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18 February - 8 March 1991

*Progress in Parametric Generation and  
 Amplification of Ultrashort Light Pulses*

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 Laser Research Center  
 Vilnius, Lithuania

# PROGRESS IN PARAMETRIC GENERATION AND AMPLIFICATION OF ULTRASHORT LIGHT PULSES

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## Key Points

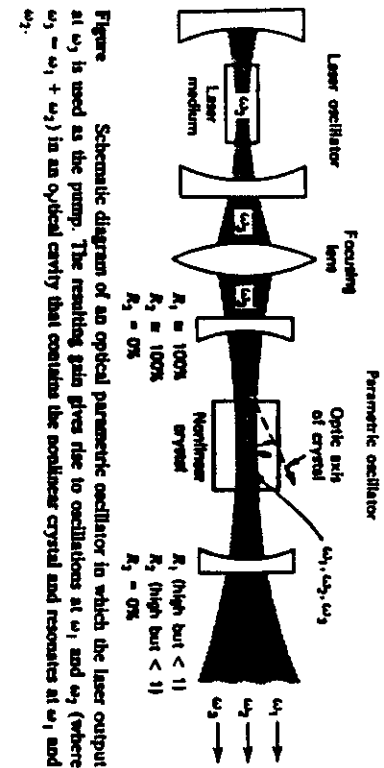
- Short Retrospective
- Main Trends in OPA & OPO Research
- Picosecond and Femto-second OPA & OPO
- Phase Conjugation
- Squeezing
- Four-Photon OPO
- New Pump Sources
- Applications

## First Papers on OPA

- ▲ Observation of Parametric Amplification in the Optical Range / Akhmanov S.A., Kovrigin A.I., Piskarskas A.S., Fadeev V.V., Khokhlov R.V. // JETP Lett. 1965 V.2, No.7, P. 191-193.
- ▲ Measurement of Parametric Gain Accompanying Optical Difference Frequency Generation / Wang C.C., Racette G.W. // Appl. Phys. Lett. 1965 V.6, No.8, P. 196-171.

## First Papers on OPO

- **Tunable Coherent Parametric Oscillation in LiNbO<sub>3</sub> at Optical Frequencies** / Giordmaine J.A., Miller R.C. // Phys. Rev. Lett. 1965 V.14, No.24, P. 973-976.
- **Tunable Parametric Light Generator with KDP Crystal** / Akhmanov S.A., Kovrigin A.I., Piskarskas A.S., Fadeev V.V., Khokhlov R.V. // JETP Lett. 1966 V.3, No.9, P. 241-245.



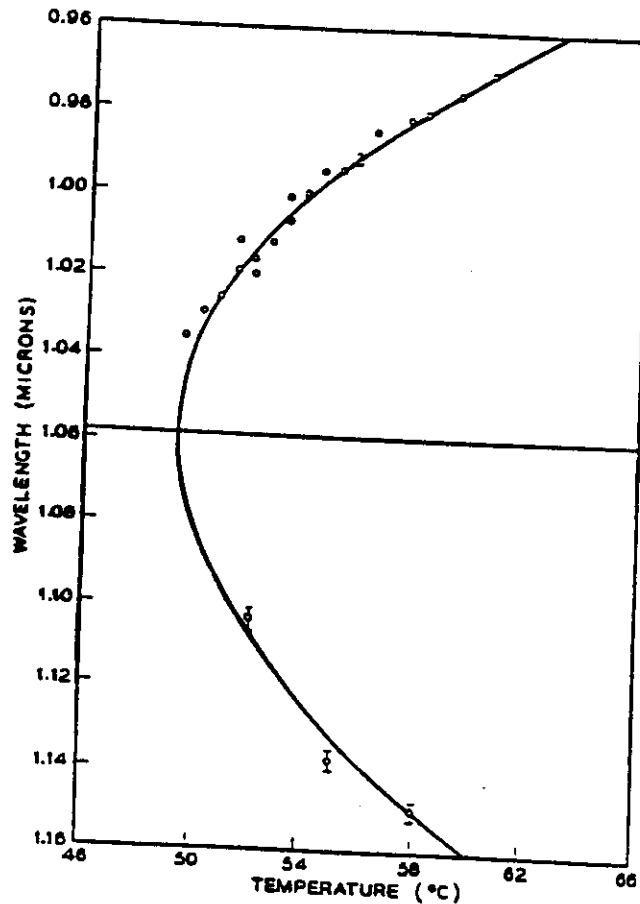


FIG. Signal and idler wavelength as a function of temperature  $T_2$  of the oscillator crystal

(by GIORDMINE J. E. & MILLER R. C.)

## PROBLEMS TO BE SOLVED

- EXTENSION OF TUNING RANGE
  - HIGH TRANSPARENT CRYSTALS THROUGH VISIBLE, UV & IR
  - UV PUMP SOURCES
- PULSE WIDTH REDUCTION
  - F<sub>2</sub> PUMP SOURCES
  - NEW APPROACH TO FAST PHASE CONTROL
- NARROW LINE OPO. BANDWIDTH LIMITED PULSES
  - PUMP OF HIGH TIME & SPACE COHER.
  - FILTERING
  - CAVITY STABILIZATION
- HIGH ENERGY OPO
  - TRAVELING WAVE OR NONCOLINEAR
  - CRYSTALS OF LARGE APERTURE
- THRESHOLD REDUCTION
  - NEW MATERIALS OF HIGH  $\chi^{(2)}$
  - HIGH QUALITY CAVITIES (MONOLIT)
  - CONFOCAL FOCUSING
- SQUEEZING (IN PROGRESS)

## EQUATIONS FOR 3-WAVE PARAMETRIC INTERACTION

$$\frac{\partial A_1}{\partial z} + v_1 \frac{\partial A_1}{\partial t} - \frac{i}{2} g_1 \frac{\partial^2 A_1}{\partial t^2} + \beta_1 \frac{\partial A_1}{\partial x} + \frac{i}{2k_1} \left( \frac{\partial^2 A_1}{\partial x^2} + \frac{\partial^2 A_1}{\partial y^2} \right) =$$

$$= -\delta_1 A_1 + \sigma_1 A_3 A_2^* \exp(-i\Delta_z z),$$

$$\frac{\partial A_2}{\partial z} + v_2 \frac{\partial A_2}{\partial t} - \frac{i}{2} g_2 \frac{\partial^2 A_2}{\partial t^2} + \beta_2 \frac{\partial A_2}{\partial x} + \frac{i}{2k_2} \left( \frac{\partial^2 A_2}{\partial x^2} + \frac{\partial^2 A_2}{\partial y^2} \right) =$$

$$= -\delta_2 A_2 + \sigma_2 A_3 A_1^* \exp(-i\Delta_z z),$$

$$\frac{\partial A_3}{\partial z} + v_3 \frac{\partial A_3}{\partial t} - \frac{i}{2} g_3 \frac{\partial^2 A_3}{\partial t^2} + \beta_3 \frac{\partial A_3}{\partial x} + \frac{i}{2k_3} \left( \frac{\partial^2 A_3}{\partial x^2} + \frac{\partial^2 A_3}{\partial y^2} \right) =$$

$$= -\delta_3 A_3 + \sigma_3 A_1 A_2 \exp(i\Delta_z z),$$

$$\frac{\partial A_1}{\partial z} + v_1 \frac{\partial A_1}{\partial t} - i \frac{g_1}{2} \frac{\partial^2 A_1}{\partial t^2} = -\delta_1 A_1 + \sigma_1 A_3 A_2^* \exp(-i\Delta_z z),$$

$$\frac{\partial A_2}{\partial z} + v_2 \frac{\partial A_2}{\partial t} - i \frac{g_2}{2} \frac{\partial^2 A_2}{\partial t^2} = -\delta_2 A_2 + \sigma_2 A_3 A_1^* \exp(-i\Delta_z z),$$

$$\frac{\partial A_3}{\partial z} + v_3 \frac{\partial A_3}{\partial t} - i \frac{g_3}{2} \frac{\partial^2 A_3}{\partial t^2} = -\delta_3 A_3 + \sigma_3 A_1 A_2 \exp(i\Delta_z z).$$



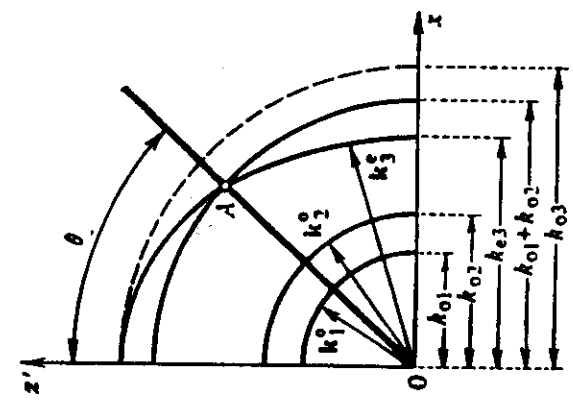
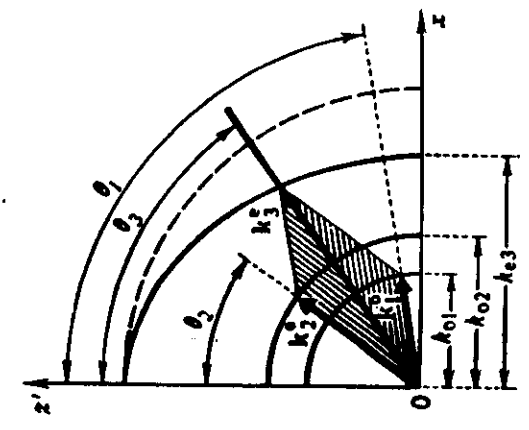
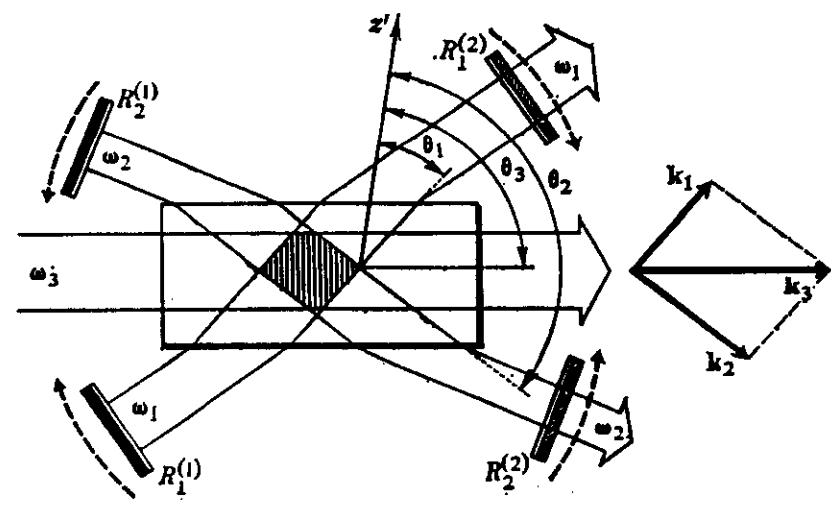
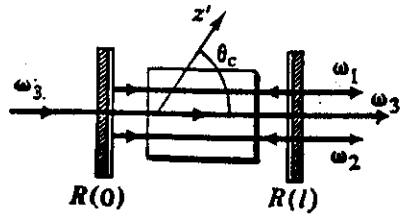
$$\omega_1 + \omega_2 = \omega_3$$

$$A_1 = A_{10} \cosh m + \sqrt{\frac{\tilde{g}_1}{\tilde{g}_2}} A_{20}^* \sinh m$$

$$A_2 = A_{20} \cosh m + \sqrt{\frac{\tilde{g}_2}{\tilde{g}_1}} A_{10}^* \sinh m$$

$$m = \sqrt{\tilde{g}_1 \tilde{g}_2} A_{30} Z$$

$$m \gg 1, A_2 = \sqrt{\frac{\tilde{g}_2}{\tilde{g}_1}} A_1^* \Rightarrow \text{phase conjugation}$$



(from R.L. BYER et al.)

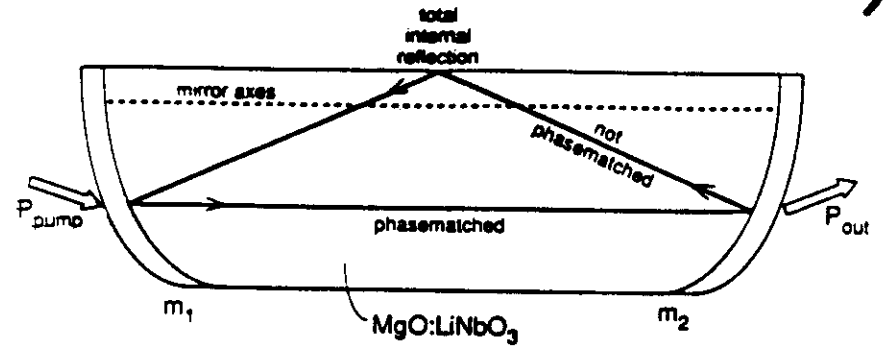


FIGURE 3.1(a). Monolithic DRO crystal cavity design. Dielectric mirrors that are highly reflective for the signal and idler and transmit the pump are deposited directly on the curved ends of the MgO:LiNbO<sub>3</sub> resonator. m1: HR 1064 nm, T = 85% 532 nm. m2: T = 0.5% 1064 nm.

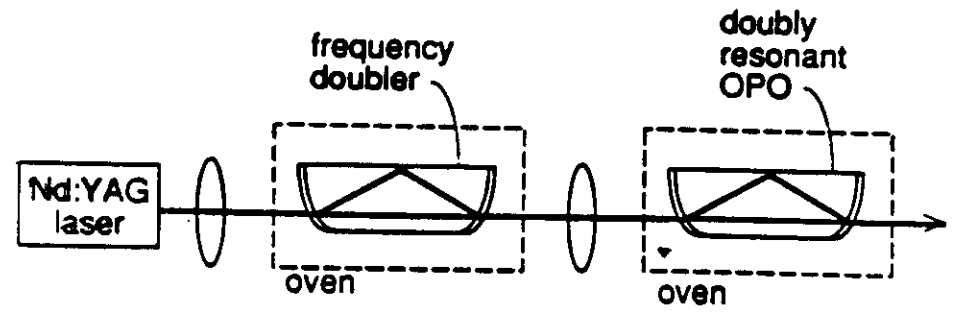
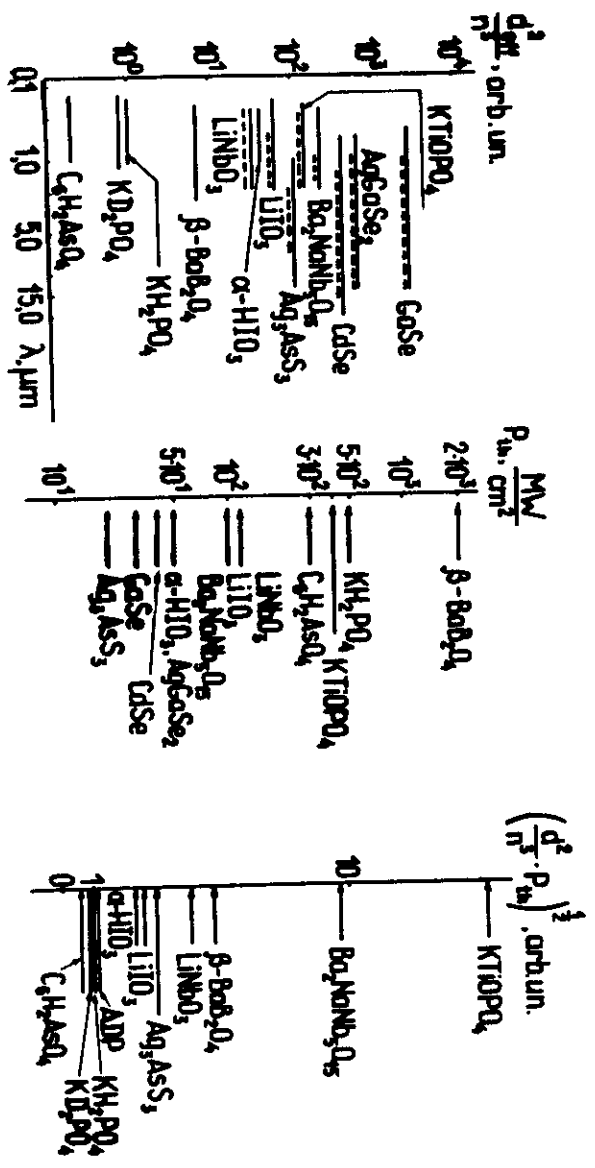


FIGURE 3.1(b). Experimental setup for the OPO showing the diode-laser-pumped Nd:YAG laser, external resonant doubler, and doubly-resonant OPO.

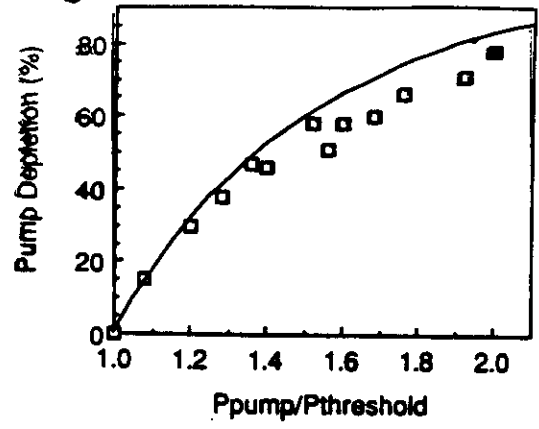
$R = 10 \text{ mm}$       $\phi = 27 \mu\text{m} (1.06 \mu\text{m})$   
 $l = 12,5 \text{ mm}$       $T_s = 0.5\%$

Nonlinear Crystals for SHG and OPO

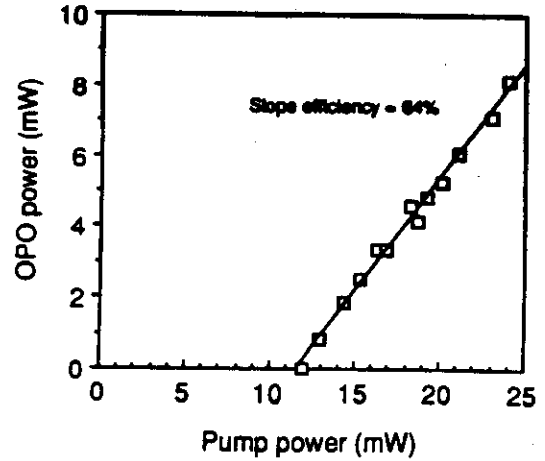


(By R.L. BYER et. al.)

$P_t = 3.2 \text{ m}$



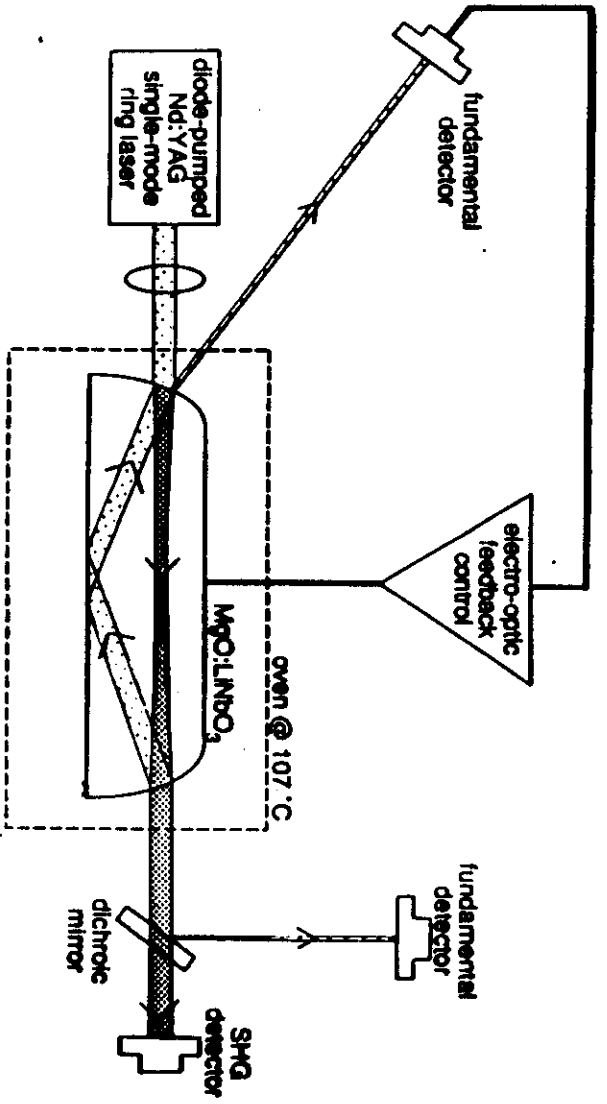
Pump depletion of the cw DRO vs. number of times above threshold (pump power divided by threshold power). The solid line is the plane-wave theory after Bjorkholm (Ref. 5).



OPO threshold and 'slope efficiency' which, surprisingly, is rather linear.

$$\left. \begin{aligned} P_{s+i} &= 8.15 \text{ mW} \\ P_p &= 24 \text{ mW} \end{aligned} \right\} \eta = 54\%$$

$$\eta_{\omega \rightarrow \omega_2} = 14.2\%, \quad \eta_{oc} = 46\% \text{ from } \theta$$



Resonant second harmonic generation from the diode-laser-pumped Nd:YAG laser. [Reproduced from Ref. 9] (BYER R. L. et al.)

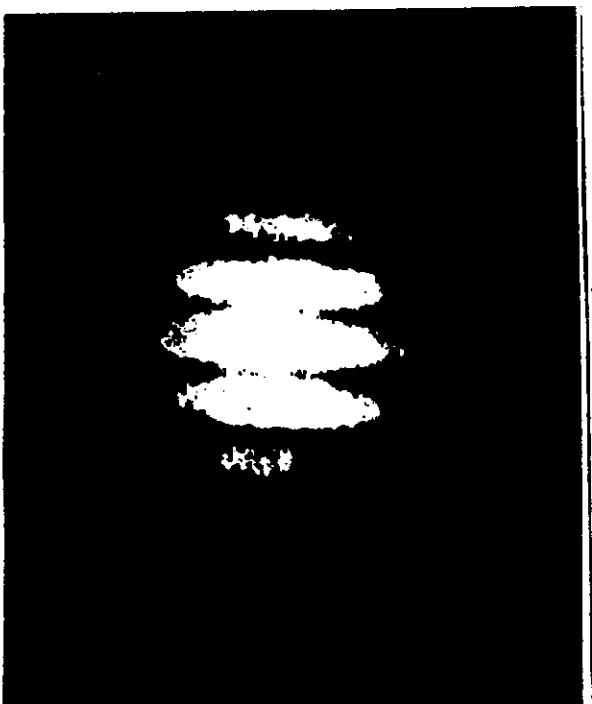
$$l = 12.5 \text{ mm}$$

$$P_{i,064} = 53 \text{ mW}$$

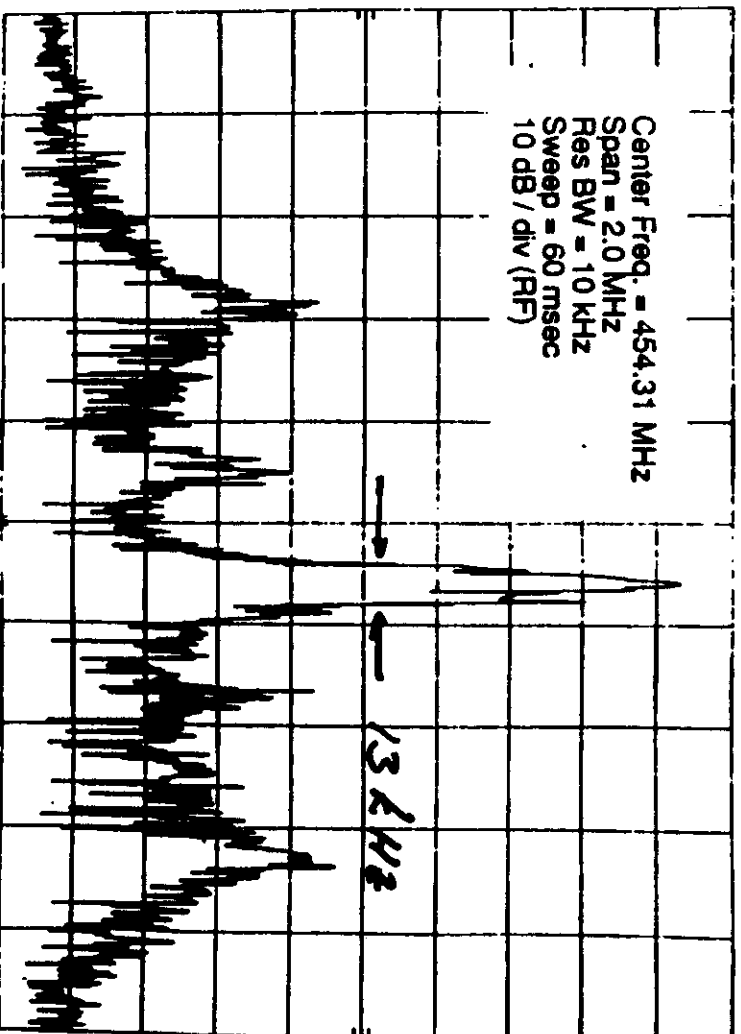
$$P_{0,53} = 30 \text{ mW} \quad \left. \right\} \eta = 56\%$$

∞



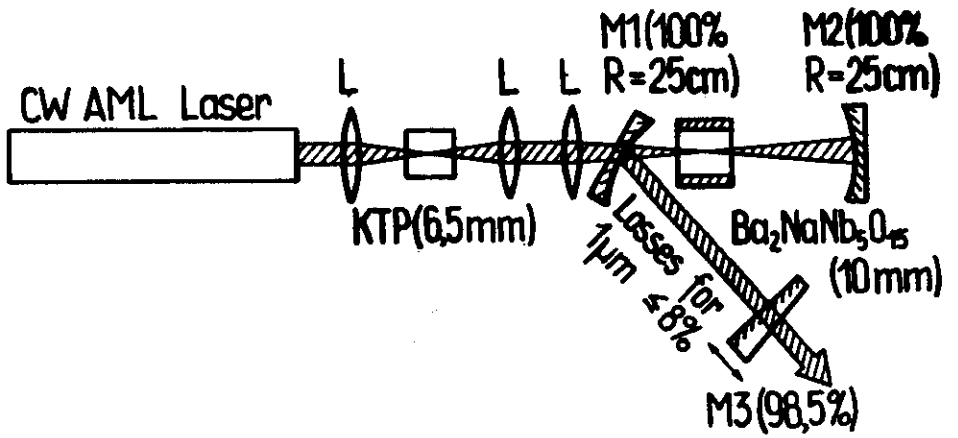


Stable fringe pattern produced by interfering the degenerate DRO beam with a reference beam from the Nd:YAG laser.  
(from R. ECKARD et. al.)



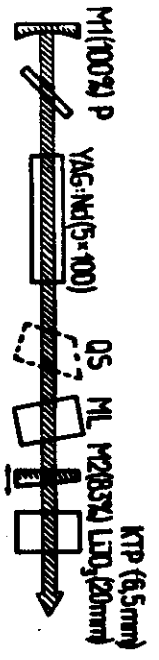
Heterodyne RF beam spectrum of the independent DRO signal and Nd:GGG laser oscillators. The 3 dB full width of the central peak is 13 KHz. (from R. ECKARD et. al.)

# CW ps OPO Setup



$P_{th,av}$ mW	$P_{th,p}$ W	$\epsilon, ps$	Tuning range, $\mu m$	$P_{av}, mW$	$P_p, W$
28	4	$\leq 37$	0,95-1,2*	55	10

## Parameters of ps CW-pumped YAG:Nd Laser



AML ( $f_{mod} = 139 MHz$ )	$\lambda = 1,064 \mu m$				$\lambda = 0,532 \mu m$				$\lambda = 0,3547 \mu m$		
	$\epsilon, ps$	$P_p, W$ ( $E_p, mJ$ )	$P_p, kW$	N	$\epsilon, ps$	$P_p, W$ ( $E_p, mJ$ )	$P_p, kW$	N	$\epsilon, \%$	$P_p, W$ ( $f_{mod} = 139 MHz$ )	$P_p, kW$
AML and QS ( $f_{mod} = 4 kHz$ )	65	(1,8)	900	30	50	(0,5) (1:30 $\mu s$ )	400	25	20 (KDP)	0,360	280
	55	8,5	1,1	$\infty$	40	1(KTP)	0,18	$\infty$	-	-	-

# CW ps OPO: Energy Conversion; Cavity Detuning

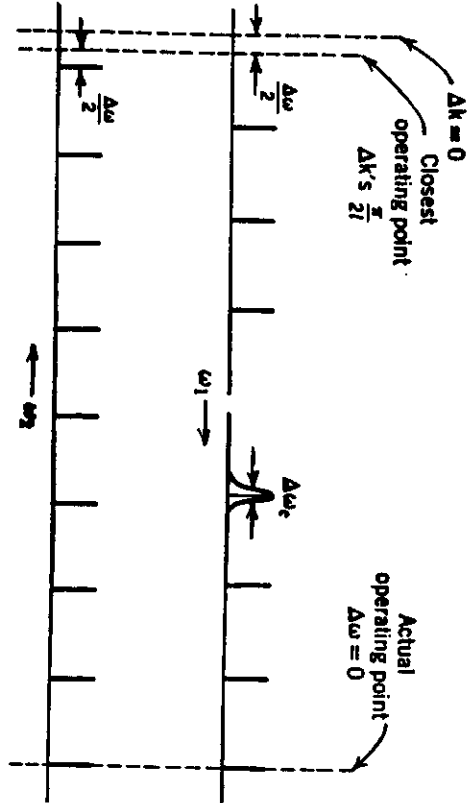
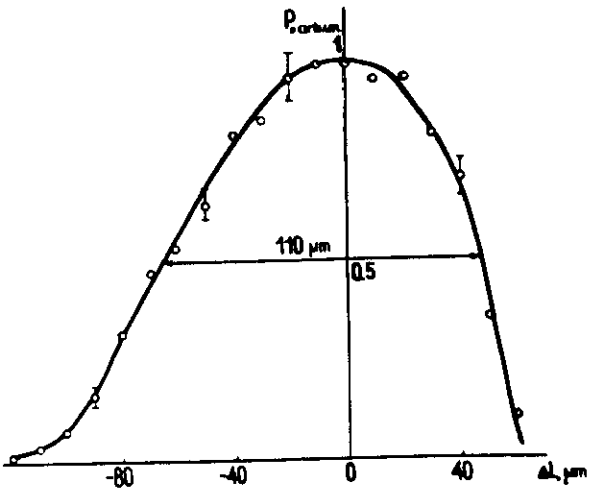
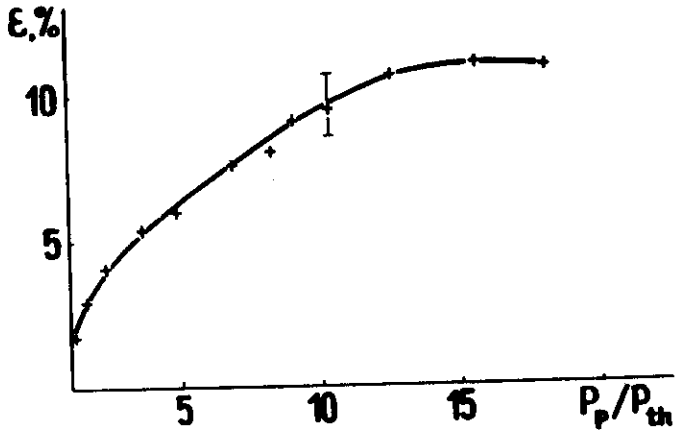
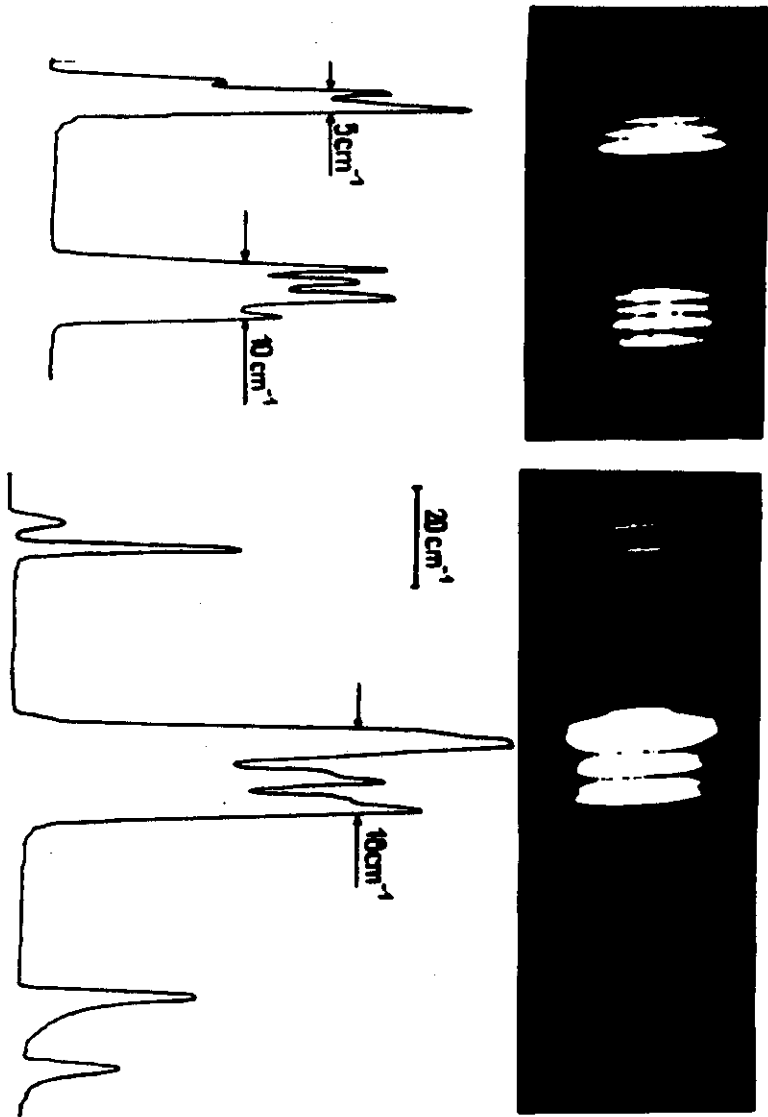


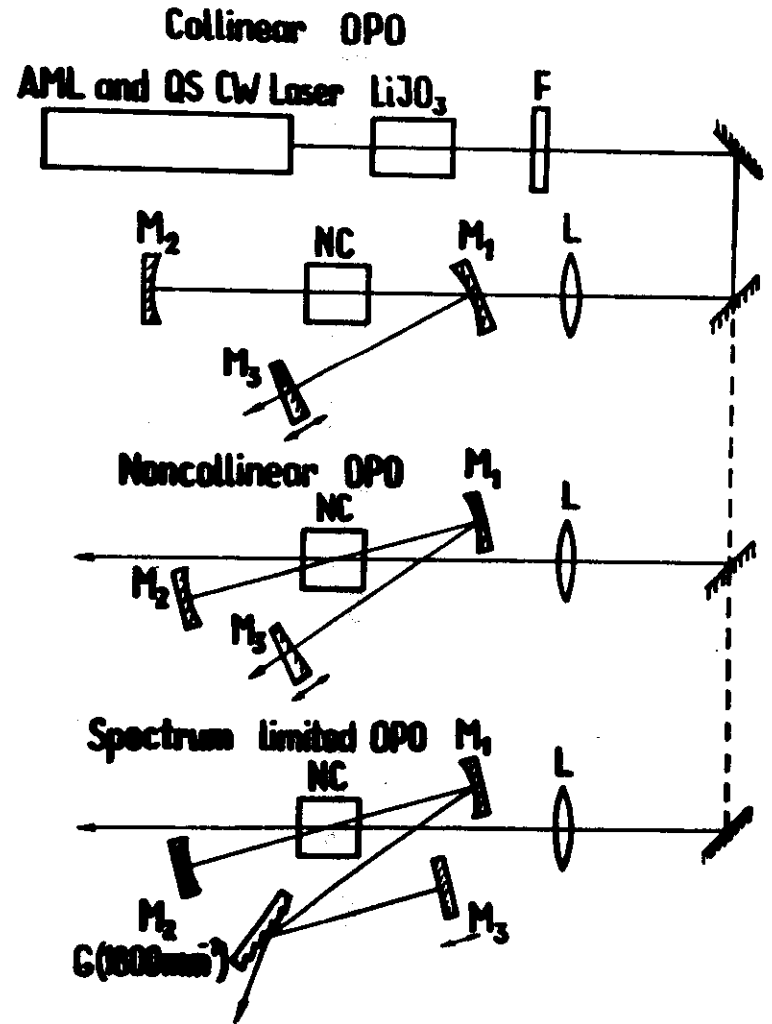
Figure Modes in the resonator of a doubly resonant oscillator. Note that  $\omega_1$  increases to the right and  $\omega_2$  to the left. Lines vertically above each other indicate the coincidence of idler and signal modes. To the left is the point where  $\omega_1$  and  $\omega_2$  are phase matched. The closer operating point is the dotted line next to it, but the gain is higher at the point furthest to the right and this is the actual operating point. After Giordmaine and Miller, in *Physics of Quantum Electronics*, P. L. Kelley et al., Eds., McGraw-Hill, New York, 1966, p. 31.

$\lambda = 1.01 \mu\text{m}$

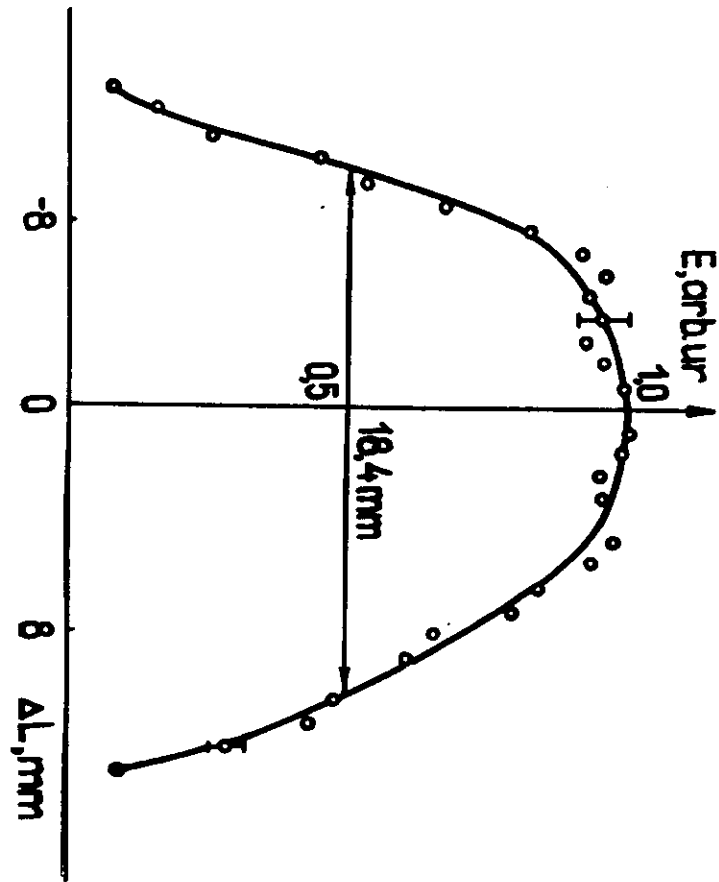
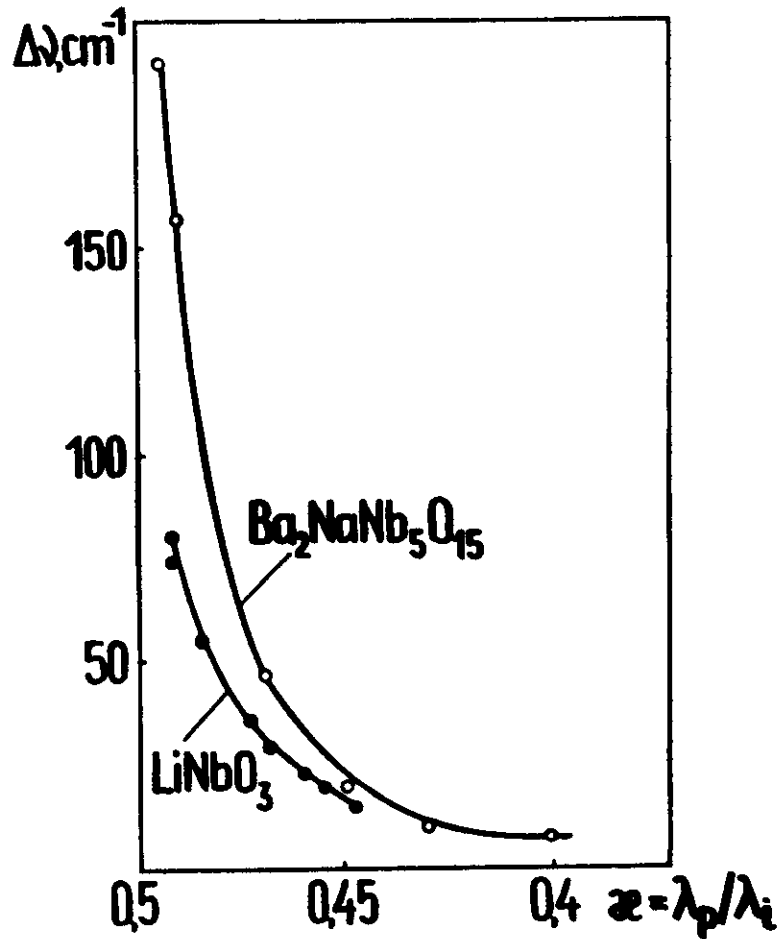
$\lambda = 1.04 \mu\text{m}$



### H.r.r. ps OPO Setup

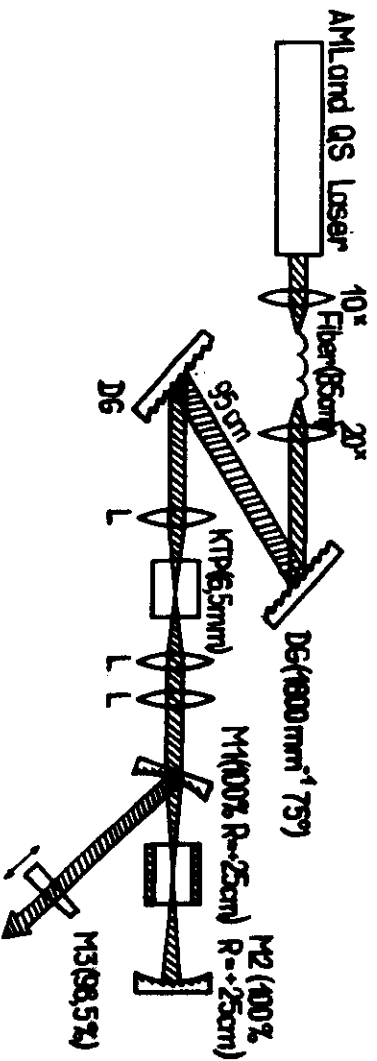


# OPO Spectrum Width Dependence on the Degeneracy Parameter



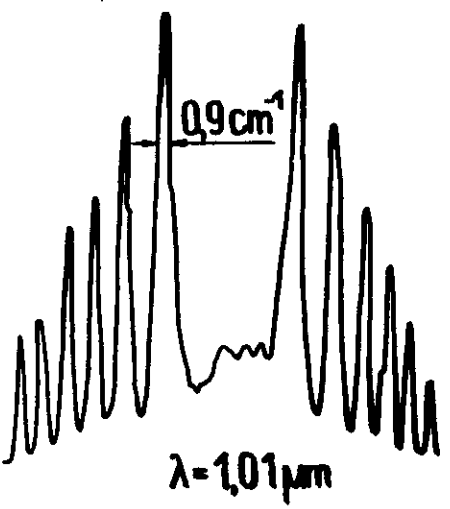
Cavity Detuning of Bandwidth Limited ps OPO

# Ps OPO Pumped by TCP of AML and QS CW YAG:Nd Laser

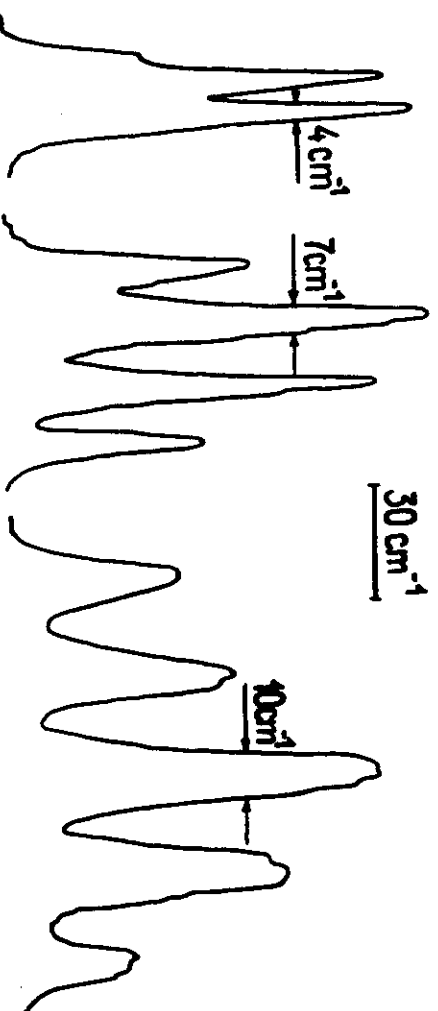


	$P_{th}, kW$	$\epsilon, \%$	$\tau, ps$	$P_p, kW$	$\lambda, \mu m$
After compression	—	—	6	130	1.064
SH after compressor	—	7	4.5	46	0.532
$Ba_2NaNb_5O_{15}$ OPO	1.1 (0.15 mW) ( $\tau=1kHz$ )	13	3.5	3	0.95 - 1.2

Bandwidth Limited ps OPO Spectrum



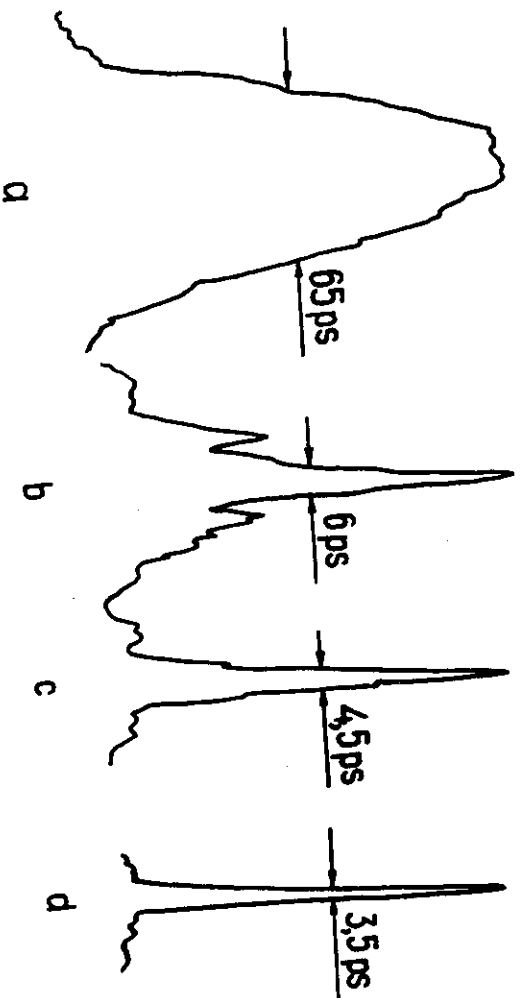
Ps OP0 Pumped by TCP. Spectrum



$\lambda = 0.96 \mu\text{m}$      $\lambda = 1.005 \mu\text{m}$

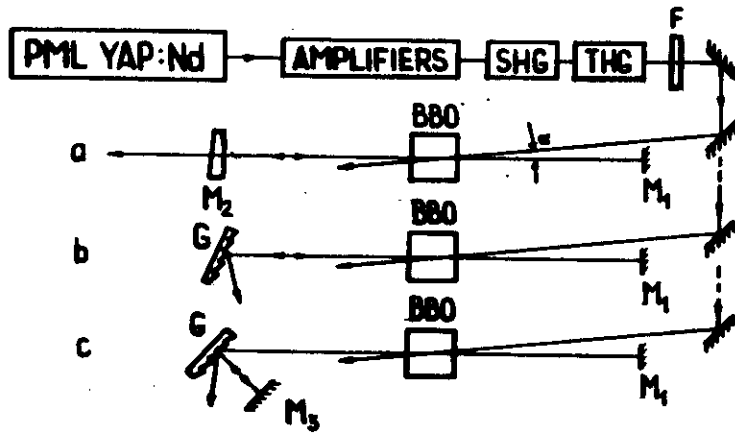
$\lambda = 1.022 \mu\text{m}$

Ps OP0 Pumped by TCP



Pulses emitted by the pump laser (a), pulse after compression (b), second harmonic pulse (c) and OP0 pulse (d)

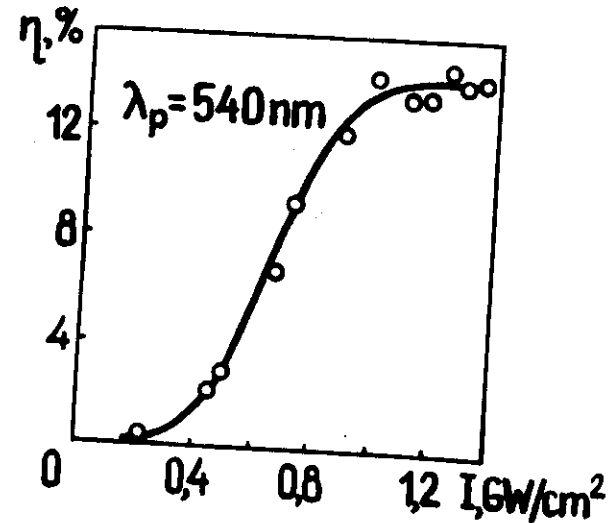
## β-BaB<sub>2</sub>O<sub>4</sub> ps OPO Experimental Setup



Pump parameters

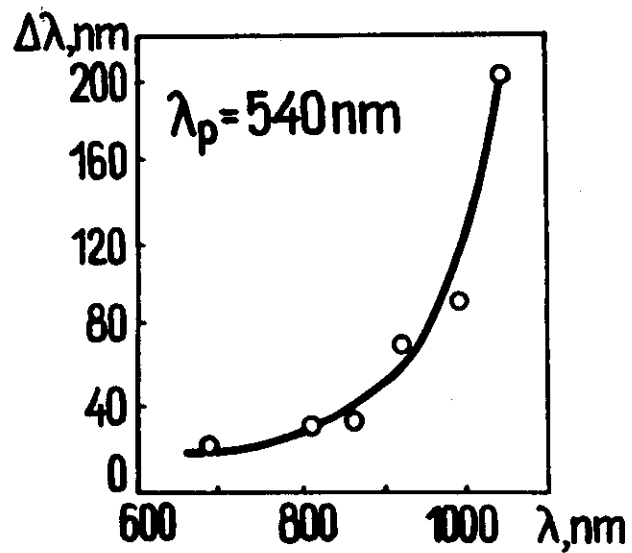
	$\lambda, \text{nm}$	$E_T, \text{mJ}$	$\tau, \text{ps}$	$\Delta\nu \cdot \tau$
Laser	1079	7	-	-
Amplifiers	1079	50	-	-
SH	540	20	25	4,3
TH	360	8	25	6,5

## β-BaB<sub>2</sub>O<sub>4</sub> ps OPO. Energy Conversion Versus Pump Intensity

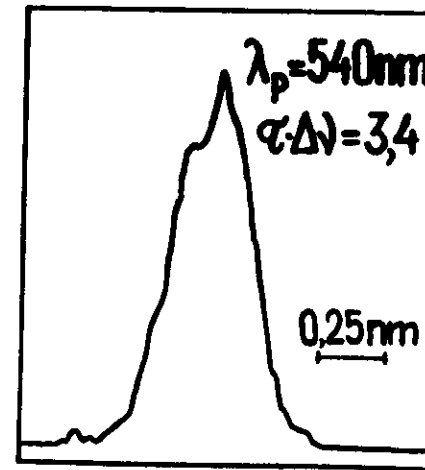




$\beta$ -BaB<sub>2</sub>O<sub>4</sub> ps OPO.  
Spectrum bandwidth

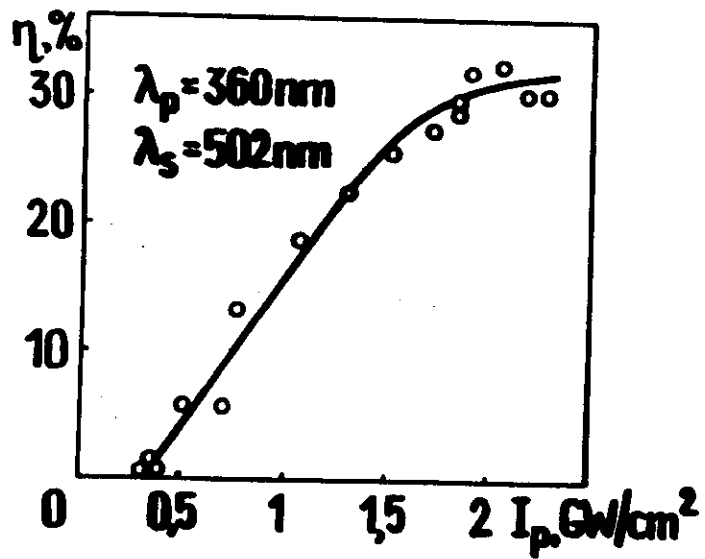


$\beta$ -BaB<sub>2</sub>O<sub>4</sub> ps OPO.  
Spectrum Bandwidth

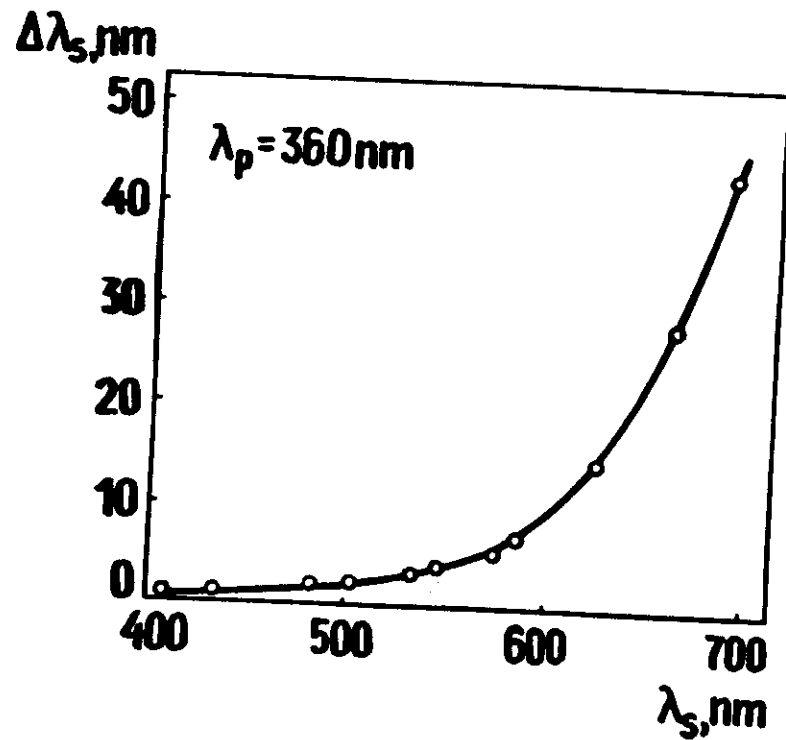


$\eta = 1,5\%$

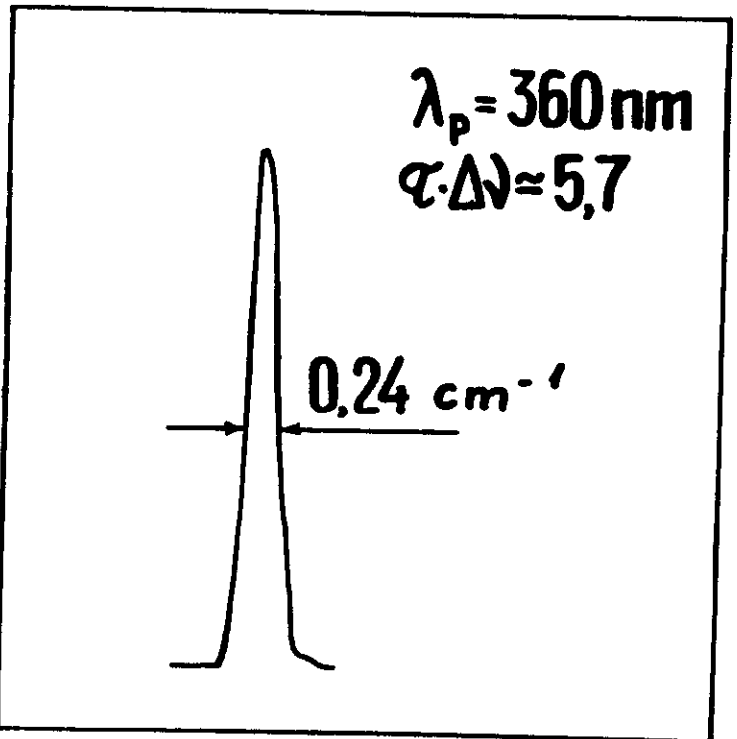
$\beta$ -BaB<sub>2</sub>O<sub>4</sub> ps OPO. Conversion Efficiency Versus Pump Intensity



$\beta$ -BaB<sub>2</sub>O<sub>4</sub> ps OPO. Spectrum Bandwidth



$\beta$ -BaB<sub>2</sub>O<sub>4</sub> ps OPO.  
Spectrum Bandwidth

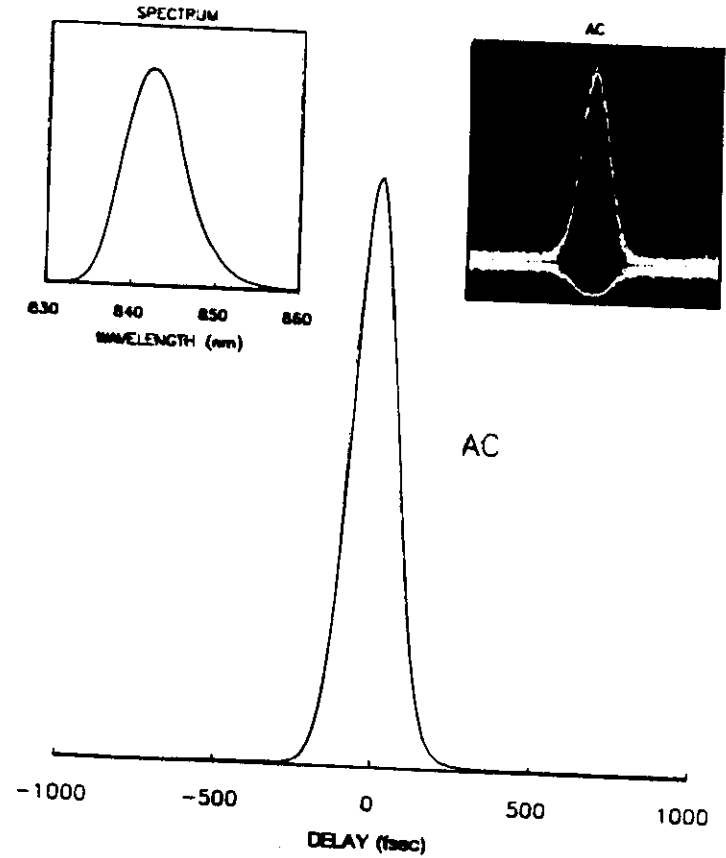
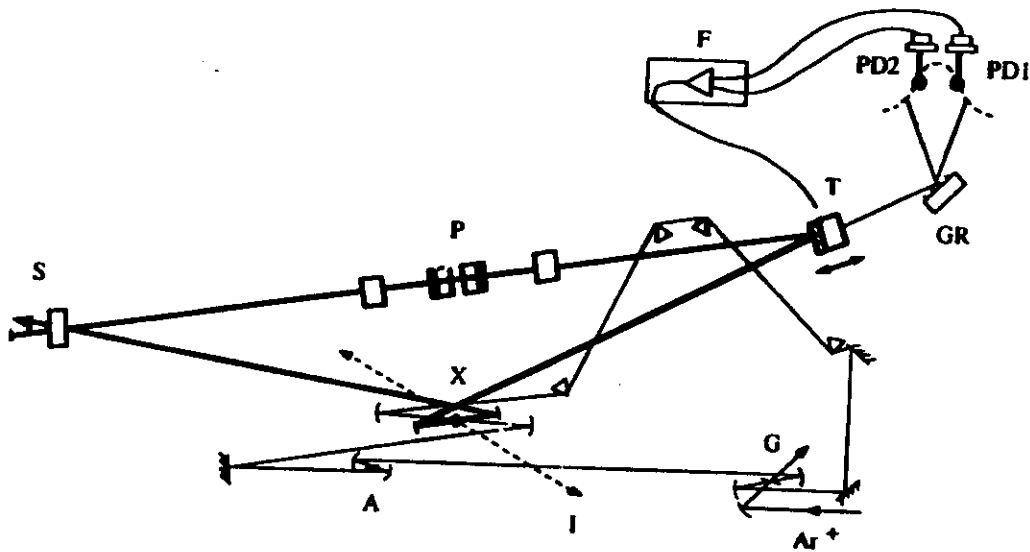


### OPO Parameters

Crystal	Length mm	$P_{th}$ kW	$\epsilon_{\text{max}}$ %	$\tau$ , ps	$P_{th}$ mW	$P_{th}$ kW	$\Delta\lambda$ $\text{cm}^{-1}$	Tuning range $\mu\text{m}$
LiNbO <sub>3</sub>	25	21	17.5	15-45	26	29	6-100	0.85-1.4
Ba <sub>2</sub> NbNb <sub>5</sub> O <sub>15</sub>	10	7	21	7-45	40	44	4-200	0.672-2.56
KTP	6.5	12	17	~40	25	27	10-30	0.95-1.2
Ba <sub>2</sub> NbNb <sub>5</sub> O <sub>15</sub> with selective resonator	10	28	8.1	12-45	29	32	$\leq 0.9$	0.672-2.56
BBO O <sub>2</sub> -0.355 $\mu\text{m}$	11.8	80	2.2	13-30	5.2	13	10-100	0.59-0.89

Configuration of the cw femtosecond OPO.

(TANG C.L. et al.)



AC of signal pulses at 840 nm for near-zero net cavity GVD; the insets show an interferometric AC envelope (right) and spectrum (left). The pulse width (a sech<sup>2</sup> fit) is 105 fsec. The time-bandwidth product of  $\Delta\nu\Delta\tau \approx 0.35$  and the symmetric spectrum are indicative of transform-limited pulses.

# INTRACAVITY fs KTiOPO<sub>4</sub> OPO

(by C.L. TANG et. al. CORNELL U.)

PUMP: CPM dye Laser

$$\tau_p = 350 \text{ ps}$$

$$P_p = 20 \text{ mW}$$

$$S_p = 1 \div 10 \text{ GW/cm}^2$$

$$P.M.M. = 10^8 \text{ Hz}$$

OPO: KTP (1.4 mm, o → e + o)

$$\alpha \leq 3\% (600 \div 900 \text{ nm})$$

$$P_s = 2 \text{ mW} \times 2$$

$$\tau_s = 220 \text{ fs} (820 - 920 \text{ nm})$$

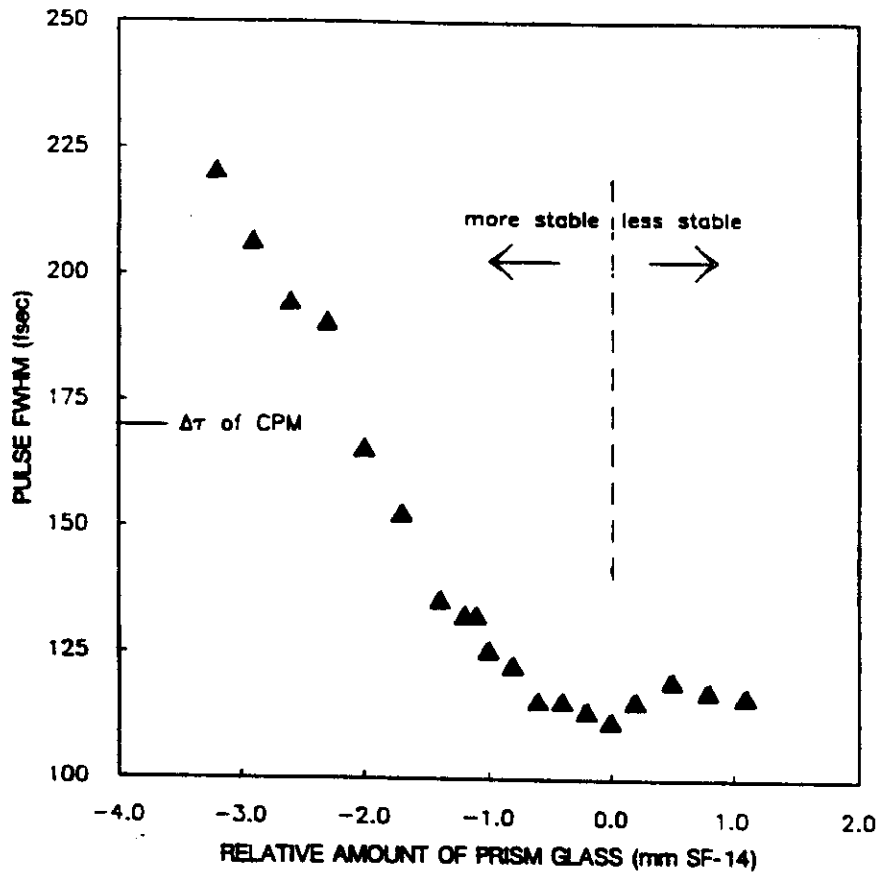
$$\tau_s = 105 \text{ fs} (840 \text{ nm, disp. comp})$$

$$\Delta\nu \cdot \Delta\tau \simeq 0,35 \rightarrow \text{sech}^2$$

FORECAST:

TUNIBILITY: 720 ÷ 4500 nm

$$\tau_s|_{\min} = 100 \text{ fs}$$



Variation of the signal pulse width with OPO prism glass at 840 nm for a pump pulse width of 170 fsec. In the region of greater negative GVD, operation is stable with pulse widths of up to 220 fsec.

(from TANG C.L. et. al.)

## Key points

-Wave Front Reversal  
and Chirp Reversal  
(similarities and differences)

-Requirements for Chirp  
Reversal

Observation (experiments)

-Phase Conjugation and  
Time-Space-Domain Squeezing

## Space and Time-Domain Phase Conjugation

$$a(x,y,t)\cos[\omega_0 t - k_0 z + \psi(x,y,t)]$$

monochromatic wave

$$a(x,y)\cos[\omega_0 t - k_0 z + \psi(x,y)]$$

wave front reversal

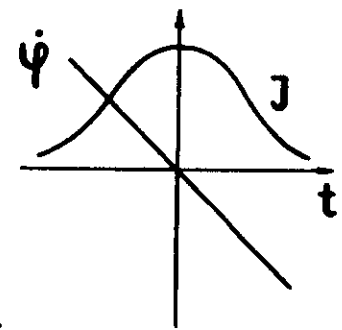
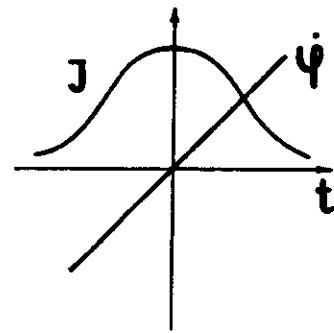
$$\psi \rightarrow -\psi$$

plane wave

$$a(t)\cos[\omega_0 t - k_0 z + \psi(t)]$$

chirp reversal

$$\psi \rightarrow -\psi, \dot{\psi} \rightarrow -\dot{\psi}$$



$$\psi \sim t^2$$

# Phase Conjugation in OPO



$$\omega_1 + \omega_2 = \omega_3$$

$$A_1 = A_{10} \text{chm} + \sqrt{\frac{\tilde{\epsilon}_1}{\tilde{\epsilon}_2}} A_{20}^* \text{shm}$$

$$A_2 = A_{20} \text{chm} + \sqrt{\frac{\tilde{\epsilon}_2}{\tilde{\epsilon}_1}} A_{10}^* \text{shm}$$

$$m = \sqrt{\tilde{\epsilon}_1 \tilde{\epsilon}_2} A_{30} Z$$

$$m \gg 1, A_2 = \sqrt{\frac{\tilde{\epsilon}_2}{\tilde{\epsilon}_1}} A_1^* \Rightarrow \text{phase conjugation}$$

# Chirp Reversal

-J.H. Marburger. Appl. Phys. Lett., 32, 372 (1978).

-A. Yariv et al. Opt. Lett., 4, 52 (1979).

## Chirp reversal of ps and fs pulses

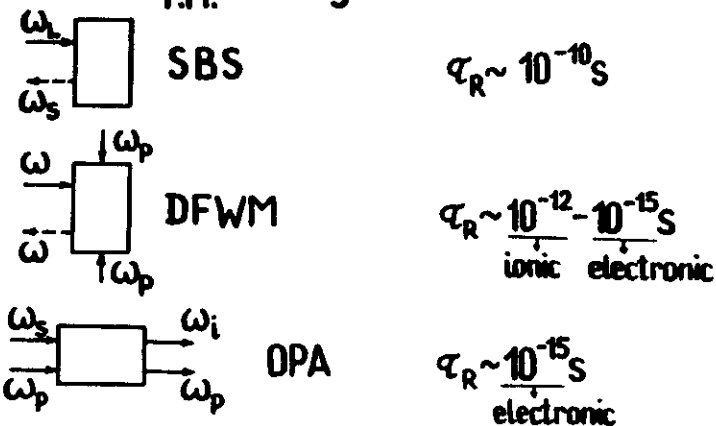
Requirements for conjugator:

-Nonlinear response

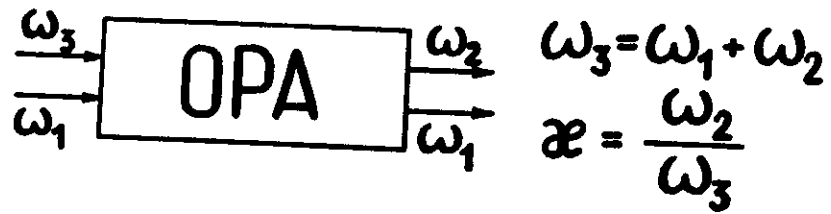
$$\tau_{\text{res}}^{\text{NL}} \ll \tau_{\text{signal correlation time}}$$

-Phase-matching bandwidth

$$\Delta \nu_{\text{P.M.}} \gg \Delta \nu_s$$



# Spectrum Bandwidth of OPA



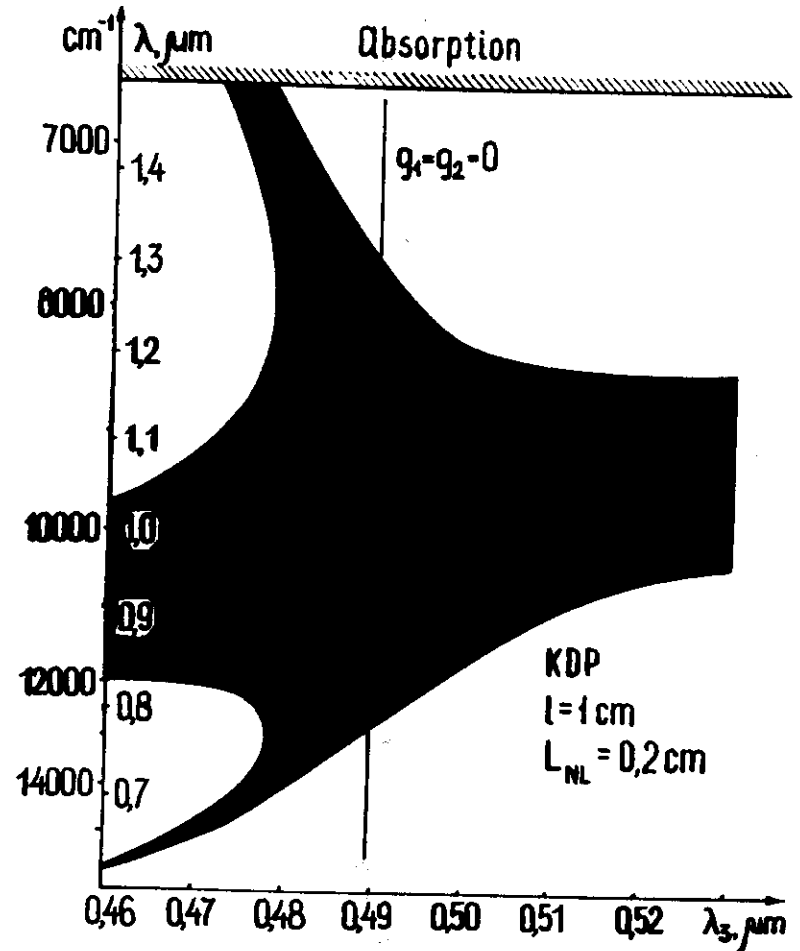
$$\alpha \neq 0,5 \quad \Delta\omega_{\text{OPA}} \sim (|V_{12}|^2 l L_{\text{NL}})^{-1/2}$$

$$\alpha = 0,5 \quad \Delta\omega_{\text{OPA}} \sim (|k''_{\omega}|^2 l L_{\text{NL}})^{-1/4}$$

$$\lambda = 1 \mu\text{m}, \quad 1 \text{ps} \rightarrow 15 \text{cm}^{-1}$$

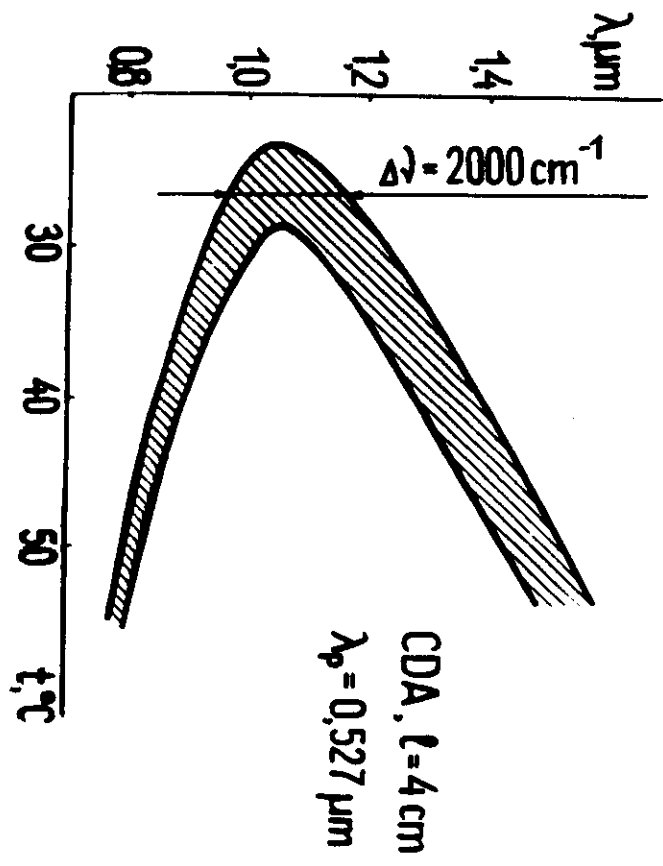
$$10 \text{fs} \rightarrow 1500 \text{cm}^{-1}$$

# OPO Spectrum versus Pump Wavelength

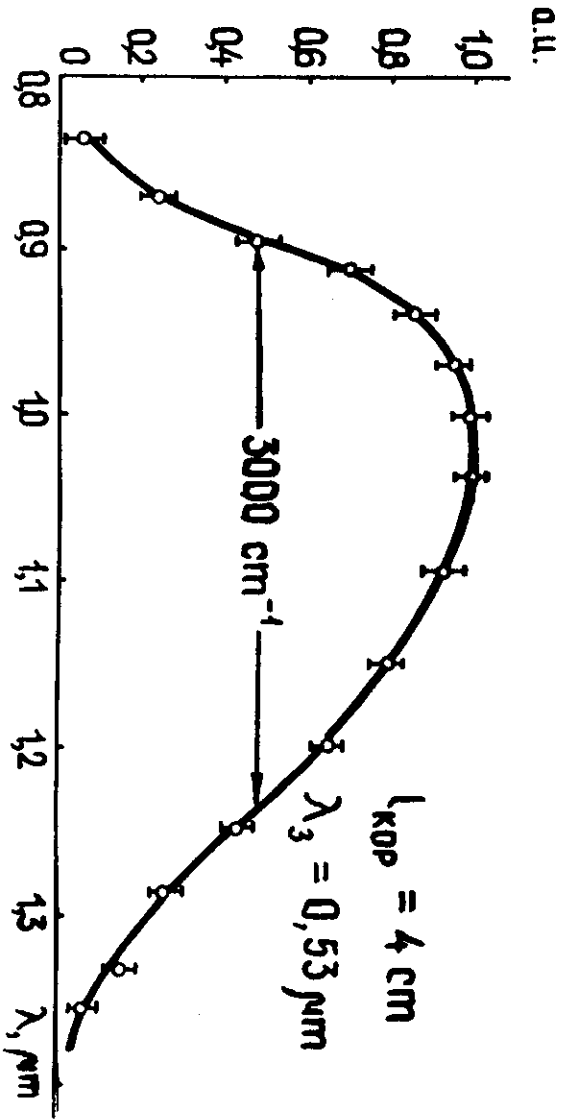




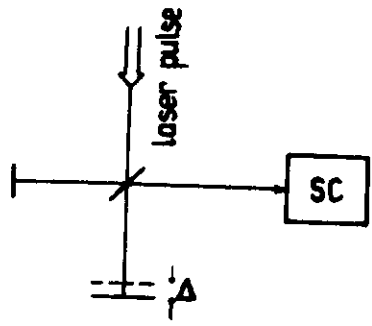
VU CDA OPA Bandwidth Dependence on Temperature Tuning



KDP (e-00) OPD Spectrum



**Michelson-Streak-Camera Type Dynamic Interferometer**



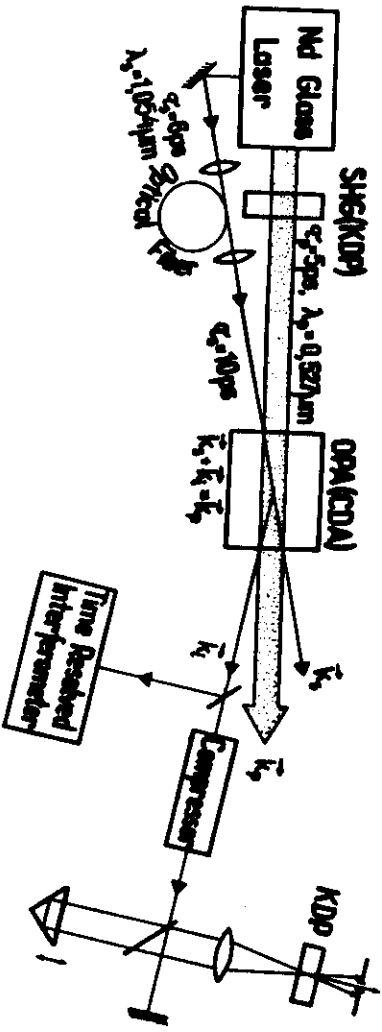
$$\frac{\partial \nu}{\partial t} = \frac{\nu}{m} \frac{dm}{dt}$$

$$\Delta \nu = \frac{1}{2\Delta}$$

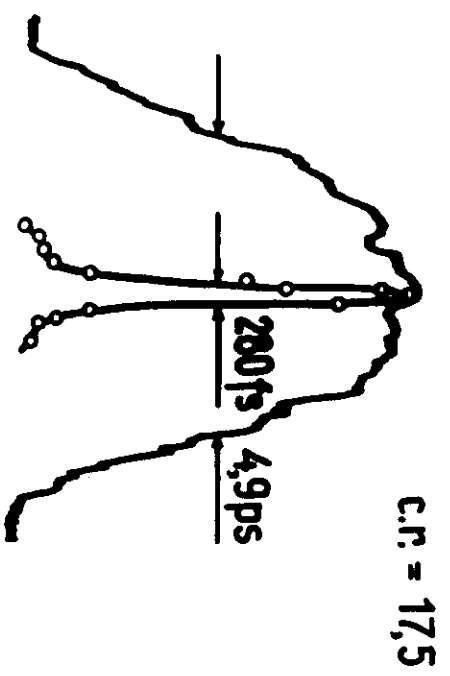


CW pumped actively  
QS and ML YAG:Nd Laser

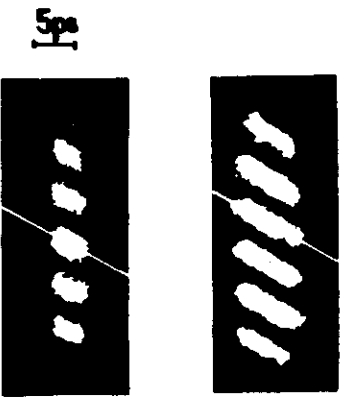
**VU**  
**Experimental Setup for Chirped ps Signal Parametric Amplification, Chirp Reversal and Compression in Positive GVD Medium**



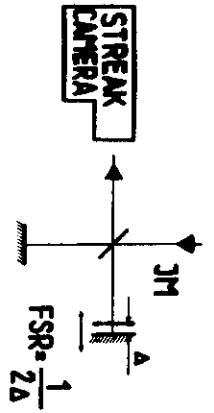
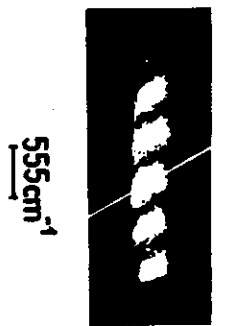
VU Compression result



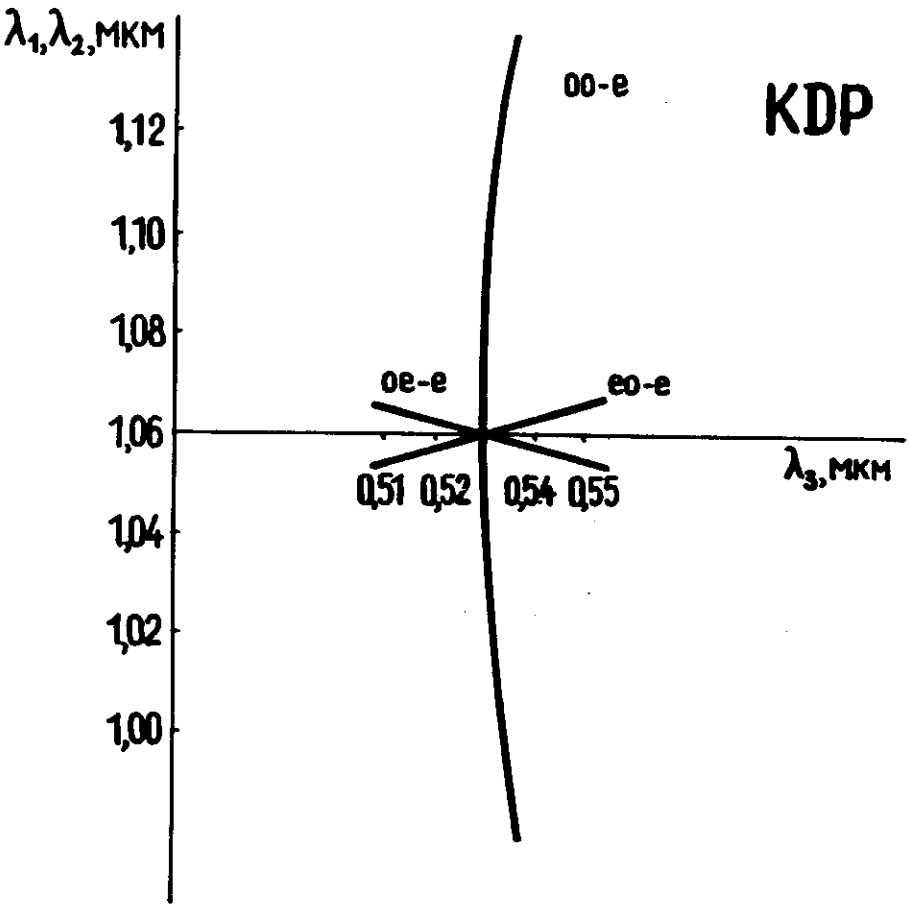
VU Chirp Reversal in CDA OPA



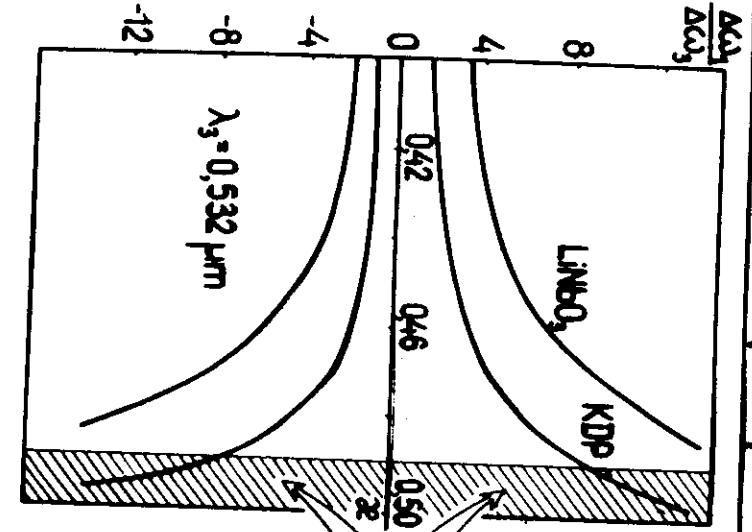
E, mJ	$\Delta\nu$ , cm <sup>-1</sup>	$\tau$ , ps	$\tau$ , ps	
10 <sup>-4</sup>	400	10	40	single-mode fiber output signal
0,5	200	5	40	amplified signal
0,5	-200	5	-40	phase-conjugated idler



# OPO Tuning Curves



## Parametric Chirp Dependence on Degeneracy Value



$$\frac{\Delta\omega_1}{\Delta\omega_3} = \frac{F}{1-2\epsilon}$$

$$\frac{\Delta\omega_2}{\Delta\omega_3} = 1 - \frac{\Delta\omega_1}{\Delta\omega_3}$$

$$z = \frac{\omega_2}{\omega_3}$$

$$F = \frac{\frac{dk_1}{dk_2} - \frac{dk_1}{dk_3}}{\frac{dk_1}{dk_2} \frac{\omega_2}{\omega_3}}$$

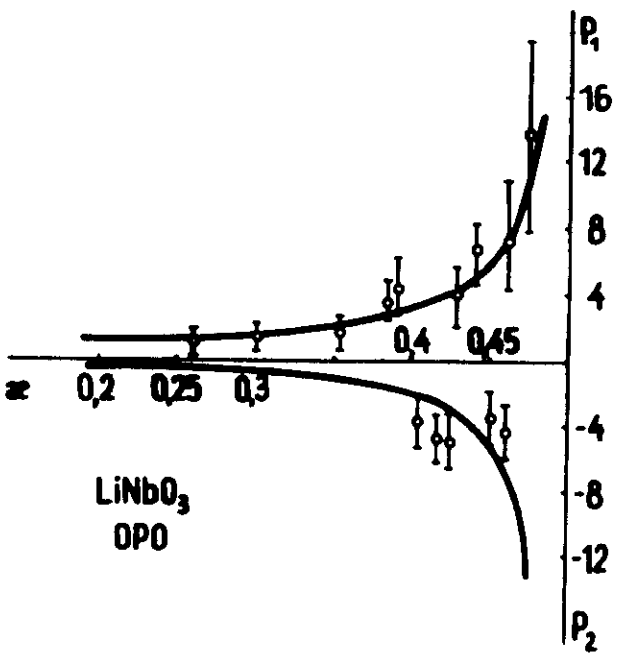
Nonlinear chirp region:

$$\frac{\Delta\omega_2}{\omega_3} > \frac{1}{10} \frac{F}{F}$$

$\lambda_1, \mu\text{m}$	LiNbO <sub>3</sub>	KDP	CDA	LiIO <sub>3</sub>
1.06	0.20			-0.21
0.53	0.54	0.16	0.39	0.56
0.35		0.57		
0.26		0.58		

F values

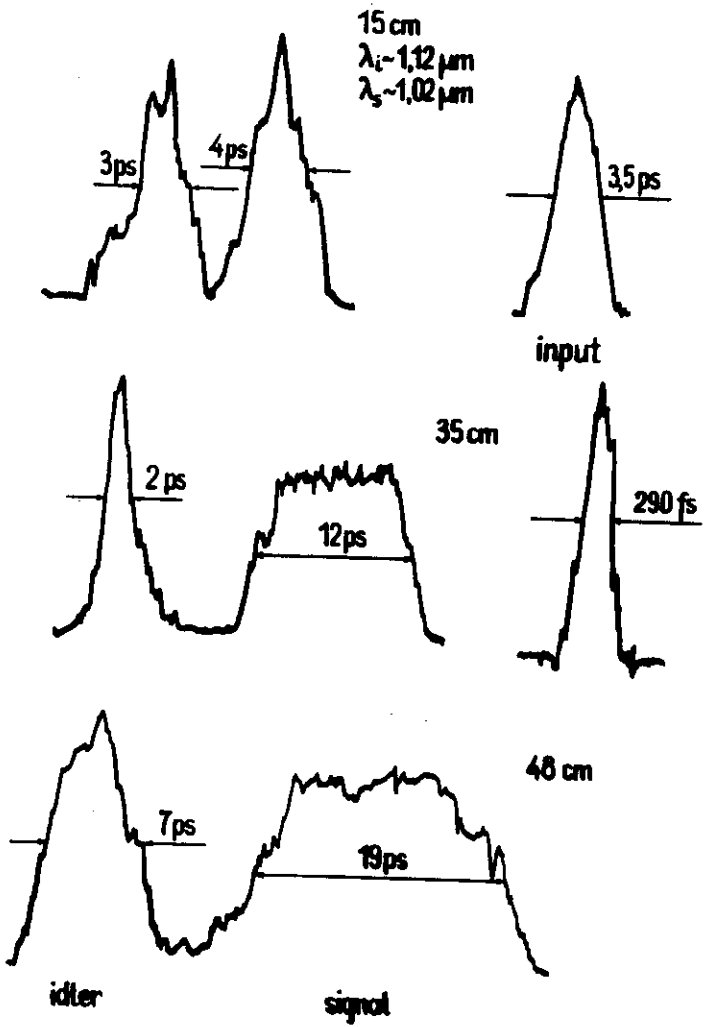
# VU Chirp Enhancement Results



## VU Evolution of Pump and OP0 Signal Chirp along Train

<p>CW pumped actively mode-locked and Q-switched</p> <p>YAG:Nd laser PRF = 10 KHz <math>\tau_p = 60</math> ps</p> <p><math>\frac{\Delta\lambda}{\lambda} = 0.0028</math> cm<sup>-1</sup>/ps</p> <p><math>\frac{\Delta\lambda}{\lambda} = 0.0058</math> cm<sup>-1</sup>/ps</p> <p><math>\frac{\Delta\lambda}{\lambda} = 0.0075</math> cm<sup>-1</sup>/ps</p>	<p>35 cm<sup>-1</sup> pump</p>	<p>Leading part</p> <p><math>\frac{\Delta\lambda}{\lambda} = 0.0028</math> cm<sup>-1</sup>/ps</p>	<p>50 cm<sup>-1</sup> signal</p>	<p>Synchronously pumped OP0 LiNbO<sub>3</sub></p> <p><math>\frac{\Delta\lambda}{\lambda} = 0.52</math> cm<sup>-1</sup>/ps</p>		
					<p>middle</p> <p><math>\frac{\Delta\lambda}{\lambda} = 0.0058</math> cm<sup>-1</sup>/ps</p>	<p>50 cm<sup>-1</sup> signal</p>
					<p>trailing</p> <p><math>\frac{\Delta\lambda}{\lambda} = 0.0075</math> cm<sup>-1</sup>/ps</p>	<p>50 cm<sup>-1</sup> signal</p>

VU Compression Results



**Fs  $\beta$ -BARIUM BORATE  
OPO**  
with INTRACAVITY CHIRP  
ENHANCEMENT & PULSE  
SELF-COMPRESSION  
(by A. LAUBEREAU et. al. BAYREUTH U.)

PUMP: SH of FCM Nd:glass

$\tau_p = 0.8 \text{ ps}$

TRAIN: 300 pulses

$E_p = 10^{-6} \text{ J}$

$\lambda_p = 527 \text{ nm}$

p.r.f. = 15 Hz

OPO: (BBO,  $L = 5.8 \text{ mm}$ )

$\Delta\lambda = 700 \div 1800 \text{ nm}$

$\tau_p = 65 \pm 7 \text{ fs}$  ( $\lambda = 1076 \text{ nm}$ )

$\eta = 3\%$

FORECAST:

$\tau_p \Rightarrow 10 \text{ fs}$

# Phase Conjugation and Squeezing in OPO

## Classical analogy

$$\omega_1 = \omega_2 = \omega_{3/2}, \quad \text{oo-e}$$

$$A = A_0 \text{chm} + A_0^* \text{shm}, \quad m \gg 1$$

$$A \sim (A_0 e^m + A_0^* e^{-m}) \Rightarrow \text{conjugated waves}$$

## Suppression of one quadrature component

$$A_0 = a_0 + i b_0, \quad A = a + i b$$

$$a = a_0 (\text{chm} + \text{shm})$$

$$b = b_0 (\text{chm} - \text{shm})$$

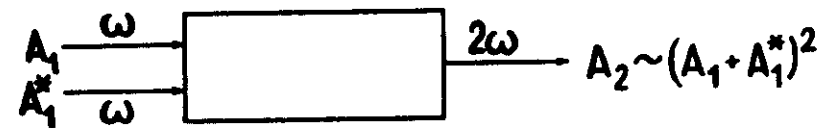
$$\overline{a^2} = \overline{a_0^2} e^{2m}, \quad \overline{b^2} = \overline{b_0^2} e^{-2m}$$

## Conclusion:

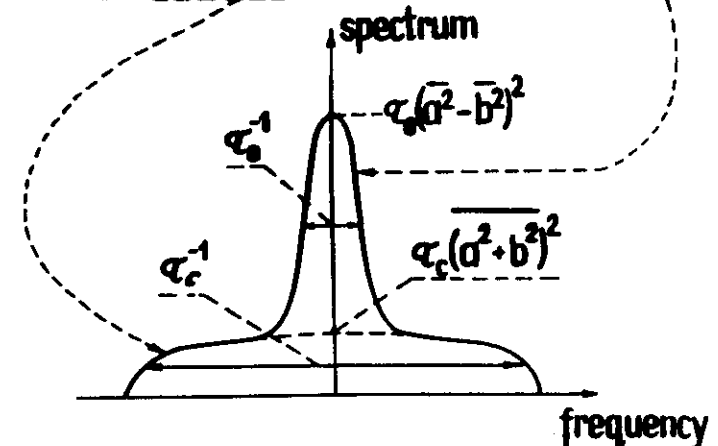
squeezing in OPO is caused by phase conjugation

# Verification of Phase Conjugation

## Nonlinear mixing

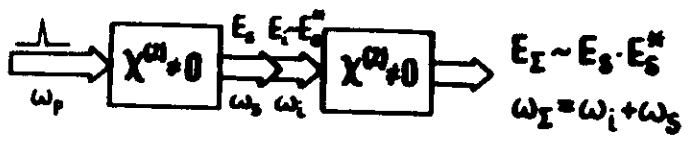


$$A_2 \sim [A_1^2 + A_1^{*2}] + 2[A_1 A_1^*]$$



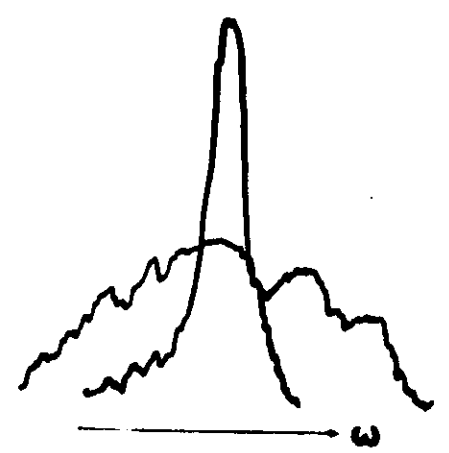
$\tau_s$  - pulse duration  
 $\tau_c$  - correlation time  
 $\tau_s \gg \tau_c$  sharp peak in SH spectrum when  $\overline{a^2} \neq \overline{b^2}$

# VU Phase Conjugation in PPO

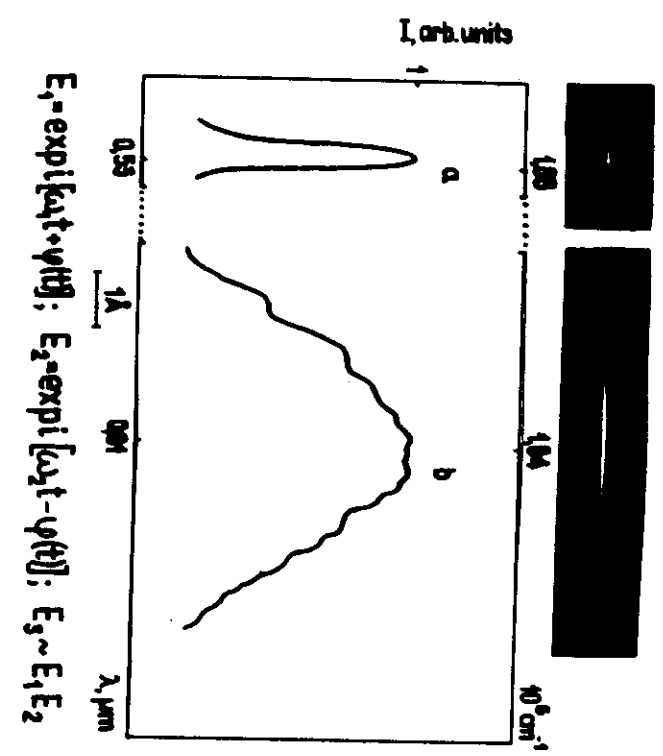


$$E_s \sim e^{i\varphi(t, \vec{r})}$$

$E_\Sigma \sim |E_s|^2$  - free-chirp pulse  
 - diffraction limited beam



VU Radiation Spectrum with Phase Modulation (b) and with Eliminated One (a)

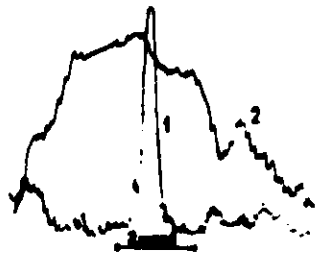


$E_1 = \text{exp}[i\omega_1 t + \varphi(t)]$ ;  $E_2 = \text{exp}[i\omega_2 t - \varphi(t)]$ ;  $E_\Sigma \sim E_1 E_2$

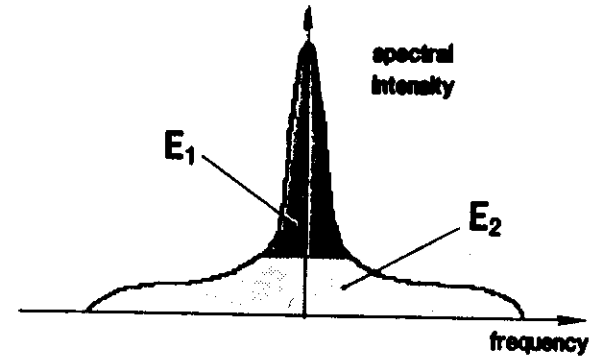


VU

Far-field angular distributions of phase conjugated (1) and nonconjugated (2) waves



## DETERMINATION OF MULTIMODE SQUEEZING



$m$  - parameter of multimode squeezing

$m = E_1/E_2 > \frac{1}{2}$  condition of multimode squeezing<sup>\*)</sup>

$$m = \frac{(1-\varepsilon)^2}{\varepsilon(\varepsilon(1+\varepsilon)^2 - (1-\varepsilon)^2)}$$

$\varepsilon = \bar{b}^2 / \bar{a}^2$  conjugation parameter

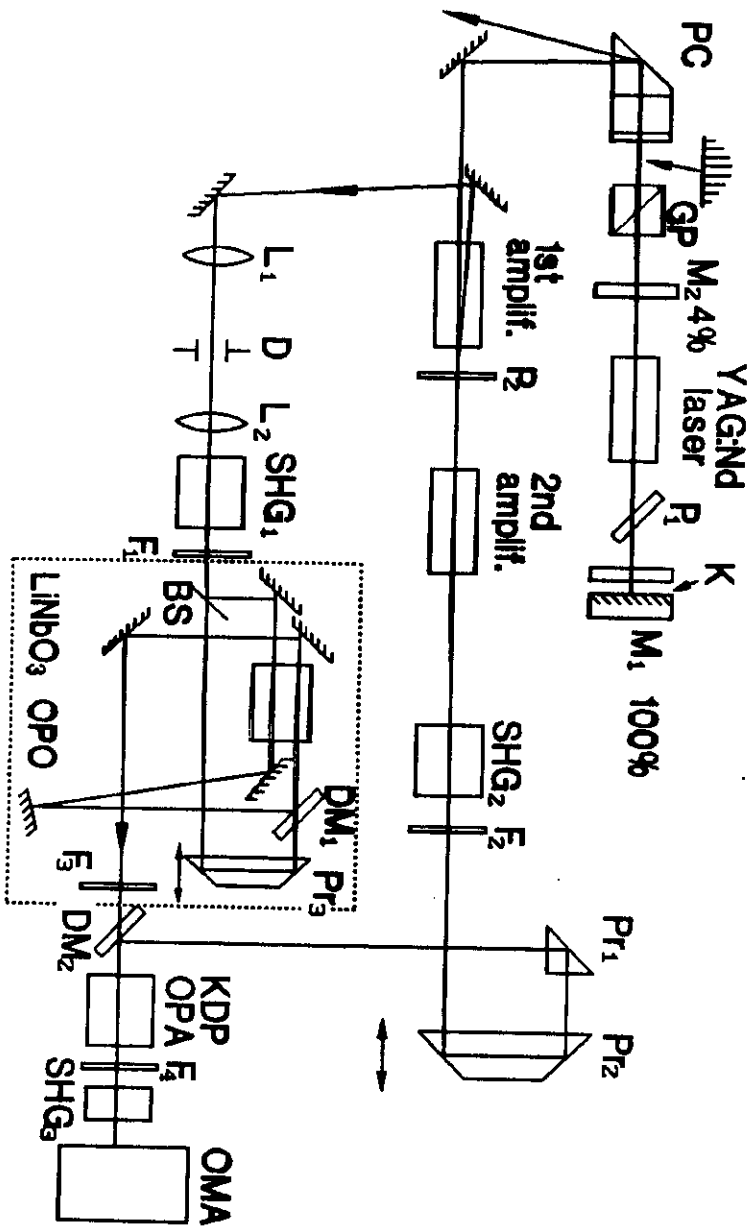
$\varepsilon = 1$  no conjugation

$\varepsilon = 0$  complete conjugation

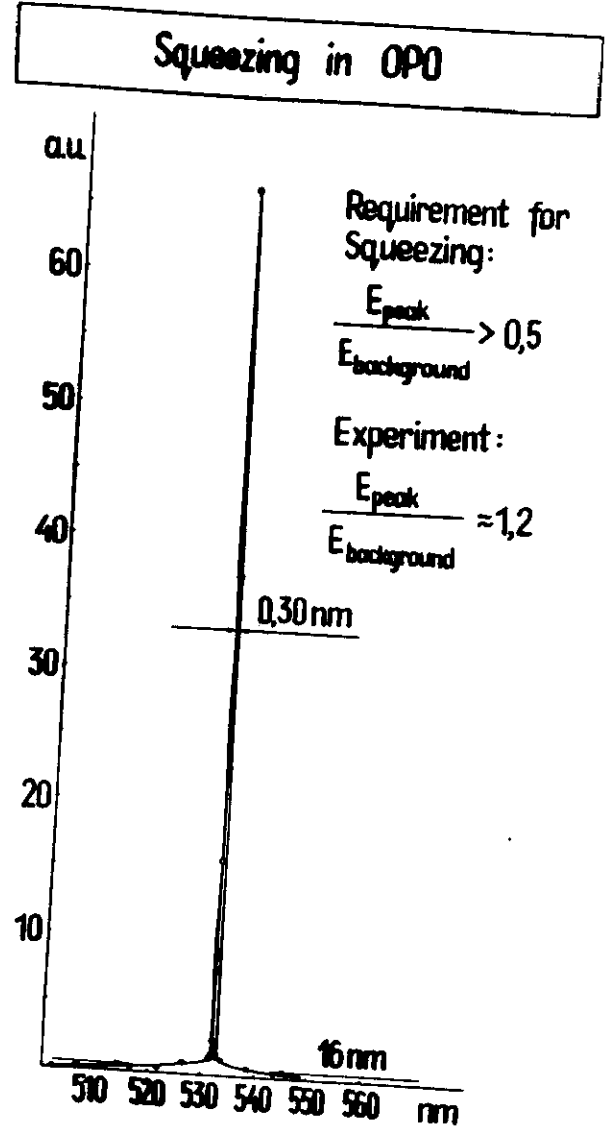
$$g_F = \frac{(\bar{a}^2 + \bar{b}^2)^2}{(\bar{a}^2 + \bar{b}^2)^2}$$

second order coherence of twin-field

<sup>\*)</sup> S.Kilin. Sov.Opt. & Spectroscopy V.66, p.733 (1989).

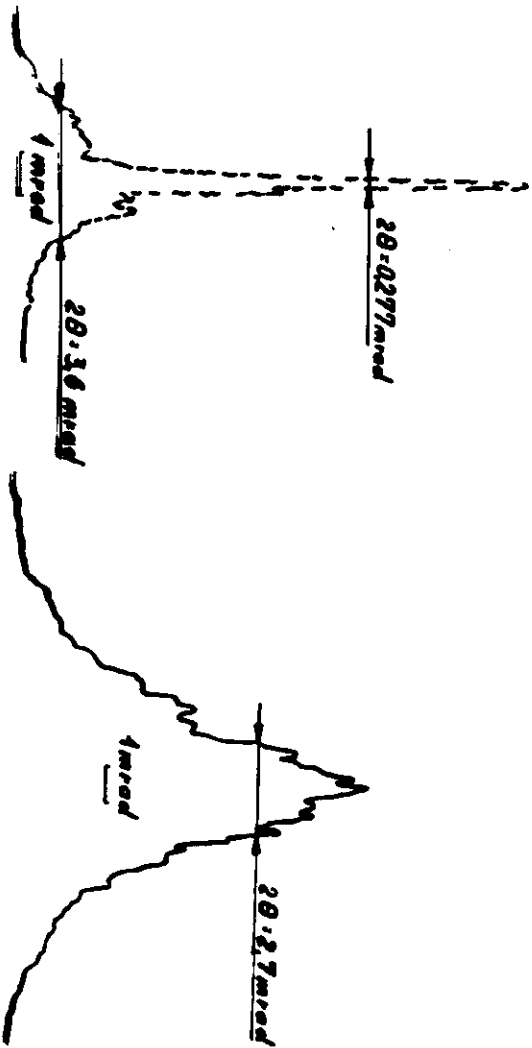


# EXPERIMENTAL SETUP



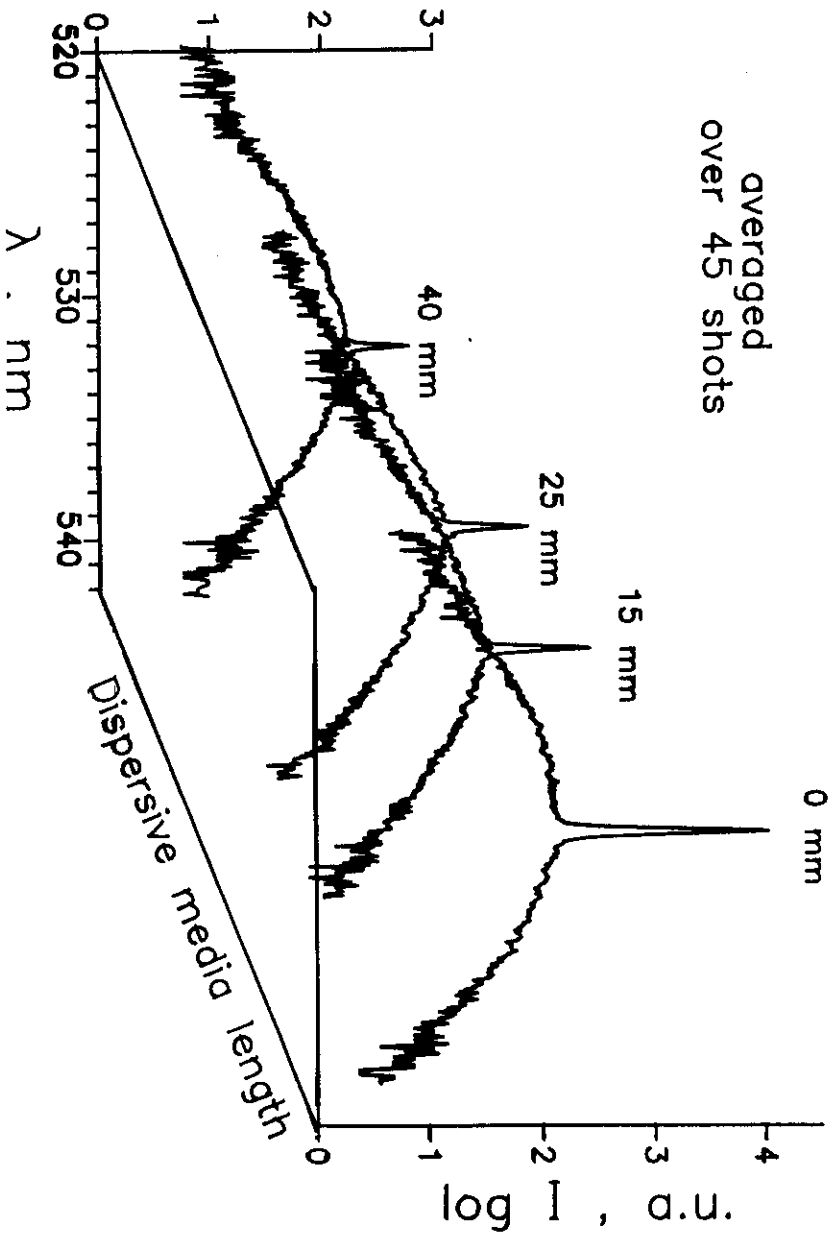
*Spatial SH Spectrum of  
Degenerated KDP OPD*

*Partial Decoujugation  
by 20mm of LiNbO<sub>3</sub>*



### SH SPECTRA OF OPA OUTPUT

averaged  
over 45 shots



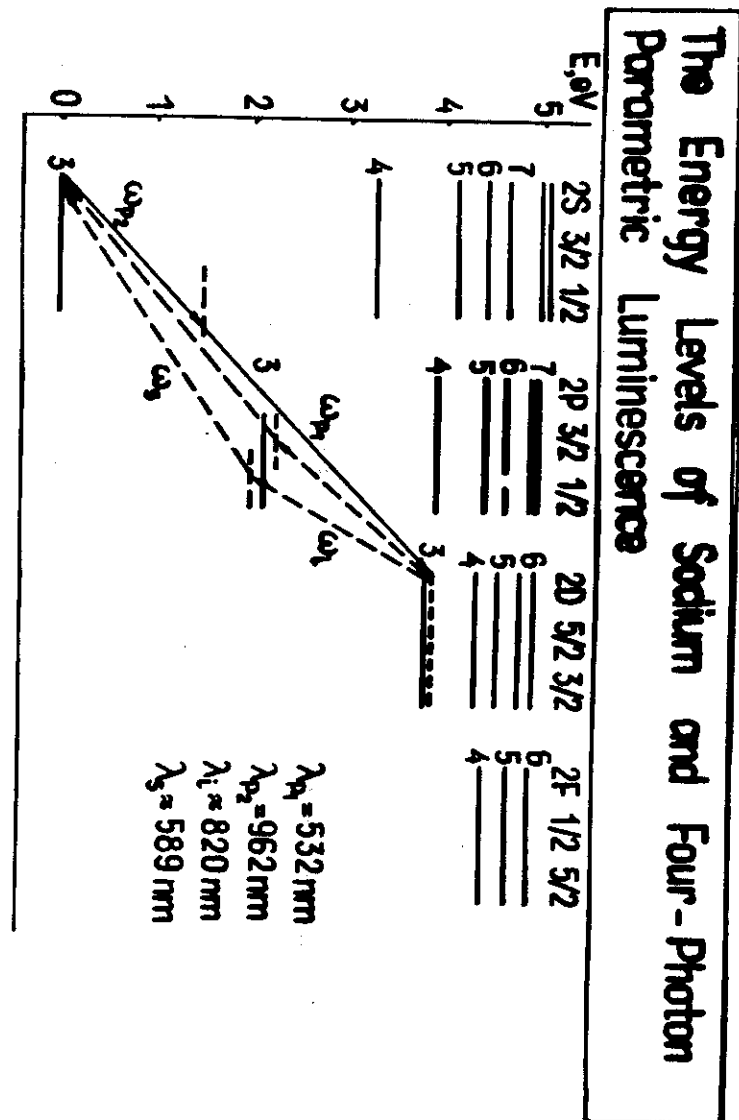
# FOUR-PHOTON SODIUM VAPOR PARAMETRIC OSCILLATOR

## The Advantages of Nonlinear Gases:

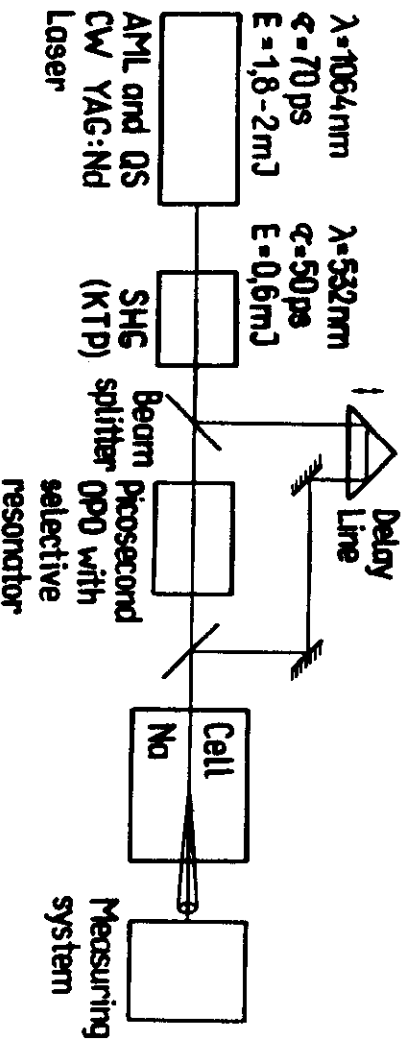
- LARGE LENGTHS
- HIGH OPTICAL DAMAGE THRESHOLD
- SELFRECOVERING
- HIGH TRANSPARENT & HOMOGENEOUS
- PHASE MATCHING
- PRECISE CALCULATIONS

TOPIC:

FIRST EXPERIMENT ON  
Na - gas  
OPO



## Experimental Arrangement for the Four-Photon Parametric Luminescence Investigations



### Pump parameters

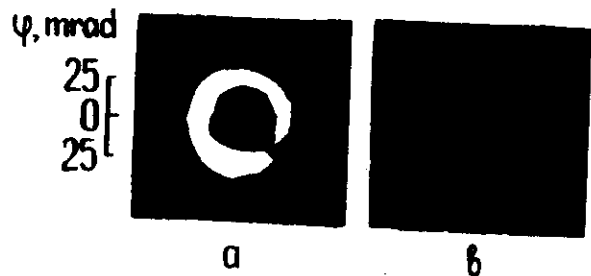
$\lambda_{p1} = 532 \text{ nm}$     $\Delta\lambda_1 = 0.8 \text{ cm}^{-1}$     $E_1 = 0.2 \text{ mJ}$     $P_1 = 200 \text{ mW}$     $\alpha_1 = 50 \text{ ps}$     $\nu = 1 \text{ kHz}$   
 $\lambda_{p2} = 962 \text{ nm}$     $\Delta\lambda_2 = 0.9 \text{ cm}^{-1}$     $E_2 = 0.01 \text{ mJ}$     $P_2 = 10 \text{ mW}$     $\alpha_2 = 45-50 \text{ ps}$     $\nu = 1 \text{ kHz}$

## Three and Four-Photon Parametric Scattering

	Three-photon interaction	Four-photon interaction
Phase matching conditions	$\vec{\omega}_p = \vec{\omega}_s + \vec{\omega}_i$ $k_p = k_s + k_i$	$\vec{\omega}_{p1} + \vec{\omega}_{p2} = \vec{\omega}_s + \vec{\omega}_i$ $k_{p1} + k_{p2} = k_s + k_i$
Collinear interaction	$ k_s  +  k_i  >  k_p $	$ k_s  +  k_i  >  k_{p1}  +  k_{p2} $
Noncollinear interaction		$ k_s  +  k_i  >  k_{p1} + k_{p2} $

**Four-Photon Parametric Luminescence Radiation from Sodium Vapor Cell in Visible Spectral Region during Noncollinear Two-Photon 3S-3D Transition Excitation**

$\lambda_{p_1} = 532 \text{ nm}$   
 $\lambda_{p_2} = 962 \text{ nm}$   
 Concentration  $N = 8 \cdot 10^{16} \text{ cm}^{-3}$



**a**-angle between pump beams 0 mrad  
**b**-angle between pump beams 17.5 mrad

**The Main Formulas for the Calculation of Four-Photon Parametric Luminescence Phase Matching**

Phase Matching Conditions

$$\vec{k}_{p_1} + \vec{k}_{p_2} = \vec{k}_1 + \vec{k}_2 \quad \omega_{p_1} + \omega_{p_2} = \omega_1 + \omega_2$$

Cone Angle

$$\cos \varphi = (k_p^2 + k_1^2 - k_2^2) / 2k_1 k_p$$

$$\vec{k}_p = \vec{k}_{p_1} + \vec{k}_{p_2}, \quad |\vec{k}_i| = \frac{n_i(\omega)\omega}{c}$$

Selmeier Equation

$$n(\omega) - 1 = \frac{N r_e}{29\pi} \sum \frac{f_{np,j}}{\omega_{np,j}^2 - \omega^2}$$

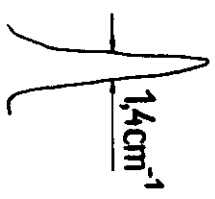
$N$ -density of sodium in  $\text{cm}^{-3}$

$r_e = 2,818 \cdot 10^{-13} \text{ cm}$

$\omega_{np,j}$ -energy of the  $nP_j$  level in  $\text{cm}^{-1}$

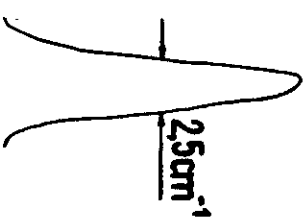
$f_{np,j}$ -the oscillator strength

**The Dependence of Four-Photon Parametric Generation Spectral Characteristics on Sodium Concentration**



$N = 2 \cdot 10^{16} \text{ cm}^{-3}$

a



$N = 7 \cdot 10^{16} \text{ cm}^{-3}$   
 $\lambda = 590 \text{ nm}$

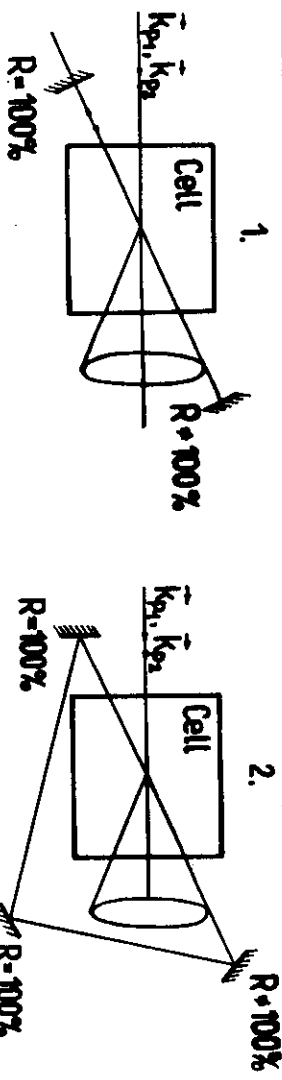
b



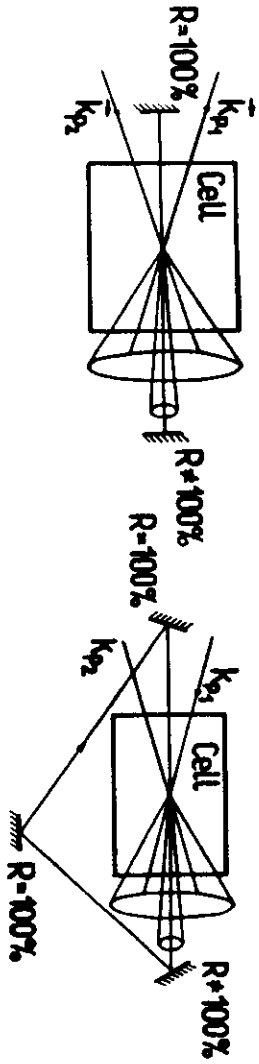
$N = 2 \cdot 10^{17} \text{ cm}^{-3}$

c

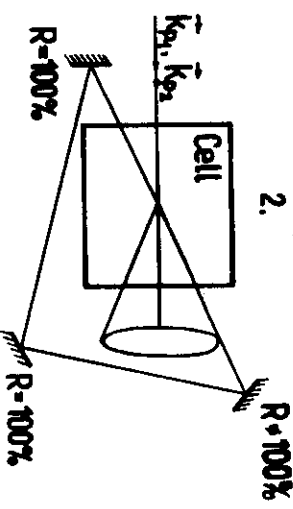
**The Types of Cavities Used for Four-Photon Parametric Generator**



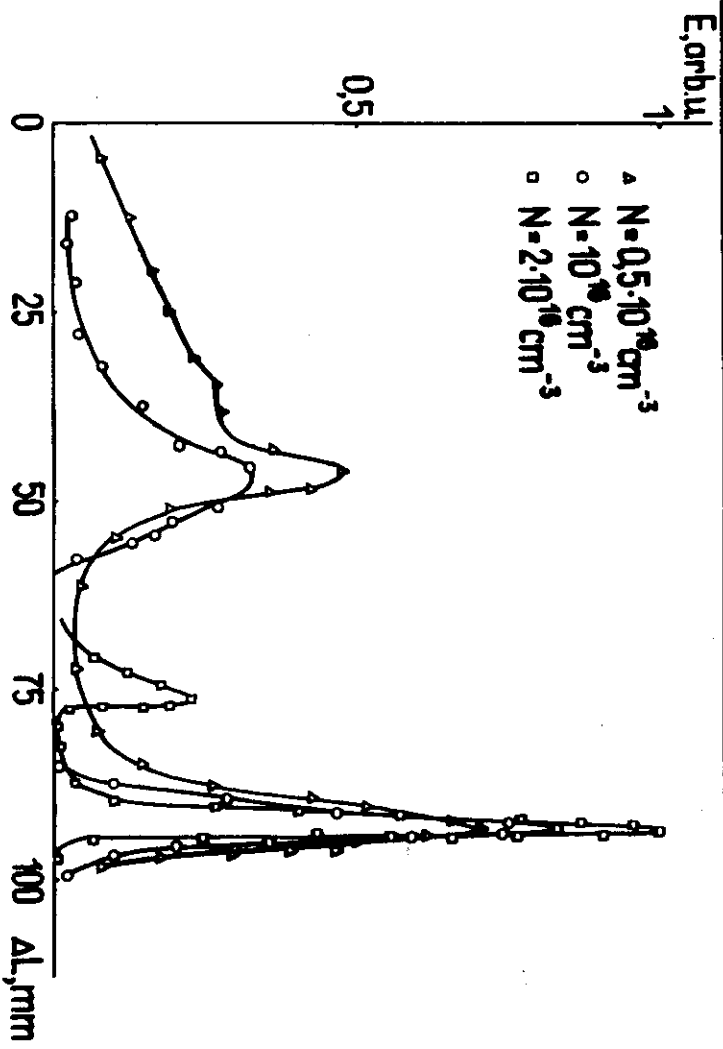
3.



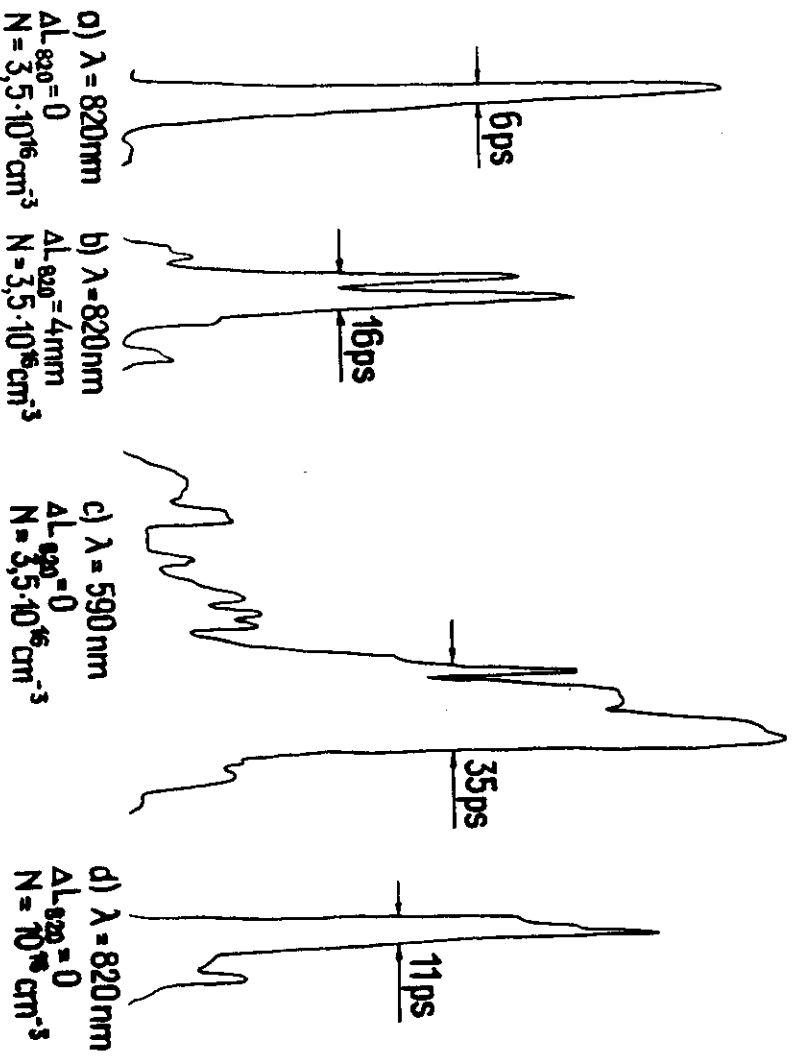
4.



## Dependence of the Four-Photon Parametric Oscillator Output Energy on the Cavity Mismatch $\Delta L$



## The Pulse Profiles of Four-Photon Parametric Oscillator





# CONCLUSION

- NEW PHENOMENA OBSERVED

- CHIRP REVERSAL
- CHIRP ENHANCEMENT
- PULSE SELF-COMPRESSION (SOLITONS)
- $\chi^{(3)}$  OPO
- SQUEEZING

- PARAMETERS ACHIEVED \*)

- PULSE WIDTH  $68 \text{ fs}$
- LINE WIDTH  $\sim 10 \text{ kHz}$
- ENERGY  $\sim 3 \text{ J}$
- TUNING  $\sim 0.3 \div 20 \text{ nm}$
- SQUEEZING  $\sim 3 \text{ dB}$

\*) UNRELATED

Dependence of the Four-Photon Parametric Oscillator Output Pulse Duration (1) and Spectral Halfwidth (2) on the Concentration of Sodium Vapor

