



INTERNATIONAL ATOMIC ENERGY AGENCY  
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
**INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS**  
I.C.T.P., P.O. BOX 586, 34100 TRIESTE, ITALY, CABLE CENTRATOM TRIESTE



UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



**INTERNATIONAL CENTRE FOR SCIENCE AND HIGH TECHNOLOGY**

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SMR/543 - 18

EXPERIMENTAL WORKSHOP ON  
HIGH TEMPERATURE SUPERCONDUCTORS AND RELATED MATERIALS  
(BASIC ACTIVITIES)

(11 February - 1 March 1991)

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" Optical Properties of High  $T_C$  Superconductors "

presented by:

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These are preliminary lecture notes, intended only for distribution to participants.



# OUTLINE

## TALK 1

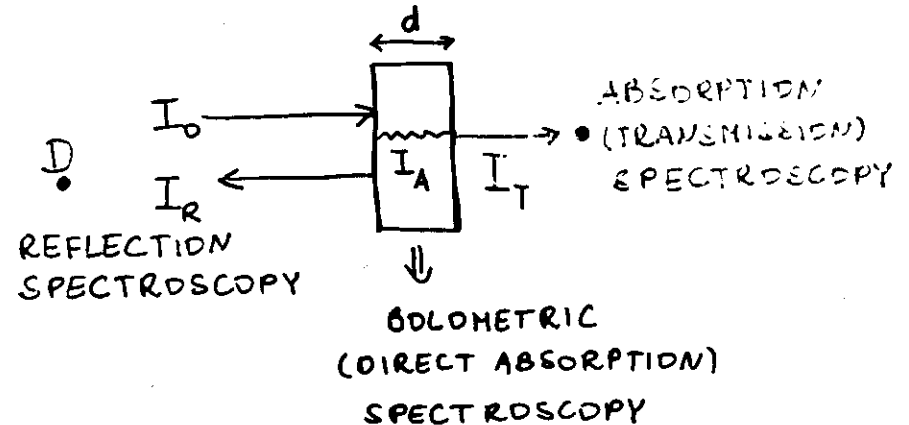
MEASUREMENT AND EVALUATION  
FUNDAMENTALS

LOW- $T_c$  SYSTEMS

NORMAL-STATE OPTICAL PROPERTIES  
OF HIGH- $T_c$  SYSTEMS

## TALK 2

SUPERCONDUCTING STATE OF HTSC  
E-PH COUPLING EFFECTS



$$I_0 = I_R + I_A + I_T$$

$$I_R = R \cdot I_0$$

$$I_A = I_0(1-R)e^{-\alpha d}$$

$$R = \frac{(n-1)^2 + k^2}{(n+1)^2 + k^2}$$

$$\alpha = \frac{4\pi k}{\lambda}$$

$$\bar{N} = n + ik = \sqrt{\epsilon}$$

# OPTICAL CONSTANTS

$$\hat{n} = \hat{\epsilon} = \epsilon_1 + i\epsilon_2 \quad \hat{n} = n + ik \quad \hat{\sigma} = \sigma_1 + i\sigma_2$$

$$\epsilon_1 = n^2 - k^2 = 1 - \frac{4\pi\sigma_2}{\omega}$$

$$\epsilon_2 = 2nk = \frac{4\pi\sigma_1}{\omega}$$

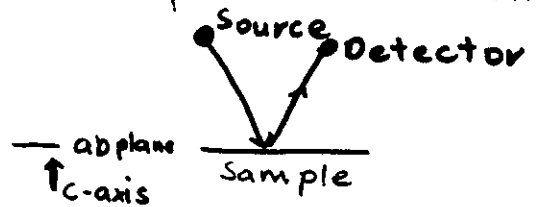
$$R = \frac{(n-1)^2 + k^2}{(n+1)^2 + k^2} = \left| \frac{1 - \sqrt{\epsilon}}{1 + \sqrt{\epsilon}} \right|^2$$

R →  $\epsilon_1, \sigma_1$  via Kramers-Kronig analysis:

$$\Theta(\omega) = \frac{\omega}{\pi} P \int_0^\infty \frac{\ln R(\omega') - \ln R(\omega)}{\omega^2 - \omega'^2} d\omega'$$

$$\tilde{n} = n + ik = \left( \epsilon_1 + i \frac{4\pi}{\omega} \sigma_1 \right)^{1/2} = \frac{1 + \sqrt{R} e^{i\theta}}{1 - \sqrt{R} e^{i\theta}}$$

Reflectivity measurements:



- home-made FIR spectrometer (McMaster)

40 - 1000  $\text{cm}^{-1}$

- BRUKER FTIR

100 - 3000  $\text{cm}^{-1}$

- PE grating spectrometer 1000 - 45000  $\text{cm}^{-1}$

- metal overcoating - normalize, correct for surface

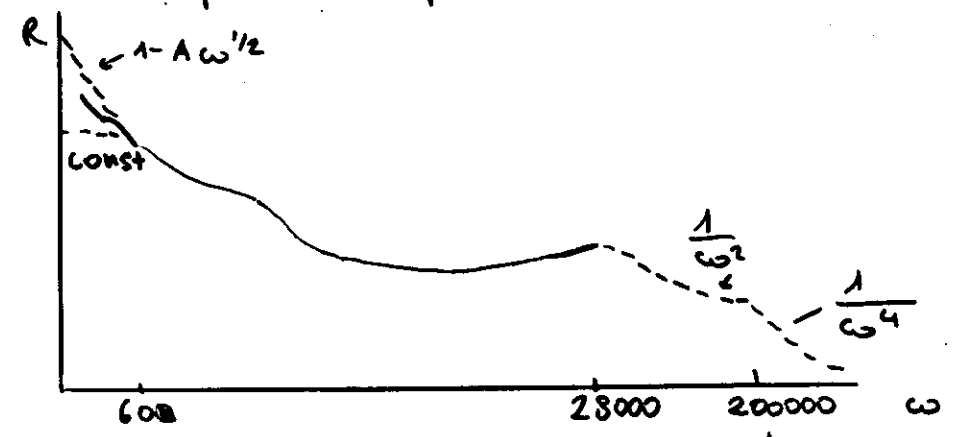
Kramers-Kronig analysis of reflectance:

$$\Theta(\omega) = \frac{\omega}{\pi} P \int_0^\infty \frac{\ln R(\omega') - \ln R(\omega)}{\omega^2 - \omega'^2} d\omega'$$

Then

$$N = n + ik = \left( \epsilon_1 + i \frac{4\pi}{\omega} \sigma_1 \right)^{1/2} = \frac{1 + \sqrt{R} e^{i\theta}}{1 - \sqrt{R} e^{i\theta}}$$

Extrapolation procedure:



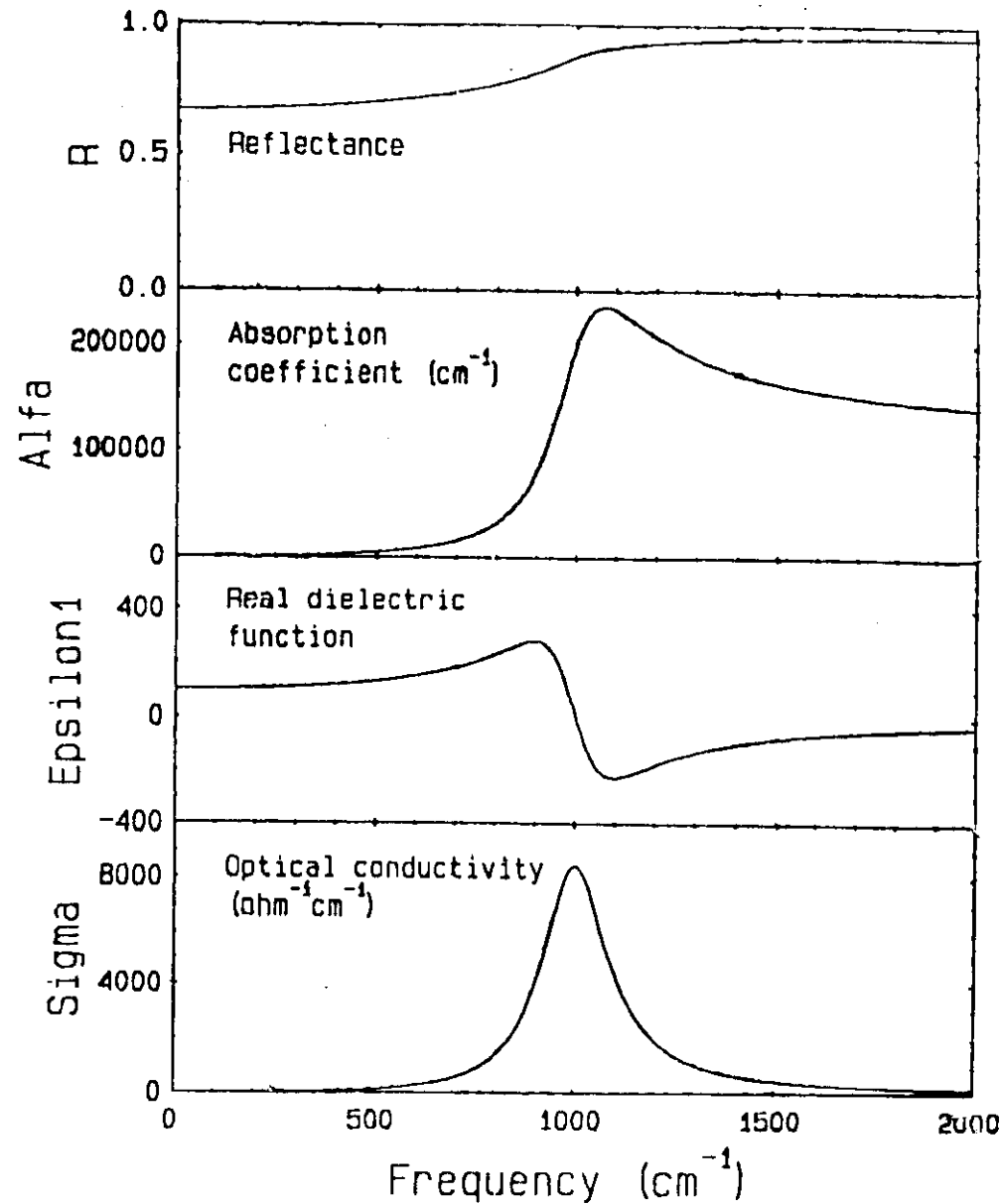
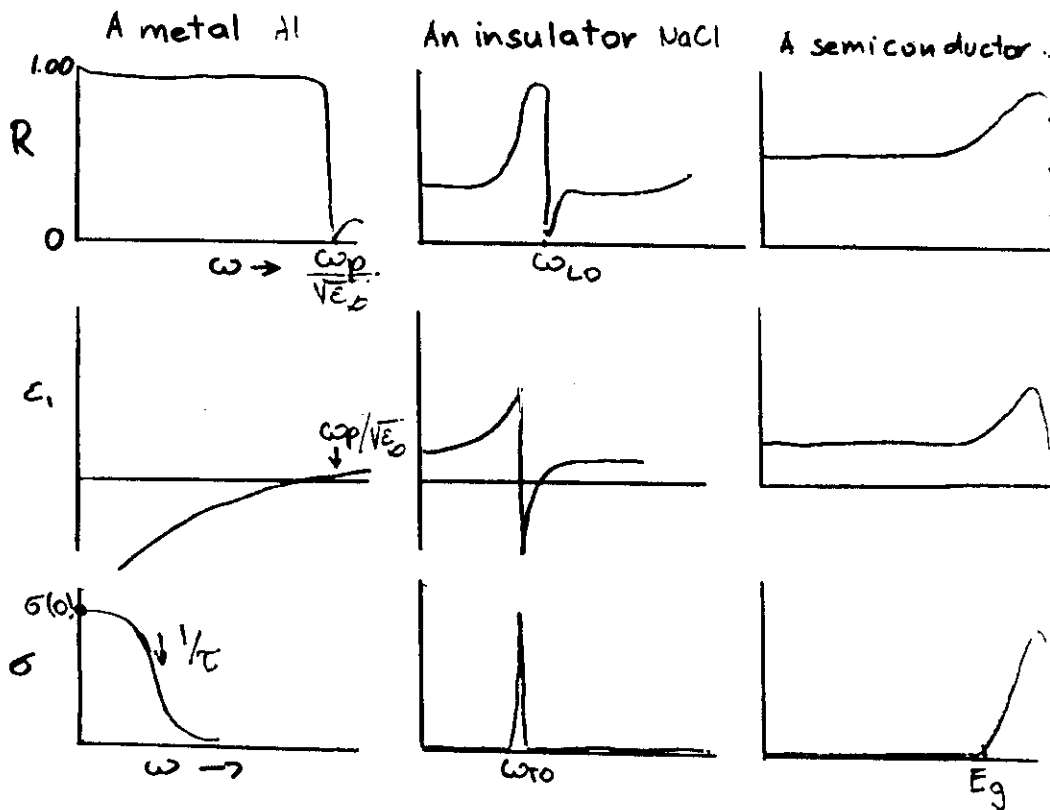
# Infrared response of solids

a) Reflectance  $R(\omega) = \left| \frac{\sqrt{\epsilon} - 1}{\sqrt{\epsilon} + 1} \right|^2$

b)  $\epsilon = \epsilon_1 + i\epsilon_2$  dielectric function

c) conductivity  $\sigma(\omega) = \frac{\omega \epsilon_2}{4\pi}$

Examples:

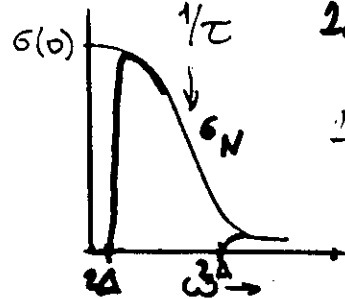


Drude conductivity:

$$4\pi\sigma(\omega) = \frac{\omega_p^2 \tau}{1 + \omega^2 \tau^2}$$

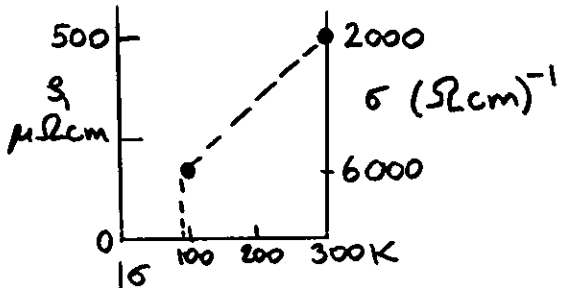
$$\omega_p^2 = \frac{4\pi N e^2}{m^*}$$

$$\tau = \frac{l}{v_F}$$



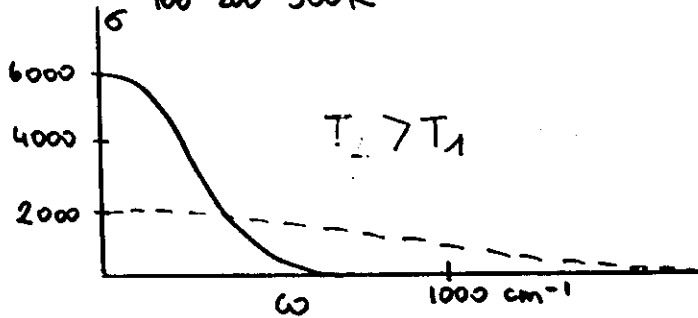
d.  
 $2\Delta \ll \frac{1}{\tau}$   
 $2\Delta \gg \frac{1}{\tau}$   
 clean

Temperature dependence:



$$\int \sigma(\omega) d\omega = \frac{\omega_p^2}{8}$$

Conductivity sum rule



EXCITATIONS OF BOUND ELECTRONS

$$\begin{aligned} \epsilon = \epsilon_\infty + \sum_i \frac{4\pi n_i e^2}{m(\omega_i^2 - \omega^2 - i\delta\omega)} &= \\ = \epsilon_\infty + \sum_i \frac{\omega_{pi}^2}{\omega_i^2 - \omega^2 - i\delta\omega} \end{aligned}$$

MOLECULAR EXCITATIONS (LOCALIZED)

CHARGE-TRANSFER EXCITATIONS

INTERBAND TRANSITIONS  
(DELOCALIZED)

## Fitting Reflectances to a Mode!

- a) Assume some form for the dielectric function:

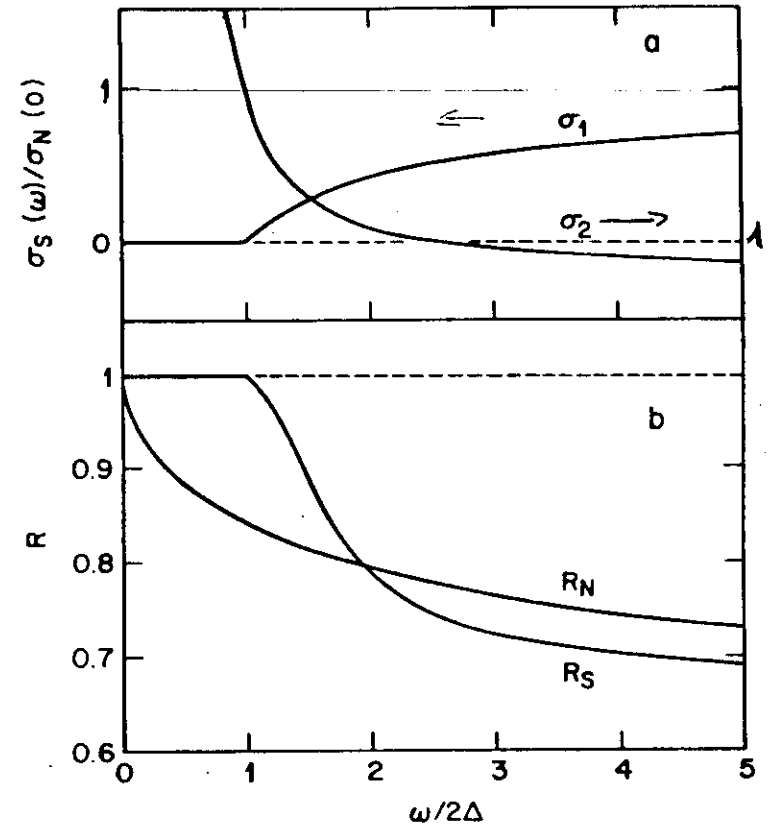
$$\epsilon(\omega) = \epsilon_\infty + \frac{\omega_p^2}{(-\omega^2 - i\omega\Gamma)} + \sum_j \frac{R_j^2}{(\omega_j^2 - \omega^2 - i\omega\delta_j)}$$

Drude, free electron term
Classical oscillators

b) Calculate  $R(\omega) = \left| \frac{\sqrt{\epsilon} - 1}{\sqrt{\epsilon} + 1} \right|^2$

- c) Least squares fit  $R(\omega)$  to experimental data to find  $R_j, \omega_j, \delta_j$  and  $\epsilon_\infty, \omega_p, \Gamma$

Region fitted  $\leq$  region measured!



G.A. Thomas et al.: Phys. Rev. B 36,  
846 (1987).

$A_s(4\text{nm})/A_s(8\text{nm}) = C_0 + C_1\omega^2$ . This quadratically increasing absorption was also reported in a number of experiments on small particles and on granular films [11, 12]. It seems reasonable to assume that the anomalous absorption of the superconducting film and the anomalous normal state absorption both have the same cause. An obvious approach to understand the physical process underlying the anomalous FIR behavior is to

extract the complex conductivity from the experimental data using the inversion procedure described earlier in section 4. Using eqs. (13) and (14), we can determine the conductivity in a straightforward way. Above the gap, both absorption and transmission are largely determined by  $\sigma_1$ , therefore the inversion process is most accurate for  $\sigma_1$ . In fig. 14 we show the result of the inversion of the experimental data shown in figs. 11 and 12, using  $R_s = 110\Omega$ . The result for  $\sigma_1$  in fig. 14(a) is in good agreement with the MB calculations (solid curve) for frequencies between  $\Delta_0$  and  $4\Delta_0$ . In fig. 14(b),  $\sigma_2$  is considerably reduced compared with the MB calculations. Above the gap the agreement is better, but these data are not very accurate due to the weak dependence of both absorption and transmission on  $\sigma_2$ . Fig. 14(b) suggests an ad hoc fit based on a renormalization of  $\sigma_2$ . A reasonable fit to the experimental  $\sigma_2$  data was obtained with a reduced MB-curve given by  $\sigma_2 = 0.7\sigma_2(\text{MB})$  as shown with a dashed line in fig. 14(b). In fig. 15 we compare the experimental absorption and transmission of this film, with a theoretical calculation  $\sigma_1 = \sigma_1(\text{MB})$  and  $\sigma_2 = \sigma_2(\text{MB}) \times 0.7$  and indeed find a good agreement. The reduction of  $\sigma_2$  happens to be of the same magnitude as was calculated for the strong-coupling superconductor Pb by Nam [22]. It is therefore tempting to assume that the increase of  $T_c$  and  $\Delta$  of ultrathin

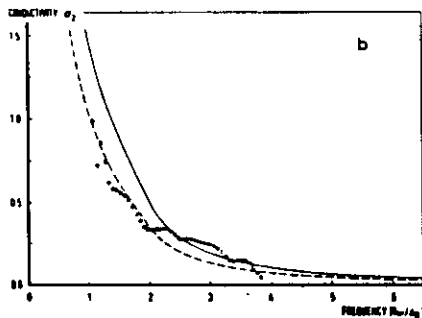
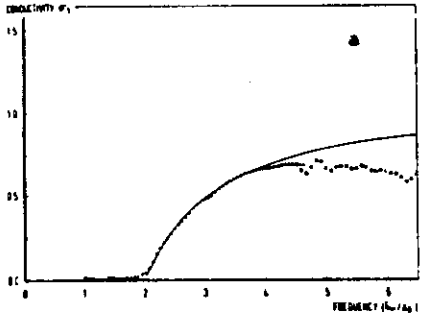


Fig. 14. a) ( $\Delta$ ) and ( $\circ$ ): Experimental result for the real part of the conductivity  $\sigma_1$  of film 6, using eq. (13) b) ( $\circ$ ): Experimental result for the imaginary part of the conductivity  $\sigma_2$  of film 6 according to eq. (14), using  $R_s = 110\Omega$ . The solid curves are calculated according to the weak-coupling theory. The dashed line in fig. 14(b) represents an ad hoc fit to the experimental points:  $\sigma_2 = 0.7\sigma_2^{\text{MB}}$ .

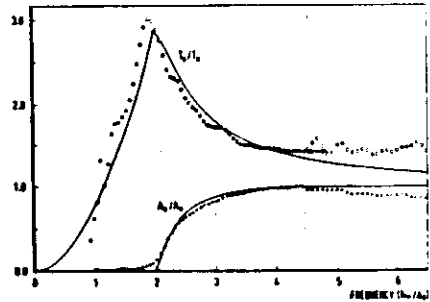
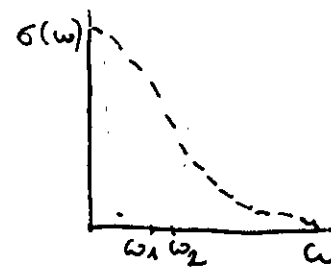


Fig. 15. Normalized absorption  $A_s/A_0$  ( $\Delta$ ) and transmission  $T_s/T_0$  ( $\circ$ ) of film 6, together with a calculation using  $R_s = 110\Omega$ ,  $\sigma_1 = \sigma_1^{\text{MB}}$  and  $\sigma_2 = 0.7\sigma_2^{\text{MB}}$ .

HOLSTEIN EFFECT  
(HOLSTEIN 1954; ALLEN 1971)

T. HOLSTEIN: PRB 96, 539 (1954)

P.B. ALLEN: PRB 3, 305 (1971)

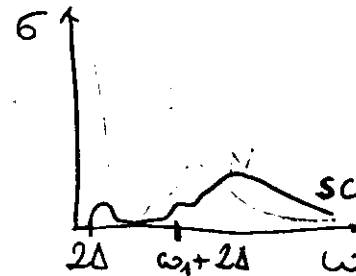


LOW T ( $T_c < T_{\text{DSEB}}$ )  
HIGH T ( $k_B T > \hbar \Delta_0$ )

$$\Gamma = (2\pi\lambda/\hbar)(k_B T + \hbar \Delta_0) / 2$$

EXTENDABLE TO OTHER EXCITATIONS  
(NOT NECESSARILY DIPOLE ACTIVE)

SUPERCONDUCTING STATE:





BY ANALOGY WITH LOW  $T_c$   
SYSTEMS:

NORMAL STATE  $\omega_p \Rightarrow N/m^2$ \*

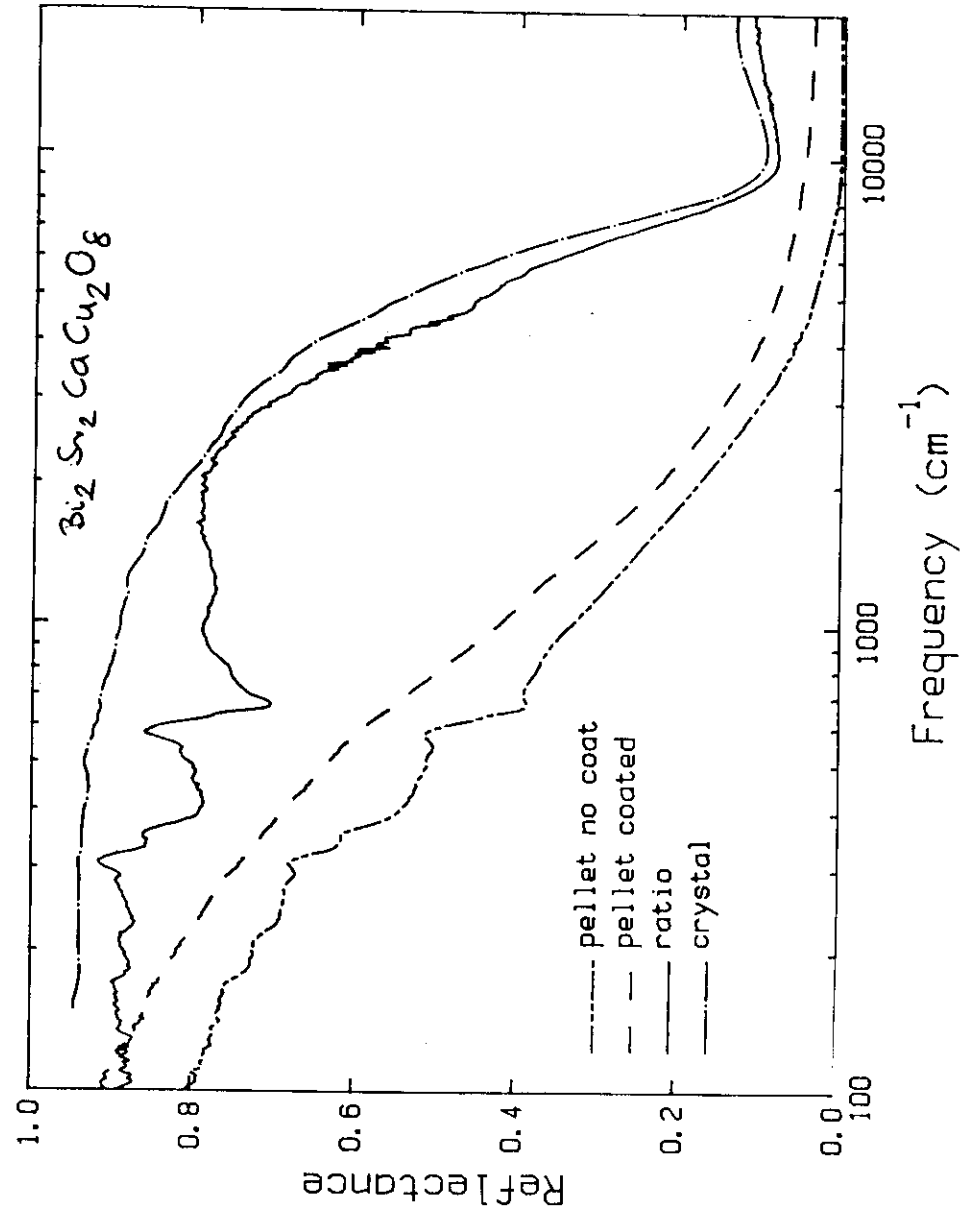
$\tau \Rightarrow \ell$

SC STATE  $R \Rightarrow \Delta$

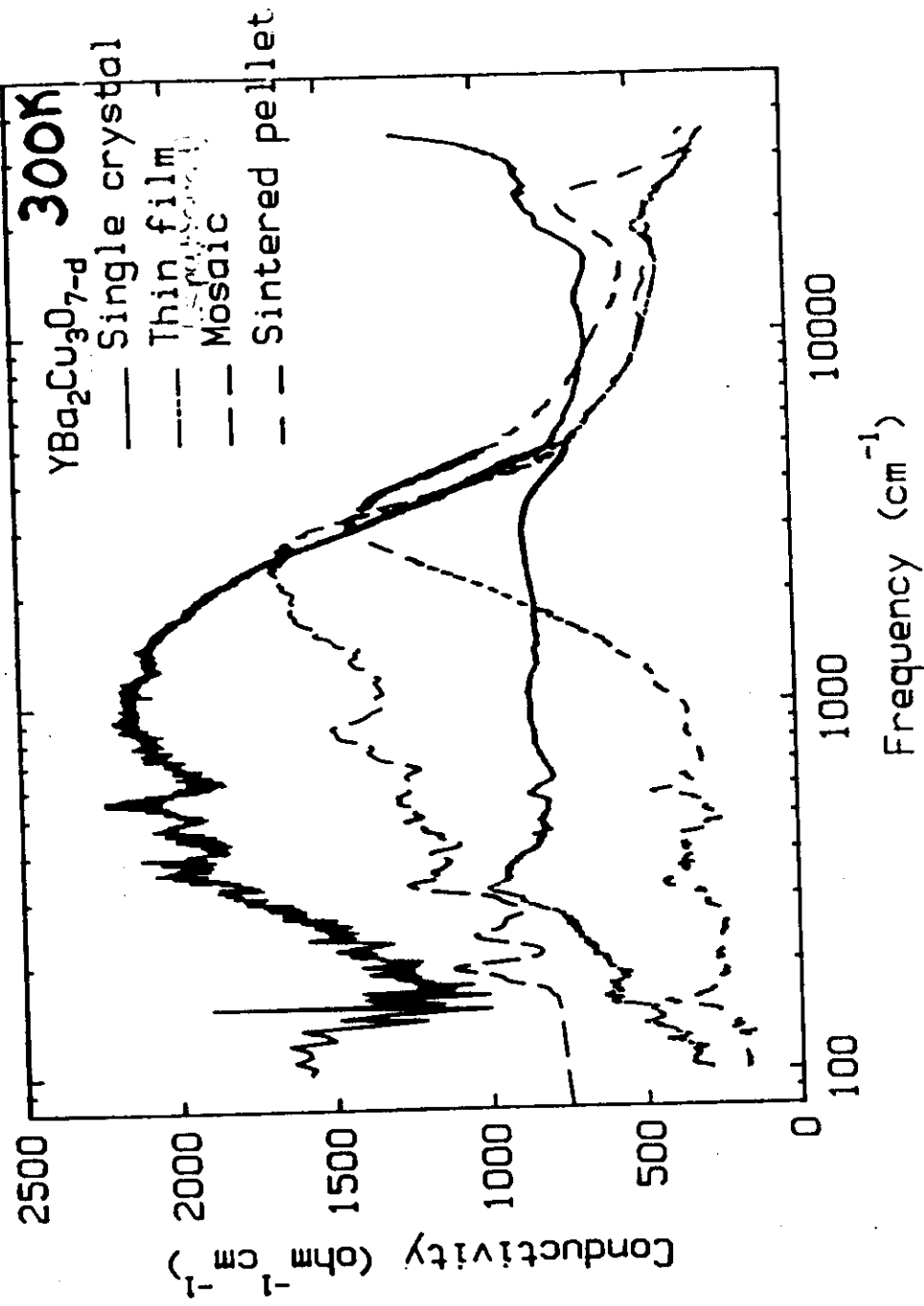
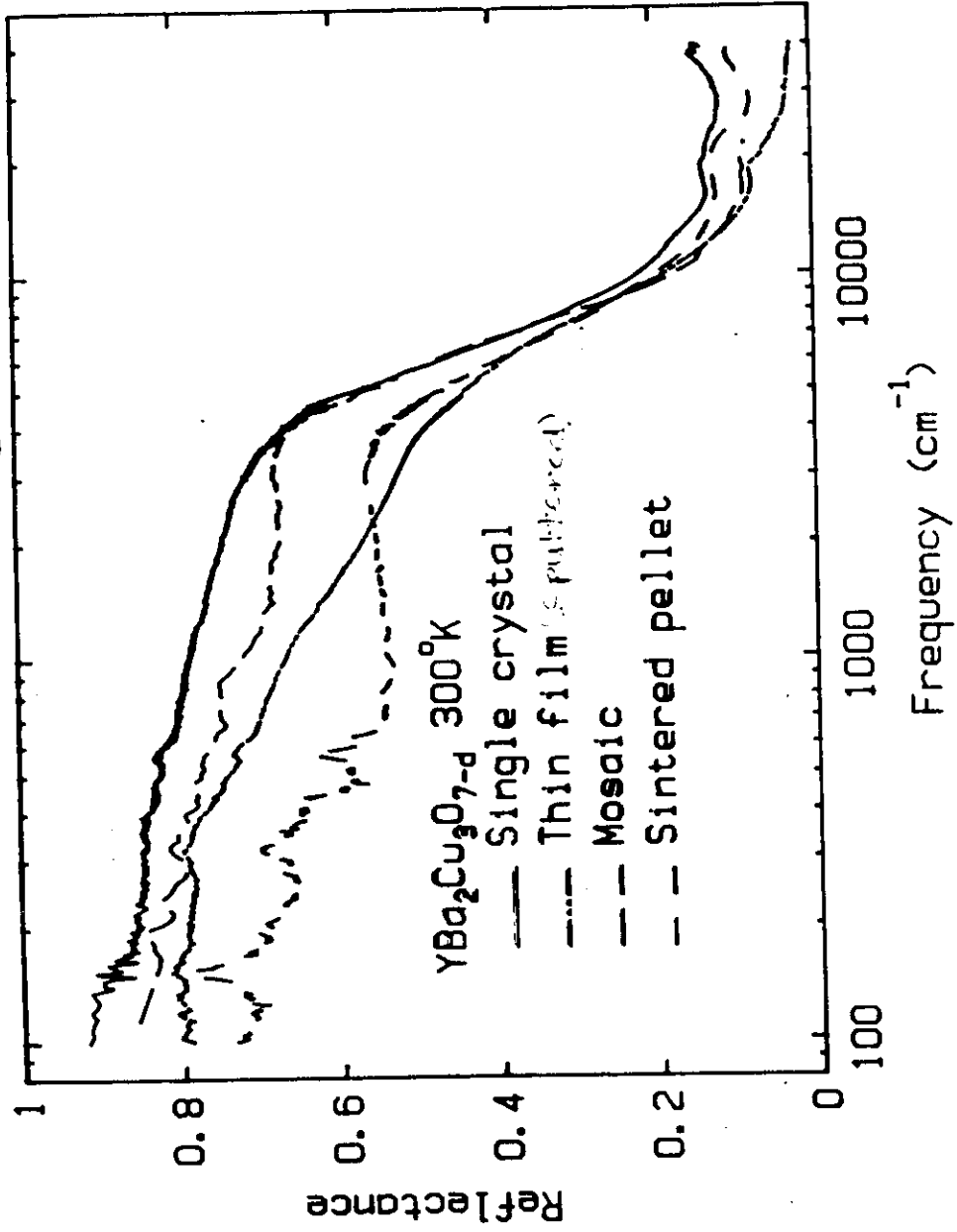
POSSIBLE HOLESTEIN EFFECT  
↓  
 $\Delta, \lambda$

IN REALITY:

LOTS OF PROBLEMS!

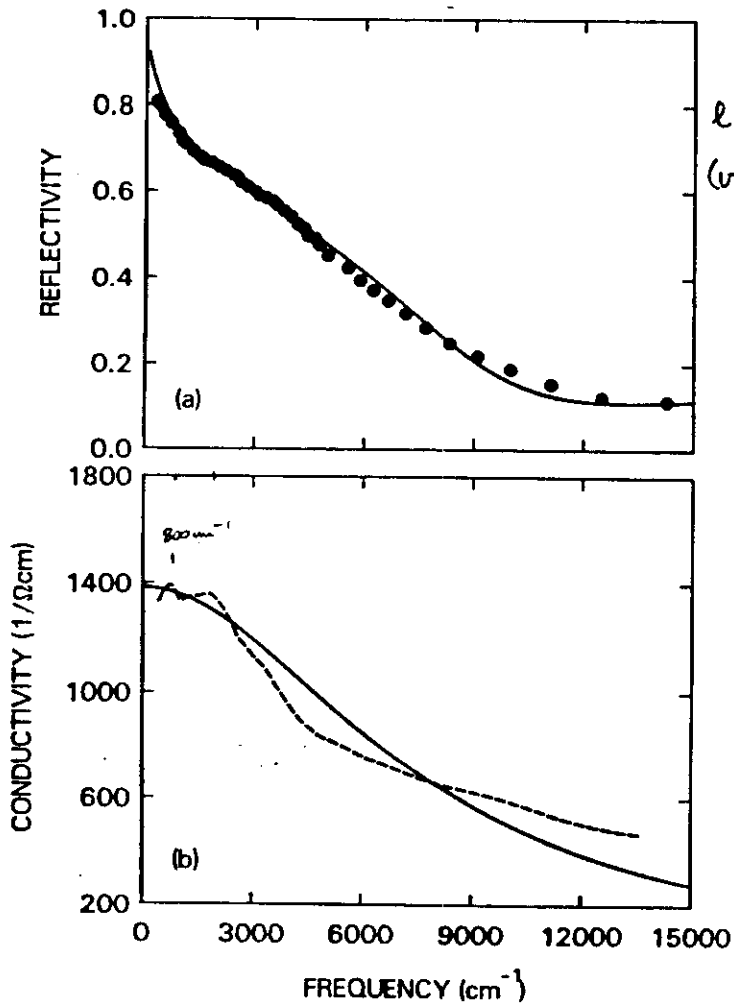


$T_c \sim 90\text{K}$



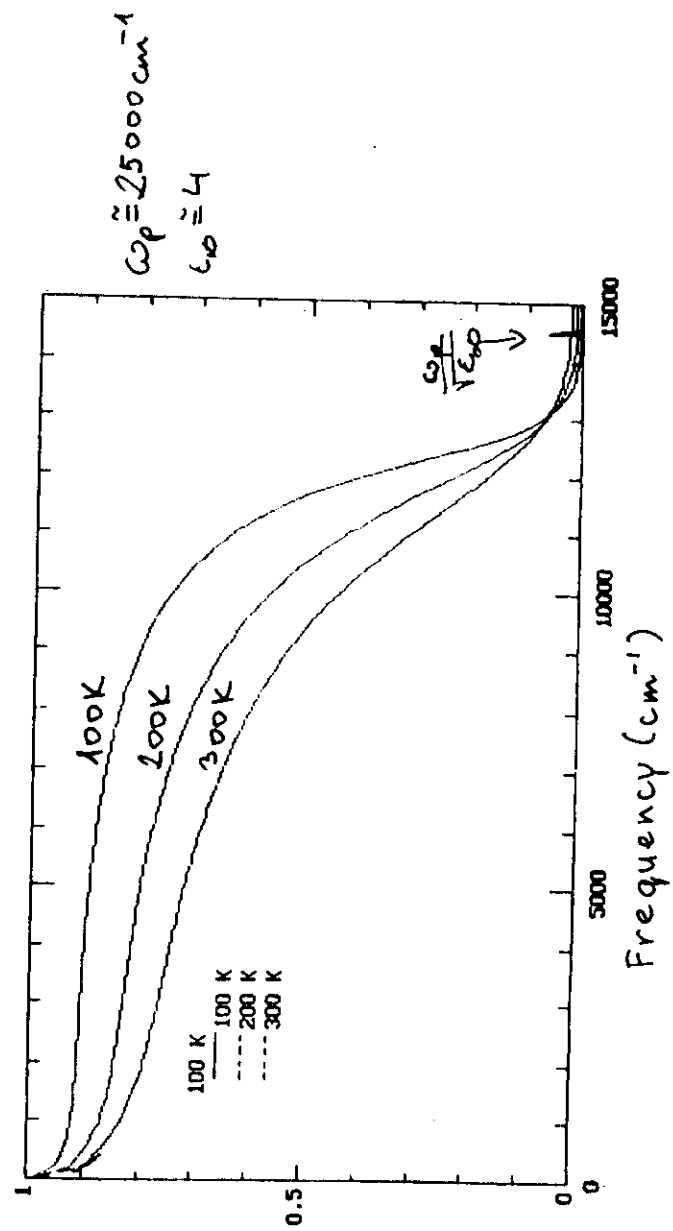
Z. Schlesinger et al: PRL 59, 1958 (1987)

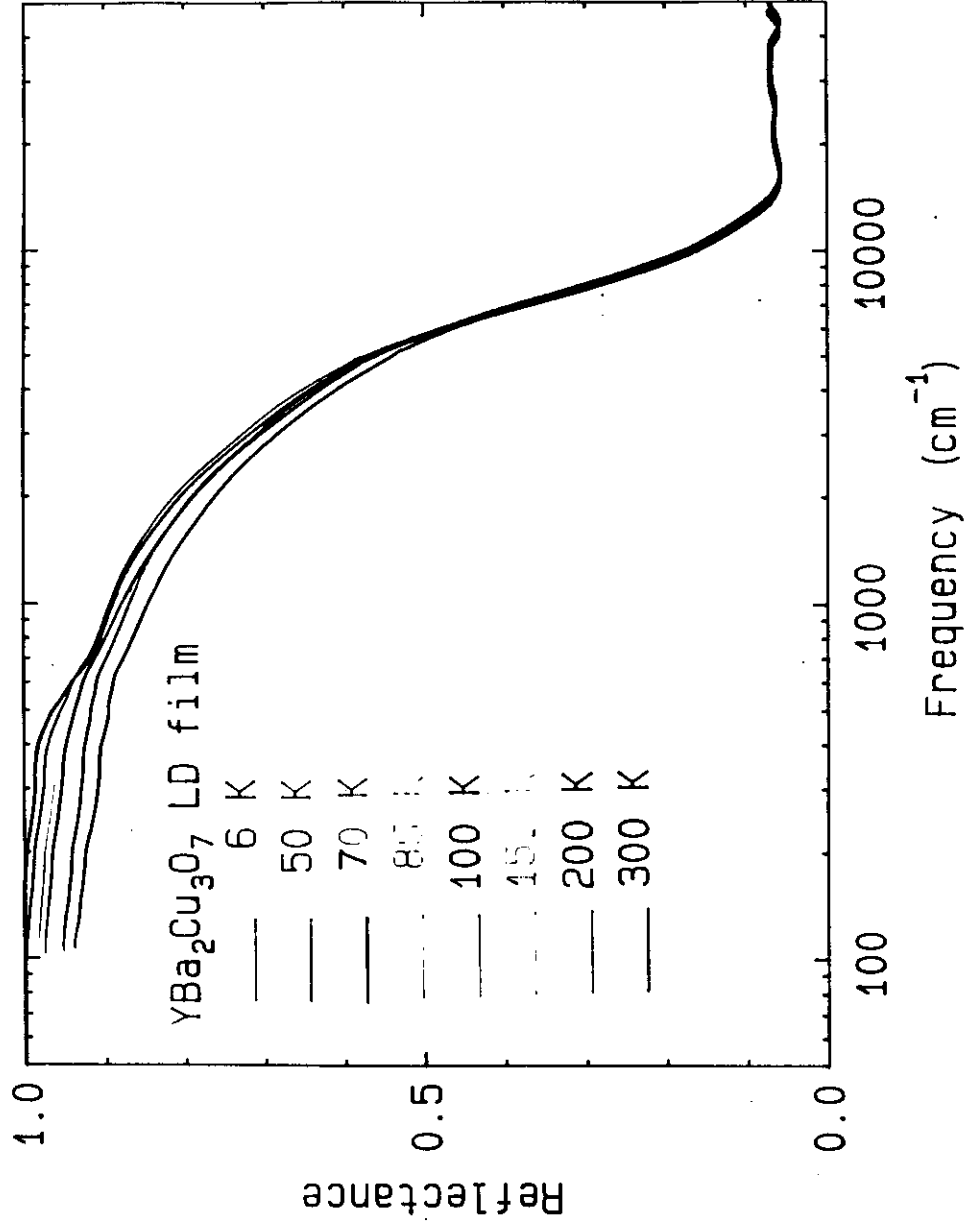
$\text{YBa}_2\text{Cu}_3\text{O}_7$  crystal  $\omega_p \approx 3\text{eV}$   
 $\tau \approx 10^{-15}\text{s}$



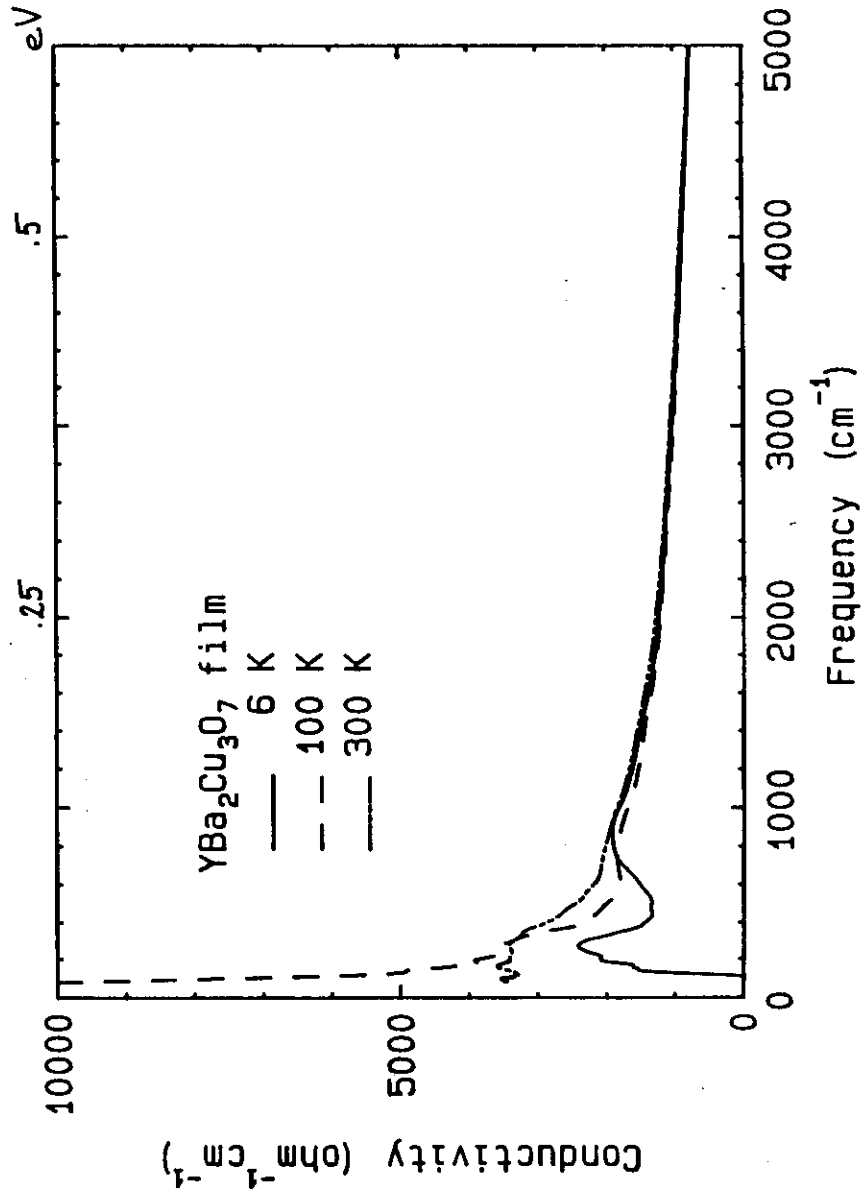
$\Downarrow$   
 $l = 1 - 3\text{\AA}$   
 $(v_F = 2 \cdot 10^7 \frac{\text{cm}}{\text{s}})$

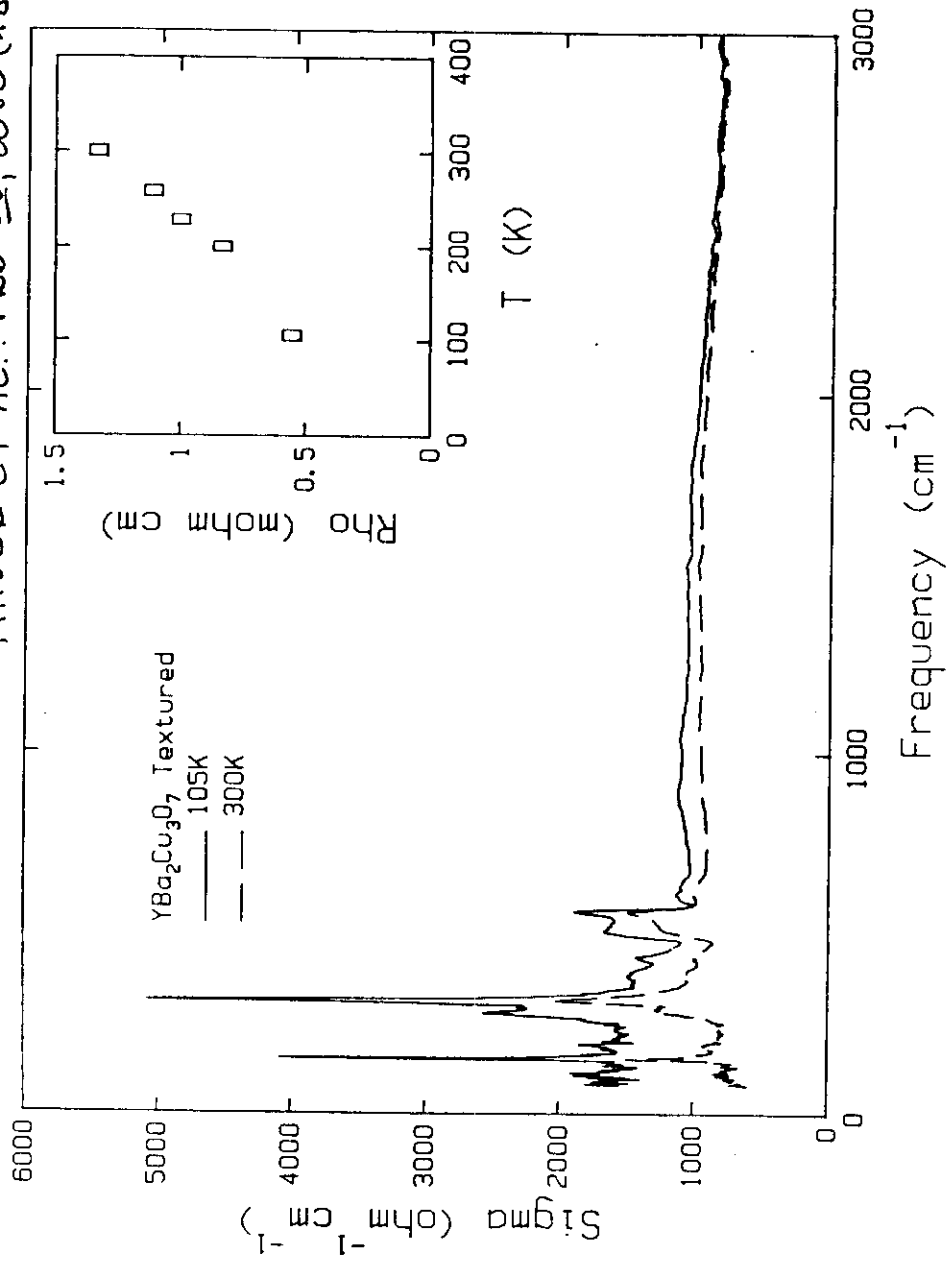
Simulation of Bragg reflectivity  
 of  $\text{YBaCuO}$  300K as a metal  
 (CT) is lower down to 100K





KAMARAS ET AL: PRL 64, 84 (1990)

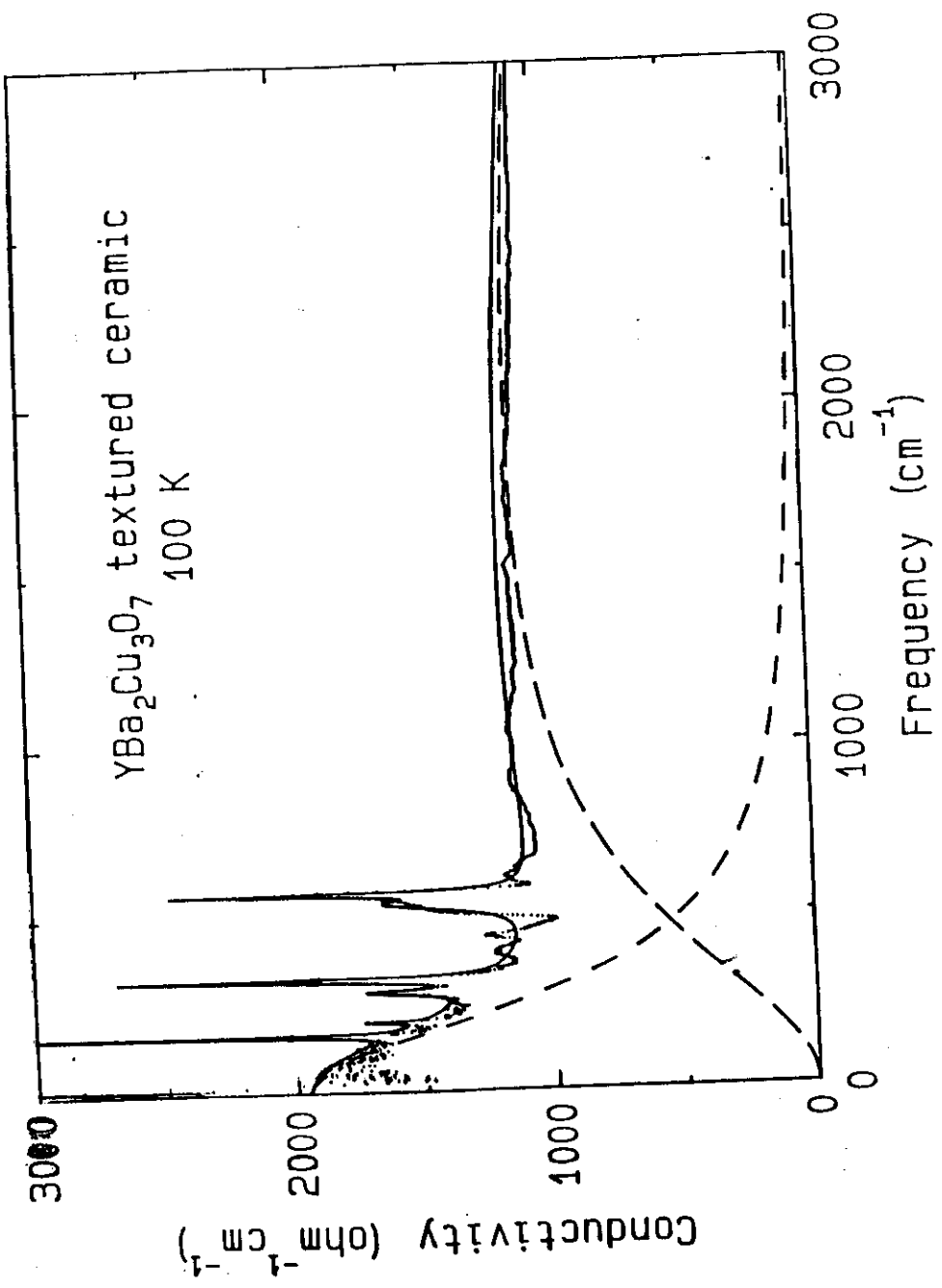




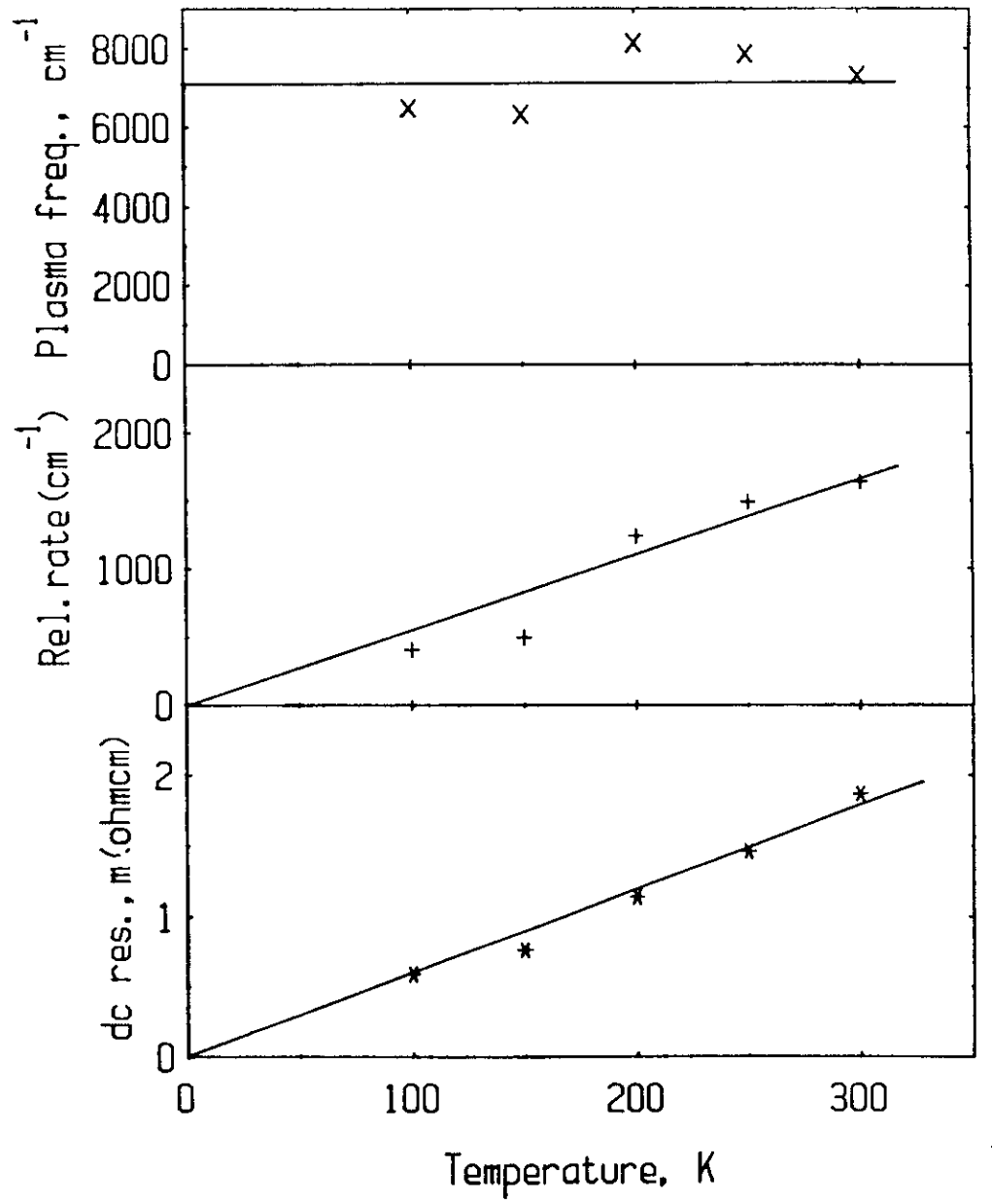
NORMAL STATE DIELECTRIC FUNCTION:

$$\epsilon(\omega) = - \frac{\omega_{pd}^2}{\omega^2 + i\omega/\tau_D} + \frac{\omega_{MIR}^2}{\omega_{0,MIR}^2 - \omega^2 - i\omega\Gamma_{MIR}} + \sum_j \frac{S_j \omega_j^2}{\omega_j^2 - \omega^2 - i\gamma_j \omega} + \epsilon_{\infty}$$

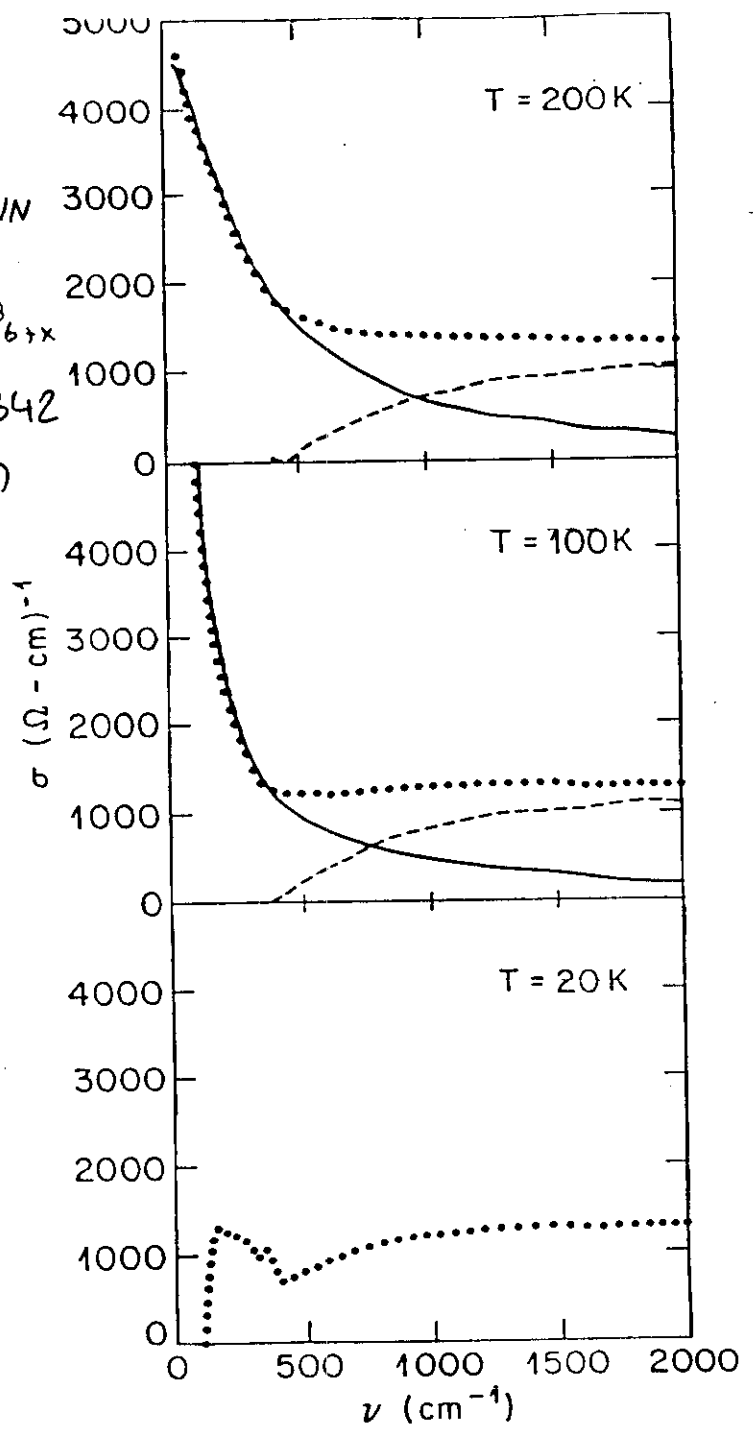
↓ FAR IR DRUDE PART      ↓ MID-IR BAND      ↓ PHONONS      ↓ ~4



YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub> SPUTTERED FILM



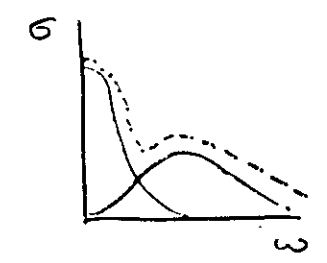
J. ORENSTEIN  
 1990  
 $YBa_2Cu_3O_{6+x}$   
 PRB 42, 6342  
 (1990)



TEMPERATURE INDEPENDENT  
 MID-INFRARED ABSORPTION

DIRECT (IR ACTIVE)  
 CHARGE TRANSFER  
 VALENCE FLUCTUATIONS  
 ETC.  
 CT EXCITATIONS  
 ON CHARGE  
 RESERVOIR

INDIRECT  
 (IR INACTIVE, COUPLED)  
 PHONONS (HOLSTEIN)  
 MAGNONS (ORENSTEIN)  
 CHARGE + SPIN (VARMA)



CONVENTIONAL SUPERCONDUCTORS:

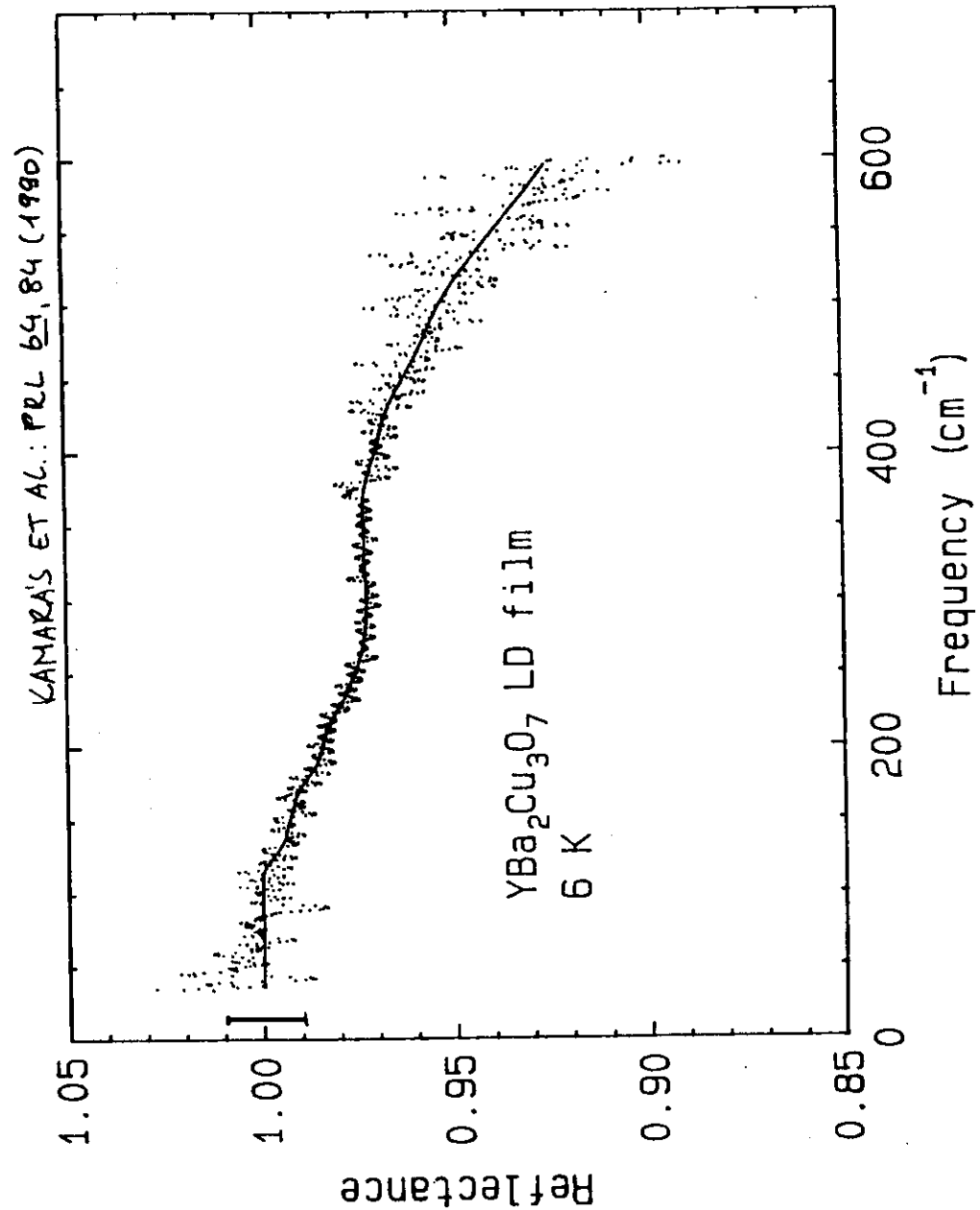
$$R = 1.00 \quad \omega < \omega_g$$

"EARLY HIGH  $T_c$ " :  $R < 1$  AT ANY  $\omega$

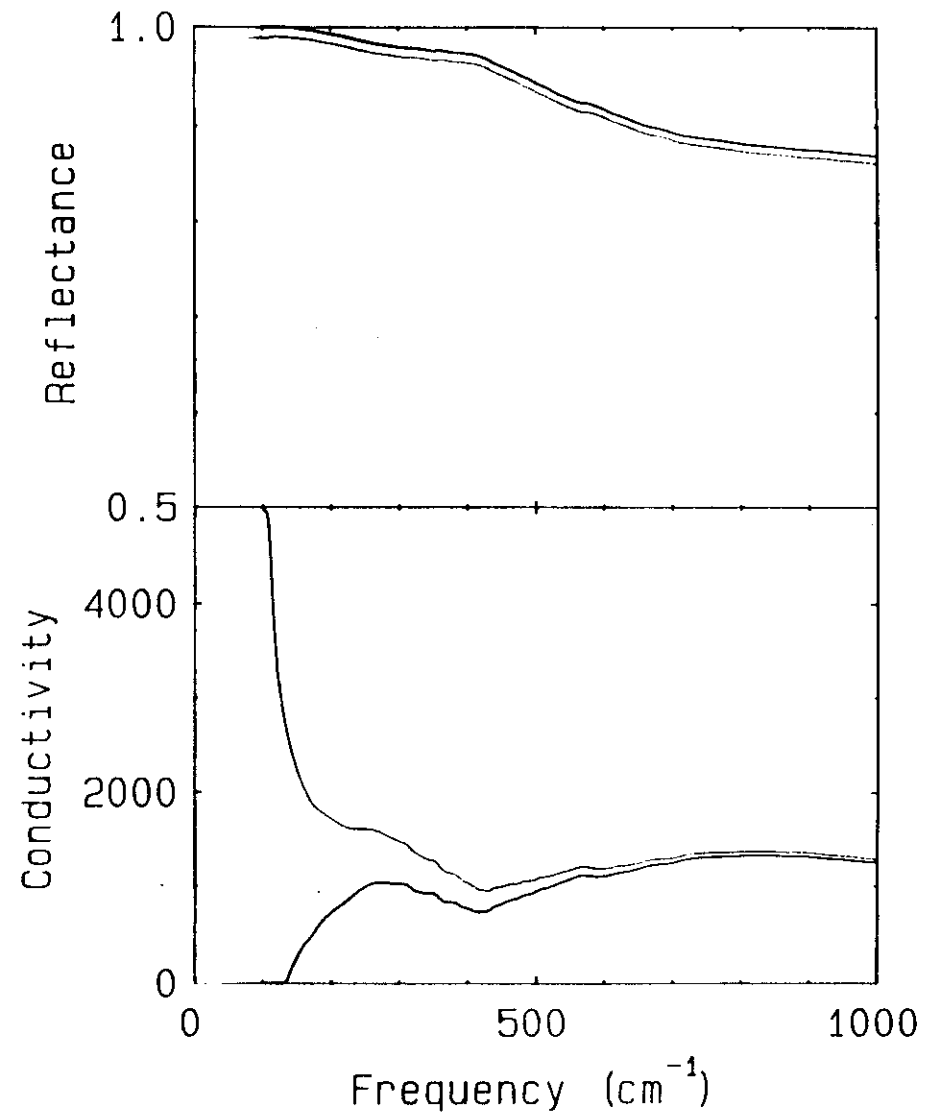
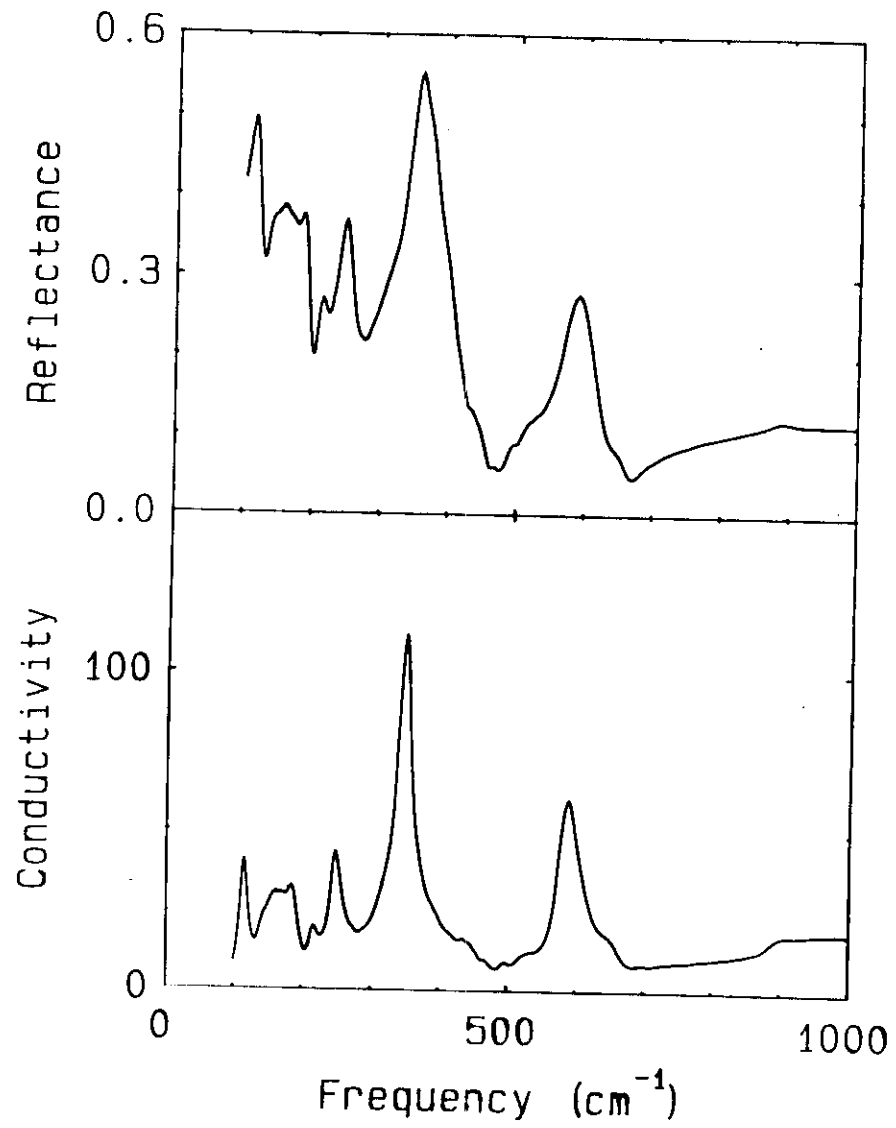
CIRCUMVENTING PROCEDURES:

- SCALE UP REFLECTIVITY
- PLOT  $R_s/R_N$   
SHOULD HAVE MAXIMUM AT DOWNTURN  
OF  $R_s$
- MORE ELABORATE METHODS TO TAKE INTO  
ACCOUNT:
  - PRESENCE OF "NORMAL" PHASE
  - C-AXIS ORIENTATION  
ETC.  
(MOSTLY EMA)

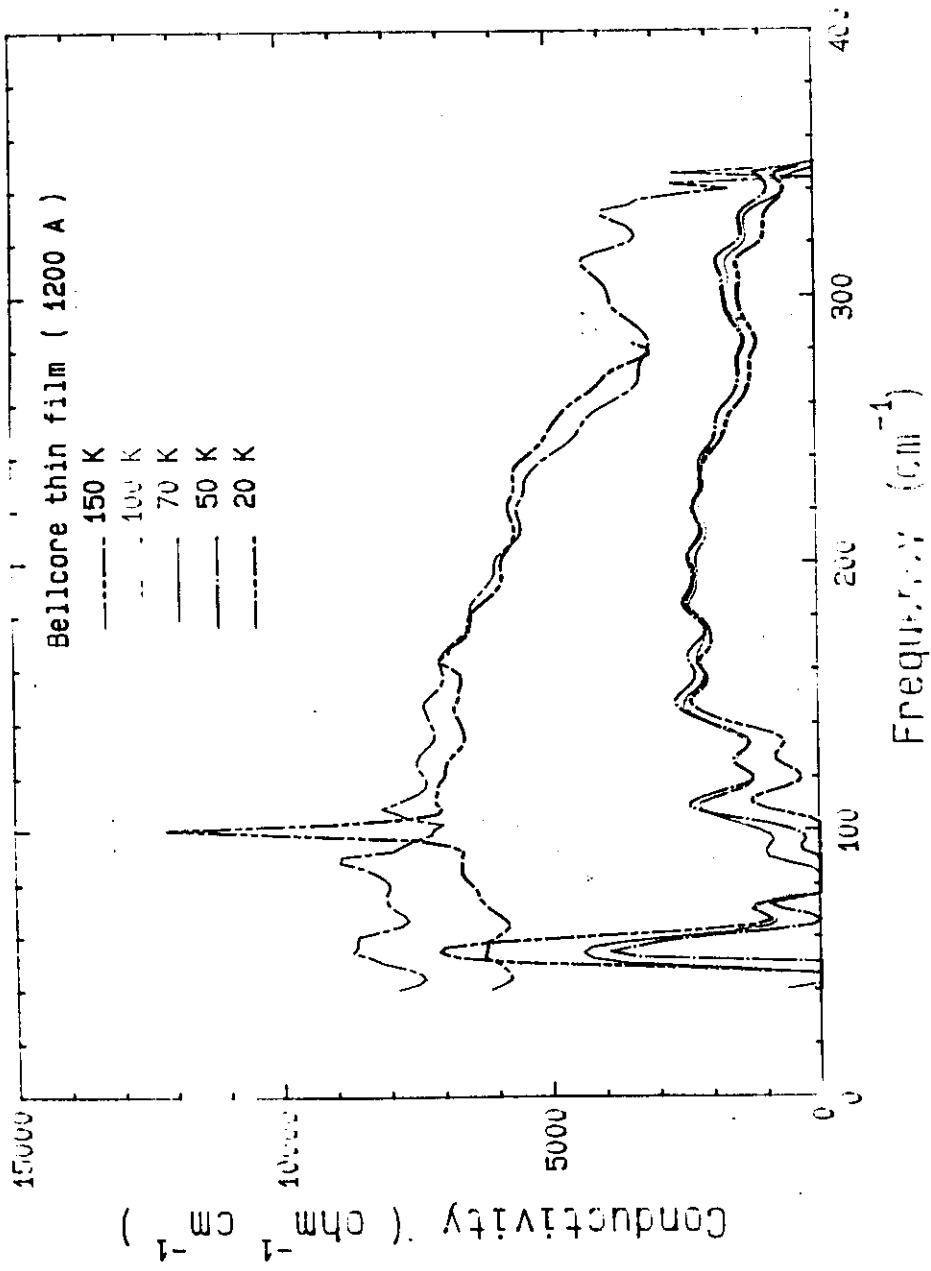
QUESTION:  $R < 1$  MATERIAL PROBLEM  
OR INTRINSIC PROPERTY?







G.L. CARR ET AL. (1989)



M. REEDYK ET AL.: PRB 38, 11984 (1988)

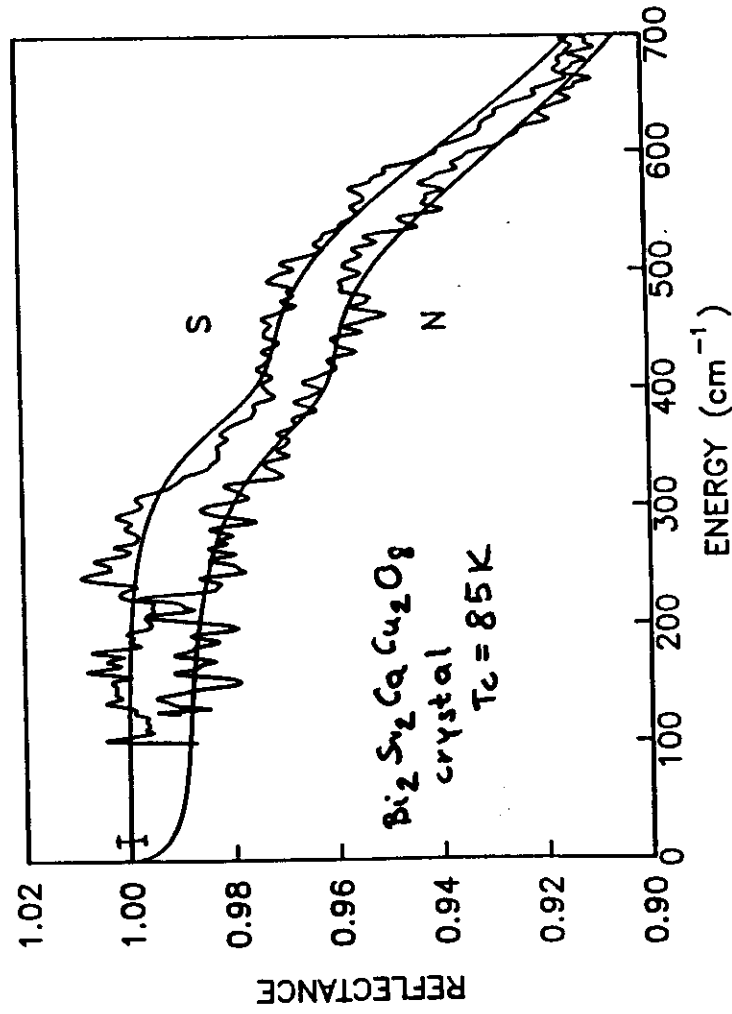
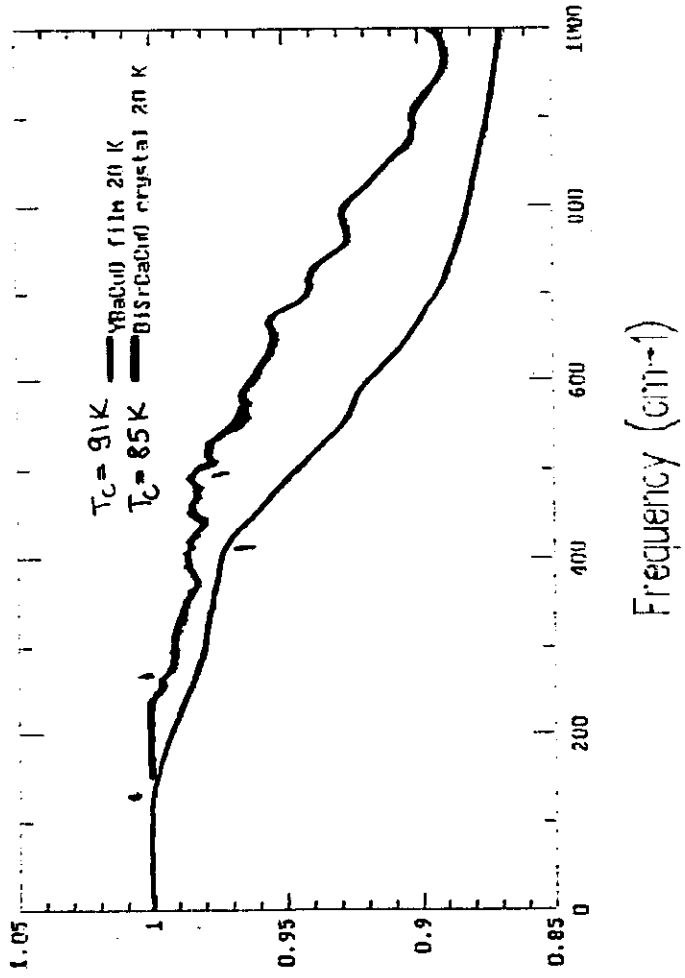
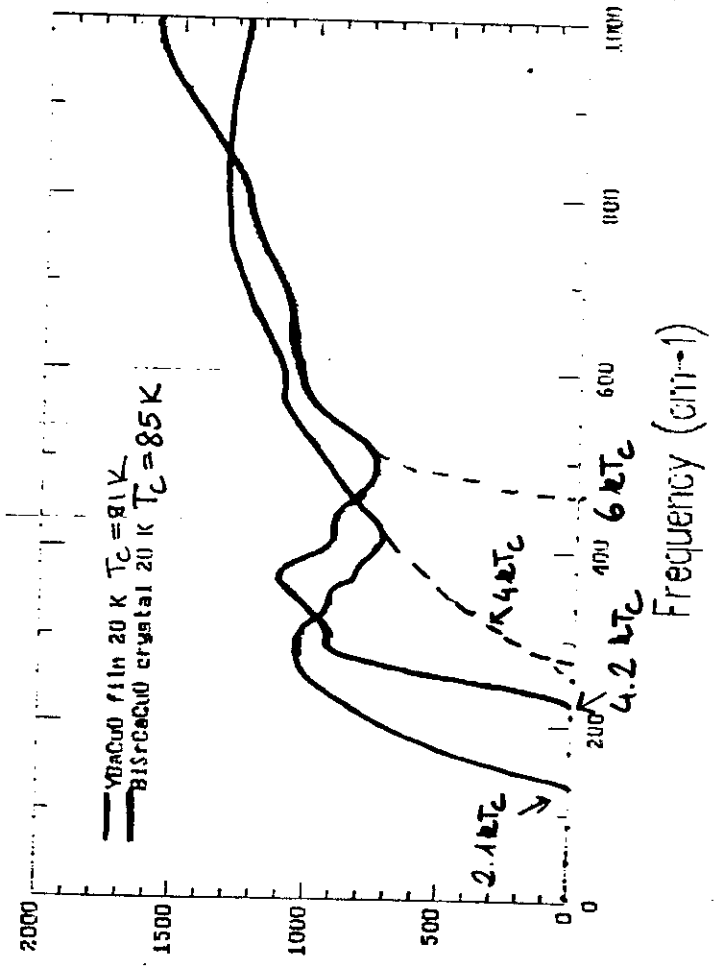


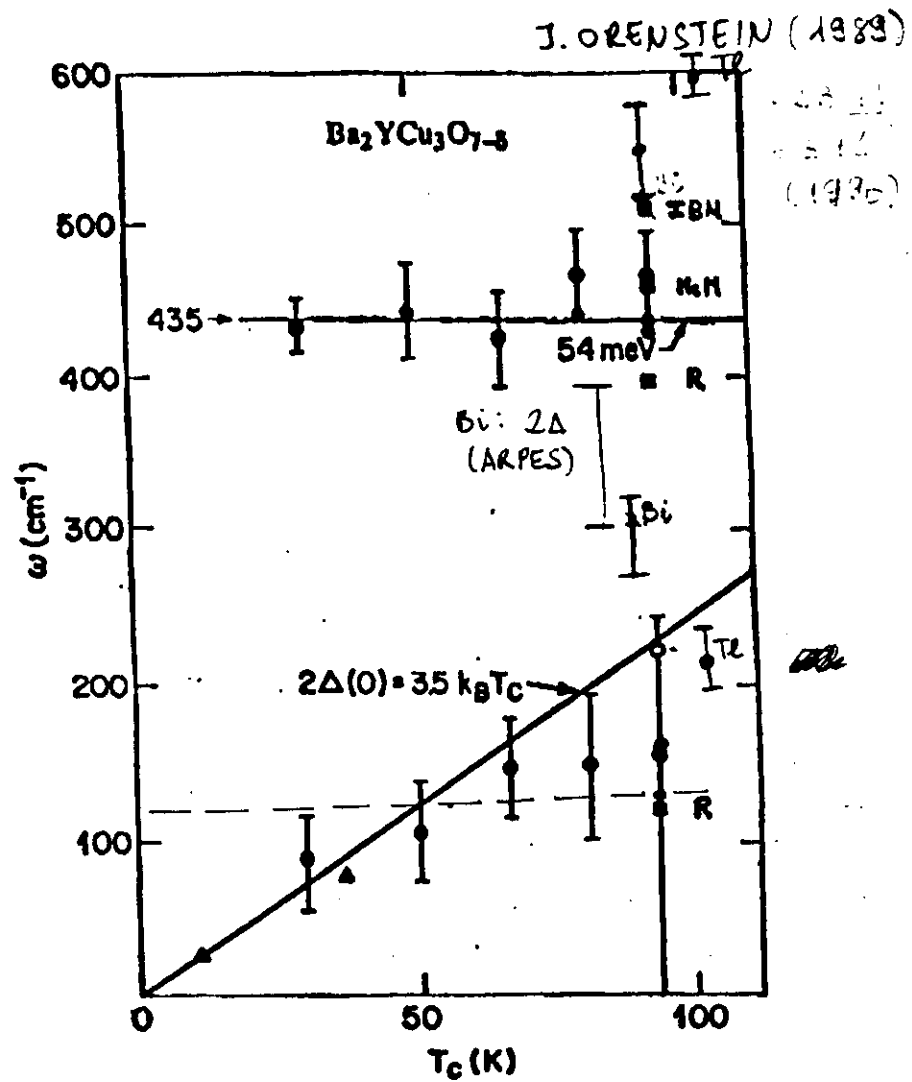
Fig 3



Frequency ( $\text{cm}^{-1}$ )



Frequency ( $\text{cm}^{-1}$ )



D. B. ROMERO ET AL. (1990)

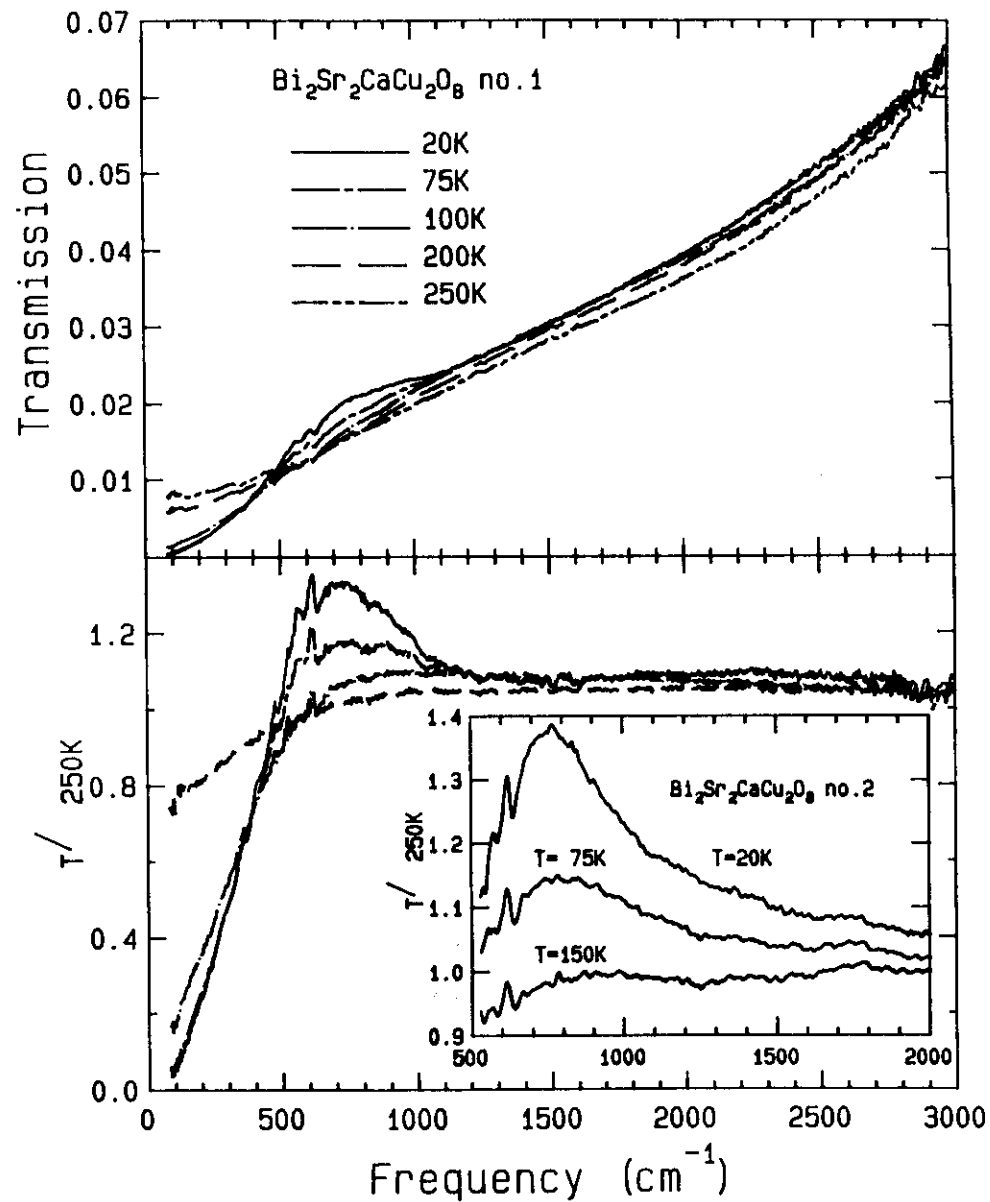
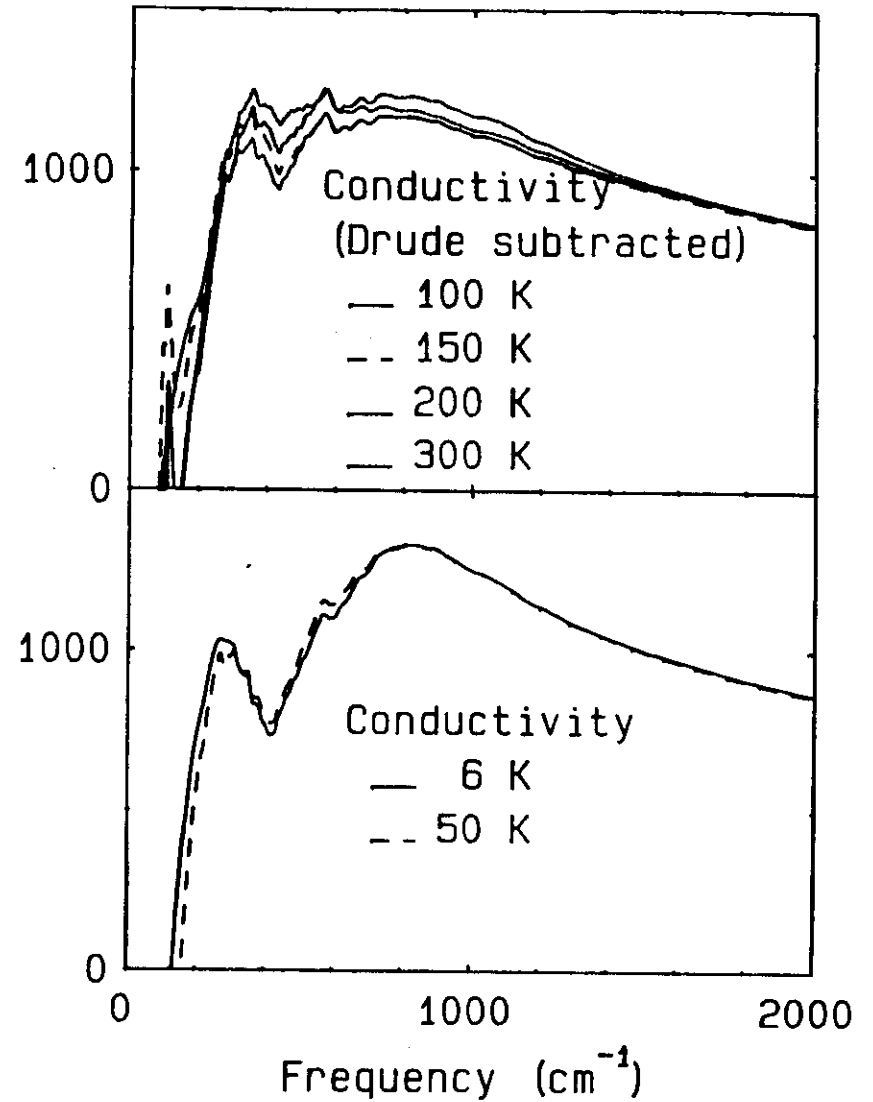


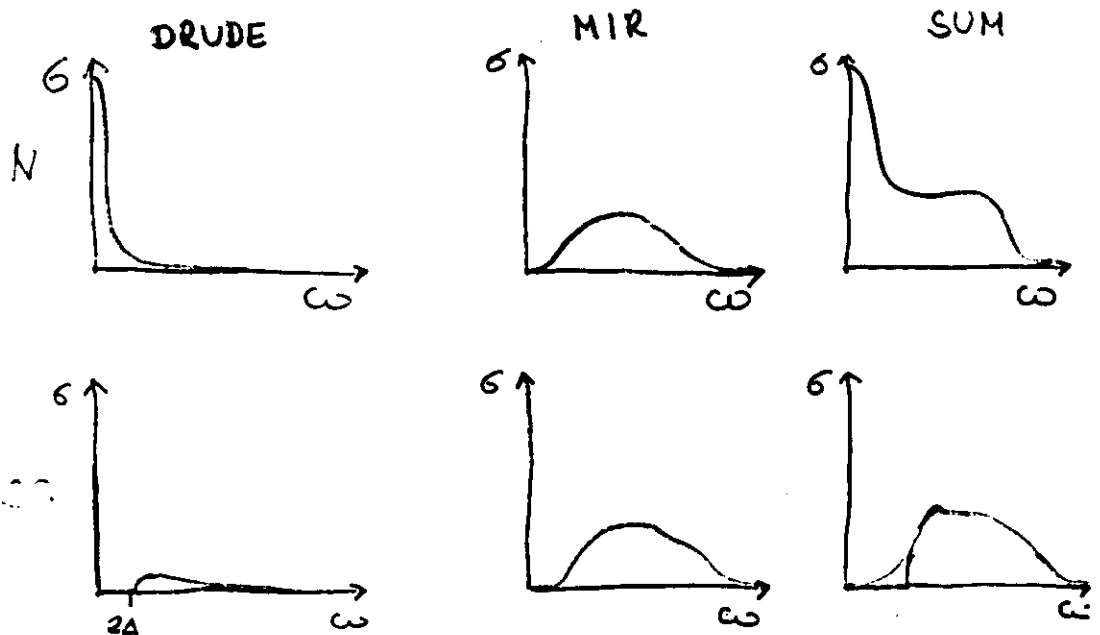
Fig 3

"GAP-LIKE FEATURES"  
IN  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$

	$2\Delta$
REFLECTIVITY:	
FIRST DOWNTURN	$4kT_c$
SECOND " - " -	$6kT_c$ NAIVE
	$3kT_c$ "MFL"
PHOTOEMISSION	$3-5kT_c$
TRANSMISSION	$12kT_c$ NAIVE
	$6kT_c$ "MFL"
NONE OF THESE CHANGE WITH T	
AT $T < T_c$	



TWO-COMPONENT ABSORPTION + CLEAN LIMIT  
 $(\gamma \ll 2\Delta)$



IMPOSSIBLE TO DETERMINE GAP  
 BY OPTICAL METHODS

DRUDE METAL:

$$\epsilon(\omega) = \epsilon_b - \frac{\omega_p^2}{\omega^2 + i\omega\Gamma}$$

if  $\Gamma \rightarrow 0$

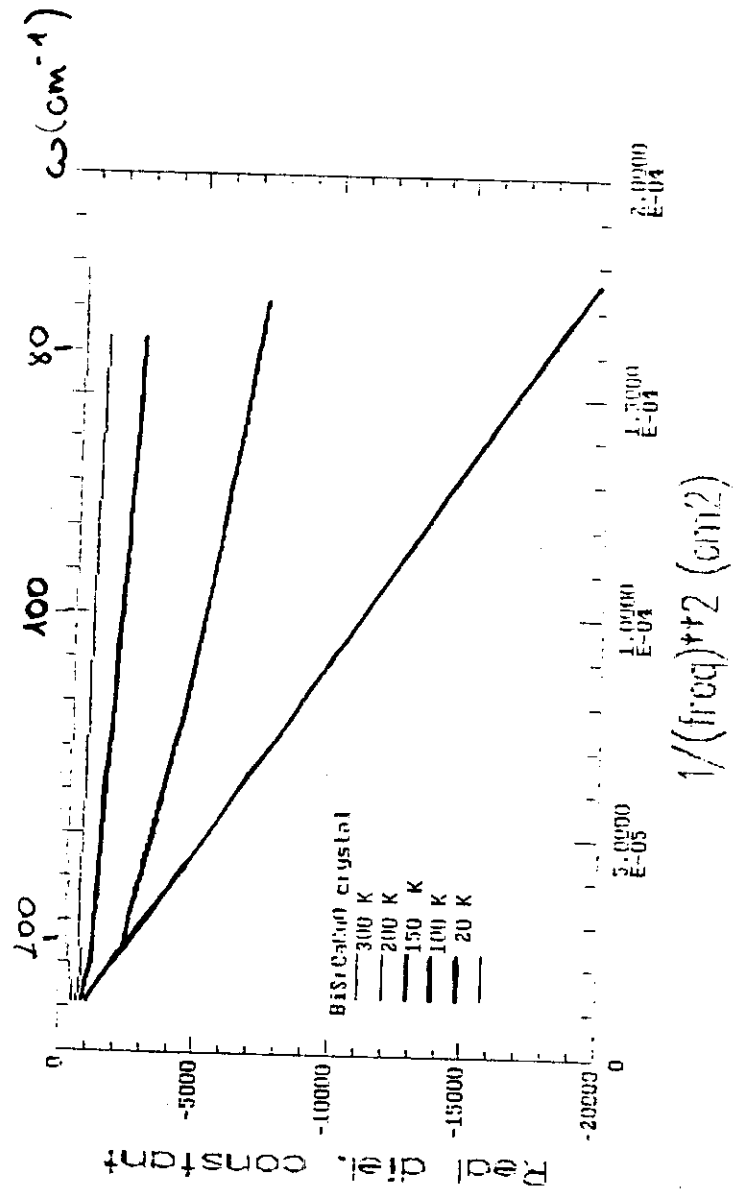
$$\epsilon(\omega) = \epsilon_b - \frac{\omega_p^2}{\omega^2} = \epsilon_1(\omega)$$

THUS, FROM  $\epsilon_1$  w.  $\frac{1}{\omega^2}$  WE GET  $\omega_p, \epsilon_b$

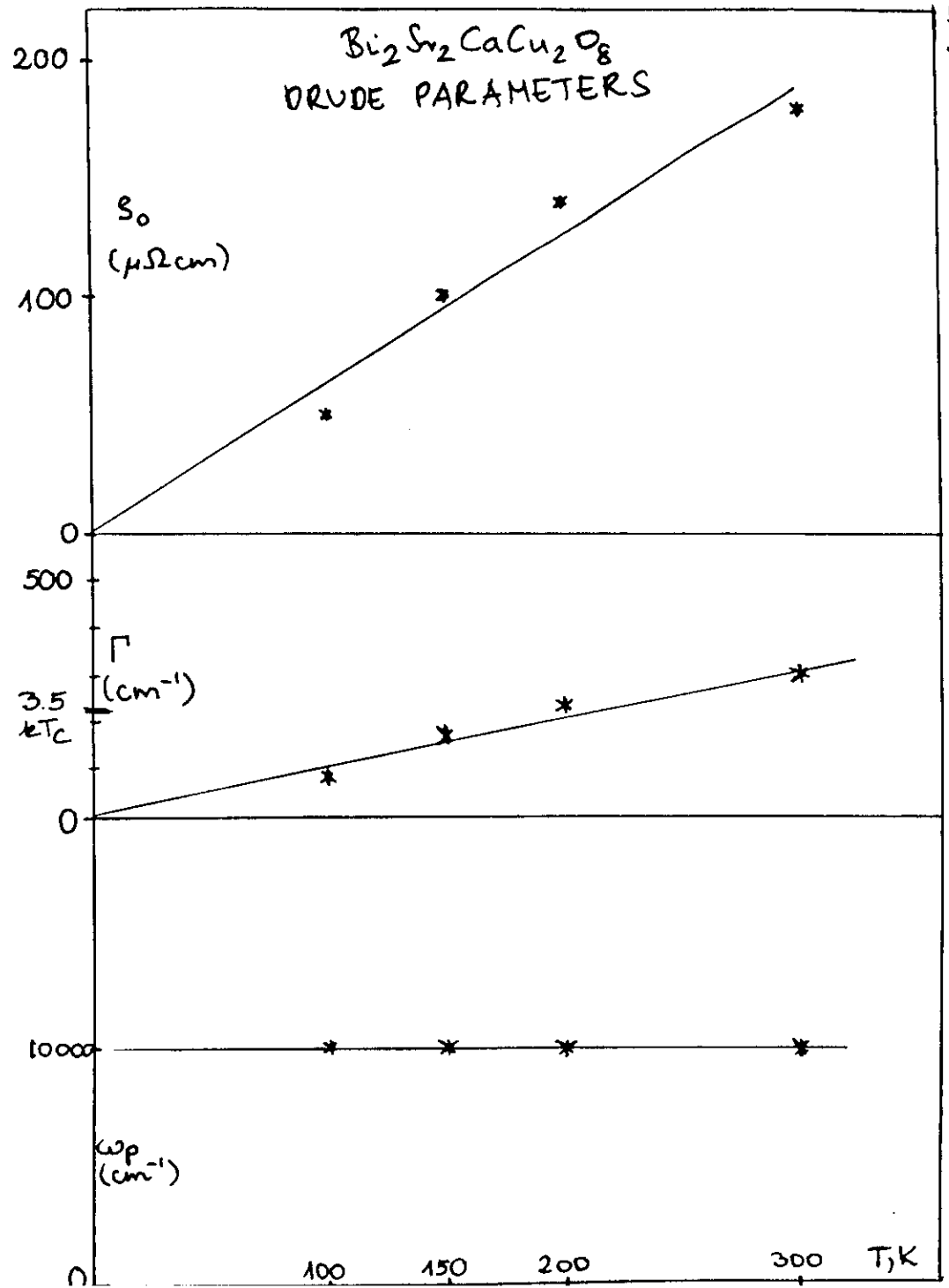
if  $\omega \ll \Gamma$

$$\epsilon_1(\omega) = \epsilon_b - \frac{\omega_p^2}{\omega^2 + \Gamma^2} \approx \epsilon_b - \frac{\omega_p^2}{\Gamma^2}$$

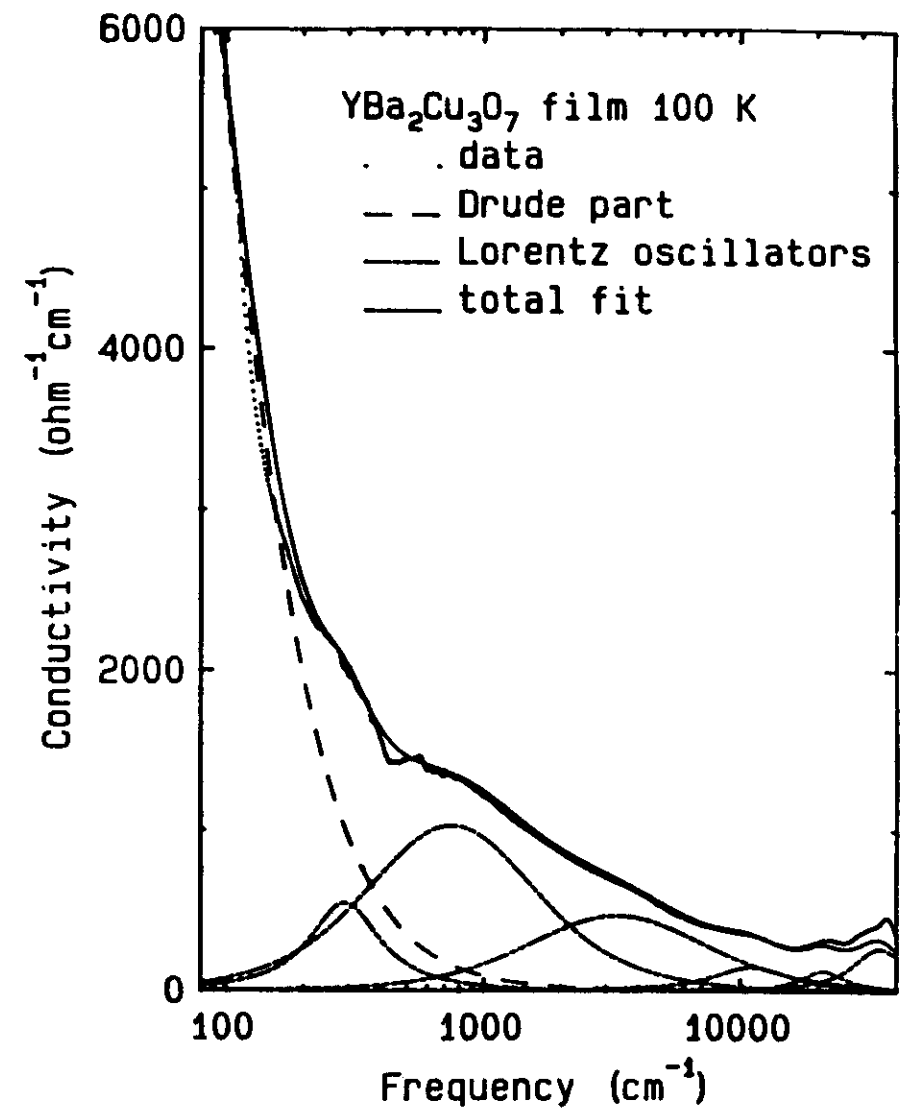
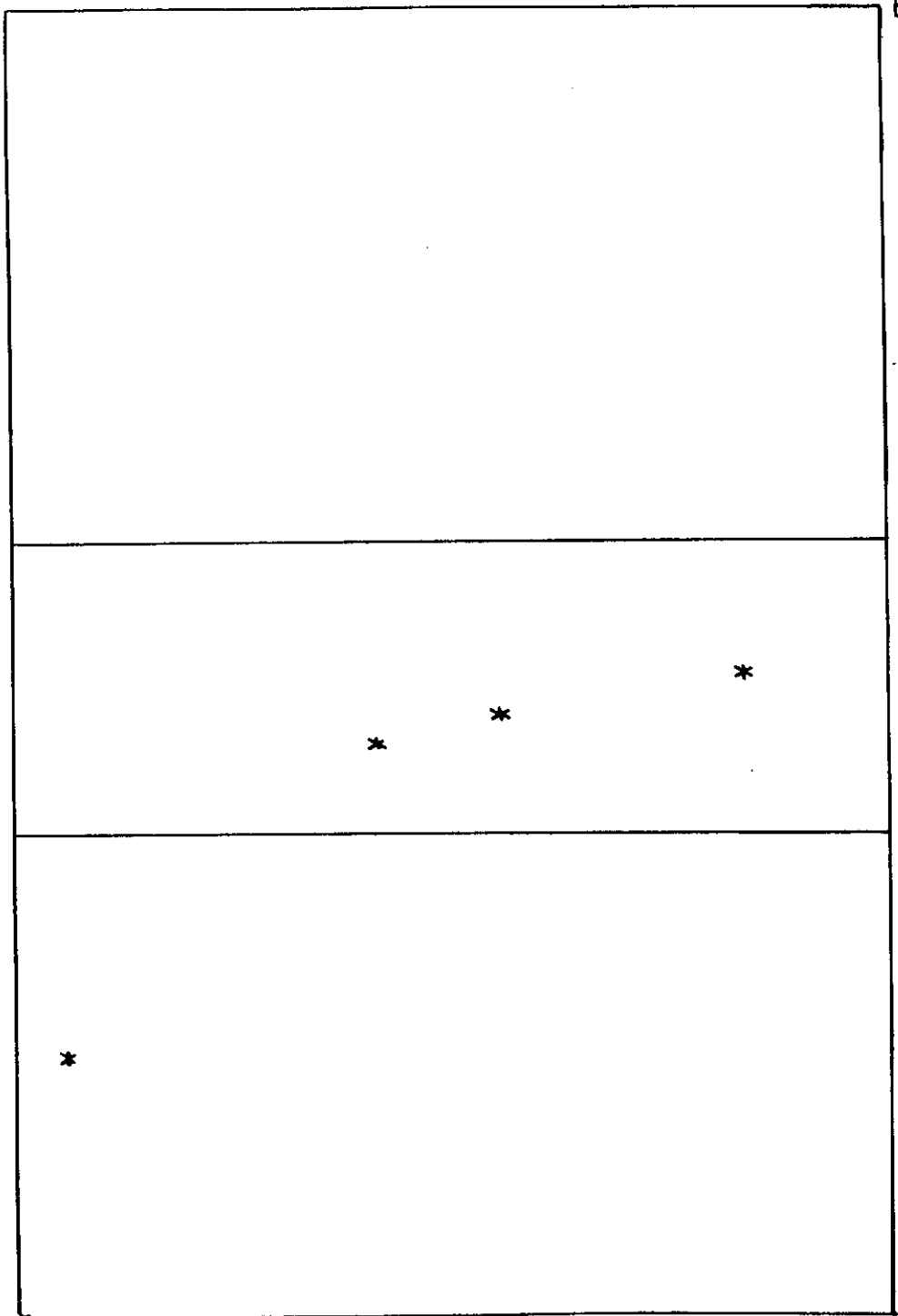
FROM  $\epsilon_1(\omega \rightarrow 0)$  WE GET  $\Gamma$



10



8





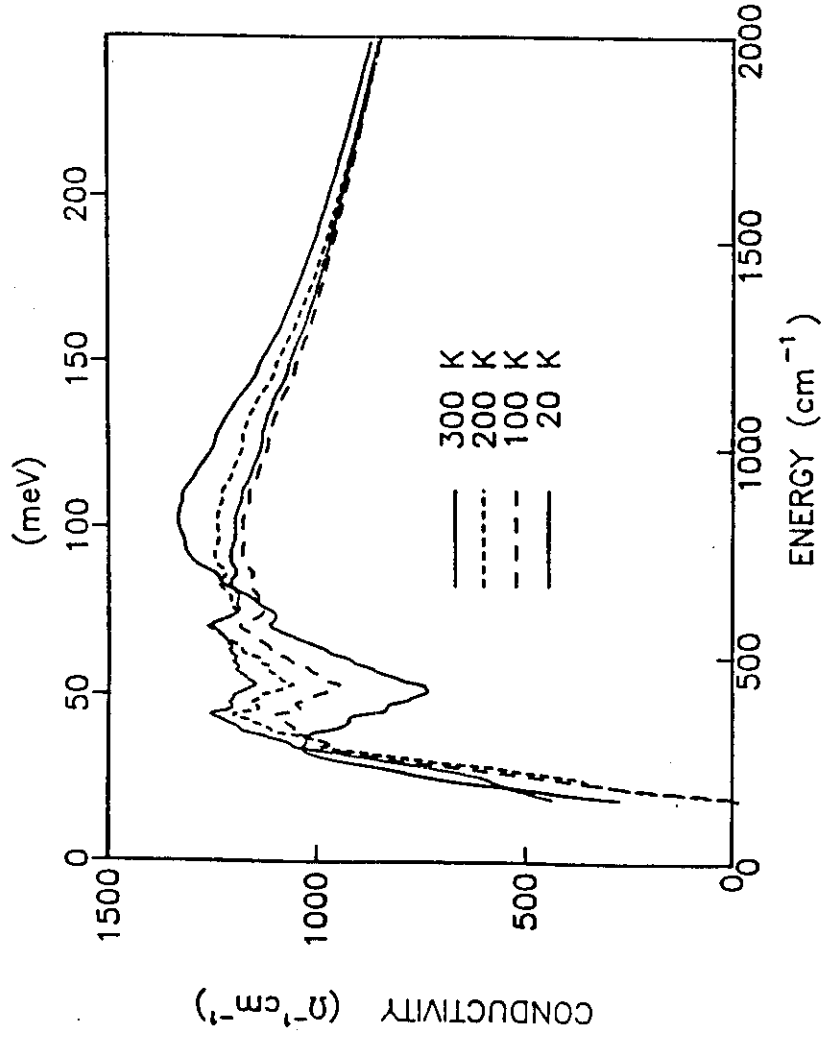
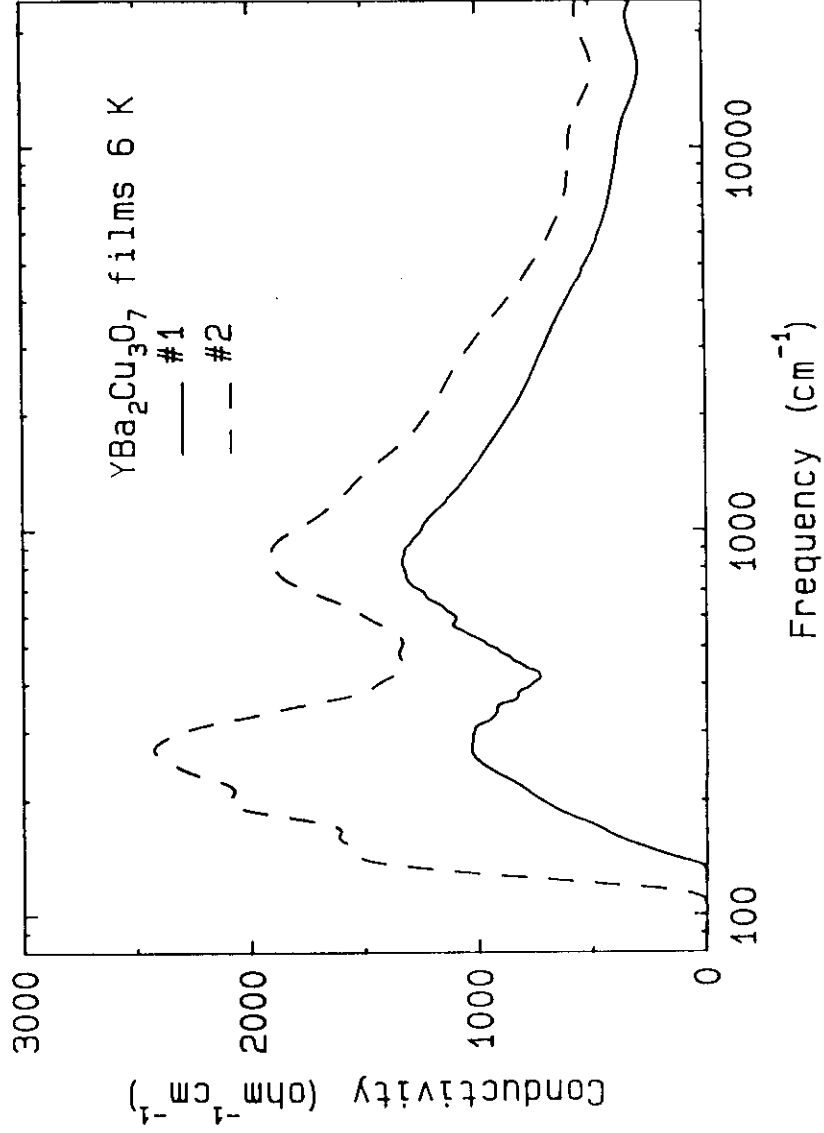


Fig. 1.



E-PH COUPLING TO 52 meV BRANCH:

$$\epsilon(\omega) = \epsilon_b + \epsilon_0 + \frac{\omega_{pe}^2}{\omega_e^2 - \frac{g^2}{m^*M\omega_0^2} D(\omega) - \omega^2 - i\omega\gamma_e}$$

$$D(\omega) = \frac{\omega_0^2}{\omega_0^2 - \omega^2 - i\omega\gamma_0}$$

$\left. \begin{matrix} \omega_{pe} \\ \omega_e \\ \gamma_e \end{matrix} \right\}$  ELECTRONIC BAND

$\left. \begin{matrix} \omega_0 \\ \gamma_0 \end{matrix} \right\}$  PHONON

$$\omega_g^2 = \frac{g}{m^*M} \quad \text{COUPLING FREQUENCY}$$

T. TILHUSK & D. B. TANNER, 1989

T. TILHUSK, D. B. TANNER, 1989

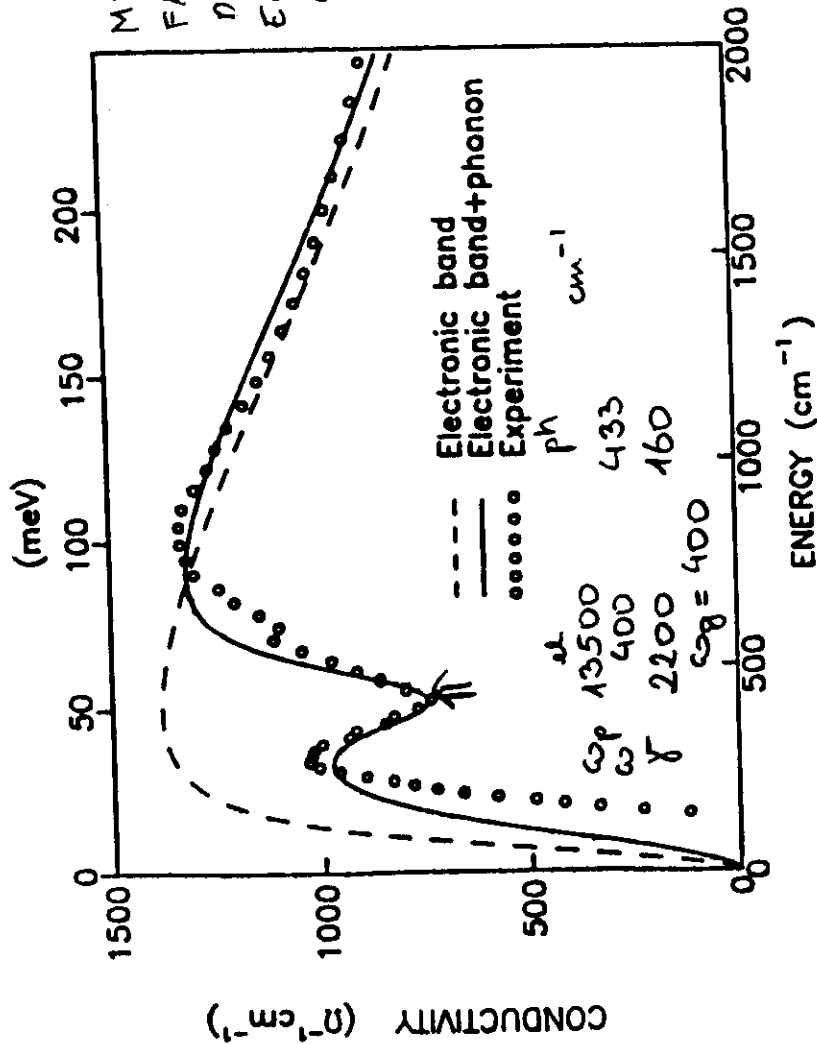


Fig 2.

## CONCLUSIONS

### ELECTRONS:

-NORMAL STATE:  
TWO-COMPONENT ABSORPTION

1. NARROW DRUDE PART
2. STRONG MID-IR BAND

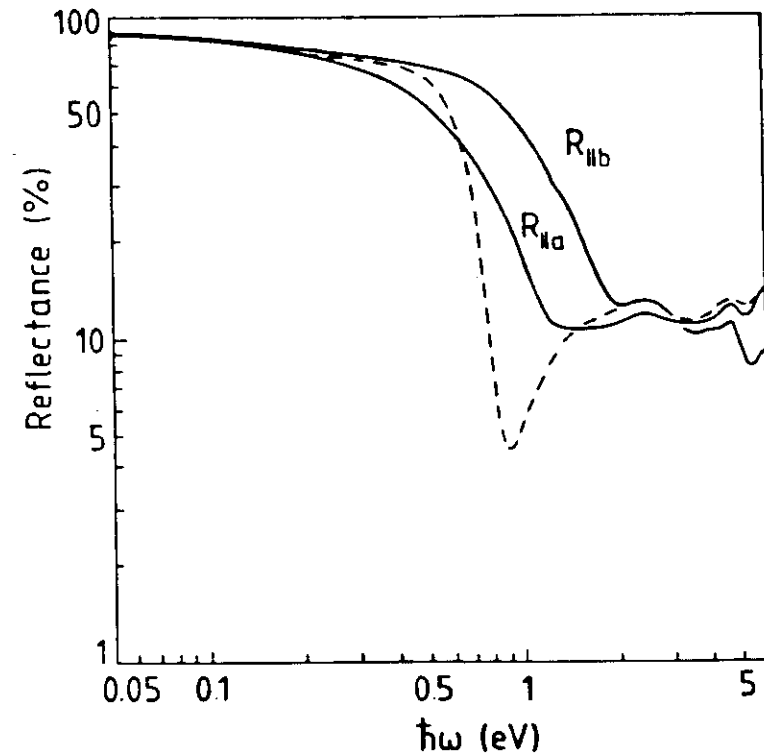
-SC STATE:

- CLEAN LIMIT
- MID-IR BAND ONLY

### PHONONS:

-NO SIGN OF DIRECT COUPLING  
ASSOCIATED WITH SUPERCONDUCTIVITY

-POSSIBLE COUPLING TO BOUND  
ELECTRONS



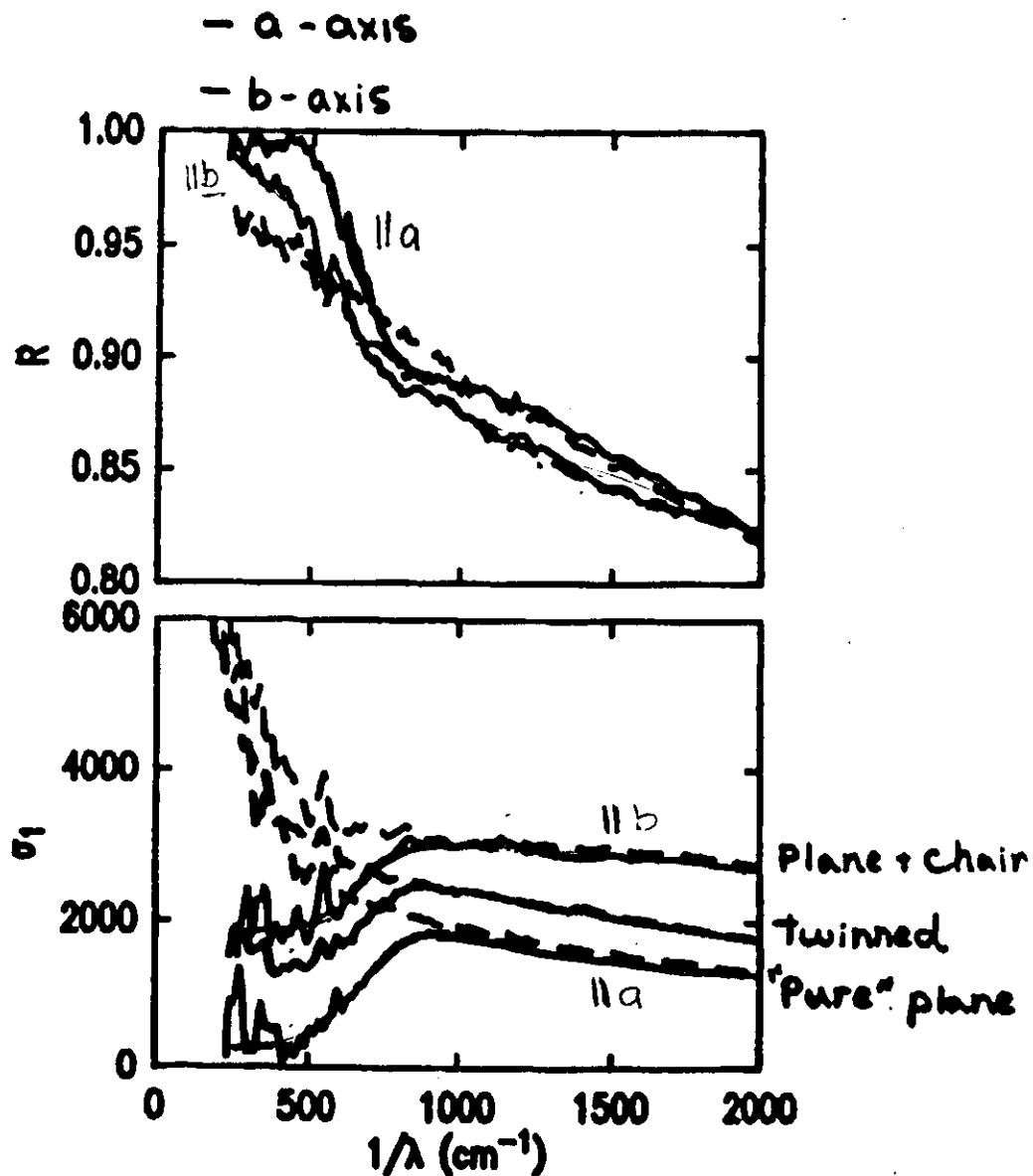
B. KOCH, H.P. GESERICH AND TH. WOLF:  
SOLID STATE COMM. 71, 495 (1989)

Fig. 1

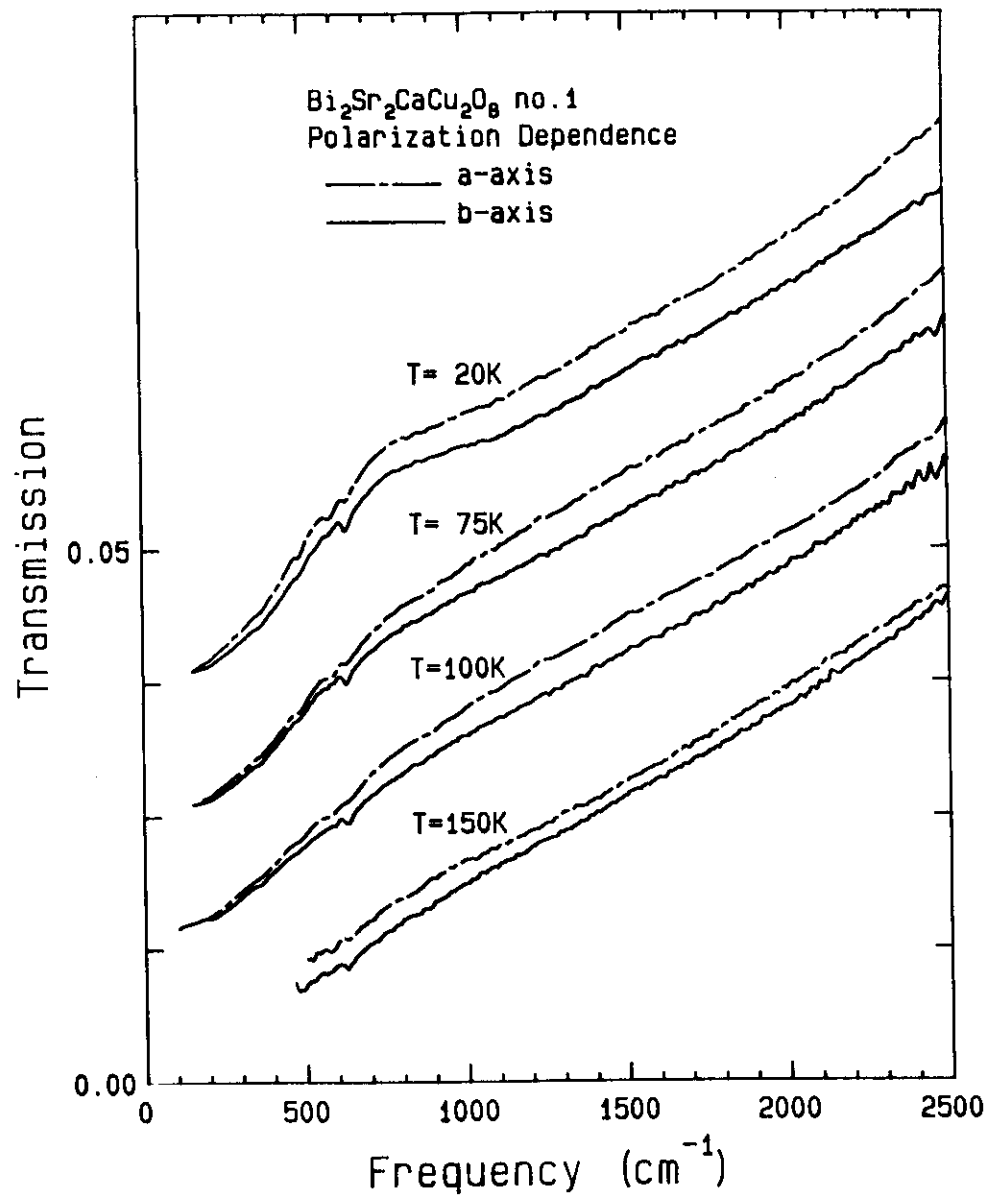
Z. SCHLESINGER ET AL:

Untwinned  $Y_1Ba_2Cu_3O_7$  PRL 65, 801 (1990)

D.B. ROMERO ET AL (1990)



-  $8KT_c$  gap - planes - isotropic



sufficiently close to the structural instability that even a single carrier locally changes the structure to that characteristic of the metallic (and superconducting) phase.

#### EXPERIMENTAL TECHNIQUES

The tetragonal semiconducting  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  ( $\delta=0.75$ ) samples were prepared by heating orthorhombic superconducting material ( $T_c=92$  K:  $a=3.8170$  Å,  $b=3.8585$  Å,  $c=11.6721$  Å,  $V=173.26$  Å<sup>3</sup>) in air at  $850^\circ\text{C}$  in an alumina boat for 3 h followed by rapid quenching to room temperature. The resulting sample was not a superconductor; resistivity measurements gave the high dc value and characteristic temperature dependence of  $\delta=0.75$ . X-ray powder patterns indicated a tetragonal unit cell:  $a=3.8590$  Å,  $b=3.8590$  Å,  $c=11.7949$  Å,  $V=175.65$  Å<sup>3</sup>. The oxygen content was determined by comparing these values with the lattice constants given by Tarascon *et al.*<sup>11</sup> For photoinduced absorption, the sintered pellet was then reground to micron-sized crystallites and mixed at a concentration of 2 wt. % with KBr powder (for the spectral range from 400–4000  $\text{cm}^{-1}$ ) or 1 wt. % with CaI powder (120–500  $\text{cm}^{-1}$ ). The mixture was pressed into thin dark grey semitransparent pellets, which were then reground and repressed to achieve greater homogeneity. This process was repeated until satisfactory transparency and homogeneity was achieved.

An IBM/98 (Bruker) Fourier-transform ir interferometer, modified to allow access onto the sample of the external beam from an Ar<sup>+</sup> laser, was used to cover the spectral range from 120 (0.015 eV) to 4000  $\text{cm}^{-1}$  (1 eV); the CaI cutoff set the low-frequency limit. For temperature control, the sample was placed on the cold finger of an Air Products Heli-tran system. The sample was optically pumped by the laser at 2.7 eV with a power level of 30  $\text{mW}/\text{cm}^2$ , and the fractional changes in ir transmission were measured<sup>12</sup> (with resolution of 2  $\text{cm}^{-1}$  in the far-infrared region and 4  $\text{cm}^{-1}$  in the mid-infrared region). The net change in the absorption coefficient ( $\delta\alpha$ ) was determined from the photoinduced change in transmission ( $\Delta T$ ); for small  $\Delta T$ ,  $-\Delta T/T = \delta(\alpha d)$  where  $d$  is the sample thickness. To obtain an acceptable signal-to-noise ratio, signal averaging ( $\sim 2$  h) was required.

#### EXPERIMENTAL RESULTS

Figure 1 shows the photoinduced absorption spectra for the semiconducting tetragonal phase  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  ( $\delta=0.75$ ) obtained in the spectral range from 120 to 4000  $\text{cm}^{-1}$  at 15 K, with the inset showing the photoinduced IRAV modes in greater detail. We found three major IRAV modes at 396, 436, and 520  $\text{cm}^{-1}$  and four major photoinduced bleachings at 192, 219, 362, and 598  $\text{cm}^{-1}$ . In addition, a broad electronic absorption peak at 1050  $\text{cm}^{-1}$  ( $\sim 0.13$  eV) was observed.

In Fig. 2 we compare the ir spectra of  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  ( $\delta=0.75$ ) at 15 and 300 K, with the ir spectrum of superconducting  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  ( $\delta < 0.2$ ). For  $\delta=0.75$ , vibrational modes were found at 164, 191, 216, 252, 361, 472,

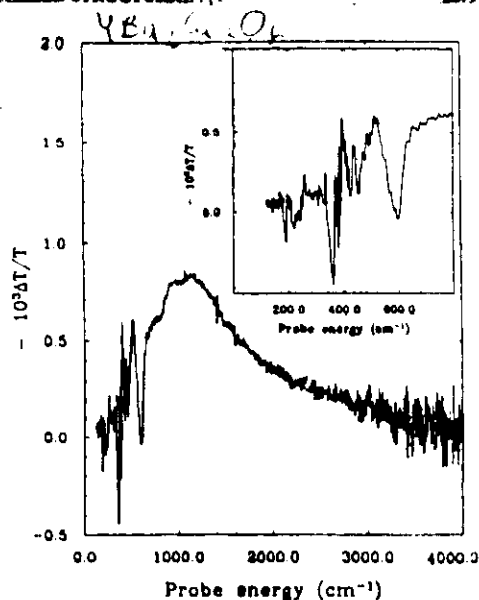


FIG. 1. Photoinduced absorption spectrum of  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  ( $\delta=0.75$ ) at 15 K (2.7-eV pump at 30  $\text{mW}/\text{cm}^2$ ); inset shows detailed IRAV features.

532, 583, and 632  $\text{cm}^{-1}$  with the sample at 300 K. Upon cooling to 15 K, we observed an increase in oscillator strength of the 359- $\text{cm}^{-1}$  mode and a 19- $\text{cm}^{-1}$  blueshift of the 583- $\text{cm}^{-1}$  mode, consistent with values reported earlier.<sup>13</sup> For the orthorhombic phase ( $\delta < 0.2$ ), we observed relatively weak ir vibrational features at 336, 454, 493, 528, and 602  $\text{cm}^{-1}$  at 300 K. They appear weak in transmission due to the strong free-carrier background in the highly conducting sample. Reflectivity data<sup>14</sup> show quantitatively that the 528- and 602- $\text{cm}^{-1}$  absorptions are relatively weak compared to the modes below 400  $\text{cm}^{-1}$ . In contrast, for the tetragonal phase we find that the modes at 532, 586, and 632  $\text{cm}^{-1}$  are much stronger than those in the far-infrared region. The ir modes associated with the two structures can be compared with the photoinduced features shown in Fig. 1 (IRAV modes at 396, 436, and 520  $\text{cm}^{-1}$  and bleachings at 192, 219, 362, and 598  $\text{cm}^{-1}$ ). In particular, the bleaching frequencies suggest that photoexcitation locally converts the structure from tetragonal to orthorhombic.

Artifacts associated with the photoinduced absorption technique can be generated by sample heating by the incident laser pump beam. In systems such as oxide superconductors, small changes in the "dark" ir absorptance caused by a strong temperature dependence can be incorrectly interpreted as photoinduced absorptions. Small shifts in frequency with changes in temperature would appear as derivative-shaped signals in the photoinduced spectra; changes in linewidth would appear as second-derivative-shaped signals. Similarly, a decrease in intensity,

