



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



INTERNATIONAL CENTRE FOR SCIENCE AND HIGH TECHNOLOGY

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SMR/543 - 16

EXPERIMENTAL WORKSHOP ON
HIGH TEMPERATURE SUPERCONDUCTORS AND RELATED MATERIALS
(BASIC ACTIVITIES)

(11 February - 1 March 1991)

" Characterization of HTS Materials by Neutron Scattering "

presented by:

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These are preliminary lecture notes, intended only for distribution to participants.

Characterization of HVS materials by Neutron Scattering.

First lecture: General remarks on Neutron Scatt.,
structures
magnetic ordering
densities of states : phonons
: magnetic excitations
role of impurities
"Do magnetic moments exist in
High T_c Superconductors?"

Second lecture: Details about magnetic
dynamics
Phonon anomalies

Experimental results from different sources:

ILL - Grenoble: Schärpf et al., Rossat-Mignod et al.

BNL - Brookhaven: Shirane et al.

Paris - Karlsruhe: Piutshovius, Reichardt,

The neutron interacts with

$$a) \text{ nuclei: } H_{Nn} \sim b \quad + b \int \vec{f} \cdot \vec{\mu}_N$$

↑ scalar
 ↑ nuclear Spin
 ↑ neutron Spin

b) magnetization densities:

$$H_{Nm} \sim \vec{m}^\perp \cdot \vec{\mu}_N$$

Interaction is weak \Rightarrow Born approx. applicable

\Rightarrow Cross section for
 momentum transfer \vec{k}
 energy transfer $\hbar\omega$

is directly proportional to

a) density-density correlation function (for nuclei)

$$\sum_{ij} \int \langle e^{i\vec{k} \cdot \vec{R}_i(0)} e^{-i\vec{k} \cdot \vec{R}_j(t)} \rangle e^{i\omega t} dt$$

\Rightarrow information about structures
 + lattice dynamics

structures: $\sim \sum \langle e^{i\vec{k}\cdot(\vec{R}_i - \vec{R}_j)} \rangle$

dynamics: $\sim \sum \int e^{i\vec{k}\cdot(\vec{R}_i - \vec{R}_j)} \langle \underset{\uparrow i}{\vec{u}_i} \cdot \underset{\uparrow j}{\vec{u}_j}(t) \rangle e^{i\omega t} dt$
displacements

\sim displacement-displacement correlation fct.
 \sim "phonons".

b) magnetization-magnetization (spin-spin) corr. fct.

$$\sim \sum \int e^{i\vec{k}\cdot(\vec{R}_i - \vec{R}_j)} \langle \vec{S}_i \cdot \vec{S}_j(t) \rangle e^{i\omega t} dt$$

\Rightarrow information about magnetic ordering
+ magnetic excitations

Separation of different correlation functions possible

- i) through indirect information + experience
- ii) polarization analysis (technically difficult,

|| Accessible wavelengths: atomic distances up to ∞

|| Accessible energy transfers: $\hbar\omega \lesssim 100 \text{ meV}$

$\sim 1000 k_B K$

- Large samples necessary!

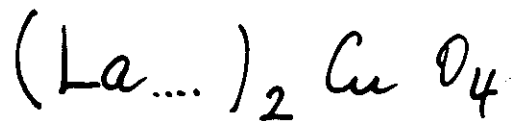
In principle we can learn everything about
lattice properties (structure + dynamics)
+ magnetic properties (order + fluctuations).

nothing about : electronic charge distributions
" polarizabilities.

In practice : Almost everything about the lattice
a lot (or not so much) about magnetism
a little bit (indirectly) about
electronic charges.

Up to now:

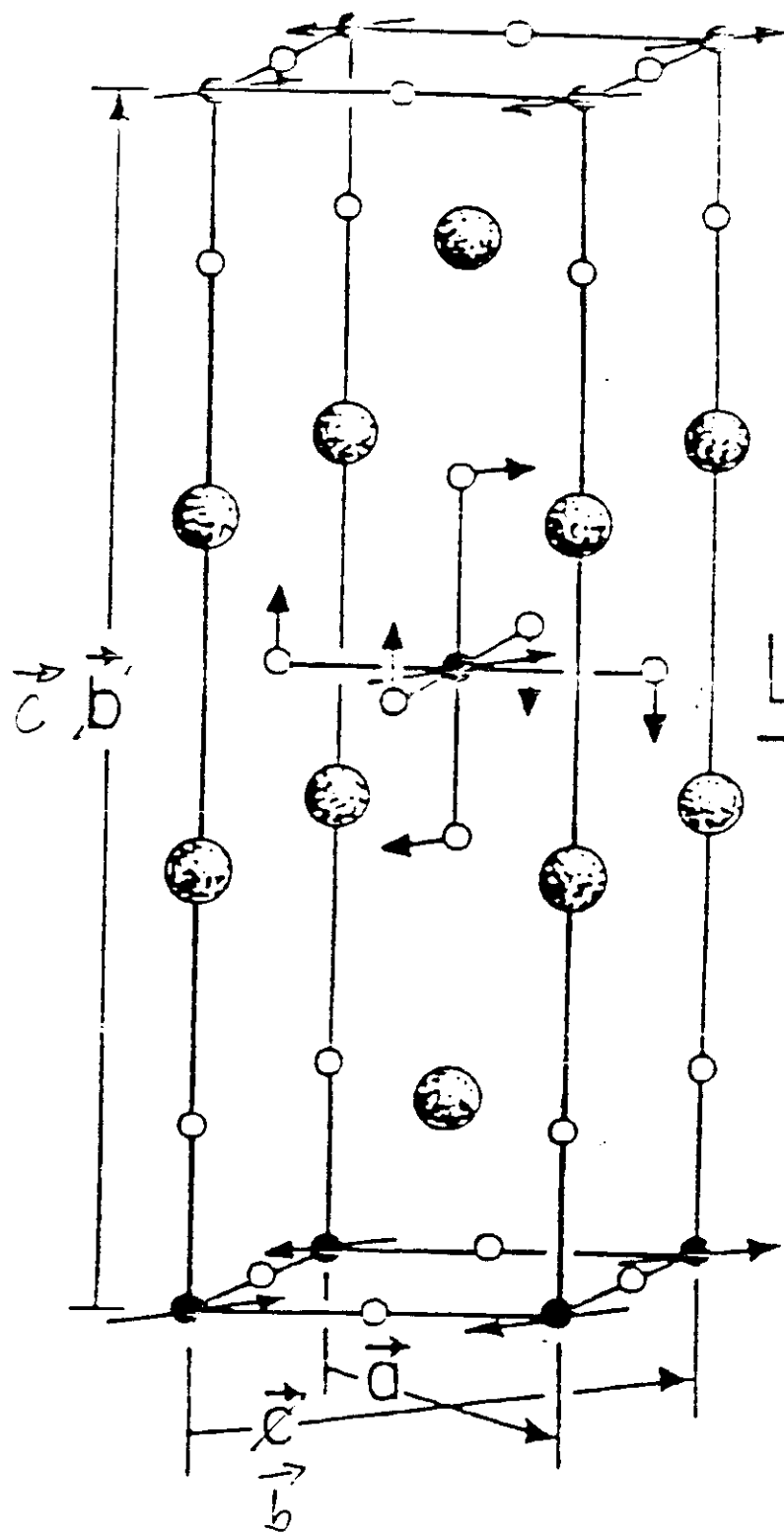
Intensive studies of magnetic properties
(BNL, ILL)



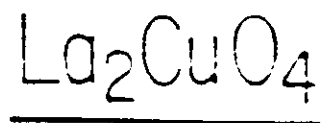
"Superconductivity because of or
despite of magnetism?"

Less attention to lattice dynamics

But: Interesting phonon anomalies
(Paris-Karlsruhe)



- Cu^{2+}
- O^{2-}
- La^{3+}



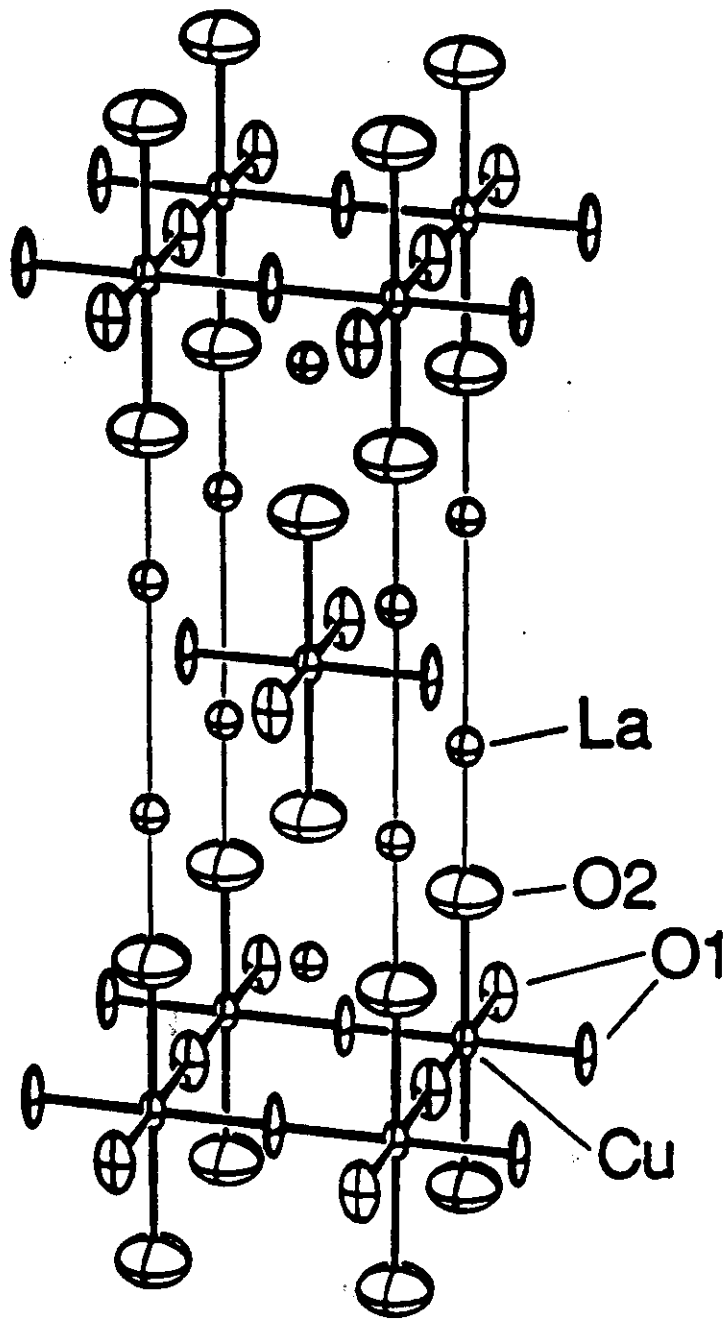
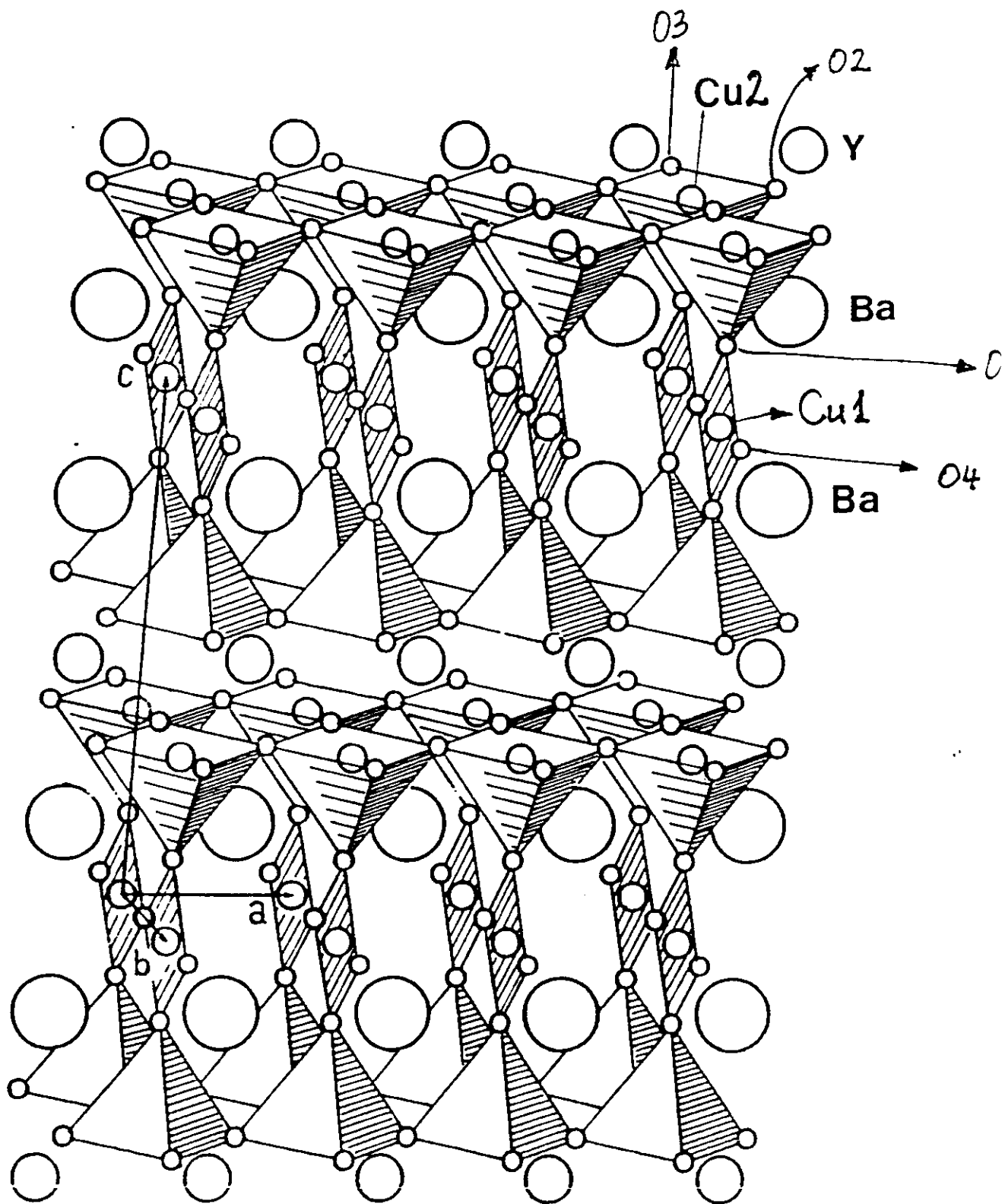
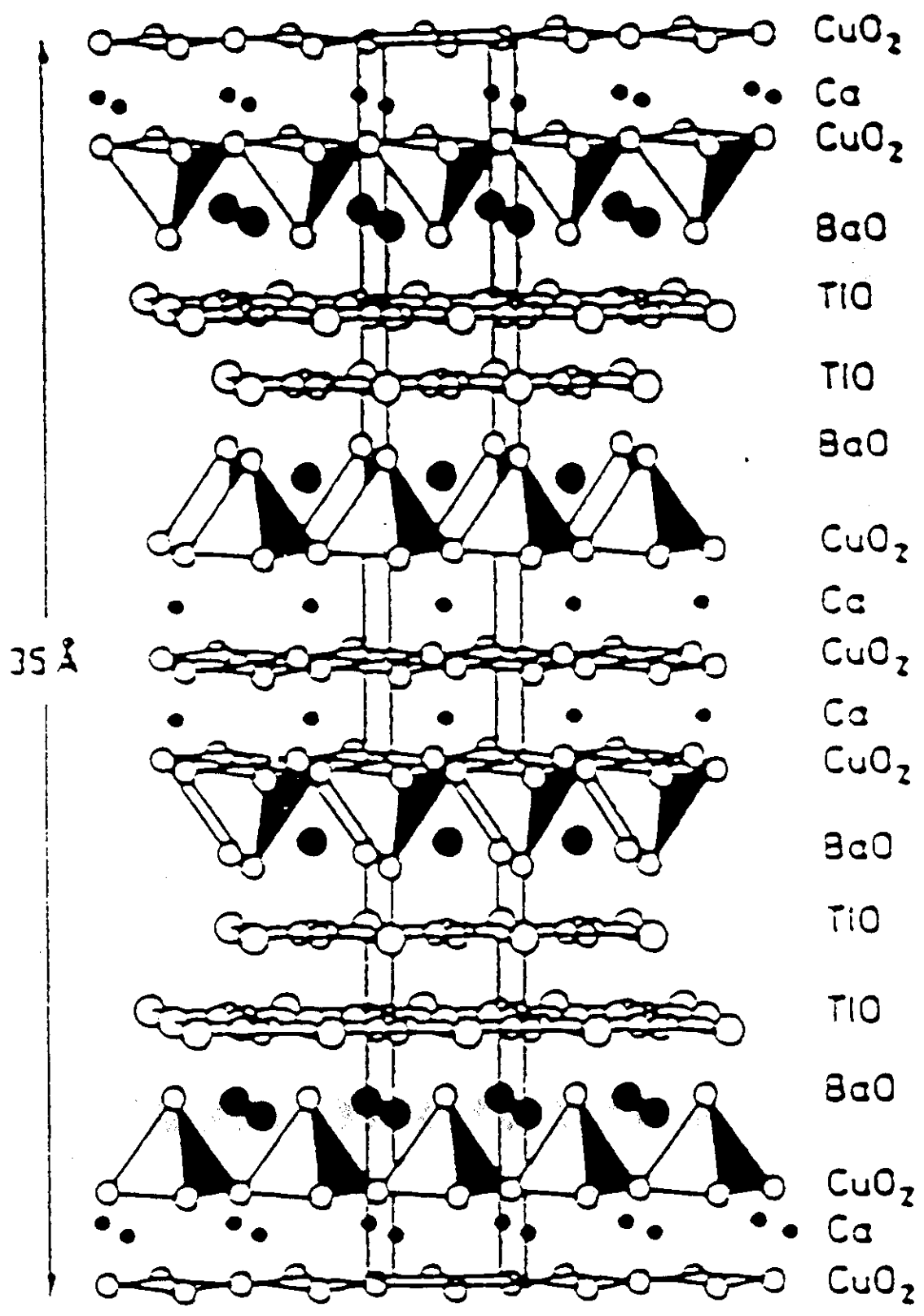


FIG. 2. The crystal structure of La_2CuO_4 , with (O1, O2) denoting the sites denoted (O_{xy} , O_z) in the text. The ellipsoids reflect the probability density resulting from neutron scattering refinements of the structure. The probability density can reflect both dynamic and quasistatic, uncorrelated displacements from the ideal sites.

that is not...



" 10 2225 ; $l_c \approx 125 \text{ \AA}$



Common elements: CuO₂ planes

+ other planes.

"Other planes" have secondary role of

a) stabilizing crystallographic structure

b) controlling electron densities
(carrier concentration) in CuO₂ planes

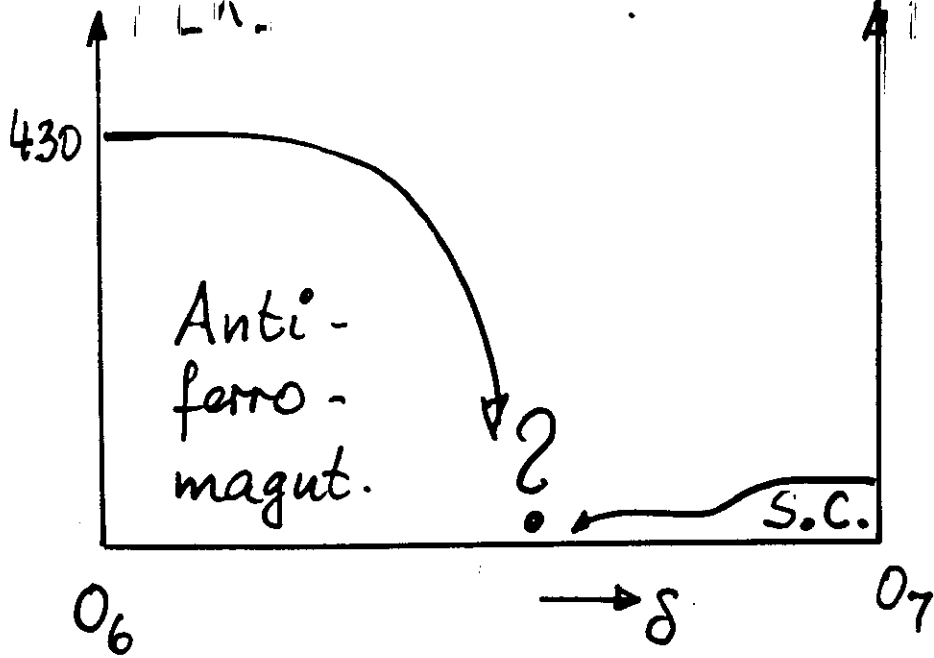
Example: Y-plane may be replaced by
3-valent rare earth (large magn.
moment) without consequences
on superconductivity.

CuO₂ - plane essential for
superconductivity, magnetism

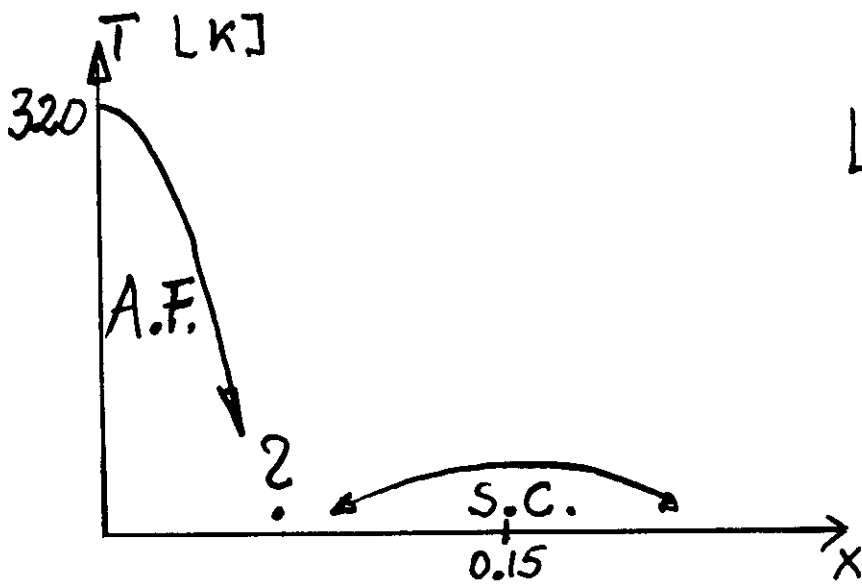
In La₂CuO₄, YBa₂Cu₃O₆ : Cu²⁺
⇒ One hole missing from full 3d-shell.

~ Spin 1/2 ; ⇒ antiferromagnetism.

"Doping" CuO₄ plane La_{2-x}Sr_xCuO₄, YBa₂Cu₃O_{6+δ}
⇒ No magnetic order but superconductivity

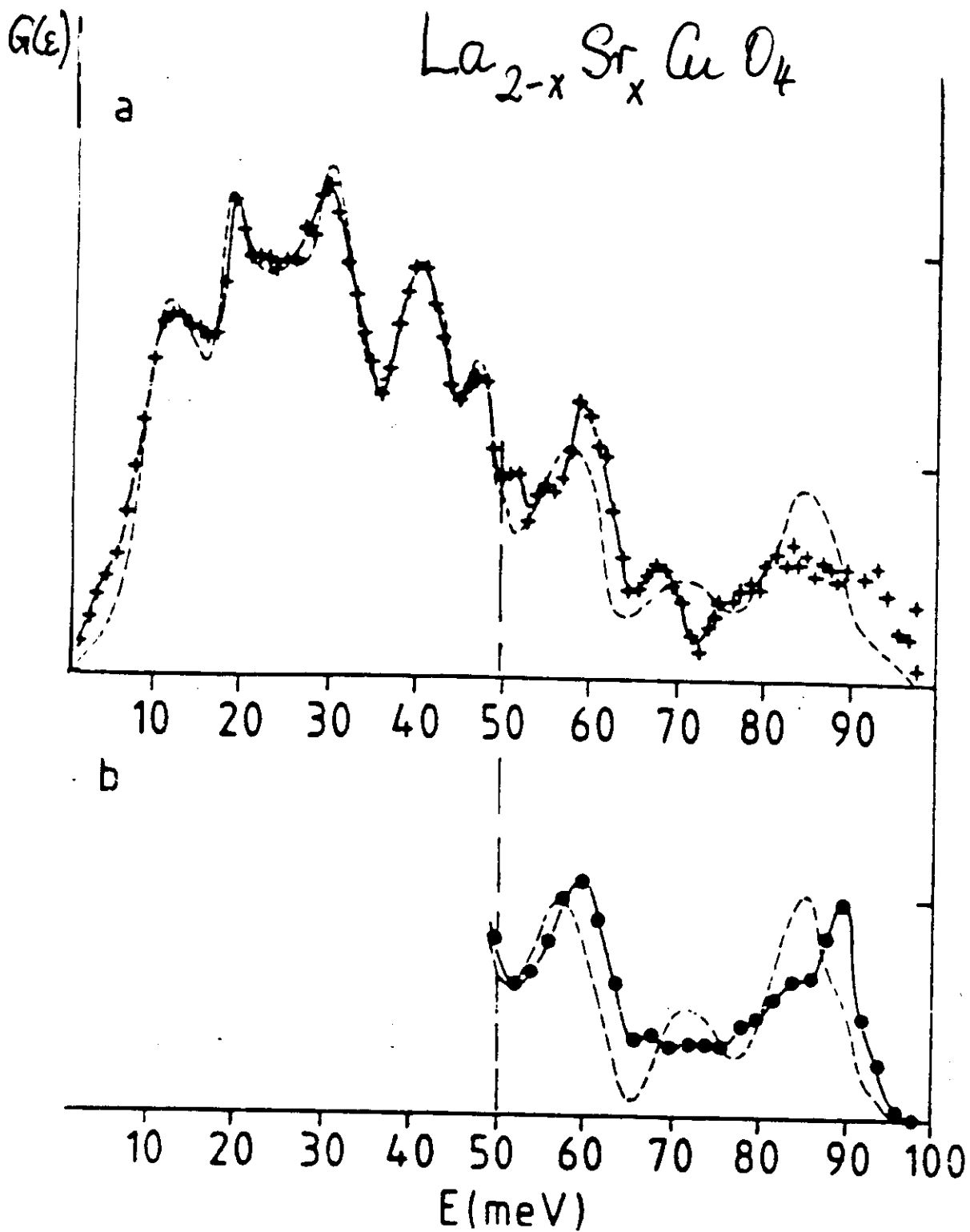


$YBa_2Cu_3O_{6+\delta}$
 $\delta \sim 0 \Rightarrow CuO_2$ plane magnetic
 $\delta \sim 1 \Rightarrow CuO_2$ planes superconducting

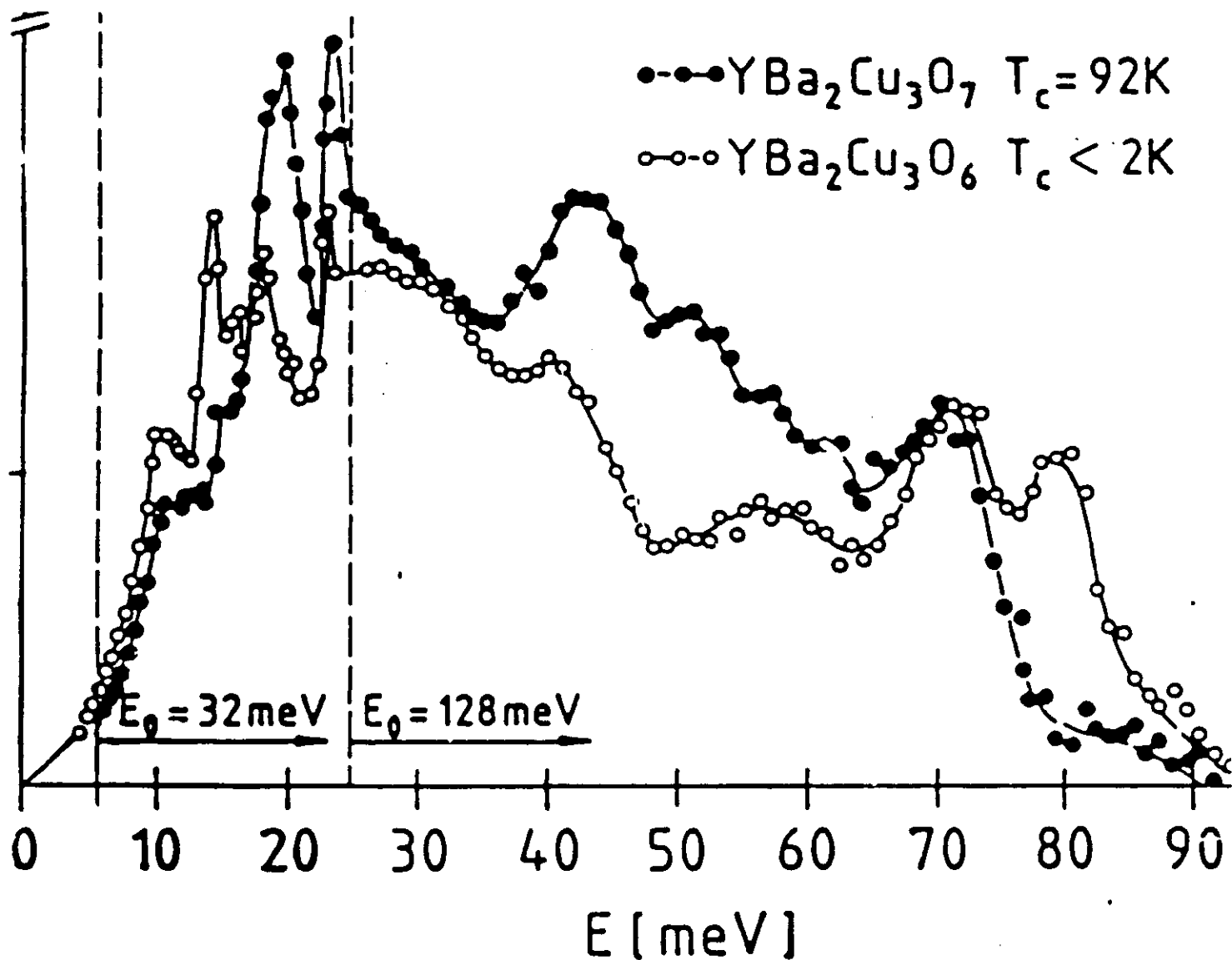


$La_{2-x}Sr_xCuO_4$
 Ba_x
 like above

Question: Magnetism disappears by
 ?
 • loss of long range order only (retaining moments + short range order)
 or
 • disappearance of local magnetic moments
 (To be discussed later).



a and **b**. Generalized phonon density of states $G(\hbar\omega)$ for La_2CuO_4 . **a** Measurement at 300 K (crosses) in energy gain of the ns. The dashed curve is the result for $\text{La}_{1.85}\text{Sr}_{0.15}\text{CuO}_4$ from **b** Measurement at 6 K with $E_0 = 128$ meV for La_2CuO_4

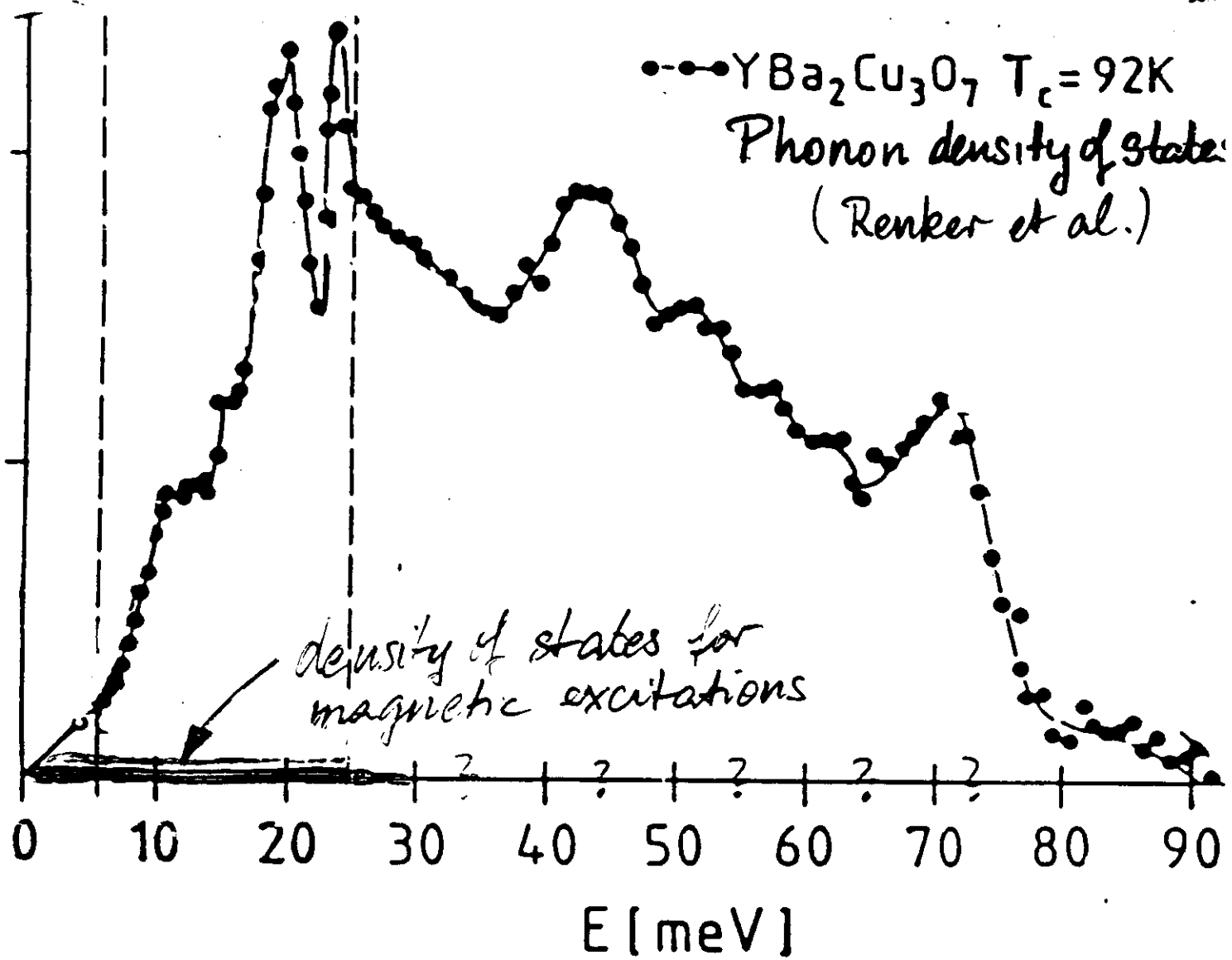


Generalized phonon density of states $G(\hbar\omega)$
 (Renker et al.)

Energy scale for phonons ~ 90 meV ~ 1000 k_B

(Typical for all High T_c materials)

High energy oxygen vibrations.



Number of magnetic degrees of freedom
 orders of magnitude smaller than lattice degree
 of freedom in energy range $< \sim 25-30$ meV.

Purely magnetic signal for general q has to
 be extracted by polarization analysis:
 Measure spin flip intensities for polarization
 in z, x, y direction ($x-y$ plane = scattering plane)

$$\Rightarrow I_{\text{magn}} \sim 2 I_{\text{SF}}^{(\vec{P} \parallel \vec{z})} - I_{\text{SF}}^{(\vec{P} \parallel \vec{x})} - I_{\text{SF}}^{(\vec{P} \parallel \vec{y})}$$

total amplitude of magnetic fluctuations
or

Do magnetic moments survive in H_Tc Supercond.?

Existence of magnetic moments requires

- separation of charge and spin-excitation spectrum
- charge excitations: high energy, $\sim eV$
- spin excitations: low energy, $\sim 10-100 meV$

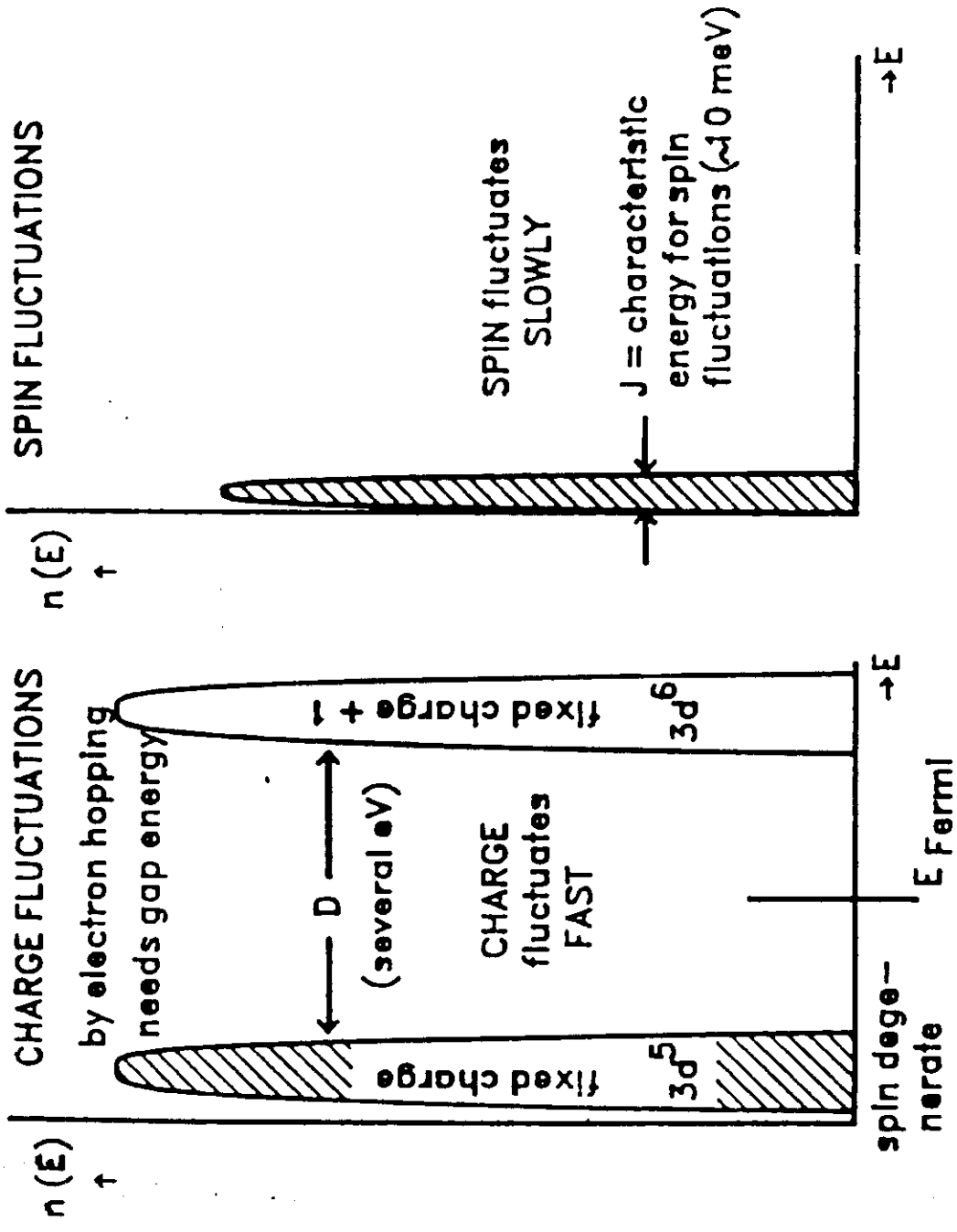
Examples: Transition metal oxides (T14)

Itinerant magnetism (Fe, Ni, Cr) (T15)

Rare earth magnetism (T16)
 $\cong HTS??$

Examples:
Transition metal
oxides

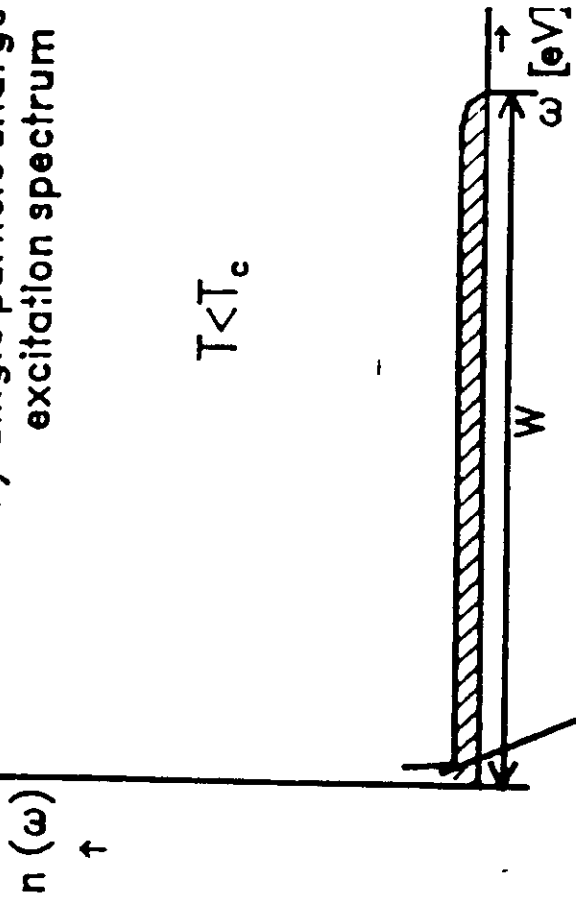
$MnO, NiO, \dots CuO$



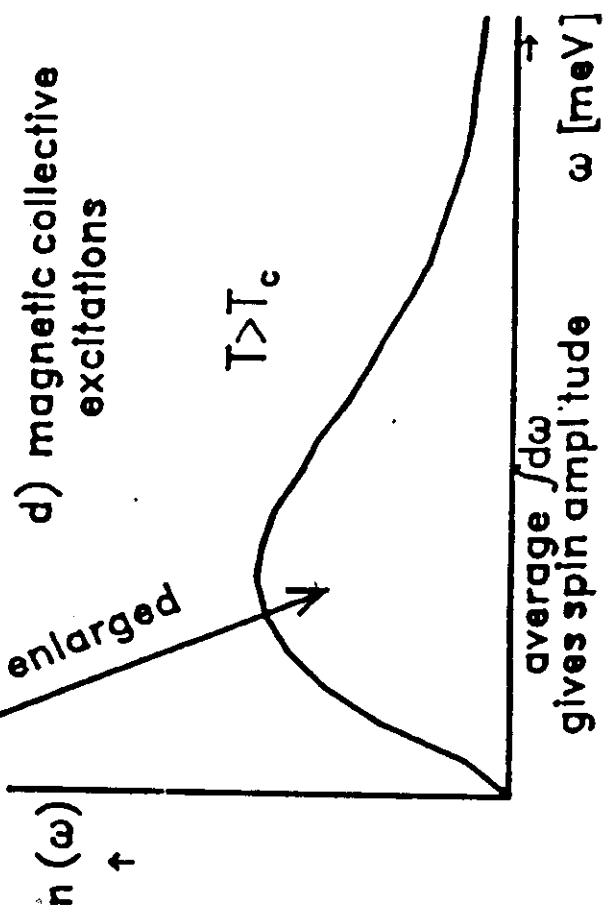
resulting spin dynamics after averaging process
 well described with constant spin amplitude and only angular freedom

plitude in magnetic insulators of the Mott type, hopping
 occurs virtually over times D^{-1} or J^{-1} respectively (as a

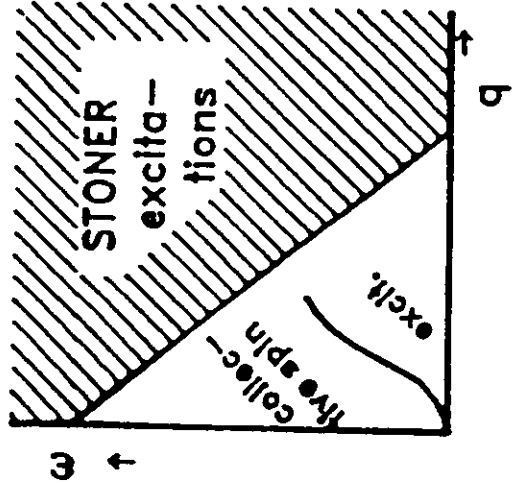
b) single particle charge excitation spectrum



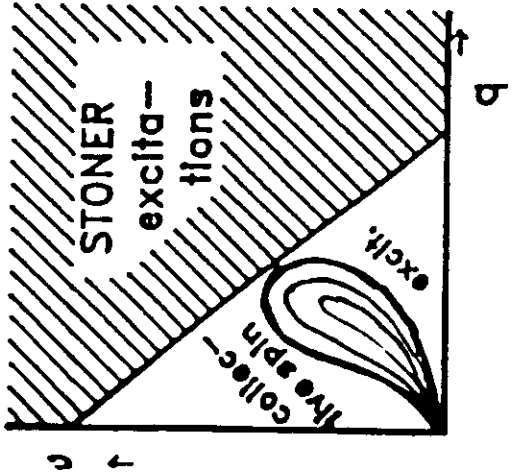
d) magnetic collective excitations



a)



c)



Examples:
 Transition meta
 Fe, Ni (ferro)
 Cr (antiferrom)
 Amplitude fluctuation possible!

Definition of amplitude in itinerant systems. Here already charge excitations are possible in the conduction band even

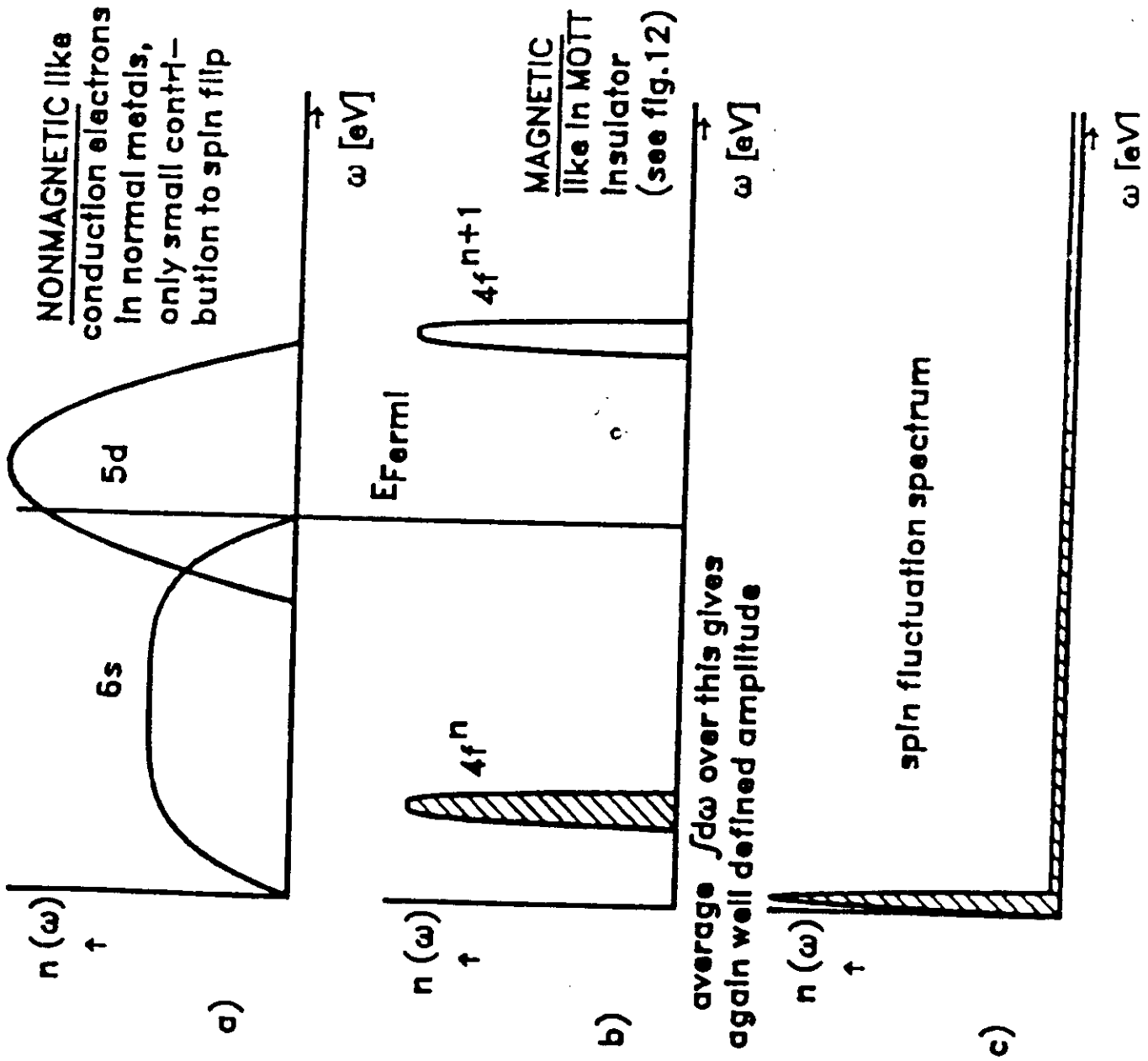
Examples:

Rare earth metals

Speculations: HTS

Oxygen electrons $\hat{=}$ non-conduction

Cu-electrons $\hat{=}$ magnetic moments



$$Y(q, \omega) \sim \sum_{ij} \int dt e^{i\omega t} e^{i\mathbf{q}(\vec{R}_i - \vec{R}_j)} \langle \vec{S}_i \cdot \vec{S}_j(t) \rangle$$

Sum rule:

$$\int_{-\infty}^{+\infty} d\omega \sum_q Y(q, \omega) \sim N \langle \vec{S}^2 \rangle = N S(S+1)$$

"Magnetic moments exist" (= are useful concept)

if $\int_{-\Omega}^{+\Omega} d\omega \sum_q Y(q, \omega)$ is sizable fraction of total intensity $N S(S+1)$ for $\Omega \ll$ charge excitation energy $\sim eV$

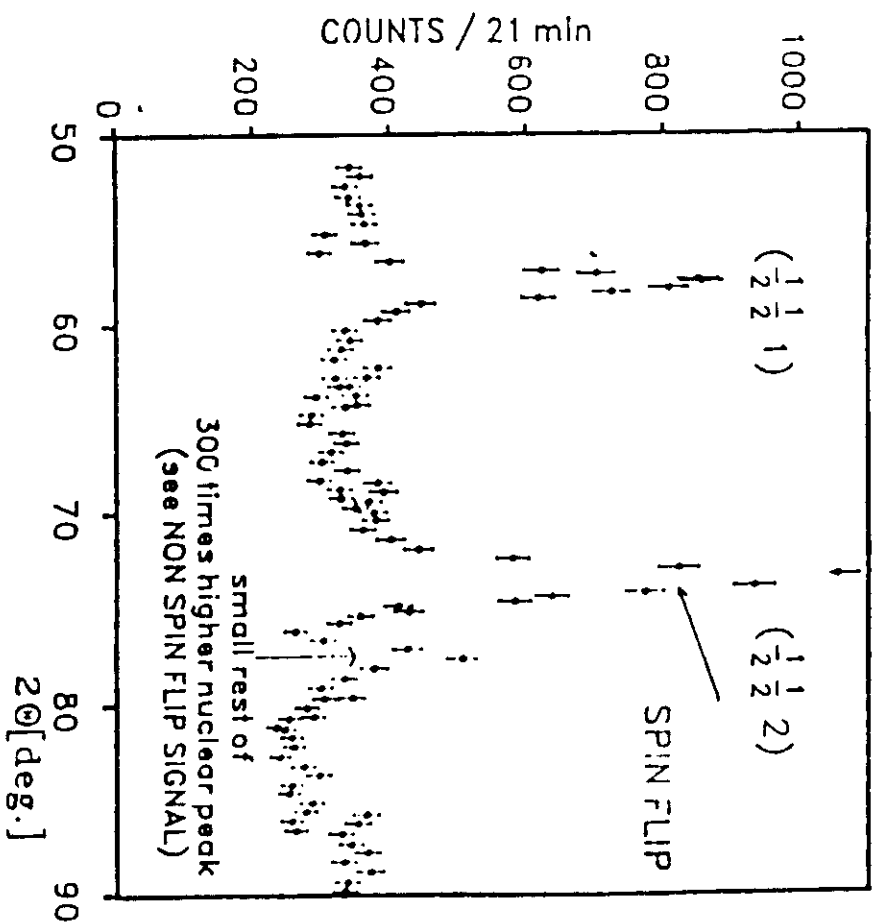
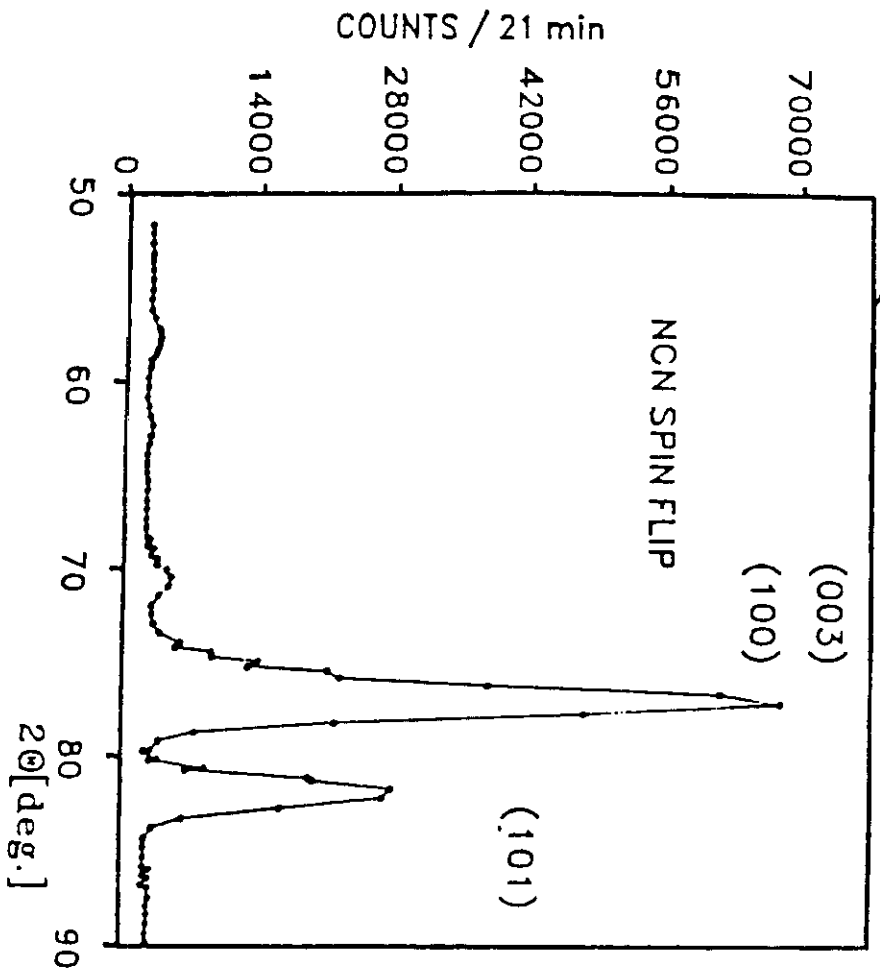
Experimentally accessible ω integration
 $\omega \lesssim 30 \text{ meV}$

Magnetic intensity is weak compared to phonon intensity.

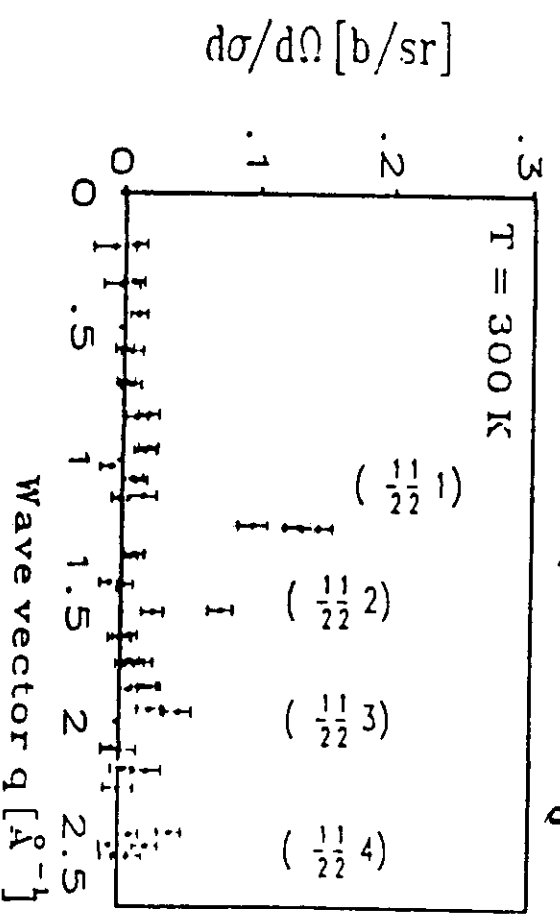
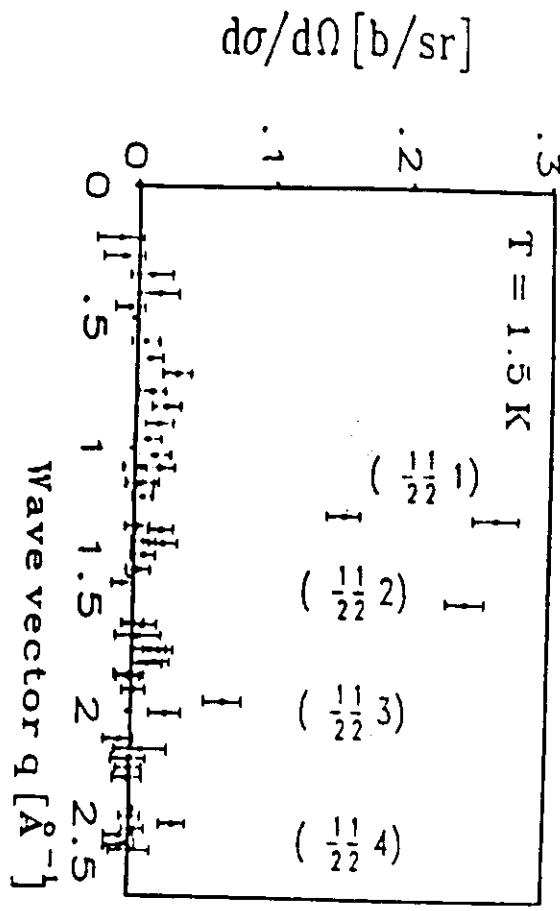
➔ Polarized neutrons + polarization analysis necessary for quantitative measurements.

YBa₂Cu₃O_{~6.1}, (sample from Philips Research Lab. Aachen.)

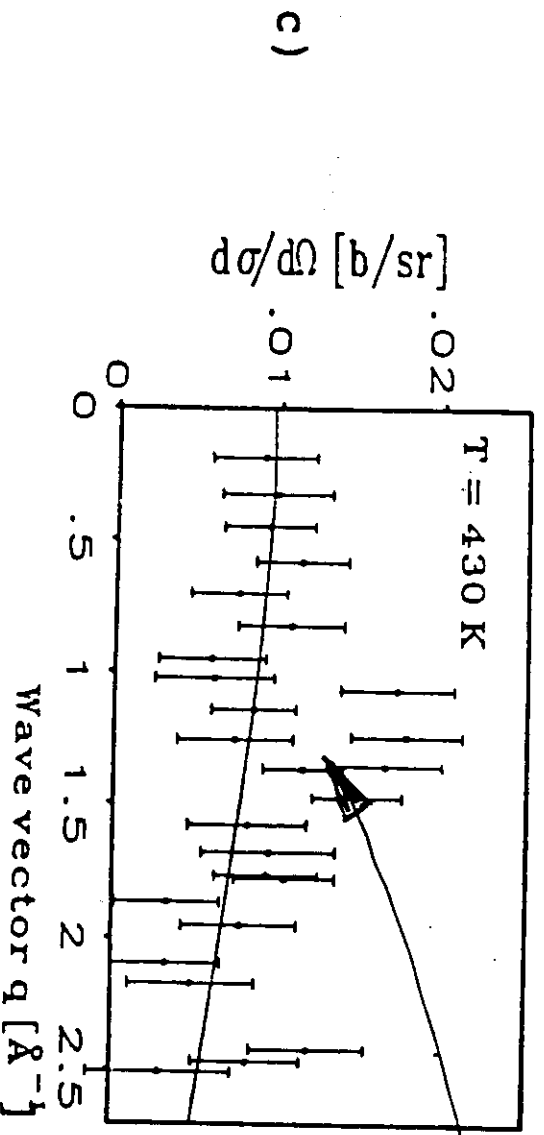
low T, antiferromagnetic order
 ordered moment ~ 0.6 - 0.7 μ_B



Energy independent magnetic response (angle averaged)

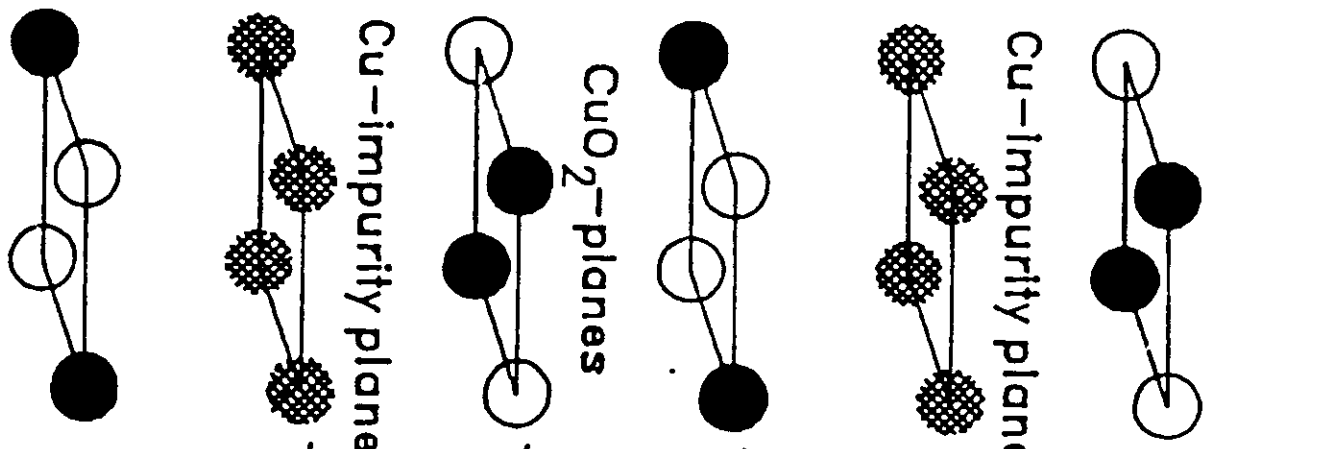


BarLus Vol. 1



Contribution of sharp magnetic ridge small!
 (Volume of ridge $\approx 10^{-3}$ x volume of Brillouin zone)

Fig. 5 Paramagnetic cross section in b/sr measured between the



contributes

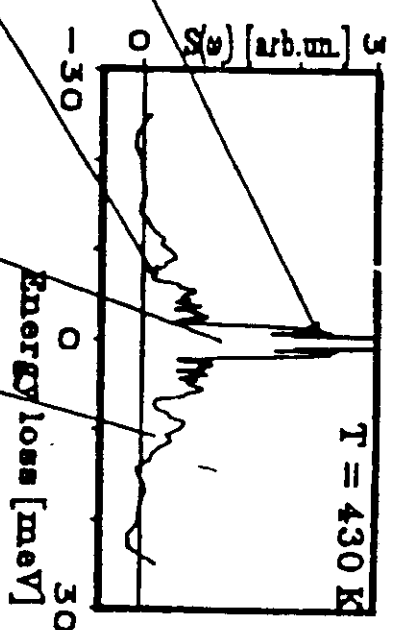
to narrow part

to wide part

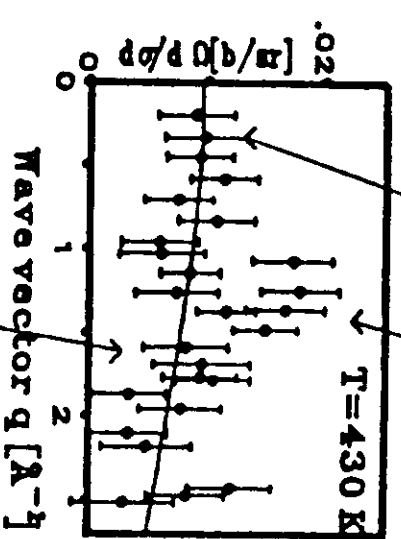
FACTOR 5 DISCREPANCY

order (0.55 μ B)

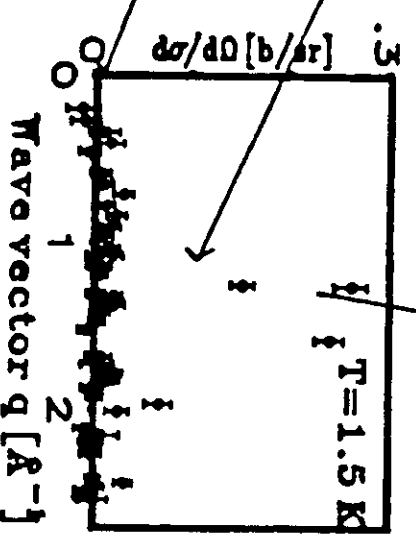
no order (0.065 b)



gives 0.065 b + 0.053 b



should give 0.065 + 0.27 b



Y Barcus Vol. 1
 $\int dt \text{rot} \langle \vec{S}_i \cdot \vec{S}_j(t) \rangle$

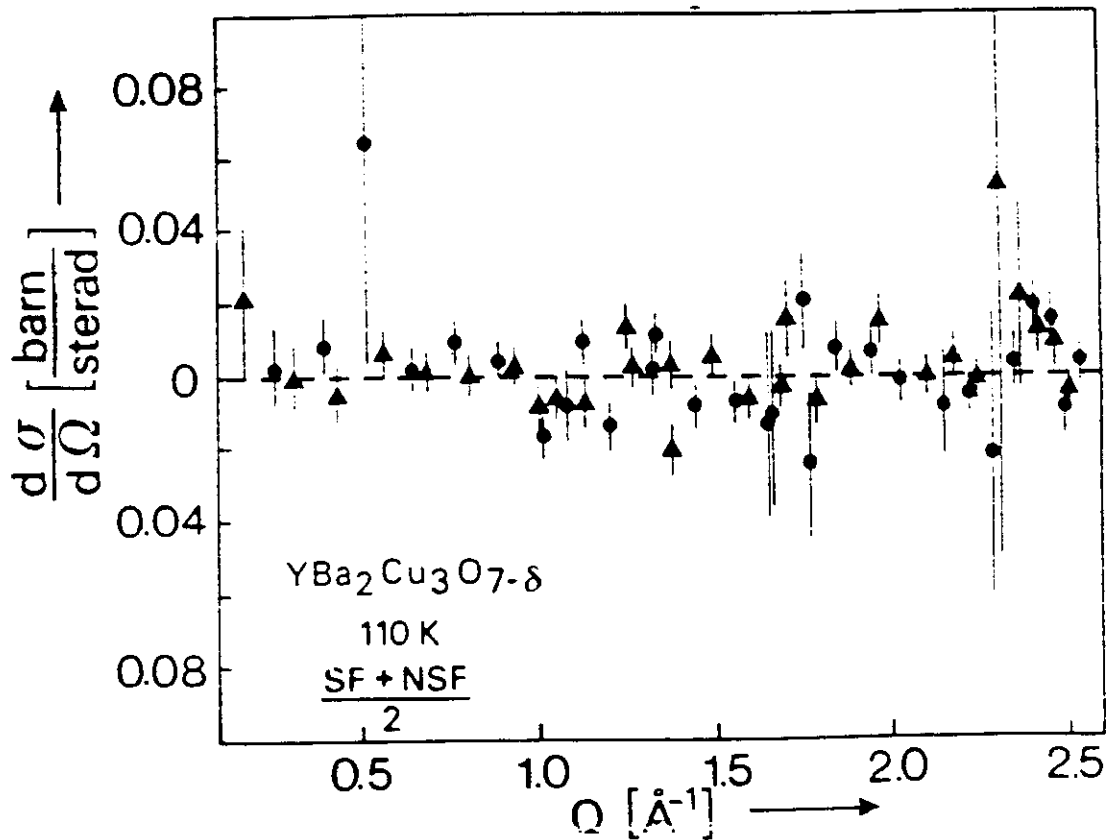
above T_N

below T_N

Results: χ $\text{Ba}_2\text{Cu}_3\text{O}_{6.9}$

$I_{\text{exp}} = 0$: No magnetism!

Error bar?



Compare to intensity of Cu - spins $\frac{1}{2}$
in energy window Ω . (What percentage
of Cu - atoms can carry a spin within
the energy window Ω ?)

$T = 110 \text{ K} : N_{\text{Cu}}(s=\frac{1}{2}; \Omega=12 \text{ meV}) < 1\%$

$T = 300 \text{ K} : N_{\text{Cu}}(s=\frac{1}{2}; \Omega=25 \text{ meV}) < 2.5\%$

total intensity of magnetic fluctuations
in energy range $\hbar\omega < 30 \text{ meV}$
is extremely small in $\text{YBa}_2\text{Cu}_3\text{O}_{6.92}$!
 $I(< 30 \text{ meV}) < 2.5\%$ of $N S(S+1)$ for $S=1/2$.

Higher energy excitations? Yes, because of
sum rule.

But: For $\hbar\omega_{\text{magn}} \sim \hbar\omega_{\text{charge}} \sim \text{eV}$

"magnetic moments" no useful concept.

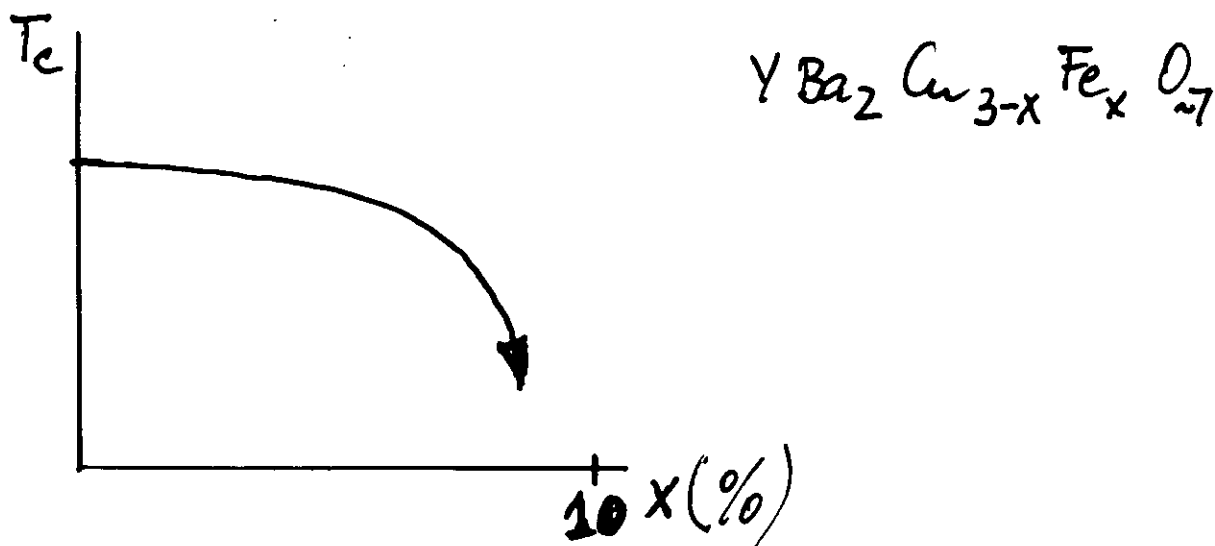
"No magnetic moments" but
electrons with charge and spin.

CuO_2 planes are magnetic for $\text{YBa}_2\text{Cu}_3\text{O}_{6.1}$,
but have no well defined magnetic
moments for superconducting $\text{YBa}_2\text{Cu}_3\text{O}_7$.

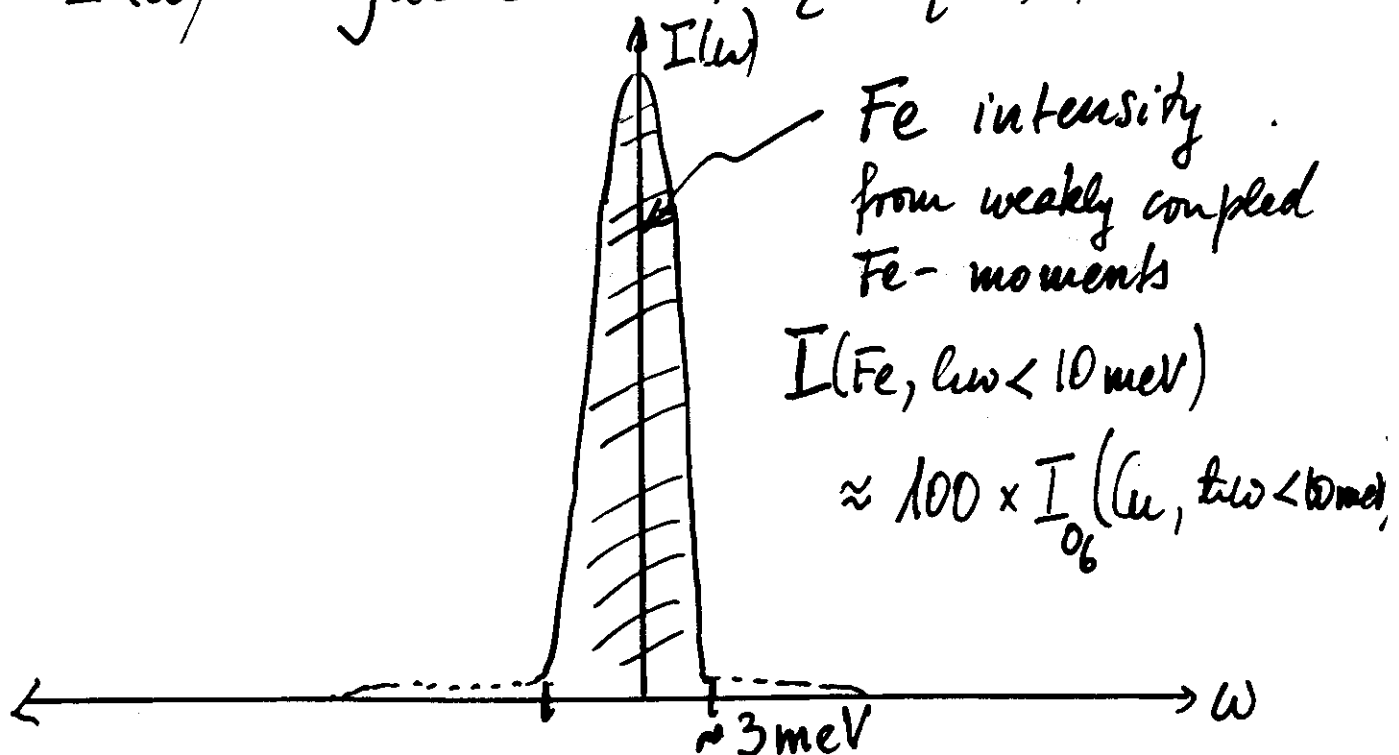
Fe has "large" magnetic moment ($S = 2$, or $5/2$).

Total intensity $\sim S(S+1)$

$$I_{\text{tot}}(\text{Fe}) \gg I_{\text{tot}}(\text{Cu})$$



$$I(\omega) = \int dt e^{i\omega t} \langle \vec{S}_i \cdot \vec{S}_i(t) \rangle$$

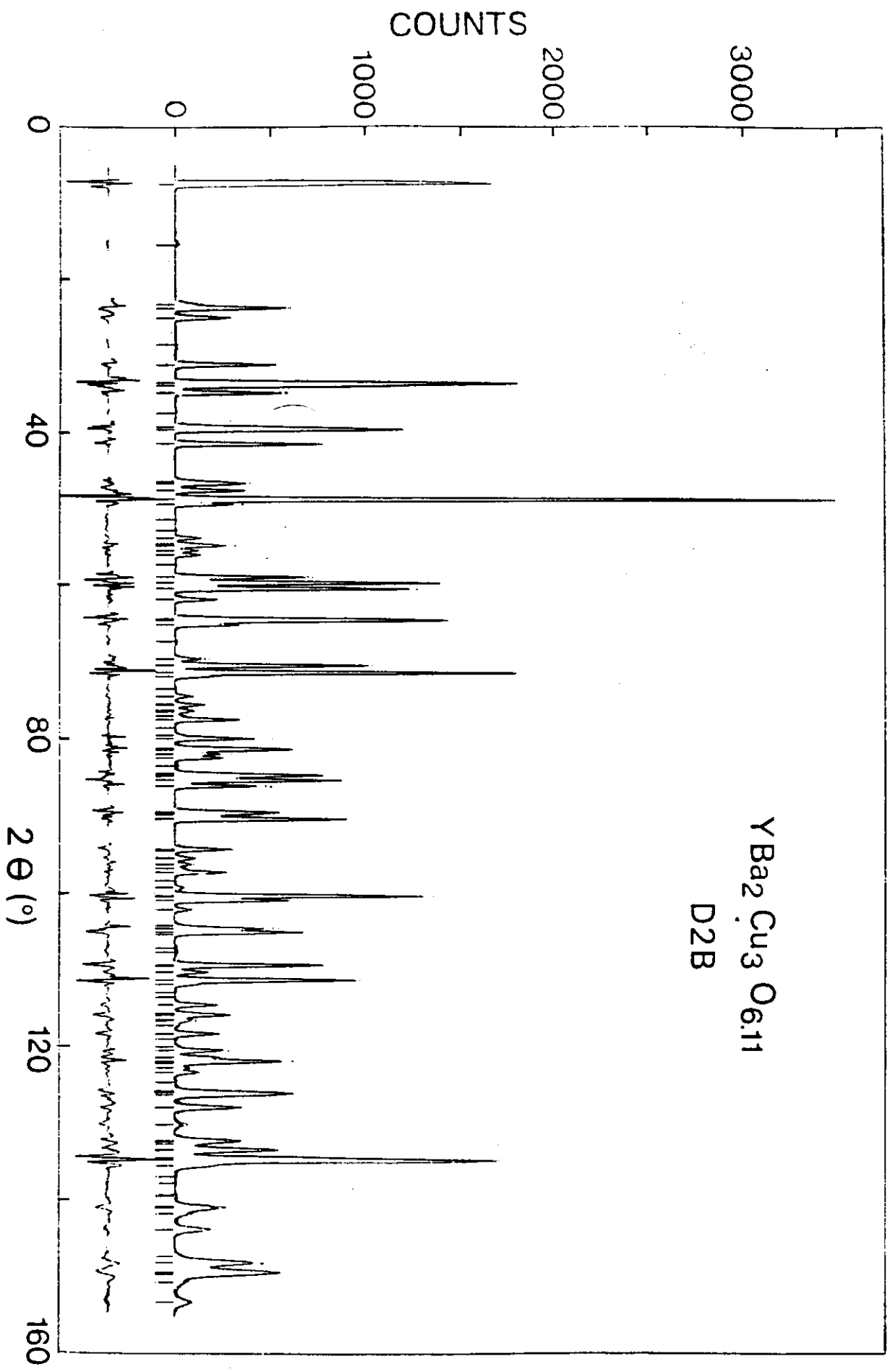


intermediate concentrations



Cu-moments in chains are "weakly coupled impurity moments".

Total intensity of magnetic fluctuations in chains (impurity) for $\hbar\omega < 10$ meV is large compared to total intensity of CuO_2 planes!



$\text{YBa}_2\text{Cu}_3\text{O}_{6.11}$

D2B