



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION



INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS

34100 TRIESTE (ITALY) - P.O.B. 586 - MIRAMARE - STRADA COSTIERA 11 - TELEPHONE: 2240-1
CABLE: CENTRATOM - TELEX 460392 - I

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**SCHOOL ON
NON-ACCELERATOR PHYSICS
25 April - 6 May 1988**

VARIABILITY (X-RAY BINARIES)

by

**T. Gaisser
University of Delaware
U. S. A.**

3. Variability (X-ray binaries)

Acceleration mechanisms
(X-ray binaries, young SN)

In close binary with powerful,
accretion-driven accelerator,
 ν -deposition expands star. ~~if~~
Expansion $\Rightarrow$ increase in accretion
rate. If $L_{\text{CR}} \propto \dot{M}$ then
process runs away. ($T \sim 50$ yrs.)

Need feedback mechanism
and variability.

R.J. Protheroe &

T. Stanev

CYGNUS X-3

BINARY SEPARATION = 1.80 SOLAR RADII

INCLINATION = 66 DEGREES

MAGNETIC MOMENT/RIGIDITY = 0.10 G.(CUBIC SOLAR RADII)/TV

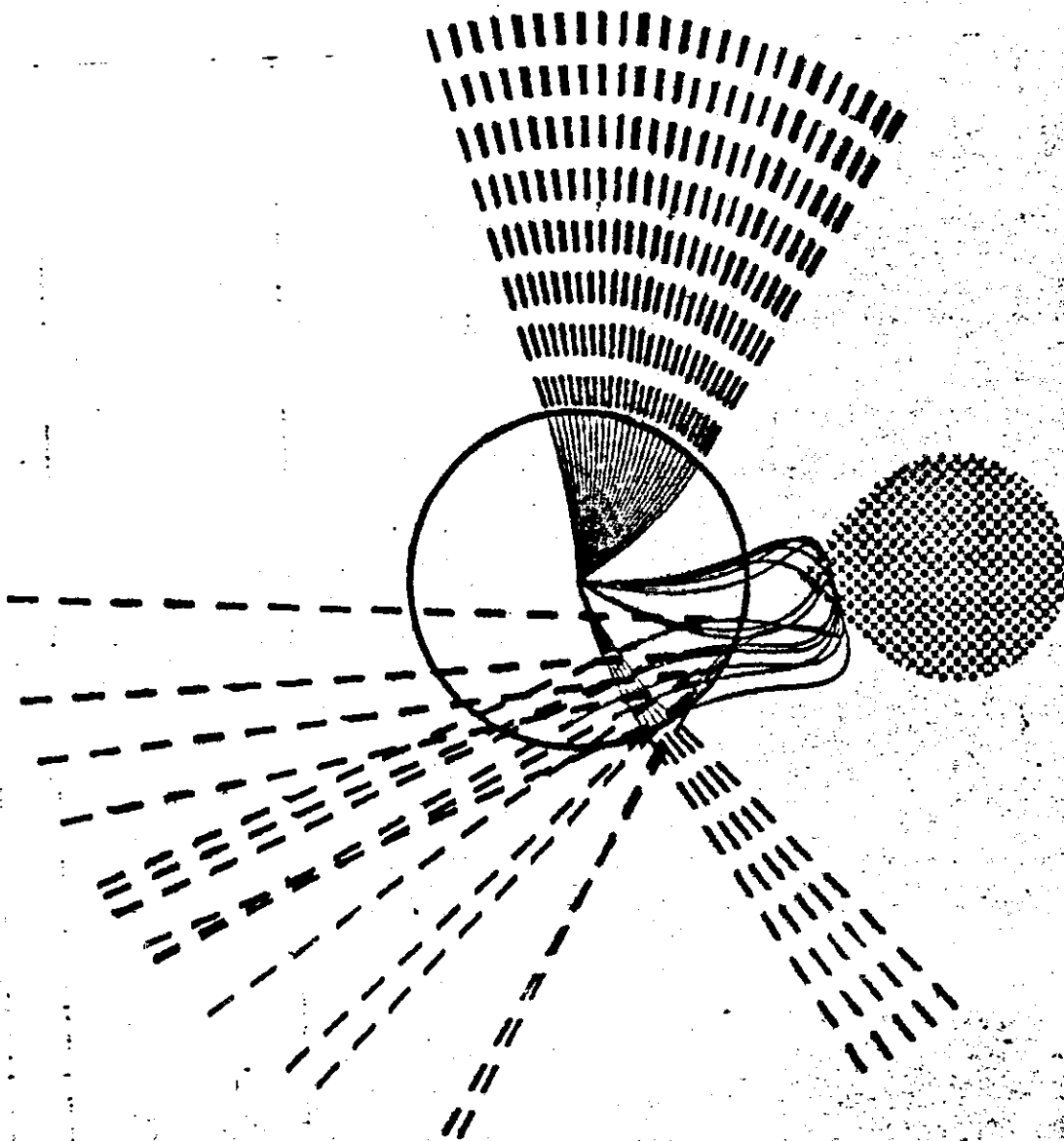
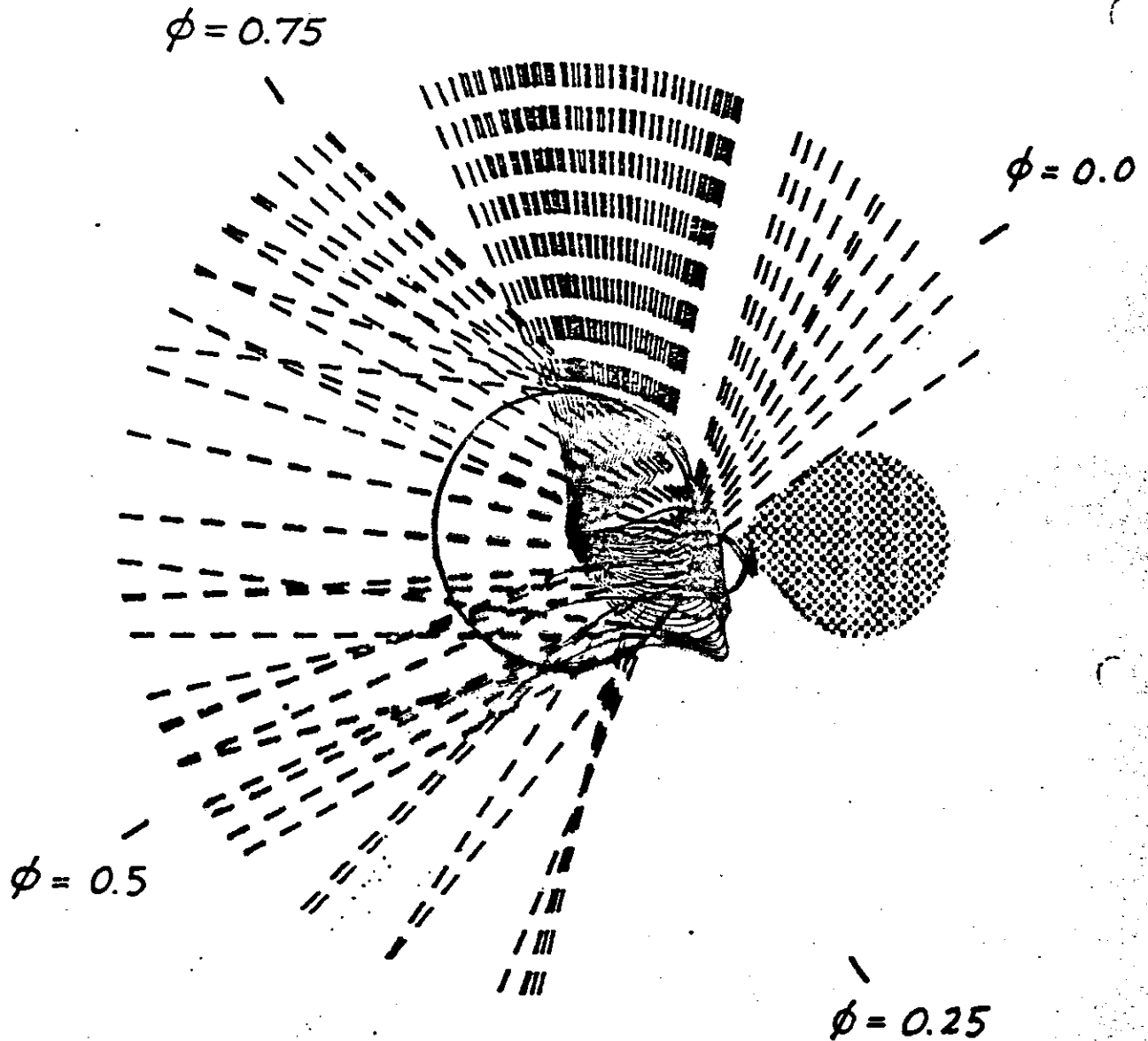
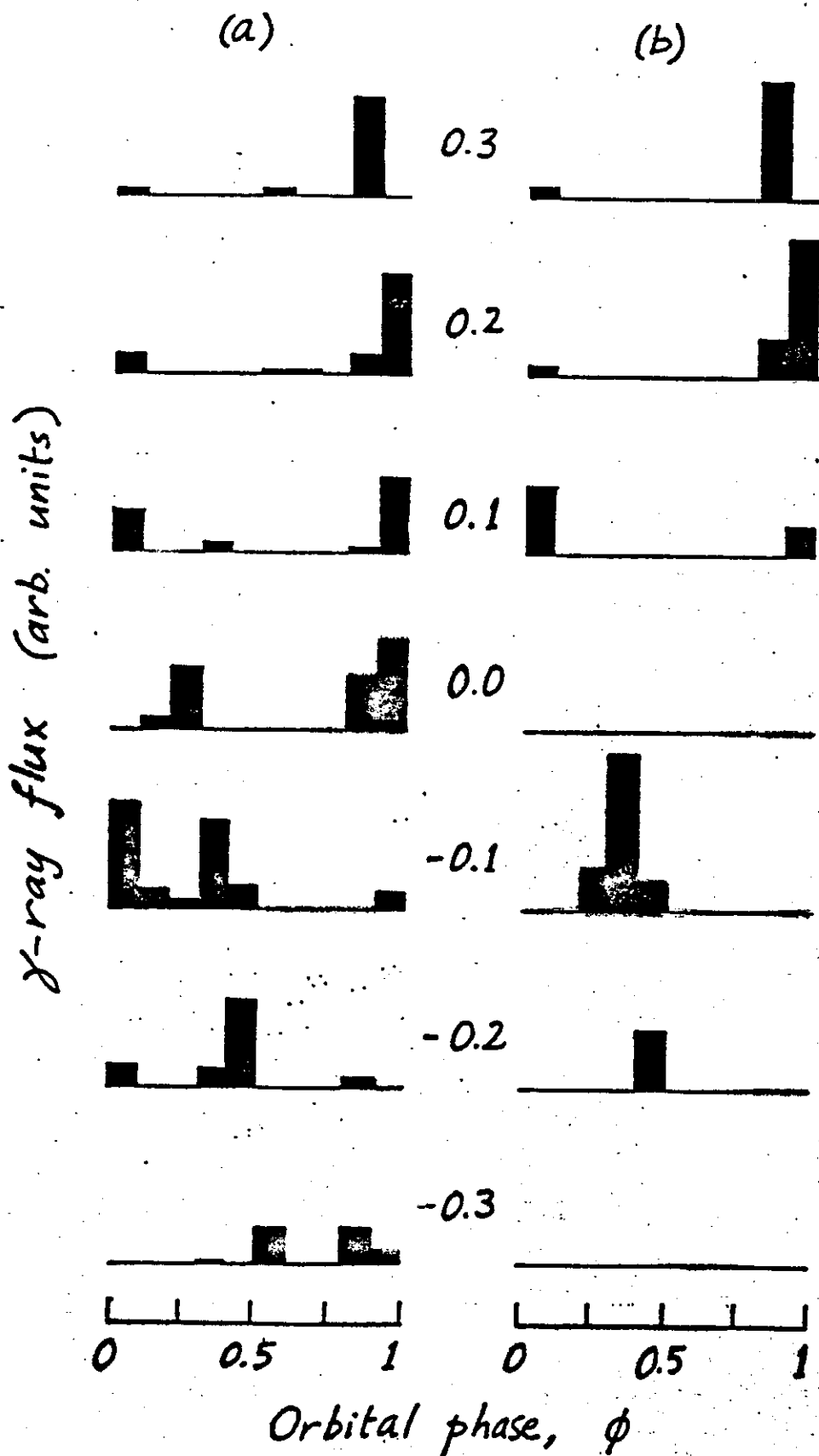


Fig. 1 ^{1.4} ^{1.00 1.32} ^{Fig.}
Protheroe & Stoney Nature 328, p. 136 (1987)





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Properties of PeV emitting binaries 19

System	binary period (days)	Companion Mass ($M_{\odot}$)	a / R_c^*	distance (kpc)	$L_{cr} (\frac{erg}{sec})$
Cyg X-3 * = ?	0.19	< 1 ?	1.6 - 2.0	≥ 10	$\geq 10^{39}$
Vela X-1	8.965	23	12	1.4	$\sim 10^{37}$
LMC X-4	1.408	19	3.5	50	$\geq 10^{41}$
Her X-1 , $> 10^{12} G$	1.7	2.4	6	4	$\sim 10^{38}$

* a from $P = 2\pi \sqrt{\frac{a^3}{G(M_{n.s.} + M_{companion})}}$

$M_{n.s.} \cong 1.4 M_{\odot}$

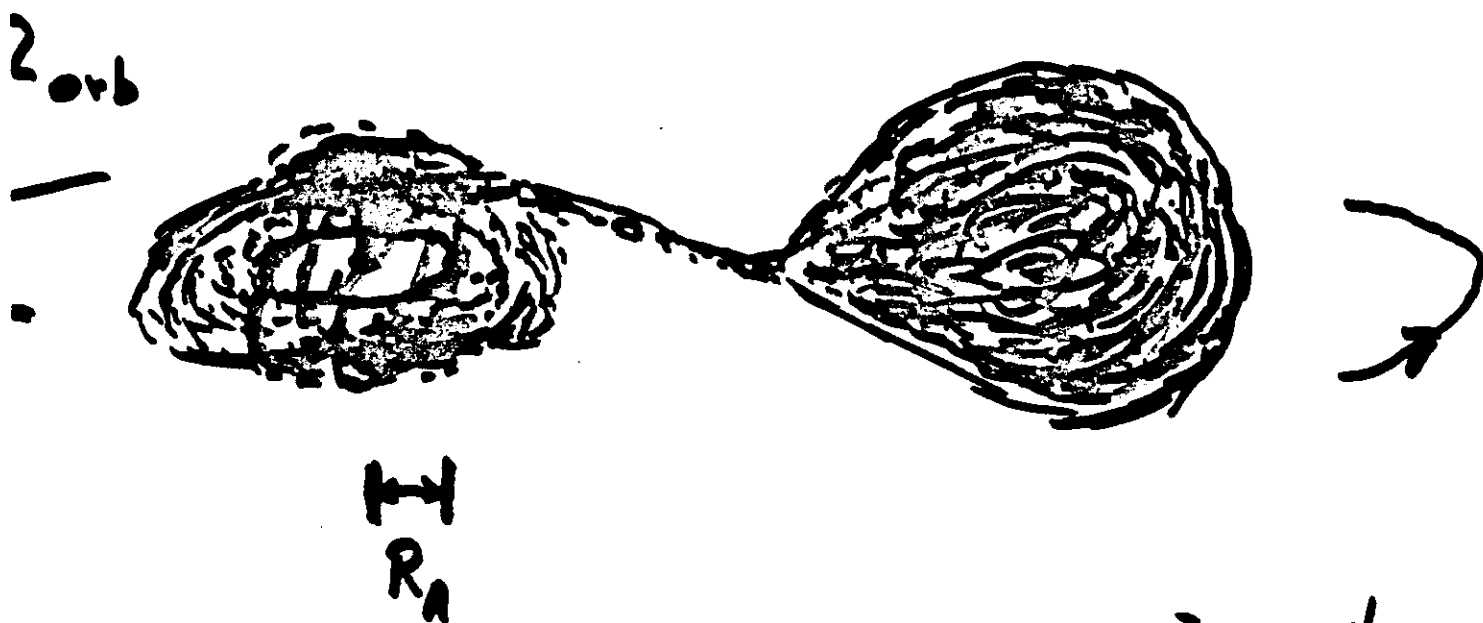
R_c = radius of main sequence companion of mass M_c

(for ν -absorption, outer part of star is not important)

Alfven radius R_A :

characteristic radius at which
inward accretion flow is balanced
by magnetic pressure due to
long-range (dipole component)
field of neutron star.

← a →



neutron star "pulsar"
has angular frequency
 Ω_p

companion star
co-rotates with
 Ω_{orb}

R_A given by solution of

$$\frac{B^2}{8\pi} = \rho v^2 \quad (1) \quad \dot{M} = \rho(r) 4\pi r^2 v$$

- 4) in $\uparrow$ give

$$(2) \quad v(r) \sim \sqrt{\frac{2GM_*}{r}}$$

$$(3) \quad B(r) = \frac{\mu_*}{r^3}$$

$$\mu_*^{4/7} (2\dot{M})^{-2/7} (2GM_*)^{-1/7}$$

in near zone
only, i.e. $r < R_L$

$$\mu_* = B_* R_*^3$$

$$(4) \quad R_L = c / \Omega_p$$

f $R_A \ll R_L$ then

"light cylinder
radius"

accretion disk penetrates

magnetosphere" and accretion onto n.s.

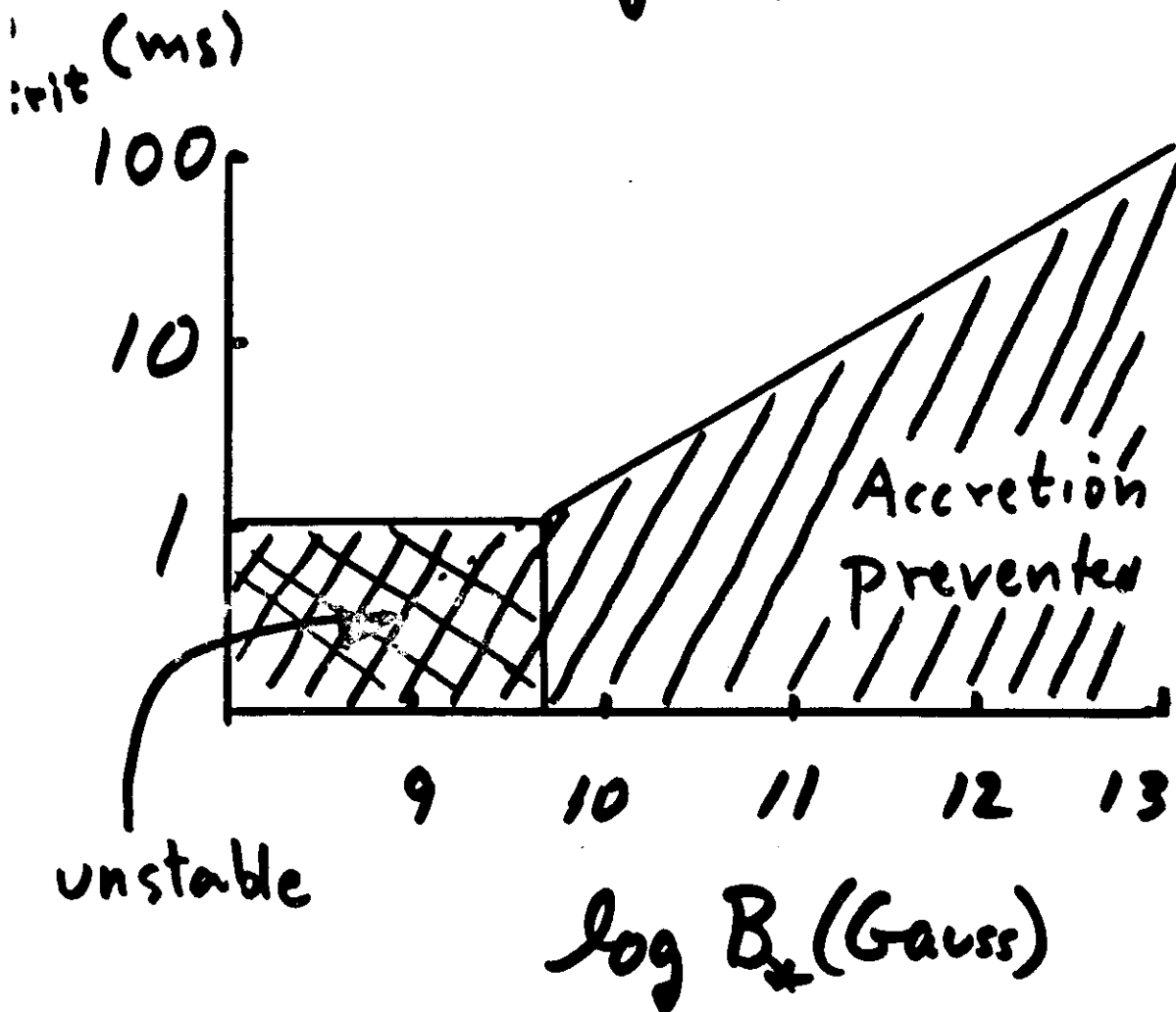
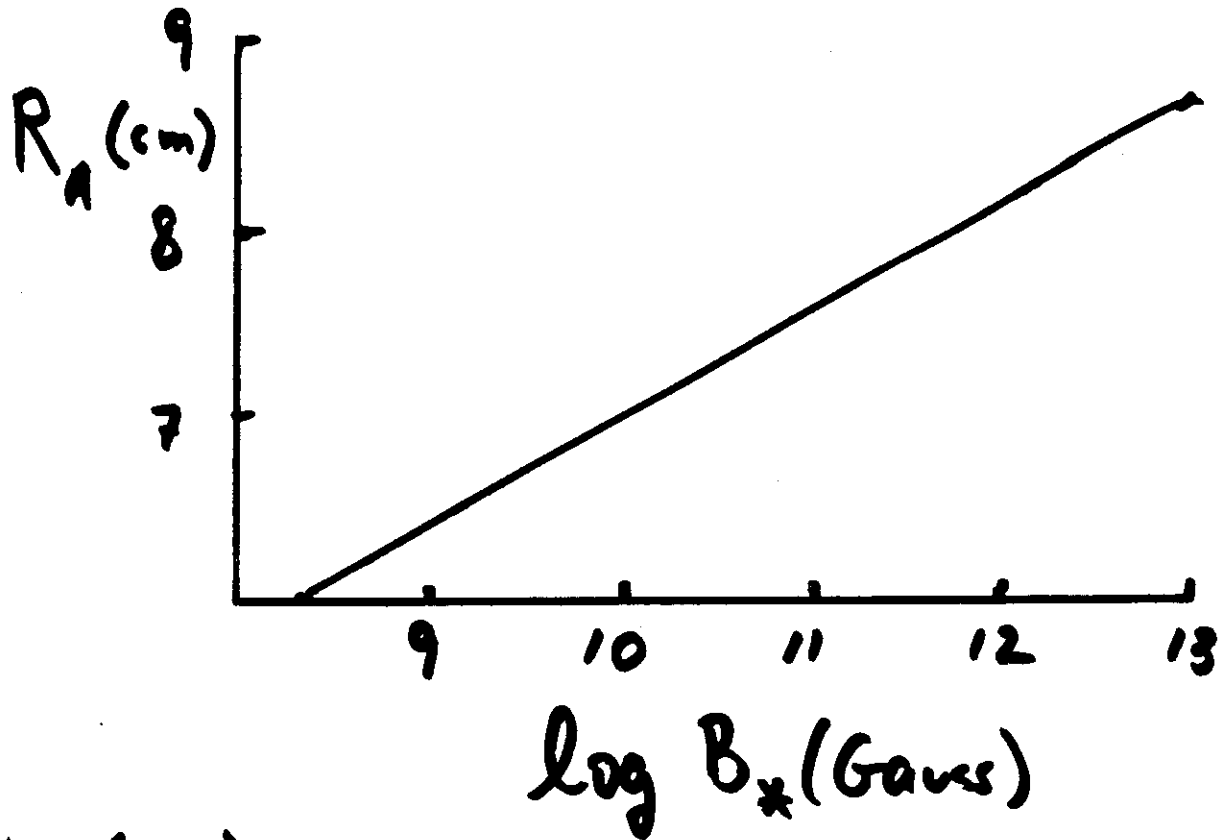
occurs along field lines onto polar regions

References: • Katz, High Energy Astrophysics

Frank, King & Raine, Accretion Power in Astrophysics

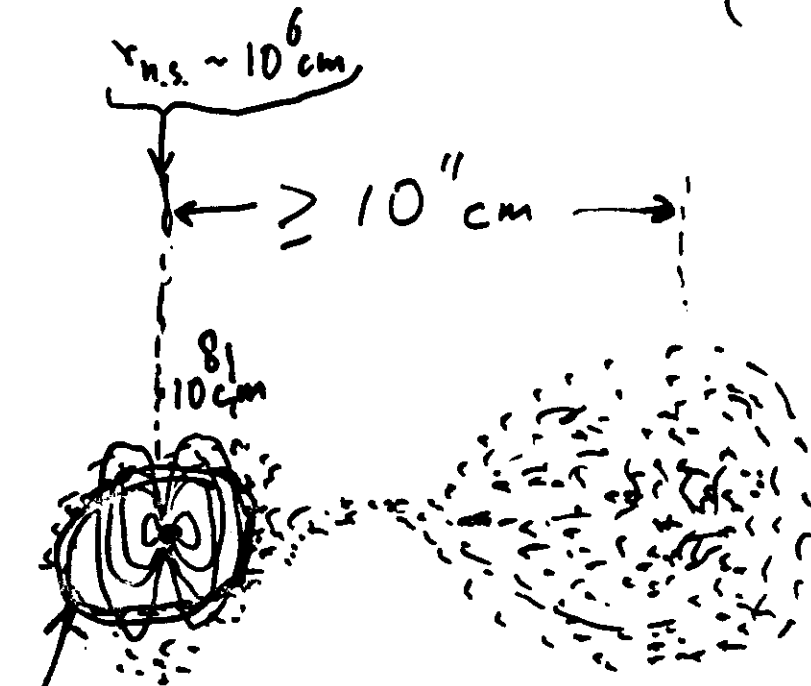
Pringle & Wade, X-ray Binaries

For $\dot{M} = 10^{18} \text{ g/s}$ ($\sim$ Eddington limit)



Example of an accretion-driven mechanism 13

Shock Acceleration: Kazanas & Ellison
(Nature 319 30 Jan 86)



shock when $\rho v^2 \sim \frac{B^2}{8\pi} \Rightarrow r \lesssim 10^8 \text{ cm}$

Strong B field: $B \sim \frac{10^{30} \text{ Gauss cm}^3}{r^3}$

E_{max} for $T_{\text{accel}} \sim T_{\text{synchrotron}}$

$$E_{\text{max}} \sim 10^5 - 10^8 \text{ GeV}$$

changing accretion rate ($\Delta \rho$)

$\Rightarrow$ change Alfvén radius

$\Rightarrow$ change E_{max} ($+\Delta \rho \Rightarrow -\Delta E_{\text{max}}$)

- Shock may occur in accretion flow at Alfvén radius but full accretion energy is not released unless $B_* \gtrsim 10^8$ Gauss so $R_A \sim R_*$.

- Shock may occur near polar cap for $B_* \gg 10^8$ Gauss

but then
$$\frac{B^2/8\pi}{\rho v^2} > 1$$

in acceleration region and shock acceleration fails (because B field dominates plasma flow rather than vice versa)

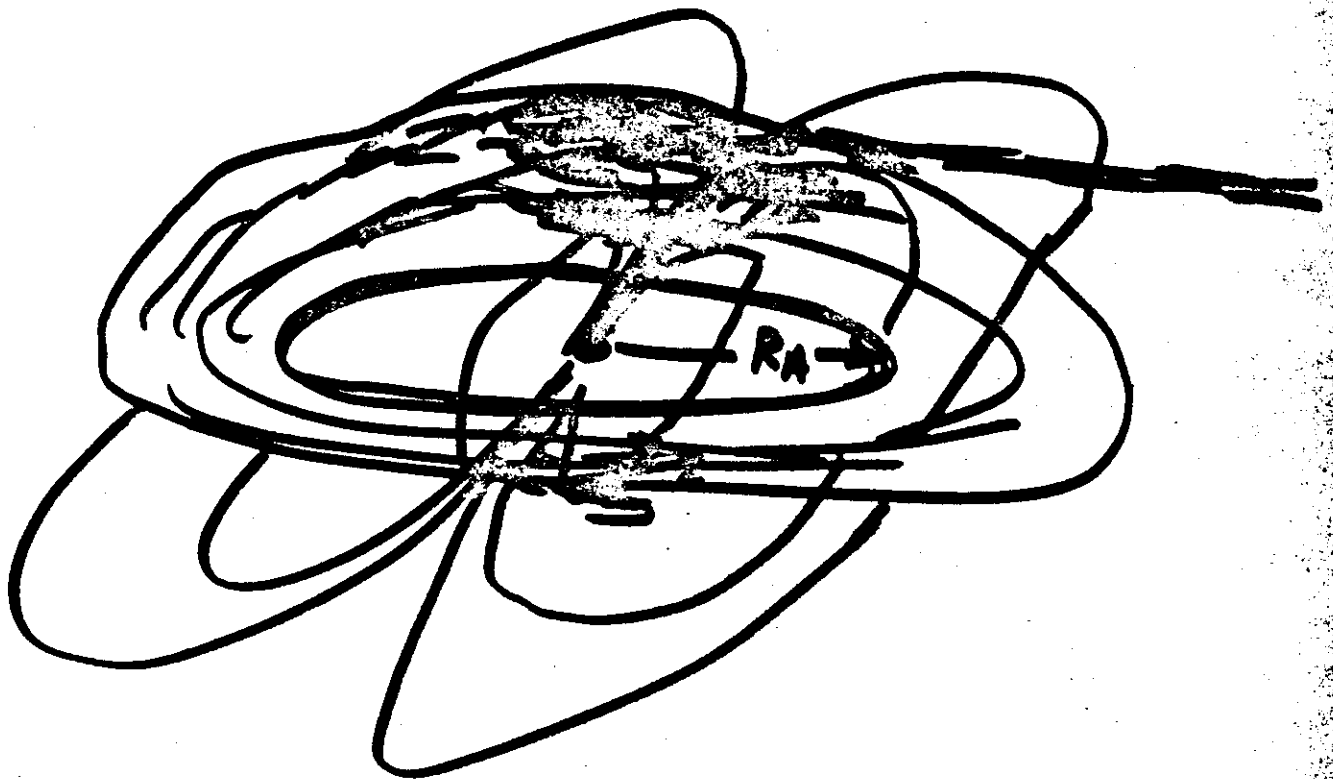
Conclusion: shock acceleration works only for accretion onto n.s. with low B

[Kozma & Elliman, Nature 319 280 (1986)]

Differential rotation of pulsar and disk (homopolar generator)

Channugan & Brecher, Nature 313, 767
(1985)

Cheng & Ruderman



$$E = \frac{c}{c} v B \Delta r \quad | \quad R \sim \Delta r \sim R_A$$

$$v_{\text{Kepler}}(R_A) = \sqrt{\frac{GM_*}{R_A}}$$

Problem: show

$$E_{\text{max}} \sim 2 \times 10^4 \text{ TeV} \quad B_8^{-3/7} \quad L_{38}^{5/7}$$

Both shock acceleration &
homopolar generator require

$B_* \geq 10^8 \text{ G}$ to work

$\therefore$ fail for the X-1, $B_* > 10^{12} \text{ G}$

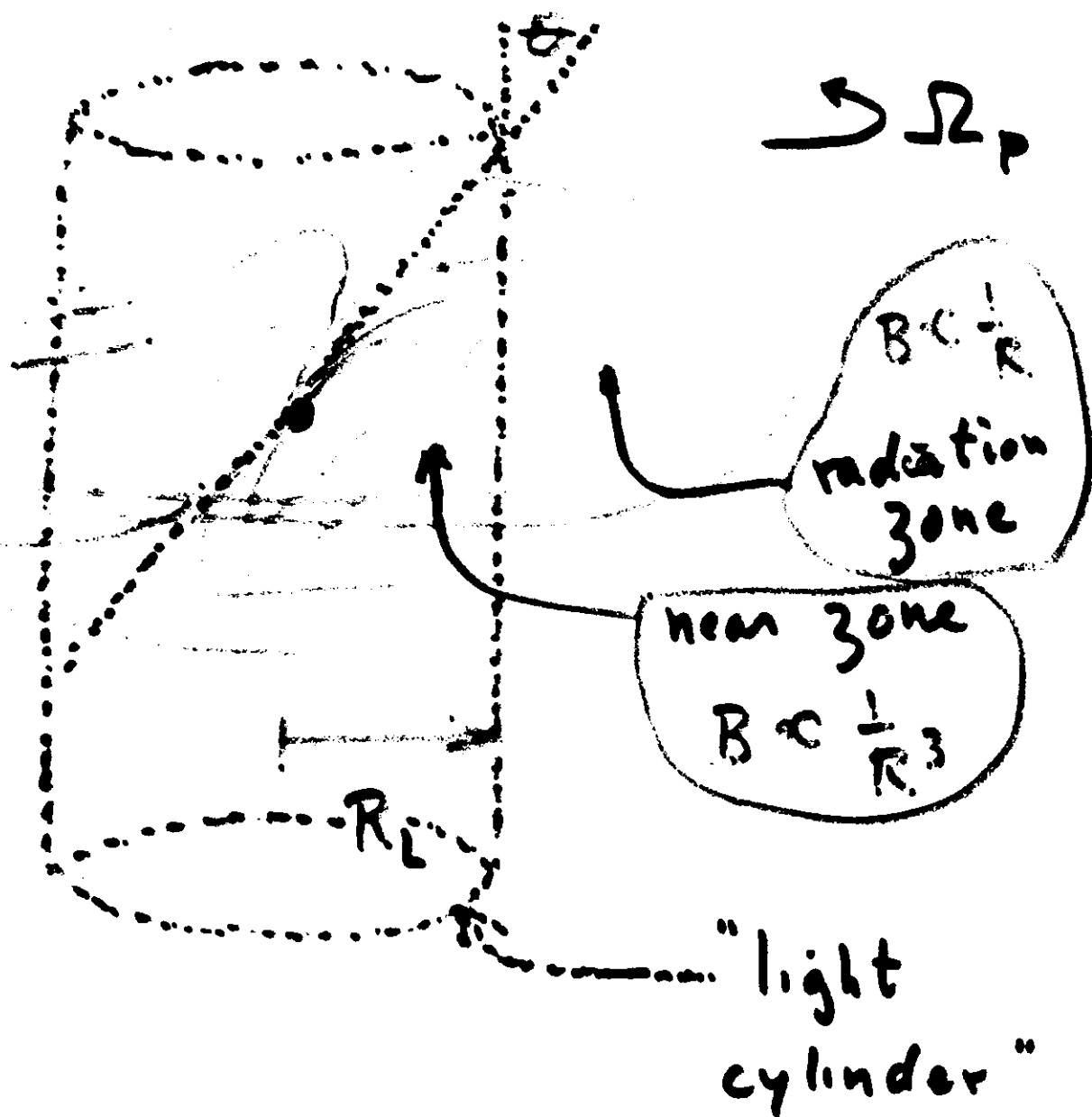
B_* (Cyg X-3) not known

Another possibility: accretion
generated turbulence in
MHD accretion flow

(more energetic analog of
acceleration of 1-10 GeV
particles by turbulence on
the Sun)

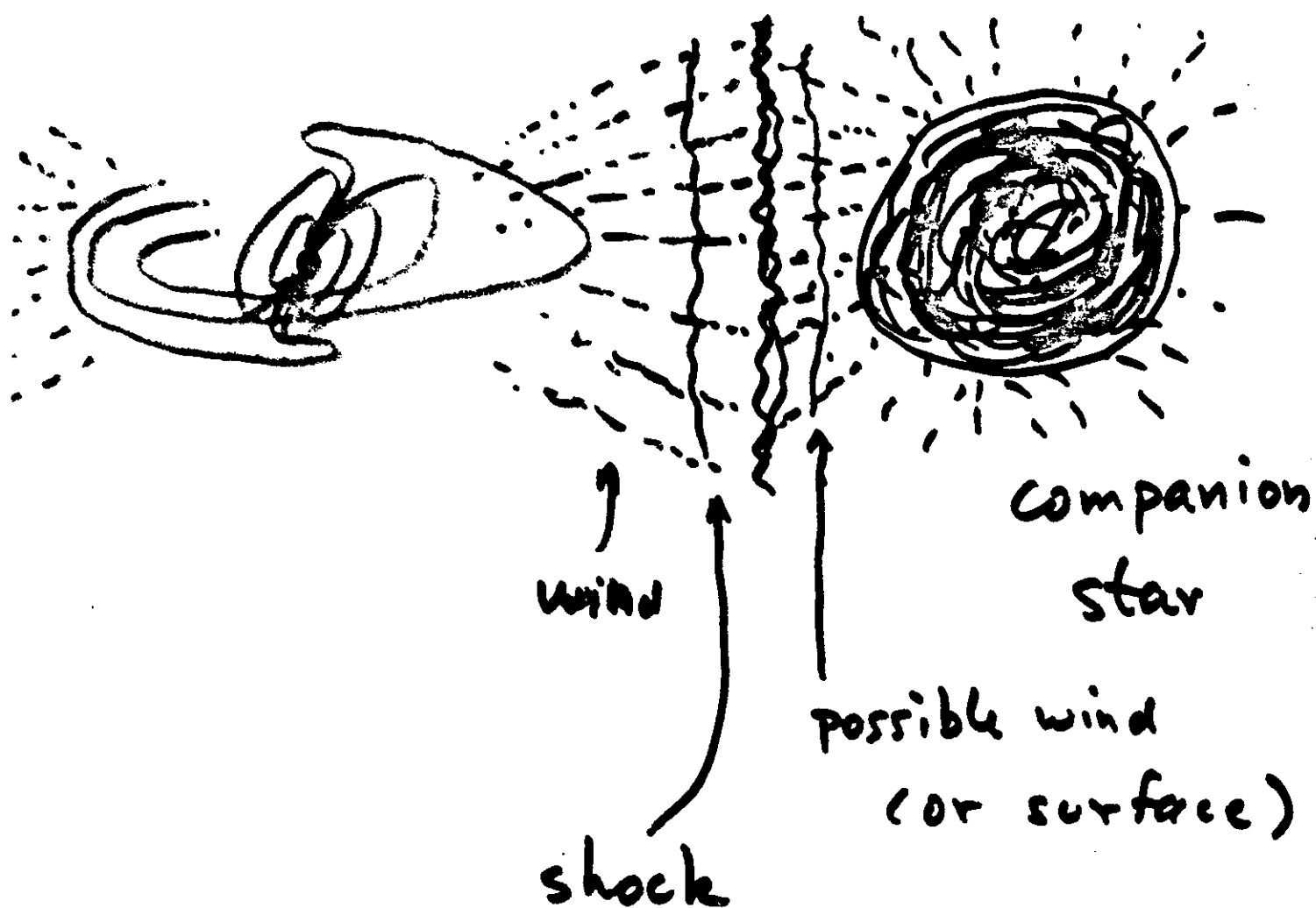
Wang, Astron. & Space Sci
121, 193 (1986).

what happens if $\Omega_p > \Omega_c$?



$$L_D = \frac{2}{3} \frac{\mu^2 \Omega_p^4}{c^3} \sin^2 \theta$$

This turns into relativistic, positronia wind of a plasma created by electrons pulled off n.s. surface by strong $\mathbf{v} \times \mathbf{B}$ force, which then cascade.



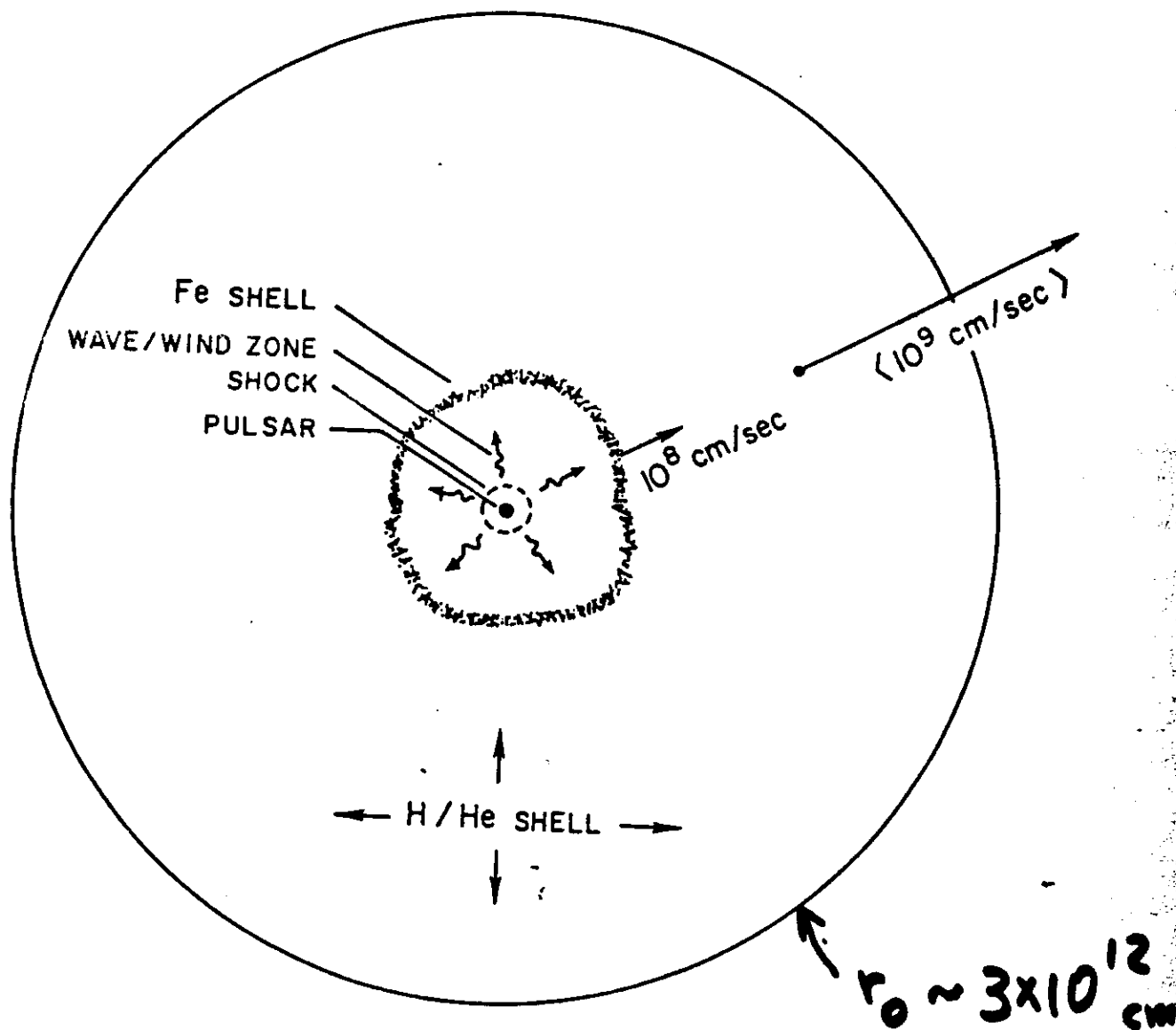
Bignami, Maraschi & Treves

Astroph. Astrophys. 55, 155 (1977)

proposed this as site of X-rays
in Cyg X-3.

The associated shock could also serve
as a site for acceleration
(TKC & A. Harding)

Michel, Kennel & Fowler, Science



Acceleration of particles:

a) How much power?

b) Character of beam —

Energy spectrum, $E_{\max}$?

a) Pulsar power

$$L = \frac{2}{3} \frac{\mu^2 \Omega^4}{c^3} \sin^2 \theta \sim 2 \times 10^{39} \frac{\text{erg}}{\text{s}} \times (B_{12}^2 P_{10}^{-4})$$

$$\mu = B_* R^3, \quad \Omega = \frac{2\pi}{P} \text{ as example}$$

scale to $B = 10^{12}$ Gauss, $P = 10$ ms.

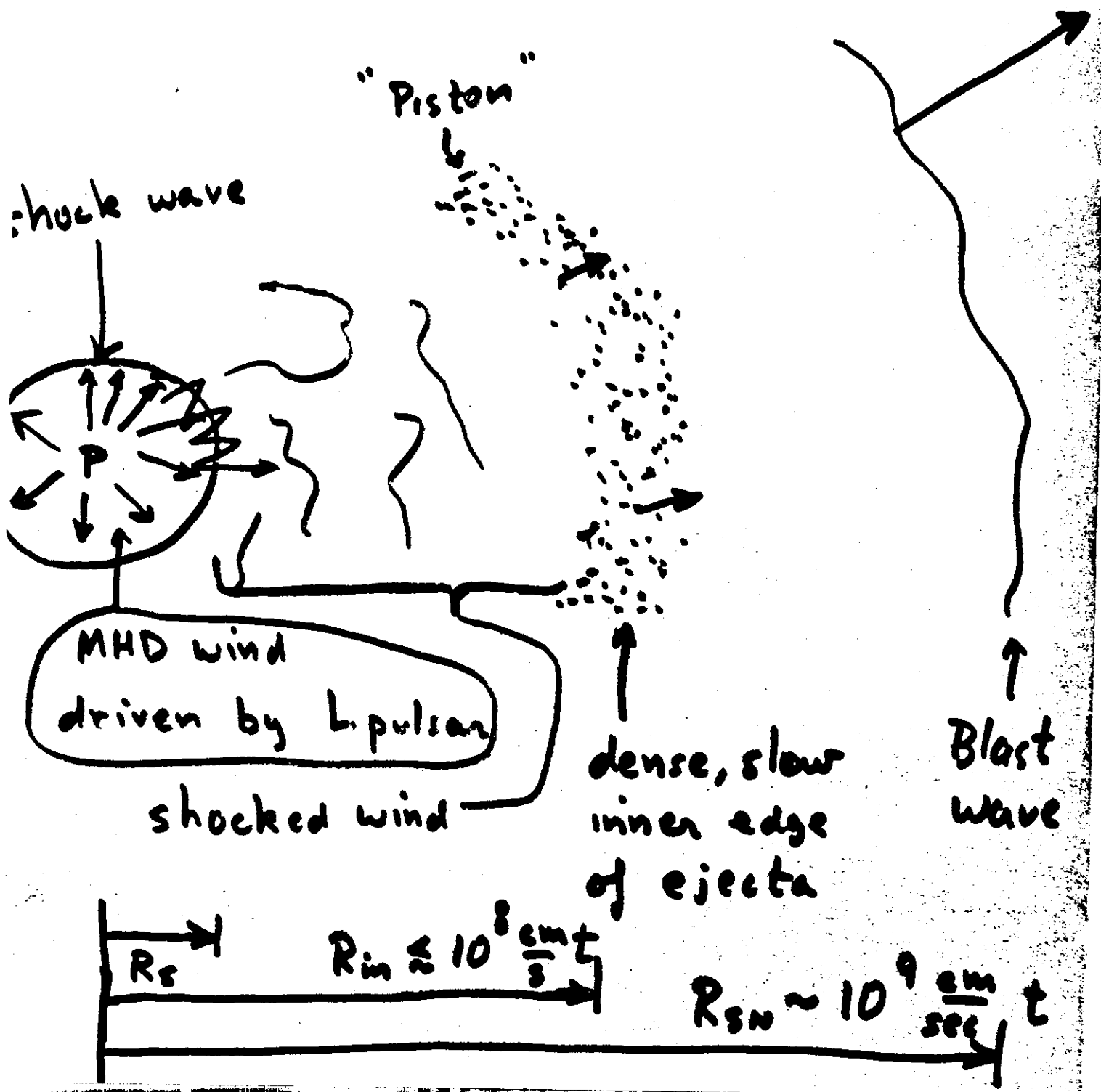
[Stability requires $P \gtrsim 1$ ms]

$$\tau_{\text{acc}} \sim \frac{\frac{1}{2} I \Omega^2}{L} \sim 3000 \text{ yrs} \left(\frac{P_{10}}{B_{12}} \right)^2$$

b) Spectrum of beam -
depends on acceleration
mechanism. One possibility:

TKG, Harding & Stanev

NATURE 329, 314 (1987)

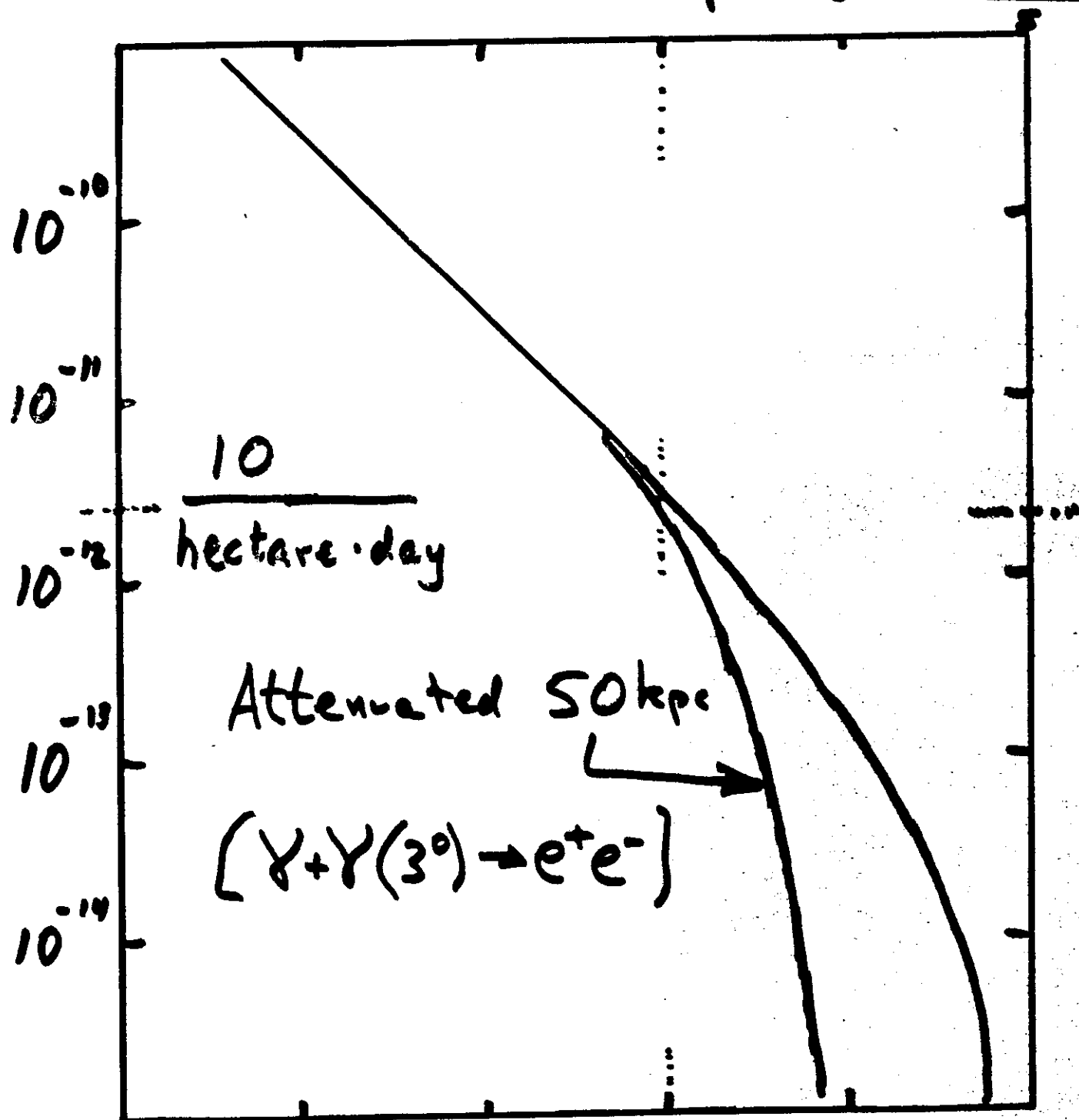


APR 12
TRG, Harding

& Stanev

$$L_p = 10^{40} \text{ erg}$$

$$F_\gamma(>E_\gamma) (\text{cm}^{-2} \text{s}^{-1})$$



10⁻¹⁰

10⁻¹¹

10⁻¹²

10⁻¹³

10⁻¹⁴

1 10 100 1000

E_γ (TeV)

$$\frac{L}{4\pi R_s^2 c} = \frac{\int L dt}{\frac{4}{3}\pi R_{in}^3} \quad \left\{ \begin{array}{l} \text{Pacini \& Salp\^ete} \\ \text{Rees \& Gunn} \end{array} \right.$$

$$\Rightarrow \frac{R_s}{R_{in}} \sim \sqrt{\frac{P_{in}}{3}} \lesssim 0.1$$

Given $R_{in} = U_{in} t$ calculate

$$B_s \sim 3 \text{ Gauss} \quad B_{12} P_{10}^{-2} t_{yr}^{-1} U_8^{-3/2}$$

$$B(r) = B_*/r^3 \quad r \leq \text{light cylinder}$$

$$B(r) = \frac{B_*}{(r_{L.e.})^3} \frac{r_{L.e.}}{r} \quad r \text{ in radiation zone}$$

E_{max} from $R_{Larmor} < R_s$

$$R_s \sim 10^{14} \text{ cm } t_{yr} U_8^{3/2}$$

$$E_{max} < e B_s R_s \sim 8 \times 10^4 \text{ TeV } (B_{12} P_{10}^{-2})$$

note cancellation of $t + U_{in}$!