



INTERNATIONAL ATOMIC ENERGY AGENCY  
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION



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SPRING COLLEGE IN CONDENSED MATTER  
ON  
"THE INTERACTION OF ATOMS & MOLECULES WITH SOLID SURFACES"  
(25 April - 17 June 1988)

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THE KINETICS AND DYNAMICS OF  
GAS-SURFACE PROCESSES  
(Lecture II)

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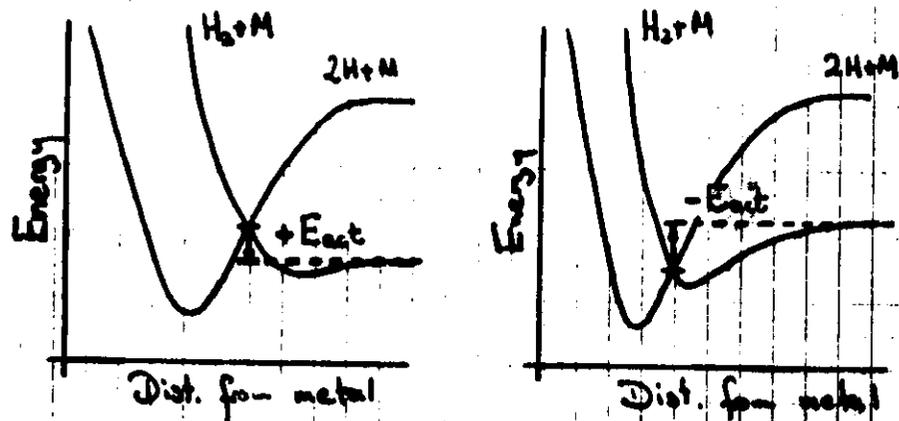
These are preliminary lecture notes, intended only for distribution to participants.

H<sub>2</sub> - Metal Interaction

Pre-history (pre 1960)

Experimental studies on powders.  
Adsorption rates measured on Ni, Cu, ...

Lennard Jones model

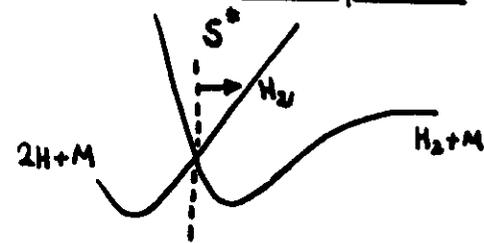


'Activated desorption'      'Non-activated'

Assuming TST to hold, what would the products look like for each of these cases?

Compa + David, Surf. Sci. Rpt. 5  
(1985)

(i) Non-activated desorption



Molecules leave surface with equilibrium distribution at T<sub>s</sub>,

$$p(v)dv \sim v^2 \cos \theta e^{-\frac{mv^2}{2kT}} dv$$

# of molecules / sec / unit solid  $\Delta$  between  $v, v+dv$

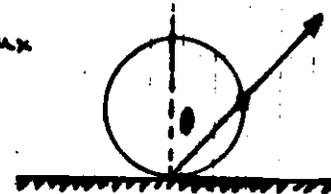
Angular dist<sup>n</sup> of emitted flux

$$N(\theta) \sim \cos \theta \quad [\text{Knudsen Law}]$$

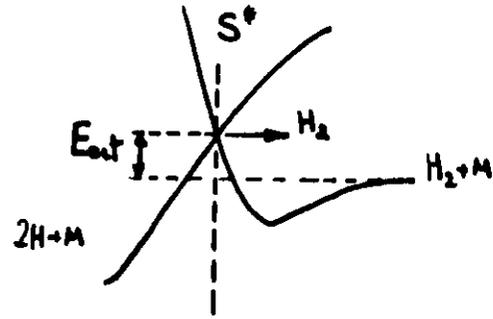
Mean energy of emitted flux in  $\theta$

$$\langle\langle E(\theta) \rangle\rangle = 2kT_s$$

Desorbing flux  
'Cos  $\theta$ '



(ii) Activated desorption



If  $\frac{1}{2} M v^2 = E_{act}$  then,

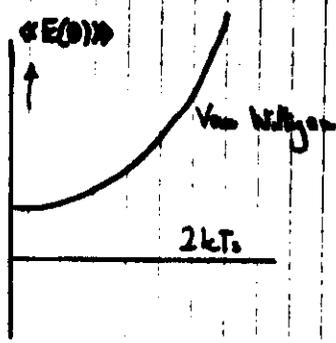
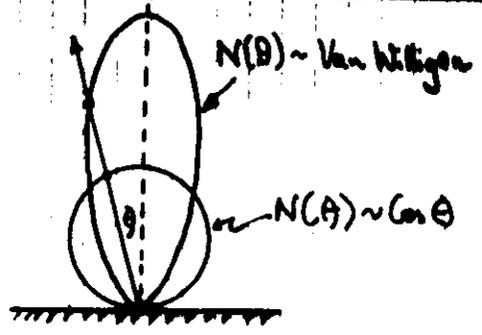
$$P(v) dv \sim v^3 \cos \theta e^{-\beta(\frac{1}{2} M v^2 - E_{act})} \Theta [v \cos \theta - v^*] dv$$

Angular dist<sup>n</sup>

$$N(\theta) \sim \left\{ \frac{E_{act} + kT_s \cos^2 \theta}{(E_{act} + kT_s) \cos \theta} \right\} e^{-\left\{ \left[ \frac{E_{act}}{kT_s} \right] \tan^2 \theta \right\}}$$

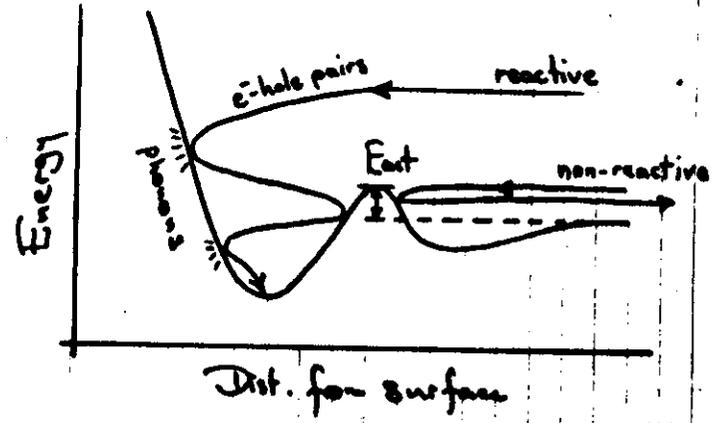
Mean energy

$$\langle\langle E(\theta) \rangle\rangle = 2kT_s \left[ 1 + \frac{1}{2} \left\{ \frac{E_{act}^2}{(E_{act} + kT_s) kT_s \cos^2 \theta} \right\} \right]$$

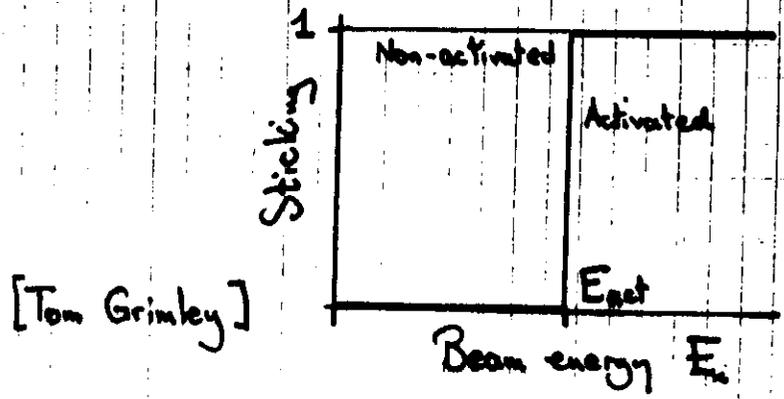


Adsorption

Let us suppose that energy transfer to the solid is super-efficient ( $\sigma=1$ ) "like a golf ball into a sand-trap"



In order to surmount the barrier the beam translational energy  $E_i > E_{act}$



[Tom Grimley]

Experimental work

Pre-history (0 → 1960)

Adsorption on powders and films.  
Irreproducible results.

$H_2$   $\left\{ \begin{array}{l} Cu - 0.1 eV \leq E_{act} \leq 1.5 eV \\ Ni - E_{act} \sim 0 eV \text{ or small!!} \end{array} \right.$

History (1960-1970)

Hydrogen found to dissociatively adsorb on Cu and Ni surfaces ( $\Delta\phi$ ).

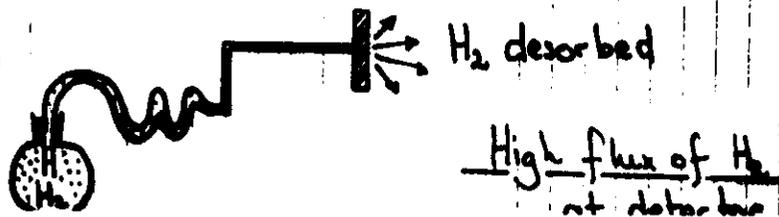
Cu -  $E_{act} \sim 0.5 eV$

Ni -  $E_{act} \sim 0.1 eV$

Experiments on evaporated films.

Pre-modern (1970-1980)

$H_2$  permeation technique exploited to study desorption



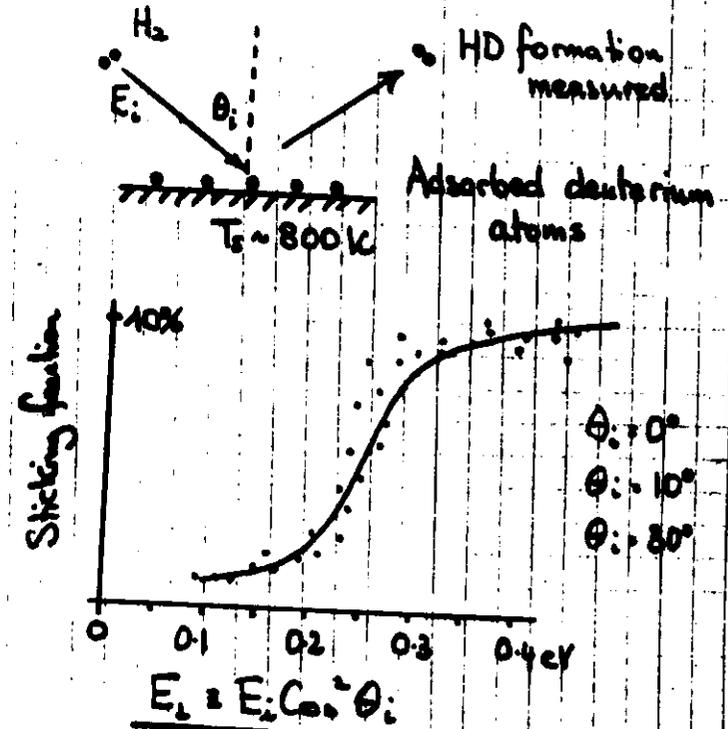
Balooch + Stickney

$H_2/Cu$

$N(\theta) \sim \cos^n \theta$  — no obvious reason for this

- $\Rightarrow Cu(100) \quad n=5 \quad E_{act} = 0.25 eV$
  - $\Rightarrow Cu(110) \quad n=2.5 \quad 0.1 eV$
  - $\Rightarrow Cu(111) \quad n=6 \quad 0.25 eV$
- } 1-D barrier

Balooch, Cardillo, Miller + Stickney



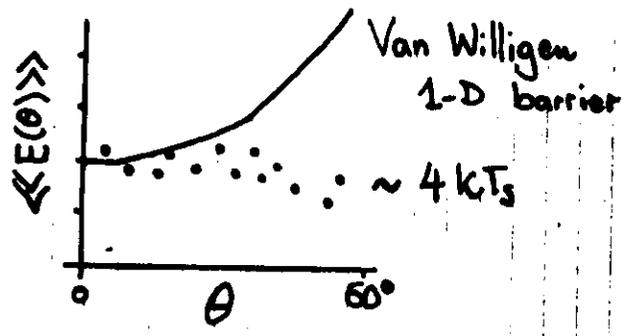
Normal energy scaling

2.7

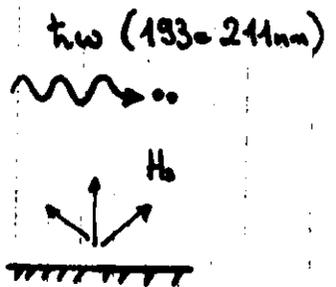
Modern (1980 - present)

Comsa + David

Permeation experiment to measure the velocity distribution of desorbing species  $f_n(\theta)$ .

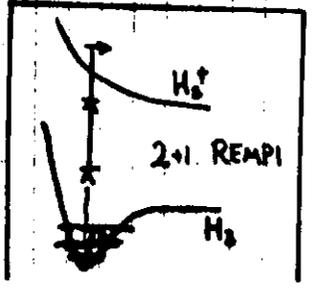


Kubiak, Sitz + Zare



Permeation of H<sub>2</sub> + D<sub>2</sub> through Cu(110) - (111).  
Measurement of vibrational and rotational distribution

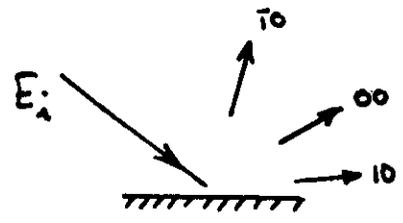
Vibrations:  $P_{v=1}/P_{v=0} \sim 90 \times \text{Boltz}$   
Rotations: Non Boltzmann  
 $\langle E_{rot} \rangle < kT_s$



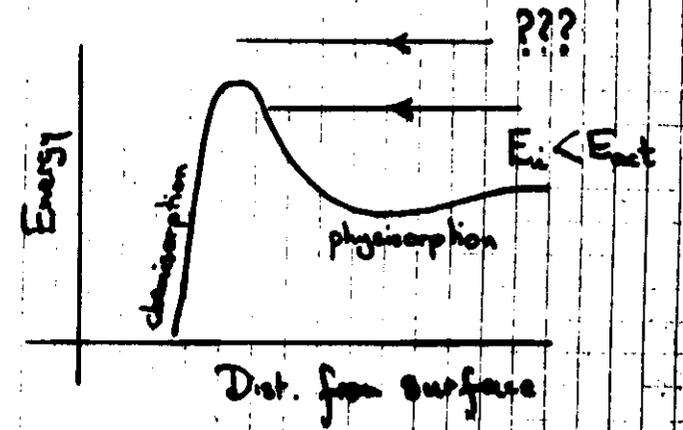
2.8

Lapujoulade + Perreau

Diffraction of H<sub>2</sub> and D<sub>2</sub> beams from Cu(110) surface.

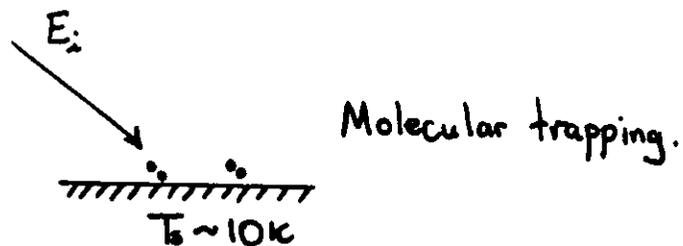


Attempting to find  $E_{act}$ , scan of diffraction with  $E_i$ :  
Nothing dramatic at 0.25eV!!

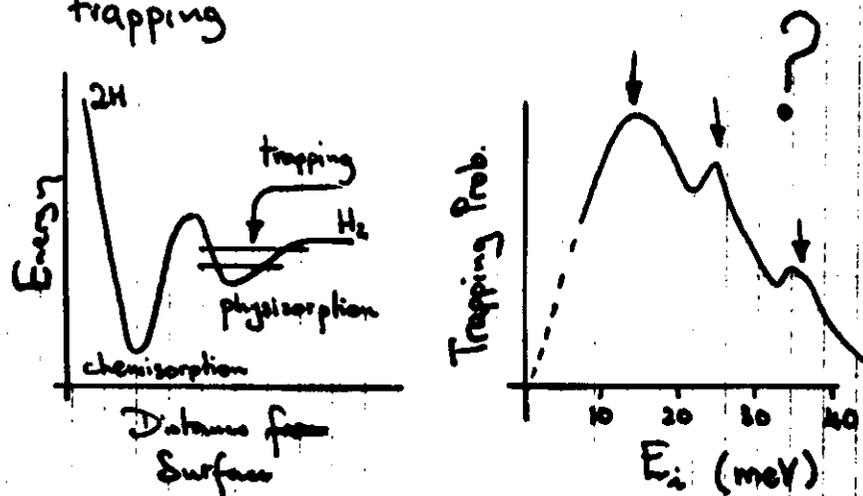


What is the nature of the barrier?

Andersson, Wilzén + Harris



In a scattering experiment, interesting resonances were observed in  $H_2$  trapping



They argued that these were not bound states of the static potential but many-body resonances.

(wip)

$H_2/Ni$

(111): Robota et al, Rendulic et al, Hayward + Taylor.

- >  $15 \leq E_{act} \leq 100$  meV
- > 'Normal' scaling of sticking not observed.
- > Strong diffraction observed at all energies.

(110): Robota et al, Rendulic et al, Hansen + Madix.

- >  $E_{int} = 0$  ! (or  $E_{int} > 34$  meV)
- > Diffraction observed
- >  $S_0 \sim 1$  (or  $0.2 \leq S_0 \leq 0.5$ )

(100): Rendulic et al, Hansen + Madix

- >  $0.1 \leq S_0 \leq 0.2$
- > Significant isotope effect  
 $S_0(H_2) > S_0(D_2)$  (opposite to results of Balogh et al on Cu)

# Theoretical Models for H<sub>2</sub>/Metal Potential Energy Surfaces.

(i) Semi-infinite [Fe-based]  
H<sub>2</sub>/Mg(001).

- > True, delocalised states on surface.
- > Exchange-correlation - LD: DFT
- > Substrate atoms included perturbatively

(ii) Cluster calculation  
H<sub>2</sub>/Cu or H<sub>2</sub>/Ni

- > "Surface" treated as a cluster of 2 atoms.
- > Exchange-correlation - LD: DFT
- > Substrate + adsorbate species treated on equal footing.

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ground. Lattice effects,  $\Delta E_H^L$ , are then accounted for by treating the difference  $\Delta V$  between the pseudopotentials from the ion cores and the potential from the positive background in first-order perturbation theory.<sup>10,11</sup> The energy of a hydrogen atom at a position  $\vec{r}$  outside the surface is thus calculated as  $E_H(\vec{r}) = E_H^L(z) + \Delta E_H^L(\vec{r})$ , where  $z$  is the distance from the surface. The weakness of the pseudopotentials makes this a reasonable procedure.<sup>10,11</sup>

The energy  $E_{H_2}(\vec{r}, R)$  of an H<sub>2</sub> molecule centered at the position  $\vec{r}$  outside the surface and with the nuclei at  $\vec{r} \pm \frac{1}{2}R$  naturally splits into two parts,<sup>10,11</sup>

$$E_{H_2}(\vec{r}, R) = E_{extra}(\vec{r}, R) + E_{intra}(z, R), \quad (2)$$

energy  $E_{intra}$  to be approximated by its value in the jellium model at each distance  $z$  from the surface and at each internuclear separation  $R$ . In the jellium model,  $E_{intra}$  has been calculated self-consistently for H<sub>2</sub> perpendicular<sup>12</sup> and parallel<sup>13</sup> to the surface. The accuracy obtained with these approximations, amounting to some tenths of an electron volt in total energies and to smaller values for energy differences, is sufficient to identify some of the concepts of adsorption kinetics and to give them an interpretation in terms of the electron structure of the adsorbate-substrate system. "Chemical accuracy" ( $\sim 0.005$  eV at room temperature) is not obtained, however.

The initial increase in energy seen in Fig. 1,

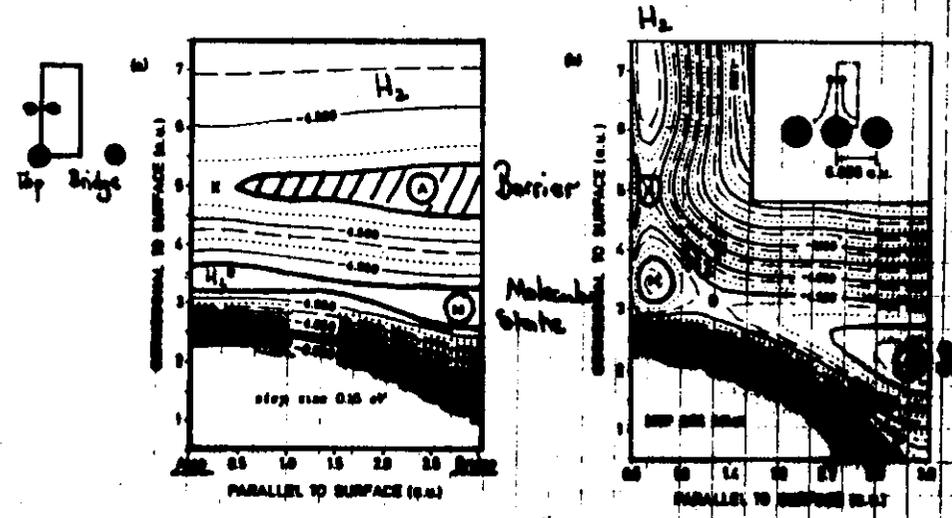


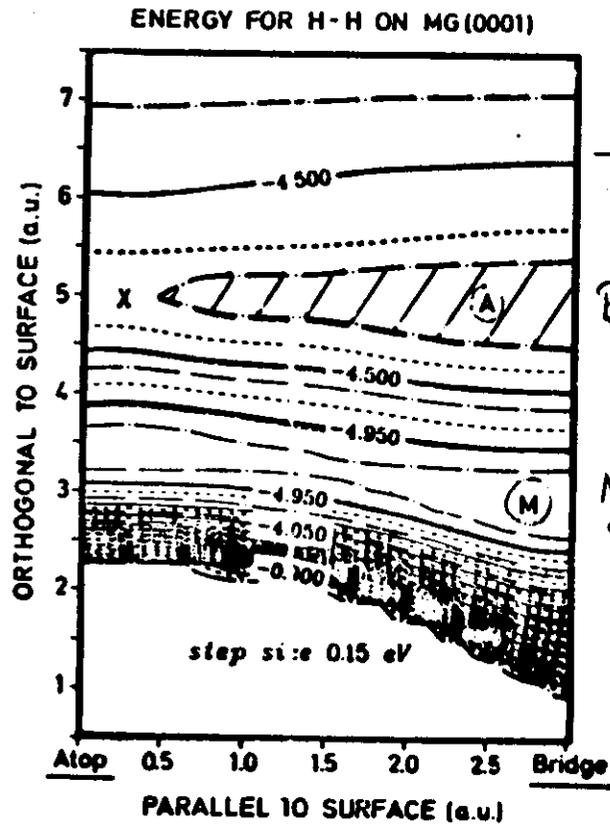
FIG. 1. Dipotential-energy curves for H<sub>2</sub> on a Mg(001) surface, (a) with H<sub>2</sub> parallel to the surface and a barrier length of  $R = 1.2$  a.u., and (b) dissociating over the step site (see geometry in text). The energies in electron volts are relative to those of the free H<sub>2</sub> molecule. The molecular dissociation energy is 4.75 eV and only 0.5 eV relative to a free molecule. The distance from the surface is measured from the first atomic layer, and the distance parallel to the surface, which in (b) equals one-half the H-H separation  $R$ , is measured from the step site towards the bridge site. The coordinates of (a) given the distance between the two protons. Both plots show only one energy curve that has represented the adsorption barrier. A second potential energy curve is shown in the inset of (a) and (b) to the surface into the H-H vibration parallel to the surface. However, the potential well is not shown in (a) and (b), even though the dissociation barrier  $D$  is of the same size as  $\Delta$ .

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Nprskar et al  
PRL 46 (1981) 257

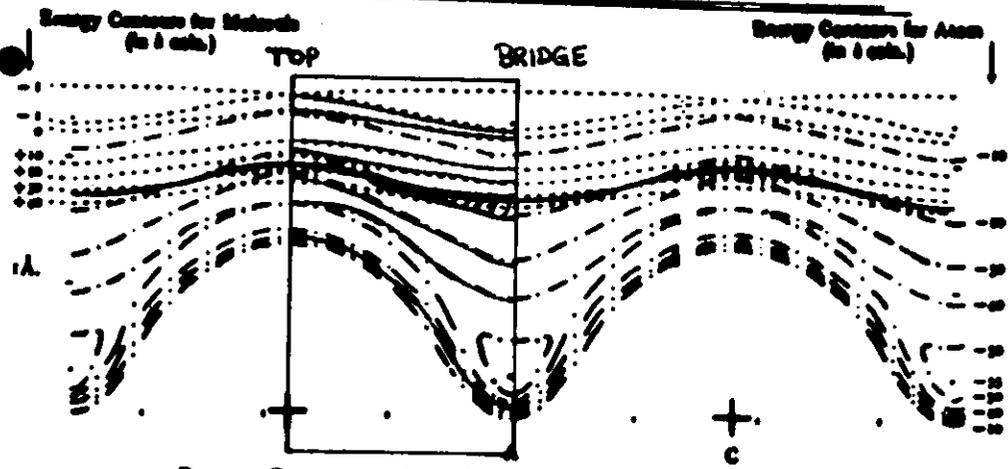
H<sub>2</sub>/Mg(001)

[c.f. Bengt Lundqvist]

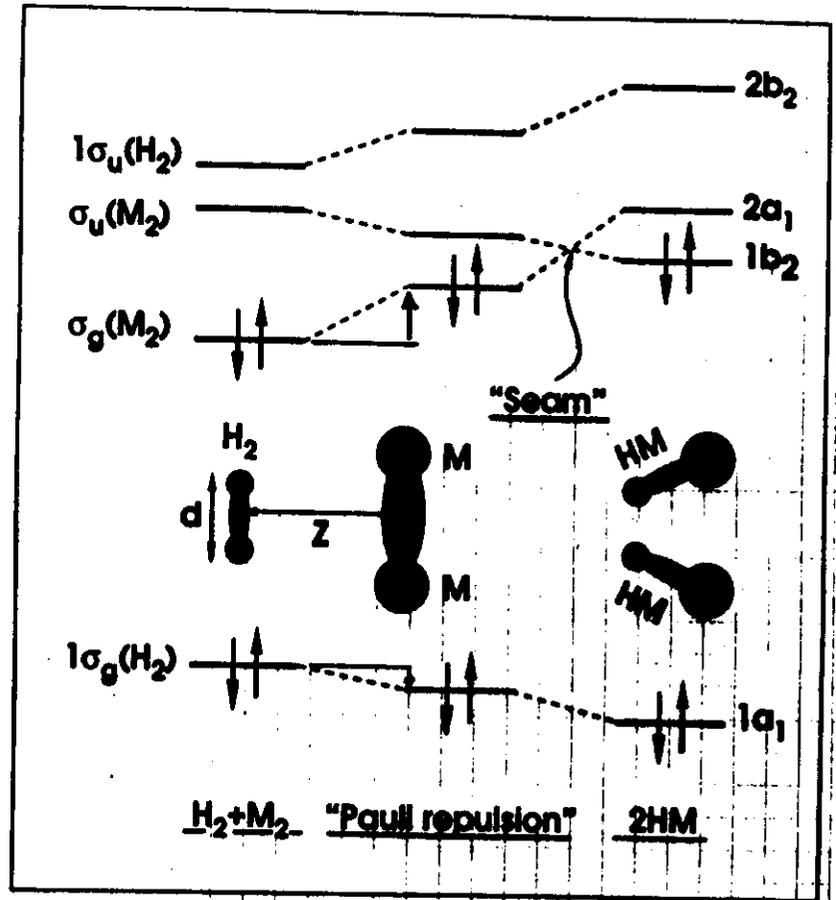


Nepukov et al  
P.R.L. 41 257 (81)

Lennard-Jones Trans. Farad. Soc. 25 888 (32)



Cluster  
Calculation

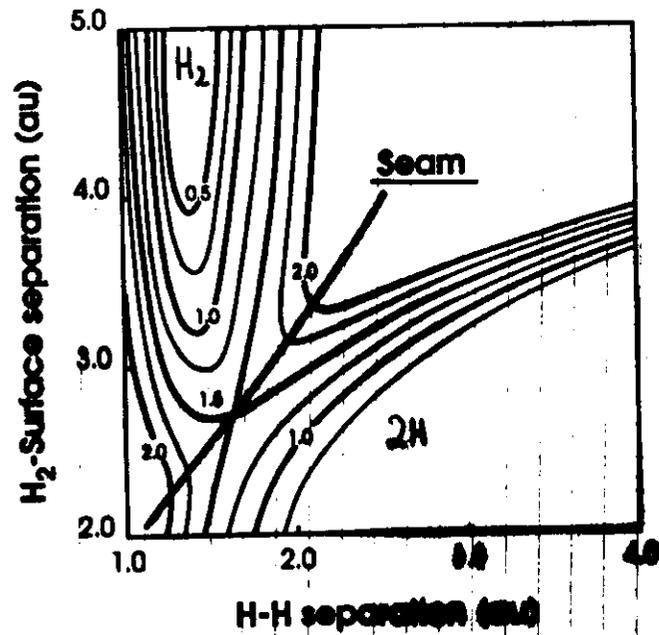
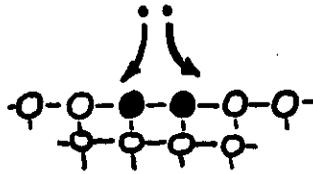


Harris, Holloway, Raman + Yang (JCP soon!)

Figure 2

H<sub>2</sub>/Cu(100)

Bridge-top site  
dissociation



Harris + Anderson PRL 55 1583 (1985)

Figure 3

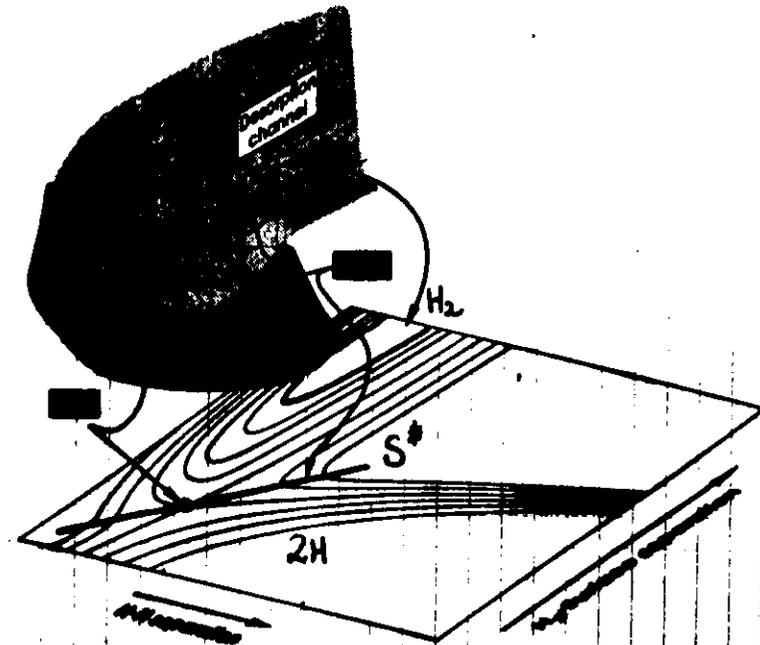
Activated Adsorption

Figure 4

