



INTERNATIONAL ATOMIC ENERGY AGENCY  
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION



**INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS**  
34100 TRIESTE (ITALY) - P.O.B. 586 - MIRAMARE - STRADA COSTIERA 11 - TELEPHONE: 2240-1  
CABLE: CENTRATOM - TELEX 460392 - I

**SMR.379/33**

**COURSE ON BASIC TELECOMMUNICATIONS SCIENCE**

**9 January - 3 February 1989**

**"Spread Spectrum Communications"**

**J. G. Lucas**

**Dept. of Electrical Engineering, University of Sydney, Australia**

**These notes are intended for internal distribution only.**

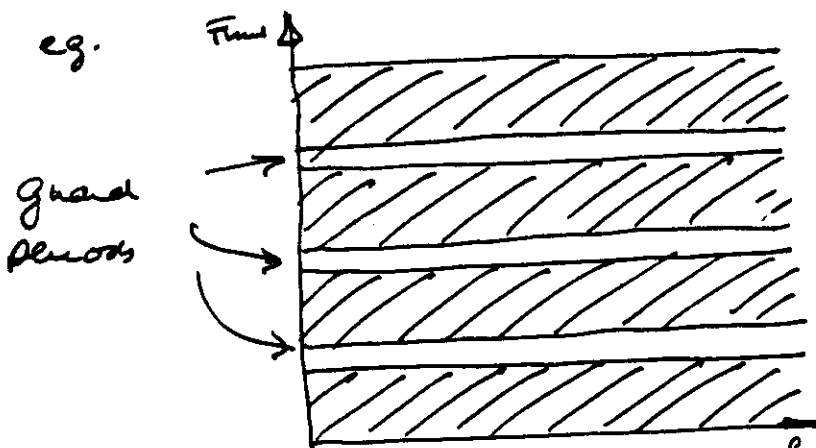
## SPREAD SPECTRUM SYSTEMS. (DS & FH).

Broadly defined as situations where we spread a signal into a spectrum which is very much larger than the minimum requirement of the mechanism of spreading is quite separate from our signal.

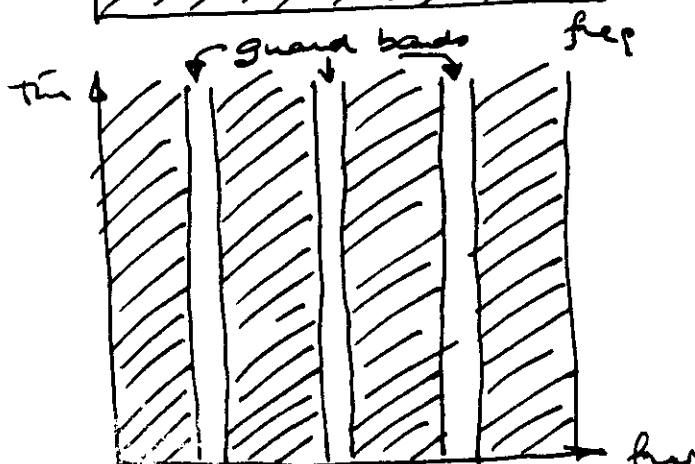
So FH is not considered to be a spread spectrum signal. However it is worth noting there can signal/wave advantages. One basic Adv is  $\propto$  duration ratio<sup>2</sup>. This is in a sense a 'Process Gain'.

A similar example might spread a single voice channel into many megahertz.

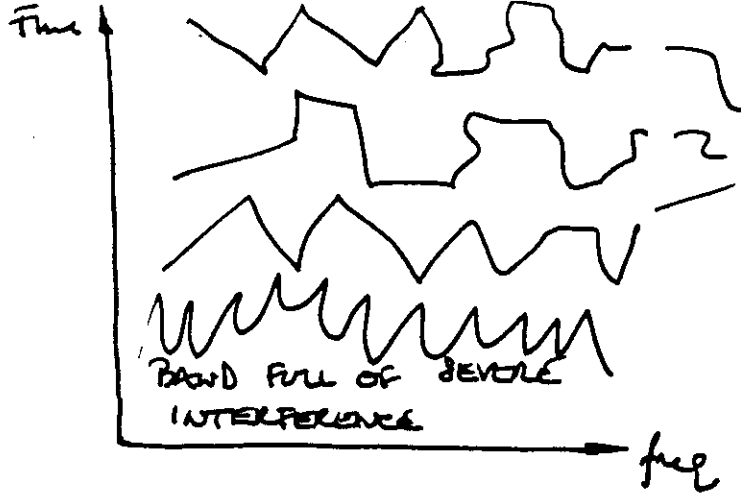
So given a band of frequency it is a function of how you use it



represents Time Domain Multiplexing - TDM.



represents Frequency Domain Multiplexing.



idea of Spread, Separately coded and Spread spectrum signals.

- no guard bands
- low power level
- immense coding

Early developments driven by military applications only, relatively recently, that SS techniques are being developed & argued in an open literature.

- again the process is being driven by the developments & ability of digital technology.

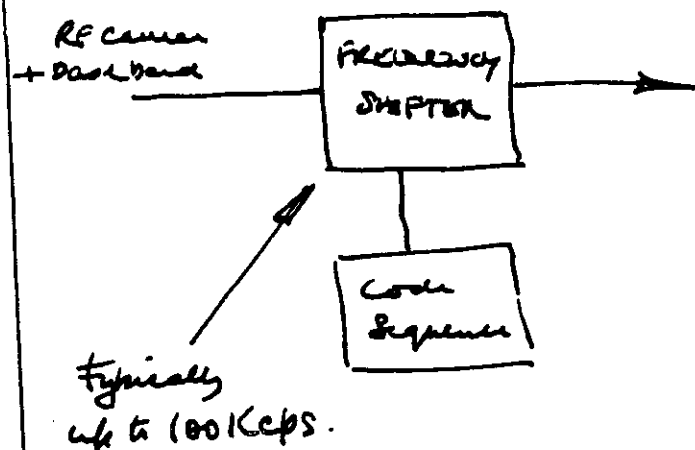
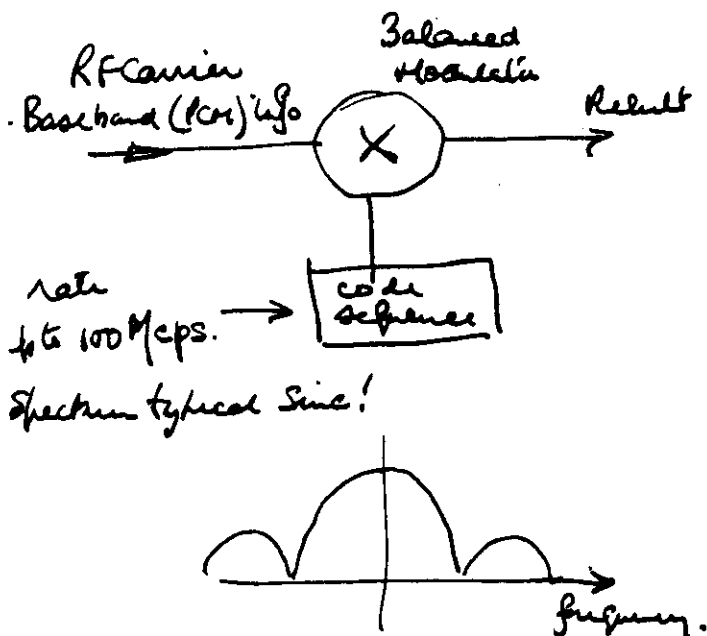
- Examples of use
- Military applications
  - Satellite communication & uplink
  - Navigation
  - Ranging - GPS (Global Positioning System).

Two main types:

when phase coherence is possible  
Effectively use subtle PSK ideas.

Called Direct Sequence (DS) } S.S.  
① Pseudo Noise (PN)

when phase coherence is not available (eg high speed aircraft transmission) we use  
FREQUENCY HOPPING (FH)



The Base Code generation clock rate is called the 'chip' rate (also equals the hop rate in FH)

Similarly, to properly receive the baseband information the receiver must also know the same code which must just be synchronized with the transmitter & then multiplied.

Whole basis of Spread Spectrum is based on Shannon's theorem of channel capacity

$$C = B \log_2 \left( 1 + \frac{S}{N} \right) \quad \text{where } \frac{S}{N} = \frac{\text{Signal}}{\text{noise}}$$

(Channel Capacity)      Bandwidth.  
bits/sec

$$\therefore \frac{C}{B} = 1.44 \log_e \left( 1 + \frac{S}{N} \right)$$

$$= 1.44 \left\{ \frac{S}{N} - \frac{1}{2} \left( \frac{S}{N} \right)^2 + \frac{1}{3} \left( \frac{S}{N} \right)^3 - \dots \right\}$$

If  $\frac{S}{N}$  very small eg  $< 0.1$

$$\text{then } \frac{C}{B} \approx 1.44 \frac{S}{N} \quad \text{i.e. } \frac{S}{N} \propto \frac{1}{B}$$

So that increasing  $B$  allows us to decrease  $\frac{S}{N}$ .

eg if  $\frac{S}{N} = \frac{1}{100}$  &  $C = 3000 \text{ bits/sec}$   $B_{\text{noise}} = 208 \text{ KHz}$ .

we define a Process Gain =  $\frac{\text{Bandwidth (Hz)}}{\text{Rate of info}}$       | eg  $\frac{208}{3} = 18.4 \text{ dB}$

The protection we have from interfering signals is defined by

$$\text{the Jamming margin} = \text{Process Gain} - \left[ \text{Loss}_{\text{spike}} + \left( \frac{S}{N} \right)_{\text{int}} \right]$$

For example

$$= 18.4 - [2 + 6] \quad \text{might be typical figures}$$

$$= 10.4$$

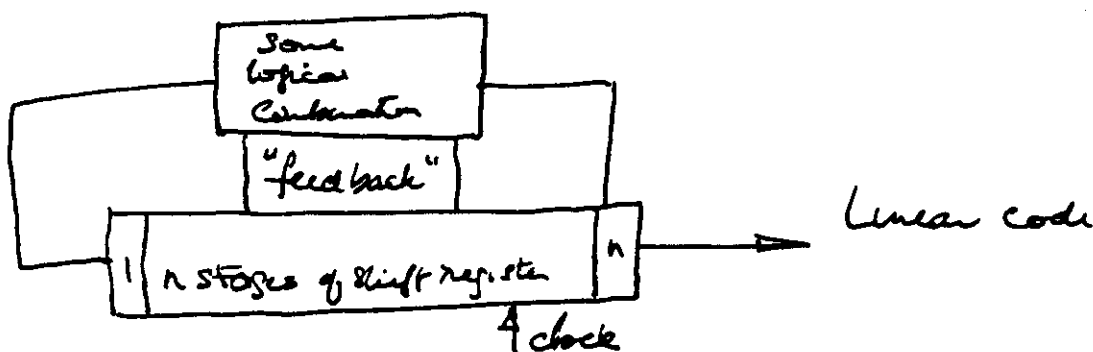
So if  $\frac{\text{interfering signal}}{\text{desired}} > 10.4$  no chance.

Narrowband interference is generally not a problem

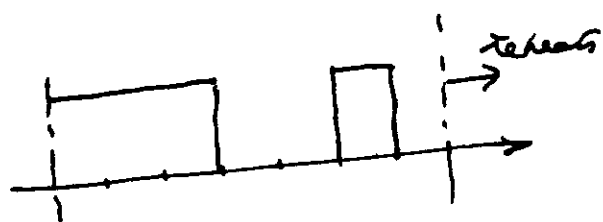
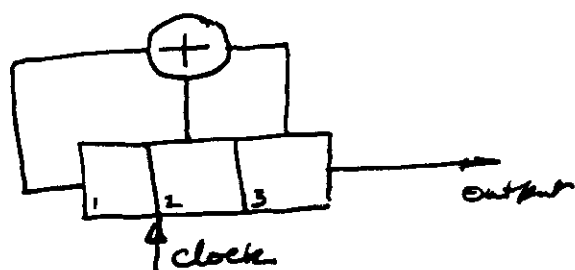
# Generating the coded sequence

Most common method used is an 'Maximal' sequence generated by a shift register

In general



Simple example 3 stage case:



Start  $u_0(\text{say})$  with all full 1's

| Shift registers |   |   | clock result |
|-----------------|---|---|--------------|
| 1               | 1 | 1 | 1            |
| 0               | 1 | 1 | 1            |
| 0               | 0 | 1 | 1            |
| 1               | 0 | 0 | 0            |
| 0               | 1 | 0 | 0            |
| 1               | 0 | 1 | 1            |
| 1               | 1 | 0 | 0            |
| --- repeats --- |   |   | repeats      |

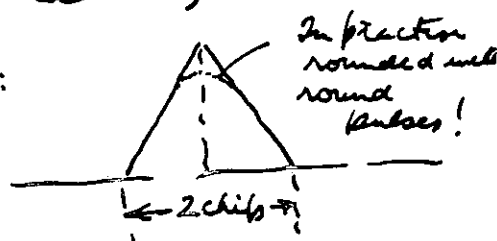
So length of sequence is  $2^n - 1$

It will contain  $\frac{2^n}{2}$  1's &  $\frac{2^n}{2} - 1$  0's !

unbalanced as mean statistically AC behaviour is small.

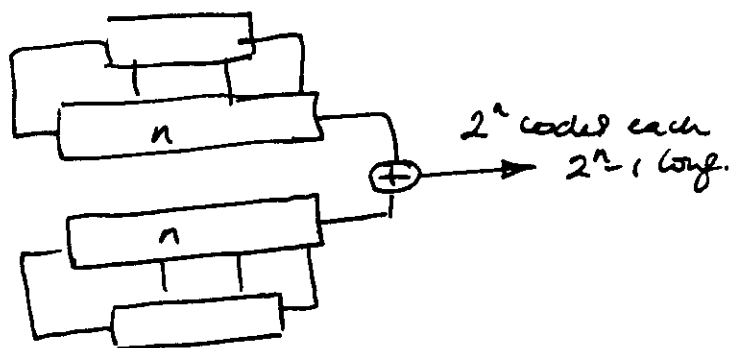
Typically use a 10 stage shift register  $\rightarrow$  1023 chips Maximal code.

Maximal sequences have the inherent property that they correlate exactly (remember convolution) & give:



easy to generate, any

eg



Example of GPS operation (see diagram)

### Some References

Spread Spectrum Systems by R.C. Dixon \* SUPPLS  
Published 1984 by WILEY BIBLIOGRAPHY.

The Spread Spectrum Concept  
by R.A. Scholtz IEEE Transactions on Communication  
vol com-25 no 8 August 1977 page 748.

Spread Spectrum Signals for Digital Communications  
Chapter 8 in PROAKIS.

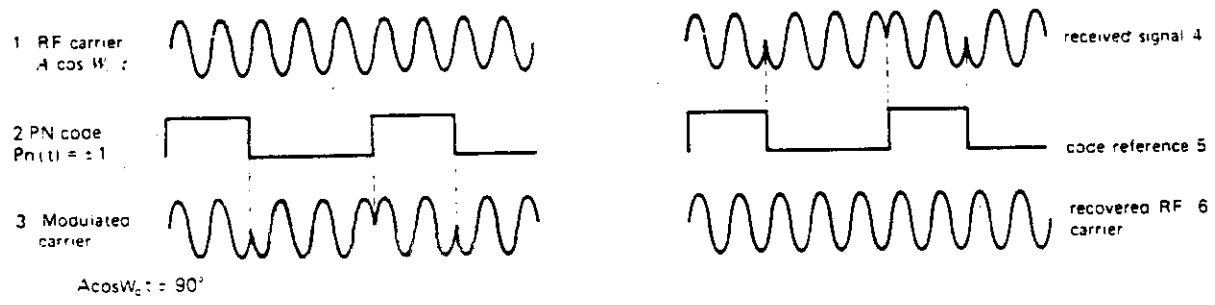
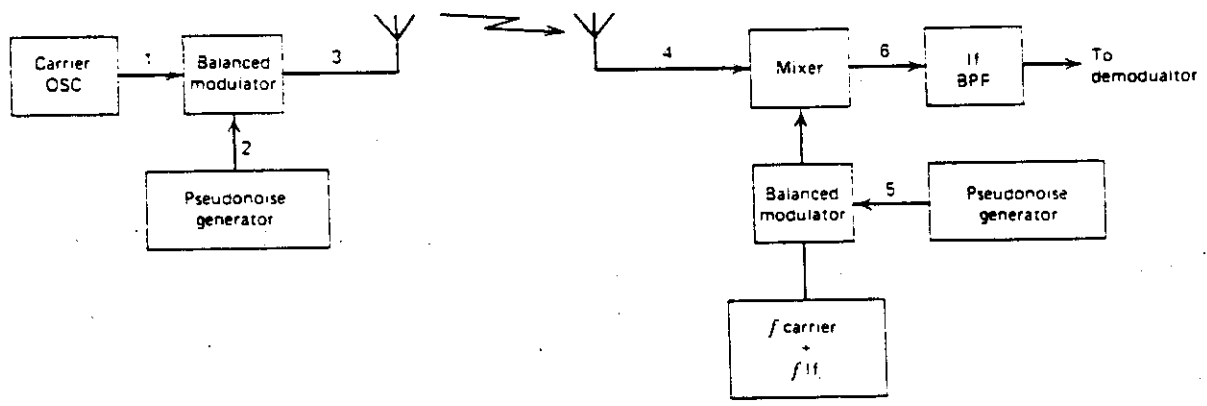
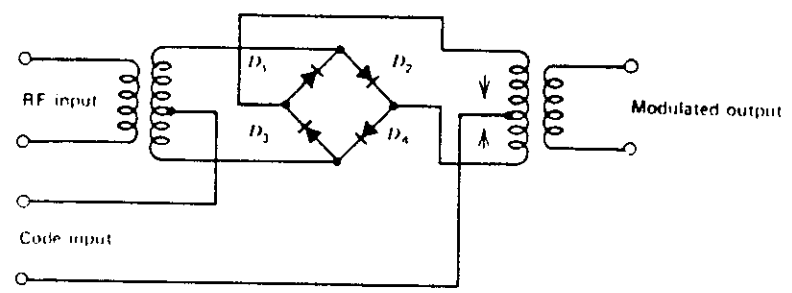


Figure 2.3 Overall direct sequence system showing waveforms.

Balanced modulation  
 very commonly available  
 up to  $> 100 \text{ MHz}$ .  
 $u_c t$   
 $B \cos W_c t$   
 $AB \cos u_c t \cos W_c t$   
 theoretically  
 no carrier  
 practically 20 - 60 dB down.



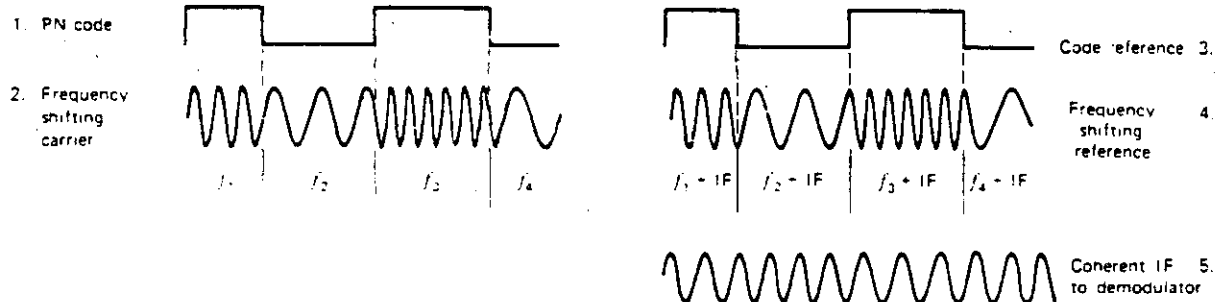
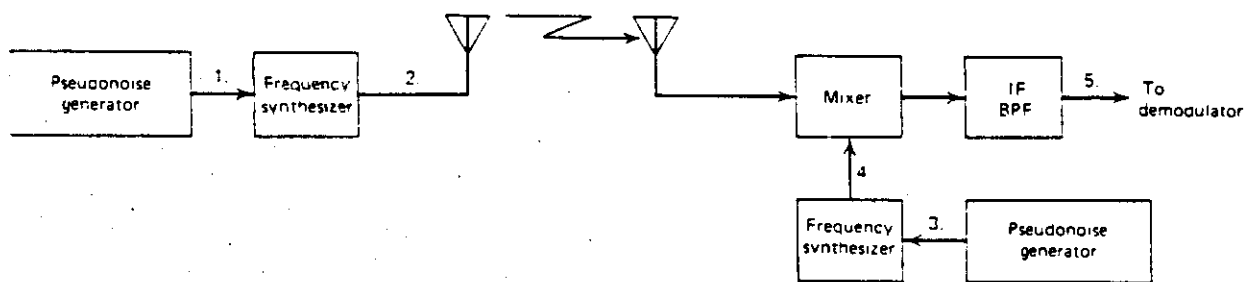
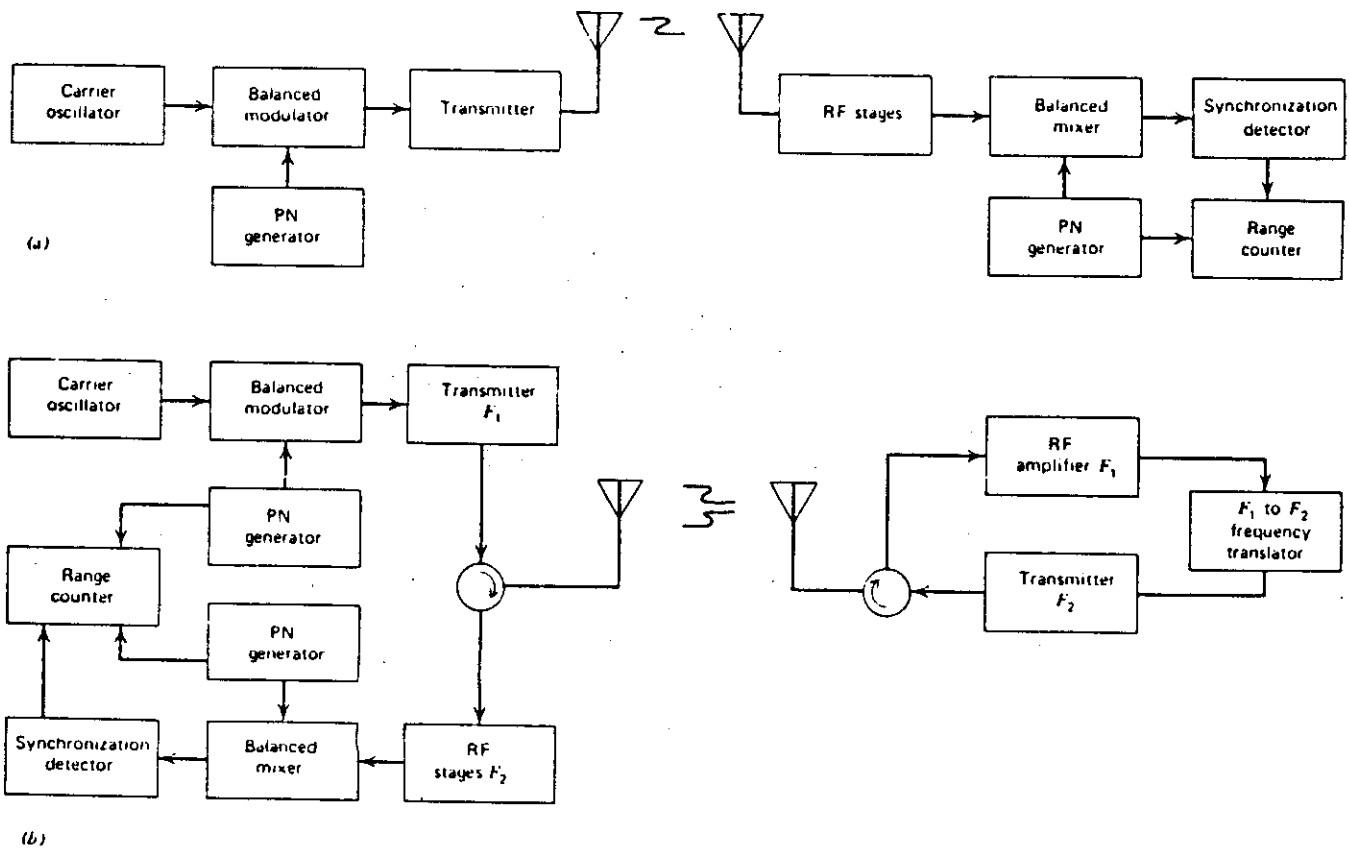


Figure 2.12 Basic frequency hopping system with waveforms.



**Figure 8.1** Simple direct sequence ranging systems: (a) transmit-receive ranging system; (b) duplex ranging system.

Short code (clear access or C/A):

1.023 Mcps  
1023 chips long  
Gold codes  
period, 1.0 msec

Long code (protected or P):

10.23 Mcps  
one week long  
 $6.19 \times 10^{12}$  chips  
mildly nonlinear code

Modulation:

1575 MHz  
I carrier, C/A code  
Q carrier, P code (suppressed 3 dB)  
1227 MHz  
P code only

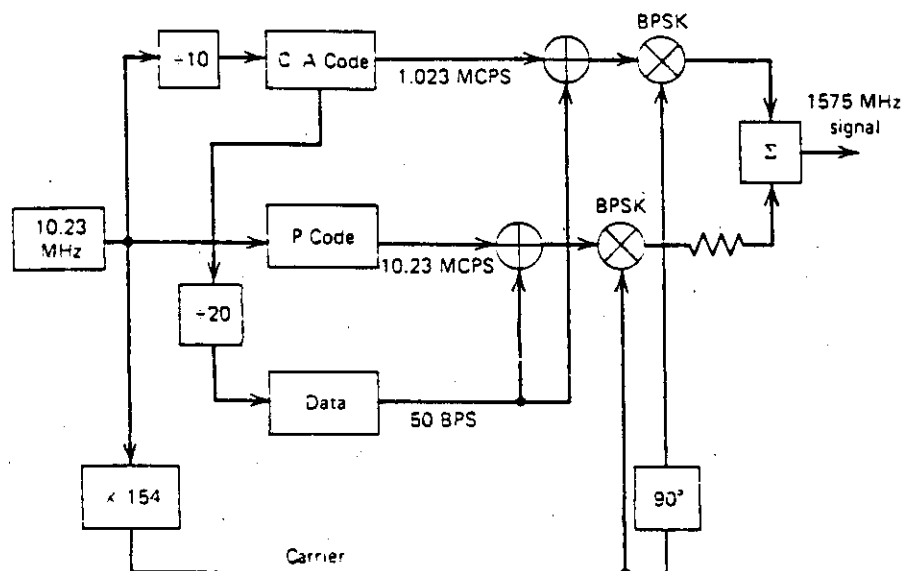


Figure 9.9 GPS modulator configuration. (L: signal)

1. A long code (one week repetition period) biphase modulated 1227 MHz signal.
2. A long code (same code) biphase modulated signal at 1575 MHz (← PROTECTED CODE.)
3. A short code (1023 chip Gold code) biphase modulated signal on an orthogonal carrier at 1575 MHz.