



INTERNATIONAL ATOMIC ENERGY AGENCY  
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
**INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS**  
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UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



**INTERNATIONAL CENTRE FOR SCIENCE AND HIGH TECHNOLOGY**

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SMR/481 - 2

**EXPERIMENTAL WORKSHOP ON  
HIGH TEMPERATURE SUPERCONDUCTORS AND RELATED MATERIALS  
(ADVANCED ACTIVITIES)**

(26 November - 14 December 1990)

"Investigation of Electron-Phonon Coupling in High-T<sub>c</sub> Oxides"

presented by:

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**INVESTIGATION OF ELECTRON-PHONON COUPLING IN  
HIGH-T<sub>c</sub> OXIDES**

D. Mihailović  
ICTP Advanced workshop, Dec. 1990

Typical energy scales for the relevant interactions in high-T<sub>c</sub> materials are given by:

$$E_F \sim 0.1 \text{ eV} \text{ (from photoemission)}$$

$$\hbar\omega_{\text{phonon}} \sim 0.06 \text{ eV (500 cm}^{-1}\text{)}$$

$$J_{\text{exchange}} \sim 0.1 \text{ eV (in insulator precursor materials)}$$

The magnetic and electron-phonon interactions are of the same order of magnitude and therefore we cannot easily ignore either one (although the size of  $J$  in the doped case is not clear).

An equivalent statement is:

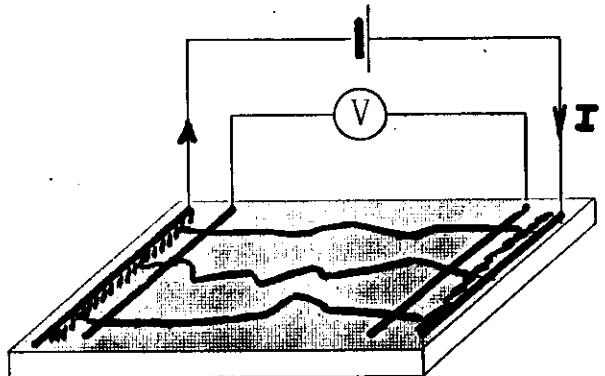
$$v_F \sim v_s$$

where  $v_s$  is the velocity of sound, and  $v_F$  is the Fermi velocity. A carrier will thus carry with it a polarization cloud: normally this is called a polaron.

The main subject of this presentation is an investigation of electron-phonon coupling. We show a number of electron-phonon coupling-induced lattice effects (anharmonicity, polar structure) and suggest that a polaron model of superconductivity which includes apex O anharmonicities should be investigated further. The presence of a polar structure casts some doubt on the interpretation of circular birefringence measurements being evidence of anyon or flux-phase superconductivity.

# INTERACTION BETWEEN SUPERCONDUCTING CURRENT & THE LATTICE:

$\text{YBa}_2\text{Cu}_3\text{O}_7$ , THIN FILM



THE TWO ARE UNDENIABLY COUPLED !!

$I = 45 \text{ mA}$  at  $4.2 \text{ K}$  (for 166h)

Prokhorov et al, JETP Lett. 51, 149 (1990)

Changes in morphology of the superconducting film under the influence of a supercurrent strongly suggests the lattice is coupled to it!

Evidence for structural instability grows available very early. Reflection from single crystals or ceramic shows that the distance is taken from the surface ( $c = 0.16 \mu\text{m}$ ) over at just  $6 \text{ K}$ . Note hysteresis.

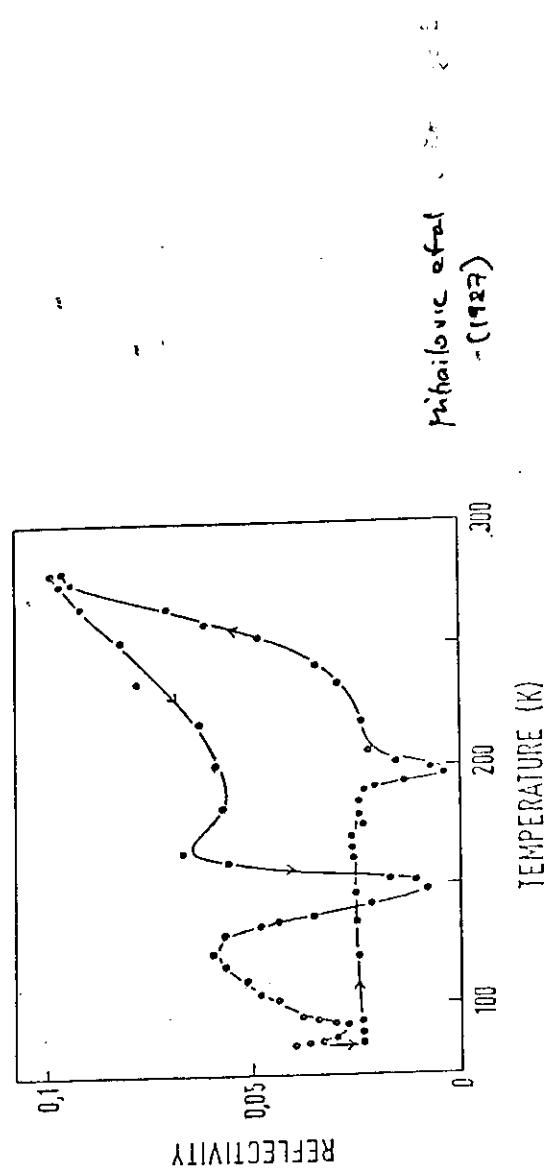


Figure 1 White light TE polarization reflectivity as a function of temperature. Data were taken in a single temperature cycle.

an anomaly in the lattice constants occurs above  $T_c$  in X-ray diffraction

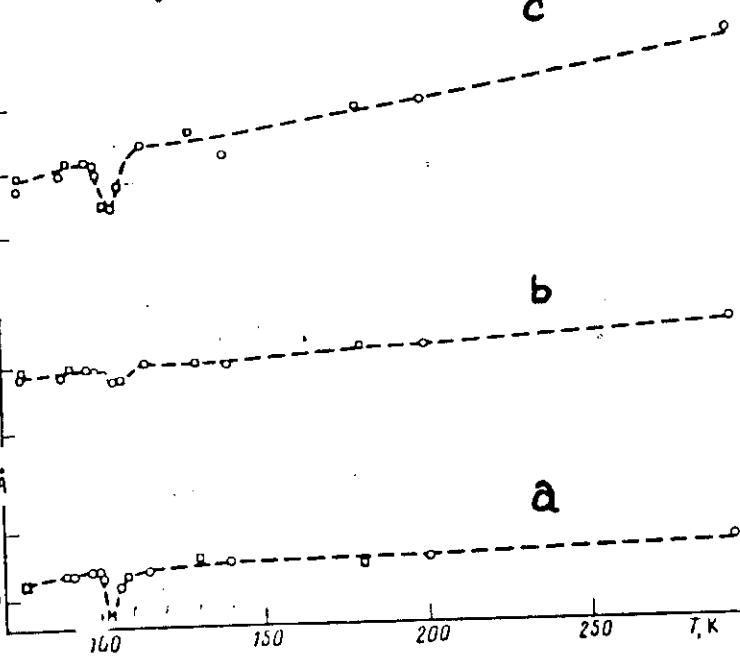
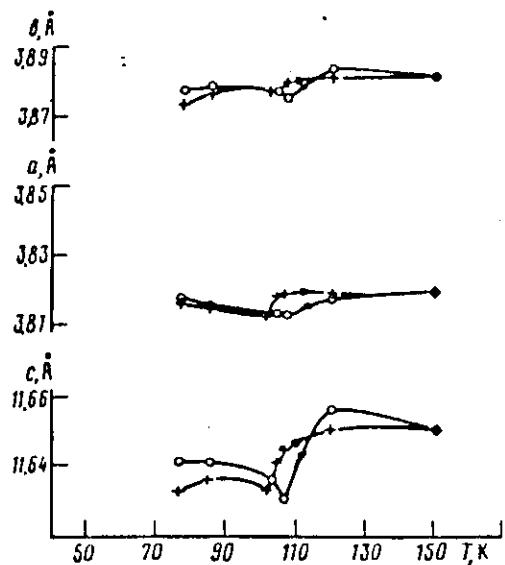


FIG. 1. Temperature dependences of the orthorhombic lattice constants  $a$ ,  $b$ , and  $c$  of the ceramic  $\text{YBa}_2\text{Cu}_3\text{O}_7$ .

Golovashkin et al.

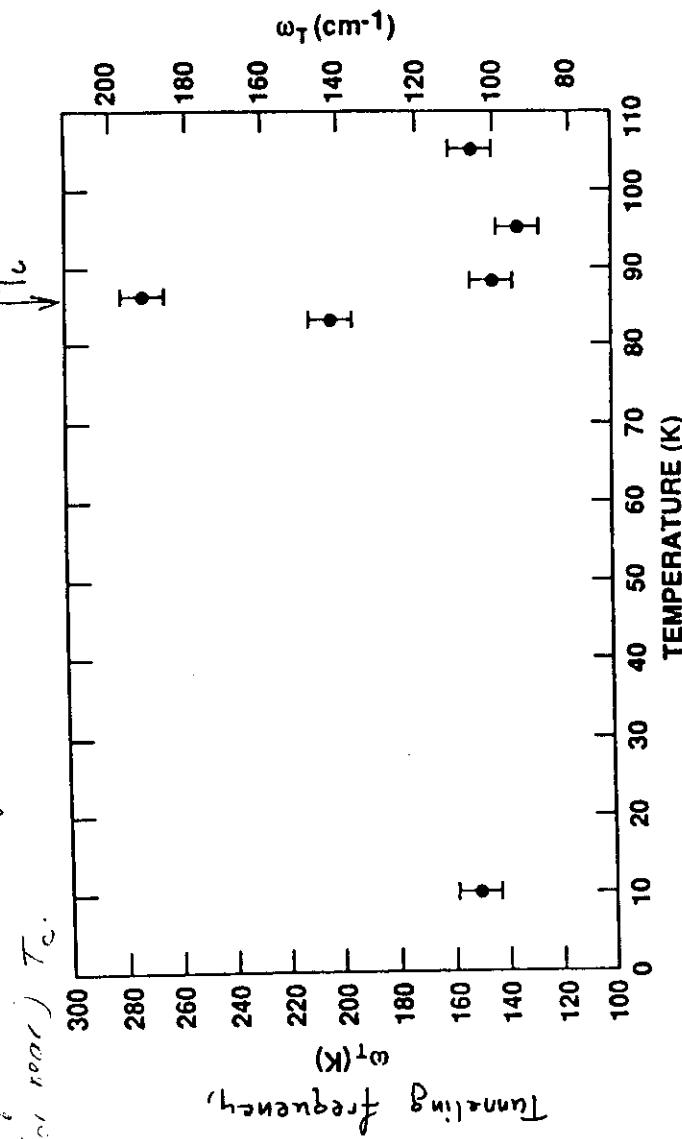
ETP Lett., Vol. 46, No. 8, 25 October 1987

The anomaly shows hysteretic behavior, indicating the involvement of effects.



J.M.6

Graph of  $T$ -dep. of XANES data shows an anomaly during a series changes in tunnelling frequency of spin O atom at (or near)  $T_c$ .



Tunnelling frequency

This interpretation supports a double-well potential for the spin O.

J. Mustre de Leon et al  
PRL (1990)

60

# The Pyroelectric Effect in $\text{YBa}_2\text{Cu}_3\text{O}_7$

(Measurements by  
S. C. Miller)

## 1. Primary pyroelectricity at constant volume

$$\left(\frac{\partial D}{\partial T}\right)_V = \left(\frac{\partial D}{\partial T}\right)_E$$

## 2. Secondary pyroelectricity arises due to strains arising from $\Delta T$ .

$$\left(\frac{\partial D}{\partial T}\right)_\sigma = \left(\frac{\partial D}{\partial \epsilon}\right) \left(\frac{\partial \epsilon}{\partial T}\right)_\sigma$$

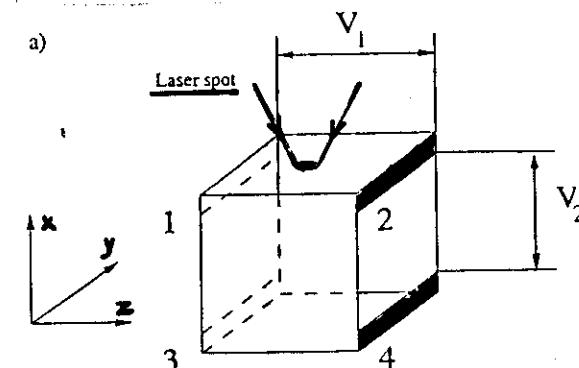
where  
 $\sigma$  = STRESS  
 $\epsilon$  = STRAIN

## 3. Tertiary pyroelectricity arises due to strains arising from non-uniform $\Delta T$ . (an artifact)

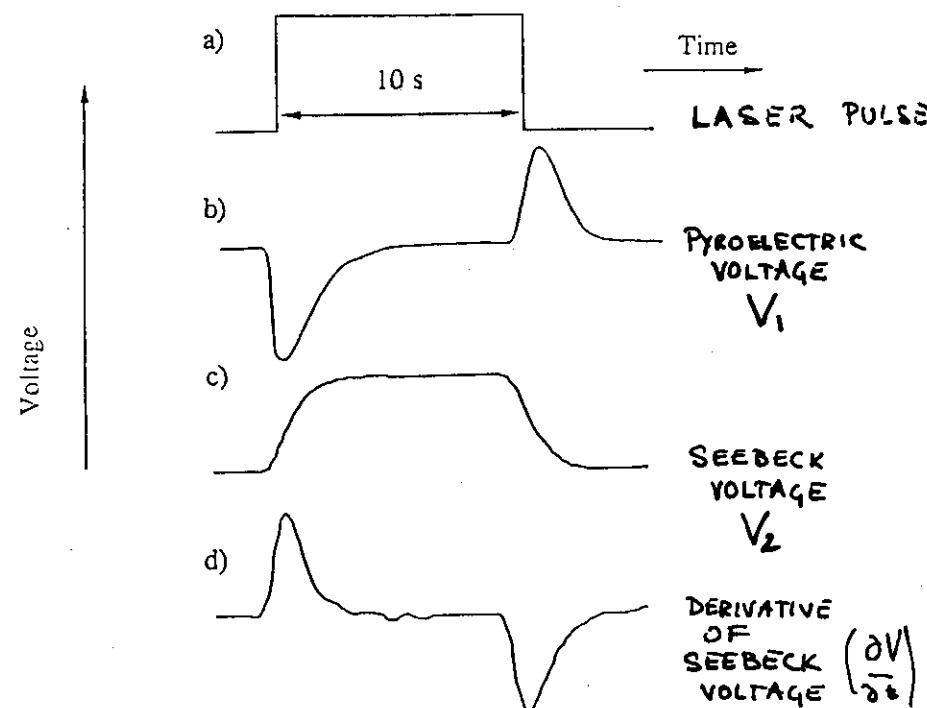
The appearance of pyroelectricity implies the existence of MACROSCOPIC POLAR regions (and NO CENTRE OF INVERSION).

Observation of PE is further evidence for a role of  $\mu$ -e-p interaction in cuprates.

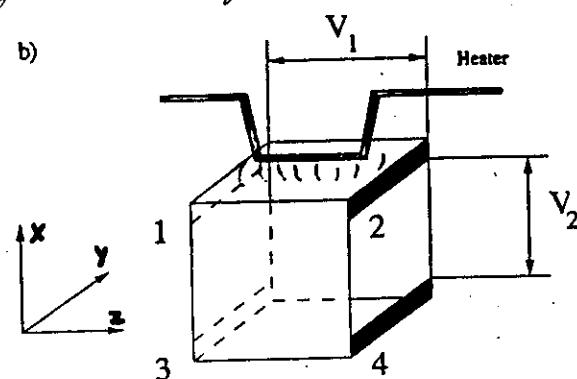
Geometric parameters



$\text{YBa}_2\text{Cu}_3\text{O}_7$  SINGLE CRYSTAL,  $\sim 1\text{mm}^3$ , source: COLLIN



Possible photovoltaic effects are eliminated by replacing the heating source:



Given that the measured  $p = (0, p)$

From Nye, only possible groups with

$$(0, 0, p)$$

are:

tetragonal: 4 ( $C_4$ ), 4mm ( $C_{4v}$ )

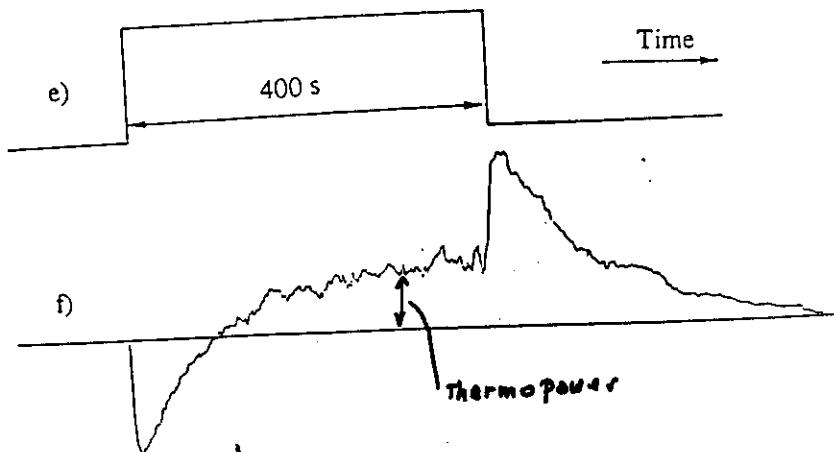
for  $\gamma\text{Ba}_2\text{Cu}_3\text{O}_7$ : orthorhombic: mm2 ( $C_{2v}$ )

(+monoclinic m ( $C_s$ ) & 1 ( $C_1$ ) group)

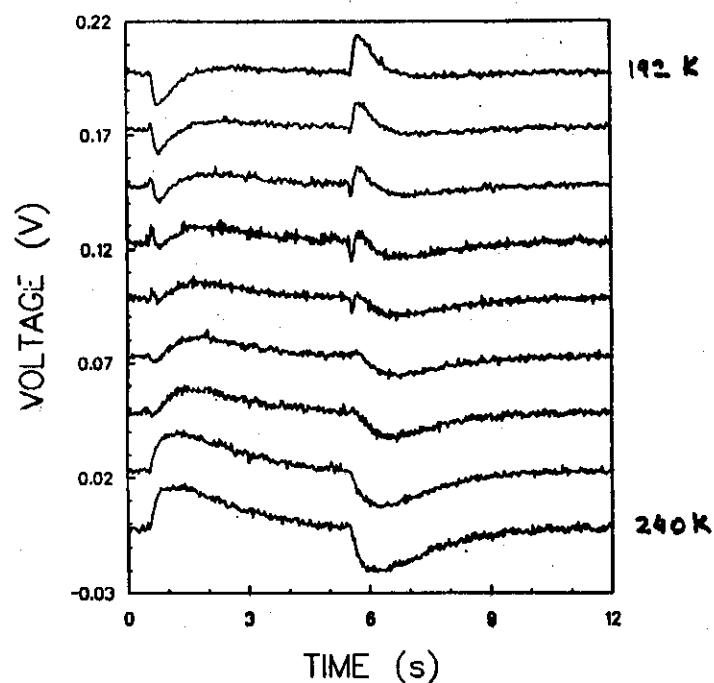
Incidentally,

The unambiguous appearance of polar structure casts doubt on recent experiments of optical circular birefringence upon reflection from the material surface as evidence for anyon or flux-phase superconductivity. Circular birefringence naturally arises in a polar structure!

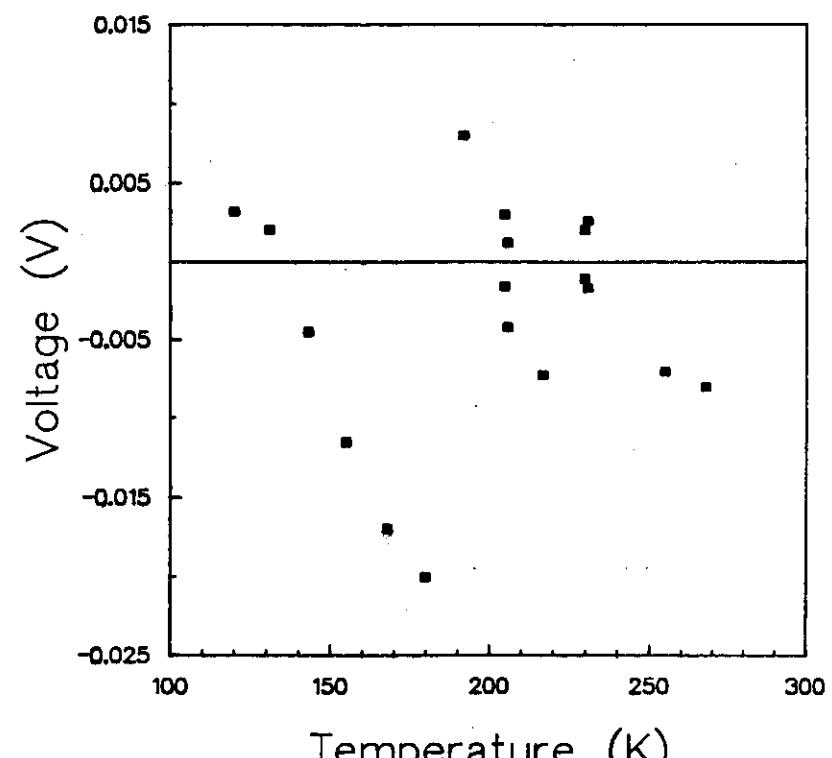
D. Hikairi: Sol. Stat. Comm. 76, 319 (1990)



POLARIZATION REVERSAL  
WITH TEMPERATURE IN  $\text{YBa}_2\text{Cu}_3\text{O}_{6.9}$   
SINGLE CRYSTAL



VARIATION OF PYROELECTRIC  
VOLTAGE WITH TEMPERATURE

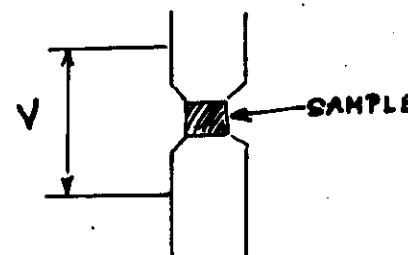
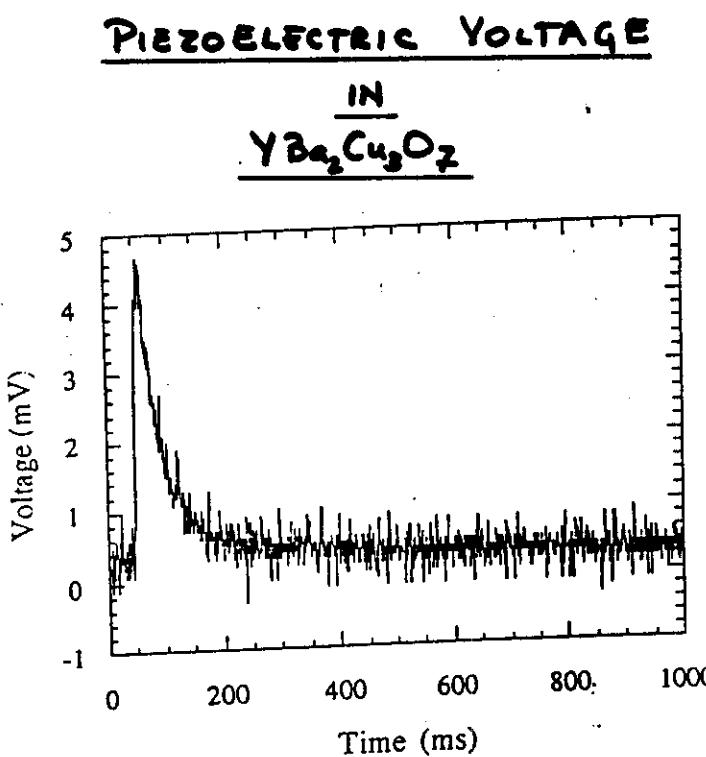


PE voltage shows polarization reversal which  
is a sign of shifting domains with temperature

Similar evidence is seen in ultrasonic measurements

ORTS

38



Confirms polar structural regions in material.

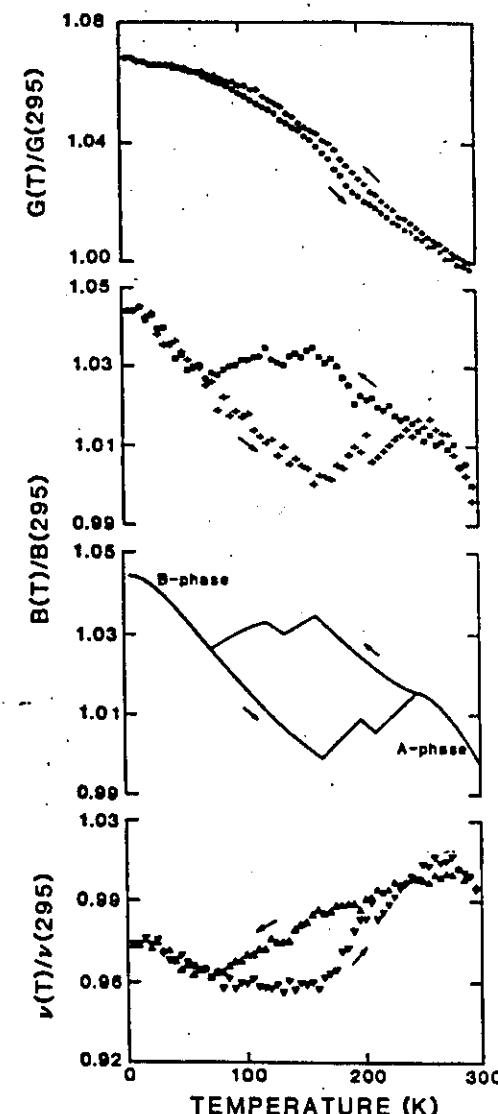


FIG. 2. For  $\text{Y}_1\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}$ , temperature variation of  $G$ =shear modulus,  $B$ =bulk modulus, and  $v$ =Poisson ratio.

## Raman Scattering in High-T<sub>C</sub> materials

### Summary of information that can be gained:

#### 1) Phonons:

- anomalies related to possible electron - phonon mechanisms can be seen at T<sub>C</sub> in the phonon spectra.
- show the effect of doping on (electronic) structure.

#### 2) Raman Scattering from Impurities and Defects

#### 3) Resonant Raman Scattering

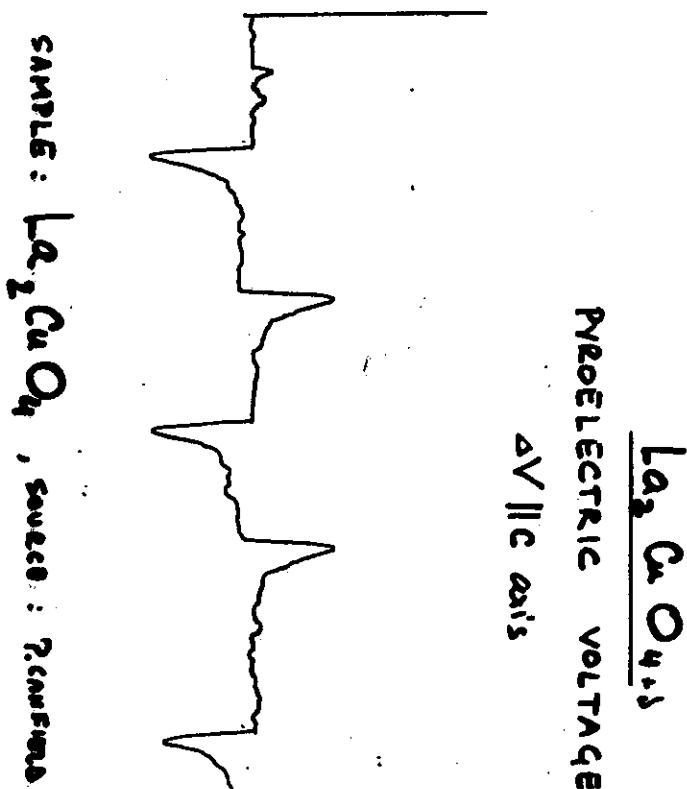
- resonance condition gives information about symmetry and structure (energy) of electronic states (bands)

#### 4) Electronic Raman Scattering

- gives low energy part of the excitation spectrum !

#### 5) Magnetic Raman Scattering

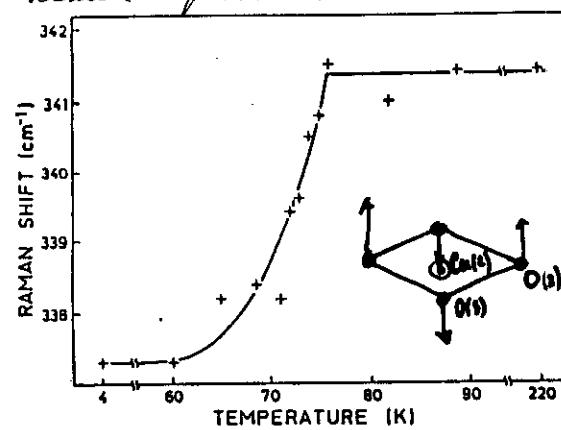
- two magnon spectra (together with neutron scattering) are the best evidence for the existence of spin-waves in high-T<sub>C</sub> cuprates



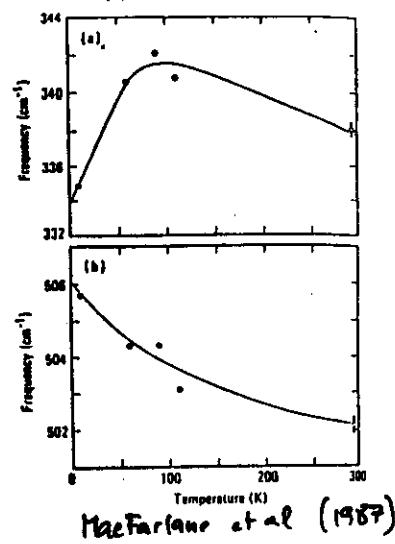
SAMPLE:  $\text{La}_2\text{CuO}_4$ , source: P. J. Custers, LBNL #1062.

The effect is also observed in  $\text{La}_2\text{CuO}_4$ , single crystals, and is not limited to  $\text{YBa}_2\text{Cu}_3\text{O}_7$ .

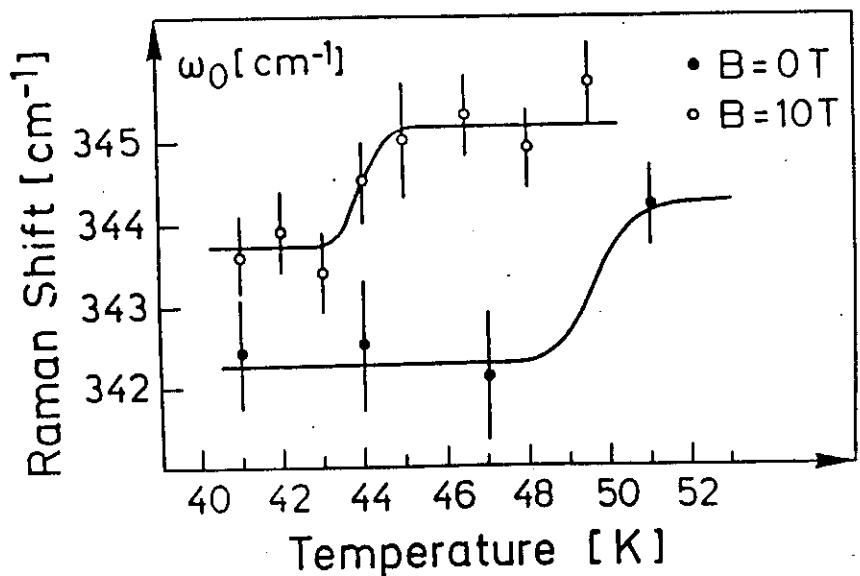
Phonon anomalies at  $T_c$  are well known from Raman spectra:



Thomsen et al (1988)



MacFarlane et al (1987)



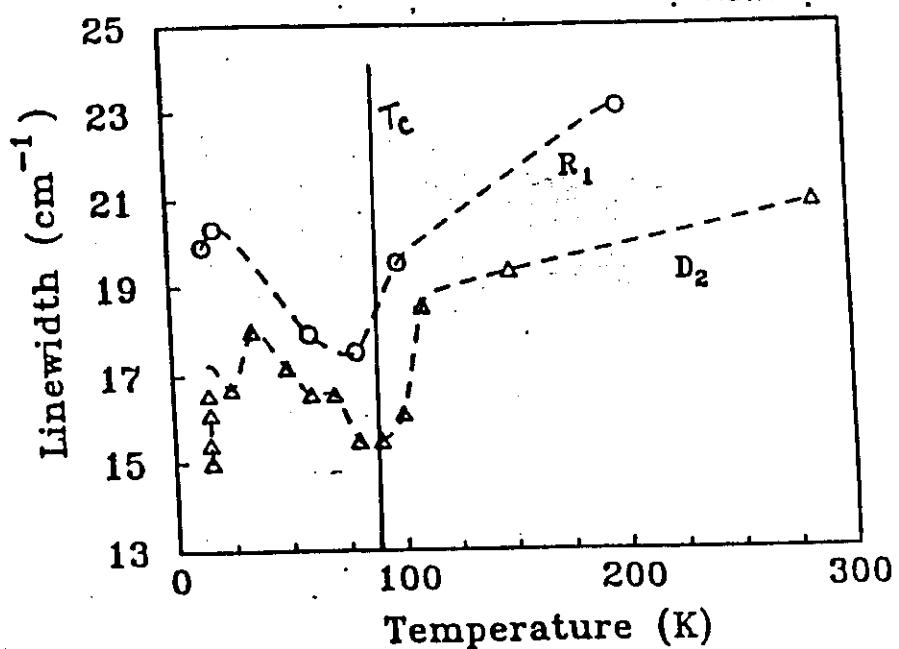
Ref et al (1988)

Phonon anomaly of  $340 \text{ cm}^{-1}$  mode in Raman

but an anomaly of the apex O, whose frequency lies well above  $2\omega = 56 \text{ Tc}$  has been observed only very recently:

### Apex ANOMALY OF O(4) VIBRATION

LINewidth  $\Delta T_c$   $T_c$



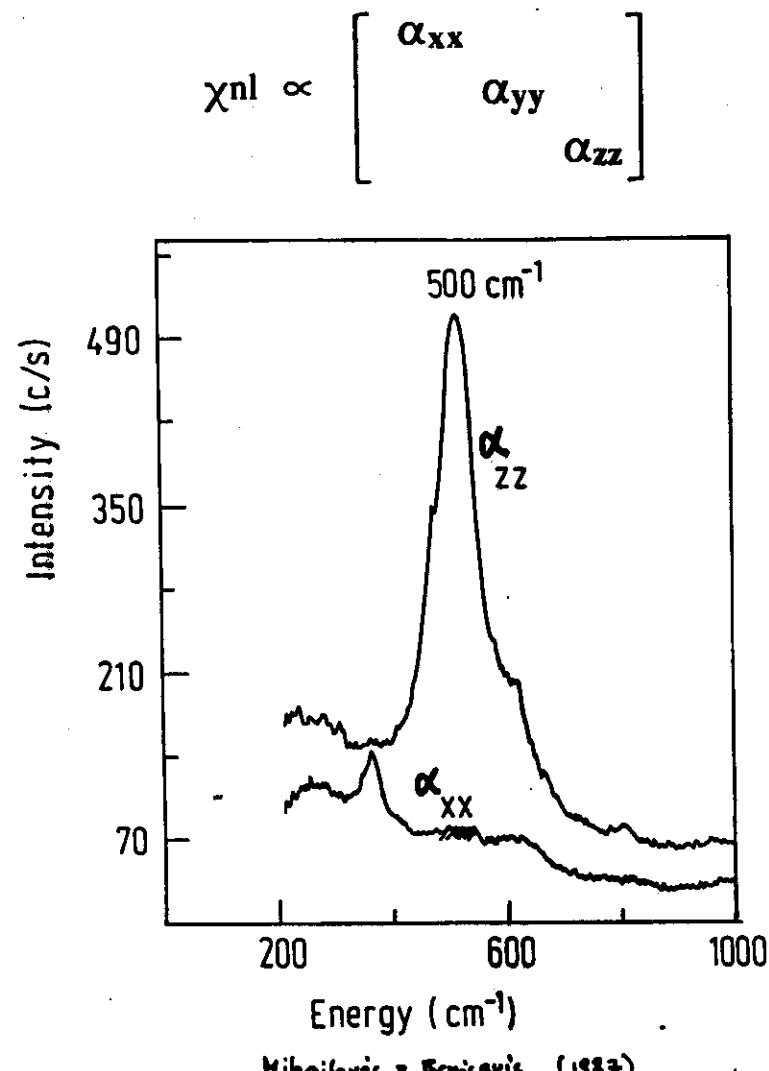
Altendorf et al, ssc 76, 591 (1990)

It is precisely this mode (one involving O(4)) which may lead to the polar symmetry in  $\text{YBa}_2\text{Cu}_3\text{O}_7$ .

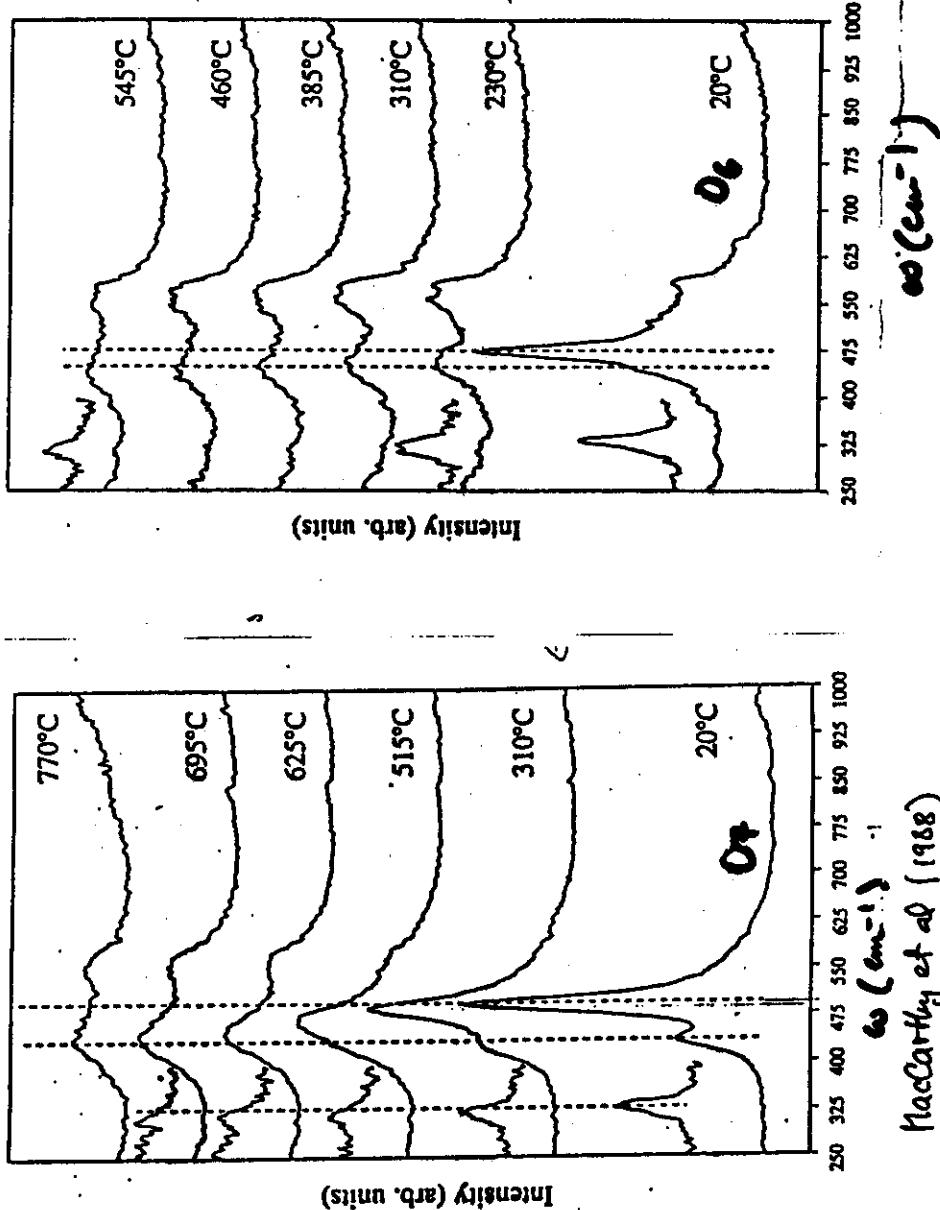
The reason for looking at Raman spectra:

$$\text{Raman intensity} \propto \chi^{\text{nl}}$$

For apex O vibration,

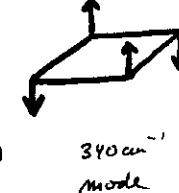
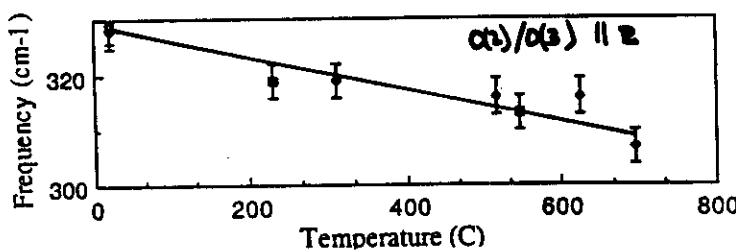
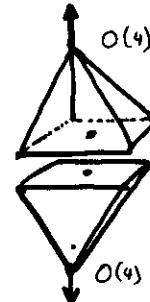
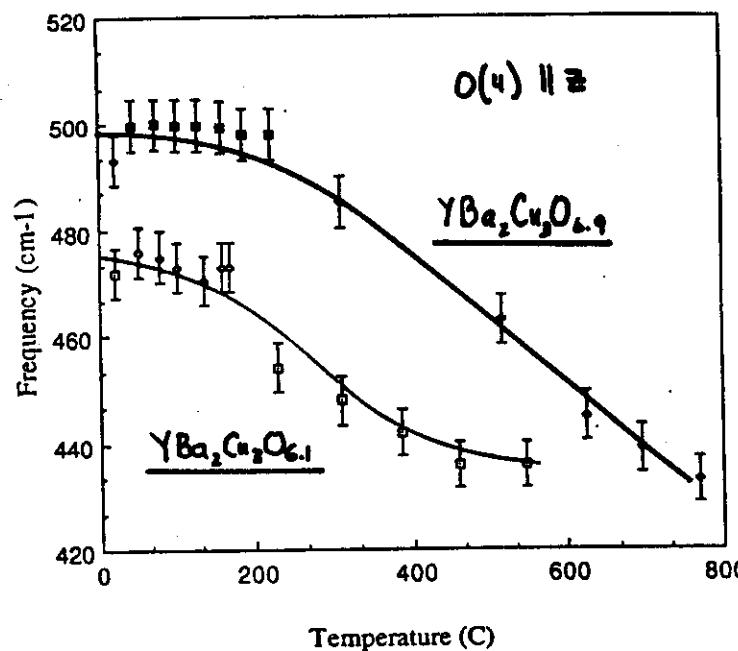


$\chi_{\text{re}}$  is also a quantity that can be related  
to intermolecular mechanisms.

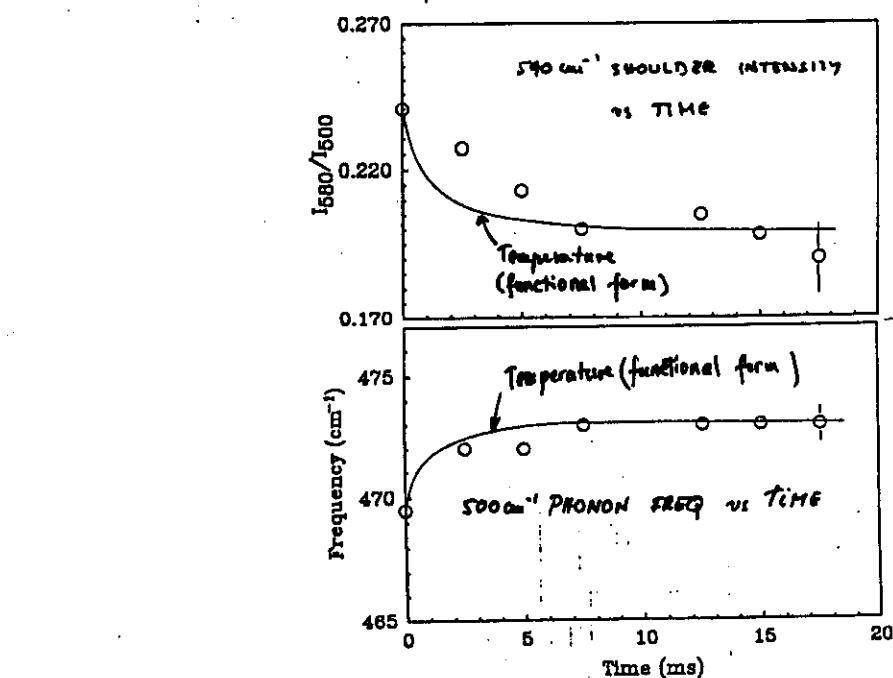
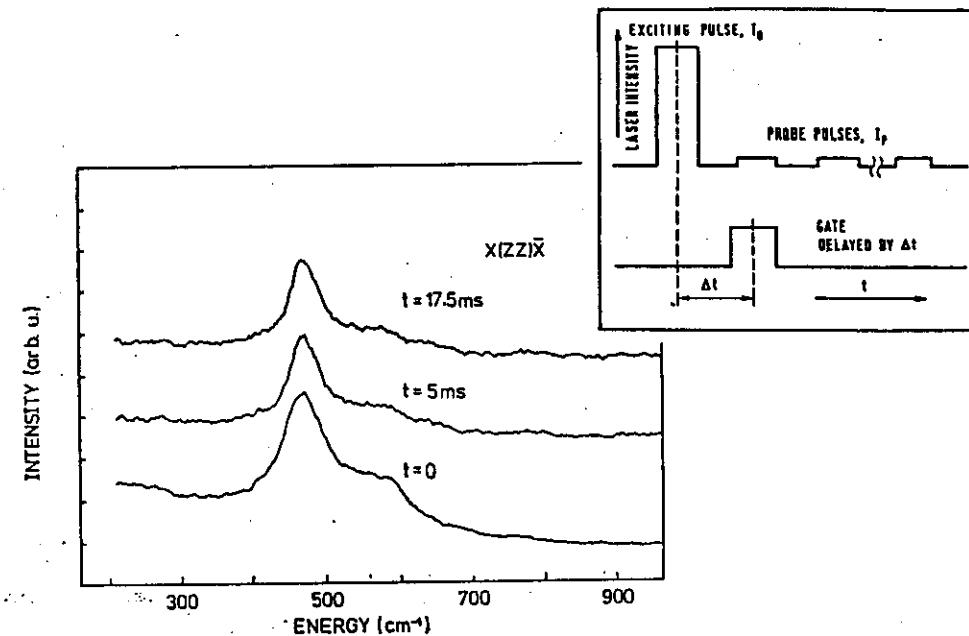


High-temperature phonon softening. Note the peak D<sub>r</sub>.

High temperature data on aged O mode shows signs of severe anharmonicity or hopping of O!

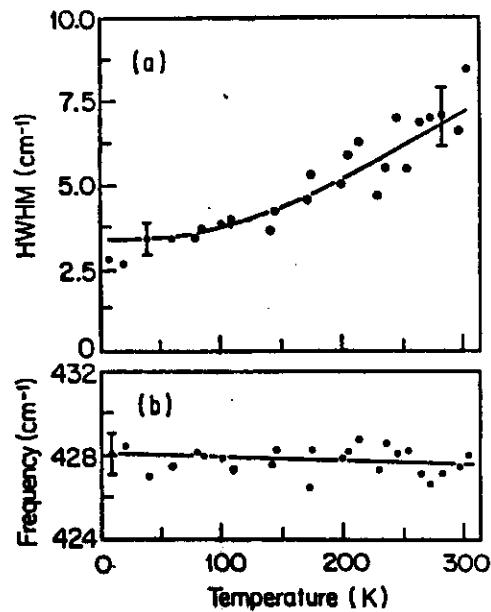
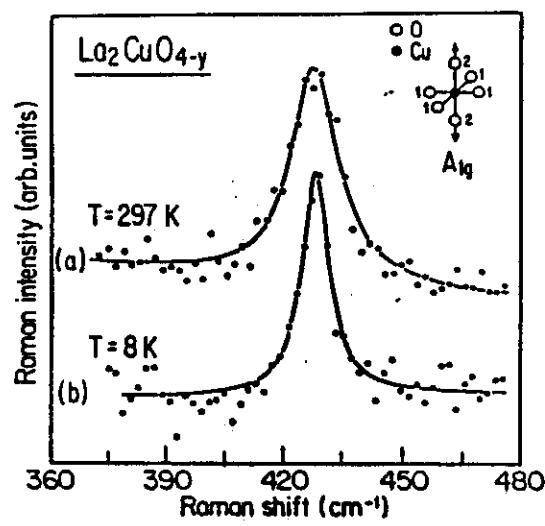


D. Mihailović et al., *Phys. Rev. B* (1990)  
FIGURE 1



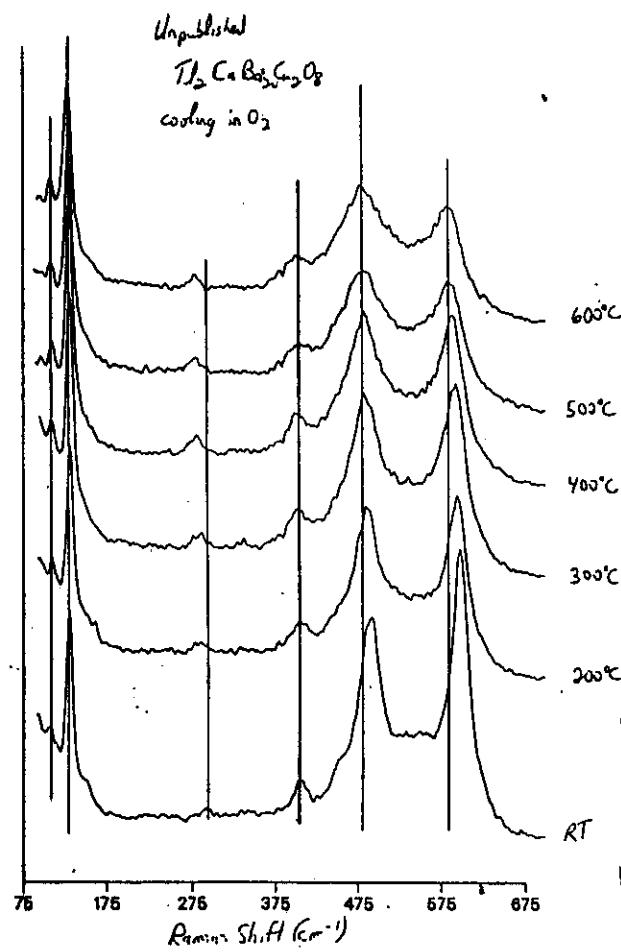
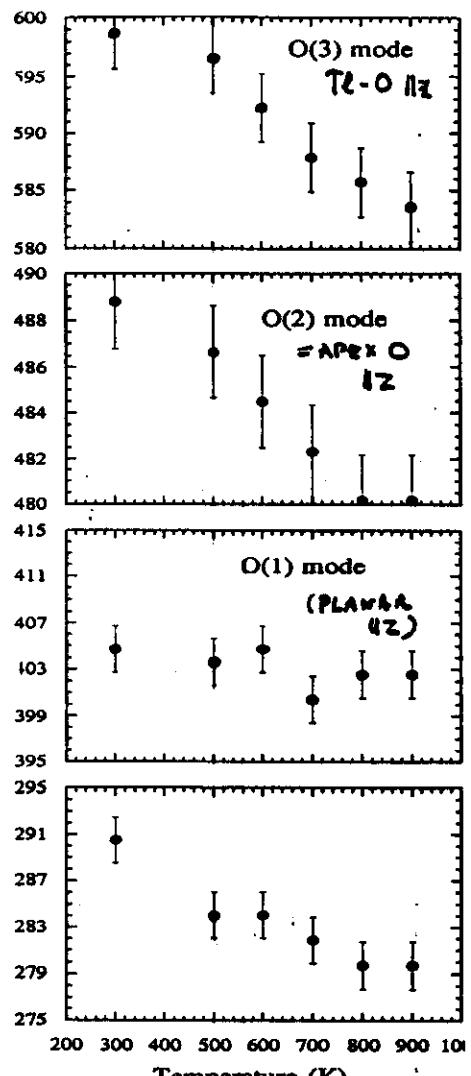
I. Poleraj et al (1990) *Phys. Rev. B*

It is conceivable and



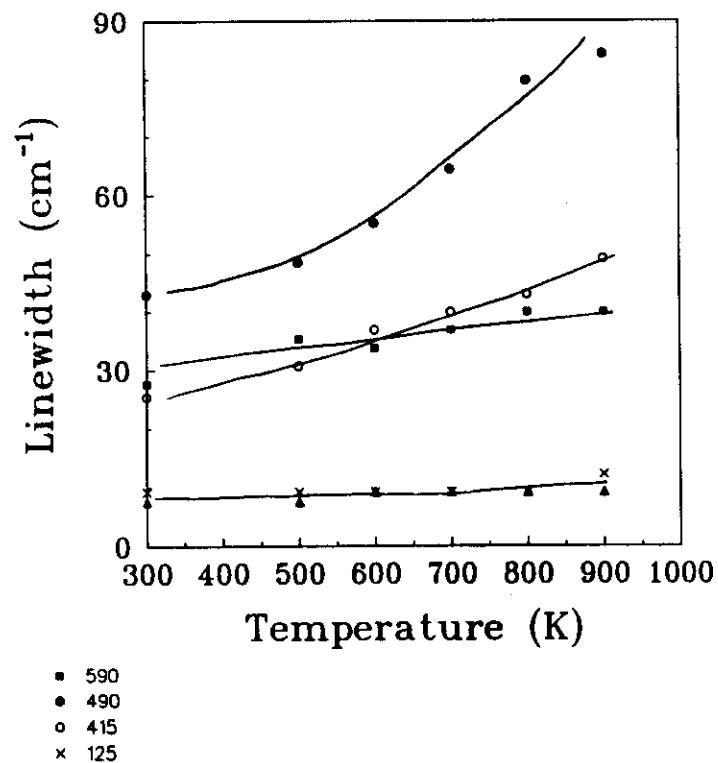
O'Hanrahan et al (1989)

Anharmonic apex O vibration is also seen  
in  $\text{La}_2\text{CuO}_{4-y}$

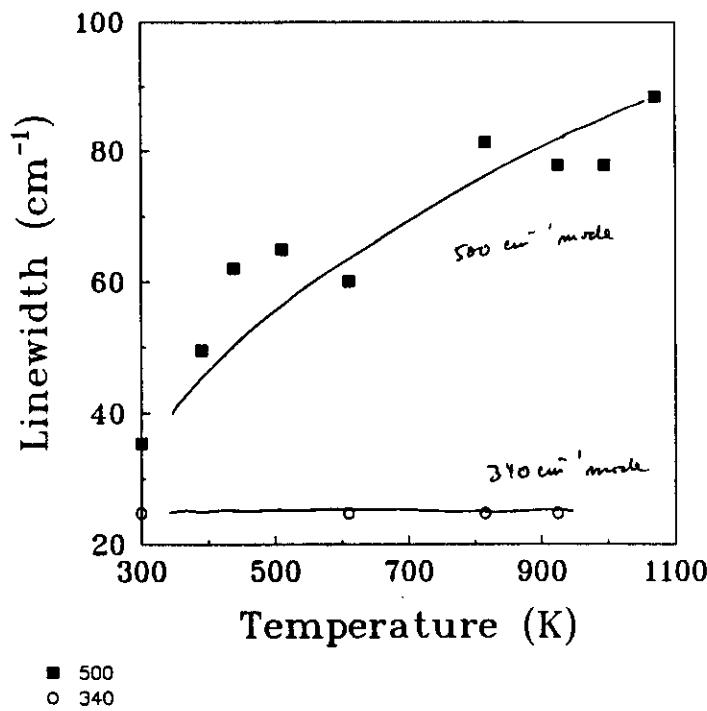


K. McCarty (unpublished)

as well as in  $\text{Tl}_2\text{CaBa}_2\text{Cu}_3\text{O}_{8-x}$ ,

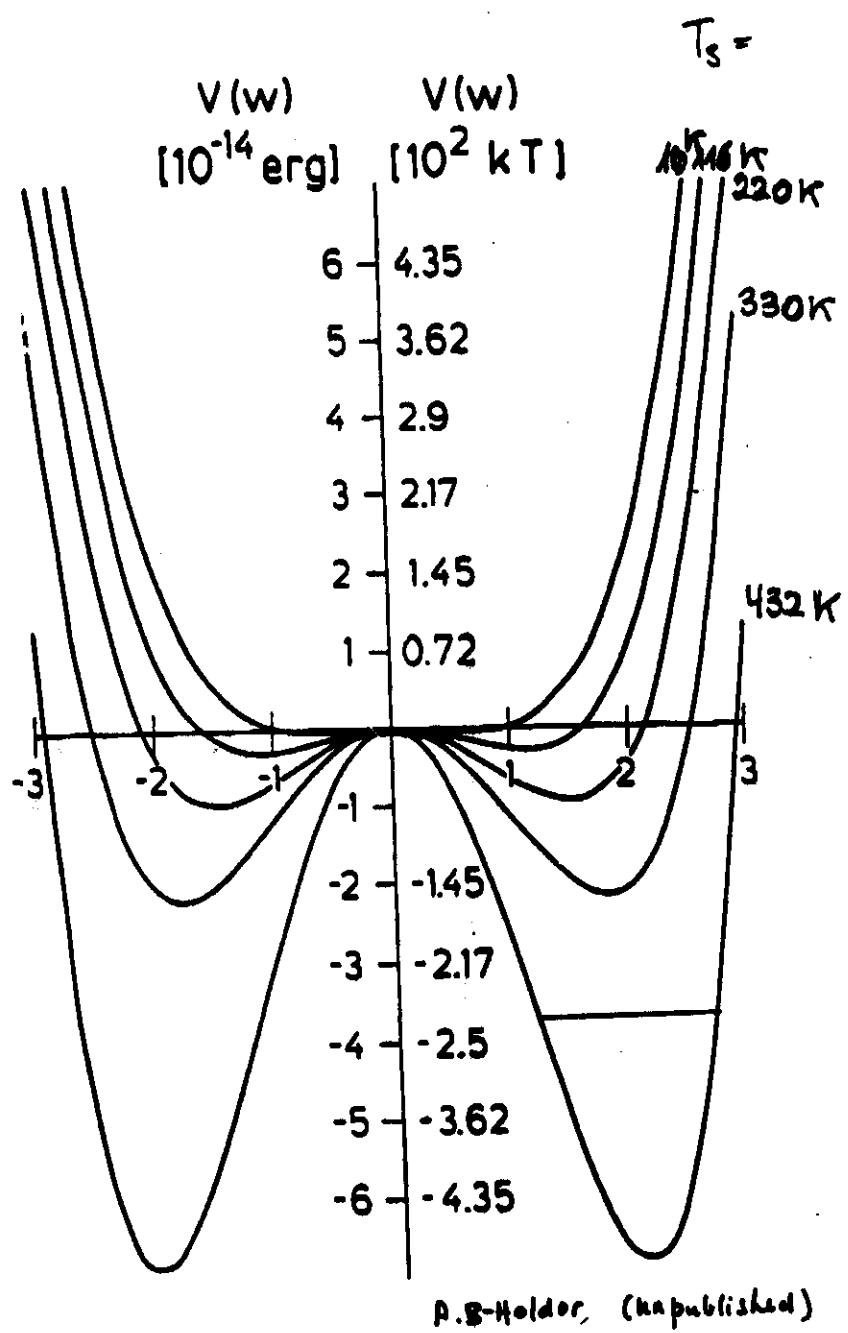
$Tl_2Ba_2CaCu_2O_{8-\delta}$ 

## YB7LWDTH Data

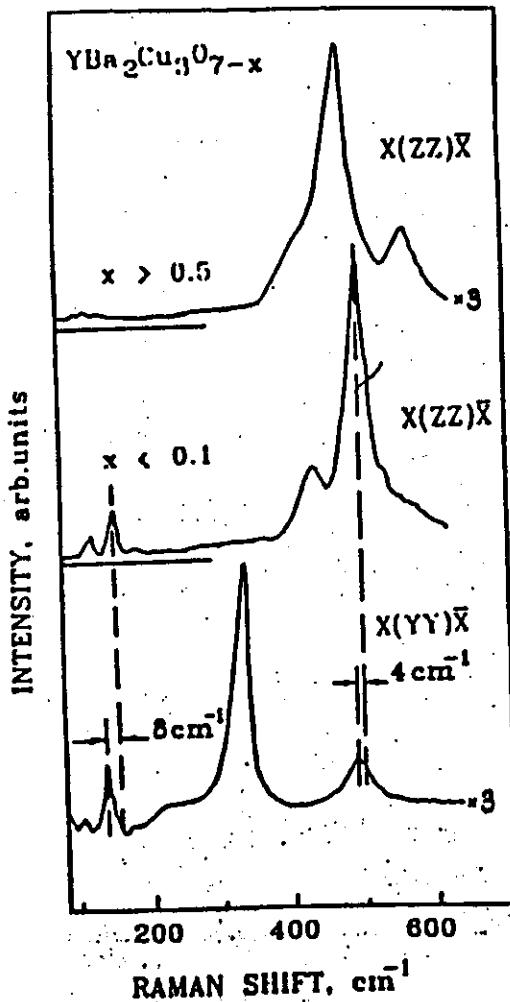


Linewidth of  $\sigma$  modes is strongly  
T-dependent, but ONLY for apex  
oxygen and  $Tl-O$  plane vibrations.

Width of apex  $O$  vibration vs  $T$ .  
Note the  $340\text{ cm}^{-1}$  mode shows no broadening.



A model potential for the apex O vibration  
 following the XANES & Raman



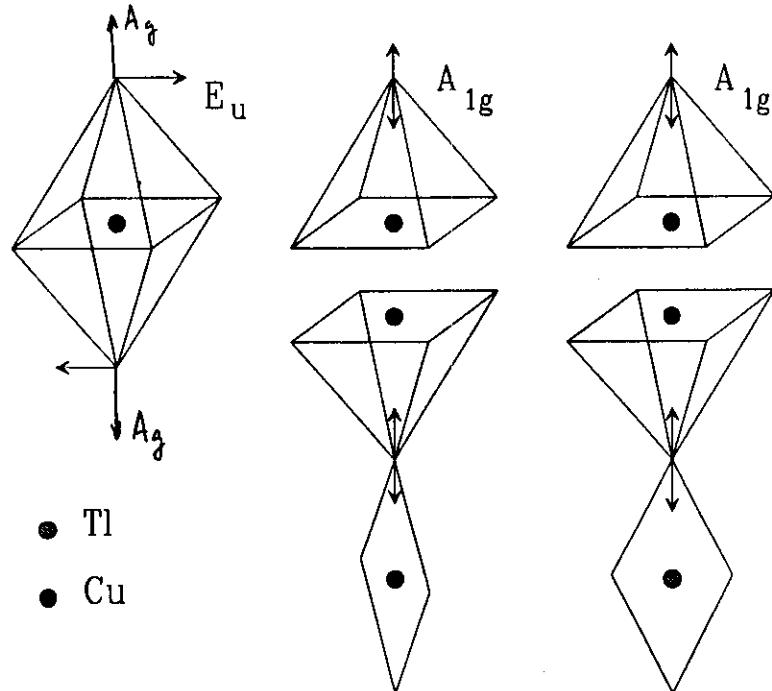
Misochko et al  
 Stanford proceedings  
 (1989)  
 Physics C

An important observation is that the phonon frequencies for apex O and Cu vibrations  
~~are~~ are different in xx and in zz!

some



Anharmonic modes



2-1-4

1-2-3

2-2-1-2

In summary : some anharmonic modes in high- $T_c$  superconductors , related to CT fluctuations .

## Raman Scattering from Magnons

Well characterized in  $K_2NiF_4$ , a prototype 2D antiferromagnet.

and  $J \sim 100 \text{ cm}^{-1}$ ,

Both lineshape and symmetry of observed Raman scattering spectrum is in good quantitative agreement with theory.

In cuprates,  $J$  is much larger (0.1 eV or  $800 \text{ cm}^{-1}$ ).

But,

- lineshape not in agreement with simple theory
- observed lineshape may be explained including next-nearest-neighbour interactions  $J'$  (J.P.Singh, 1990)
- symmetry of observed scattering is not in agreement with theoretical predictions for a 2D AF.
- significant spin-lattice interaction is seen in temperature dependence of the 2-magnon peak (Knoll et al 1990)

### UPON DOPING:

- scattering intensity drops dramatically, (and disappears ?)
- peak in spectrum shifts to lower energy,

**But what is the spectrum that remains in the superconducting phase?**

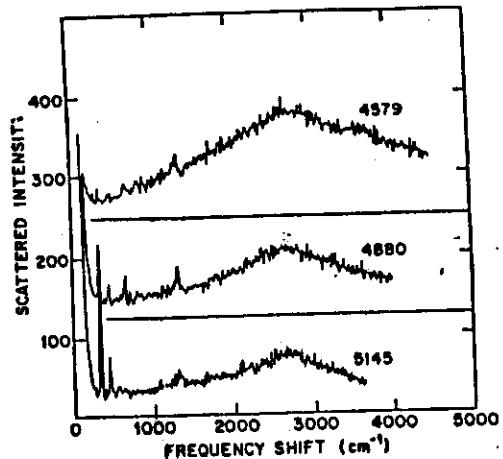


Figure 1

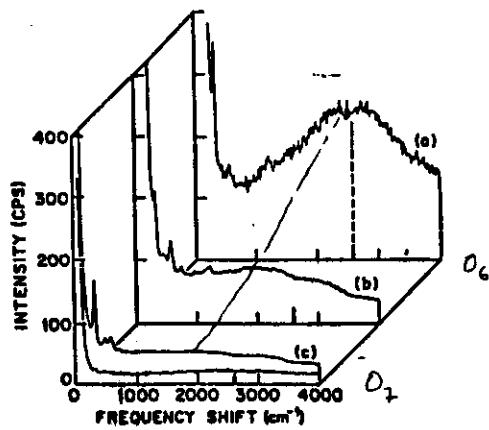


Figure 3

K.B. Lyons et al;

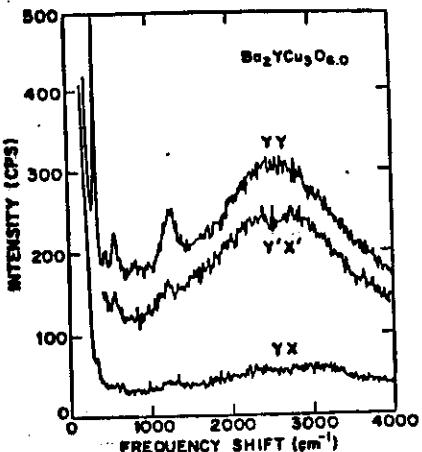


Figure 2a

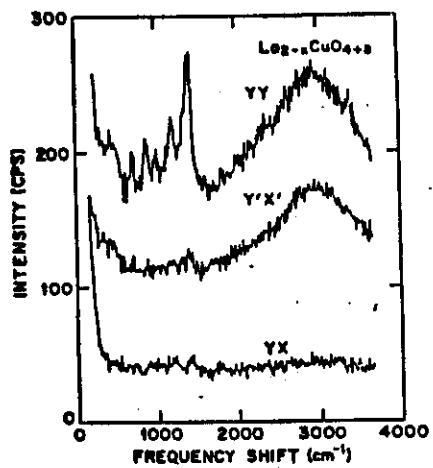
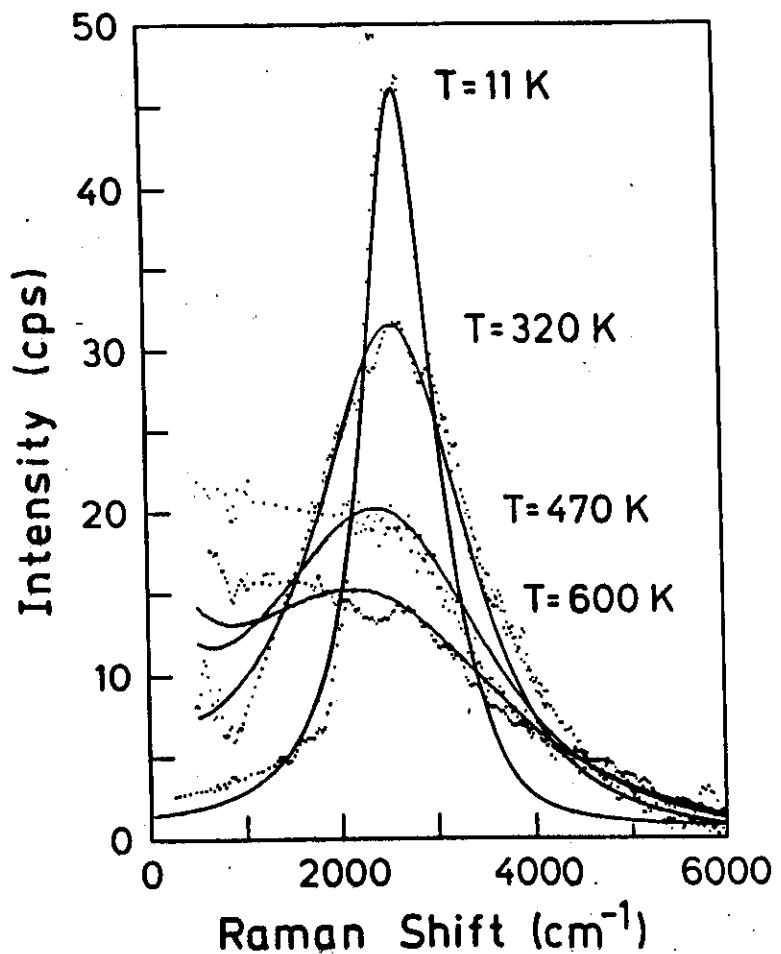
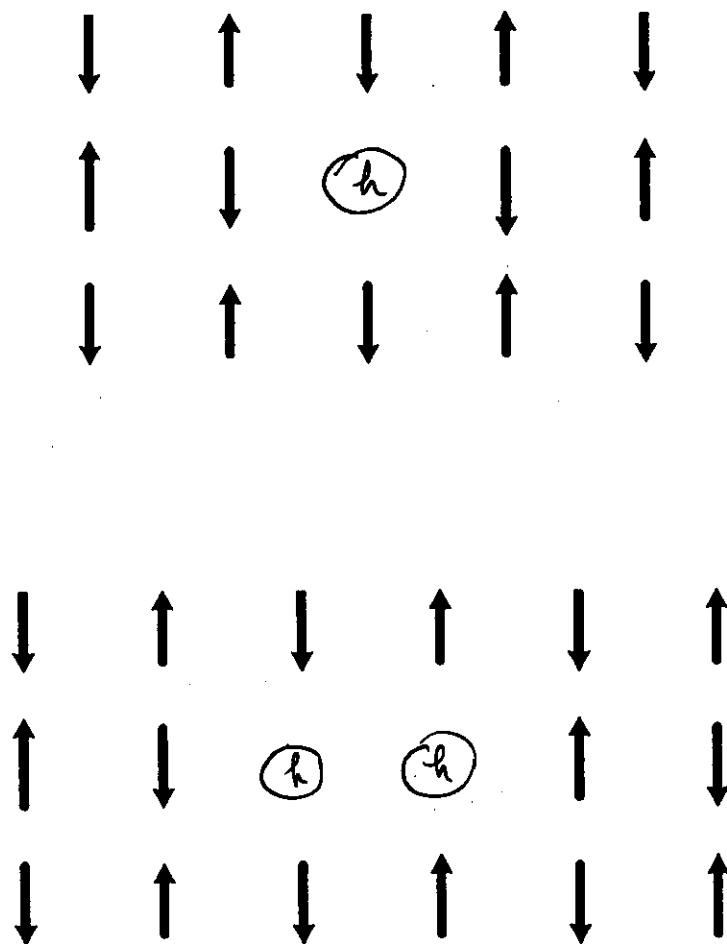


Figure 2b

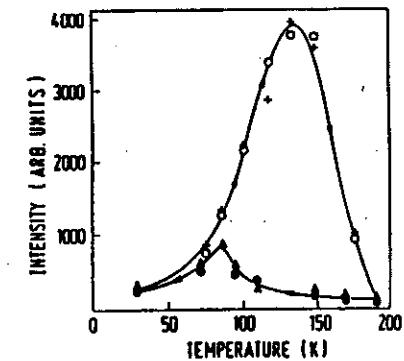
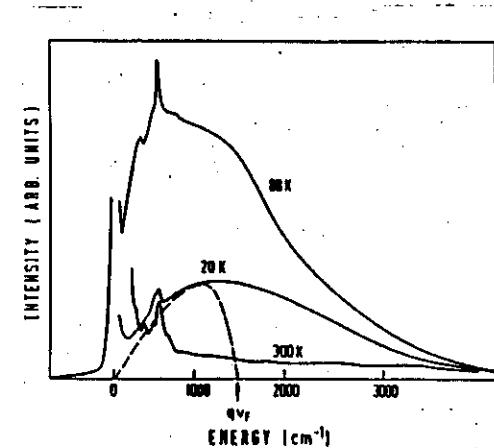


Linewidth of 2-magnon peak is strongly temperature dependent, suggesting a very strong spin-lattice interaction.



## Electronic Raman Scattering

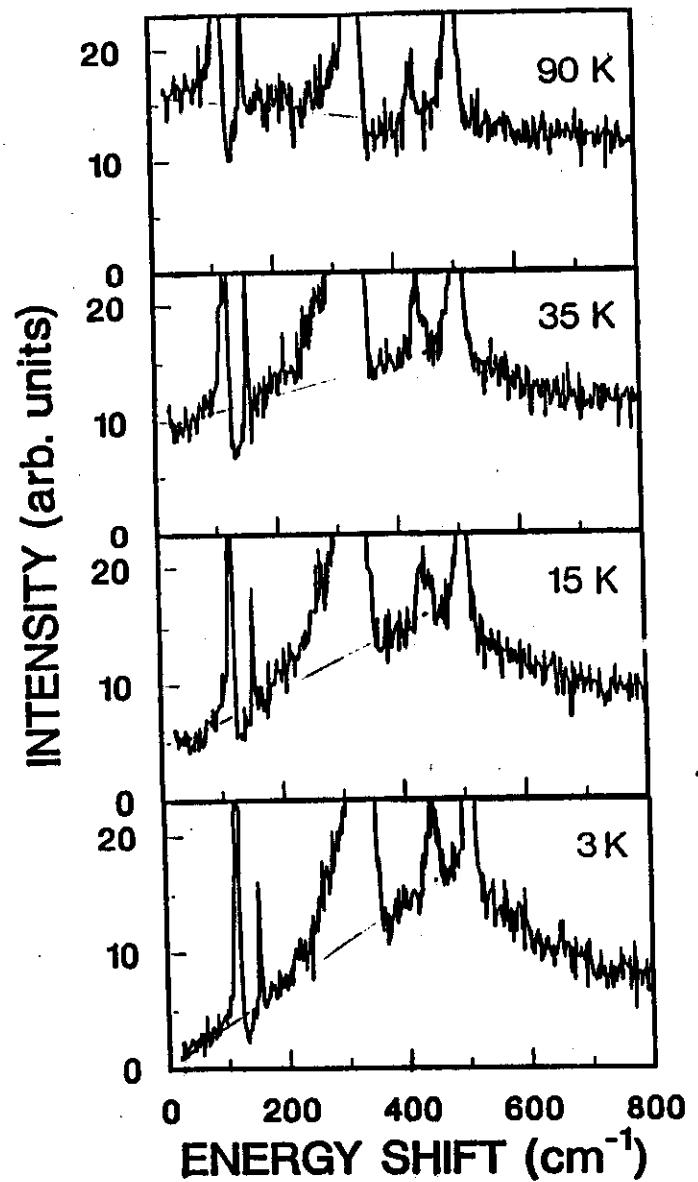
Originally observed in ceramic  $\text{YBa}_2\text{Cu}_3\text{O}_7$  (1987)



Behaved rather unexpectedly:

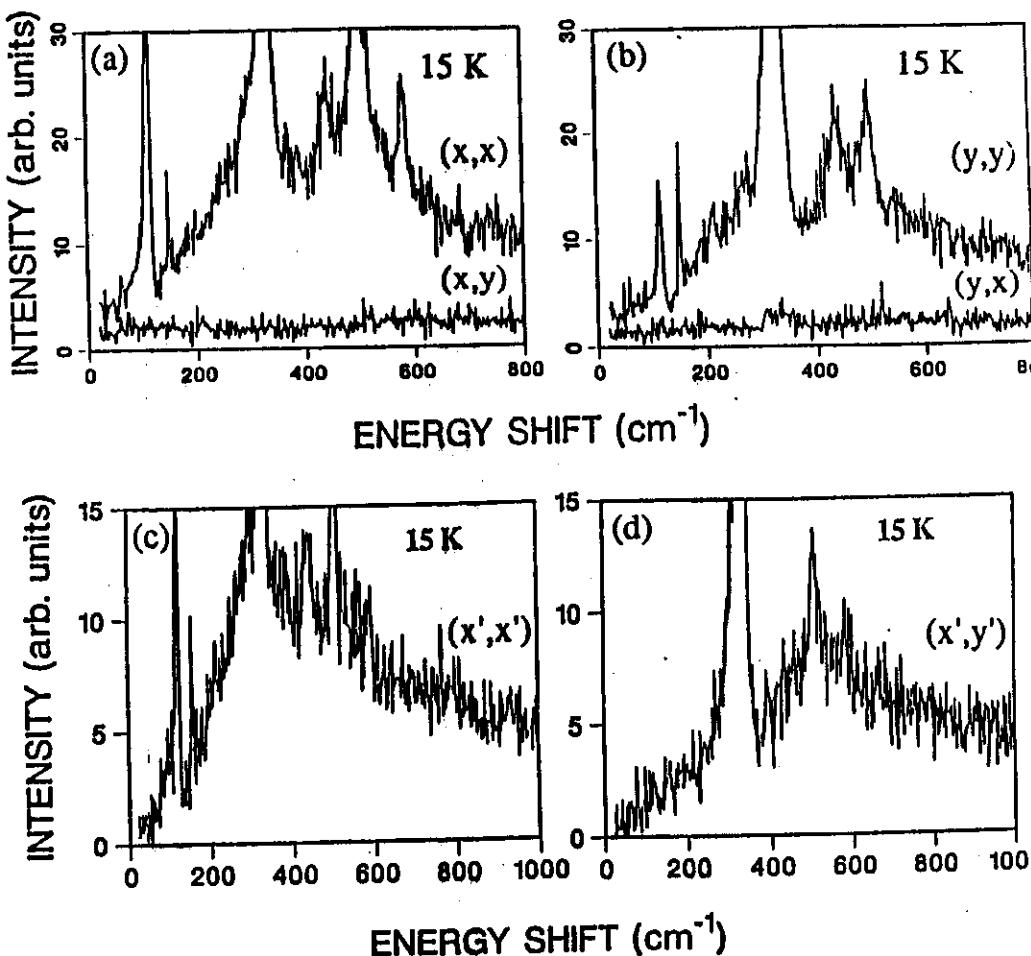
- redistribution of states was seen above  $T_c$

Further work on  $\text{YBa}_2\text{Cu}_3\text{O}_7$  single crystals with  $T_c > 90\text{K}$  showed a clear redistribution of states below 90K (e.g. Cooper et al, 1988)



More recent results on  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  with  $T_c = 60\text{K}$  show different components of the scattering (Slakey et al, 1990) behaving differently:

Part of the spectrum ( $\text{Ag}$  symmetry) shows a redistribution of states above  $T_c$  (similar to the original suggestions on ceramic material) (Slakey et al, 1990)



$\text{Ag}$  component of the scattering intensity at  $500 \text{ cm}^{-1}$  (at  $\sim 8 k_B T_c$ ) shows a clear maximum just above  $T_c$ , with similar

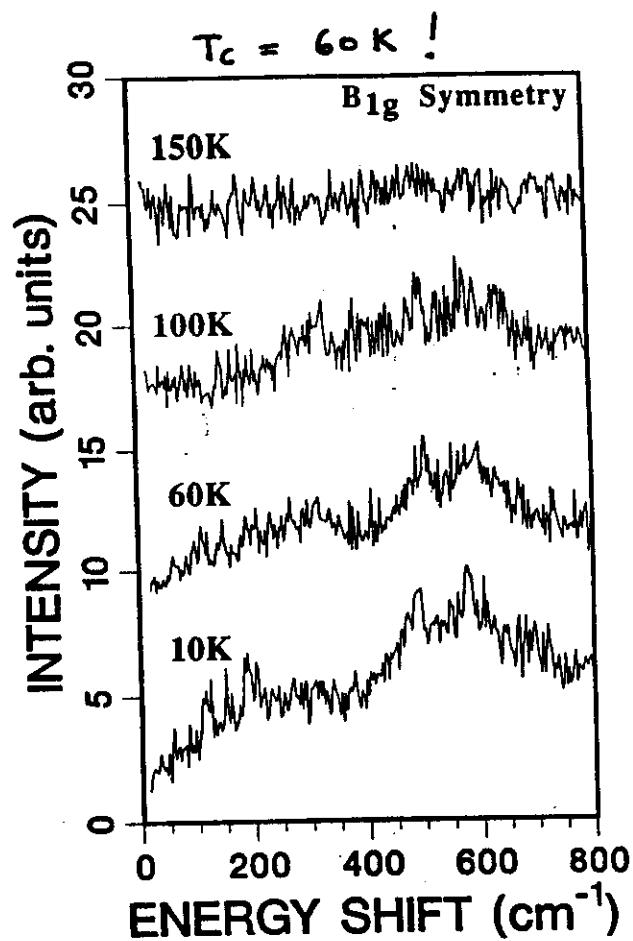
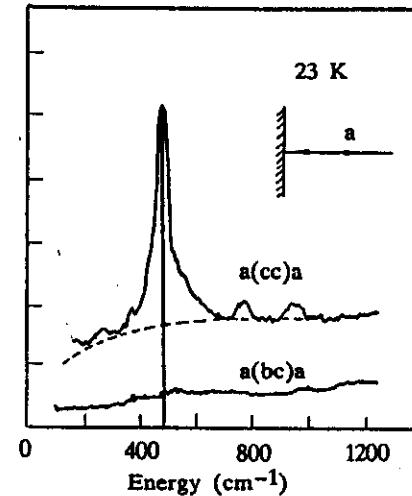
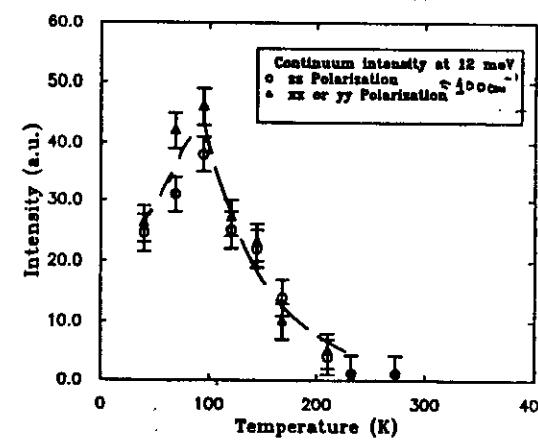


Fig 5.

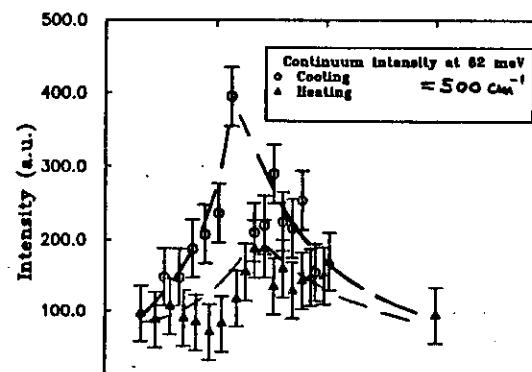
Energy "gap" shows up above  $T_c$  -  
results are from Staley et al (1990), for  
 $\gamma\text{Ba}_2\text{Cu}_3\text{O}$  sample with  $T_c \sim 60 \text{ K}$ . The redistribution



zz SCATTERING!

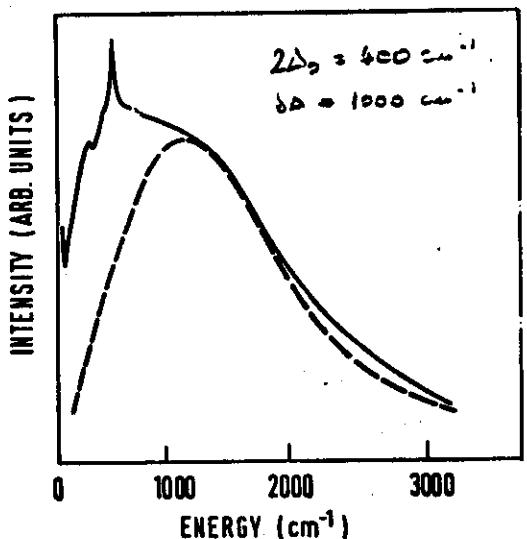


CT fluctuations:  
Normalized  
continuum intensity  
at 12 and 62 meV  
in  $\gamma\text{Ba}_2\text{Cu}_3\text{C}_{6.9}$  shows  
a peak near  $T_c$   
(is hysteretic)

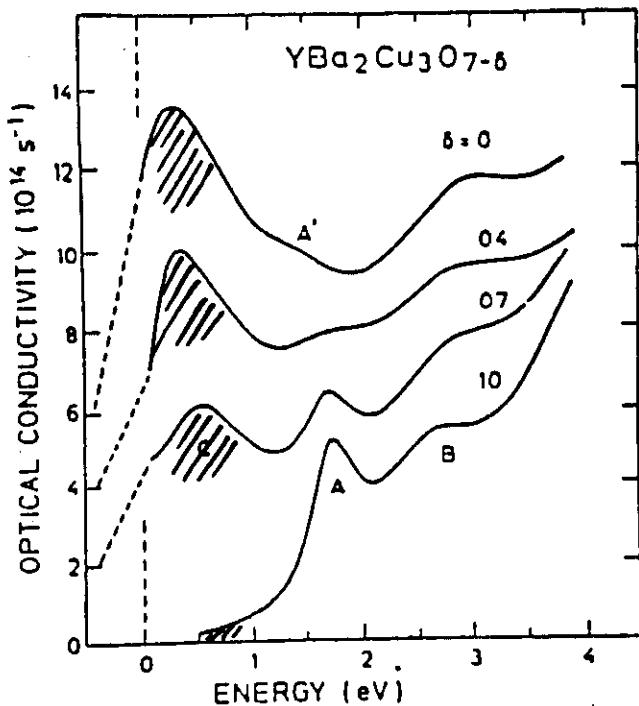


## Electronic RS: Conclusions

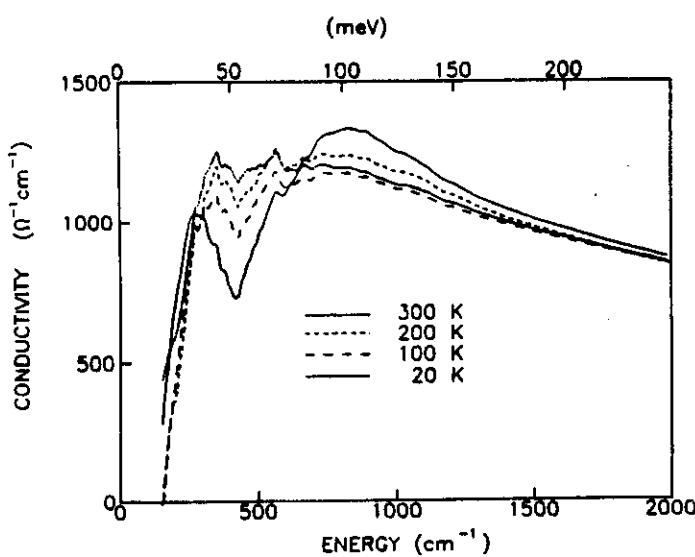
- a) The shape of the spectrum can be fitted using a
  - BCS model,
  - marginal Fermi Liquid (Ruvalds et al, 1989)
  - Mott-Hubbard model (Shriram et al 1990).
  
- b) The symmetry of the scattering can possibly be used for a more unambiguous determination of the origin of the scattering.
  
- c) Hysteresis in Ag spectra suggests also the presence of hot luminescence or scattering associated with O defects
  
- d) The effects of changing resonance condition with T (due to band edge shift) have not yet been properly taken into account.



FIT: BCS WITH GAP ANISOTROPY



GARRIGA et al (1988)



RAMARÁS et al (1990)

Polaron model for mid-IR peak:

$$H = H_e + H_L + H_{e-L}$$

where

$$H_e = \sum_{i,j,\sigma} t_{ij} c_{i\sigma}^{\dagger} c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

$$H_L = \sum_k \omega_k a_k a_k$$

$$H_{e-L} = \sum_{k,i,\sigma} \omega_k \alpha_k e^{-ikR_i} (a_k + a_{-k}) n_{i\sigma}$$

↑ Holstein Linear chain model

via Kubo's formula, we can calculate the frequency dependent conductivity,

$$\sigma(\omega) = \sqrt{2\pi} \frac{J^2 e^2 N}{\hbar^3 \omega_0^2} e^{-\eta} \left\{ \frac{\omega_0}{\omega} \right\} \left( \frac{\omega}{\omega_0} + \frac{3}{2} \right) e^{\left( \frac{\omega}{\omega_0} \right)^2} \eta \left( \frac{\omega_0}{\omega} \right)$$

e.g. Reik et al, (1963)

Mid-IR peak upon doping

Fig 1

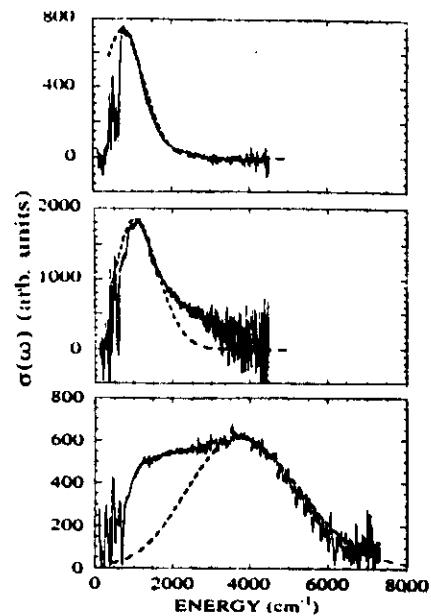
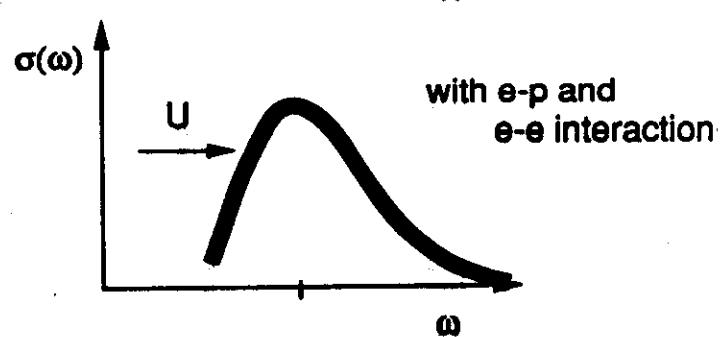
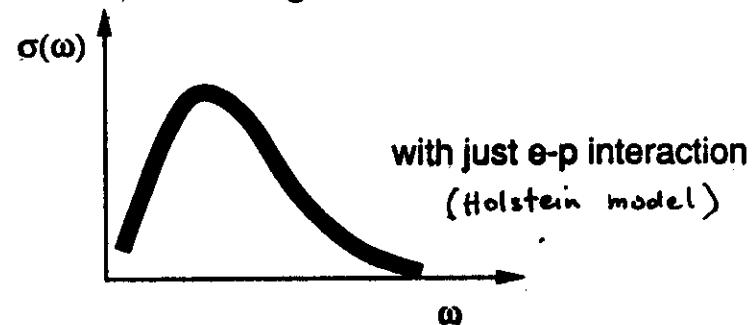
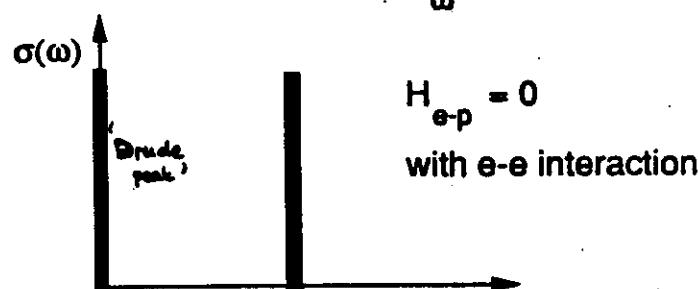
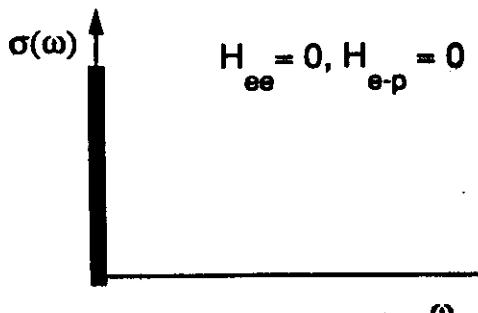


FIG. 1. The photoinduced infrared conductivity  $\sigma_p(\omega)$  (solid lines) in the insulator precursors for  $Tl_2Ba_2CaCu_3O_7$  (top),  $YBa_2Cu_3O_7$  (middle), and  $La_{2-x}Sr_xCuO_4$  (bottom) compared with fits to polaron-transport theory  $\sigma_{PT}(\omega)$  as calculated using Eq. (1) (dashed lines).

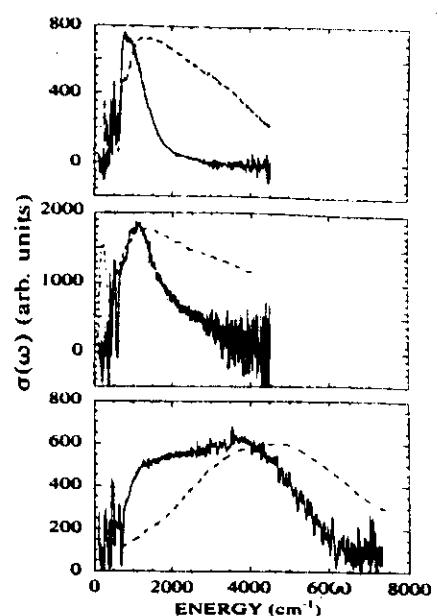


FIG. 2. The infrared conductivity  $\sigma(\omega)$  (dashed lines) for  $Tl_2Ba_2CaCu_3O_7$  (top),  $YBa_2Cu_3O_7$  (middle), and  $La_{2-x}Sr_xCuO_4$  (bottom) compared with the photoinduced infrared conductivity  $\sigma_p(\omega)$  (solid lines) in their respective insulator precursors.

Calculated fit to mid IR in 3 materials  
(Mihailovic et al  
(Phys Rev B, 1990))

### $m^*$ , coupling constants

	$m^*/m_e$	$\eta$	$\omega_0 (\text{cm}^{-1})$
$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$	23	10	450
$\text{YBa}_2\text{Cu}_3\text{O}_7$	13	7	200
$\text{Tl}_2\text{Ba}_2\text{CaCu}_2\text{O}_8$	11	5.6	200

### PEAK IN $\sigma(\omega)$ OF VARIOUS PEROVSKITES

	$T_c (\text{K})$	Mid-IR peak (eV)
$\text{SrTiO}_3$	0.38	>18
$\text{Ba}_{1-x}\text{Pb}_x\text{BiO}_3$	136	1.26
$\text{La}_2\text{CuO}_4$	34	0.5
$\text{YBa}_2\text{Cu}_3\text{O}_7$	93	0.13
$\text{Tl}_2\text{Ba}_2\text{CaCu}_2\text{O}_8$	110	0.09

The mid-IR peak is present in all perovskite superconductors! Is it "just a defect"?

### Conclusions

The e-p interaction in High-Tc materials manifests itself in a number of ways:

Anaharmonicity of apex O modes

Pyroelectricity, incipient ferroelectricity

Anomalous T-dependences in Raman spectra

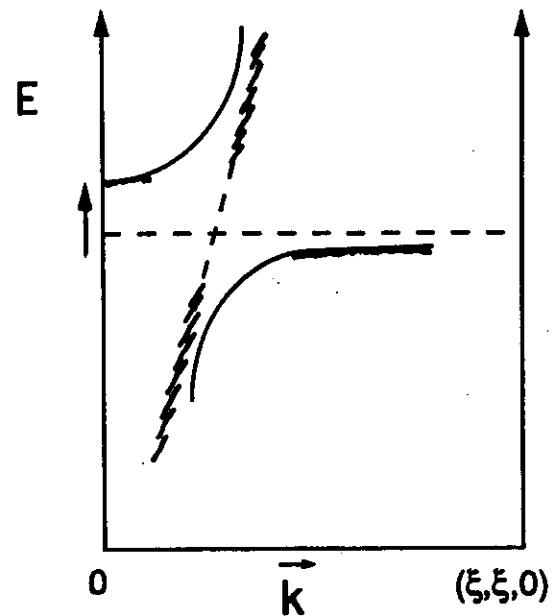
Local distortions suggest apex oxygen involvement in vibronic interaction

Polaron hopping gives  $\sigma(\omega)$  in mid-IR

Phonon (structural) anomalies at  $T_c$  (or just above  $T_c$ )

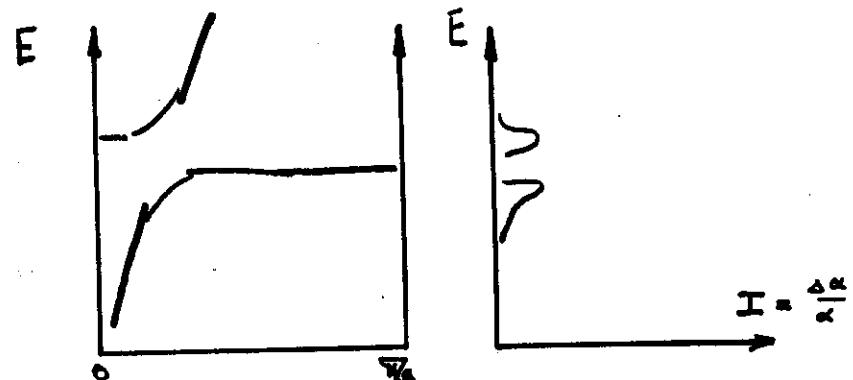
Conclude: whatever the effect of other interactions, e-p coupling has clearly been shown to be important in describing the normal properties of the superconducting perovskites.

Neutron data : results of elastic scattering



### Photoinduced Local Mode Spectroscopy (PLMS)

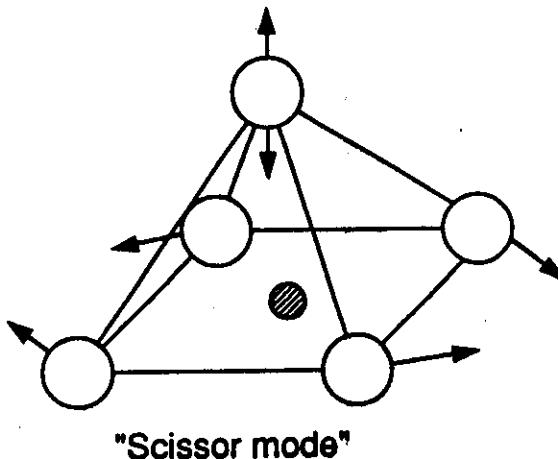
No  $q = 0$  selection rule!



### Photoinduced absorption spectroscopy

$$\Delta\alpha(\omega)/\alpha(\omega) = \Delta\sigma(\omega)/\sigma(\omega)$$

where  $\Delta\alpha(\omega)$  is due to the effect of optically excited carriers (electrons and holes).



Reichardt et al. (1990)

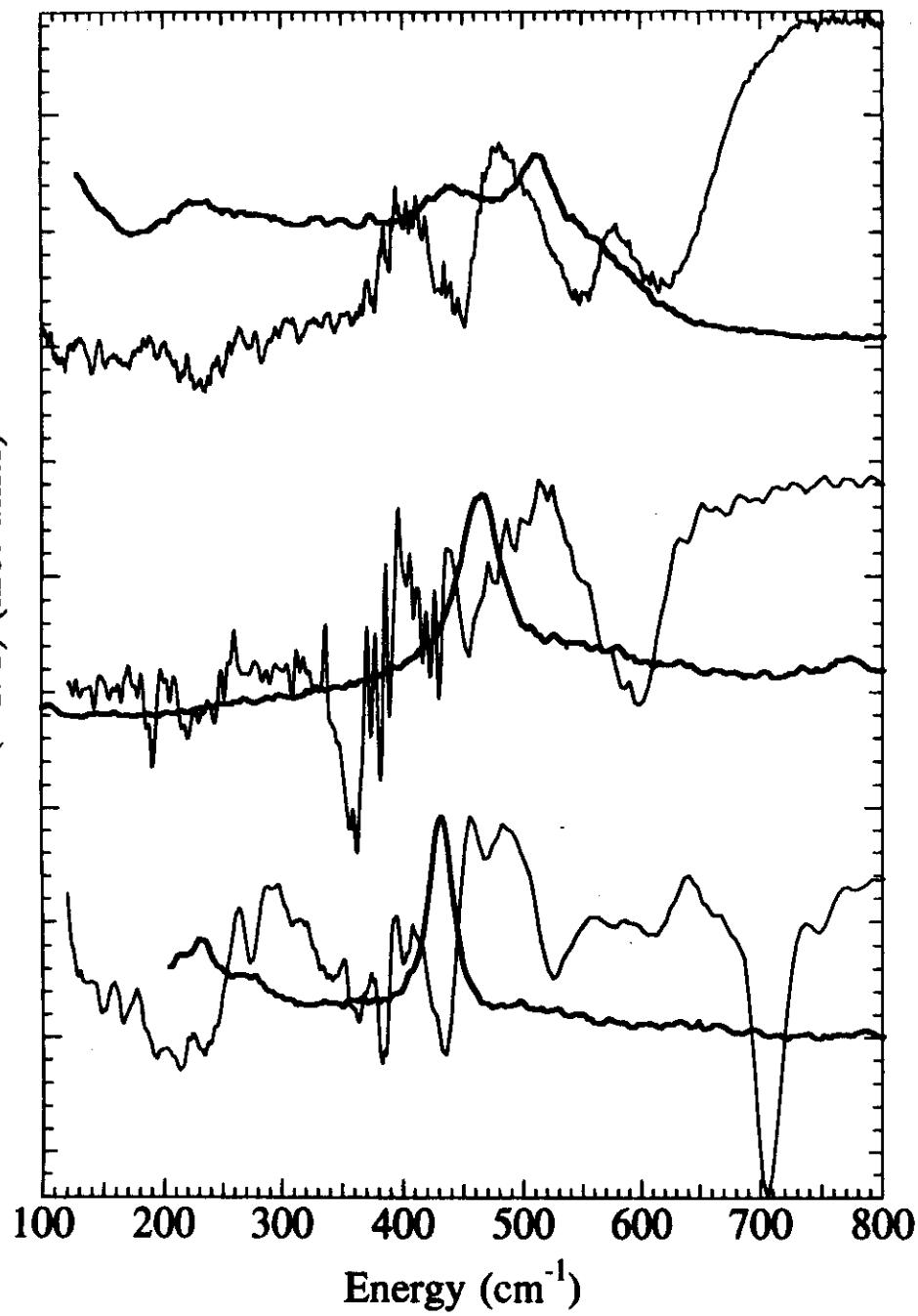
$-(\Delta T/T)$  (arb. units)

FIG. 1. Photoinduced local vibrational modes (PILMs) (thin lines) in  $\text{La}_2\text{CuO}_4$ ,  $\text{YBa}_2\text{Cu}_3\text{O}_{6.3}$  and  $\text{Tl}_2\text{Ba}_2\text{Ca}_{1-x}\text{Gd}_x\text{Cu}_2\text{O}_8$

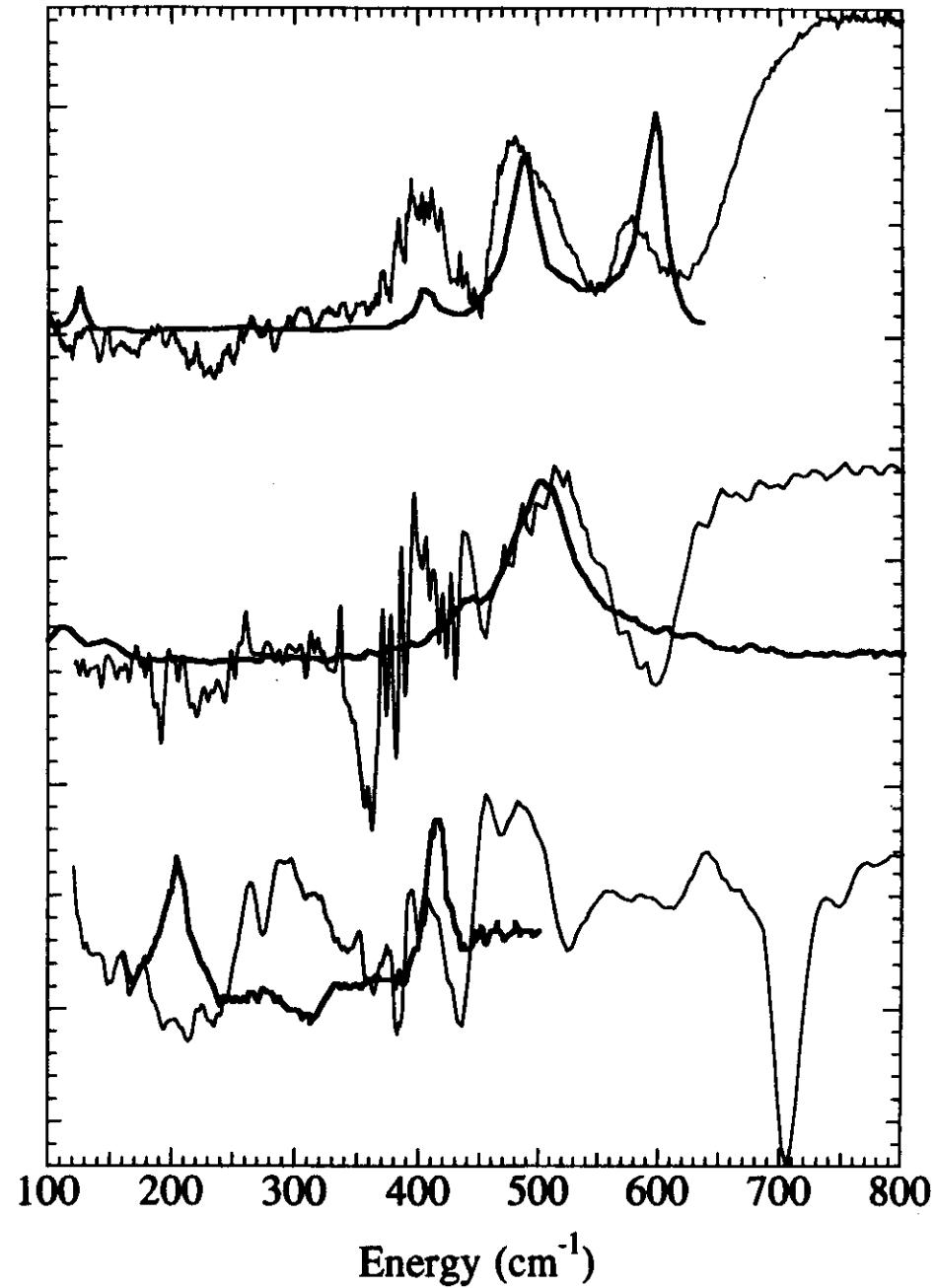
 $-(\Delta T/T)$  (arb. units)

FIG. 2. Photoinduced local vibrational modes (PILMs) (thin lines) in  $\text{La}_2\text{CuO}_4$ ,  $\text{YBa}_2\text{Cu}_3\text{O}_{6.3}$  and  $\text{Tl}_2\text{Ba}_2\text{Ca}_{1-x}\text{Gd}_x\text{Cu}_2\text{O}_8$  are compared with Raman spectra (thick lines) of metallic

References related to subjects presented in the lectures

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2. Phonon anomalies

340 cm<sup>-1</sup> mode:

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- C.Thomsen et al (see reviews)
- Cardona Phys.Rev.Lett. (1990)

500 cm<sup>-1</sup> mode;

- Conradson et al (1988) (XANES)
- Altendorf et al, SSC, 76 391 (1990) (Raman)
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Elastic Neutron scattering

- Pintacovius et al, Physica C: Stanford Proceedings, (1989)
- see also same authour, Dubna proceedings (1990)

3. Electronic Raman Scattering

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- Kim et al, Phys.Rev.B 38, 6478 (1988)
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