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**SUMMER SCHOOL IN HIGH ENERGY PHYSICS AND COSMOLOGY**

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NEUTRINO PHYSICS

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Please note: These are preliminary notes intended for internal distribution only.

# Neutrino Physics

- role of neutrinos
- Historical Introduction
- Neutrinos as a Test of The standard electroweak model
- Neutrinos as a probe of The nucleon, QCD, CKM
- Intrinsic Properties
  - motivations
  - basic properties
  - neutrino counting
  - electromagnetic moments
  - mass models, mixing
    - laboratory
    - solar neutrinos
    - cosmology, decay
    - 17 keV

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School on High Energy  
Physics and Cosmology  
ICTP, Trieste 7/92

## Role of Neutrinos in particle physics, astrophysics, cosmology

- neutrinos central to most studies of weak interactions
  - $\Rightarrow$  { Fermi Theory ( $\beta$  decay)  
electroweak theory,  $m_\pi$  (WNC)
- sensitive probe of new physics:
  - $\beta, \mu$ , decay
  - WNC scattering
  - $\nu$  mass
- probe of structure of nucleon, QCD
- cosmology/astrophysics
  - $\nu$  ( $300/\text{cm}^3$ ) and  $\bar{\nu}$  ( $400/\text{cm}^3$ ) are most numerous inhabitants of Universe
  - Hot dark matter ( $m_\nu = 0(10 \text{ eV})$ )
    - $\Rightarrow$  most of energy density
  - Solar  $\nu$ : probes center of sun and  $\nu$  properties
  - Supernova: 99% of energy emitted in  $\nu$ 's
  - nucleosynthesis:
    - primordial:  $N_\nu \Rightarrow \frac{^4\text{He}}{\text{H}}$  ratio
    - heavy elements (stars, SN)
      - $\leftrightarrow$  weak transitions

## 2st of standard model:

- U. Amaldi et al., PRD 36, 1385 (1987)
- P.L., A. Mann, M. Luo, RMP 64, 87 (92)
- "W and Z Physics" in "TeV Physics" ed. T. Huang et al (Gordon & Breach, 1991)

## neutrino mass (General)

- "Neutrino mass", in "Testing The Standard Model" (TASI-90) ed M. Cretic, PL (World, 1991)
- "Scenarios For Neutrino mass", UPR-0511 T

## star v

- S.A. Bludman et al., UPR-0516 T, PRD 45, 1810 (92); Nucl. Phys. B373, 498 (92)
- M. Cretic and PL, UPR-0505 T

## 2 keV

- D.O. Caldwell and PL, PRD 44, 823 (91)

## Weak Interactions

- $\beta$  decay (1896)
- neutrino (Pauli 1931)

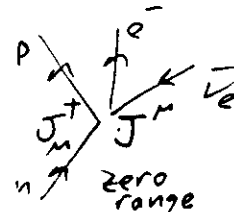
$\nu_e$  Reines, Cowan, 1953

$\nu_\mu$  Lederman, Schwartz, Steinberger, 1962

$\nu_\tau$  ? ( $\tau^-$ : 1975)

## - Fermi Theory (1933)

$$H = \frac{G_F}{\sqrt{2}} J_\mu^+ J_\mu^-$$



$$J_\mu^+ \sim \bar{p} \gamma_\mu n + \bar{\nu}_e \gamma_\mu e^-$$

$n \rightarrow p, e^- \rightarrow \nu_e$

$$J_\mu^- \sim n \gamma_\mu p + e^- \gamma_\mu \nu_e$$

$p \rightarrow n, \nu_e \rightarrow e^-$

$$G_F = 1.17 \times 10^{-5} \text{ GeV}^{-2}$$

[Fermi Constant]

## - modified to include:

- $\mu, \tau$
- strangeness (Cabibbo)
- quark model
- heavy quarks (CKM)
- parity violation (V-A) Lee, Yang, Wu ...
- correctly describes
  - $\mu, \tau$  decay
  - $B, K$ , hyperon, heavy quark dec.
  - $\nu_{\mu e} \rightarrow \mu \nu_e, \nu_\mu n \rightarrow \mu p, \nu_\mu N \rightarrow \mu X$

However, Fermi Theory violates unitarity at high energy

$$\sigma(\nu_e e^- \rightarrow e^- \nu_e) \rightarrow \frac{G_F^2 s}{\pi}$$

$s \equiv E_{cm}^2$

Pure S-wave:

unitarity  $\Rightarrow \sigma < \frac{16\pi}{s}$

- Fails for

$$\frac{E_{cm}}{2} = \frac{\sqrt{s}}{2} \gtrsim \sqrt{\frac{\pi}{G_F}} \approx 500 \text{ GeV}$$

- higher order terms don't help

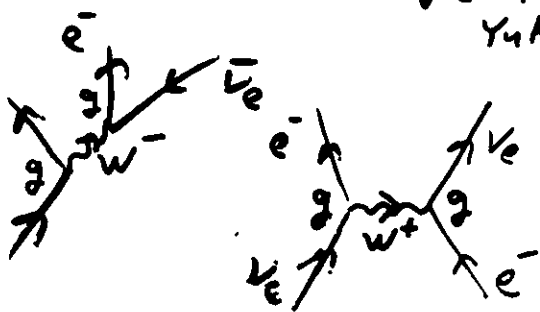
- divergent integral

$$\int d^4k \frac{k + m_e}{k^2 - m_e^2} \frac{k}{k^2}$$

- non-renormalizable

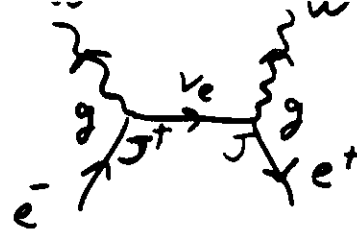
## Intermediate Vector Boson Theory

Yukawa 1935, Schwinger 1957



$$\frac{G_F}{\sqrt{2}} \sim \frac{g^2}{8m_W^2} \gg |Q|$$

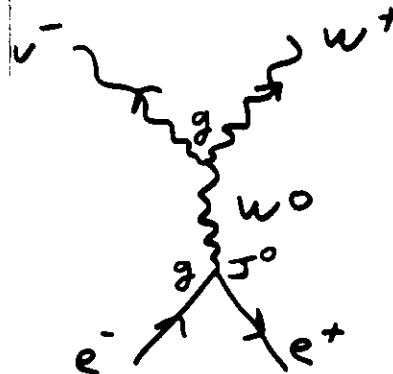
-  $\nu_e e^- \rightarrow \nu_e e^-$  better behaved [not S-wave]



- however,  $e^+e^- \rightarrow W^+W^-$  violates unitarity for  $\sqrt{s} \geq 500 \text{ GeV}$

-  $A_\mu \sim \frac{k_\mu}{m_W}$  for longitudinal polarization  
- non-renormalizable

Can Cancel:



- introduce  $W^0$   
- Fixes  $W^0 W^+ W^-$  and  $e^+e^- W^0$  vertices

$$[J, J^\dagger] \propto J^0$$

$\Rightarrow$  Gauge Theory couplings ( $SU_2$ )  
- not realistic

Glashow Model (1961):

-  $W^\pm, Z, \gamma$   
- no mechanism for  $m_W, m_Z$

Weinberg, Salam (1967):

- applied Higgs mechanism  $\Rightarrow m_W, m_Z$

Renormalizable (1971) (by Hooft, ...)

Flavor-Changing Neutral Current:

- GIM mechanism (c quark)

weak neutral current discovered 1973  
 $W, Z$  discovered 1983

$\nu_e, \nu_\mu, \nu_\tau$  and  $\nu_s$

# Weak Neutral Current

- weak neutral current: primary test of unification part of  $SU_2 \times U_1$
- ) mid 1970's: successful prediction of  $SU_2 \times U_1$  discovery: 1973 Gargamelle
- ) late 1970's: 2nd generation experiments  $\Rightarrow$  "model independent" fits  $\Rightarrow SU_2 \times U_1$  correct to 1st approximation
- ) 1980's: 3rd generation experiments  $\Rightarrow$  stringent limits on new physics rough test of rad. corrections

pure weak:  $\begin{cases} \nu N \rightarrow \nu X \\ \nu p \rightarrow \nu p, \nu N \rightarrow \nu \pi X \\ \nu e \rightarrow \nu e \end{cases}$

weak-elm interference:  $\begin{cases} e^+ e^- \rightarrow e^+ e^- \\ \text{atomic parity violation} \\ e^+ e^- \rightarrow e^+ e^- \mu^+ \mu^-, \tau^+ \tau^-, c\bar{c}, b\bar{b} \end{cases}$

1989 - 1990's ultrahigh precision  $Z$ -pole physics LEP (SLC)  
 $M_W, M_Z, \Gamma_Z, \Gamma_{\ell\ell}, \Gamma_{had}, N_{\nu}, A_{FB}, A_{pol}(\tau)$   
 later  $A_{LR}, A_{FB}^{pol}; M_W; A_{pol}^{\nu}; R_L; \dots$

# Neutrinos as a Test of The standard Electroweak model

- WNC discovered in  $\nu N \rightarrow \nu X, \nu e \nu e$
- primary quantitative test of WNC prior to LEP
- $\Rightarrow$  uniqueness of  $SU_2 \times U_1$ ;  $\sin^2 \theta_W$ ;  $m_X$  limit ( $\nu N \rightarrow \nu X$  very sensitive)

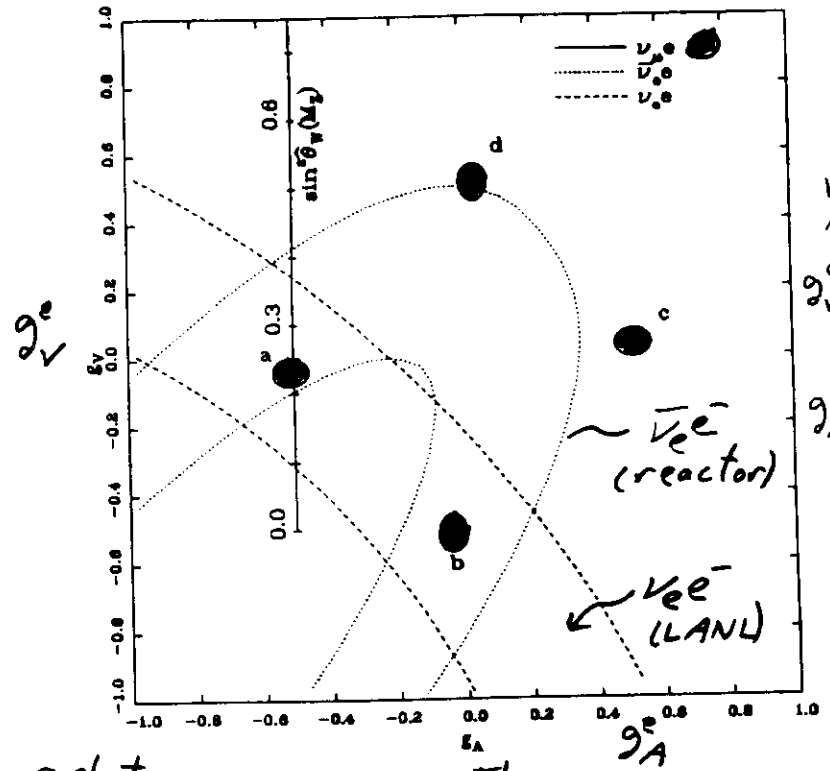
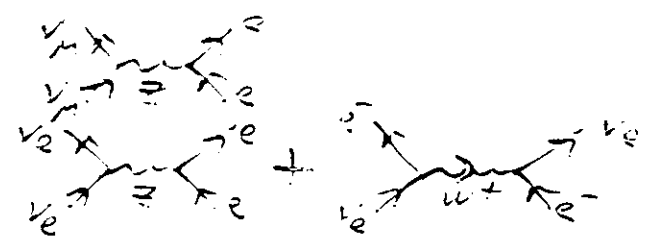
## Present/Future

$\Delta \sin^2 \theta_W|_{\nu N} \sim 0.005 \rightarrow 0.002$   
 (present; mainly theory  $\nu(d,s) \rightarrow \mu^+ c$ )  
 - FNAL  
 - higher energy/c  
 - new beam ( $10^6$  kg)  
 - higher intensity

$\sin^2 \theta_W$  not competitive with LEP ( $\Delta \sin^2 \theta_W|_{m_2} \sim 0.0003$  for fixed  $m_X, m_H$ )

- but
- (1)  $\nu N \rightarrow \nu X$  still useful in  $m_X$  limit
  - (2) still sensitive to new physics (eg  $Z'$ ) (LEP only sensitive to  $Z$  properties)

$$\begin{aligned} \nu_\mu e^- &\rightarrow \nu_\mu e^- \\ \nu_e e^- &\rightarrow \nu_e e^- \end{aligned}$$



arbitrary gauge theory

$$-L^{\nu e} = \frac{G_F}{\sqrt{2}} \bar{\nu} \gamma^\mu (1-\gamma^5) \nu \bar{e} \gamma_\mu [g_V^e - g_A^e \gamma^5] e$$

$$SU_2 \times U_1: \quad \begin{aligned} g_V^e &\sim -\frac{1}{2} + 2 \sin^2 \theta_W \\ g_A^e &\sim -\frac{1}{2} \end{aligned}$$

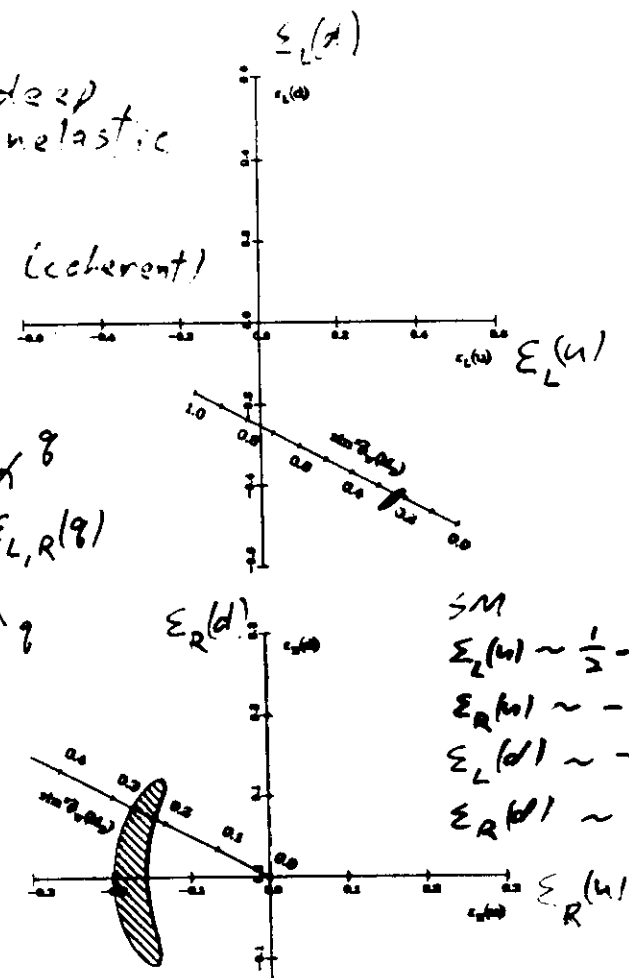
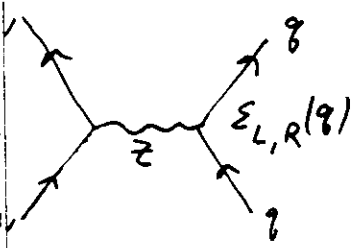
$$\sigma_{\nu \bar{\nu} e}^{NC} \simeq \frac{(\frac{1}{2} m_e E_\nu)}{2\pi} [(g_V^e + g_A^e)^2 + \frac{1}{3} (g_V^e - g_A^e)^2]$$

$$\nu_e e^-: \quad g_{V,A}^e \rightarrow g_{V,A}^e + 1$$

$$\begin{aligned} \nu N &\rightarrow \nu X \\ \nu p &\rightarrow \nu X \\ \nu n &\rightarrow \nu X \\ \nu p &\rightarrow \nu p \end{aligned} \quad \left. \begin{array}{l} \text{deep} \\ \text{inelastic} \end{array} \right\}$$

$$\nu N \rightarrow \nu \pi^0 N \text{ (coherent)}$$

pure NC



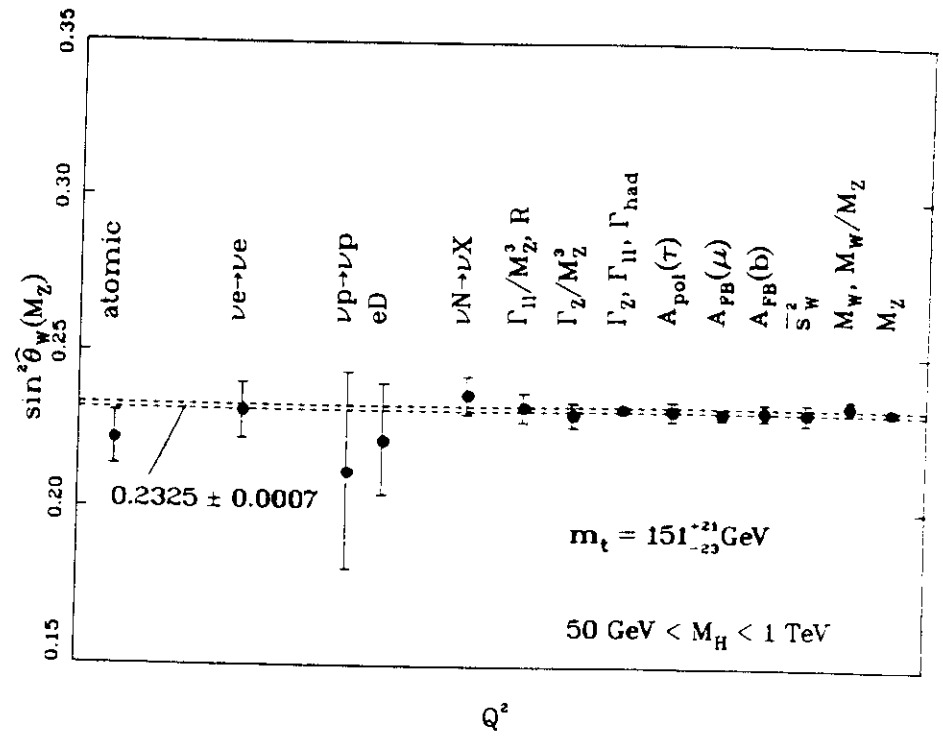
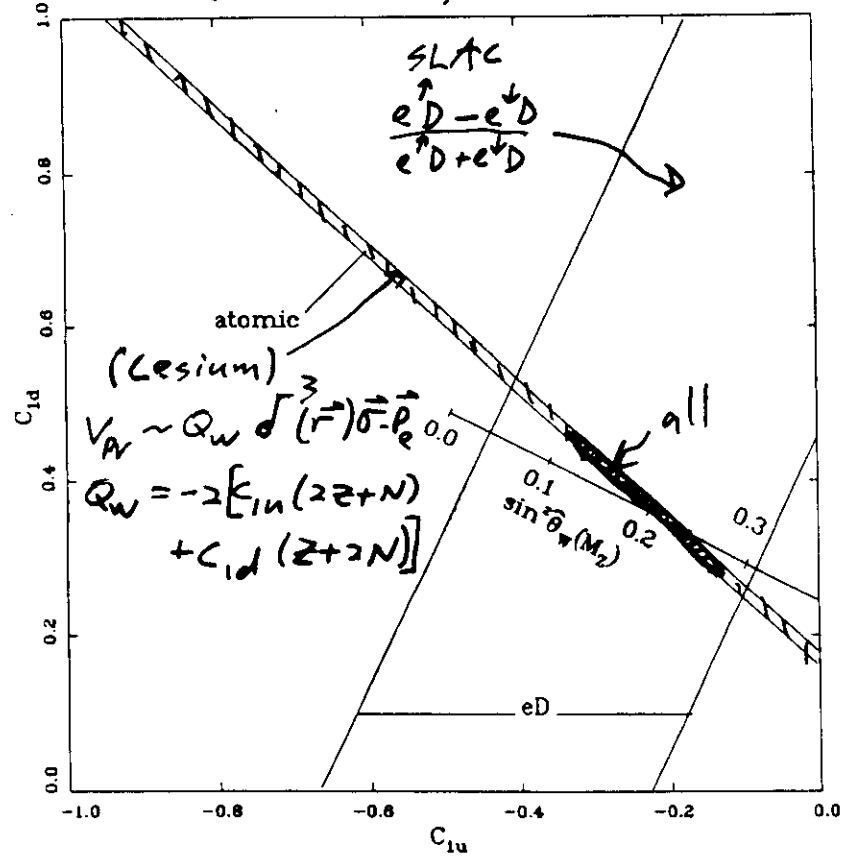
arbitrary gauge theory:

$$-L^{\nu N} = \frac{G_F}{\sqrt{2}} \bar{\nu} \gamma^\mu (1-\gamma^5) \nu \sum_{i=u,d} [\epsilon_L(i) \bar{q}_i \gamma_\mu (1-\gamma^5) q_i + \epsilon_R(i) \bar{q}_i \gamma_\mu (1+\gamma^5) q_i]$$

$$\left\{ \begin{aligned} R_\nu &= \frac{\sigma_{\nu N \rightarrow \nu X}}{\sigma_{\nu N \rightarrow \mu^+ X}} \sim g_L^2 + g_R^2 \\ r &= \frac{\frac{1}{3} + \epsilon}{1 + \epsilon} = \frac{\sigma_{\nu N}^{CC}}{\sigma_{\nu e}^{CC}} \end{aligned} \right.$$

$$\begin{aligned} R_{\bar{\nu}} &\sim g_L^2 + \frac{g_R^2}{r} \\ g_{L,R}^2 &= \epsilon_{L,R}^2(u) + \epsilon_{L,R}^2(d) \end{aligned}$$

unitarity violation in  $e\bar{e}$  system  
 $\gamma^* \rightarrow e^+e^-$  weak- $e\bar{e}$  interference



arbitrary gauge theory:

$$i\mathcal{L}_{PV} = \frac{G_F}{\sqrt{2}} \sum_{i=1,2} [C_{1i} \bar{e} \gamma^\mu \gamma^5 e \bar{\nu}_i \gamma_\mu \nu_i + C_{2i} \bar{e} \gamma^\mu \nu_i \bar{\nu}_i \gamma_\mu e]$$

$SU_2 \times U_1$ :

$$C_{1u} \sim -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W$$

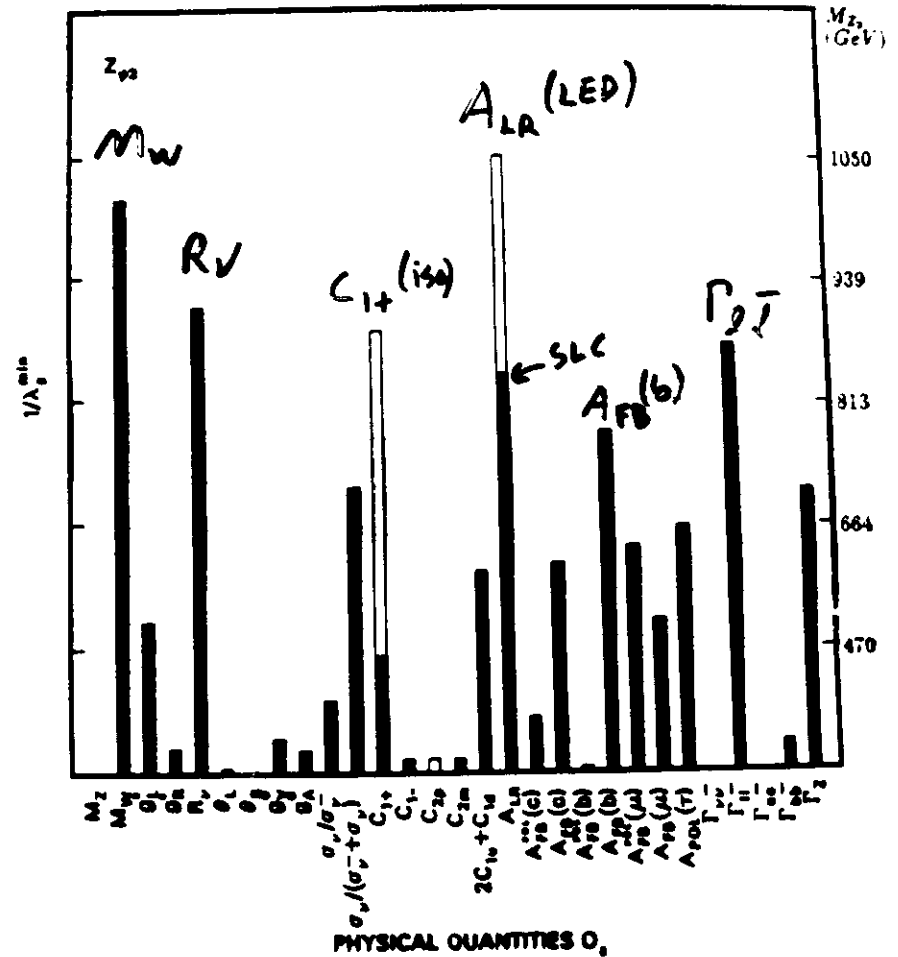
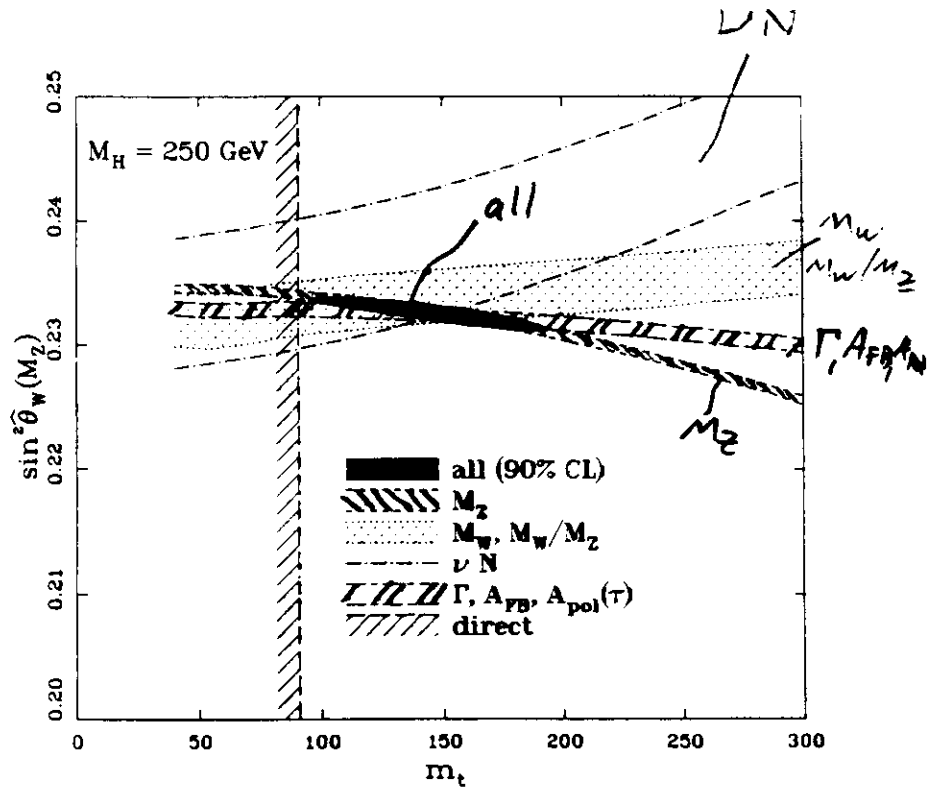
$$C_{1d} \sim \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W$$

$$C_{2u} = -C_{2d} = -\frac{1}{2} + 2 \sin^2 \theta_W$$

Z<sub>4</sub>

P.L., Lao,  
Mann

Figure 5.4: The new physics of Z<sub>4</sub> with  $C = -(2/3)^{1/2}$ :  
solid bar for C<sub>1+</sub>, C<sub>2+</sub>, and A<sub>LR</sub>(SLC);  
open bar for C<sub>1+</sub>(iso), C<sub>2+</sub>(1), and A<sub>LR</sub>(LEP).



13:  $\sin^2 \hat{\theta}_W(M_Z) = 0.2325 \pm .0007$   
n-shell  $1 - \frac{M_W^2}{M_Z^2} = 0.2257 \pm .0026$

$m_t = 151^{+21}_{-23} {}^{+18}_{-14} \text{ GeV}$   
 $M_H = 250 \xrightarrow{1000} \text{ GeV}$   
 $\xrightarrow{50}$

$m_t < 193 (199) \text{ GeV at } 90 (99)\% \text{ CL}$   
For  $M_H \leq 1 \text{ TeV}$  4/92



neutrinos as a probe of QCD, nucleon, CKM

$\nu(E)$  charged current:  $\begin{cases} \nu N \rightarrow \mu^+ X \\ \bar{\nu} N \rightarrow \mu^- X \\ \ell^+ N \rightarrow \ell^+ X, \ell = e, \mu \end{cases}$

$\frac{1}{2} = E - E'$   $\bar{\nu} N$ : parity violation and Flavor change  $\Rightarrow \bar{Q}/Q$ , etc  
 $x = \frac{Q^2}{2m_N E}$ ,  $Q^2 = -q^2 > 0$

$\bar{\nu} N \rightarrow \ell^+ X$

$$\frac{d^2\sigma}{dx dy} \sim \frac{4\pi\alpha^2 s}{Q^4} \left[ (1-y) F_2^{\ell N} + y^2 x F_1^{\ell N} \right]$$

$$F_2^{\ell N}(x, Q^2) \stackrel{\text{spin } -\frac{1}{2}}{=} 2x F_1^{\ell N}(x, Q^2)$$

$$\text{quark parton: } \simeq \frac{4}{9} x(u + \bar{u}) + \frac{1}{9} x(d + \bar{d})$$

$$QCD (\Rightarrow \alpha_s): \quad + \ln Q^2 \text{ terms} \\ + (s, c, b, \dots)$$

$\nu \rightarrow \mu^+ X$

$$\frac{d^2\sigma}{dx dy} \sim \frac{G_F^2 s}{2\pi} \left[ (1-y) F_2^{\nu N} + y^2 x F_1^{\nu N} \pm \left(1 - \frac{y^2}{2}\right) F_3^{\nu N} \right]$$

$$\begin{aligned} F_2^{\nu N} &\stackrel{\text{spin } -\frac{1}{2}}{=} 2x F_1^{\nu N} \simeq 2x [u + \bar{d}] + \ln Q^2 \\ F_2^{\bar{\nu} N} &\simeq 2x F_1^{\bar{\nu} N} = 2x [d + \bar{u}] + \text{"} \\ F_3^{\nu N} &\simeq 2x [u - \bar{d}] + \text{"} \\ F_3^{\bar{\nu} N} &\simeq 2x [d - \bar{u}] + \text{"} \end{aligned} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \begin{array}{l} \text{QCD} \\ (\alpha_s) \end{array}$$

$\underbrace{\hspace{10em}}_{QPM} \quad + (s, c, b, \dots)$

probe: - quark distributions  
 - scaling violation (QCD)  
 - quark charges:

- For isoscalar target ( $e, C$ ):  
 $u = d \equiv \bar{q}, \quad \bar{u} = \bar{d} \equiv \bar{\bar{q}}$

$$\Rightarrow F_2^{\nu N} = F_2^{\bar{\nu} N} = 2x(\bar{q} + \bar{\bar{q}})$$

$$F_2^{\ell N} = \frac{5}{9} x(\bar{q} + \bar{\bar{q}}) = \frac{5}{18} F_2^{\nu N}$$

$$\begin{aligned} - \bar{Q}/Q \text{ of nucleon: } \bar{Q} &= \int_0^1 x \bar{q}(x) dx \\ Q &= \int_0^1 x q(x) dx \end{aligned}$$

$$\frac{d\sigma^{\nu N}}{dy} = \frac{G_F^2 s}{\pi} [Q + (1-y)^2 \bar{Q}]$$

$$\frac{d\sigma^{\bar{\nu} N}}{dy} = \frac{G_F^2 s}{\pi} [\bar{Q} + (1-y)^2 Q]$$

- charm production

$$\bar{\nu}_\mu N \rightarrow \mu^+ \mu^\pm X$$

$$\nu_\mu (d, s) \rightarrow \mu^- c X_1 \rightarrow \mu^+ X_2$$

$$\bar{\nu}_\mu (\bar{d}, \bar{s}) \rightarrow \mu^+ \bar{c} X_1 \rightarrow \mu^- X_2$$

$$\Rightarrow d \rightarrow c: |V_{cd}|^2$$

Future (P):  $\nu p \rightarrow \nu p$  - also, threshold for  $R, \bar{\nu}$   
 $s$  content of proton

# Intrinsic Properties of Neutrinos

(and implications for grand unification, large scale structure of universe, nucleosynthesis, stellar astrophysics,...)

- motivations for  $\nu$  mass
- basic properties
- neutrino counting
- electromagnetic moments
- neutrino mass
  - models
  - mixing
  - experimental constraints
- cosmology, decay
- solar neutrinos
- 17 keV

## Motivations

### - New physics

$m_\nu \neq 0$  in most SM extensions  
usually,  $m_\nu \sim \frac{v}{M}$   $v = \text{weak scale}$   $M = \text{new scale}$

### - Solar $\nu$ spectrum / deficit

$$r = \frac{\varphi_{\text{observed}}}{\varphi_{\text{SSM}}} = \begin{cases} 0.28 \pm 0.04, \text{ CL} \\ 0.49 \pm 0.08, \text{ Kam.} \end{cases}$$

- excludes cool sun at  $>99\%$  CL  
Bahcall, Bethe  
Bludman, (Hata), Kennedy, PL

GALLEX:  $83 \pm 19 \pm 8$  SNU  
(SAGE 12/91:  $20^{+15}_{-20} \pm 30$  SNU)

- SSM:  $132^{+7}_{-6}$  SNU

nonstandard SM:  $> 80$  SNU

$$\Rightarrow \nu_e \rightarrow \nu_x, \Delta m^2 = m_x^2 - m_e^2 \sim 10^{-5} \text{ eV}^2$$

### - 17 keV

scenario:  $m_{\nu_e} = 17 \text{ keV} \leq m_{\nu_\mu}$

$\nu_e \rightarrow \nu_s$  in Sun,  $\Delta m^2 \sim 10^{-5} \text{ eV}^2$   
light sterile

### - atmospheric $\nu_\mu/\nu_e$ deficit

$$\frac{(\nu/\bar{\nu})_{\text{data}}}{(\nu/\bar{\nu})_{\text{MC}}} = \begin{cases} 0.65 \pm 0.06 \pm 0.06, \text{ Kamiokande} \\ 0.64 \pm 0.09 \pm 0.12, \text{ IMB} \end{cases}$$

(singlet)  
 $\nu_\mu \rightarrow \nu_x, \Delta m^2 \sim (10^{-3} - 1) \text{ eV}^2$ , large mixing

### - hot dark matter (?)

$$m_{\nu_e} \sim (1 - 28) \text{ eV}$$

↑ irrelevant closure

- need galaxy seeds

{ cosmic strings  
decaying  $\nu$

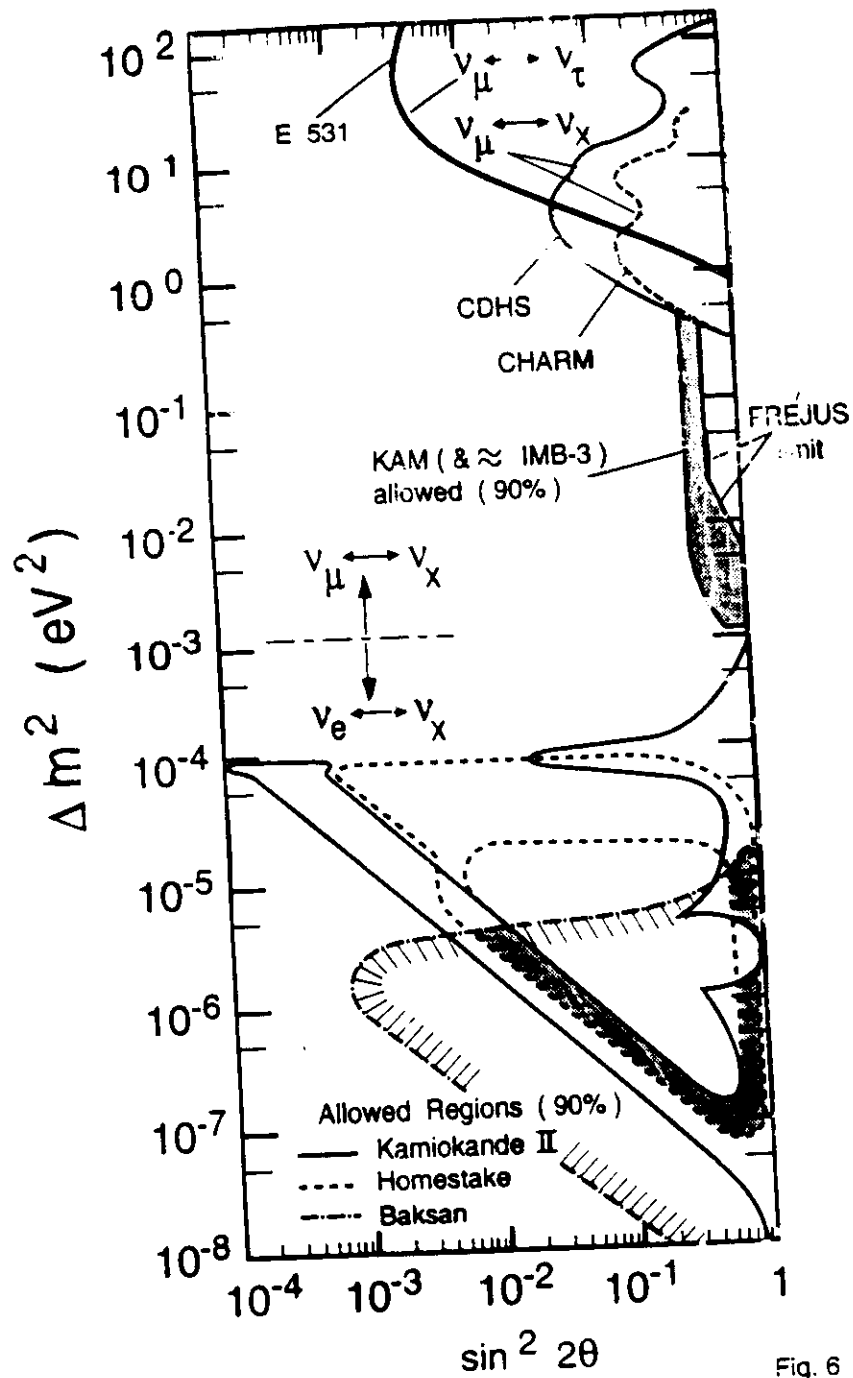


Fig. 6

Hirata  
et al

Homestake,  
Kamiokande,  
GALLEx

