



INTERNATIONAL ATOMIC ENERGY AGENCY  
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
**INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS**  
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SMR.627-5

**MINIWORKSHOP ON  
STRONGLY CORRELATED ELECTRON SYSTEMS**

15 JUNE - 10 JULY 1992

**"ELECTRONIC PROPERTIES"**  
**Part II**

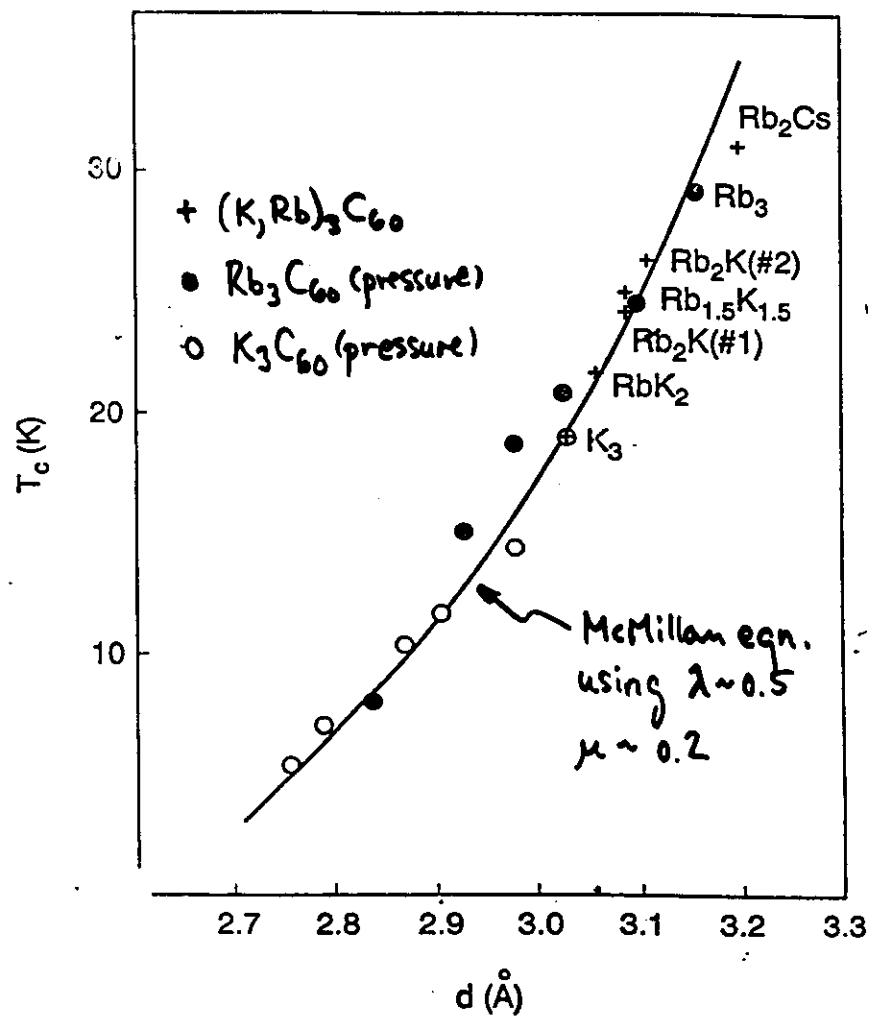
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U.S.A.

**ELECTRONIC PROPERTIES**

- $A_6C_{60}$ 
  - Filled band insulator
- $A_2C_{60}$  and  $A_4C_{60}$ 
  - Gap in  $Na_2$  by photoemission (Gu, et al)
  - $^{13}C$  NMR  $T_1T$  strong function of T
- Most  $A_3C_{60}$  metallic and superconducting
  - $^{13}C$   $T_1T$  doubles for  $Na_2Rb$  from 290K to 100K and 6X for  $Na_3$

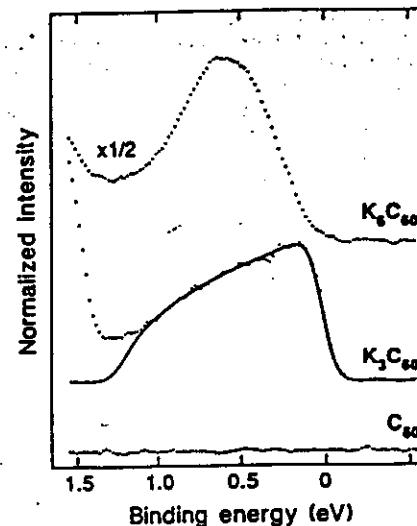
## Variation of $T_c$ with lattice constant

M. Schlüter et al, preprint



## Photoemission Spectroscopy in $K_xC_{60}$

C.T. Chen et al, Nature 352, 603 (1991)



## Photoemission of Metallic + Insulating Phases

Gu et al, PRB 45, 6748 (1992)

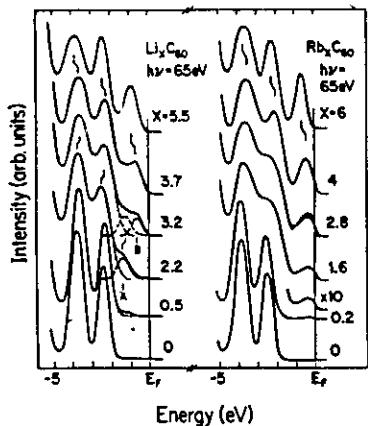


FIG. 1. Photoemission spectra for  $\text{Li}_x\text{C}_{60}$  and  $\text{Rb}_x\text{C}_{60}$  with energies referenced to the Fermi level of the spectrometer,  $E_F$ . The nonmetallic behavior of  $\text{Li}_x\text{C}_{60}$  for all  $x$  values is indicated by the lack of emission at  $E_F$ . In contrast,  $\text{Rb}_x\text{C}_{60}$  films exhibit metallic Fermi edges. Doping to  $\text{A}_3\text{C}_{60}$  produces complete filling of the LUMO-derived band and recovery to the insulating molecular-solid configuration. The dashed lines for  $\text{Li}_x\text{C}_{60}$  provide a guide to the eye for bands A and B. That for  $\text{Rb}_x\text{C}_{60}$  shows the effect of enhanced experimental resolution.

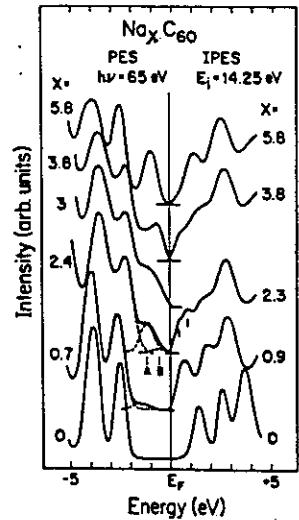


FIG. 2. Photoemission and inverse photoemission results for  $\text{Na}_x\text{C}_{60}$  showing the evolution of the occupied and empty states near  $E_F$ . Feature A corresponds to  $\text{Na}_2\text{C}_{60}$  and feature B reflects conversion to the  $\text{Na}_3\text{C}_{60}$  phase. For  $\text{Na}_2\text{C}_{60}$ , splitting is evident in the leading conduction-band feature. The movement of spectral features relative to  $E_F$  reflects changes in screening with pinning of  $E_F$  at the conduction-band minimum.

## Pseudo-Gap at the Fermi Level in $\text{K}_3\text{C}_{60}$

Takahashi et al, PRL 68, 1232 (1992)

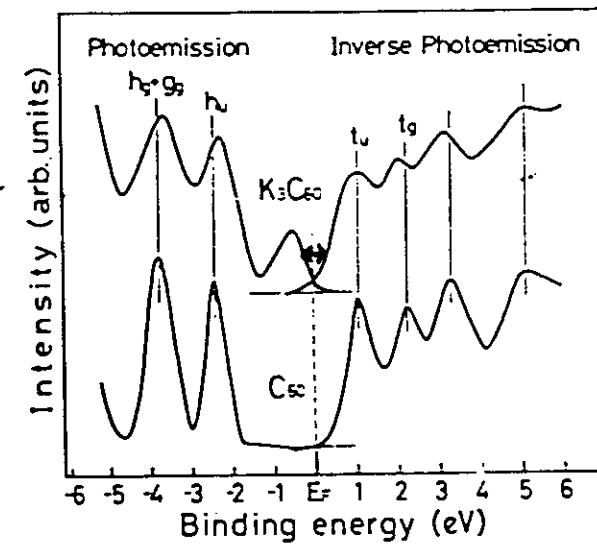


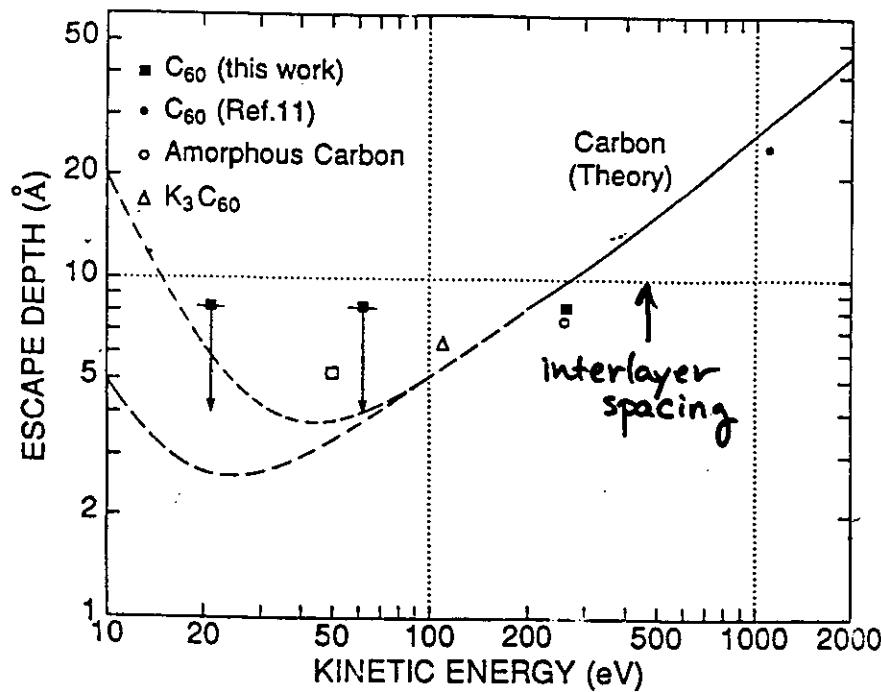
FIG. 1. Photoemission and inverse photoemission spectra of  $\text{C}_{60}$  and  $\text{K}_3\text{C}_{60}$ .

- Chen et al PRL (comment) -

- samples not annealed
- surface effects dominate (Raman study)
- IPES not consistent w/ Minnesota data showing  $t_{1u}$  intersects Fermi level at  $x = 3$ .

## Surface Effects in Photoemission

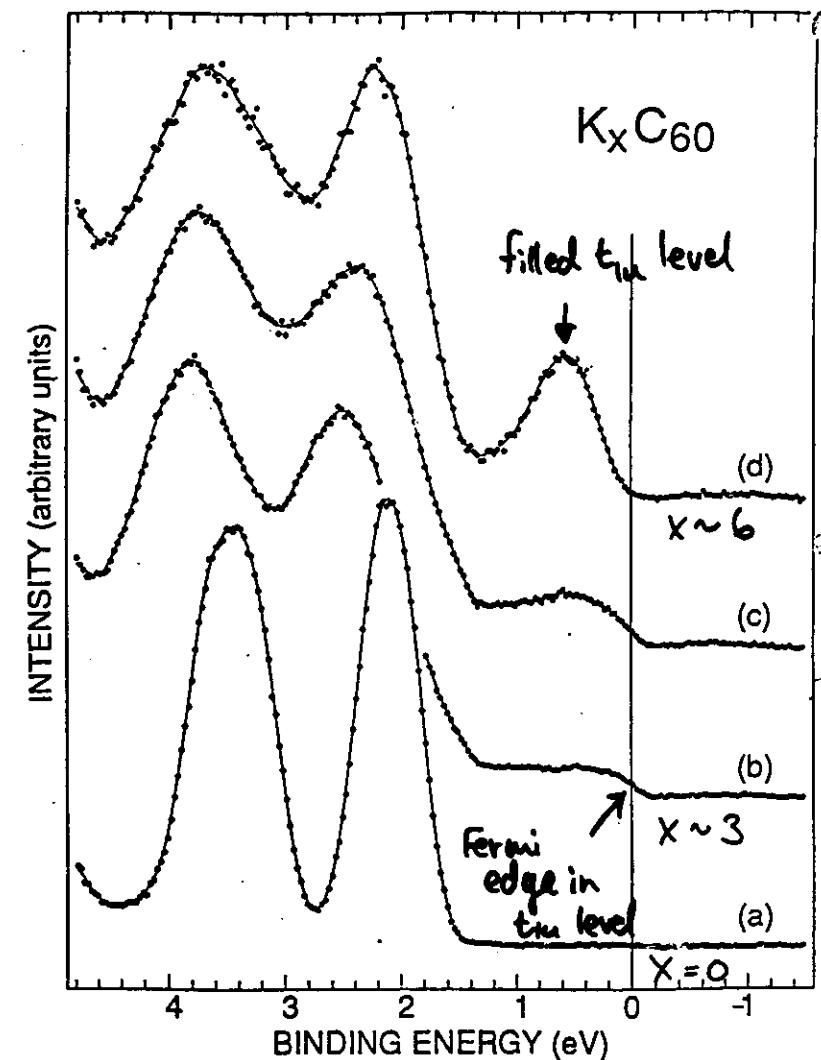
Wertheim et al., preprint



- Molecular solids pose special problem for PES
- In  $\text{C}_{60}$ , only 1st monolayer probed.

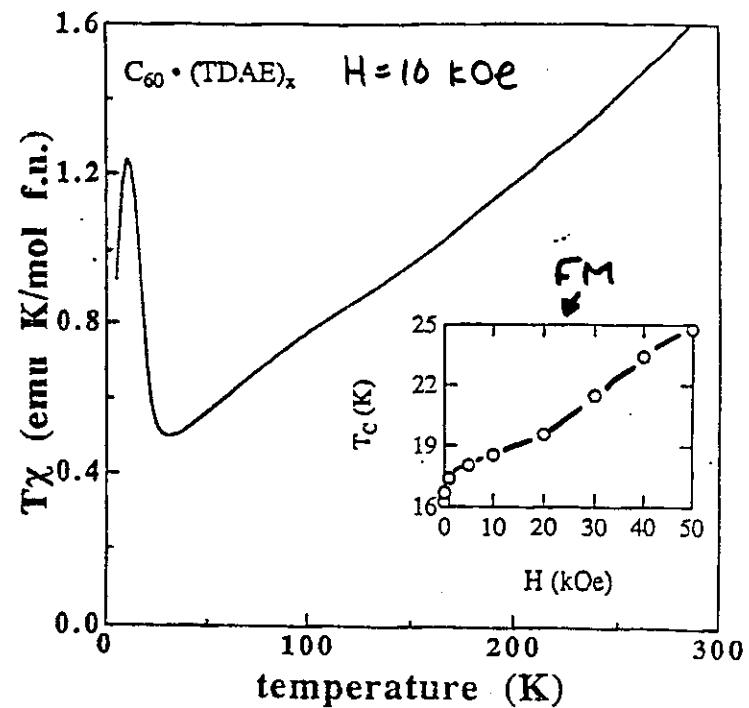
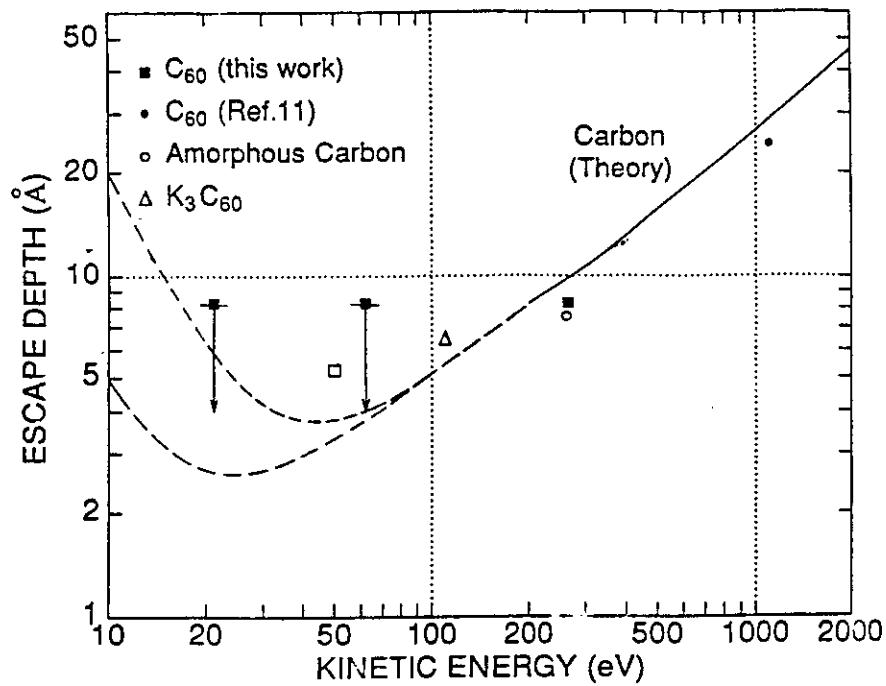
## Surface effects in Photoemission

Wertheim et al., preprint



## Ferromagnetism in $C_{60}(TDAE)_x$

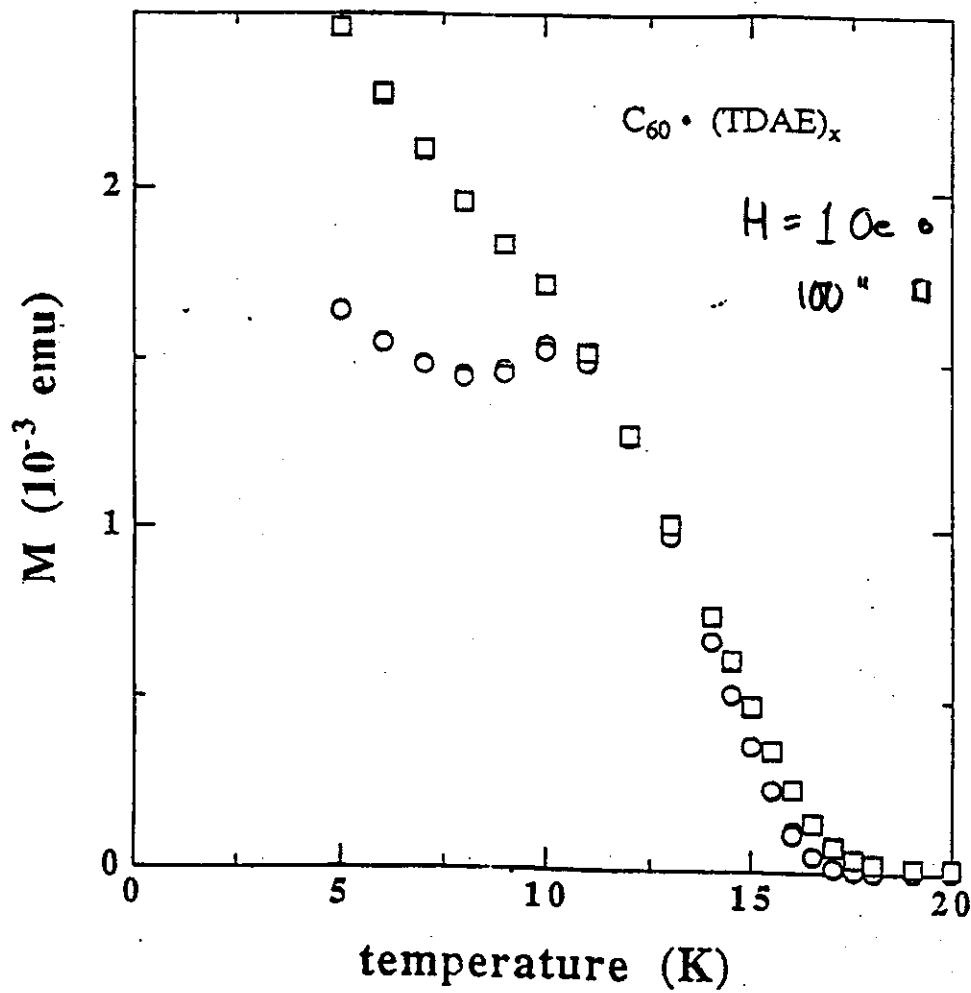
Allemand, et al



- Increasing  $T_c$  with  $H$  signals FM state.

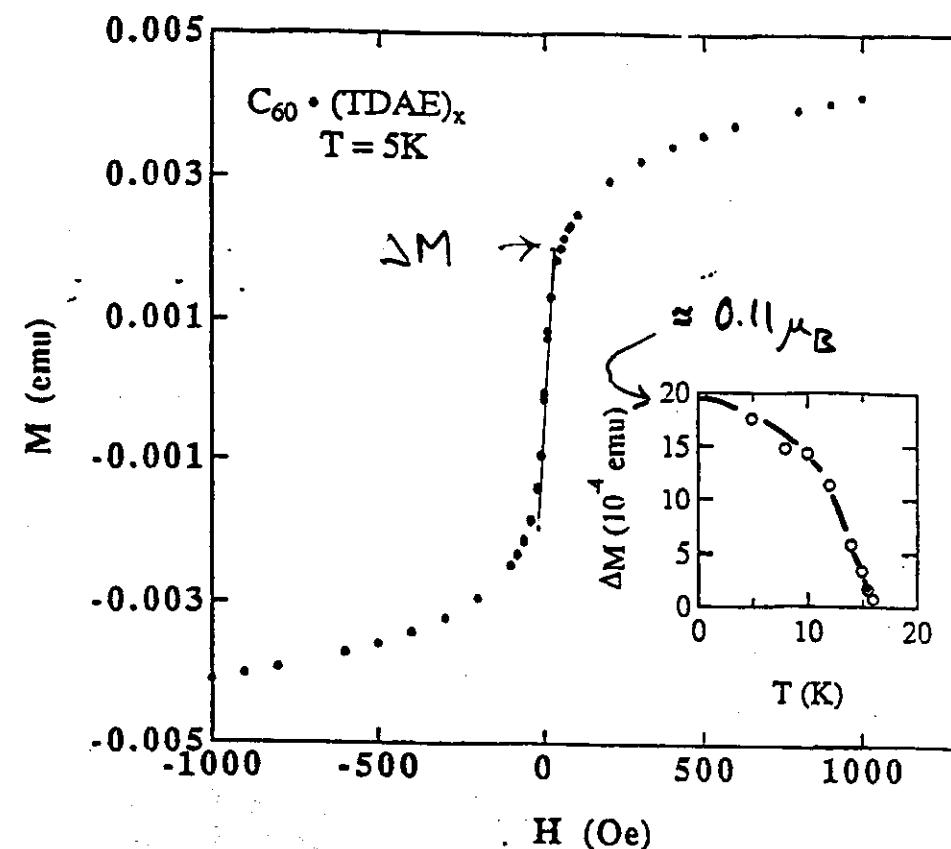
Ferromagnetism in  $C_{60} \cdot (TDAE)_x$

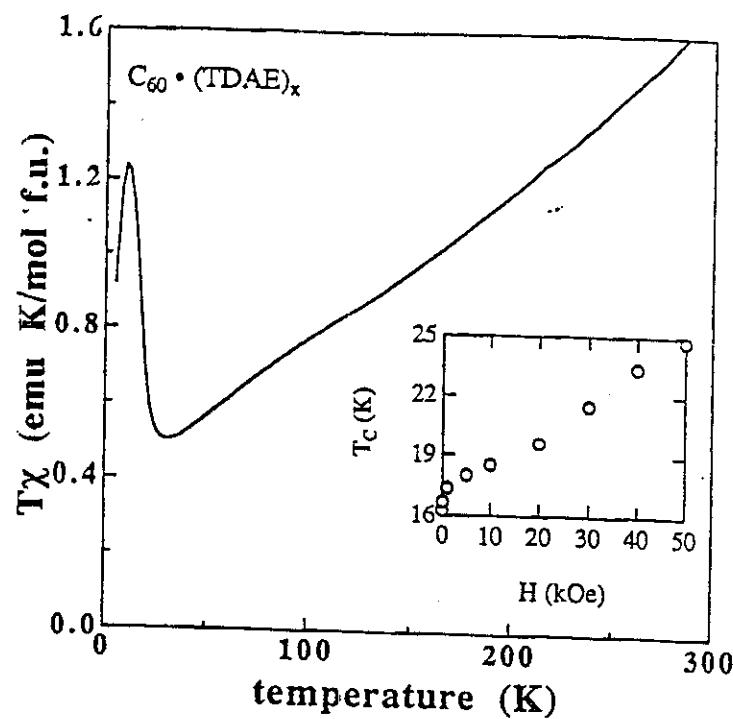
Allcmand, Wudl, et al.,



Ferromagnetism in  $C_{60} \cdot (TDAE)_x$

Allcmand et al.





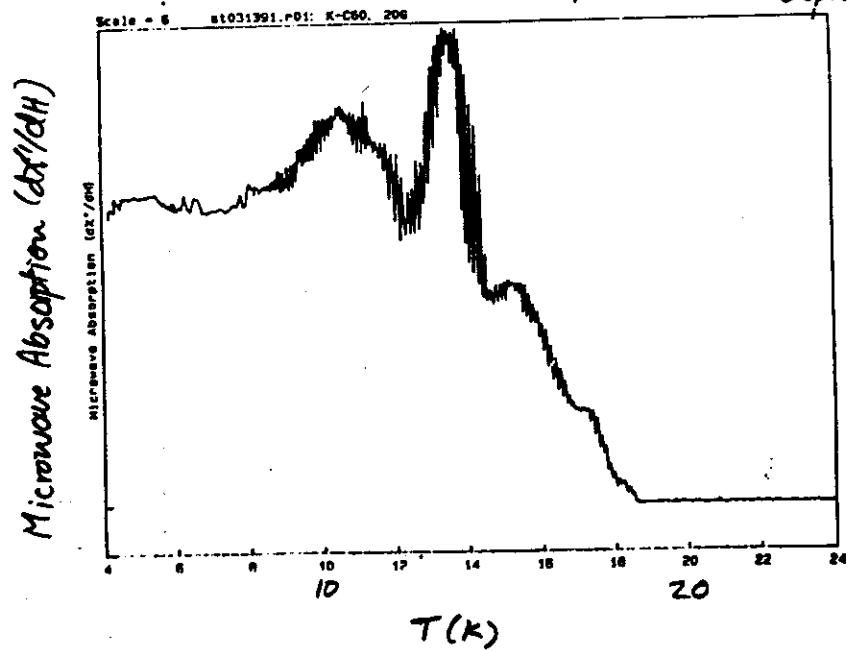
Microwave absorption in  $K_x C_{60}$  S. Glarum

freq.  $\sim 9$  GHz

$$\text{surface impedance } S = i\omega\lambda/c$$

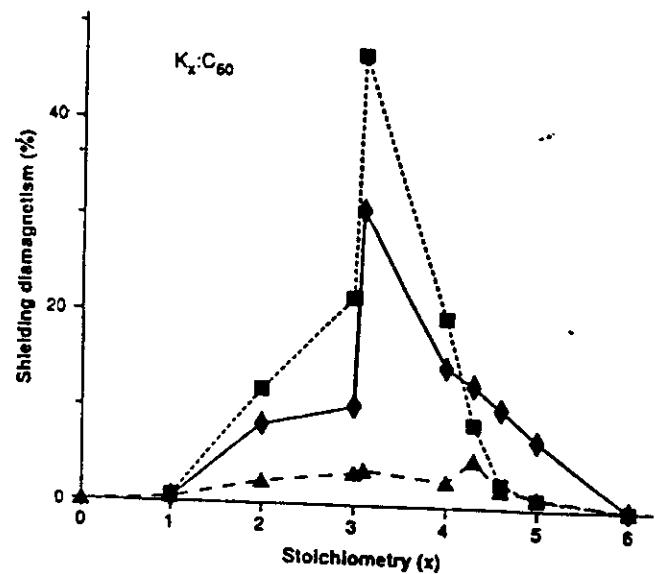
$$1/\lambda^2 = (4\pi/c^2)(ne^2/m + i\omega\sigma) = i/\lambda_L^2 + 1/\lambda^2$$

London penetration depth.  
↑ skin depth



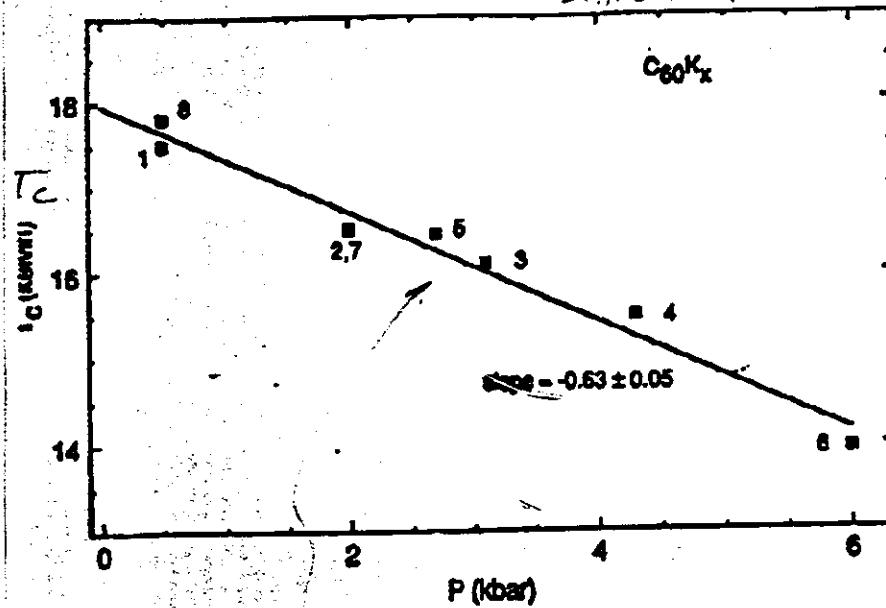
## Stoichiometry and Diamagnetic Shielding

Holczer et al., Science 252, 1154 (1991)



Use pressure-dependence to estimate Bulk Modulus (B)

Stinber et al (Sandia)



$$\frac{\partial T_c}{\partial P} = -0.63 \frac{K}{kbar}$$

$$\frac{\partial T_c}{\partial V} = 0.088 \frac{K}{A^3} \text{ (from } K_3 \text{ to } Rb_x \text{ doping)}$$

$$\left. \begin{array}{l} B_{A_3C_60} \approx 36 \text{ GPa} \\ B_{C_60} \approx 18 \text{ GPa} \end{array} \right\} \text{ (Dudos)}$$

$A_3C_60$  is twice as "stiff" as  $C_60$

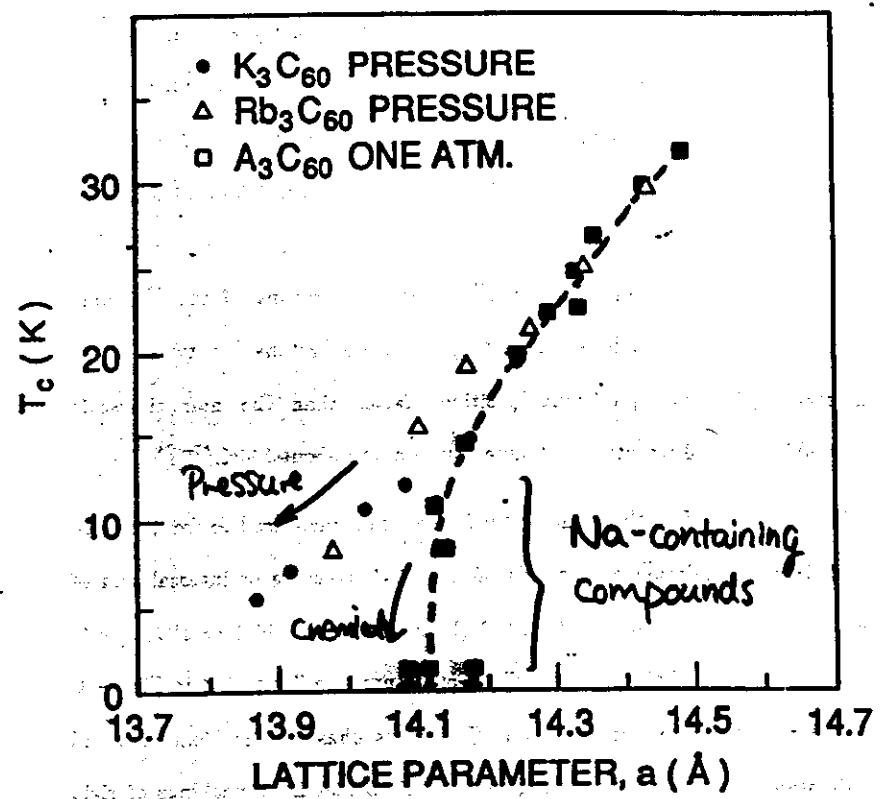
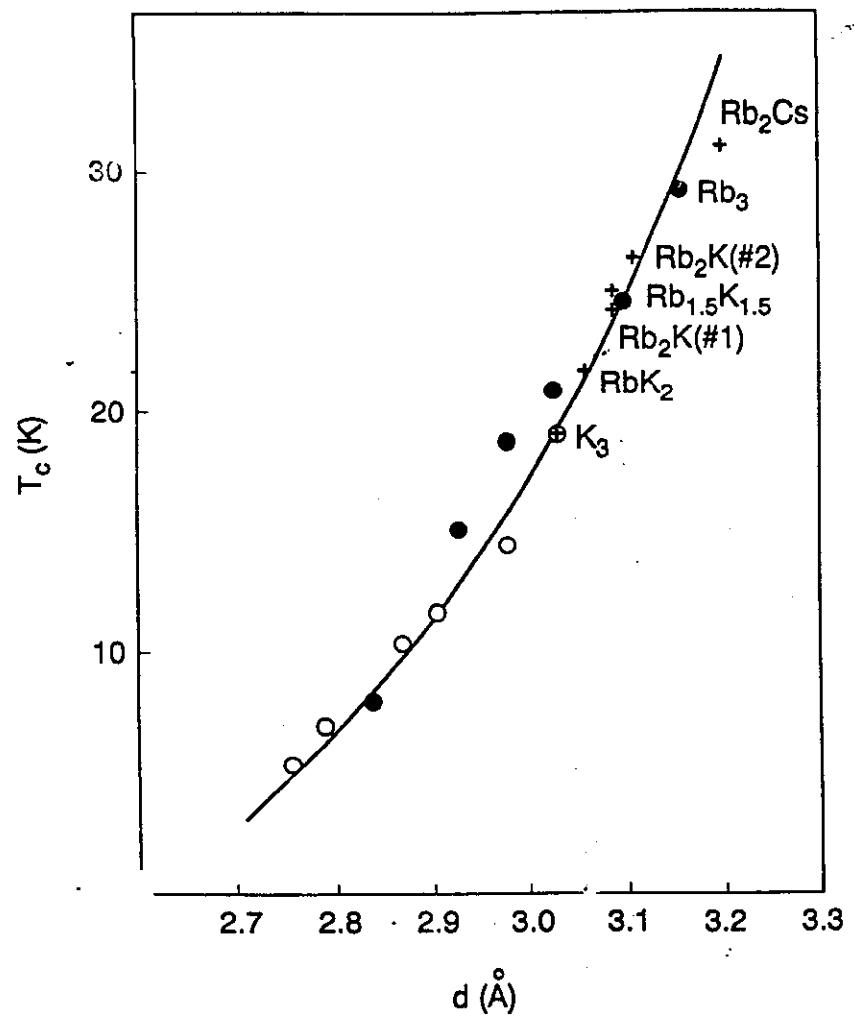


FIGURE 7

## What Controls $T_c$ ?

Naive approach -

Lattice constant



Density of States



$T_c$

(via the usual phonon theories  
-but need high  $\omega$ )

## Intermolecular Phonon-Mediated Pairing

Zhang, Ogata + Rice , PRL 67, 3452 (1991)

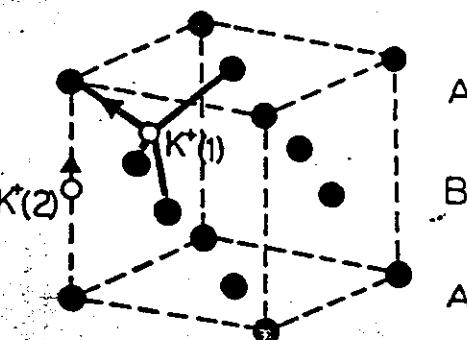


FIG. 1. The fcc lattice structure of  $K_2CuO_3$ . Solid circles represent  $CuO_3$ -molecules. They are surrounded by eight  $K^+(1)$  at the center of the tetrahedron consisting of four nearest-neighbor  $CuO_3$ , and six  $K^+(2)$  located at the middle of every two next-nearest-neighbor  $CuO_3$ . Only one of each is shown by an open circle. The ratio of  $K^+(1)$  and  $K^+(2)$  sites is 2:1. The arrows indicate  $K^+$  motion toward the more negatively charged  $CuO_3$ . A and B represent the two sublattices for CDW consideration.

- $K^+$ -ion optic phonons strongly couple to electrons
- fcc lattice frustrated  $\therefore$  superconductivity is favored over a CDW state.

The  $(K, Rb)_3 C_{60}$  study begs the questions:

How far can the lattice be pulled apart?

What are the neighboring structures?

Are they superconducting?

## Forming a microscopic description of Superconductivity

### McMillan equation

$$T_c = \frac{\langle \omega \rangle}{1.2} \exp \frac{-1.04(1+\lambda)}{\lambda - \mu^*(1-0.62\lambda)}$$

$\langle \omega \rangle$  - frequency of "phonons"

$\lambda$  - elect.-phon. coupling strength ( $= N_a V$ )

$\mu^*$  - elect.-elect. interaction

Need to place bounds on  $\langle \omega \rangle, \lambda, \mu^*$ .

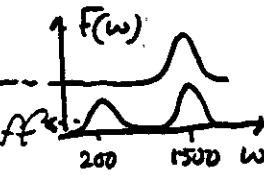
## Current Theoretical Models for pairing in $A_3C_{60}$

(4)

- Intramolecular phonons

- Varma, Zaanen + Raghavachari
- Schlüter, Launois, Needels + Baraff  
+ Tománek
- $\omega \sim 1400\text{ K}$  ( $H_g$ ) modes (intraball)

$$N \sim 10 \text{ states/eV spin } C_{60} \text{ (intraball)}$$



- Intermolecular phonons

- Zhang, Ogata + Rice
- Negative U from K-optic phonon ( $\omega \sim 200\text{ K}$ )
- SC stabilized via vortices CDW by frustration

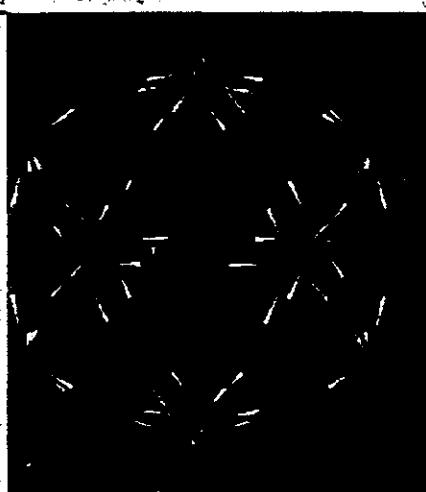
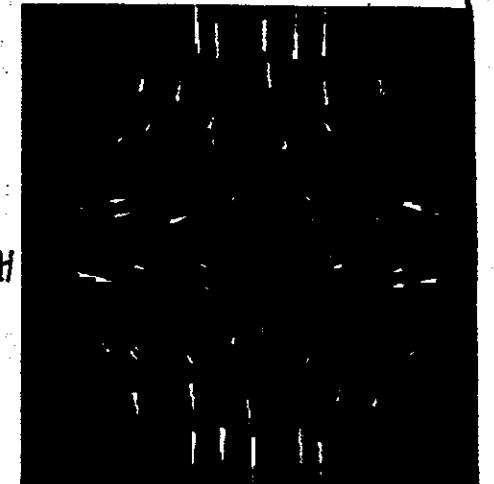
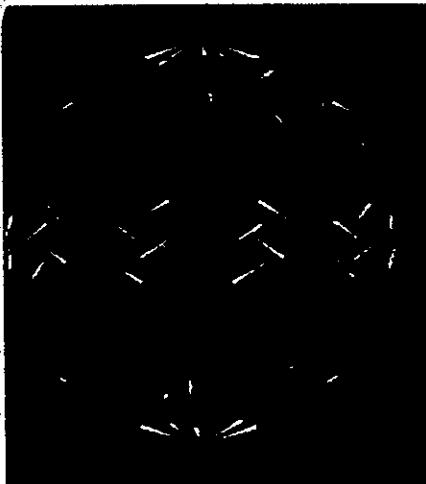
- Electron-Electron pairing

- Chakravarty + Kivelson
- Negative U results from spin-charge decoupling in an RVB state.
- Boskaran + Tosatti

$\uparrow \downarrow \mu^*$   
 $\lambda \mu^*$   
electronic  
experiments

TOP  
DO NOT AFFIX OVERLAYS ALONG THIS SURFACE

YG NO



In

11

## Electronic Correlations, Superconductivity in $A_xC_60$

Chakravarty, Kivelson, Gelfand, Science 254, 970 (1992)

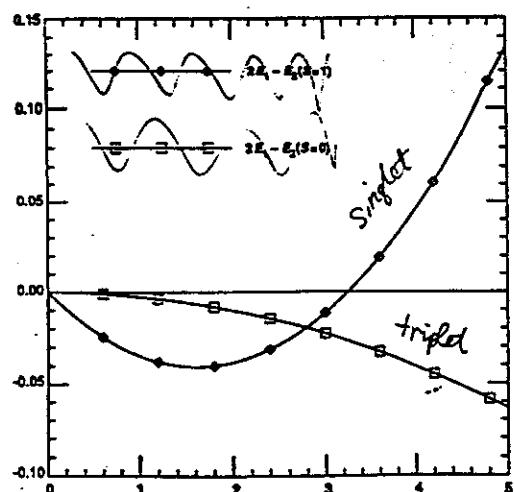


Fig. 1. The  $C_{60}$  singlet and triplet  $E_psi$  (in units of  $t$ ) as functions of  $U/t$  for  $r' = 1$ .

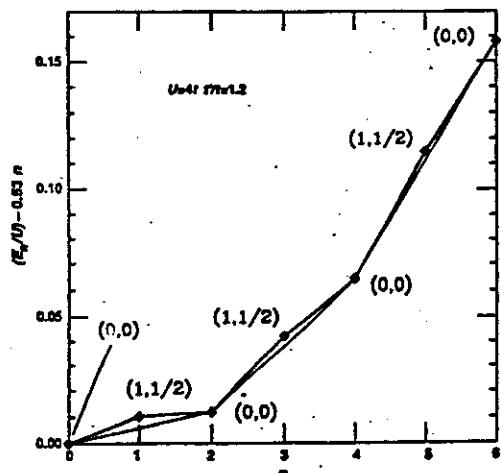


Fig. 2. The energy  $E_psi$  (in units of  $t$ ) versus  $n$ , for  $C_{60}$  at  $U = 4t$ ,  $r'/t = 1.2$ . Note that a linear piece has been subtracted for clarity. The values of  $L$  and  $S$  for the lowest energy states at each  $n$  are indicated in the form of  $(L, S)$ .

## Our Approach

- Assume for the present the interaction is mediated by phonons (evidence to follow)
- Measure and analyze thermo-magnetic data  $\alpha$ ,  $X$ ,  $\Delta C$  in terms of phonons (Hückel eqn.)
- Does this approach fail?
- Hope to distinguish between high- and low-energy phonons (inter- or intra).

## Inelastic Neutron Scattering

Prassides et al, Nature 354 462(1992)

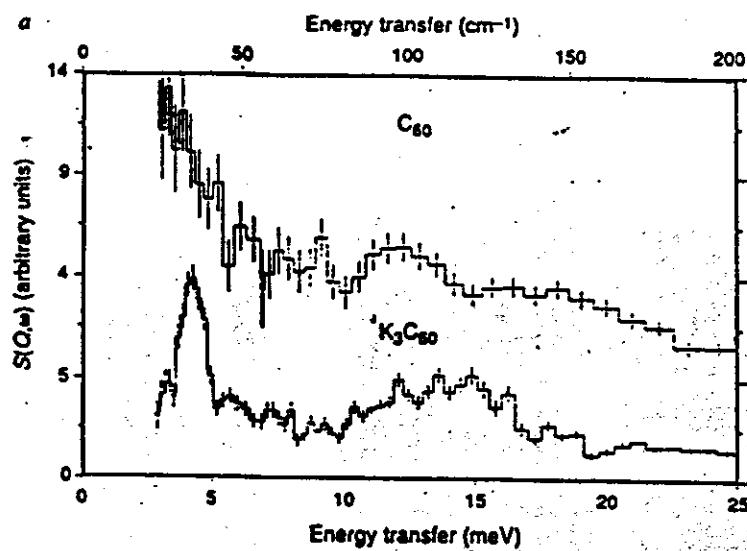


FIG. 1 Inelastic neutron scattering spectra in the energy regions (a) 0-25 meV and (b) 25-200 meV of  $C_{60}$  at 20 K (top) and  $K_3C_{60}$  (bottom); the  $K_3C_{60}$  data were collected at 5 K and 30 K and summed. The instrumental

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- Significant changes in peak positions + intensities on doping.
- Buckling modes  $H_g^{(2)}, H_g^{(8)}$  disappear

## Effect of Alkali doping on Vibrational modes

Duclos et al

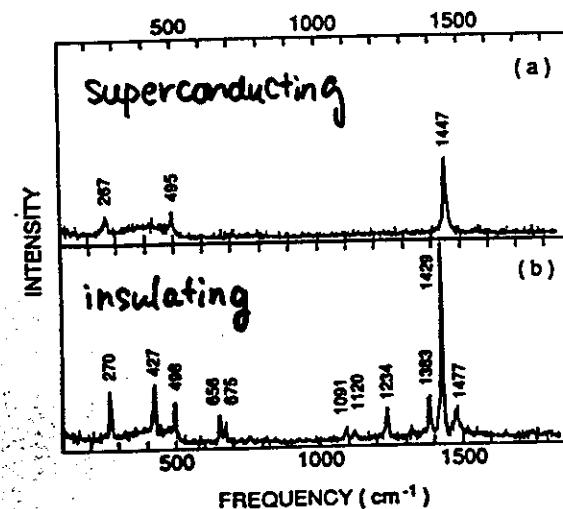
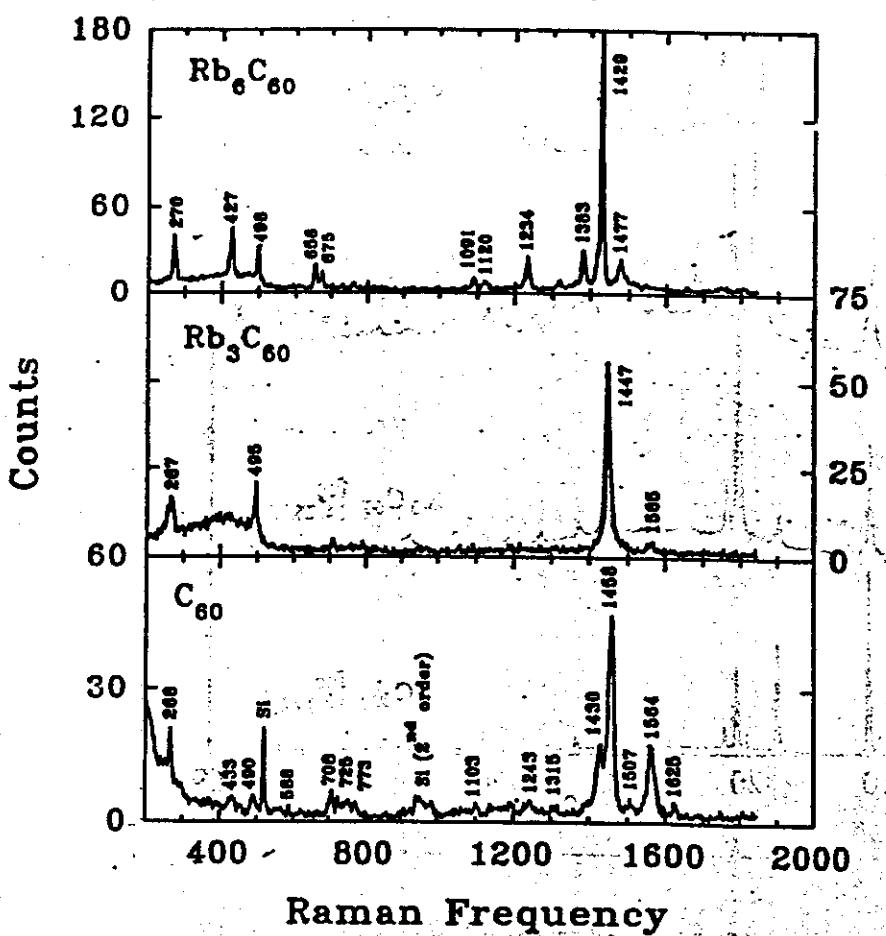


Figure 4. *In situ* Raman spectra of a  $C_{60}$  film taken during rubidium doping: (a) superconducting and (b) insulating.

*Tell*

$C_{60}$  fulleride Raman spectroscopy  
Room temperature



Isotope Effect

(APR et al PRL, Feb 92)

- Can distinguish between phononic ( $T_c \propto M^{-\alpha}$ ) and electronic mechanism.
- Use  $\alpha$  along with  $T_c$  to determine  $\lambda, \mu^*$ , for a given  $\langle n \rangle$ .

Intermediate Coupling  $\lambda < 1$  (McMillan)

$$T_c = \frac{\langle n \rangle}{1.2} \exp \left[ -\frac{1.04(1+\lambda)}{\lambda - \mu^*(1+0.62\lambda)} \right]$$

$$\alpha = -\frac{\partial \ln T_c}{\partial \ln M} = \frac{1}{2} \left[ 1 - \left( \mu^* \ln \frac{\langle n \rangle}{1.20 T_c} \right)^2 \frac{1+0.62\lambda}{1+\lambda} \right]$$

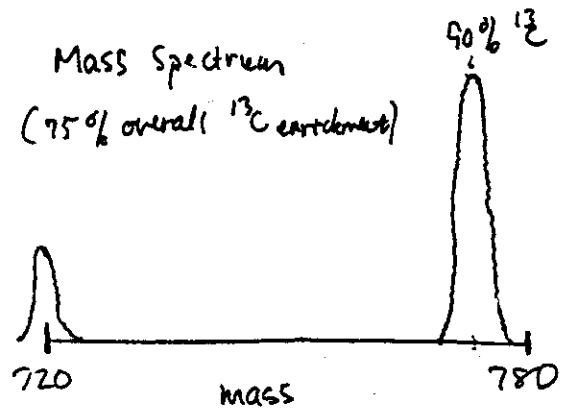
Strong Coupling  $\lambda \gg 1$  (Kresin)

$$T_c = 0.181 \frac{1}{M} \langle n \rangle$$

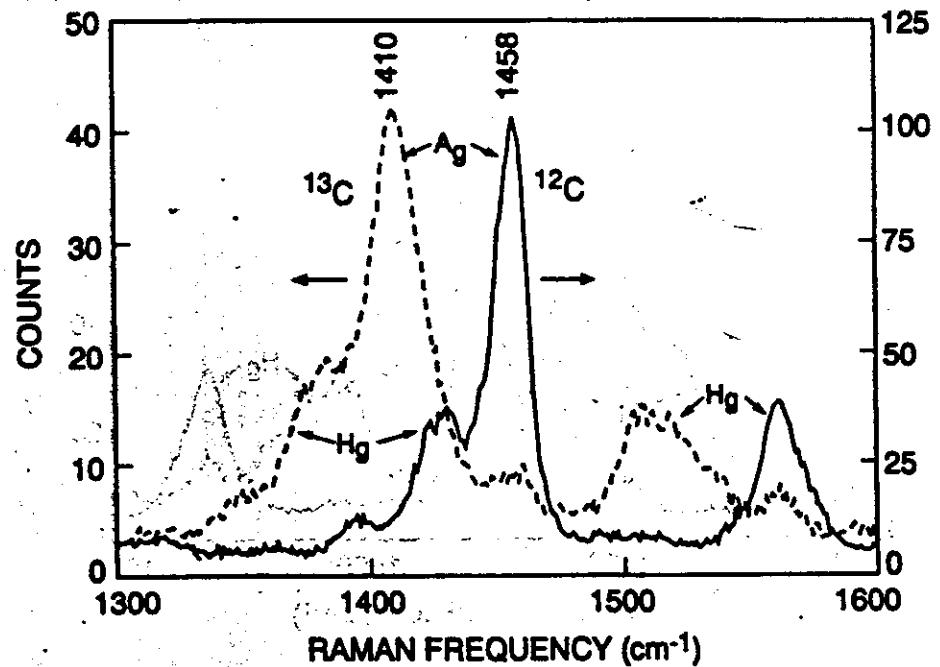
$$\alpha = \frac{1}{2} \left[ 1 - \frac{1.3 \mu^{*2}}{1 + 2.6 \mu^*} \right]$$

### Isotope Effect Sample Preparation

- Mix 75% (weight)  $^{13}\text{C}$  powder with 25%  $^{13}\text{C}$  (universally labelled) Glucose.
- Press @ 14kbar, a 1/4" rod.
- Heat to 250C to polymerize the glucose.
- Graphitize at T > 2500 C.
- Standard procedure for synthesizing  $\text{C}_{60}$ .
- 10 grams of rod yielded 37 mg  $\text{C}_{60}$ .
- Prepared a control  $\text{A}_3^{12}\text{C}_{60}$  sample, along with  $^{13}\text{C}$  sample using Penn method.

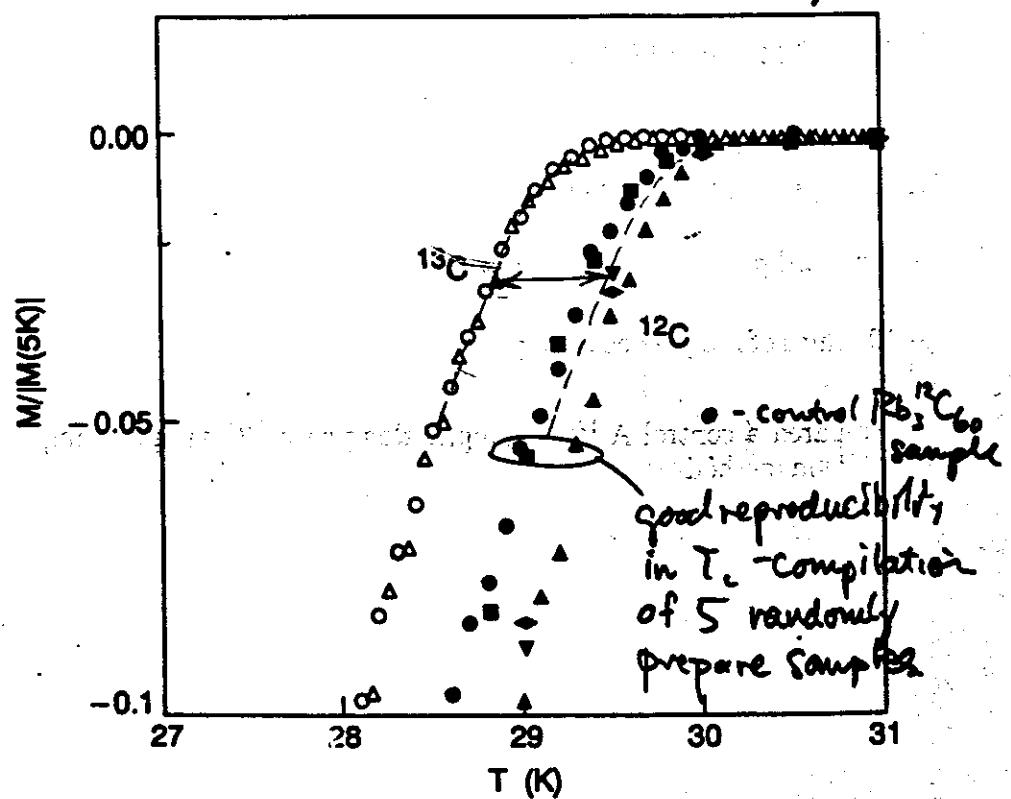


Raman Spectrum (Intramolecular modes)



## Isotope Shift in $Rb_3C_60$

Ramirez, Kortam, Rosschinsky, Duclos, Mujica  
 Hadden, Murphy, Mathija, Zahurak, Lyons  
 PRL 68, 1058 (92)



- High reproducibility of  $T_c$  good evidence for a line phase.

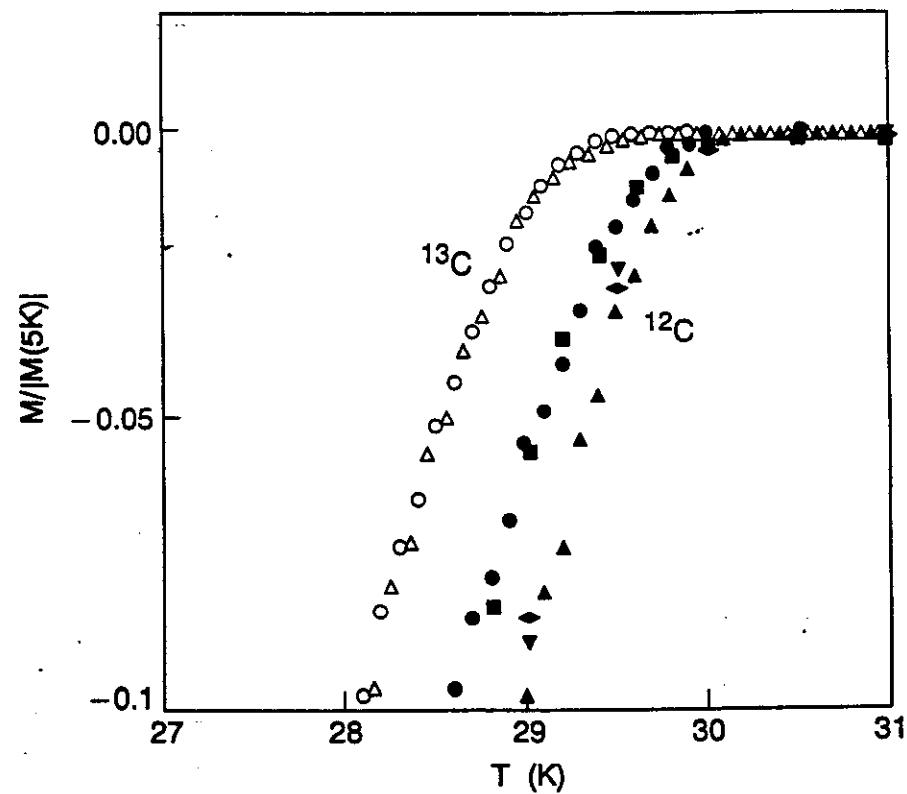


Fig. 2

## Isotope Effect in $K_3^{13}C_{60}$

Chen + Lieber, J. Am. Chem. Soc., 114, 3141 (1992)

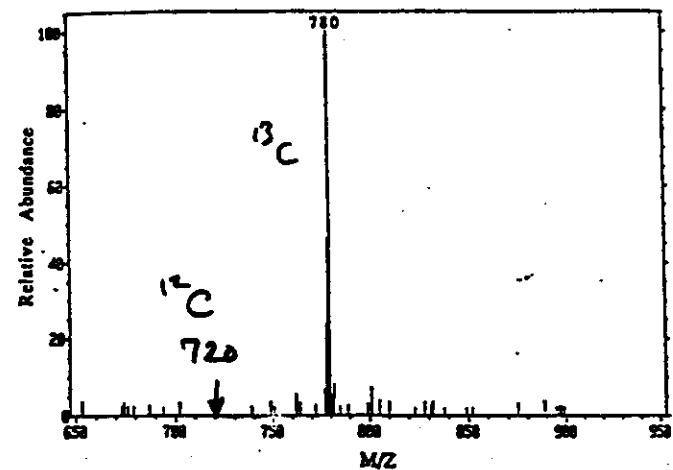


Figure 1. Field desorption (FD) mass spectrum of a purified  $^{13}C_{60}$  sample ( $M^+$ , 780) recorded using a JEOL AX50SH spectrometer. Experimental conditions were as follows: 30 mA FD emitter current; 3 keV ion energy; 9 keV extraction energy. Similar spectra were recorded using fast atom bombardment.

- 99%  $^{13}C$  enrichment
- $\alpha \approx 0.3 \pm 0.06$

## Isotope Effect - $Pb_3 C_{60}$

Ebbesen et al. Nature 355, 620 (1992)

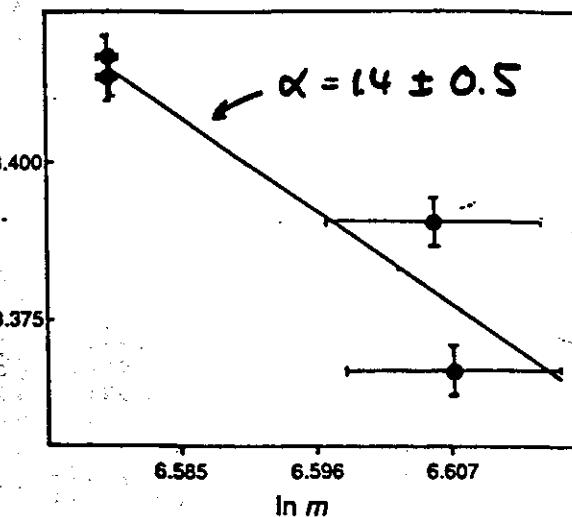
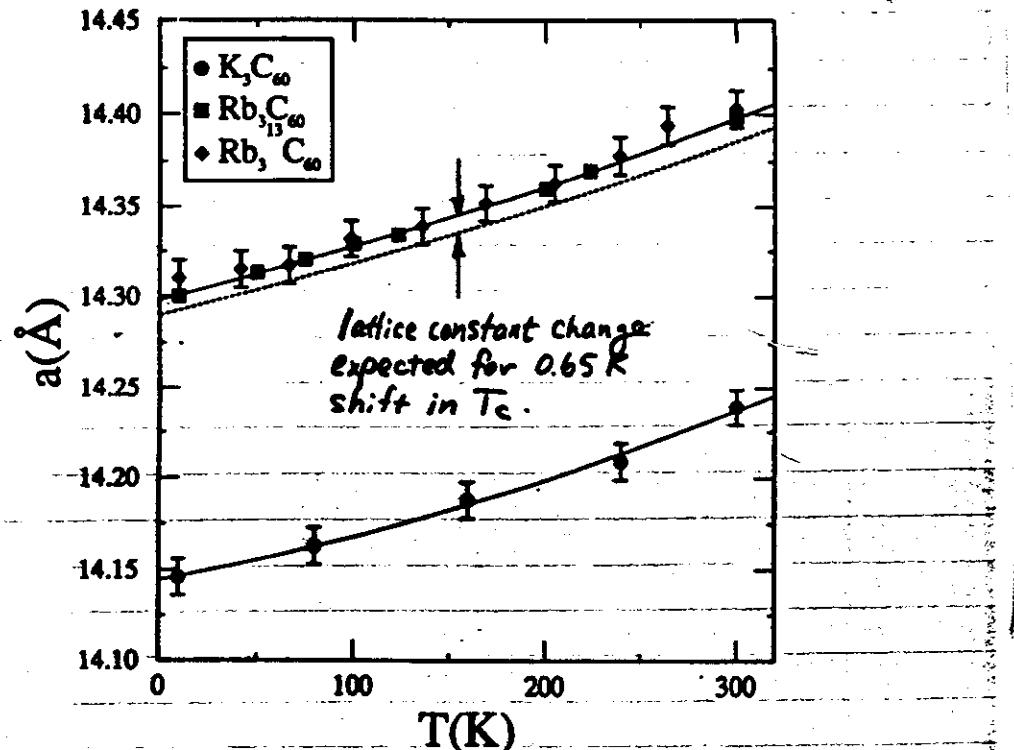


FIG. 3 Relationship between  $\ln T_c$  and  $\ln m$  (average  $C_{60}$  mass). The large horizontal error bars are due to the statistical spread of the  $C_{60}$  masses at a given average  $^{13}C$  content.

- Samples only 33% enriched.

## High-accuracy lattice constant determination

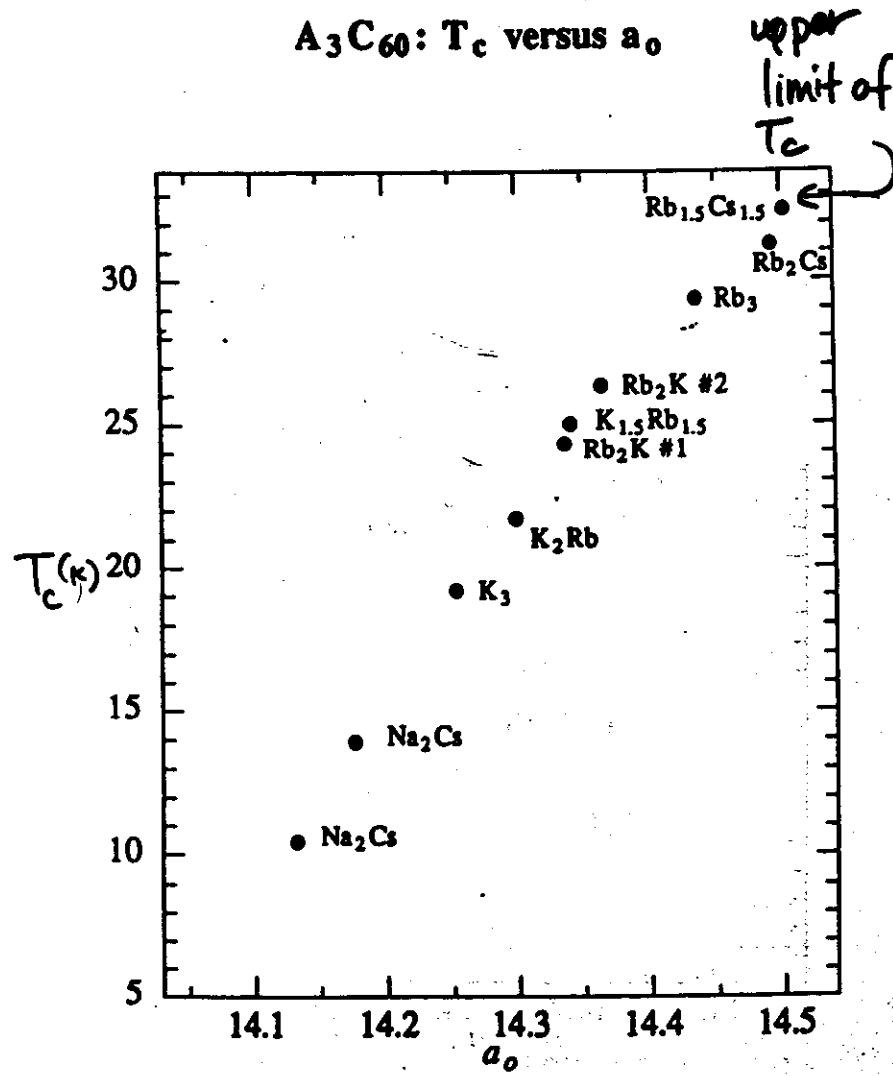
Fleming



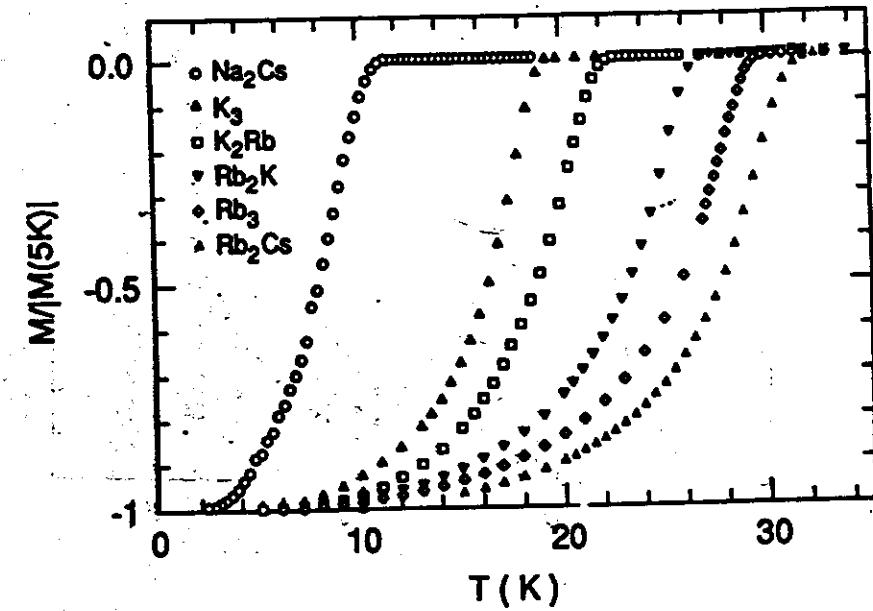
- Null result consistent with  $T_c$  shift driven by phonon-frequency change, not change in  $N_0$  by zero-point fluctuation lattice change.

## Isotope Effect — Conclusion

- After accounting for mass spectrum (75% overall enrichment) find  $\alpha = 0.37 \pm 0.05$
- If  $\langle n \rangle = 1400$  K, then find  $\lambda = 0.72, \mu^* = 0.15$ .
- If  $\langle n \rangle = 200$  K, then use strong coupling expressions, and find  $\lambda > 2, \mu^* \approx 1$ . (consistent w/ tunnelling)
- If  $\langle n \rangle = 200$  K from alkali optic modes, then  $\alpha = 0.5(M_{\text{Rb}}/M_{\text{CeO}})^{\frac{1}{3}} \approx 0.05$  (unlikely)
- Conclude -  $T_c$  affected by phonons similar to regular phonon-coupled superconductors.
- Still can't say if weak or strong coupling.



### Chemical Tuning of $T_c$

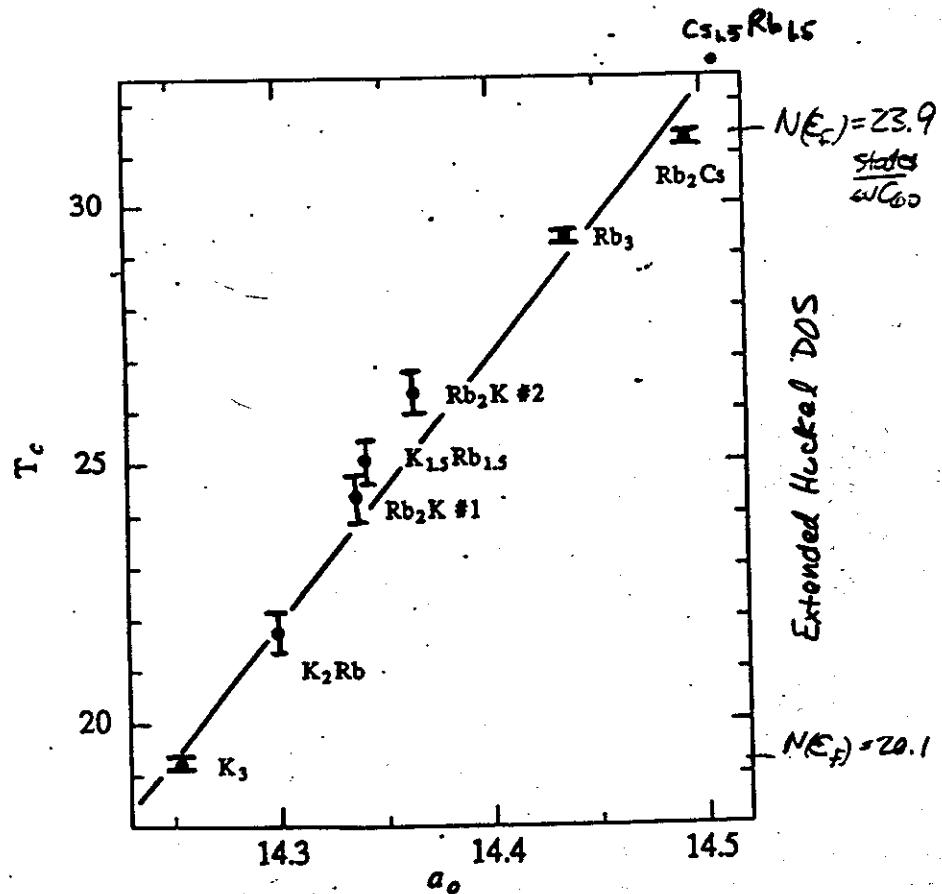


This suggests, via lattice-constant ( $a$ ) change that the density of states ( $N$ ) is driving  $T_c$  changes.

$T_c$  vs. lattice parameter (FCC)

(37)

Fleming, Ramirez, Rosseinsky, Murphy, Haddon, Zahurak  
Mathija, Nature 352, 787 (1991)



Density of States  $N(E_F)$  from bulk  
 $g=0$  measurements (48)

Go back to free electrons

Pauli paramagnetic susceptibility  $\chi_p$

$$\chi_p = \mu_B^2 N(E_F)$$

Specific heat linear term  $C = \gamma T$

$$\gamma = \frac{\pi^2 k_B^2}{3} N(E_F)$$

## Density of States $N_0$ in $A_3C_{60}$

- Band structure -  $W \approx 0.5$  eV  $\rightarrow N_0 \approx 6$  states/spin-eV- $C_{60}$
- Extended Huckel theory - 20% increase, K to Rb.
- Parameters  $\lambda$  and  $\mu^*$  not known well enough to predict  $T_c$ .  
However, can look at systematic trends,  $T_c$  vs.  $N_0$ .
- First, different measurements must be in agreement:

XPS, NMR, X<sub>p</sub>, C.

$$X_{\text{part}} = 2\mu_B^2 N_b (1 - I)^{-1}$$

$$\gamma = \frac{2}{3} \pi^2 k_B N_b (1 + \lambda + f(I))$$

specific heat  $C \propto T$

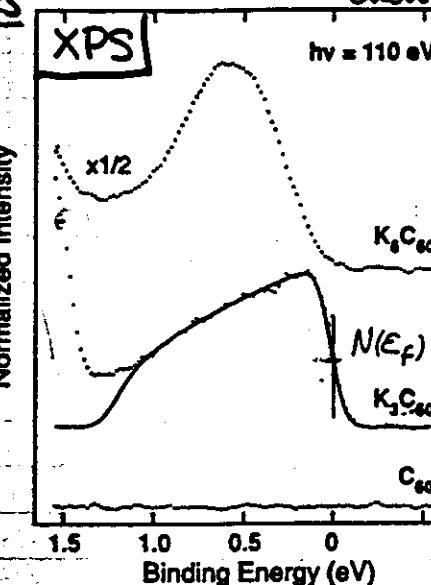
bare density of states

Spin fluctuation mass enhancement

electron-phonon coupling strength

## Density of States

$N(E_F)$



Chen et al

1.9 states  
 $eV C_{60}$

Science 253, 884 (1991)

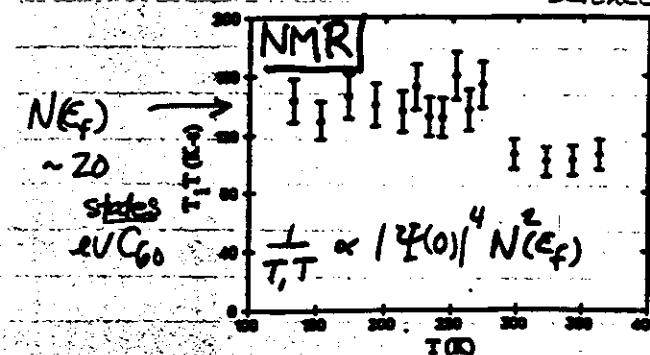
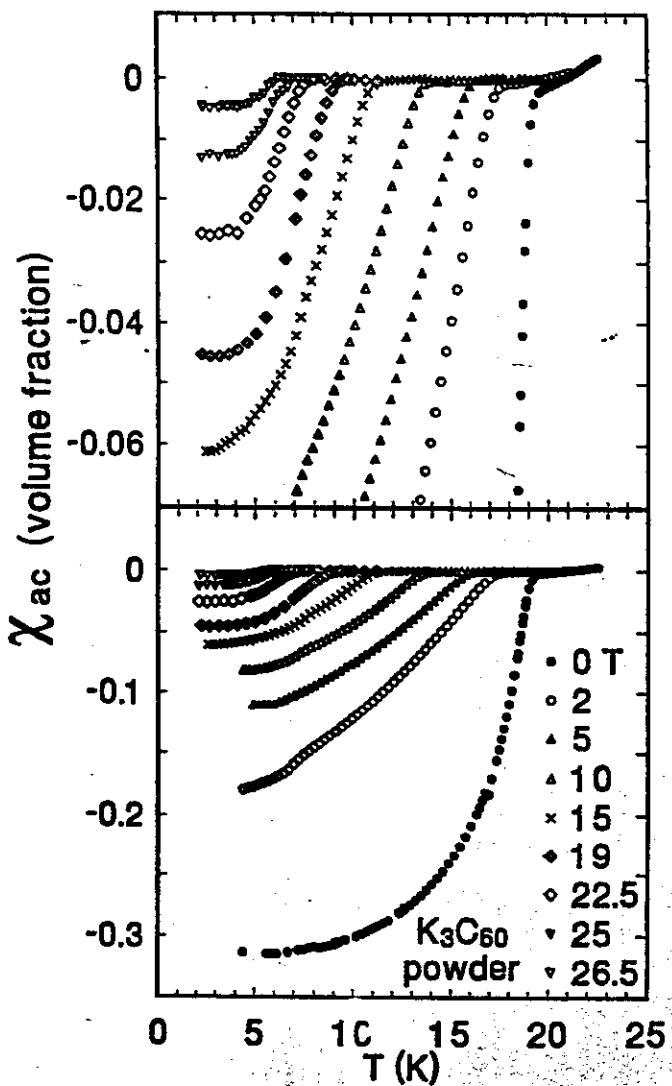


Fig. 4. Temperature dependence of the  $^{13}\text{C}$  spin-lattice relaxation time  $T_1$  in  $K_3C_{60}$  plotted as  $T_1 T$  versus  $T$ .

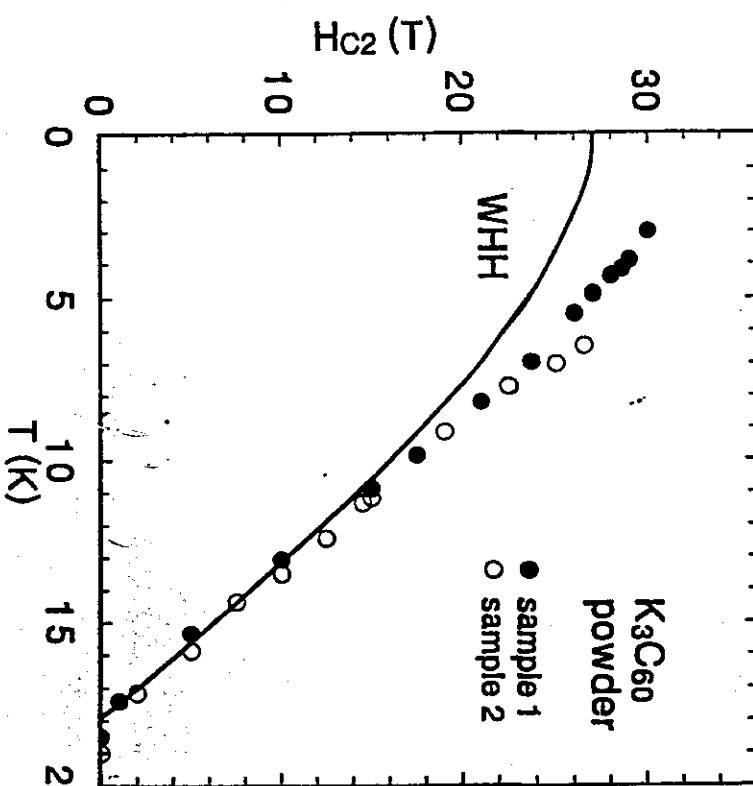
## Upper Critical field in $K_3C_{60}$

Boebinger, Palstra et al., preprint



③

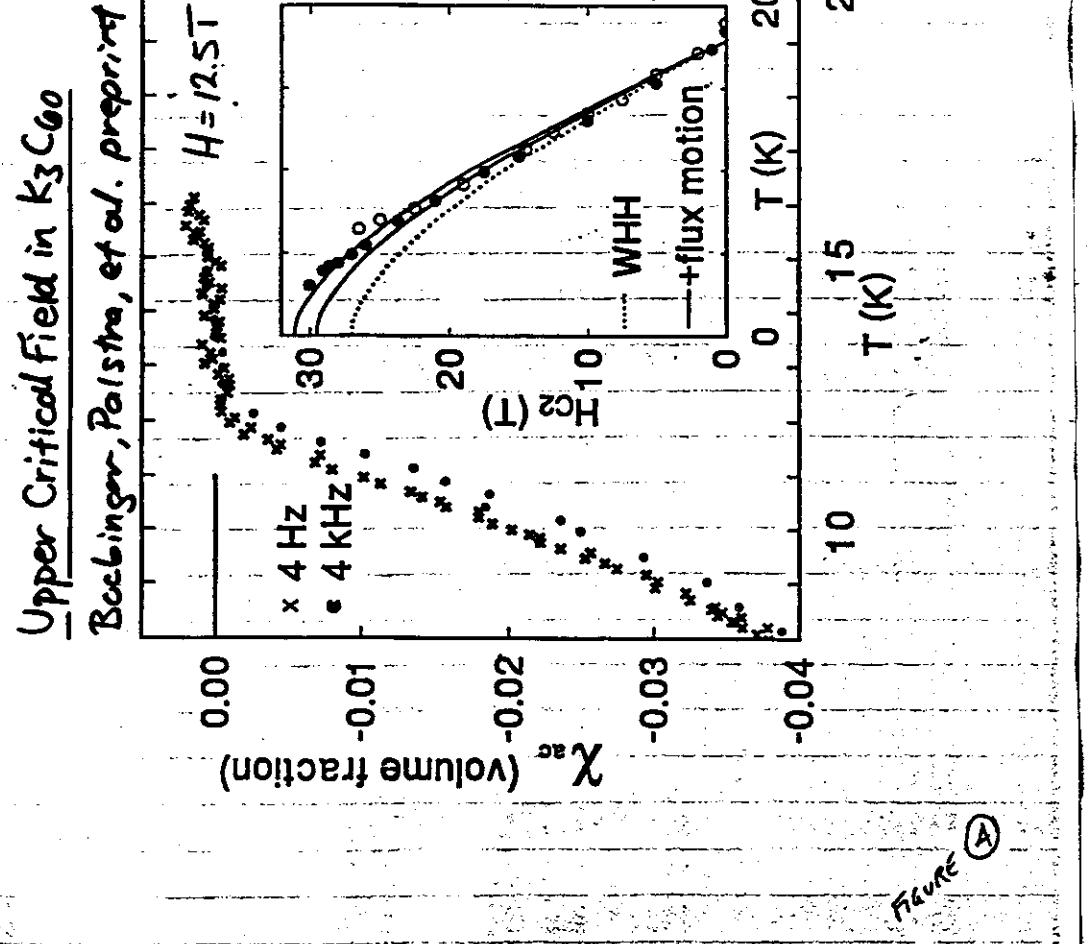
②



Upper Critical field in  $K_3C_{60}$

Boebinger, Palstra et al., preprint

### Upper Critical Field in $K_3C_{60}$



$(KRS)_3C_{60}$

This study begs question: how far can the letters be pulled apart?  
 $Rb_2CsC_{60} \rightarrow T_c \sim 33K$ .

Also: what are neighbouring structures?  
are they S.C.

### Ring Currents in Icosahedral $C_{60}$

Pasquarello, Schlüter, Haddon, preprint

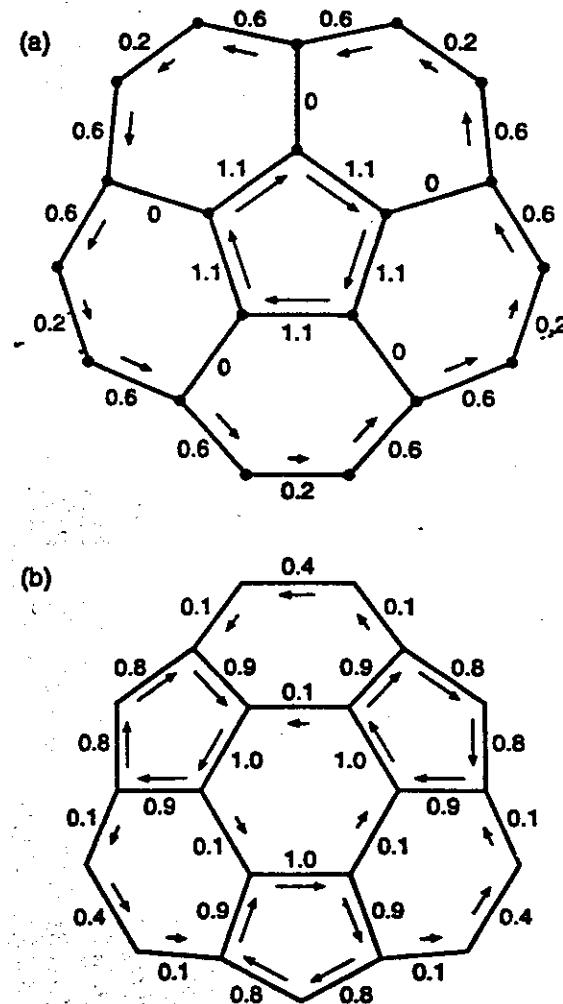


Figure 1

# Ring Currents in Icosahedral C<sub>60</sub>

Pasquarello, Schlüter, Haddon, preprint

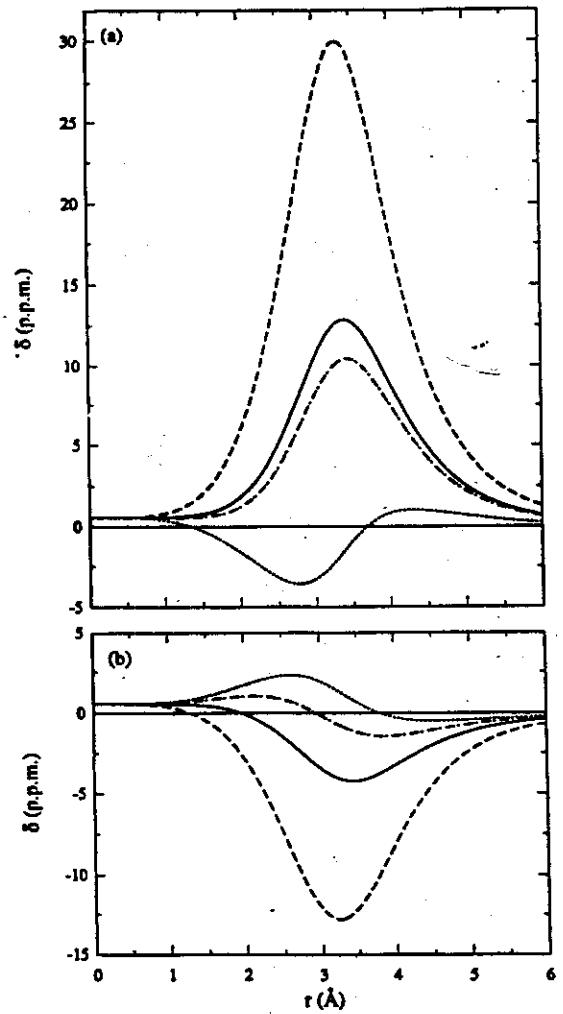


Figure 2

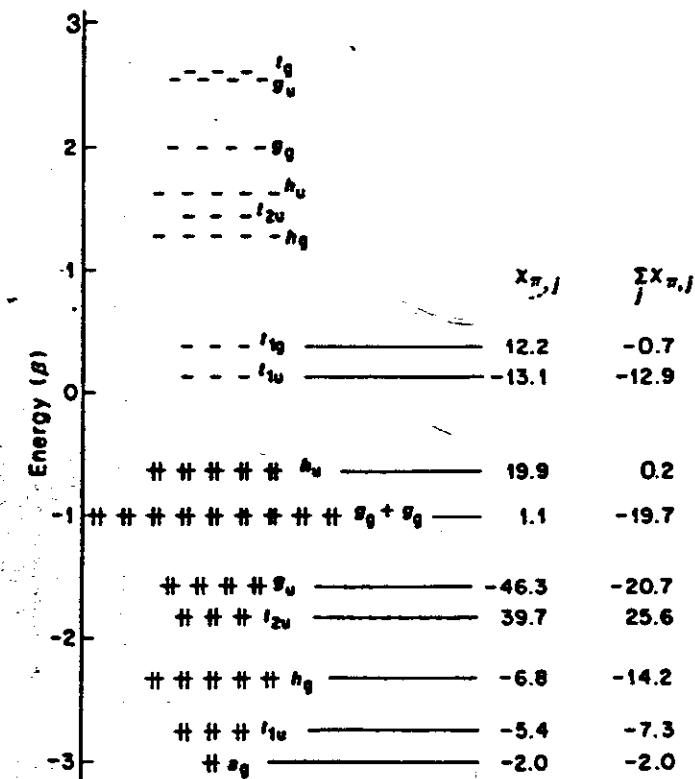


Fig. 2 Hückel molecular orbital<sup>20</sup>,  $j$ , energy levels in units of  $\beta$  and  $\pi$ -orbital magnetic susceptibilities in units of  $|\chi_\pi^{\text{benzene}}|$  calculated for  $C_{60}$  with a common resonance integral. Occupation of an orbital is denoted by a solid vertical line; labels refer to irreducible representations of the icosahedral point group.

## Contributions to Normal State Susceptibility

$$\chi_{\text{exp}} = \chi_p + \chi_{\text{orb}} + \chi_L + \chi_{\text{core}}$$

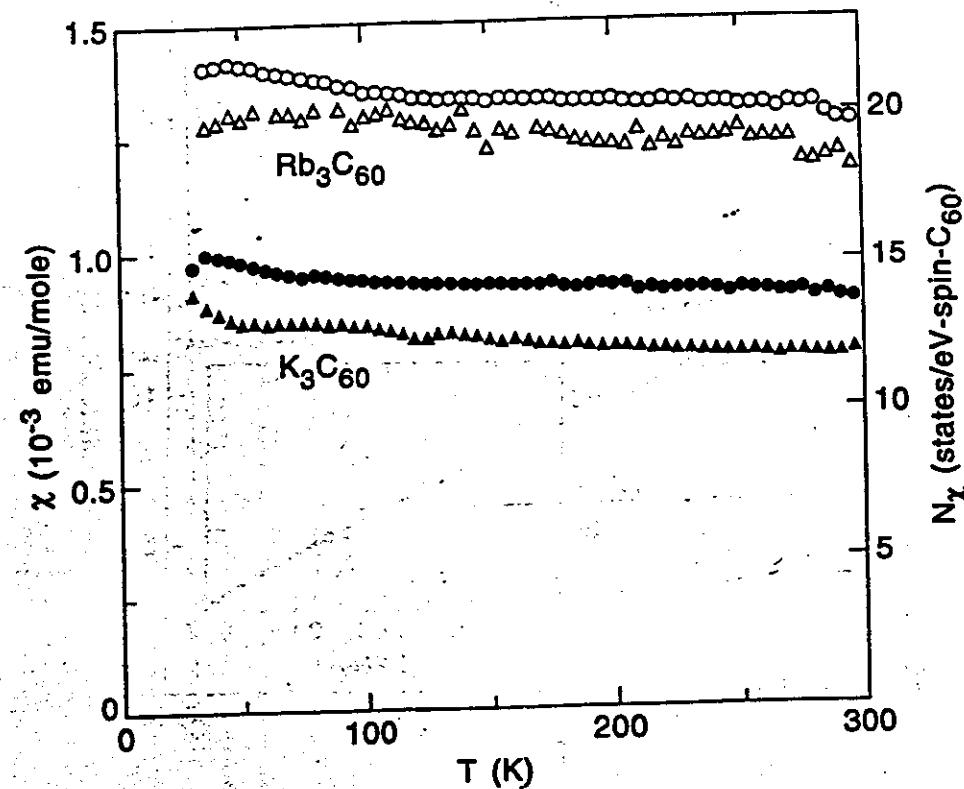
Pauli spin susceptibility (+)  
 $\chi_p = \mu_B^2 N(E_F)$

Conduction electron orbital analogue of van Cnick (+)  
 Orbital-energy denominator large -  
 High symmetry (ring currents) cancel (neglect)

Landau diamagnetism (-)  
 Landau - neglect for strong disorder  
 (is this reasonable?)

Core diamagnetism (-)  
 Core - atomic (alkali) + molecular ( $C_60$ )  
 $\chi_{\text{core}} \approx 80 + 260 \text{ ppm} \approx \frac{1}{3} \chi_{\text{exp}}$

## Normal State Susceptibility - $K_3C_60$ , $Rb_3C_60$

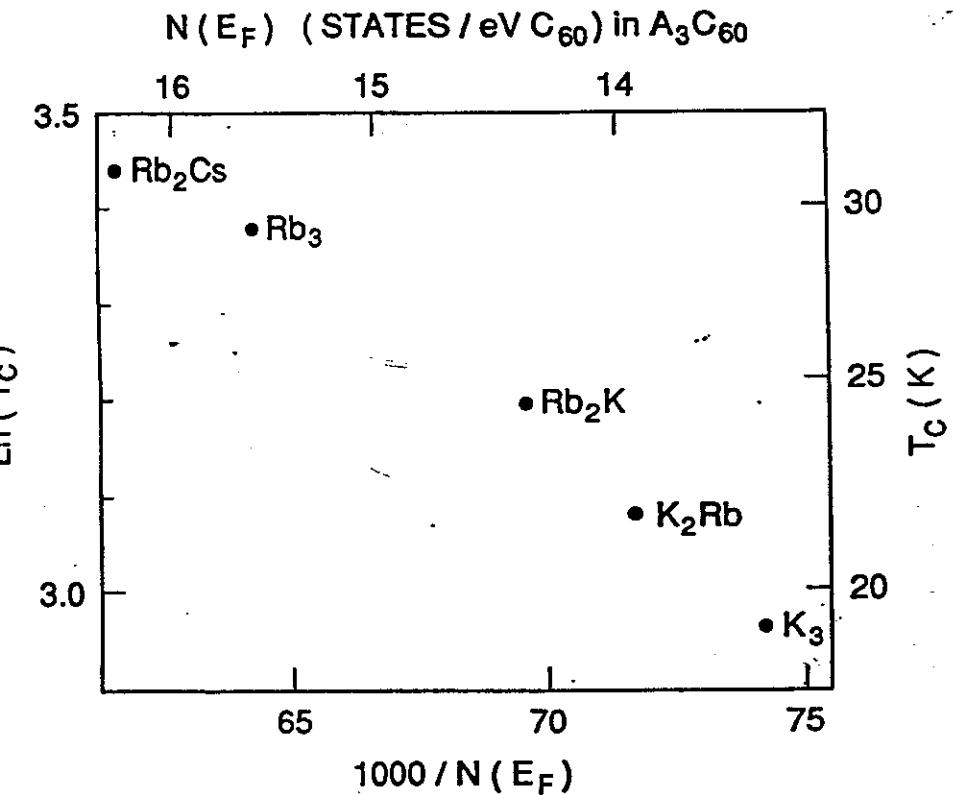


- Note large ~35-40% change in  $\chi$
- Compare to 14% change (Hückel)  
22% " (LDA)

Fig 1.

## Density of States - $T_c$ Relationship

Haddon, Accs. Chem. Res.

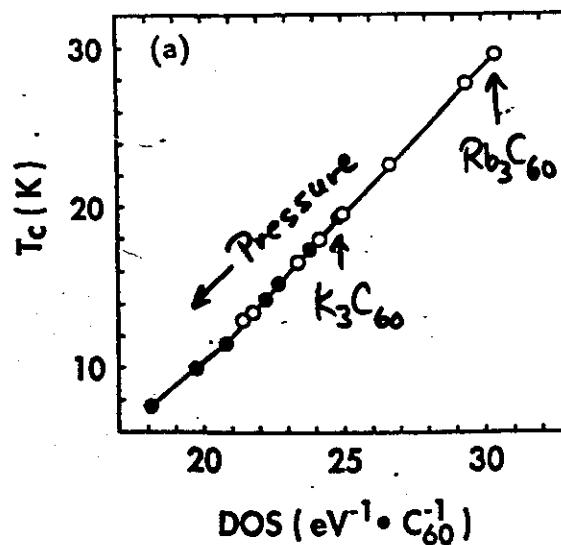


- DOS calculated by extended Hückel method
- $N_o(Rb_3C_{60})/N_o(K_3C_{60}) = \underline{1.14}$

(7)

## Density of States - $T_c$ Relationship

Oshiyama + Saito, Sol. St. Comm., 82, 41 (1992)



- DOS calculated w/ LDA using measured lattice constants
- $N_o(Rb_3C_{60})/N_o(K_3C_{60}) \approx 1.22$

## Effect of Orientational Disorder on Electronic Structure

Gelfand - Lu, PRL, 68, 1050 (1992)

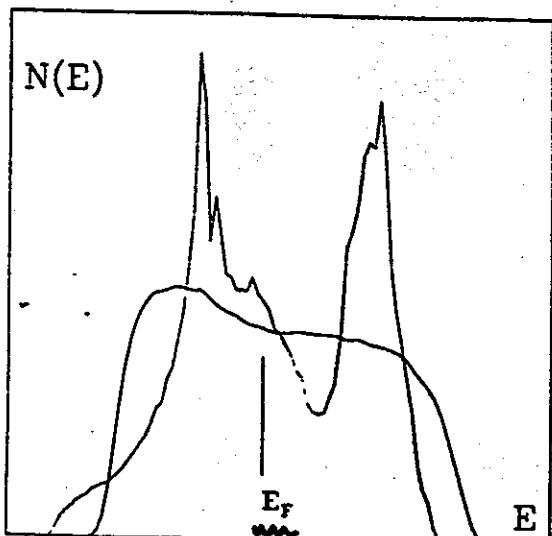


FIG. 3. Densities of states vs energy for the  $Fm\bar{3}$  structure and its maximally disordered version; the former is the one with two large peaks. The Fermi energy for three electrons per molecule is indicated; it is nearly unchanged upon disordering.

- Use radial  $p_z$  (Hückel) orbitals
- Two inequivalent ( $\pi/2$ ) orientations  $\Rightarrow$  vastly different hopping amplitudes (wf. phase mismatch)
- Little effect on  $N_e$

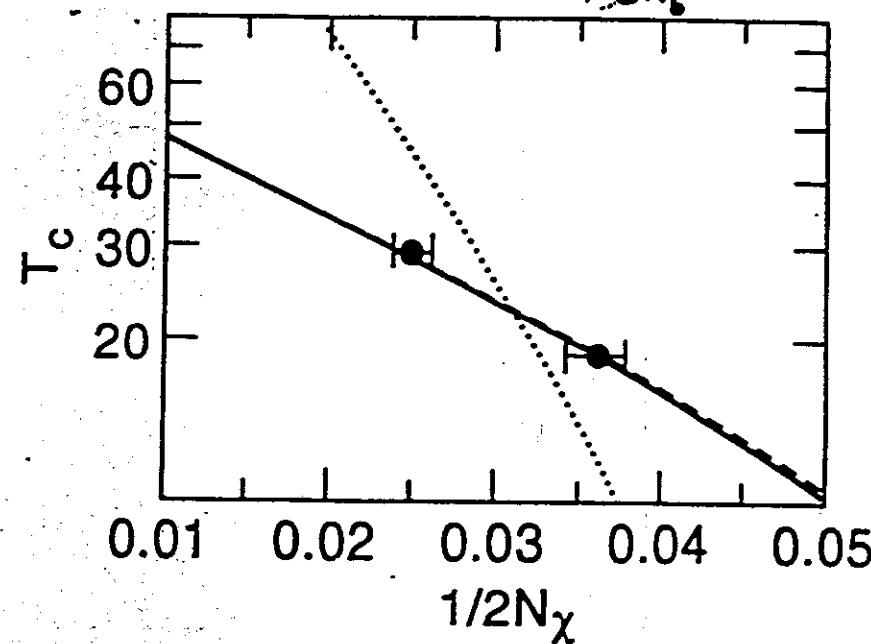
## Variation of $N$ within McMillan formalism

$$T_c = \frac{\langle \omega \rangle}{1.2} \exp \left[ -\frac{1.04(1+\lambda)}{\lambda - \mu^*(1+0.62\lambda)} \right]$$

.....  $\langle \omega \rangle = 1400$  K

—  $\langle \omega \rangle = 200$  K

---  $\langle \omega \rangle = 1400$  K and  $N_x = \frac{N_0}{1-IN_b}$ ,  $I=0.05$



One way to explain large  $N(\epsilon_F)$  changes

Stoner enhancement -

$$N_{\text{meas}} = \frac{N_{\text{bare}}}{1 - I N_{\text{bare}}}$$

$N_{\text{meas}}$  = measured density of states

$N_{\text{bare}}$  = bare density of states ( $N$  in McMeagn.)

Then, assuming  $\omega_{\text{ex}} = 1400$  K, get 2-3 enhancement's of  $N$ .

$$N_{\text{bare}}(K) \approx 4.5 \text{ states/eV spin}^{(2)}$$

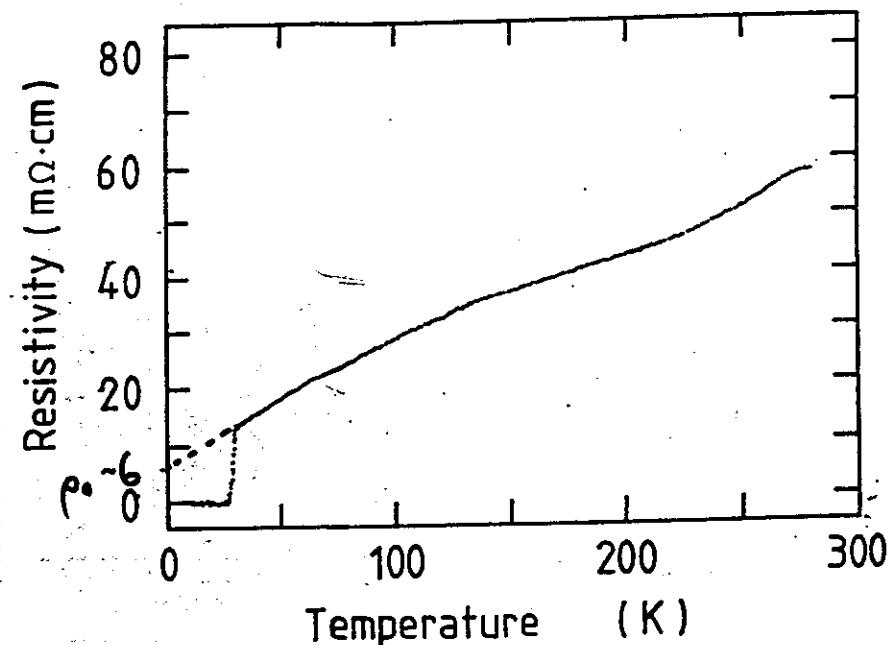
$$N_{\text{bare}}(R6) \approx 5.6 \text{ " " " }$$

"Explains" discrepancy between NMR, photoemission

Introduces extra parameter, relating to spin fluctuations - (effect on superconductivity?)

### Resistivity of single crystal used in Thermopower measurement

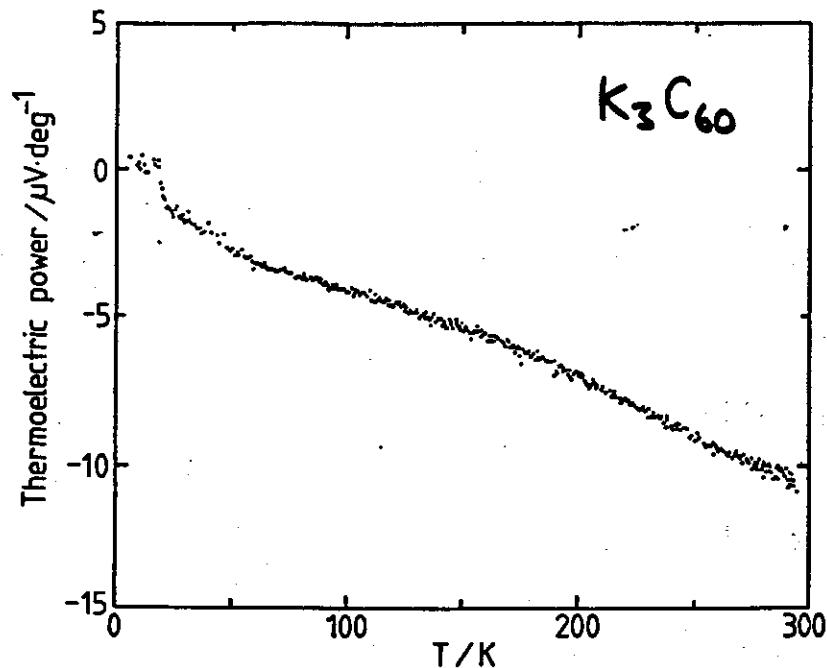
Inabe et al., preprint



- Large  $\rho_0 \sim 6 \text{ m}\Omega\text{-cm}$  illustrates problem of doping single crystals.

## Thermopower in single crystal $K_3C_{60}$ , $Rb_3C_{60}$

Inabe et al., preprint



$$S(T) = \frac{\pi^2 k^2 T}{3e} \frac{1}{2E_F} \Rightarrow E_F \sim 0.35 \text{ eV}$$

(electrons)

$$N_{Rb}/N_K \sim 1.5 - 1.8$$

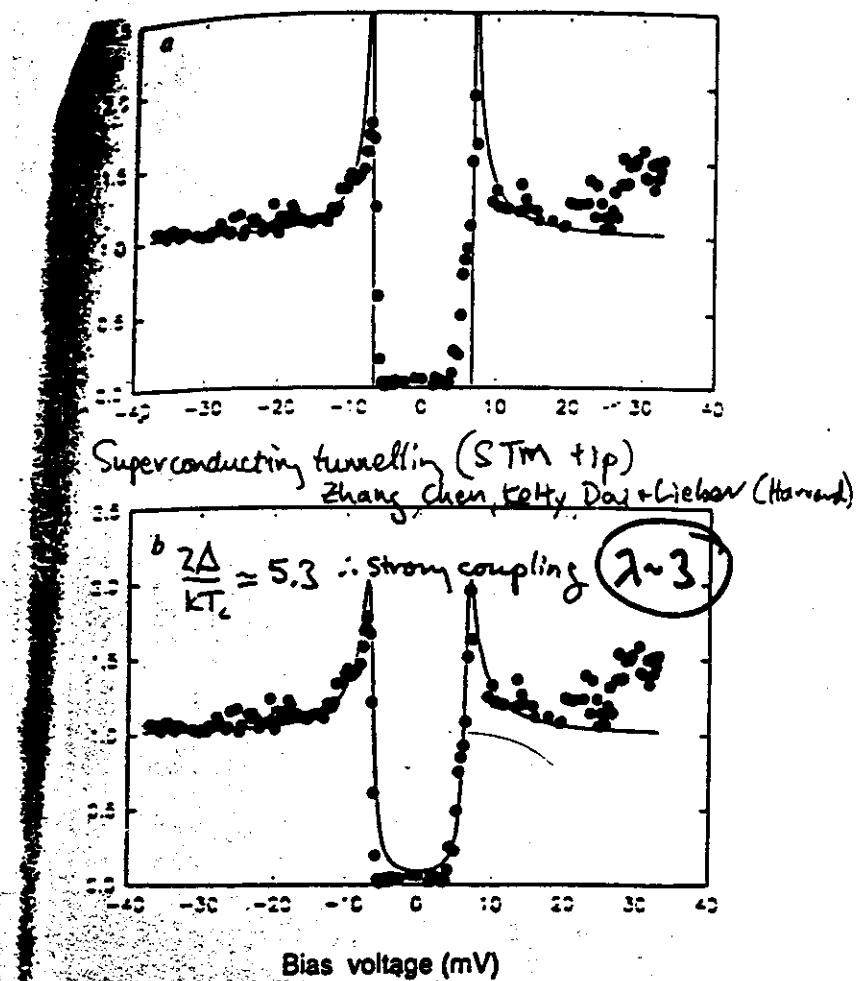


Fig. 3 Plots of  $dI/dV$  against voltage (mV) for  $Rb_3C_{60}$  at 4.2 K. The experimental data for conductance (solid circles) were calculated numerically from the  $I-V$  data in Fig. 2a. a. The data are fitted with the expression  $dI/dV = eV/[(eV)^2 - \Delta^2]^{1/2}$  (solid curve) with  $\Delta = 6.8$  meV. b. The data are fitted with the expression  $dI/dV = Re[(eV - i\Gamma)/(eV - i\Gamma)^2 - \Delta^2]^{1/2}$  which includes broadening by  $\Gamma$ . The values of  $\Delta$  and  $\Gamma$  are 6.6 and 0.6 meV, respectively.

NMR

VOLUME 68, NUMBER 12

PHYSICAL REVIEW LETTERS

Tycho

23 MARCH 1992

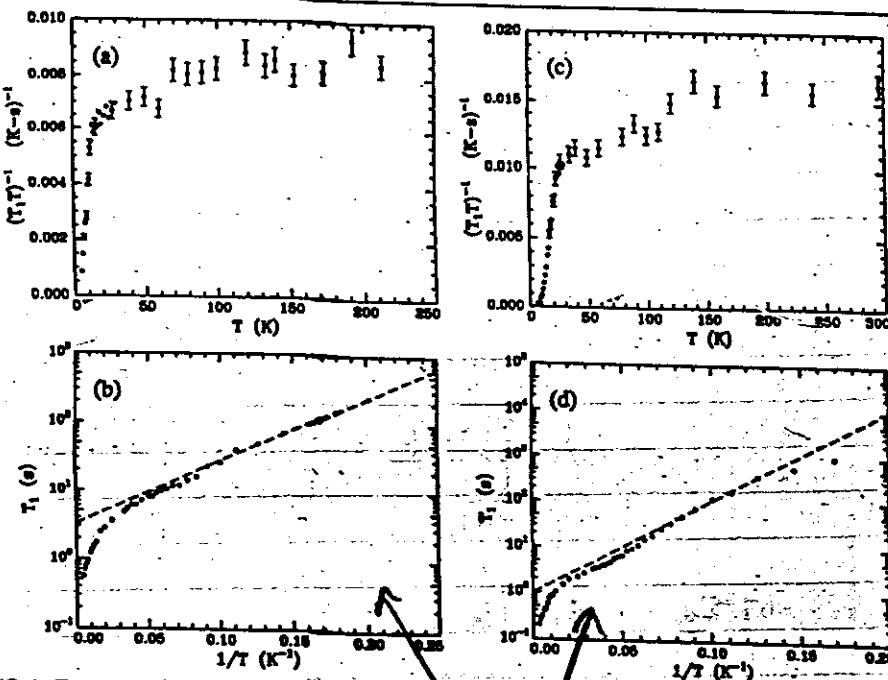


FIG. 1. Temperature dependence of the  $^{13}\text{C}$  spin-lattice relaxation time  $T_1$  in (a), (b)  $K_3\text{Co}_6$  and (c), (d)  $Rb_2\text{Co}_3$ , plotted as  $(T_1/T)^{-1}$  vs  $T$  [(a), (c)] and as  $\log T_1$  vs  $T^{-1}$  [(b), (d)]. Error bars indicate 1 standard deviation. Dashed lines are fits of the data below 9 K [(b)] and from 8 to 12 K [(d)] by Arrhenius law, leading to energy gaps  $\Delta_1 \approx 42$  K and  $\Delta_2 \approx 94$  K.

$$\frac{\Delta_1}{kT_c} \sim 3-4$$

$$2 \sim 1$$

### Specific Heat Jump at $T_c$

- Can distinguish between strong and weak coupling.

$$\Delta C \approx 1.43(1 + \lambda^2). \text{ (see graph)}$$

- Critical field technique found  $\Delta C = 90 \pm 15 \text{ mJ/mole-K}^2$ , consistent with BCS relation  $\Delta C = 1.43$ , and  $x_p$ .

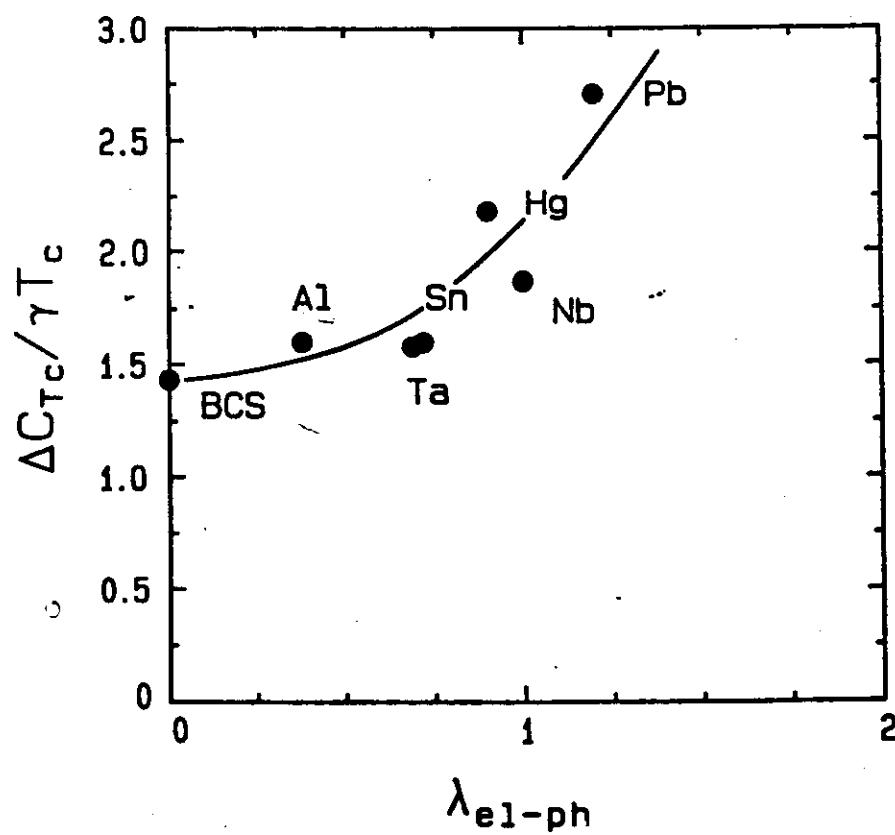
- Want to measure directly to check value.

- Use adiabatic technique. (good accuracy)



### Sample quality ( $K_3(C_6)$ )

- Neutron Rietveld refinement - < few % 2nd phase
- NMR - < few % 2nd phase (no detectable  $C_{60}$  signal)
- Diamagnetic shielding  $\sim 35\%$  among the highest measured for a powder sample, and consistent with 100% transformed fraction. Measured before + after - no change.



### Magnetization finite-size effect

Clem and Kogan, Jpn. J. App. Phys., 26, 1161 (1987)  
(also Schoenberg)

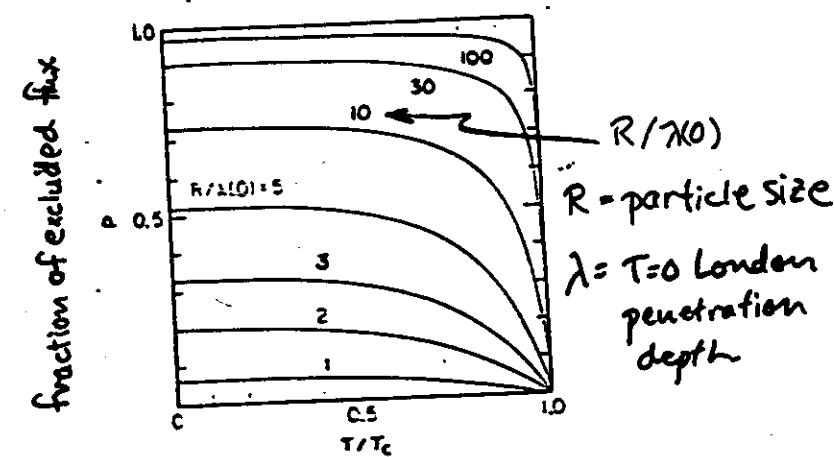


Fig. 1.  $P(R/\lambda)$  versus  $T/T_c$ .

FINITE-SIZE effects cont.

34

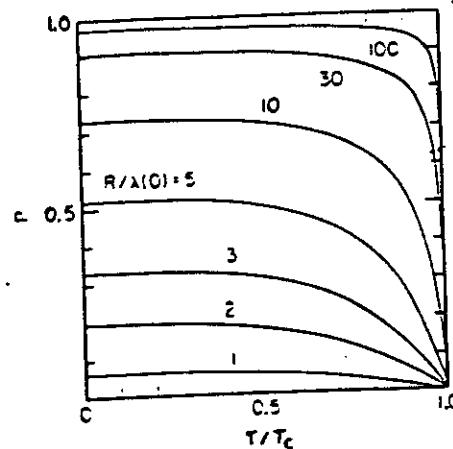
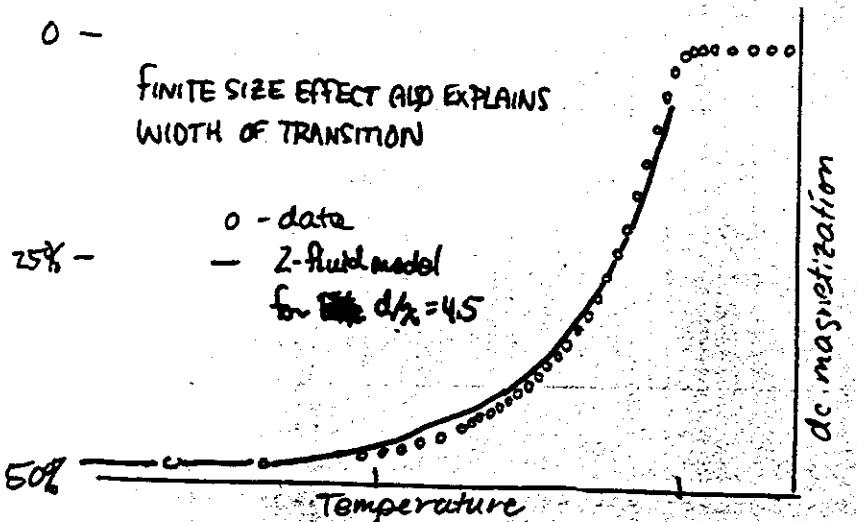
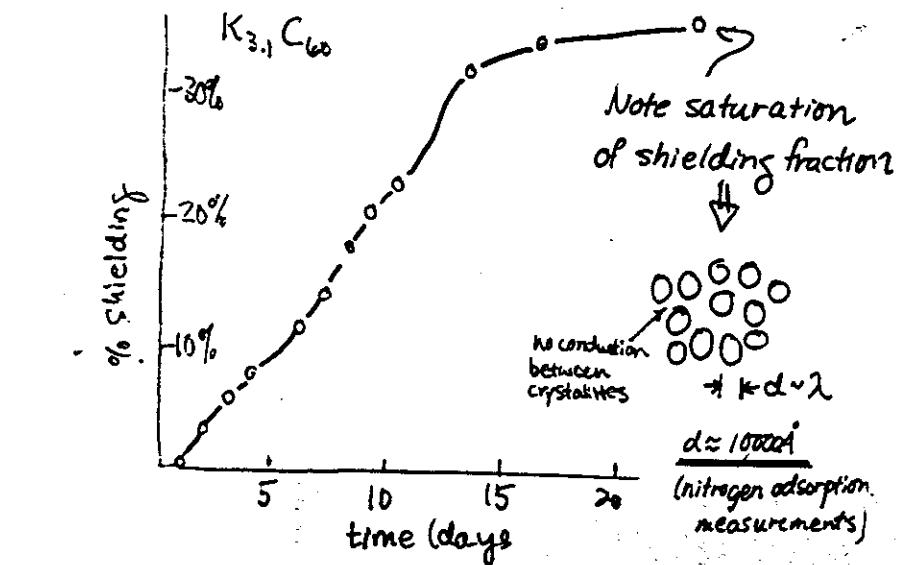
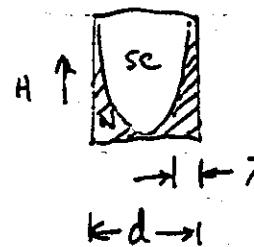


Fig. 1.  $P(R/\lambda)$  versus  $T/T_c$ .

## FINITE-SIZE effects

We know



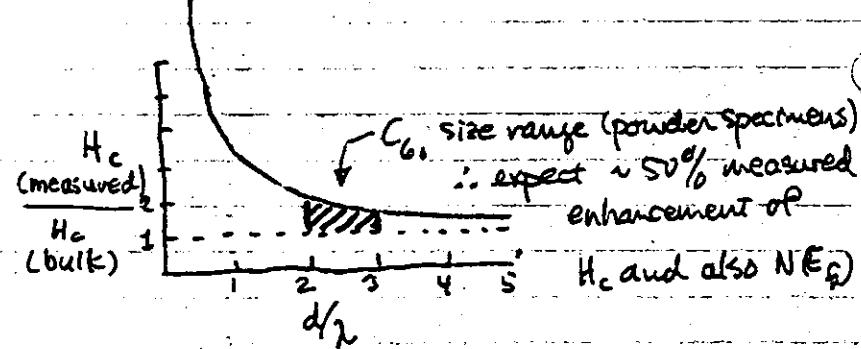
for small specimens,

$$|\bar{M}| < \frac{H}{4\pi}$$

Therefore, the critical fields are enhanced

$$\int_0^{H_c} M dH = F_s - F_v$$

e.g., for thin films. (London theory)

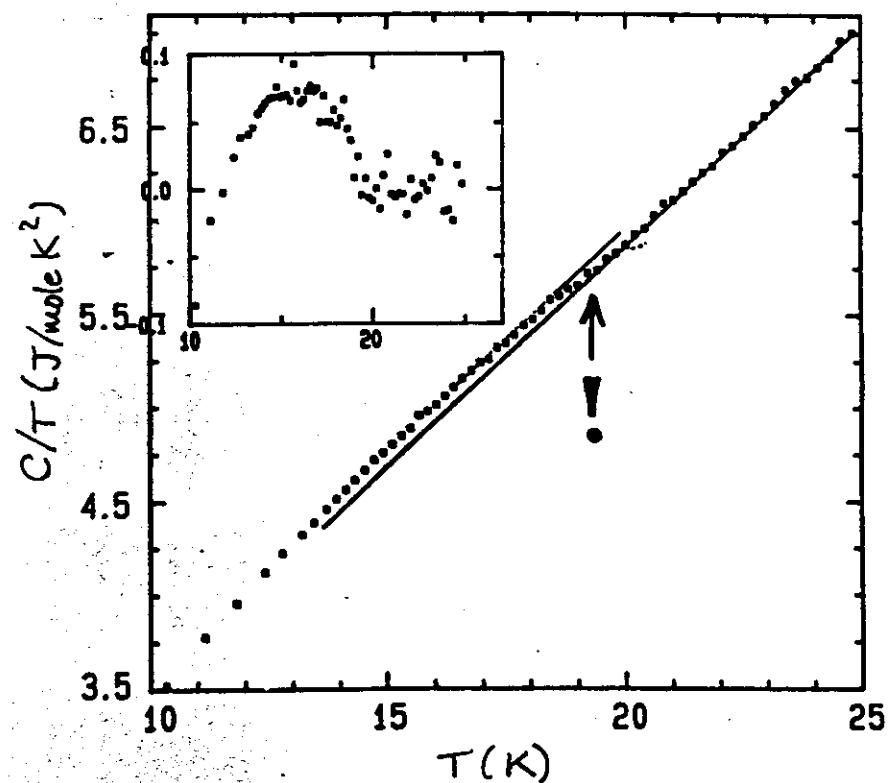


$$\therefore \text{Size-Corrected } N(E_F) \approx 15 \pm 5 \text{ states/eV } C_{60}$$

Close to Band value  $\approx 10$  states/eV  $C_{60}$   
(correlation effects)

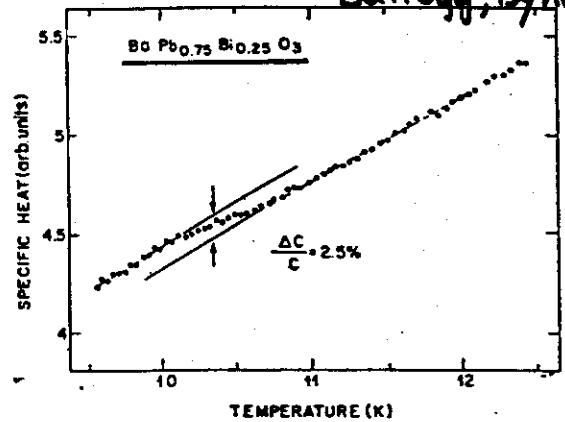
## Specific Heat Jump in $K_3C_{60}$

High precision - with addendum



## Specific heat jump at $T_c$ - polycrystalline samples

Ba+logg, Dynes Physica 1268(1984)



High resolution measurements of the specific heat. The small anomaly at  $T_c$  corresponds to a Sommerfeld constant  $\gamma$  of  $1.5 \pm 0.2 \text{ mJ/mole K}^2$ .

Ramirez et al., PRB (1987)

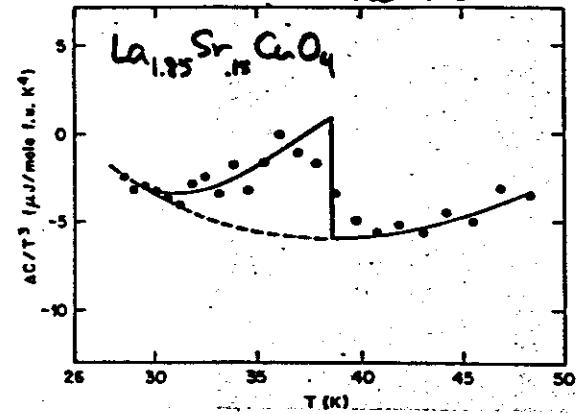
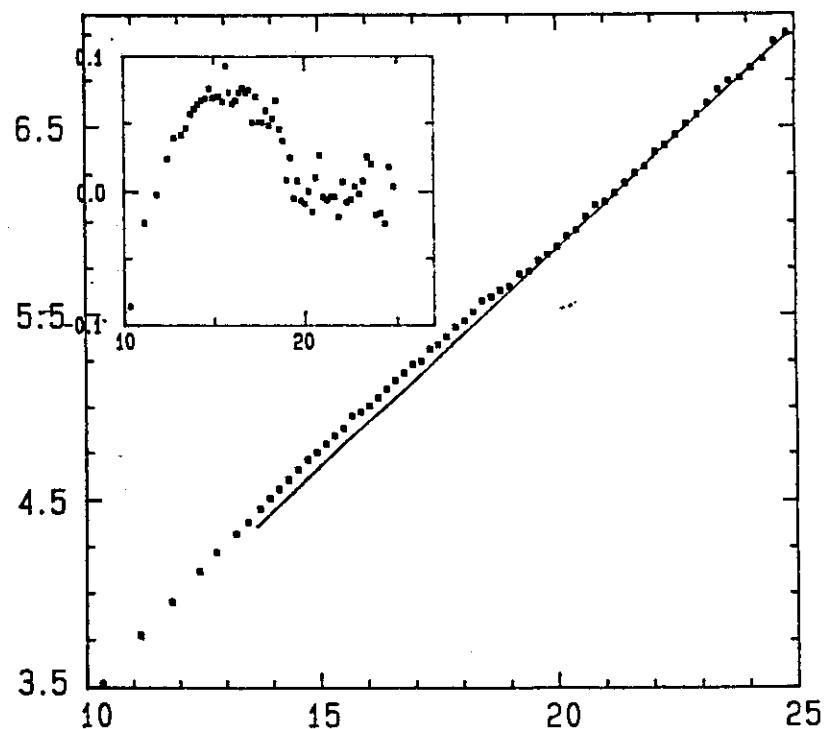


FIG. 4. The specific-heat difference  $\Delta C$  between the measured values and the results of the fitting procedure as described in the text, in the vicinity of  $T_c$ . The curves shown here are guides to the eye and the jump at  $T_c$  is estimated to be  $10 \pm 2 \text{ mJ/mole f.u. K}^2$ .



## Specific Heat of $K_3C_{60}$

Ramirez, Rosseinsky, Murphy, Haddon  
preprint, AT+T.

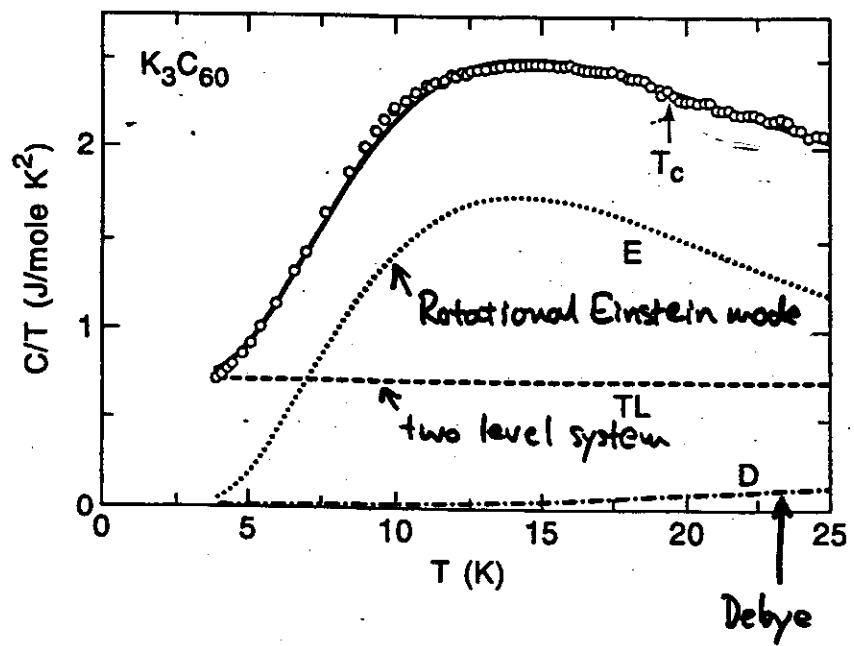


Fig. 2

## Specific Heat of $K_3C_{60}$

Ramirez, Rosseinsky, Murphy, Haddon  
preprint, AT+T

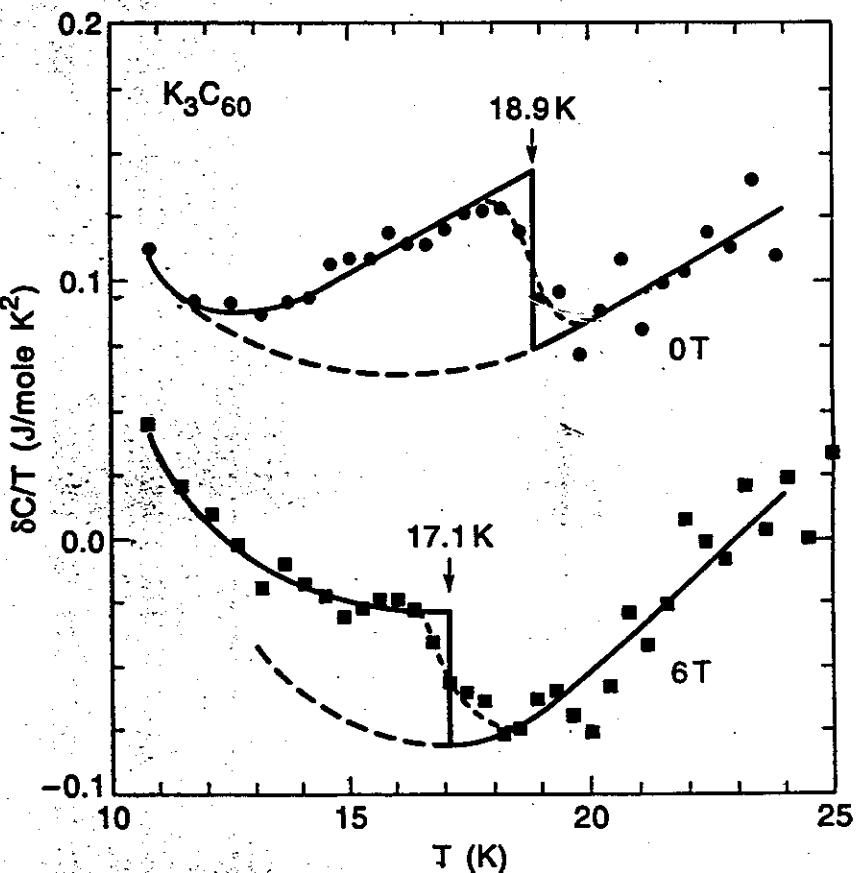


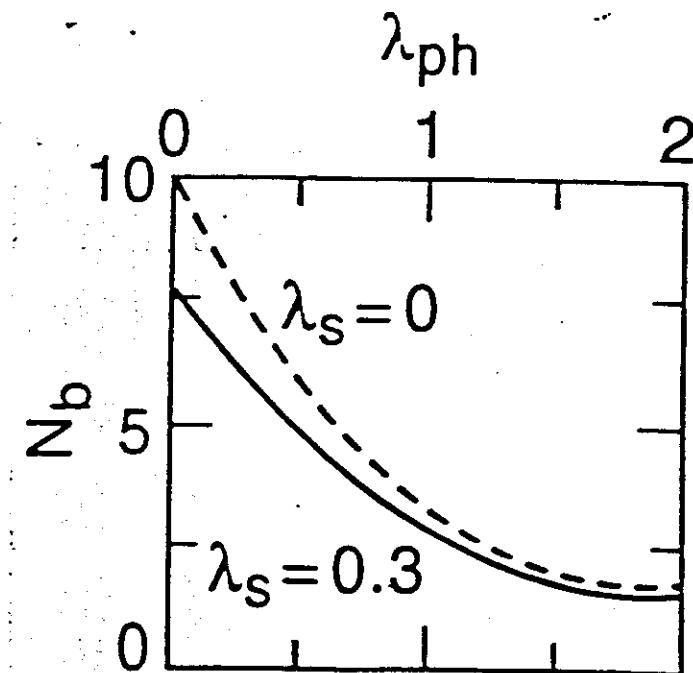
Fig. 3

Specific Heat Jump

$$\frac{\Delta C}{T_c} \approx 68 \pm 13 \text{ mJ/molek}^2$$

$$\frac{\Delta C}{T_c} = 1.43(1 + 0.5\lambda_{ph}^2) x$$

$$x = \frac{2\pi^2 k_B^2}{3} (1 + \lambda_{ph} + \lambda_S) N_b$$



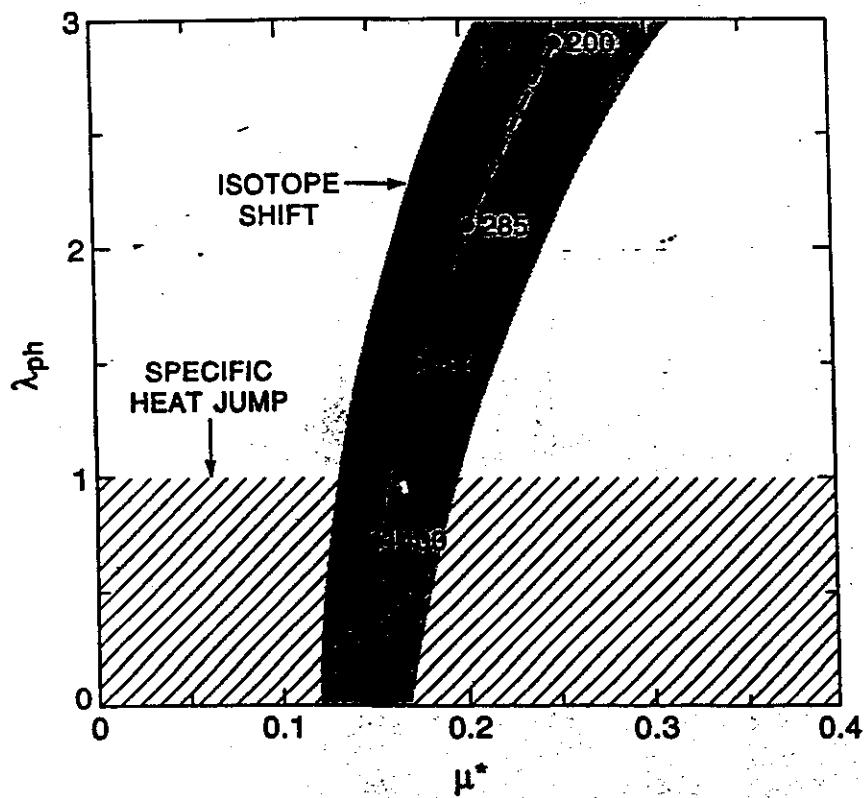
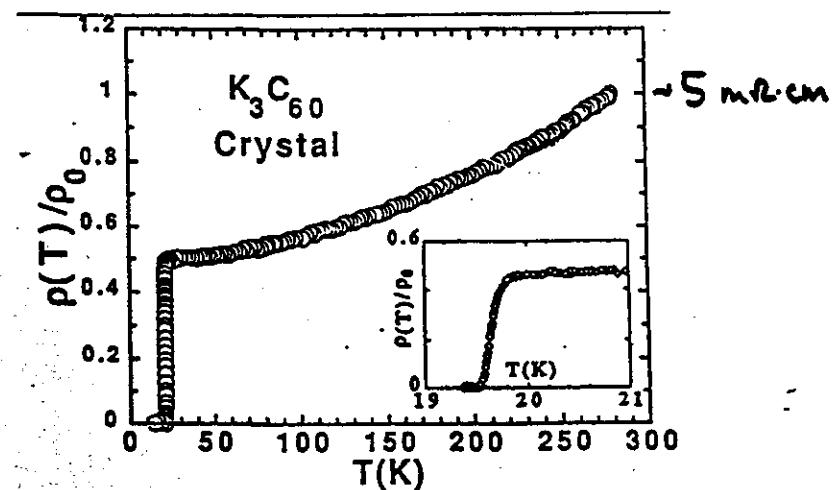


Fig. 4

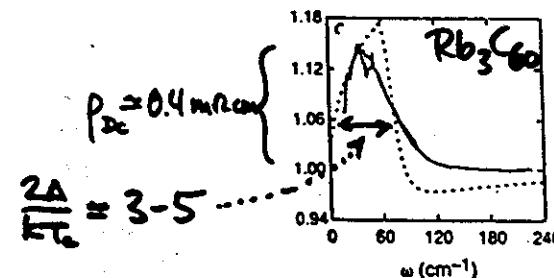
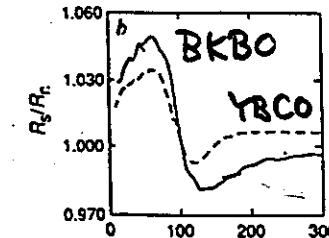
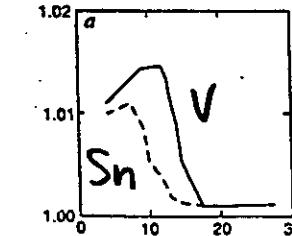
## Resistivity of single crystal $K_3C_{60}$

Xiang et al., Science, May 1992



- $\rho(T_c) \sim 2.5 \text{ m}\Omega\cdot\text{cm} \approx \rho_{\text{film}}(T_c)$
- Possible diffusion barrier

Infrared Reflectivity  
Rotter et al, Nature, 355, 532 (1992)



$$\rho_{dc} = \frac{\pi R_n^2}{2 \omega n} \left( \frac{R_s}{R_n} - 1 \right)^2$$

FIG. 1. a, The ratio of reflectivity in the superconducting state to that in the normal state measured in a cavity geometry is shown for vanadium (solid line) and tin (dashed). From these data, Richards and Tinkham<sup>4</sup> inferred energy gaps of  $2\Delta = 3.5kT_c$  for these superconductors. b, Similar reflectivity ratio from  $\text{Ba}_2\text{K}_3\text{BiO}_3$ , from which a gap  $2\Delta = 3.5kT_c$  was inferred<sup>5</sup>. The dashed curve is  $R_s/R_n$  for  $\text{YBa}_2\text{Cu}_3\text{O}_7$ , scaled on the frequency axis by 0.15 (ref. 12). c, Ratio of the superconducting (8 K) to normal (35 K) reflectivities for  $\text{Rb}_3\text{C}_60$ . The dotted curve shows for comparison a calculation<sup>16</sup> of  $R_s/R_n$  for a superconductor/sapphire interface for a moderately dirty superconductor ( $\rho_{dc} = 0.4 \text{ m}\Omega \text{ cm}$ ) with  $2\Delta = 60 \text{ cm}^{-1}$ .

Specific heat jump - continued.

Relationship between  $\gamma$ ,  $H'_{C2} = dH_{C2}/dT$

Clean limit

$$H'_{C2} = -1.5 \times 10^{-4} \gamma^2 T_c$$

$\uparrow$                        $\uparrow$   
 $2 \text{ Tesla/K}$        $\gamma \approx 38 \text{ mJoule/K}^2$   
 $\swarrow$                        $\downarrow$   
 $? \approx 0.2 \text{ Tesla/K}$

∴ Dirty limit

$$H'_{C2} = -0.89(1.5 \times 10^{-4} \gamma^2 T_c + 4.7 \times 10^{-4} \gamma \rho)$$

↓ Resistivity

Can derive  $\rho = 0.5 \text{ m}\Omega \text{ cm}$

$\bullet$   $\Gamma = v_F z = 48 \times 10^3 / \rho \approx 10 \text{ \AA} \text{ high orient. disorder}$

Explains low  $\xi_{GL} = \sqrt{\xi_0 \Gamma} \approx 26 \text{ \AA}$   
 for  $\xi_0 \approx 120 \text{ \AA}$

agrees with IRM theory

# Fermi Surface of $K_3C_{60}$

Erwin and Pickett, Science 254, 842 (1991)



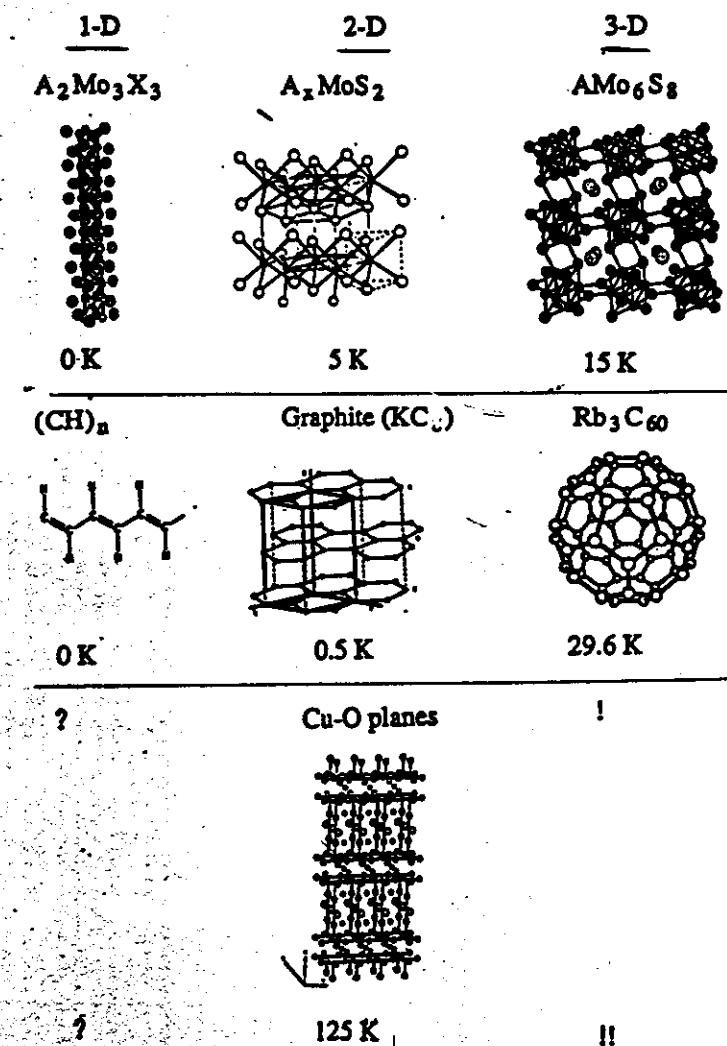
Fig. 2. First (blue) and second (yellow) sheets of the  $K_3C_{60}$  Fermi surface, each enclosing unoccupied states. Part of the second sheet is cut away to reveal the first sheet inside.



Fig. 3. Repeated-zone representation for the second sheet of the Fermi surface for  $K_3C_{60}$ , which holds the charge carriers that become superconducting. The two symmetry-equivalent pieces (shown in different colors) are multiply connected along Cartesian axes; although interconverting

## DIMENSIONALITY AND SUPERCONDUCTIVITY

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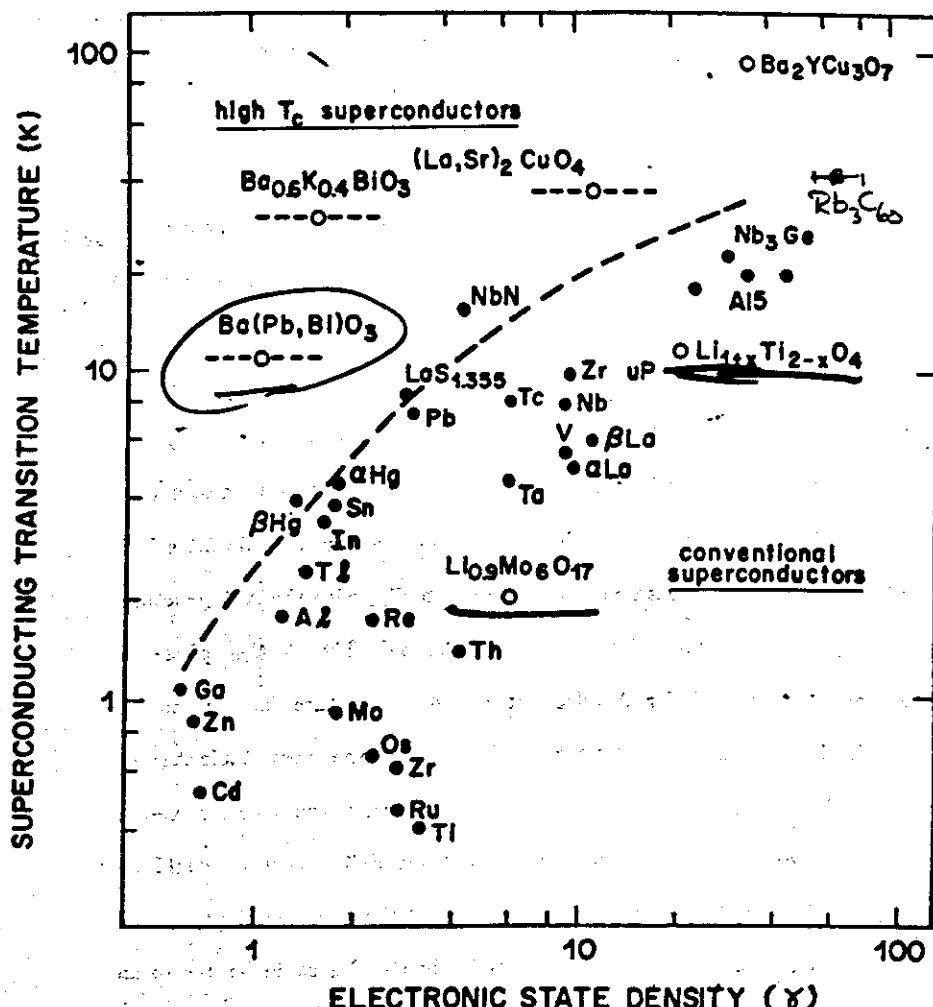
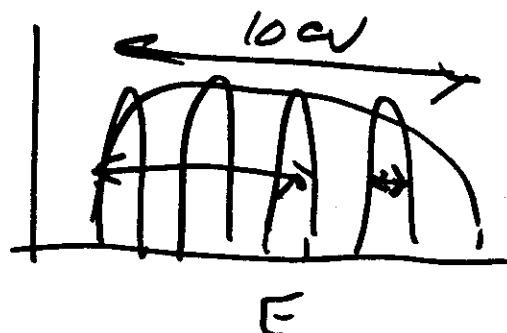


### Specific Heat — Conclusion

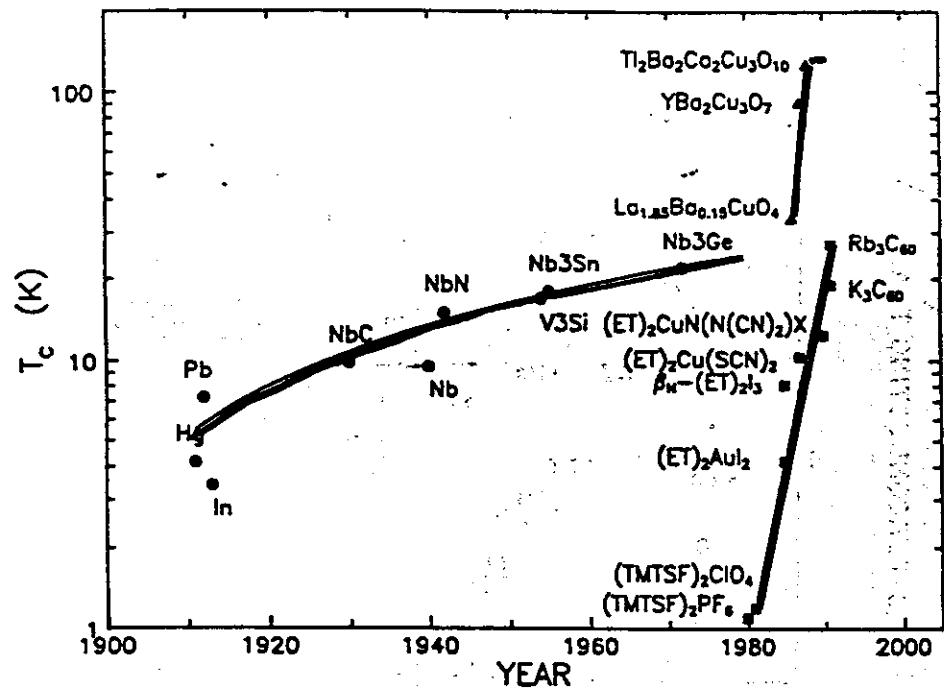
- Magnitude of jump,  $\Delta C/T_c$  is consistent with weak coupling,  $\lambda \lesssim 1$ , and probably not with the tunneling  $\lambda$ .

### General Conclusions

- $A_3C_{60}$  looks like a conventional phonon mediated superconductor, where  $\langle\omega\rangle$  is an intramolecular phonon frequency,  $\approx 1500$  K.
- Still have problem with Migdal's theorem.
- Unlikely to find  $T_c > 33$  K by electron doping into the  $t_1$  levels.
- Superconductivity in  $A_3C_{60}$  demonstrates the principle of working towards 3-dimensional molecular systems for higher  $T_c$ 's.

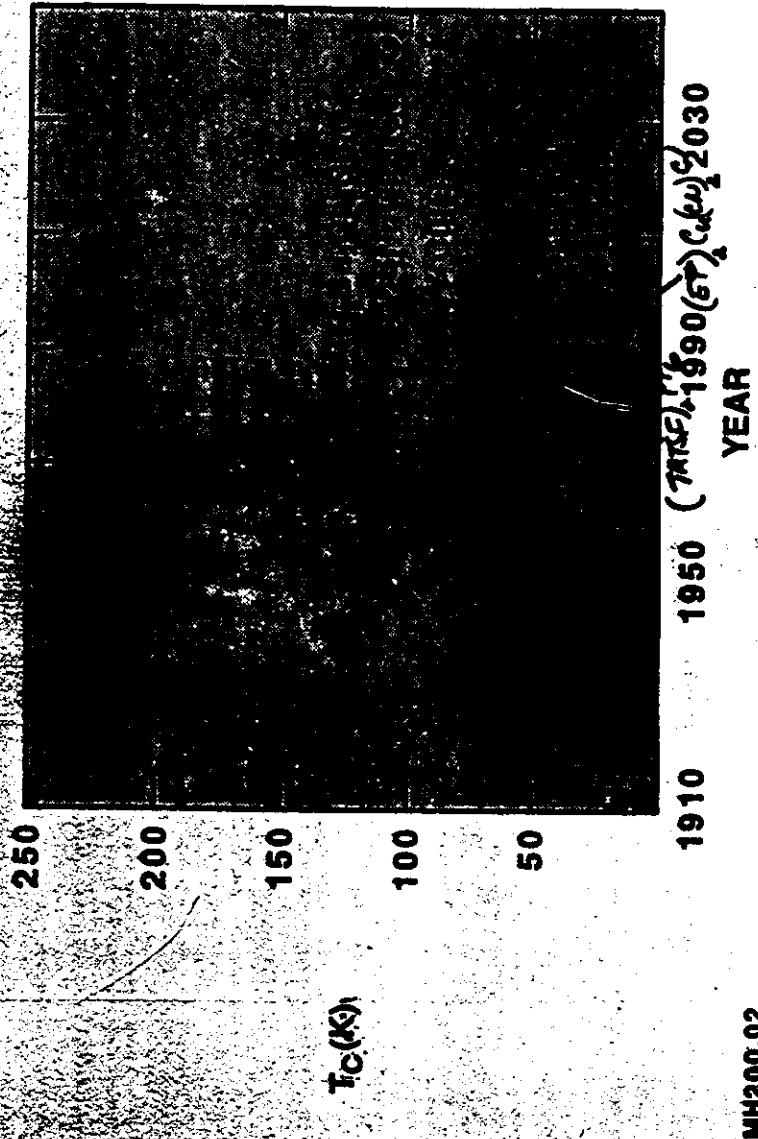


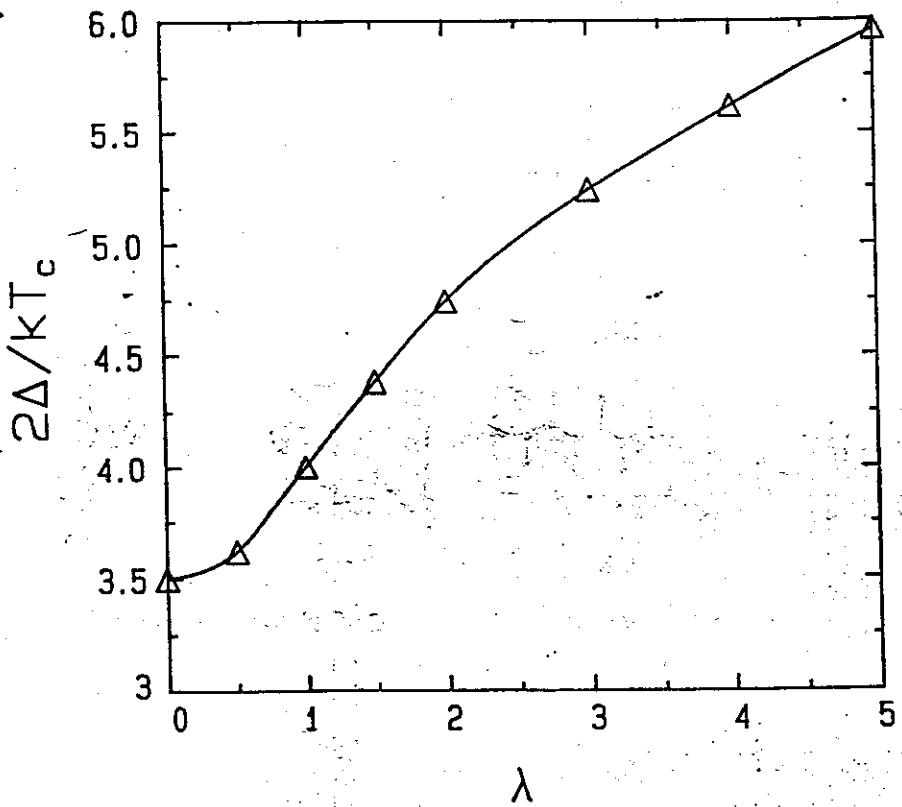
## PROGRESS of $T_c$ with TIME



Jerome  
Cond. Mat. News 1 (1992)

## MAXIMUM $T_c$ vs. TIME





### Density of States (cont.)

- Specific heat  $N_0$  consistent with band structure  $N_0$ .
- Susceptibility  $N_0$  magnitude also consistent, but change from  $K_3$  to  $Rb_3$  is twice too large.
- Can reconcile with Stoner enhancement,  $N_{\text{meas}} = N_{\text{bare}} / (1 - IN_{\text{bare}})$ .  
Need  $I \approx 2$ , for high energy phonons.
- If  $\langle n \rangle$  is small,  $\approx 200$  K, however, then no enhancement.

### Density of States $A_3C_{60}$ - Summary

	$N_{\text{bare}}$	$N_x$	$N_g$
NMR	-	20	-
XPS	2	-	-
critical fields	-	-	13
Susceptib. "4-5"	20	-	
specific heat	"4-6"	-	"13"
LDA	6		

$$N_x \approx \frac{N_b}{1 - IN_b}$$

$$N_g = N_b(1 + \lambda_{ph})$$

Specific Heat Jump  $K_3C_{60}$   
(phonon background subtracted)

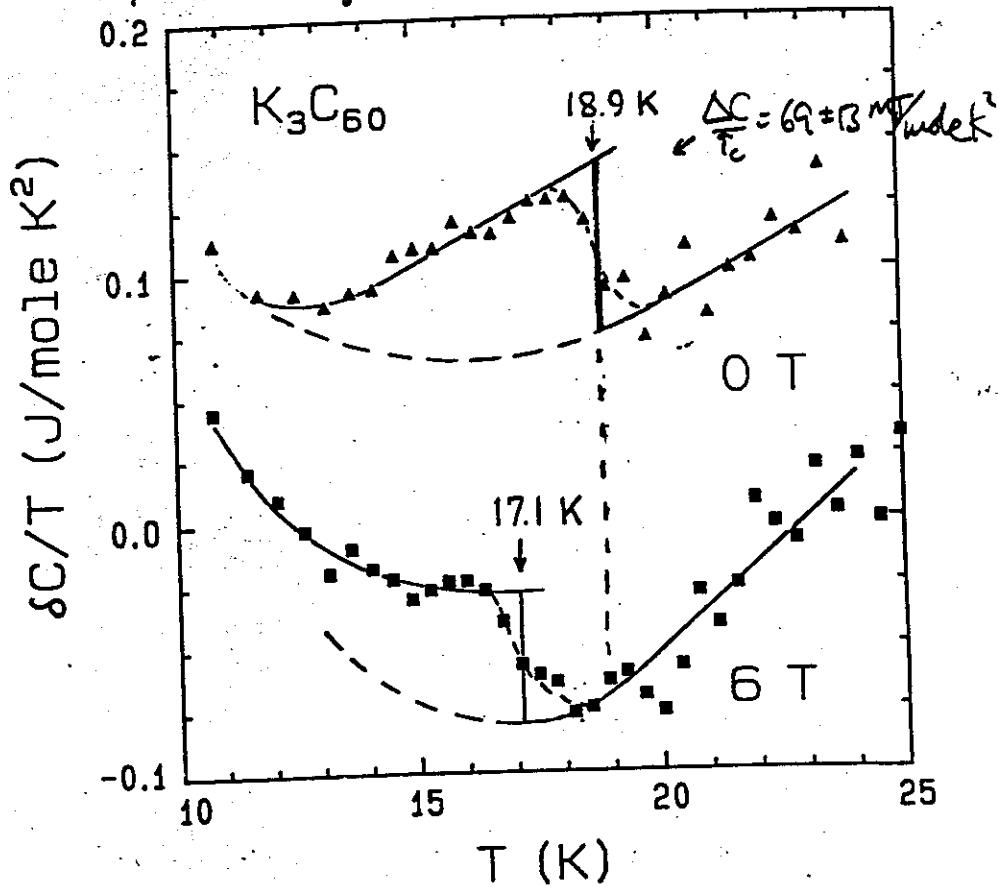


Fig. 2

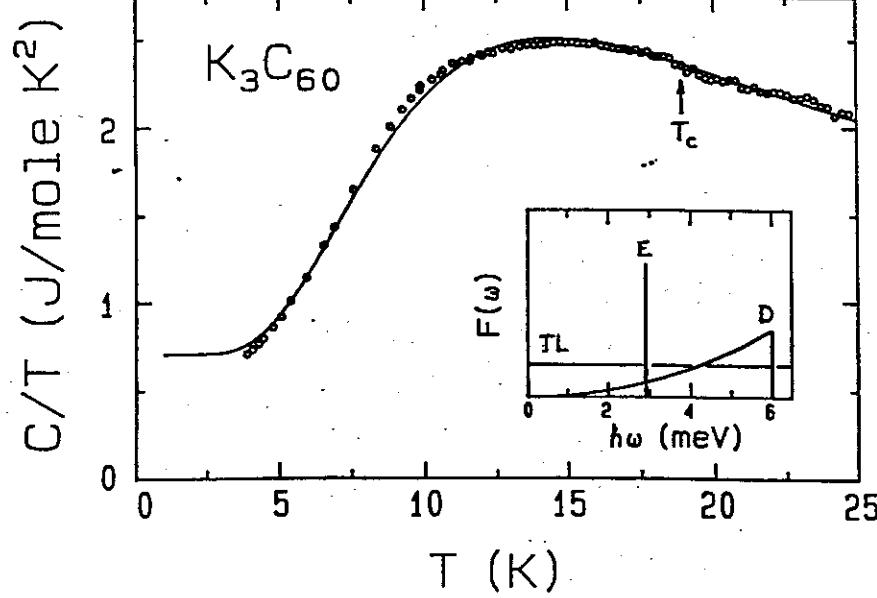


Fig. 1

Can large change in  $N_x$  be reconciled with the McMillan eqn.?

$$\lambda = N_b V \quad T_c = \frac{\pi \hbar \omega}{1.2} \exp \left[ \frac{-1.04(1+\lambda)}{1 - \mu^2(1+0.62\lambda)} \right]$$

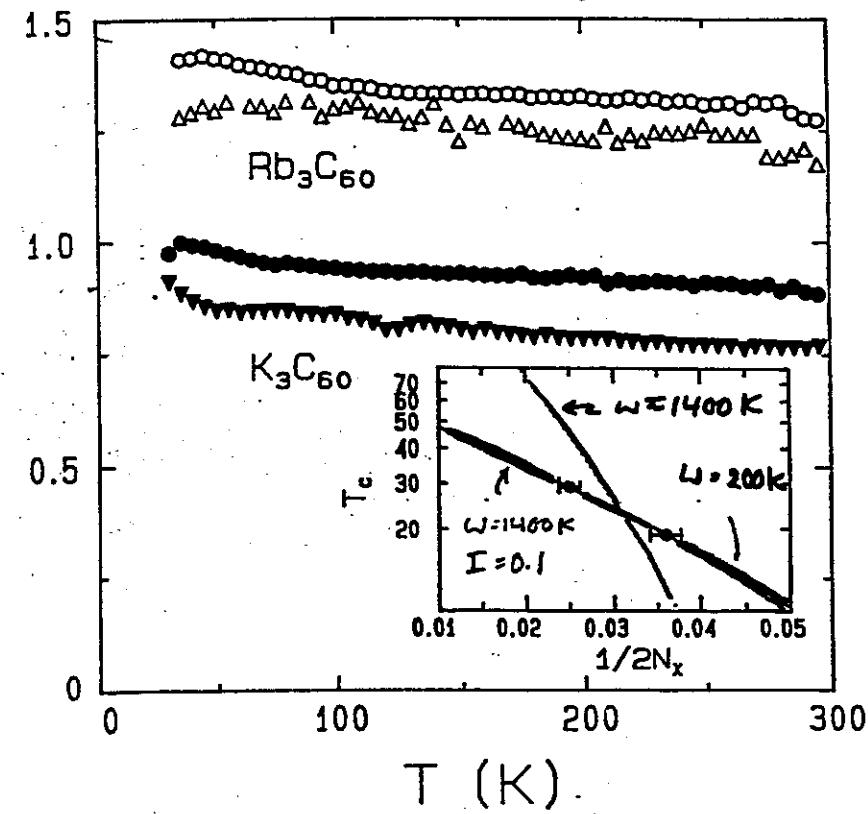


Fig. 3

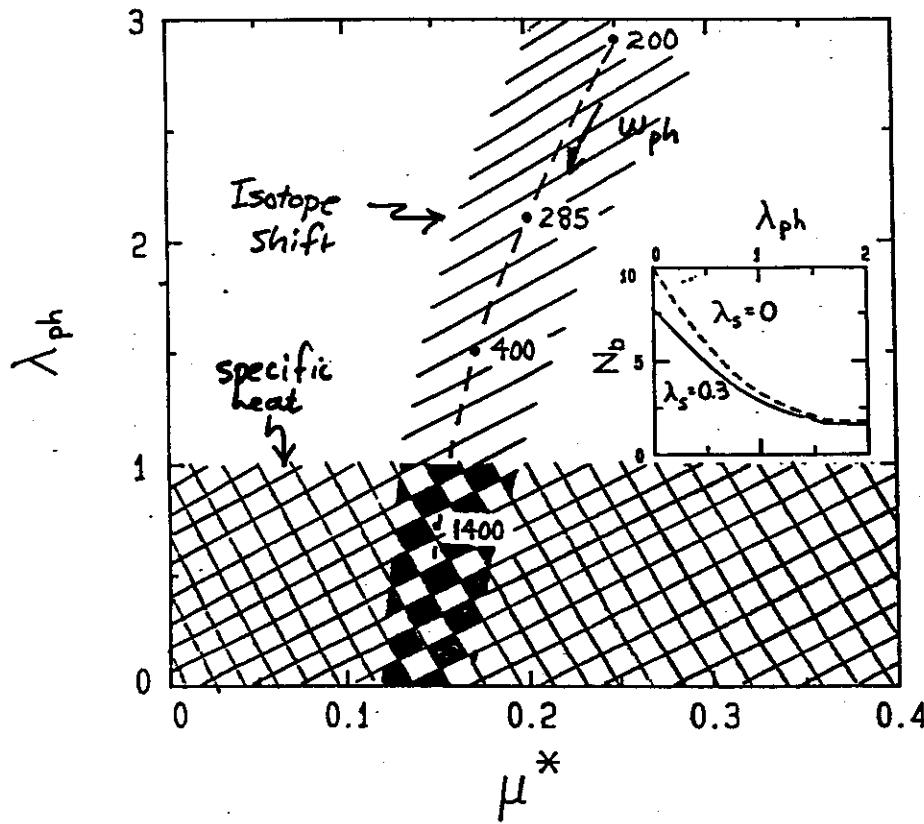


Fig. 4

### Determination of $N(\epsilon_F)$ through critical field measurements

Rutgers Relation

$$F_u - F_s = \frac{H_c(T)}{8\pi} *$$



$$\frac{\Delta C}{T_c} = \frac{(H_c')^2 V_{mol}}{4\pi}$$

assume BCS ( $\Delta C/T_c = 1.43 \gamma$ )

$$N(\epsilon_F) = \frac{3}{\pi^2 k_B^2} \frac{1}{1.43} \frac{V_{mol}}{4\pi} (H_c')^2$$

$$* H_c^2 = H_{c1} H_{c2} ; \frac{H_{c1}}{H_{c2}} = \frac{\ln K}{2K^2}$$

## Upper Critical Field, $H_{c2}$ , determination

(45)

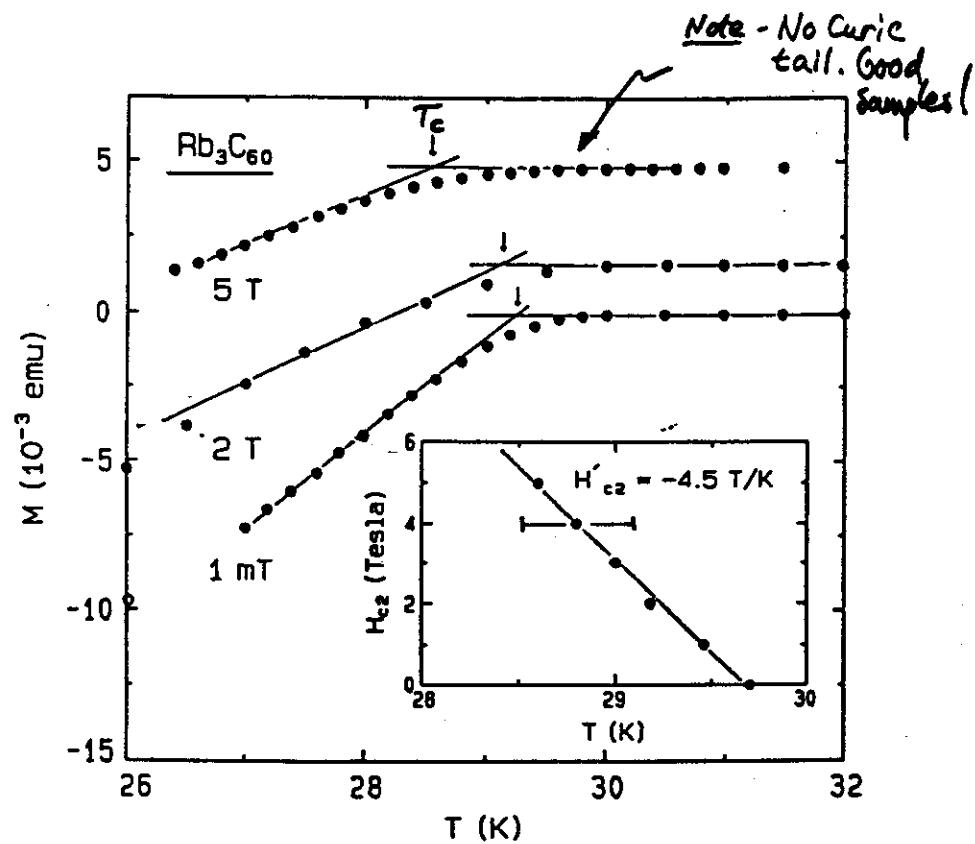
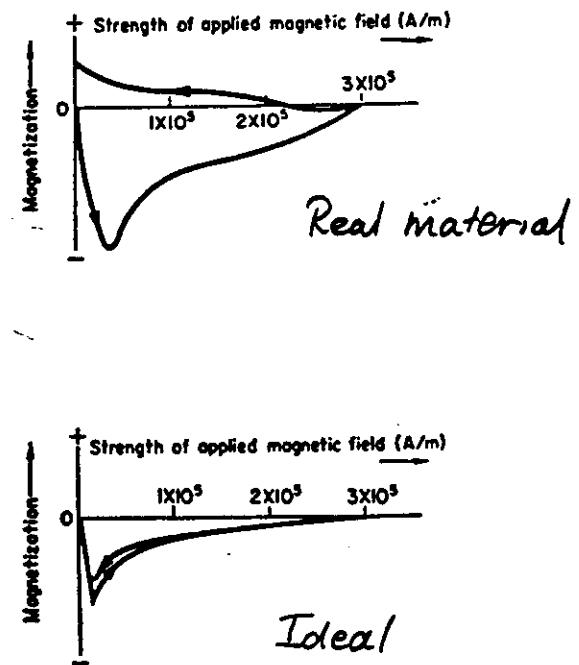
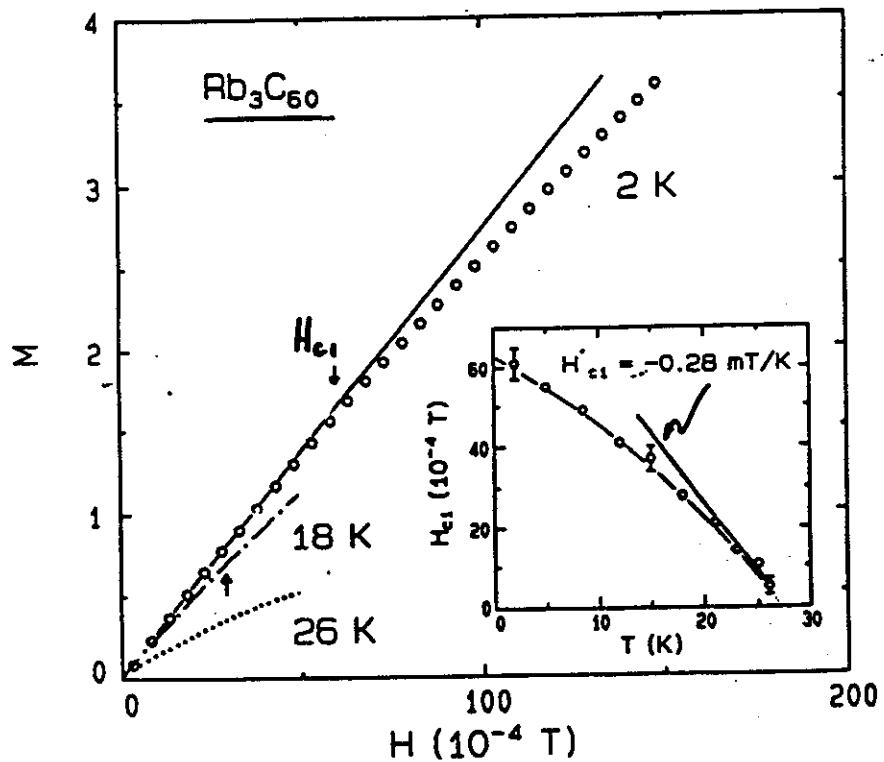


FIG. 3



Lower Critical Field,  $H_{c1}$ , determination.



$$H_{c1} = \frac{\Phi_0}{4\pi\lambda^2} \ln \kappa \Rightarrow \lambda \sim 3500 = 900 \text{ \AA}$$

In good agreement with  $\mu\text{SR}$ :  $\lambda \approx 4500 \text{ \AA}$

FIG. 2

$\mu\text{SR}$  penetration depth Uemura et al.

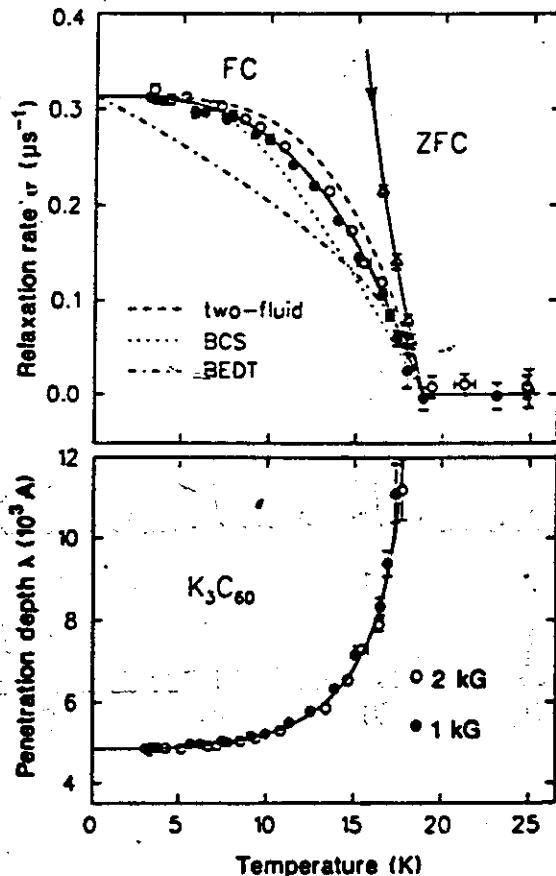


FIG. 2 a. Temperature dependence of the muon-spin-relaxation rate  $\sigma(T)$  in  $\text{K}_3\text{C}_60$ . The solid line shows a fit to  $\sigma(T) = [1 - (T/T_c)^{3/2}]$  with  $T_c = 18.9 \text{ K}$ . Also shown are curves expected for the two-fluid model, the BCS weak-coupling model and a recent  $\mu\text{SR}$  result in the BEDT system after normalizing by  $T_c$ . b. The magnetic field penetration depth  $\lambda$  in  $\text{K}_3\text{C}_60$  derived from  $\sigma \propto \lambda^{-2}$ .

## Derived Superconducting Parameters Rb<sub>3</sub>C<sub>60</sub>

$$K_{GL} \approx 200$$

$$H_{c1} \approx 60 \text{ Oe} / H'_{c1} = -0.28 \text{ mT/K}$$

$$H_{c2} \approx 100 \text{ T (clean limit)} / H'_{c2} = -4.5 \text{ T/K}$$

$$\gamma \approx 60 \pm 10 \text{ mJ/mole C}_60 \text{ K}^2 \text{ (BCS)}$$

$$N^r(E_F) \approx 13 \pm 3 \text{ states/eV C}_60 \text{ (Strong coupling limit)}$$

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$$\text{If } \lambda(eNV) \approx 0.4 \text{ then } N^r \approx 6$$

