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A STRONG-COUPLING MECHANISM IN THE  
HIGH- $T_c$  COPPER OXIDES

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# IDENTIFYING THE PAIRING MECHANISM IN HIGH- $T_c$ SUPERCONDUCTORS

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## ABSTRACT

It is argued that the origin of the high transition temperatures observed in  $Ba_{1-x}K_xBiO_3$  and the copper-oxide superconductors with perovskite-related structures is due to two factors: (1) overlap of a partially filled  $\sigma^*$  band of primarily cation character and a  $\pi$  or  $\pi^*$  band of mostly O-2p<sub>x</sub> parentage permits charge transfer between cation and anion subarrays with oxygen-atom displacement perpendicular to a M-O-M bond axis and (2) bondlength mismatch places the M-O-M bondlength under a compressive or tensile stress. Relief of a compressive stress by the bending of a M-O-M bond from 180° introduces a strong electron-lattice interaction with holes; a 180° Cu-O-Cu bond allows strong electron-lattice coupling with electrons of a  $Cu^{2+/+}$  redox couple, but not with holes in a  $Cu^{3+/2+}$  redox couple.

## INTRODUCTION

A superconductor is a normal metal above its transition temperature  $T_c$ ; at temperatures  $T < T_c$ , a condensation of electron pairs is stabilized by the opening up of an energy gap  $2\Delta$  in the density of electron states at the Fermi energy  $E_F$ . Any alternate mechanism for opening up an energy gap  $E_g$  at  $E_F$  in the Hartree-Fock one-electron states, which would yield a normal semiconductor, is competitive with superconductivity.

Two cooperative phenomena that open up an energy gap  $E_g$  at  $E_F$  and thus compete with superconductivity are the formation of a charge-density wave (CDW) -- or a spin-density wave (SDW) -- and the correlation splitting (CS) associated with localized atomic magnetic moments [1]. The oxide system  $Ba_{1-x}K_xBiO_3$  represents a competition between CDW formation and superconductivity; the high- $T_c$  copper-oxide systems all represent a competition between CS and superconductivity.

The condensation of superconductive electron-pair states requires the existence of a coupling energy between the paired electrons that is greater than their coulomb repulsion. In conventional superconductors, Cooper pairs are formed by electron-phonon interactions. However, this pairing mechanism gives an upper limit to  $T_c$  near  $T_c = 40$  K; therefore, the observation of a  $T_c$  as high as 120 K has forced consideration of alternate mechanisms. Three basic approaches have been formulated: (1) a new type of electronic state: e.g., the resonating-valence bond (RVB) [2], (2) an electron-electron interaction to replace the conventional electron-phonon interaction; e.g., atomic polarization [3], excitons [4], magnetic bags [5], or spin-spin interactions between itinerant and localized electrons [6], and (3) strong electron-lattice interactions -- probably enhanced by a high electronic polarizability -- that may give rise to the condensation of large polarons visualizable in real space [7]. In order to distinguish between these three approaches, it is necessary to inquire into two aspects of the high- $T_c$  oxide superconductors: their distinguishing electron configurations near  $E_F$  and any unique structural features that could introduce unusual electron-lattice coupling.

## THE SYSTEM $Ba_{1-x}K_xBiO_3$

The compound  $BaBiO_3$  has a structure derived from the cubic perovskite structure, Fig. 1. In this ABO<sub>3</sub> structure, the tolerance factor

$$t = (r_A + r_O)/\sqrt{2}(r_B + r_O) \quad (1)$$

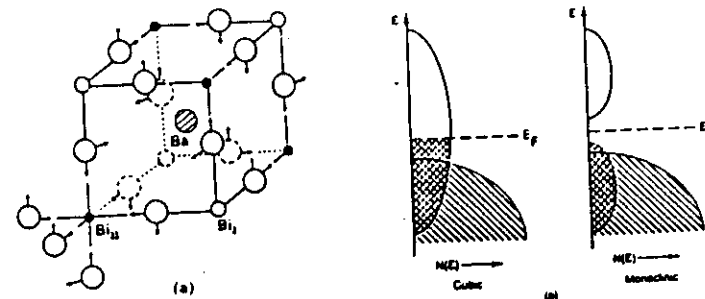
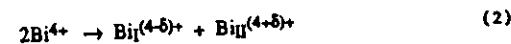


Fig. 1 (a) The cubic perovskite structure of high-temperature  $BaBiO_3$  and, arrows, the direction of the oxygen-atom displacements on transforming to the monoclinic structure. (b) The energy density  $N(E)$  of one-electron states near  $E_F$  for (i) cubic and (ii) monoclinic  $BaBiO_3$ .

which relates the A-O and B-O bond lengths, represents ideal bondlength matching for  $t = 1$ . Since the A-O and B-O bonds have different thermal-expansion coefficients,  $t$  increases with increasing temperature; therefore the condition  $t = 1$  can, at best, only be satisfied at one temperature. At  $t = 1$  at the formation temperature results in a  $t < 1$  at lower temperatures. A  $t < 1$  places the B-O bonds under compression, the A-O bonds under tension. This incompatibility can be relieved by a cooperative rotation of the  $BO_6$  octahedra that bends the B-O-B bond. In  $BaBiO_3$ , such a cooperative rotation about a [110] axis represents only one component of the oxygen-atom displacements. The second component shown in Fig. 1 is due to the formation of a "negative U" CDW.

In an octahedral site of oxide ions, covalent mixing between Bi-6s and O-2p<sub>g</sub> orbitals makes small (< 2 eV) any intraatomic CS between the 6s<sup>1</sup> and 6s<sup>2</sup> energy levels at  $Bi^{4+}$  and  $Bi^{3+}$  ions and it introduces a significant 180° Bi-O-Bi interatomic interaction. In this situation, a bandwidth  $W > U$ , where  $U$  is the CS, suppresses the formation of any bismuth magnetic moment in the absence of an applied magnetic field; however, the bandwidth is narrow enough to sustain the formation of a CDW. As shown in Fig. 1, oxygen displacements toward  $Bi_{II}$  atoms and away from  $Bi_I$  atoms introduces distinguishable Bi subarrays and a charge transfer represented formally by



A  $\delta = 1$  would correspond to the chemical disproportionation of  $Bi^{4+}$  into  $Bi^{3+}$  and  $Bi^{5+}$ ; in fact, a smaller  $\delta = 0.5$  occurs [8]. The resulting change in translational symmetry introduces a splitting of the  $\sigma^*$  band of primarily Bi-6s parentage, and monoclinic  $BaBiO_3$  is a diamagnetic semiconductor.

The CDW has its maximum stability where a band is half-filled [1]. Shifting of  $E_F$  either up or down by reduction or oxidation of the  $BiO_3$  array requires a change in the wavelength of the CDW with subsequent lowering of its stability and hence of the transition temperature  $T_1$  below which it is formed. Although a single-band picture would be symmetric with respect to reduction vs oxidation, it is apparent from Fig. 1(b) that this symmetry may not be applicable to  $BaBiO_3$  because of the overlap of the  $\sigma^*$  and  $\pi$  bands.

Substitution of K for Ba in  $Ba_{1-x}K_xBiO_3$  oxidizes the  $BiO_3$  array, which lowers  $E_F$  into the lower  $\sigma^*$  band and/or the  $\pi$  band. A tentative phase diagram for the system [9,10] shows that the commensurate CDW associated with the monoclinic structure of low-temperature  $BaBiO_3$  gives way to a more complex CDW in the compositional interval

$0.1 < x < 0.25$ ; complete suppression of the CDW in the interval  $0.3 < x < 0.5$  gives a cubic superconductor with a  $T_c$  as high as 30 K at smaller  $x$ . This phase appears to be described as a Bardeen-Cooper-Schrieffer (BCS) superconductor with weak to moderate electron-phonon coupling.

The cubic phase is characterized by a large-amplitude oxygen vibration perpendicular to the Bi-O-Bi bond axis [11]. Oxygen displacements perpendicular to the bond axis introduce (or enhance) a  $\pi$  component into the conduction-band states at  $E_F$ , which would stabilize electrons at neighboring Bi atoms. Thus the large-amplitude oxygen vibrations would couple strongly to conduction electrons because the overlap of  $\sigma^*$  and  $\pi$  bands makes polarization fluctuations sensitive to the oxygen displacements.

#### THE SYSTEM $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

Where  $W = U$  occurs at a bandwidth  $W$  that is too great for CDW formation, a half-filled band having  $W < U$  is split in two by the correlation splitting  $CS$  [1]. A  $CS$  has its maximum stability where the conduction band is half-filled; the atoms associated with the half-filled band are all single-valent.

The introduction of either electrons into the upper Hubbard band or holes into the lower Hubbard band creates a mixed-valent situation; the charge carriers thus created may move diffusively as small polarons, as itinerant charge carriers without any activation energy in the mobility, or by variable-range hopping from one dopant center to another. Small polarons do not give rise to a well-defined Fermi surface and hence do not condense out as superconductive pairs. The mobile charge carriers are transformed from small polarons to itinerant carriers as the bandwidth increases to the value  $W = U$  where the bandgap  $E_g$  due to  $CS$  disappears. Moreover, the introduction of charge carriers into either the upper or lower Hubbard band reduces  $U$ . Therefore doping an antiferromagnetic semiconductor ( $W < U$ ) having a  $W$  only a little smaller than  $U$  for a half-filled band may lower  $U$  to where the condition  $W > U$  applies. As  $W$  exceeds  $U$  with increased doping, the Néel temperature  $T_N$  below which long-range antiferromagnetic ordering occurs must decrease; the atomic magnetic moment also decreases, but a  $CS$  and reduced atomic magnetic moments may persist into a phase exhibiting only short-range magnetic order.

This situation appears to be illustrated by the system  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ ; but as in the case of  $\text{Ba}_{1-x}\text{K}_x\text{BiO}_3$ , the band symmetry is removed by an overlap of the  $\sigma^*_{x^2-y^2}$  conduction band and a  $\pi^*$  band of primarily  $\text{O}-2p_x$  parentage, see below.

Fig. 2 illustrates the high-temperature tetragonal structure of the antiferromagnetic semiconductor  $\text{La}_2\text{CuO}_4$ . The tolerance factor  $t$  relating the  $\text{La}-\text{O}$  and  $\text{Cu}-\text{O}$  bondlengths is identical to that of the perovskite structure, equation (1), and a thermal-expansion mismatch makes  $(1-t)$  increase with decreasing temperature. The resulting compressive stress on the  $\text{Cu}-\text{O}$  bonds is relieved by a cooperative tilting of the elongated  $\text{CuO}_6$  octahedra around a  $[110]$  axis, which reduces the symmetry from tetragonal to orthorhombic at lower temperature.

Band-structure calculations for  $\text{La}_2\text{CuO}_4$  give a Fermi energy  $E_F$  lying in a broad  $\sigma^*$  band just above the top of a  $\pi^*$  band [12,13]. However, the observation of antiferromagnetic order with a copper magnetic moment  $\mu_{\text{Cu}} = 0.5 \mu_B$  [14] indicates that the band-structure calculation must be amended by the introduction of a  $CS$  of the  $\sigma^*$  band, Fig. 3(a). Moreover, observation of a  $\mu_{\text{Cu}}$  demonstrates that the top of the  $\sigma^*$  band is primarily of  $\text{Cu}-3d$  parentage, and a large tetragonal ( $c/a > 1$ ) distortion of the  $\text{CuO}_6$  octahedra makes the assignment primarily  $\text{Cu}-3d_{x^2-y^2}$  parentage. A  $\sigma^*_{x^2-y^2}$  band containing one hole per  $\text{Cu}$  atom is just half-filled, and the reduction of  $\mu_{\text{Cu}}$  from  $1 \mu_B$  indicates that  $W < U$  approaches  $W = U$ .

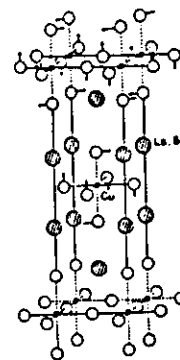


Fig. 2 The tetragonal (T)  $\text{K}_2\text{NiF}_4$  structure of high-temperature  $\text{La}_2\text{CuO}_4$ . Arrows indicate directions of oxygen-atom displacements on transforming to the orthorhombic phase.

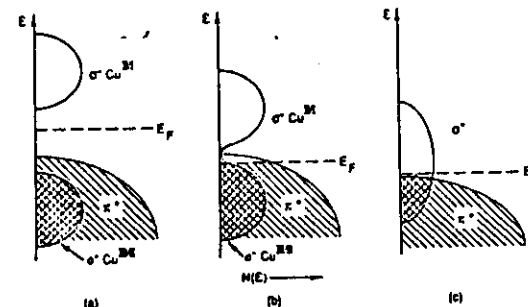


Fig. 3 Schematic energy density  $N(E)$  of one-electron states for  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ : (a)  $x = 0$ , (b)  $x = 0.15$ , (c)  $x = 0.4$ .

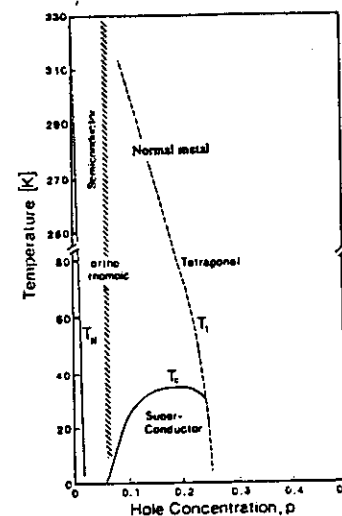


Fig. 4 Tentative phase diagram for  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ .

Substitution of  $\text{Sr}^{2+}$  for  $\text{La}^{3+}$  oxidizes the  $\text{CuO}_2$  layers and yields the tentative phase diagram shown in Fig. 4 provided a high pressure of oxygen is used for  $x > 0.15$  to retain full oxygen stoichiometry [15]. We address three questions:

- How does  $\mu_{\text{Cu}} = 0.5 \mu_{\text{B}}$  in  $\text{La}_2\text{CuO}_4$  change on crossing the transition from an antiferromagnetic semiconductor to a superconductor?
- Where are the mobile holes that condense into superconductive pairs?
- Can we identify an unusual electron-lattice coupling?

In order to investigate the first question, we prepared  $\text{La}_2\text{CuO}_{4+\delta}$  at 23 kbar and 800 °C in a double high-pressure cell containing  $\text{CrO}_3$  on one side and  $\text{La}_2\text{CuO}_4$  on the other of a stabilized-zirconia disc permeable to oxygen [16]. Decomposition of  $\text{CrO}_3$  to  $\text{Cr}_2\text{O}_3$  and  $\text{O}_2$  creates a high oxygen pressure on the sample. Introduction of interstitial oxygen oxidizes the sample, and it becomes a superconductor ( $T_c = 30$  K). The interstitial oxygen enters sites between two  $\text{LaO}$  layers that are coordinated by four La and four O atoms [17]. We had predicted that the interstitial oxygen would be present in this site as  $\text{O}^{2-}$ , a prediction born out for the interstitial oxygen in  $\text{La}_2\text{NiO}_{4.13}$  [18]. However, in  $\text{La}_2\text{CuO}_{4.03}$  cooled rapidly enough to lowest temperatures that phase separation below room temperature -- observed in polycrystalline samples [19] -- did not occur, the interstitial oxygen forms a complex cluster with two of the four neighboring oxygen atoms [17]. From the O-O distances of the cluster, it might be argued that one hole per interstitial oxygen is trapped at the interstitial oxygen. However, trapping of one hole at an oxygen cluster centered at the interstitial oxygen does not reconcile the discrepancy in the value of  $\delta = 0.05$  determined by iodometric titration and  $\delta = 0.14$  by thermogravimetric analysis (TGA) [16]. A similar discrepancy was reported for samples prepared at lower oxygen pressures [20]. We interpreted the discrepancy to indicate  $\delta = 0.05$  interstitial  $\text{O}^{2-}$  ions in the bulk and ca. 0.1 superficial oxygen introduced at high pressure. In either case, the observed  $T_c$  is consistent with the introduction of about 0.1 holes per Cu atom in the  $\text{CuO}_2$  sheets.

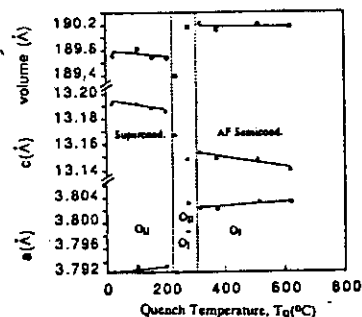


Fig. 5 Variation of room-temperature volume and lattice parameters with quench temperature  $T_q$  for  $\text{La}_2\text{CuO}_{4+\delta}$  heated successively to higher  $T_q$ .

Whatever the exact character of the interstitial oxygen, the TGA curve shows an abrupt loss of oxygen in the interval 225 <  $T$  < 275 °C [16]. Fig. 5 gives the variation in room-temperature lattice parameter with quench temperature  $T_q$  for a high-oxygen-pressure sample raised successively to higher  $T_q$  in air before quenching to room temperature for X-ray diffraction. A first-order phase change occurs in the interval 225 <  $T_q$  < 275 °C, which yielded two phases: the low-temperature superconductor and the high-temperature antiferromagnetic semiconductor. A small increase in volume with loss of interstitial oxygen results from a remarkable increase in  $1/2(a+b)$ . The increase in Cu-O bondlength on going to the antiferromagnetic phase is even more pronounced as the Cu-O-Cu bond angle becomes more removed from 180°. This finding demonstrates that shortening of the Cu-O bond in the  $\text{CuO}_2$  sheets on oxidation is consistent with an important suppression of  $\mu_{\text{Cu}}$  as  $W < U$  becomes  $W > U$ . An expansion of the Cu-O bondlength on passing from the

superconductive to the antiferromagnetic phase is characteristic of all the copper-oxide superconductors [21].

Independent magnetic [22] and neutron-scattering [23] measurements indicate that the presence of a  $\mu_{\text{Cu}}$ , though reduced, persists into the superconductive compositional range of  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ . However, there is no indication that the existence of a  $\mu_{\text{Cu}}$  enhances the superconductive  $T_c$ . What is remarkable is the fact that it does not suppress the superconductivity. This observation leads inexorably to the question of the location of the mobile holes responsible for the superconductivity.

The most definitive answer to this questions comes from electron spectroscopy [24-27]. It places the holes in states that are predominantly of O-2p $\pi$  character lying in the  $\text{CuO}_2$  sheets. We have argued elsewhere [28] that the Madelung stabilization of the O-2p states just balances the ionization energy required to remove one electron from a  $\text{Cu}^{2+}$  ion to an  $\text{O}^-$  ion. This balance causes the  $\text{Cu}^{3+/2+}$  redox energy to be overlapped by the O-2p energies, and covalent mixing between  $\text{Cu}3d_{xy}$  and O-2p $\pi$  orbitals can result in a  $\pi^*$  band that is primarily O-2p $\pi$  in character while mixing of  $\text{Cu}3d_{x^2-y^2}$  and O-2p $\sigma$  orbitals results in a  $\sigma^*$  band that is primarily Cu-3d $_{x^2-y^2}$  in character. Moreover, so long as a  $\mu_{\text{Cu}}$  persists, there is a correlation splitting of the  $\sigma^*$  band that places the top of the  $\pi^*$  band above the top of the lower  $\sigma^*$  band as illustrated in Fig. 3(b). As a consequence, the role of a residual  $\mu_{\text{Cu}}$  in the superconductive phase appears to be the maintenance of a CS of the  $\sigma^*$  band, which results in mobile holes in  $\pi^*$  bands of primarily O-2p $\pi$  character. These holes can give rise to superconductivity, but holes in a correlation-split  $\sigma^*$  band would not.

Demonstration of this latter assertion comes from the suppression of  $T_c$  for  $x > 0.25$ . With the total disappearance of  $\mu_{\text{Cu}}$  with increasing  $x$ , the correlation splitting vanishes; in this case, holes would be more stable in  $\sigma^*$ -band states, which are the more strongly antibonding, so the Cu-O-Cu bond angle would straighten out to 180°, which would remove the mixed symmetry. Such a straightening results in an orthorhombic-to-tetragonal transition, and superconductivity vanishes in the tetragonal phase. There remains some controversy in the literature over whether the superconductivity-to-normal metal transition coincides with the orthorhombic-to-tetragonal transition; the experimental situation may be confused by the possibility of introducing excess oxygen in a portion of the sample under the preparative conditions used to supply a high partial pressure of oxygen.

This analysis leads to two predictions: movement of  $E_F$  from the  $\pi^*$  band into the  $\sigma^*$  band as shown in Fig. 3(c) would result in (i) a transition from p-type to n-type conductivity in the normal metal and (ii) a transition from a Cu-2p spectrum characteristic of  $\text{Cu}^{2+}$  to one characteristic of  $\text{Cu}^{3+}$  as found in  $\text{NaCuO}_2$  [29]. Preliminary measurements appear to confirm both of these predictions [30].

Finally, the possibility of a strong interaction between the conduction electrons and the transverse optical-mode oxygen vibrations perpendicular to a Cu-O-Cu bond axis has already been pointed out. If the  $\text{CuO}_2$  plane is under compression, this interaction is strong where the Cu-O-Cu bond angle is bent from 180° and the charge carriers are holes; a hole stabilizes a straightening of the bond angle, and the relatively slow response of the oxygen displacement provides time to attract a second hole. The mechanism represents a strong electron-phonon interaction that is enhanced by the polarizability of the conduction-electron charge density resulting from an overlap of the  $\sigma^*$  and  $\pi^*$  bands. In this strong-coupling limit, the Cooper pairs become condensed into a volume of sufficiently small coherence length ( $\xi \sim 10$  Å) that the distinction between a Cooper pair and a large bipolaron may become blurred.

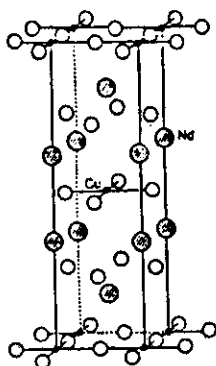


Fig. 6 The tetragonal (T) structure of  $\text{Nd}_2\text{CuO}_4$ .

Conversely, if the  $\text{CuO}_2$  plane is under tension, the Cu-O-Cu bond angle is  $180^\circ$  and the electron-lattice interaction is strong where the charge carriers are electrons of the  $\text{Cu}^{2+}$  couple; in this case an electron stabilizes a bending of the Cu-O-Cu bond angle, and the relatively slow response of the oxygen displacement provides time to attract a second electron. This situation is realized in the tetragonal T structure of  $\text{Nd}_2\text{CuO}_4$ , Fig. 6[31], where the smaller  $\text{Nd}^{3+}$  ion -- relative to  $\text{La}^{3+}$  -- creates so small a tolerance factor  $t$  that the c-axis oxygen of the tetragonal T phase of high-temperature  $\text{La}_2\text{CuO}_4$ , Fig. 2, are displaced to the plane of tetrahedral sites of the Nd bilayer. This displacement expands the a-axis, thereby removing the compression of the Cu-O bonds of a  $\text{CuO}_2$  plane. Doping this phase p-type by Sr substitution for Nd leaves the system semiconducting [32]; but doping it n-type by, for example, Ce substitution for Nd leads to a superconductive phase in a narrow compositional range [33]. According to the model of electron-lattice coupling we are proposing, n-type superconductivity requires sufficient electron doping to make  $W > U$  and thus suppress  $\mu_{\text{Cu}}$ , but insufficient doping to destroy the phase.

#### SYSTEMS WITH THE $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ STRUCTURE

Extension of the ideas presented above to the other high- $T_c$  copper oxides is straightforward. In every case there is an interface between a  $\text{CuO}_2$  layer and an MO layer that is subject to the tolerance-factor constraint of equation (1). Moreover, they are p-type conductors in their normal state with a Cu-O-Cu angle bent from  $180^\circ$  in their superconductive state. However, in the phases with multiple  $\text{CuO}_2$  sheets separated by  $\text{Y}^{3+}$  and/or  $\text{Ca}^{2+}$  ions, the bending of the Cu-O-Cu bond angle from  $180^\circ$  is induced by the symmetry of the structure; the magnitude of the bending merely adjusts to relieve any stresses introduced by a  $t \neq 1$ . In this case, a larger concentration of holes may be introduced into the  $\text{CuO}_2$  sheets before the Cu-O-Cu bond angle is straightened out to  $180^\circ$ . Since  $T_c$  appears to vary with the concentration of mobile holes in the  $\text{CuO}_2$  sheets [34-36], at least for smaller  $E_{\text{VB}} - E_{\text{F}}$ , the maintenance of a bent Cu-O-Cu bond angle to higher hole concentrations allows the realization of a higher value of  $T_c$ .

In view of this situation, it is relevant to review briefly the evidence for  $\pi^*$ -band holes in the  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  structure and for a  $T_c$  varying with the  $\pi^*$ -band hole concentration.

Placement of the mobile holes responsible for superconductivity into  $\pi^*$ -band states of the  $\text{Cu(2)O}_2$  sheets that are primarily of  $\text{O-2p}_\pi$  character comes from XPS evidence for a trapping out of mobile holes at oxygen-atom clusters centered at a-axis oxygen in the  $\text{Cu(1)O}_x$  planes of  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  [26]. A trapping out of mobile holes in the  $\text{Cu(1)O}_x$  layers for  $x > 1$  was verified independently by Hall measurements on the system  $\text{Nd}_{1-y}\text{Ba}_2\text{yCu}_3\text{O}_{6+x}$  [35]. We have also shown that, by co-doping with Ca and La in the system  $\text{Y}_{1-z}\text{Ca}_z\text{Ba}_{2-y}\text{La}_y\text{Cu}_3\text{O}_{6+x}$ , it is possible to change the magnitude of the internal electric field

parallel to the c-axis so as to suppress hole trapping at disordered oxygen in the  $\text{Cu(1)O}_x$  planes [38]. As is illustrated in Fig. 7, a  $T_c > 80$  K is maintained in samples annealed in  $\text{O}_2$  at  $400^\circ\text{C}$  followed by slow cooling to  $250^\circ\text{C}$ , provided there is no hole trapping;  $T_c$  decreases essentially linearly with  $x$  above a critical oxygen concentration  $x_c$  that increases with Ca concentration  $z$ . The figure also illustrates that  $T_c$  is independent of the orthorhombic-tetragonal phase transition associated with oxygen ordering in the  $\text{Cu(1)O}_x$  plane, an observation that is consistent with the hypothesis that the Cu-O-Cu bond angle is the critical structural feature for high- $T_c$  superconductivity. Attempts to correlate a fall-off in  $T_c$  with total oxidation state cannot be valid; what would be valid is any correlation with the concentration of mobile holes in the  $\text{CuO}_2$  sheets and the Cu-O-Cu bond angle in these sheets. The interesting data of Tokura et al [39] should be reconsidered from this perspective.

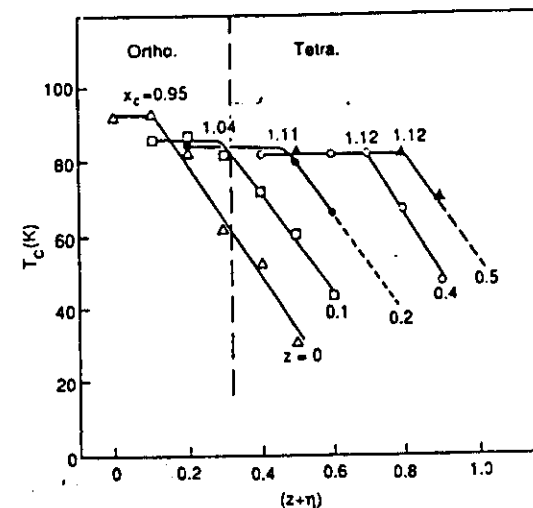


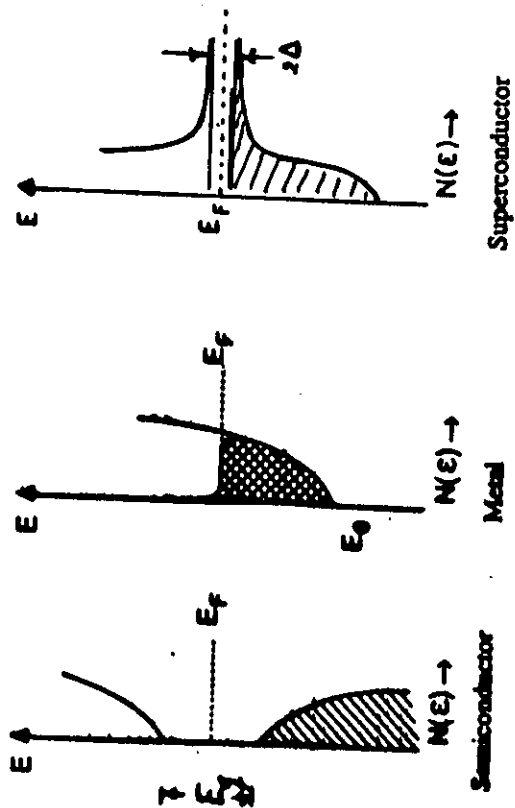
Fig. 7 Variation of  $T_c$  with  $y = z + \eta$  for various values of  $z$  in the system  $\text{Y}_{1-z}\text{Ca}_z\text{Ba}_{2-y}\text{La}_y\text{Cu}_3\text{O}_{6+x}$  annealed in air at  $400^\circ\text{C}$ .

In order to perform a correlation of the latter type, it is necessary to be aware of the complex hole transfer that occurs between  $\text{Cu(1)O}_x$  planes and  $\text{Cu(2)O}_2$  sheets. In addition to the possibility of hole trapping at disordered oxygen in the  $\text{Cu(1)O}_x$  planes, there is also the problem of hole trapping at  $\text{Cu(1)}$  atoms oxidized from  $\text{Cu}^+$  to  $\text{Cu}^{2+}$ . The  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  phase diagram provides evidence that, in the ordered structures, holes are transferred to the  $\text{Cu(2)O}_2$  sheets once the  $\text{Cu(1)}$  atoms neighboring an oxygen in the  $\text{Cu(1)O}_x$  plane are oxidized to  $\text{Cu}^{2+}$  [40]. The phase diagram exhibits a step in  $T_c$  vs  $x$  near  $x = 0.67$ . Electron microscopy has established the appearance of interchain ordering at  $x = 0.5$ ; with perfect ordering, half of the  $\text{Cu(1)}$  atoms would remain  $\text{Cu}^+$  ions coordinated to only two c-axis oxygen, so 0.125 holes per  $\text{Cu(2)}$  atom would be transferred to the  $\text{Cu(2)O}_2$  sheets. Further oxidation of the  $\text{Cu(1)O}_x$  planes would convert the remaining  $\text{Cu(1)}$  from  $\text{Cu}^+$  to  $\text{Cu}^{2+}$  ions in the interval  $0.5 < x < 0.75$  before additional holes were transferred to the  $\text{Cu(2)O}_2$  sheets. Long-range intrachain and interchain ordering within an untwinned grain of an  $x = 0.75$  sample has now been observed [41]. However, the realization of perfect long-range order is never achieved uniformly over a bulk sample, so the step in  $T_c$  vs  $x$  due to oxidation of  $\text{Cu(1)}$  from  $\text{Cu}^+$  to  $\text{Cu}^{2+}$  covers a narrower compositional range than  $0.5 < x < 0.75$  and is not flat as would be expected for a two-phase compositional range.

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Determining Factors

1. Electronic, e.g.  $N(E_F)$
2. Electron - Lattice Coupling

## ISOTOPE EFFECT

### Definitions

Atomic mass numbers:  $A = Z + N$

( $Z$  = # of protons;  $N$  = # of neutrons)

Isotopes = nuclei of same  $Z$ , different  $N$

### Experiment:

$$MT_c = \text{const}$$

for isotopes of a superconductor

### BCS Theory

$$T_c \sim 1.14 \Theta_D \exp(-1/\lambda)$$

$$\lambda = N(E_F)[V_C - V_{\text{coul}}]; \Theta_D \sim M^{-1/2}$$

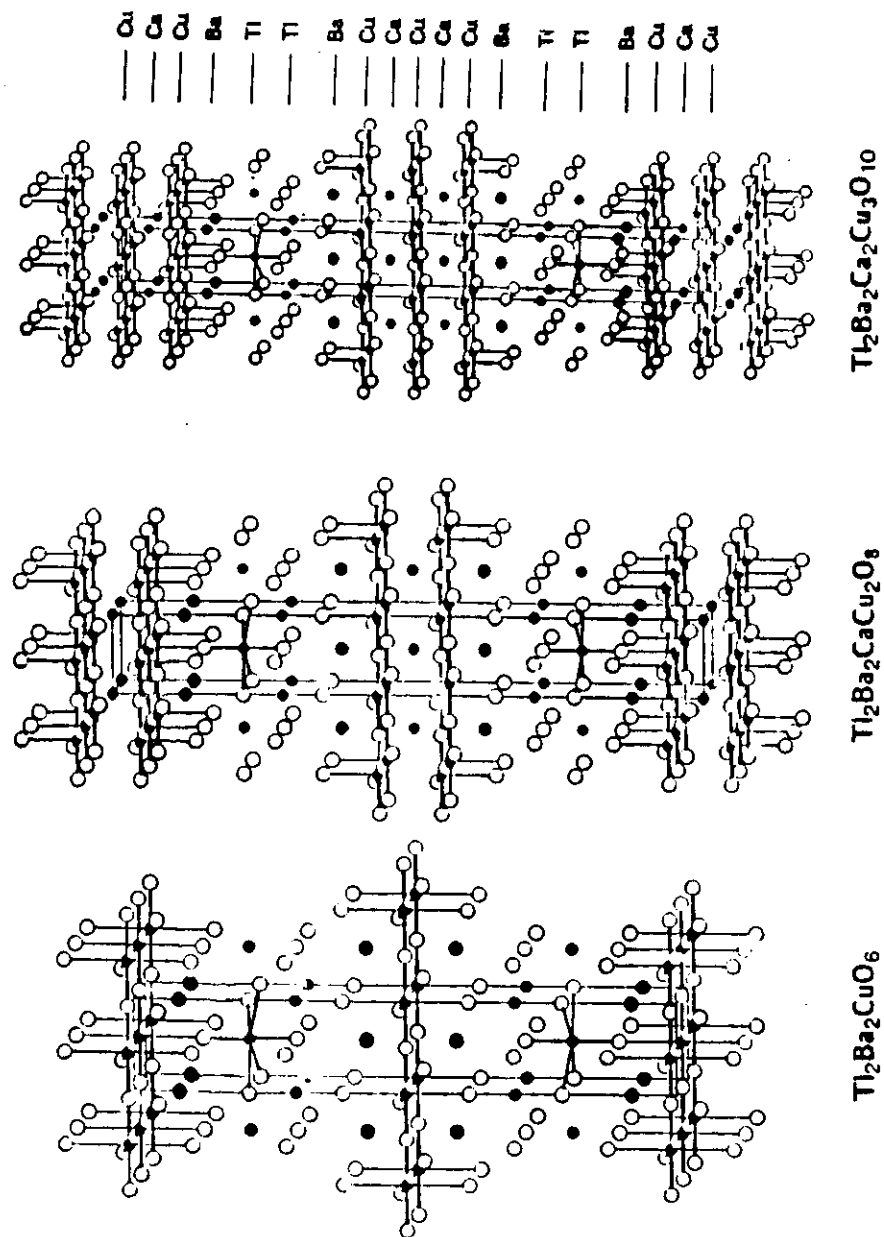
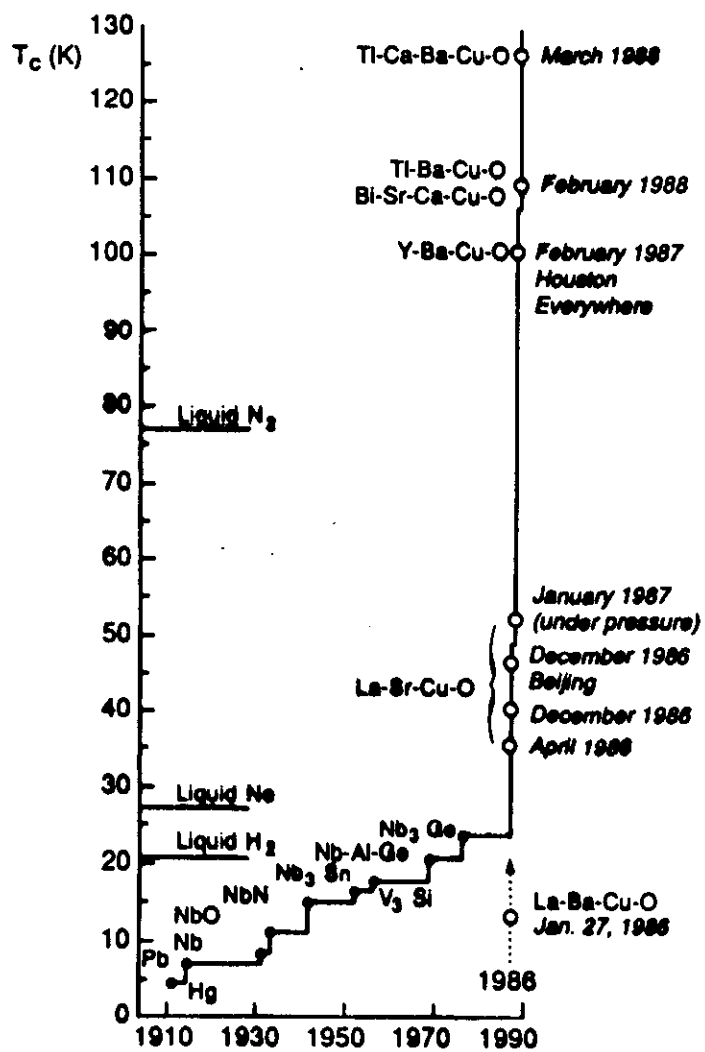
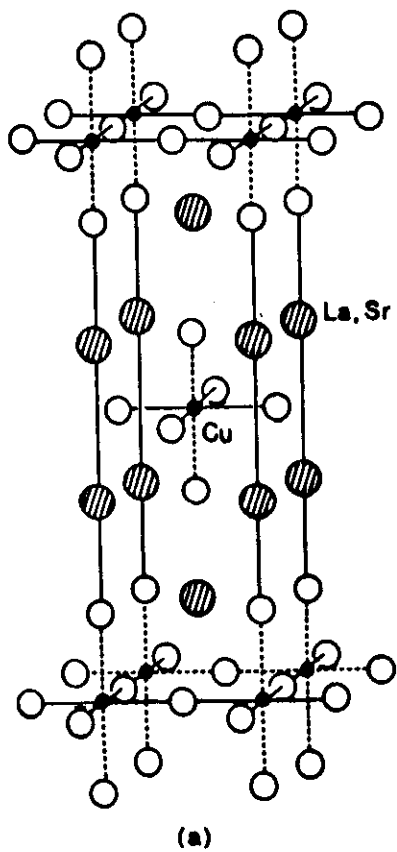


Figure 4.

$Tl_2Ba_2Ca_2Cu_3O_{10}$





$\text{La}_2\text{CuO}_4$

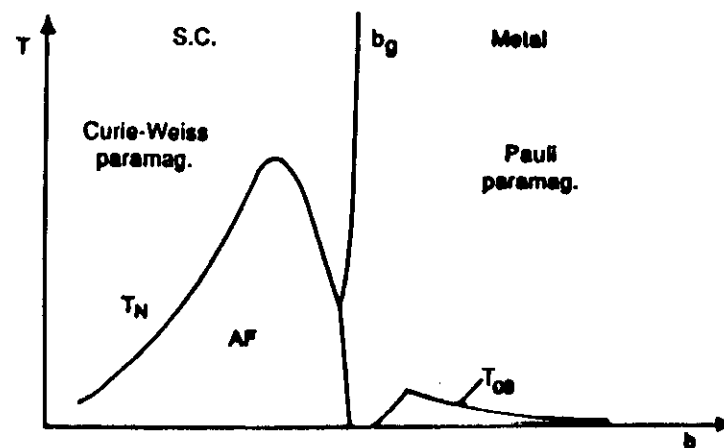
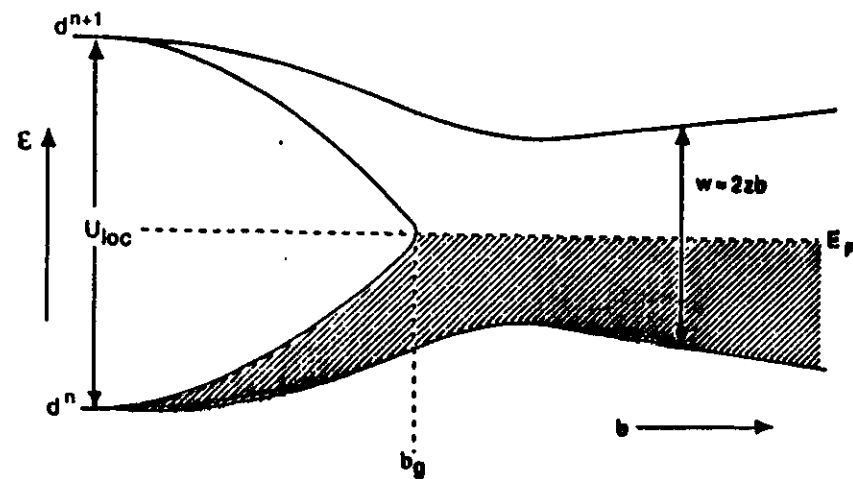
Cu-O-Cu interactions

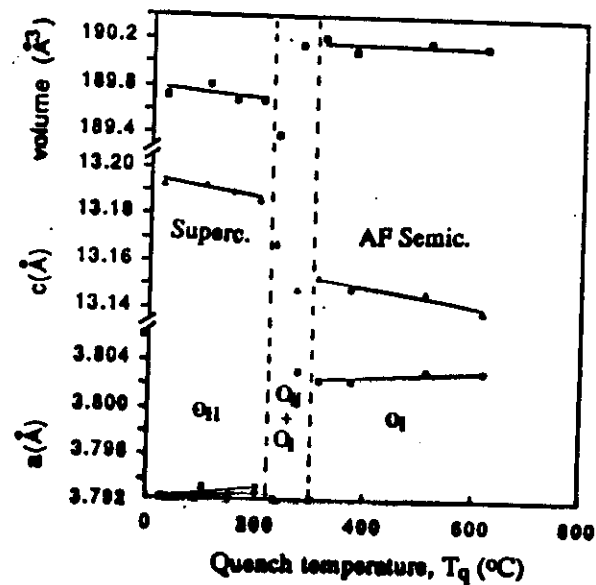
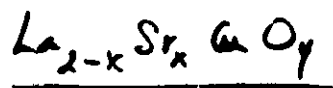
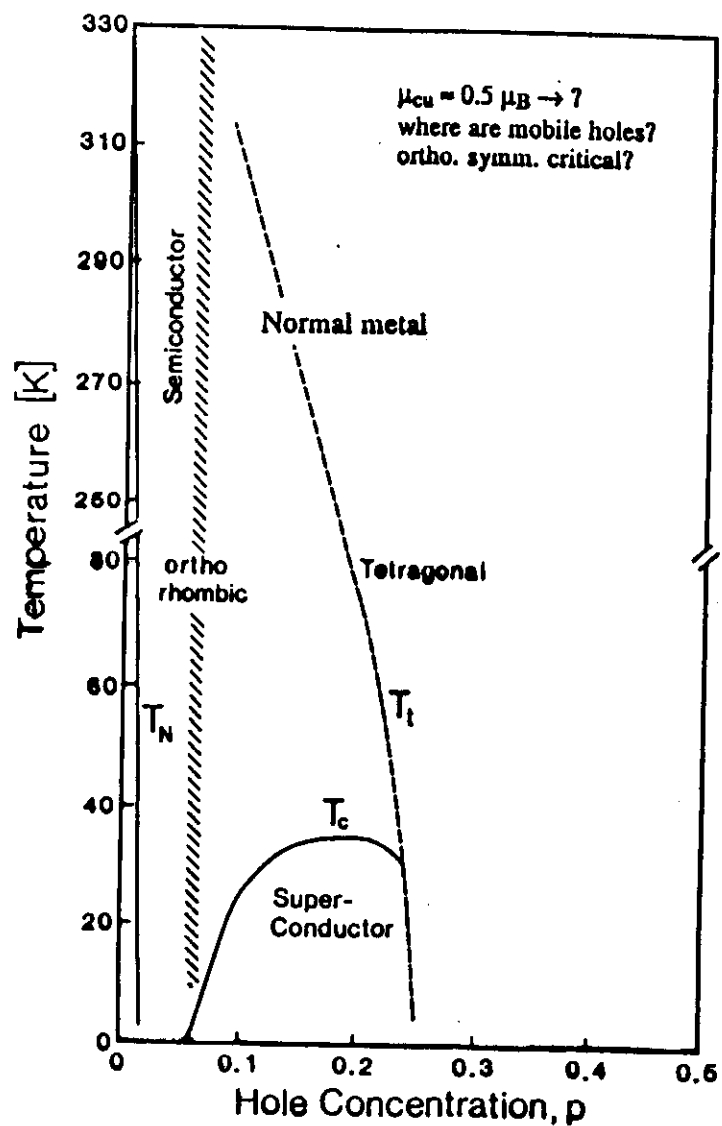
$$\psi_{x^2-y^2} = N_{\sigma} (f_{x^2-y^2} - \lambda_{\sigma} \phi_{\sigma} - \lambda_{\pi} \phi_{\pi})$$

$$b = (\psi_L H' \psi_j) = e_{ij} N_{\sigma}^2 \lambda_{\sigma}^2$$

$$T_N \sim b^2/U - \lambda_{\sigma}^4/U$$

$$W = 2zb - \lambda_{\sigma}^2$$

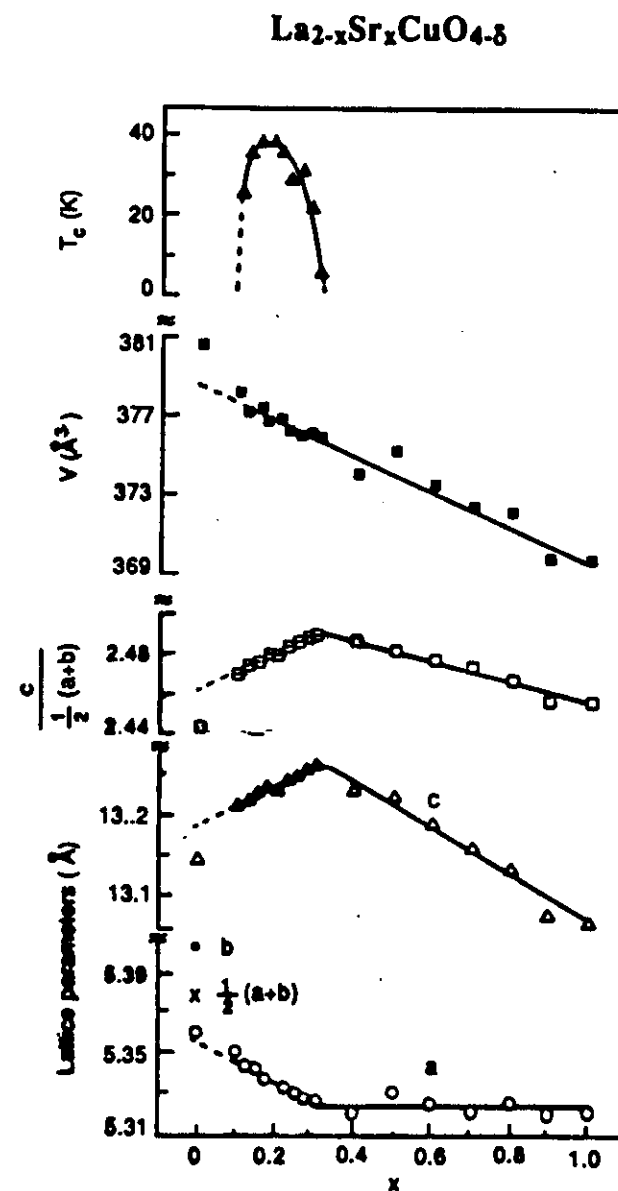
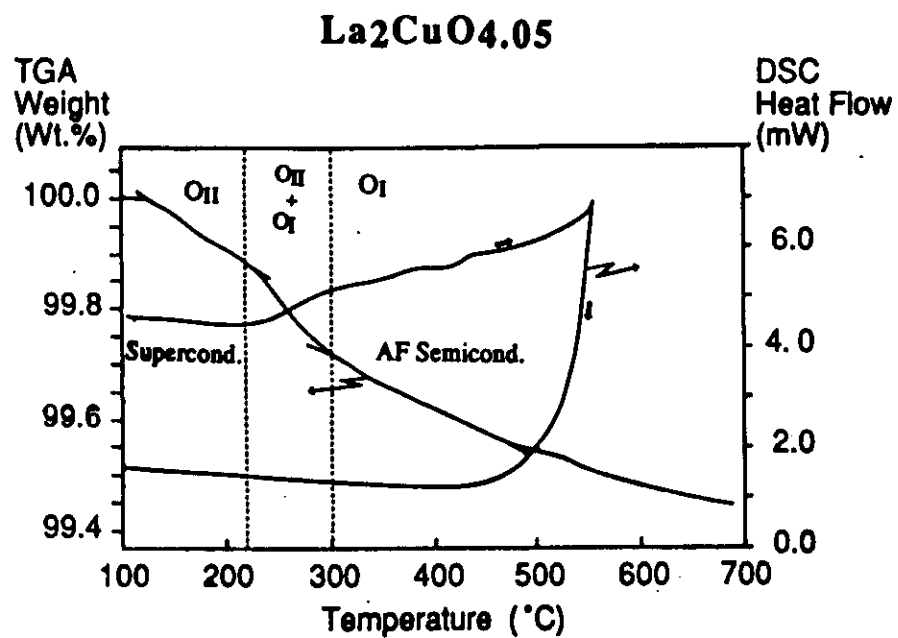




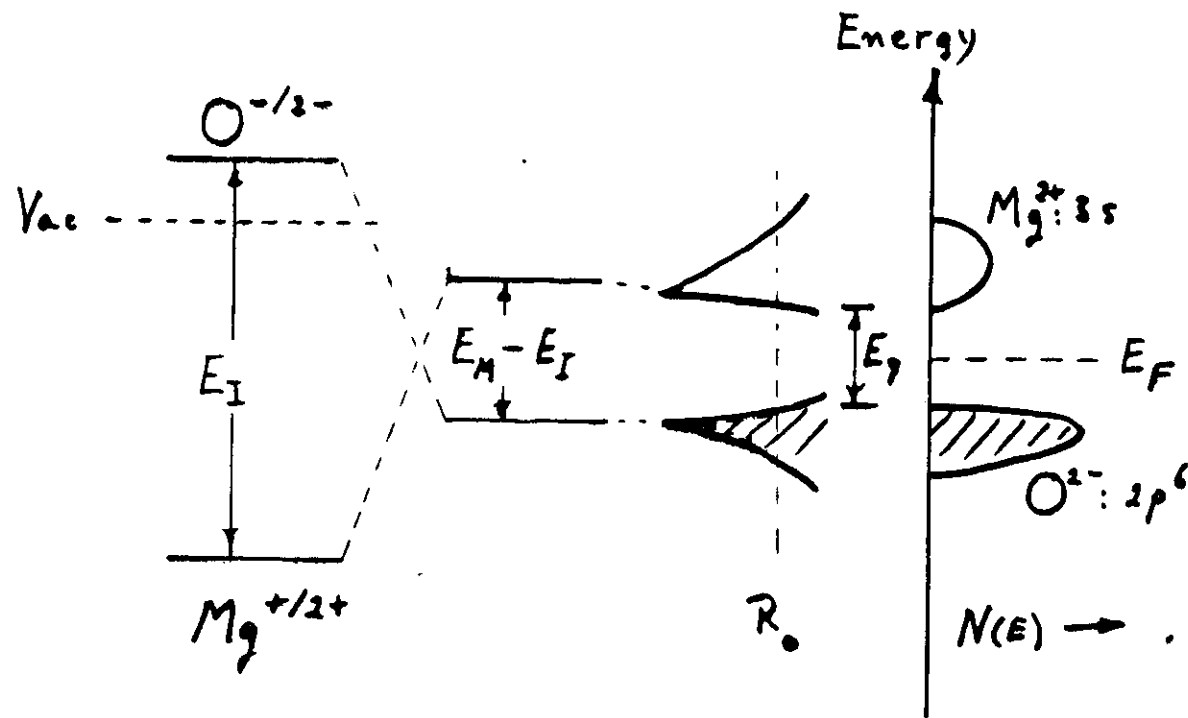
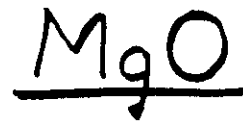
Heated in air from room T to  $T_q$

$La_2CuO_{4+\delta}$  obtained at  $800^{\circ}\text{C}$  and 23 kbar oxygen pressure  
 $\delta = 0.05$  by iodometry  
 $\delta = 0.14$  by TGA

J. Zhou



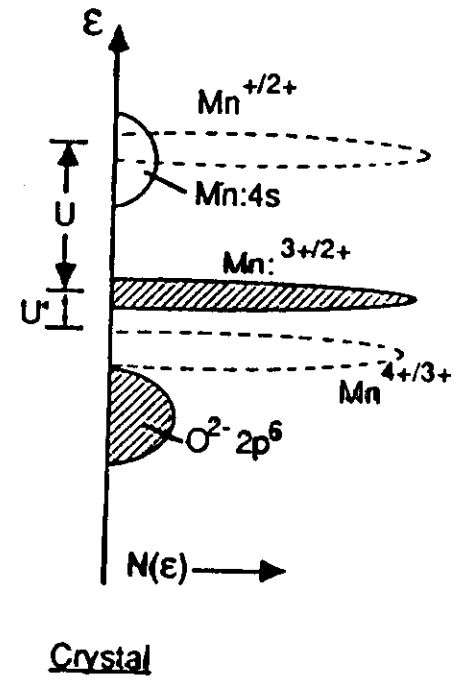
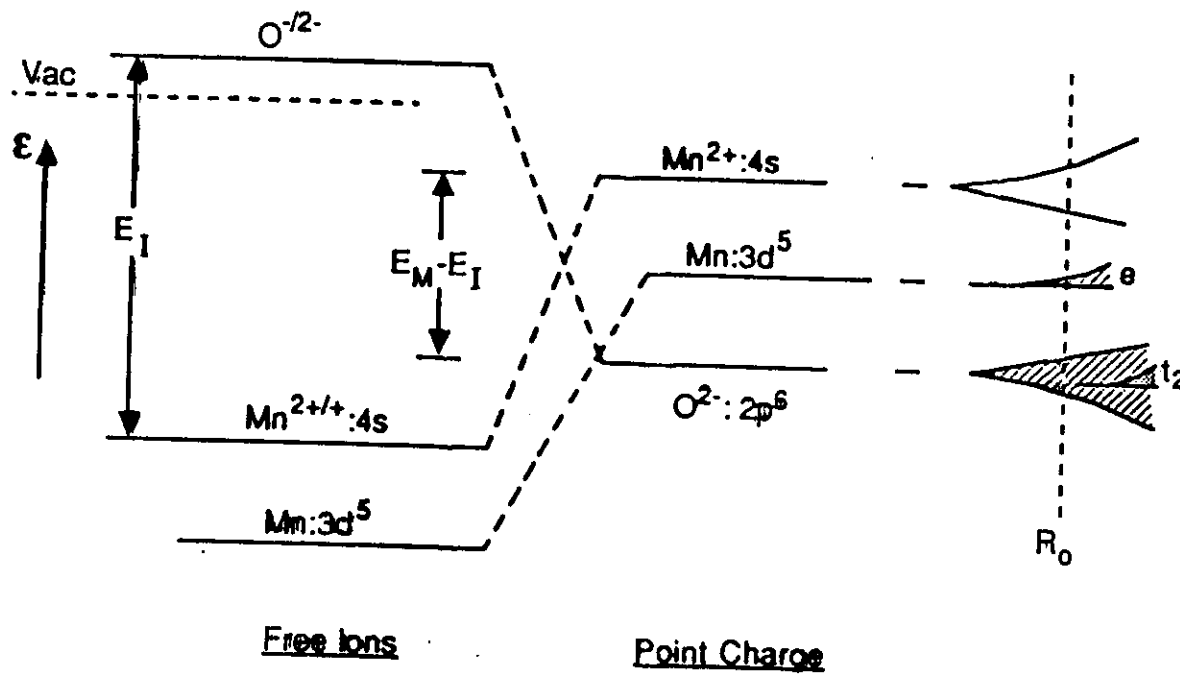
Tarascon et al

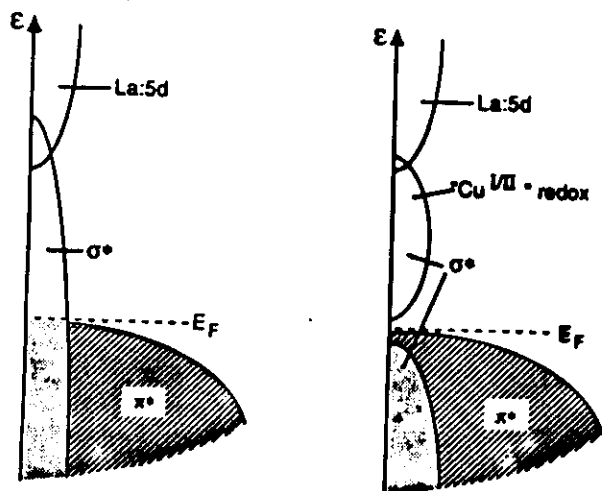


Free  
Ion

Point  
charge

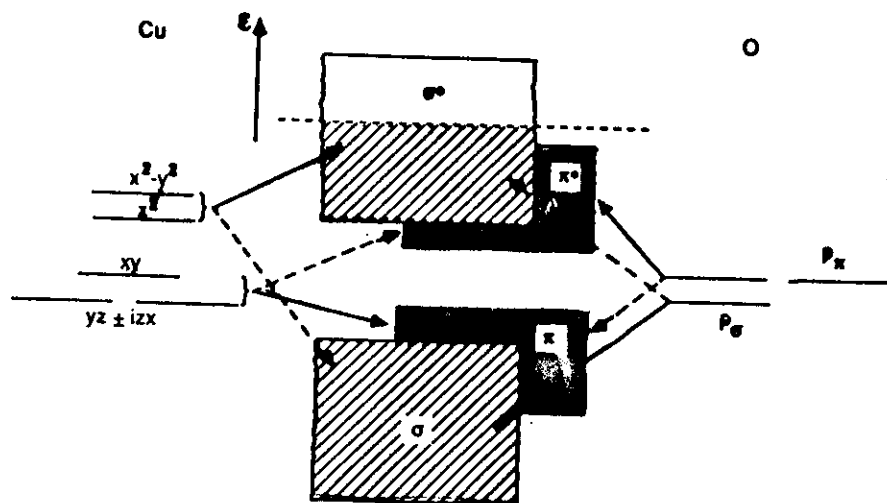
# MnO





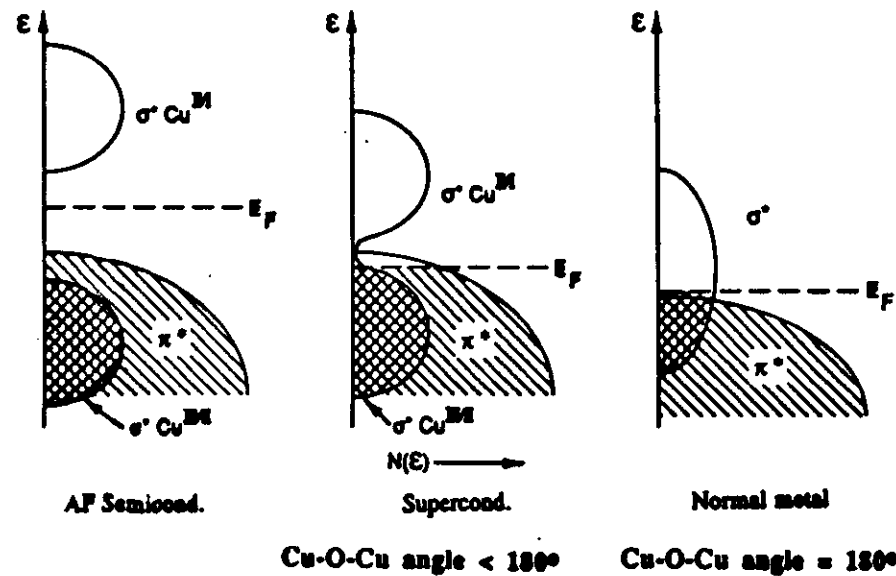
Uncorrelated

Correlated (AF)



Origin of primarily O-2p character for  $\pi^*$ -band holes in superconductive state.

## DENSITY OF ONE-ELECTRON STATES VS ENERGY FOR $\text{La}_2\text{CuO}_4$



AF Semicond.

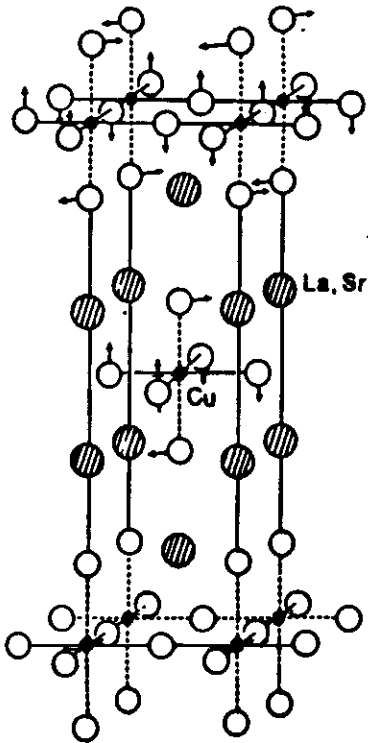
Supercond.

Normal metal

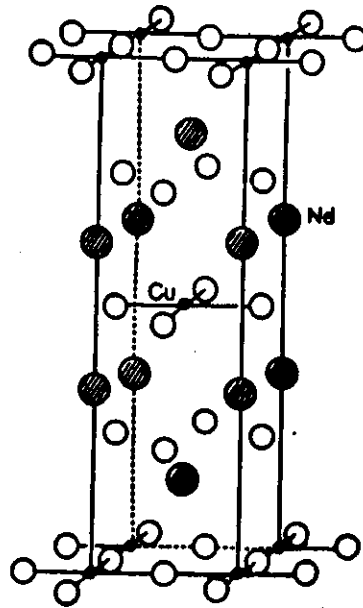
Cu-O-Cu angle < 180°

Cu-O-Cu angle = 180°

$$t = \frac{(r_{La} + r_o)}{\sqrt{2}(r_{Cu} + r_o)}$$



$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  - p-type  
Cu-O-Cu angle  $< 180^\circ$



$\text{Nd}_{2-x}\text{Ce}_x\text{CuO}_4$  - n-type  
Cu-O-Cu angle  $\approx 180^\circ$

- Large polarizability
- Orbital hybridization adjusts readily to bond changes associated with lattice vibrations
- Strong electron-lattice coupling

Hybridization (or polarization) fluctuation mechanism

Takagi et al.

