



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION



INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS

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UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



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**Research Workshop in Condensed Matter,
Atomic and Molecular Physics
[22 June - 11 September 1992]**

**Working Party on:
"Energy Transfer in Interactions with
Surfaces and Adsorbates"
(31 August - 11 September 1992)**

**"Structures of Rh(110) Surface and their
Phonon Spectra"**

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These are preliminary lecture notes, intended only for distribution to participants.

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Structures of Rh(110) surface and their phonon spectra.

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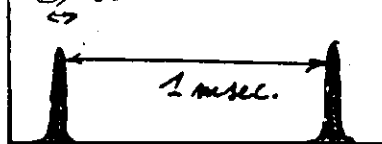
² Università di Trieste, 34000 Trieste-Italy

³ Università di Trento, Povo-Italy

⁴ also at Dipartimento di Fisica dell' Università di Trieste.

Rh (110) surface within the same T range
presents different structures as a function of
different temperature treatment and oxygen coverage!

Two clean (1×1) , (1×2) and one oxygen covered
structure (2×2) , are reported

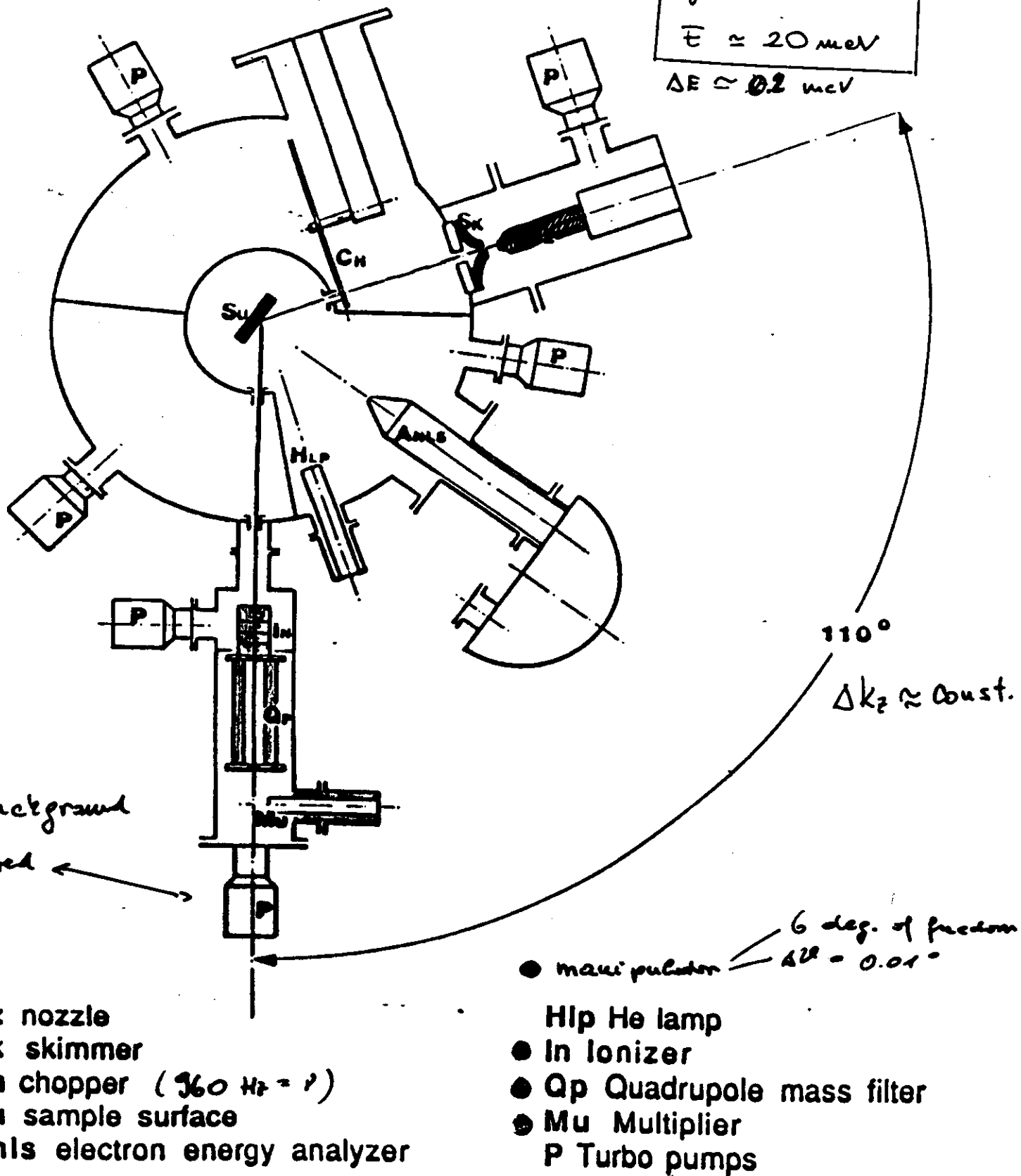


$$v \approx 1000 \text{ m/sec}$$

$$\frac{\Delta v}{v} = 1\%$$

$$E \approx 20 \text{ meV}$$

$$\Delta E \approx 0.2 \text{ meV}$$



1e background
lowered

- Nz nozzle
- Sk skimmer
- Ch chopper (360 Hz = 1)
- Su sample surface
- Anls electron energy analyzer

- manipulator
- Hlp He lamp
- In Ionizer
- Qp Quadrupole mass filter
- Mu Multiplier
- P Turbo pumps

beam: $4 \cdot 10^6$ atoms per pulse $\square$; $5 \mu\text{sec}$
 $\times$; $8 \cdot 10^{-6} \text{ sr}$

surface spot: $0.7 \mu\text{m}$

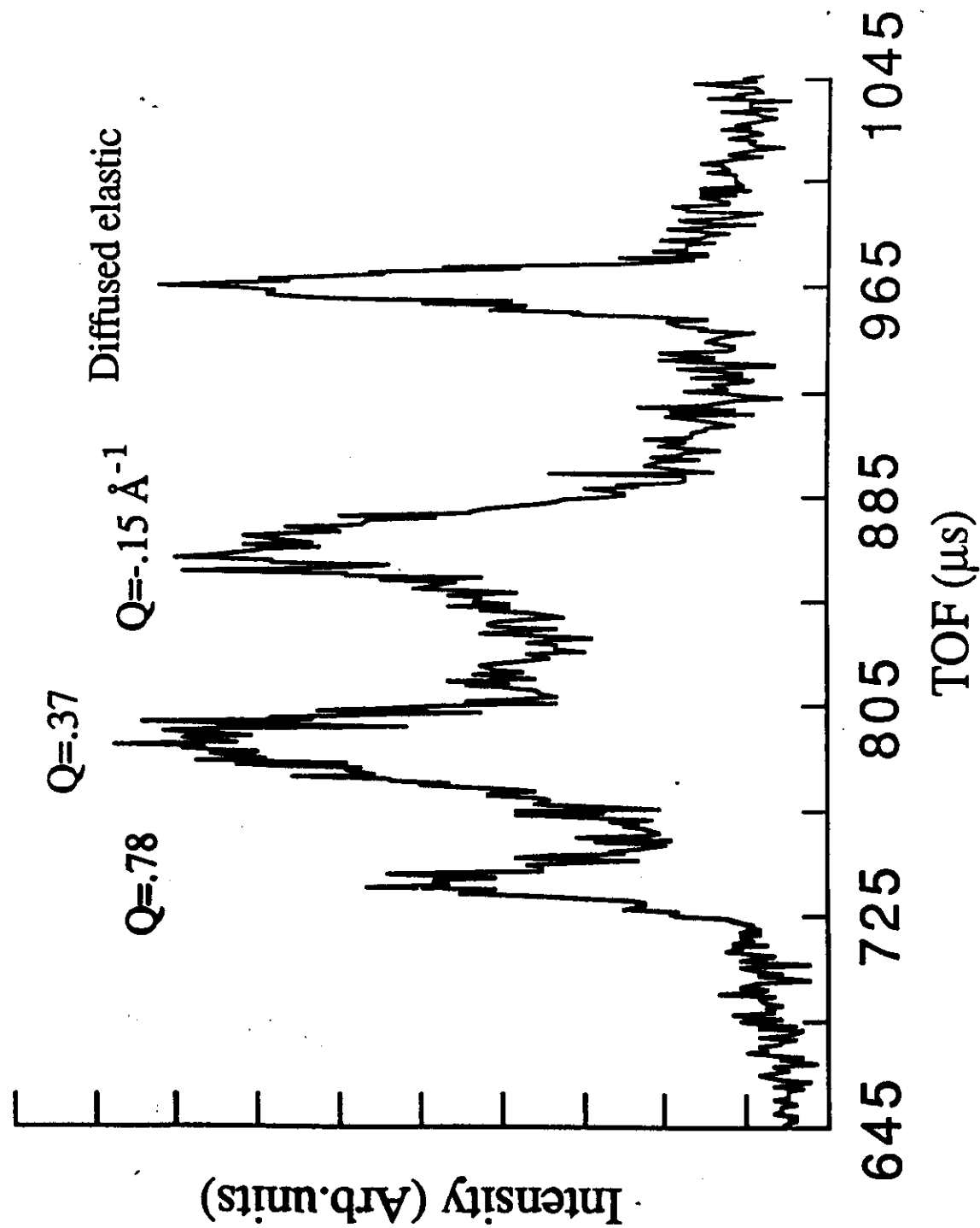
$E_{He} = 18.62 \text{ meV}$

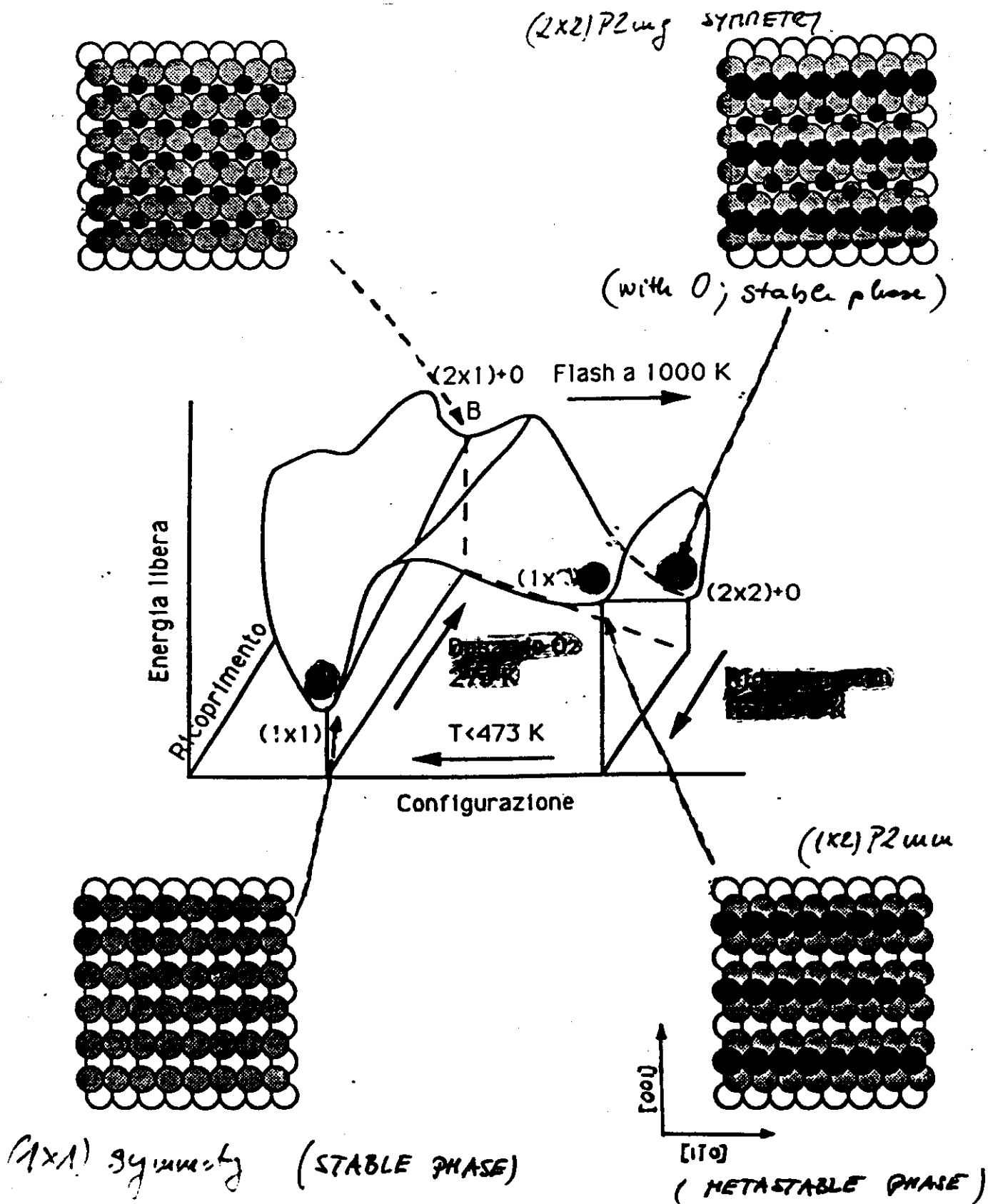
$\Delta E \approx 0.2 \text{ meV}$

Rh(110)(1x1) [001]

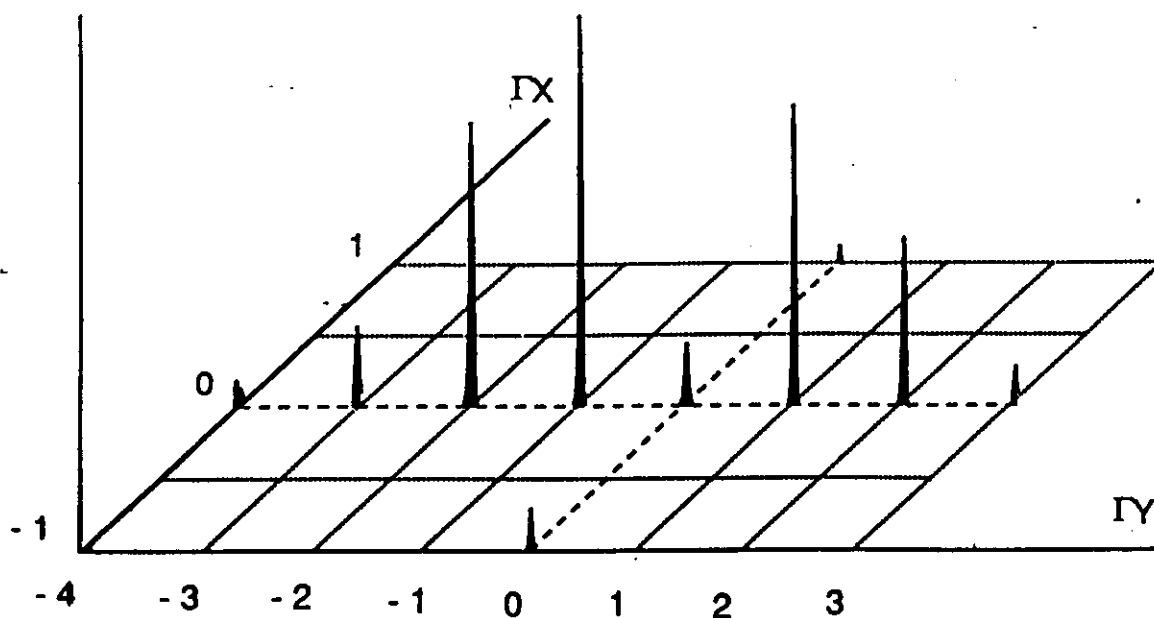
Angle of incidence = 61°

Sampling time $\sim 20 \text{ min.}$





All three symmetry structures exist at 370 K (according to the previous temperature/(O,H) treatment!



Diffraction pattern, $T=470\text{K}$

He beam energy = 18.62 meV

$(0,-4) \times 10$

$(0,\pm 3) \times 5$

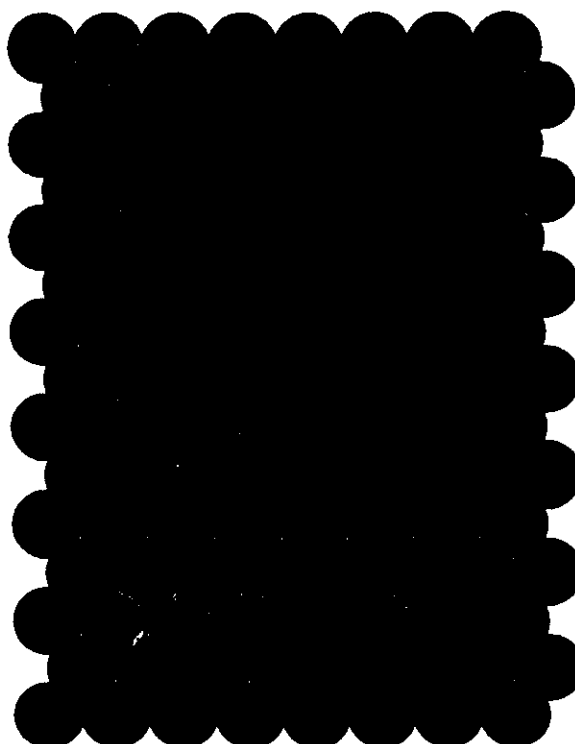
$(\pm 1,0) \times 100$

Unit mesh on $\Gamma Y = 0.72\text{\AA}^{-1}$, on $\Gamma X = 2.2\text{\AA}^{-1}$

● Rh top layer

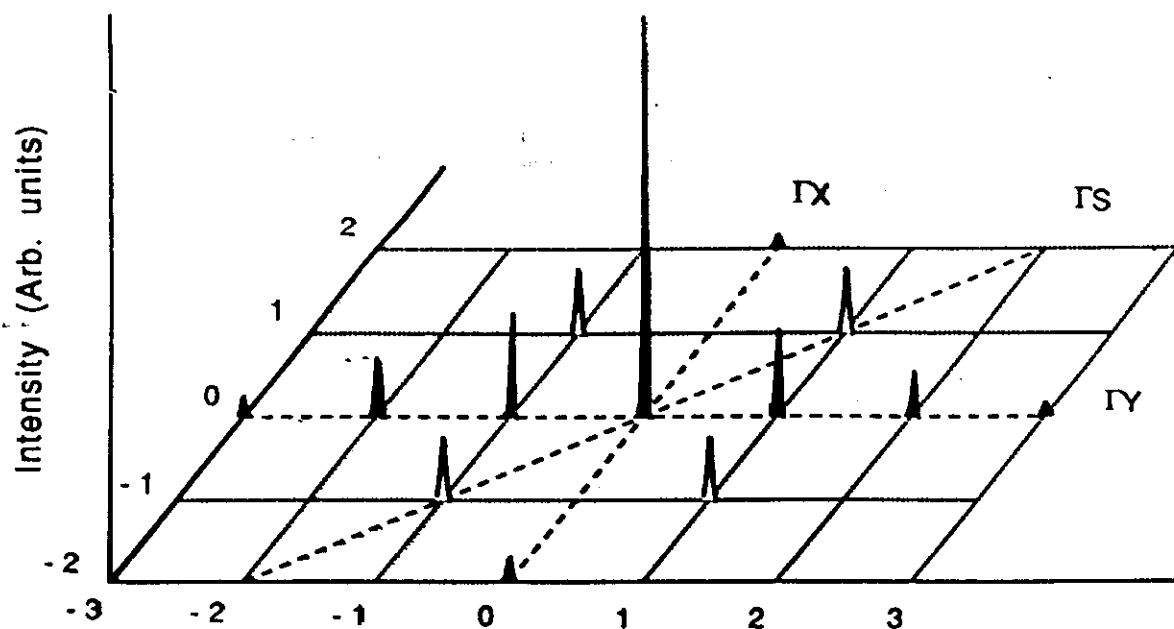
● Rh 2nd layer

● Rh 3rd layer



$\langle 001 \rangle$

$\langle 110 \rangle$

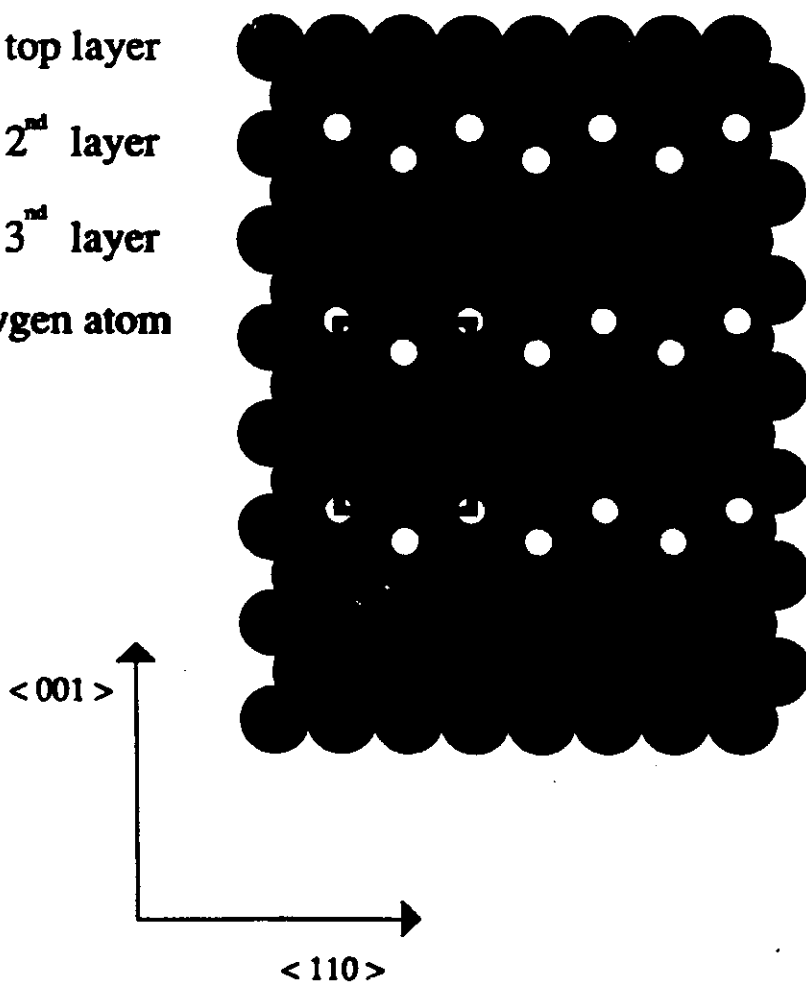


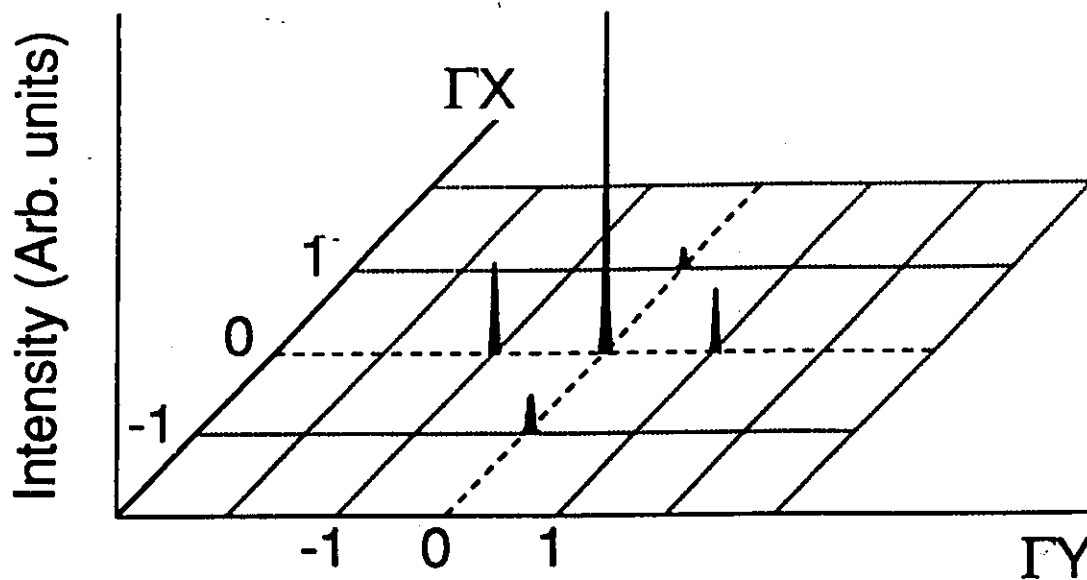
Sample: Rh(111), T=600K

He beam energy = 18.62 meV

Unit mesh along $\Gamma Y = 1.1 \text{ \AA}^{-1}$, and along $\Gamma X = 1.1 \text{ \AA}^{-1}$

- Rh top layer
- Rh 2nd layer
- Rh 3rd layer
- oxygen atom





~~Figure 10.13~~ T=600K

He beam energy = 18.62 meV

(0,±1) x 2

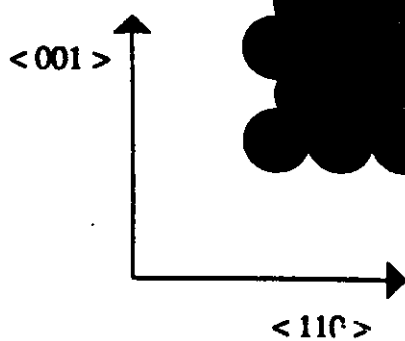
(±1,0) x 20

Unit mesh along $\Gamma Y = 1.61 \text{ \AA}^{-1}$, and along $\Gamma X = 2.23 \text{ \AA}^{-1}$

● Rh top layer

● Rh 2nd layer

● Rh 3rd layer



in order to interpret the Diffraction patterns:

- Assume a certain form of the surface interaction potential.
- Solve the scattering problem.

1) Hard corrugated wall (HCW)

gives for the corrugation along $\langle 001 \rangle$:

Surface	ξ
(1x1)	0.6 Å
(1x2)	0.8 Å
(2x2)	$\approx (0.25 \text{ Å})$

$\Rightarrow$ Implies the high corrugated 'missing row' model

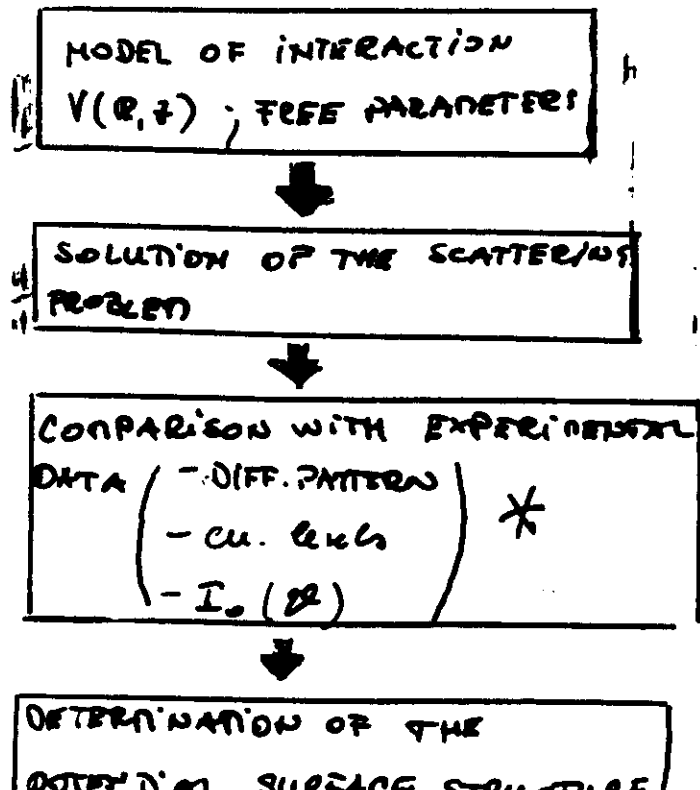
2) Realistic potential:

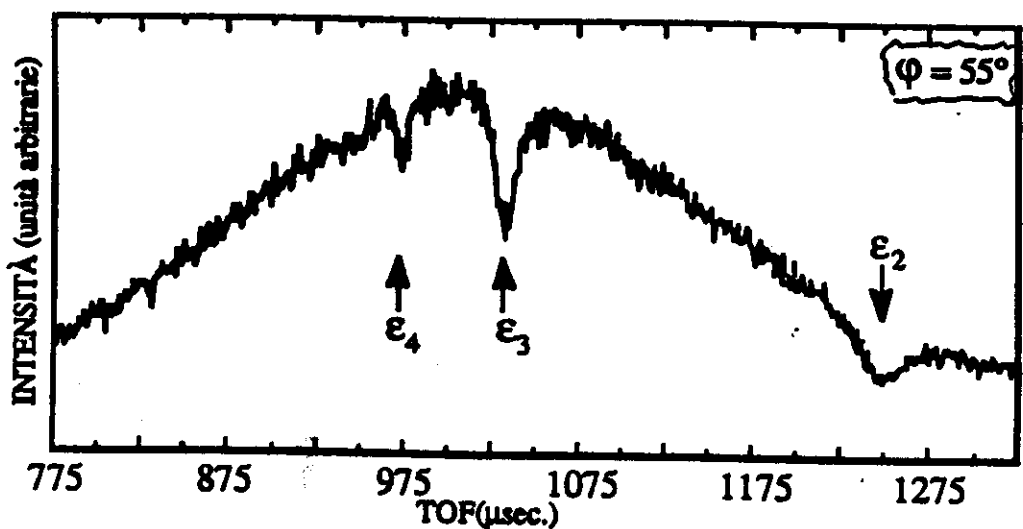
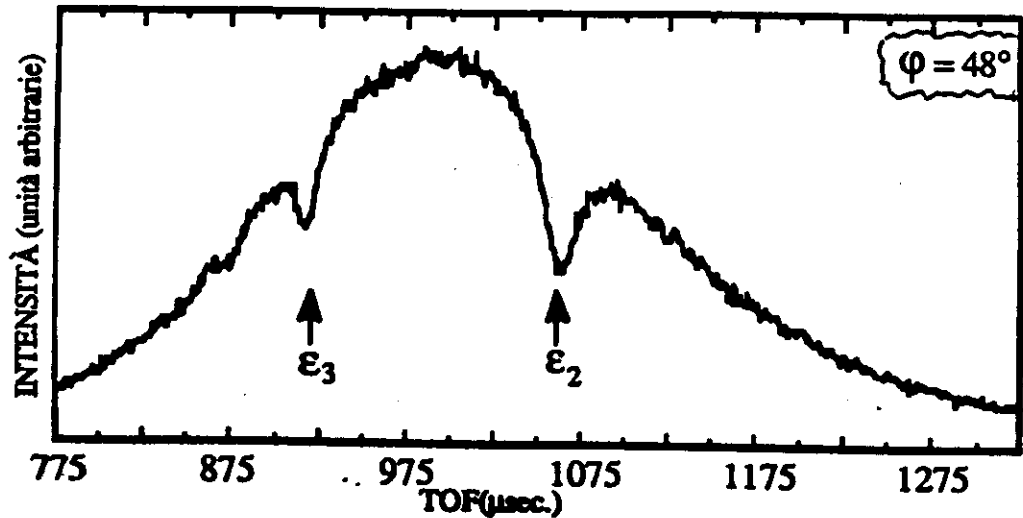
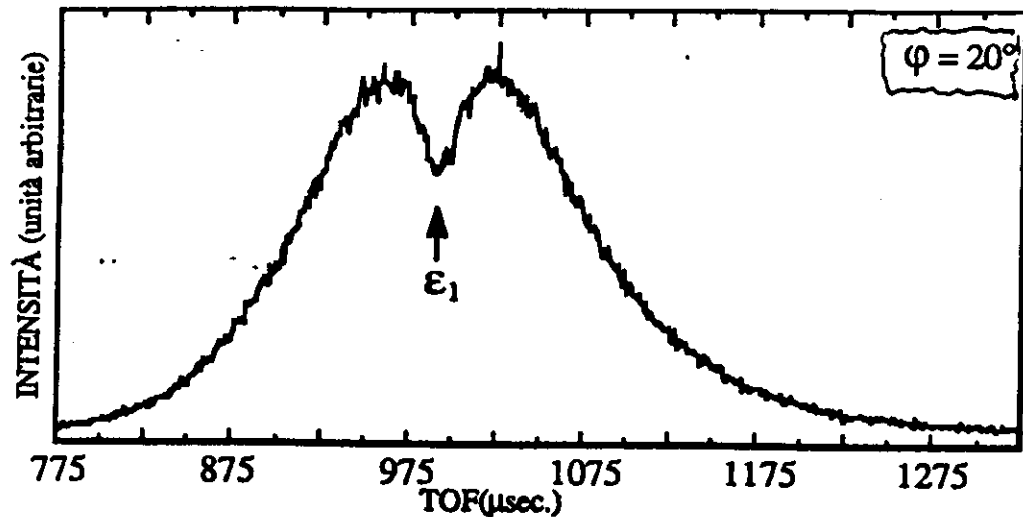
$$V(R, z) = \sum_i u(r_i - r) - \frac{C}{(z - z_0)^3}$$

+ C.C.C. calculations!

$$V_R = \alpha \cdot \bar{u}(R, z) \Rightarrow$$

Surface	ξ (Å)
(1x1)	0.15 Å
(1x2)	1.6 Å

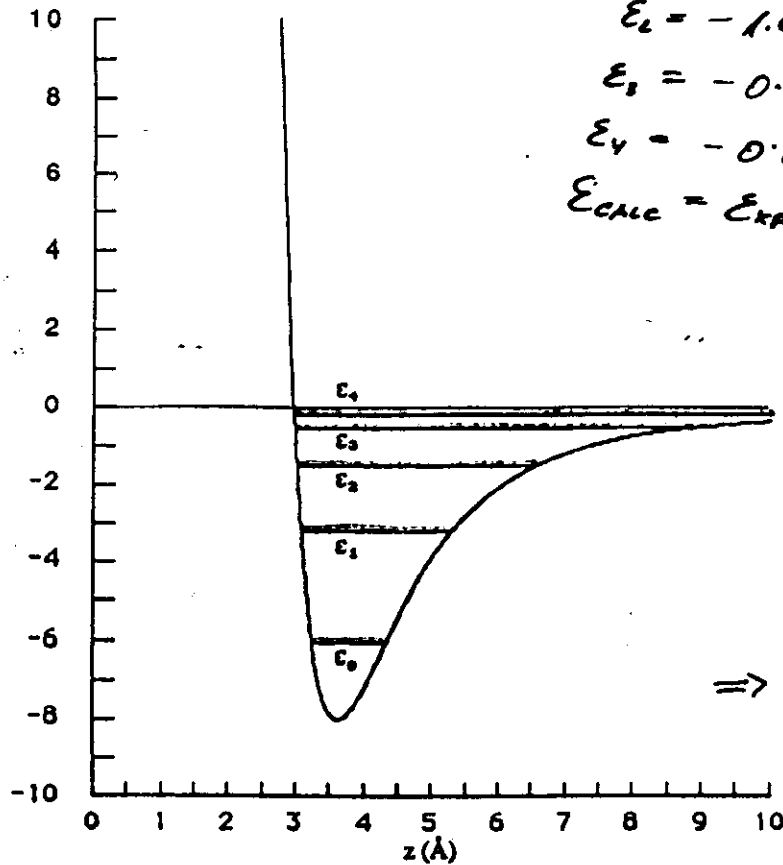




$$\frac{\hbar^2}{2m} (K_i^2 + k_{i0}^2) = \frac{\hbar^2}{2m} (K_i + G)^2 + \epsilon_v$$

$$V(\mathbf{r}, \mathbf{r}) = V_0(z) + \sum_{\mathbf{G} \neq 0} V_{\mathbf{G}}(\mathbf{r})$$

$V_0(z)$
for the (1x1)
surface



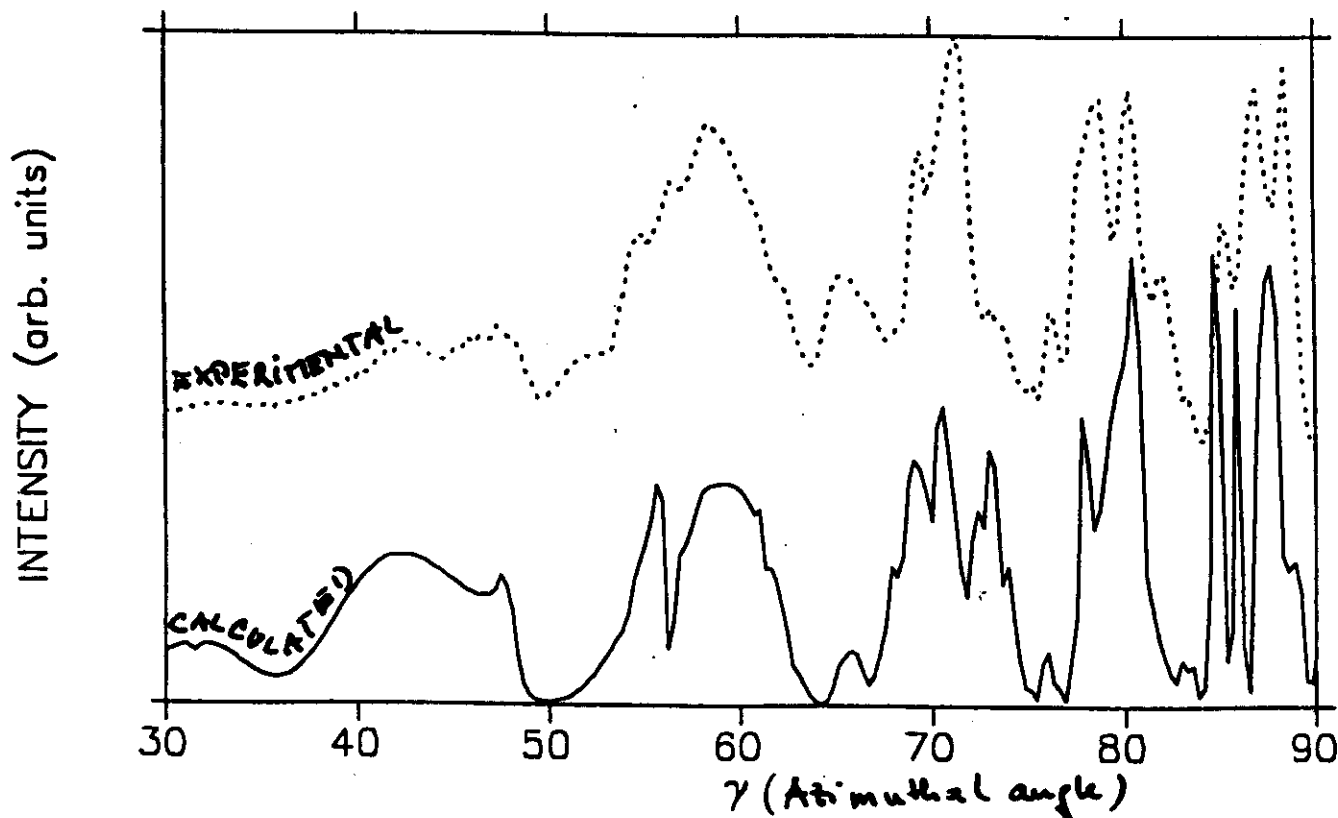
EXP

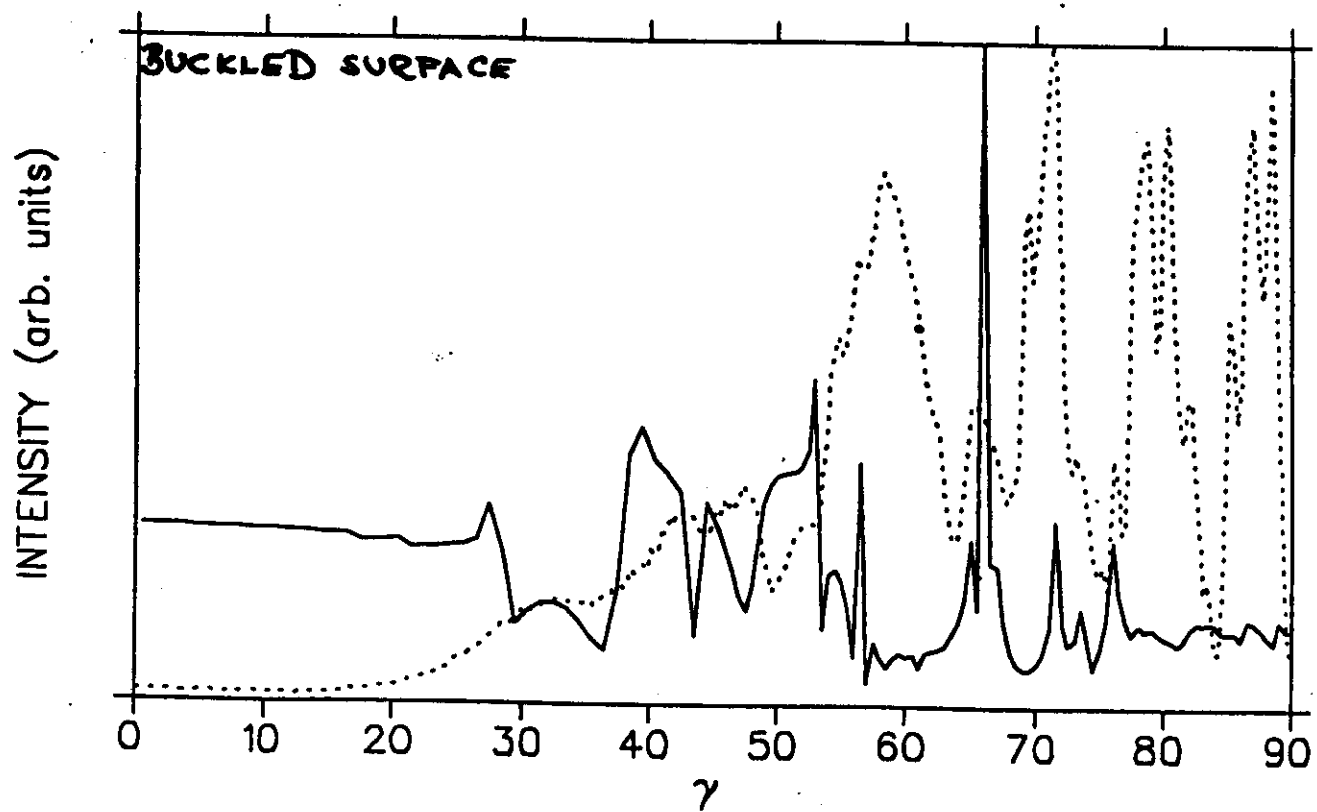
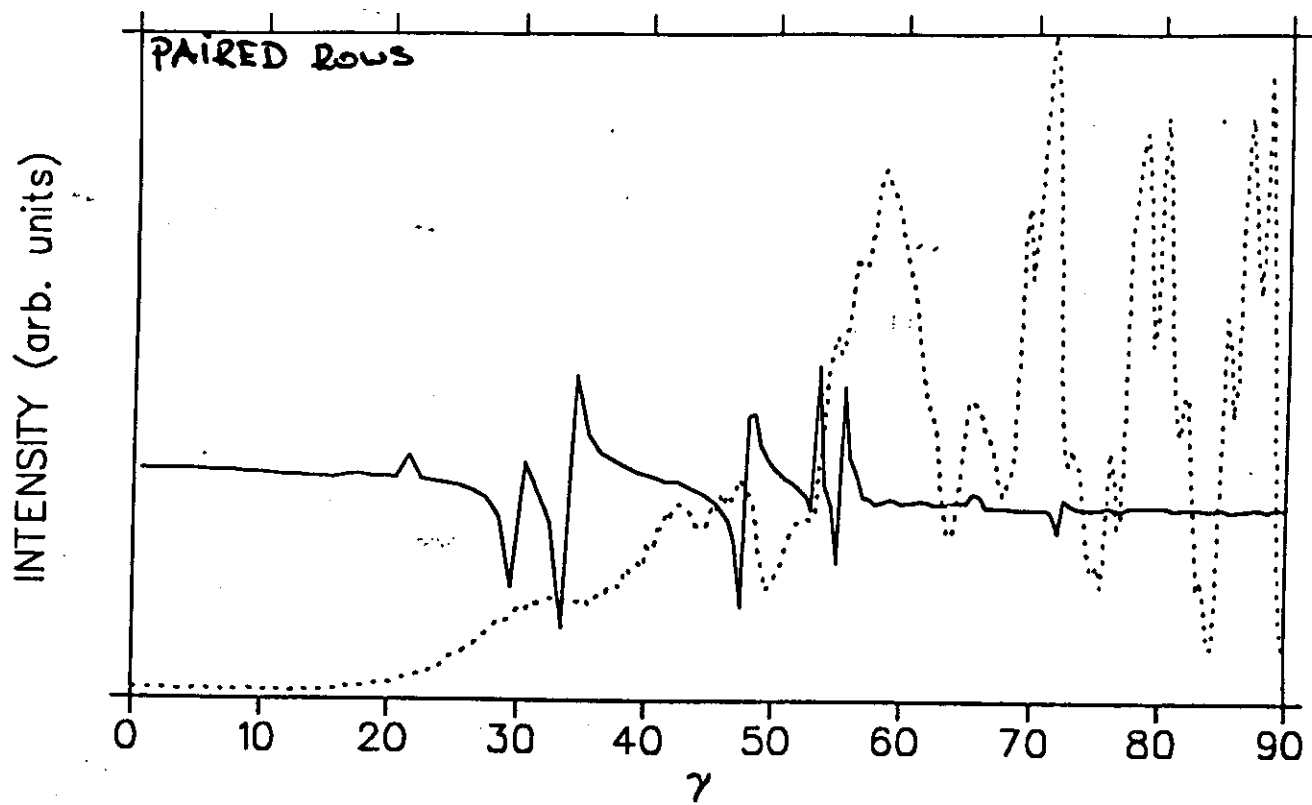
$$\begin{aligned} E_1 &= -3.20 \pm 0.02 \text{ meV} \\ E_2 &= -1.47 \pm 0.02 \\ E_3 &= -0.85 \pm 0.02 \\ E_4 &= -0.16 \pm 0.02 \\ E_{\text{calc}} &= E_{\text{exp}} (1 \pm 0.02) \end{aligned}$$

⇒ DETERMINE SOME
PARAMETERS OF
THE POTENTIAL!

$I_0(z)$ for (1x2) "missing row" structure

⇒ relaxation of (0-10%)

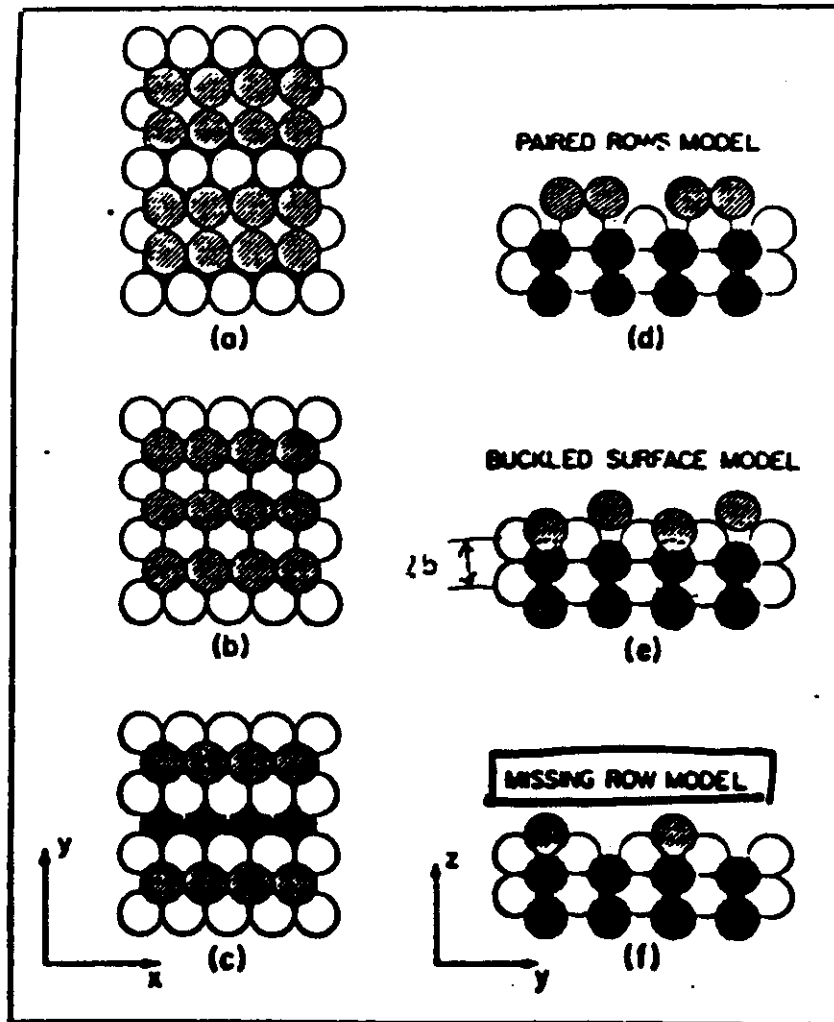




VARIOUS MODELS OF THE (1x2)

10) SURFACE.

thice: $a = 3.80$



$$a_1 = 3.40 \text{ \AA}$$

$$a_2 = 4.20 \text{ \AA}$$

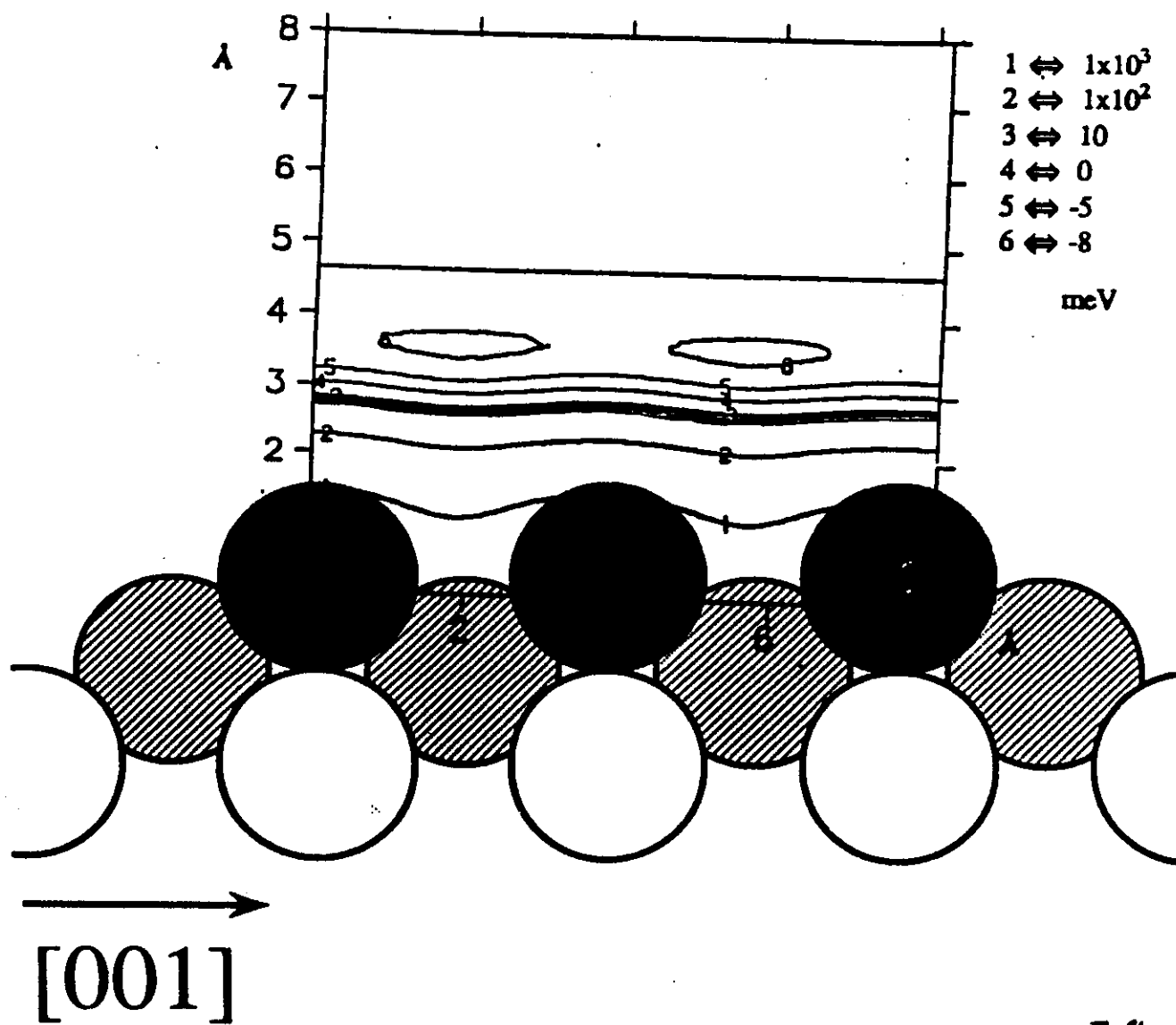
$$b_1 = 1.15 b$$

$$b_2 = 0.85 b$$

FROM HCLW MODEL:

ALTA CORRUAZIONE $\Rightarrow$ "MISSING ROW"

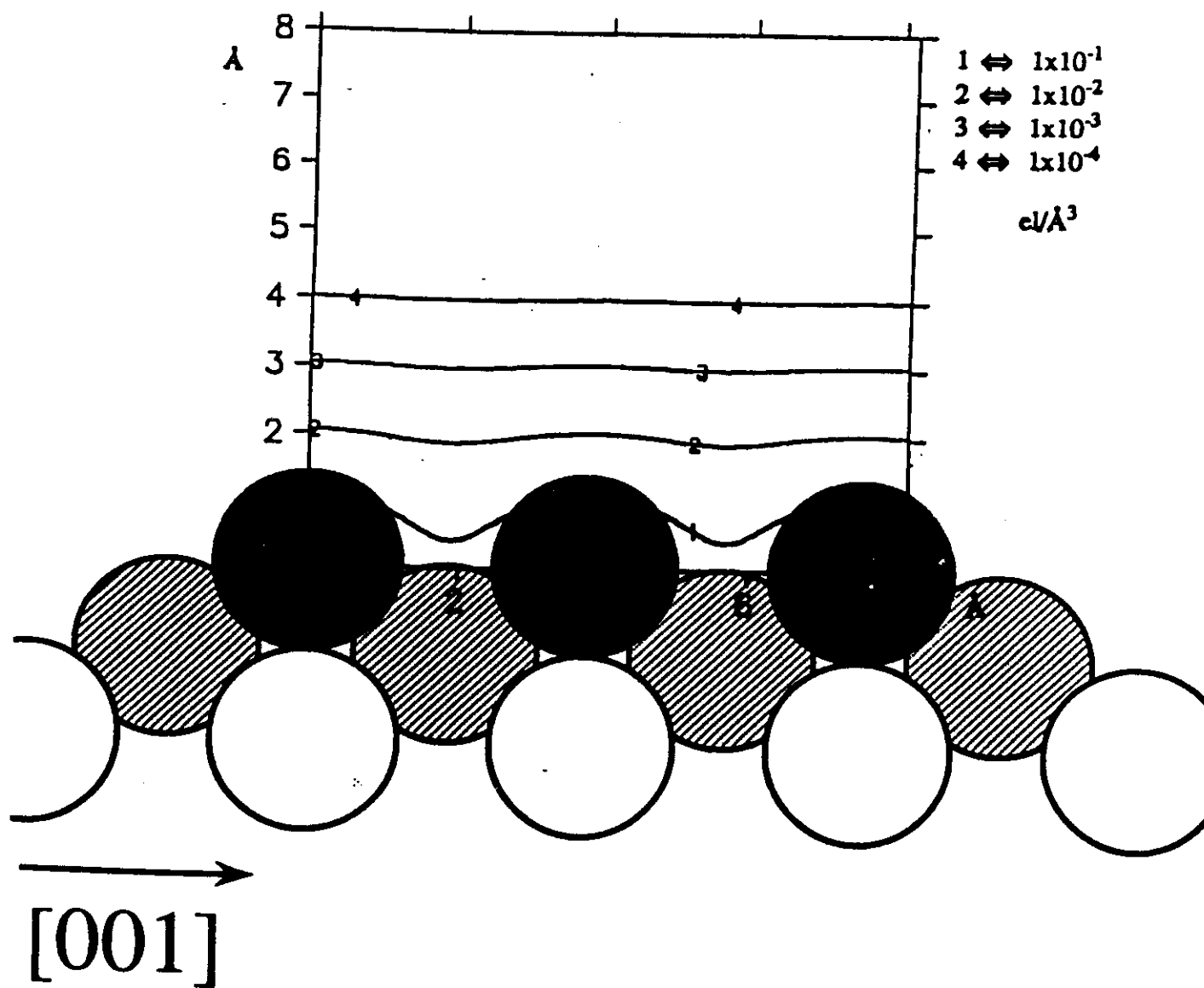
CURVE EQUIPOTENZIALI



$2h(110)(1 \times 1)$ structure

7%

CURVE DI ISODENSITÀ ELETTRONICA.

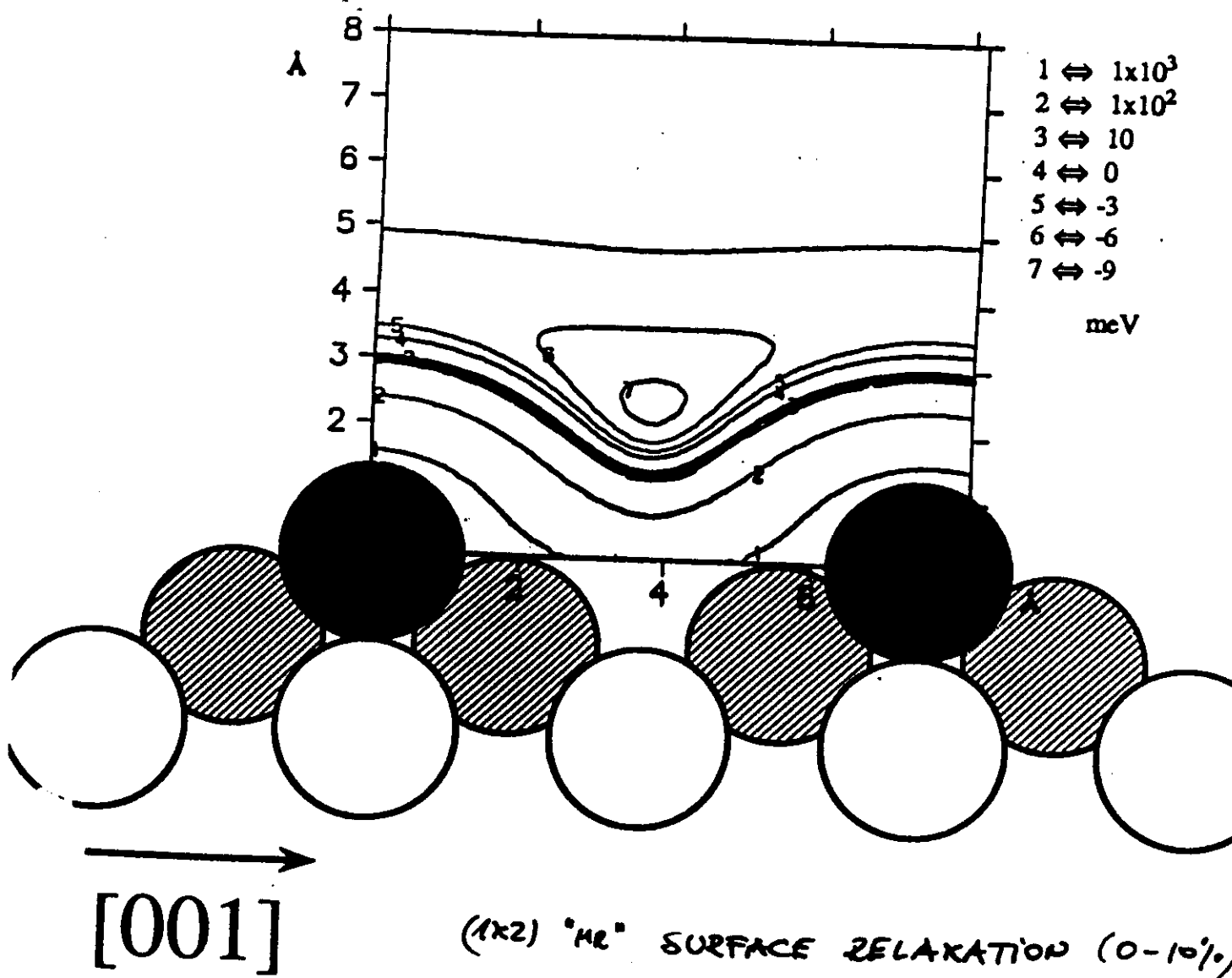


$\text{Zn}(110)(1 \times 1)$ structure

7% = REL.

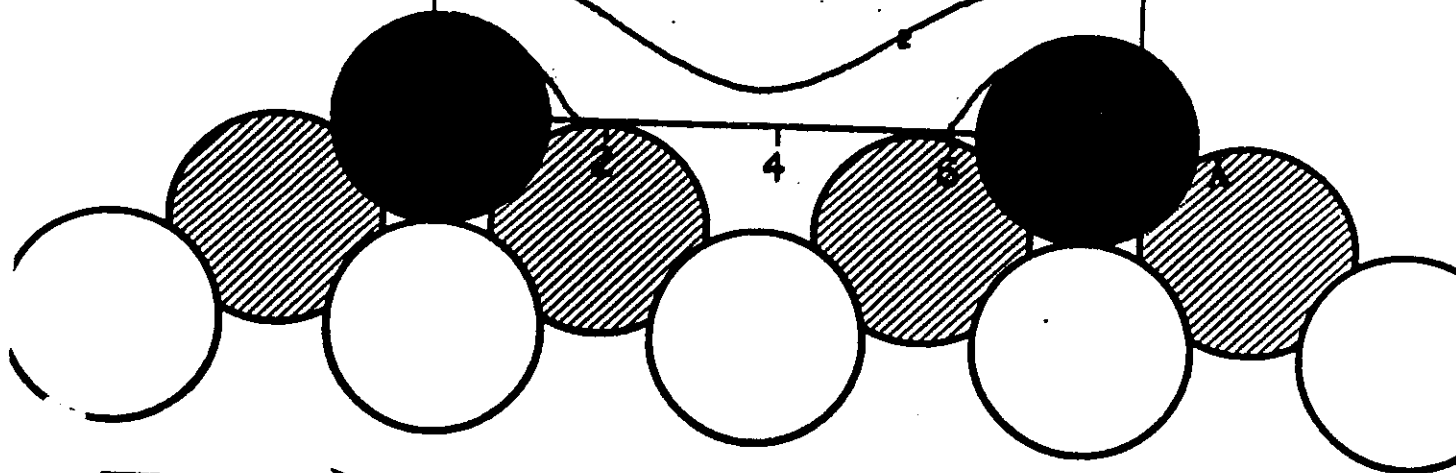
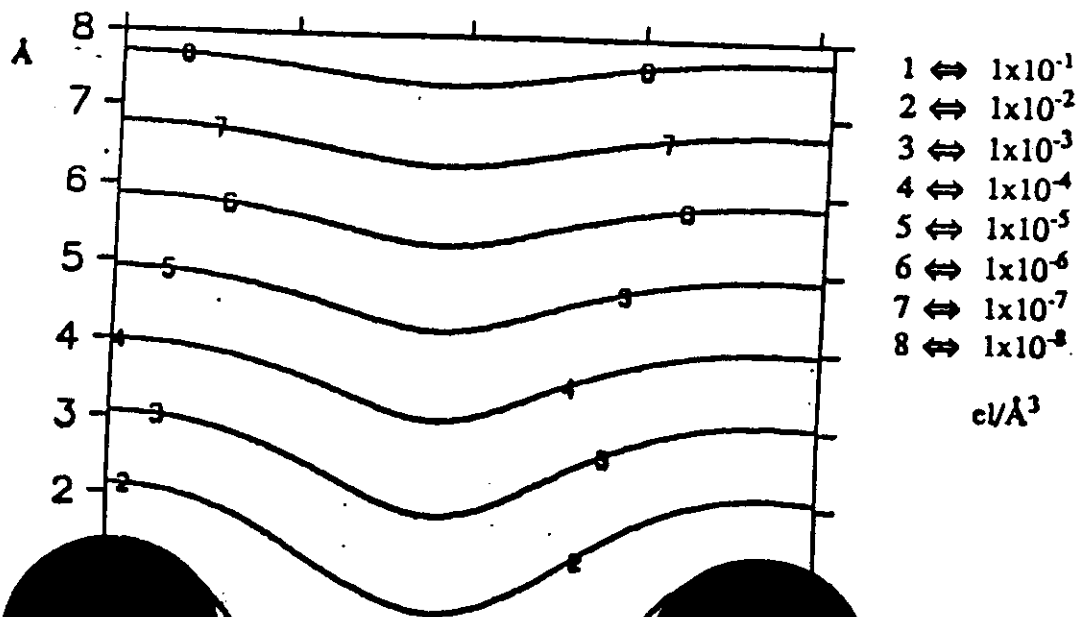
(1x2) Ru (110) "MISSING ROW" SURFACE STRUCTURE

CURVE EQUIPOTENZIALI



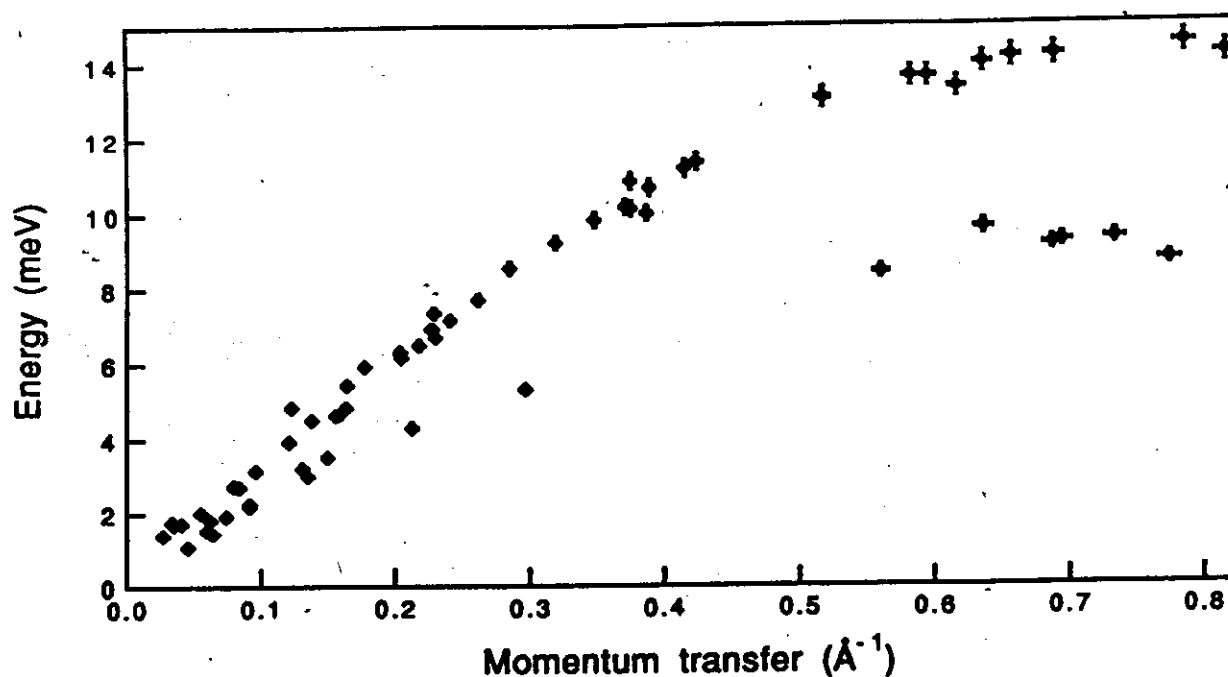
xN)

CURVE DI ISODENSITÀ ELETTRONICA



$[001]$

(1x2) "1x2" SURFACE RELAXATION (0-10%)

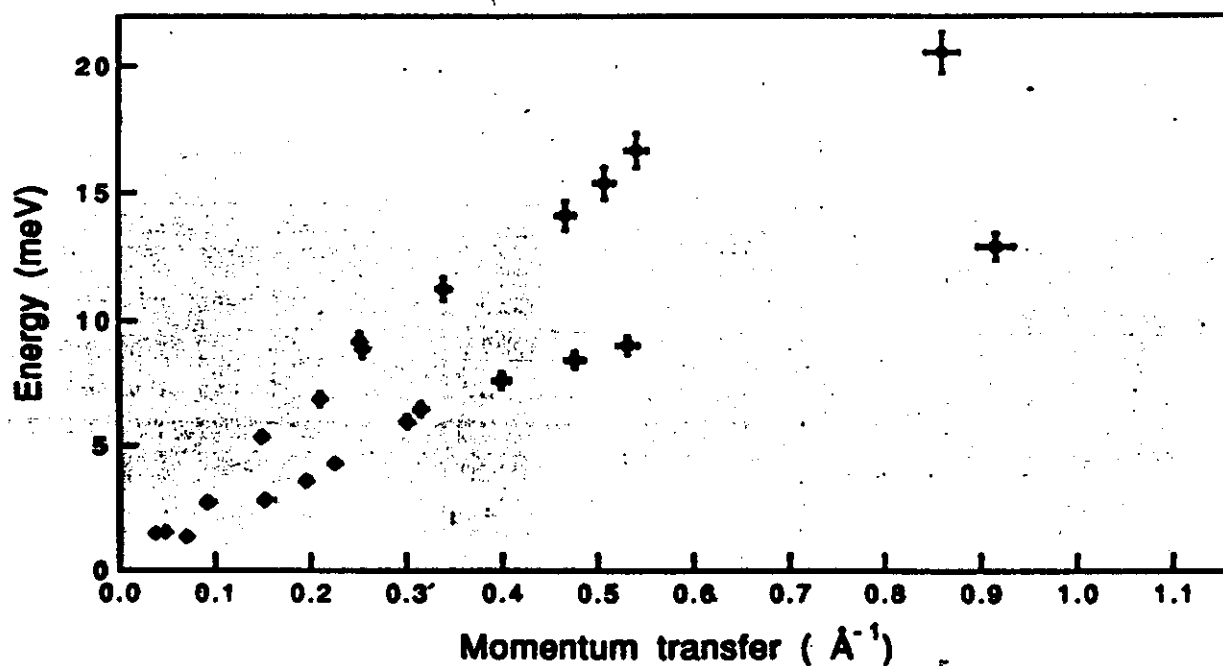


Phonon dispersion curve along $G_y/2 = 0.824 \text{ \AA}^{-1}$

He beam energy = 18.62 meV, $T=600\text{K}$,

Zone boundary, $G_y/2 = 0.824 \text{ \AA}^{-1}$

sampling time = 10 min. per point

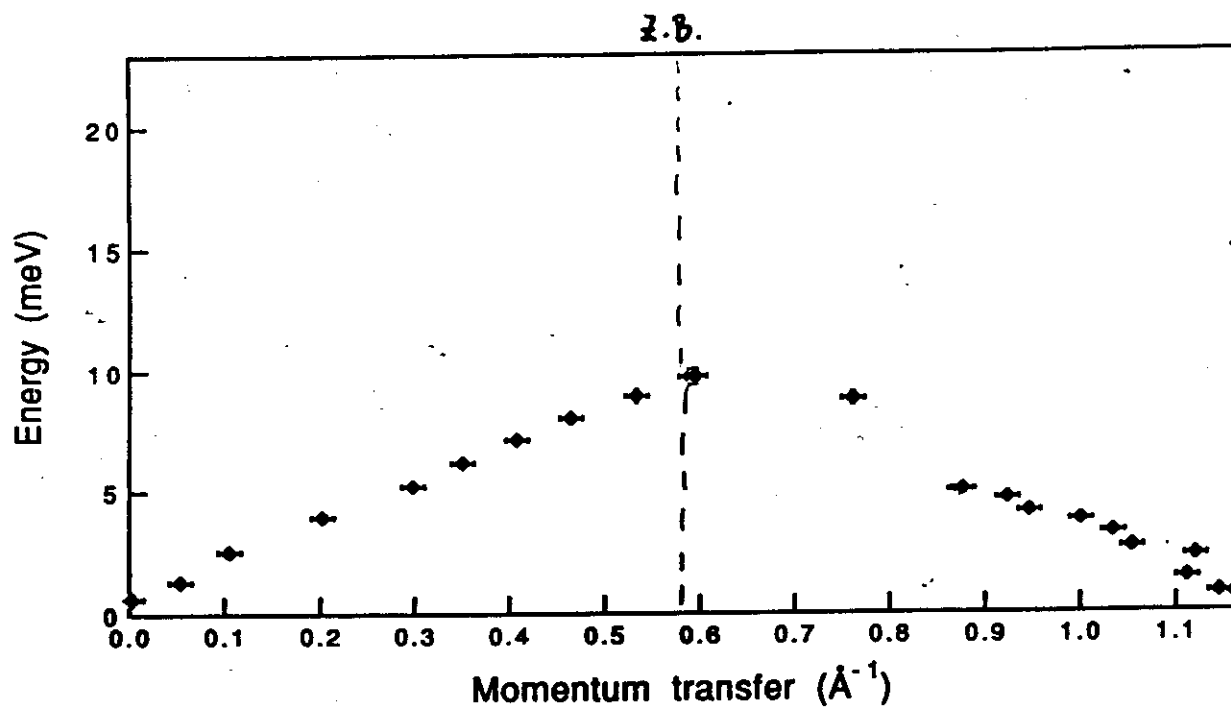


Phonon dispersion along $G_x/2 = 1.165 \text{ \AA}^{-1}$

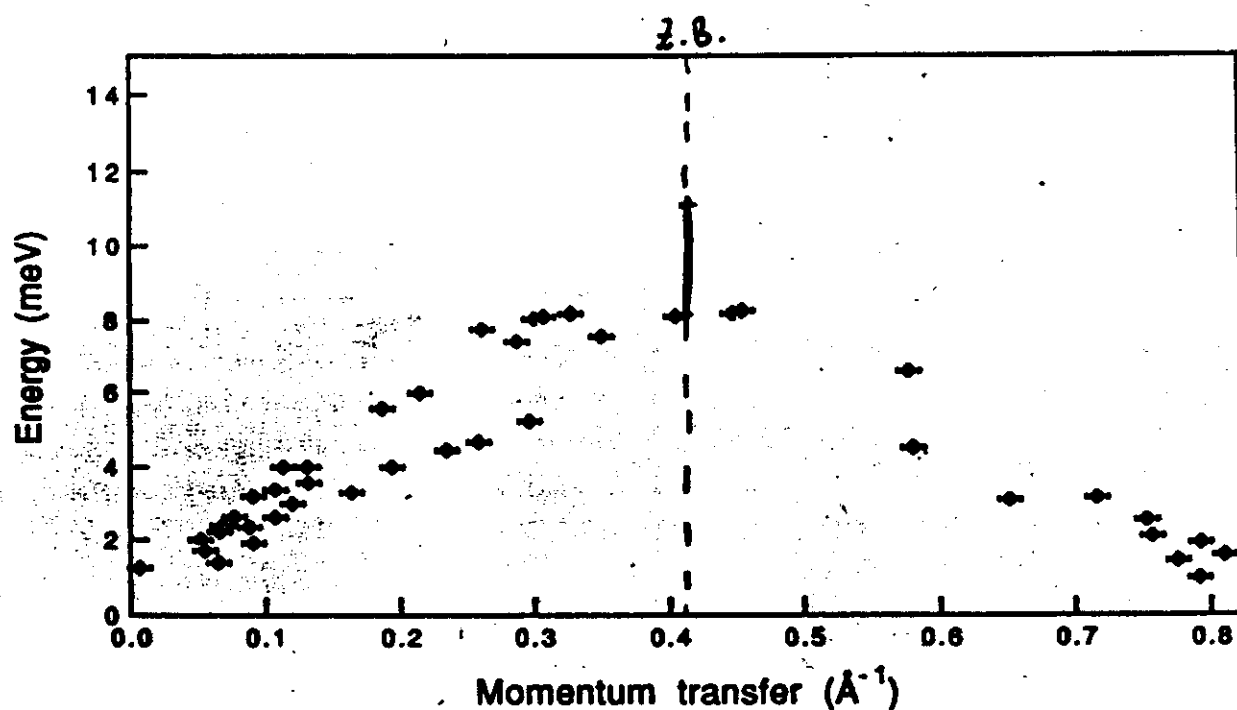
He beam energy = 18.62 meV, $T=600\text{K}$

(1x1) Zone boundary, $G_x/2 = 1.165 \text{ \AA}^{-1}$

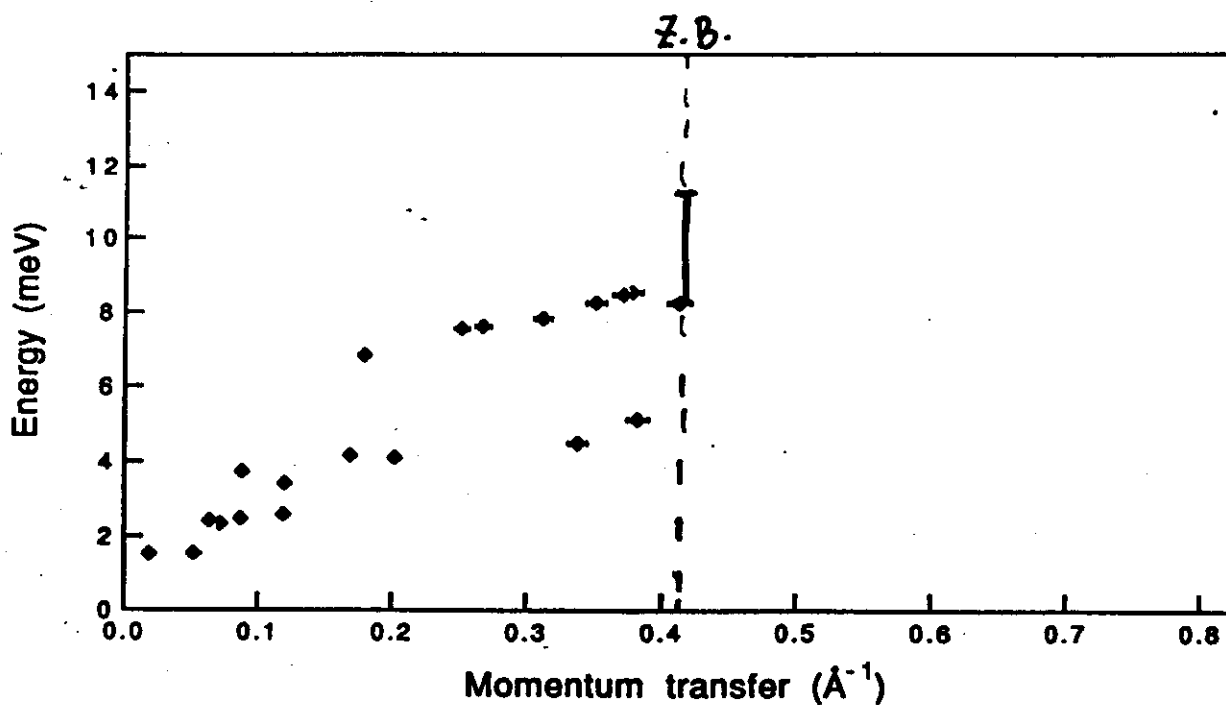
sampling time = 20 min. per point



Phonon dispersion curve along Γ
 He beam energy = 18.62 meV, $T=600\text{K}$,
 (2×2) zone boundary, $G_x/2 = 0.5825 \text{ \AA}^{-1}$,
 sampling time ... min. per point.



Phonon dispersion curve along Γ
 He beam energy = 18.62 meV, $T=600\text{K}$,
 (2×2) zone boundary, $G_y/2 = 0.412 \text{ \AA}^{-1}$,
 sampling time 20 min. per point.



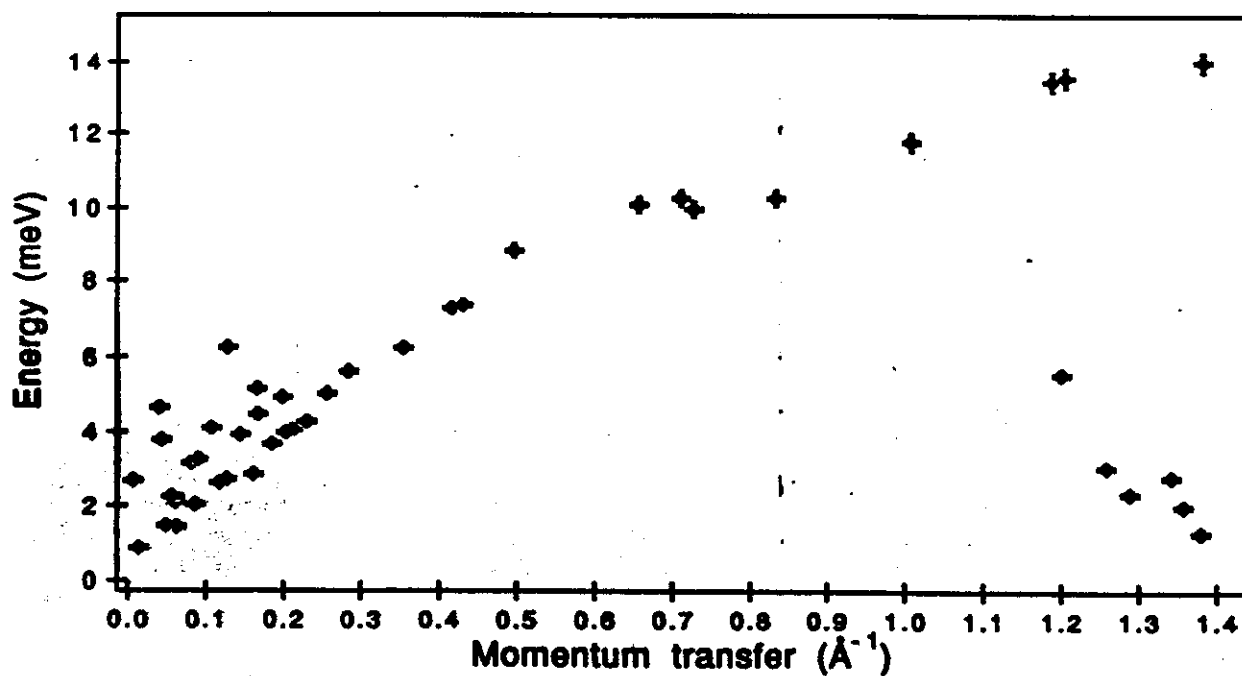
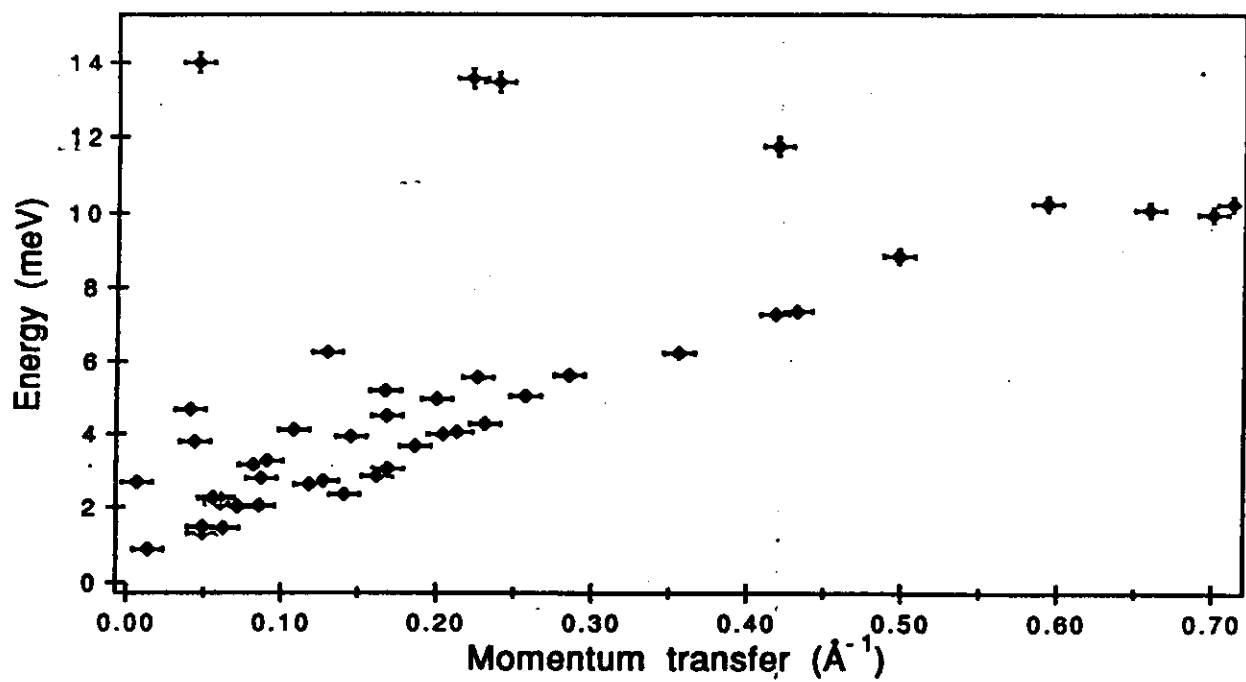
Phonon dispersion along Z.B.
 He beam energy = 18.62 meV, T=370K
 (1x2) Zone boundary, $G_y/2 = 0.412 \text{ \AA}^{-1}$
 sampling time = 20 min. per point

Summary: (1x1) No bulk phonon measurements
 No bulk phonon calculations
 Surface phonon calculations in progress

Rh (1x2); ΓY : - Substantial softening at the Z.B.
 - No folded dispersion seen

O/Rh (2x2); ΓY : - Perfectly matching the 1x2 spectra
 (No effect due to Oxygen)

ΓX : - No changes with respect to (1x1) case (apart from lower symmetry! (lower branch)



Phonon dispersion curve along
 He beam energy = 18.62 meV, T=600K
 S point at $1.427 \text{ \AA}^{-1}$,
 sampling time = ... min. per point.

Atom-Surface Interaction Potential

Long-range polarization attraction:

$$V_{\text{long}}(\mathbf{r}) \propto - \frac{C}{z^3}$$

[Zaremba and Kohn, 1976]

Short-range repulsion:

$$V_{\text{short}}(\mathbf{r}) = \alpha n(\mathbf{r})$$

with $\alpha = 30 \text{ eV } \text{\AA}^3$

[Esbjerg and Nørskov, 1980]

problem: $V(\mathbf{r}) = V_{\text{short}}(\mathbf{r}) + V_{\text{long}}(\mathbf{r})$

Sum of pairwise terms $u_j(\mathbf{r})$:

$$V(\mathbf{r}) = \sum_j u_j(\mathbf{r})$$

$$V(\mathbf{r}) = V_{0,0} + \sum_{\mathbf{G}} V_{\mathbf{G}}(z) e^{(i\mathbf{G}\mathbf{r})}$$

Atom Surface Interaction Potential from Empirical Data

- Solving the Schrödinger Equation:
the solutions have lateral Bloch-wave character:

$$\psi_{\mathbf{K}}(\mathbf{r}) = \sum_{\mathbf{G}} c_{\mathbf{G}}(z) e^{i(\mathbf{K} + \mathbf{G}) \cdot \mathbf{R}}$$

and the Schr. eq. becomes a system of coupled differential equations in the incognitæ $c_{\mathbf{G}}(z)$, given the Fourier components $V_{\mathbf{G}}(z)$ of the interaction potential.

- Analysis of diffraction intensities within the Hard Corrugated Wall Model: corrugation function $\zeta(\mathbf{R})$

$$V(\mathbf{r}) = 0 \quad \text{for } z > \zeta(\mathbf{R})$$

$$V(\mathbf{r}) = \infty \quad \text{for } z \leq \zeta(\mathbf{R})$$

- Bound State Resonance Data

levels of $V_{0,0}(z)$

POTENZIALE ATOMO - SUPERFICIE

$$V(R, z) = \sum_{k_{\text{em}}} U(r - r_{k_{\text{em}}}) - \frac{C}{(z - z_0)^3 + \sigma^3 \exp\left(-\frac{1}{2}\left(\frac{z - z_0}{\sigma}\right)^3\right)}$$

CORTO RAGGIO
LUNGO RAGGIO

POTENZIALE ATOMO - ATOMO

TOMMASINI et al.
Phys. Rev.

$$U(r_{k_{\text{em}}}) = \eta_x \eta_y A \exp(-\beta r_{k_{\text{em}}}) \left\{ 1 - \exp[0.36\beta(r_{k_{\text{em}}} - \sigma)] \right\}$$

$$r_{k_{\text{em}}} = \sqrt{(z - z_k)^2 + \eta_x^2 (x - x_{k_{\text{em}}})^2 + \eta_y^2 (y - y_{k_{\text{em}}})^2}$$

η_x, η_y parametri di anisotropia

A, β • POTENZIALE A
CORTO RAGGIO

C, z_0 • POTENZIALE
A LUNGO RAGGIO

σ • ATRAZIONE A
CORTO RAGGIO
• REPULSIONE A
LUNGO RAGGIO

POSIZIONI ATOMICHE.