



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
I.C.T.P., P.O. BOX 586, 34100 TRIESTE, ITALY, CABLE: CENTRATOM TRIESTE



H4.SMR/449-10

**WINTER COLLEGE ON
HIGH RESOLUTION SPECTROSCOPY**

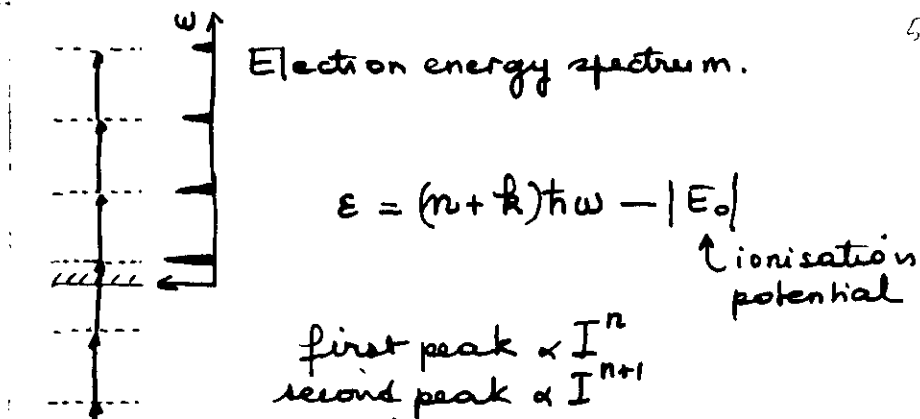
(8 January - 2 February 1990)

MULTIPHOTON IONISATION OF ATOMS

IV Electron Energy Spectrum

M. CRANCE

**Laboratoire Aime Cotton
Centre National
de la Recherche Scientifique
Orsay Cedex 91495
France**



Probability to reach

first peak: $\left[\sum \frac{V_{0\alpha} V_{\alpha i} V_{i\beta} V_{\beta k}}{(\omega - \omega_\alpha)(2\omega - \omega_i)(3\omega - \omega_\beta)} \right]^2$

second peak: $\left[\sum \frac{V_{0\alpha} V_{\alpha i} V_{i\beta} V_{\beta j} V_{j\kappa}}{(\omega - \omega_\alpha)(2\omega - \omega_i)(3\omega - \omega_\beta)(4\omega - \omega_j)} \right]^2$

third peak: $\left[\sum \frac{V_{0\alpha} V_{\alpha i} V_{i\beta} V_{\beta j} V_{j\gamma} V_{\gamma\ell}}{(\omega - \omega_\alpha)(2\omega - \omega_i)(3\omega - \omega_\beta)(4\omega - \omega_j)(5\omega - \omega_\gamma)} \right]^2$

$4\omega - \omega_j$ may vanish
→ replace $\int \frac{1}{4\omega - \omega_j}$ by p.p. $\int \frac{1}{4\omega - \omega_j} + i\delta(4\omega - \omega_j)$

Interpretation

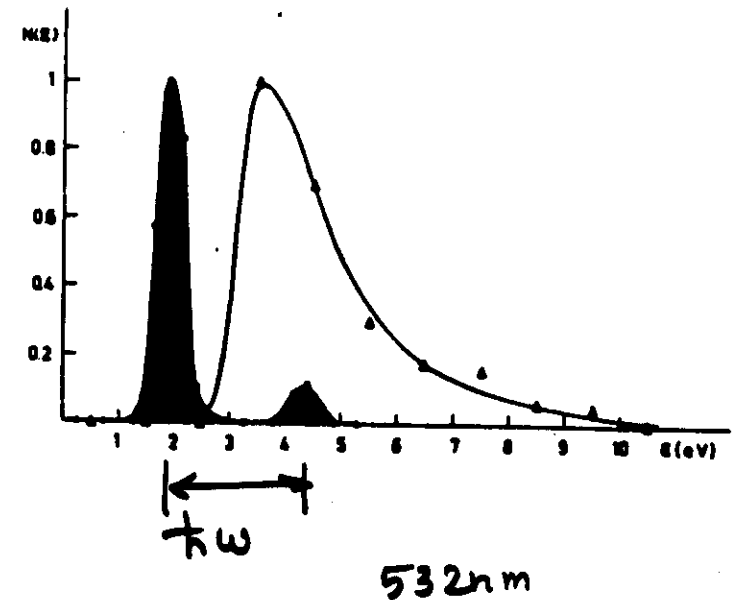
Probability amplitude to absorb 4+1 photons

$$M_{05} + i M_{04} M_{45}$$

M_{05} simultaneous absorption of 5 photons, no resonant step

$M_{04} M_{45}$ simultaneous absorption of 4 photons.

immediately followed by absorption of 1 photon.



P. Agostini F. Fabre G. Mainfray
G. Petite N.K. Rahman
Phys Rev Lett. 42 1127 (79).

Xenon
1.06 μ
Kruit et al 1981

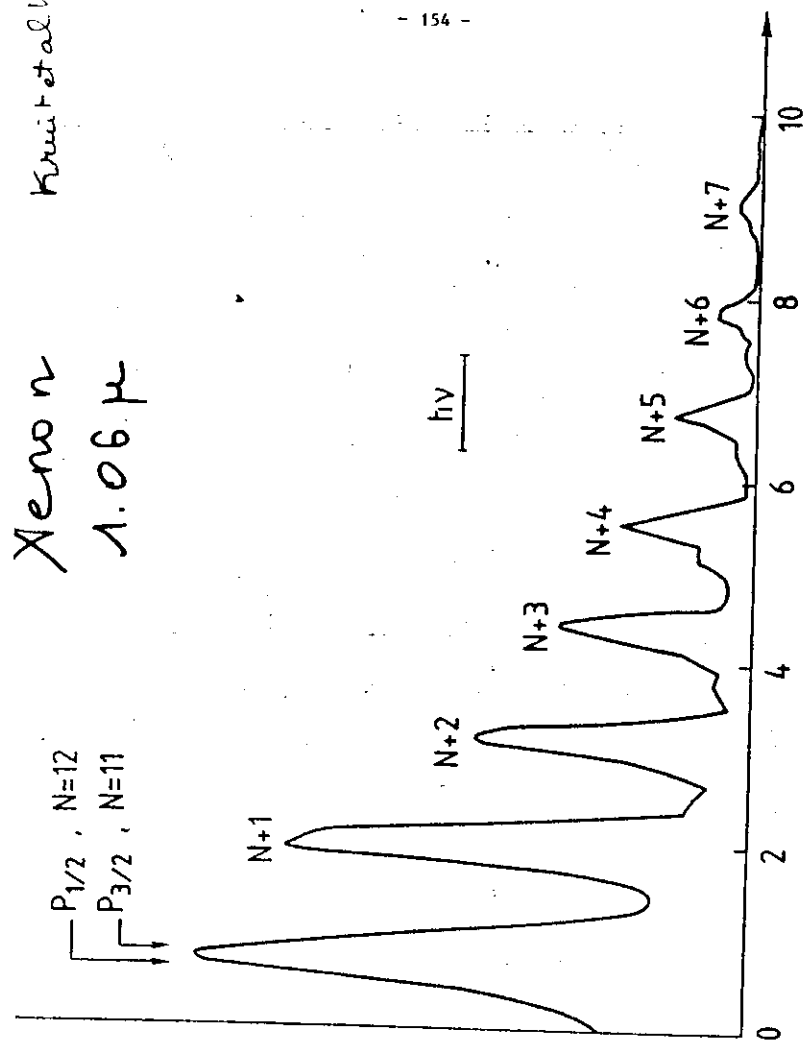


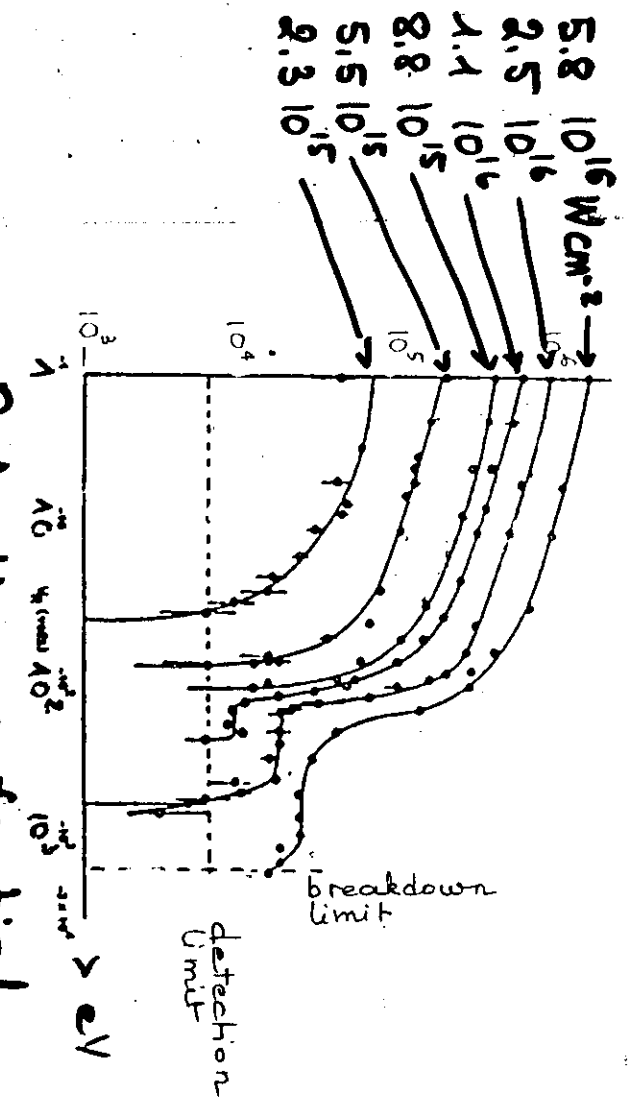
Figure 44 - Spectre énergétique des photoélectrons provenant de l'ionisation du Xénon pour $\lambda = 1,06 \mu\text{m}$. (Kruit et al. / 27 /).

58

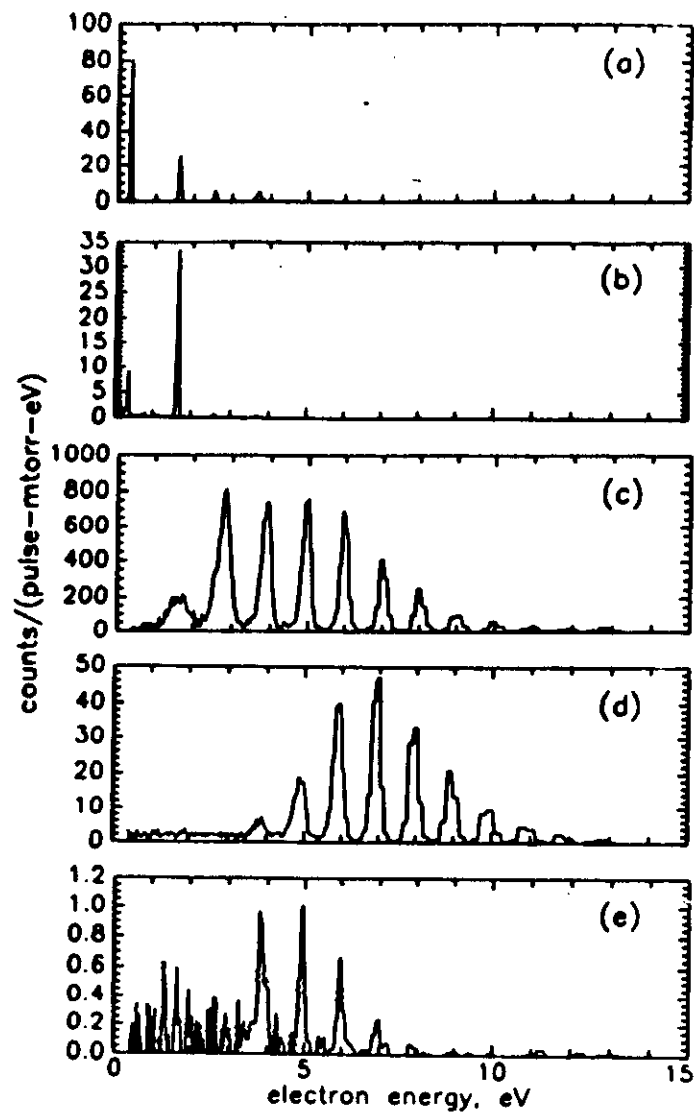
the
1.06 μ

Boreham et al 1981

Retarding potential



59



J. H. Bucksaum, M. Boshkany, R. R. Freeman, T. J. Heilath
 Phys Rev Lett. 56 2590 (86)

60

Angular distribution

Removing an electron of momentum ℓ by absorption of n photons provides an electron of momentum $\ell + n$ for circular polarization

$\ell + n$, or $\ell + n - 2$ or $\ell + n - 4$ for linear polarisation

For each possible momentum in final state

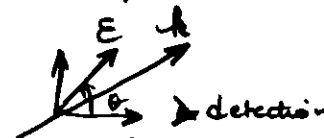
$$M_{0\ell} = \sum_{\text{interm. state}} \langle \ell | V G V G \dots | \ell \rangle$$

$|\ell\rangle$ stands for $R(r) Y_{\ell m}(\theta, \varphi)$ $R(r) \rightarrow \sin(kr + \delta_\ell)$

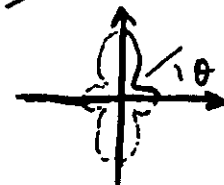
Probability to detect an electron in direction θ, φ .

$$P(\theta, \varphi) = \left| \sum_{\ell} M_{0\ell} Y_{\ell m}(\theta, \varphi) \bar{e}^{i\delta_\ell} \right|^2$$

Linear polarisation



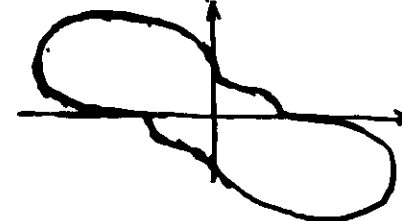
circular polarisation



2 axis of symmetry



elliptic polarisation



conserved in π -rotation

Multiphoton ionisation by 1.06μ in elliptic polarization

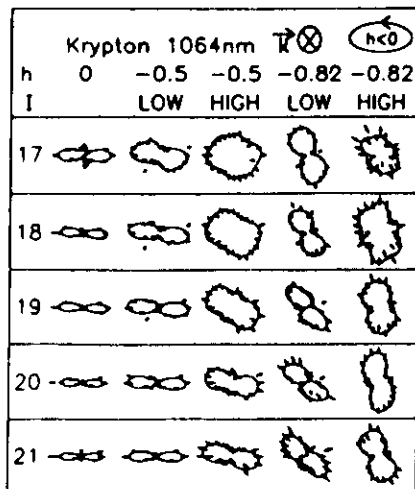


FIG. 4. Azimuthal distributions for various retardations and laser intensities, for krypton photoionized by 1064-nm light. Numbers to the left of each row designate photons absorbed to the $P_{3/2}$ ion final state for each ATI peak. First column: linear polarization, $I_{\text{peak}} = 2.5 \times 10^{11}$ W/cm². Second column: $\delta = -0.5$, $I_{\text{peak}} = 2 \times 10^{11}$ W/cm². Third column: $\delta = -0.5$, $I_{\text{peak}} = 4 \times 10^{11}$ W/cm². Fourth column: $\delta = -0.82$, $I_{\text{peak}} = 2 \times 10^{11}$ W/cm². Fifth column: $\delta = -0.82$, $I_{\text{peak}} = 4 \times 10^{11}$ W/cm².

Multiphoton ionisation of hydrogen
Angular distribution for various
peaks in electron energy spectrum
 0.532μ

0, 355 μ m

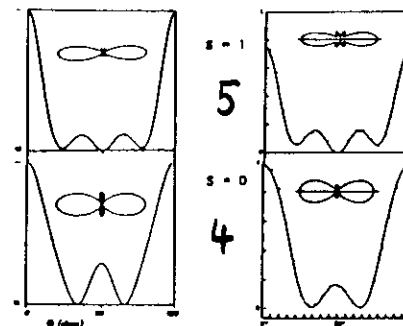


Figure 1. Photoelectron angular distributions at 355 nm. s is the number of photons above threshold. Left column: calculated in this work. Right column: experiment [1,6] normalized to highest signal.

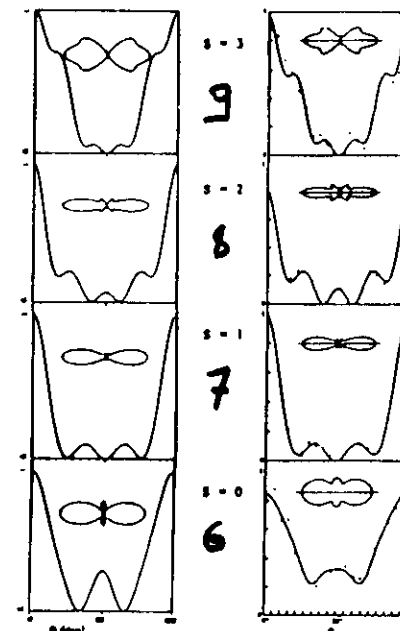


Figure 2. Photoelectron angular distributions at 532 nm (notation as in Figure 1).

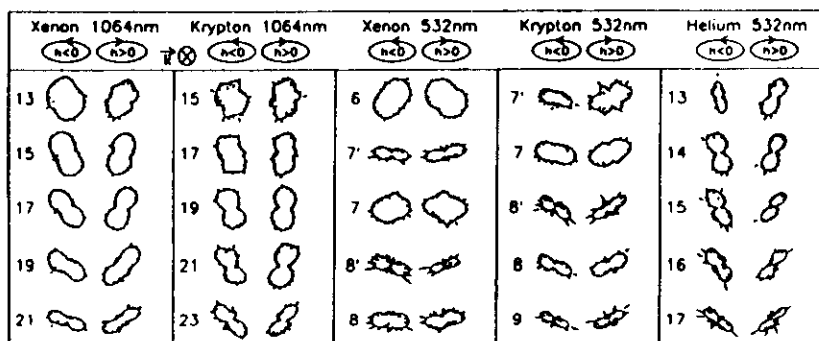


FIG. 3. Comparison between data obtained with positive-helicity light ($\delta = +0.82$), and data obtained under the same conditions with the helicity reversed ($\delta = -0.82$). The laser pulse width was 0.10 to 0.12 nsec. Xe 1064 nm: $I_{\text{peak}} = 4 \times 10^{11}$ W/cm²; $P_{1/2}$ & $P_{3/2}$ final states were not resolved, so numbers indicate photons absorbed for the $P_{3/2}$ final state. Kr 1064 nm: $I_{\text{peak}} = 4 \times 10^{11}$ W/cm²; $P_{3/2}$ final states only. Xe 532 nm: $I_{\text{peak}} = 1 \times 10^{11}$ W/cm²; primed numbers designate photons absorbed to the final $P_{1/2}$ state; primed numbers designate the $P_{3/2}$ state. Kr 532 nm: $I_{\text{peak}} = 1.5 \times 10^{11}$ W/cm²; primes mean the same as for Xe 532 nm. Helium 532 nm: $I_{\text{peak}} = 1 \times 10^{11}$ W/cm².

Bashkansky Bucksbaum Schumacher PRL 60 2458 (88)

exp: Feldmann Wolff Wernhöner Welge Z.f. Phys (1987)
th: Kracke Marxer Broad Briggs Z.f. Physik (1988)

Electron energy spectrum

development in time ∞
 $\dot{n}_0 = -\gamma n_0$ $\gamma = \sum_1^{\infty} P_k$

$$\dot{n}_k = P_k n_0$$

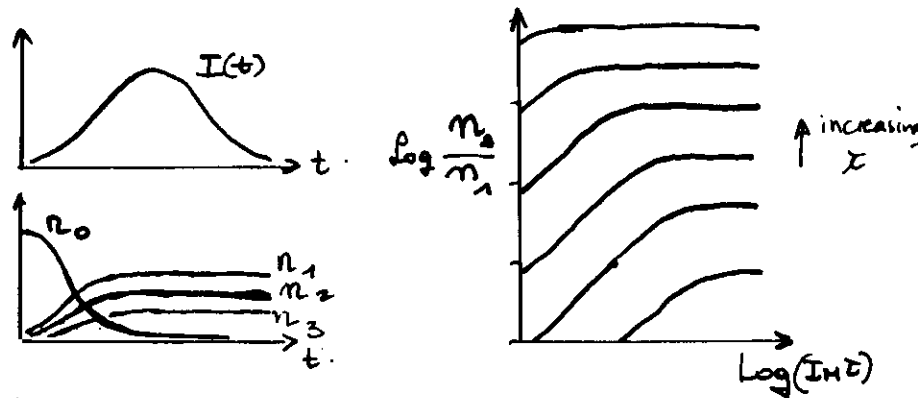
$n_0(t)$ probability to remain neutral at time t
 $n_k(t)$ probability to reach peak k before time t
 P_k probability per unit time to transit to peak k .

number of electrons in peak k $n_k(t \rightarrow \infty)$

$$n_k(t \rightarrow \infty) = \int_{-\infty}^{+\infty} P_k(I(t)) n_0(t) dt$$

low intensity $\rightarrow \propto P_k(I_N)$

saturation intensity and above



Pulse duration determines saturation intensity I_3
 For $I > I_3$ peaks remain in the ratio $n_1(I_3) : n_2(I_3) : n_3(I_3)$
 The only way to increase higher order peaks is to decrease the pulse duration.

4 photon ionisation of Cesium

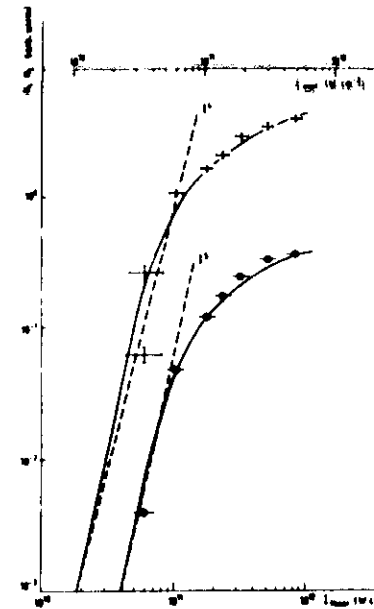


FIG. 11. $N_2(\theta=0)$ and $N_1(\theta=0)$ in arbitrary units as functions of intensity. Crosses and circles are experimental. Solid lines are calculated. Dashed straight lines of slope 4 and 5 are shown for comparison. Note the different experimental (I_{exp}) and theoretical (I_{theor}) intensity scales.

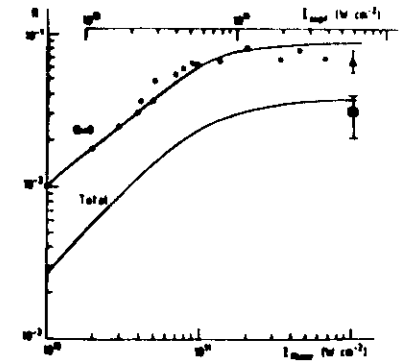


FIG. 12. Ratio N_2/N_1 as a function of intensity. Experimental values (dots) are normalized to the value at $6 \times 10^{11} \text{ W cm}^{-2}$ discussed in the text. Solid lines are theoretical. Note again the different intensity scales. Experimental point on the lower curve gives the experimental determination of the total signal rate resulting from our angular-distribution measurements.

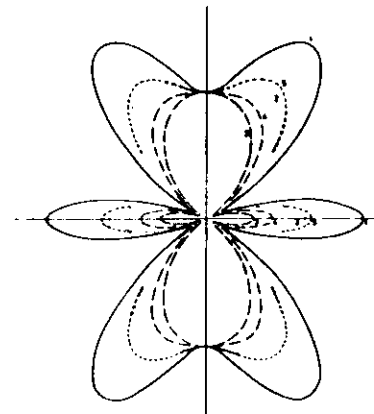


FIG. 2. Angular distributions for the four-photon ionization of cesium for different intensities (in W cm^{-2}): curve 1, 1×10^9 ; curve 2, 10^{10} ; curve 3, 10^{11} ; curve 4, 2×10^{11} ; curve 5, 3×10^{11} .

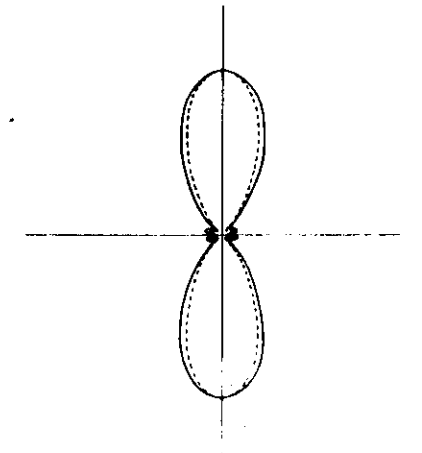
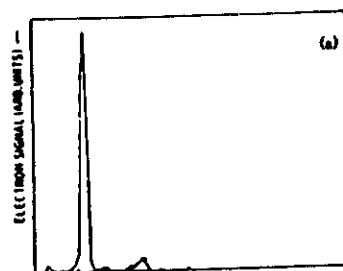


FIG. 3. Angular distributions for the five-photon ionization of cesium for two intensities: 10^9 W cm^{-2} (solid line), $10^{11} \text{ W cm}^{-2}$ (dashed line).

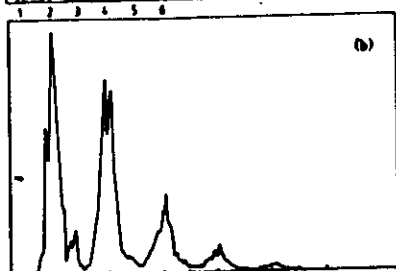
Petite Fabre Agostini Cranu Aymar PR#29 677 (84)

Multiphoton ionisation of Xenon
620 nm 100 fs

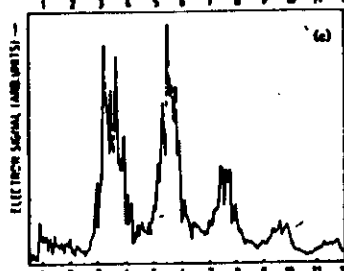
66



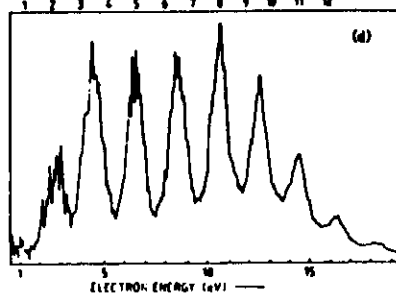
11 μ J



24 μ J



29 μ J



35 μ J

Multiphoton ionisation of Xenon 1.06 μ m

67

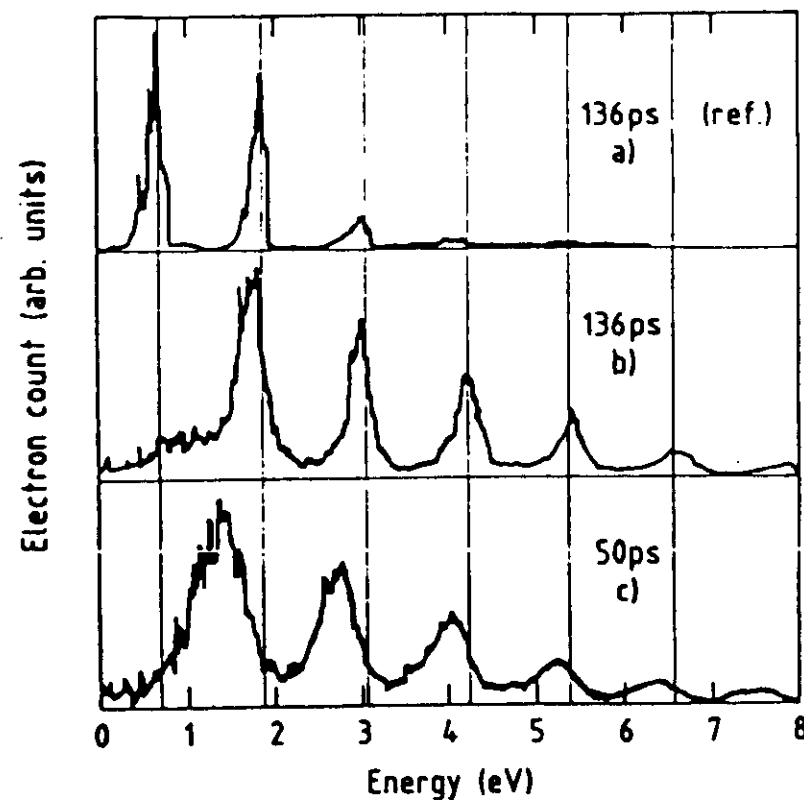


FIG. 2. Electron energy spectra for different laser intensities and pulse durations. (a) reference spectrum, $I = 2.2 \times 10^{12} \text{ W cm}^{-2}$; (b) and (c) $I = 7.5 \times 10^{12} \text{ W cm}^{-2}$.

Agostini, Krukowski, Kompre, Petite, Vergeau
PRA 36 4-111 (87)

Muller, vander Meer, Agostini, Petite, Antonelli, Franco, Rigus
PRL 60 565 (88)

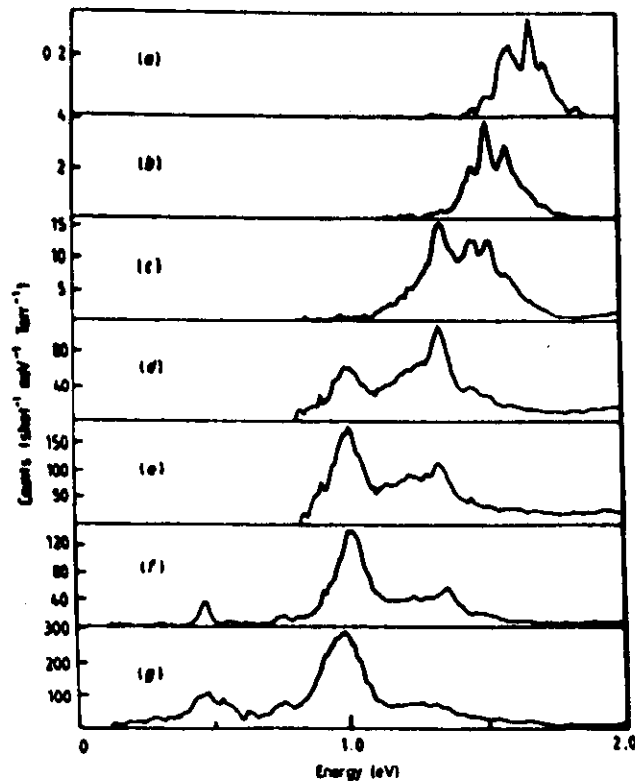
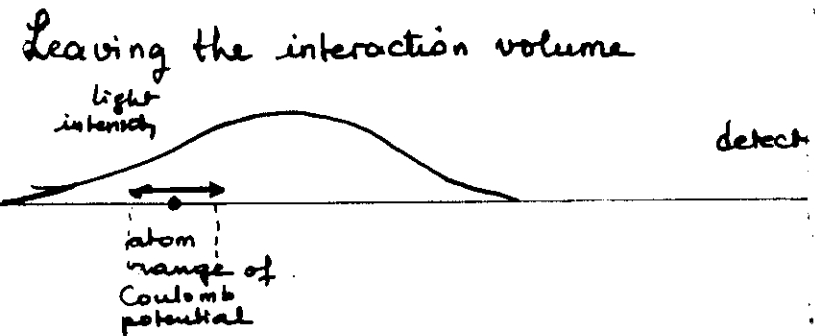


Figure 1. Selected electron energy spectra. The laser intensity increases from $1 \times 10^{13} \text{ W cm}^{-2}$ (a) to $3 \times 10^{13} \text{ W cm}^{-2}$ (g).

Agostini et al JPhys B 22
(1989) 1971



A free electron in a light beam has a quiver motion
 $m\ddot{y} = qE \cos \omega t \quad v = \frac{qE}{m\omega} \sin \omega t \quad \frac{1}{2} m v^2 = \frac{q^2 E^2}{2m\omega^2} \sin^2 \omega t$
 Quiver energy $\frac{q^2 E^2}{4m\omega^2}$

The energy of an electron in a light beam is at least $\frac{q^2 E^2}{4m\omega^2}$
 $\vec{p} = q(\vec{E} + \vec{v} \wedge \vec{B}) \rightarrow \infty$
 Replace ∞ in $\vec{E}$ and $\vec{B} \rightarrow \vec{p} = q(\vec{E} + \vec{v} \wedge \vec{B}) - \frac{q^2}{4m\omega^2} \nabla E^2$
 when $\vec{E}$ is time independent
 $\rightarrow$ potential $\frac{q^2 E^2}{4m\omega^2}$
 gradient force

Right after ionisation $E = \frac{1}{2} m v_T^2 + \frac{q^2 E^2(r)}{4m\omega^2}$

The electron leaves the light beam with velocity v_T
 the quiver energy decreases to zero $\frac{q^2 E^2}{4m\omega^2} \text{ lost}$

The electron gains the work of the gradient force $\frac{q^2 E^2}{4m\omega^2}$

For a 'long pulse'

Electron energy on the detector = energy right after ionisation

LONG PULSE : $\Delta \gg R/v_T$
 duration waist translation velocity

(conversely for a short pulse, the quiver energy is!)

Electron energy on the detector =
 energy right after ionisation - quiver energy

Short strong pulse

Quiver energy can be interpreted as a "threshold shift"
A.C. Stark shift.

From perturbation theory at lowest order:

Ground state is a little shifted down δI

High Rydberg states are shifted as the threshold ΔI

An electron is emitted at time t , point $\vec{r} \rightarrow I(\vec{r}, t)$

Energy conservation

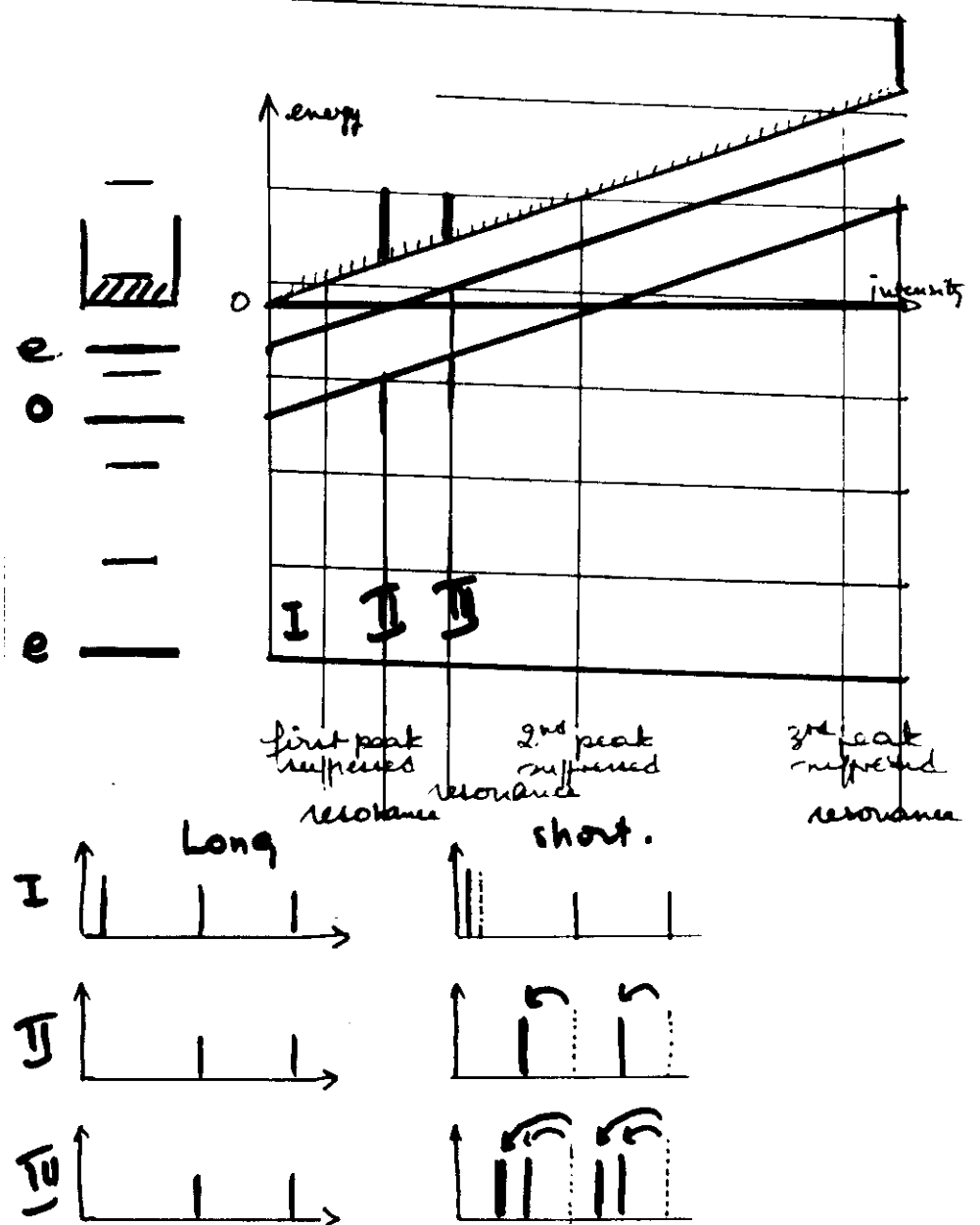
$$E_0 + \delta I + m\hbar\omega = \Delta I + E_T \quad E_T = \frac{1}{2}mv_T^2$$

$\rightarrow E_T$ is a function of $I(\vec{r}, t)$

The electron energy spectrum reflects the ionisation probability as a function of intensity.

$\rightarrow$ sub peaks indicate transient resonances.

Strong short pulse



Interpretation of transient resonances

$$E_g + \delta I + 6\hbar\omega = \Delta_q I + E = E_v + \Delta_r I + \hbar\omega$$

$$E = \frac{6\Delta_r - 5\Delta_q - \delta}{\Delta_r - \delta} \hbar\omega + \frac{E_r(\Delta_q - \delta) + E_g(\Delta_r - \Delta_q)}{\Delta_r - \delta}$$

Assign resonances by varying $\hbar\omega$

OK for large $n\ell$

A puzzle remains: missing peaks - extra peaks

Light shift in Hydrogen.

Complex dilatation method with a finite basis of complex functions.

Eigenstates: low energy : H-states.
high energy : wave packets of continuum + highly excited states.

→ interpretation

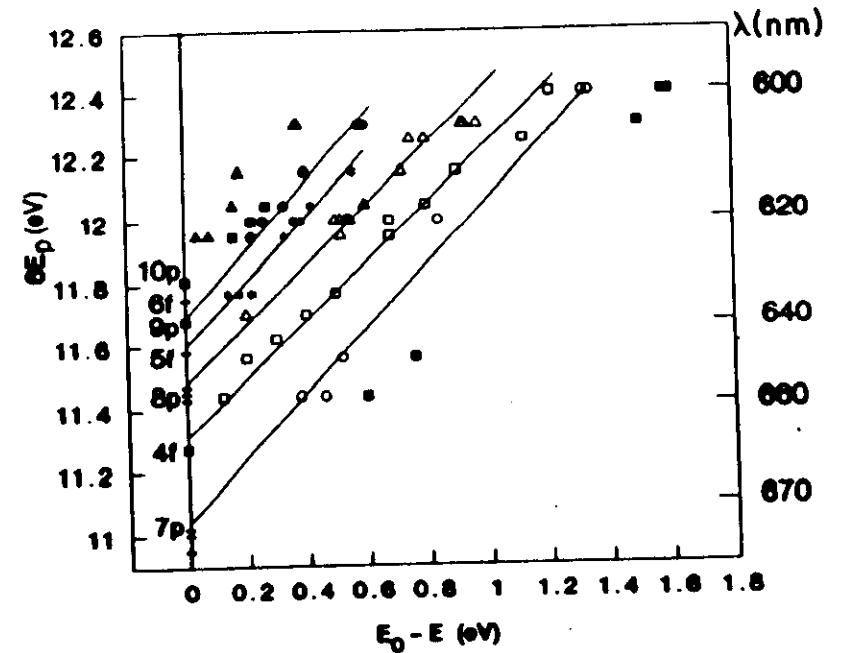
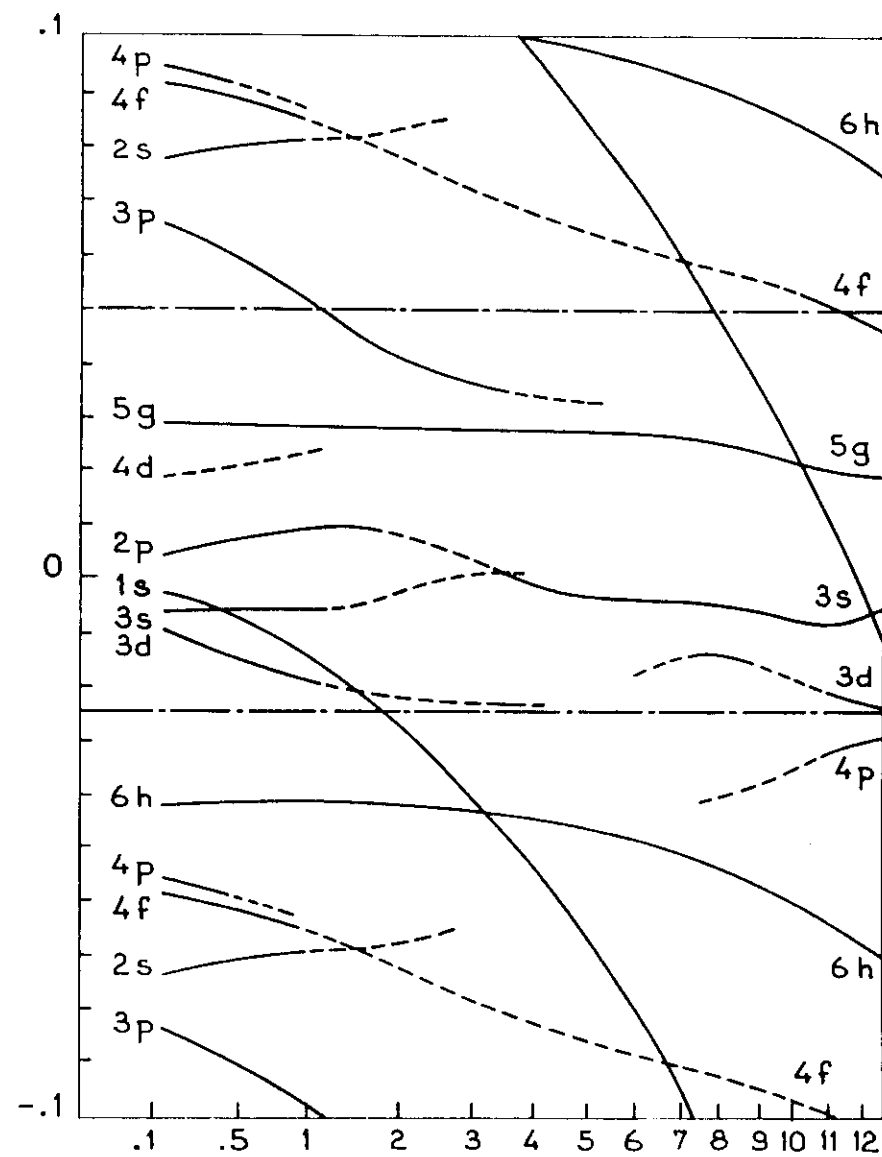
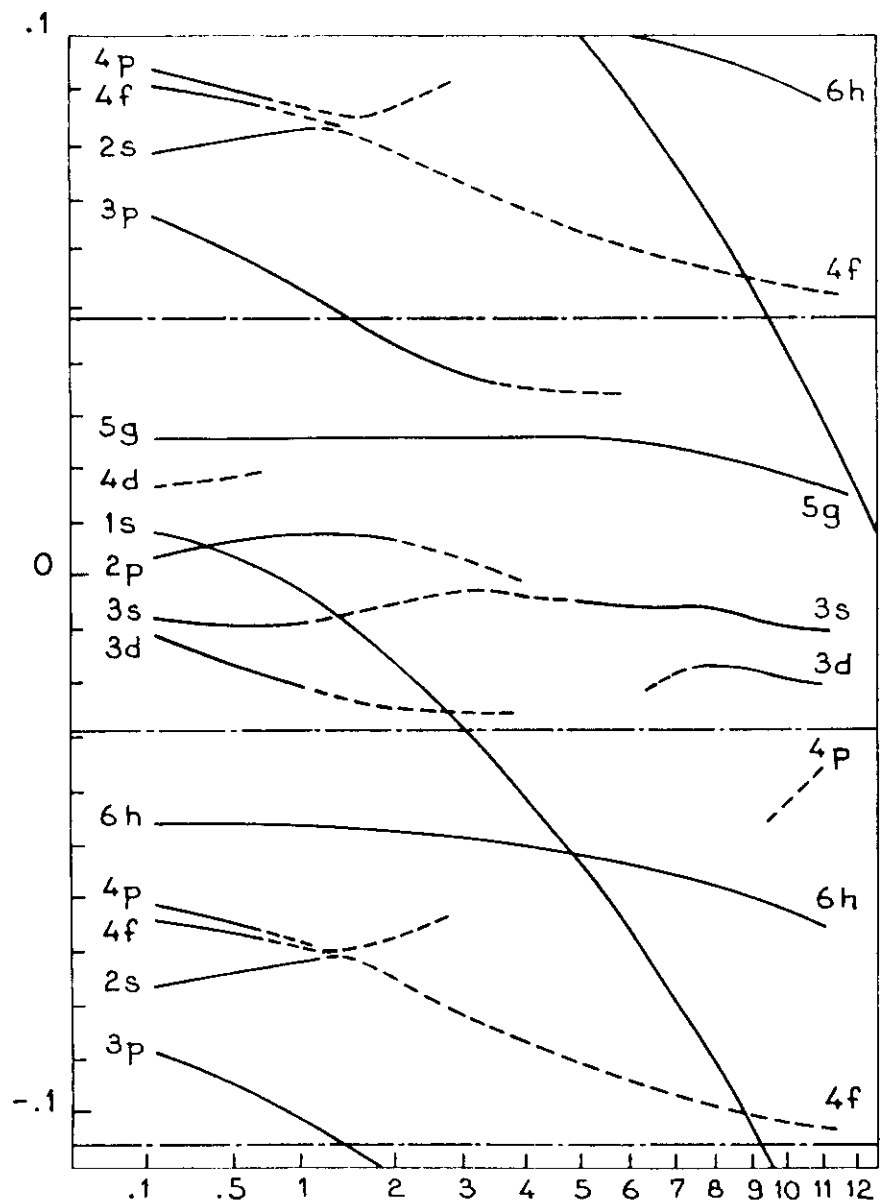


FIG. 2. Plot of $6E_p$ as a function of $E_0 - E$. For clarity, only a few lines have been drawn as guides to the eye. The filled squares below the line corresponding to the $7p$ state may be assigned to the $6p$ but do not extrapolate to the zero-field position of this state.

P. Agostini P. Breger A. L'Huillier H. G. Muller G. Petite
PRL 63 2208 (89)



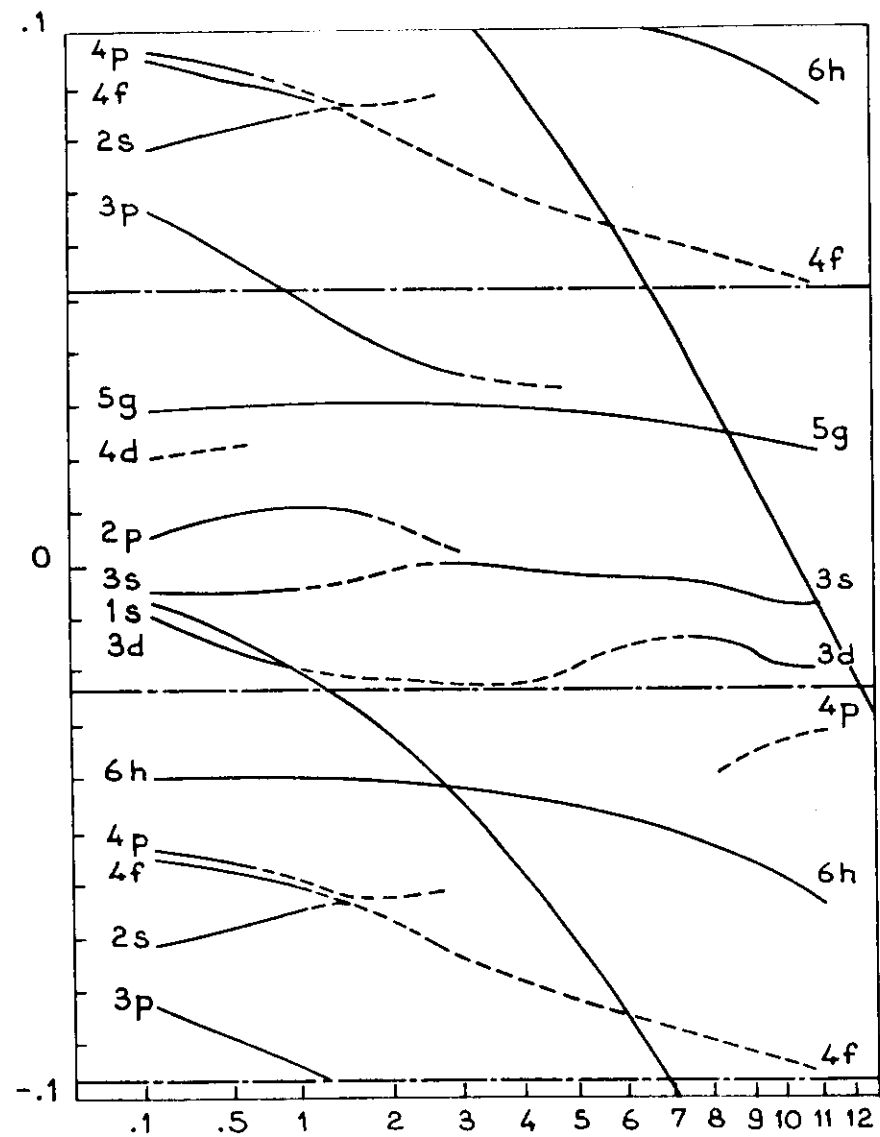


Fig. 1c