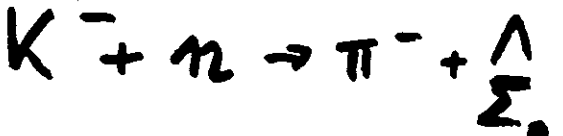
associated production

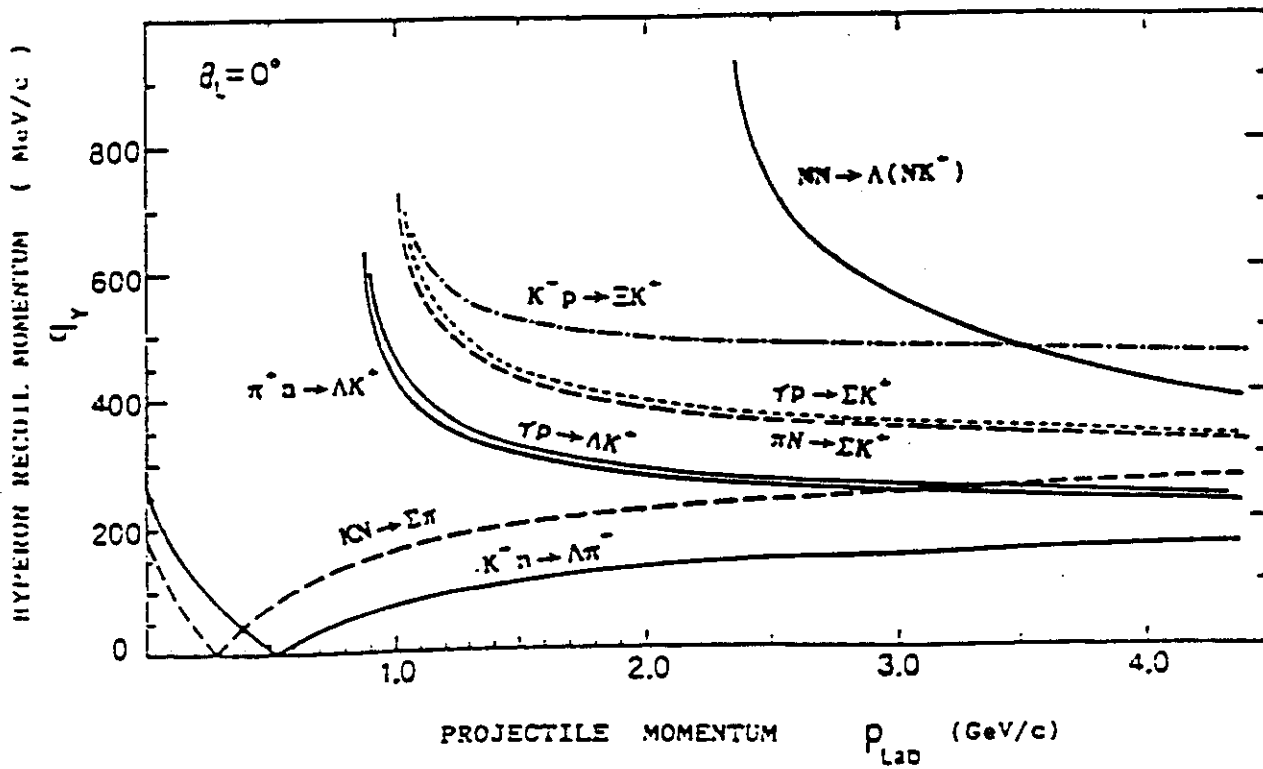
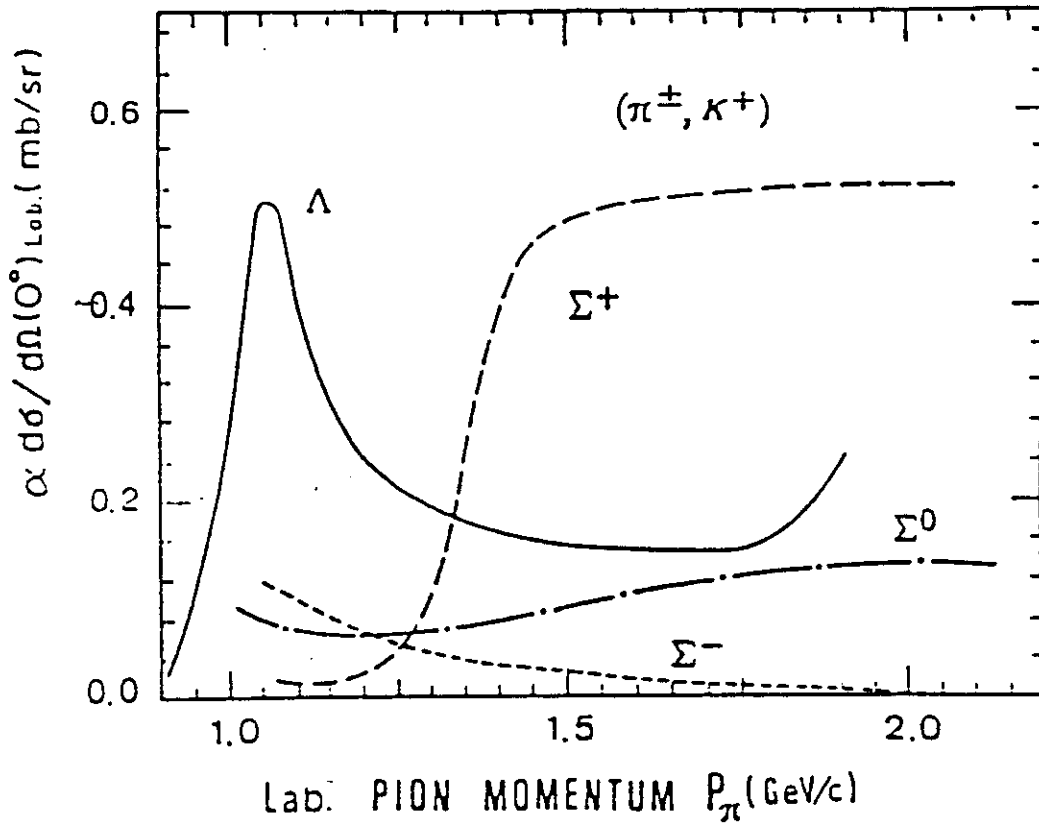
$$p + p \rightarrow p + \Lambda + K^+$$

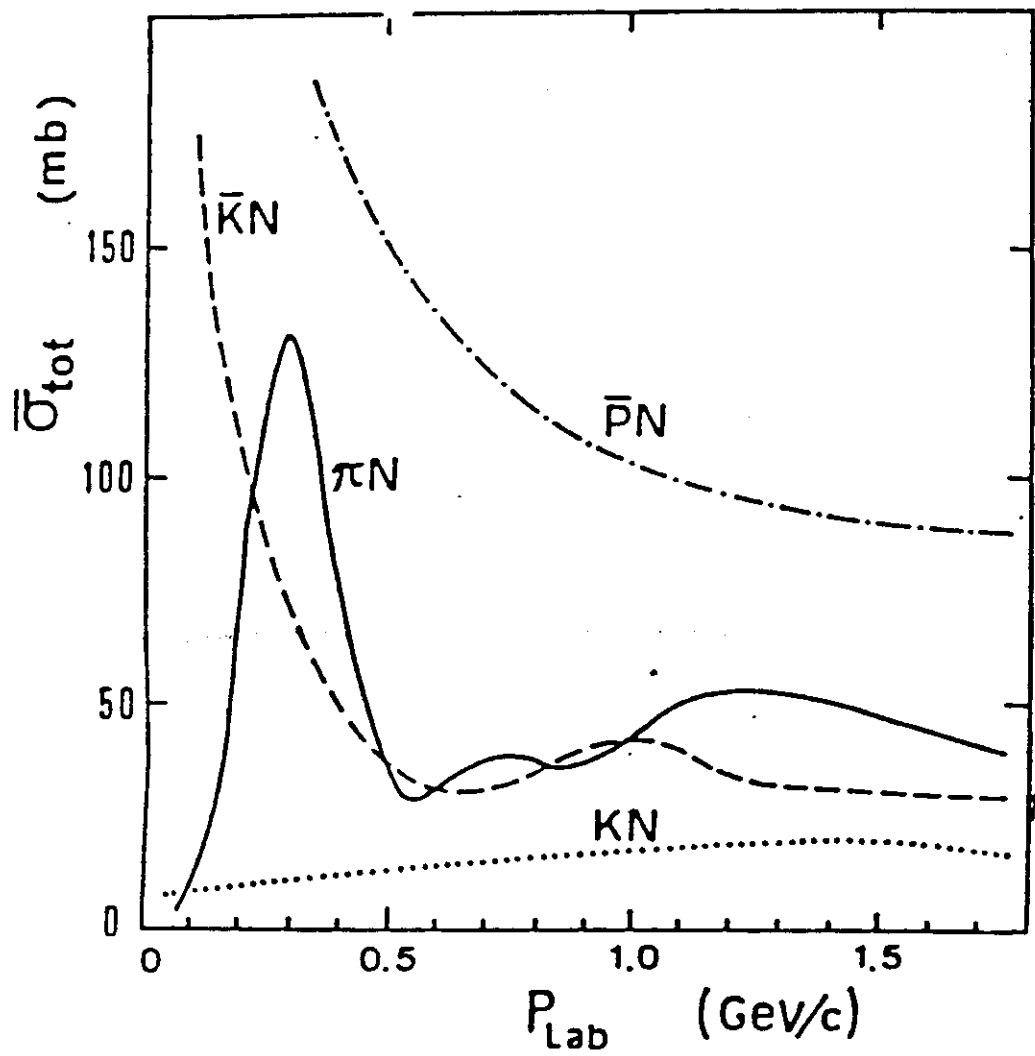
$T_p = 2.85 \text{ GeV} \quad \sigma_E = 51 \pm 12 \text{ } \mu\text{b}$

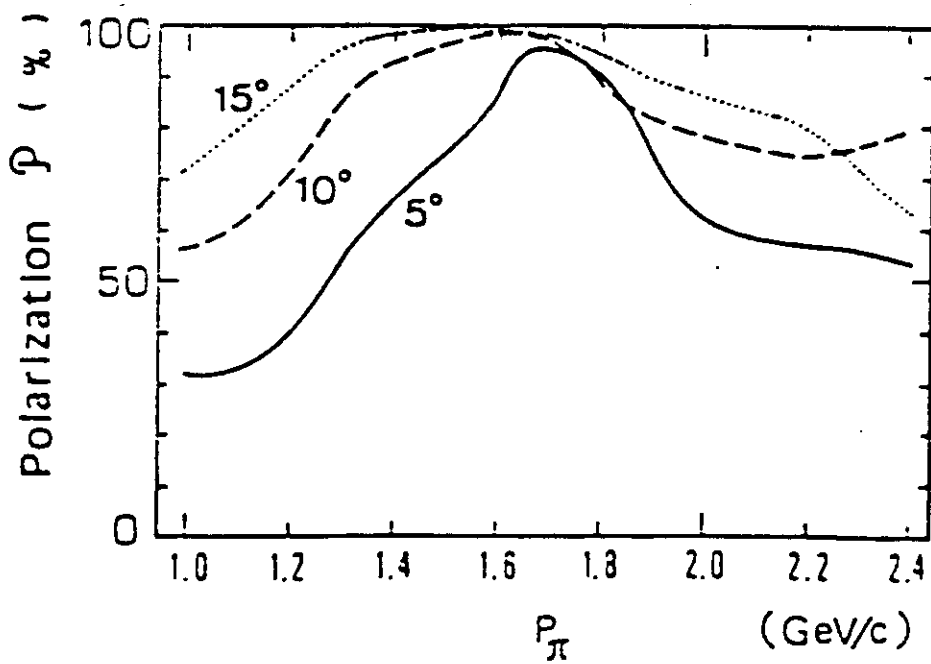
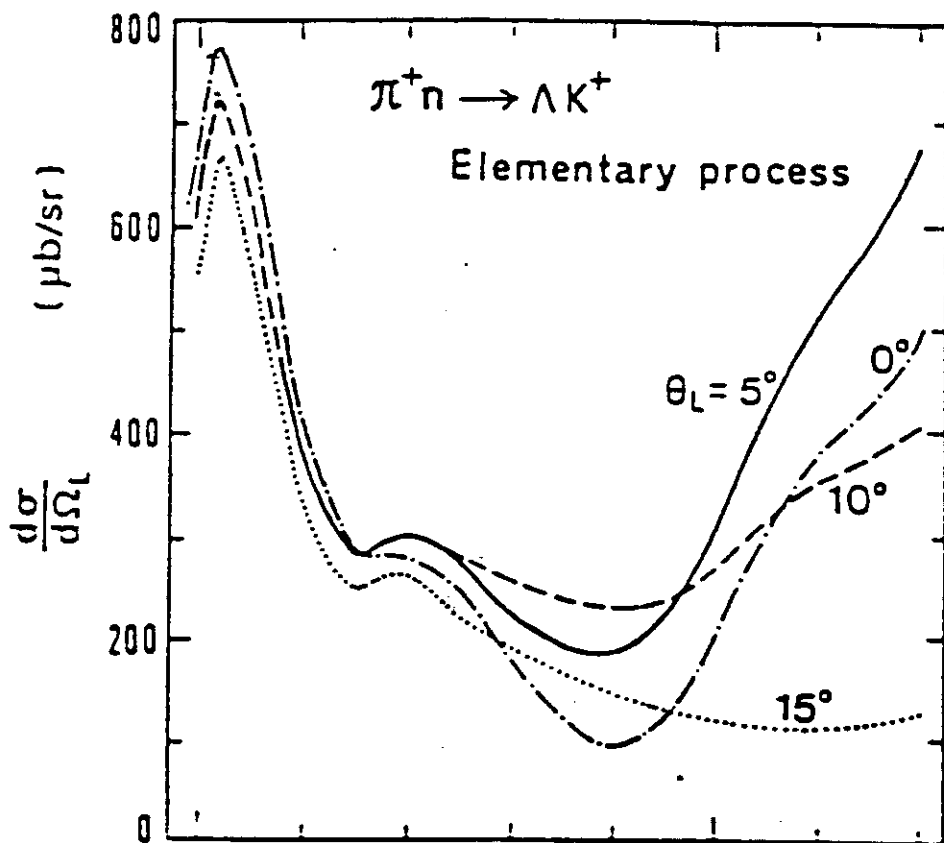


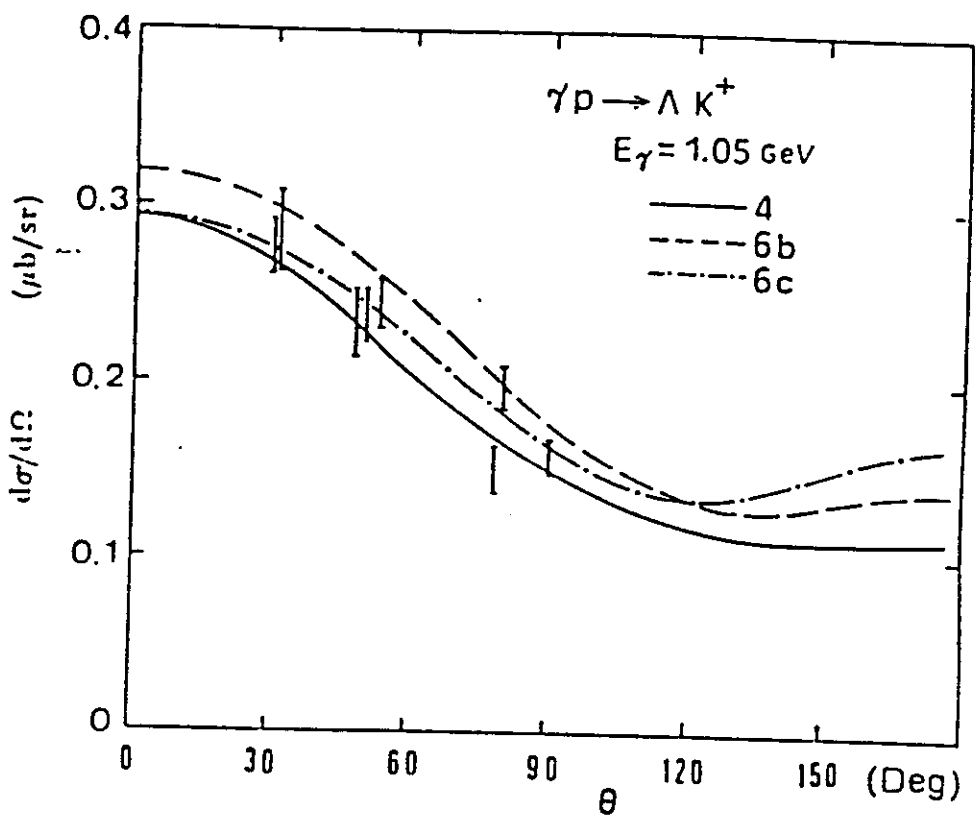
strangeness exchange



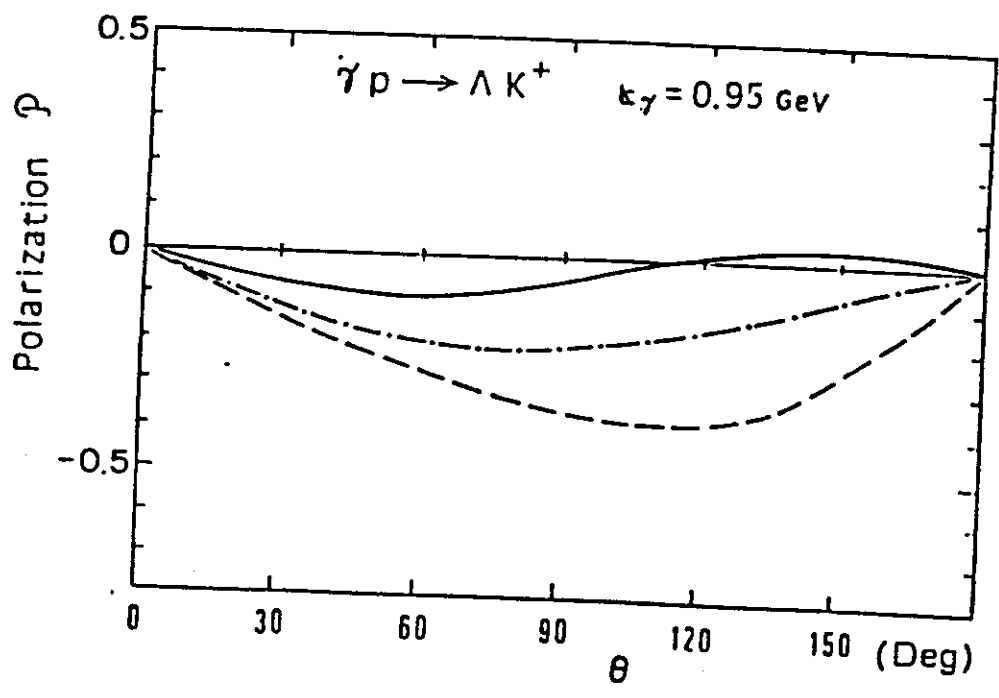


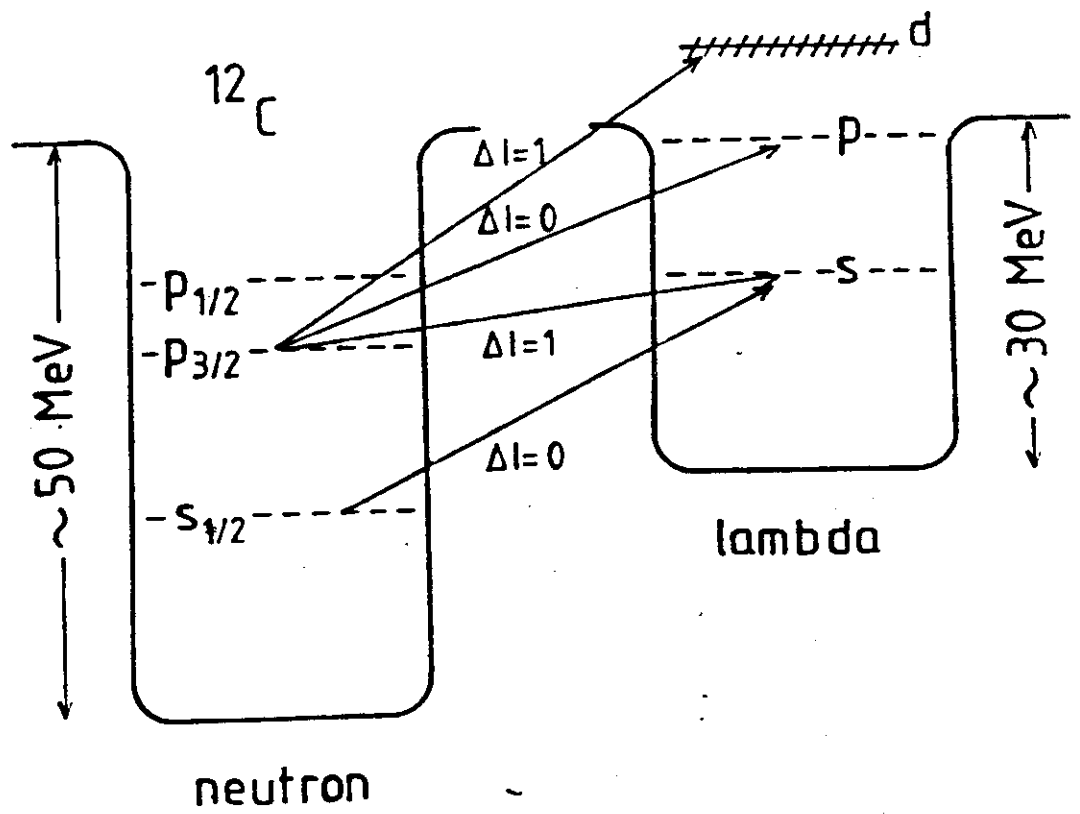
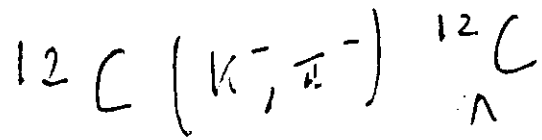






H. Bawli et al. Int. J. Mod. Phys.
to be pub.





$$\Gamma_{ph} = \Gamma_p \times \Gamma_h$$

$$E_K - E_\pi = M_{HY} - M_A + \cancel{F}_{HY}$$

$$T_{HY} \approx \frac{q^2}{2M_H}$$

$$= M_C + M_{\Lambda\Sigma} - B_{\Lambda\Sigma} - M_A$$

$$= \cancel{M}_C + M_{\Lambda\Sigma} - B_{\Lambda\Sigma} - (\cancel{M}_C + M_{\pi\tau} - B_{\pi\tau})$$

$$= M_{\Lambda\Sigma} - M_{\pi\tau} - (B_{\Lambda\Sigma} - B_{\pi\tau})$$

$$\downarrow$$

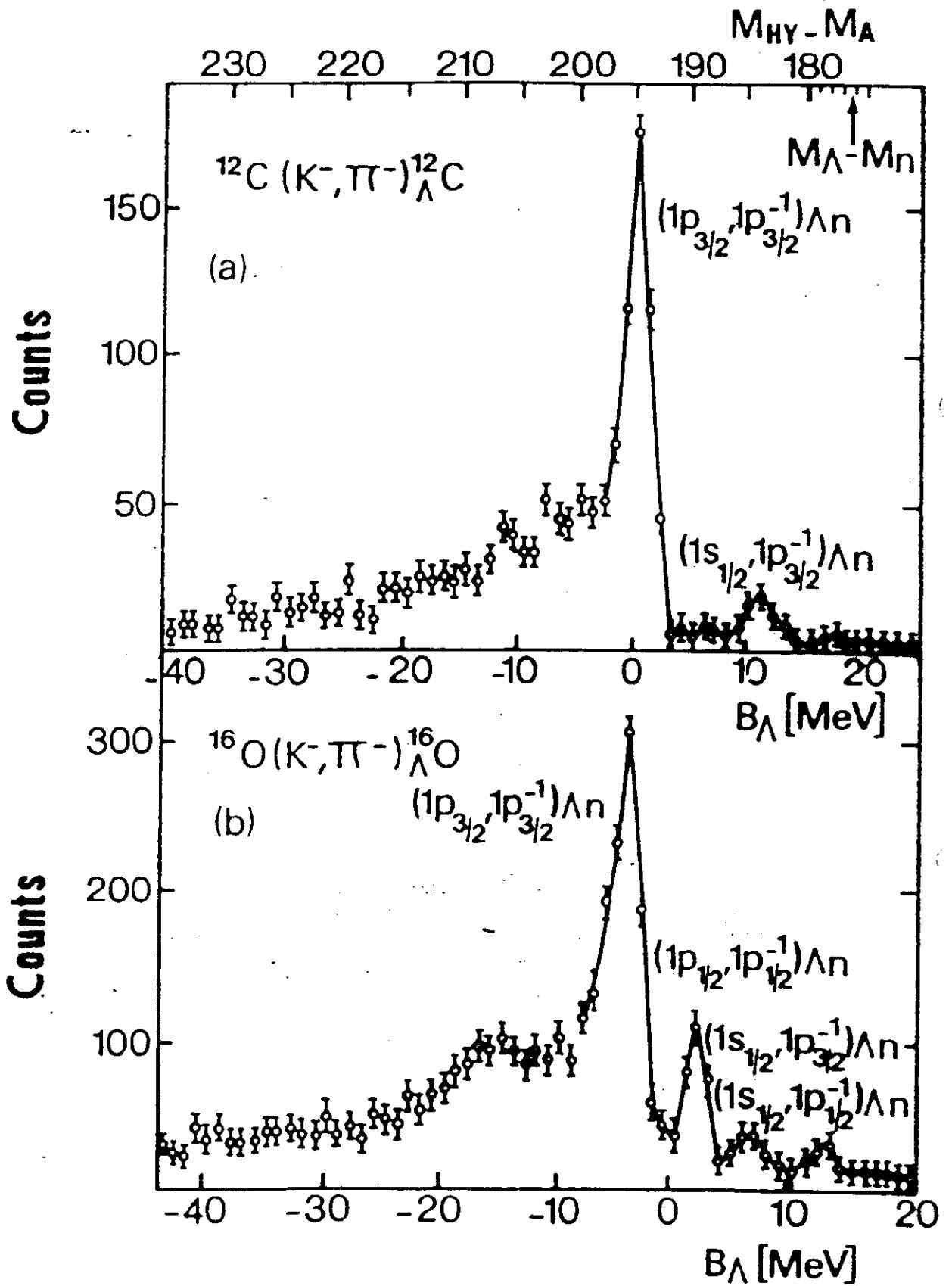
$$- \Delta B_{\pi\Lambda\Sigma}$$

$$\Delta B_{\pi\Lambda\Sigma} = M_{HY} - M_A - (M_{\Lambda\Sigma} - M_{\pi\tau})$$

$$\downarrow$$

$$E_K - E_\pi$$

$$p_{K^-} = 720 \text{ MeV}/c$$



W. Brückner et al. P.L. 79 B (1978) 157

Potential $V(r)$

Central

$$V(r) = -V_0 f(r)$$

$$f(r) = (1 + \exp(r-R)/a)$$

$$R = r_0 A^{1/3} \quad r_0 = 1.1 \text{ fm}$$

$$a = .6 \text{ fm.}$$

Spin orbit term

$$V_{LS} \vec{l} \cdot \vec{s} \left(\frac{\hbar}{m_{\pi} c} \right)^2 \frac{1}{r} \frac{df(r)}{dr}$$

+ Lame term

$$(V_1/A) \vec{l} \cdot \vec{T}_{A-1}$$

but

$$\boxed{\text{residual}} V_{YN} \boxed{\text{residual}}$$

interaction

Quasi free

No momentum limitation due to Pauli principle

$$-k_F \leq k \leq +k_F$$

$$\omega = M_\Lambda - U_\Lambda + (k+q)^2 / 2M_\Lambda - [M_N - U_N + k^2 / 2M_N] = E_k - E_{\bar{u}}$$

$$\omega = M_\Lambda - U_\Lambda + (U_N - M_N) + \frac{q^2}{2M_\Lambda} + \frac{k_3 q}{M_\Lambda} + \frac{k^2}{2M_\Lambda M_N} (M_N - M_\Lambda)$$

but $k^2 \approx \frac{k_F^2}{2}$

$$\omega = M_\Lambda - M_N + (U_N - U_\Lambda) + \frac{q^2}{2M_\Lambda} + \frac{k_3 q}{M_\Lambda} + \frac{M_N^2}{2M_\Lambda M_N} (M_N - M_\Lambda)$$

if $k_3 = 0$

$$\frac{dN}{dk_3} = \frac{3}{4k_F} \left(1 - \frac{k_3^2}{k_F^2} \right)$$

$$\frac{dN}{d\omega} = \frac{dN}{dk_3} \frac{dk_3}{d\omega} = \frac{dN}{dk_3} \frac{M_\Lambda}{q} = \frac{M_\Lambda}{q} \frac{3}{4k_F} \left(1 - \frac{k_3^2}{k_F^2} \right)$$

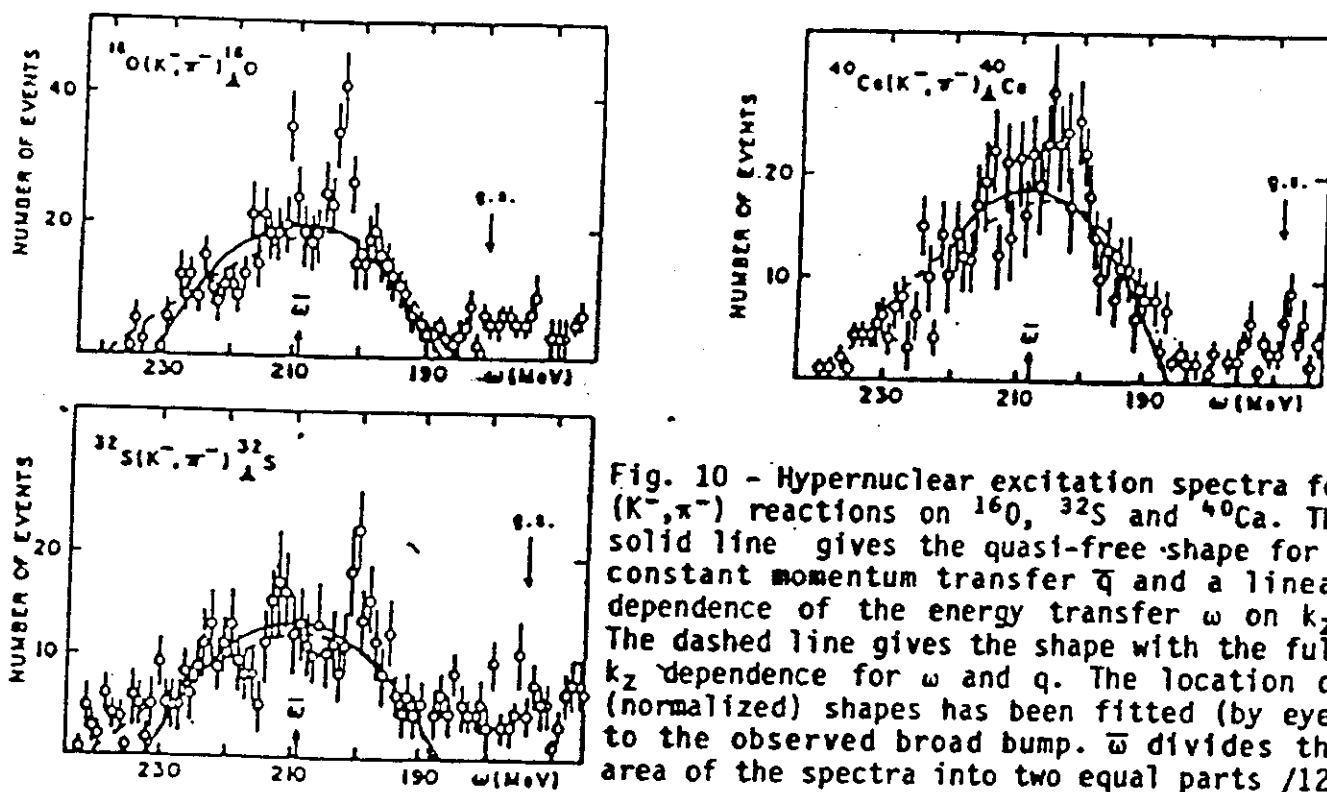
but $\omega - \bar{\omega} = \frac{k_3 q}{M_\Lambda} \rightarrow k_3 = (\omega - \bar{\omega}) \frac{M_\Lambda}{q}$

$$\frac{dN}{d\omega} = \frac{3}{4} \frac{M_\Lambda}{q k_F} \left(1 - \frac{M_\Lambda^2}{q^2 k_F^2} (\omega - \bar{\omega})^2 \right)$$

$$p_K \approx 900 \text{ MeV}/c$$

W. Brückner et al.
Phys. Lett. 62B (1976) 481

R. H. Dalitz and
A. Gal
Phys. Lett. 64B (1976)
154



↓

$$V_0^{\wedge} \approx 30 \text{ MeV}$$

$$V_{\Lambda N}(r_{\Lambda} - r_N) = V(r_{\Lambda} - r_N) (1 - \epsilon' + \epsilon' P_x)$$

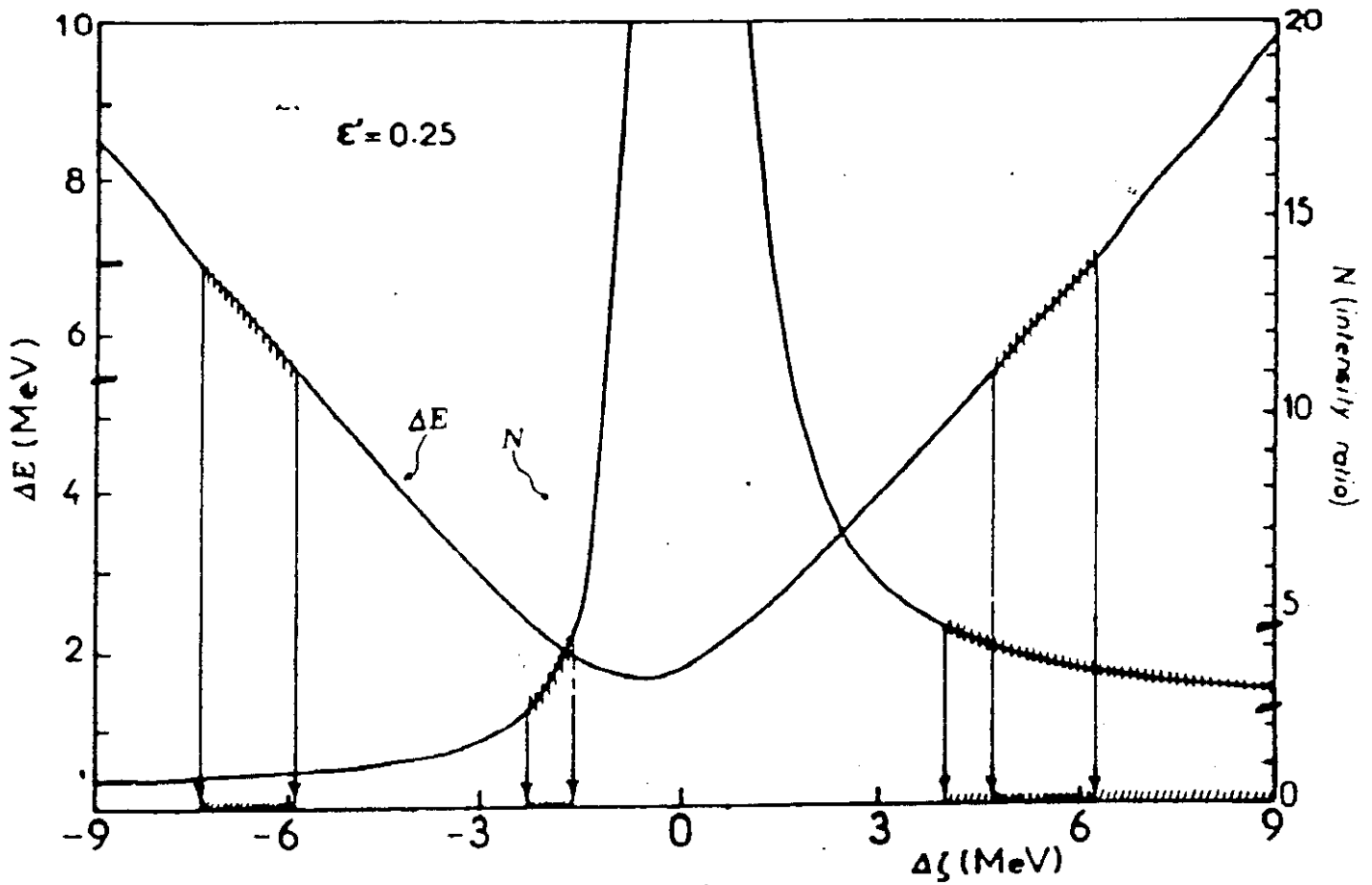
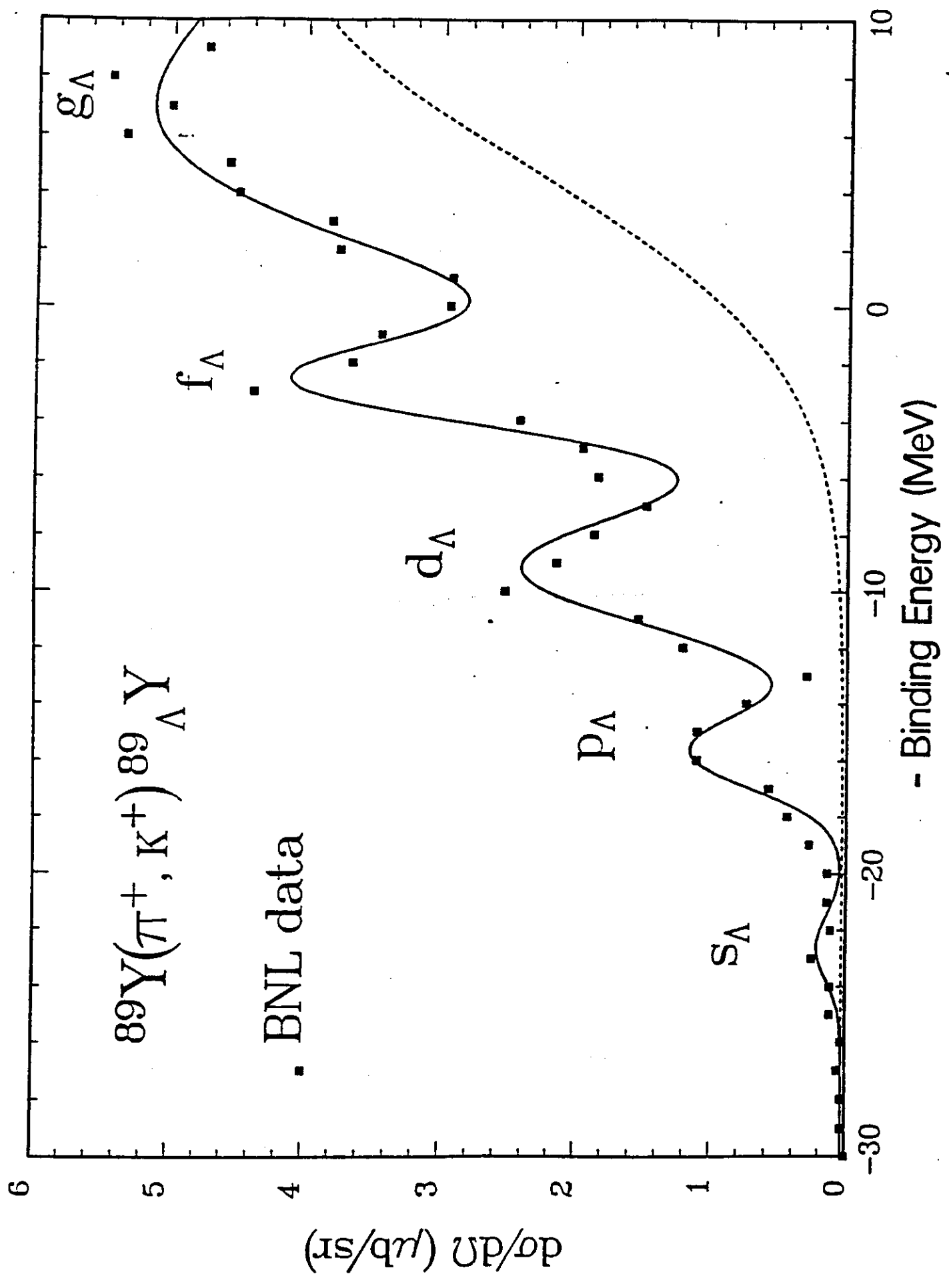


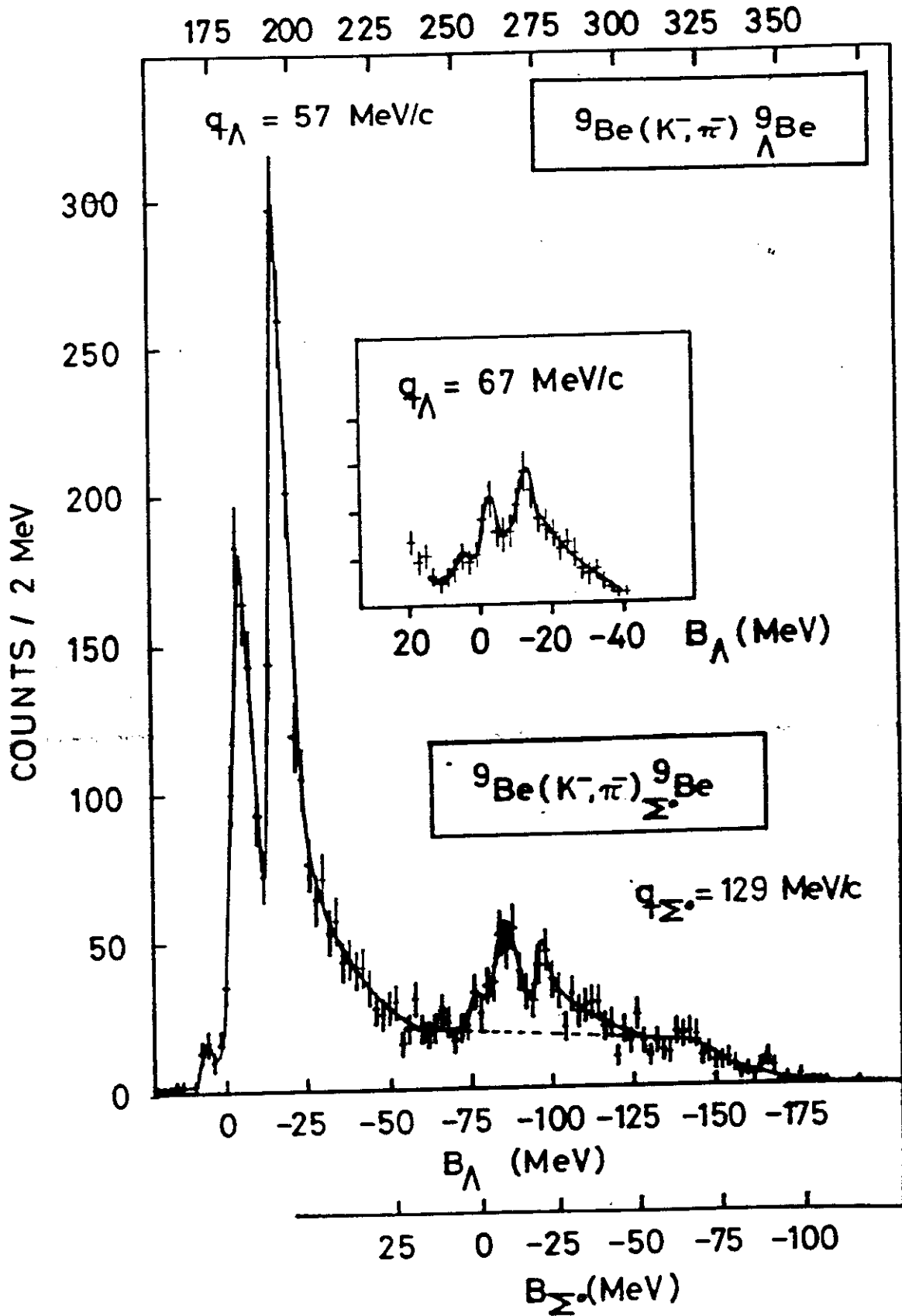
Fig. 1. Separation energy (on the left scale) and intensity ratio (on the right scale) as functions of the spin-orbit difference. The solid line corresponds to the gaussian interaction with a range $\mu = 1.04$ fm. The experimental and theoretical uncertainties on ΔE ($5.5 < \Delta E < 7$) and on N ($2.5 < N < 4.5$) impose constraints on $\Delta\zeta$ (indicated by slashes). The overlap (if any) gives the value of the spin-orbit difference. A value $\epsilon' = 0.25$ has been taken for the exchange mixture parameter.

A. Bouyssy P.L. 91 B (1980) 15



$$p_K = 720 \text{ MeV}/c$$

$$M_{HY} - M_A \text{ (MeV)}$$



R. Bertini et al.

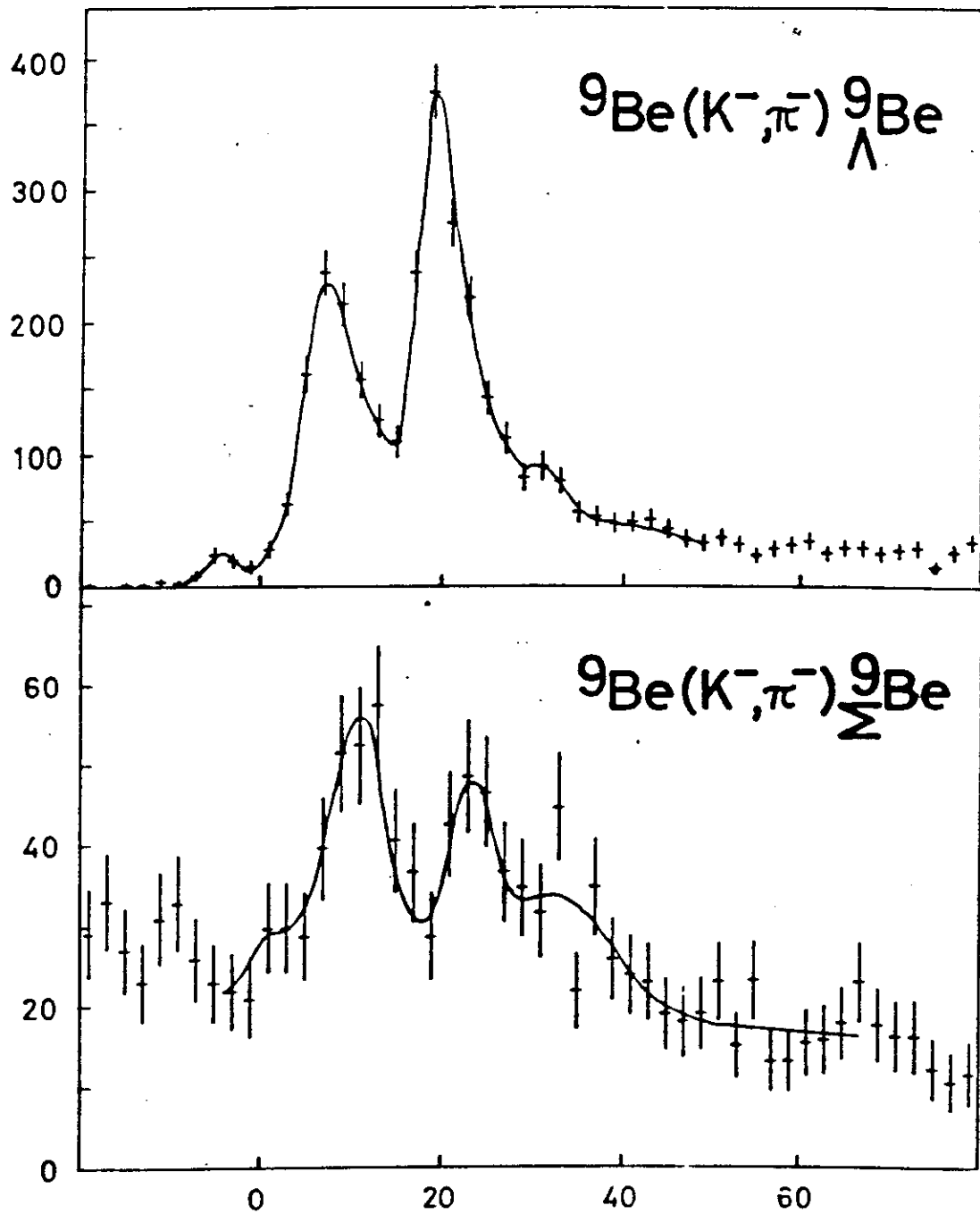
Phys. Lett. 90 B (1982) 320

Hyp ($S = -1$)	Mass (MeV)	I	J^P	τ (sec.) / Γ (MeV)	Mode	%
Λ	1115.6	0	$1/2^+$	$2.6 \cdot 10^{-10}$ $4.1 \cdot 10^{-12}$	$p\pi^-$ $n\pi^0$	64. 36.
Σ^+	1189.4	1	$1/2^+$	$.8 \cdot 10^{-10}$ $8.2 \cdot 10^{-12}$	$p\pi^0$ $n\pi^+$	52. 48.
Σ^0	1192.5	1	$1/2^+$	$7.4 \cdot 10^{-21}$ $8.9 \cdot 10^{-3}$	$\Lambda\gamma$	100.
Σ^-	1197.4	1	$1/2^+$	$1.5 \cdot 10^{-10}$ $4.4 \cdot 10^{-12}$	$n\pi^-$	100.

but in the nuclear matter



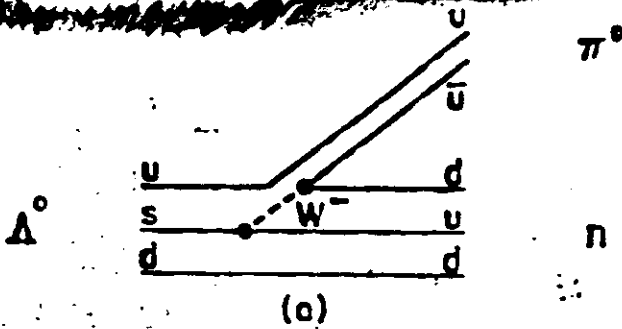
COUNTS / 2 MeV



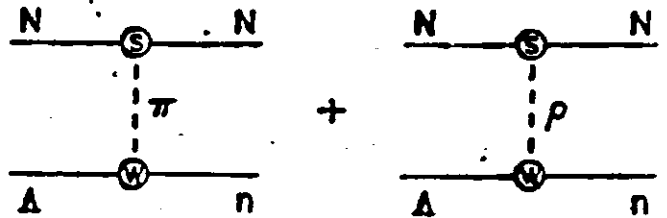
$$\Delta B_{NY} = M_{YA} - M_A - (M_Y - M_N) = B_N - B_Y$$

NONLEPTONIC WEAK INTERACTIONS

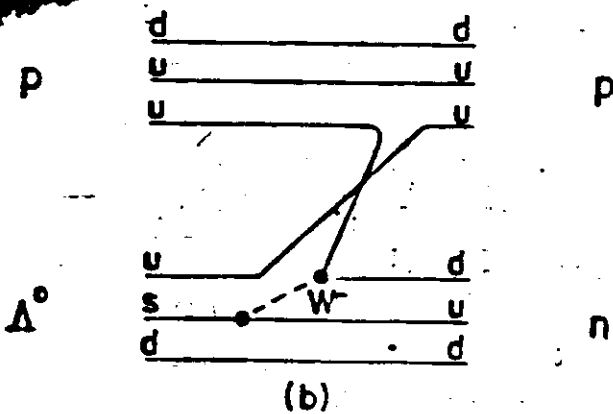
MESONIC $\Lambda^0 \rightarrow n + \pi^0$



MESON Exchange Calculations



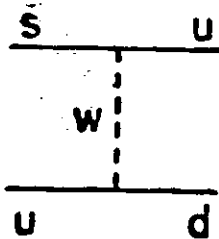
NONMESONIC $\Lambda + p \rightarrow n + p$



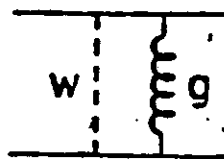
$$H_{VA} = \frac{G_F}{\sqrt{2}} \sin \vartheta_c \cos \vartheta_c Q_{VA} + c.c.$$

" $\Delta I = \frac{1}{2}$ rule"

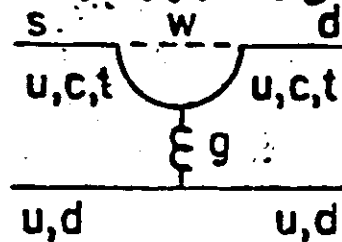
Strong interaction corrections



V-A interaction



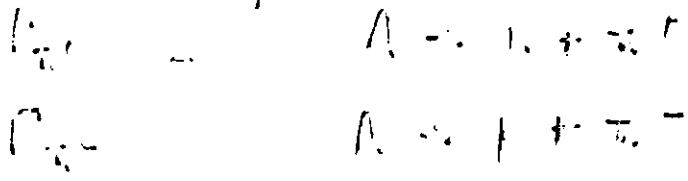
gluon radiative correction



Penguin diagram

Non leptonic decay rates

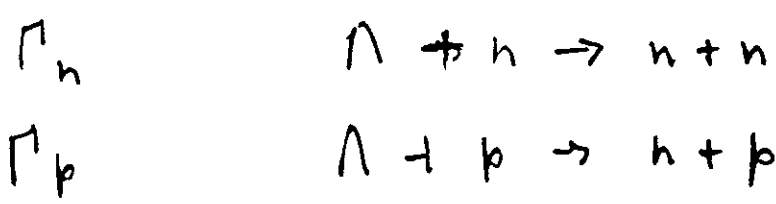
Mesonic decay



Energy release

$+20 \text{ MeV} - (m_{\pi^+} + m_{\pi^0})$

Non mesonic decay



$+176 \text{ MeV} - (B_{\Lambda} + B_N)$

- $\Gamma_p = .49^{+0.3}_{-0.2} \quad) \quad \Gamma_{\Lambda}$
- $\Gamma_n = .65^{+0.2}_{-0.3} \quad) \quad \Gamma_{\Lambda}$
- $\Gamma_{\pi^+} = .05^{+0.06}_{-0.03} \quad) \quad \Gamma_{\Lambda}$
- $\Gamma_{\pi^0} = .06^{+0.08}_{-0.05} \quad) \quad \Gamma_{\Lambda}$

$\Gamma_{\Lambda} = \text{free } \Lambda$
decay rate

$\dots \pm 1.02$

$\Gamma_{\Lambda} = 2.11 \pm 0.31 \quad \Gamma' / \Gamma_{\Lambda} = 1.25 \pm 0.18$

$\Gamma' = \Gamma_{\pi^+} + \Gamma_{\pi^0} + \Gamma_n + \Gamma_p$

$^{11}\text{B}_6$
AA

$$R_{AA} = 17.7 \pm 1 \text{ Mu.}$$

$^{11}\text{B}_6$
AA

$$R_{AA} = 17.7 \pm 1 \text{ Mu.}$$

↓ ↓ ↓

H particles

K^-, K^+ reaction

$S=0$ Resonances

$I=1/2$ nucleon resonances N^*

$I=3/2$ Δ resonances

$\Gamma \approx 100 - 200 \text{ MeV}$

$S=-1$ Resonances

$I=0$ Λ resonances

$I=1$ Σ resonances

$\Gamma \approx 15 - 60 \text{ MeV}$

$S'=-2$ Resonances

$I=1/2$ Ξ resonances

$\Gamma \approx 10 - 20 \text{ MeV}$

Hyperon Level Scheme

$$\frac{3}{2}^- \overline{\Sigma(1820)} \quad \Gamma = 26 \text{ MeV}$$

$$\frac{1}{2}^- \overline{\Lambda(1670)} \quad \Gamma = 40 \text{ MeV}$$

S_{01}

$$\frac{3}{2}^- \overline{\Sigma(1670)} \quad \Gamma = 57 \text{ MeV}$$

D_{13}

$$\frac{1}{2}^- \overline{\Lambda(1520)} \quad \Gamma = 16 \text{ MeV}$$

D_{03}

$$\frac{3}{2}^+ \overline{\Sigma(1530)} \quad \Gamma = 21 \text{ MeV}$$

P_{13}

KN threshold

$$\frac{1}{2}^- \overline{\Lambda(1405)} \quad \Gamma = 40 \text{ MeV}$$

S_{01}

$$\frac{3}{2}^+ \overline{\Sigma(1385)} \quad \Gamma = 35 \text{ MeV}$$

P_{13}

$$\frac{1}{2}^+ \overline{\Sigma(1315)}$$

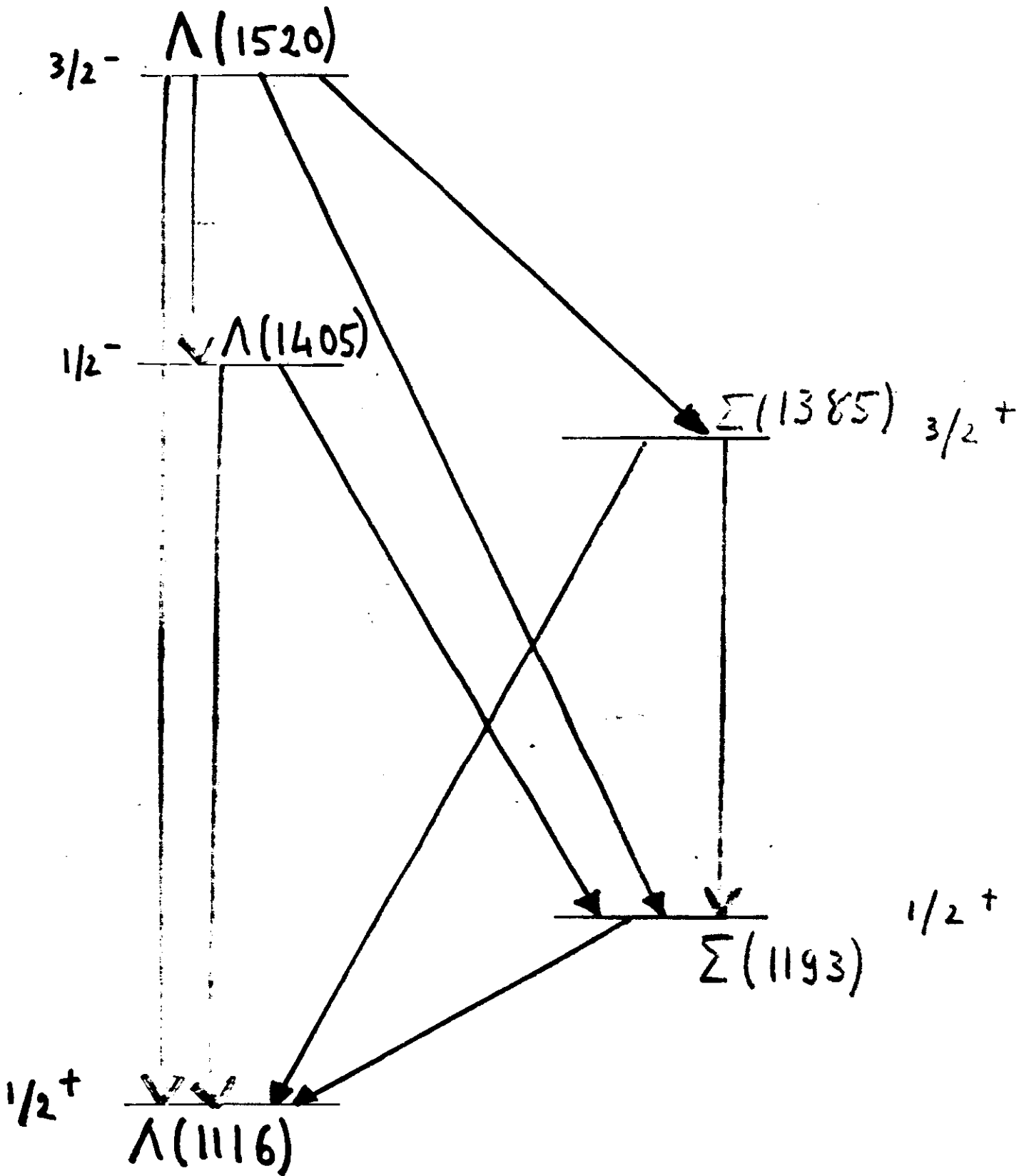
$$\frac{1}{2}^+ \overline{\Sigma(1192)}$$

$$\frac{1}{2}^+ \overline{\Lambda(1116)}$$

$$I=0, S=-1$$

$$I=1, S=-1$$

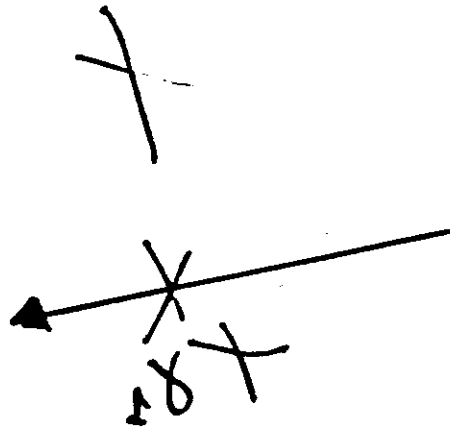
$$I=1/2, S=-2$$



↑ 2
↑ 1
↑ 1

$$s/p_2 = \left[\begin{matrix} \downarrow (1) \\ 0=I, 0=2 \end{matrix} \right]$$

$$s_2 = \left[\begin{matrix} \downarrow (1) \\ 1=I, 1=2 \end{matrix} \right]$$



$$s/p_2 = \left[\begin{matrix} \downarrow (1) \\ 0=I, 0=2 \end{matrix} \right]$$

$$V \pm N \pm 1 \pm 1 = (M \pm 1) \pm 1$$

$$2 = \left[\begin{matrix} \uparrow (1) \\ 1=I, 1=2 \end{matrix} \right] \frac{5}{2} + \left[\begin{matrix} \downarrow (1) \\ 1=I, 0=2 \end{matrix} \right] \frac{1}{2}$$

$$M \pm 1 \pm 1 \pm 1 = 11 \pm 3 \pm 1 \pm 1$$

$$s_2 = \left[\begin{matrix} \downarrow (1) \\ 0=I, 0=2 \end{matrix} \right]$$

$$\sigma_{\text{tot}} = 4\pi \lambda^2 (J + 1/2) \alpha_c$$

$$\alpha_c = \frac{\Gamma_{el}}{\Gamma} = .45$$

$$\sigma_{\gamma} = 4\pi \lambda^2 \cdot \alpha_c \cdot (J + 1/2) \frac{\Gamma_{\gamma}}{\Gamma} = 74 \cdot \frac{\Gamma_{\gamma}}{\Gamma}$$

E.W. correction = .5 \rightarrow $\sigma_{\text{eff}} = 57 \text{ mb.}$

$$\frac{d\sigma_{\text{eff}}}{d\Omega} = \frac{57}{4\pi} = 2.94 \text{ mb/sr.}$$

$$V_{\gamma}^c = N_k \times D_{\text{Time}} \times \Delta \Omega_{\gamma} \times \epsilon_{NaI} \times \sigma_{\text{eff}} \times \frac{\Gamma_{\gamma}}{\Gamma} \times N_{\text{Tag.}} \times \epsilon_{\text{KCl}} \times \Delta \Omega_{\text{KCl}}$$

$$= 3.5 \cdot 10^8 \times .9 \times 5.8 \cdot 10^{-2} \times .70 \times 2.9 \cdot 10^{-27} \times \frac{\Gamma_{\gamma}}{\Gamma} \times 7.7 \cdot 10^{23} \times 1 \times 1$$

$$= 3.0 \cdot 10^4 \frac{\Gamma_{\gamma}}{\Gamma}$$

$$V_{\gamma_0}^c = 63 \pm 20$$

$$N_{\gamma_2}^c = 90 \pm 32$$

\downarrow

$$\Gamma_{\gamma_0}^c = 33 \pm 11 \text{ KEV}$$

\downarrow

$$\Gamma_{\gamma_2}^c = 47 \pm 17 \text{ KEV}$$

$$\frac{\Gamma_{\gamma_2}}{\Gamma_{\gamma_0}} = 1.4 \pm .7$$

exp. Value

$$\frac{\Gamma_{\gamma_2}}{\Gamma_{\gamma_0}} = 3.8$$

$$\leftrightarrow \frac{\Gamma_{\gamma_2}}{\Gamma_{\gamma_0}} = .37$$

$$\frac{\Gamma_{\gamma_2}}{\Gamma_{\gamma_0}} = .8$$

Resonance propagation in nuclei

Free space no Fermi
motion !

$$d_{\Delta} = v t \approx \frac{p_{\Delta}}{m_{\Delta} \Gamma_{\Delta}} \approx 5 \text{ fm}$$

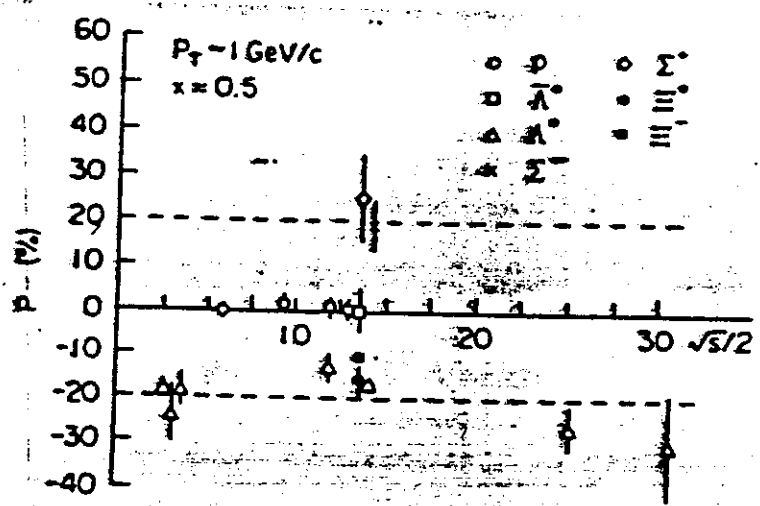
$$d_{\Lambda(1520)} = v t \approx \frac{p_{\Lambda}}{m_{\Lambda} \Gamma_{\Lambda}} \approx 6 \text{ fm}$$

Decay modes :

$$\Lambda(1520) \rightarrow \begin{cases} \bar{K} N & 45\% & \pm 1 \\ \pi \Sigma & 42\% & \pm 1 \\ \Lambda \bar{u} \bar{u} & 10\% & \pm 1 \\ \bar{\Sigma} \pi \pi & 9\% & \pm 1 \end{cases}$$

Hyperon Polarisation

Reaction $p + A \rightarrow \bar{Y}$



- Regularities:
- Λ , Σ and Ξ are polarized for $p_T >$
 - P_Λ has opposite sign to P_Σ
 - $P_{\bar{\Lambda}}$ always $= 0$ but $P_{\bar{\Lambda}} \neq 0$ for the reaction $\bar{p} + A \rightarrow \bar{\Lambda}$



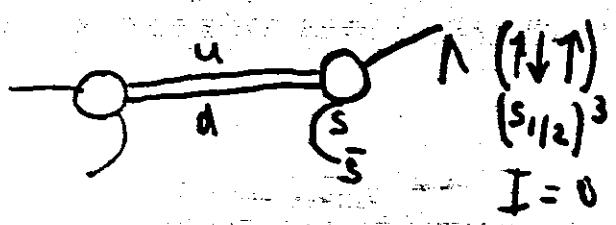
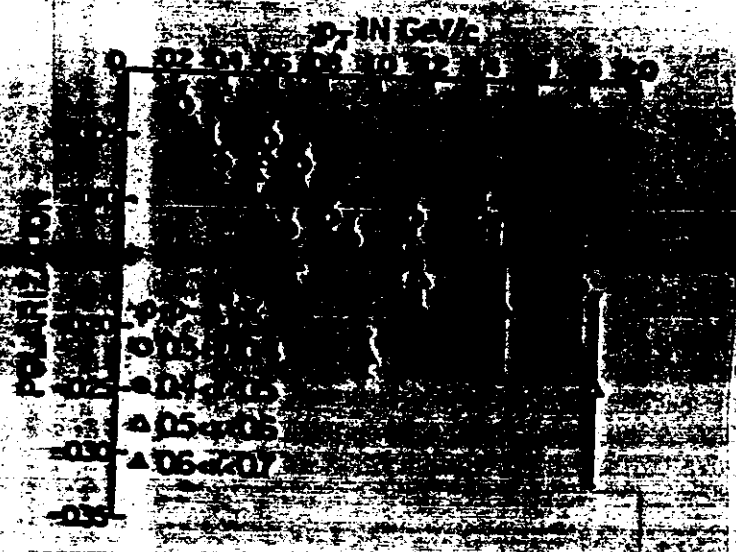
When 1 or 2 squarks are picked up from the quark sea $P_y \neq 0$ when 3 $P_y = 0$



Question: why $P_y \neq 0$ if squark picked up from sea



Models ad hoc: QFRC
 Ex. $p \rightarrow \bar{\Lambda}$ VVS
 $uds \rightarrow uds$



For p_T large $p_T \approx \underbrace{q_T}_{\text{diquark}} + \underbrace{k_T}_{\text{squark}}$

In this framework: there should not be a correlation between the spin direction of the incoming proton and the spin of the Λ
 there should be a correlation between the spin direction of the incoming proton and the spin of the

With the inclusive reaction $p + A \rightarrow \Lambda$ problems:

1) $p \rightarrow \Lambda$ directly
but also
 $p \rightarrow \Sigma^+ \Lambda$

2) measurements performed at forward angles only
 $\theta_{\Lambda} \leq 10^\circ$ usually

AE Saturated!

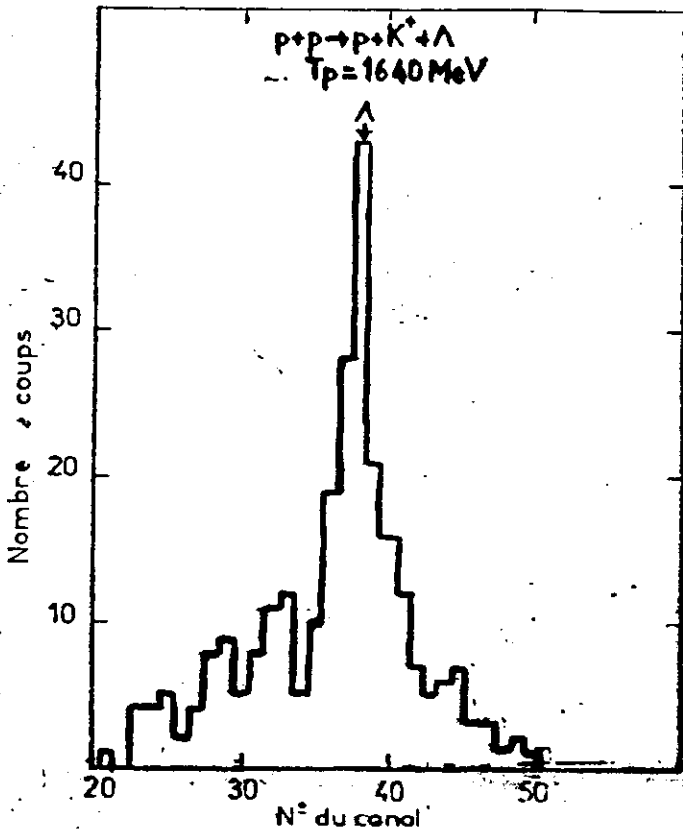
$pp \rightarrow p k^+ \Lambda$ exclusive
 $\rightarrow p \pi^- \alpha = -0.64$
choose the right angle θ_{Λ}
for same p_T

Also possible:

$pp \rightarrow p k^+ \Sigma^0 \Lambda$

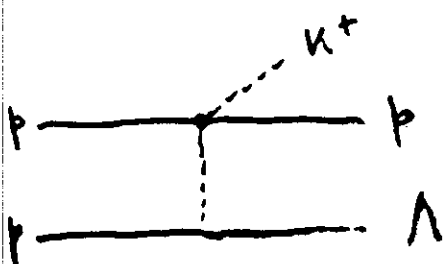
$pp \rightarrow k^+ n \Sigma^+ \Lambda$
 $k^0 p \rightarrow p \pi^0 \alpha = -0.98$

$pp \rightarrow p k^+ \Sigma^- \Lambda$

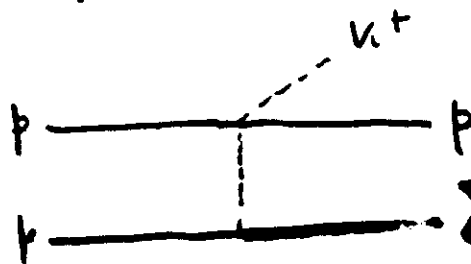


Measurement of spin correlation parameters

Comparison with OBEM



$$\frac{G_{\Lambda}^2}{4\pi}$$



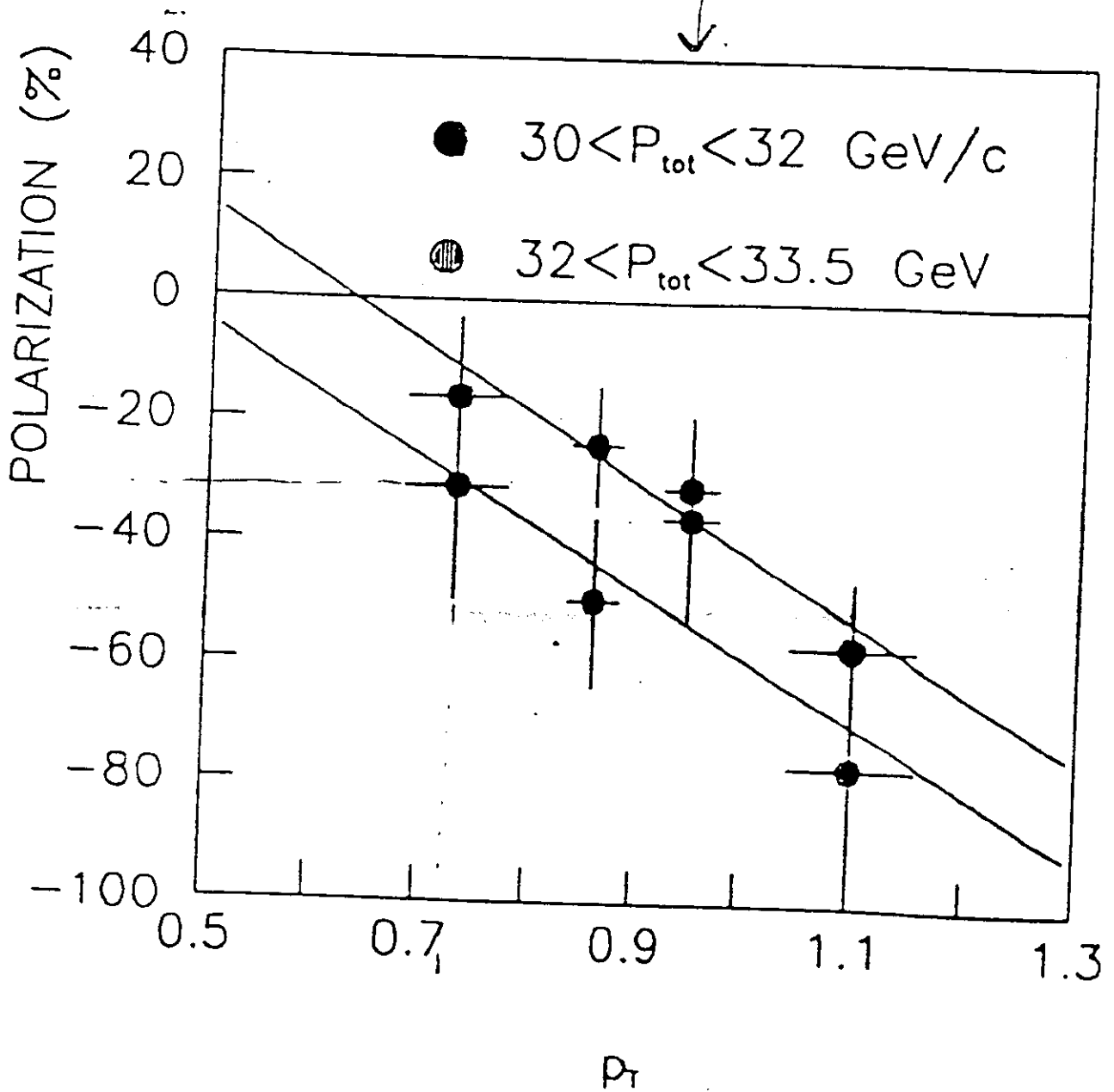
$$\frac{G_{\Sigma}^2}{4\pi} \sim 5$$

$\Sigma^0 (\Sigma^+)$

Laget calculations

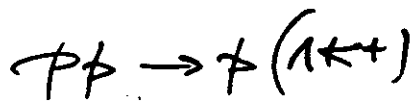


$$2.1 \leq M_{\Lambda K^+} \leq 2.5$$



[PRELIMINARY RESULTS]

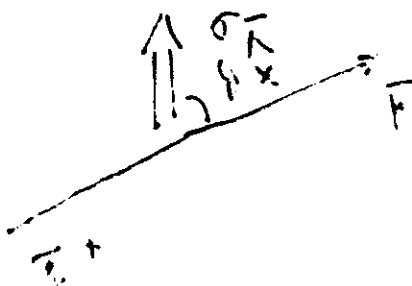
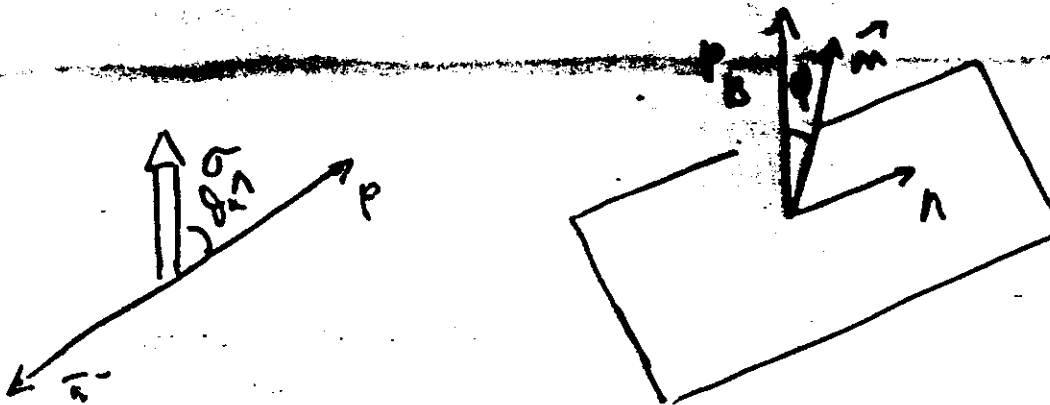
CERN ISR $\rightarrow \sqrt{s} = 63 \text{ GeV}$
(R608)



$$A_N = \frac{1}{P_B \cos \psi} \frac{N^\uparrow(\psi) - N^\downarrow(\psi)}{N^\uparrow(\psi) + N^\downarrow(\psi)}$$

$$D_{NN} = \frac{1}{P_B \cos \psi} [P_\Lambda^\uparrow - P_\Lambda^\downarrow]$$

$$\frac{dN}{d\cos\theta^x} = N_0 (1 + \alpha P_\Lambda \cos\theta^x)$$



$$p \rightarrow p(k^+ \Lambda) N^* \rightarrow p \bar{u}^-$$

$$p \rightarrow p(k^+ \Sigma^0) N^* \rightarrow p \bar{u}^-$$

$$p \rightarrow p k^+ \Lambda^*$$

$$p \rightarrow p k^+ \Lambda^* \rightarrow p \Lambda^* \rightarrow p \Sigma^*$$

$$p \rightarrow p k^+ \Sigma^*$$

Nuclei

$$p A \rightarrow p k^+ \Lambda^* X$$

$$\rightarrow p k^- \Lambda^* \rightarrow p \Sigma^*$$

$$p A \rightarrow p k^+ \Sigma^0 X$$

$$V(r) = V_0(r) + s.o. + L.T. + r.i$$

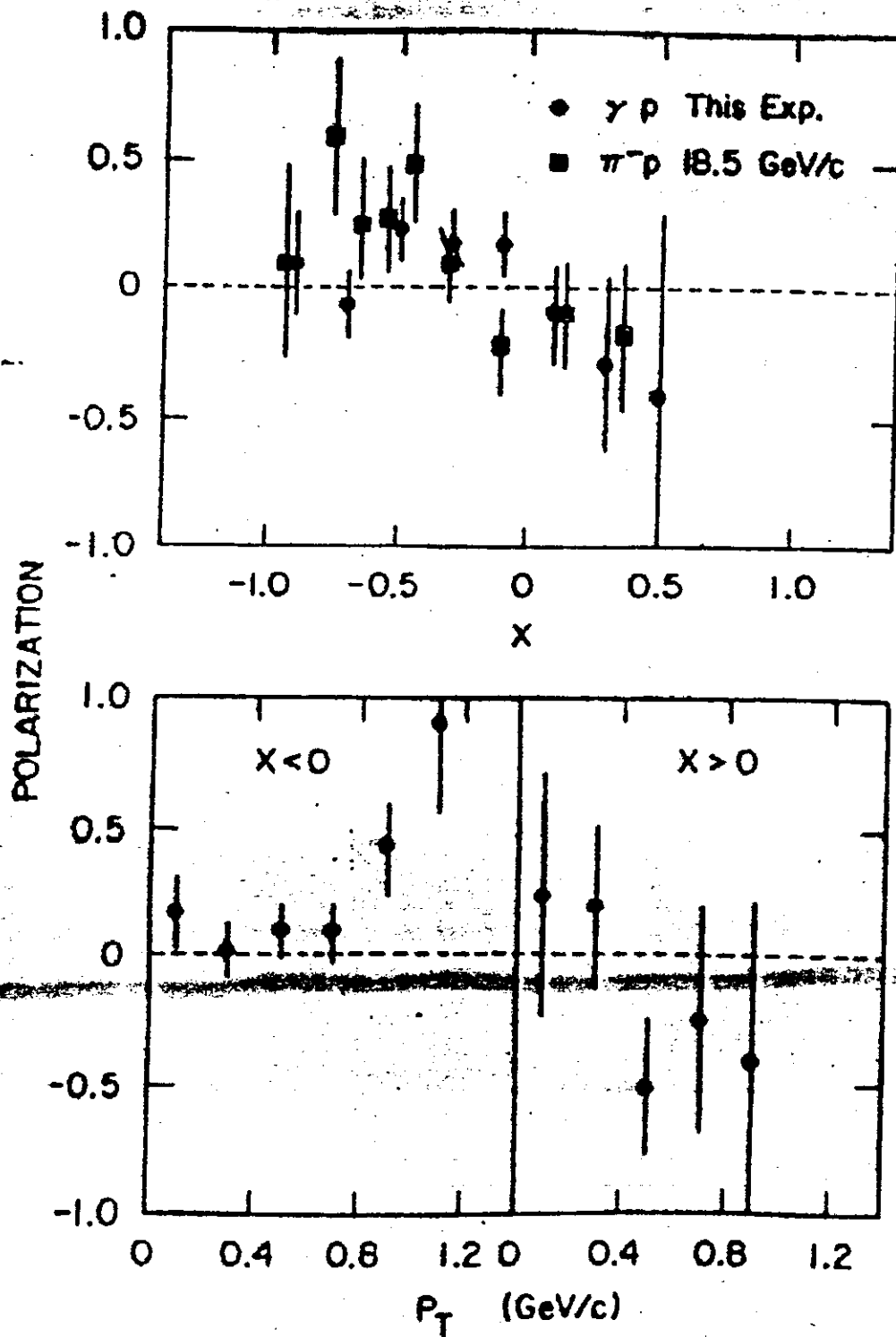


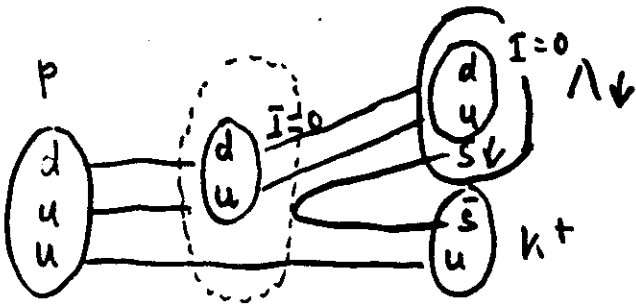
FIG. 8. Average polarization of Λ 's as a function of x and p_T . The open square points are from Ref. 1.

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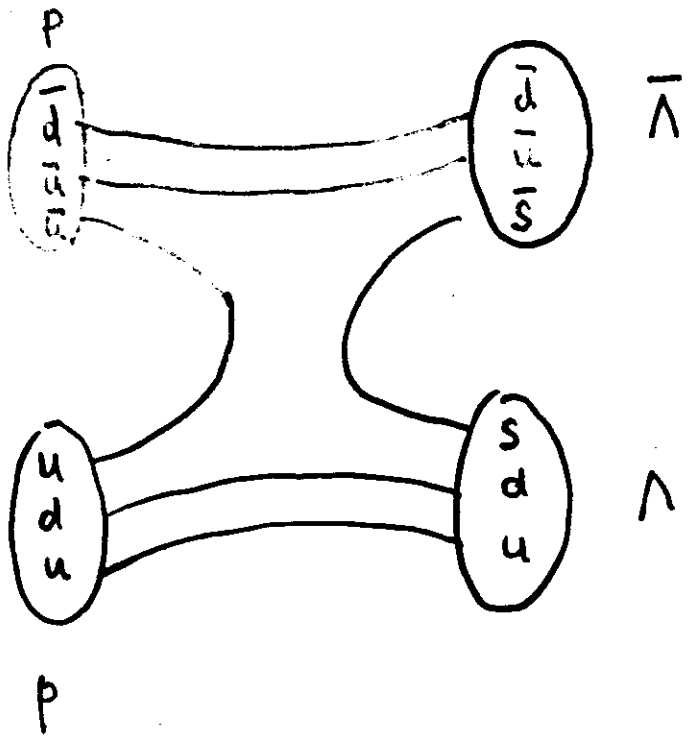
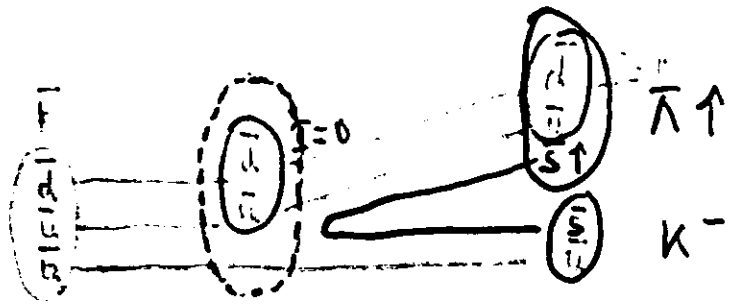
Phys. Rev. D 29(1984) 1877

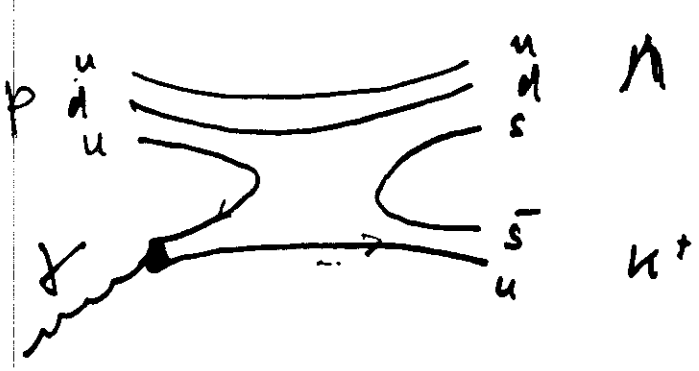
Strangeness

$N-N$



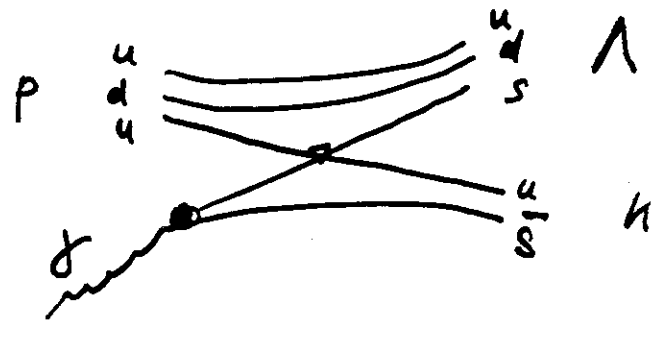
$\bar{N}N$





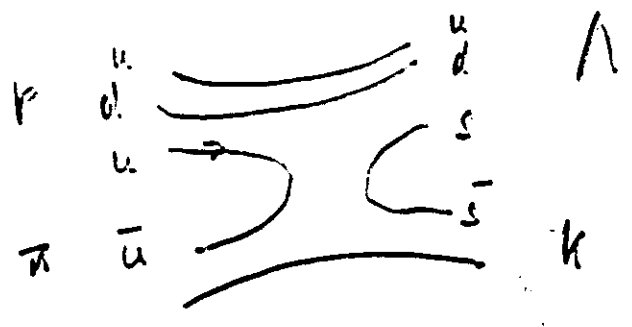
Λ

k^+



Λ

k



Λ

k



Λ

k

