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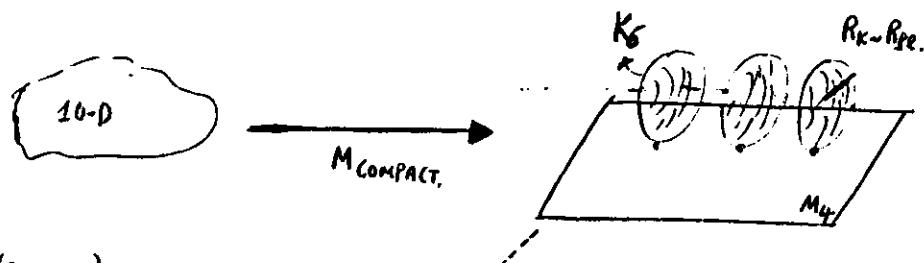
SCHOOL ON
NON-ACCELERATOR PHYSICS
25 April - 6 May 1988

SUPERSTRINGS IMPLICATIONS TO PARTICLE PHYSICS & COSMOLOGY (2)

by

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PHYSICS:



SUPERSTRING IMPLICATIONS TO PARTICLE PHYSICS/COSMOLOGY

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ICTP

3-5/5/88

SCHOOL ON NON-ACCC.
PHYSICS.

(F-H-S-W)

Outside
Implications:
1) $N=2$ SUSY $\rightarrow \Lambda_c = 0$

$M_4 \times K_6$

Calabi-Yau manifold!
↳ 3 large class of them

1) \nexists Extra gauge interactions!

2) \nexists Anomalies after compactification: $(F \wedge F)_6$ or $(R \wedge R)_5$

$$E_8 \times E_8 \xrightarrow{M_c} E_6 \times E_8' \xrightarrow{\text{commute with}} \text{gravitationally!}$$

$$(F_{mn})_{E_6} = (F_{mn})_{E_8'} = 0 ! \quad (\text{WATCH IT!})$$

3) Particle content:

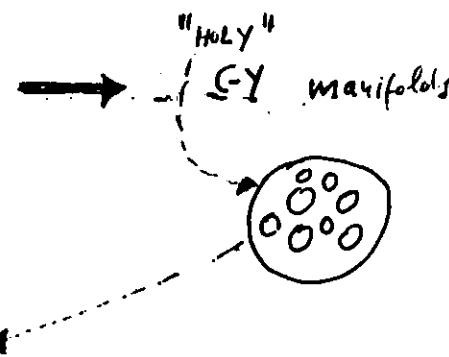
$$248 = \underbrace{(78, 1)}_{\text{"gauge bosons":}} + \underbrace{(27, 3)}_{\geq 24_{\text{SUSY}}} + \underbrace{(27, \bar{3})}_{8_g + 3_{W+L_g}} + \underbrace{(1, 8)}_{\text{SUSY}}$$

"matter":

$$\supset (10 + \overline{5})_{SU(5)} = (d)_L + (e)_L + u_{R_i} d_{R_i} e_R$$

$N_g = \# \text{ generations?}$

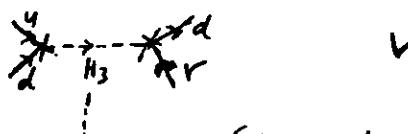
5)

E₆-breakinge) N_g3) Embarrass. Yukawa relations:
(wrong masses
first proton decay)

• Ng can be 3 ✓

• Easily avoid dual GUT relations: u_d=u_e ✓

$$\begin{pmatrix} H \\ H \\ H/3 \\ H^+ \\ H^0 \end{pmatrix} \rightarrow W-S \text{ Higgs}$$

Can you be light!
NO HIERARCHY PROBLEMS!... E₆-breaking : (Solenoid / B-A) / HOSOTANI MECHANISM

$$A_M^{(78)} = (A_h^{(78)}, "A_{scalars}")$$

↓
gauge bosons ↓ "scalars"

VERY SPECIFIC BREAKING PATTERNS!

$$E_6 \longrightarrow \begin{aligned} &SU(3) \times SU(2) \times SU(2) \times U(1)_Y \times U(1)_E \\ &SU(3) \times SU(2) \times U(1)_Y \times U(1)_E \\ &\quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ &SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_E \quad * \quad (?) \end{aligned}$$

$$\begin{aligned} "27" = & g_s \left(\frac{G_m}{d_L} + \frac{1}{3} d_R + \frac{1}{6} R + \frac{1}{6} e_L + \frac{1}{3} e_R + \frac{1}{3} b_L + \right. \\ & \left. + \frac{1}{6} \bar{b}_R + \frac{1}{3} \bar{e}_L + \frac{1}{3} \bar{e}_R + \right. \\ & \left. - \frac{1}{6} \bar{R} + \frac{2}{3} \bar{d}_L + \frac{1}{3} \bar{d}_R \right. \\ & \left. + \frac{1}{6} D_R + \frac{1}{3} \bar{D}_L \quad \{ \text{heavy "d-type quark": } q = -q_3 \} \right. \\ & \left. + \frac{\epsilon^a}{6} \quad \{ Q=0 \} \right) \end{aligned}$$

• Allowable V.R.V.S.: UNIQUE

$$\langle \bar{H} \rangle \geq \bar{V}; \quad \langle H \rangle \leq V; \quad \langle N \rangle \leq X$$

Superpotential: UNIQUE

$$f = \underbrace{g_{abc} H_b \bar{H}_c N_d}_{(a,b,c: 1,2,3)} + \underbrace{k_{abc} D_a D_b N_c}_{\text{and "}} +$$

$$+ \underbrace{h_{abc} H_a Q_b U_c}_{(a,b,c: 1,2,3)} + h'_{abc} \bar{H}_a Q_b D_c + \tilde{h}_{abc} L_a \bar{H}_b E_c$$

No problems with:

B	✓
L	✓
F(NC)	✓
Weak lepto. coupl.	?

$$\text{J}_f = \begin{cases} \textcircled{1} \quad \lambda' D^c L q + \lambda'' D^c u^c + \lambda_D D d^c & (\text{C-E-E-N}) \\ \textcircled{2} \quad \lambda''' D Q Q + \lambda'''' D^c u^c d^c & (\text{C-R}) \\ \textcircled{3} \quad \lambda_D D^c L q + \lambda_D' D^c u^c & (\text{OR}) \\ \textcircled{4} \quad \lambda_D D d^c & (\text{OR}) \end{cases}$$

• **(OR) → Conserv. of B-number**

Existence of one set of vertices \rightarrow C-decay!

$\cancel{\text{XXX}}$ No mixing between D-L ! Weak univ. V
⇒ B-conserv. guaranteed!

.. All above couplings + $\lambda H L v^c$

- i) large m_H
- ii) large t-H mixing

Are the **ONLY** ones allowed by parametric fig?

→ We need DISCRETE SYMMETRY $\sim \frac{1}{\sqrt{2}} \text{diag}(X)$ TO FIX UP
ONLY THE EXISTENCE OF $H L v^c \oplus \delta f_{\text{I}} \oplus \delta f_{\text{II}}$
NOT SO PECULIAR!!!

$$\text{e.g.: } \# H L v^c + \delta f_{\text{I}} \rightsquigarrow \begin{cases} z_2 : [SU(3), 3, \bar{3}] \rightarrow (-1) [] \\ z'_2 : v^c \rightarrow (-1) [] \end{cases}$$

$$\# H L v^c + \delta f_{\text{II}} \rightsquigarrow \begin{cases} z_2 : (L, e^c, v^c) \rightarrow (-1) [] \\ z'_2 : v^c \rightarrow (-1) [] \end{cases}$$

... 3 HAN coupling FUNDAMENTAL

- 1) $w_{H_L} \neq 0$
- 2) $\tilde{H}, \tilde{H}, \tilde{N}$ massive
- 3) $\#$ "wrong" choices!

(C-E-E-N)

(E-F-N-Z)

∴ 1) Uniqueness of low energy gauge group G_0 :

$$G_0 \equiv SU(3)_c \times SU(8)_L \times U(1)_Y \times U(1)_E$$

with only 3-generations allowed!
(27)

2) Generically at low energies only 3 (27) allowed

No 27 or parts of it? at low energies!

3) Allowed U.E.V.P.: unique !

4) Allowed η^c : unique !

VERY RESTRICTIVE

$$M_X \approx 4.4 \cdot 10^{17} \text{ GeV}$$

$$\sin^2 \theta_W(M_W) \approx 0.91$$

Supersymmetric term											
Rare process		1	2	3	4	5	6	7	8	9	10
λ_{HQQ}	λ_{HLL}	λ_{HQQ}	λ_{DQQ}	$\lambda_{\text{D'Q'}}$	λ_{DPV}	λ_{DPLQ}	$\lambda_{\text{DPR'}}$	a_0	a_0	a_0	
λ_{HQQ^2}	λ_{HLL^2}	λ_{HQQ^2}	λ_{DQQ^2}	$\lambda_{\text{D'Q'}^2}$	λ_{DPV^2}	λ_{DPLQ^2}	$(q\bar{q}\gamma^0) = 0$	$(q\bar{q}\gamma^0) \neq 0$	$(q\bar{q}\gamma^0) \neq 0$	$(q\bar{q}\gamma^0) \neq 0$	
16 $\text{Im}(K^0 \rightarrow \bar{K}^0)$	-	-	-	1×10^{-6}	2×10^{-3}	2×10^{-2}	-	2×10^{-3}	2×10^{-3}	2×10^{-3}	
17 $e^+ e^-$	-	-	-	-	-	-	-	-	-	5×10^{-1}	
18 $P(K \rightarrow \pi\pi\pi)$	-	-	$\sqrt{\lambda_{\text{HLL}}} < 6 \times 10^{-3}$	-	-	-	-	-	-	-	
19 a_0	$\sqrt{\lambda_{\text{HQQ}}} < 6 \times 10^{-3}$	-	$\sqrt{\lambda_{\text{HQQ}}} < 2 \times 10^{-3}$	-	$\sqrt{\lambda_{\text{HQQ}}} < 6 \times 10^{-3}$	-	$\sqrt{\lambda_{\text{HQQ}}} < 6 \times 10^{-3}$	2×10^{-3}	-	-	
20 $\pi \rightarrow e\mu$	-	-	$\sqrt{\lambda_{\text{HLL}}} < 1 \times 10^{-3}$	-	-	-	-	-	-	-	
21 $\pi^0 \rightarrow ee$	-	-	$\sqrt{\lambda_{\text{HLL}}} < 0.2$	-	-	-	-	-	-	-	
22 U_{eff}	-	-	-	-	-	-	-	-	-	-	

Bounds on Yukawa couplings from flavour-changing neutral currents and other rare processes.
The generation structure of the couplings has not been taken explicitly into account, but it is clear,
(for each process studied, which fermion generations are involved).

(CEEGW)

Best limit (process)		z mass	Weak universality	CP violation ($\text{Im } \lambda$)
Re λ	$D^0 \rightarrow \bar{D}^0$	2×10^{-4}	8×10^{-4}	1×10^{-1}
Re λ	$\mu \rightarrow e\gamma$	8×10^{-4}	8×10^{-4}	1×10^{-6}
Im λ	$D^0 \rightarrow \bar{D}^0$	2×10^{-4}	2×10^{-4}	2×10^{-3}
Im λ	$\mu \rightarrow e\gamma$	2×10^{-4}	2×10^{-4}	2×10^{-3}
				$K^0 \rightarrow \bar{K}^0$
				$B^0 \rightarrow \bar{B}^0$
				2×10^{-1}
				5×10^{-1}
				$\text{Im}(K^0 \rightarrow \bar{K}^0)$
				$\text{Im}(K^0 \rightarrow \bar{K}^0)$

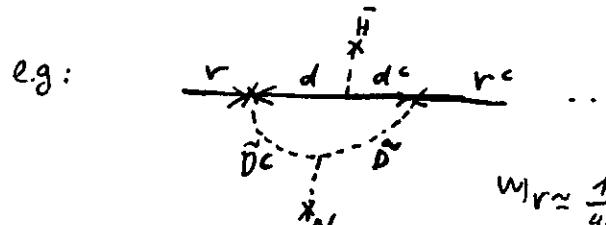
L- Physics

$\begin{pmatrix} \text{MNS} \\ \text{CKM} \\ \text{EM} \\ \text{N=0} \end{pmatrix}$

$$f_L = g_L H L r^c + [g' D^c L Q + g'' D e^c u^c] + g_D D d^c r^c$$

- 1) # Majorana mass \rightarrow no "see-saw" mechanism
 $\lambda_L < 10^{-9}$!!! \rightarrow **CUT**

- 2) \exists Possibl. for Radiat. induced small Dirac m_ν



$$m_\nu \approx \frac{1}{q_0^2} \cdot \lambda' \cdot \lambda_D m_d$$

(e.g.): $\lambda' \sim \lambda_D \sim 10^{-3}$ $\rightarrow m_\nu \approx 50 \text{ eV}$
 $m_{\nu_\mu} \approx 1 \text{ eV}$
 $m_{\nu_e} \approx 10^{-2} \text{ eV}$ } Dirac!

Consequences

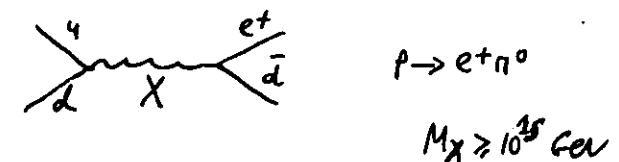
- 1) No. valence 2- β decay / No. $\nu - \bar{\nu}$ oscill.
- 2) JTEP ... (?)
- 3) Solar neutrino problem V [M-S solution]
- 4) \exists 3-Dirac- $\nu \approx 6 = 2 \text{ comp } V$
 \rightarrow PRIMARY NUCLEOSYNT

ORDINARY GUTS

Grand Unification: $SU(3)_C \times SU(2)_L \times U(1)_Y \subset G \left(\begin{array}{l} \text{SU(5)} \\ \text{SO(10)} \\ \text{E6} \end{array} \right)$
 new interactions \rightarrow gauge: X, Y, \dots
 \rightarrow matter: H_3, \dots

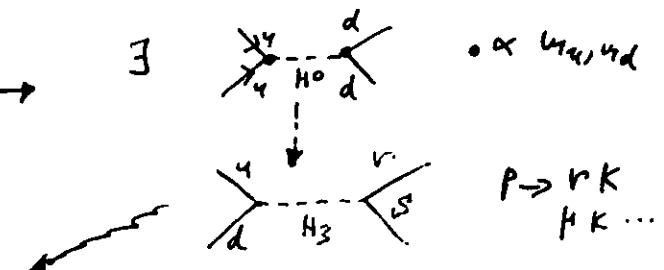
e.g.: $\begin{pmatrix} d \\ \bar{d} \\ e \\ \bar{e} \\ r \\ \bar{r} \end{pmatrix} \quad \begin{pmatrix} (4) \\ (1) \\ u^c \\ \bar{u}^c \\ \ell^c \\ \bar{\ell}^c \end{pmatrix}$

"gauge decay"



$$M_X \geq 10^{15} \text{ GeV}$$

"matter decay"



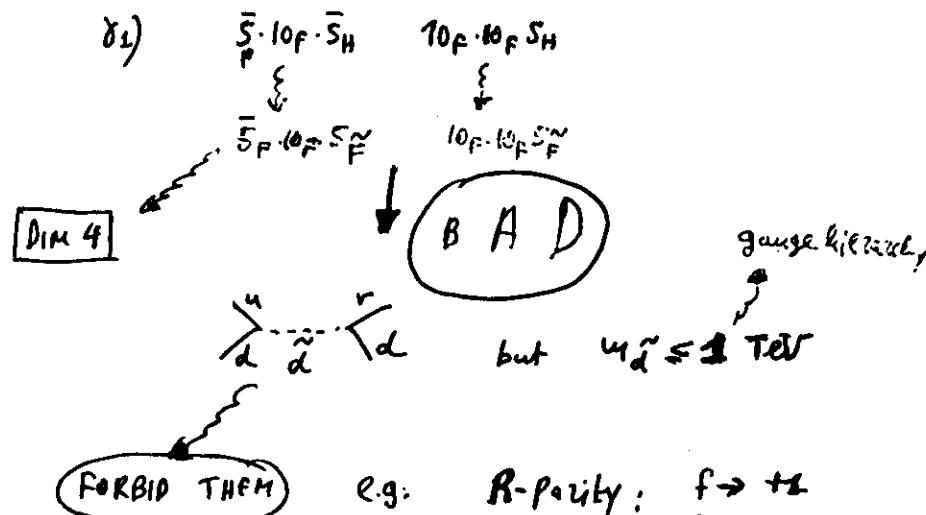
$$M_{H_3} \geq 10^{11-12} \text{ GeV}$$

WATCH IT

SUSY GUTS

Are the above \oplus "NEW STUFF"

- $M_X \rightarrow 10^{16} \text{ GeV} \rightarrow \text{gauge decay } ?$
- "Matter decay" $\rightarrow H_3 \rightarrow$ interesting in certain scenarios
 $\left\{ \begin{array}{l} \text{inflation} \rightarrow \text{phase transition} \\ \hookrightarrow M_{H_3} \sim 10^11 - 10^{13} \text{ GeV!} \end{array} \right.$
 $\rightarrow p \rightarrow \{ \tilde{\nu} K \}$
- NEW**

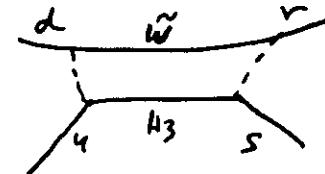


$$\delta_2)$$

$$\bar{S}_F \cdot 10_F \cdot \bar{S}_F \cdot \left\{ \begin{array}{l} S_F \\ 10_F \end{array} \right\} \quad 10_F \cdot 10_F \cdot S_F \cdot \left\{ \begin{array}{l} S_E \\ 10_F \end{array} \right\}$$

DIM 5

R-Parity \vee



$p \rightarrow \tilde{\nu} K$
 $(\tilde{\nu} K)$

$$\tau \sim \alpha^2 \cdot \left(\frac{m_u \cdot m_s}{M_W^2} \right)^2 \cdot \left(\frac{1}{M_X \cdot M_W} \right)^2 \quad \checkmark$$

* DIM 5 forbidden if \exists extra U(1)'s!

** Supergravity/non-renormalizable interact

↳ similar results:

$p \rightarrow K + \text{lepton}$

AND THAT THE WAY IT WAS
UNTIL ...

SUPERSTRINGS

(CEENG)
NG.

all the above \oplus **NEW!**

a) $M_X \sim M_{\text{compact.}} (\sim 10^{18} \text{ GeV} ?) \rightarrow$ gauge decay ?

b) "Matter decay"

b₁) # odd. dim 4 bad couplings \rightarrow extra $U(1)$

b₂) # \exists new dim 4 bad couplings

barnish them:
 discrete symm.
 \leftrightarrow la R-parity
 and/or
 topology

CERN model example

b₃) dim 5 \rightarrow are out.
 \rightsquigarrow \exists extra gauge symmetry

Good!

b₄) extra terms from \int out heavy degrees of freedom
 { field theory
 Superstring models

respect symmetries

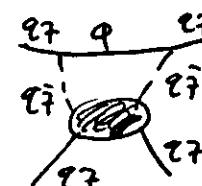
e.g.: $h \frac{(27\bar{2}\bar{7})(2\bar{7}\bar{2}\bar{7})}{M}$

$T_P \sim \frac{M^4}{m_{\text{rot}}^5}$!

need incomplete multiplets

\downarrow can't be "dressed up" to provide ffff BX interact.

EVEN if $h' \neq (27\cdot 2\bar{7})$



$\hookrightarrow (1,8) \epsilon (248)_{68}$

B-violating !!!!

$$T_P \sim \left(\frac{f h'}{M M_Q} \right)^2 \cdot m_{\text{rot}}^{-5} : \text{All modes: incl. } \overline{17}'$$

$\therefore \exists$ extra gauge interact. at low energies

\hookrightarrow proton stable !!!!!

You find proton decay:

extra gauge symm.
 at low energy

- a) $E_6 \rightarrow$ badly broken $\xrightarrow{?} (3,8,1)$
- b) $SO(10), SU(5) \dots$
- x) $\mathbb{T} \oplus$

P \rightarrow K + lepton

DARK MATTER (?)

Why (?)

- Solar neighbourhood
- Galactic disc / halo
- Small groups and clusters of galaxies
- INFLATION: $\Omega_B = 1$ (large scales)

Rotation curves.
[Virial theorem...]

- Help Galaxy formation

- i) $\frac{dp}{dt} \rightarrow$ enter the horizon \rightarrow no growth until matter/rad. separation
- ii) $\frac{dp}{dt} \sim R(t) \sim \frac{1}{T}$ but.
 $\frac{dp}{dt} \sim 1$ at least before $T \approx T_{dec} \sim 10^9 K$
 (Galaxies; quasars,...)
- iii) $\frac{dp}{dt} \sim 1 \cdot \frac{(4 T_0)}{\frac{1 \text{ eV}}{T_0}} \sim 10^{-3}$
 $\sim \frac{\Delta T}{T} < 10^{-4}$
BAD !!!

BUT if \exists Dark matter \rightarrow matter domination earlier ($T > \frac{1 \text{ eV}}{m_{\tilde{\chi}}}$) \rightarrow avoid the clash !!!

- ... Dark matter: non-baryonic cause $\Omega_B < 0.2$

?
...
anions

COSMIC RELICS

LIGHTEST $S(\text{nn})$ PARTICLE (LSP)

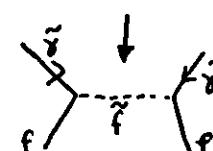
(EHNOS
EHN
OHNOS
CEHNOS)

R-parity \rightarrow \exists stable S -particle
(usually)

neutral / weakly interacting

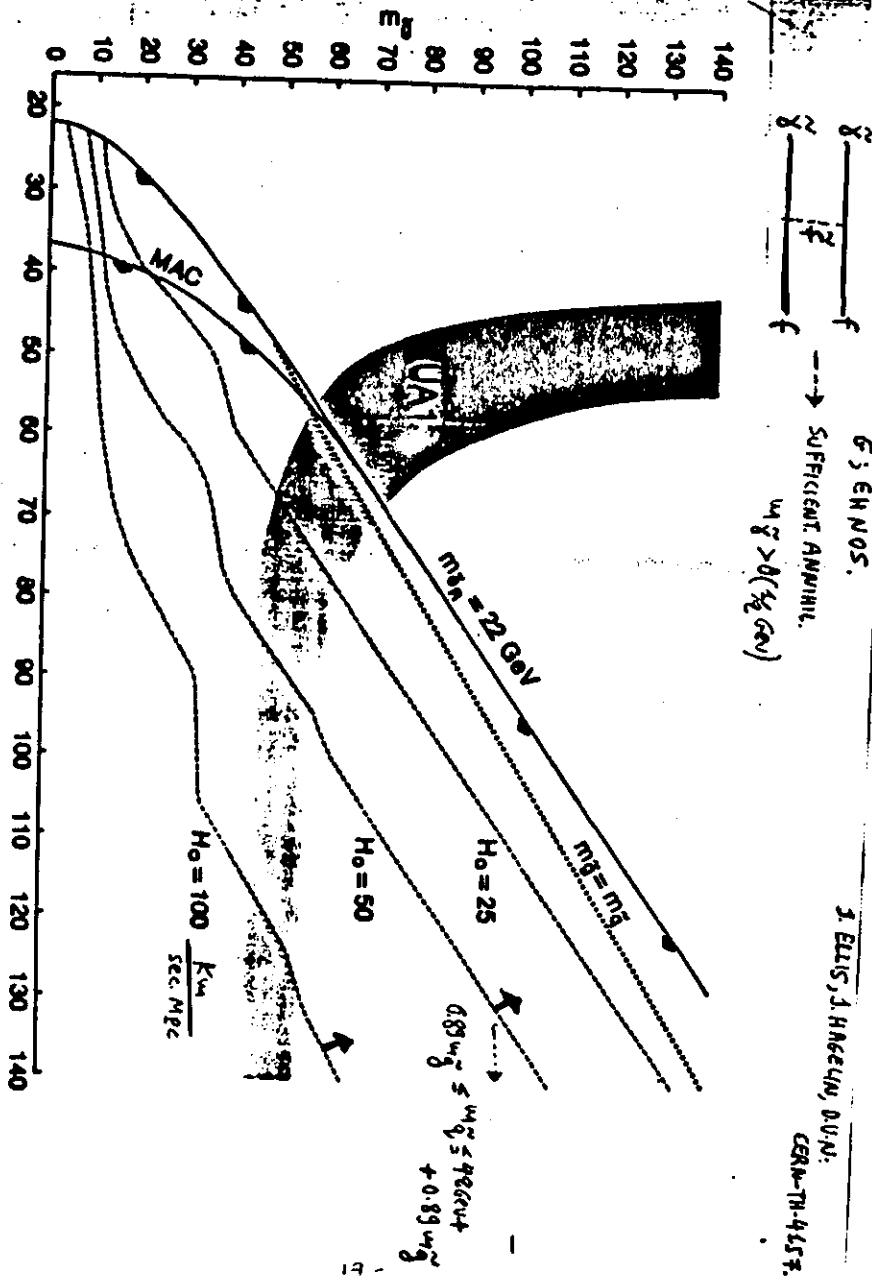
Possibilities:

- | | spin 0 | spin $\frac{1}{2}$ | spin $\frac{3}{2}$ |
|--|--|--------------------|--------------------|
| Unlikely: | $\tilde{\nu}$ | " $\tilde{\chi}$ " | $\tilde{G}_{3/2}$ |
| a) $m_{\tilde{\nu}} \sim m_{\tilde{\chi}}$ | | ↓ | |
| b) trapped in earth | | YES | |
| +
too many neutrinos | | | |
| "not seen" in | | | |
| Proton decay detector | | | |
| * NEW | 8) | | |
| | Dark Matter Detectors
exclude $\tilde{\nu}$
in the range $(10^6 - 10^7) \text{ GeV}$! | | |



$m_{\tilde{\chi}} \gg T_d$: "COLD" DARK MATTER (CDM)

Figure 1. For $H_0 = 50$: $m_{\tilde{g}} = (45-60) \text{ GeV}$; $m_{\tilde{\chi}} = (80-95) \text{ GeV}$; $m_{\tilde{e}} = (70-85) \text{ GeV}$; $m_{\tilde{\nu}} = (70-80) \text{ GeV}$.



Example: A Sun inspired model (EENZ)

gauge sector: $E_6 \supset SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_F$

SUSY: Spin 1 : $\tilde{W}_3 \quad \tilde{B} \quad \tilde{B}_E$

Spin $1/2$: $\tilde{W}_3 \quad \tilde{B} \quad \tilde{B}_E$

Matter sector:

$\langle H^0 \rangle = u$

$\langle \tilde{H}^0 \rangle = \bar{u}$

$\langle N \rangle = x$

④

3 H-H-N coupling

$$27 = (\underbrace{10 + \bar{5} + 1}_{\text{generation}}) + 10 + \underbrace{10}_{\text{}} + 1$$

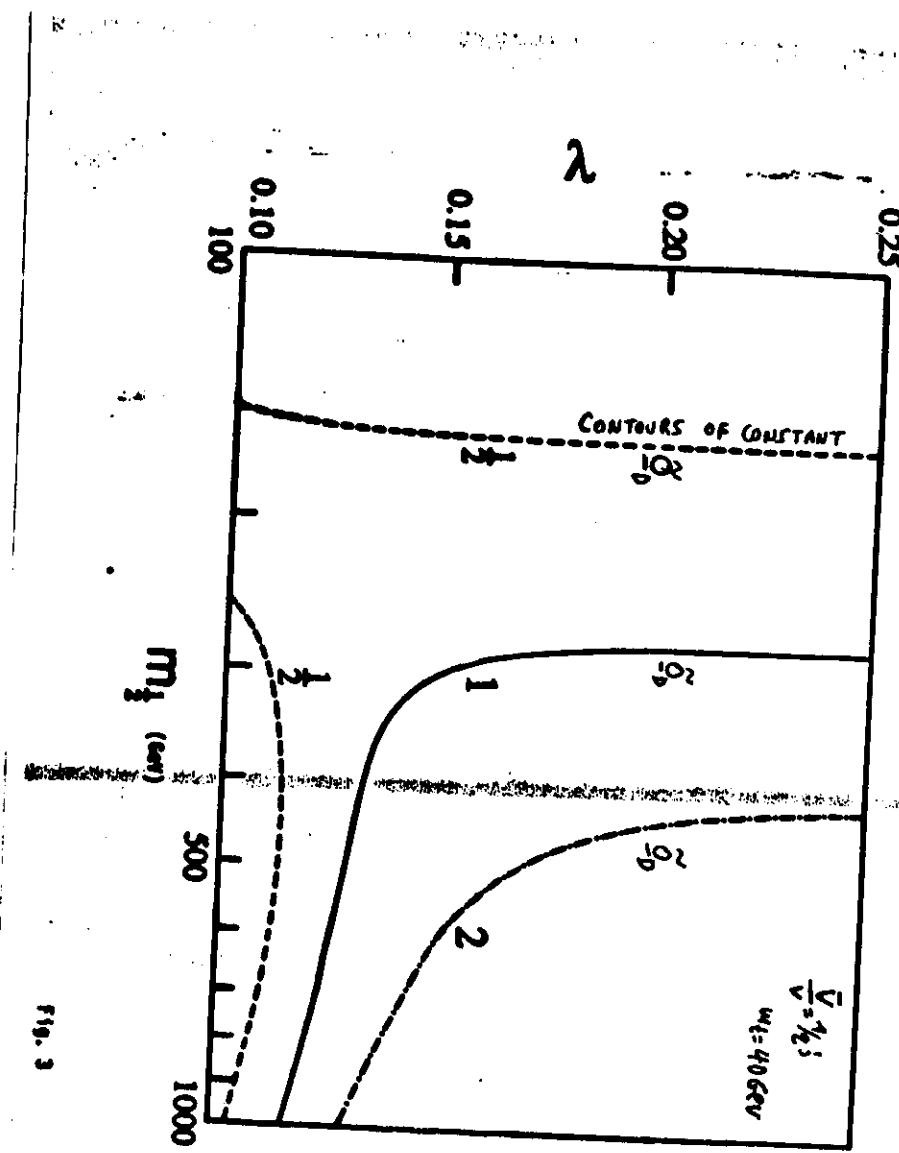
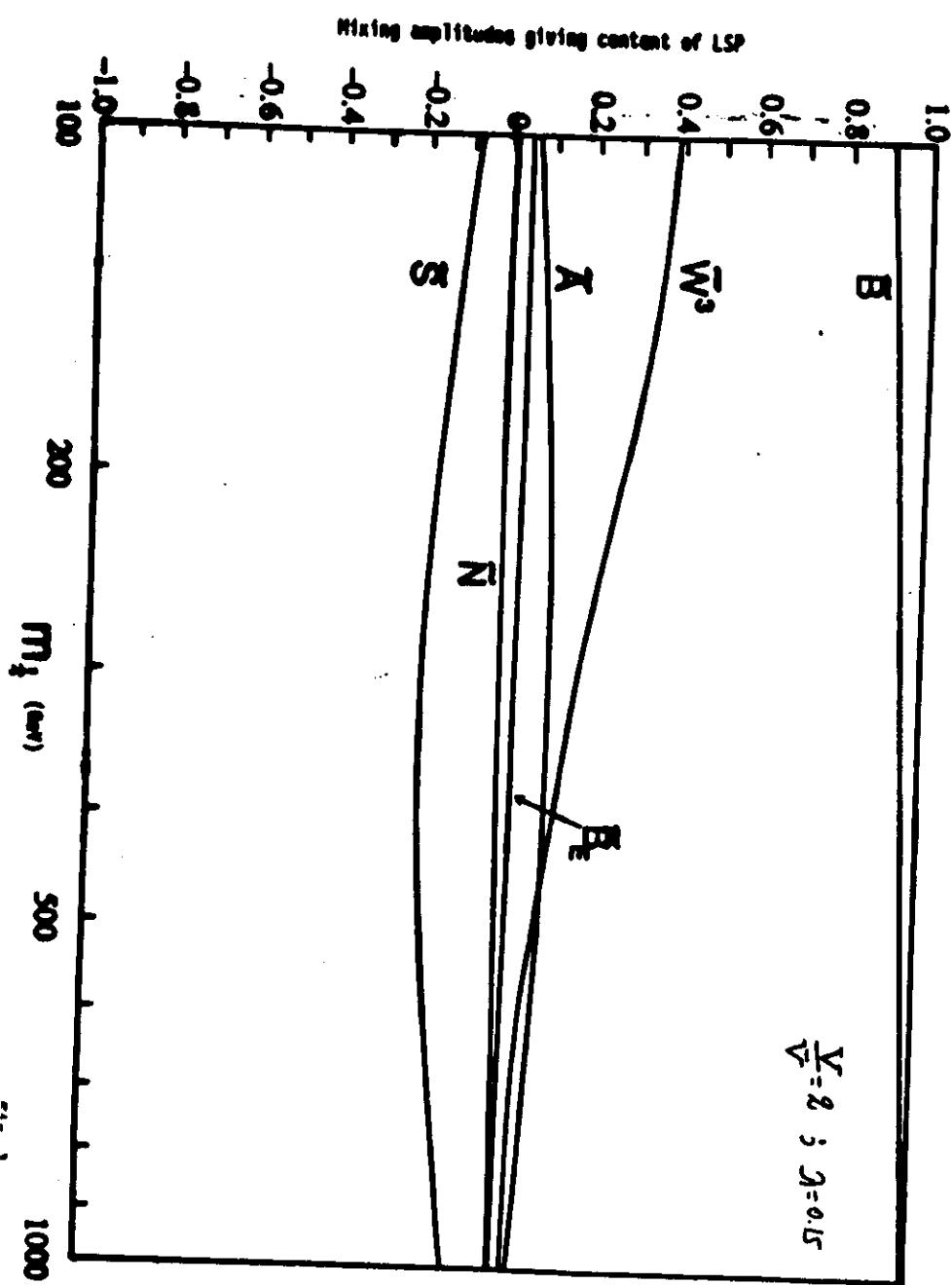
Spin 0 : $H^0 \quad \tilde{H}^0 \quad N$

SUSY:

Spin $1/2$: $\tilde{H}^0 \quad \tilde{\tilde{H}}^0 \quad \tilde{N}$

$$\tilde{\chi}_i = a_i \tilde{W}_3 + b_i \tilde{B} + c_i \tilde{H}^0 + d_i \tilde{\tilde{H}}^0 + e_i \tilde{B}_E + f_i \tilde{N}$$

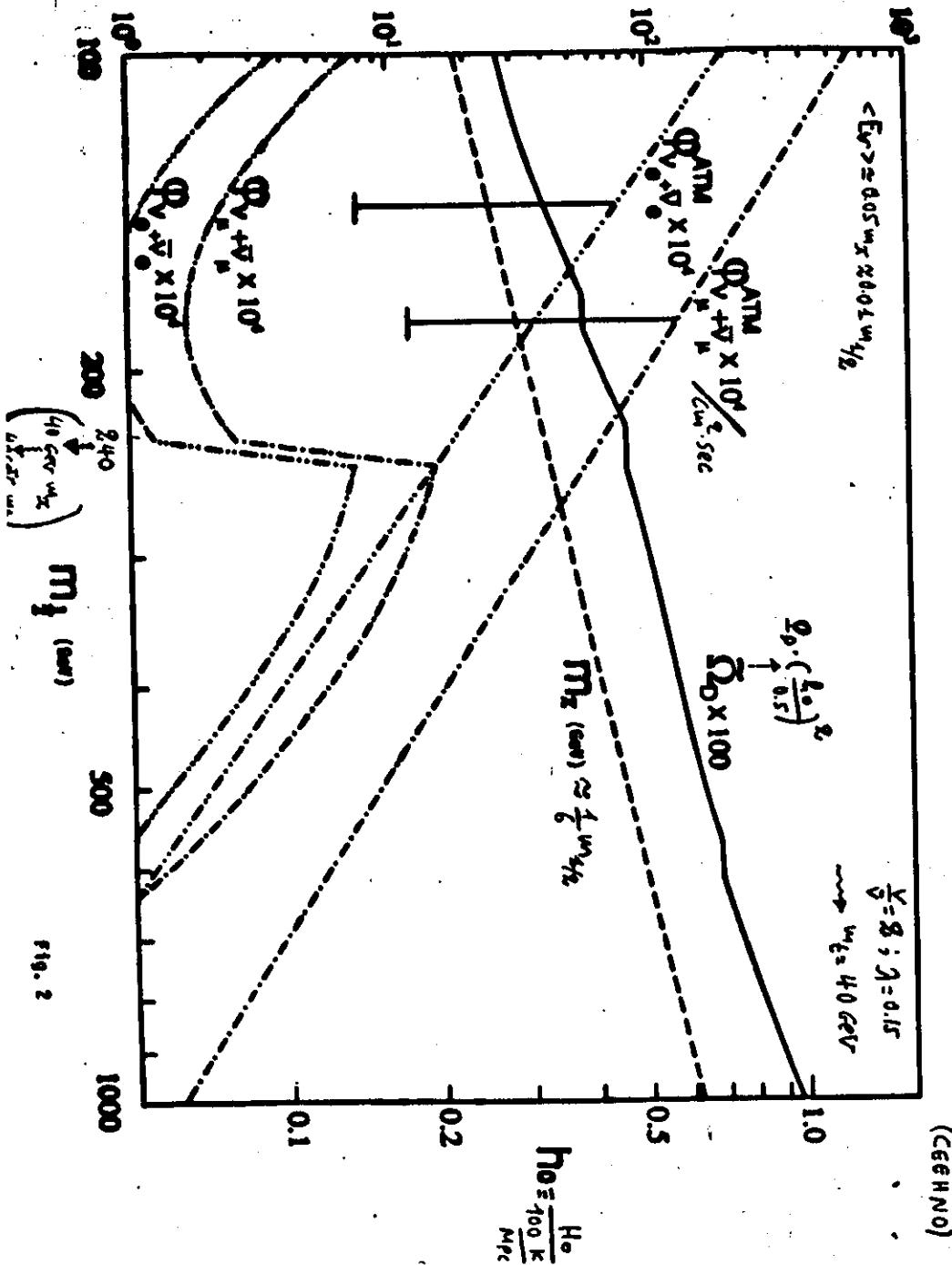
- 1) Relic cosm. mass density : ρ_X
- 2) neutrino fluxes from LSP annih. in the sun.
- 3) Rates in P.M.D.



(CEENNO)

$$\tilde{\rho}_D = \left(\frac{\rho_D}{\rho_{\text{air}}} \right) \cdot \left(\frac{f_D}{f_{\text{air}}} \right)^2$$

(CEENNO)



RESULTS

- 1) $\Omega_D = \frac{\rho_D}{\rho_{cr}} = 2^{0.5} \left(\frac{0.5}{h_0} \right)^2$!
- 2) Solar neutrino fluxes.
acceptable/observable
IFF: $\begin{cases} m_X \leq m_t \\ m_{1/2} \leq 6m_t \end{cases}$

Assuming $\Omega_D = 2$ [INFLATION]

\rightarrow (for $h_0 = 1/2$) $\rightarrow m_t \geq 40$ GeV !!!

$\therefore \Omega_D = 1$ / heavy top **(FIT WELL)**

Refer in DMD:

$$m_X = (20, 30, 40) \text{ GeV}$$

$$\# \frac{\text{events}}{\text{kg}^2 \text{day}} = (23, 8, 6) \times 10^3$$

$\downarrow \sim \text{BG.}$

$(^{47}\text{Ar}; ^{63,75}\text{Ge})$

* $\langle E \rangle = \frac{m_\chi^2 \cdot m_{Z,A}}{(m_\chi^2 + m_{Z,A})^2} v^2 / \text{Collision}$ e.g. $\langle E \rangle \approx 1 \text{ keV}$ for $m_\chi \approx 4 \text{ GeV}$