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UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
**INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS**  
I.C.T.P., P.O. BOX 586, 34100 TRIESTE, ITALY, CABLE: CENTRATOM TRIESTE



UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



**INTERNATIONAL CENTRE FOR SCIENCE AND HIGH TECHNOLOGY**

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SMR/543 - 11

EXPERIMENTAL WORKSHOP ON  
HIGH TEMPERATURE SUPERCONDUCTORS AND RELATED MATERIALS  
(BASIC ACTIVITIES)

(11 February - 1 March 1991)

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" High Temperature Superconducting Thin Films and Their Applications "

PART II

presented by:

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The Technical University of Denmark  
Physics Laboratory I  
Building 309  
DK-2800 Lyngby  
Denmark

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These are preliminary lecture notes, intended only for distribution to participants.

## II. HTS JOSEPHSON JUNCTIONS

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DK-2800 LYNGBY

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- 1) FILMS
- 2) JUNCTIONS
- 3) APPLICATIONS

For almost all <sup>electronic</sup> applications, Josephson junctions (active elements) are required.

comperison:

Same role as transistors in normal electronics

(DRAFT FINAL REPORT)

HIGH TEMPERATURE SUPERCONDUCTORS:

ASSESSMENT STUDY FOR SPACEBORNE SENSORS APPLICATIONS.

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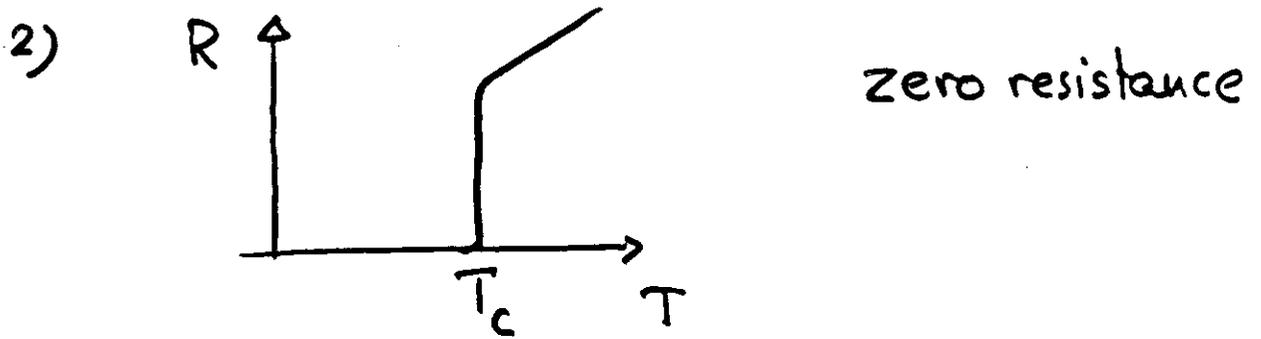
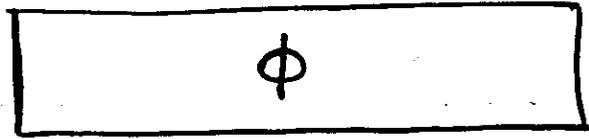
P.J. De Boer, ESTEC.

EUROPEAN SPACE AGENCY  
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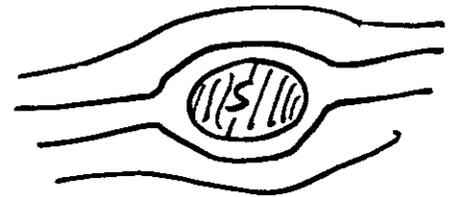
# SUPERCONDUCTIVITY

1) Macroscopic phase coherence

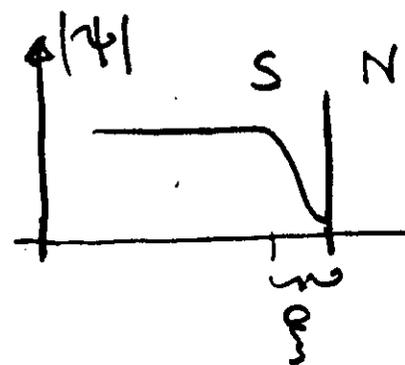


3) Meissner effect

flux (exclusion)  
expulsion

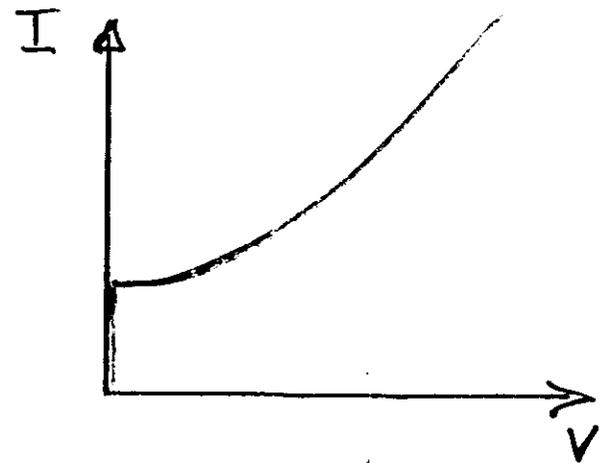
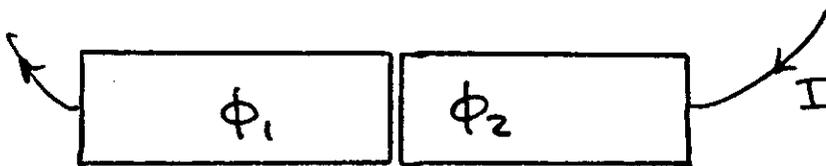
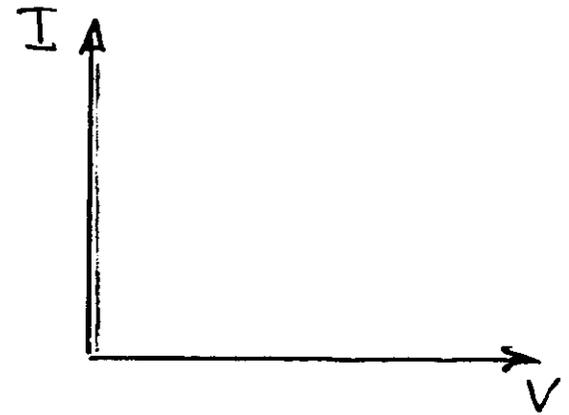
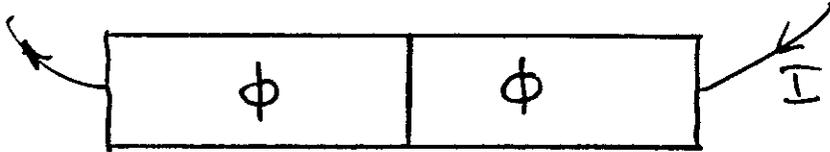
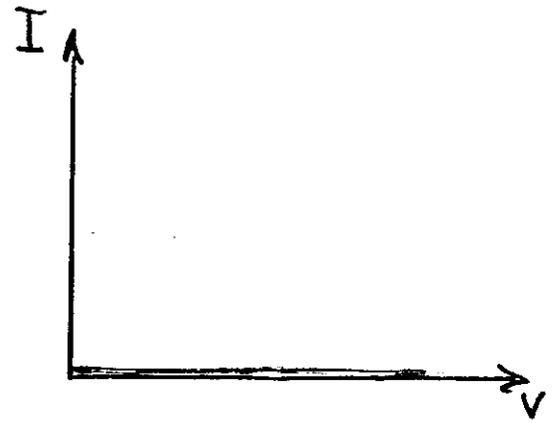
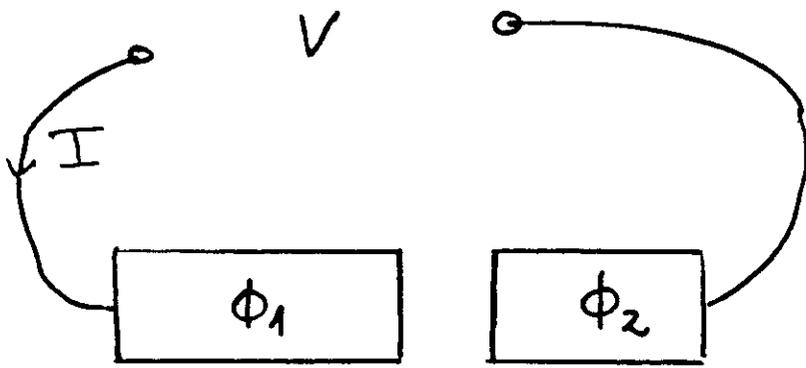


4) Coherence length  $\xi$   
(size of pairs)



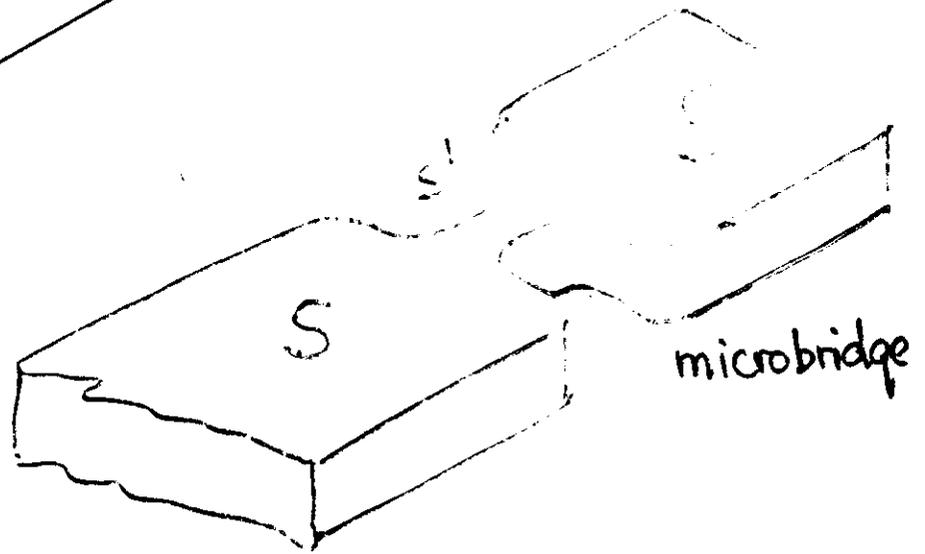
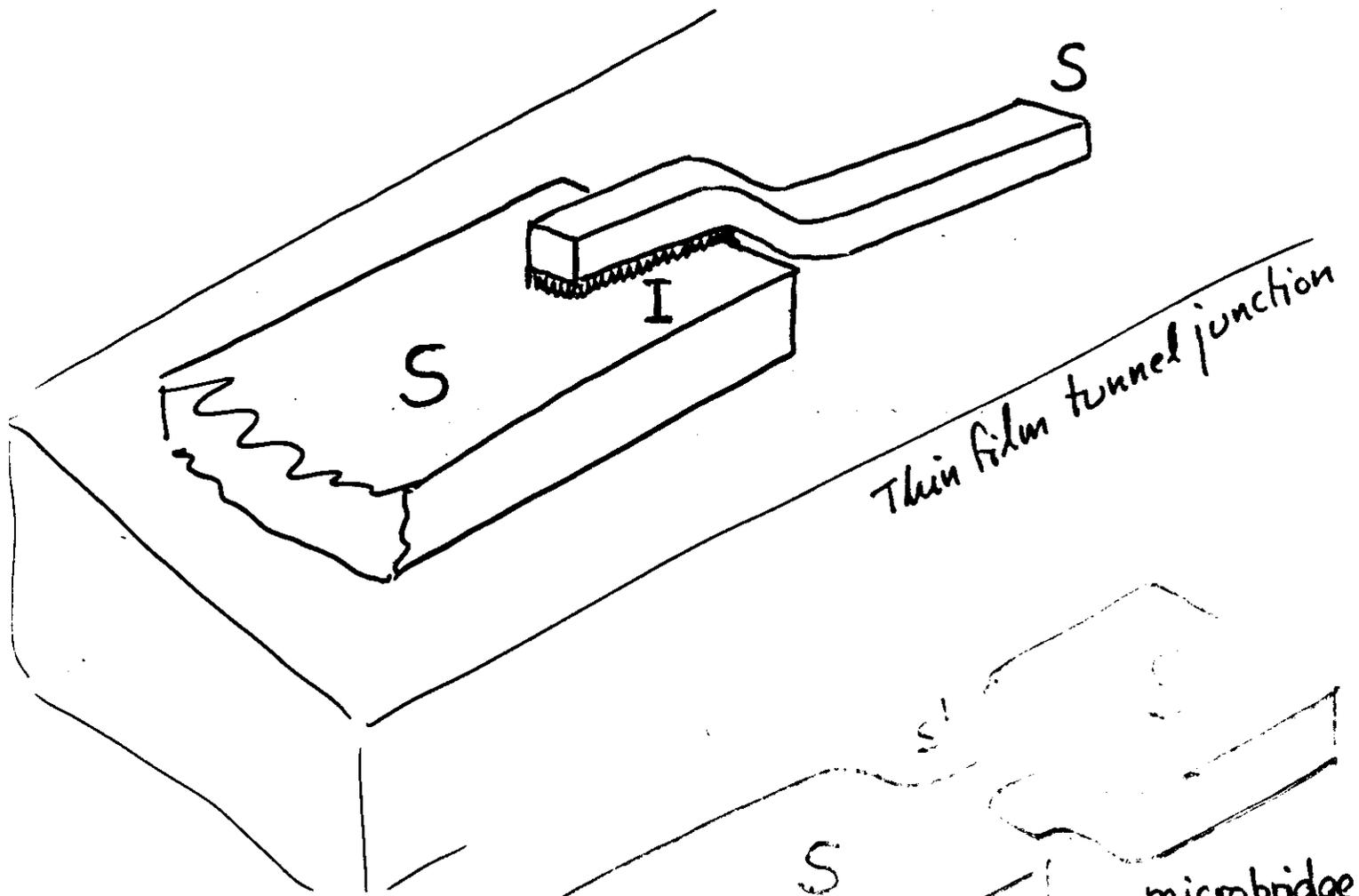
5) Penetration depth  $\lambda$   
magnetic field penetration

# WEAKLY COUPLED SUPERCONDUCTORS

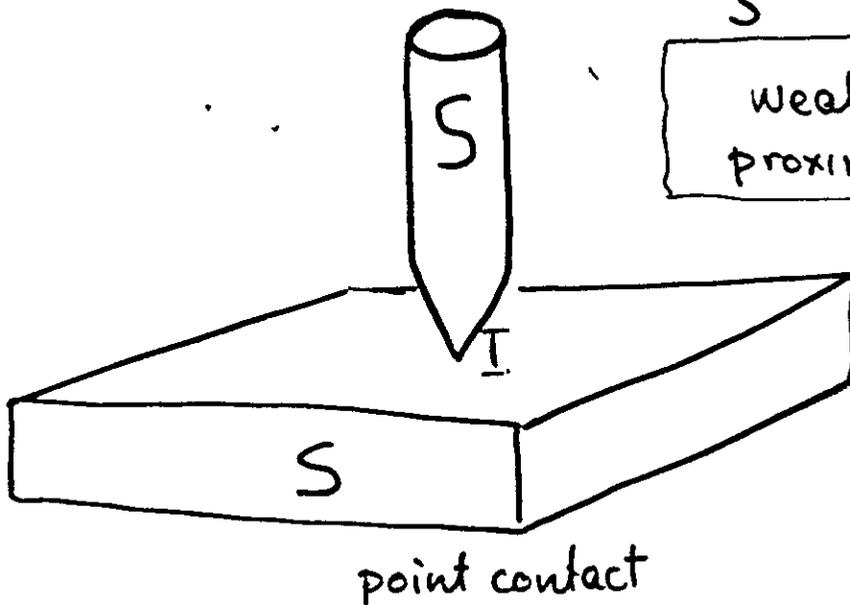
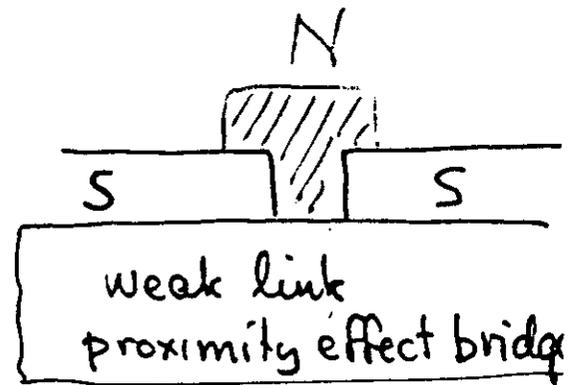


$$\phi = \phi_1 - \phi_2$$

supercurrent + ohmic current.

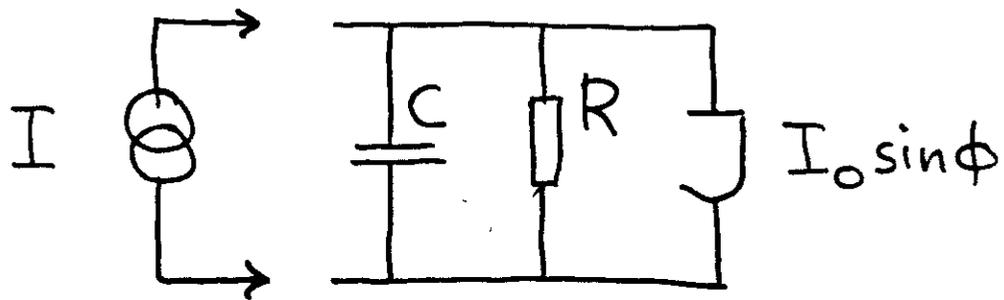
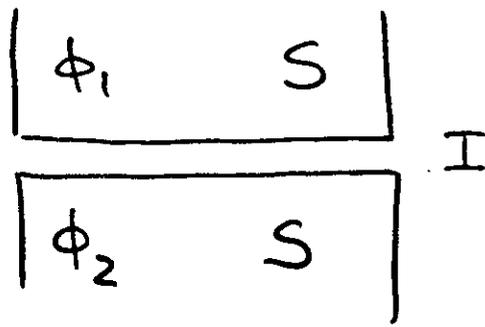


STRUCTURES  
FOR WEAKLY  
COUPLED  
SUPERCONDUCTORS



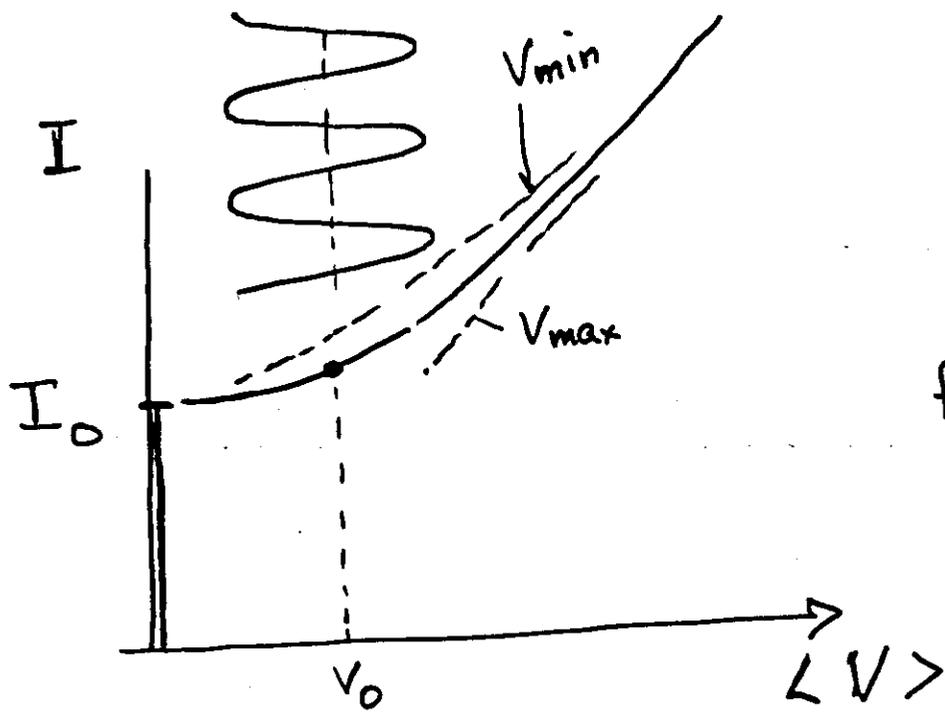
# JOSEPHSON JUNCTIONS

low  $T_c$



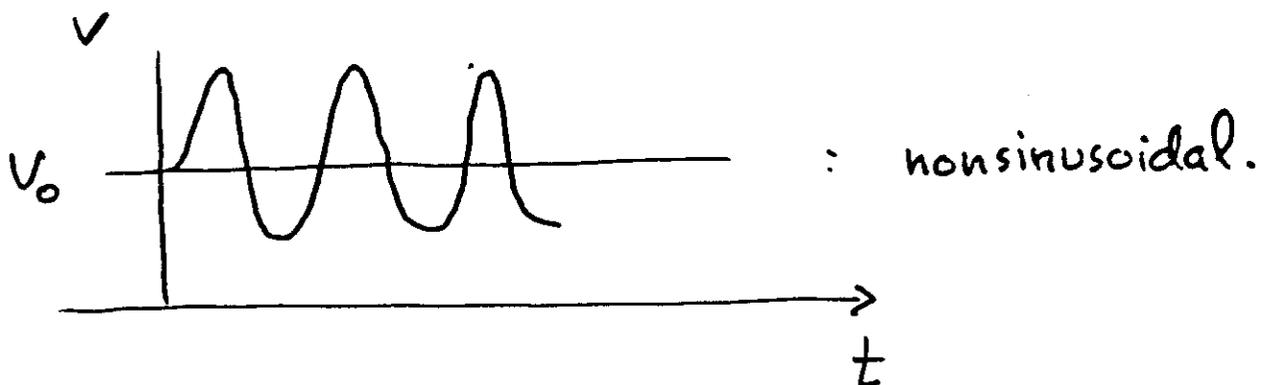
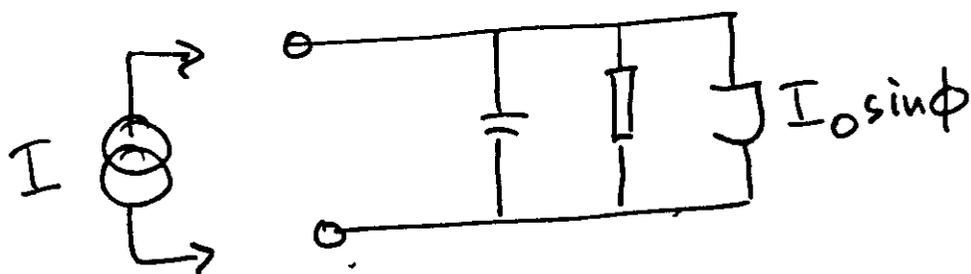
$$I = I_0 \sin \phi + \frac{V}{R} + C \frac{dV}{dt}$$

$$\frac{d\phi}{dt} = \frac{2e}{\hbar} \cdot V \quad \left( 484 \frac{\text{GHz}}{\text{mV}} \right)$$

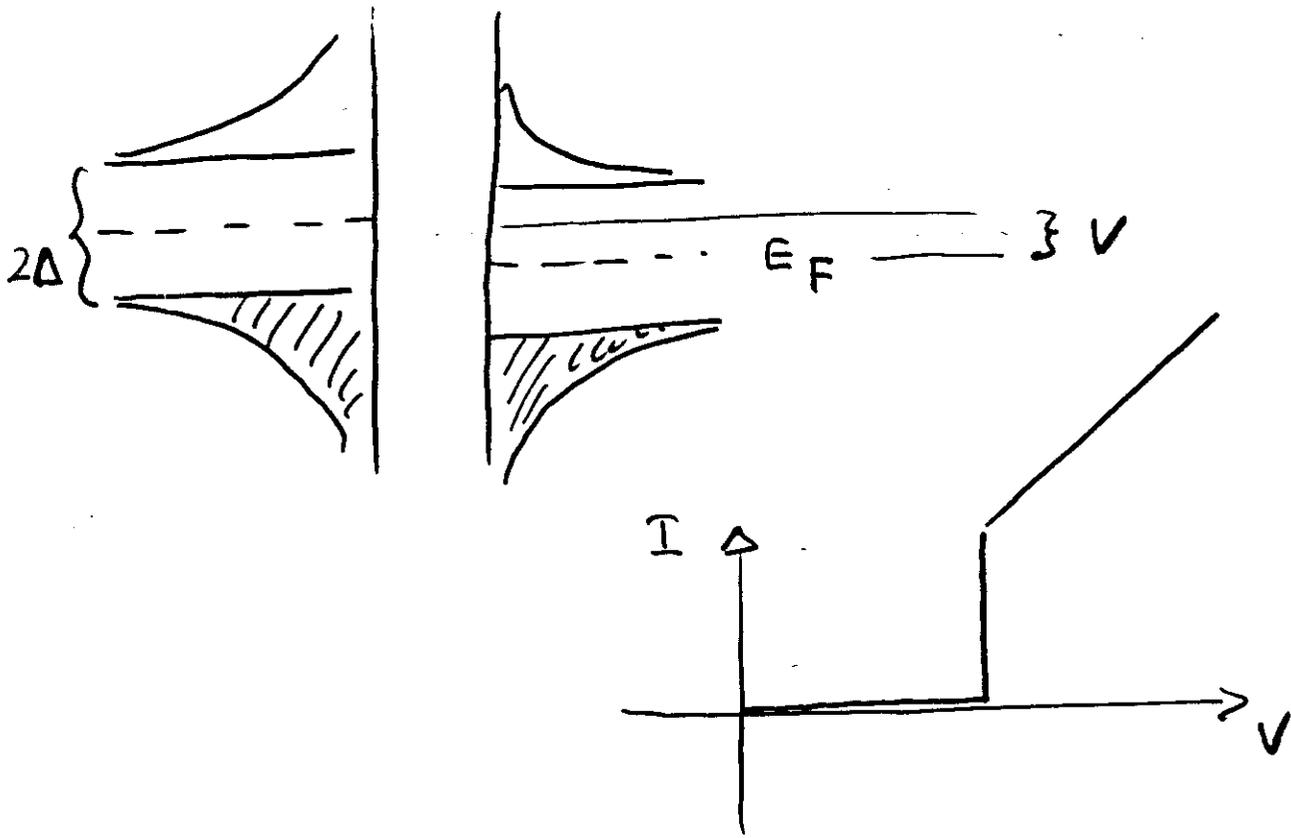


$$I = I_0 \sin\phi + \frac{V}{R} + C \cdot \frac{dV}{dt}$$

$$\frac{d\phi}{dt} = \frac{2e}{\hbar} \cdot V$$



$N(E)$



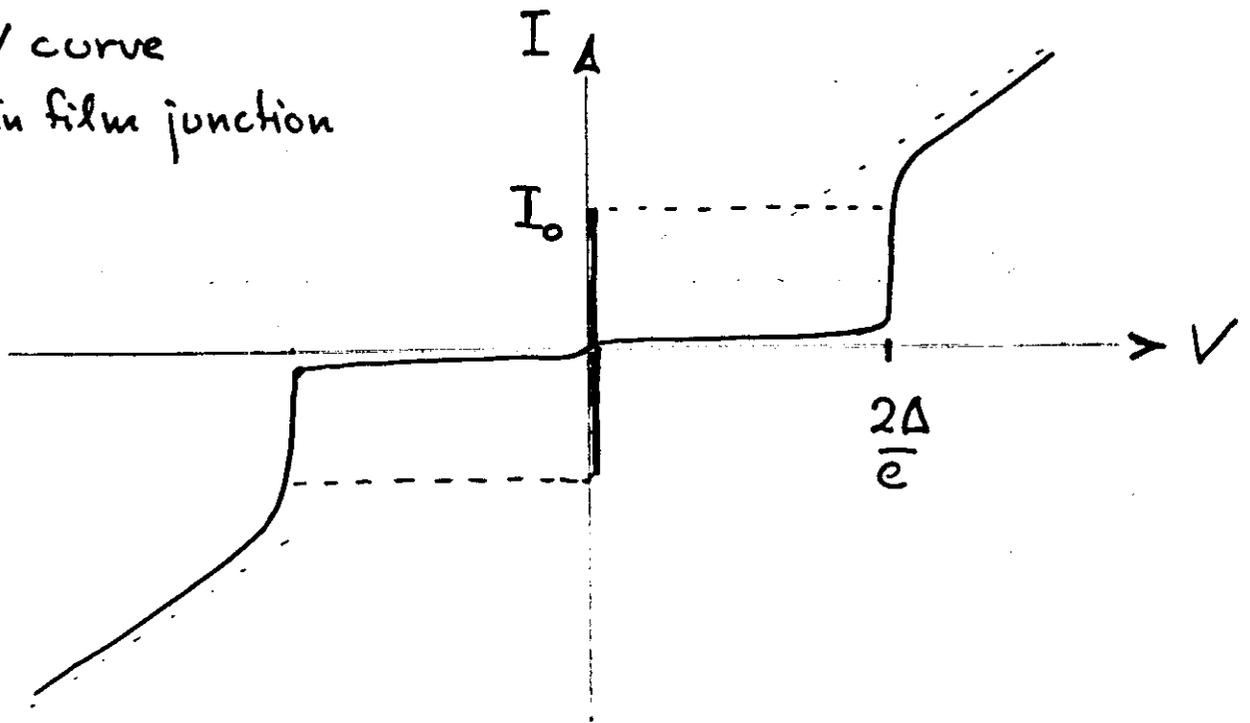
Tunneling of quasiparticles  
(normal electrons)

Supercurrent: Tunneling of Cooper pairs.

low  $T_c$

# Josephson junctions

IV curve  
thin film junction



Materials

Nb /  $Al_2O_3$  / Nb

Pb / Pb oxide / Pb

⋮

Area

$10 \mu m \times 10 \mu m$

Fabrication

Sputtering, E-beam, ...

Photolithography

Example:

microprocessor  
on one chip.

$2 \times 10^4$  junctions

# JOSEPHSON JUNCTIONS

Time characteristic properties leads to three tests.

1) AC - Josephson effect

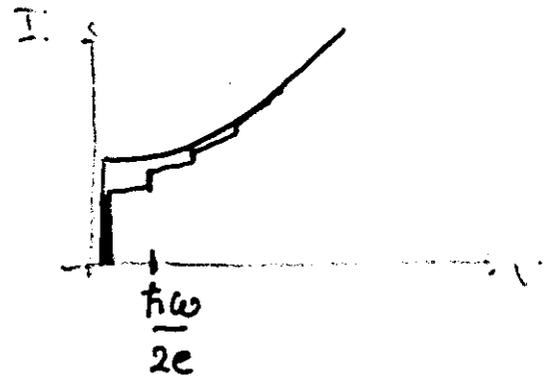
$$f_J = \frac{2e}{h} V = 483.6 \times 10^{12} \text{ Hz/V}$$

leads to „Staircase“ steps with applied microwave radiation.

Frequency to Voltage.

$$\phi = \phi_0 + \phi_1 \cdot \sin \omega t$$

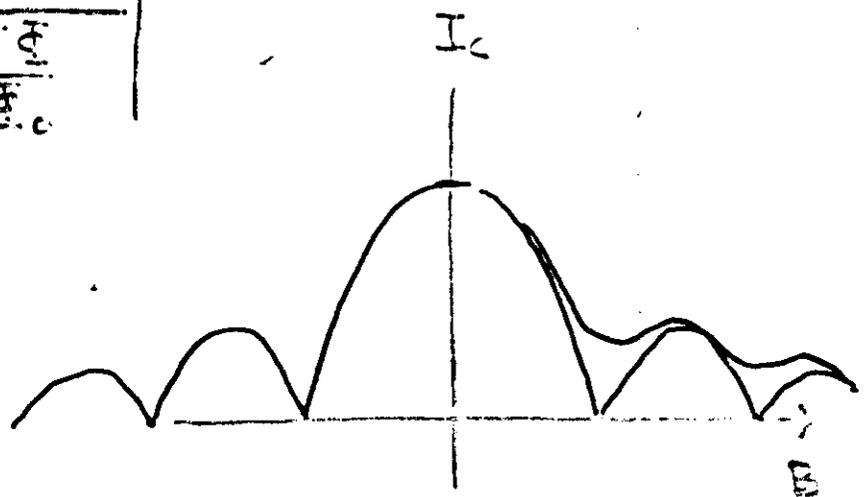
$\sin \phi$



2) Periodic dependance of  $I_c$  on magnetic flux.

$$I_c(\phi) = I_c(0) \left| \frac{\sin \frac{\pi \phi}{\phi_0}}{\frac{\pi \phi}{\phi_0}} \right|$$

Flux to voltage.



# JOSEPHSON JUNCTIONS

Low  $T_c$

BCS theory

Kierthamer theory

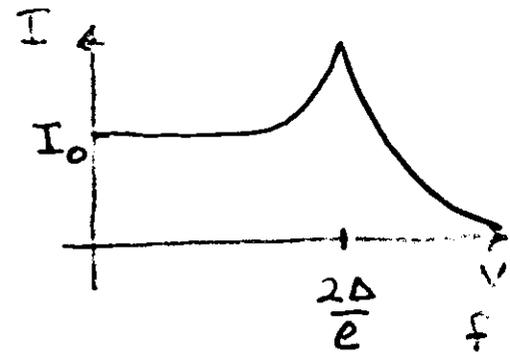
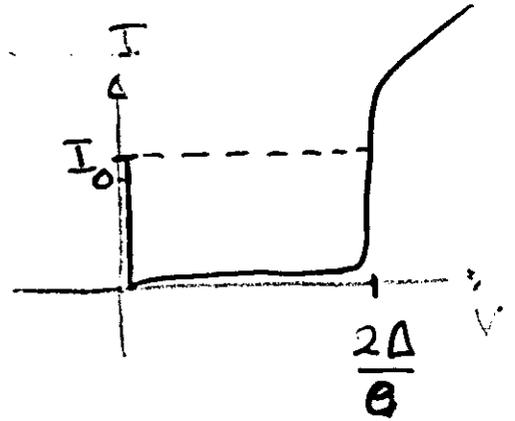
fully developed.

$RI_0$  = Measure of quality

$$RI_0 = \frac{\pi}{4} \frac{2\Delta}{e}$$

$$2\Delta \sim 3.5 \cdot kT_c$$

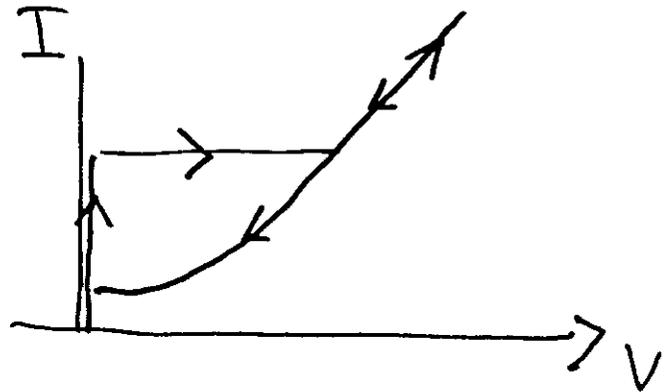
$RI_0$  measures high frequency cutoff.



	$RI_0$	$T_c$	$f_{\text{cutoff}}$
Low $T_c$	$\sim 3 \text{ mV}$	$\sim 10 \text{ K}$	1 THz
high $T_c$	$\sim 30 \text{ mV}$	$\sim 100 \text{ K}$	10 THz

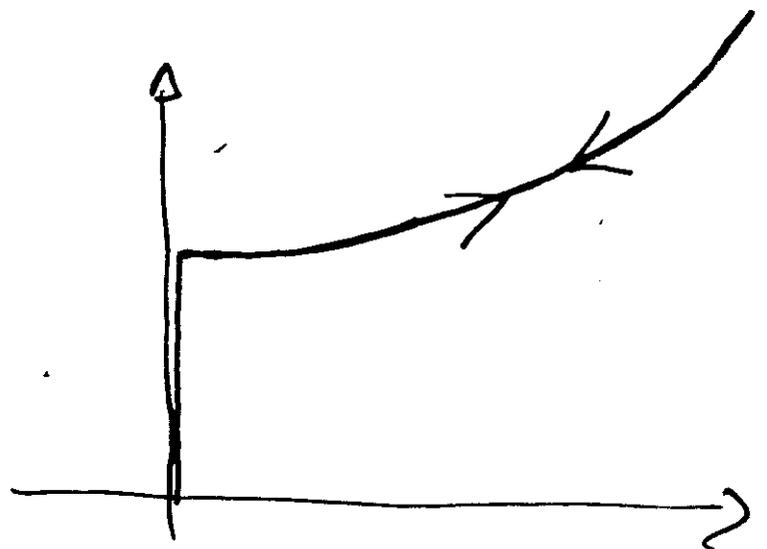
I V curve :

Hysteresis



or

not hysteresis



$$I = I_0 \sin \phi + \frac{V}{R} + C \frac{dV}{dt}$$

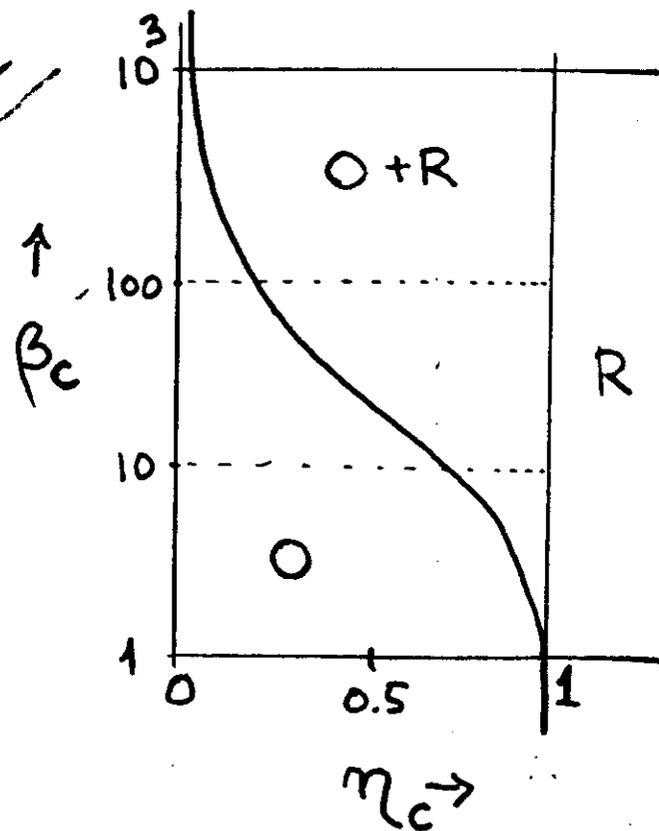
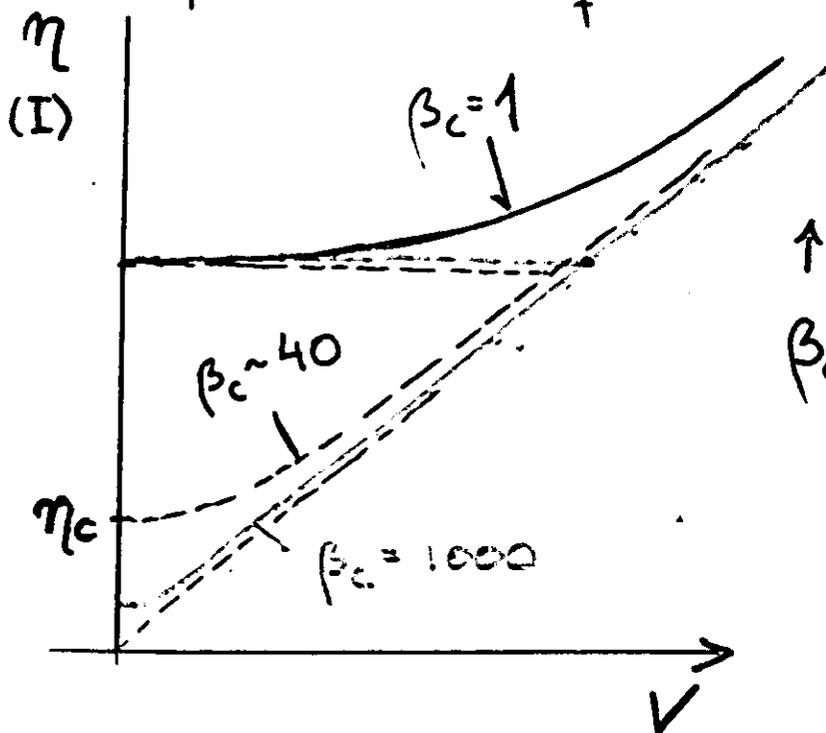
$$\frac{d\phi}{dt} = \frac{2eV}{\hbar}$$

$$\frac{d^2\phi}{d\tau^2} + \alpha \frac{d\phi}{d\tau} + \sin\phi = \eta$$

$$\alpha = \frac{1}{\sqrt{\beta_c}}, \quad \beta_c = \frac{2e I_0 R^2 C}{\hbar}, \quad \eta = \frac{I}{I_c}$$

new time  $\tau = \omega_0 t$ ,  $\omega_0 = \sqrt{\frac{2e I_0 C}{\hbar}}$

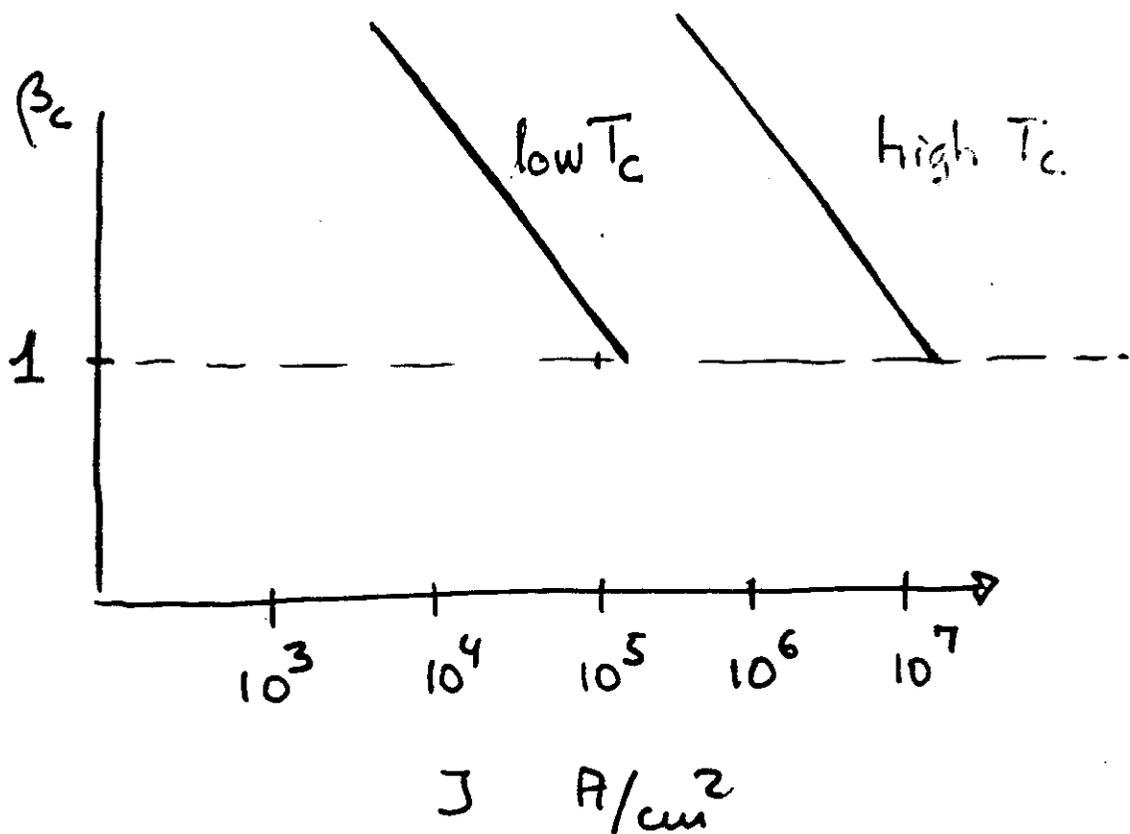
pendulum equation.



large damping  $\alpha \sim 1$  } no hysteresis  
 $\beta_c \sim 1$  }

$$\beta_c = \frac{2e}{\hbar} I_0 R^2 C \sim (RI_0)^2 \cdot \frac{C}{I_0}$$

$$\beta_c \propto I_0^{-1} \Delta^2$$



Remember: Film current density  $\sim 10^7 \frac{\text{A}}{\text{cm}^2}$

Hysteresis :

A word of caution:

Thermal effects (heating)

multiple junctions

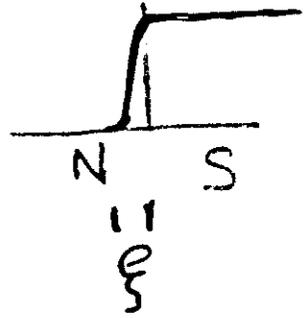
and other irregularities

may lead to hysteresis,

and wrong interpretation of  
IV curves.

## High $T_c$

$\xi$ , the coherence length measures extension of superconductivity.



## For thin film junctions

1) Oxide thickness  $d \ll \xi$

2) Surface planar to better than  $\xi$

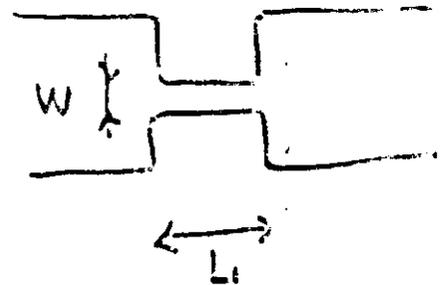


Low  $T_c$        $\xi = 500 - 1500 \text{ \AA}$

High  $T_c$        $\xi_{\perp} \approx 5 \text{ \AA}$ ,       $\xi_{\parallel} \approx 30 \text{ \AA}$

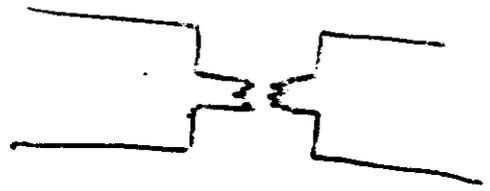
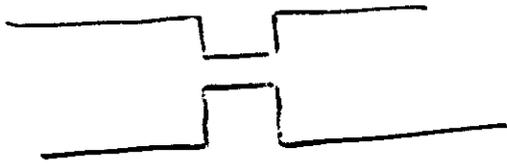
## For weak links:

To destroy superconductivity in weak section dimensions must be small compared to  $\xi$ .

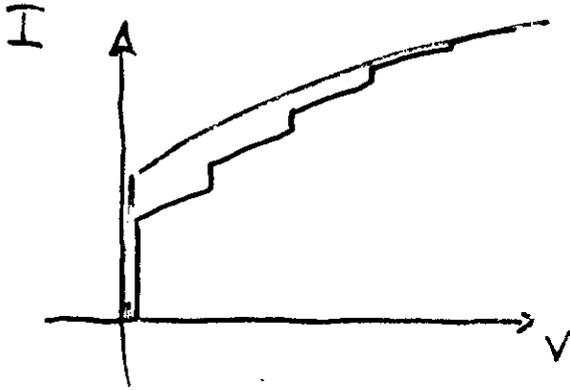


$$L, W \ll \xi.$$

# HIS point contact junctions



break junction



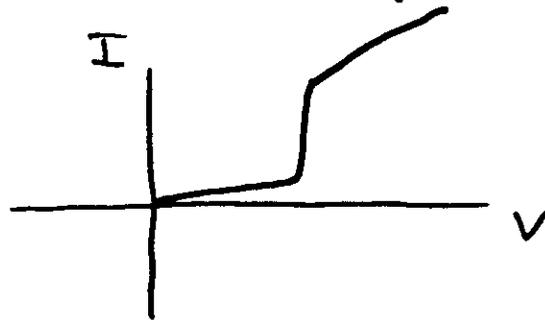
Test: rf indexed steps.  
OK

but unstable.

Work in several groups  
Nanjing, Lyngby, Chalmers  
.....

~

## Scanning tunneling microscope (STM)



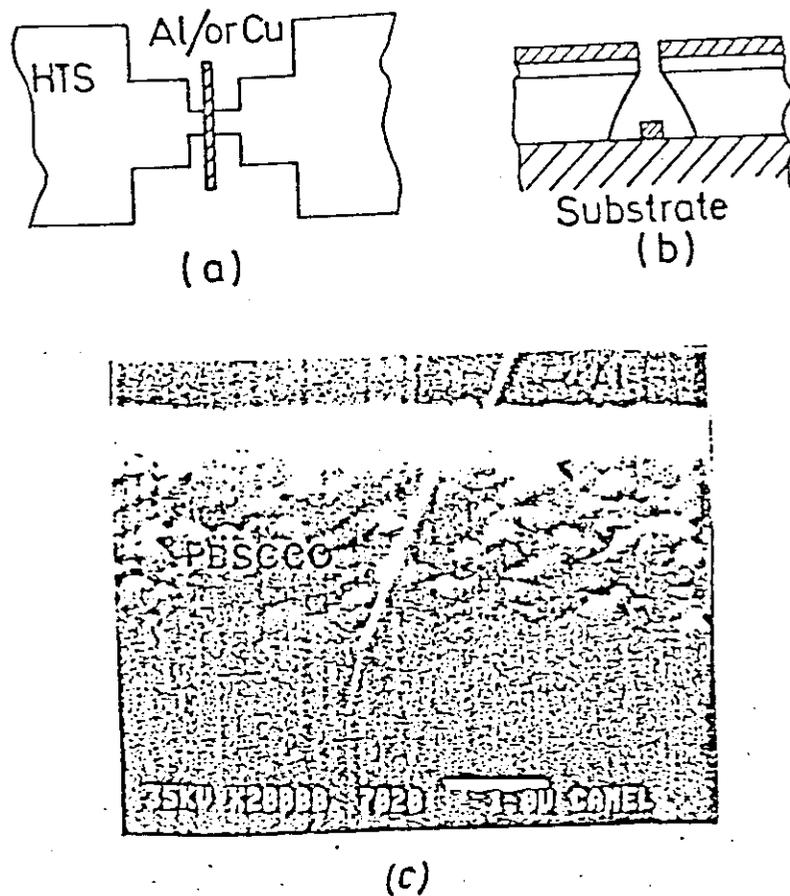


Fig. 3. Device design (a), fabrication process (b) and SEM micrograph of the experimental device (d).

ESA report 1990, C.S. Jacobsen

deposited. To form the weak link, the HTS strip was annealed in oxygen at different temperatures. Several weak links have been produced and some preliminary results are discussed below.

Fig. 4 shows the I-V curves for the proximity effect bridge of YBCO with Al strip before (a) and after (b) heating in oxygen at 430°C for 15 minutes. Even at such a low temperature the diffusion of Al was crucial for the superconducting properties of the YBCO strip and the supercurrent was depressed completely. The next proximity effect bridge was developed by using BSCCO film with a  $T_c$  of 66K. The heating was performed in air at 300°C for 3 min in  $O_2$ . In Fig. 5 it is shown the I-V curve of this weak link measured at temperature 24K. Note the positive curvature characteristic of a Josephson junction at low bias. The I-V curve was non-hysteretic with a critical current times normal resistance product of 40  $\mu V$ .

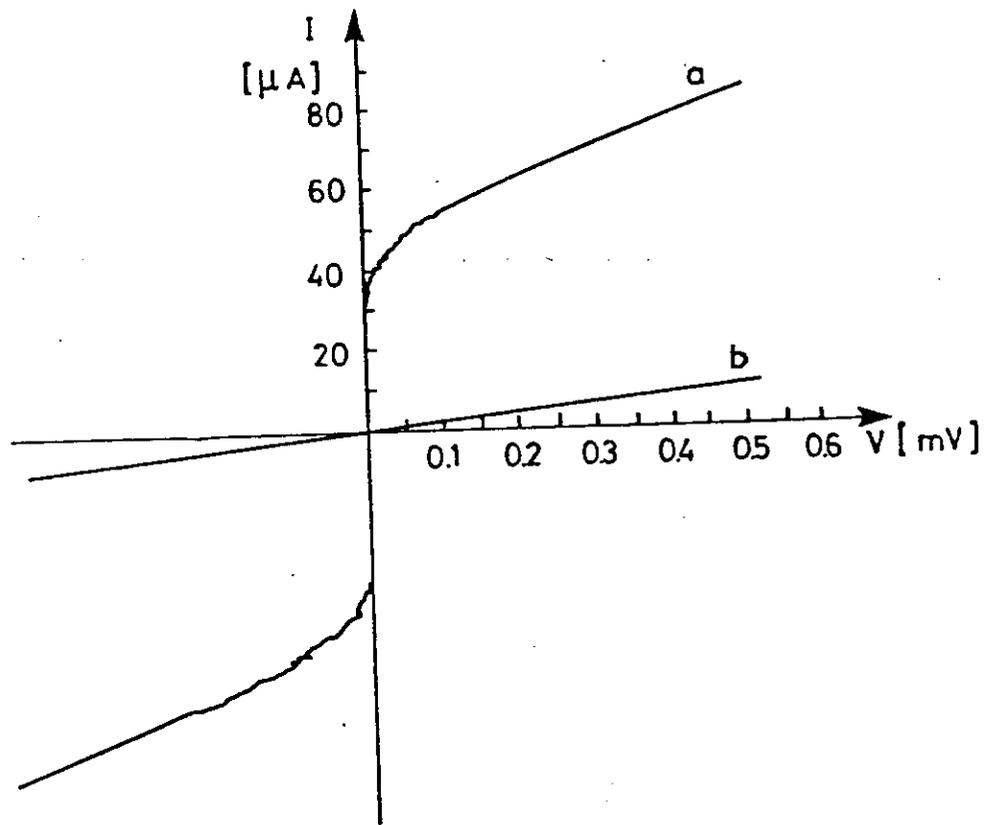


Fig. 4. I-V curves of the proximity effect bridge of YBCO with 70 nm wide Al strip line: (a) before heating; (b) after heating at 430 C for 15 min.

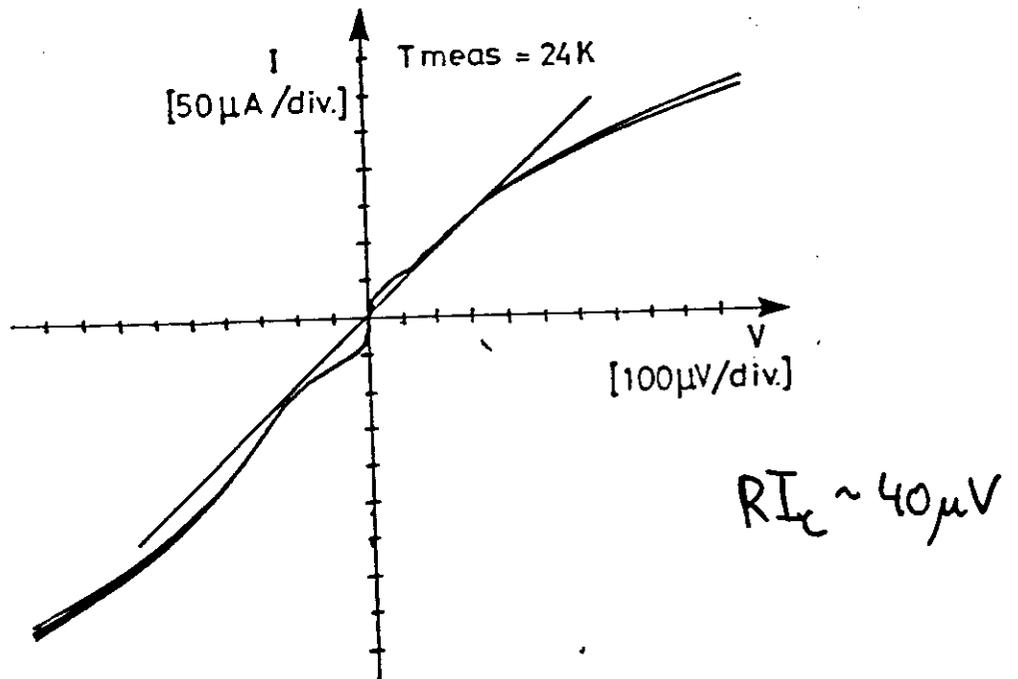
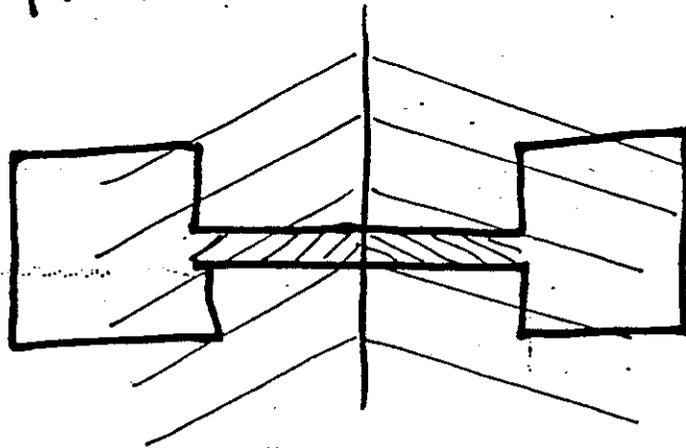
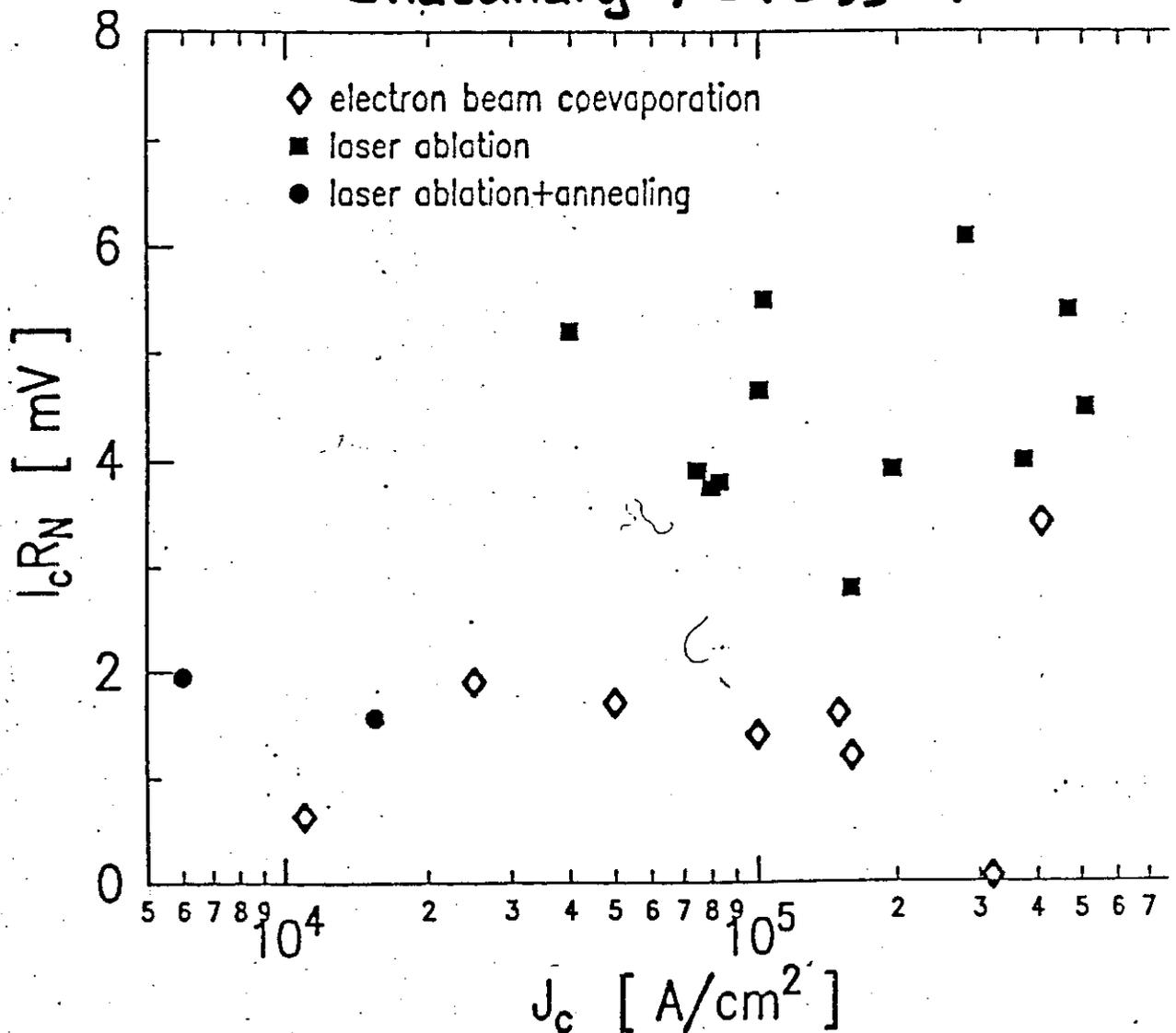


Fig. 5. I-V curve of the proximity effect bridge of BPSCCO film with 70 nm wide Al strip line after heating at 300 C for 3 min.

# Grain boundary junctions: epitaxial film on SrTiO<sub>3</sub> substrate



Chaudhary, Gross, IBM



BICRYSTAL GRAIN BOUNDARY WEAK LINKS

SrTiO<sub>3</sub>

\* D.Dimos, P. Chaudhari, J. Mannhart, and F.K. LeGoues, Phys. Rev. Lett., 61 (1988) 219.

\* R.Gross, P.Chaudhari, M.Kawasaki, M.B.Keichen, and A.Gupta, Appl.Phys.Lett., 57 (1990) 727.

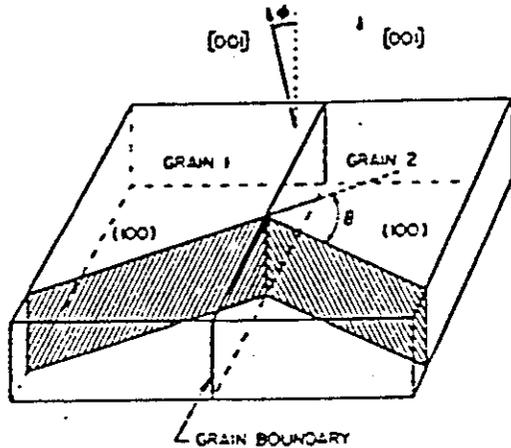


FIG. 1. Schematic diagram showing the important crystallography of the SrTiO<sub>3</sub> bicrystals which were used as substrates for the thin-film deposition.

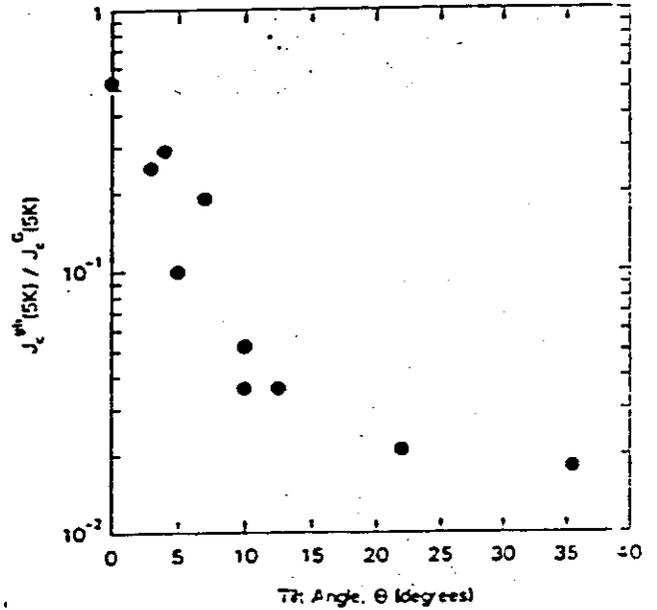


FIG. 3. Plot of the ratio of the grain-boundary critical current density to the average value of the critical current density in the two grains at 4.2-5 K vs the misorientation angle in the basal plane.

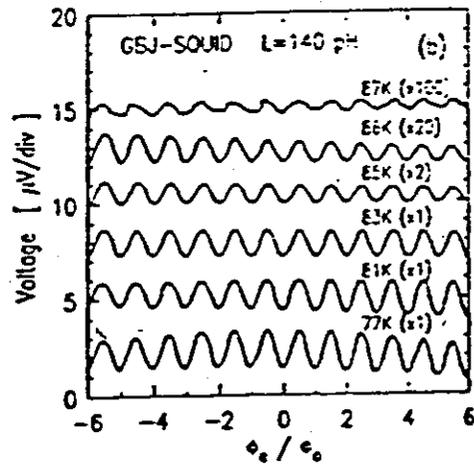
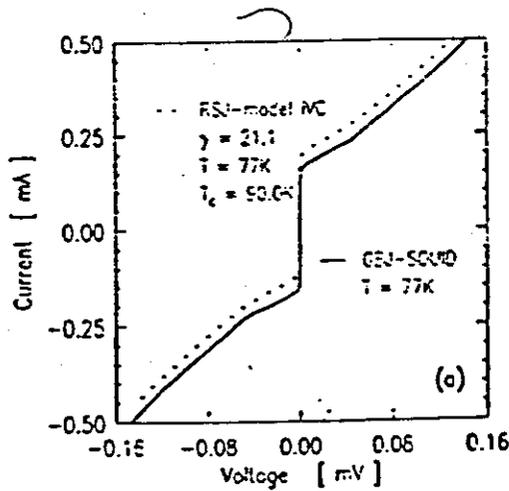


FIG. 2. Current-voltage characteristic of a GBJ SQUID at 77 K (a), and its voltage-flux characteristics for different temperatures between 77 and 87 K (b). The  $V(\Phi_e)$  curves are displaced along the voltage axis.

# VARIABLE THICKNESS BRIDGES

\* M.G. Forrester, J. Talvacchio, J.R. Gavaler, M. Rooks, J. Lindquist, IEEE Trans. Magn. MAG-27 (1991) to be publ.

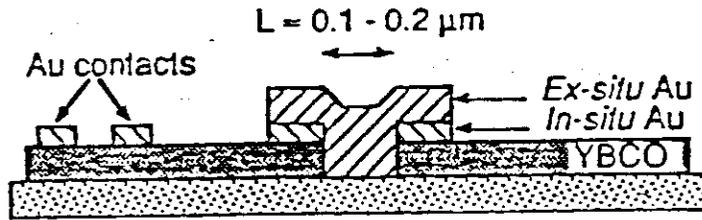


Figure 1. (a) Micrograph of a  $a = 0.1 \mu\text{m}$ -wide slot in a Au/YBCO bilayer, formed by electron-beam lithography and broad-beam ion milling. (b) Schematic diagram of completed planar junction.

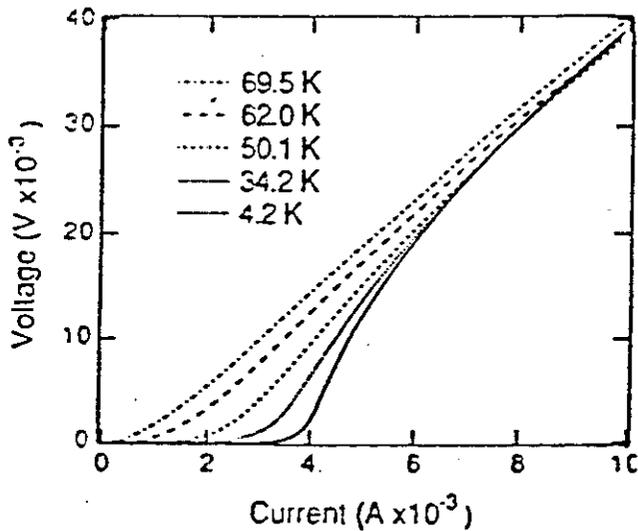


Figure 2. Current-voltage characteristics for a  $a = 0.1$  long e-beam-fabricated YBCO/Au/YBCO junction.

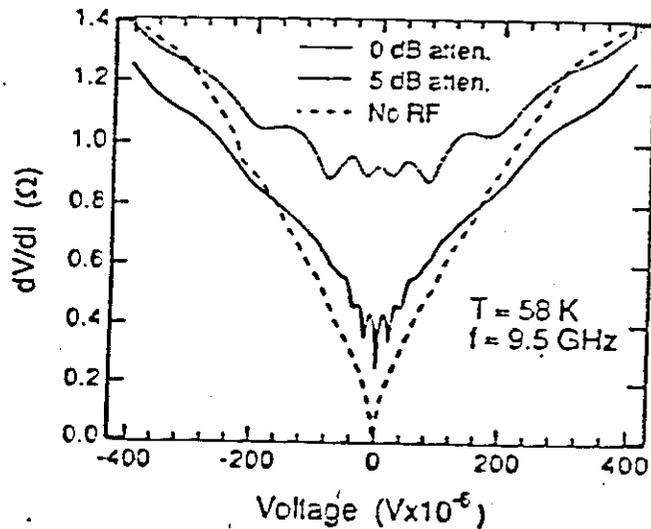
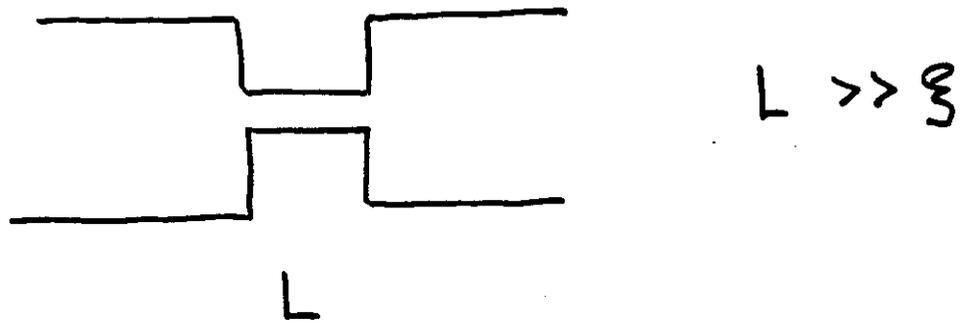


Figure 5. Differential resistance vs. voltage for the e-beam junction of Fig. 2, showing rounded Shapiro steps induced by 9.5 GHz radiation. The "0 dB" and "5 dB" curves are displaced vertically by  $0.5 \Omega$  and  $0.25 \Omega$ , respectively, for clarity.

ESA report 1990 ; CS Jacobsen

Junction microbridges



Large microbridges  $L \gg \xi$

may show behaviour somewhat similar to small (e.g. Josephson effect)

This is due to coherent vortex flow and show "shapiro steps" etc.

$\lambda$  rather than  $\xi$  sets the length scale for such behaviour

Less desirable than "real" Josephson effect but may be used in SQUIDS

Susceptible to defects, hysteresis.

HTS

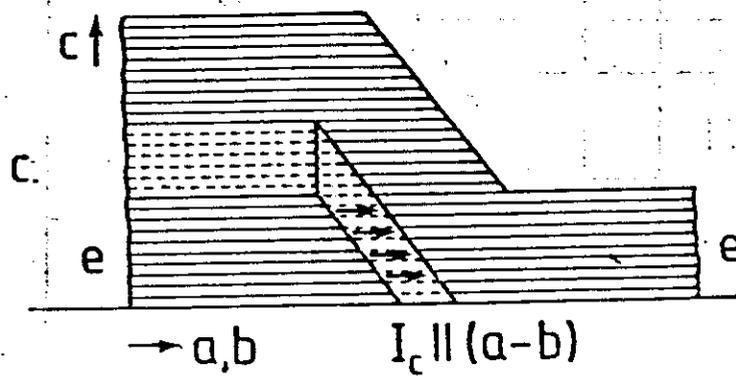
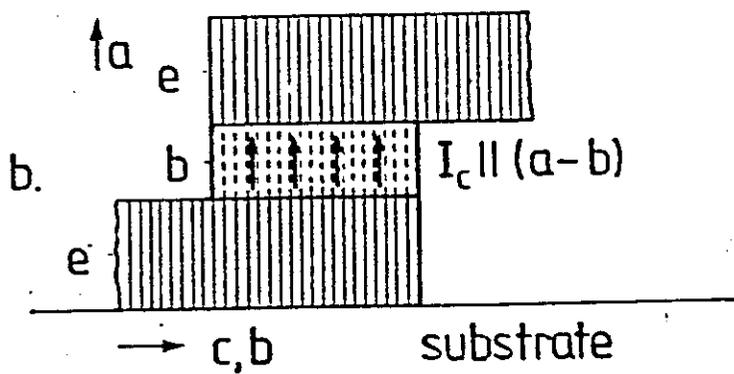
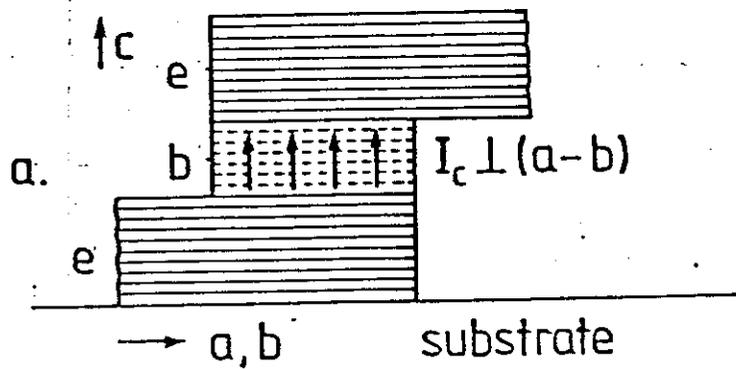
Sandwich thin film tunnel junctions ?



probably only candidate for large scale electronics

In situ fabrication

$$\xi = \begin{cases} 5 \text{ \AA} & c \\ 30 \text{ \AA} & a, b \end{cases}$$



A. Braginski 1990

\* All high  $T_c$  edge junctions and SQUIDS

R.B.Laibowitz, R.H.Koch, A.Gupta, G.Koren, W.J.Gallagher, V.Foglietti, B.Oh, and J.M.Viggiano, Appl.Phys.Lett., 57 (1990) 686.

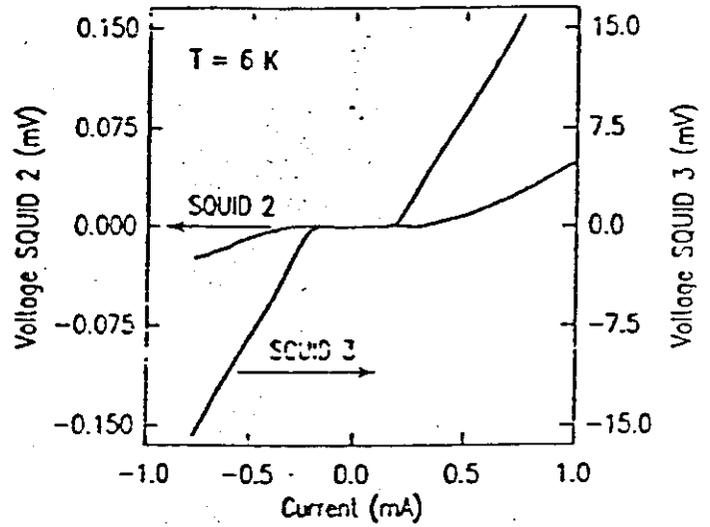
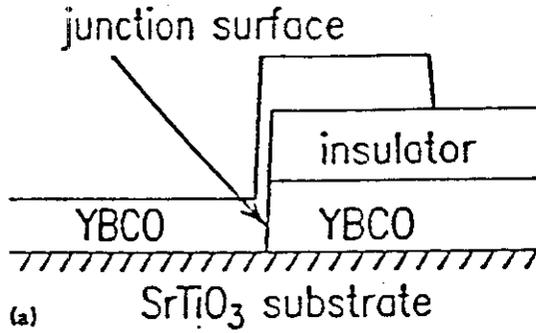
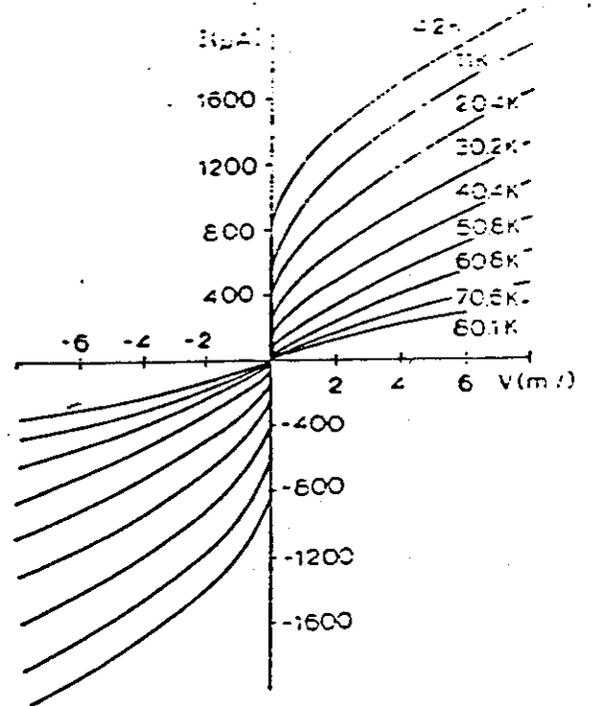
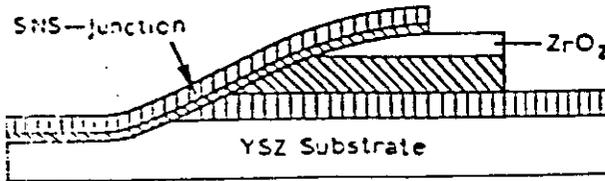
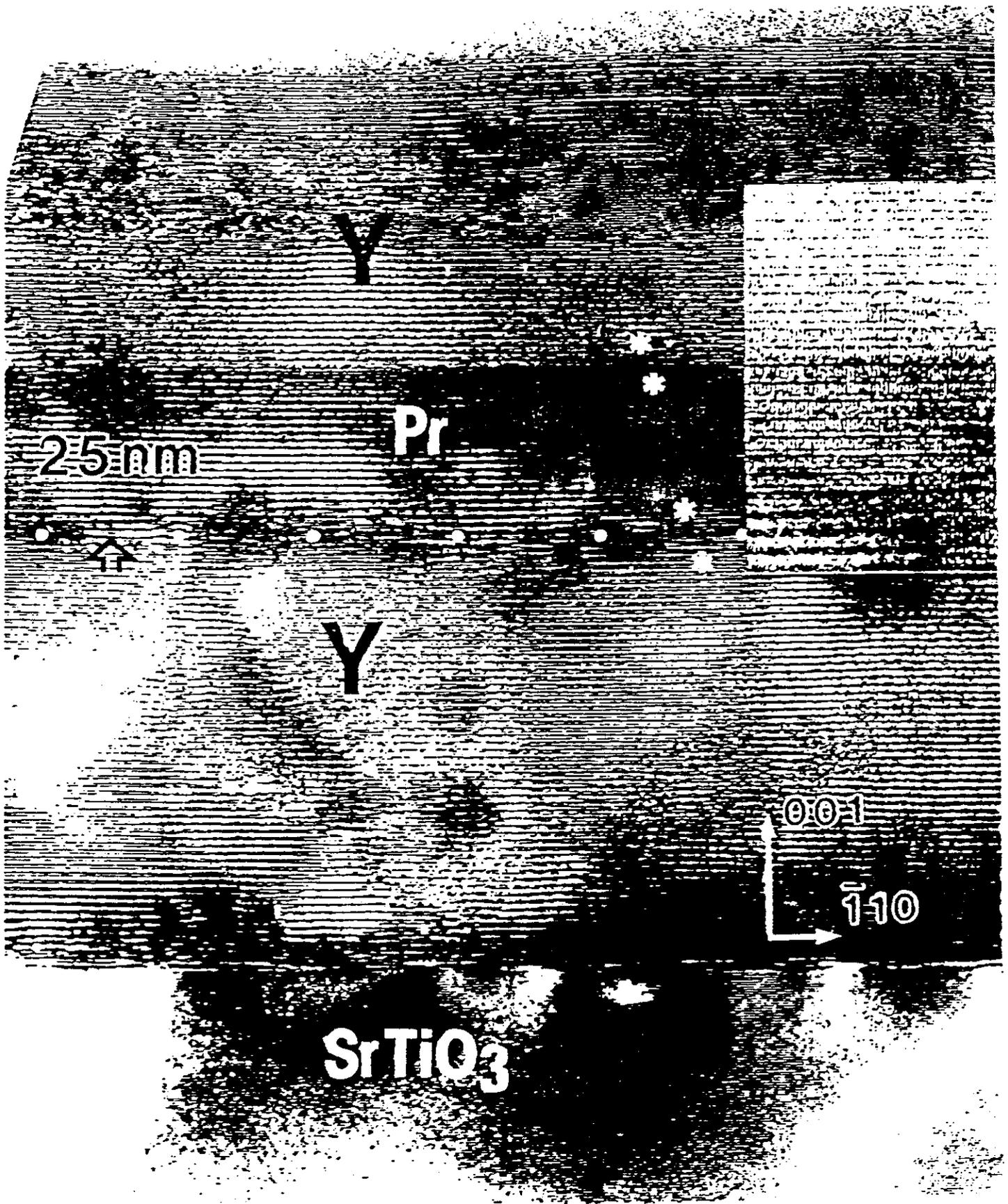


FIG. 2. Current-voltage characteristics for two SQUIDS fabricated in different runs measured at 6 K.

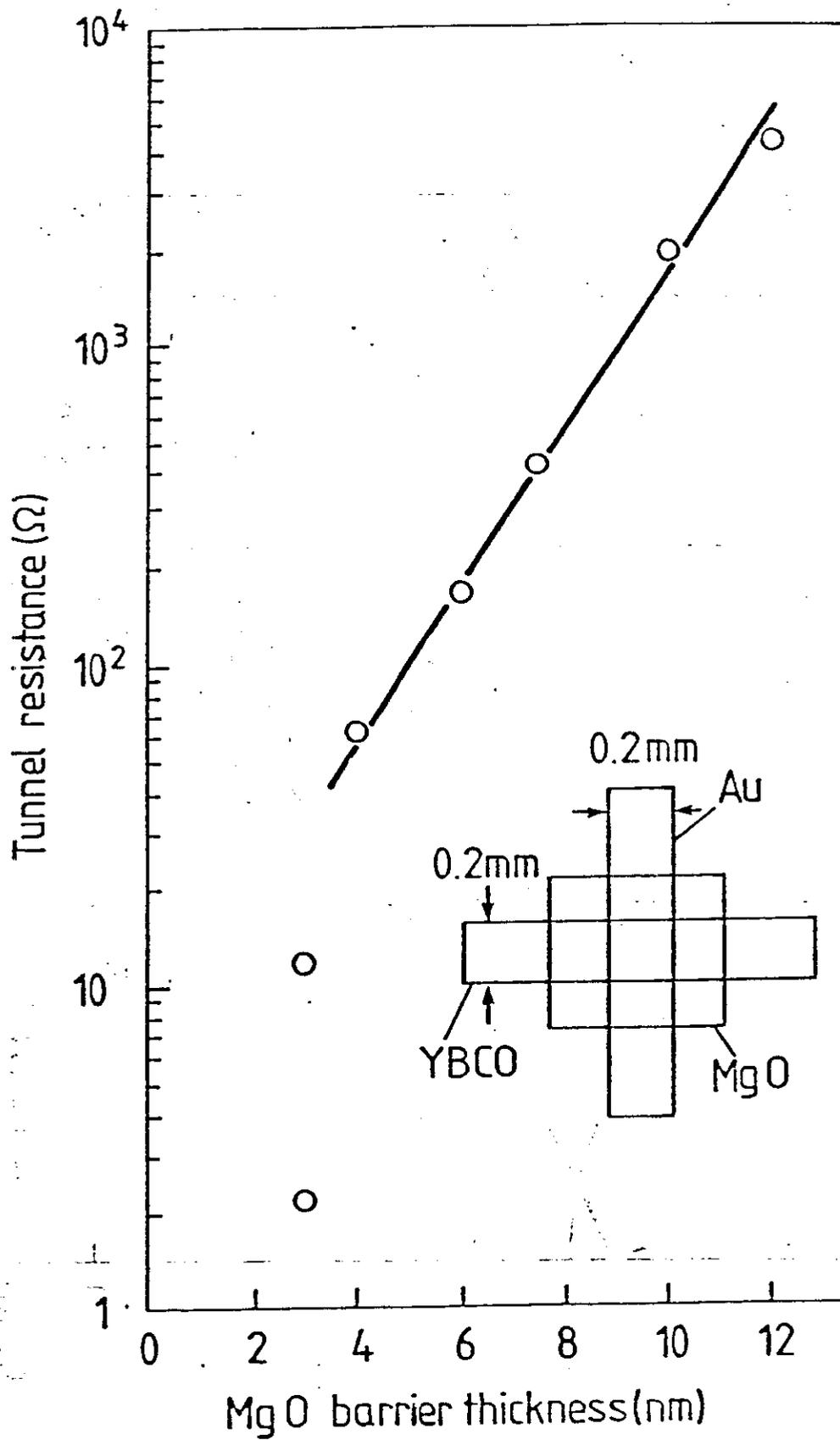
\*\* Controlled Preparation of All High- $T_c$  SNS-type Edge Junctions and Dc-SQUIDS

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