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**"Selfconsistent Green's Function Method
for Disordered Bulk and Surfaces"**

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These are preliminary lecture notes, intended only for distribution to participants.

SELFCONSISTENT GREEN'S FUNCTION
METHOD FOR
DISORDERED BULK & SURFACES

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We develop a scheme which allows to treat electronic properties of ordered and disordered alloys, their surfaces, interfaces and overlayers from a unified point of view on the ab-initio level. This scheme:

- (i) describes electronic states within first-principles TB-LMTO
- (ii) includes electron correlations within LSDA
- (iii) takes into account a true semi-infinite geometry, for description of surfaces, interfaces and overlayers
- (iv) uses spherical potentials, but the non-spherical part of charge density is taken into account to describe behaviour of electrons close to the surface (surface barrier)
- (v) employs the CPA, and its generalization to inhomogeneous systems like surfaces, to describe disorder
- (vi) relativistic effects can be included via r-TB-LMTO method

Unifying feature is the use of GF formalism, inevitable for treatment of disorder and surfaces.

Development of computer codes to solve equations for realistic systems is unseparable part of theory.

TB-LMTO METHOD FOR SOLIDS: features

1. Fixed basis set : minimal basis possible as in empirical LCAO method
2. ASA : WS cells $\Rightarrow$ WS spheres (no interstitial space)
Potential: inside AS - spherical LDA-potential
outside AS - constant ($E=0$) potential
common for all elements (transferability)
3. Separation of structural (lattice) and atom-dependent parts of any operator (e.g. H)
4. Infinite number of LMTO basis sets (representations) : alloys, open structures, surfaces
5. Reliable description of metals, semiconductors and insulators for energies ± 0.5 Ry around chosen energy of interest (center of occupied bands, E_F , middle of gap region, etc).

DEFINITION OF MTO: α -REPRESENTATION

$$L = lm$$

$$r_R = r - R$$

$$\chi_{RL}^{\alpha}(r_R) = \Phi_{RL}(r_R) + \sum_{R'L'} \dot{\Phi}_{RL'}^{\alpha}(r_{R'}) h_{RL',RL}^{\alpha} + \chi_{RL}^{\alpha,i}(r_R) \quad \left. \vphantom{\sum_{R'L'}} \right\} \text{full space}$$

$$\dot{\Phi}_{RL}^{\alpha}(r_R) = \dot{\Phi}_{RL}(r_R) + \sigma_{RL}^{\alpha} \Phi_{RL}(r_R) \quad \leftarrow \text{(nonzero in own AS)}$$

$$\Phi_{RL}, \dot{\Phi}_{RL} = \frac{\partial \Phi_{RL}}{\partial E} \rightarrow \text{solution of SE in atomic sphere at } R \text{ evaluated for } E = E_{vL}$$

$$\sigma_{RL}^{\alpha} \rightarrow \text{such that } \partial \ln \dot{\Phi}_{RL}^{\alpha} / \partial \ln r \text{ has correct value at sphere boundary}$$

$$h_{RL,R'L'}^{\alpha} = (c_{RL}^{\alpha} - E_{vRL}) \delta_{RR'} \delta_{LL'} + (\Delta^{\alpha})_{RL}^{1/2} S_{RL,R'L'}^{\alpha} (\Delta^{\alpha})_{R'L'}^{1/2},$$

$$S^{\alpha} = S^0 (1 - \alpha S^0)^{-1}$$

$S_{RL,R'L'}^0$ - canonical structure constant: depends only on the lattice type, not on atoms on it and lattice constant

$\alpha \rightarrow \alpha_{RL}$ - specifies given MTO-representation

$\chi_{RL}^{\alpha,i}$ - interstitial part of χ_{RL}^{α} (vanishes in ASA)

$\epsilon^\alpha - E_v, \Delta^\alpha, \sigma^\alpha$ - potential parameters which characterize scattering properties of individual atoms; they depend on lattice constant

$$\epsilon^\alpha - E_v = -P^\alpha / \dot{P}^\alpha, \quad \Delta^\alpha = 1 / \dot{P}^\alpha, \quad \sigma^\alpha = \ddot{P}^\alpha / 2 \dot{P}^\alpha \quad (\dot{X} = \frac{dX}{dE} |_{E_v})$$

$$P^\alpha \equiv \frac{P^0(E)}{1 - \alpha P^0(E)} \Big|_{E_v}, \quad P_{RL}^0(E) = \frac{D_{RL}(E) + l + 1}{D_{RL}(E) - l},$$

$$D_{RL}(E) = \frac{\partial \ln \Phi_{RL}(r, E)}{\partial \ln r} \Big|_{r = \text{AS radius}}$$

Potential parameters are determined from first-principles { not fitted like in empirical TB method } in self manner (LSDA)

Physical meaning of $P_{RL}^0(E)$:

$$P_{RL}^0(E) \propto \cotg \eta_{RL}(E), \quad \eta_{RL}(E) - \text{phase shift}$$

SUMMARY OF BASIC PROPERTIES OF LMTD BASIS SETS

- (i) $|\chi_{RL}^\alpha\rangle$ depend on lattice type - via $S^\alpha(S^0)$
- (ii) $|\chi_{RL}^\alpha\rangle$ depend on properties of atom sitting at site R - via potential parameters
- (iii) localization of $\langle r|\chi_{RL}^\alpha\rangle$ in real space and overlap $\langle \chi_{R'L'}^\alpha | \chi_{RL}^\alpha \rangle$ vary with LMTD representation $\propto$ (surfaces!)
- (iv) evaluation of $\langle \chi_{RL}^\alpha | \chi^{op} | \chi_{R'L'}^\alpha \rangle$ is straightforward: product of structure constants and radial integrals (advantage over LCAO!)
- (v) variational principle: perturbations added easily!

LMTD set can be 'tailored' to lattice, material and physical problem of interest

HAMILTONIAN & OVERLAP MATRICES IN ASA

$$O_{RL, R'L'}^\alpha = \langle \chi_{RL}^\alpha | \chi_{R'L'}^\alpha \rangle, \quad H_{RL, R'L'}^\alpha = \langle \chi_{RL}^\alpha | -\Delta + V^{LDA} | \chi_{R'L'}^\alpha \rangle$$

$$O^\alpha = (1 + h^\alpha \sigma^\alpha)(\sigma^\alpha h^\alpha + 1), \quad H^\alpha = (1 + h^\alpha \sigma^\alpha)(h^\alpha + E_v(1 + \sigma^\alpha h^\alpha))$$

Orthogonal MTO-representation: $\alpha_{RL} = \delta_{RL}$, $\sigma_{RL}^\alpha \equiv 0$!

$$O_{RL, R'L'} = \delta_{RR'} \delta_{LL'} \quad (\text{no overlap}) \quad S^2$$

$$H_{RL, R'L'} = \underbrace{C_{RL}}_{\text{levels}} \underbrace{\delta_{RR'} \delta_{LL'}}_{\text{widths}} + \underbrace{\Delta_{RL}^{1/2} \{ S^0 (1 - \delta S^0)^{-1} \}}_{\text{distortions}} \underbrace{\Delta_{R'L'}^{1/2}}_{\text{distortions}}$$

(i) Structural (S^0) & atomic (C, Δ, δ) features separated

(ii) Factor $(1 - \delta S^0)^{-1}$ important for s,p-states

RANDOM ALLOY $A_x B_{1-x}$

$x = C, \Delta, \delta$ are random: $X_{RL} = \begin{cases} X_L^A & \dots & x \\ X_L^B & \dots & 1-x \end{cases}$

S^0 is non-random for substitutional alloys

CPA averaging of $G(z) = (z.1 - H)^{-1}$ impossible in
orthogonal MTO repres (off-site disorder)
[S^2 is random] 7

COHERENT POTENTIAL APPROXIMATION

Soven: PR 156 (1967) 809 Velichy' et al: PR 175 (1968) 742
 Kaplan & Gray; Hockerjee and coworkers

Multiple scattering formalism

Embedded cluster method, Augmented space formalism,
 Recursion method (cluster effect $\propto Z^{-1}$, dimensionality)

random V_R^Q
 $= A, B$ $\left\{ \begin{array}{ccc} \circ & \circ & \circ \\ \circ & \circ & \circ \\ \circ & \circ & \circ \end{array} \right\} \xrightarrow[\text{aver}]{\text{conf}} \begin{array}{ccc} \odot & \odot & \odot \\ \odot & \odot & \odot \\ \odot & \odot & \odot \end{array} \quad \begin{array}{l} \text{effective} \\ \text{non-random} \\ \text{medium } \Sigma(z) \end{array}$

$$\begin{array}{ccc} \odot & \odot & \odot \\ \odot & \odot & \odot \\ \odot & \odot & \odot \end{array} = c_A \begin{array}{ccc} \odot & \odot & \odot \\ \odot & \circ & \odot \\ \odot & \odot & \odot \end{array} + c_B \begin{array}{ccc} \odot & \odot & \odot \\ \odot & \circ & \odot \\ \odot & \odot & \odot \end{array}$$

$$0 = c_A T_R^A(z) + c_B T_R^B(z) \quad \dots \text{no scattering}$$

$$T_R^Q(z) = (V_R^Q - \Sigma_R(z)) \left\{ 1 + \bar{G}_{RR}(z, \Sigma(z)) (V_R^Q - \Sigma_R(z)) \right\}^{-1}$$

CPA equation for $\Sigma(z)$

COMMENTS:

- (i) Equation is related to a single site R
(no multisite scatterings)
- (ii) Non-linear equation for unknown $\Sigma_R(z)$
- (iii) $\Sigma_R(z)$ is complex, energy-dependent
 - $\text{Re } \Sigma_R(z)$ level shift due to disorder
 - $\text{Im } \Sigma_R(z)$ damping of states due to disorder
- (iv) CPA is exact in
 1. low concentration limit (c_A or $c_B \rightarrow 0$)
 2. weak scattering limit
 3. split-band limit (separated bands)

First-principles alloy theory (LDA)

KKR CPA : Gyorfly & Stocks, Winter & Stocks (scf)
Livermore & Oak Ridge, Staunton (magnetic state)
Staunton, Weinberger (relativity)

LMTD CPA : present approach

CPA FOR TB-LMTO HAMILTONIAN: 3 steps.

1st: Transform exactly to non-random MTO repres β

$$G_{RL,R'L'}^{\beta}(z) = \lambda_{RL}^{\beta}(z) \delta_{RR'} \delta_{LL'} + \mu_{RL}^{\beta}(z) g_{RL,R'L'}^{\beta}(z) \mu_{R'L'}^{\beta}(z),$$

$$g_{RL,R'L'}^{\beta}(z) = \left\{ (P^{\beta}(z) - S^{\beta})^{-1} \right\}_{RL,R'L'}; \quad \lambda_{RL}^{\beta}, \mu_{RL}^{\beta} \equiv f(C_{RL}, \Delta_{RL}, \tau_{RL})$$

$$P_{RL}^{\beta}(z) = \frac{z - C_{RL}}{\Delta_{RL} + (\tau_{RL} - \beta_{RL})(z - C_{RL})} \rightarrow \text{random, site-diagonal}$$

$$S_{RL,R'L'}^{\beta} = \left\{ S^0 (1 - \beta S^0)^{-1} \right\}_{RL,R'L'}; \quad \beta \rightarrow \beta_{RL} \equiv \beta_L \rightarrow \begin{matrix} \text{non} \\ \text{random} \end{matrix}$$

Non-random β $\Rightarrow$ $\beta_{RL} \equiv 0$ - canonical: $S^0(k)$ - Ewald summ
(examples) $\beta_{RL} \equiv (\beta_s, \beta_p, \beta_d)$ - most localized: $S^{\beta}(k)$ - Bloch $2NN$

2nd: CPA averaging of $g^{\beta}(z) \rightarrow$ only site-diagonal disorder (like KKR CPA)

$$\langle g^{\beta}(z) \rangle = (P^{\beta}(z) - S^{\beta})^{-1}, \quad g_{RL}^{\beta}(z) \equiv g_L^{\beta}(z) \rightarrow \begin{matrix} \text{coherent} \\ \text{potential function} \end{matrix}$$

Set of CPA-equations to be solved:

$$P_L^{\beta}(z) = \Omega_L^{\beta}(z) + [\Phi_L^{\beta}(z)]^{-1}, \quad \Phi_L^{\beta}(z) = \frac{1}{N} \sum_k \left\{ (P^{\beta}(z) - S^{\beta}(k))^{-1} \right\}_{LL} =$$

$$= x (P_{L,A}^{\beta} - \Omega_L^{\beta}(z))^{-1} + (1-x) (P_{L,B}^{\beta} - \Omega_L^{\beta}(z))^{-1} \quad \left[\begin{matrix} L = s, p, t_{2g}, e_g \text{ for} \\ \text{cubic lattices} \end{matrix} \right]$$

3rd: Transform back to orthogonal MTO repres

$$\langle G(z) \rangle_{RL, R'L'} = \Lambda_L^\beta(z) \delta_{RR'} \delta_{LL'} + M_L^\beta(z) \langle g^\beta(z) \rangle_{RL, R'L'} M_{L'}^\beta(z), \text{ where}$$

$$\Lambda_L^\beta(z), M_L^\beta(z) \equiv f(p_L^{\beta,A}, p_L^{\beta,B}, p_L^\beta) - \text{details: PRB } \underline{41} (1990) \text{ p. 7515}$$

EFFECTIVE HAMILTONIAN

$$\langle G(z) \rangle_{RL, R'L'} = \{ (z. I - H^{\text{eff}}(z))^{-1} \}_{RL, R'L'}, \text{ where}$$

$$H_{RL, R'L'}^{\text{eff}}(z) = \tilde{C}_L(z) \delta_{RR'} \delta_{LL'} + \tilde{\Delta}_L^{1/2}(z) \{ S^0 (1 - \tilde{J}(z) S^0)^{-1} \}_{RL, R'L'} \tilde{\Delta}_{L'}^{1/2}(z)$$

$\tilde{C}(z), \tilde{\Delta}(z), \tilde{J}(z)$ - non random coherent potential parameters
renormalizing random potential parameters $C_{RL}, \Delta_{RL}, J_{RL}$

Empirical TB-CPA: only $\tilde{C}(z) \rightarrow \Sigma(z)$ determined within CPA,
 $\tilde{J}(z)$ and $\tilde{\Delta}(z) \rightarrow J^{\text{VCA}}, \Delta^{\text{VCA}}$

SELFENERGY with respect to H^{ref}

J. Phys. Chem. Sol.
49 (1988) 349

$$\langle G(z) \rangle_{RL, R'L'} = \{ (z. I - H^{\text{ref}} - \Sigma(z))^{-1} \}_{RL, R'L'}; H^{\text{ref}} = H^{\text{VCA}}, H^{\text{host}}, \dots$$

$$\Sigma_{RL, R'L'}(z) = z \delta_{RR'} \delta_{LL'} - H_{RL, R'L'}^{\text{ref}} - \{ \langle G(z) \rangle^{-1} \}_{RL, R'L'}$$

closed expression
or
for
 $\langle G(k, z) \rangle^{-1}$

$$\Sigma_{LL'}(k) = z \delta_{LL'} - H_{LL'}^{\text{ref}}(k) - \{ \langle G(k, z) \rangle^{-1} \}_{LL'}$$

$\Sigma(z)$ is k -dependent (not site-diagonal) although

$p_L^\beta(z)$ is site-diagonal { k -independent in ETB-CPA }

CHARGE SELFCONSISTENCY

Charge density in random alloy $A_x B_{1-x}$ (CPA)

$$n^Q(r) = \frac{1}{4\pi} \sum_L 2 \int_{-E_F}^{E_F} |\varphi_L^Q(E, r)|^2 g_L^Q(E) dE \quad (Q = A, B)$$

and

(cubic symmetry)

$$g_L^Q(E) = -\frac{1}{\pi} \frac{dP_L^{B,Q}(E)}{dE} \operatorname{Im} \left(P_L^{B,Q}(E) - \Omega_L^B(E+i0) \right)^{-1} \equiv -\frac{1}{\pi} \operatorname{Im} \langle G(E+i0) \rangle_{RL,RL}$$

$$\phi_L^B(z) = \frac{1}{N} \sum_k \left\{ (P_L^B(z) - S^B(k))^{-1} \right\}_{LL}, \quad \Omega_L^B(z) = P_L^B(z) - \left\{ \phi_L^B(z) \right\}^{-1}$$

and $\varphi_L^Q(E, r)$ is the solution of radial SE in AS

with the LDA potential $V^Q(r)$

$$V^Q(r) = -\frac{2Z^Q}{r} + 2 \int_0^{s^Q} \frac{n^Q(r')}{|\vec{r} - \vec{r}'|} 4\pi r'^2 dr' + \mu_{xc}(n^Q(r))$$

set LDA - CPA LOOP

i -th $\Rightarrow i+1$ -th

$$\begin{matrix} \varphi_L^{Q(i)}(E, r) & P_L^{Q(i)}(z) \\ \mathcal{P}_L^{(i)}(z) \end{matrix} \Rightarrow \boxed{\text{CPA solver}} \Rightarrow \begin{matrix} \varphi_L^{Q(i+1)}(z) & n^{Q(i+1)}(r) \\ g_L^{Q(i+1)}(E) & V^{Q(i+1)}(r) \end{matrix} \Rightarrow$$

$$\boxed{\text{LDA solver}} \Rightarrow \frac{\partial \ln \varphi^Q(r, E)}{\partial \ln r} \bigg|_{r=s^Q} \Rightarrow \begin{matrix} P_L^{B,Q(i+1)}(z) \\ P_L^{(i+1)}(z) \end{matrix} \Rightarrow \text{next loop}$$

Details of self LDA-CPA loop:

(i) Zig-Zag CPA-LDA iterations

{ neither CPA - $\rho(r)$ nor LDA - $V^Q(r)$ are solved till self in a given loop }

(ii) Mixing of old/new $V^Q(r)$ necessary to prevent oscillations (divergency) : $\alpha_{mix}^{LDA} \sim \text{few \% of new}$
 { especially delicate: alloys close to ferro instab }

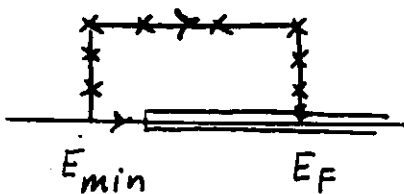
(iii) LDA loop can be terminated if:

$$\delta \| r V(r) \| < \epsilon \quad \text{for each } r \in (0, s^Q)$$

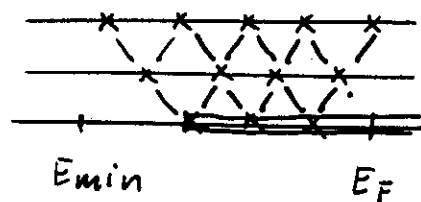
$$\delta \| P^Q(E) \| < \epsilon \quad \text{for each } E \text{ and } Q = A, B$$

$$\delta \| n^Q(r) \| < \epsilon \quad \text{for each } r \in (0, s^Q) \quad \text{etc ...}$$

(iv) E-integration for $n^Q(r)$:



or



$$\oint \rightarrow \oint$$

complex contour
integrations

analytic deconvolution
back to real axis

(v) Brillouin-zone integration:

1. Standard (regular mesh, rays, tetrahedrons...)
2. Surface-like:

$$\dots \left[\begin{array}{|c|} \hline \text{bulk} \\ \hline \end{array} \right] + \left[\begin{array}{|c|} \hline \text{bulk} \\ \hline \end{array} \right] + \dots \equiv \dots \left[\begin{array}{|c|} \hline \text{bulk} \\ \hline \end{array} \right] \dots$$

3. Weyl-type (fast LMTO CPA)

(vi) CPA equation:

We solve CPA equation for coherent interactor $\Omega_L^\beta(z)$ rather than for coherent potential function $\mathcal{P}_L^\beta(z)$:

$$\begin{aligned} \phi_L^\beta(z) &= \frac{1}{N} \sum_k \left\{ (\mathcal{P}_L^\beta(z) - S^\beta(k))^{-1} \right\}_{LL} && (\text{cubic lattices, } L \leq 2) \\ \Omega_L^\beta(z) &= \mathcal{P}_L^\beta(z) - \left\{ \phi_L^\beta(z) \right\}^{-1} && (\text{interactor}) \\ \tilde{\phi}_L^\beta(z) &= \sum_{A,B} c^A \left(\mathcal{P}_L^{\beta,A}(z) - \Omega_L^\beta(z) \right)^{-1} && (\text{CPA equation}) \\ \mathcal{P}_L^{\beta, \text{new}}(z) &= \Omega_L^\beta(z) + \left\{ \tilde{\phi}_L^\beta(z) \right\}^{-1} \end{aligned}$$

This form of CPA converges in each case with $\alpha_{\text{mix}}^{\text{CPA}} = 1$

CPA selfconsistency is reached if $\delta \|\Omega_L^\beta(z)\| < \epsilon$

for each z simultaneously with LDA

(vii) Possibility for selfconsistency with respect to the choice of WS-radii s^A (charge neutrality in AS)

FAST LMTD-CPA METHOD : Weyl k -integration

Akai (1989) : KKR CPA, Abrikosov et al (1991) : LMTD CPA

Repeated IBZ integration in each LSDA-CPA loop is the most numerically demanding part of calculations

$$\Phi_{LL'}^{(n)}(z) = \frac{1}{V} \int \left\{ (\hat{\mathcal{P}}(z) - \hat{S}(k))_{LL'}^{-1} \right\} d^3k \quad \text{— central quantity for LSDA \& CPA}$$

Consider a set of k -points $\{k_n\}$ distributed uniformly in IBZ

$$I^N = \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{n=1}^N f(k_n) \longrightarrow I = \frac{1}{V} \int f(k) d^3k$$

Monte Carlo : convergence rate to I is $1/\sqrt{N}$

$$\text{Weyl : } k_n^\alpha = n k_0^\alpha - [n k_0^\alpha] \quad (\alpha = x, y, z; k_n^\alpha \in \text{IBZ})$$

k_0^α — irrational

convergence rate to I is $1/N$

Basic trick :

I^N is continuously improved by adding additional k -points without recalculating previous one

$$\Phi_{LL'}^{(n)}(z) = (1-r_n) \Phi_{LL'}^{(n-1)}(z) + r_n \left\{ \hat{\mathcal{P}}(z) - \hat{S}(k_n) \right\}_{LL'}^{-1}$$

Simplest choices:

(i) $r_n = 1/n$

(ii) $r_n = \frac{w_n}{S_n}$, $S_n = S_{n-1} + w_n$, $S_0 = 0$

$w_n = 1 - \alpha^n$ ($\alpha \approx 0.99$). If $w_n = 1$, $r_n = 1/n$

{weighting factor to get rid of bad history of early steps}

Practical procedure:

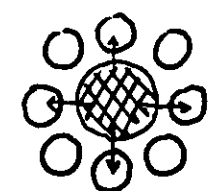
- (i) start from some guess for $\phi(z)$, say summing up first 50 k -points without CPA $\propto$ LDA
- (ii) perform LDA $\propto$ CPA loop
- (iii) add few additional k -points (1-5) and perform LDA $\propto$ CPA loop etc

Advantages / disadvantages

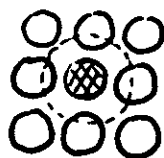
- (i) numerical requirements comparable to those for hsc crystal
- (ii) large number of LSDA $\propto$ CPA loops can be done (alloys close to magnetic instability)
- (iii) uniform distribution; oscillatory convergence of k -points

ALLOY OF ATOMS WITH DIFFERENT SIZES

• Single MT-impurity model



real case



single MT-model

○ Cu



● Pd or Au

- (i) Charge sc is performed in smaller sphere $\Rightarrow$ overscreening (shift Pd/Au d-band downwards of host Cu d-band)
- (ii) Distances (hoppings) Cu-Pd (Cu-Au) become underestimated (overestimated) $\rightarrow$ Pd/Au widths overestimated

• Cu-rich random alloy

- (i) overscreening slightly suppressed $\rightarrow$ Pd/Au MT-impurity in effective, Cu-dominated medium

Cure: charge sc also on 1nn (beyond CPA) or in enlarged Pd/Au-spheres (possible in ASA - neutral AS:.)

- (ii) lattice distortions stronger $\rightarrow$ finite probability for 1nn Pd-Pd / Au-Au pair

We account approximately for both effects in

TB-LMTO-CPA

ALLOY $\text{Cu}_{75}\text{Au}_{25}$: ordered, disordered, with LRO

The problem requires the solution of coupled CPA eqs on four interpenetrating sc lattices $\Rightarrow \text{Cu}_3\text{Au}$ lattice

$S_{Rl, R'l'}^{\beta, \text{fcc}}$ decomposed into four $S_{R_\alpha L, R'_\alpha L'}^{\beta, \text{sc}}$ ($\alpha, \alpha' = 1, 2, 3, 4$ or $\text{Cu}, \text{Cu}, \text{Cu}, \text{Au}$)

We solve 36×36 CPA problem with sublattice component concentrations $c_Q(\alpha)$: $Q = \text{Cu}, \text{Au}$; $\alpha = \text{Cu}, \text{Cu}, \text{Cu}, \text{Au}$

$$\begin{aligned} c_{\text{Cu}}(\text{Cu}) &= \frac{3+S}{4} & c_{\text{Au}}(\text{Cu}) &= \frac{1-S}{4} \\ c_{\text{Cu}}(\text{Au}) &= \frac{3}{4}(1-S) & c_{\text{Au}}(\text{Au}) &= \frac{1+3S}{4} \end{aligned} \Rightarrow S \in (0,1) \text{ is the LRO parameter}$$

$S=0 \equiv$ disordered $\text{Cu}_{75}\text{Au}_{25}$; $S=1 \equiv$ ordered Cu_3Au

ALLOY $\text{Cu}_{75}\text{Au}_{25}$: ordered, disordered, with LRO

(i) Ordered Cu_3Au alloy (no lattice relaxations)

Crystal Cu/Au potential parameters transferable:

just scale them to account for difference $w^{\text{Cu}}/w^{\text{Au}}$
and $w^{\text{Cu}_3\text{Au}}$ (w - WS radii) - Andersen

(ii) Disordered $\text{Cu}_{75}\text{Au}_{25}$ alloy (9x9 CPA problem for spd-LMTO's)

We perform calculations for model without and
with lattice relaxations

(iii) $\text{Cu}_{75}\text{Au}_{25}$ alloy with LRO

$$X^{\text{LRO}} = S X^{\text{Cu}_3\text{Au}} + (1-S) X^{\text{Cu}_{75}\text{Au}_{25}}; \quad X = C, \Delta, \uparrow; \quad S - \text{LRO param}$$

The problem requires the solution of coupled CPA eqs
on four interpenetrating sc lattices $\Rightarrow \text{Cu}_3\text{Au}$ lattice

$$S_{R_L, R'_L}^{\beta, \text{fcc}} \text{ decomposed into four } S_{R_L, R'_L}^{\beta, \text{sc}} \quad \left(\alpha, \alpha' = 1, 2, 3, 4 \text{ or } \text{Cu, Cu, Cu, Au} \right)$$

We solve 36x36 CPA problem with sublattice component
concentrations $c_Q(\alpha)$: $Q = \text{Cu, Au}$; $\alpha = \text{Cu, Cu, Cu, Au}$

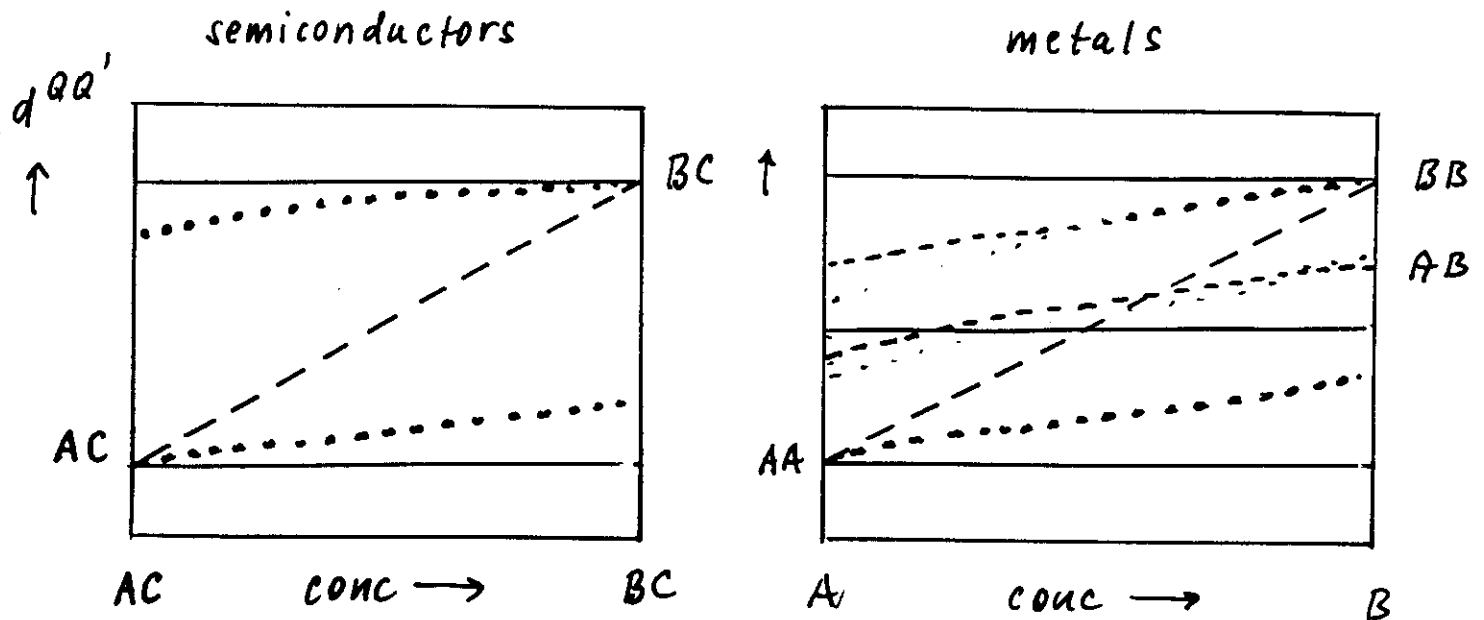
$$\begin{aligned} c_{\text{Cu}}(\text{Cu}) &= \frac{3+S}{4} & c_{\text{Au}}(\text{Cu}) &= \frac{1-S}{4} \\ c_{\text{Cu}}(\text{Au}) &= \frac{3}{4}(1-S) & c_{\text{Au}}(\text{Au}) &= \frac{1+3S}{4} \end{aligned} \Rightarrow \begin{array}{l} S \in (0,1) \text{ is the} \\ \text{LRO parameter} \end{array}$$

$$S=0 \equiv \text{disordered } \text{Cu}_{75}\text{Au}_{25}; \quad S=1 \equiv \text{ordered } \text{Cu}_3\text{Au}$$

LATTICE RELAXATIONS

Mismatch in sizes of atoms $\rightarrow$ local distortions,
different bond-lengths in random alloys

Models - experiments



- full relaxation (conc. indept, pure QQ -values preserved)
- no relaxation (linear conc variation, all bonds same)
- experiment (EXAFS - real situation: in between)

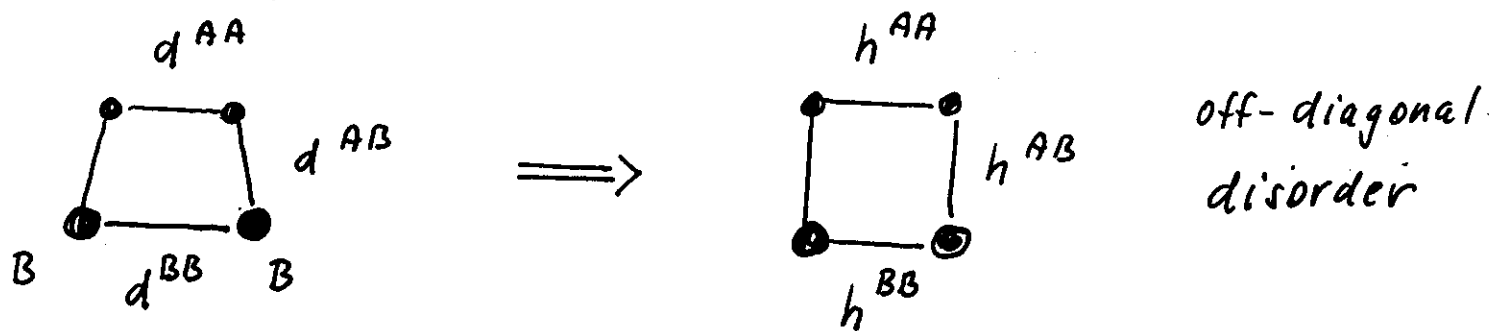
Remarks

(i) in metallic alloys $d^{AB} \approx (d^{AA} d^{BB})^{1/2} \approx \frac{d^{AA} + d^{BB}}{2}$
both for exp and fully relaxed model

(ii) It are most relevant in Q-rich cases, so that
for $Q=A$ are d^{AA} and especially d^{AB} important
(error in model for d^{BB} has less importance)

$$N^{AA} \propto C_A^2, N^{AB} \propto 2C_A C_B \gg N^{BB} \propto C_B^2 \text{ for } C_A \gg C_B$$

Modelling of lattice relaxations (TB, TB LMTD):



$S_{RR'}^\alpha$ is now random, configuration dependent and approximations are inevitable:

(i) terminal-point approximation

$$S_{RR'}^\alpha \Rightarrow S_{RR'}^{\alpha, QQ'} \quad \text{depends only on occupation of } R, R' \rightarrow \text{not on all alloy!}$$

(ii) neglect of any angle distortions — close packed

$$S_{RR'}^{\alpha, QQ'} \propto \lambda_R^Q S_{RR'}^{\alpha(0)} \lambda_{R'}^{Q'} \quad \text{non-random ideal lattice}$$

Remarks: (i) simple choice: $\lambda_{RL}^Q \propto (W_{LL}^{\text{alloy}} / S_R^Q)^{l+1/2}$

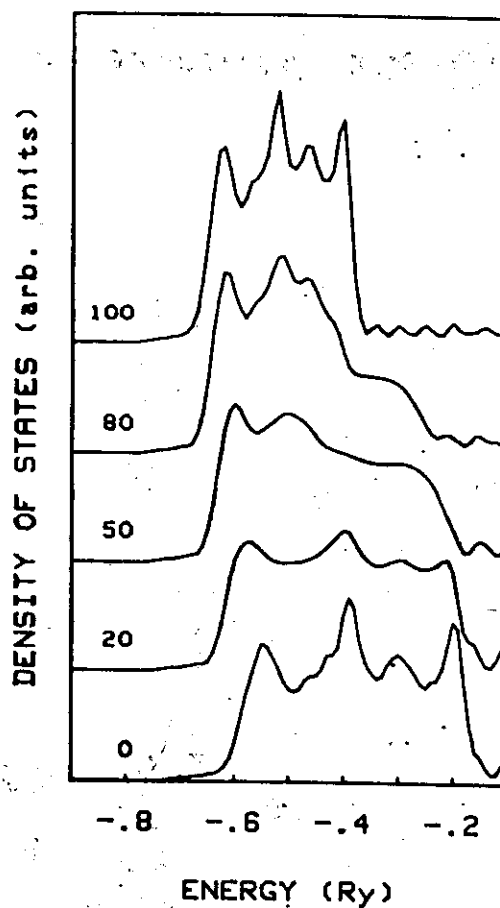
(ii) such mapping is valid only approximately but represents a reasonable first step

(iii) λ_R^Q are absorbed by $\Delta_R^Q, \tilde{\Delta}_R^Q$ and give rise to a modified $\tilde{\Delta}_R^Q, \tilde{\tilde{\Delta}}_R^Q$ as expected

(iv) transformation of spherical functions under shift

(v) real-space description (recursion method)

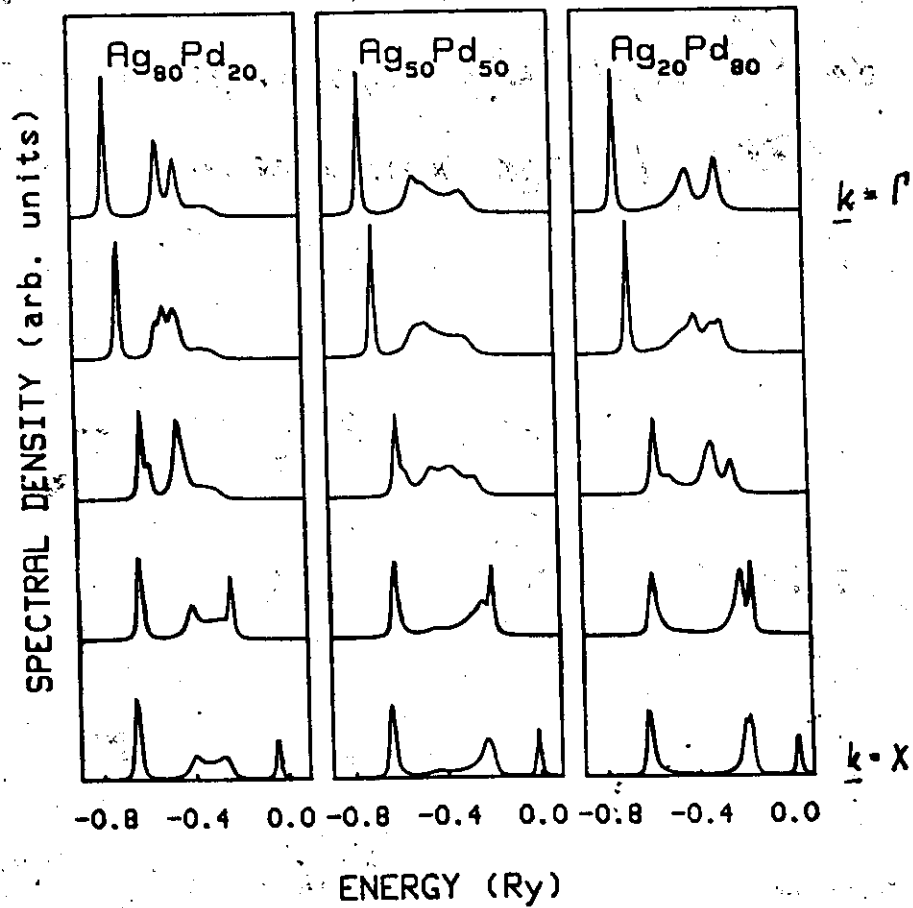
Total DOS



Dominating 'level' disorder,
non-negligible 'width' disorder

DOS: Ag_xPd_{1-x} random alloys

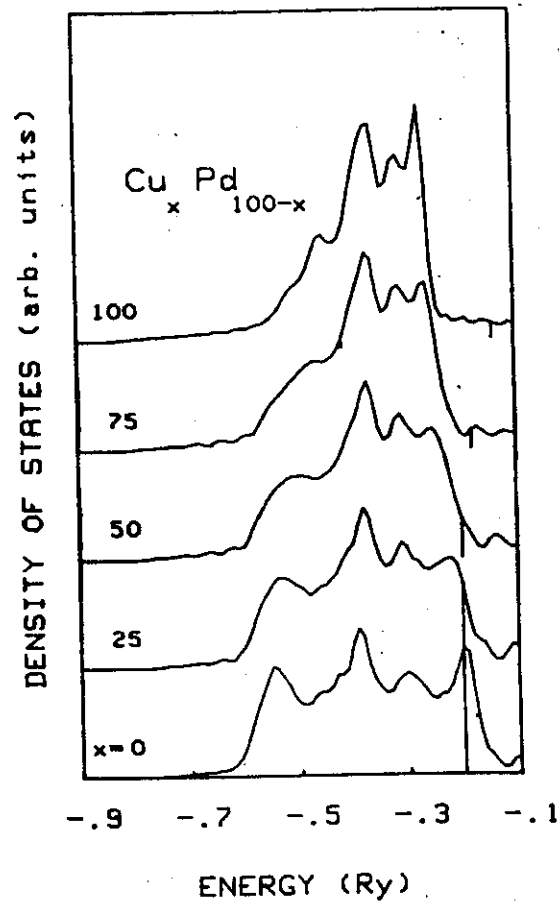
k -resolved spectral density $A(k, E)$



$$A(k, E) = -\frac{1}{\pi} \text{Im} \text{tr} \bar{G}(k, E + i0), \quad k \in \text{BZ}$$

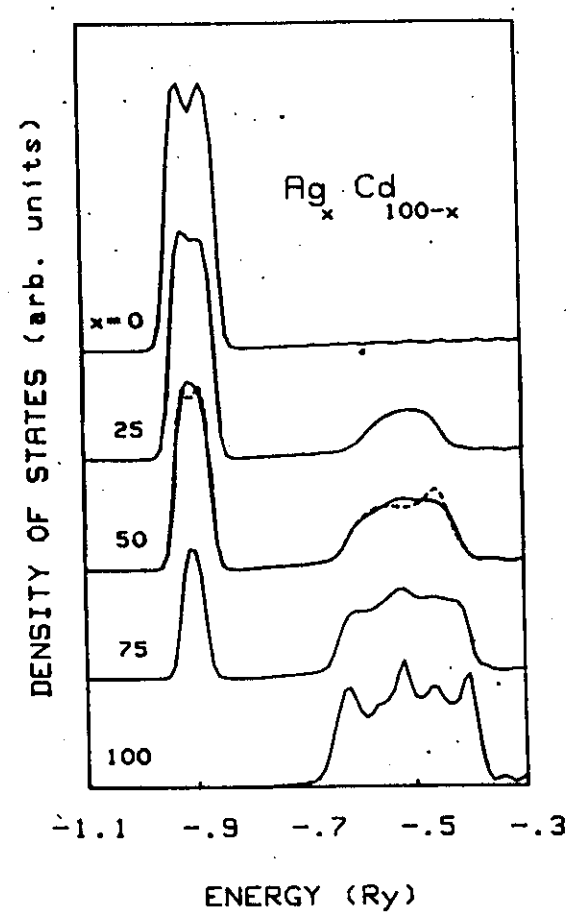
$$A^0(k, E) = \sum_n \delta(E - E_n(k)) \quad - \text{pure crystal}$$

Total DOS



common alloy band
dominating 'band-width' disorder,
negligible 'level' disorder

Total DOS



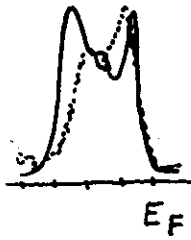
split-band limit alloy

— KKRCPA

..... experiment:

PES, Cooper minimum

$\Rightarrow$ Pd
LDOS

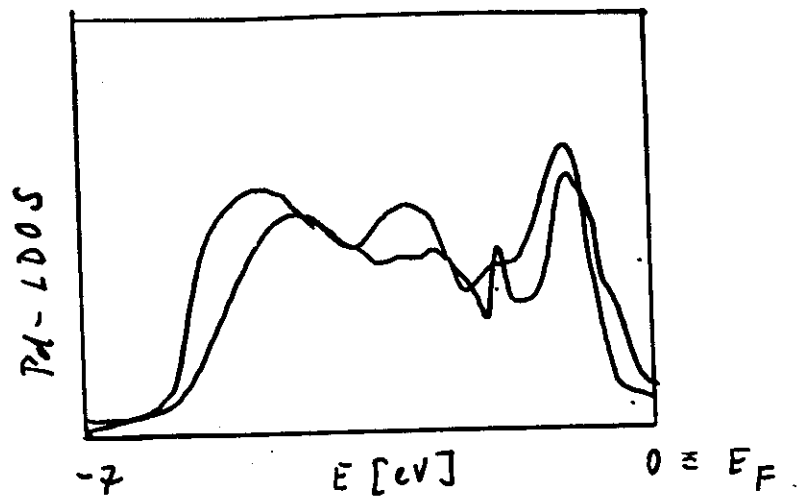


$\text{Cu}_{75}\text{Pd}_{25}$ alloy

— TB-LMTO-CPA (1r incl)

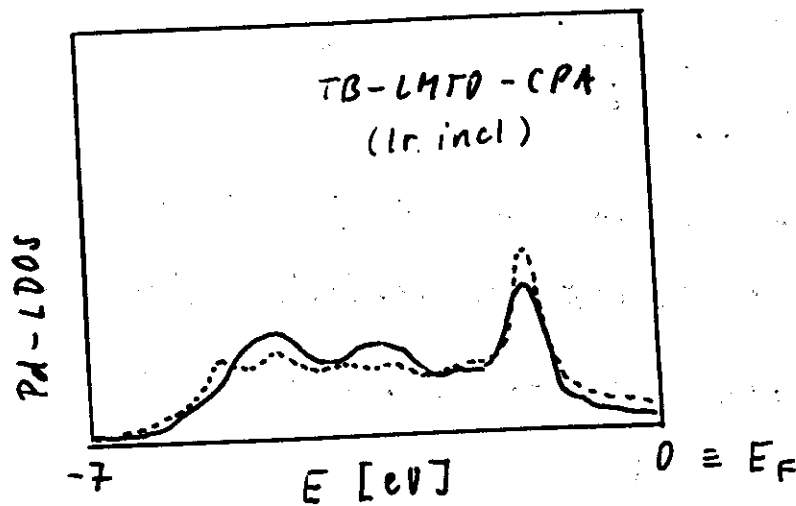
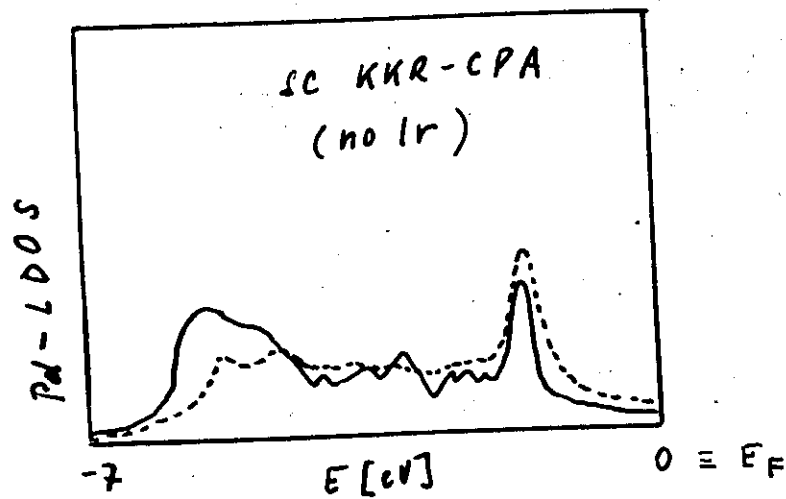
— KKRCPA (sc in equal-size HT's)

FWHM narrowing of
TB-LMTO-CPA



Cu₉₅Pd₅ alloy

---- single impurity calc : Dederichs et al
(broadened) SSC 62 (1987) 735



Experiment

Krummacher, Sen, Gudat, Johnson, Grey, Ghijsen:

Z. Phys. B 75 (1989) 235

Ref. 17 (Calculations)

Ginatempo, Staunton:

J. Phys. 18 (1988) 9985

241

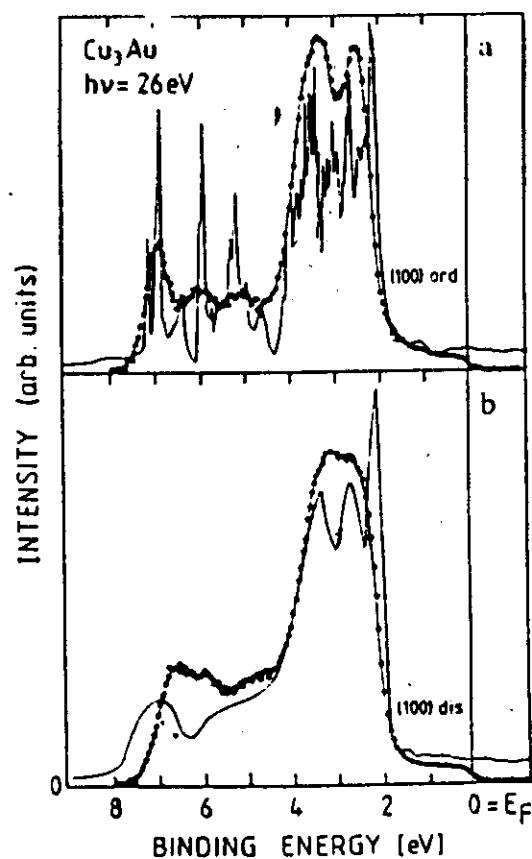


Fig. 4a and b. Comparison of the experimental valence band spectrum of Cu₃Au(100) with relativistic density of states calculations: a self-consistent KKR calculation for the ordered state. b KKR CPA calculation for the random alloy, using the same potential function as in a). Calculations from Ref. 17.

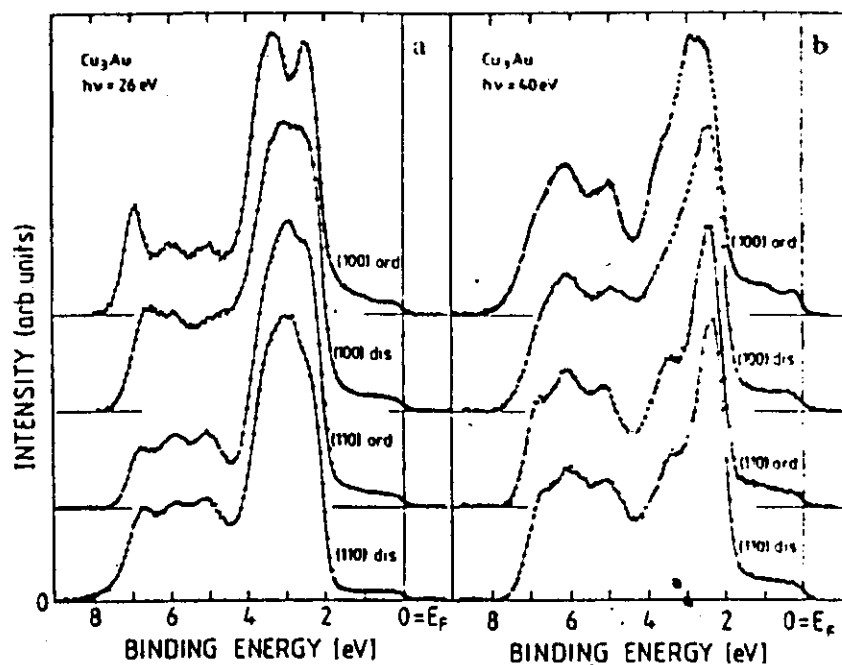
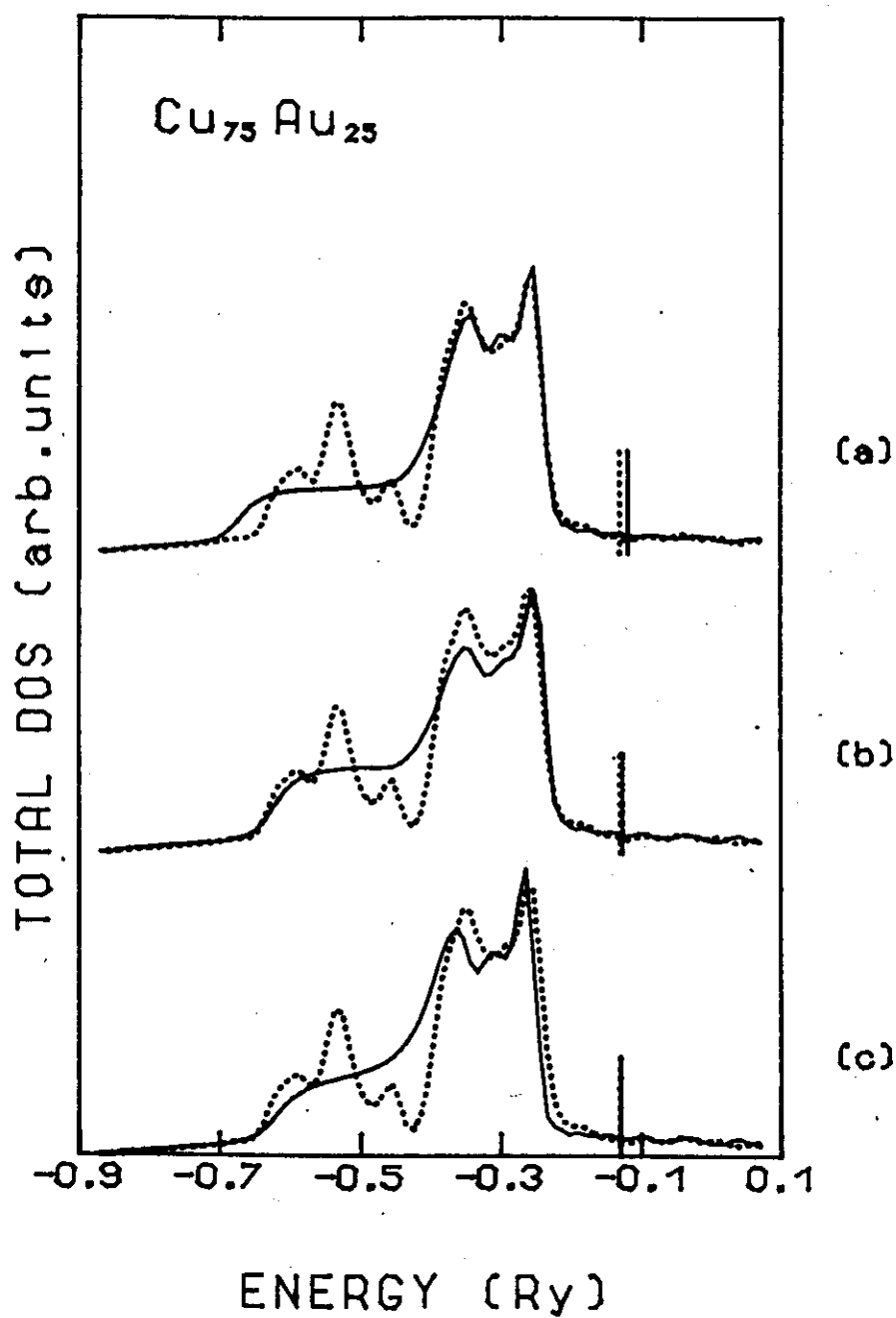


Fig. 8a and b. Comparison of valence band spectra of ordered and disordered Cu₃Au(100) and Cu₃Au(110) surfaces from Figs. 3 and 5 to 7 at a 26 eV photon energy and b 40 eV photon energy

(a) - no lr

(b) - lr incl

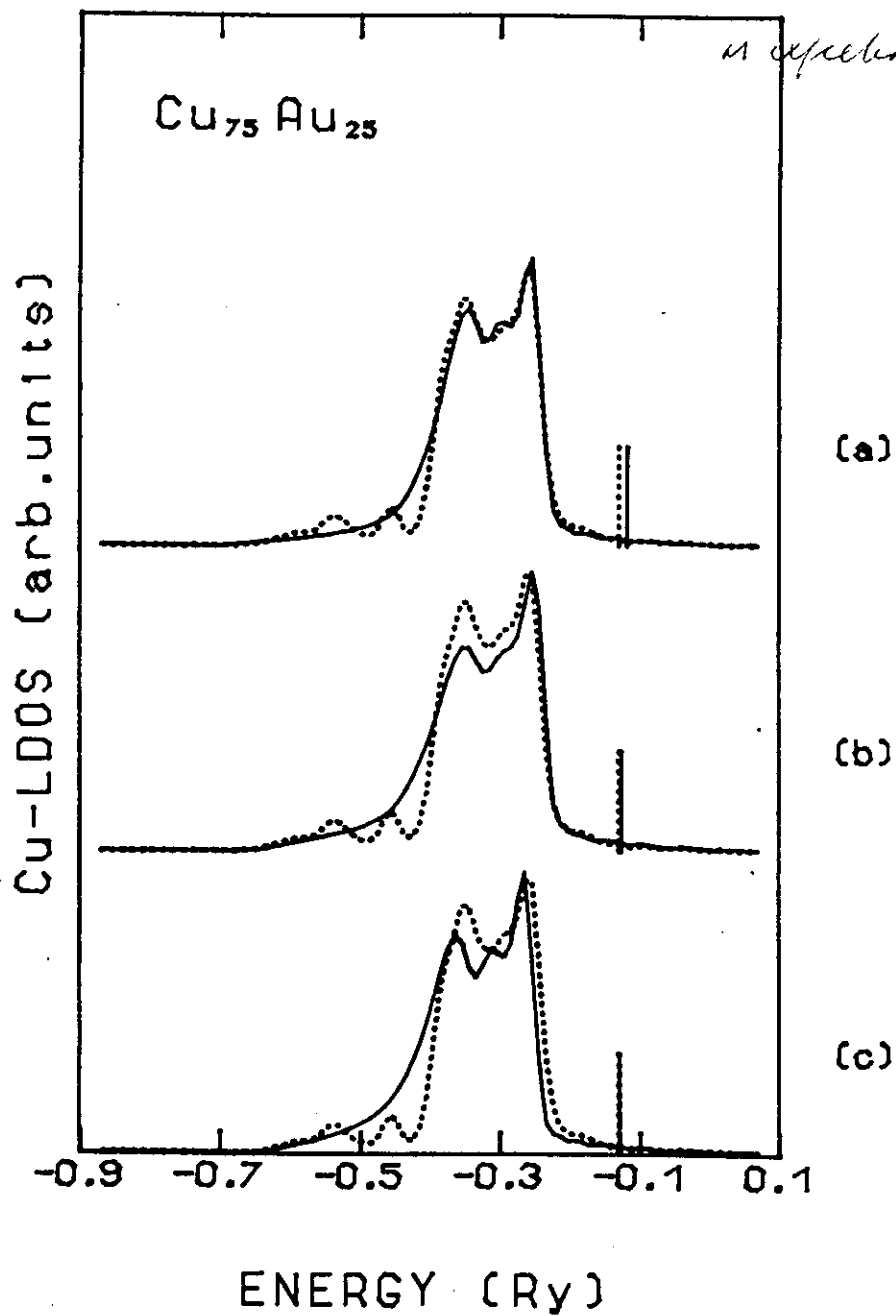
(c) - lr incl + neutr



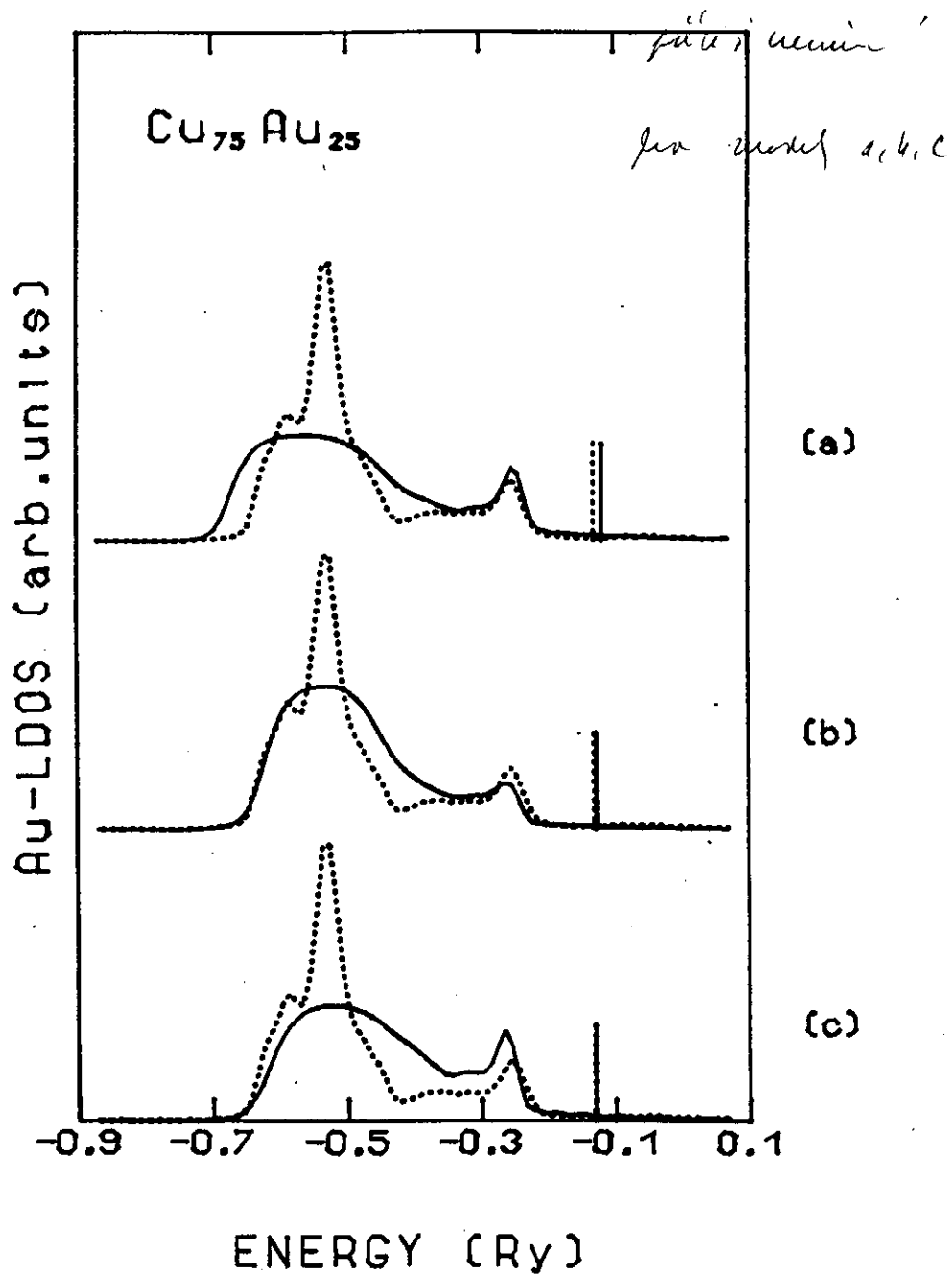
fin 60 -

u de^c 10 - LDOS

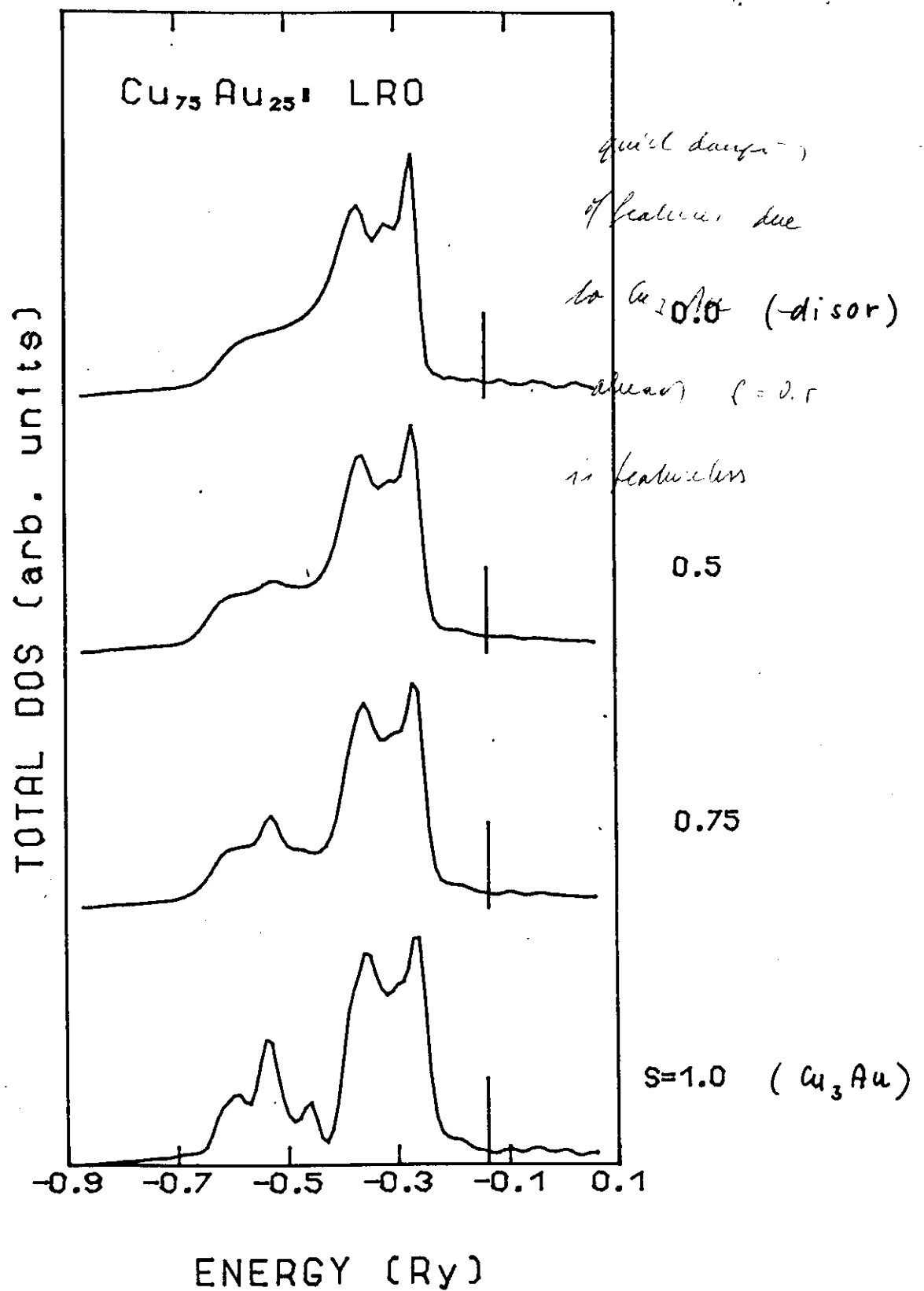
is expected



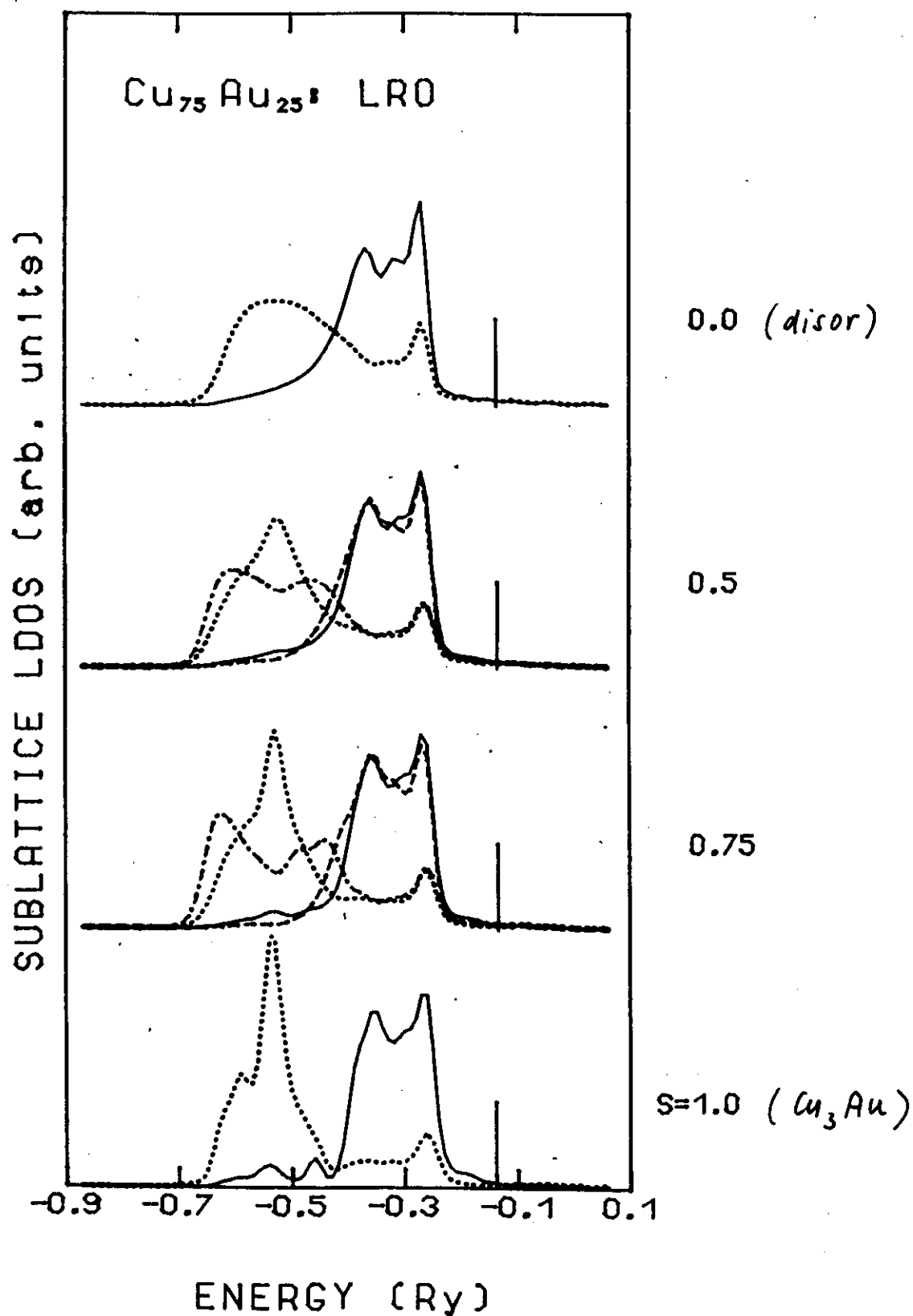
60- (10) u

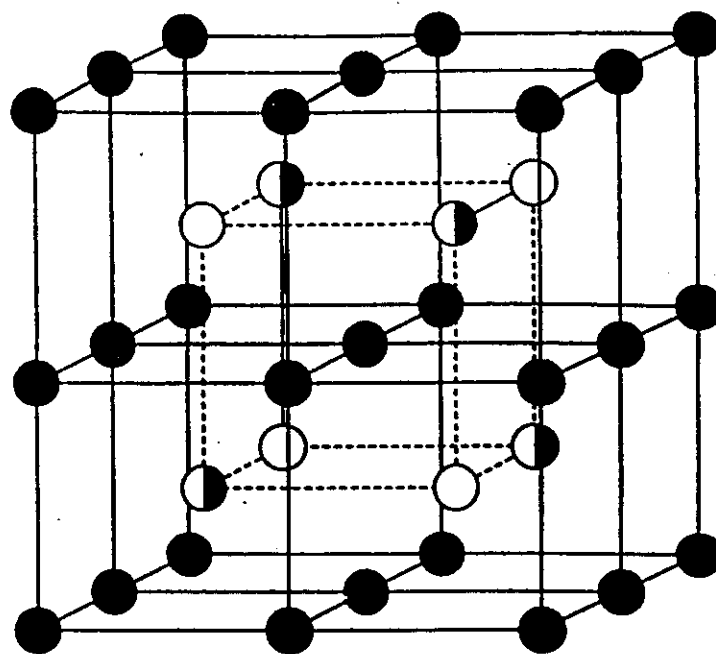


$S \equiv$ LRO parameter

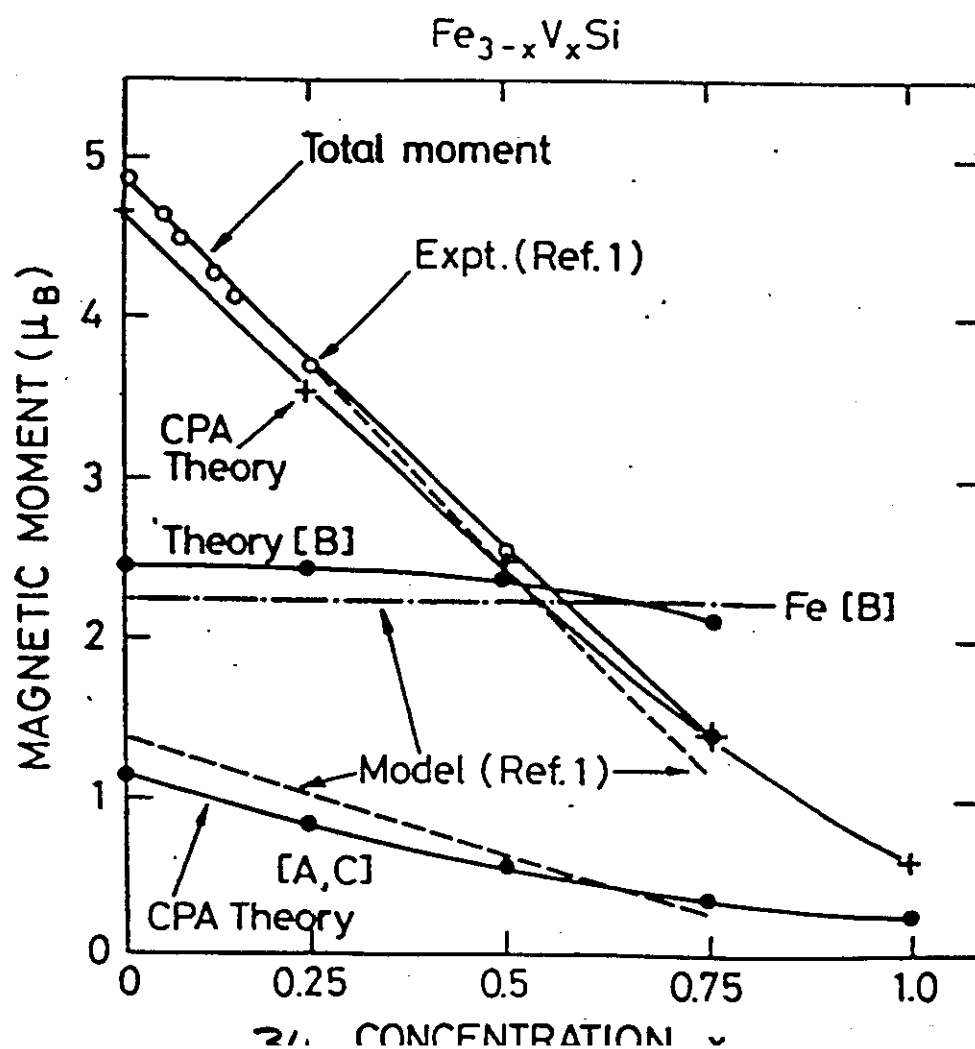


— Cu-LDOS on Au sublattice
 Au-LDOS on Au sublattice
 ---- Cu-LDOS on Cu sublattice
 - - - - Au-LDOS on Cu sublattice





- Fe[A,C] ◐ Fe[B]
 ○ Si[D]



— total

— minority

— majority

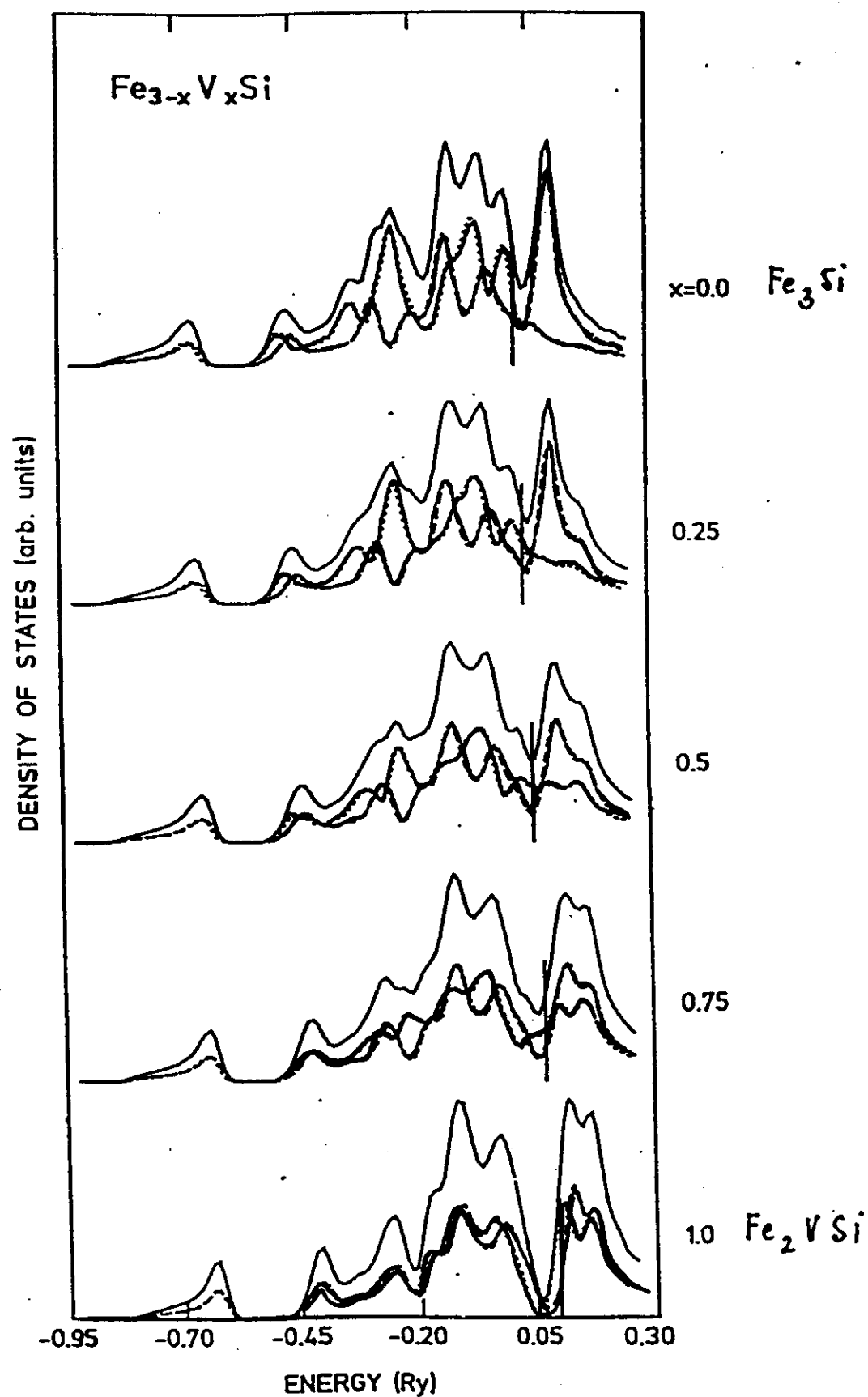


FIG. 8. Fe_{3-x}V_xSi. Total (solid lines) minority-spin (dashed) and majority-spin (dotted) DOS functions. The Fermi-level positions are indicated by vertical lines

— Fe[B]

---- Fe[A,C]

.... V[B]

----- Si[D]

Minority - spin

Majority - spin

