



INTERNATIONAL ATOMIC ENERGY AGENCY  
 UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
**INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS**  
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UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



**INTERNATIONAL CENTRE FOR SCIENCE AND HIGH TECHNOLOGY**

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Winter College on Ultrafast Phenomena

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*Wavelength Tuning of Distributed  
 Feedback Dye Lasers*

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Wavelength Tuning  
 of Distributed  
 Feedback Dye  
 Lasers

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# Spectral Width of a bandwidth-limited Gaussian Pulse:

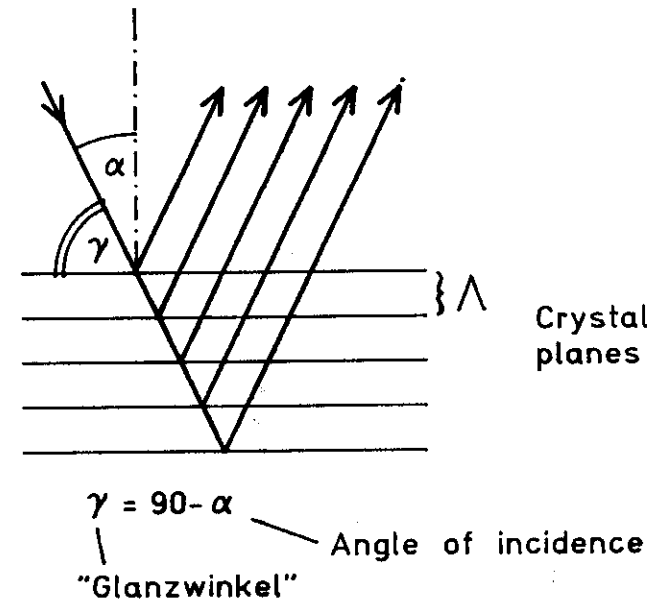
$$\Delta\nu \cdot \Delta t_p = 0.44$$

$$\Delta\lambda = \frac{\lambda^2}{c} \cdot \frac{0.44}{\Delta t_p}$$

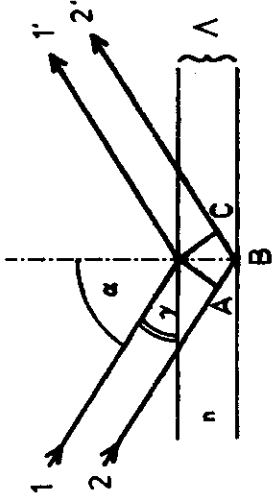
$$\lambda = 500 - 600 \text{ nm}$$

$\Delta t_p$	$\Delta\lambda$
100 fs	4 nm
1 ps	0.4 nm
100 ps	4 pm

# Bragg Scattering



# Bragg Scattering



Optical path difference:  $\Gamma = (\overline{AB} + \overline{BC}) \times n$

$$\overline{AB} = \overline{BC} = n \times \Lambda \times \cos \alpha$$

$$\Gamma = 2 \times n \times \Lambda \times \cos \alpha$$

$$\gamma = 90 - \alpha$$

Condition for Intensity Maxima

$$\Gamma = 2 \times n \times \Lambda \times \sin \gamma = m \times \lambda$$

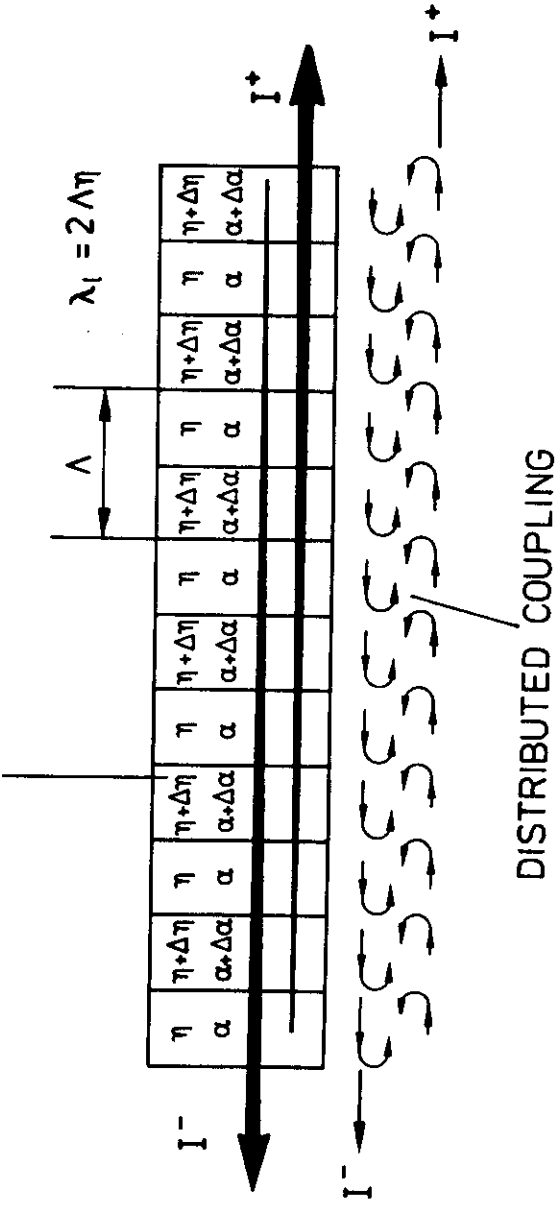
**Bragg's Law**

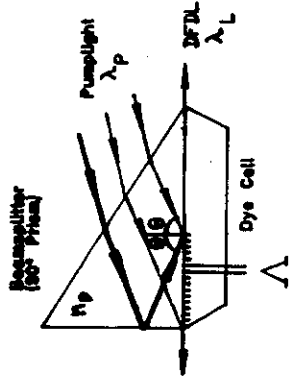
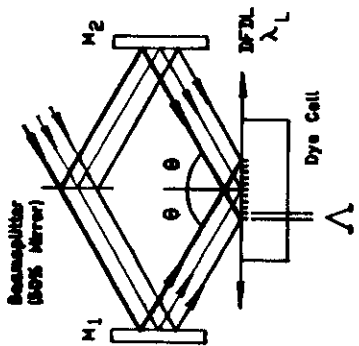
$\gamma = 90^\circ$  Normal Incidence  $2 \times n \times \Lambda = m \times \lambda$  Working Condition of DFDL interference order

w

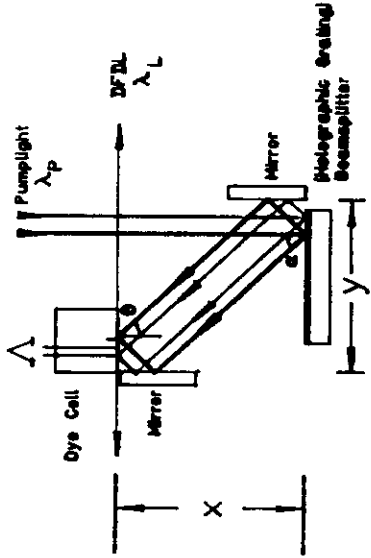
## PRINCIPLE OF DISTRIBUTED FEEDBACK LASER

MEDIUM WITH SPATIALLY PERIODIC MODULATION OF REFRACTIVE INDEX AND GAIN





$\Lambda = \frac{\lambda_p}{2 \sin \theta}$	Fringe Spacing
$\lambda_L = 2 n_s \Lambda$	DFDL Wavelength
$\lambda_L = \frac{n_s \lambda_p}{n_p \sin \theta}$	DFDL Wavelength



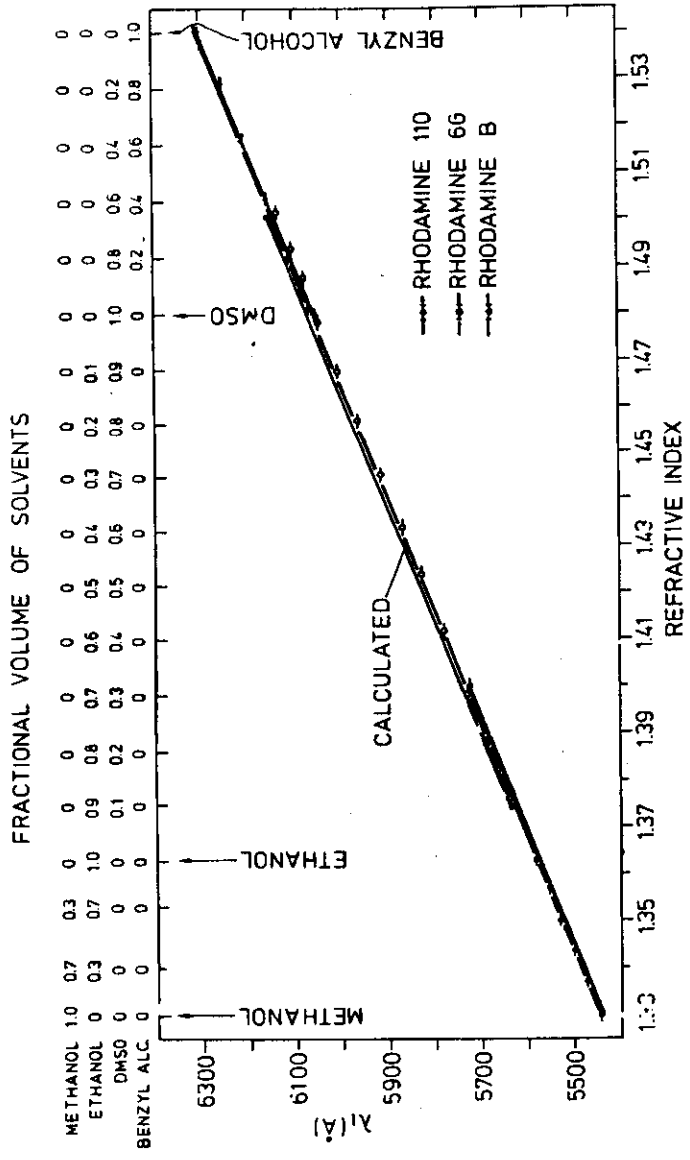
$\Lambda = \frac{\lambda_p}{2 \sin \theta}$	Fringe Spacing
$d \sin \alpha = \lambda_p$	Grating Equation
Condition for $\alpha = \theta$ : $x/y = \sqrt{(d/\lambda_p)^2 - 1}$	
$\Lambda = d/2$	
$\lambda_L = 2 n_s \Lambda$	DFDL Wavelength
$\lambda_L = n_s d$	DFDL Wavelength

## Wavelength Tuning of the Distributed Feedback Dye Laser

$$\lambda_D = \frac{2 \times n_s \times \Lambda}{m}$$

$n_s$  = refractive index of dye solution depends on:

solvent composition  
temperature  
pressure



Dependence of refractive index  $n$  on temperature and pressure is given by the LORENTZ-LORENZ formula (1880):

$$\alpha = \frac{3}{4\pi N} \frac{\epsilon - 1}{\epsilon + 2} = \frac{3}{4\pi N} \frac{n^2 - 1}{n^2 + 2}$$

Maxwell's Relation  $\epsilon = n^2$

$\alpha$  = mean polarizability  
 $\epsilon$  = dielectric constant  
 $N$  = number density

Introducing the molar refractivity  $A$

$$A = \frac{4\pi}{3} N_m \alpha$$

$N_m = 6.02 \cdot 10^{23}$  molecules/mole  
 Avogadro's Number

$$A = \frac{4\pi}{3} N_m \alpha$$

Molar  
Refractivity

$$\frac{N_m}{N} = \frac{(M)}{\rho}$$

(M) = molecular weight

$\rho$  = mass density

T = absolute temperature

p = pressure

$$A = \frac{(M)}{\rho} \frac{n^2 - 1}{n^2 + 2} \approx \text{const}$$

$$\rho = \rho(p)$$

$$\rho = \rho(T)$$

$$\kappa = \frac{1}{\rho} \left( \frac{\partial \rho}{\partial p} \right)_T$$

$$\gamma = \frac{1}{\rho} \left( \frac{\partial \rho}{\partial T} \right)_p$$

$\kappa$  = Compressibility  
of the liquid

$\alpha'$  = linear } expansion  
 $\gamma$  = cubic } coefficient

$$\gamma = 3\alpha'$$

$$\frac{n^2 - 1}{n^2 + 2} = \frac{A}{(M)} \rho$$

Temperature dependence of n :

$$\frac{d\left(\frac{n^2 - 1}{n^2 + 2}\right)}{dn} \cdot \frac{dn}{dT} = \frac{A}{(M)} \cdot \frac{d\rho}{dT}$$

$$\frac{6n}{(n^2 + 2)^2} \cdot \frac{dn}{dT} = \frac{A}{(M)} \cdot \frac{d\rho}{dT}$$

$$\frac{dn}{dT} = \frac{A}{(M)} \cdot \frac{(n^2 + 2)^2}{6n} \cdot \frac{d\rho}{dT}$$

$$\lambda_D = 2 \cdot n \cdot \Lambda$$

$$\frac{d\lambda_D}{dT} = 2\Lambda \cdot \frac{dn}{dT}$$

Liquid	Density g cm <sup>-3</sup>	$\gamma$ K <sup>-1</sup>	$\kappa$ atm <sup>-1</sup>
Acetone	0.791	1.43 · 10 <sup>-3</sup>	1.26 · 10 <sup>-4</sup>
Ethanol	0.789	1.10	1.14
Methanol	0.792	1.19	1.20

at 18°C

12.2.91 / DF DL10.MCD  
 Temperaturabhängigkeit der Laserwellenlänge  
 (vgl. Lusty & Dunn (1987))

$$\phi := 10^{-3} \quad \frac{dn}{dT} \text{ für organ. Lösungsmittel}$$

$$\lambda_p := 532 \cdot \text{nm} \quad \text{Pumpwellenlänge}$$

$$\theta := 50 \cdot \text{deg} \quad \text{Pump-Einfallswinkel}$$

$$\frac{\lambda_p}{\sin(\theta)} = 694.477 \cdot \text{nm}$$

$$\Delta \lambda_L = \frac{d\lambda}{dT} = \left( \frac{d\lambda}{dn} \right) \cdot \left( \frac{dn}{dT} \right)$$

$$\Delta \lambda_L := \frac{\lambda_p}{\sin(\theta)} \cdot \phi \quad \frac{d\lambda}{dT} \text{ für den DF DL}$$

$$\Delta \lambda_L = 0.694 \cdot \text{nm} \quad \text{pro grad}$$

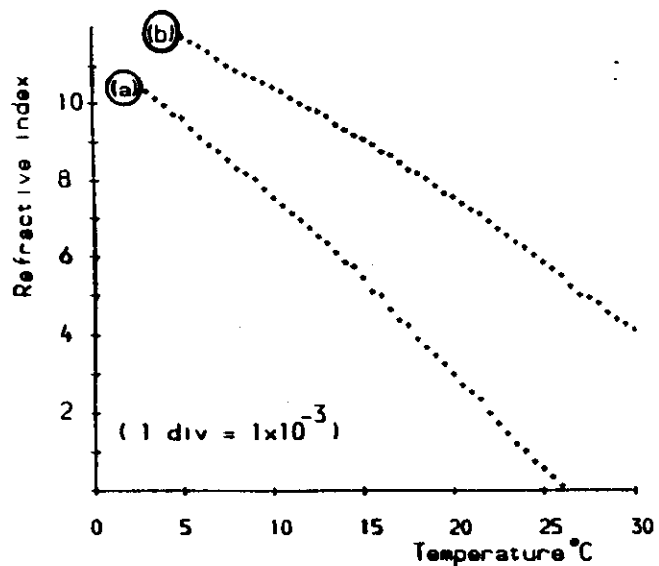


Fig. 1. Refractive index against temperature of a methanol, and b ethylene glycol. Vertical axis divisions correspond to a change in refractive index of  $1 \times 10^{-3}$ . Methanol had the largest  $dn/dT$  of any of the solvents measured

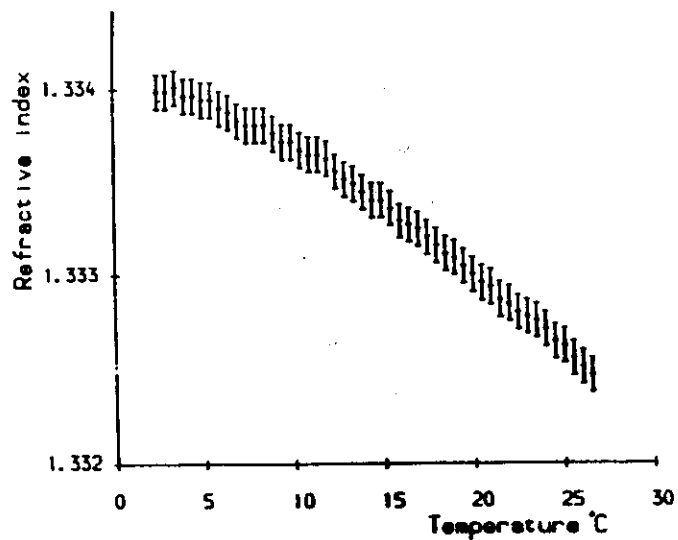


Fig. 3. Refractive index against temperature of pure water. Vertical axis divisions correspond to a change in refractive index of  $1 \times 10^{-3}$ . Around 4°C refractive index is constant i.e.  $dn/dT=0$

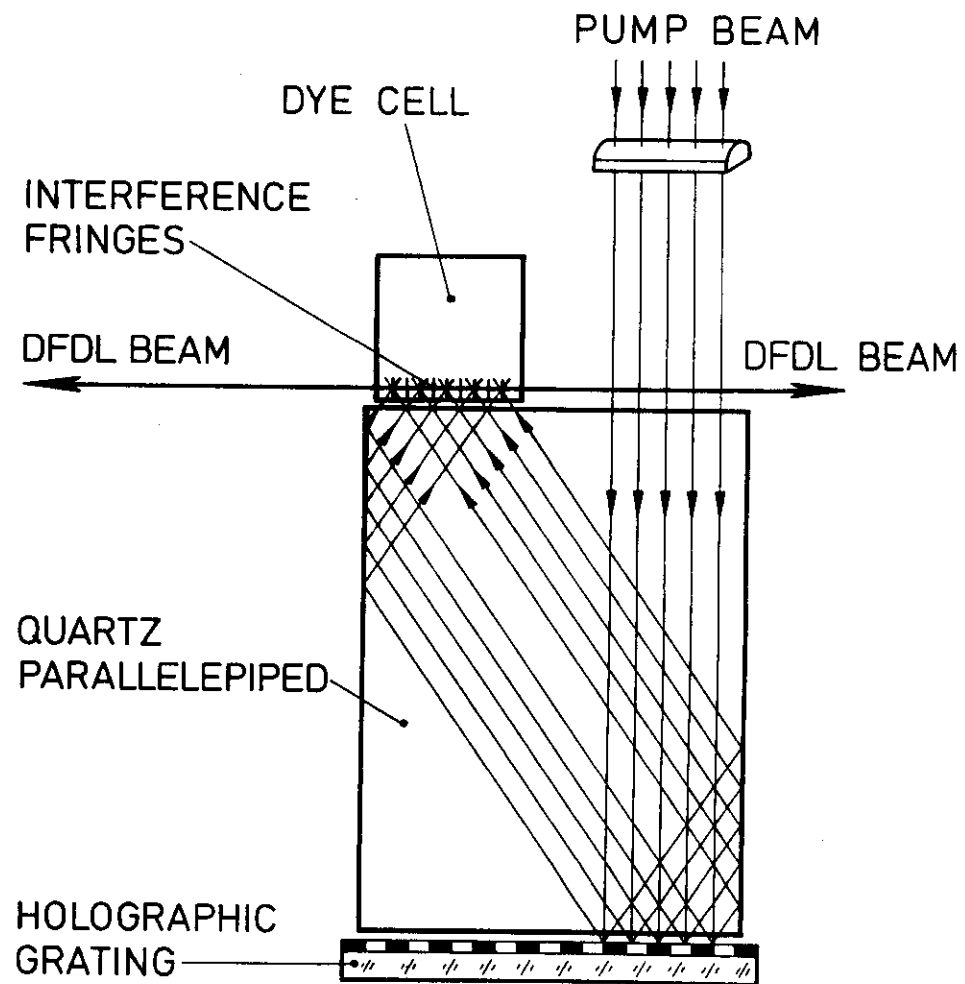
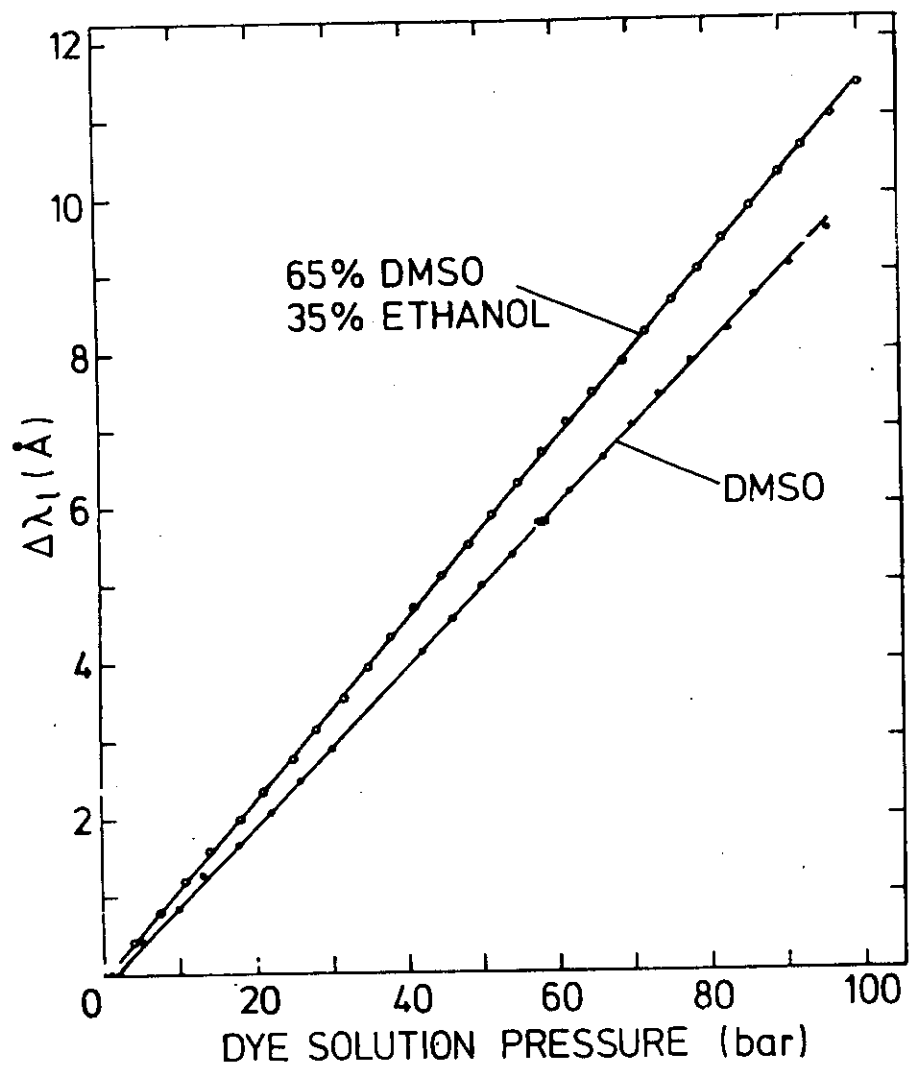
Table 1. Measured values of  $dn/dT$  (over range 5-25°C) for organic solvents. For convenience refractive index data for the individual solvents is given in brackets, and is taken from CRC [8] tabulated values

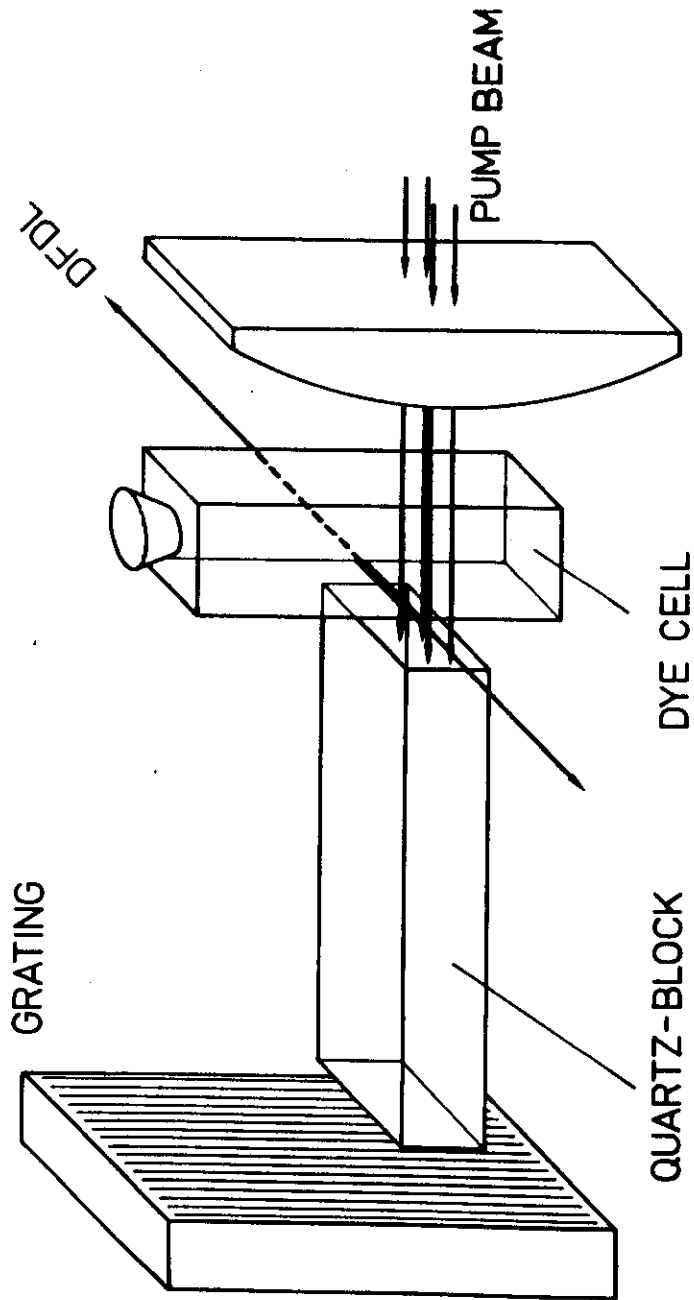
Solvent	$n(20^\circ\text{C})$	$dn/dT$ [ $-1$ $\times 10^{-5} \text{K}^{-1}$ ] (5-25°C)
Methanol	(1.327)	46.8(1.1)
Ethanol	(1.360)	43.8(0.4)
Ethylene glycol	(1.431)	30.6(0.3)
Benzyl alcohol	(1.540)	42.0(0.4)
Propylene carbonate	(1.421)	38.0(0.4)
50/50 BA/PC	(1.471)	42.0(0.5)

LUSTY AND DUNN (1987)

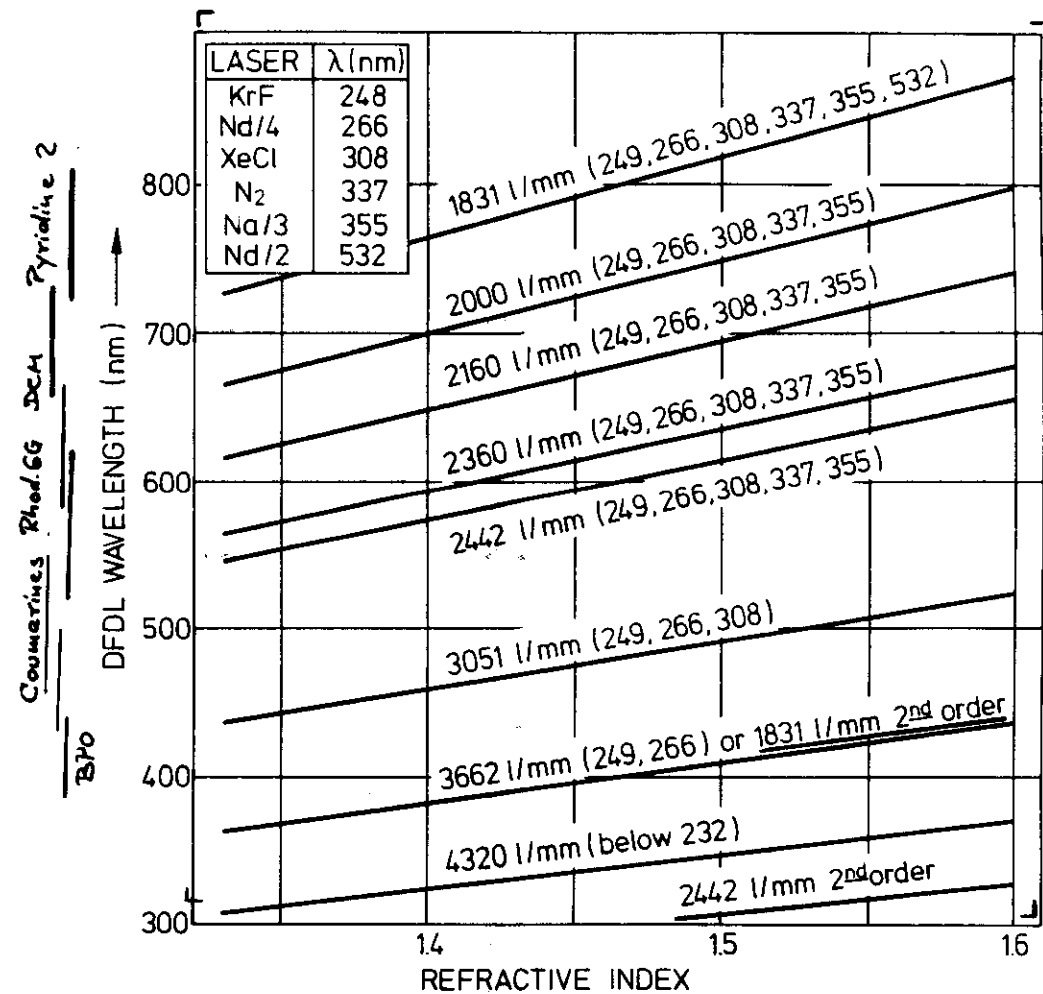
8







$$\lambda_L = \frac{2 n_s \Lambda}{m} = \frac{2 n_s d}{m}$$



- METHANOL
- WATER
- ACETONE
- ETHANOL
- $\alpha$ -HEXANE
- 1-PROPANOL
- 1-BUTANOL
- 1-PENTANOL
- P-DIOXANE
- 1-HEPTANOL
- CYCLOHEXANE
- 1-OCTANOL
- ETHYLENE GLYK
- CHLOROFORM
- CCl<sub>4</sub>
- GLYCERINE
- DMSO
- TOLUENE
- BENZENE
- BENZ. ALCOH.
- DIPHENYLETHER

DFDL with holographic grating as beamsplitter

$$\lambda_L = \frac{2 n_s \Lambda}{m}$$

Operation in 2<sup>nd</sup> order:  $m=2$

grating constant: 1831 lines/mm

pump laser: nitrogen  
(Lambda Physik M-1000)

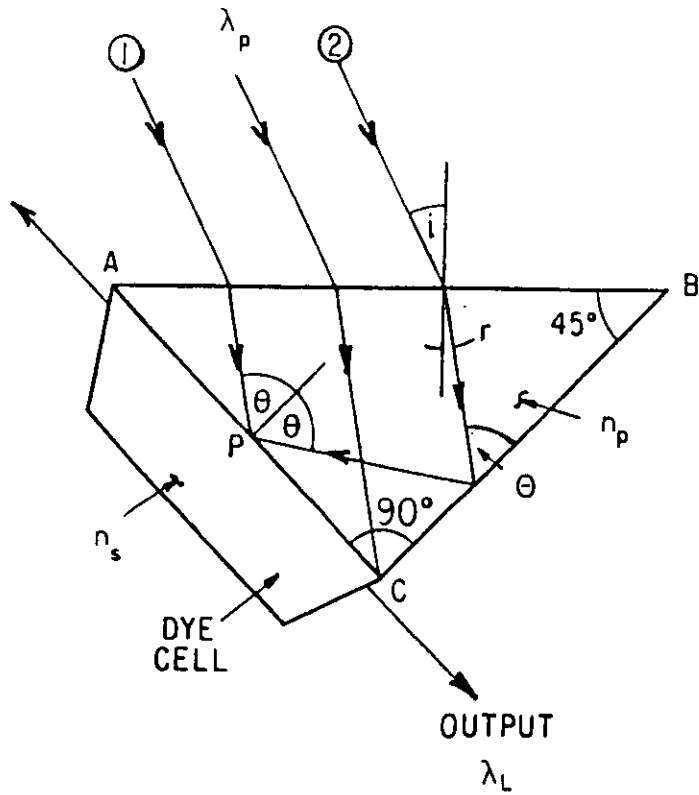
DYE	CONCENTRATION MOL/L	SOLVENT	LASING WAVELENGTH NM
PBD	$5 \cdot 10^{-3}$	38% ETHANOL 62% METHANOL	363
BIBUQ	$1 \cdot 10^{-3}$	80% DIOXANE 20% ETHANOL	383
BIBUQ	$1.5 \cdot 10^{-3}$	100% DIOXANE	388
DPS	$1 \cdot 10^{-3}$	90% TOLUENE 10% ETHANOL	404
STILBEN 1	SATURATED	50% DIMETHYLSULFOXIDE 50% DIPHENYLETHER	413
BIS-MSB	$1 \cdot 10^{-3}$	25% DIOXANE 75% DIPHENYLETHER	421

Wavelength Tuning of the Distributed Feedback Dye Laser

$$\lambda_D = \frac{2 \times n_s \times \Lambda}{m}$$

$\Lambda$  = Separation of Interference Fringes

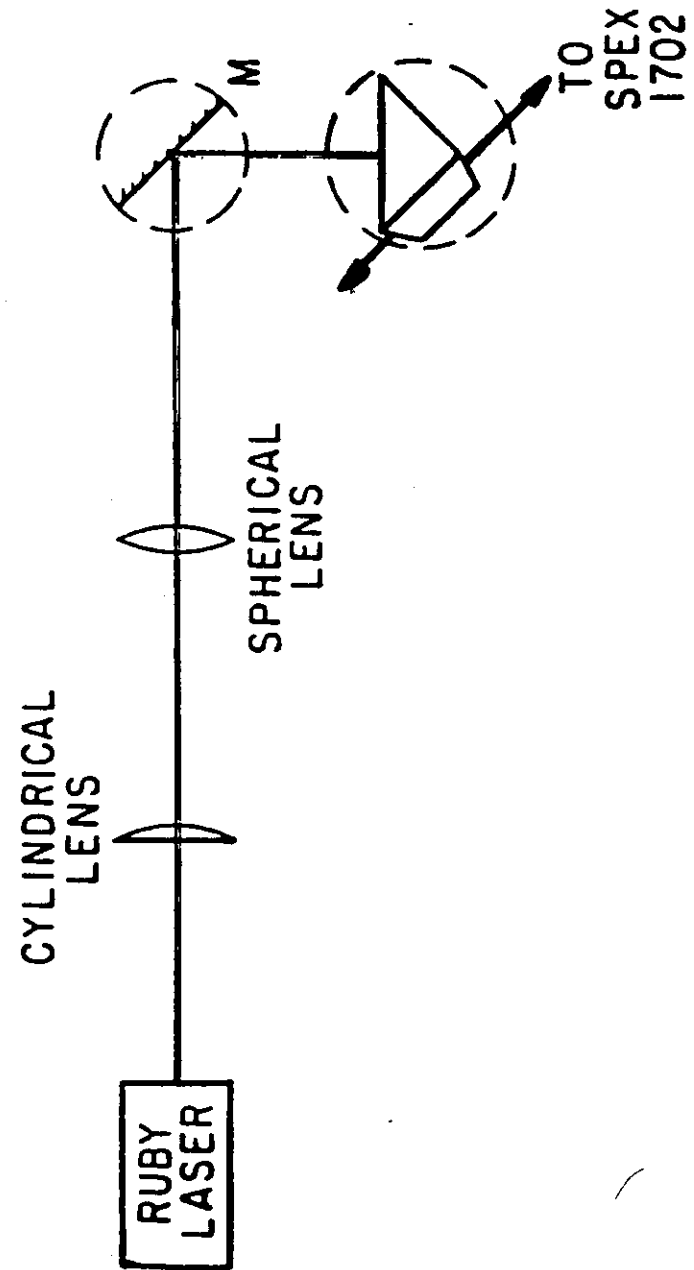
# Prism Dye Laser



$$\lambda_L = \frac{n_s \lambda_p}{n_p \sin \theta} \quad \theta = \frac{\pi}{4} + r$$

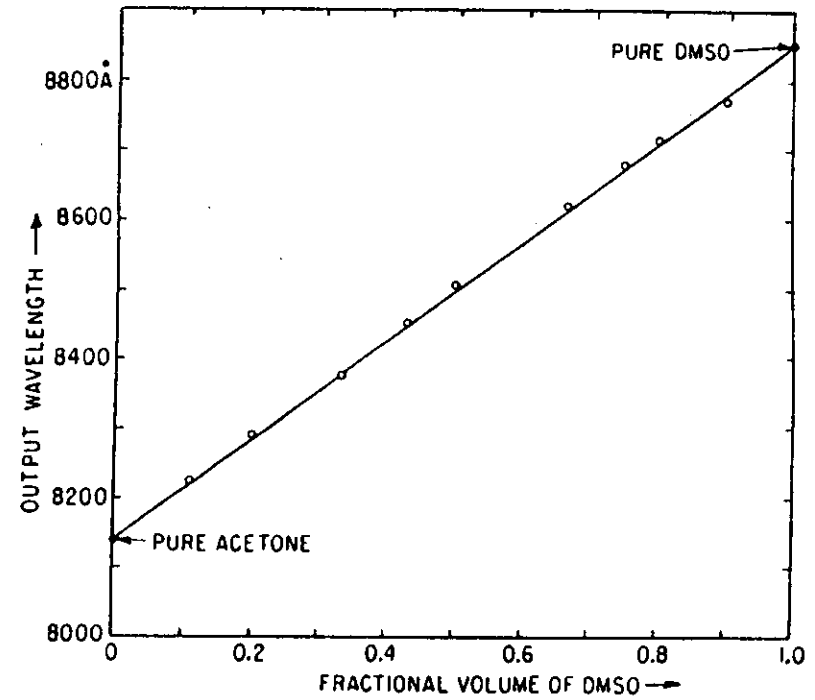
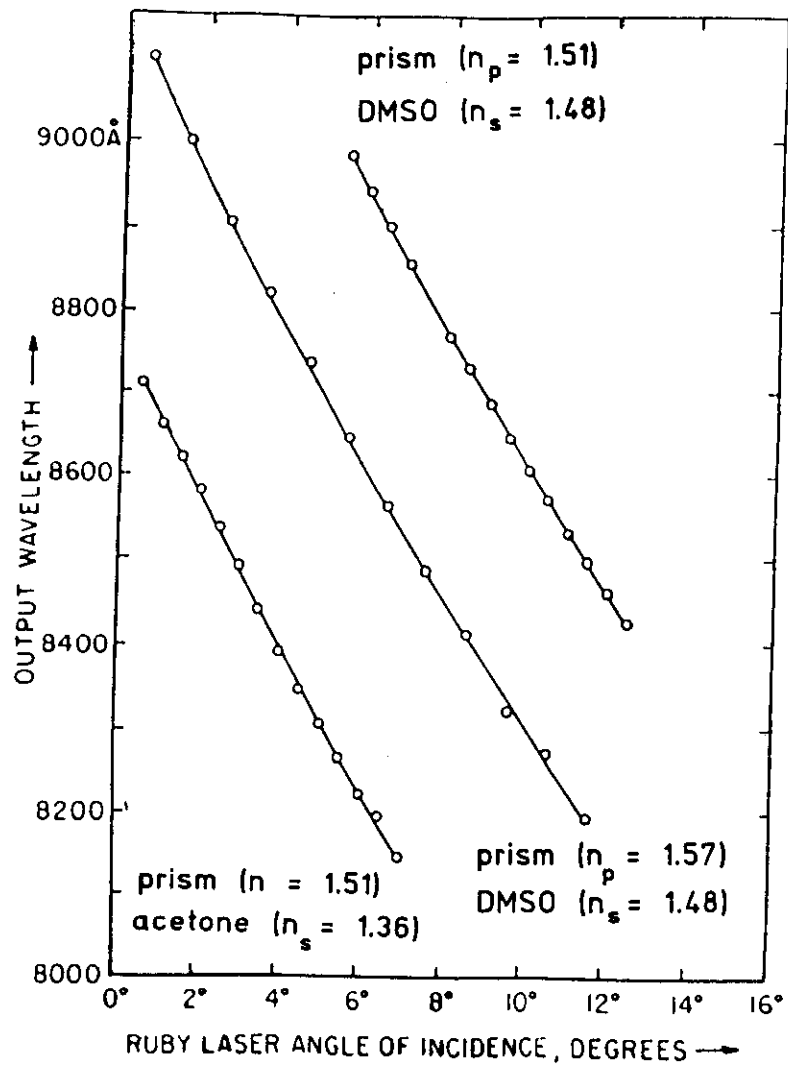
$$\lambda_L = \frac{n_s \lambda_p}{n_p \sin \left[ \frac{\pi}{4} + \arcsin \left( \frac{\sin i}{n_p} \right) \right]}$$

Chandra et al. (1972)



Chandra et al. (1972)

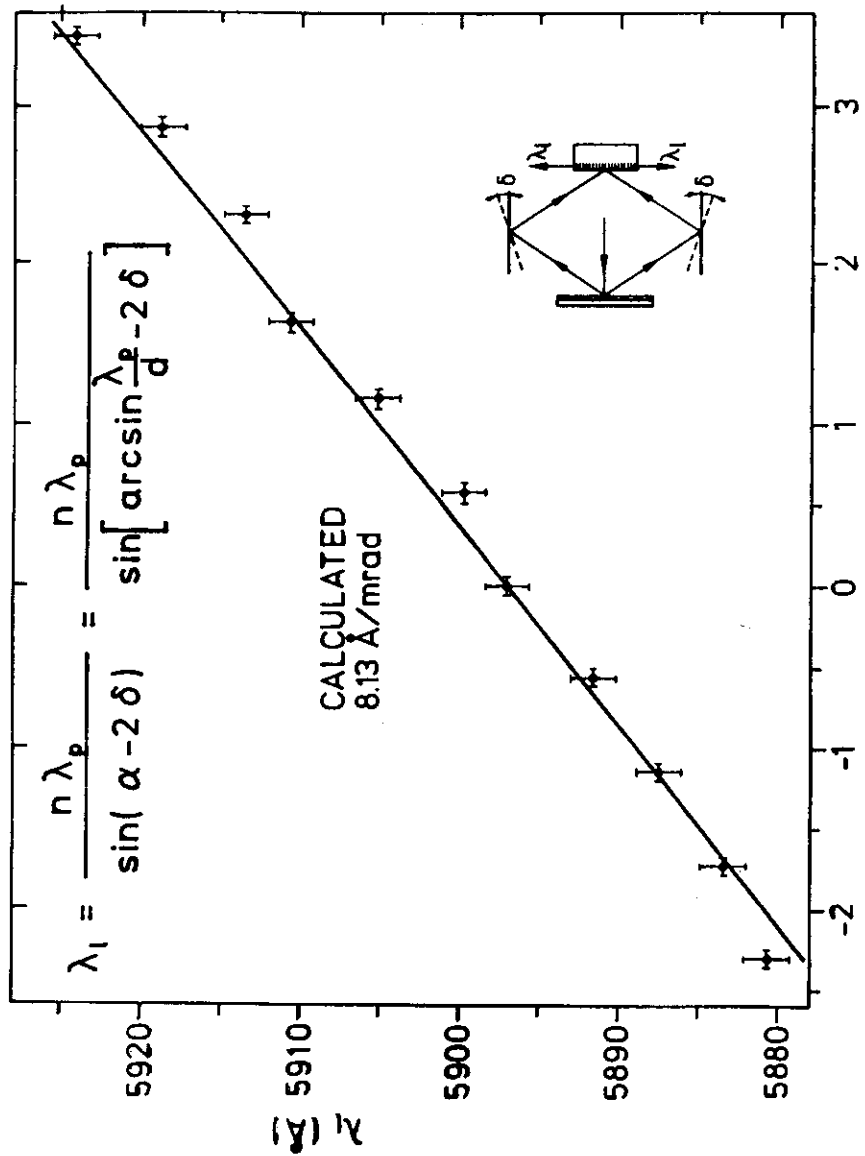
# Prism Dye Laser



Chandra et al. (1972)

Chandra et al. (1972)

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$\delta$  (mrad)  $\rightarrow$

75

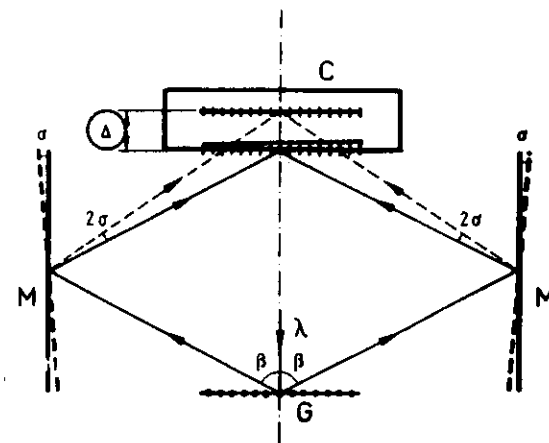


Fig. 4. Displacement of the coherence plane in the dye cuvette, if the mirrors (or prisms) are rotated.

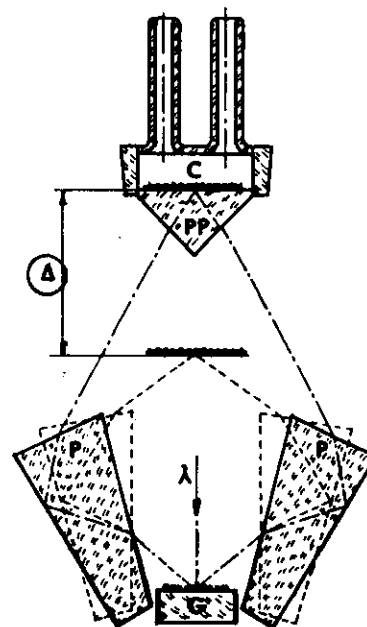
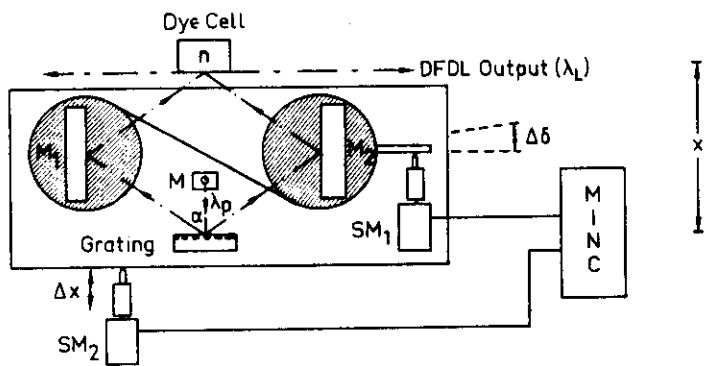


FIG. 2. Displacement of the coherence plane, if prisms P are rotated.

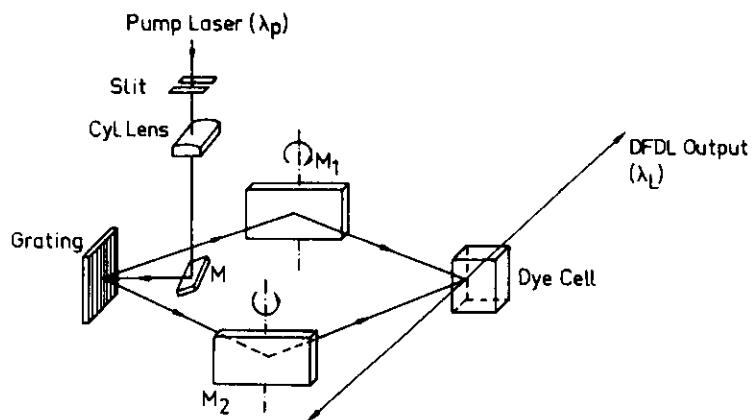
Computer Controlled Distributed Feedback Dye Laser



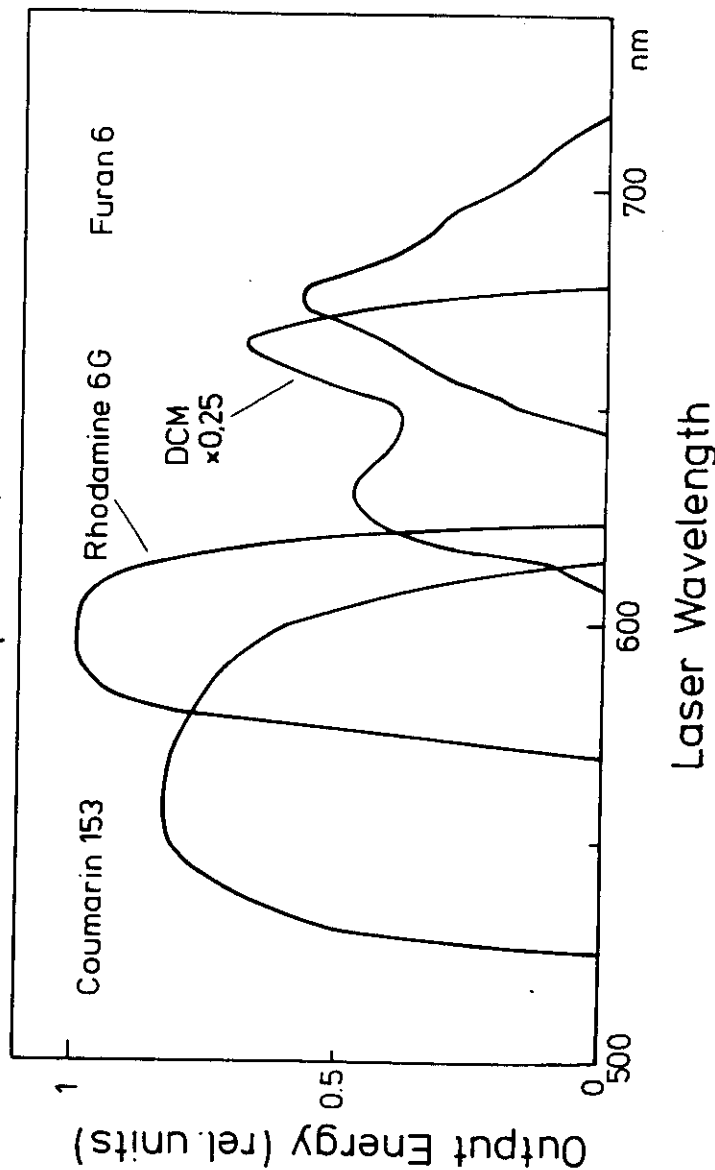
$$\Delta\delta = \frac{1}{2} [\alpha - \arcsin(n \frac{\lambda_p}{\lambda_L})]$$

$$\Delta x = \frac{x}{2} [\operatorname{tg} \alpha \cdot \operatorname{tg}(90 - \alpha + 2\Delta\delta) - 1]$$

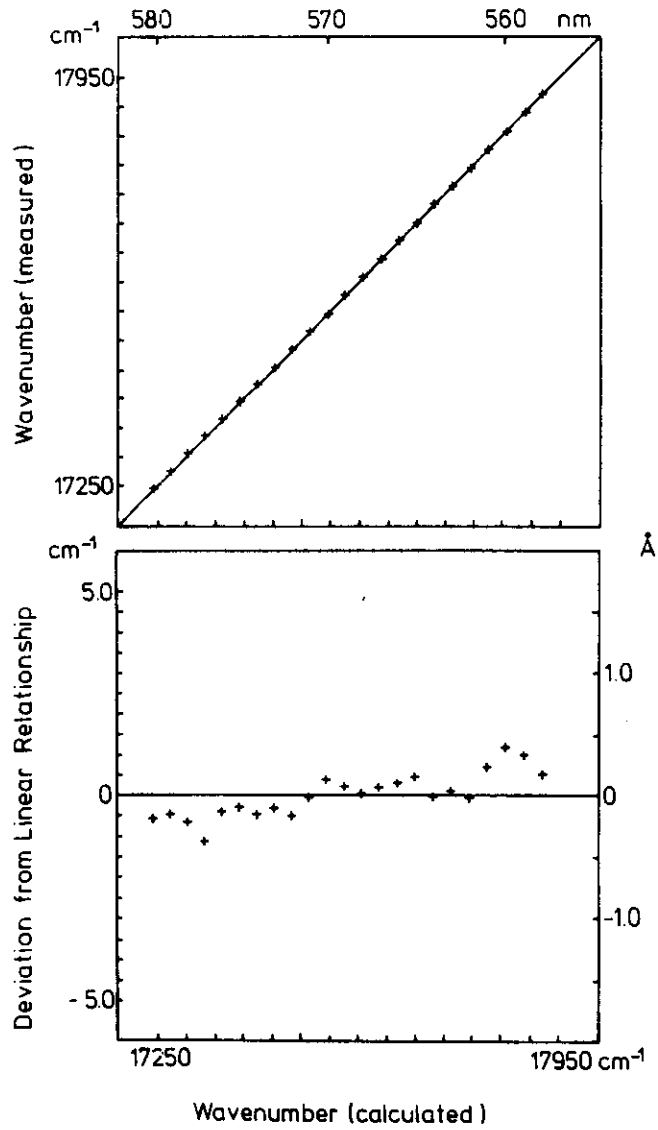
$$\alpha = \arcsin(\frac{\lambda_p}{d})$$



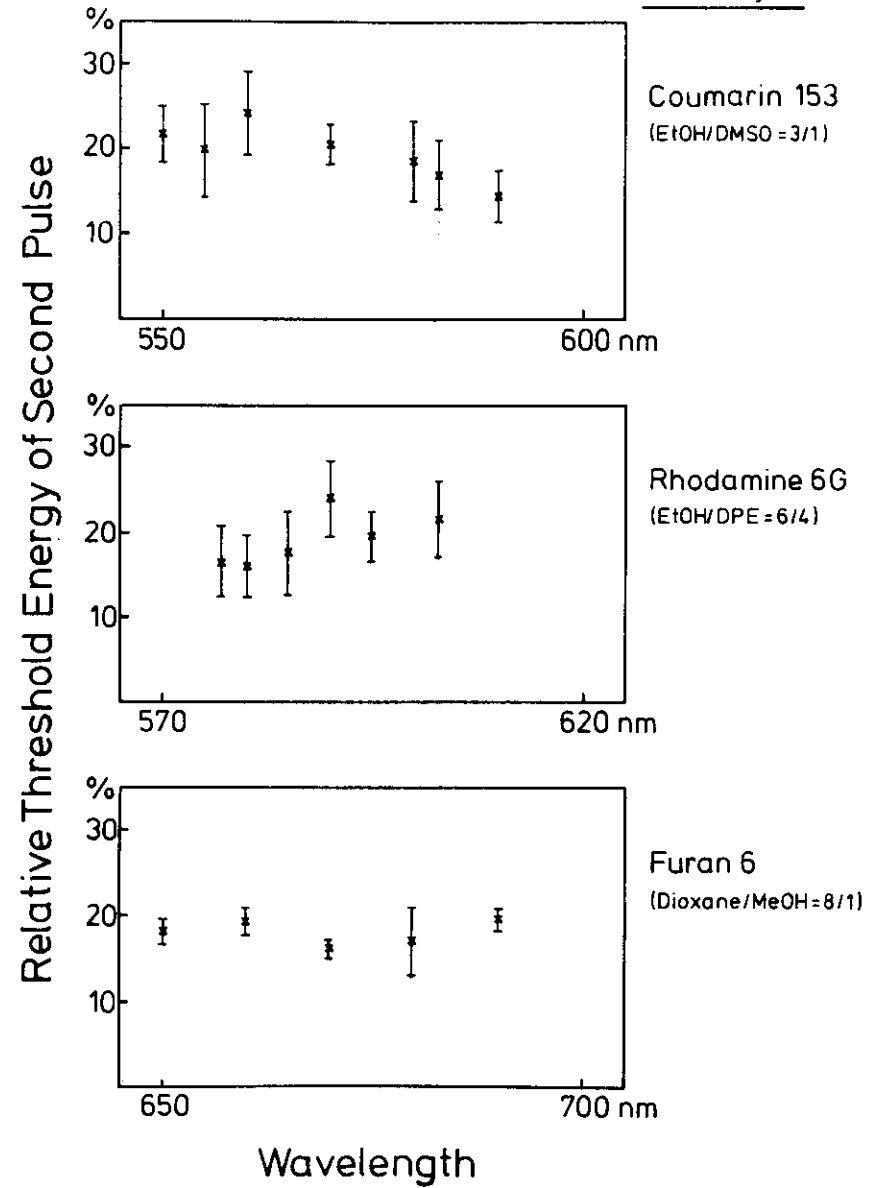
Tuning curves of computer controlled DFDL (Single picosecond pulses)



Computer Controlled DFDL  
Accuracy of tuning for Coumarin 153



Laser Dyes





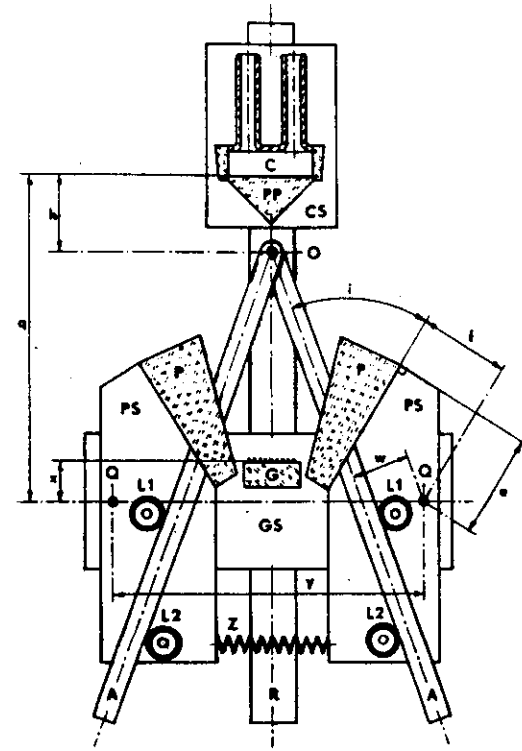
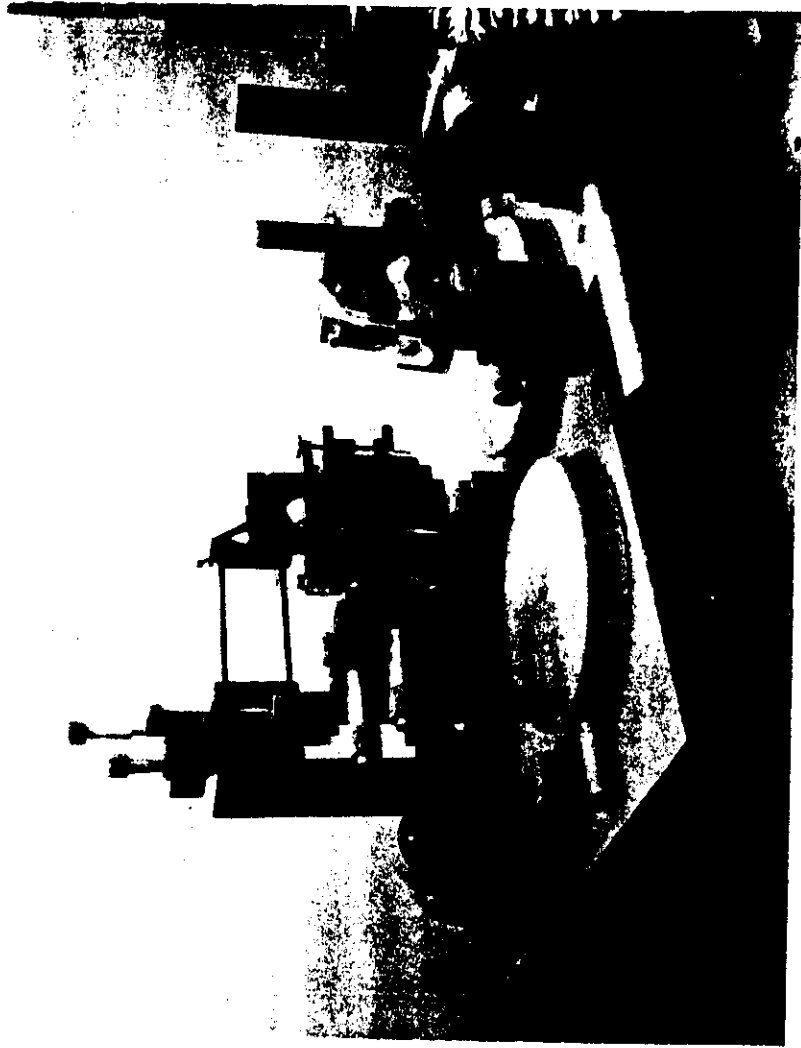


FIG. 3. Mechanical arrangement of the DFDL (see text). JASNY (1986)

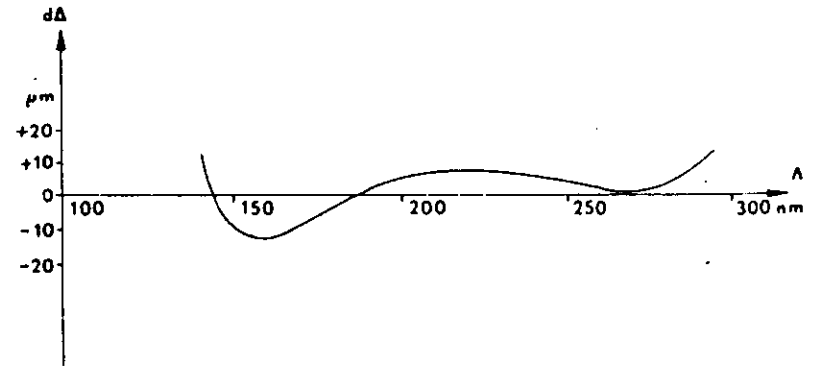
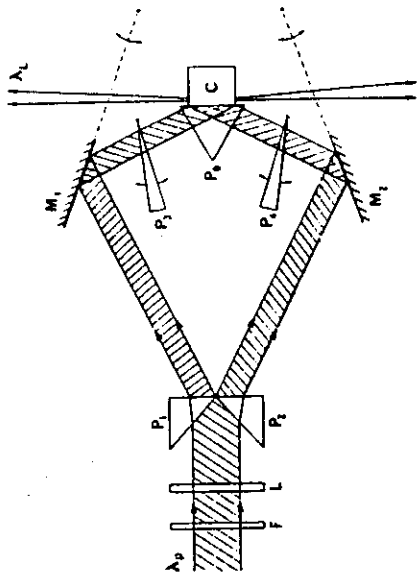
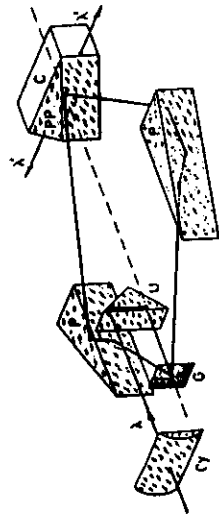


FIG. 4. Displacement error  $d\Delta$  (see text), as a function of fringe constant  $\Lambda$ .

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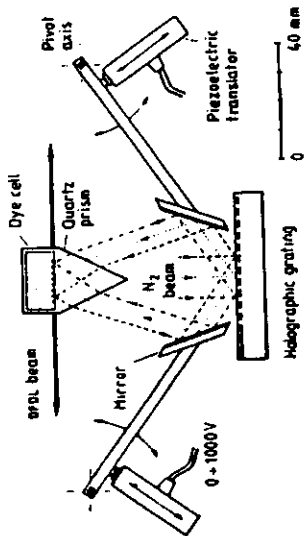
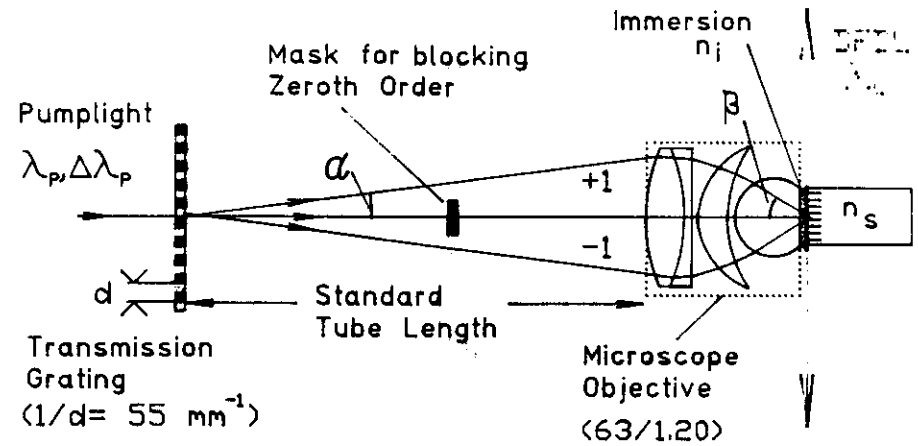


G.M.Gale, P.Ranson, M.Denariez-Roberge  
*Appl.Phys.* B44, 221 (1987)

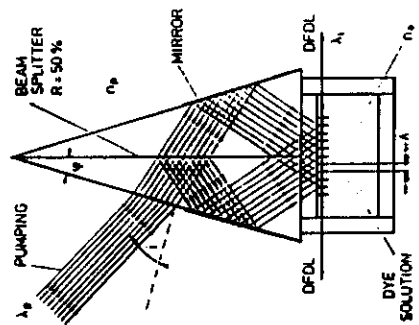


J.Jasny  
*Opt.Commun.* 53, 4 (1985)

# Microscope - DFDL



J.Hebling, Zs.Bor  
*J.Phys.E:Sci.Instr.* 17, 1077 (1984)



Zs.Bor, G.Szabo  
*Appl.Phys.* B (1988)

$$\Lambda = \frac{\lambda_p}{2(n_1 \sin \beta)} = \begin{cases} \frac{\lambda_p}{2 NA} \\ \frac{d \sin \alpha}{2 n_1 \sin \beta} \sim \text{independent on } \lambda_p \end{cases}$$

$$\lambda_L = 2 n_s \Lambda = \begin{cases} 1.3 \frac{n_s \lambda_p}{NA} = 390 \text{ nm (Min)} \\ n_s d \frac{\sin \alpha}{n_1 \sin \beta} \approx n_s \frac{d}{M} \end{cases}$$

Variable Magnification  $M \rightarrow \lambda_L$  - Tuning

Szatmari & Sch&fer (1988)

18

Selected Literature on DFBL wavelength  
tuning:

- (1) Zs. Bor, A. Müller : IEEE J. Quant. El.  
[QE-22], 1524 - 1533 (1986)  
Review paper
- (2) C.V. Shank et al. : Appl. Phys. Lett. [18], 395 (1971)
- (3) S. Chandra et al. : Appl. Phys. Lett. [21], 114 - 116 (1972)
- (4) Zs. Bor : Opt. Commun. [29], 103 - 108 (1979)
- (5) M.E. Lusty, M.H. Jung : Appl. Phys. [44B], 193 - 198  
(1987)
- (6) J. Hebling, Zs. Bor : J. Phys. E: Sci. Instr.  
[17], 1077 - 1080 (1984)
- (7) G.M. Gale et al. : Appl. Phys. [44B], 221 - 233 (1987)
- (8) J. Jesny : Rev. Sci. Instr. [57], 1303 - 1307 (1986)
- (9) S. Szetmari, F.P. Schäfer : Appl. Phys. [46B],  
305 - 311 (1988)

