



INTERNATIONAL ATOMIC ENERGY AGENCY  
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
**INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS**  
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UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



**INTERNATIONAL CENTRE FOR SCIENCE AND HIGH TECHNOLOGY**

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SMR/543 - 21

EXPERIMENTAL WORKSHOP ON  
HIGH TEMPERATURE SUPERCONDUCTORS AND RELATED MATERIALS  
(BASIC ACTIVITIES)

(11 February - 1 March 1991)

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" Tunnelling in Conventional and High  $T_c$  Superconductors "

presented by:

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These are preliminary lecture notes, intended only for distribution to participants.



M. Gurevitch

# Two Lectures on Tunneling

(Trieste, Feb 1991)

Plan:

- Lecture 1:
1. History of tunneling: Sch. eq. n; Oppenheimer; Fowler & Nordheim, Ya. Fraunkel, Gurevitch, McMillan-Parell, Josephson
  2. Turn across the rectangular barrier; some numbers
  3. Tunneling at  $V \leq 1V$  - background conductance; Eschinger, & El barrier height and width
  4. Superconducting density of states
  5. N-I-N, N-I-S, S-I-S tunn. curves; examples
  6. Josephson effect, applications:  $T_{JS}$ ,  $V_m$ , RSFQ.

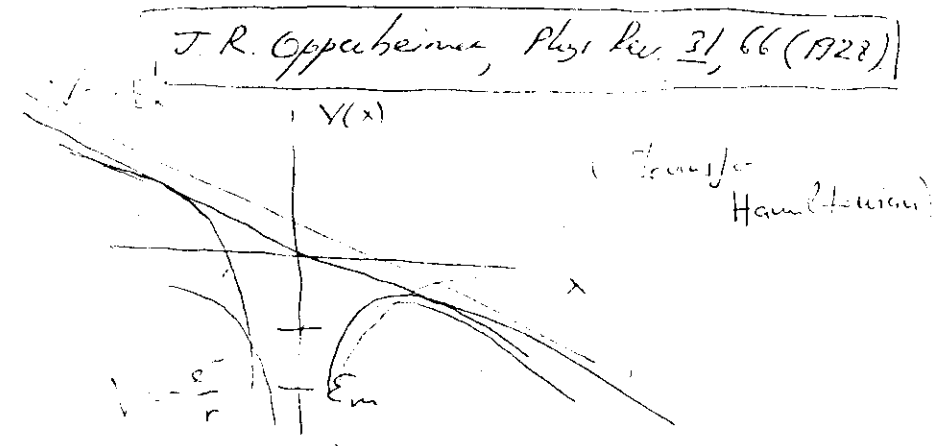
~~all about tunneling circuits, etc~~  
~~at the end of the course~~

1. Some points from Lecture 2 revisited:
  - a)  $dI/dV = N_s(E)$
  - b) Harrison's argument
2. Tunneling and coherence length
3. Tunneling spectroscopy
4. Tunneling in HTSC
  - a) Different kinds of junctions
  - b) Josephson tunneling; prospects for applications
  - c) Large area vs point contact tunneling

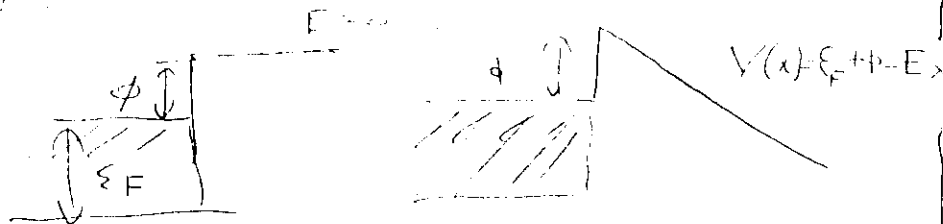
## 1. Historical background:

(1) (2)

1928: field emission of atomic hydrogen



same year | Fowler and Nordheim field emission  
 [Proc Roy Soc (London) A119, 173 (1928)]  
 continuous from the bulk metal into vacuum



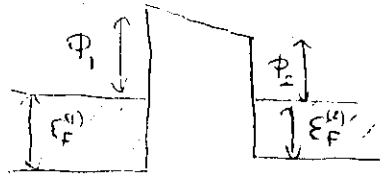
V. L. Frankel (Phys. Rev. 36, 1664 (1910))

metal junctions

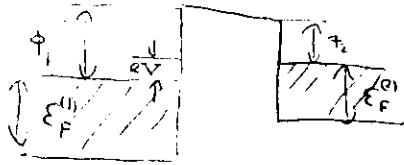
alpha-decay (Gamow), 1928

Frohlich (1932)

work function



vacuum barrier



elastic or "horizontal" tunneling

A number of people considered metal-semiconductor junctions (Wilson and others).

Sumner-Jeld and Bethe (1933): insulator as a barrier.

At that time results applied to pressed metallic contacts

The discovery that thermal oxidation gives uniform thin oxide barriers was made only in 1960's

J.C. Fisher and I. Giaever, J. Appl. Phys. 32, 172 (1961).

I. Giaever, PR 15, 147 (60)  
15, 464 (60).

Zener (1974) - internal field emission

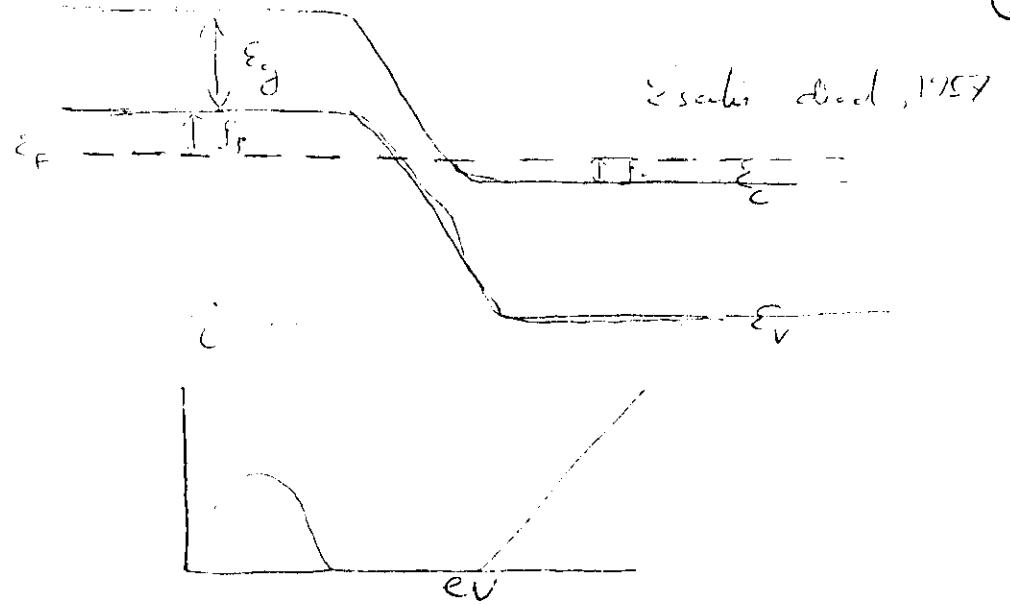
Esaki (1957): tunnel diode (p-n)

legendarily defect p-n diode

2

Esaki

Esaki



Esaki diode, 1957

Giaever, 1960: Al-Al<sub>2</sub>O<sub>3</sub>-Pb, measured  $A_{p/b}$ .

NB the  $G = \frac{dI}{dV}$  appeared to be a direct measure of the many-body bulk DOS in contrast to the predictions of one-electron theory  
McMillan & Rowell (late 60's): tunneling spectroscopy  
Giaever's discovery also led to re-examination of a theory.

Also, J. Nicol, S. Shapiro and P.H. Smith, PR 15, 461 (60).

Another major discovery was that of  
 the Josephson tunneling effects

(4)

B.D. Josephson, Phys. Letters 1, 251 (1962)

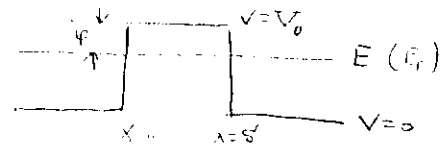
J.W. Anderson and J. Rowell, PRL 10, 230 (1963)

J.M. Rowell, PRL 11, 200 (63)

M.D. Fiske, Rev. Mod. Phys. 36, 221 (1964)

2. Tunneling across the rectangular barrier:

(5)



$$\hat{H}\psi = E\psi; \quad \hat{p} = \frac{\hbar}{i}\nabla; \quad \hat{p}^2 = \frac{\hbar^2}{2m}\nabla^2 = -\frac{\hbar^2}{2m}\Delta; \quad \hat{H} = \hat{K} + \hat{V} = -\frac{\hbar^2}{2m}\Delta + V(x)$$

$$-i = \frac{\hbar}{i}, \quad (-i)(-i) = +i^2 = -1, \quad \frac{\hbar}{i} \cdot \frac{\hbar}{i} = -1$$

$$\nabla^2\psi + \frac{2m}{\hbar^2}(E-V)\psi = 0;$$

$$k_1 = \frac{1}{\hbar}\sqrt{2mE}; \quad k_2 = \frac{1}{\hbar}\sqrt{2m(E-V_0)}; \quad k_3 = k_1,$$

$$\begin{array}{l} x < 0: \psi = e^{ik_1x} + Ae^{-ik_1x} \\ 0 < x < S: \psi = Be^{ik_2x} + Ce^{-ik_2x} \\ x > S: \psi = De^{ik_1x} \end{array} \left\{ \begin{array}{l} A, B, C, D \text{ determined from} \\ \text{matching of the cont. } \psi, \psi' \\ \text{at } x=0, S. \end{array} \right.$$

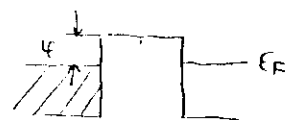
$$I_{\rightarrow} \propto x < S, \quad \alpha_2 = \frac{1}{\hbar}\sqrt{2m(V_0-E)}, \quad k_2 = i\alpha_2$$

Assume that  $e^{-\alpha_2 S} \ll e^{\alpha_2 S}$  i.e.  $\alpha_2 S \gg 1$ . Then transmission coefficient

$$T = |D|^2 = \frac{16e^{-2\alpha_2 S}}{\left[1 + \left(\frac{\alpha_2}{k_1}\right)^2\right]\left[1 + \left(\frac{k_1}{\alpha_2}\right)^2\right]}$$

(see facts in QM,  
 e.g. D. Bohm, Quantum Theory,  
 p. 240)

It is an interesting analogy with tunneling between metals



$E = E_F$ ;  $V_0 - E = V_0 - E_F = \phi$ , work function, or barrier height.

$$\frac{k_1^2 k_2^2}{(k_1^2 + k_2^2)(k_1^2 + k_2^2)} = \frac{k_1^2 k_2^2}{(k_1^2 + k_2^2)^2} = \frac{\epsilon_F \phi}{(\epsilon_F + \phi)^2}$$

$$= \frac{\epsilon_F \phi}{(\epsilon_F + \phi)^2} = \frac{\phi/\epsilon_F}{1 + (\phi/\epsilon_F)} \approx \frac{\phi}{\epsilon_F} \text{ assuming } \phi \ll \epsilon_F$$

(say 2v vs 10v)

$$T \approx \frac{16}{\epsilon_F} \phi \ell - 2 \frac{\sqrt{\phi} 2m \cdot S}{\hbar}$$

[the 2nd term is negligible for small  $\epsilon_F$ ]

$$T \approx \frac{16}{\epsilon_F} \phi \ell - \frac{2^{3/2} m^2 \phi^{3/2} S}{\hbar}$$

Note:  $G \propto T$   
 $R \propto T^{-1}$

Current in a field will be  $j = \sigma E$   
or  $i = \sigma V$ ,  $i = 6V$   
ie  $i \propto \text{current} \cdot \phi \cdot \ell$  - this is the correct form!

Some numbers:  $\hbar = 1.05 \cdot 10^{-27}$  erg sec.  
 $m_e = 9.1 \cdot 10^{-28}$  g.  
if we use  $\phi$  in eV and  $S$  in  $\text{\AA}$ , we must use coefficient of  $1 \text{ eV} = 1.602 \cdot 10^{-12}$  erg and  $1 \text{ \AA} = 10^{-8}$  cm

$$-\alpha \ell; \alpha = \frac{2^{3/2}}{\hbar} m^2 \phi^{3/2} S =$$

$$= \frac{2^{3/2} \cdot (9.1 \cdot 10^{-28})^{3/2} \cdot (1.602 \cdot 10^{-12})^{3/2} \cdot 10^{-8}}{1.05 \cdot 10^{-27}} (\phi^{3/2} S) =$$

$$= 1.03 \phi^{3/2} S \approx \phi^{3/2} S \text{ where } [\phi] = \text{eV}; [S] = \text{\AA}$$

~~$T \approx \frac{16}{\epsilon_F} \phi \ell - \frac{2^{3/2} m^2 \phi^{3/2} S}{\hbar}$~~

Note: the absence of numerical coefficient is just the coincidence; also: numerical coefficient has dimensions, such that  $[A \phi^{3/2} S] = 1$ .

$$T \approx \frac{16 \phi}{\epsilon_F} \ell - \phi^{3/2} S; [\phi] = \text{eV}; [S] = \text{\AA}$$

Some numbers:  
Take  $\phi = 2 \text{ eV}; S = 15 \text{ \AA}; \epsilon_F = 10 \text{ eV}$ .

Then  $T \approx 3.2 \cdot \ell^{-2.5} \cdot 15 \approx 2 \cdot 10^{-9}$   
(2,15)

For a barrier one monolayer thick,

$$S = 12 \text{ \AA}$$

$$T = 3.2 \cdot \ell^{2.5} \cdot 4.26 \cdot 10^{-9} = 1.36 \cdot 10^{-7}$$

(2,12)

$$\frac{T_{(2,12)}}{T_{(2,15)}} \approx 0.7 \cdot 10^2 = 70;$$

How do we get from  $T$  to the current?

(8)

$T$  is dimensionless.

$i = GV$ , therefore we will have to

have  $i = \text{const} \cdot T \cdot \frac{e^2}{h} V$ , where  $\frac{e^2}{h}$  is the

fundamental unit of conductance.

Let's write the incident current in the interval  $E \in [E, E+dE]$  (for a wave normalized to  $|a|^2=1$ )

$$i_{inc}^{E, dE} = e v R = e \cdot \frac{\hbar k}{m} \cdot \left( \frac{dk}{dE} \right) \cdot f(E) dE \quad (2)$$

$f(E)$  - Fermi function.

$\frac{dk}{dE}$ : 1-Dim. DOS: density of points in  $k$ -space is more equidistant at  $\frac{\pi}{L}$ ; so in  $dk$ , there are  $\frac{dk}{(\frac{\pi}{L})}$  points, or, for  $L=1$ ,

$$= \frac{dk}{\pi}; \quad E = \frac{\hbar^2}{2m} k^2; \quad dE = \frac{\hbar^2 k}{m} dk; \quad \text{so } \frac{dk}{dE} = \frac{m}{\hbar^2 k}$$

$$\pm \left[ \frac{dk}{dE} = \frac{m}{\hbar^2 k} \right]$$

Note: velocity is  $\propto k$   
DOS  $\propto \frac{1}{k}$ , hence

every dependence in the DOS cancels

out: Harrison's argument

PR 127, 25 (1961) In a

represent.

if current does not cancel

so we get from (2)

$$i_{incident}^{E, dE} = e \frac{\hbar k}{m} \frac{m}{\hbar^2 k} f(E) dE = \frac{e}{\hbar} f(E) dE$$

Let's: if  $dE = eV$ , ( $f=1$ ),  $i(E, dE) = 2 \frac{e^2}{h} dV$  - current units. The

meaning is not clear, however (indeed,  $\frac{h}{e^2} \sim 10,000 \Omega$ )

that's the equivalent to resistance of the argument

\* Note:  $L=1$  is equivalent to assuming  $|a|^2=1$ ; alternatively,  $\frac{dk}{dE} = \frac{1}{\hbar^2 k}$  and  $|a|^2 = \frac{1}{2}$ ; (indeed,  $\frac{1}{2}$  is the value for  $|a|^2=1$ ?)

Tunneling

(13)



Background!

Image files were considered by J.G. Simmons \*

see J.G. Simmons, J. Appl. Phys 34, 1753 (1963)  
34, 2581 (1967)  
PR 10, 10 (1967)

and in Burstein  
also described in J.P.M. Rowell's article in Burstein

We said that  
At very low  $eV$ ,  $I_{tun}$  is obvious: this regime really nonexistent, if one looks carefully along a

plot for the expansion of  $T = \frac{|A|^2}{|B|^2}$   
for  $mV$ ; At  $eV \gtrsim 2V$  volt current becomes exponential (Fowler-Nordheim regime).

Next interesting domain is in the range  $0-1V$ .

Look again at (11):

$$j \propto T, \quad j = j_0 \bar{\varphi} \exp(-S \bar{\varphi}^{1/2})$$

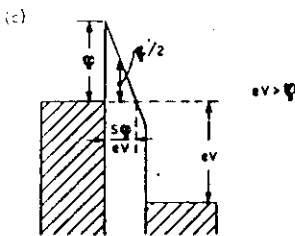
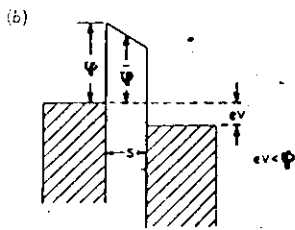
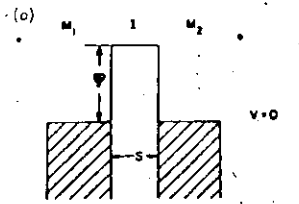


Fig. 1. Representation of the simplest type of potential barrier between two metals. (a) The barrier is symmetrical for  $V=0$ . Shown are the average height and thickness of the barrier for (b) intermediate ( $eV < \phi$ ) and (c) high ( $eV > \phi$ ) voltage ranges.

In case of  $eV < \phi$  intermediate range)

$$J = J_0 \left\{ \left( \phi - \frac{eV}{2} \right) \exp \left[ -S \left( \phi - \frac{eV}{2} \right)^{3/2} \right] - \left( \phi + \frac{eV}{2} \right) \exp \left[ -S \left( \phi + \frac{eV}{2} \right)^{3/2} \right] \right\}$$

Therefore, dropping terms of the order of  $V^4$  and higher finds

$$I = \alpha (V + \delta V^3)$$

$$J_{21} = J_0 (\bar{\phi} + eV) \exp \left[ -S (\bar{\phi} + eV)^{3/2} \right] \quad (14)$$

$$J = J_{12} - J_{21}^* \quad ; \quad \text{(slow barriers)} \quad \text{where } \bar{\phi} \text{ is the tunneling energy (slow barriers) and } J_{21}^* \text{ is the other direction}$$

in the intermediate range  $eV < \phi$

$$S = \text{const, but } \bar{\phi} = \phi - \frac{eV}{2};$$

Substituting, we obtain

$$J = J_0 \left\{ \left( \phi - \frac{eV}{2} \right) \exp \left[ -S \left( \phi - \frac{eV}{2} \right)^{3/2} \right] - \left( \phi + \frac{eV}{2} \right) \exp \left[ -S \left( \phi + \frac{eV}{2} \right)^{3/2} \right] \right\}$$

For  $eV < \phi$ , expanding, and keeping terms to  $V^3$

$$I = \alpha (V + \delta V^3) \text{ or}$$

$$\frac{dI}{dV} = \alpha + 3\alpha\delta V^2;$$

Note: where  $\frac{dI}{dV} = 2\alpha$ ,  $3\alpha\delta V^2 = \alpha$ ;  $V^* = \left( \frac{1}{3\delta} \right)^{1/2}$ ; or  $\delta = \frac{1}{3V^{*2}}$

From Simmons (J Appl. Phys. 34, 238 (63)) =



Data of J. M. Rowell

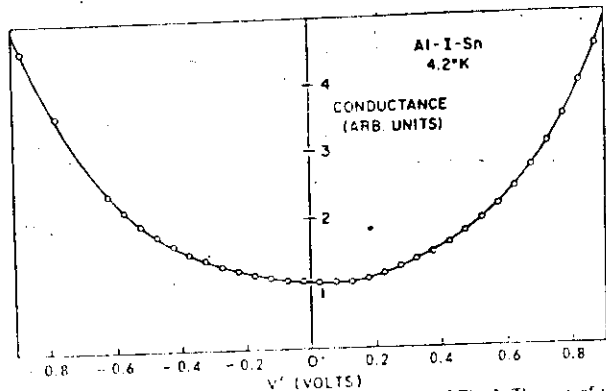
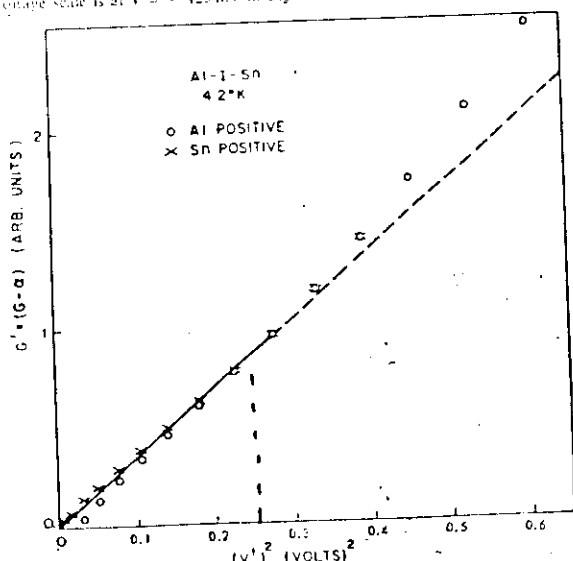
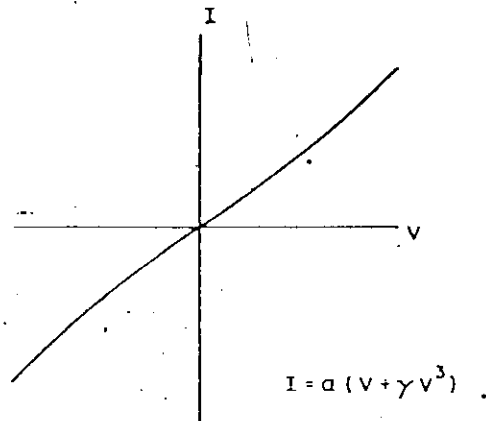


Fig. 5. Conductance versus voltage  $V^1$  for the junction of Fig. 3. The zero of this  $V^1$  voltage scale is at  $V = -125$  mV in Fig. 3.



$$G - a = 38V^2$$

$$V^1 = 500 \text{ mV}$$



$$\frac{dI}{dV} = G(V) = a(1 + 3\gamma V^2)$$

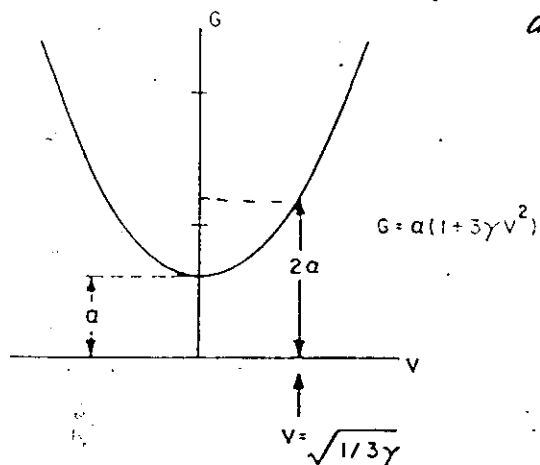


Fig. 2. Current and conductance versus voltage for an ideal symmetrical barrier of the type shown in Fig. 1 (a). The conductance is a constant plus a parabolic term which is symmetric about  $V = 0$ .

$$c = \cancel{0.015} 0.0115 \frac{E^2}{6} - \frac{0.0115}{\sqrt{4}} S \approx 0.0115 \frac{E^2}{6};$$

val.  $S$  in  $\bar{A}$ ,  $S > 10\bar{A}$ , i.e.  $S^* \gg S$

Also from previous

$$\alpha = 3.16 \cdot 10^{10} \frac{\bar{\varphi}^{\frac{1}{2}}}{S} \exp(-S\bar{\varphi}^{\frac{1}{2}})$$

Let us call  $S\bar{\varphi}^{-\frac{1}{2}} = f$ . Then

$$\gamma = 0.0115 f^2, \text{ or } f = \left( \frac{\gamma}{0.0115} \right)^{\frac{1}{2}} = \frac{1}{\sqrt{\gamma}} \left( \frac{1}{0.0115 \cdot 3} \right)^{\frac{1}{2}} =$$

$$= \frac{5.38}{\sqrt{\gamma}};$$

$$\frac{\gamma}{3.16 \cdot 10^{10}} = \frac{1}{f} \exp(-f\bar{\varphi}); \quad -f\bar{\varphi} = \ln \frac{\alpha f}{3.16 \cdot 10^{10}}, \quad f\bar{\varphi} = \ln \frac{3.16 \cdot 10^{10}}{\alpha f};$$

$$\bar{\varphi} = \frac{1}{f} [\ln 3.16 + 10 \ln 10 - \ln \alpha f] = \frac{1}{f} (24.18 - \ln \alpha f)$$

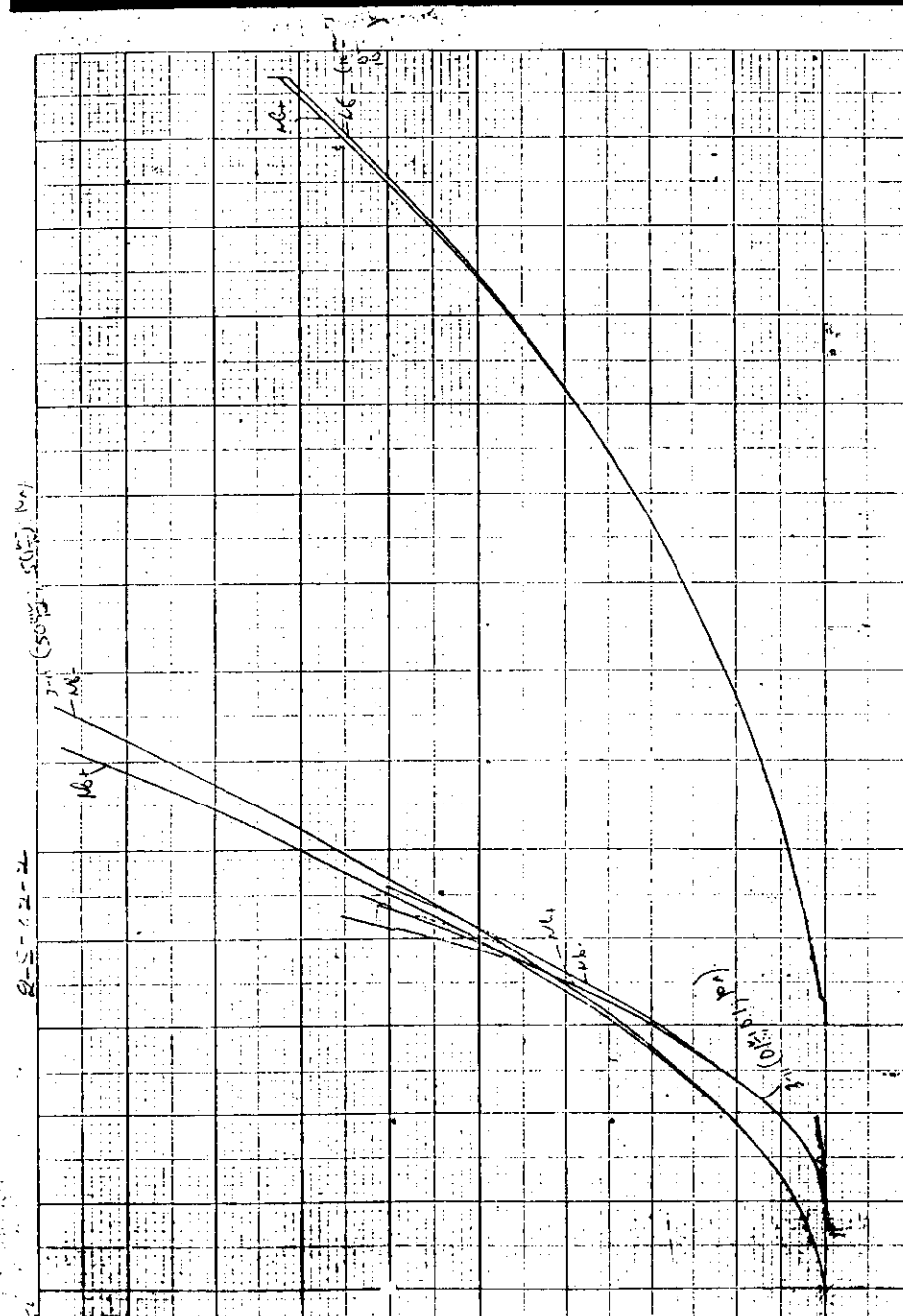
So we have

$$\begin{cases} f = \frac{5.38}{\sqrt{\gamma}} \\ \bar{\varphi} = \frac{1}{f} (24.18 - \ln \alpha f) \\ S = f \bar{\varphi}^{\frac{1}{2}} \end{cases}$$

where we know (usually)  
 $V^*$  and  $\alpha$ .

Example:  $V^* = 0.54v$ ;  $\alpha = 6.91 \text{ mhos/cm}^2$

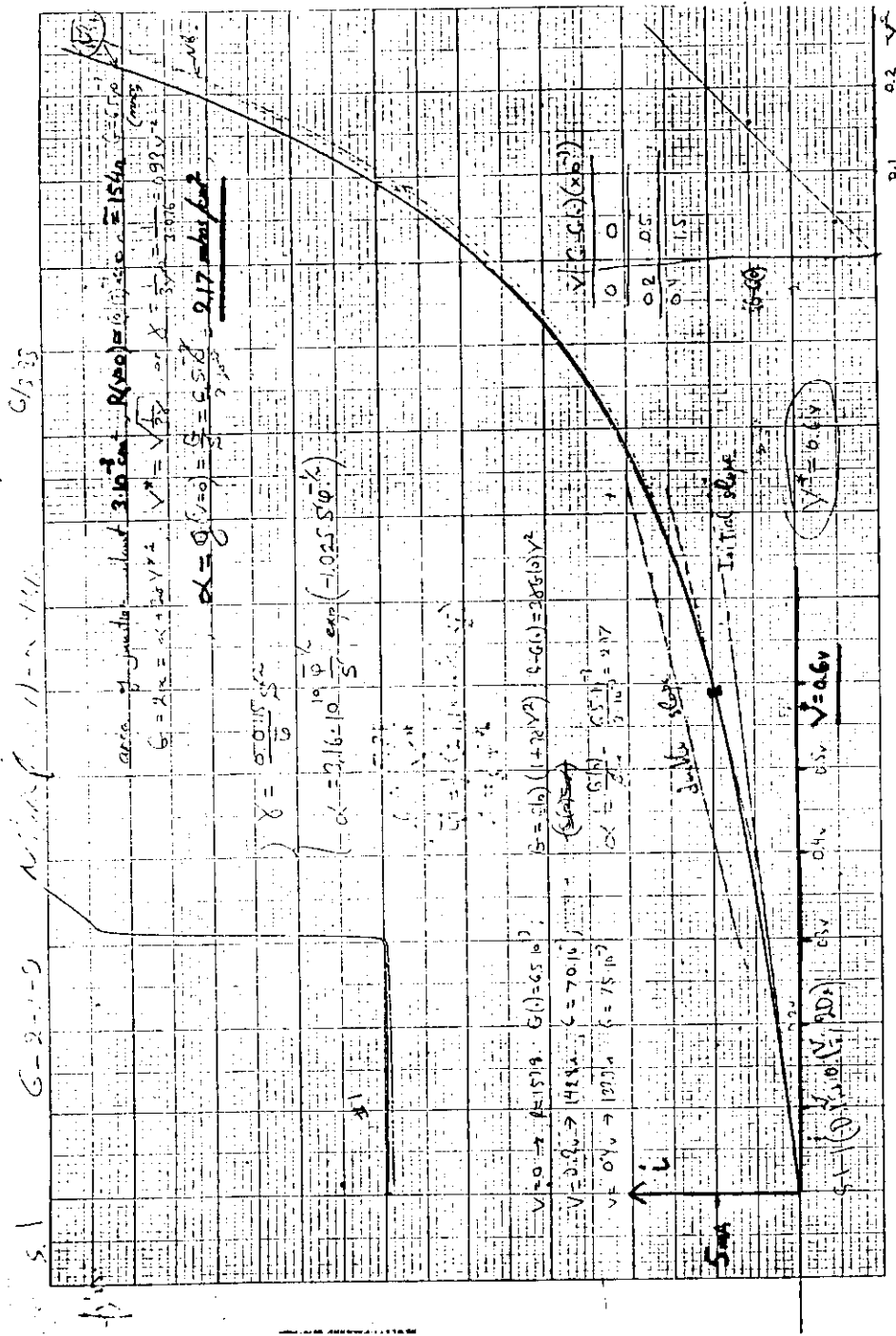
$$f = 9.96; \quad \bar{\varphi} = 2.0v; \quad S = 14A; \quad (\text{correct})$$



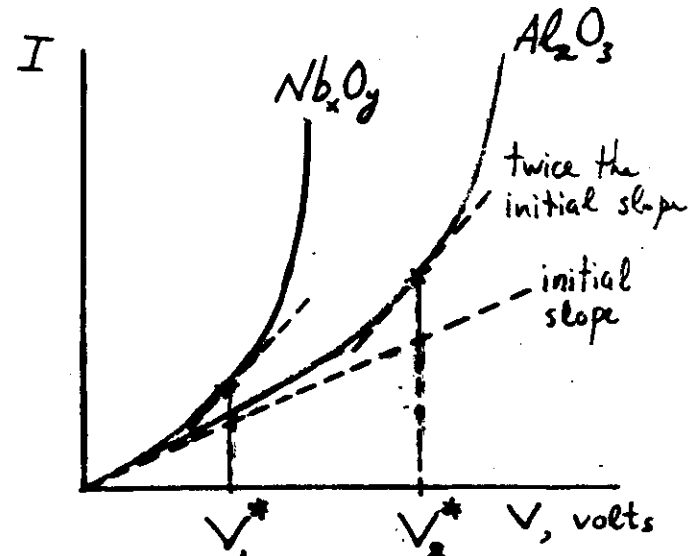
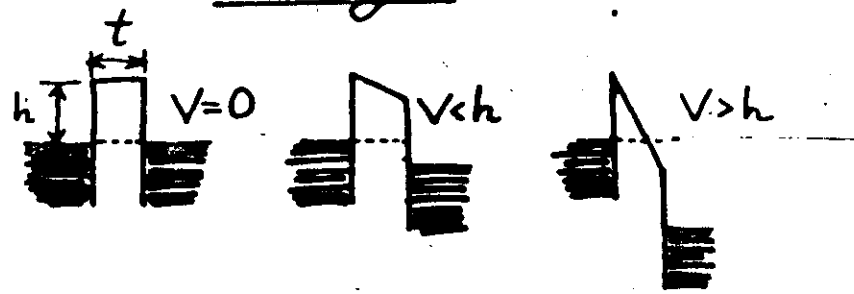
ily example  $V^* = 0.6 v$ ;  $\alpha = 2.17 \text{ mho/cm}^2$

$\xi = \frac{5.73}{0.6} = 9.97$ ;

$\bar{v} = 2.36 v$ ;  $\xi = 13.8 \text{ \AA}$  ;



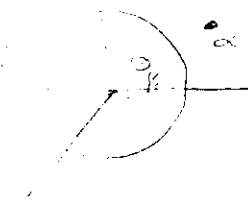
# I-V curves at higher voltage



Nb:  $t = 26 \text{ \AA}, h = 0.31 \text{ V}$   
 with Al:  $t = 135 \pm 1.0 \text{ \AA}, h = 2.0 \pm 0.2 \text{ V}$

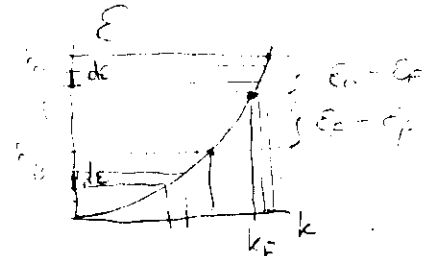
## Excitations:

Excitation from the ground state into  $\epsilon_1$



We measure energies from  $\epsilon_F$

$$E = (\epsilon_\alpha - \epsilon_F) + (\epsilon_F - \epsilon_\beta)$$

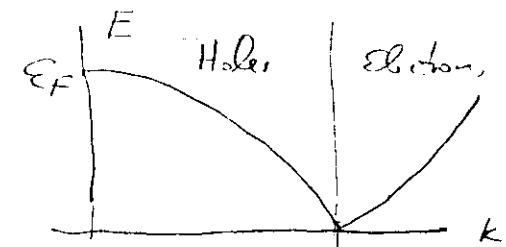
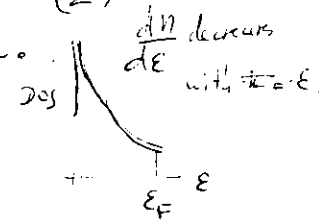


$$\epsilon = \frac{\hbar^2 k^2}{2m}$$

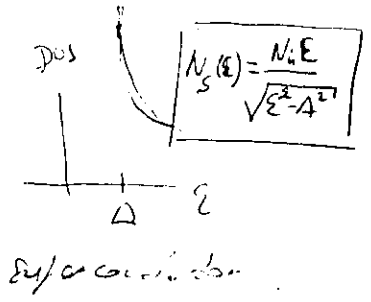
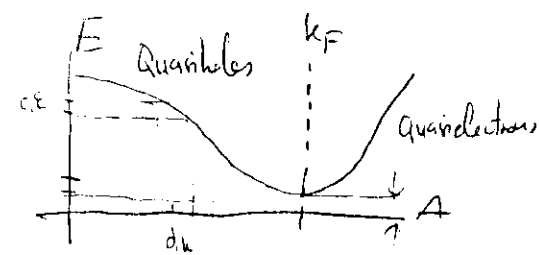
$\frac{dk}{2\pi}$  points to  $dk$

Excitation energy is always positive

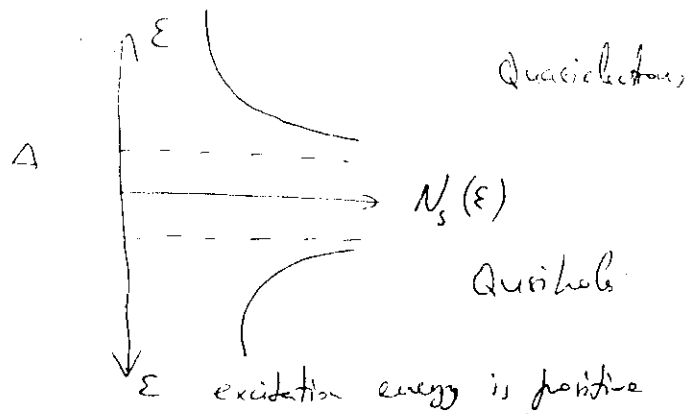
$$E = |\epsilon - \epsilon_F|$$



normal metal



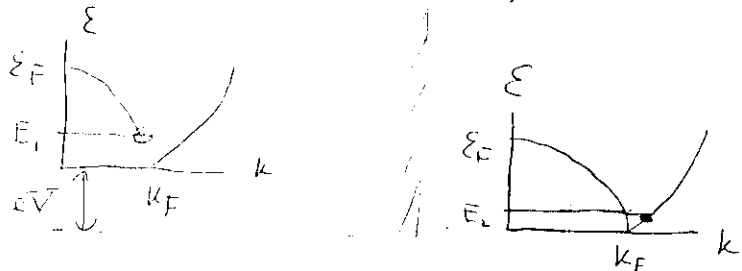
$$N_s(E) = \frac{N_s E}{\sqrt{E^2 - \Delta^2}}$$



$$I_{\text{net}}(T=0) = \frac{2\pi c A}{t} \int_0^{eV} |T_{12}|^2 N_1(\epsilon - eV) N_2(\epsilon) d\epsilon =$$

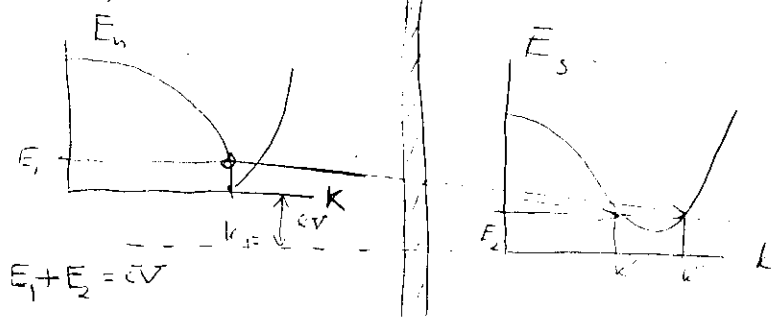
$$= 2\pi A \frac{e^2}{t} |T_{12}|^2 N_1(0) N_2(0)$$

For 2 normal metals, tunneling can be visualized as



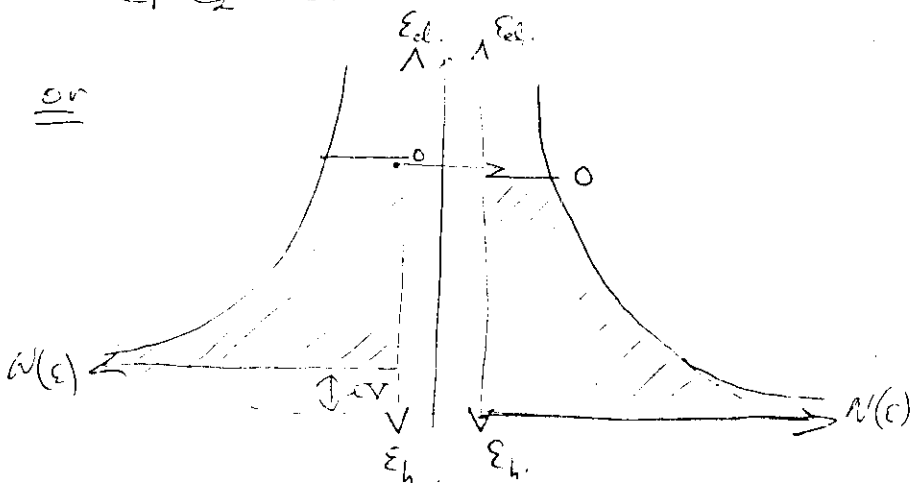
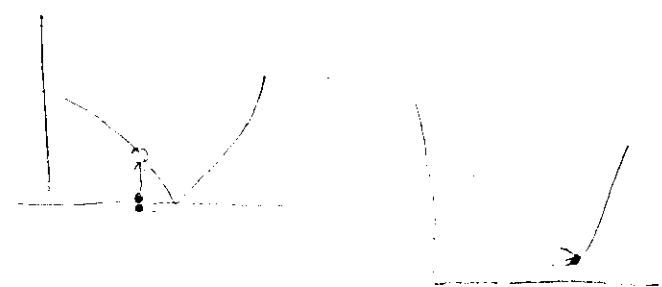
$$E_1 + E_2 = eV$$

N-I-S'



This is equivalent to considering the energy in  $k$  to be with out considering tunneling  $\epsilon$  about  $k_F$

S-I-S;



J-2 Tunneling

(11)

$$N_s(E) = N_2(e) u_s(E)$$

$$u_s(E) = \frac{E}{\sqrt{E^2 - \Delta^2}}$$

$$I_{ns} = ATN_1N_2 \int \frac{|E|}{\sqrt{E^2 - \Delta^2}} [f(E) - f(E - eV)] dE$$

$$\text{at } T=0 \quad f(E - eV) - f(E) = \begin{cases} 1 & 0 < E < eV \\ 0 & E < 0, E > eV \end{cases}$$

$$\text{so } I_{ns} = ATN_1N_2 \int_0^{eV} u_s(E) dE$$

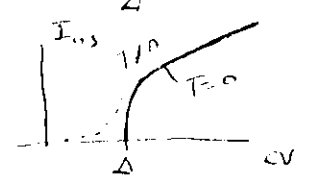
$$G_{ns} = \frac{dI_{ns}}{dV} = cATN_1N_2 u_s(eV)$$

i.e.  $G_{ns}$  close to  $T=0$  gives  $u_s(E)$ ,  $E = eV$ .

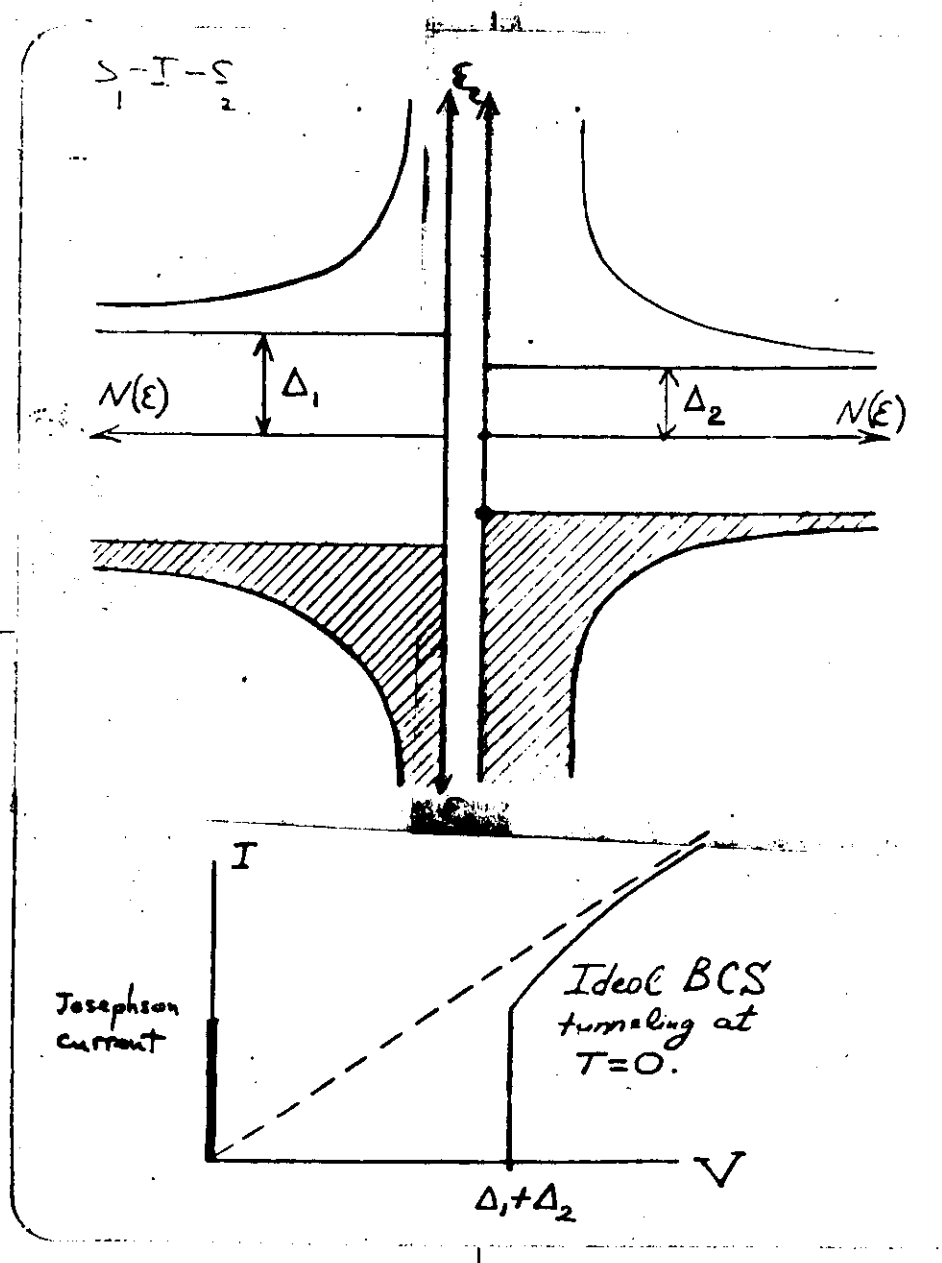
For  $eV < \Delta$ ,  $u_s = 0$  and  $I_{ns} = 0$

For  $eV > \Delta$

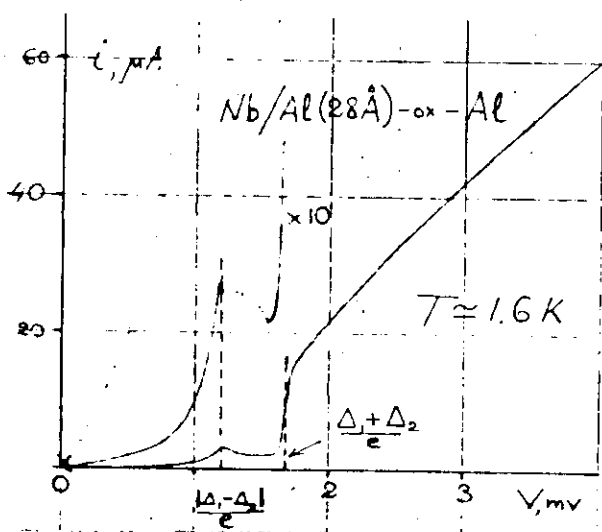
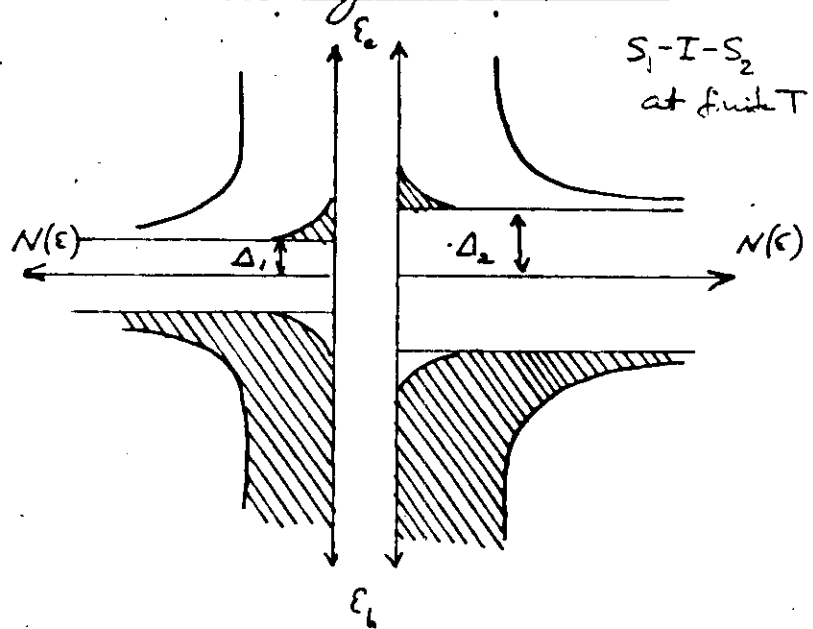
$$I_{ns} = ATN_1N_2 \int_{\Delta}^{eV} \frac{E dE}{\sqrt{E^2 - \Delta^2}} = ATN_1N_2 \sqrt{(eV)^2 - \Delta^2}$$



note:  $eV \gg \Delta$ ,  
 $I_{ns} \rightarrow ATN_1N_2 eV$

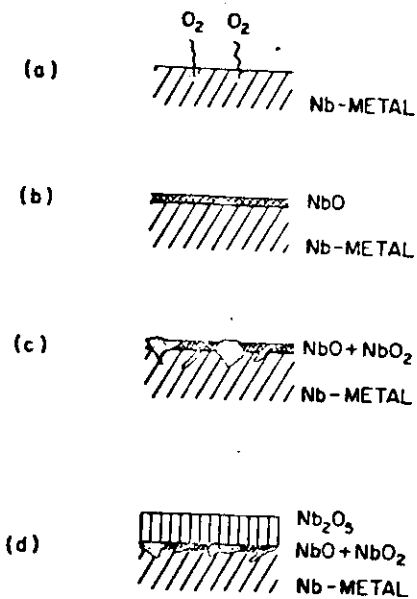


# Tunneling I-V curves



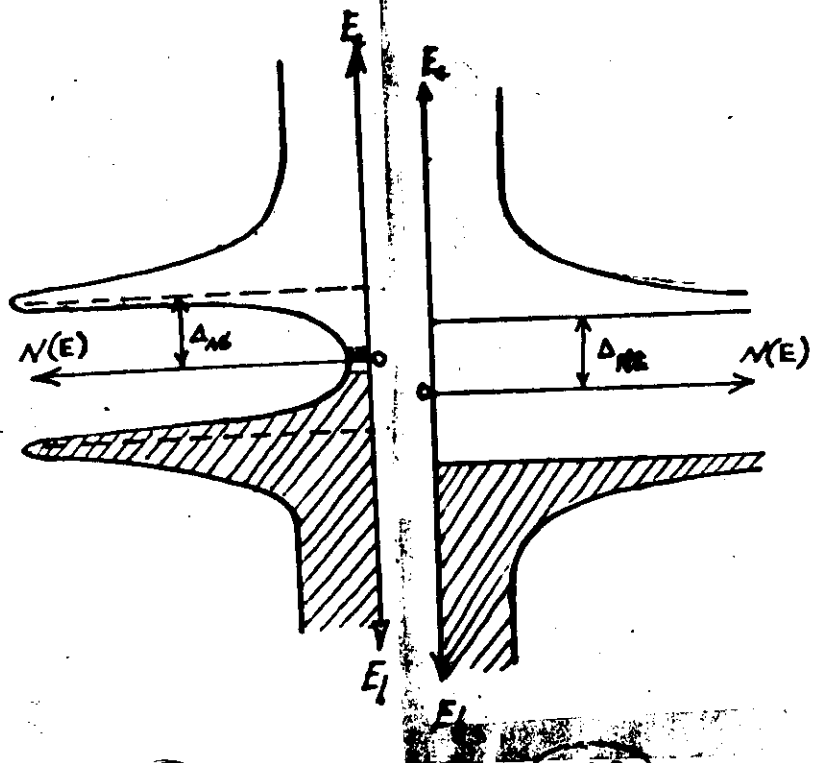
DO NOT AFFIX OVERLAYS ALONG THIS SURFACE

# Stages of oxidation of Nb



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from I. Lindau and W.E. Spicer,  
J. Appl. Phys. 45, 3720 (1974).



Nb

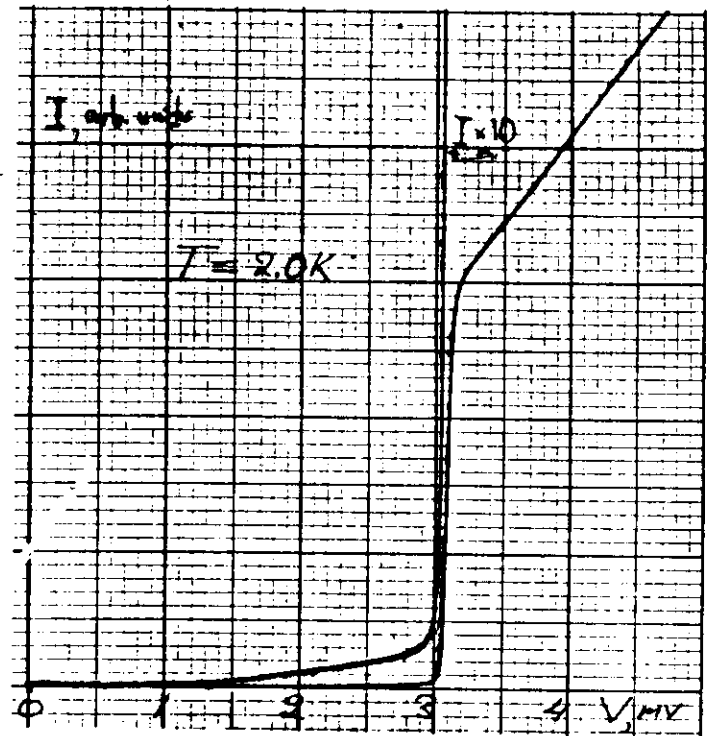
PbBi

$$T = 2K = 0.17 \text{ meV}$$

Bell Laboratories

SEQUENCE NO

14



Nb/Al(21Å)-oxide (20 min, air) - PbBi<sub>0.9</sub>Bi<sub>0.1</sub>

$$\Delta_{\text{PbBi}} = 1.53 \Rightarrow \Delta_{\text{Nb}} = 1.57 \text{ meV}$$

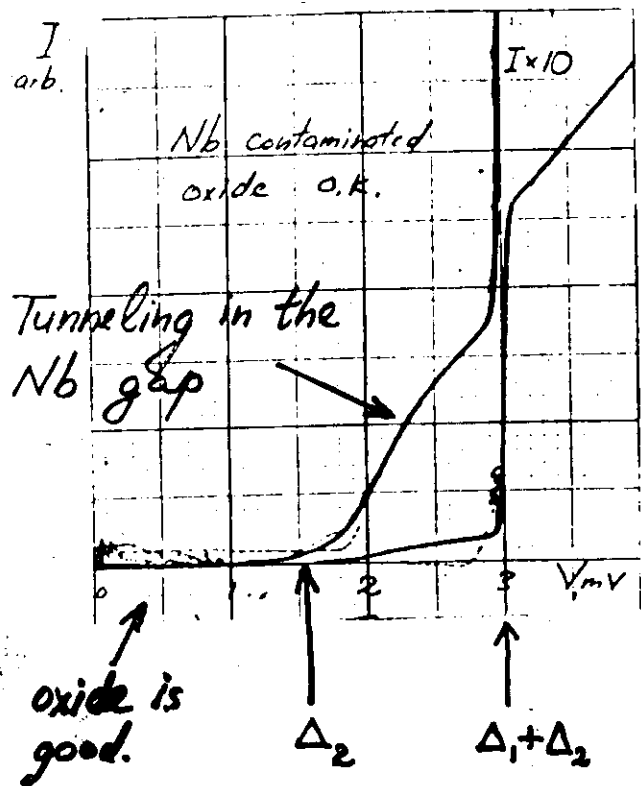
$$\frac{I(2\text{mV})}{I(4\text{mV})} = 2.5 \cdot 10^{-3} \left( \frac{I(2\text{mV})}{I(4\text{mV})} \right) \sim 6 \cdot 10^{-5}$$

ideal

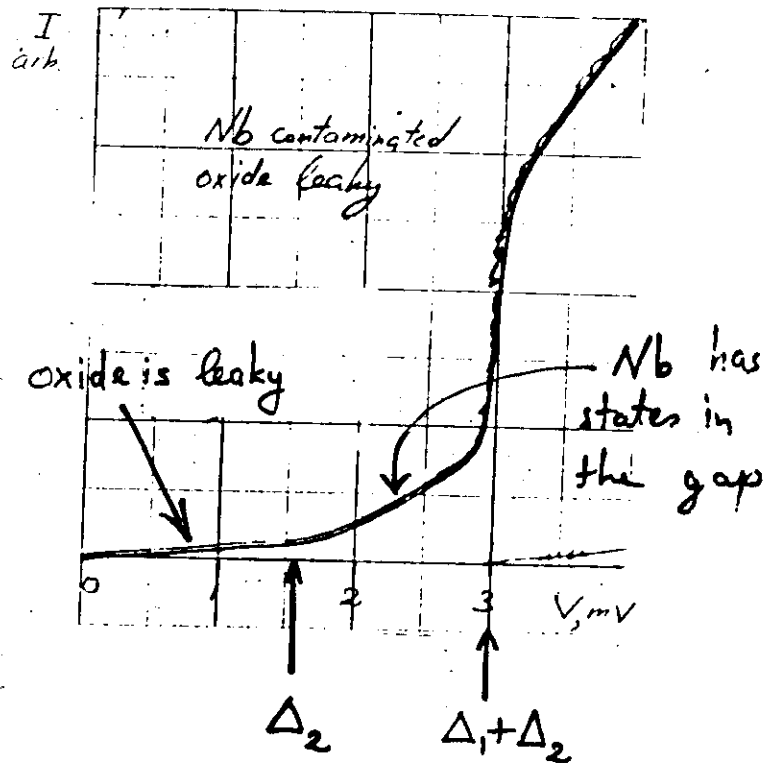


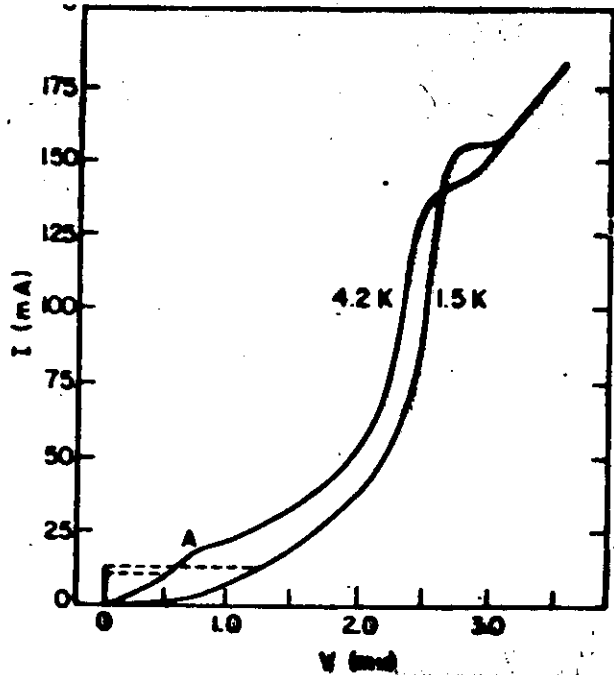
1 2

Nb/Al-oxide - PbBi<sub>0.9</sub>0.1



Nb-oxide - PbBi





Nb-oxide - Cu(8Å)/Nb  
 G. Hawkins and J. Clarke  
 (1975).

Feynman Efecto the Feynman effect

$$\frac{\partial \underline{P}(\vec{r}, t)}{\partial t} = -\nabla \cdot \vec{J}$$

then  $\underline{P}(\vec{r}, t) = \Psi^*(\vec{r}, t)\Psi(\vec{r}, t)$

$$\frac{\partial \underline{P}}{\partial t} = \Psi^* \frac{\partial \Psi}{\partial t} + \Psi \frac{\partial \Psi^*}{\partial t}$$

take Schr eqn for  $\Psi = \frac{\partial \Psi}{\partial t}, \frac{\partial \Psi^*}{\partial t}$

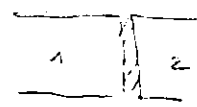
$$\vec{J} = \frac{1}{2} \left\{ \left[ \frac{\hbar}{m} \nabla \Psi \right]^* \Psi + \Psi \left[ \frac{\hbar}{m} \nabla \Psi \right] \right\}$$

where  $\Psi = \sqrt{\rho(\vec{r})} e^{i\theta(\vec{r}, t)}$

$$\vec{J} = \frac{\hbar}{m} (\nabla \theta - \frac{q}{\hbar c} \vec{A}) \cdot \rho$$

$$\left( \vec{p} = \hbar \nabla \right) \text{ or } m\vec{v} = \hbar \nabla - q\vec{A}$$

$\Psi_1$  - amplitude for an electron to be on the left side  
 $\Psi_2$  - " " " " " " on the right side



$$\begin{cases} i\hbar \frac{\partial \Psi_1}{\partial t} = U_1 \Psi_1 + K \Psi_2 \\ i\hbar \frac{\partial \Psi_2}{\partial t} = U_2 \Psi_2 + K \Psi_1 \end{cases}$$

$K$  - characteristic of a junction.

$$U_1 - U_2 = qV$$

... von ...

$$\begin{cases} i\hbar \frac{\partial \psi_1}{\partial t} = \frac{qV}{2} \psi_1 + k \psi_2 \\ i\hbar \frac{\partial \psi_2}{\partial t} = -\frac{qV}{2} \psi_2 + k \psi_1 \end{cases}$$

$$\psi_1 = \sqrt{p_1} e^{i\theta_1}, \quad \psi_2 = \sqrt{p_2} e^{i\theta_2}$$

$$p_1 = p_2 = p_0$$

... real and imaginary part, and define  $\theta_1, \theta_2 = \delta$ ,

$$\dot{p}_1 = -\frac{2}{\hbar} k \sqrt{p_1 p_2} \sin \delta \quad \left. \begin{array}{l} \dot{p}_1 = -\dot{p}_2 \end{array} \right\}$$

$$\dot{p}_2 = -\frac{2}{\hbar} k \sqrt{p_1 p_2} \sin \delta$$

$$\dot{\theta}_1 = \frac{k}{\hbar} \sqrt{\frac{p_2}{p_1}} \cos \delta - \frac{qV}{2\hbar}$$

$$\dot{\theta}_2 = \frac{k}{\hbar} \sqrt{\frac{p_1}{p_2}} \cos \delta + \frac{qV}{2\hbar}$$

$$\dot{p}_1 = -\dot{p}_2 = J$$

$$J = \frac{2k}{\hbar} \sqrt{p_1 p_2} \sin \delta$$

$J_0$

$$J = J_0 \sin \delta$$

$$\delta = \theta_2 - \theta_1 = \frac{qV}{\hbar}, \quad q = 2e$$

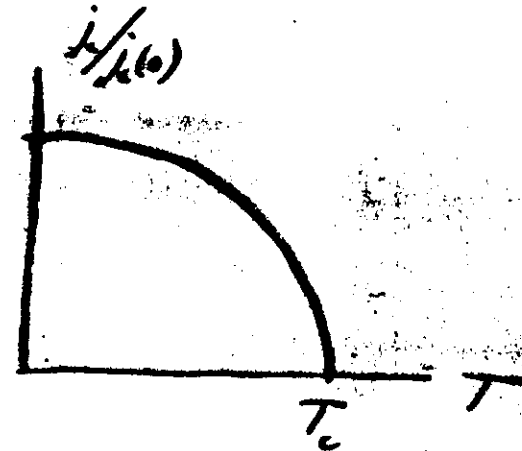
$$\left| \dot{\delta} = \frac{2e}{\hbar} V \right| \quad \text{when } \omega = \frac{2e}{\hbar} V, \text{ current flows}$$

V. Ambegaokar and A. Baratoff

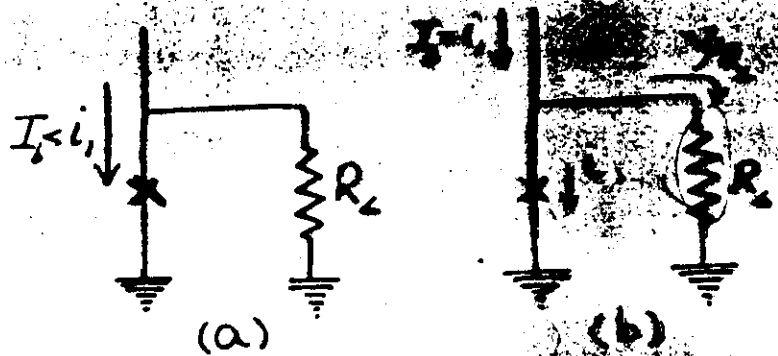
Phys. Rev. Lett. 11, 104 (1963)

$$\Delta_1 = \Delta_2$$

$$j_c = \frac{1}{R_n S} \frac{\pi \Delta(T)}{2e} \tanh \frac{\Delta(T)}{2k_B T}$$



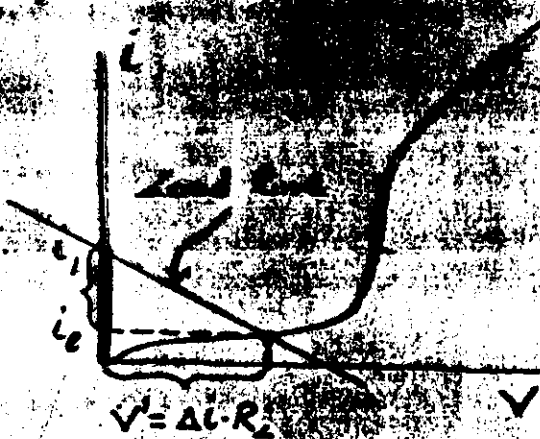
# JJ as a switch



Switching takes place when  $I_s$  reaches the value of  $i_c$

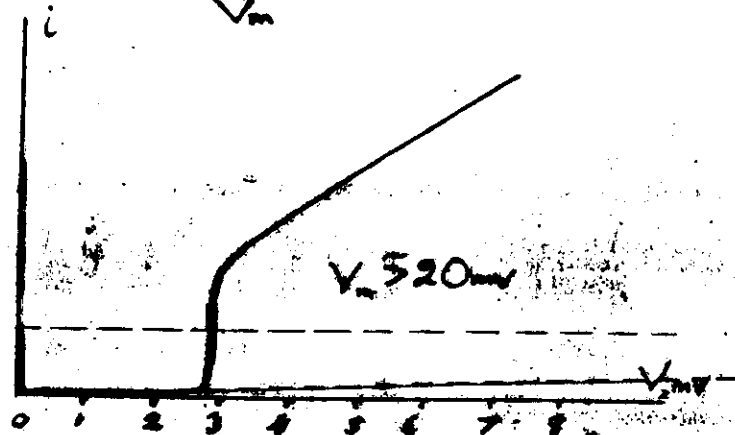
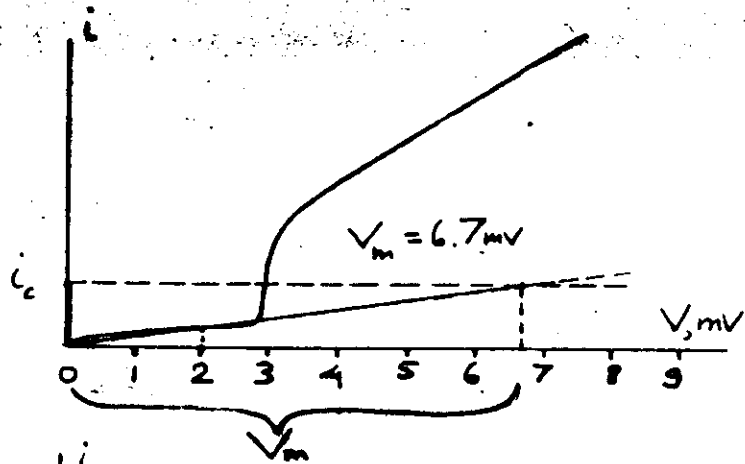
$$i_1 = i + \frac{V}{R_2} \quad \text{or} \quad i = i_1 - \frac{V}{R_2}$$

$\Delta i = i_1 - i_c$   
fan-out  
CURRENT



$$V = \Delta i \cdot R_2$$

A quantitative measure of quality:  $V_m = i_c \cdot R(2m\Omega) = 2 \times \frac{i_c}{(12m\Omega)}$



Fan-out current

$$\Delta i = i_c \left(1 - \frac{2}{V_m}\right)$$

DO NOT AFFIX OVERLAYS ALONG THIS SURFACE

DO NOT AFFIX OVERLAYS ALONG THIS SURFACE

For junction with 20µm width, and  
 $\lambda(Pb) = 390 \text{ \AA}$ ,  $\bar{\phi}_0$  is the junction capacitance  
to  $B = 13 \cdot 10^{-4} \frac{\text{Wb}}{\text{m}^2}$  or 12.9 G.



Circuit applications of small or shunted junctions. RSFQ

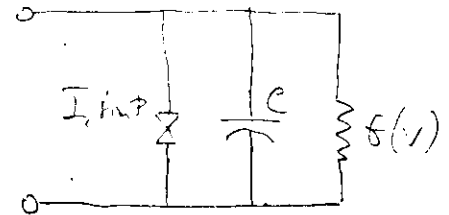
$$I = I_c \sin \phi$$

$$\frac{\partial \phi}{\partial t} = \frac{2e}{\hbar} V \quad (*)$$

Displacement current (C)

Leakage current, quasiparticle current (G (T))

Equivalent circuit



$$I = I_c \sin \phi + G \cdot V + C \frac{dV}{dt}$$

Using (\*),

$$I = \frac{\hbar C}{2e} \frac{d^2 \phi}{dt^2} + \frac{\hbar G}{2e} \frac{d\phi}{dt} + I_c \sin \phi$$

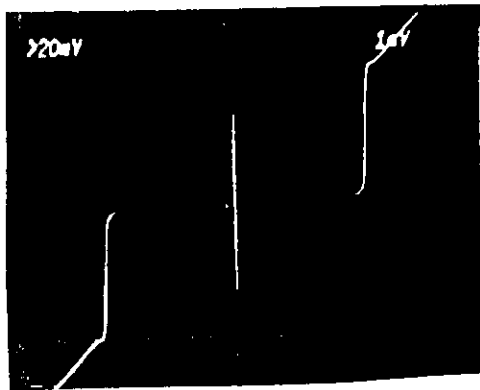
Let us introduce a new variable

$$\theta = \omega_c t, \text{ then } \omega_c = \frac{2e}{\hbar} \left( \frac{I_c}{G} \right)$$

$$\beta_c = \frac{\omega_c C}{\hbar} = \frac{2e}{\hbar} \left( \frac{I_c}{G} \right) \left( \frac{\hbar C}{2e} \right) = \frac{2e I_c C}{G}$$

$$j_c = 480 \frac{\text{A}}{\mu\text{m}^2}$$

$$V_m = 48 \text{ mV}$$



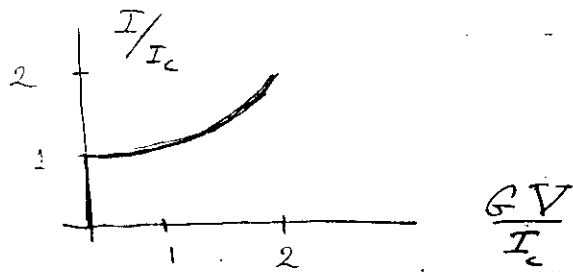
Nb (3000Å) / Al (50Å) - oxide - Nb (3000Å)

$$\frac{I}{I_c} = \beta_c \frac{d^2\phi}{d\theta^2} + \frac{d\phi}{d\theta} + \sin\phi$$

For  $C=0$ ,  $\beta_c=0$  and

$V=0$  for  $I < I_c$

$$V = \frac{I_c}{G} \cdot \sqrt{\left(\frac{I}{I_c}\right)^2 - 1} \quad \text{for } I > I_c$$



Mechanical analogy: Driven Pendulum.

$$\text{Torque } T = M \cdot \frac{d^2\phi}{dt^2};$$

$M$  - moment of inertia.

$$T = T_{\text{app}} + \underbrace{mgl \sin\phi}_{\text{grav. torque}} + \underbrace{D \frac{d\phi}{dt}}_{\text{damping torque}}$$

$$\text{So } \left\{ M \frac{d^2\phi}{dt^2} + D \frac{d\phi}{dt} + mgl \sin\phi = T \right.$$

$$\text{Comp. } \left\{ \frac{I_c}{2e} \frac{d^2\phi}{dt^2} + \frac{I_c G}{2e} \frac{d\phi}{dt} + I_c \sin\phi = I \right.$$

We see that

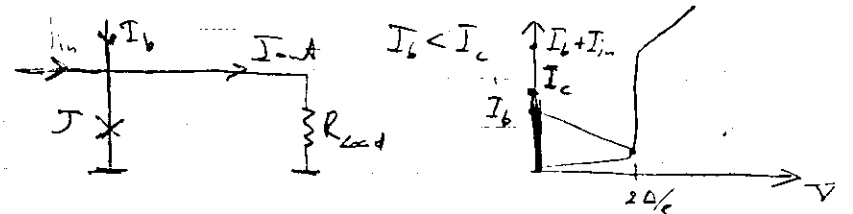
- the angle  $\phi$  is the analog of the flux difference
- $\frac{d\phi}{dt}$  (angular vel.) "—" of voltage
- $M \leftrightarrow$  capacitance
- $D \leftrightarrow$  conductance
- Max. grav. torque  $\leftrightarrow I_c$ .
- Applied torque  $\leftrightarrow$  analog of source current

$$\beta_c = \mu g l \cdot \frac{M}{D^2};$$

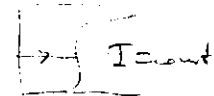
RSFQ:

$$\text{Josephson power } P = \frac{V^2}{R_{\text{eff}}} \ll 1 \mu\text{watt}$$

Logic gate is "IBM-type" logic (latching logic)



$$I_{in} + I_b = I_J + I_{out}$$



$$V_J = R_J I_J; \quad V_L = V_J = R_2 \cdot I_{out} = V;$$

$$R_J I_J = R_2 I_{out}; \quad I_{out} = \frac{R_J}{R_2} I_J$$

leakage is difficult: latching logic.

due to switch off  $I_b$ .

need AC (RF) power supply

This limit <sup>glob</sup> frequency to a few GHz.

Also, punch through effect is a problem for  $f > 1$  GHz

Fujitsu 8-bit microprocessor, 23,000 T

clock frequency  $\sim 1$  GHz

$$\text{LSFQ (35): } \int V(t) dt = \Phi_0 = \frac{h}{2e} = 2.07 \text{ mV} \times \mu\text{s},$$

overdamped JJs.

30 GHz operation was demonstrated in 86.

> 100 GHz now, at 5  $\mu\text{m}$  rules.



$2\pi$  - loop of  $\Phi$

$$\tau_0 = \frac{\pi}{\omega_c}$$

## Books:

1. C.B. Duke, Tunneling in Solids, Academic Press, N.Y. and London, ~~1966~~ 1969 (Supplement 10, Solid State Physics)
2. "Tunneling Phenomena in Solids", Ed. by Burstein and Lundqvist, Plenum Press, N.Y. 1969.
3. L. Solymar, Superconductive Tunneling and Applications, Wiley-Interscience, 1972.
4. T. Van Duzer and C.W. Turner, Principles of Superconductive Devices and Circuits, Elsevier, NY-Oxford, 1981.
5. W. & L. McMillan and J.M. Rowell, Tunneling and Strong-coupling superconductivity, in Superconductivity, Ed. by Pines, 1969.
6. Tunneling Spectroscopy, Ed. by P.K. Hansma, Plenum, 1982.

# Lecture 2 (Trieste)

1. Points from L.1
2. Tunneling  $I_0$
3. Spectroscopy: finding  $\alpha^2 F(\omega)$
4. Tunneling in HTSC

## 1. Return to some points from

### Lecture 1:

a) We did not really show that

$$\frac{dI}{dV} = N_s(E) = N_{2n}(0) \cdot \frac{E}{\sqrt{E^2 - \Delta^2}} \quad (\text{BCS})$$

~~$$I_{ns} = A T N_2 \int_{-\infty}^{\infty} \frac{E}{\sqrt{E^2 - \Delta^2}} [f(E) - f(E - eV)] dE$$~~

$$\underline{T=0:}$$

$$I_{ns} = \frac{2\pi e A}{\hbar} \int_{\Delta}^{eV} |T|^2 N_n(E - eV) N_s(E) dE \Rightarrow$$

A - junction area.

Assuming  $N_n(E) \approx N_n(E - eV) \approx N_n(0)$  (weakly coupled)

DOS, as  $N_s(E) \approx N_n(0) \frac{E}{\sqrt{E^2 - \Delta^2}}$ , at  $T = \text{const}(E)$

$$\Rightarrow = \frac{2\pi e A}{\hbar} |T|^2 N_n(0) N_2(0) \int_{\Delta}^{eV} \frac{E dE}{\sqrt{E^2 - \Delta^2}}$$

$$= G_n/e$$

~~Derivation of  $G_n$~~

Note:  $[|T|^2 N_n N_s = 1, \text{ for } G_n \text{ must have another } e^2/h]$

$$\int_{\Delta}^{eV} \frac{E dE}{\sqrt{E^2 - \Delta^2}} = \frac{1}{2} \int \frac{d(E^2 - \Delta^2)}{\sqrt{E^2 - \Delta^2}} = \frac{1}{2} \int \frac{dE}{\eta} =$$

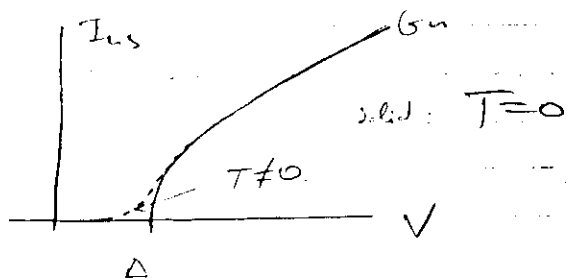
$$= \frac{e}{2} \cdot \eta^{\frac{1}{2}}$$



$$= \int_{\Delta}^{eV} \frac{eV \, d\epsilon}{\Delta \sqrt{\epsilon^2 - \Delta^2}} = \frac{eV}{\Delta} \sqrt{\epsilon^2 - \Delta^2} \quad (3)$$

$$= \sqrt{\epsilon^2 - \Delta^2} \Big|_{\Delta}^{eV} = \sqrt{(eV)^2 - \Delta^2},$$

$$I_{\text{tun}} = G_n \frac{G_0}{e} \sqrt{(eV)^2 - \Delta^2}, \quad I_{\text{tun}} = 0 \text{ for } eV < \Delta$$



$$\frac{dI_{\text{tun}}}{dV} = \frac{G_0}{e} \frac{1}{\sqrt{(eV)^2 - \Delta^2}} \frac{d(eV)}{dV} = G_n \frac{V}{\sqrt{V^2 - (\frac{\Delta}{e})^2}}$$


---

for  $eV > \Delta$ ;

$$\frac{dI}{dV} = 0 \quad \text{for } eV \leq \Delta.$$

### b) "Harrison's argument"

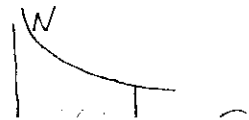
In its most simplified form it is a demonstration that normal state density of states can not be measured by tunneling - the energy dependence cancels out

not the wavefunction on the left has  $\psi(x) = Ae^{ik_1 x}$ . Consider current incident on a tunnel barrier in the energy interval  $(E, E+dE)$

$$L_{\text{inc}}(E, E+dE) = e \int_{E}^{E+dE} N_{\epsilon} d\epsilon = e \frac{2\pi k_1}{m} \left( \frac{d\psi}{d\epsilon} \right)_D f(E) dE$$

where  $k_1 = \frac{1}{\hbar} \sqrt{2mE}$ ,  $\left( \frac{d\psi}{d\epsilon} \right)_D$  is the 1-D DOS and  $f(E)$  - F-D occupation function

$$N = \left( \frac{d\psi}{d\epsilon} \right)_D = \frac{m L}{\pi \hbar^2 k_1} = \frac{m L \hbar}{\pi \hbar^2 \sqrt{2mE}} = \frac{m^{1/2} L}{2^{1/2} \pi \hbar} E^{-1/2}$$



6

From normality of the wavefunction we find

$|a|^2 = \frac{1}{L}$ ;  $f(\epsilon) = \begin{cases} 1 & \epsilon < \epsilon_F \\ 0 & \epsilon \geq \epsilon_F \end{cases}$

We can consider infinitesimal voltage

$d\epsilon \delta V = e \delta V$   $e \delta V = d\epsilon$ .

$$I_{inc}(\epsilon, \epsilon + d\epsilon) = \frac{e^2}{m} \frac{v}{\pi} \frac{m}{\hbar} \delta V$$
  
$$= e^2 \cdot |a|^2 \cdot \frac{\hbar v}{m} \cdot \frac{m}{\hbar} \delta V = 2 \frac{e^2}{h} \delta V$$
  
$$\frac{1}{\hbar}$$

Note: the transmitted current will be  $I_{inc} \cdot T$ .

The point is that  $v$ , from the velocity cancels with  $\frac{dv}{d\epsilon} \propto \frac{1}{k}$ ; there is no energy dependence left.

Tunnelling current  $I_{inc} \cdot T$  will be independent on the energy variation of the DOS.

2. Tunneling and coherence length

a) Meaning of the coherence length:

Cooper Order parameter or a macroscopic wavefunction.

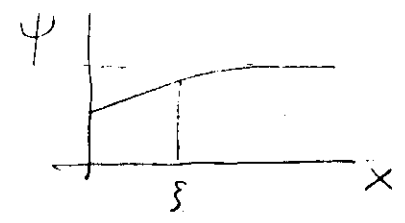
$\Psi(\vec{r}) = |\Psi(\vec{r})| \cdot \exp i \theta(\vec{r})$

Ginzburg-Landau postulated an additional contribution to the free energy  $\frac{\hbar^2 |\nabla \Psi|^2}{2m}$ .

We say that  $\Psi$  is "stiff", or that it opposes rapid spatial variations.

$|\Psi|^2$  - density of electron pairs.

Solving G-L eq-us for non-uniform superconductors, one finds that  $\Psi$  can change over characteristic length  $\xi_{GL}(T)$ .



$\xi_{GL}(T) = \frac{\hbar |\Psi_0(T)|}{(2m^* m_0)^{1/2} H_c(T)}$

(7)

### Cooper Coherence Length

Non-local character of Cooper

eqn -  $\vec{j} = c\vec{A}$

current density at a certain point will be affected by  $\vec{A}$  in a region of about

plus minus range of phase coherence of a wavefunction.

$$\xi_0 = 0.18 \frac{\hbar v_F}{k_B T_c}$$

In the presence of impurities ( $\ell = \text{mfp}$ )

$$\frac{1}{\xi} \approx \frac{1}{\xi_0} + \frac{1}{\ell}$$

Cooper:  $\ell/\xi_0 \gg 1$  : pure limit

$\frac{\ell}{\xi_0} \ll 1$  dirty limit

order parameter  $\Delta(\vec{r}) = \frac{3.07 k_B T_c}{\pi x} \psi(\vec{r})$

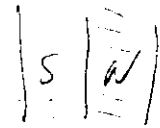
in the pure limit (applicable to HTSC):

$$\xi_{GL}(T) = \frac{0.74 \xi_0}{\sqrt{1 - \frac{T}{T_c}}}$$

25

(8)

In previous systems

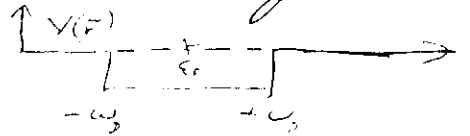


Pair potential  $\Delta(\vec{r})$

can be expressed as

$$\Delta(\vec{r}) = V(\vec{r}) F_{Co}(\vec{r}) \text{ where}$$

$V(\vec{r})$  is ~~the~~ the e-ph interaction potential (very short range)

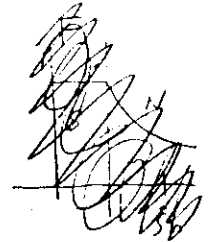


and  $F_{Co}(\vec{r})$  is the condensate amplitude

( $|F|^2$  give the density of pairs)

The main result is

$$(*) \quad F_{Co}(x) = \Phi(x) \cdot e^{-k_n |x|}$$



$\Phi(x)$  - slowly varying function of  $x$   
( $x \gg \frac{1}{k_n}$  required for (\*) to be true)

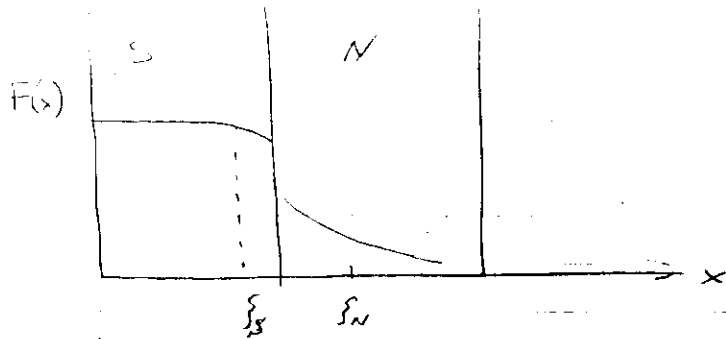
$k_n$  depends on a number of factors ( $\ell, T_c, \text{etc}$ )

For clean Normal and superconducting materials

$$\frac{1}{k_n} = \frac{\hbar v_F}{2\pi k_B T} = \xi_n \text{ - coherence length in a normal metal.}$$

$\ell \gg \xi_n \text{ or } V_c < 0 \text{ (reduction)}$

9



$$\xi_S = 0.18 \frac{\hbar v_S}{k_B T_c}; \quad \xi_N = 0.16 \frac{\hbar v_N}{k_B T_c}$$

Note: can not gain indefinitely by reducing T.

In reality,  $\xi_N \approx 0.16 \frac{\hbar v_N}{k_B T_c}$  also.

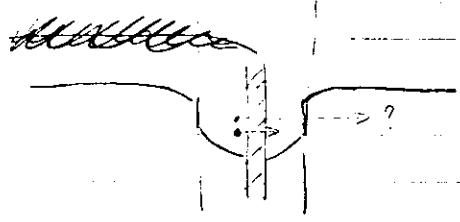
~~change go~~

insert ←

Traveling out of : suppose we have N regions near the barrier.

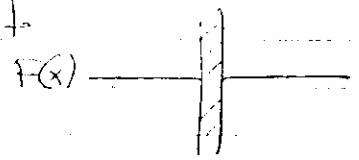


F



Does Electron go just across, on a distance l from the barrier?

as effort to



$$\frac{dI_{NS}}{dV} = C_{NS} \frac{eV}{[(eV)^2 - \Delta^2]^{3/2}}, \quad eV > \Delta, \\ = 0, \quad eV < \Delta.$$

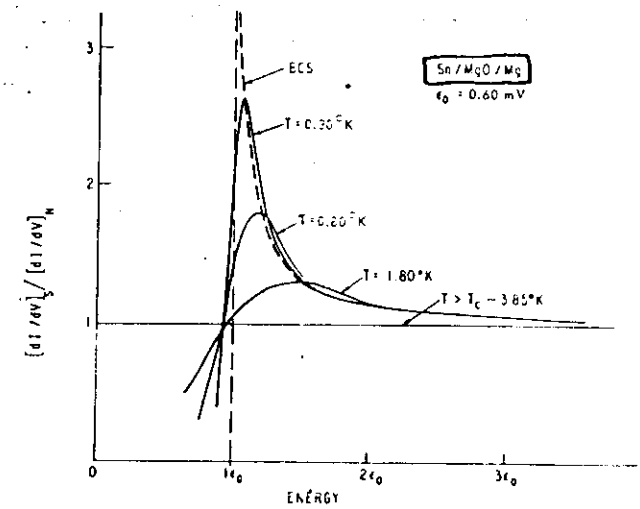


Fig. 5. The density of states in a superconductor obtained by taking the ratio of the derivatives of the current-voltage characteristics in the superconducting and normal states. As the smearing due to temperatures is reduced, the curves approach the BCS predictions. From I. Giaever, H. R. Hart, and K. Megerle, Phys. Rev. 126:941 (1962).

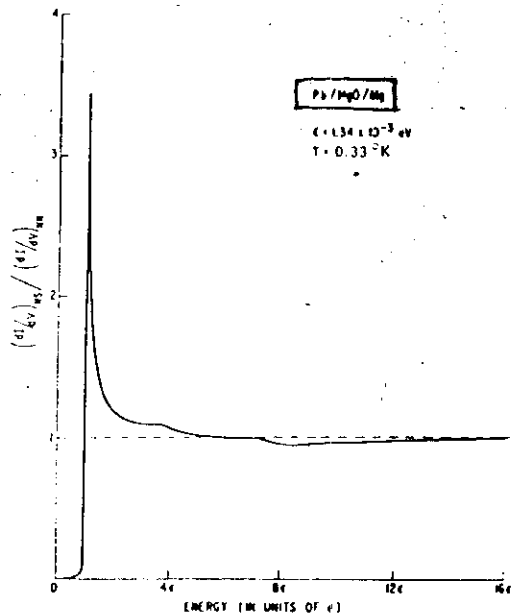
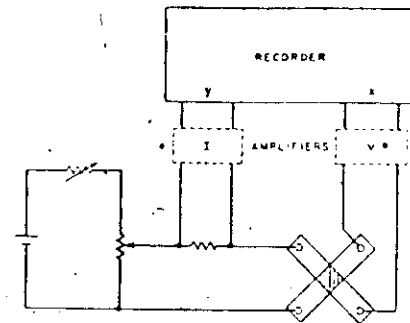
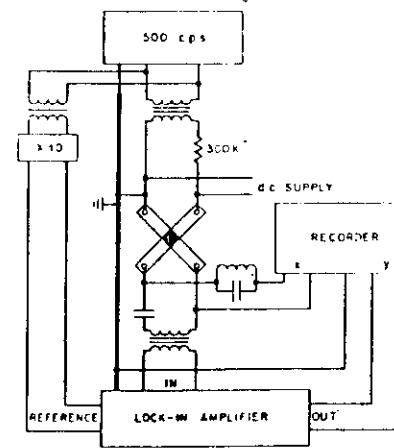


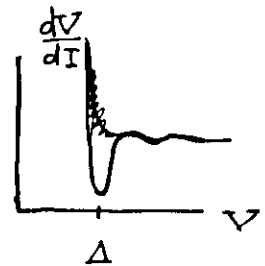
Fig. 6. The density of states for Pb, definitely different from the BCS theory. It turns out that the bumps in the curve reflect the phonon spectrum in Pb. Mg is a normal conductor. From I. Giaever, H. R. Hart, and K. Megerle, Phys. Rev. 126:941 (1962).



Circuit to display the  $I$ - $V$  characteristic of a junction on an AF-recorder.



Circuit to measure directly  $dV/dI$  of a junction by the ac modulation technique.



Applied DC bias current is modulated with a small constant AC current  $\delta I$ ; the generated voltage is picked up with the lock-in amplifier.

$$\frac{dV}{dI} = \frac{1}{\left(\frac{dI}{dV}\right)}$$

(11)

Schrieffer, Scalapino and Wilkins calculated  
the phonon spectrum of lead with two  
Fermion peaks and reproduced structure

in  $\Delta(\omega)$  very well

$\Delta(\omega)$  was complex, and

$$\frac{dI}{dV} \propto \text{Re} \left[ \frac{E}{\sqrt{E^2 - \Delta(E)}} \right]$$

$\Delta^2 F(\omega)$  - electron-phonon matrix element (interaction)  
from the phonon density of states.

$\alpha^2 F(\omega)$  and  $\mu^*$  (renormalized Coulomb  
repulsion) are the central parameters  
of the Eliashberg theory.

McMillan and Rowell procedure

to bring calculated  $N(\omega)$  in agreement

with measured  $N(\omega)$ , and find  $\alpha^2 F, \mu^*, \Delta(\omega)$ .

as a result: show the change

(2)

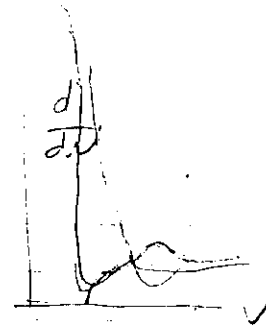
Discuss circuits (show circuits).

1.  $I-V$       2.  $dV/dI$

One needs to measure  $\left(\frac{dV}{dI}\right)_S$  and

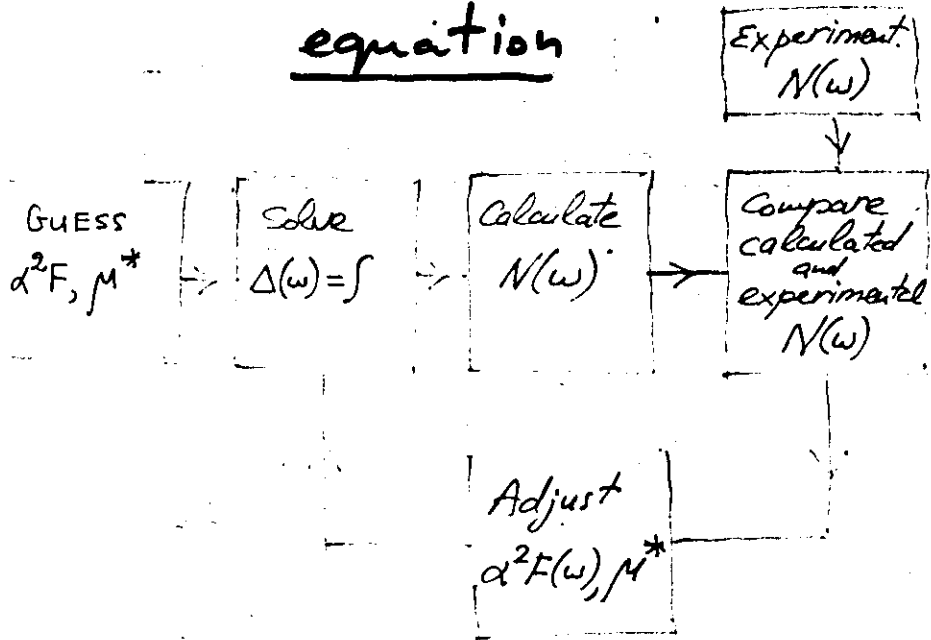
$\left(\frac{dV}{dI}\right)_{\text{normal}}$  at the same  $V$ .

Second derivative is also measured.



Normal state measured in  $H$  or at  $T > T_c$ .

# Schematic of the method used to "invert" the gap equation



After 6-8 solutions,  $\alpha^2 F(w)$  reproduced measured  $N(w)$  to one part in  $10^3$

From McMillan & Rowell, 1965

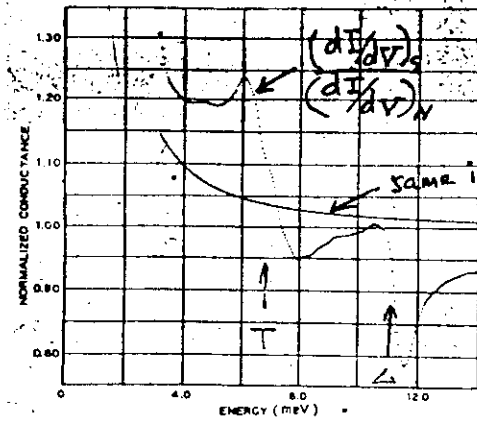
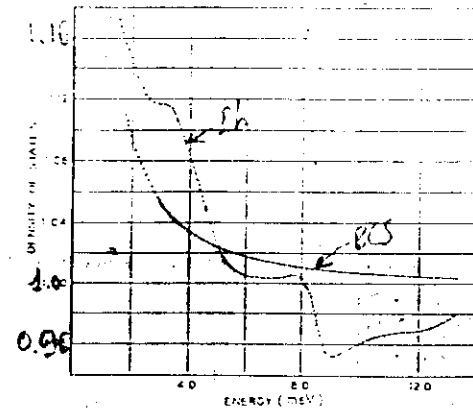


Fig. 19. Conductance  $dI/dV$  of a Pb-I-Pb junction in the superconducting state normalized by the conductance in the normal state vs. voltage. Also shown is the two-superconductor conductance calculated from the BCS density of states which contains no phonon structure.

Phonon energy corresponds to  $(E_{\text{gap}} - 2\Delta)$

BCS



Electronic density of states  $N(E)$  for lead vs.  $E - J_0$  obtained from the data of Fig. 19. The smooth curve is the BCS density of states.

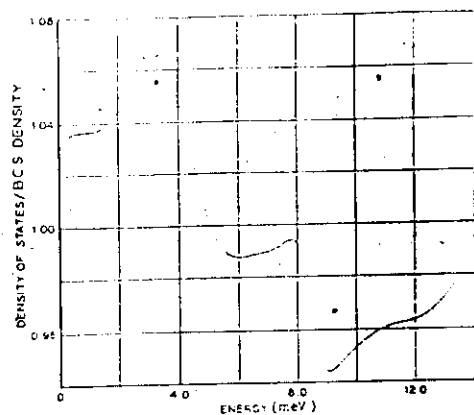


Fig. 24. Electronic density of states of Pb divided by the BCS density of states vs.  $E - J_0$ .

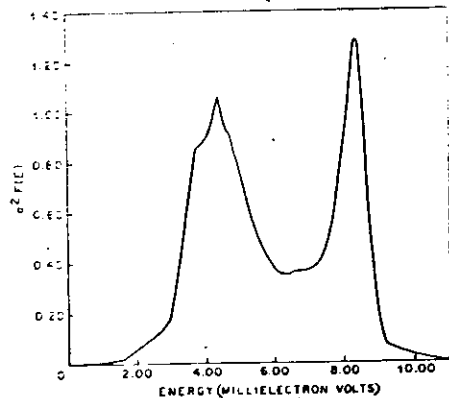


Fig. 25.  $\alpha^2 F(\omega)$  for Pb found by fitting the data of Fig. 24.

$\alpha^2 F(\omega)$   
for Pb  
 $\mu^* = 0.12$

$$\lambda = 2 \int_0^{\infty} \frac{\alpha^2 F(\omega)}{\omega} d\omega \rightarrow \text{e-pb inter. constant.}$$

$$(m^* = m_{BS} (1 + \lambda); v_F^* = \frac{v_{FS}}{1 + \lambda} \text{ etc.})$$

Find  $\lambda_{Pb} = 1.5$

Table I

$T_D$ (°C)	$\Delta$ (meV)	$\lambda$	$\mu^*$	$\bar{\omega}$ (meV)	$\langle \omega \rangle$ (meV)	$\langle \omega^2 \rangle$ (meV <sup>2</sup> )	$T_c$ calc.
<75°C	1.51	0.96	0.15	17.2	14.6	252	8.4
Nb°C	1.52	0.97	0.15	16.8	14.2	240	8.4

$T_D$  is the deposition temperature.

$J_0$  is the energy gap.

$$\lambda = 2 \int \frac{\alpha^2(\omega)F(\omega)}{\omega} d\omega; A^2 = \int \alpha^2(\omega)F(\omega) d\omega; \bar{E} = \int \alpha^2(\omega)F(\omega)\omega d\omega$$

$$\bar{\omega} = \bar{E}/A^2; \langle \omega \rangle = 2A^2/\lambda; \langle \omega^2 \rangle = 2\bar{E}/\lambda$$

$T_c$  is calculated from the McMillan equation.

proximity effect [23] on the same junctions, as after some months, including sending them by mail from Murray Hill to Karlsruhe, they had increased in resistance and the characteristics had deteriorated to such an extent that the well-known Nb problem of a small or negative  $\mu^*$  resulted when  $\alpha^2(\omega)F(\omega)$  was unfolded conventionally. This results from the weakened  $N(E)/N_{BCS} - 1$ , especially at low energies, as the deteriorated characteristics for  $10 < t < 30 \text{ \AA}$

Table II

Sample	$t$	$J_0$ (meV)	$\lambda$	$\mu^*$	RMS dev. (%)	$d/\ell$	$R$
J152	14	1.53	1.04	0.18	0.7	0.04	0.006
J153	10	1.53	1.07	0.19	0.9	0.05	0.005
J192	7	1.50	1.00	0.17	1.7	0.04	0.005
J292	42	1.50	0.95	0.18	0.6	0.07	0.008
J294	22	1.47	1.00	0.19	0.8	0.06	0.006
J252	16	1.50	0.95	0.16	0.6	0.08	0.009
J274	8	1.49	0.96	0.18	0.3	0.09	0.011
J122	22	1.49	1.05	0.19	0.6	0.05	0.004
	22	1.49	0.97	0.16	0.5	0.03	0.006
NbO5	0	1.49	1.09	0.17	0.4	0.14	0.010

$t$  is the Al overlayer thickness.

$d$  = thickness of assumed proximity layer.

$v_F$  = Fermi velocity of electrons in the proximity layer.

$\ell$  = mean free path of electrons in the proximity layer.

$R = 2d/hv_F$ .

gave values comparable to the data of fig. 10 for the sample with only 1.3 Å of Al. The criteria used for the convergence of the proximity effect program were to minimize the RMS deviation between the measured and calculated density of states and ensure that  $\alpha^2(\omega)F(\omega)$  became zero above its high energy cutoff. Using these criteria,  $\alpha^2(\omega)F(\omega)$  for eight different junctions agrees excellently with the data of fig. 11 and the resulting parameters are given in table II.

### 7. Conclusions

We have shown that a few monolayers of Al

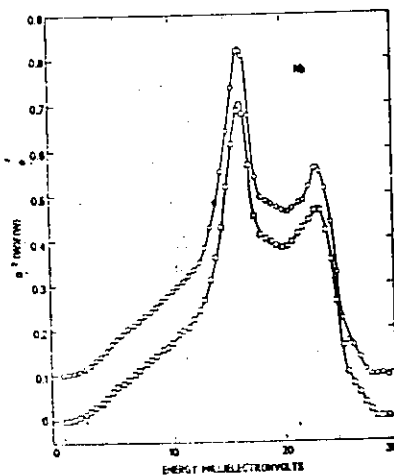
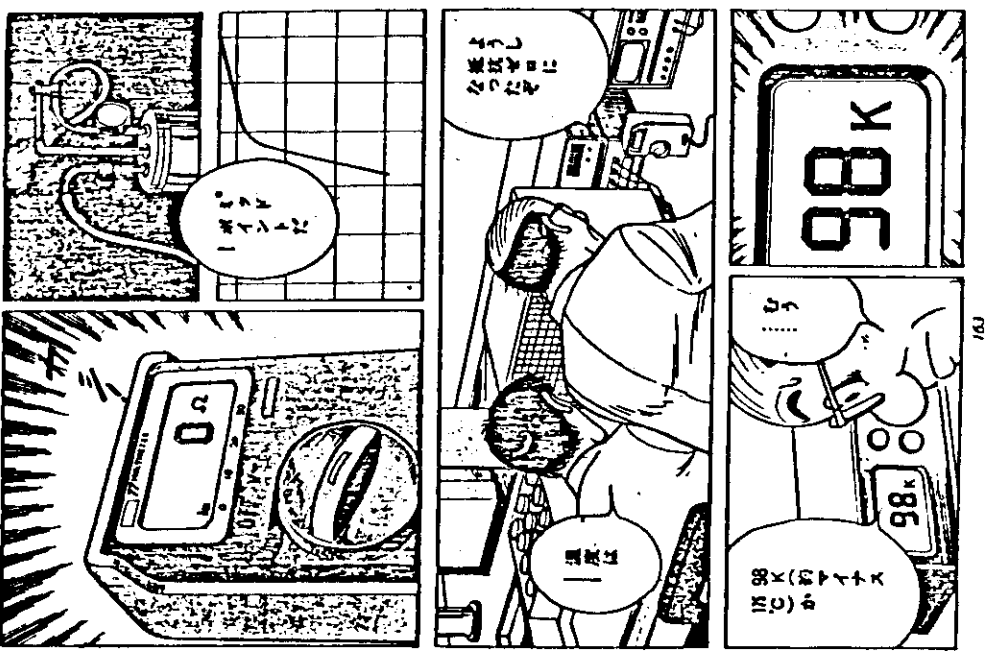
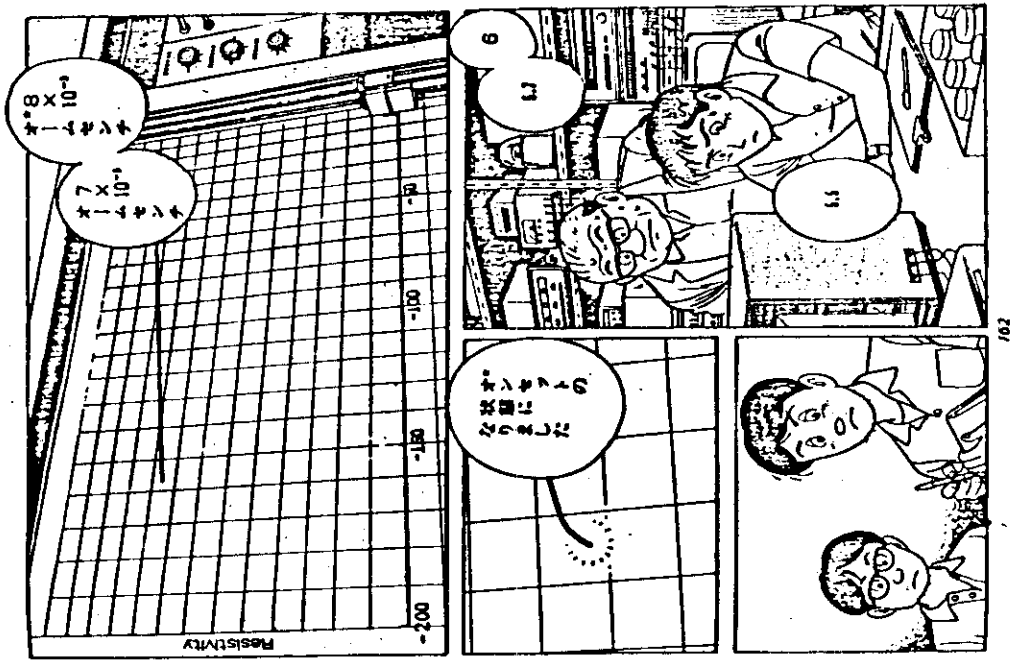


Fig. 11. The electron-phonon coupling function,  $\alpha^2(\omega)F(\omega)$  derived from two Nb/Al wide gap junctions, the upper having a Nb film made at 600°C, the lower at <75°C.





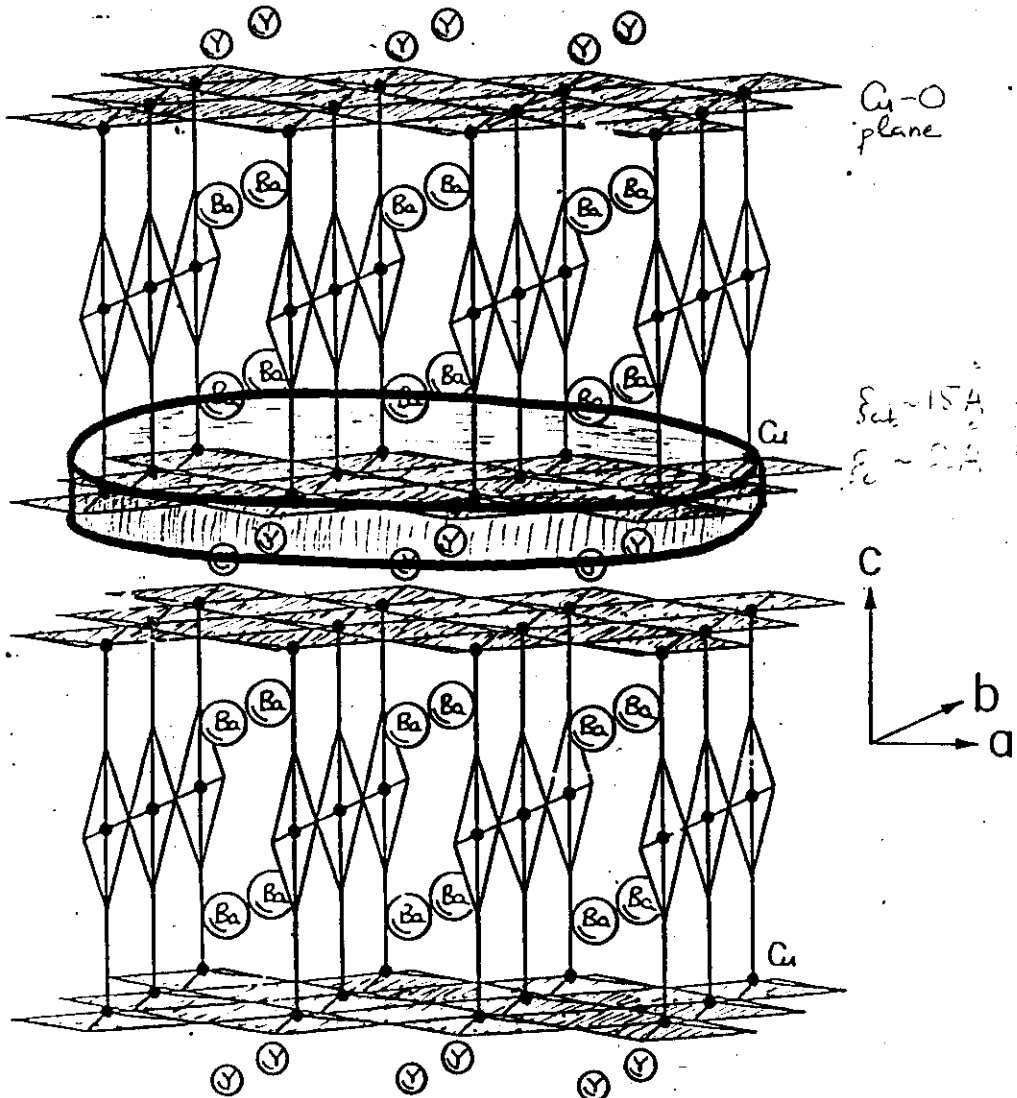
HTSC

for a review of tunneling  
see J.R. Kirtley, Int. J. of  
Modern Physics B ...

M. Gurvitch, in  
Superconductivity and  
Applications, Ed. Kwok et.al  
Plenum Press, N.Y. 1990.

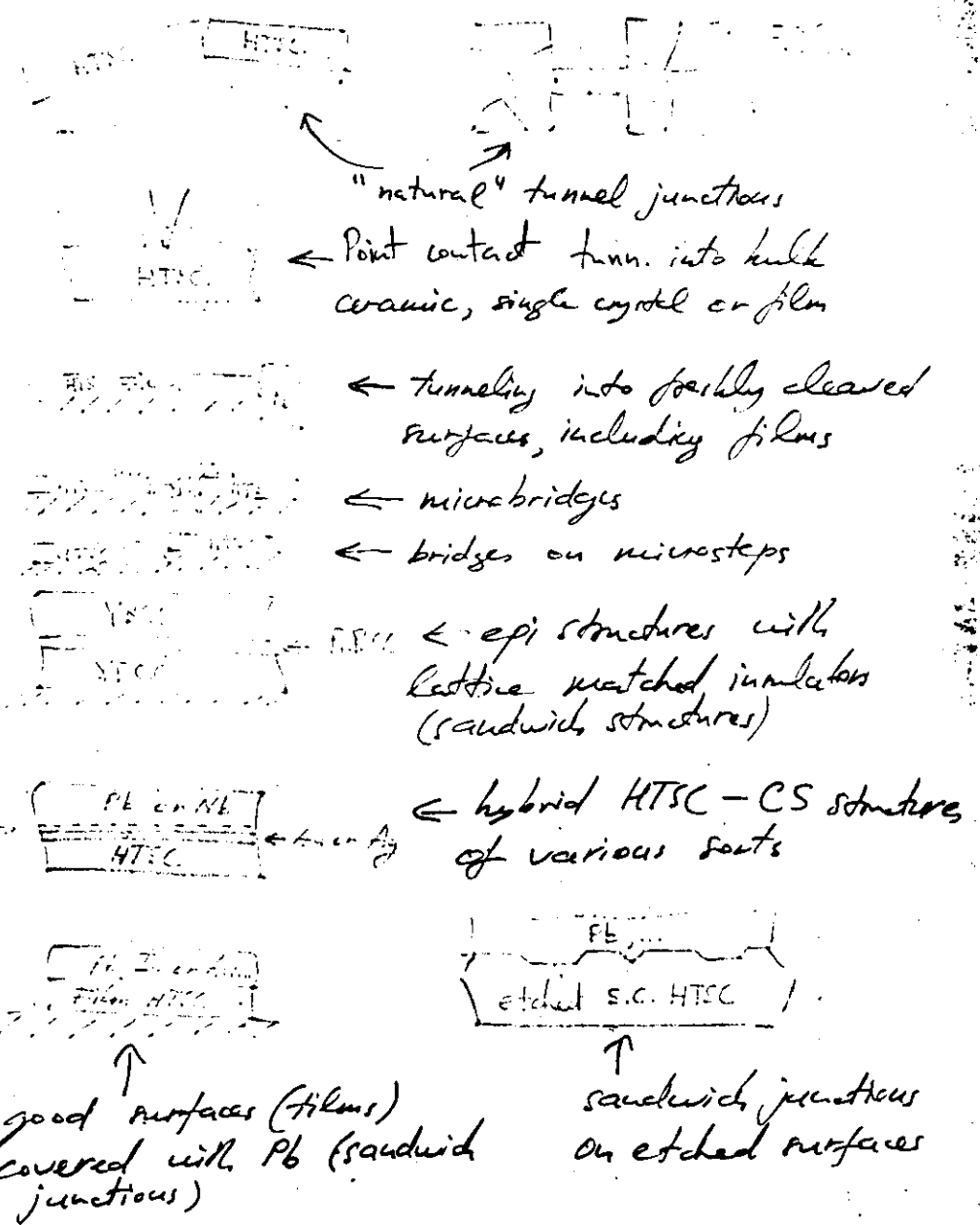
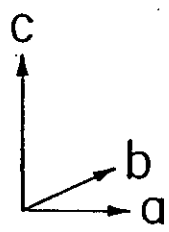
*Gurvitch*

Cooper pair in  $YBa_2Cu_3O_7$






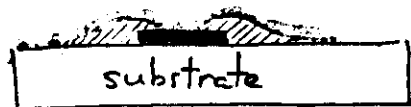
Cu-O plane

Set - ISA  
E - 2A

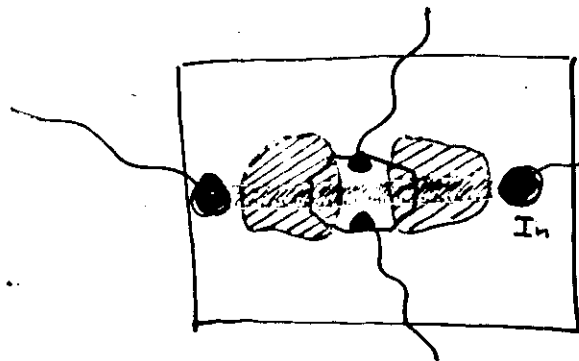


# Tunnel junction

-  YBCO
-  epoxy
-  FL

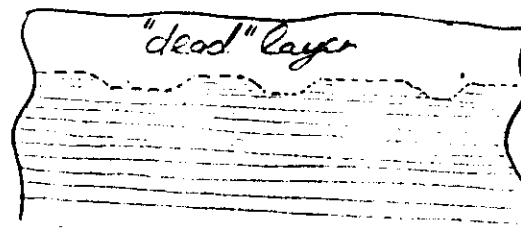


side view



Au wire

top view



← contamination,  
off-stoichiometry,  
carbonate...

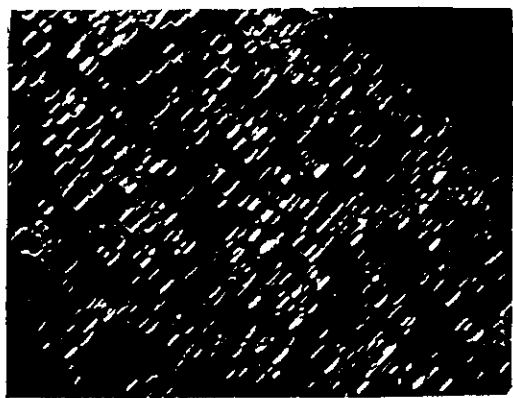
(1+10)

1. 1 mMole  $\text{HClO}_4$  / 1 Mole  $\text{NaClO}_4$  in  $\text{H}_2\text{O}$

(B. Miller, Bell)

2. 1% Br in methanol (or ethanol)

(R.P. Vasquez et al. *APL* 53, 2692 (88))



(x160)

Etch-pits after 5min in  
 10 mM  $\text{HClO}_4$  / 1 Mole  $\text{NaClO}_4 \cdot \text{H}_2\text{O}$ .



Thick ribbon after 50min in 10 mM  $\text{HClO}_4$

"Thick ribbon" after  
 50min in 10 mM

x160



T. ribbon

Pit after 10min in 10 mM x 700

Single pit (one also)



Wavy after 50 min 10 mM x 160

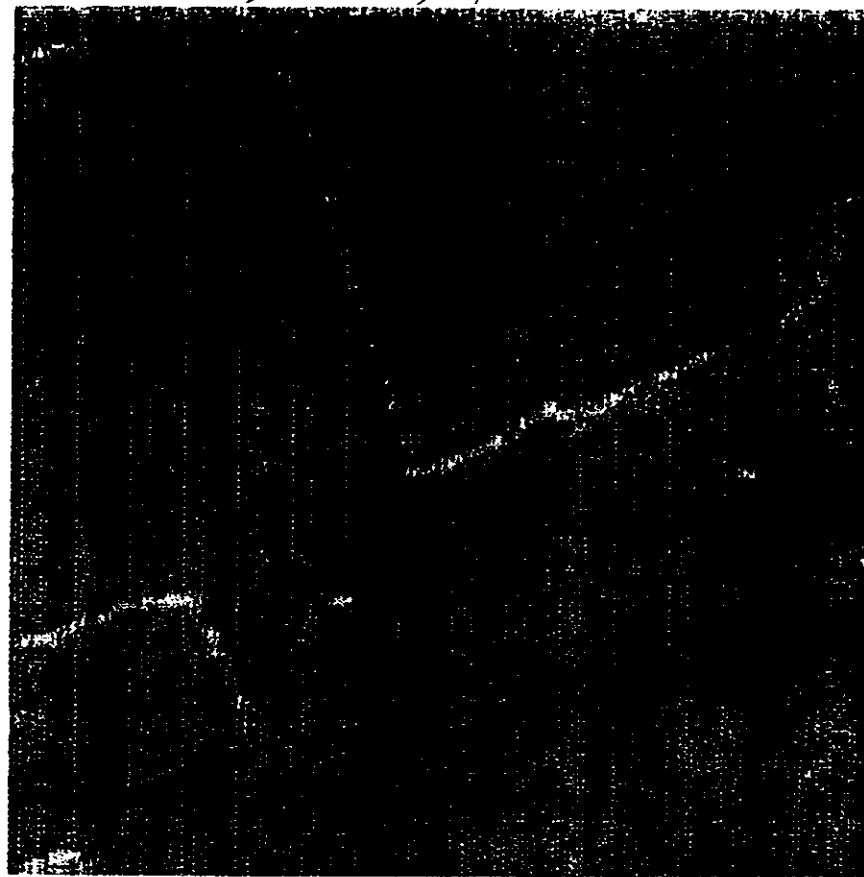
"Wavy" after

50min. 10 mM

H. Hess, M. Gurevitch, unpublished STM.



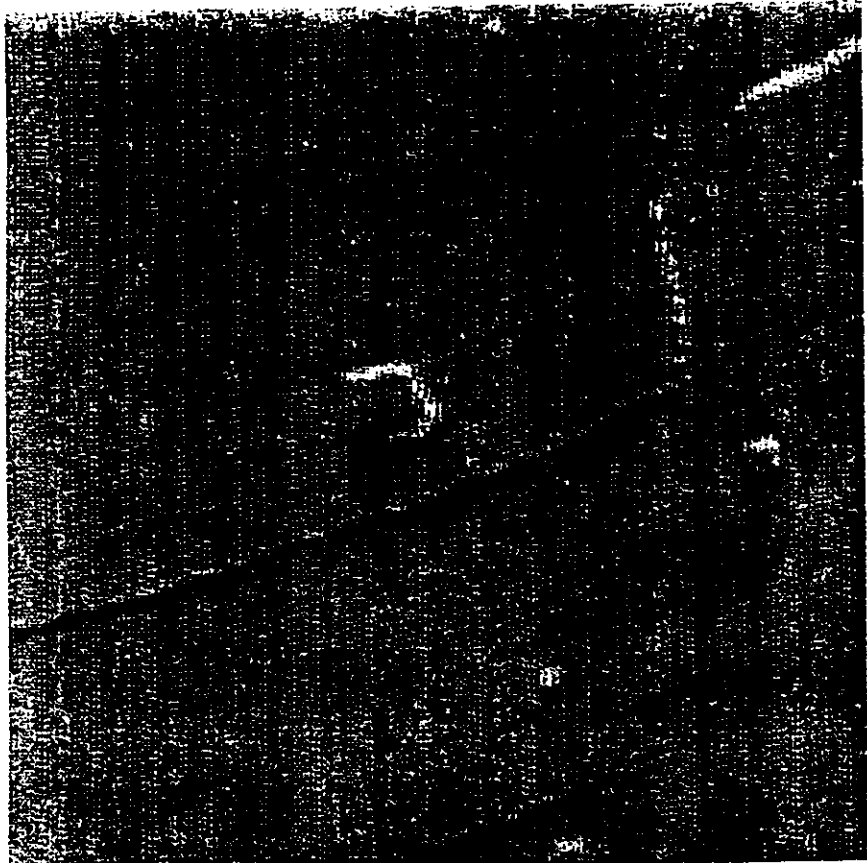
H. Hess, M. Gurevitch, unpublished STM.



FILE:e:\rc\hh022589.005  
Scan angle = 0 degrees, Scan range = 600 Angstrom.  
Time delay = 800, there are 128 data points.  
Bias = 0 volts.  
There are 78 integral values of height ranging over 0.4 A.



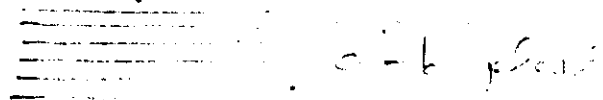
H. Hess, M. Guvitch, unpublished STM



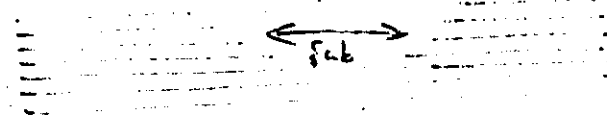
FILE:e:\rc\hh022589.003  
Scan angle = 0 degrees, Scan range = 500 Angstrom.  
Time delay = 800, there are 128 data points.  
Bias = 0 volts.  
There are 89 integral values of height ranging over 0.45 Å.

## Etch pits and tunneling

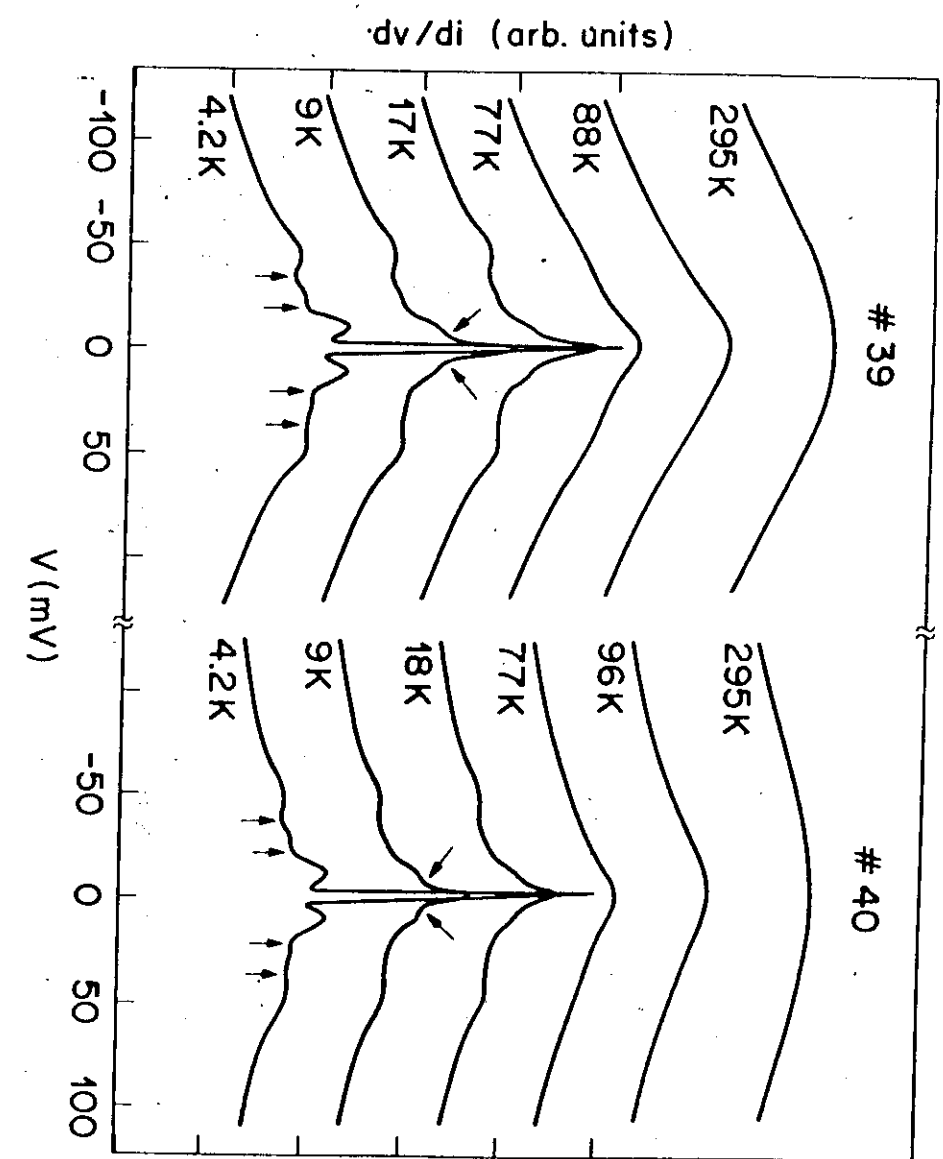
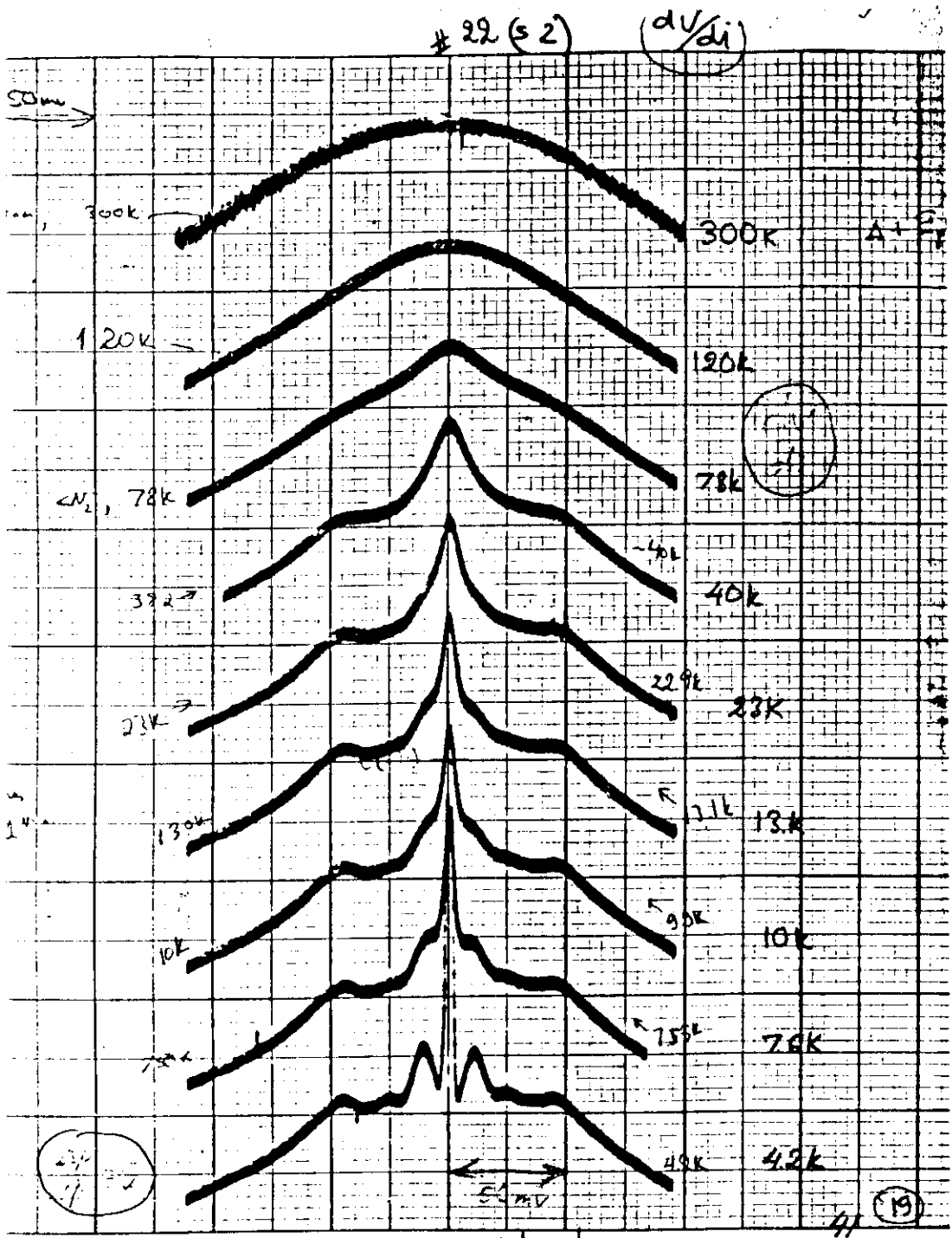
↓  $\xi_c \sim 1-2 \text{ \AA}$



↓  $\xi_c$



$\xi_{ab} \sim 10-15 \text{ \AA}$



1374-1400, 1989, 1990, 1991, 1992, 1993, 1994, 1995, 1996, 1997, 1998, 1999, 2000, 2001, 2002, 2003, 2004, 2005, 2006, 2007, 2008, 2009, 2010, 2011, 2012, 2013, 2014, 2015, 2016, 2017, 2018, 2019, 2020, 2021, 2022, 2023, 2024, 2025, 2026, 2027, 2028, 2029, 2030, 2031, 2032, 2033, 2034, 2035, 2036, 2037, 2038, 2039, 2040, 2041, 2042, 2043, 2044, 2045, 2046, 2047, 2048, 2049, 2050, 2051, 2052, 2053, 2054, 2055, 2056, 2057, 2058, 2059, 2060, 2061, 2062, 2063, 2064, 2065, 2066, 2067, 2068, 2069, 2070, 2071, 2072, 2073, 2074, 2075, 2076, 2077, 2078, 2079, 2080, 2081, 2082, 2083, 2084, 2085, 2086, 2087, 2088, 2089, 2090, 2091, 2092, 2093, 2094, 2095, 2096, 2097, 2098, 2099, 2100, 2101, 2102, 2103, 2104, 2105, 2106, 2107, 2108, 2109, 2110, 2111, 2112, 2113, 2114, 2115, 2116, 2117, 2118, 2119, 2120, 2121, 2122, 2123, 2124, 2125, 2126, 2127, 2128, 2129, 2130, 2131, 2132, 2133, 2134, 2135, 2136, 2137, 2138, 2139, 2140, 2141, 2142, 2143, 2144, 2145, 2146, 2147, 2148, 2149, 2150, 2151, 2152, 2153, 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0) FILM

b) SINGLE CRYSTAL

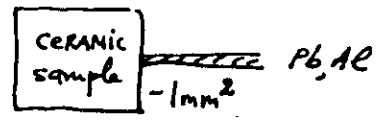
dV/dI (arb. units)

VOLTAGE (mV)

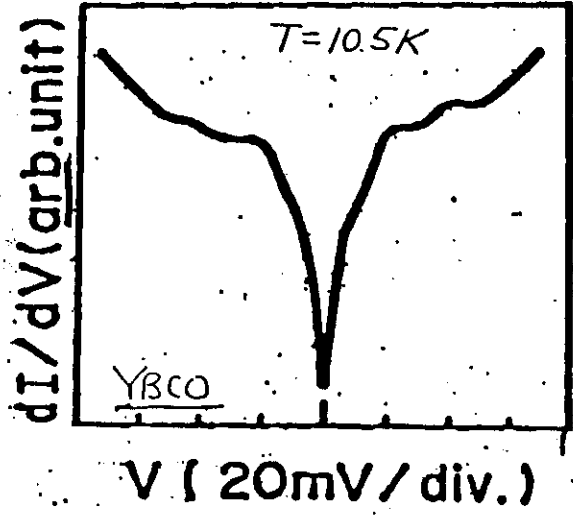
Fig. 3

I. Takeuchi, J.S. Tsai et al. *Physica C* 158, 83(89).

1:2:3  
2212  
2223



- natural surface
- cleaved at He
- sand paper

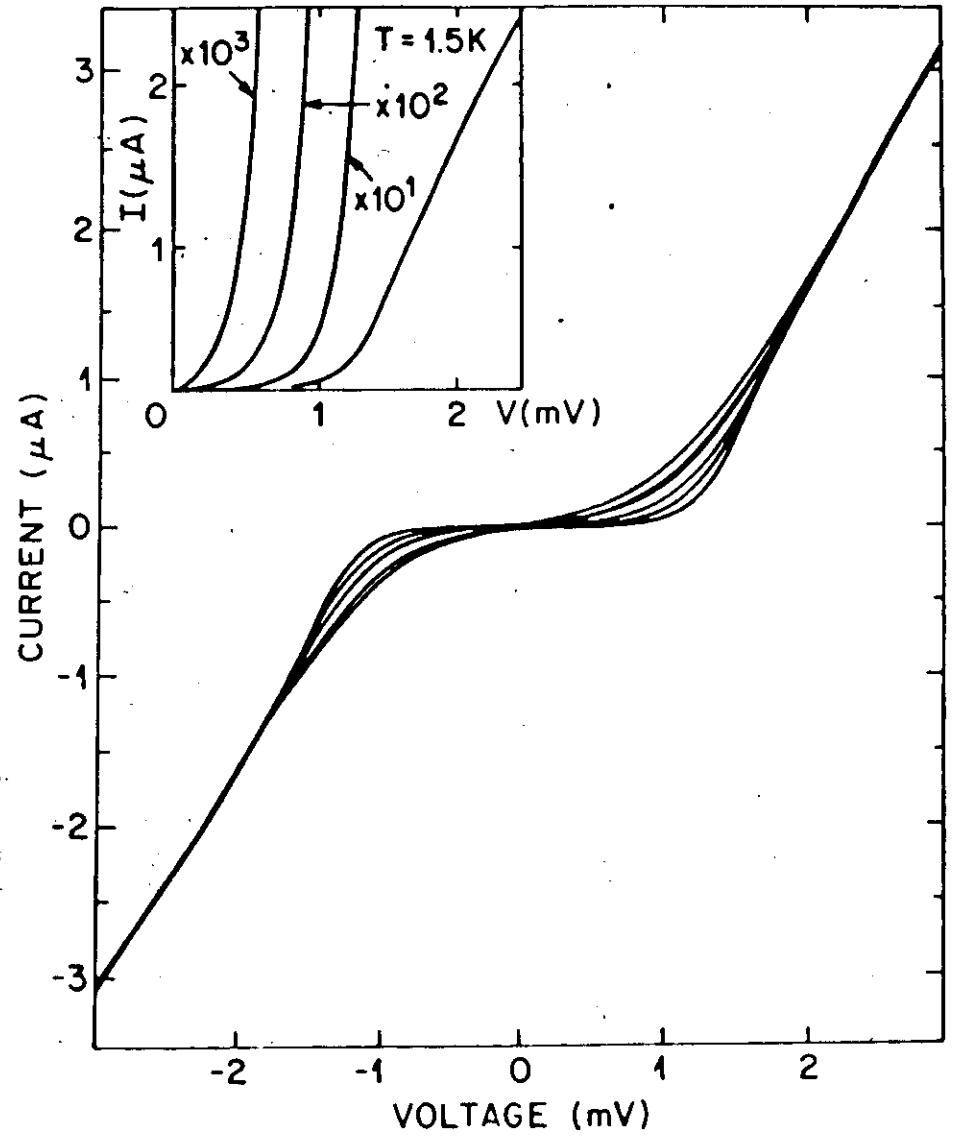
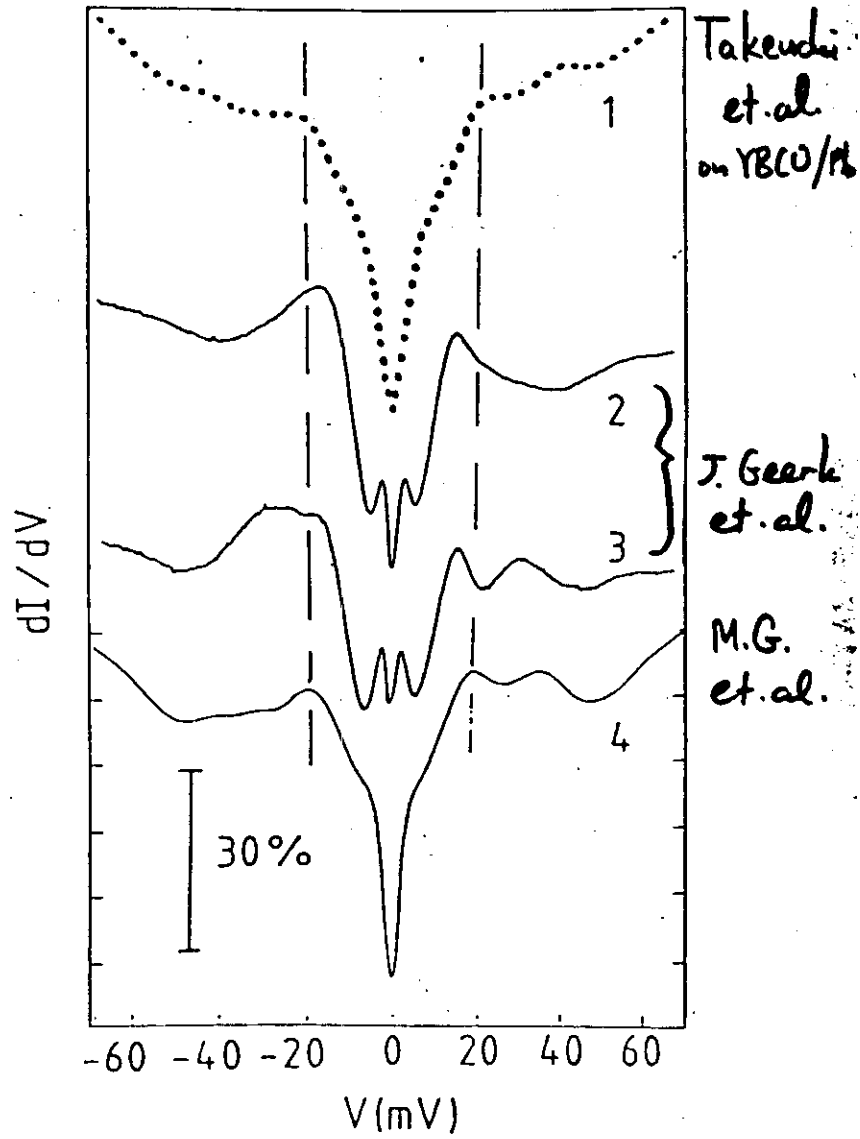


Authors:  
internal  
SIS?

30 300



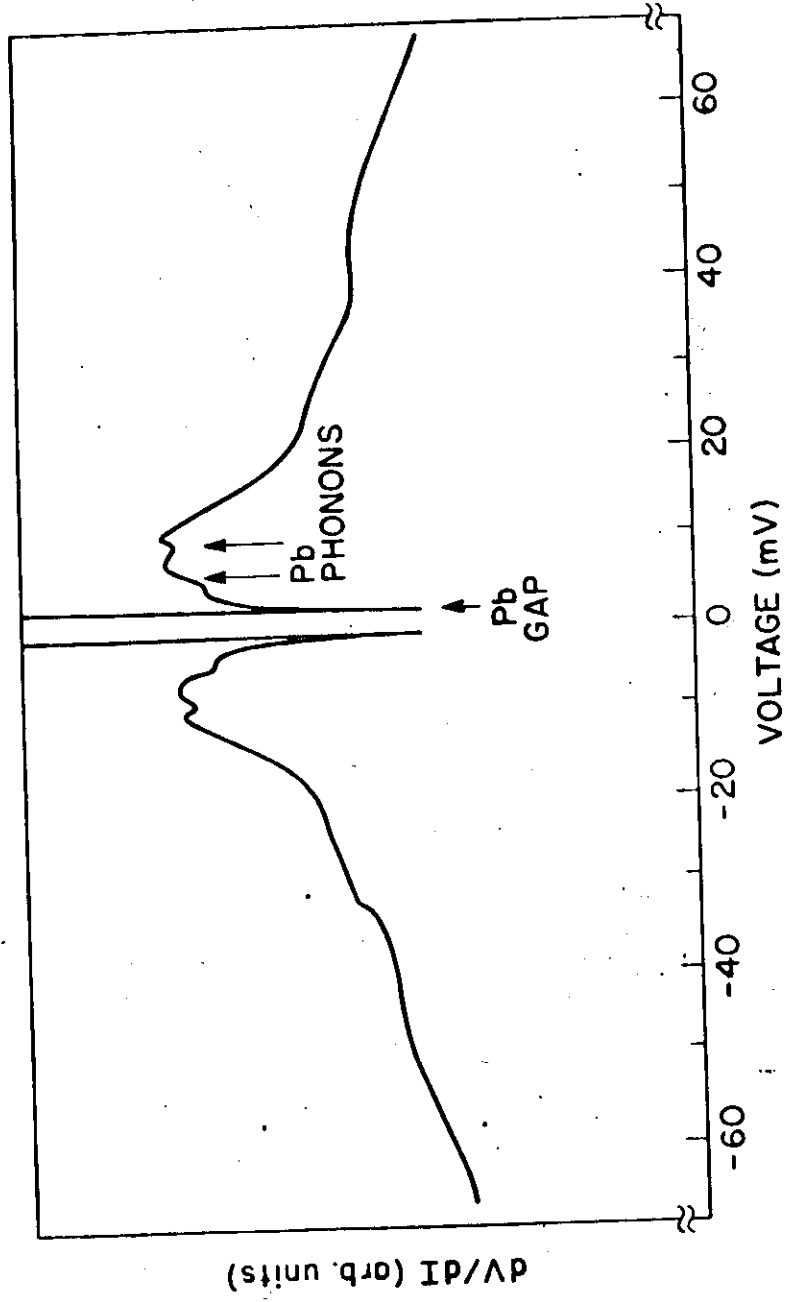
Comparison from J. Geerk et al.  
 N<sup>s</sup>-HTSC, Stanford



~~Fig 1~~

2k

20

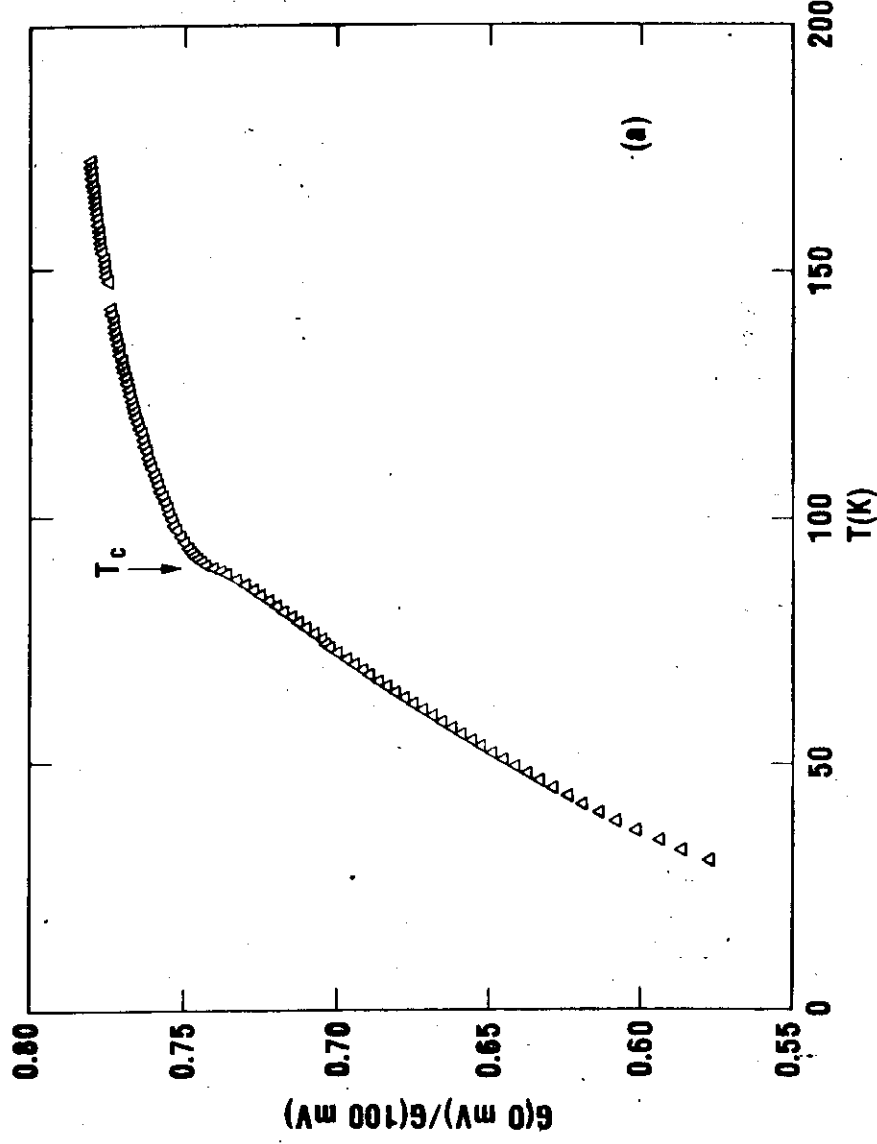


50

DO NOT AFFIX OVERLAYS ALONG THIS SURFACE

VG. NO.

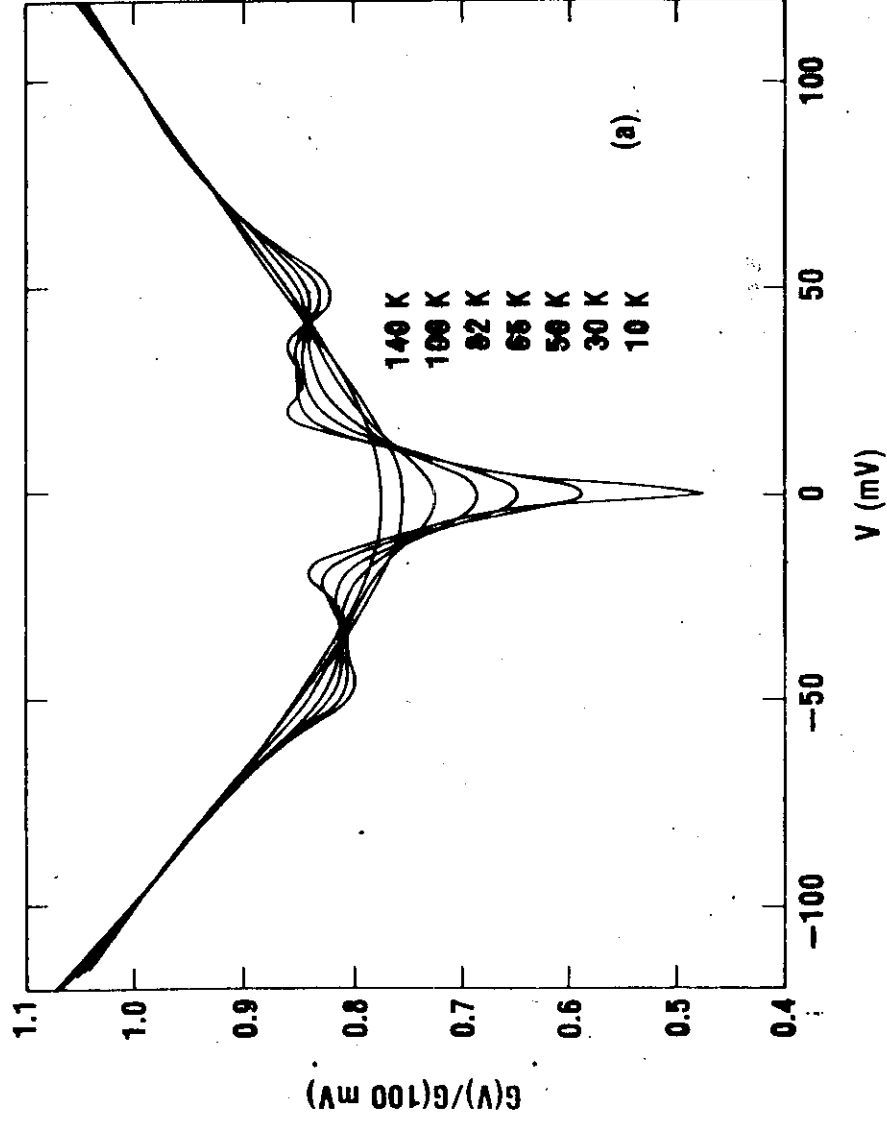
47



23

TOP  
DO NOT AFFIX OVERLAYS ALONG THIS SURFACE

VG. NO. \_\_\_\_\_

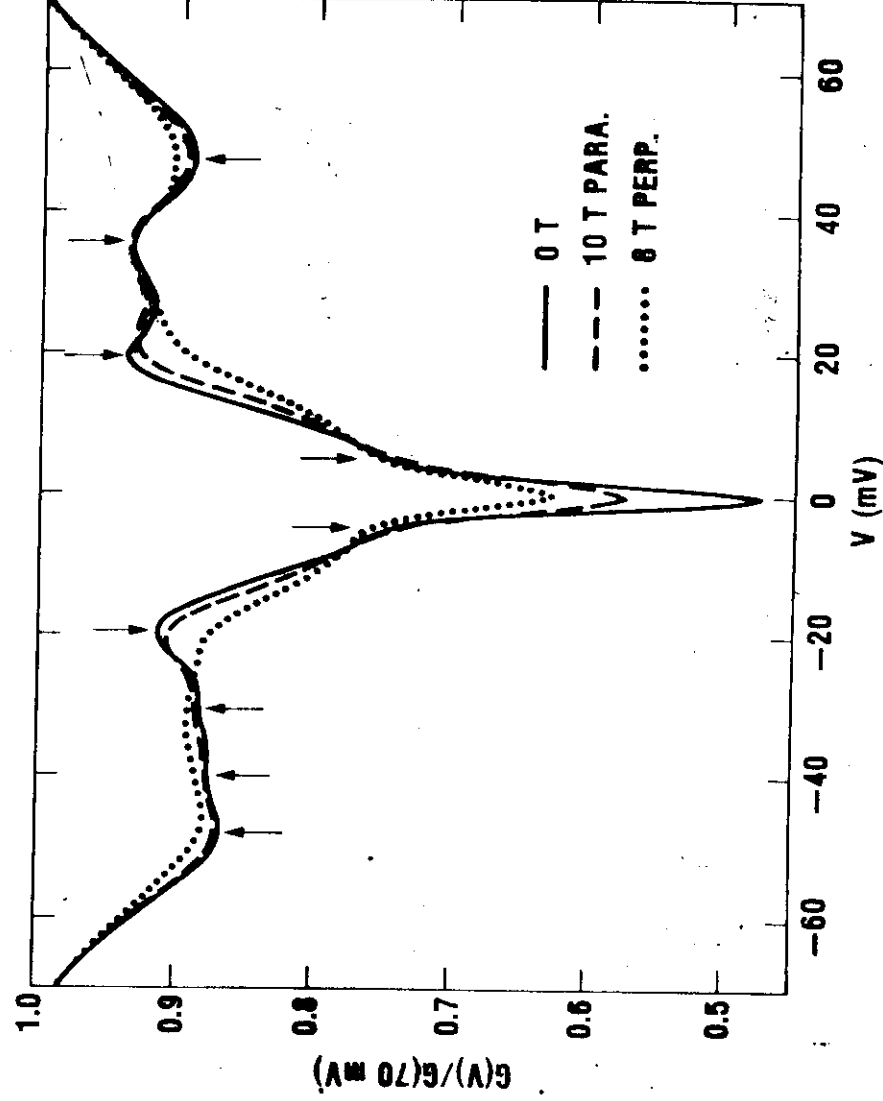


E-9148 (6-85)  
BELL LABORATORIES



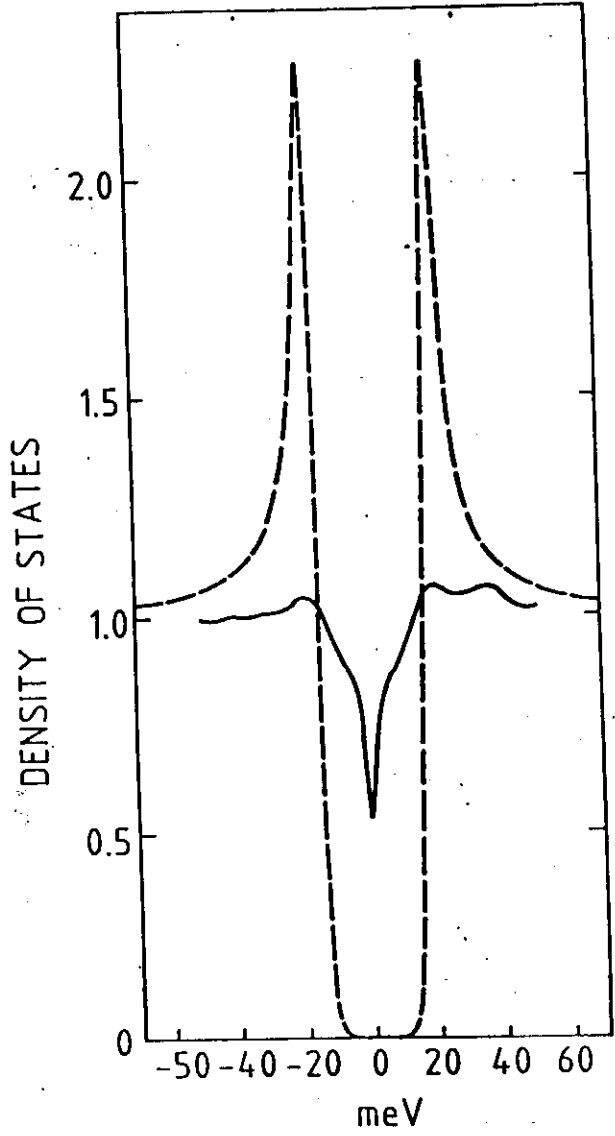
TOP  
DO NOT AFFIX OVERLAYS ALONG THIS SURFACE

VG. NO. \_\_\_\_\_



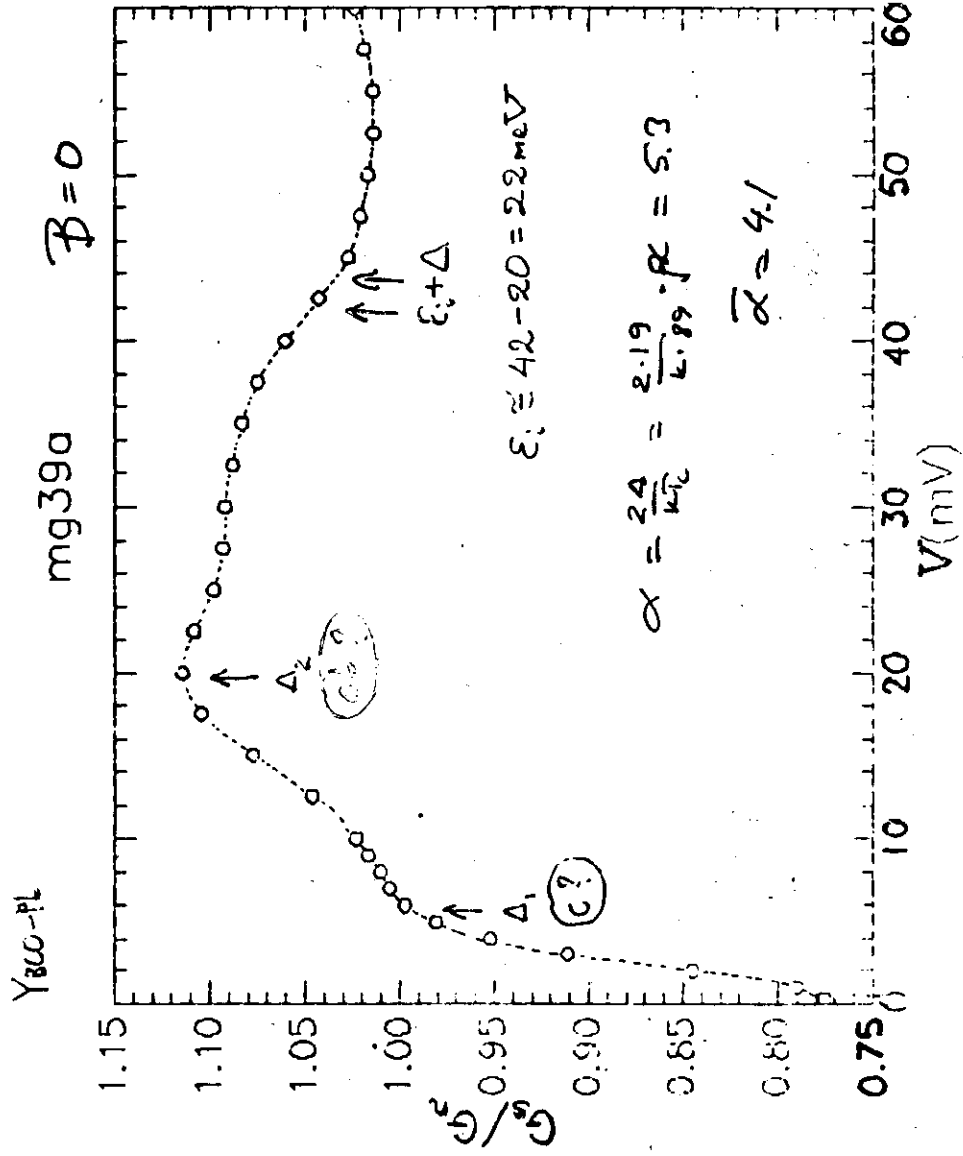
E-9148 (6-85)  
BELL LABORATORIES





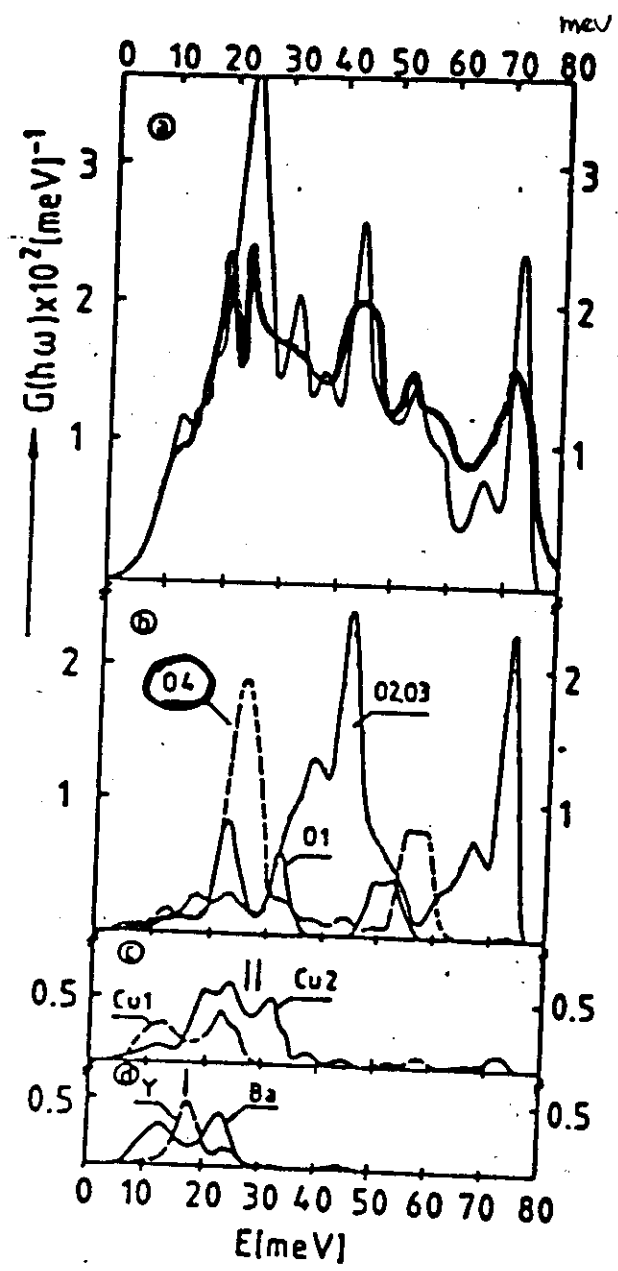
S-I-N

52 M. Gurvitch, J.M. Valles, K.C. Hynes, H. M. Garcia, and L.F. Schneemeyer 2/24

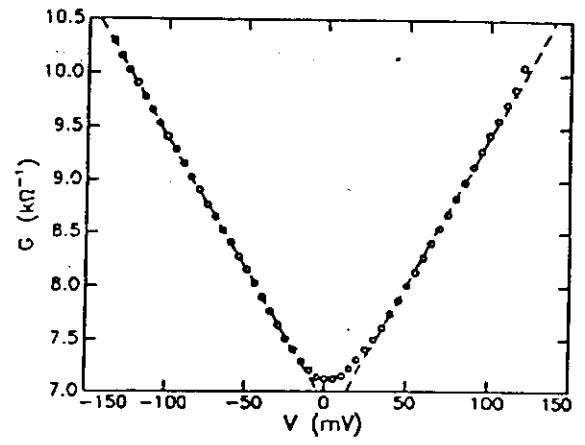


28

Tunneling conductance  $G(V)$  in the normal state



~~phonon~~  
phonon  
 $G(\omega)$   
 Renker et al.  
 Physica C 153-155  
 p. 272, 1988.



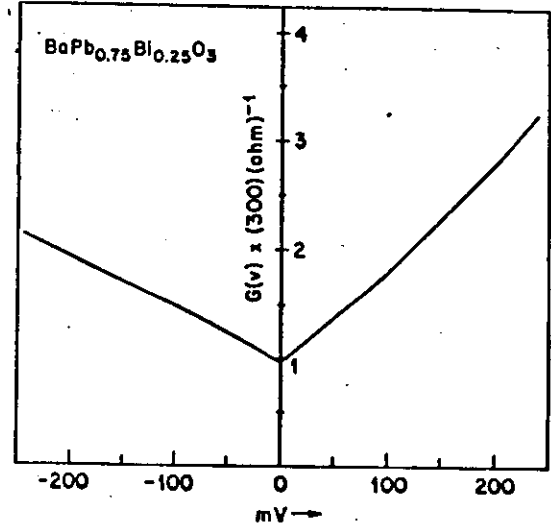
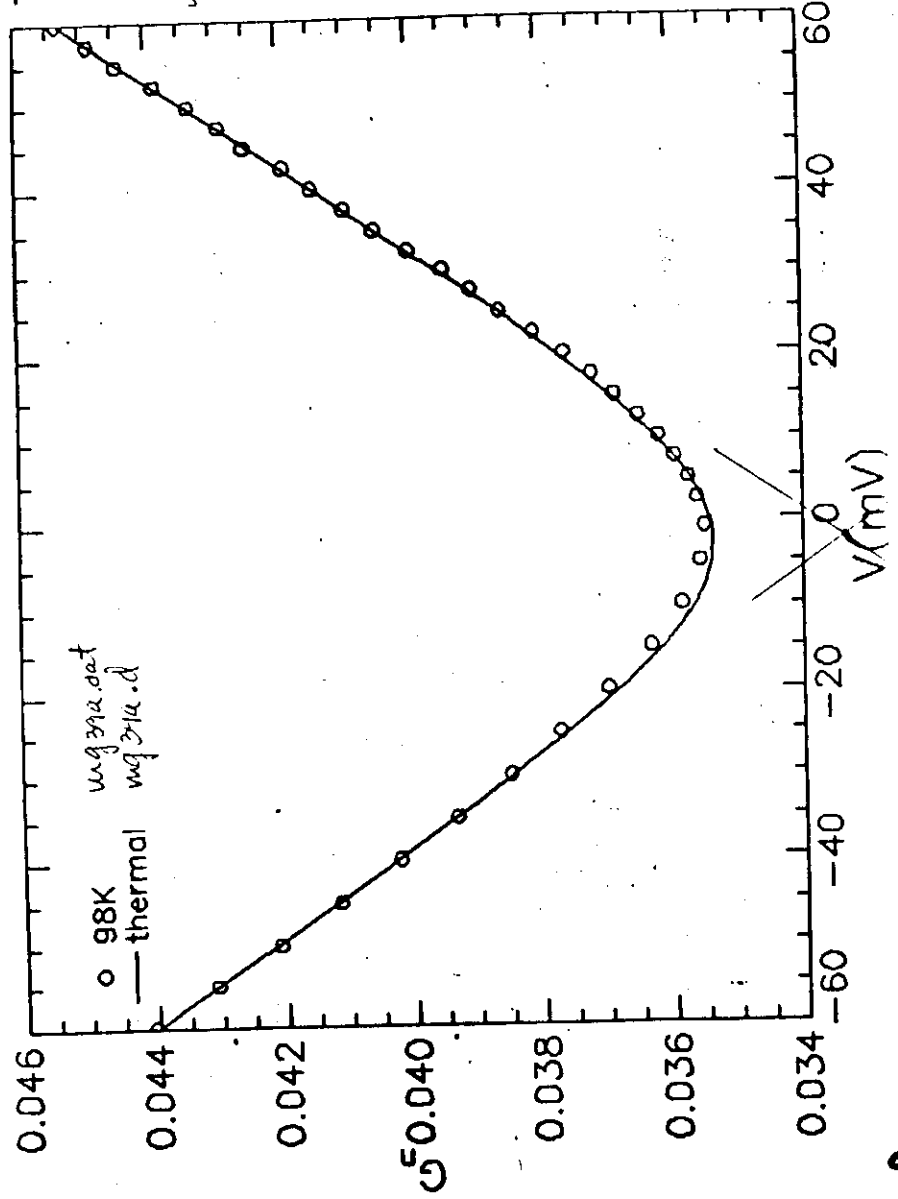
Tunneling conductance of  $\text{YBa}_2\text{Cu}_3\text{O}_{6.9}$ , from Ref. (8), M. Gurvitch et al., and J. Valles (unpublished).

FIGURE 3  
 Partial PDOS. solid line: calculation.

3/6/89

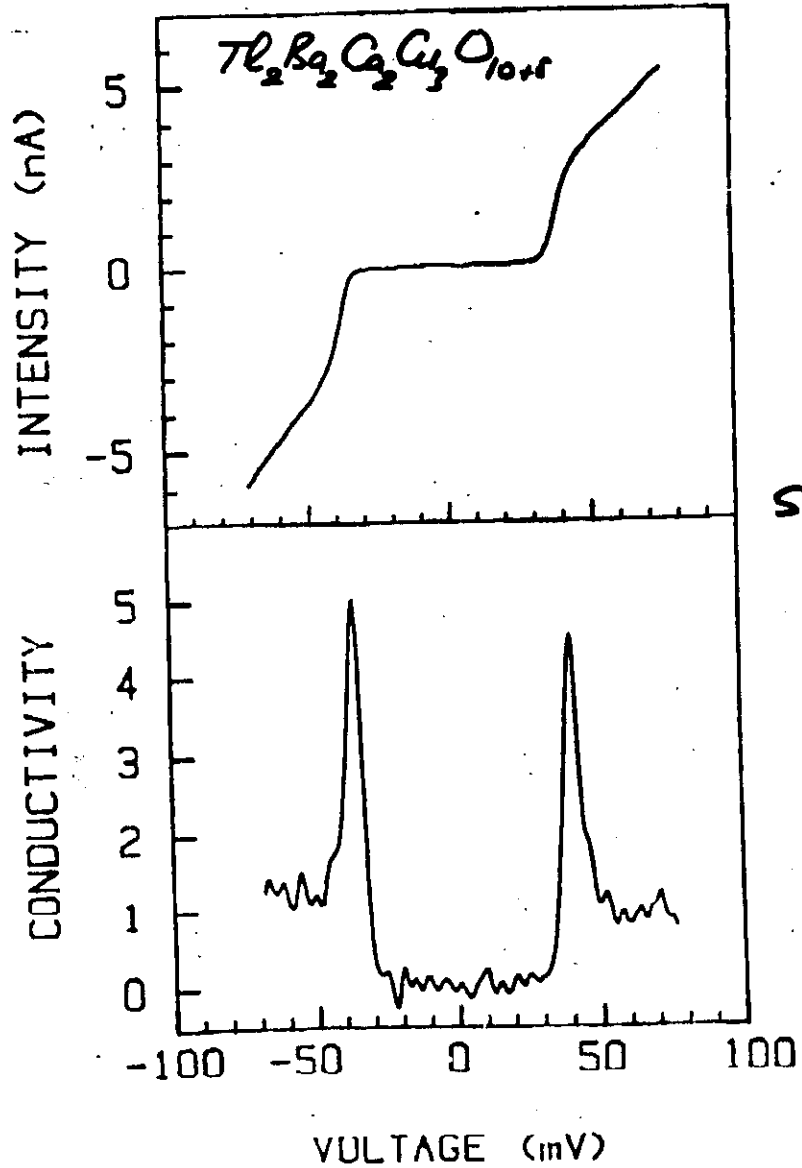
mg39a.dat and mg39a.d (tline1.f)

thermal fit  
 using  
 + line 1.f  
 w/ mp = .1946E  
 bb = .3367  
 wcn = -.1908E  
 bn = .3257  
 intersec = -.



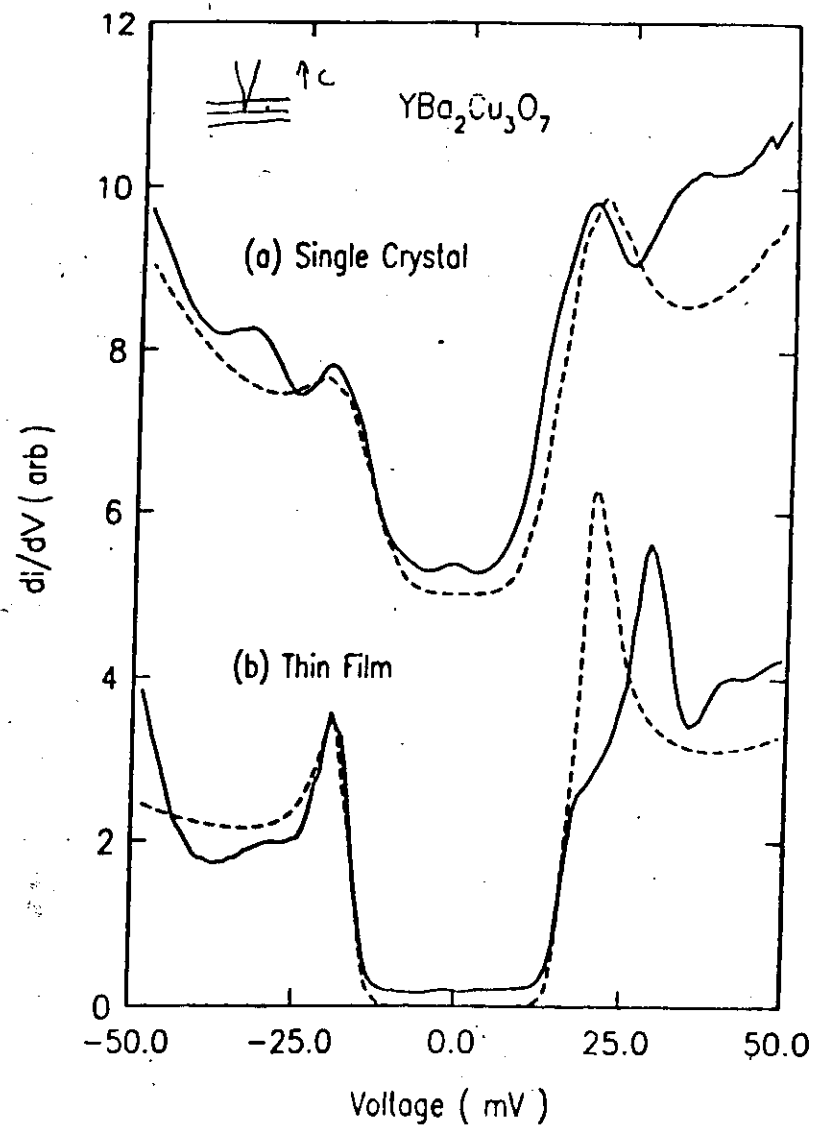
Tunneling conductance of BaPb<sub>0.75</sub>Bi<sub>0.25</sub>O<sub>3</sub> (R.C. Dynes)

S. Vieira, J.G. Rodrigo, M.A. Ramos, K.V. Rao  
and Y. Makino (Phys. Rev. Rapid Comm.)



J.R. Kirtley et al. PR B35, 1996 (37)

Point contact data



*M. T. H. Chi, unpublished  
H. Kojima, preprint*

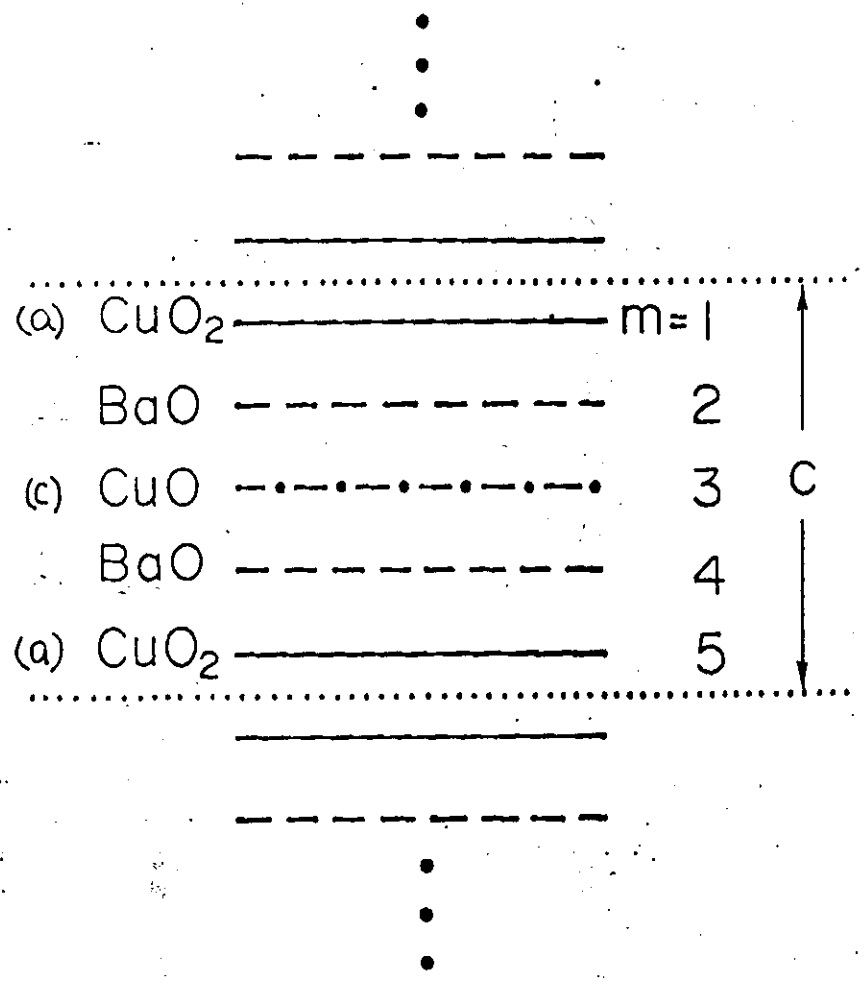


Fig.1

56

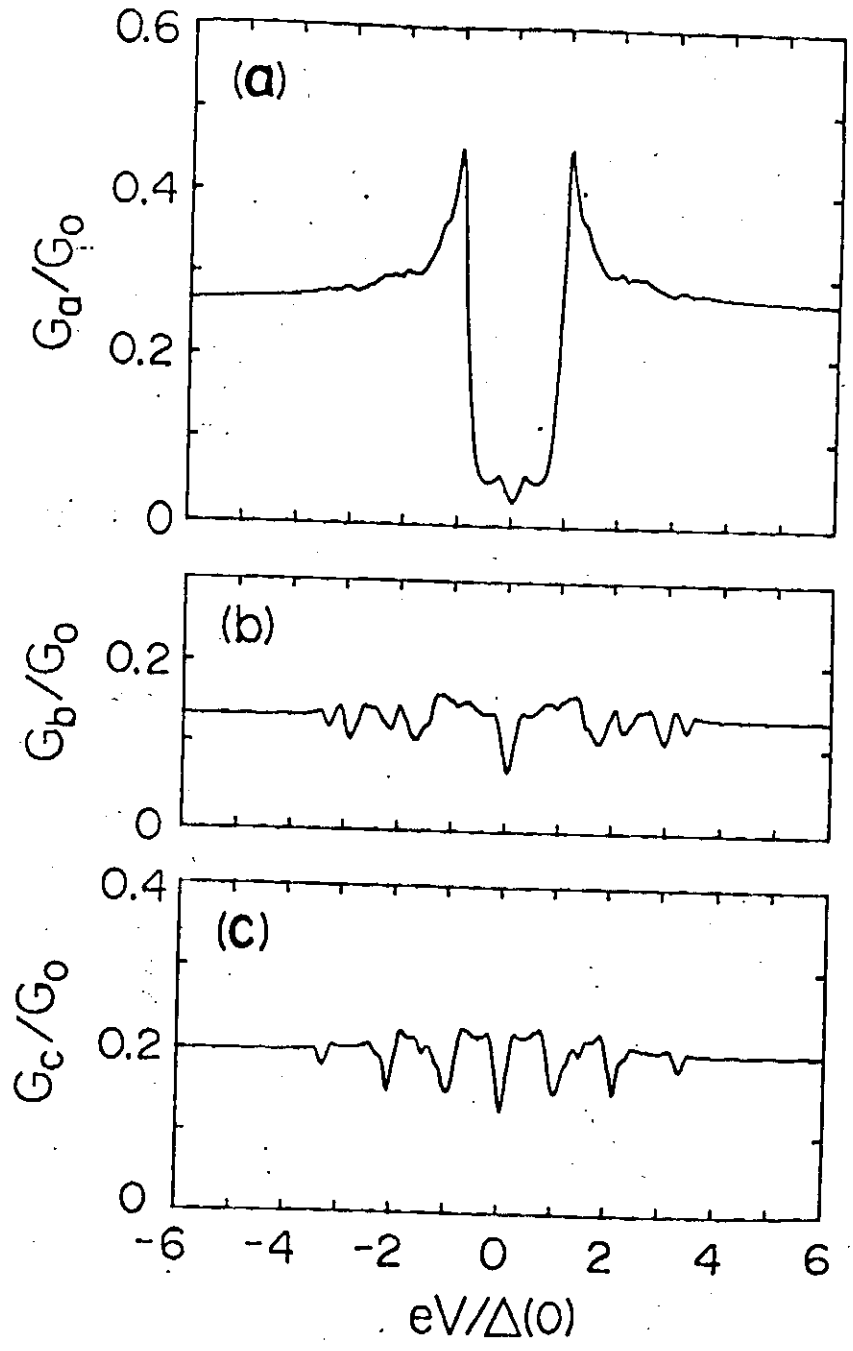


Fig.3



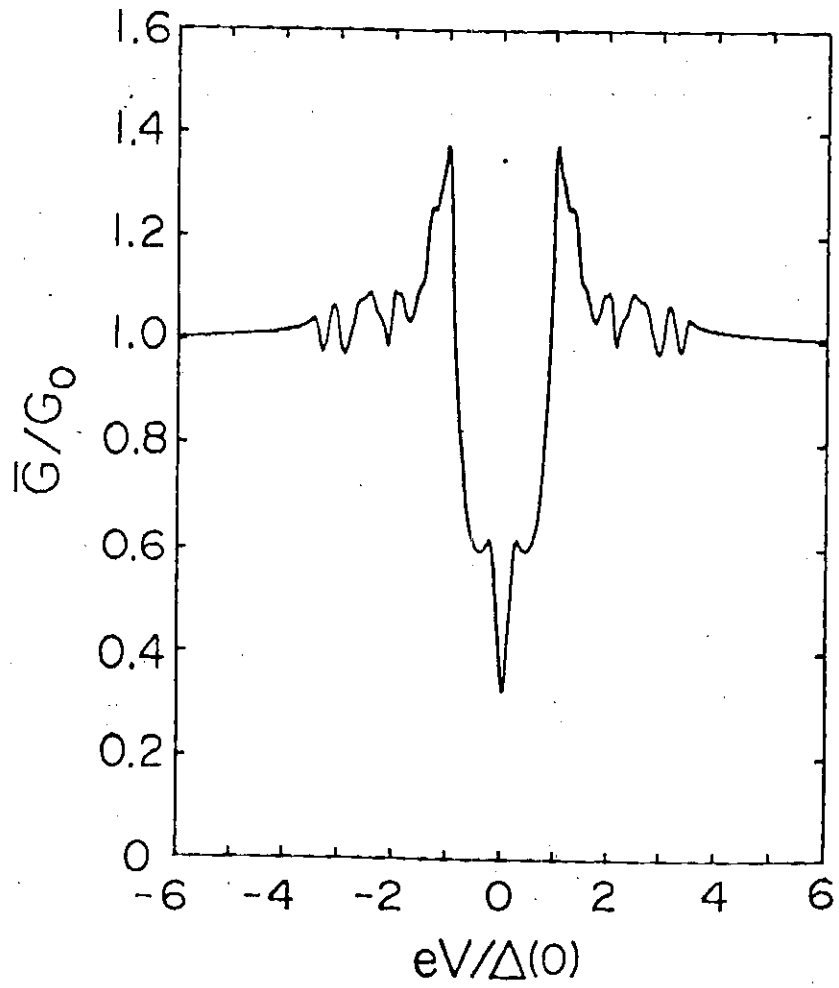


Fig.5

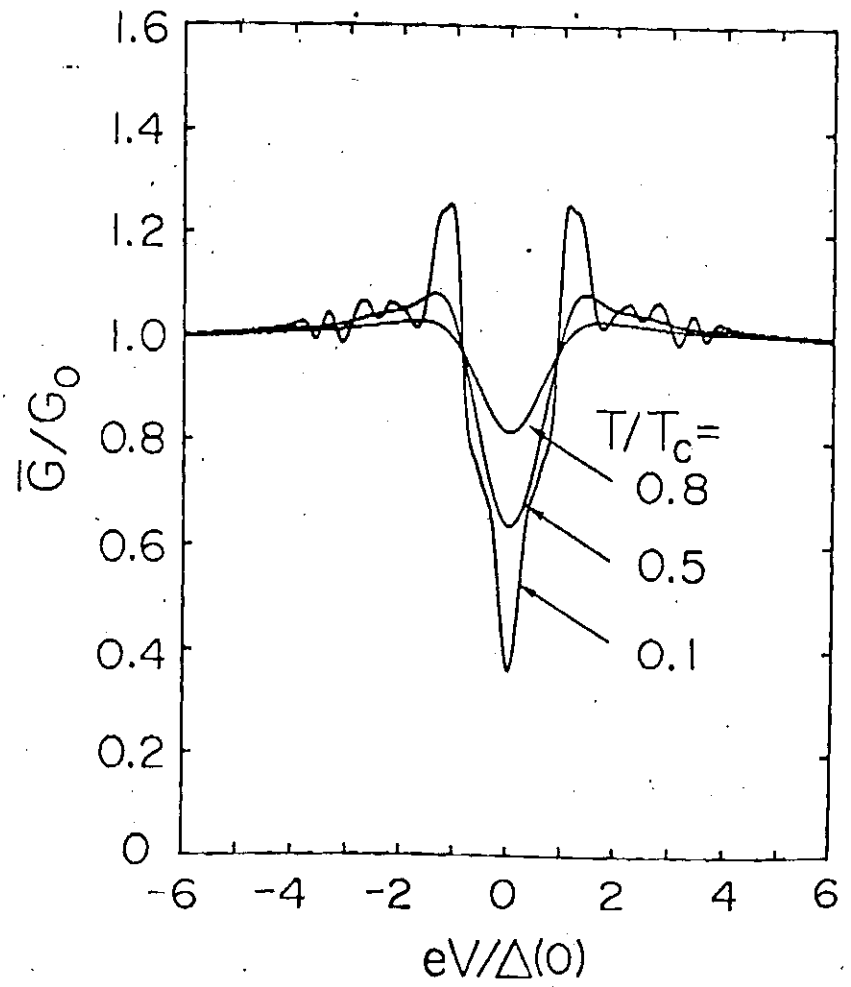


Fig.11

