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INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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SMR.550 - 19

**SPRING COLLEGE IN MATERIALS SCIENCE ON
"NUCLEATION, GROWTH AND SEGREGATION IN MATERIALS
SCIENCE AND ENGINEERING"
(6 May - 7 June 1991)**

**ELECTRON PROBE MICROANALYSIS
AND RAMAN SPECTROSCOPY**

P.R. GRAVES
AEA Industrial Technology
Harwell Laboratory
Didcot
Oxfordshire OX11 0RA
United Kingdom

Raman spectroscopy and electron probe microanalysis

- Lecture 1: Raman spectroscopy- simplified theory, instrumentation, analytical applications to materials science
- Lecture 2: Electron probe microanalysis- theory, instrumentation, application to high temperature corrosion. Raman spectroscopy - phase determination in crystal growth of high temperature superconductors, characterisation of surface phases on high temperature superconductors.
- Lecture 3: More advanced Raman spectroscopy- polarisation measurement, factor group analysis, lattice defect characterisation, thin film stress measurement.

These are preliminary lecture notes, intended only for distribution to participants.

SUPPLEMENT—Recent Scientific and Technical Books

NOT TO BE REMOVED FROM



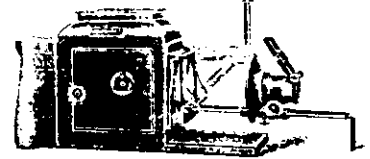
A WEEKLY JOURNAL OF SCIENCE

*"To the solid ground
Of Nature trusts the mind which builds for aye."*—WORDSWORTH

No. 3048, Vol. 121] SATURDAY, MARCH 31, 1928, [PRICE ONE SHILLING

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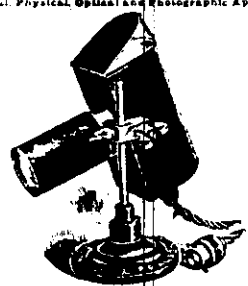
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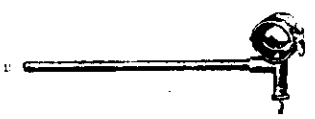
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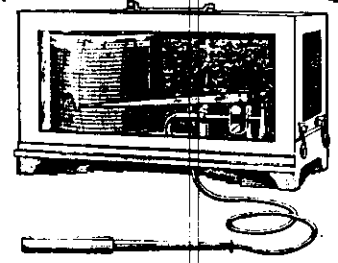
1. The important features of the Hossack Clamp are the uniform strain, and the regularity of the pressure up to a safe maximum, the preserving the pressure's accurate adjustment which is a frequent necessity when the usual type of clamp is employed.
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RECORDING
THERMOMETERS

RAMAN SPECTROSCOPY

KEY POINTS

- NON-DESTRUCTIVE
- NON-INVASIVE
- USES VISIBLE LIGHT
- GIVES CHEMICAL AND STRUCTURAL INFORMATION
- CAN BE USED IN ALMOST ANY ENVIRONMENT

It recurred to me in connection with the green ray which has appeared in NATURE promptly, me to put on a diagram the history of the phenomenon which occurred several years ago, but which I have re-trained myself to believe in the hope of securing proof. I do not say so in any dogmatically that the phenomenon is not an illusion or after image. No person is in the observation of optical effects, both real subjective, who has seen the phenomenon at its will have no doubt about its reality. There is no question in my mind but that the usual illusion of a phoric dispersion is quite correct. I am quite at a loss to answer it. Why is it seen so much even in conditions which appear to be the favourable conditions for its appearance and have

have come to the ocean some thirty times and have added to the "hay" at every favorable opportunity. Then I found clear sky, no haze or clouds on the sun at sunset, and a calm sea and yet I have swum out only three or four occasions, and only when it was really striking. This occasion was an eastward trip of the *Homard*, sailing from New York June 19, 1925. The color of the vanishing horizon was a faint and cold green, and the color of a faded and cold light. On other occasions I have observed a redness of the horizon, but the color change was from red or orange to yellow.

the sun to follow. The sun's position is the determining factor in the development of the air and the ocean. Warm air and water would flatten the tropics of the earth and cause the sun to set abnormally early. The flattening of the tropics in case of local mirage, however, is the curvature of the rays is reversed. In cold water and warm air, on the contrary, the refractive index would be increased. Consequently the rays augmented and sunset would be delayed, and a greater opportunity for atmospheric play.

the water, and come into play. Pattern of the broken line suggests a loss of data regarding water. I have then furnished with data regarding air and water temperatures in the trip. On the ocean, which is observed, the water temperatures at all water were practically the same at sunset, the other two favourable instances, on which we used to see an average of the phenomenon, the ocean from twelve to fourteen degrees warmer than the water. I hope that this note may prompt the interest of the green ray to some data on the air and water temperature, both for assessing on the water, as well as those on which it is important.

to W. Wood

R. W. Wood.

College of Arts and Sciences, University of
Tennessee,
Knoxville, Tennessee

It is also clear that the X-ray scattering of the disordered type observed by Bragg-Compton corresponds to the normal or average state of the atoms. It is probable, while the disordered scattering of energy waves length correspond to their fluctuations in that state it would follow that we should expect in the case of ordinary heat two types of properties: one determined by the normal or average properties of the atoms or molecules, and another representing a fluctuation from their fluctuation from their normal state. It is strongly become necessary to test either this is actually the case. The experiments have made have confirmed this anticipation, and

42

shown that in every case in which light is scattered by the molecules in disperse liquids or gases, the diffuse radiation of the ordinary kind, having the same wave length as the incident beam, is accompanied by a modified scattered radiation of decreased frequency.

The new type of light scattering discovered by us naturally requires very powerful illumination for its observation. In our experiments a beam of sunlight was converged adductively by telescope objective of 19 cm. aperture and 230 cm. focal length and by a second lens of 3 cm. focal length. At the focus of the second lens was placed the scattering material, which is either liquid, carefully purified by repeated distillation or vapour of its distillate vapours. To detect the presence of a modified scattered radiation the method of complementary light-filters was used. A blue-violet filter, when coupled with a yellow-green filter and placed in the incident light, completely extinguished the track of the light through the liquid or vapour. The reappearance of the track when the yellow filter is transferred to a place between it and the observer's eye is proof of the existence of a modified scattered radiation. Spectroscopic confirmation is also available.

[illegible]

210 D. W. Azar, S. G. G. G.
D. W. Azar, S. G. G. G.
D. W. Azar, S. G. G. G.

Land-locked Salmon.

This term "land-locked" is generally used to denote places of slavery, such as that from which I have just received in Natchez, 14,000 pounds of cotton. Western and Eastern, and even for the Spanish Colonies. The word is only a technical one, and is not always true, and that it does to indicate the true circumstance.

It is not that Lake Samon has a stock of salmon that it was originally possessing from the sea, but the fish first became accessible to mankind, and they could scarcely have prevented it from becoming what they wished, so that none found it. It seems clear that in the days when the lake was accessible from the sea, and salmon went through it shown in its thousands, some of the shoals that descended into the lake came to rest there, and so formed a non-migratory stock, which became known later, similarly with the lochs there, and so the shoals, reaching the bottom, from there went back to the sea and fed on the bottom and bottom fish, and so formed a variety of lake-salmon, that was lost when the lake became inaccessible.

The trout forms freshwater colonies in every river and lake that it enters. One of this species he called a "brook trout" or "brook salmon." On this point of the

No. 2048, Vol. 24

Atlantic the
tion to the tr
only in steep
lakes with m
with even qu
to produce th
no trout. The
result.

Briggs M.

Appendix

In a paper
presented at
the meeting
conducted at
the University
of California,
the author
discussed the
importance of
the study of
the history of
the world.

The first
 thing I did
 was to go
 to the
 bank and
 get a
 checkbook
 and a
 pen. I
 then went
 to the
 post office
 and got a
 stamp. I
 then went
 to the
 grocery
 store and
 got some
 food. I
 then went
 to the
 drug store
 and got
 some
 medicine.

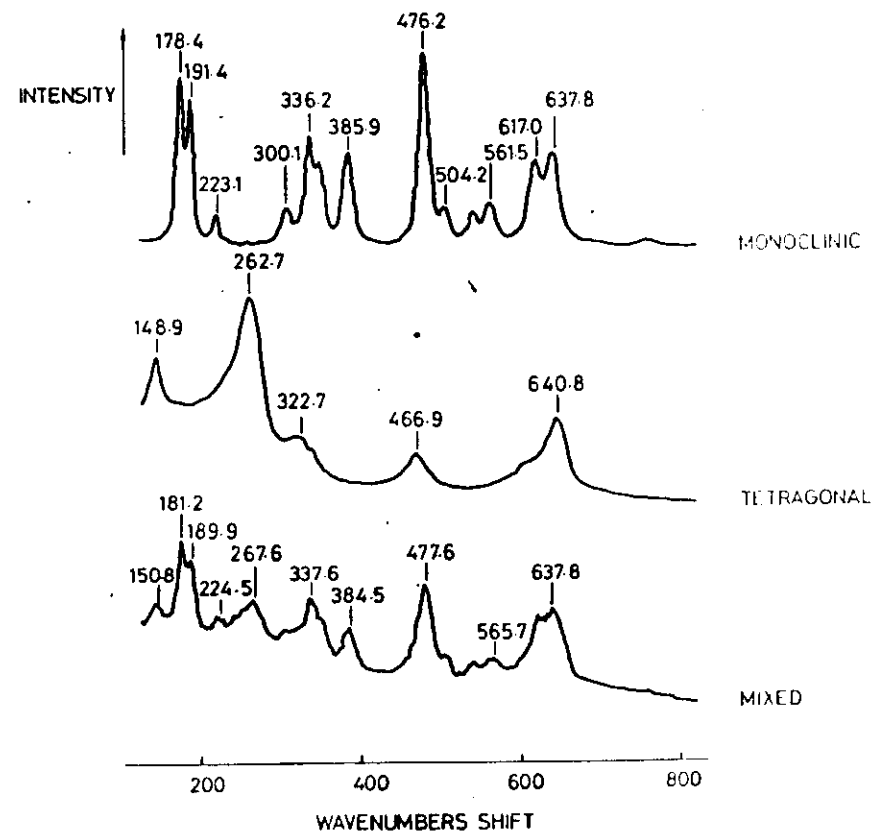
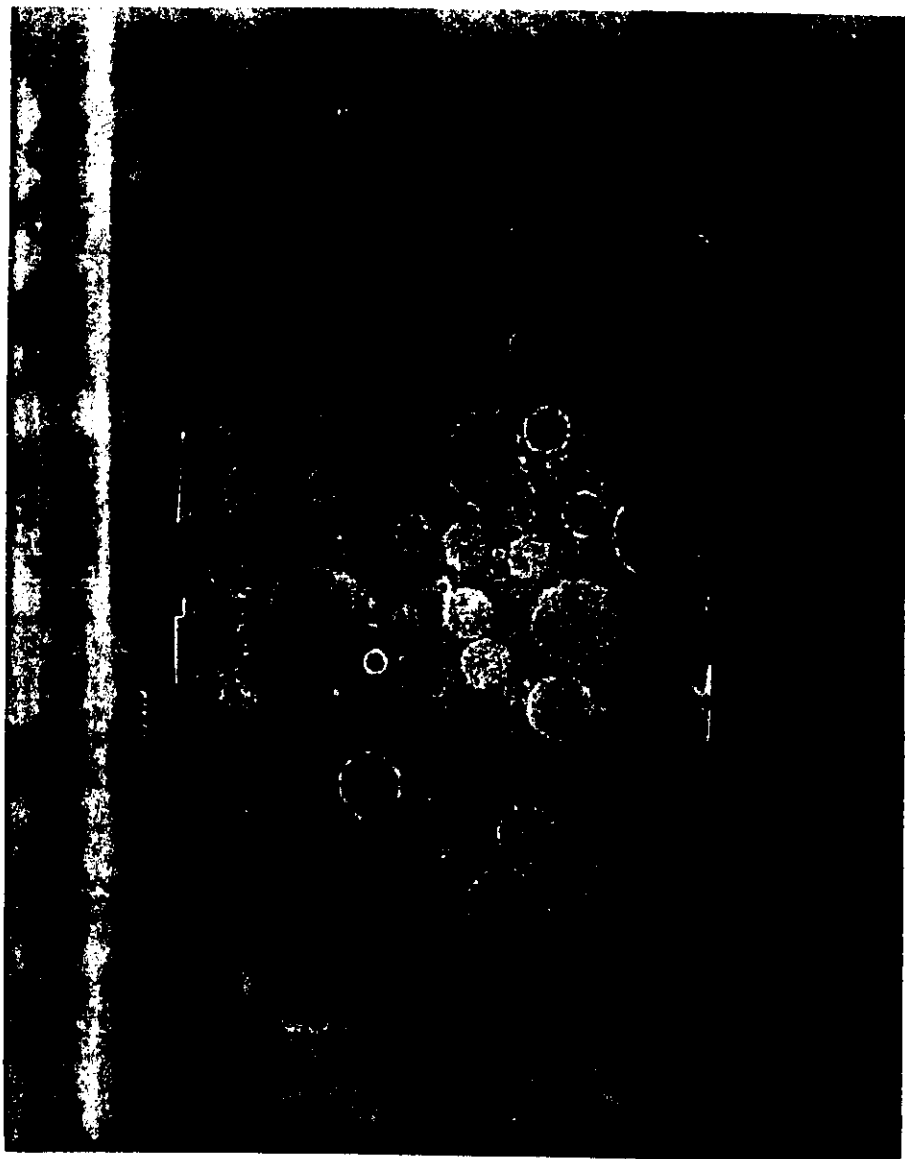
$$\begin{aligned} & \mathcal{N}_{\text{total}} = \mathcal{N}_{\text{in}} + \mathcal{N}_{\text{out}} \\ & \mathcal{N}_{\text{in}} = \mathcal{N}_{\text{in}}^{\text{in}} + \mathcal{N}_{\text{in}}^{\text{out}} \\ & \mathcal{N}_{\text{out}} = \mathcal{N}_{\text{out}}^{\text{in}} + \mathcal{N}_{\text{out}}^{\text{out}} \\ & \mathcal{N}_{\text{in}}^{\text{in}} = \mathcal{N}_{\text{in}}^{\text{in}} + \mathcal{N}_{\text{in}}^{\text{out}} \\ & \mathcal{N}_{\text{out}}^{\text{in}} = \mathcal{N}_{\text{out}}^{\text{in}} + \mathcal{N}_{\text{out}}^{\text{out}} \\ & \mathcal{N}_{\text{in}}^{\text{out}} = \mathcal{N}_{\text{in}}^{\text{out}} + \mathcal{N}_{\text{in}}^{\text{in}} \\ & \mathcal{N}_{\text{out}}^{\text{out}} = \mathcal{N}_{\text{out}}^{\text{out}} + \mathcal{N}_{\text{out}}^{\text{in}} \end{aligned}$$

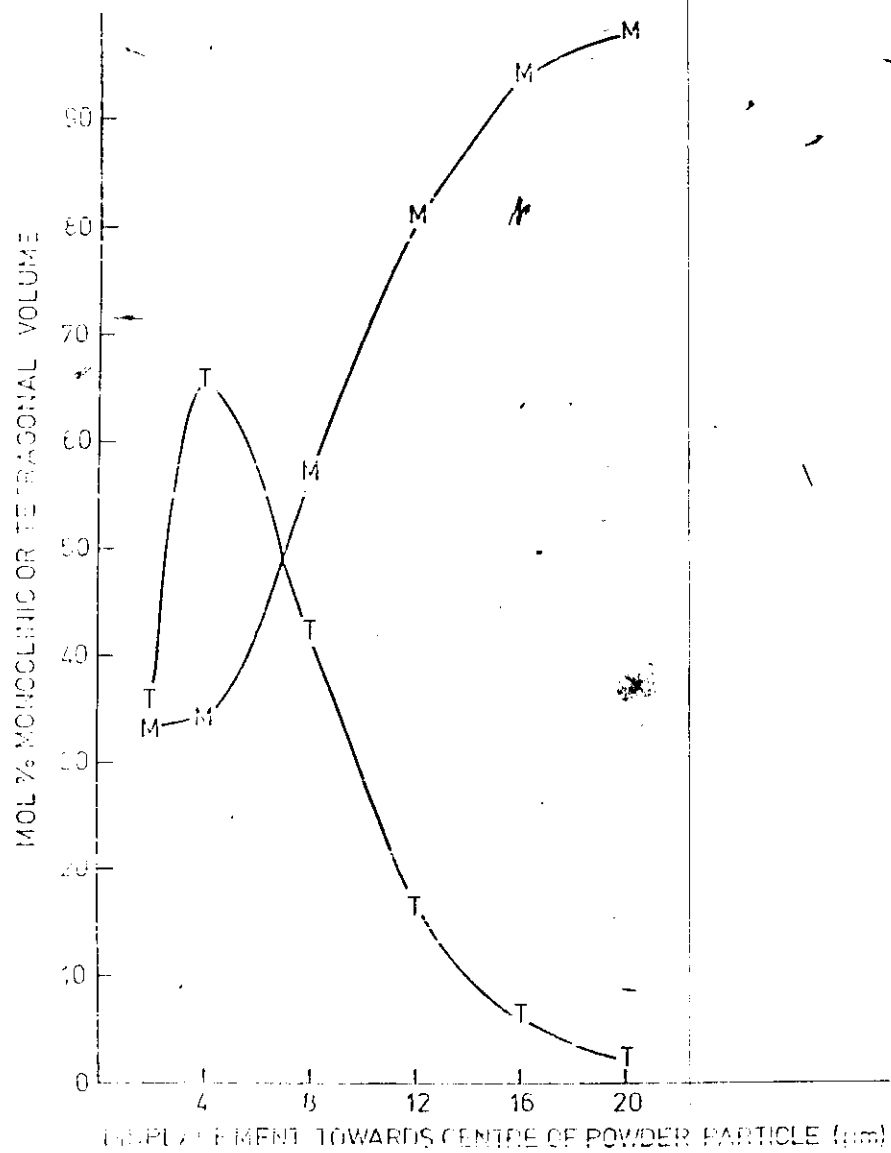
— *Journal of the American Medical Association*

[illegible]

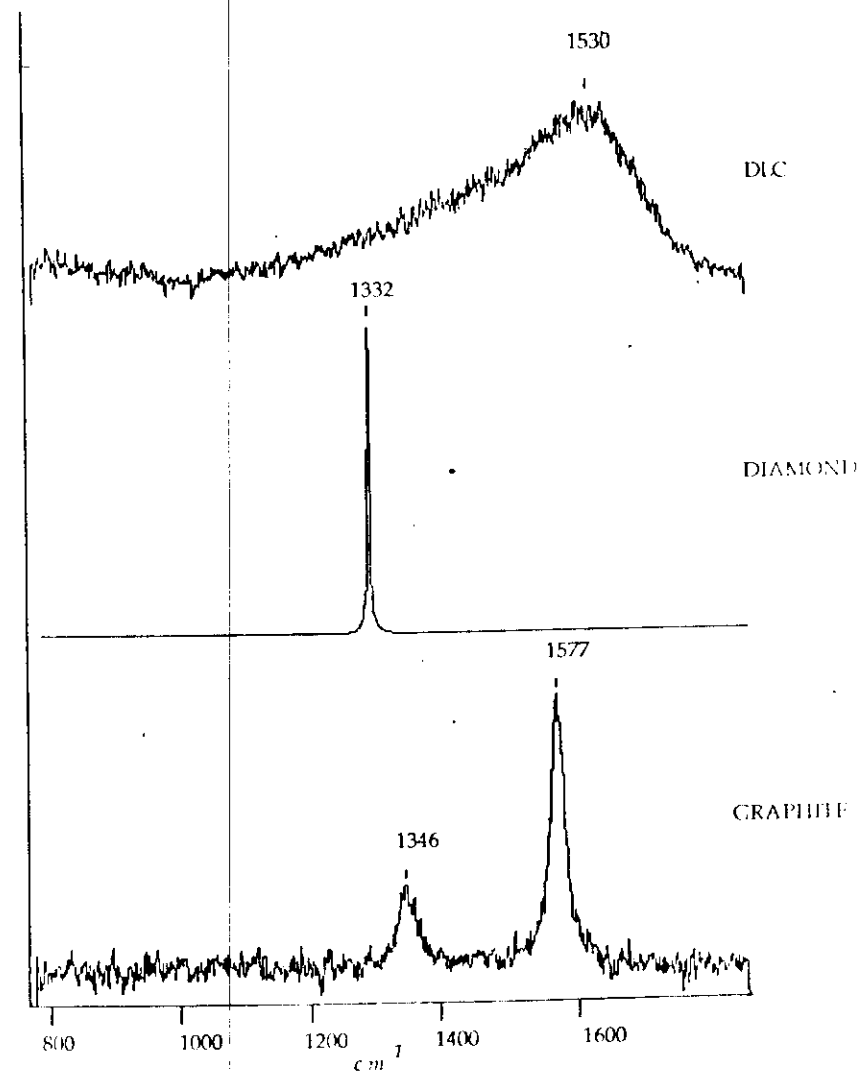
Summary



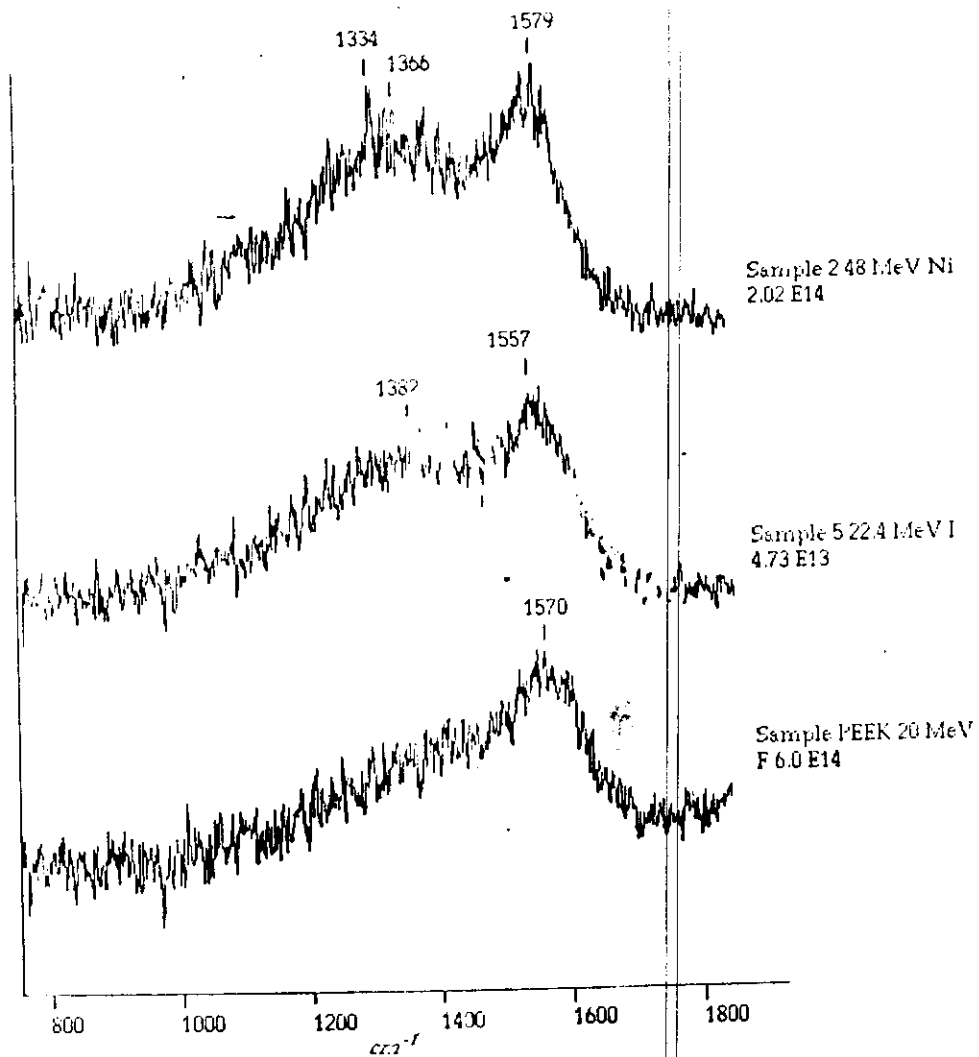




RAMAN ANALYSIS OF 10% WT Y_2O_3 SOL/GEL PRECURSOR FILM
 SHOWS THE RELATIVE PERCENTAGES OF MONOCLINIC AND
 TETRAGONAL PHASES BASED ON NORMALISED RAMAN
 SIGNALS OF THE 291 cm^{-1} (M) AND 381 cm^{-1} (T) BANDS.



Raman spectra of diamond, graphite and diamond like carbon
 'DLC'.



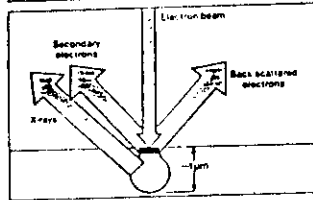
Raman spectra of irradiated polymers as a function of dose and energy, showing sp^2 and sp^3 and diamond sp^3 bonding.

ELECTRON PROBE MICROANALYSIS KEY POINTS

- quantitative elemental analysis for $Z > 4$ (WD) and $Z > 11$ (ED)
- better than 1 micron spatial and depth resolution
- point, line and image maps possible
- nominally non-destructive
- used in moderate vacuum
- almost all materials are suitable for EPMA

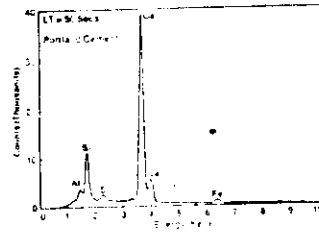
EMPA Electron Microprobe Analysis

PROCESS



AN EXAMPLE

EMPA is used to investigate elemental composition in solids eg. cements. Cement can be used for intermediate radioactive waste encapsulation.

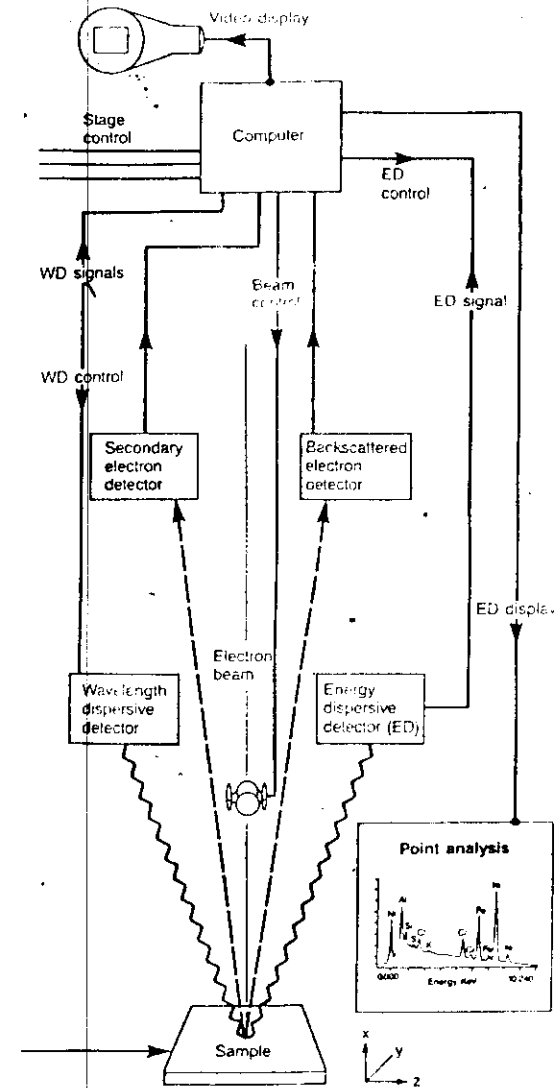


EMPA

A JEOL 8600 scanning microprobe

A CAMECA CAMEBAX scanning microprobe

- ☐ Fully quantitative analysis
- ☐ Generation of multi-element line scans
- ☐ Digital mapping of elemental distributions
- ☐ Automated feature detection



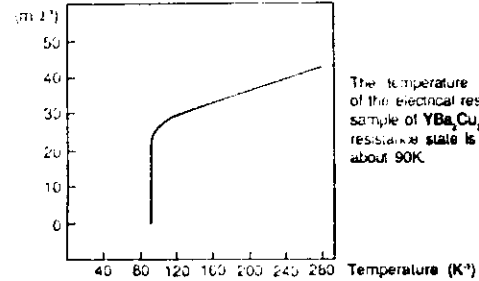
Schematic diagram of a Cameca Camebax electron microprobe

PROPERTIES OF SUPERCONDUCTORS

Zero Resistance

When superconductors are cooled below their critical temperature they have zero electrical resistance.

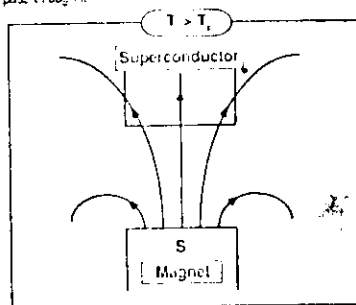
Resistance



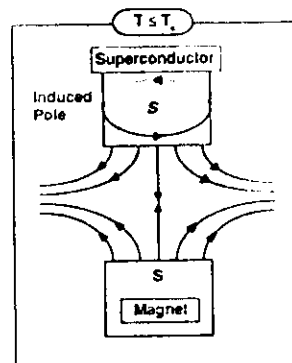
The temperature dependence of the electrical resistance of a sample of $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$ - a zero resistance state is achieved at about 90K.

The Meissner Effect

When the temperature (T) of a superconductor is above its critical temperature (T_c) an external magnetic field will pass through it.



When a superconductor is cooled below its critical temperature it exhibits perfect diamagnetism, it is repelled by a magnetic field.



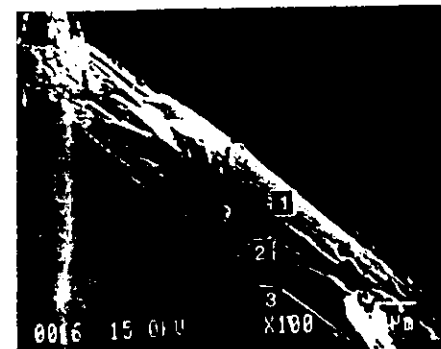
When a superconductor is cooled to its critical temperature, or below, it exhibits perfect diamagnetism - The Meissner Effect - an external magnetic field will induce an electric current to circulate within the superconductor. This circulating current generates a magnetic field in such a direction that it opposes the force that is creating it (Lenz's Law). As there is zero electrical resistance within the superconductor the induced magnetic field and the electric current will remain until the temperature of the superconductor is greater than its critical temperature. The external field and the induced magnetic field are in opposite directions and so repel each other, hence the levitation.



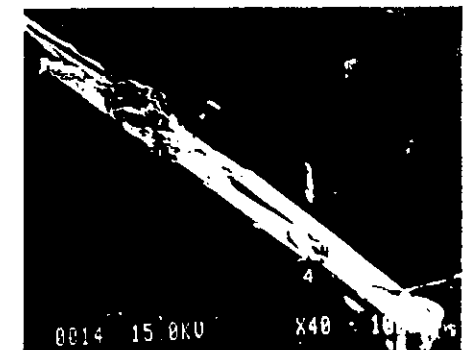
Sample 1



Sample 3



Sample 4

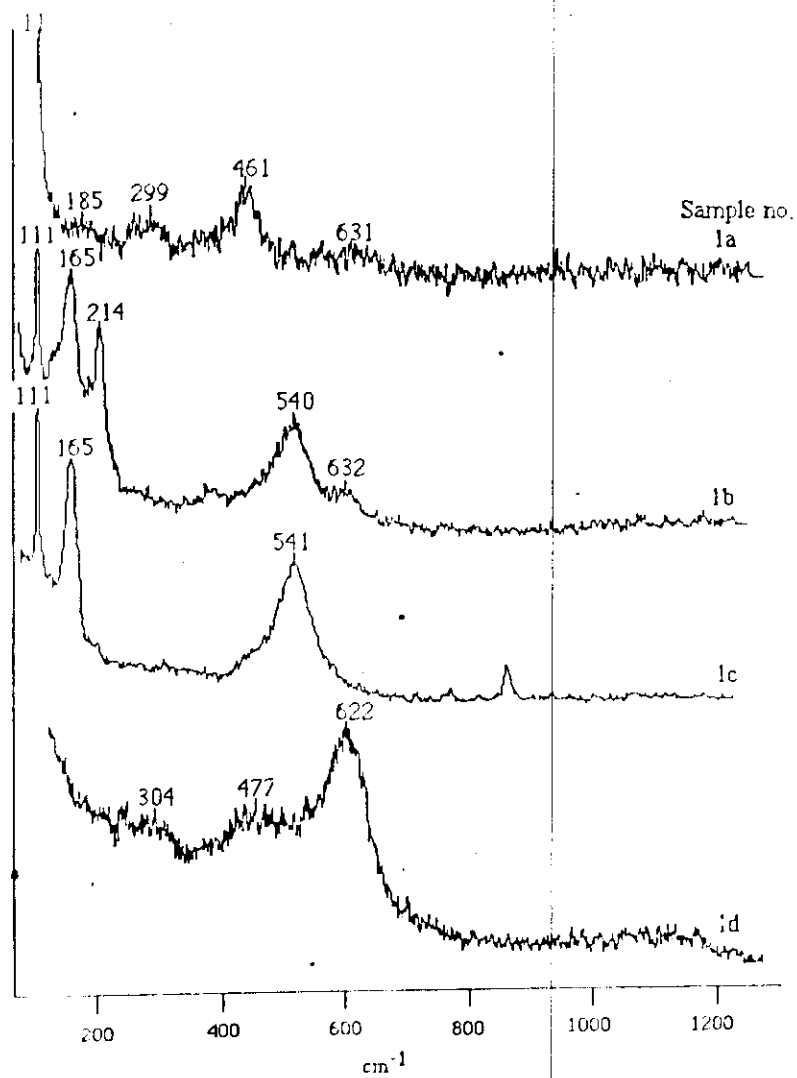


Sample 4

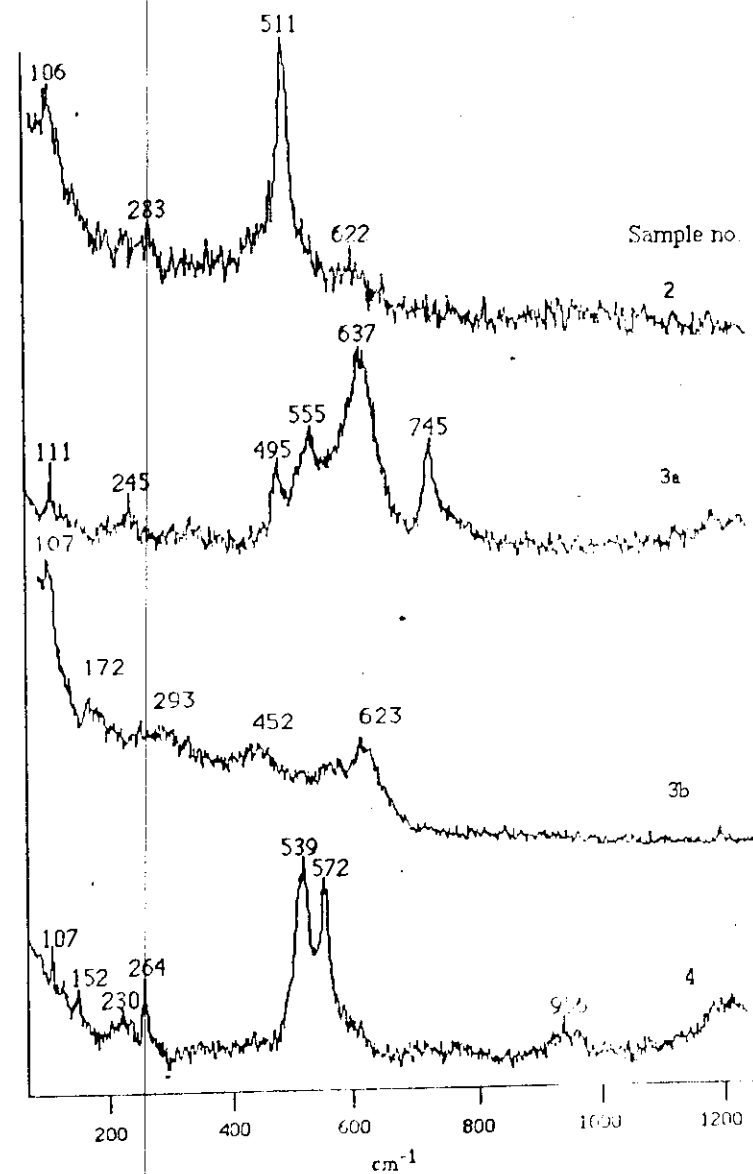


Sample 6

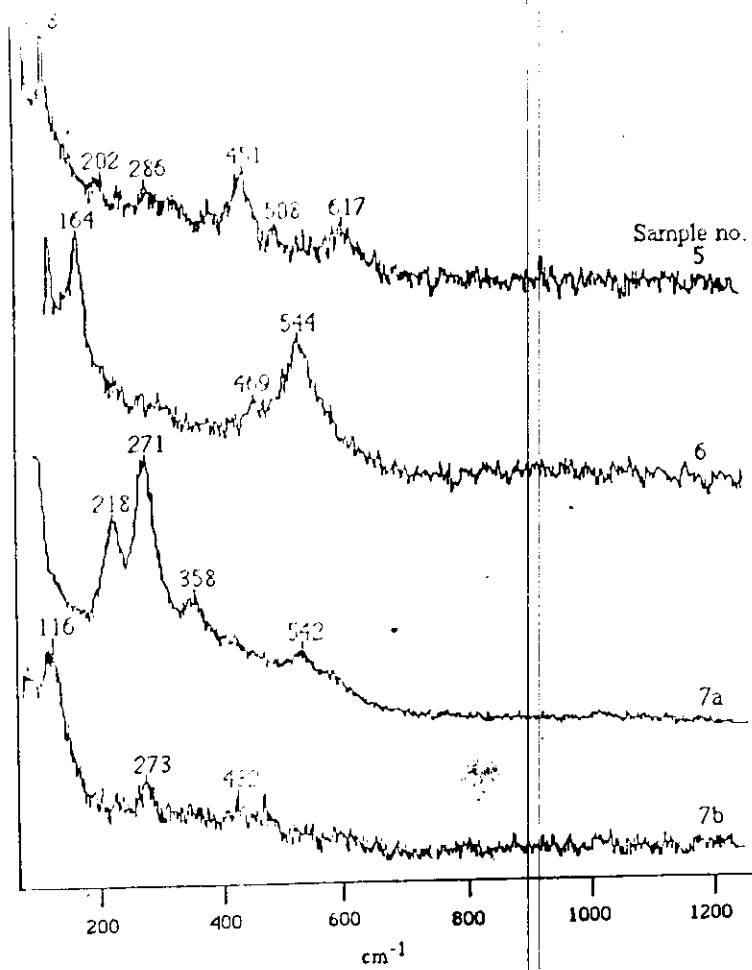
Secondary electron images of samples showing positions of EMPA measurements.



A single sample obtained from a CuO flux was analysed in four different positions. The Raman spectra from each position are significantly different.



Raman spectra of crystals 2, 3 and 4, obtained from CuO flux. Samples 3 and 4 were from the same batch, sample 2 from another.



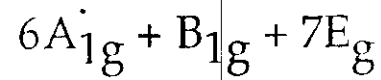
Raman spectra of three crystals obtained by growth from a KCl flux. Samples 6 and 7 were from the same batch whereas sample 5 was from a separate batch. Spectrum (b) from sample 7 was recorded with a defocused spot, averaging a larger area.

Table 1
Summary of results with chemical phases

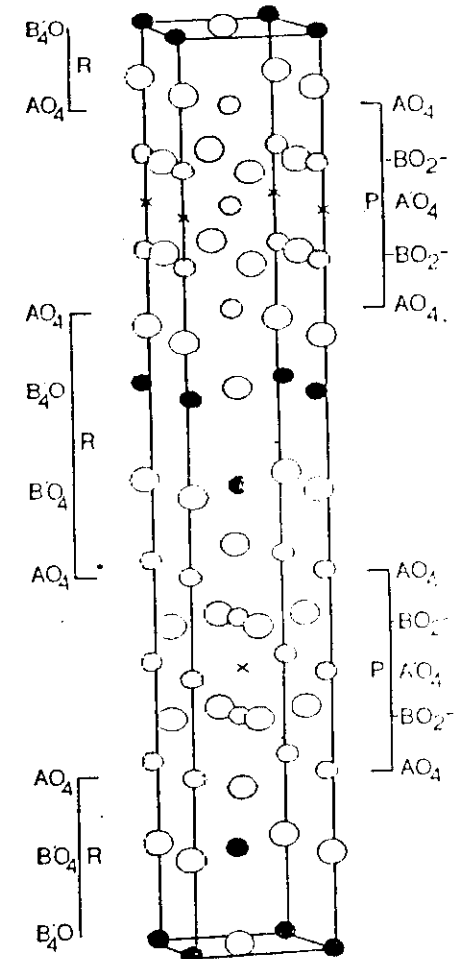
Sample no. / Point	EMPA Atom % Bi/Sr/Ca/Cu/O	Total w/%	Phase	RAMAN Sample no. / Point	Frequency (cm ⁻¹)
1/1	32:12:3:12:41	93	Bi ₂ Sr ₂ CaCu ₂ O ₈	1/a	113, 299, 461, 631
1/2	32:10:2:12:44	91		1/b	111, 165, 541
1/3	14:14:5:14:52	95		1/c	111, 165, 541
1/4	30:12:3:9:47	90		1/d	304, 477, 622
3/2	14:10:5:13:57	93	Bi ₂ Sr ₂ CaCu ₂ O ₈	3/b	107, 172, 293, 452, 623
3/3	14:14:5:14:52	95	Bi ₂ Sr ₂ CaCu ₂ O ₈		
3/4	18:17:7:18:40	93			
4/3	0:13:14:30:43	90	SrCaCu ₃ O ₄	4/a	107, 152, 230, 264, 539, 572, 956
4/4	0:16:15:33:37	92			
5				5/a	108, 451, 617
6/2	20:11:12:16:41	90		6/a	164, 544
7				7/a	218, 271, 358, 542
7				7/a	116, 273 (defocused)

-Group theory of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$

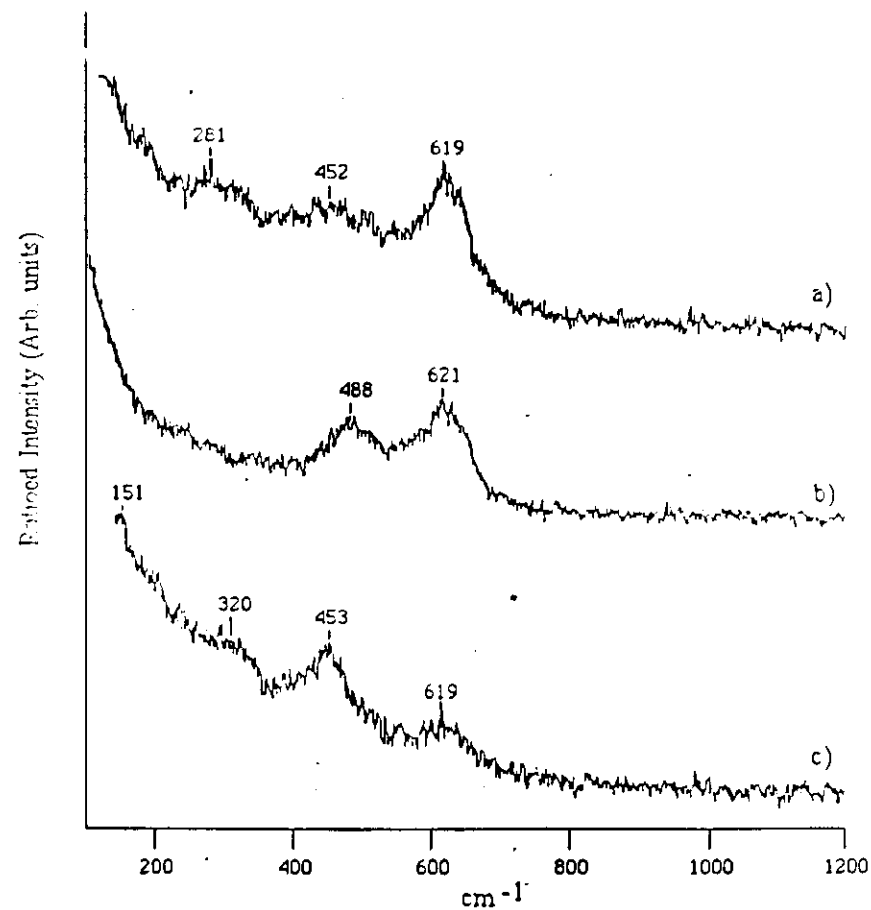
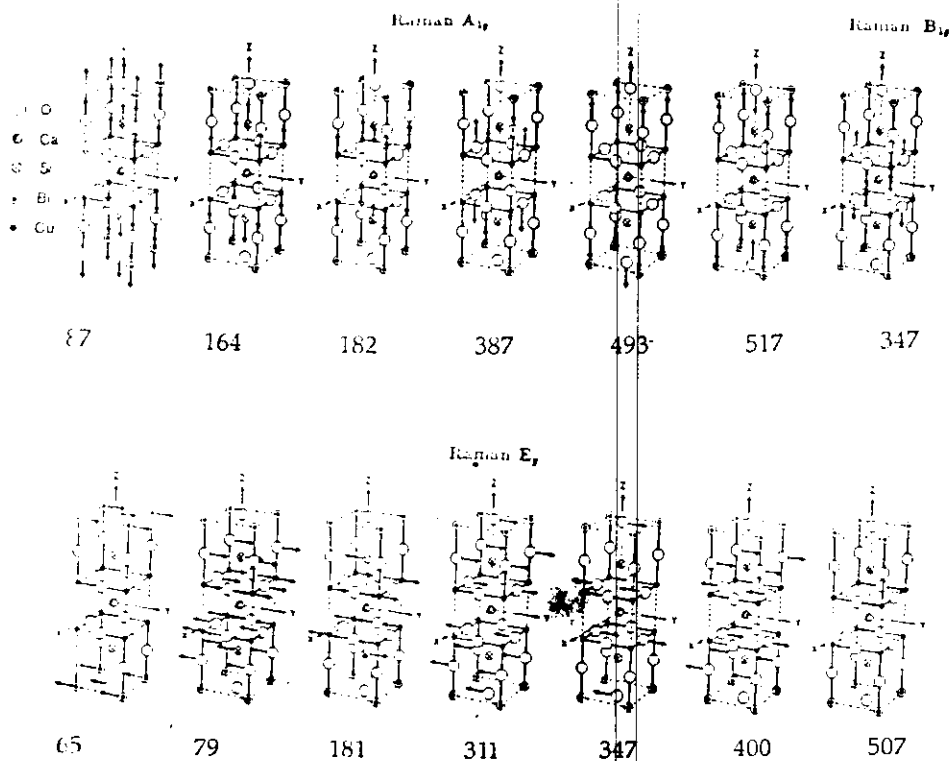
- Factor group- D_{2h}
- Symmetry- Distorted tetragonal
- Raman active vibrational modes-



- $A'(\text{Ca})$ ○
- $A(\text{Sr})$ ○
- $B'(\text{Bi})$ ●
- $B(\text{Cu})$ ○
- Oxygen ○
- oxygen vacancy ×



Structural unit cell of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$ showing perovskite octahedra (P) and rock salt octahedra (R)



Calculation of Raman- and infrared-active modes of $\text{Bi}_2\text{CaS}_2\text{Cu}_2\text{O}_8$

J. Prade,* A. D. Kulkarni, and F. W. de Wette
Department of Physics, University of Texas, Austin, Texas 78712

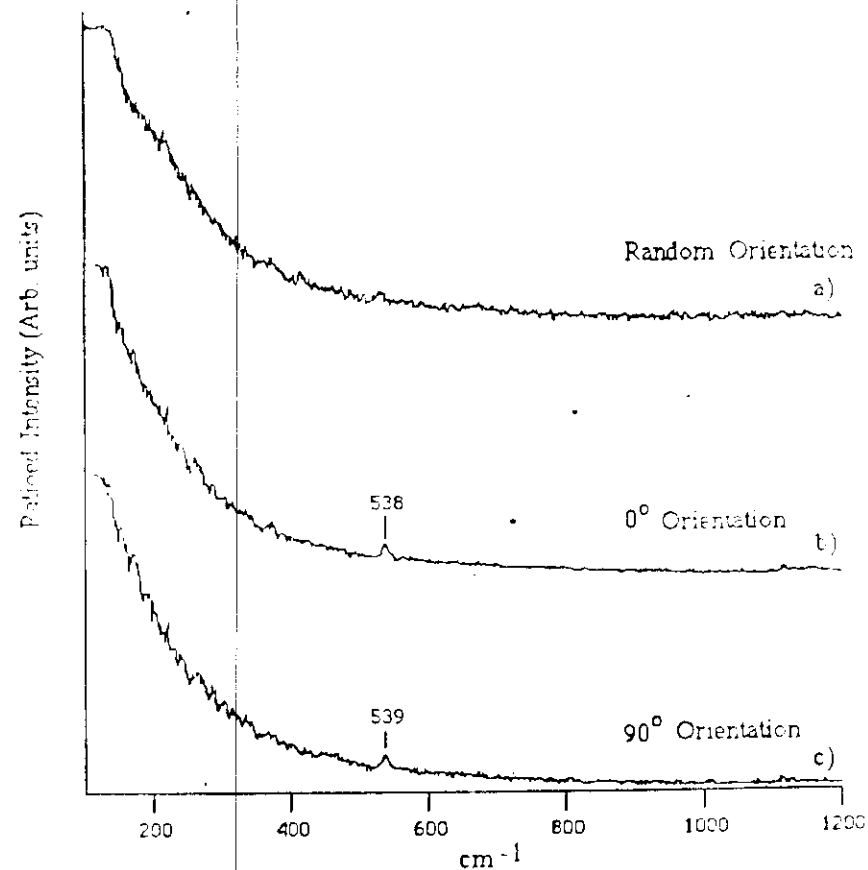
U. Schröder
Universität Regensburg, D-8400 Regensburg, Federal Republic of Germany

W. Kress
Max-Planck-Institut für Festkörperforschung, D-7000 Stuttgart 80, Federal Republic of Germany
(Received 6 September 1988)

Raman excitations observed after exposure to laboratory atmosphere of single crystal face. Curves (a), (b), (c) were obtained from different, but randomly chosen, locations.



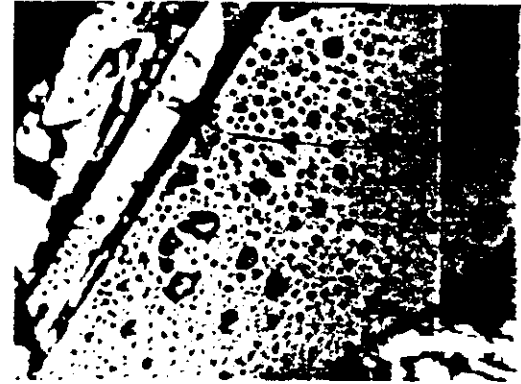
Micrograph of freshly cleaved crystallite face, analysed by Raman microscopy (length bar=80 μm).



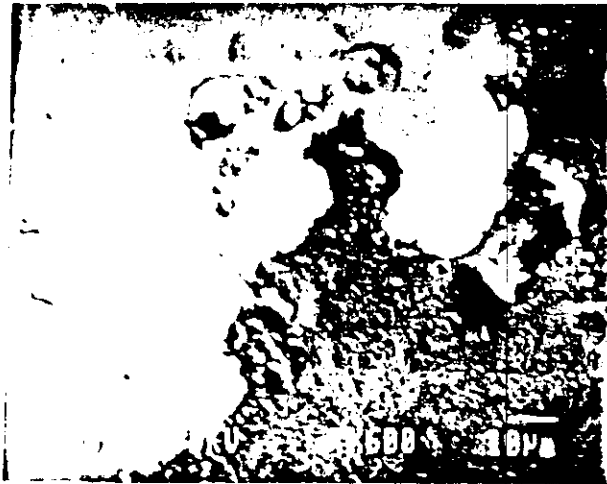
Raman spectra for a freshly cleaved single crystal at (a) random ab plane orientation, and (b) and (c) 90° rotation in the ab plane with respect to a crystal edge (see Figure 2).



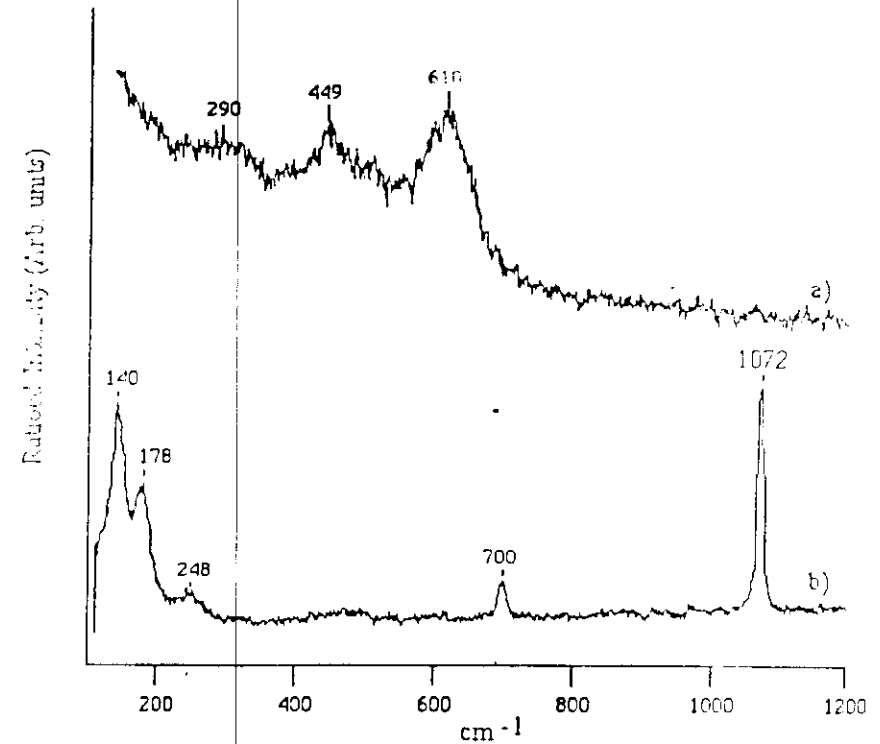
Micrograph of crystallite face after 0.5 hr
saturated steam attack.



Micrograph of crystallite face after 10 hrs
of saturated steam attack.



SEM image of crystallite face after 10hrs of saturated steam attack.



Raman features observed during the early (a) and late (b) stages of degradation by saturated steam.

THEORY OF RAMAN SCATTERING

$$\underline{P} = \underline{\alpha} \cdot \underline{e}$$

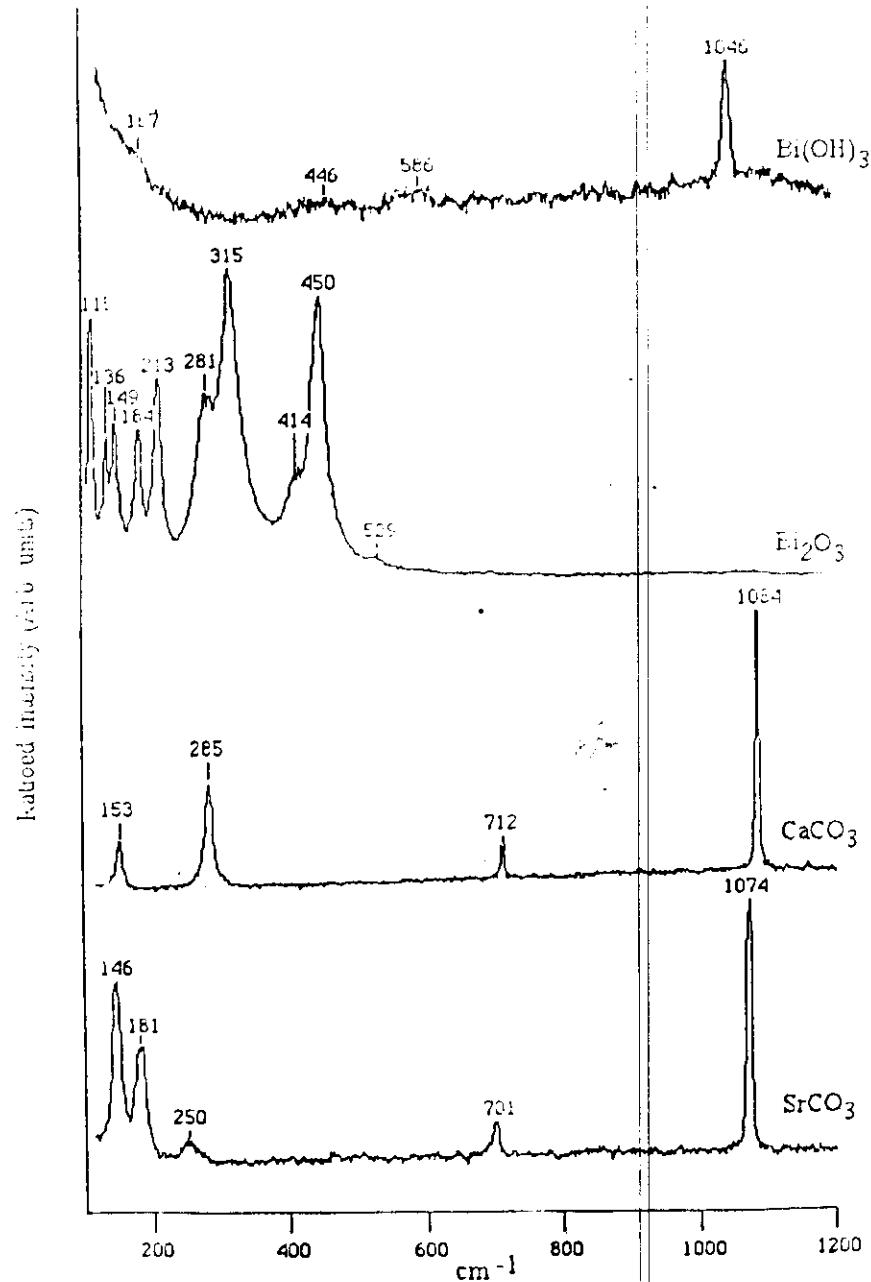
$\underline{P}$ induced dipole vector
 $\underline{\alpha}$ polarisability tensor
 $\underline{e}$ laser electric vector

Generally,,

x	a b c	x
y	d e f	y
z	g h i	z

-For phonon scattering, α is always symmetric

-Every vibrational mode has a particular scattering tensor, whose symmetry reflects that of the mode



The results of Raman analysis of model degradation compounds. The sharp feature at 1046 cm⁻¹ in the spectrum of Bi(OH)₃ is due to nitrate contamination.

EXPERIMENTAL DETAILS

- Align crystal with respect to laboratory axes and laser beam electric vector with respect to the Raman microscope

- PORTO notation defines the experiment:

A (B C) D

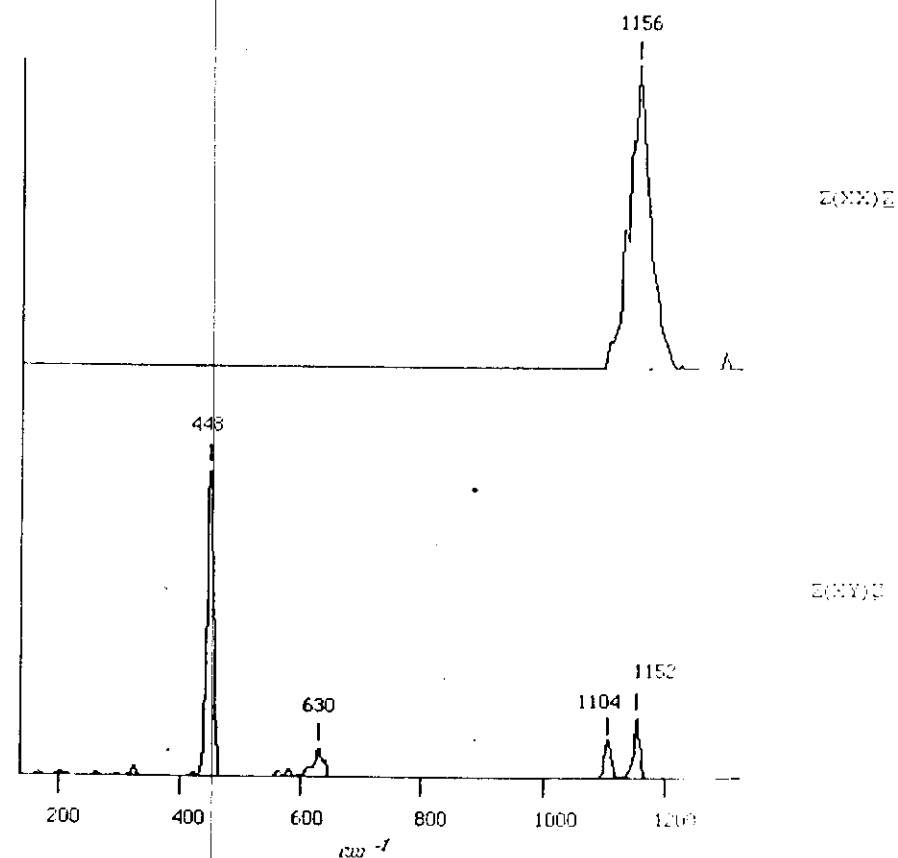
A- direction of incident laser beam

D- direction of collection of scattered light

B- polarisation of laser electric vector

C- polarisation of scattered light analyser

- We can now select the elements of the polarisability tensor detected and hopefully identify the Raman vibrations as specific modes.



Polarised Raman spectra of single crystal uranium dioxide. Porto notations show the experimental conditions.

URANIUM DIOXIDE

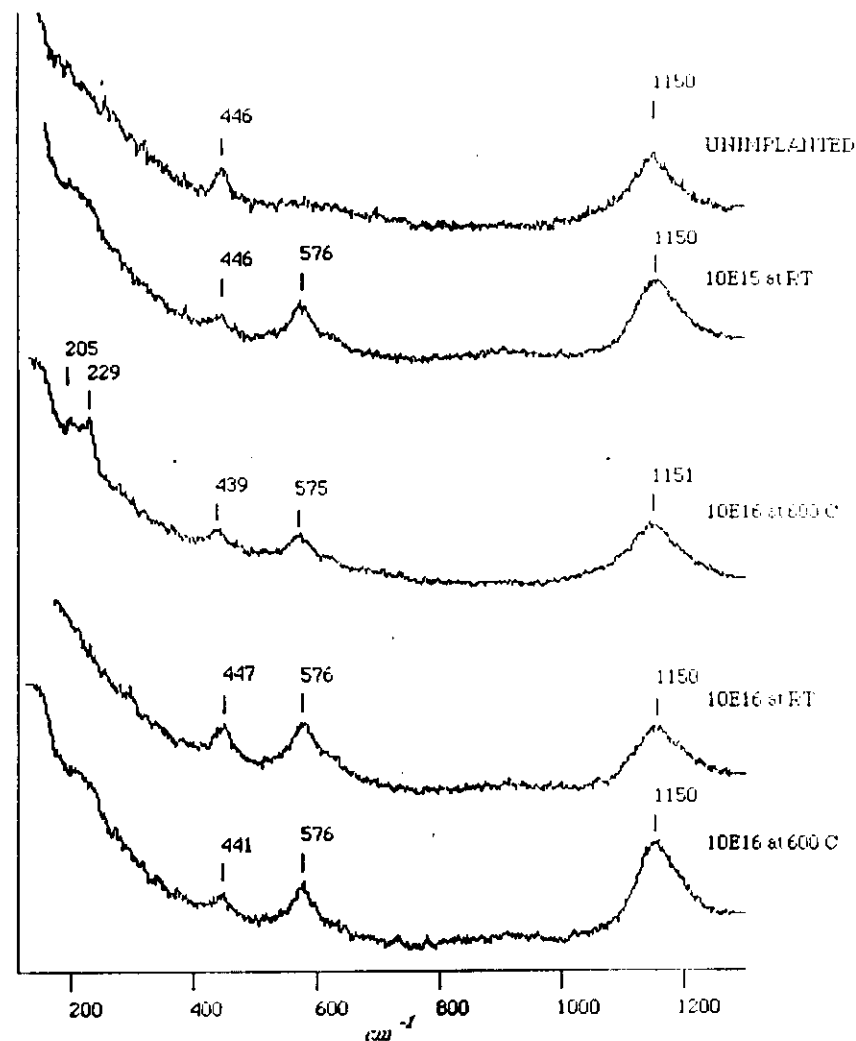
STRUCTURE: Fluorite

SPACE GROUP: O_h^5

Group theory : $T_{2g} + T_{1u}$ vibrational modes

Scattering tensor α :

$$T_{2g} = \begin{pmatrix} 000 & 00d & 0d0 \\ 00d & 000 & d00 \\ 0d0 & d00 & 000 \end{pmatrix}$$



Raman spectra of Kr ion implanted uranium dioxide pellets. Implantation was carried out at the indicated doses (cm^{-2}), at 200 KeV energy and at the temperatures given. The calculated range of the implant is 400 Å.

3. RESULTS

Figure 4 shows the measured dispersion curves for the symmetric directions $[001]$, $[110]$, and $[111]$, or, in group-theory notation (see Appendix 1), Δ , Σ , and A . The frequencies of some selected normal modes are given in Table I. The experimental uncertainty is generally ~ 2 or 3% in frequency, but may be considerably larger for the branches of highest frequency.

TABLE I
Frequencies of selected normal modes of vibration in uranium dioxide at 296°K (No space-group symbol is shown for the T_{1g} modes at $q = 0$ which are split by the macroscopic electric field)

Wave vector coordinates (q_x, q_y, q_z)	Mode	Frequency (units 10^3 c.p.s.)
(0, 0, 0)	(Longitudinal) T_{1g}	16.7 ± 0.60
	(Transverse) T_{2g}	13.4 ± 0.16
(0, 0, 1.0)	M_1	8.54 ± 0.11
	M_2	18.2 ± 1.0
	M_3	17.6 ± 0.21
	M_4	6.98 ± 0.12
	M_5	5.27 ± 0.08
	M_6	5.27 ± 0.08
(0, 0, 0.5)	$T_{1g}(1)$	10.8 ± 0.7
	$T_{1g}(2)$	14.0 ± 0.5
	$T_{2g}(1)$	9.8 ± 0.29
	$T_{2g}(2)$	1.43 ± 0.11
	$T_{2g}(3)$	4.04 ± 0.07
	$T_{2g}(4)$	4.22 ± 0.16
(0.5, 0.5, 0.5)	T_{1g}	17.2 ± 1.2
	T_{2g}	12.6 ± 0.4
	T_{3g}	13.2 ± 0.4
	T_{4g}	10.57 ± 0.25
	T_{5g}	8.23 ± 0.10
	T_{6g}	2.73 ± 0.04

It is interesting to note that the longitudinal acoustic ($\Delta_1(A)$) and the longitudinal optic (Δ_1') branches are accidentally degenerate at the zone boundary (M) within the limits of experimental error, a fact which impeded precise frequency measurements in this region.

The steeply rising Δ_1' branch shows that there is no gap in the frequency distribution between the optic and the acoustic modes such as one might expect as a result of the large difference in mass between oxygen and uranium. Detailed calculations of the distribution (Fig. 5, Section 4) show that there is probably no gap in any part of the frequency spectrum.

The initial slopes of the acoustic branches are consistent with independent measurements of the elastic constants (Wachtman *et al.* 1965), and the frequencies of the TO and LO modes at $q = 0$ are consistent with the measured static (Priggs 1964) and high-frequency (Ackermann *et al.* 1959) dielectric constants (ϵ_0 and ϵ_∞ respectively) through the relation (Lyddane *et al.* 1941)

$$(3) \quad \left(\frac{\rho v_{LO}^2}{\rho v_{TO}^2} \right)_{q=0} = \frac{\epsilon_0}{\epsilon_\infty}$$

446 cm⁻¹
RAMAN T_{2g} mode

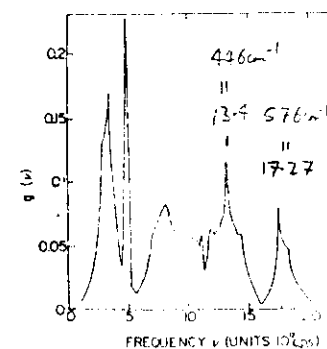


Fig. 5. The frequency distribution function calculated from the best-fit shell model (Model III). The statistical fluctuations in the curve (which are, in fact, a histogram) are too small to be shown in this figure.

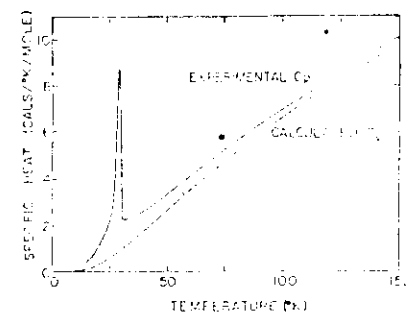


Fig. 6. The measured total specific heat C_p and the calculated lattice specific heat C_l of UO_2 . The observed anomaly at 30°K is due to antiferromagnetic ordering.

measurements. A surprising feature, as shown by Fig. 6, is the magnitude of the magnetic specific heat above the antiferromagnetic ordering temperature, T_a . This suggests that there is considerable short-range magnetic order well above T_a . The contribution of the normal modes to the entropy at 298.16°K is calculated to be 16.12 cal/°K mole, whereas that measured by Jones *et al.* (1952) is 18.63 cal/°K mole. The discrepancy between the calculated specific heat, C_v , and the measured C_p at 250°K is 0.60 cal/°K mole. This discrepancy probably arises from the difference between C_p and C_v , the antiferromagnetic contribution to the specific heat, and the errors in the measurements of the

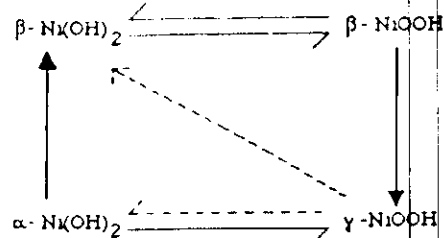


FIG. 1. Nickel oxyhydroxide electrode reaction scheme.

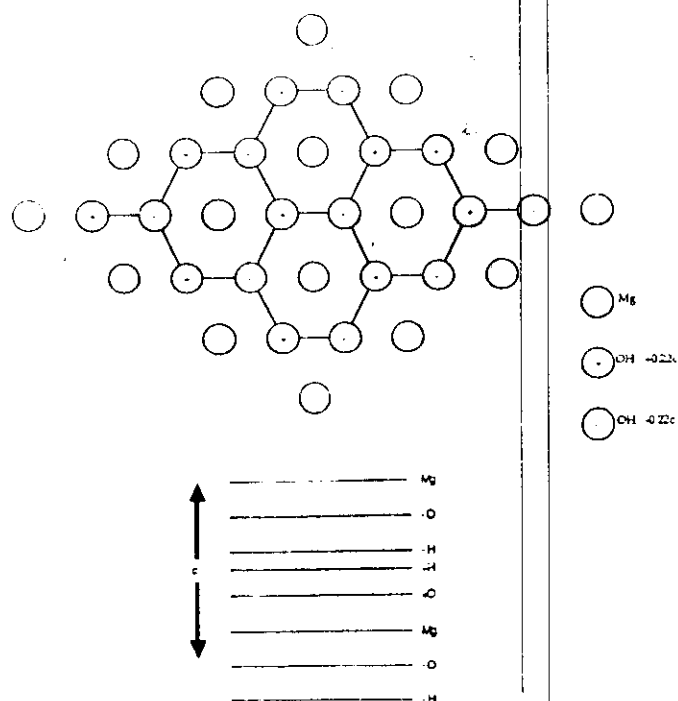
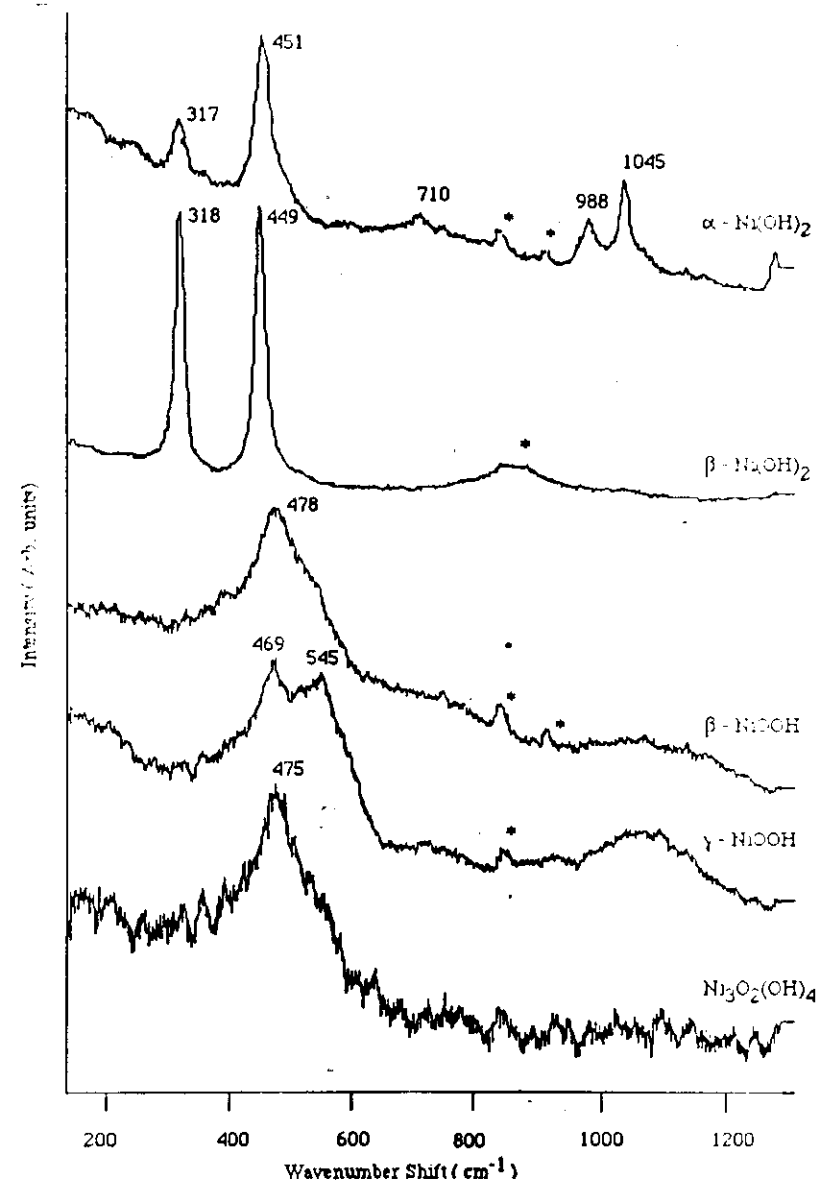
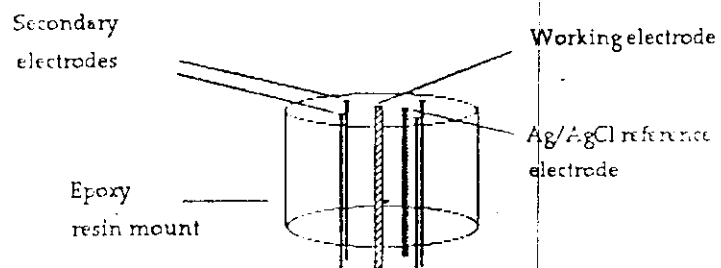


Fig. 2. Graphical representations of the common Bragg structure $M_2(OH)_2$ showing the hexagonal arrangement of the hydroxyl ions around the metal ion and the layer structure.

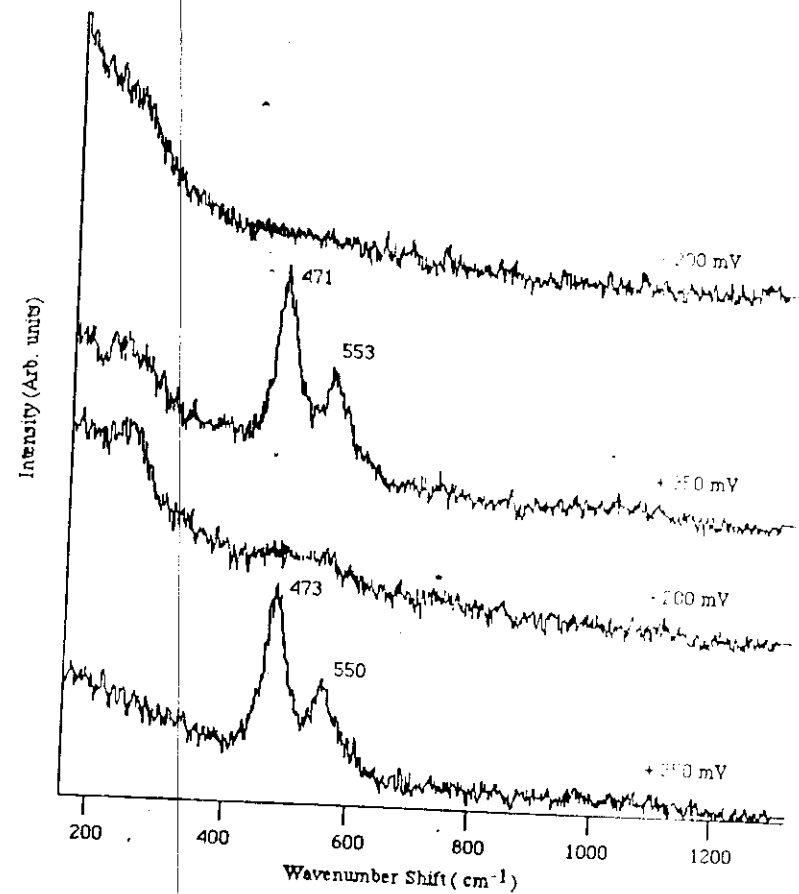


Raman spectra obtained from the reference compounds
 α - $\text{Ni}(\text{OH})_2$, β - $\text{Ni}(\text{OH})_2$, β - NiOOH , γ - NiOOH
 and $\text{Ni}_3\text{O}_2(\text{OH})_4$ * LRM objective bands.

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Electrochemical cell for insitu Raman measurements



Raman spectra obtained from the surface of a cycled Nickel oxyhydroxide electrode (NOE) with an electrolyte of 8 M KOH (aq).

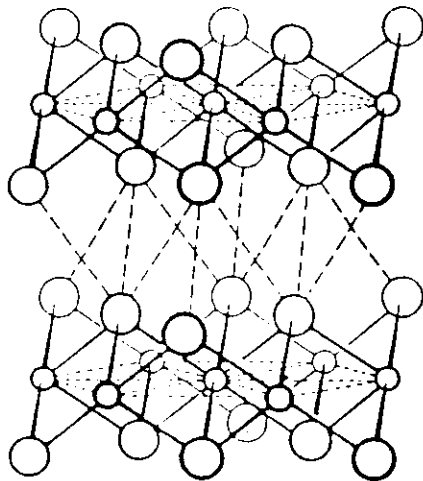


FIG. 9. Portions of two layers of the CdI₂ structure. The small circles represent the metal atoms.

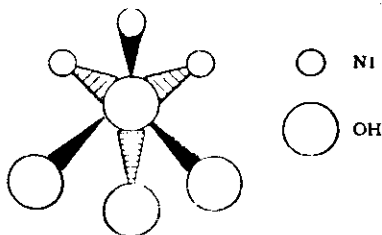


FIG. 10. Unit cell derived from the CdI₂ structure.

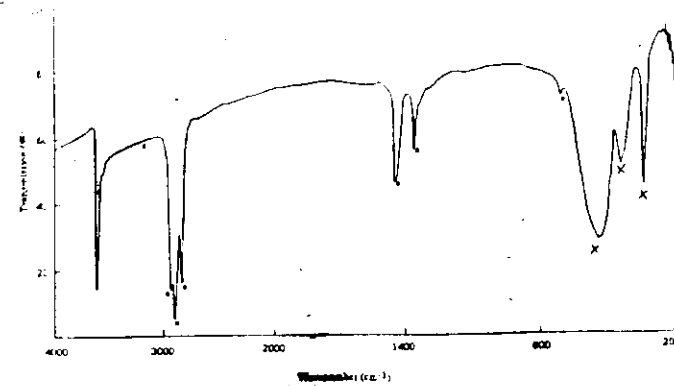


FIG. 5. Infrared spectrum of β -Ni(OH)₂. (x) Bands due to nujol.

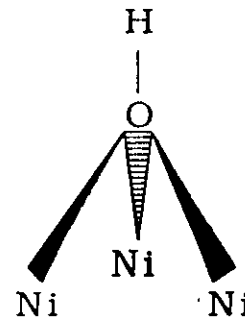


FIG. 11. The spectroscopic unit cell.

C_{3v}	E	$2C_3$	$3C_2$	
A_1	1	1	1	z
A_2	1	1	-1	R_z
E	2	-1	0	$(x, y) (R_x, R_y) (x^2 - y^2, xy) (xz, yz)$

This gives the reducible representations, χ^d :

C_{3v}	E	$2C_3$	$3C_2$
χ^d_{All}	15	0	3
χ^d_{Trans}	3	0	1
χ^d_{Rot}	3	0	-1

This reduces to give the irreducible representation, Γ :

$$\Gamma_{\text{All}} = 4A_1 + A_2 + 5E$$

$$\Gamma_{\text{Rot}} = A_2 + E$$

$$\Gamma_{\text{Trans}} = A_1 + E$$

Now,

$$\Gamma_{\text{All}} = \Gamma_{\text{Vib}} + \Gamma_{\text{Rot}} + \Gamma_{\text{Trans}}$$

$$\rightarrow \Gamma_{\text{Vib}} = 3A_1 + 3E$$

TABLE IV. Mode assignments for Raman and infrared bands of β -Ni(OH)₂.

Frequency (cm ⁻¹)	Activity	Symmetry type	Assignment
3630	IR	A_1	Asymmetric ν_{OH}
3580	IR, Raman	A_1	Symmetric ν_{OH}
553	IR	E	Deformation δ_{OH}
450	IR, Raman	A_1	ν_{NiO}
350	IR	E	OH libration
318	Raman	E	Ni OH lattice