



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
I.C.T.P., P.O. BOX 586, 34100 TRIESTE, ITALY, CABLE: CENTRATOM TRIESTE



H4-SMR 393/52

SPRING COLLEGE ON PLASMA PHYSICS

15 May - 9 June 1989

RADIO FREQUENCY HEATING IN TOKAMAKS

Electron Cyclotron Resonance Heating

D. F. Start

Jet Joint Undertaking
Oxfordshire
Abingdon OX14 3EA
U. K.

Electron Cyclotron Resonance Heating

$$2\pi f = eB/\gamma m_e \quad \gamma = (1 - v^2/c^2)^{-1/2} \text{ - relativistic mass correction}$$

Ex $B = 2T$ $f = 56 \text{ GHz}$, $\lambda_{\text{free space}} = 5.4 \text{ mm}$

Experiments $28 \text{ GHz} < f < 80 \text{ GHz}$

Dispersion Relation - Appleton-Hartree

$$N^2 = 1 - \frac{2\alpha\omega^2(1-\alpha)}{2\omega^2(1-\alpha) - \omega_c^2 \sin^2\theta \pm \omega_c \Delta}$$

ω = wave freq

ω_c = cycl. freq.

θ angle between \mathbf{k} & \mathbf{B}

$$\Delta^2 = \omega_c^2 \sin^4\theta + 4\omega_c^2(1-\alpha)^2 \cos^2\theta$$

$$\alpha = \omega_p^2 / \omega^2$$

$$\omega_p = \text{plasma freq (rad s}^{-1}\text{)} = 5.6 \times 10^9 \sqrt{n_0} \text{ (cm}^{-3}\text{)}$$

2 Modes [O, X]

$$\theta = \pi/2$$

$$\theta = 0$$

+ve sign Ordinary [O] mode $E_{||}$ to B

LH polarized

-ve sign Extraordinary [X] mode E_{\perp} to B

RH polarized

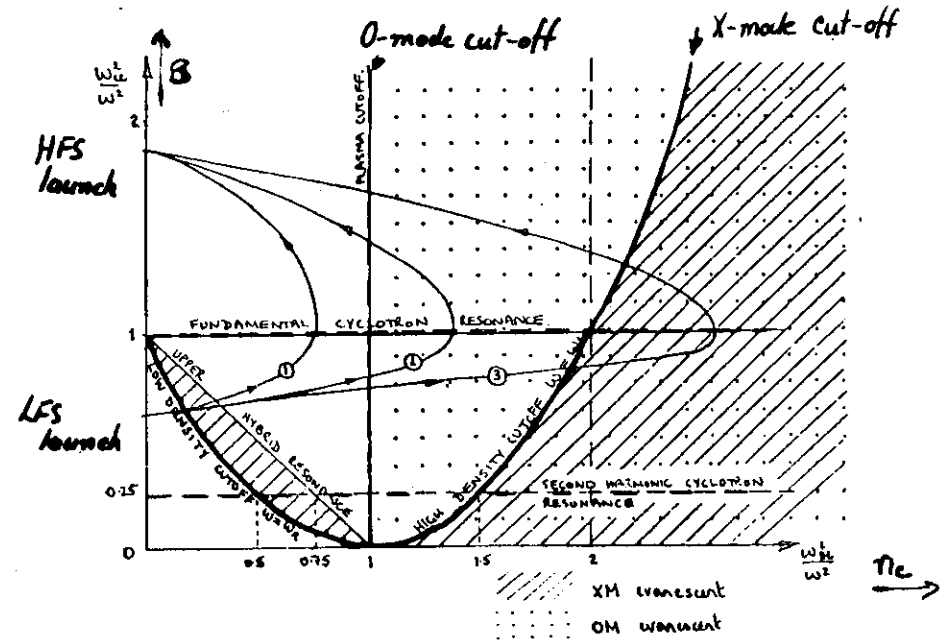
Cut-offs when $N \rightarrow 0$

O mode $\omega = \omega_p$

X mode $\omega_{R,L} = \left(\omega_p^2 + \frac{\omega_c^2}{4} \right)^{1/2} \pm \frac{\omega_c}{2}$

Plasma resonance when $N \rightarrow \infty$

Upper hybrid resonance $\omega_{UH}^2 = \omega_c^2 + \omega_p^2$



Cut-offs limit values of $(\omega_p/\omega_c)^2$

O-mode

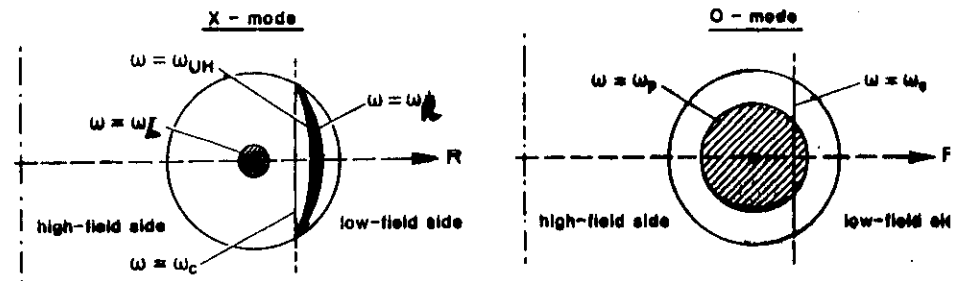
X-mode

fund. $\omega = \omega_c$ 1

2 (HFS)

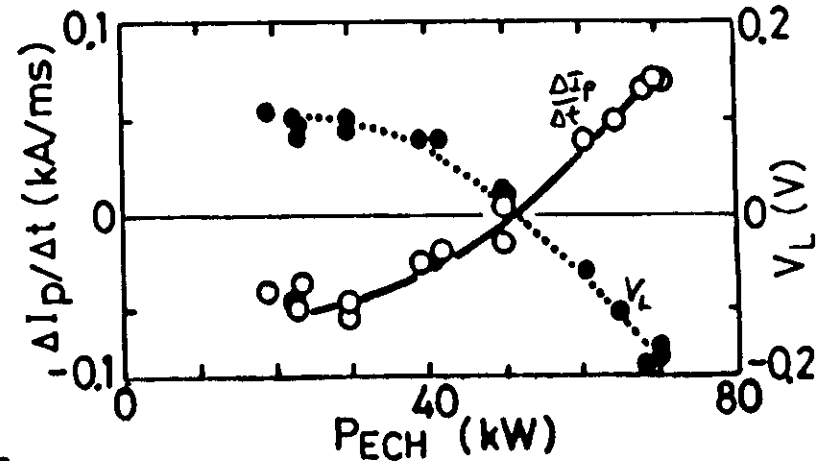
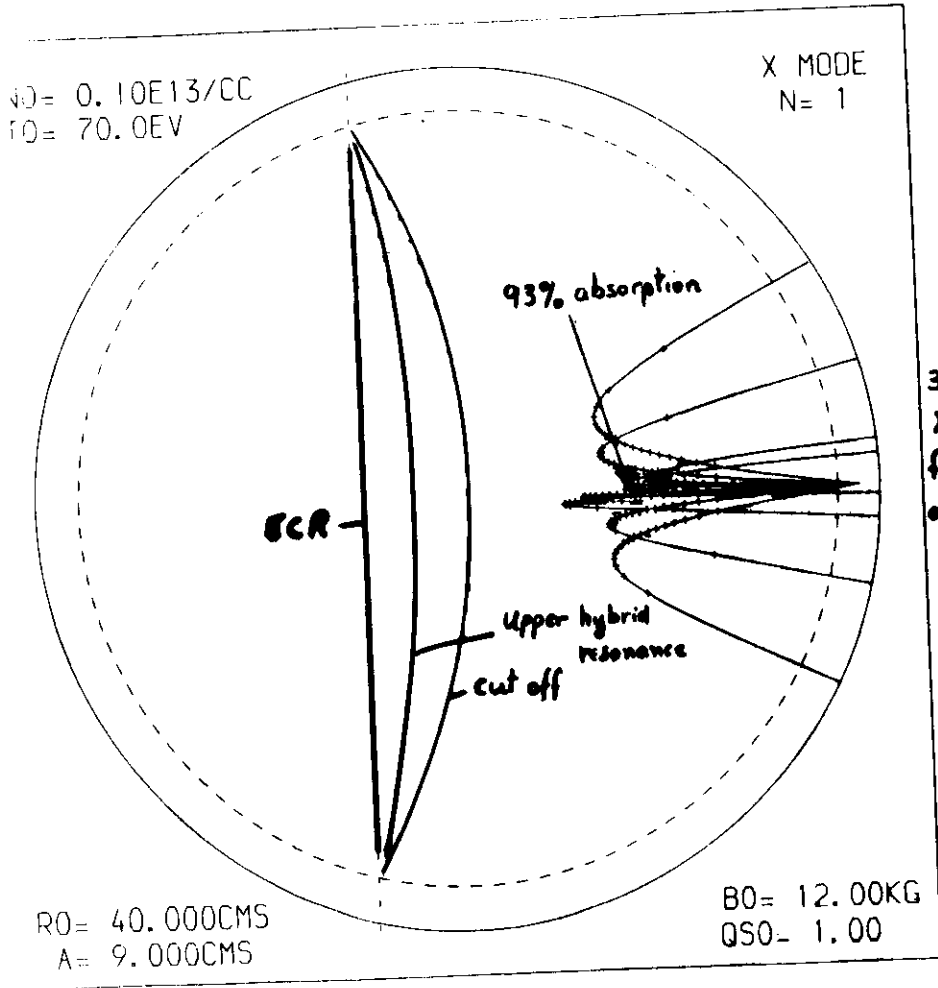
2nd Harm $\omega = 2\omega_c$ 4

2

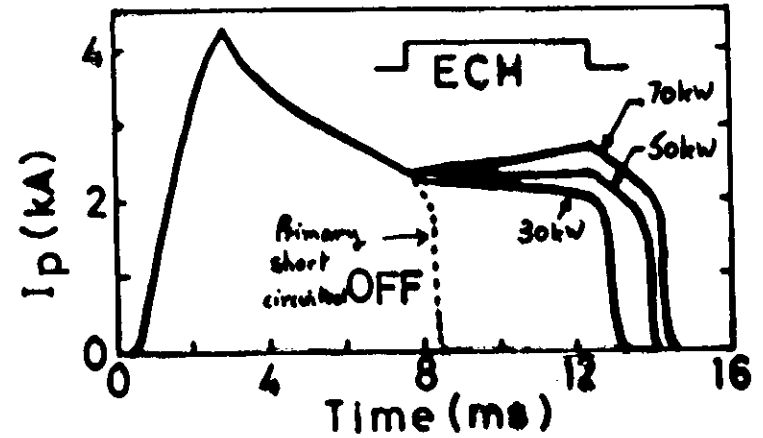


W1-2

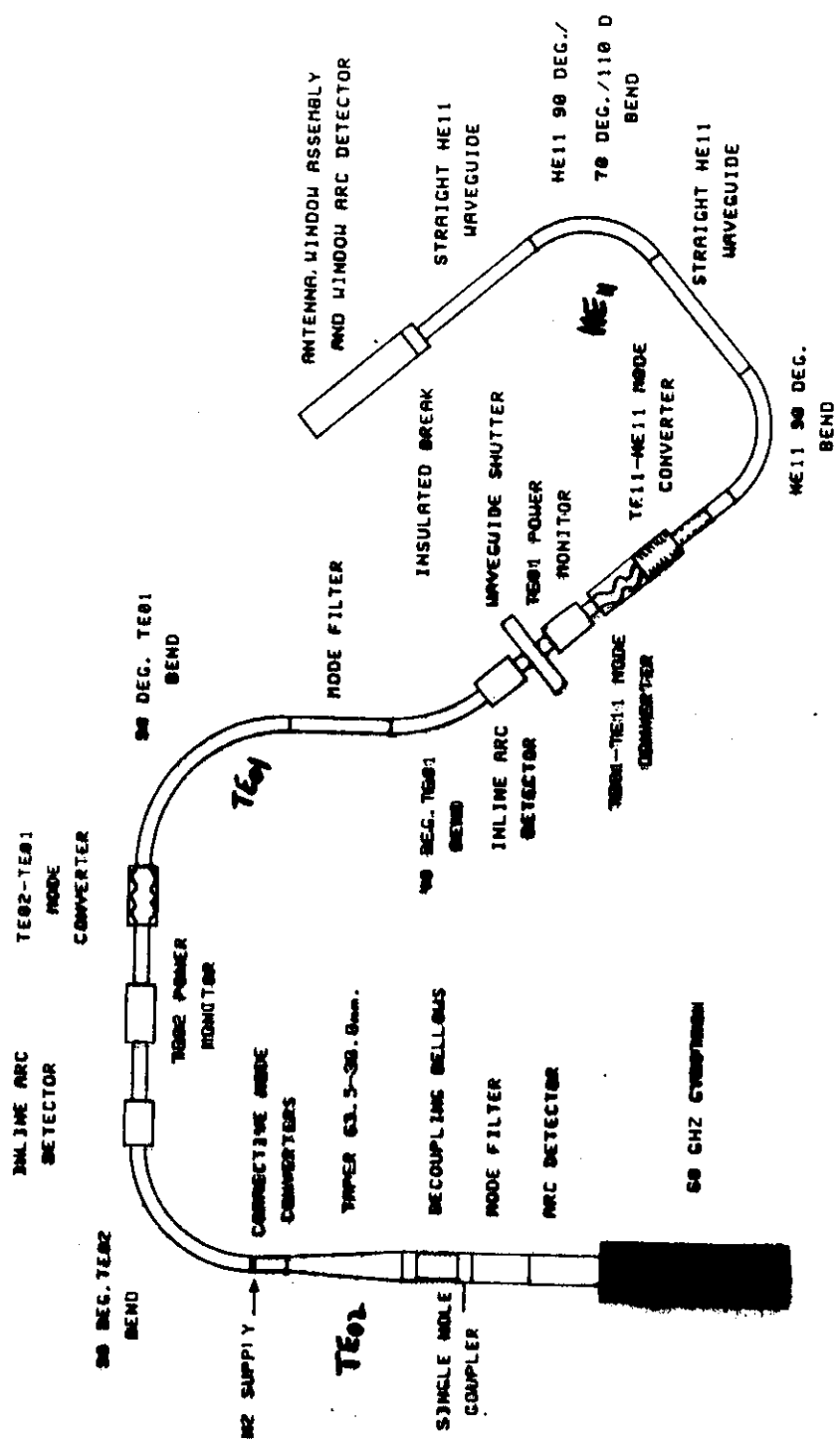
X-mode fundamental, 35.6 GHz outside launch
 co, ctr & lr into slideaway OH plasma $T_e = 70\text{eV}$ $n_e = 2 \times 10^{12}\text{cm}^{-3}$



Co-injection



lr & ctr injection reduce V_L but do not produce reversal



SCHEMATIC OF COMPASS CIRCULAR VESSEL E.C.R.H. SYSTEM

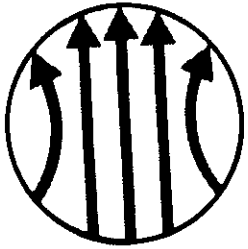
N. AINSWORTH 27-5-66



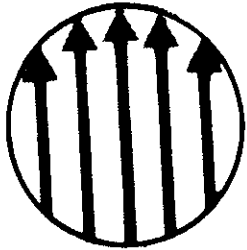
Output from gyrotron, TE_{02} , i.e. Transverse Electric circular field in a 2-ring pattern.



After conversion to TE_{01} , i.e. circular 1-ring pattern

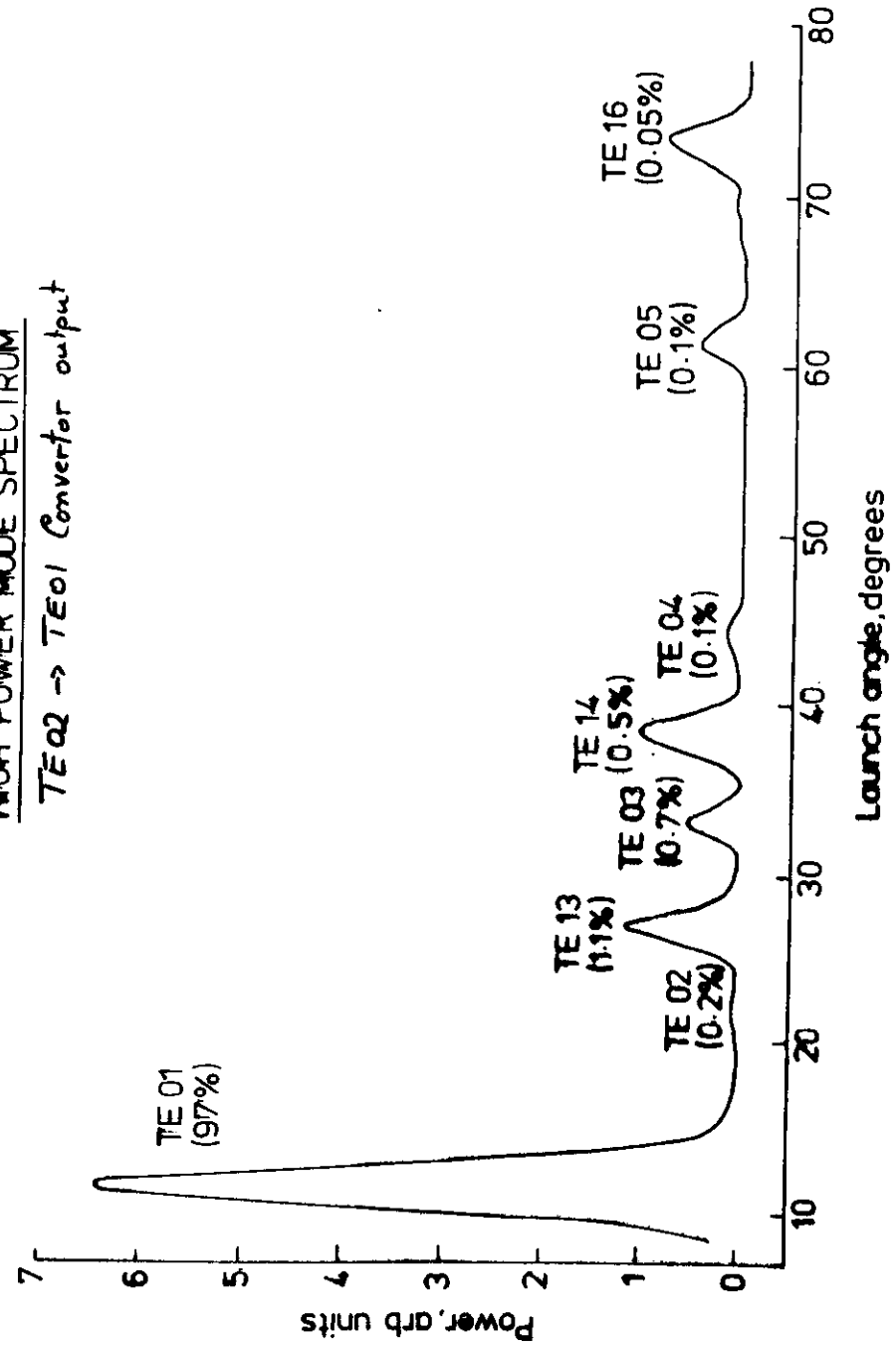


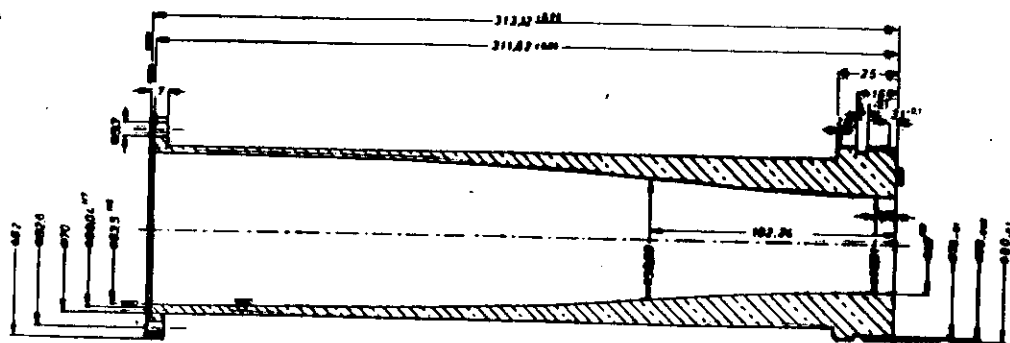
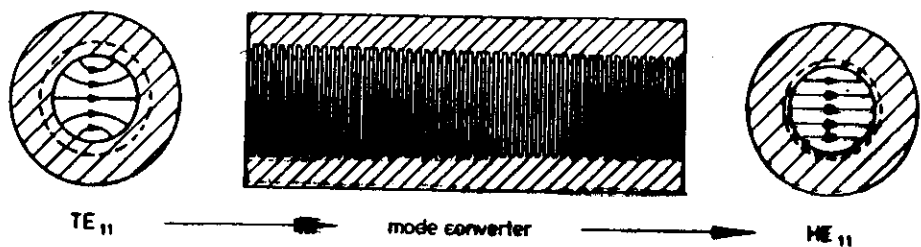
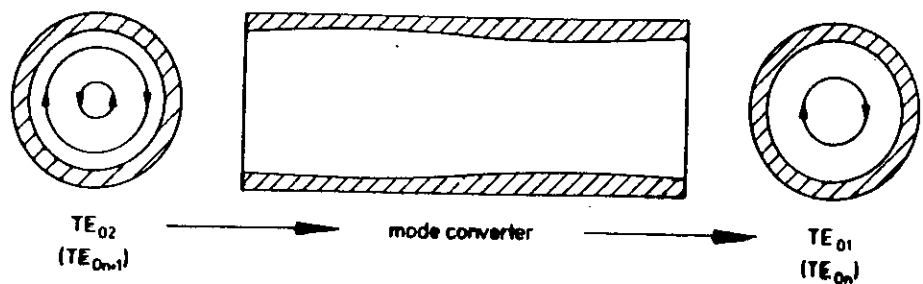
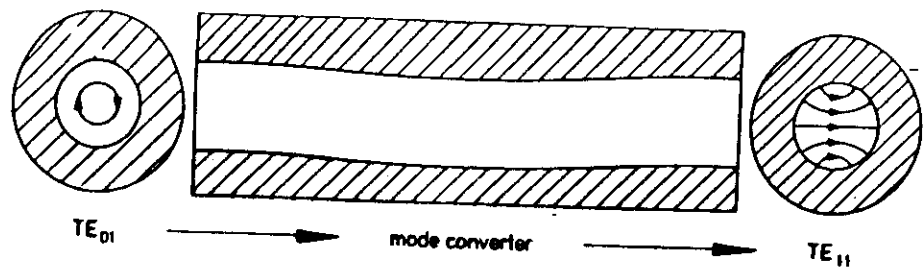
After conversion to TE_{11} , i.e. near parallel field pattern



After conversion to linearly polarised HE_{11} (Hybrid) mode.

HIGH POWER MODE SPECTRUM
 $TE_{02} \rightarrow TE_{01}$ Converter output

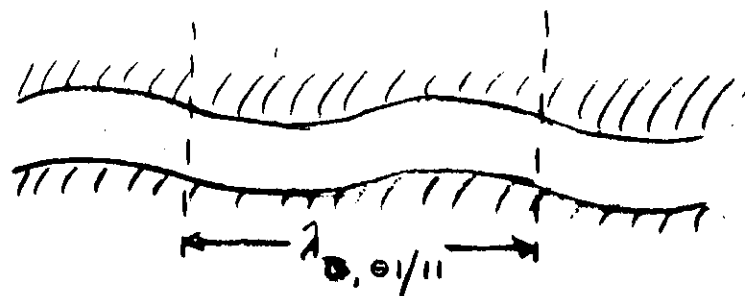
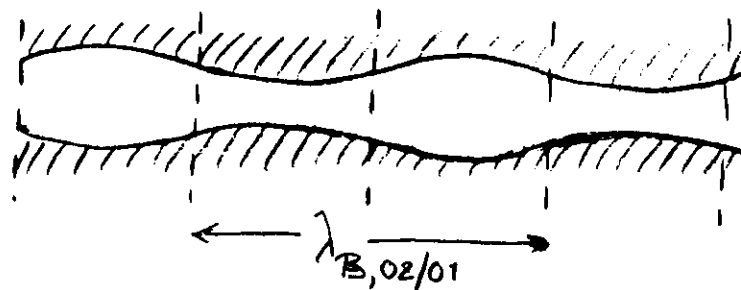




CROSS-SECTIONAL VIEW OF AN OPTIMUM TAPER ($TE_{01} \leftrightarrow TE_{02}$ COUPLING)

28 GHz |
60 GHz | mode converters

$$TE_{02} \rightarrow TE_{01} \quad (l = 6 \lambda_{B,02/01})$$



$$TE_{01} \rightarrow TE_{11} \quad (l = 10 \lambda_{B,01/11})$$

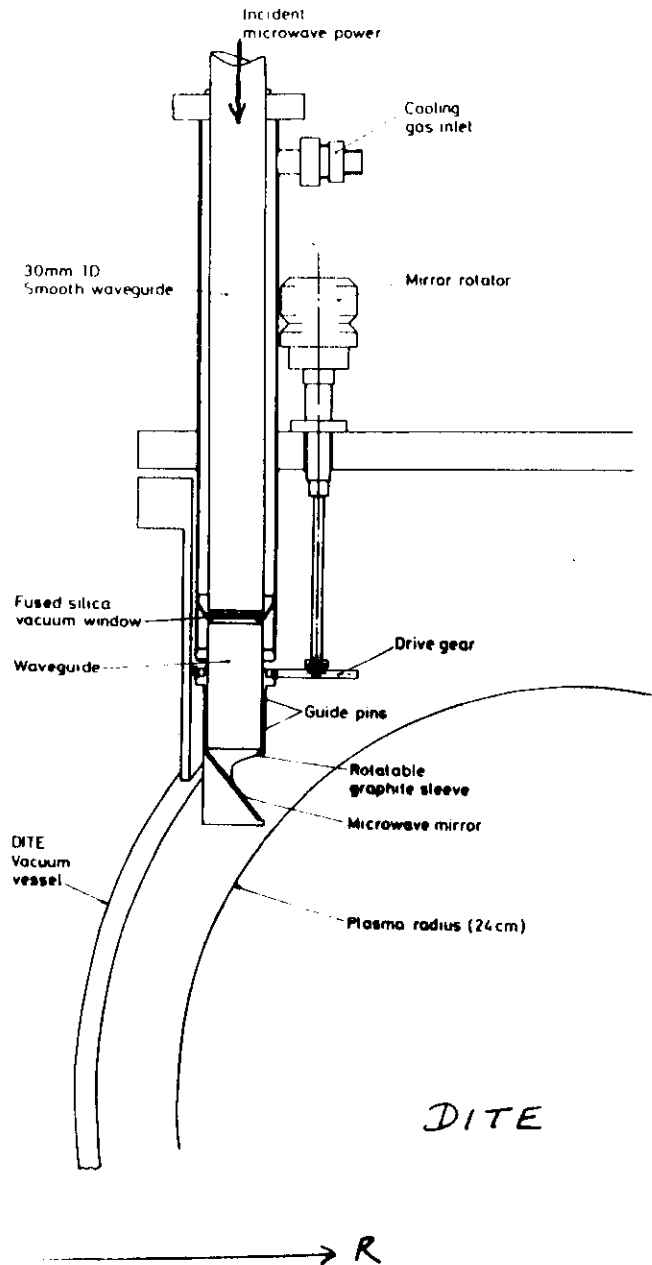
Overall lengths (for 60 GHz)

$$6 \lambda_B (02/01) = 0.59 \text{ m}$$

$$10 \lambda_B (01/11) = 3.11 \text{ m}$$

Results

- High T_e plasmas
- Peaked T_e profiles
- Power deposition profiles
- Evidence for electron trapping
- Effect on MHD activity - sawteeth
- $m=2$
- Central density pump-out
- Relativistic effects - downshifted freq.
BCRH

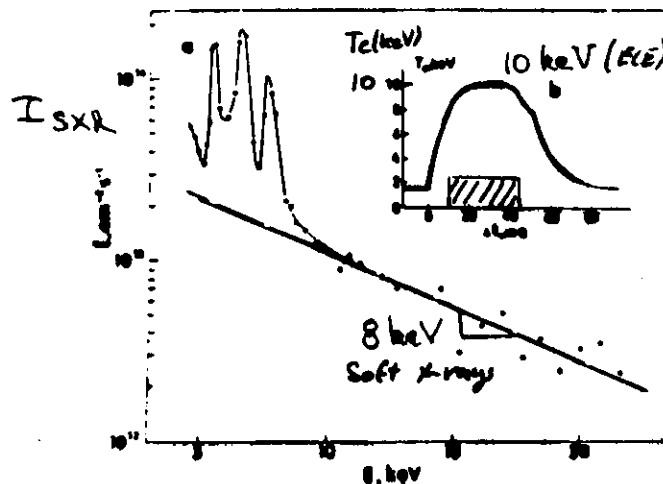


High T_e Plasmas

- Temperatures as high as 10 keV obtained with 4 MW in T-10
- High temperatures, 5 keV, also attained in DIII-D
- These cases show that high temperature, low density discharges with ECH can still be thermal
- These discharges are excellent targets for electron cyclotron current drive studies

T-10

Central heating (± 6 cm); $P_{\text{ABS}} \sim 2$ MW
 Nearly 10 W/cm^3 !



$$\bar{n}_e = 1.5 \times 10^{19} \text{ m}^{-3}$$

$$\tau_E^{\text{OH}} = 50 \text{ ms}$$

$$\tau_E^{\text{ECH}} = 7 \text{ ms}$$

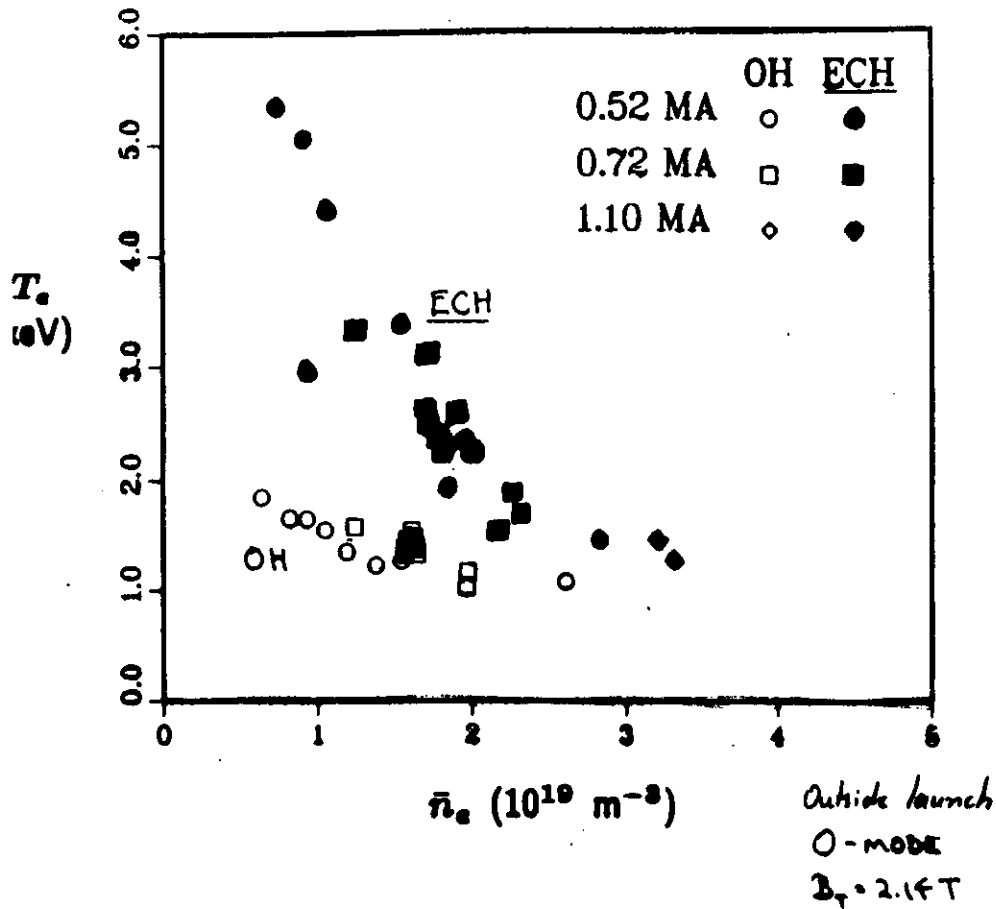
$$\tau_E^{\text{KG}} = 8 \text{ ms}$$

Outside L.
 O-mode

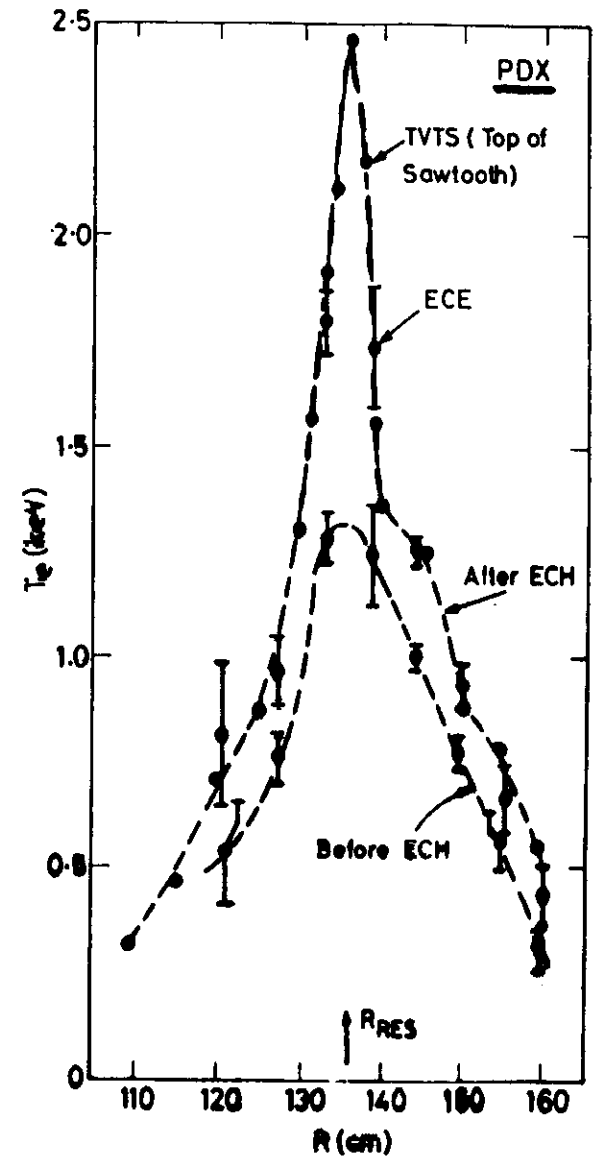
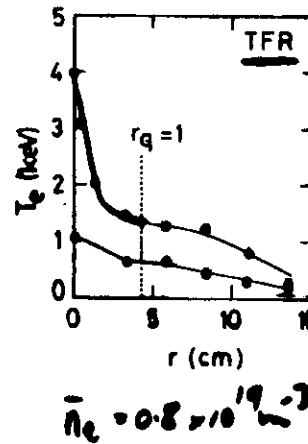
Fig. 5 a) X-ray spectrum detected for the time interval shown in Fig. 5b. 10 gyrotrons. $I_p = 210$ kA, $B_0 = 2.827$, $n_0 = 1.5 \cdot 10^{19} \text{ cm}^{-3}$, before carbonization. The dashed line is the simulation for $T_e(0) = 8$ keV and a typical $T_e(r)$.
 b) temporal behaviour of $T_e(0)$ recorded by ECE. Labeled by arrows is the interval over which the spectrum was recorded.

Difference between 8 keV from SXR PHA and 10 keV from ECE can be understood from Fokker-Planck calculations (R. Harvey) (Quasi-perpendicular launch)

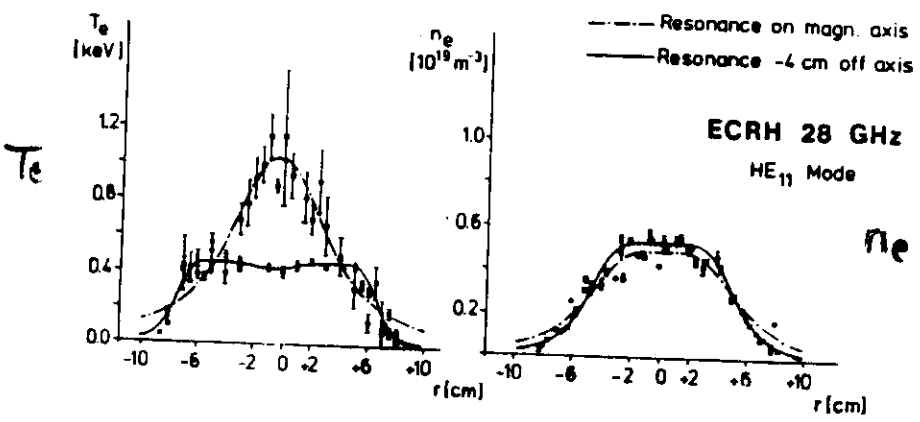
CENTRAL ELECTRON TEMPERATURE AS A FUNCTION OF DENSITY



Resonance on axis



$P = 75 \text{ kW}$ $I_p = 0.26 \text{ MA}$
 $n_e(0) = 1.2 \times 10^{19} \text{ m}^{-3}$

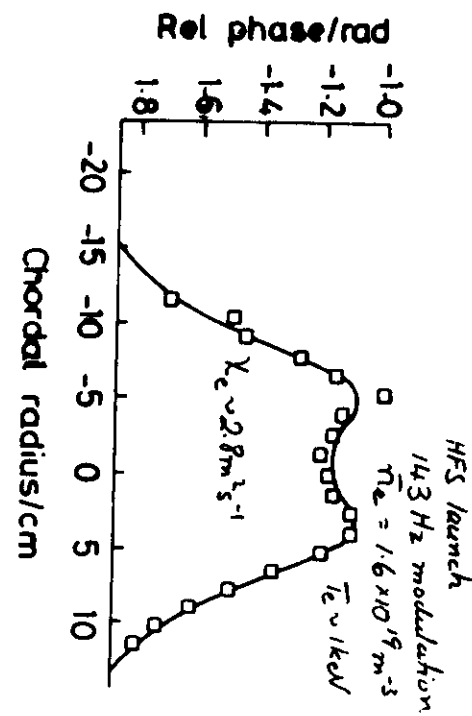
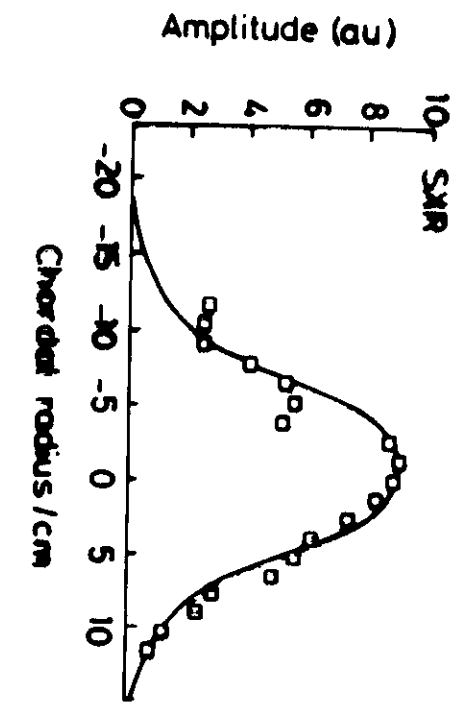
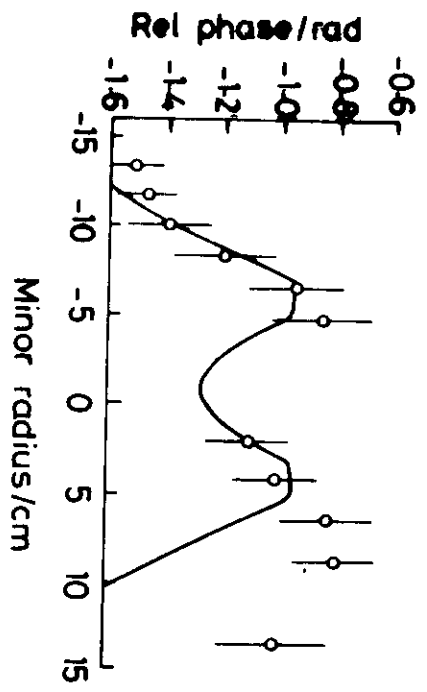
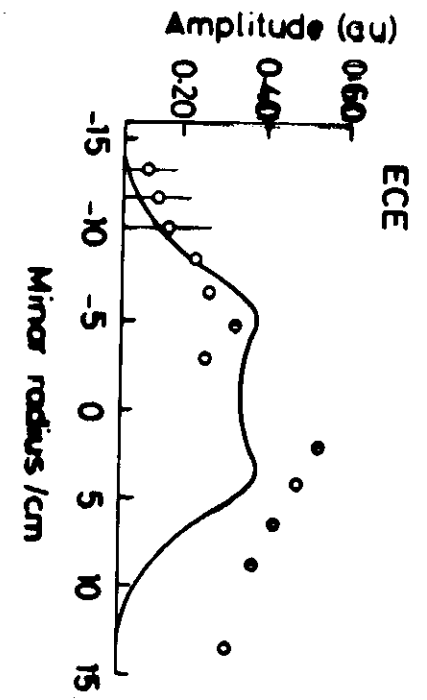


Erckmann et al. (1985)

$P_{RF} \approx 170 \text{ kW}$
 $\rightarrow 190 \text{ kW}$

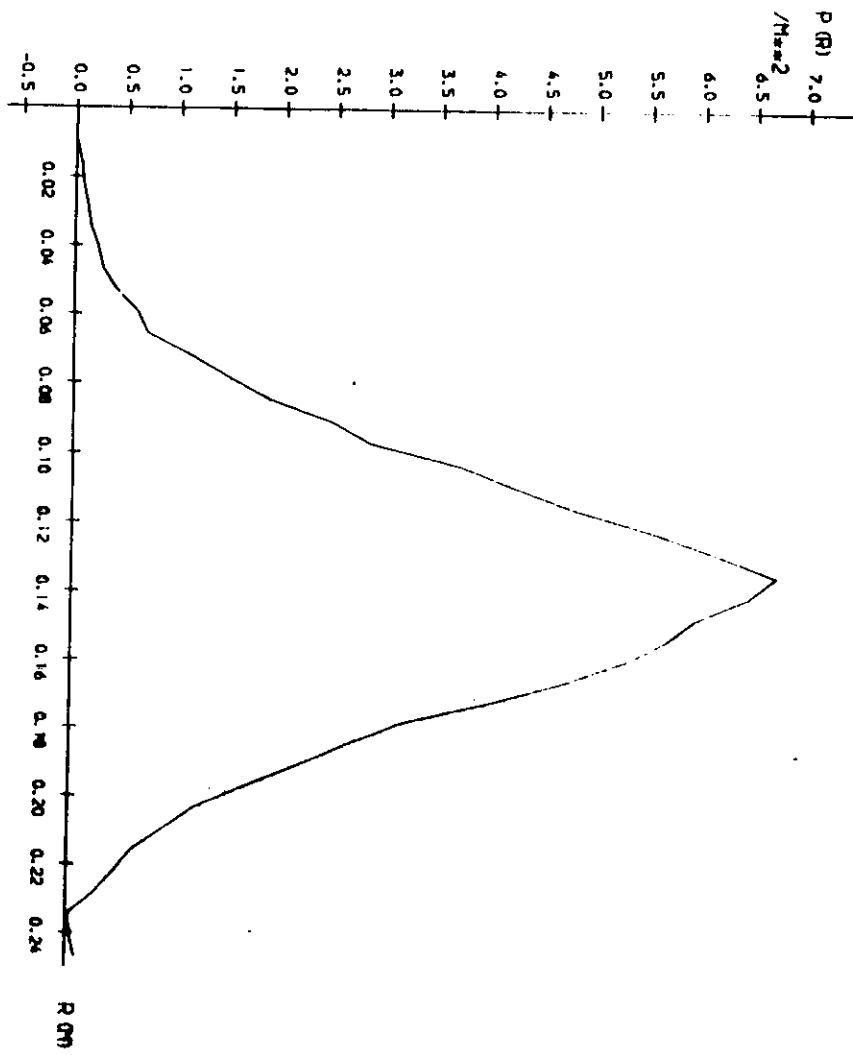
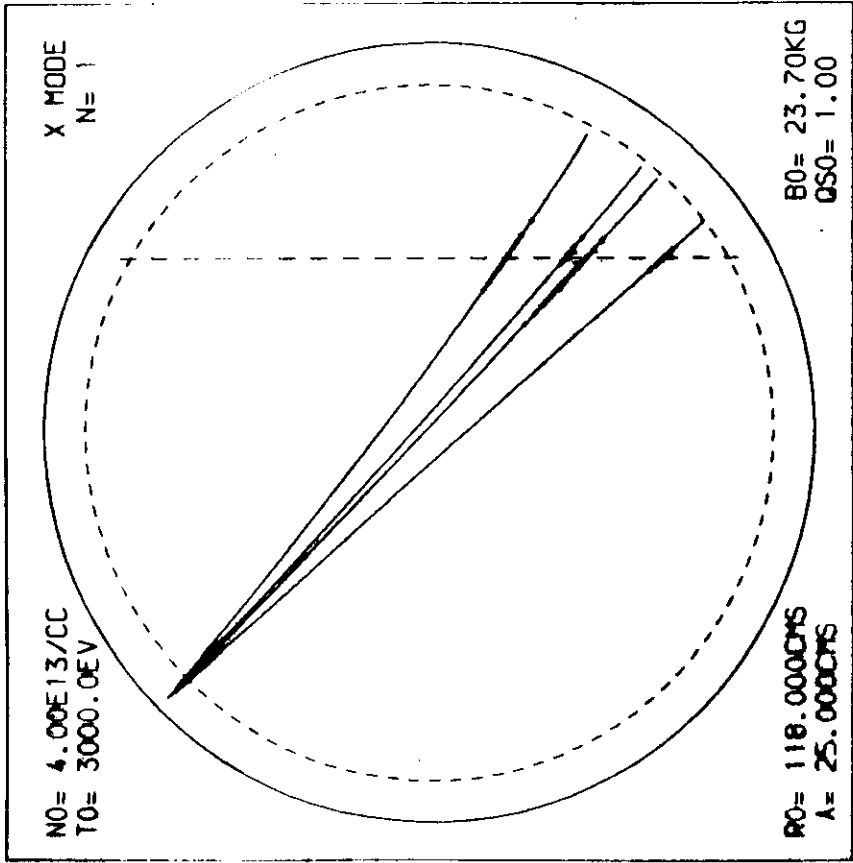
Change of resonance position
 \rightarrow change of power deposition
 \rightarrow change of plasma profiles

No "profile consistency"

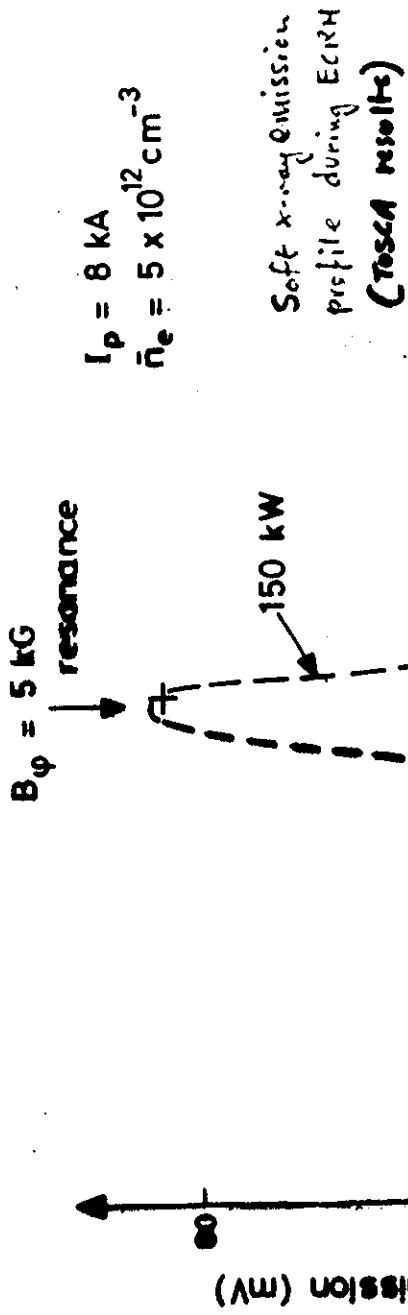


ECRH Modulation Experiments on DITE

60 GHz X-mode track
 HFS launch
 143 Hz modulation
 $\bar{n}_e = 1.6 \times 10^{19} \text{ m}^{-3}$

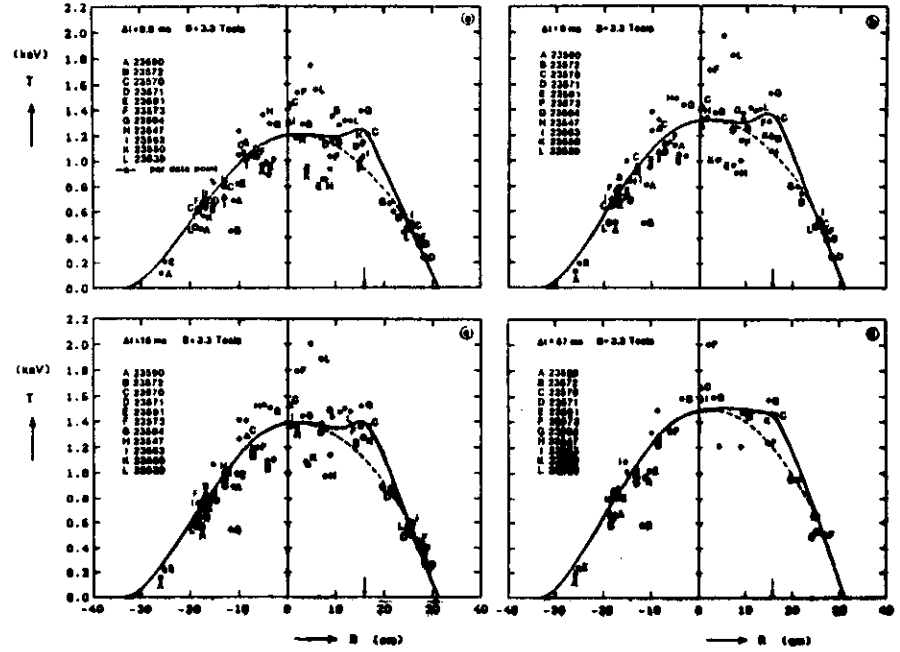


Evidence for Energetic Trapped Electrons - Tosca



T10

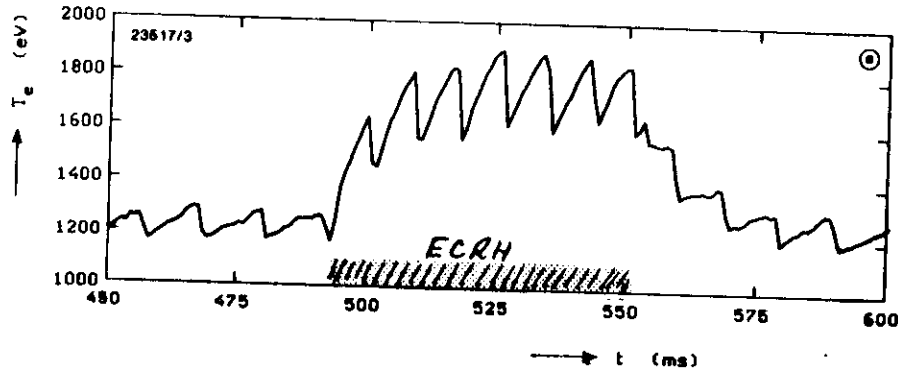
ECE



ECRH: Sawtooth Response

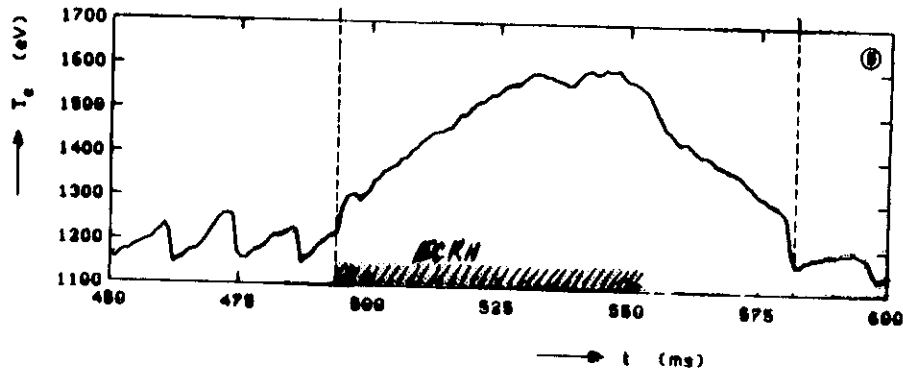
T10 $R = 1.48\text{ m}$ $a = 0.34\text{ m}$ $f = 84\text{ GHz}$, 500 kW
 $\theta = 90^\circ$ $O\text{ mode } 70\%$ $X\text{ mode } 30\%$

On axis $B = 3.0\text{ T}$ $I_p = 0.44\text{ MA}$ $\bar{n}_e = 4.5 \times 10^{19}\text{ m}^{-3}$



(From ALE)

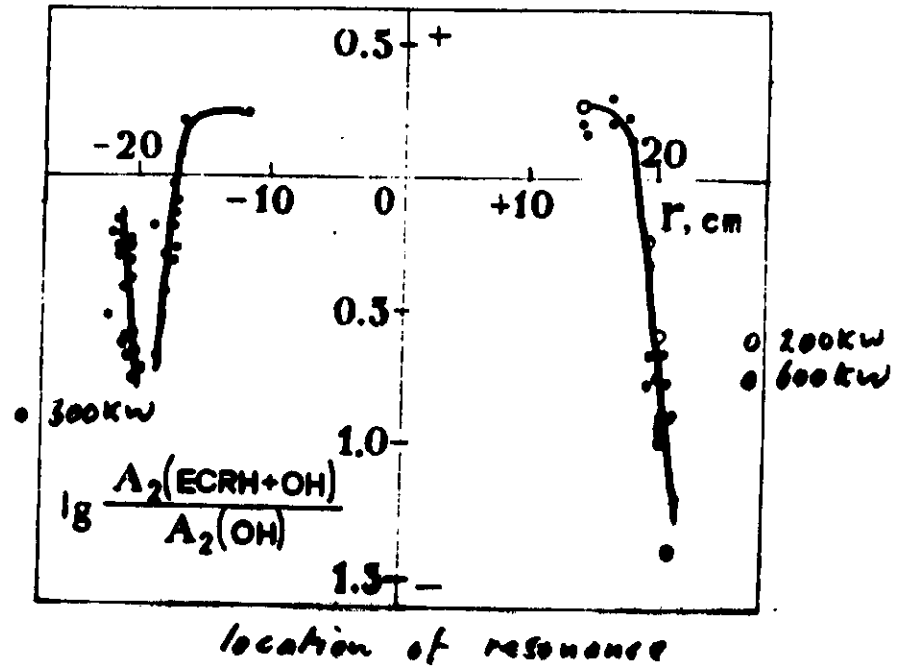
Off axis (+16cm) $B = 3.3\text{ T}$ $I_p = 0.35\text{ MA}$ $\bar{n}_e = 4.2 \times 10^{19}\text{ m}^{-3}$



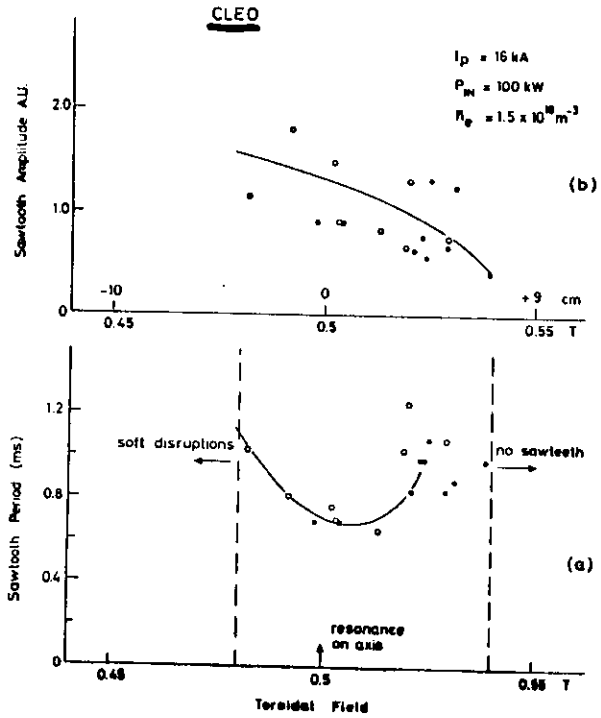
(From ALE)

T10 Hlikaev and Kajumova (1985) Varenna

Suppression of $m=2$ mode



$$P_{\text{abs.}} \approx 0.75 P_{\text{aux.}}$$

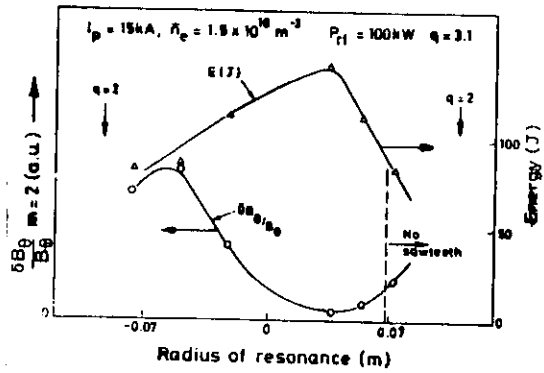
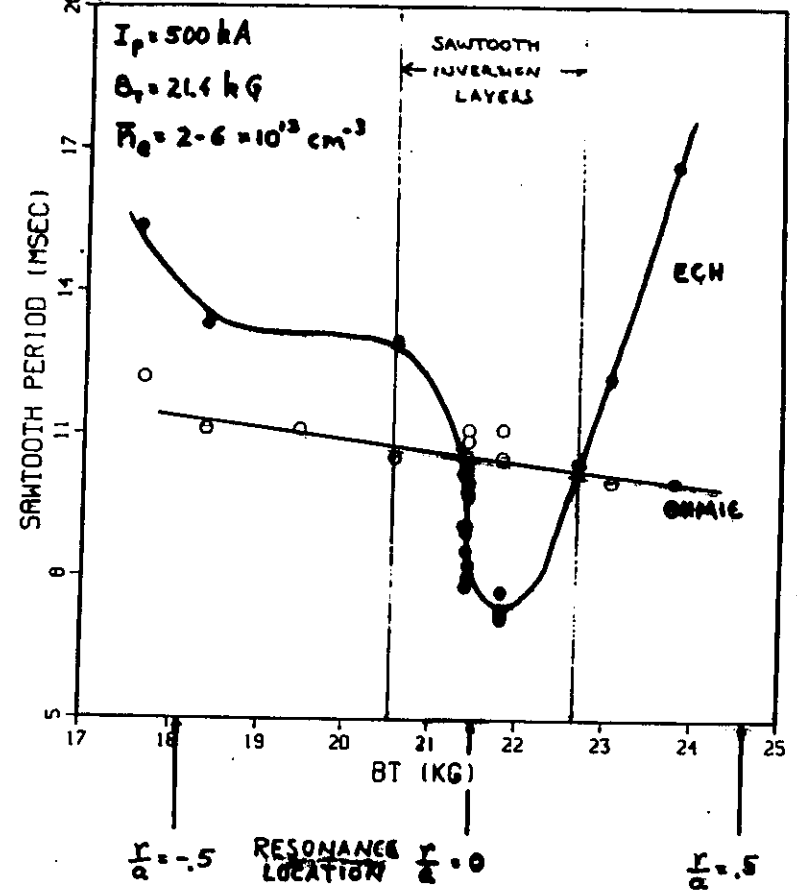


28 GHz zone
 $q_a = 3$

DiII

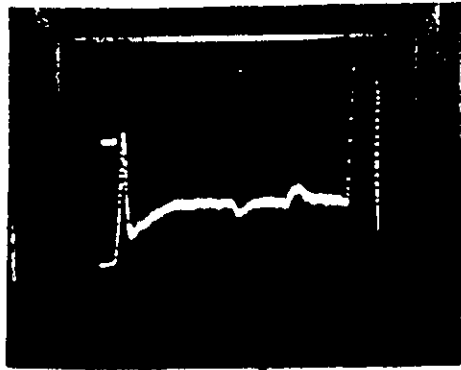
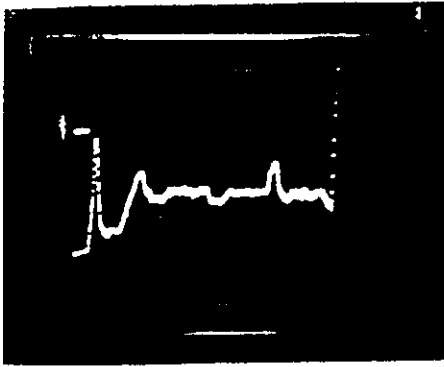
SAWTOOTH PERIOD VERSUS TOROIDAL FIELD FOR ECH AND OHMIC DISCHARGES

$n_e < n_c$

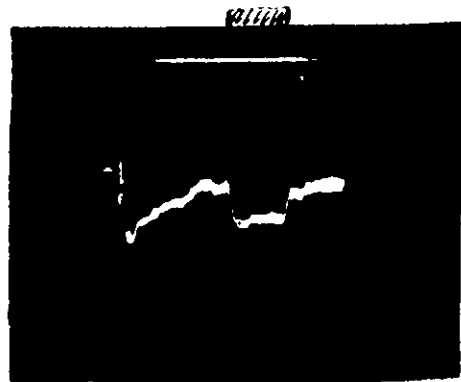
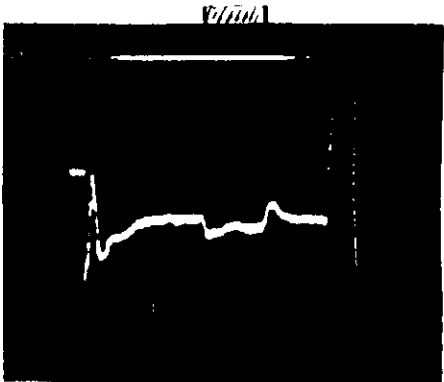


CLEO 28 GHz

$\omega_{ce} = 15 \text{ KH}$
 $n_{e0} = 5 \cdot 10^{12} \text{ cm}^{-3}$

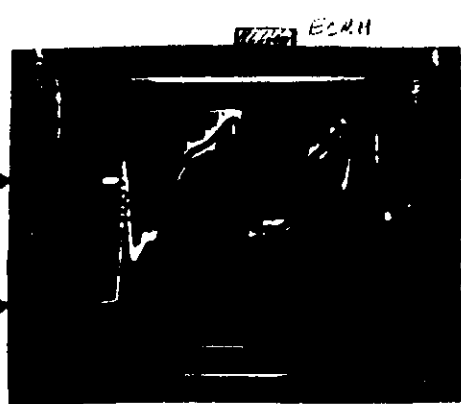


$1.9 \times 10^{12} \text{ cm}^{-3}$



$2.4 \times 10^{12} \text{ cm}^{-3}$

$3.4 \times 10^{12} \text{ cm}^{-3}$



$\bar{n}_e = 4 \cdot 10^{12} \text{ cm}^{-3}$
 before ECRH

$5.9 \times 10^{12} \text{ cm}^{-3}$

3 fringe
 $4 \cdot 10^{12}$

T10

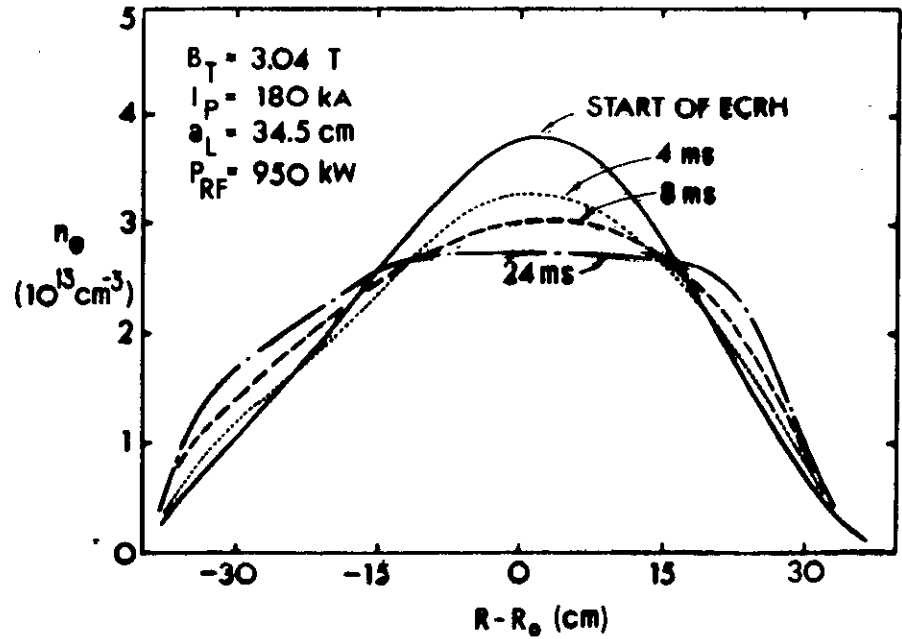


FIG. 10

Relativistic Effects

• Relativistic form of EC resonance condition

- mass increase with increasing energy

$$\omega - \Omega(1 - v^2/c^2)^{1/2} = k_{||} v_{||} \quad \Omega = eB/m_0$$

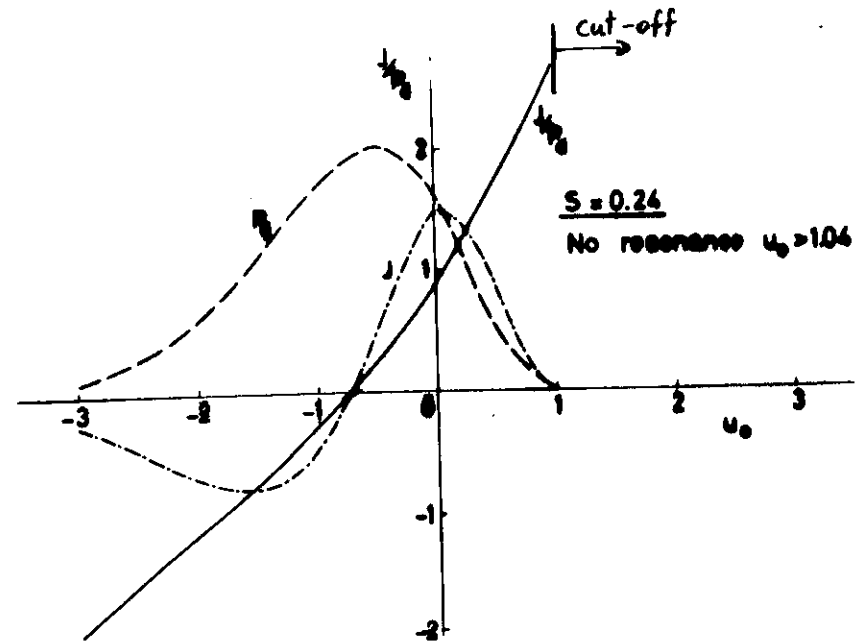
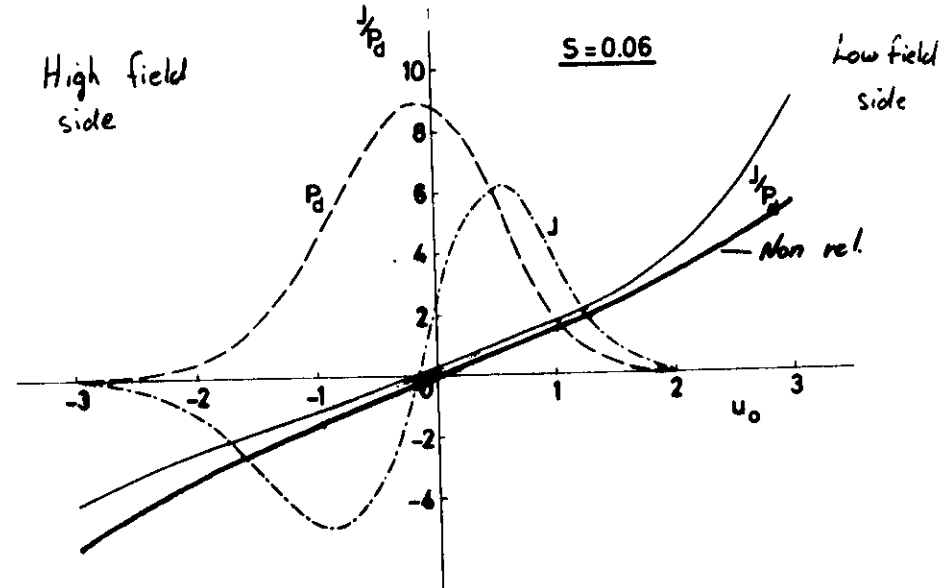
relativistic mass increase
down-shifts gyrofreq.

Doppler
shift

$\omega < \Omega$ (high field side resonance)
electrons with +ve or -ve values of $v_{||}$ can resonate

$\omega > \Omega$ (low field side resonance)
only electrons with $v_{||}$ same sign as $k_{||}$ can resonate
& those electrons have larger $|v_{||}|$ than in non-rel. case

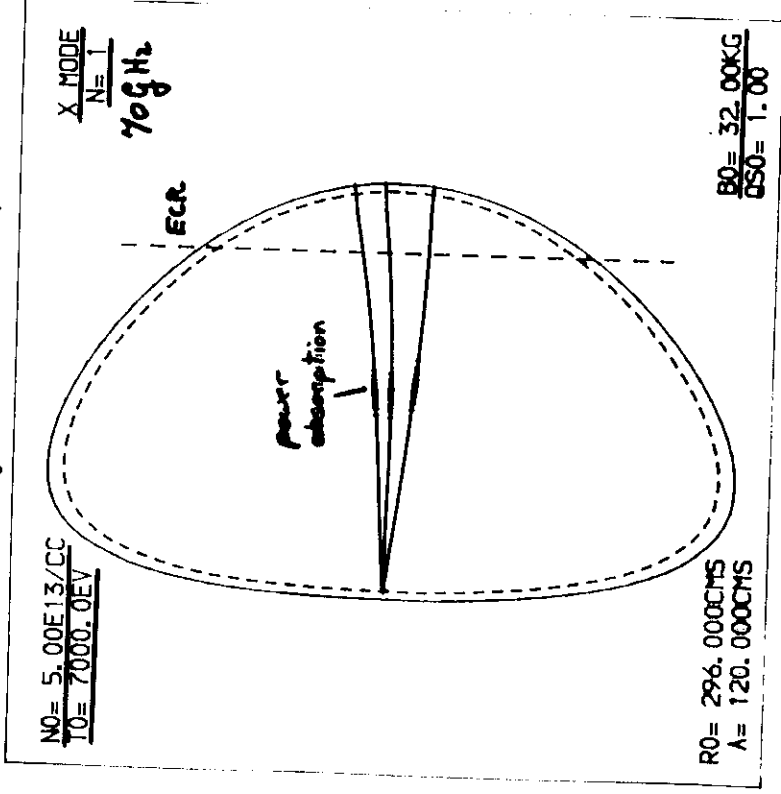
Effect of relativistic resonance condition on power deposition and current drive



$$\omega - \Omega(1 - v^2/c^2)^{1/2} = k_{||} v_{||} \Rightarrow \underbrace{\frac{\omega - \Omega}{k_{||} v_e}}_{\text{Doppler}} + \underbrace{\frac{\Omega v_e}{2k_{||} c^2}}_{\text{rel.}} \frac{v_{||}}{v_e^2} = \frac{v_{||}}{v_e}$$

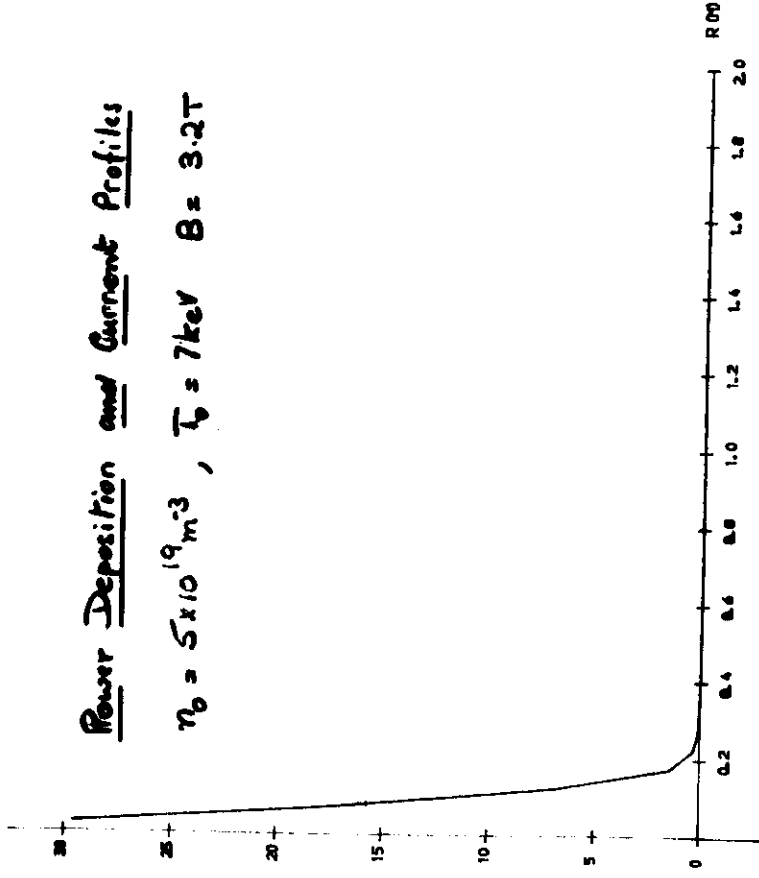
$$T_e = T_0(1-\psi) \approx T_0(1-r_{\text{ECR}}^2) \quad \text{or } n_e \text{ similarly.}$$

Launch angle 50° to \vec{B}_0



Power Deposition and Current Profiles

$$n_0 = 5 \times 10^{19} \text{ m}^{-3}, \quad T_0 = 7 \text{ keV}, \quad B = 3.2 \text{ T}$$



Evidence for down-shifted resonance (DIRE)

