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INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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H4.SMR. 405/14

SECOND WORKSHOP ON TELEMATICS

6 - 24 November 1989

Optical Fibre Overview: Propagation and Transmission Properties

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These notes are intended for internal distribution only

OPTICAL FIBRE OVERVIEW:

PROPAGATION AND TRANSMISSION PROPERTIES

(R. CAPONI - CSELT-TORINO)

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1) INTRODUCTION TO OPTICAL TRANSMISSIONS:

- GENERAL CHARACTERISTICS, ADVANTAGES
- THE OPTICAL FIBRE (BASIC PARAMETERS)

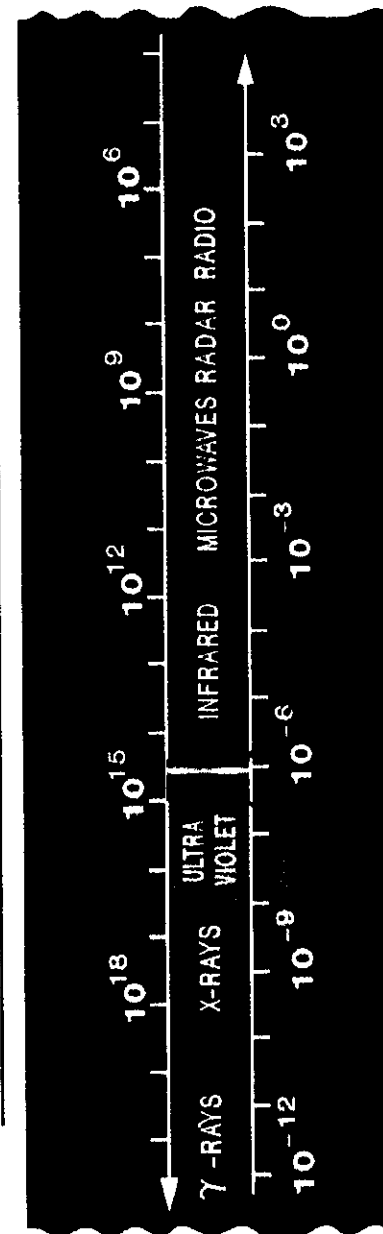
2) FIBRE PROPAGATION:

- E.M. MODES
- FIBRE TYPES
 - MULTIMODE
 - SINGLE MODE
- NORMALIZED FREQUENCY

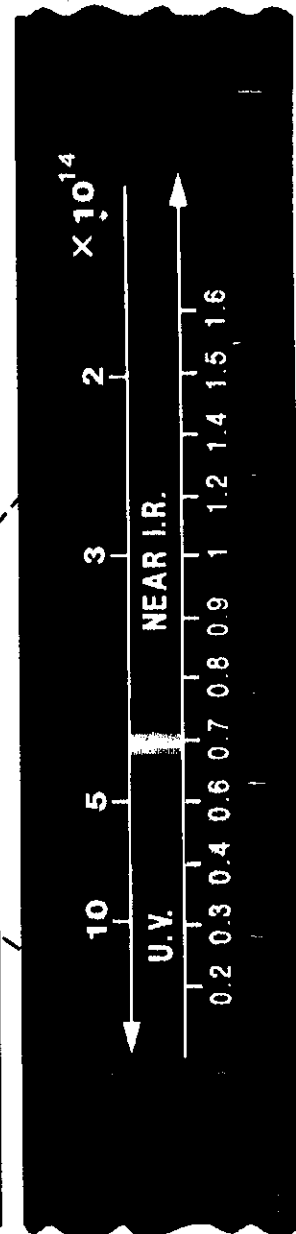
3) BASIC O.F. TRANSMISSION PROPERTIES:

- ATTENUATION
- DISPERSION

THE ELECTROMAGNETIC SPECTRUM

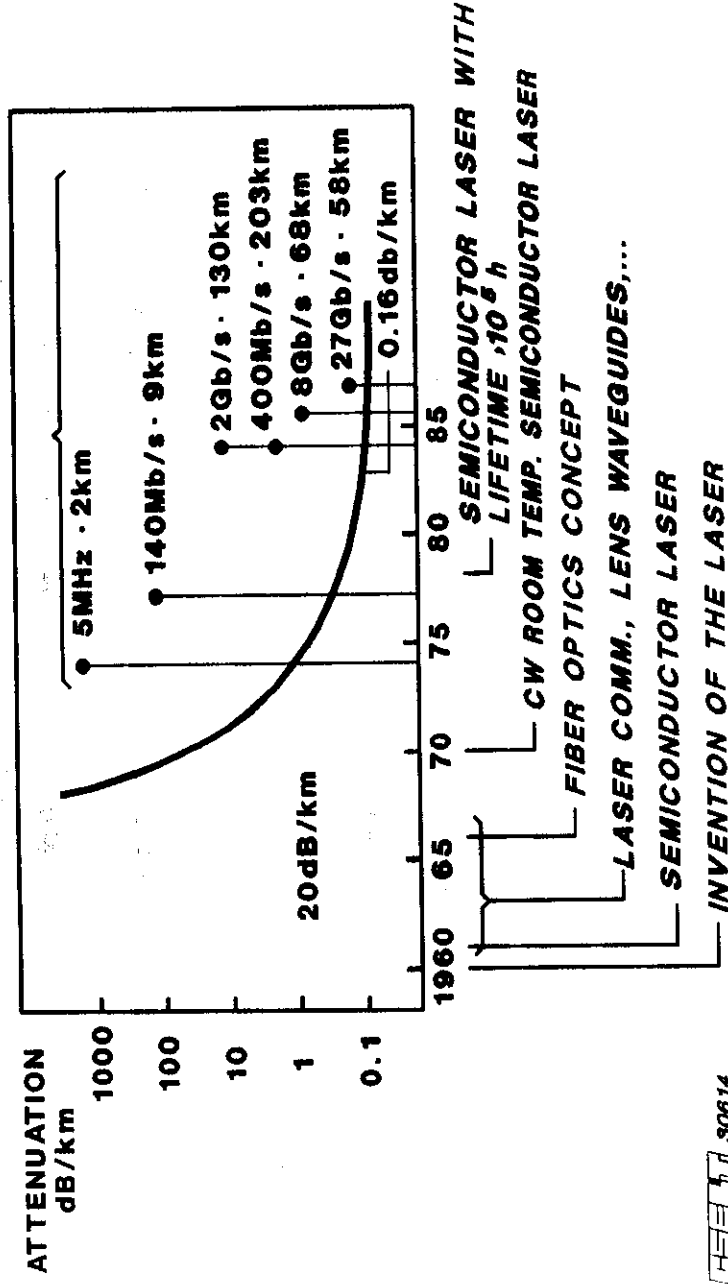


THE OPTICAL SPECTRUM



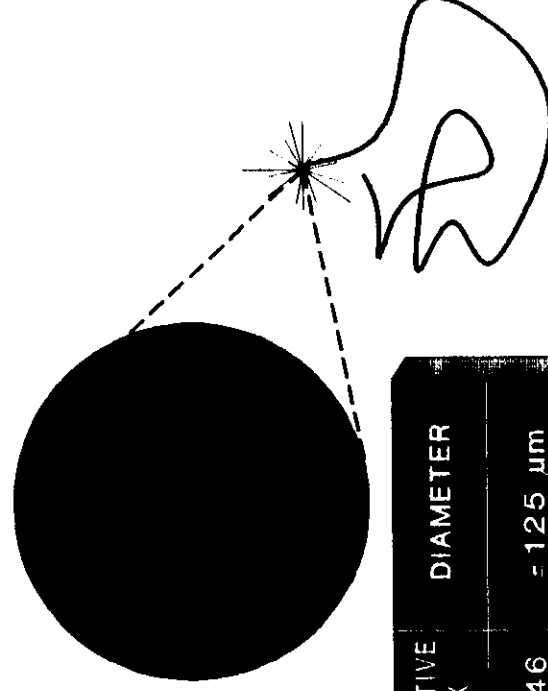
$\lambda f = c$ (vacuum speed of light)

DEVELOPMENT OF OPTICAL COMMUNICATIONS



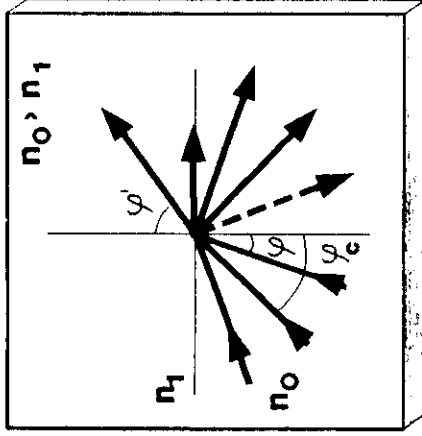
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THE OPTICAL FIBRE



	REFRACTIVE INDEX	DIAMETER
CLADDING	$n_1 = 1.46$	$\approx 125 \mu\text{m}$
CORE	$n_1 + 5-10\%$	$\approx 5-10; 50 \mu\text{m}$

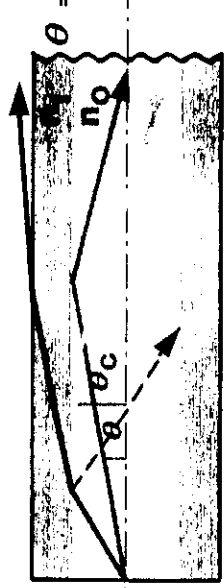
TOTAL INTERNAL REFLECTION



- SNELL'S LAW: $n_0 \sin \varphi = n_1 \sin \varphi'$
- LIMITING CONDITION: $\varphi' = 90^\circ \rightarrow n_0 \sin \varphi_c = n_1$
- TOTAL REFLECTION RANGE: $\varphi > \varphi_c$

LIMITING ANGLE
FOR GUIDED RAYS:

$$\theta = 90^\circ - \varphi : \theta_c = 90^\circ - \varphi_c \rightarrow \cos \theta_c = \frac{n_1}{n_0}$$

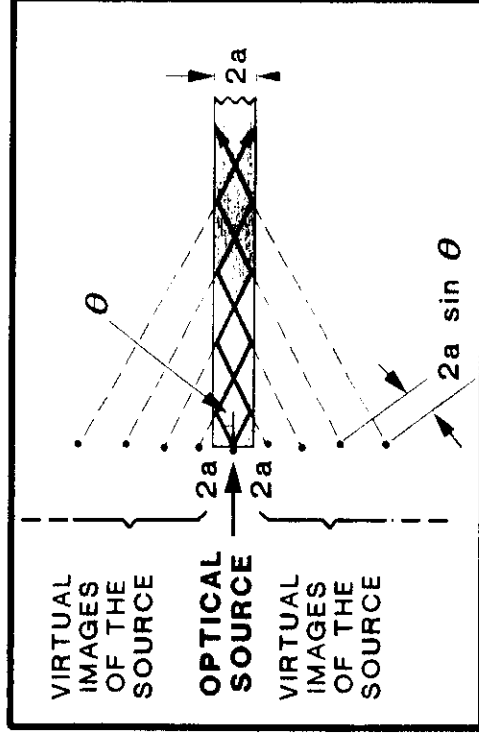


GUIDED RAY
(TOT. INTERNAL
REFLECTION):
 $\theta < \theta_c$

NUMERICAL APERTURE: $A = n_0 \sin \theta_c$

$$A = \sqrt{n_0^2 - n_1^2} = \sqrt{2 n_1 (n_0 - n_1)} \quad (\text{TYPIC.: } A = 0.1-0.2)$$

A RAY-OPTICAL APPROACH TO E.M. MODES



THE PLANAR (MIRROR)
WAVEGUIDE MODEL

EQUIVALENCE WITH A
GRATING OF PERIOD: $2a$

DIFFRACTION AND
INTERFERENCE DETERMINE
GUIDANCE CONDITION

ONLY THE RAYS UNDERGOING A CONSTRUCTIVE
INTERFERENCE ARE ALLOWED TO PROPAGATE (grating equation)

$$\text{that is: } 2a \cdot \sin \theta = m \cdot \lambda \quad (m = 0, 1, 2, \dots)$$

ONLY DEFINITE E.M. CONFIGURATIONS - LABELLED
BY INTEGER(S) - PROPAGATE IN A WAVEGUIDE:
E.M. MODES

GUIDED MODES

• DIELECTRIC GUIDE (SLAB):

$$v_{\text{MEDIUM}} < c_{\text{(FREE SPACE)}} \quad (\Rightarrow n = \frac{c}{v} > 1)$$



$$\lambda = \frac{\lambda_{\text{(F.S.)}}}{n} < \lambda_{\text{(F.S.)}} \text{ replaces } \lambda \text{ in relev. eqs.}$$

Therefore :

① mode eq. (approx.!) : $2a \sin \vartheta = m\lambda = m\lambda/n$

② guidance condition : $n \sin \vartheta \leq A$



$$\begin{cases} \vartheta = \vartheta_m \\ m\lambda = 2a n \sin \vartheta_m \leq 2aA \end{cases}$$

CONCLUSION : The m -th mode is guided if;

$$2\pi a A > m \cdot \pi$$

RADIAL PART of the FIELD:

$$\vec{E}(z) = \vec{E}_t(z) + \hat{z} E_z$$

$$\vec{H}(z) = \vec{H}_t(z) + \hat{z} H_z$$

SCALAR WAVE EQUATION: $\vec{E}_t \rightarrow \phi(z)$

$$\phi''(z) + \frac{\phi'(z)}{z} + \left[\left(\frac{2\pi}{\lambda} \right)^2 n^2(z) - \beta^2 - \left(\frac{v \pm 1}{z} \right)^2 \right] \phi(z) = 0$$

$$E_z = -\frac{j}{k} \left(E'_z \pm \frac{v \pm 1}{z} E_z \right) \quad \left[k(z) = \frac{2\pi}{\lambda} n(z) \right]$$

$$H_z = -\frac{j}{k} \left(H'_z \pm \frac{v \pm 1}{z} H_z \right)$$

$$E_z(z) = \begin{cases} A_0 \phi_0(z) & , z < a \quad |\phi_0(0)| < \infty \\ A_1 \phi_1(z) & , z > a \quad |\phi_1(\infty)| < \infty \end{cases}$$

CONTINUITY CONDITIONS at $z=a$:

$$\frac{\phi'_0(a)}{\phi_0(a)} = \frac{\phi'_1(a)}{\phi_1(a)} \quad \begin{array}{l} \text{CHARACTERISTIC} \\ \text{EQUATION} \end{array}$$

FOR EACH v -VALUE $\rightarrow$ TWO FAMILIES OF SOLUTIONS:

[$v \pm 1$]

~~HE₁₁ MODE~~

(UPPER SIGN)

~~HE₁₂ MODE~~

(LOWER SIGN)

MODE DEGENERACY: LP MODES

• $HE_{\nu+1\delta}$ and $EH_{\nu-1\delta}$ FOLLOW THE SAME EQUATION

→ THEY HAVE THE SAME β and PROPERTIES



COMPOSED MODE:



LINEARLY POLARIZED

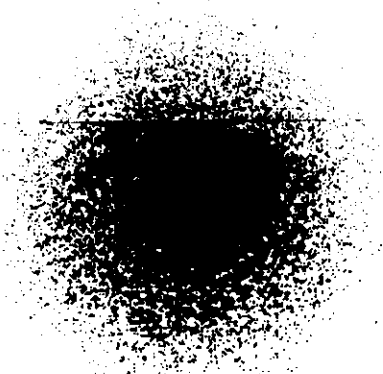
• $\nu=0$ ONLY ONE MODE $LP_{0\delta} \equiv HE_{1\delta}$

• $\nu=1$ THREE MODES COMBINED:

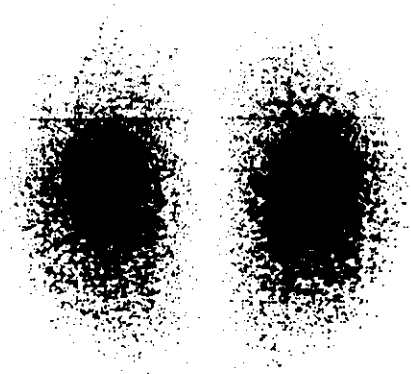
$$LP_{1\delta} \equiv \begin{cases} HE_{2\delta} + TE_{0\delta} \\ HE_{2\delta} + TM_{0\delta} \end{cases}$$

PHYSICAL MEANING OF ν and δ

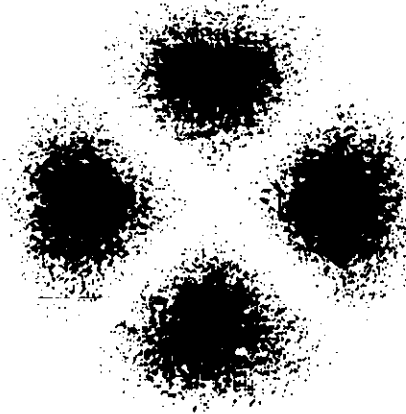
- 2ν NUMBER OF MAXIMA OF THE FIELD INTENSITY IN A TURN AROUND THE FIBRE AXIS
- δ NUMBER OF MAXIMA OF THE FIELD INTENSITY



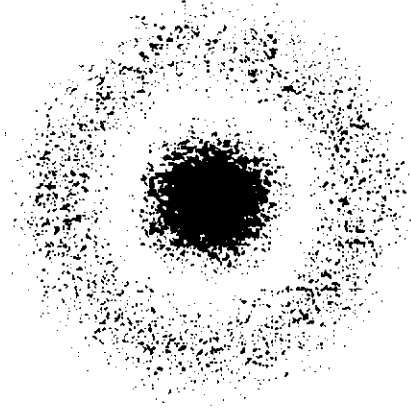
LP_{01}



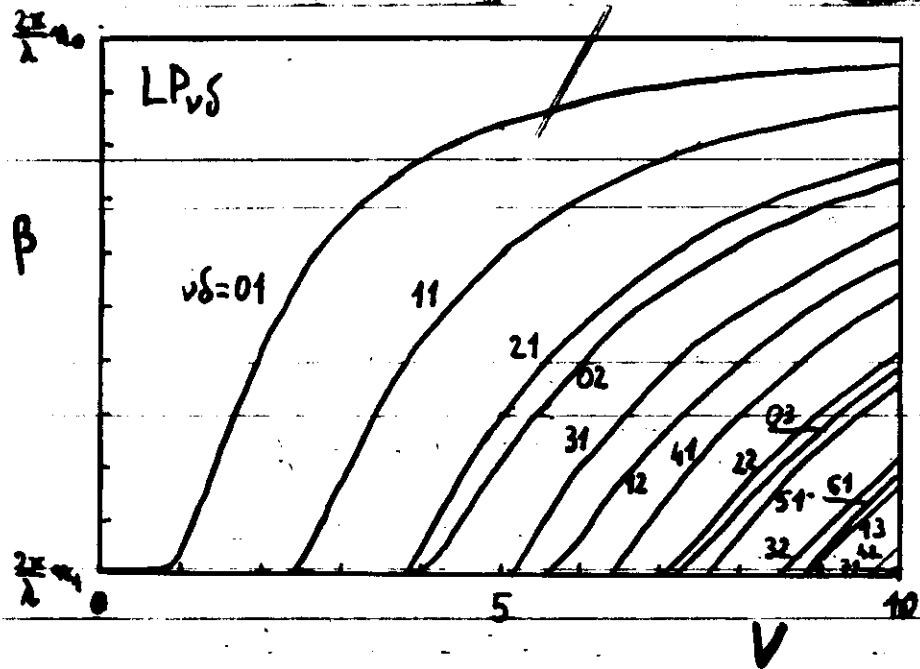
LP_{11}



LP_{21}



LP_{02}



CUT-OFF

LP_{01} MODE IS GUIDED ONLY IF:

$$V > V_{01}^{EO} \quad \text{or} \quad \lambda < \lambda_{01}^{EO} = \frac{2\pi a A}{V_{01}^T}$$

CUT-OFF WAVELENGTH OF LP_{01} MODE

IF $V < V_{01}^{CO}$ ($\lambda > \lambda_{01}^{CO}$) FIBRE GUIDES ONLY

: FUNDAMENTAL MODE

NORMALIZED FREQUENCY:

$$V = \frac{\pi}{\lambda} \cdot (\text{CORE DIAMETER}) \cdot (\text{NUMERICAL APERTURE})$$

↑ No. GUIDED MODES $\propto V^2$

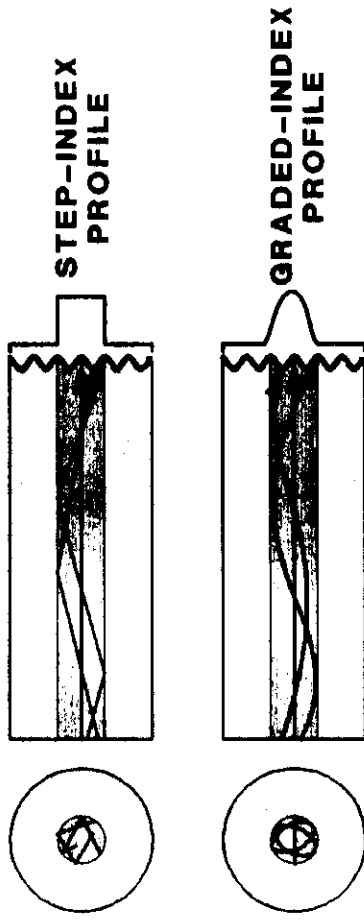
ULTIMOE

ANGLE-M

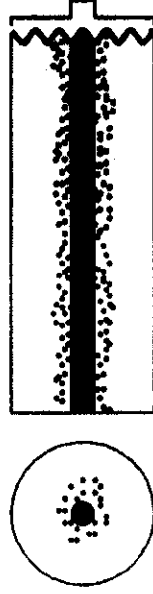
CONDITION

FIBRE TYPES

MULTIMODE FIBRE



SINGLE-MODE FIBRE



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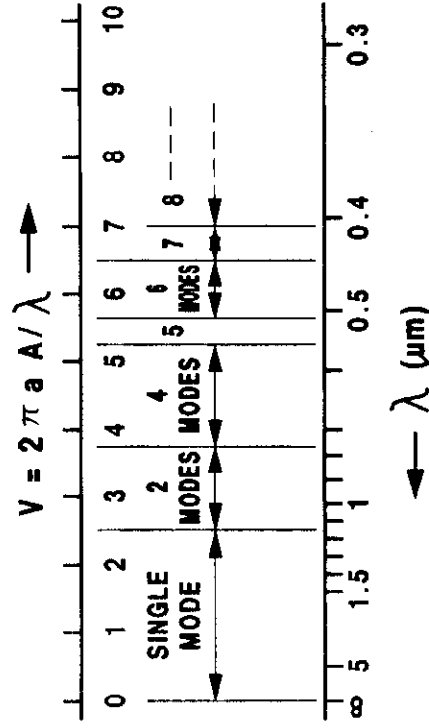
CUT-OFF V-VALUES OF THE LOWEST ORDER MODES

MODES LP_{nl}	$V_{\text{CUT-OFF}} (LP_{nl})$	
	STEP PROFILE	PARABOLIC PROFILE
LP_{01}	0	0
LP_{11}	2.4	3.5
LP_{02}	3.8	5.1
LP_{21}	3.8	5.7
LP_{31}	5.1	7.8
LP_{12}	5.5	7.5
LP_{41}	6.4	9.9
LP_{03}	7.0	9.2

EXAMPLE (step-index profile):

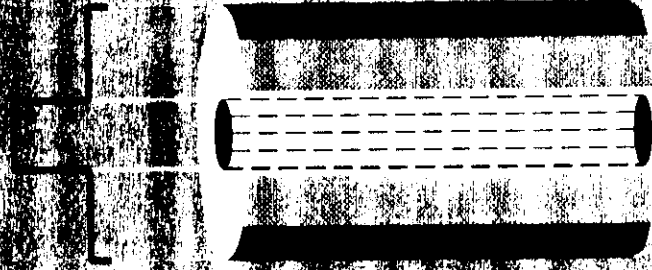


$$aA = 0,45 \mu\text{m} \quad \left\{ \begin{array}{l} 2a = 9 \mu\text{m} \\ A = 0,1 \end{array} \right.$$



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THE SINGLE-MODE FIBRE



Refractive Index profile: $n(r)$

	REFRACTIVE INDEX	DIAMETER
CLADDING	$n_2 = 1.48$	$A = 125 \mu\text{m}$
CORE	$n_1 = 1.46$	$a \leq 5-10 \mu\text{m}$

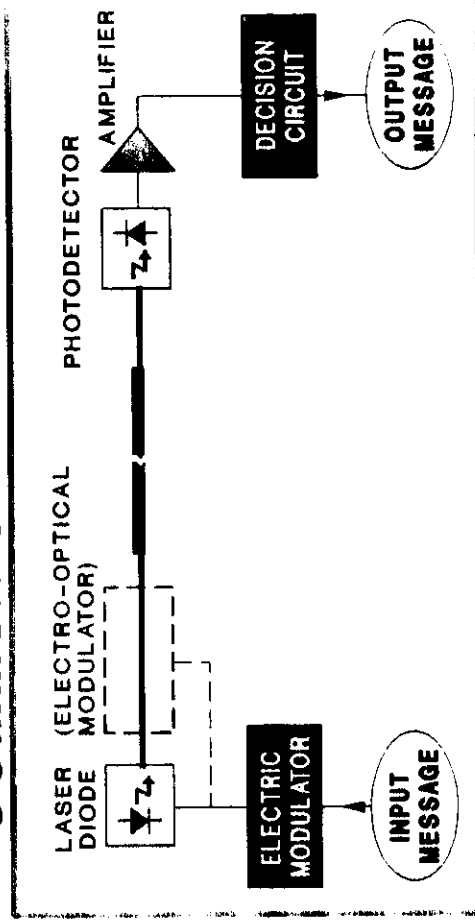
- Numerical Aperture:

$$A = \sqrt{n_{\text{MAX}}^2 - n_{\text{MIN}}^2} \approx \sqrt{2n \cdot \Delta n}$$

$$(\Delta n = n_{\text{MAX}} - n_{\text{MIN}})$$
- Normalized frequency:

$$V = \frac{2\pi}{\lambda} a A \approx \frac{2\pi}{\lambda} a \sqrt{2n \Delta n}$$

SCHEME OF A FIBRE-OPTIC COMMUNICATION SYSTEM



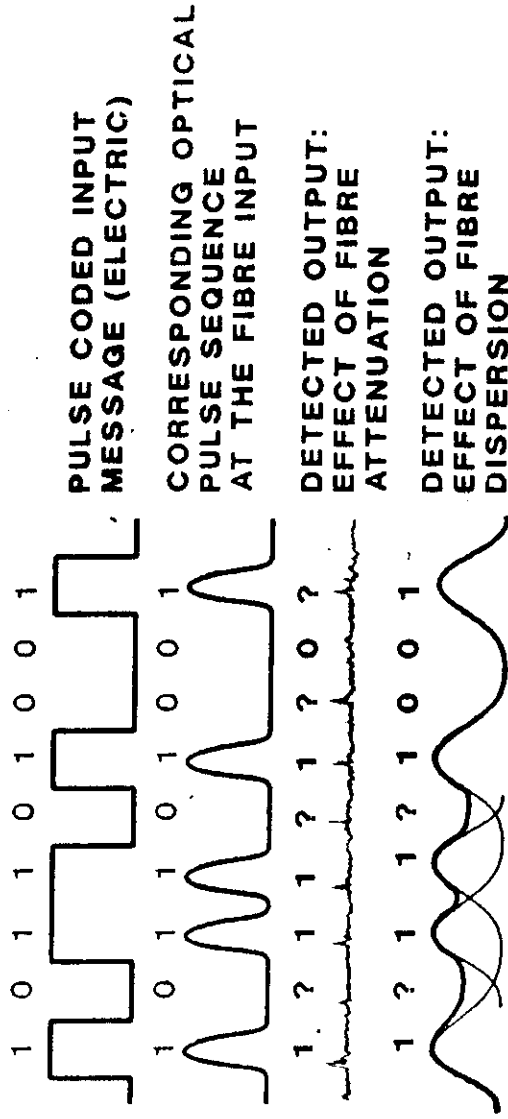
SYSTEM PERFORMANCE:

- REPEATER SPACING
- TRANSMISSION BANDWIDTH

CORRESPONDING FIBRE PROPERTIES:

- TOTAL ATTENUATION
- PULSE DISTORTION

INFORMATION LOSS DUE TO ATTENUATION AND DISPERSION



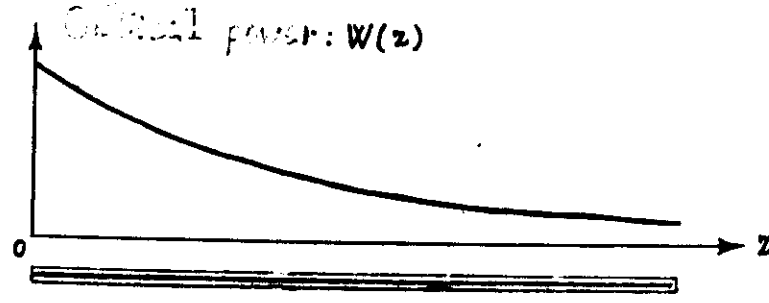
OUTPUT SIGNAL SEPARATED FROM NOISE:

→ MAX. ATTENUATION ALLOWED

ADJACENT PULSES DISTINGUISHED IN TIME:

→ MAX. DISPERSION ALLOWED

ATTENUATION



$$W(z) = W_0 e^{-\alpha z}$$

(power coefficient α)

$$\alpha = \frac{1}{L} \ln \frac{W(0)}{W(L)}$$

→ (dB/km) (ONLY)

DEFINITION OF THE ATTENUATION COEFFICIENT α IN DB/KM.

EXTRINSIC SOURCES OF ATTENUATION

● ION ABSORPTION

TRANSITION METAL IMPURITIES: { Fe ++ , Ne + + + , Cu + +
Cr + + + , Mn + + + , V + + +

EXCESS ATTENUATION.: 1-5 dB/km FOR 1 ppb

OH⁻ GROUP IMPURITIES

3 PEAKS AT 0.94 , 1.24, 1.38 μ m WITH RESPECTIVE

EXCESS ATTENUATIONS.: 1, 1.4, 70dB/km FOR 1 ppm

● OPTICAL AND GEOMETRIC ANOMALIES

CORE DIAMETER/NUMERICAL APERTURE FLUCTUATIONS, FIBRE
NON-CIRCULARITY AND FABRICATION DEFECTS IN GENERAL

● MICROBENDING

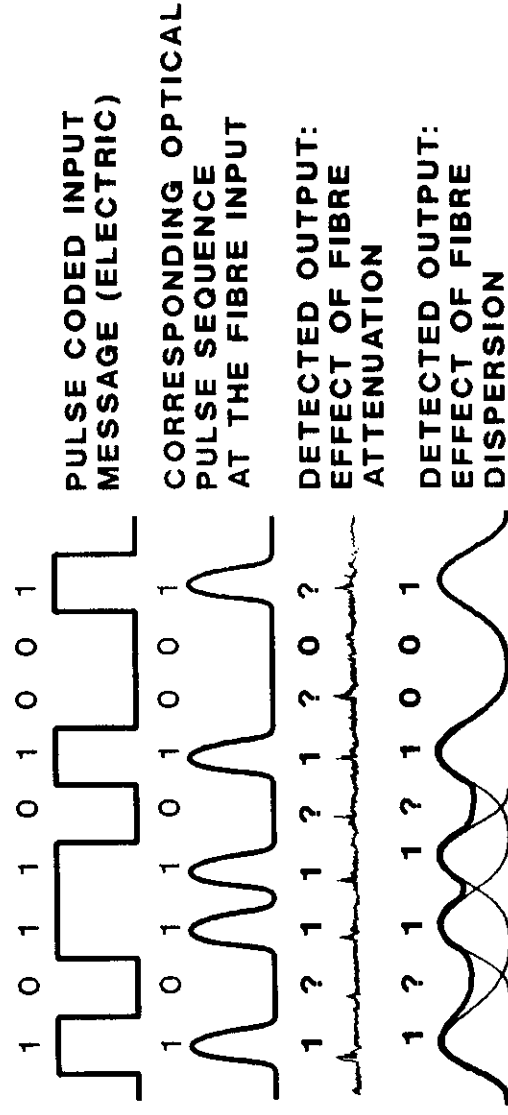
DUE TO CABLING OPERATIONS

● BENDING

FROM SPLICES, CONNECTORS, INSTALLATION

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INFORMATION LOSS DUE TO ATTENUATION AND DISPERSION



OUTPUT SIGNAL SEPARATED FROM NOISE:

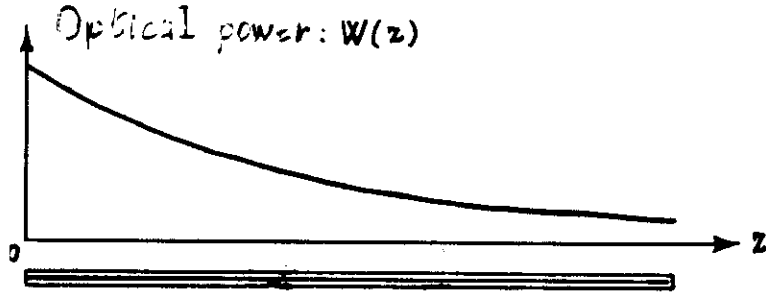
→ MAX. ATTENUATION ALLOWED

ADJACENT PULSES DISTINGUISHED IN TIME:

→ MAX. DISPERSION ALLOWED

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ATTENUATION



$$W(z) = W_0 e^{-\alpha z} \quad (\text{pure exponential} \Rightarrow)$$

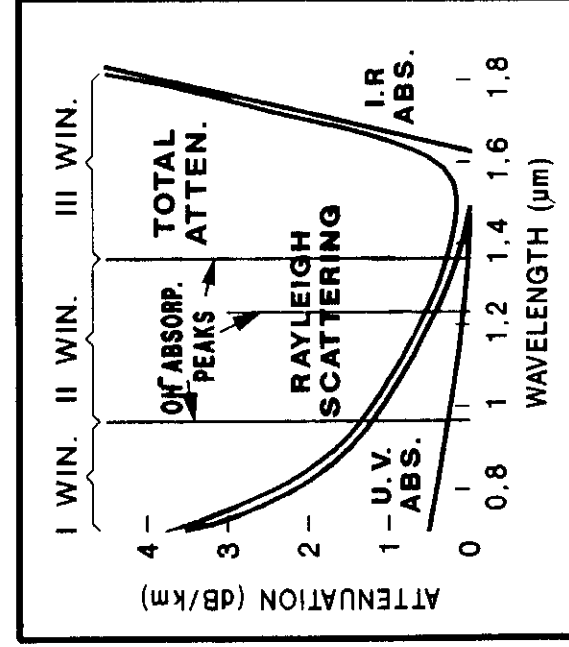
$$\alpha = \frac{1}{z_2 - z_1} \log_{10} \frac{W(z_2)}{W(z_1)}$$

$\Rightarrow$ ONE MODE ONLY)

DEFINITION OF THE ATTENUATION
COEFFICIENT in dB/km

ATTENUATION INTRINSIC SOURCES

- DEPENDENT ON GLASS COMPOSITION AND STRUCTURE
- UNAVOIDABLE

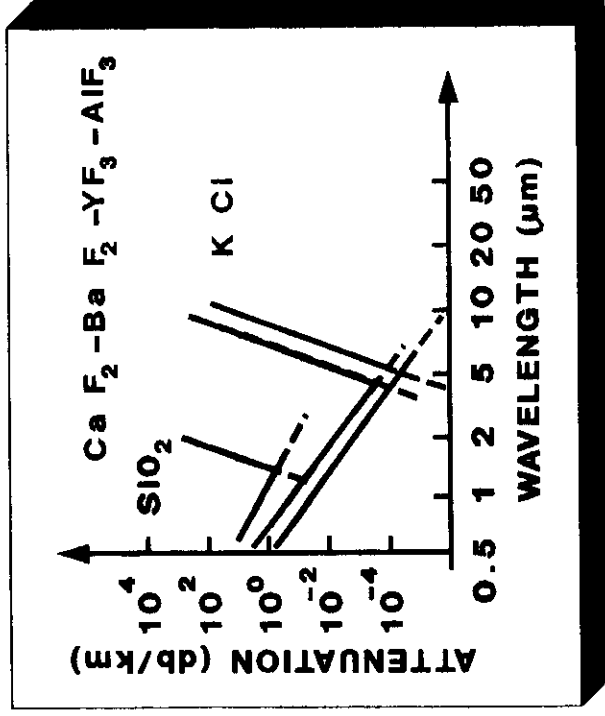


RAYLEIGH SCATTERING
(DENSITY FLUCTUATIONS
AT THE MOLECULAR LEVEL)

UV ABSORPTION
(ELECTRONIC TRANSITIONS)

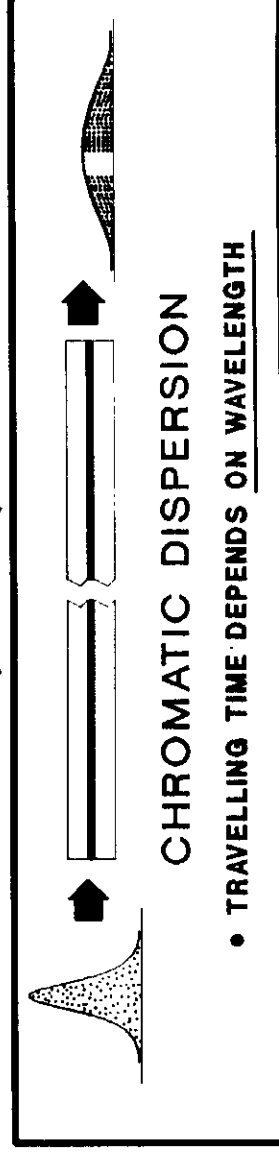
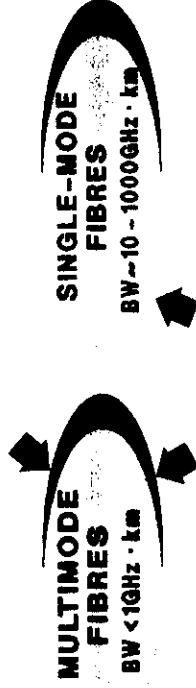
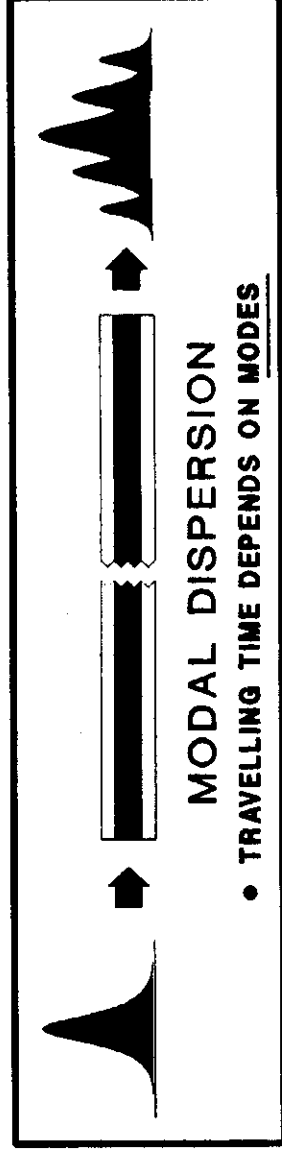
IR ABSORPTION
(MOLECULAR TRANSITIONS)

POSSIBLE ATTENUATION WITH DIFFERENT MATERIALS FOR MID-I.R.



IEEE 30630

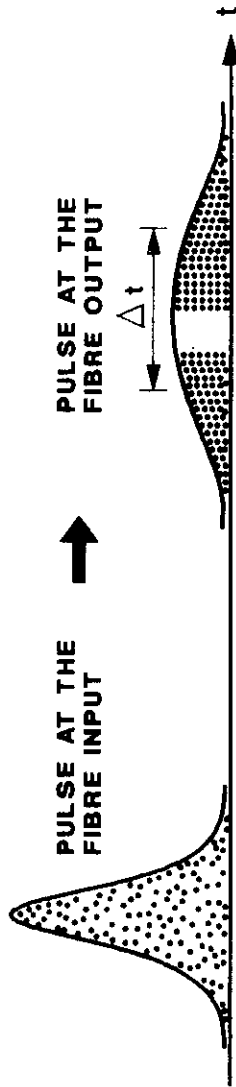
SOURCES OF PULSE DISPERSION



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CHROMATIC DISPERSION

(TRAVELLING TIME DEPENDS ON λ)
- THE ONLY SOURCE OF DISPERSION IN SINGLE-MODE FIBRES -



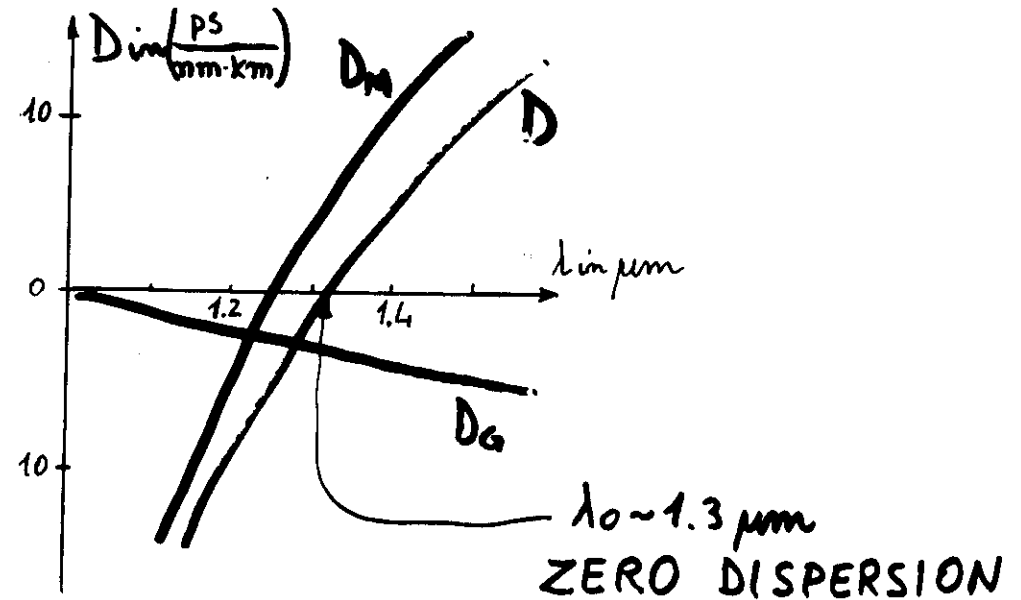
τ : TRAVELLING TIME OVER
1 km FIBRE LENGTH
 $D = d\tau/d\lambda$: CHROMATIC
DISPERSION

$$\Delta t = L \cdot \Delta \lambda \cdot D$$

L : FIBRE LENGTH
 $\Delta \lambda$: SOURCE SPECTRAL LINEWIDTH

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- τ DEPENDS on λ :
 1. THROUGH THE GUIDE EFFECT
 2. BECAUSE THE MATERIAL IS DISPERSIVE ($n = n(\lambda)$)
- ➔ D HAS TWO CONTRIBUTIONS:
 1. GUIDE DISPERSION : D_G
 2. MATERIAL DISPERSION: D_M



BANDWIDTH

$$p_{out} = g(t) * p_{in}(t)$$

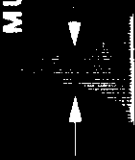
$$P_{out}(\omega) = G(\omega) P_{in}(\omega)$$

$$G(\omega) = \int_{-\infty}^{+\infty} g(t) \exp(-i\omega t) dt$$

$$\sigma_f^2 = \sigma_{out}^2 - \sigma_{in}^2$$

$$B(\text{GHz}) = 0.187/\sigma_f(\text{ns})$$

BANDWIDTH OF SINGLE-MODE FIBRE TRANSMISSIONS

	λ (μm)	D [ps/nm · km]	BW (GHz · km)
MULTIMODE LASER  $\Delta\lambda \sim 2 \text{ nm}$	1.3	-1	-100
	1.5	-10	-10
SINGLE-MODE LASER  $\Delta\lambda \sim 0.1 \text{ nm}$	1.3	-1	-2000
	1.5	-10	-200

index profile									
dispersion [ps/nm.km]	-1	0	-6	-	-	0.3	3	0	0
slope [ps/nm ² .km] at 155 μ m	0.08	0.06	0.154	-	-	0.052	0.09	0.075	-
zero disp [μ m]	1.56	1.55	1.59	1.56	1.56	1.544	1.52	1.55	1.55
reproducibility [μ m]	-	-	-	-	-	± 0.01	-	± 0.01	-
loss [dB/km] at 155 μ m	0.32	0.2	0.20	0.2	0.33	0.21	0.24	0.21 (0.17)	0.22
splice loss [dB]	-	-	0.04 ± 0.03	-	-	0.06	-	0.12	-
manufacturing process	VAD	VAD	VAD	VAD	MCVD	MCVD	VAD	OVD	MCVD
year	1982	1982	1986	1986	1984	1983/84	1985	1985/86	1984
literature	[27]	[28]	[15]	[10]	[8]	[7,22,23]	[14]	[9]	[12,13]

status of dispersion shifted SM - fibres

(FROM P.K. BACKMANN)
ELOC '86

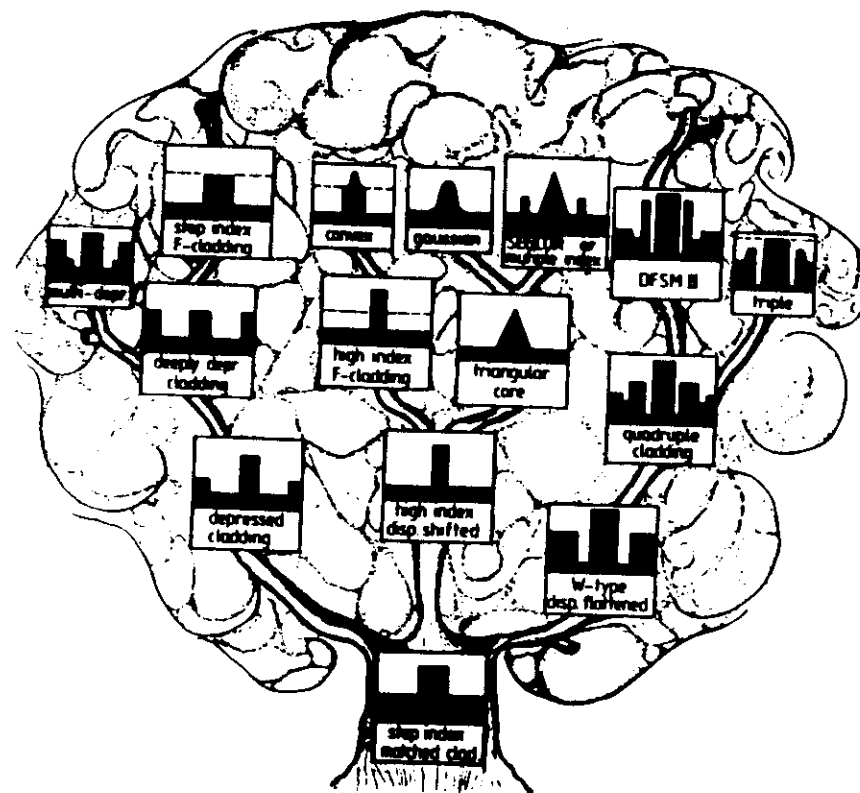


fig. 3: family tree of single mode fibres

(FROM P.K. BACKMANN)
ELOC '86

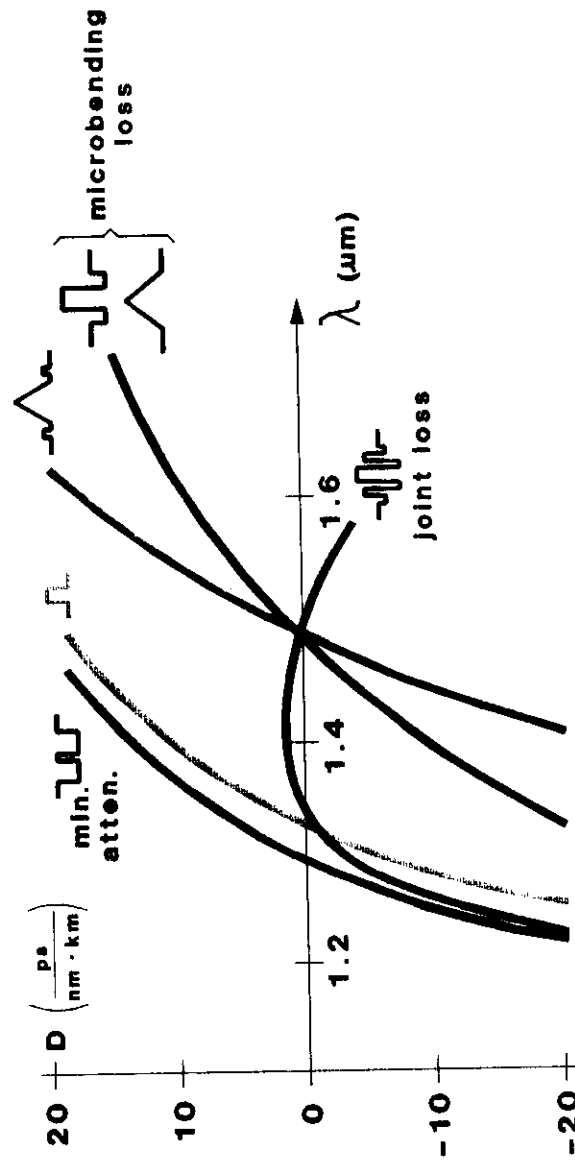
REFRACTIVE INDEX DESIGNS OF SINGLE-MODE FIBRES

	MATCHED CLADDING	1300 nm OPTIMIZED
	DEPRESSED CLADDING	LOWER BEND LOSSES
	"W" TYPE	DISPERSION MODIFIED
	PURE SILICA CORE	MINIMUM ATTENUATION
	TRIANGULAR CORE	1550 nm OPTIMIZED
	SEGMENTED CORE	1550 nm OPTIMIZED LOWER BEND LOSSES
	QUADRUPLE CLADDING	DISPERSION FLATTENED

[——— SiO_2 LEVEL]

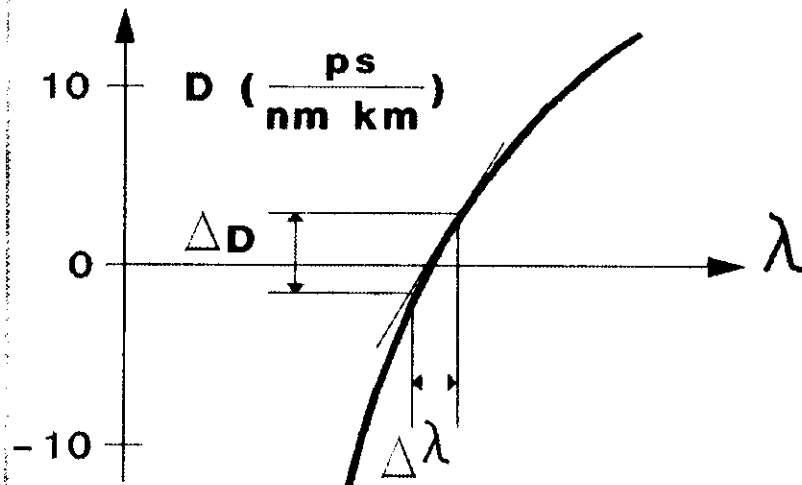
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DISPERSION OPTIMIZATION



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CHROMATIC DISPERSION (CCITT STANDARD)



λ_o : zero dispersion wavelength

$$S_o = \left. \frac{\Delta D}{\Delta \lambda} \right|_{\lambda = \lambda_o} \quad D \text{ slope at } \lambda = \lambda_o$$

- $\lambda_{o \text{ MIN}} = 1295 \text{ nm}$; $\lambda_{o \text{ MAX}} = 1322 \text{ nm}$; $S_{o \text{ MAX}} = 0,095 \frac{\text{ps}}{\text{nm}^2 \text{ km}}$

• Equivalent to:

