



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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**College on Medical Physics:
Imaging and Radiation Protection**

31 August - 18 September 1992

*Radiographic Sensitized
Material Evaluation*

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International Atomic Energy Agency
Division of Nuclear Safety
Vienna, Austria

RADIOGRAPHIC SENSITIZED MATERIALS EVALUATION

- * *Test new image registration system*
(strictly connected with progress in Radiology)

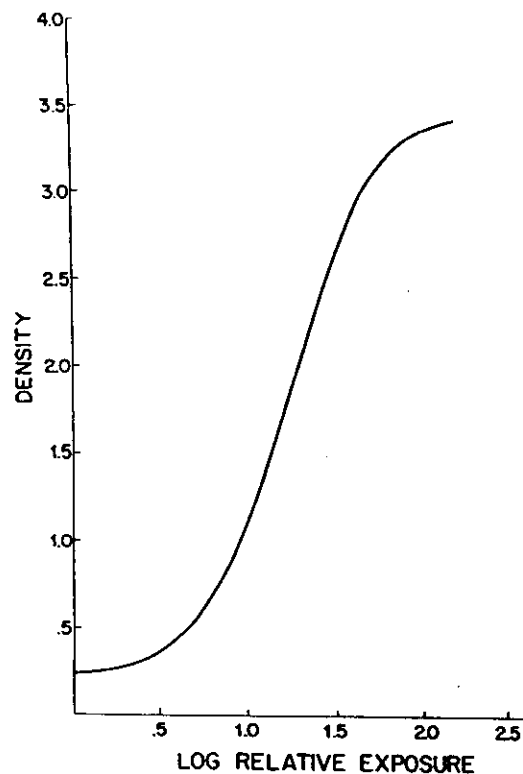
**** Purchasing criteria**

FUNDAMENTAL PHYSICAL PARAMETERS WHICH DETERMINE THE QUALITY OF A FILM -SCREEN SYSTEM

- * **IMAGE QUALITY**
 - Characteristic curve*
 - Spatial resolution*
 - Noise*

**** PATIENT DOSE Sensitivity**

CHARACTERISTIC CURVE



CONTRAST = 1° Derivative of characteristic curve

$$\text{GAMMA} = \frac{D_2 - D_1}{\log E_2 - \log E_1}$$

$$\text{LATITUDE} = E_2 - E_1$$

$$\text{AVERAGE CONTRAST} = \frac{1.75}{\log E_4 - \log E_3}$$

SENSITIVITY

The reciprocal of exposure required to obtain an optical density of 1 (above the base plus fog level)

NOTE

It is commonly used the parameter SPEED instead of sensitivity:

$$\text{Sensitivity(mR)} = 128 / \text{Speed}$$

SPATIAL RESOLUTION

Spatial resolution means the capability of a receptor to reproduce small size, high contrast detail.

If the system is isoplanar and linear



MTF (Modulation Transfer Function)

Is the parameter most commonly used to describe the spatial resolution.

It is a monodimensional function which represents the contrast dependence on spatial frequency.

NOISE

QUANTUM NOISE

local statistical variation in the number of x-ray photons

STRUCTURAL NOISE

not uniformity size of grains of the screen and of the film

INTRINSIC NOISE

film granularity

OTHER SOURCES NOISE

manufacturing and developing process

*** INCOMPLETE DESCRIPTION standard deviation**

*** DETAILED ANALYSIS Wiener spectrum**

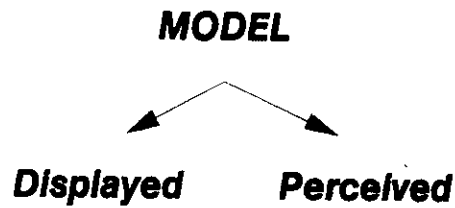
IMAGE QUALITY :

SYNTHESIS OF VARIOUS PHYSICAL CHARACTERISTICS
(non mutually independent)



SINGLE QUALITY INDEX

*** Diagnostic accuracy: measure of visual image quality**



The *displayed statistical decision theory model* $SNR_{S,D}^2$

$$SNR_{S,D}^2 = k\gamma^2 \frac{\left(\int_0^{\infty} O^2(u)M^2(u)u \cdot du \right)^2}{\int_0^{\infty} O^2(u)M^2(u)W(u)u \cdot du}$$

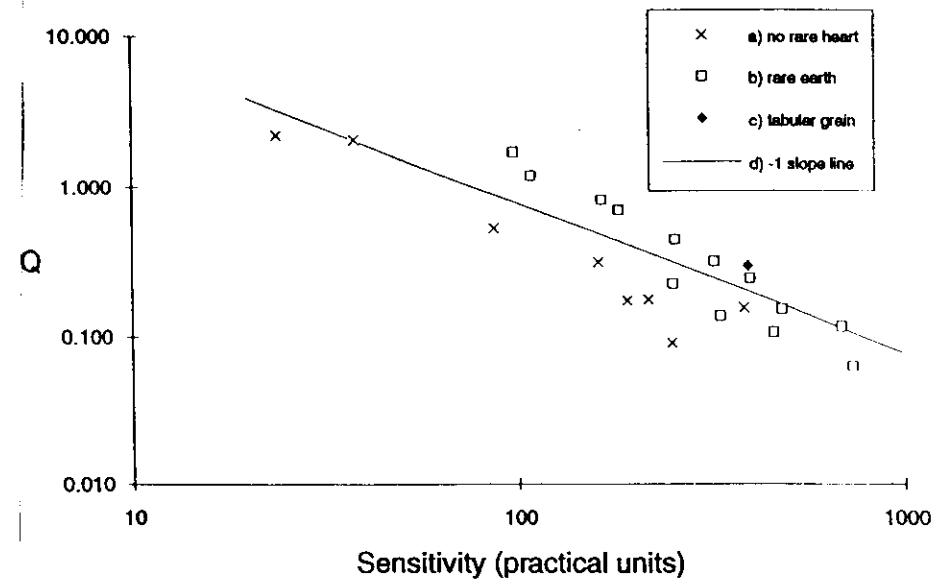
The *displayed amplitude model* $SNR_{A,D}^2$

$$SNR_{A,D}^2 = k\gamma^2 \frac{\left(\int_0^{\infty} O(u)M(u)u \cdot du \right)^2}{\int_0^{\infty} W(u)u \cdot du}$$

$$IQ = G^2 \frac{M^2(f_0)}{V}$$

Global quality ("the technological level")

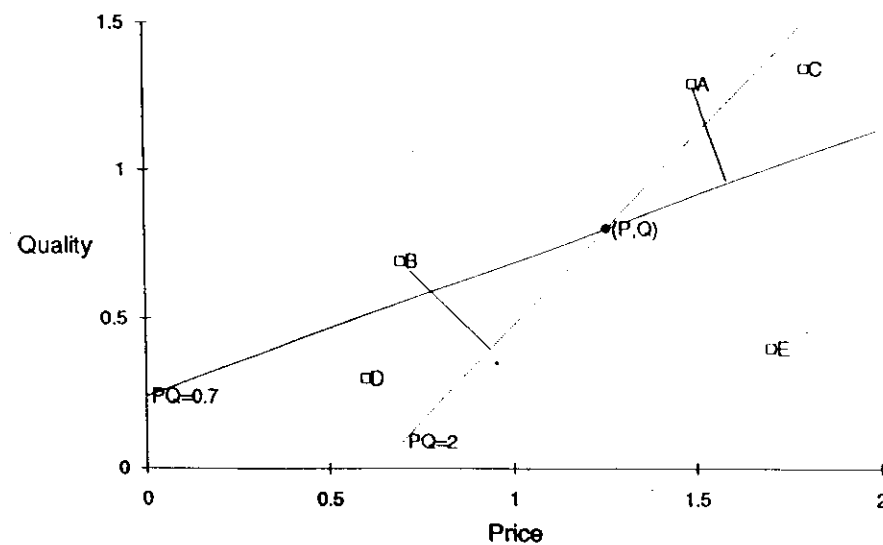
$$Q = IQ \cdot S$$



Bid specification and purchasing criteria

$$QP = \frac{\frac{\Delta Q}{Q}}{\frac{\Delta P}{P}} = \frac{P}{Q} \cdot \frac{\Delta Q}{\Delta P}$$

$$\frac{\Delta Q}{\Delta P} = QP \cdot \frac{Q}{P}$$



CHARACTERISTIC CURVE

SHAPE depends on: intrinsic propriety of the film
developing conditions

does not depends on light emission spectra of the screen

ABSOLUTE POSITION (sensitivity) depends on the radiant energy
absorbed by the film

METHOD FOR OBTAINING THE CURVE

Sensitometer

Direct x-ray exposure

SENSITOMETER

Density	Log relative exposure	Relative exposure
.21	0.0	1.00
.22	0.1	1.26
.23	0.2	1.58
.25	0.3	2.00
.28	0.4	2.51
.31	0.5	3.16
.35	0.6	3.98
.40	0.7	5.01
.45	0.8	6.31
.50	0.9	7.94
.55	1.0	10.0
.60	1.1	12.6
.65	1.2	15.8
.70	1.3	20.0
.75	1.4	25.1
.80	1.5	31.6
.85	1.6	39.8
.90	1.7	50.1
.95	1.8	63.1
1.00	1.9	79.4
1.05	2.0	100.0
1.10	2.1	125.9
1.15	2.2	158.5

ADVANTAGE

easy
quick

DISADVANTAGE

useful only to obtain the shape

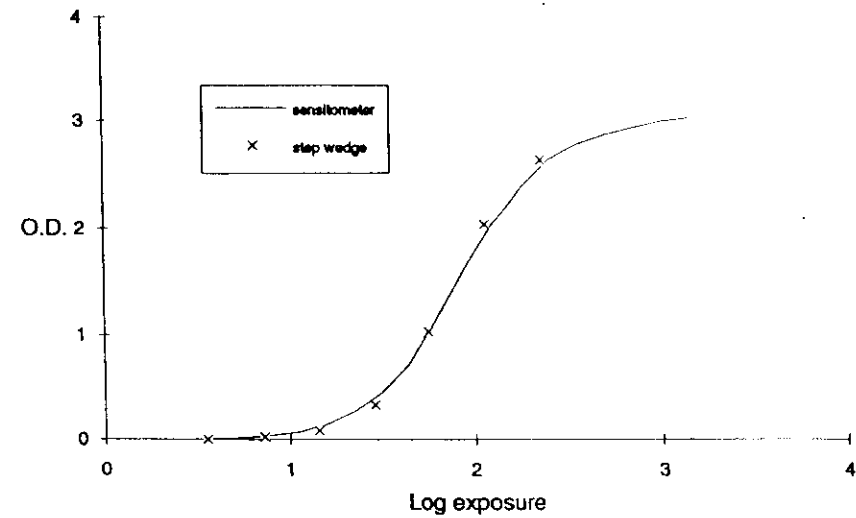
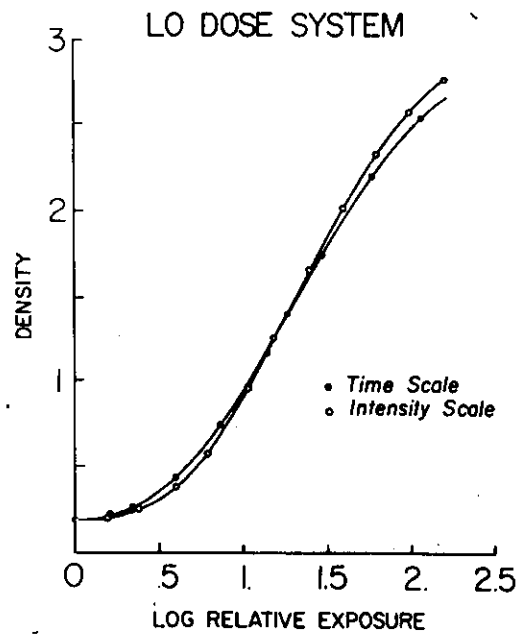
(QUALITY CONTROL OF DEVELOPING PROCESS)

DIRECT X-RAY EXPOSURE

TIMING SCALE

INTENSITY SCALE: - metal step wedge

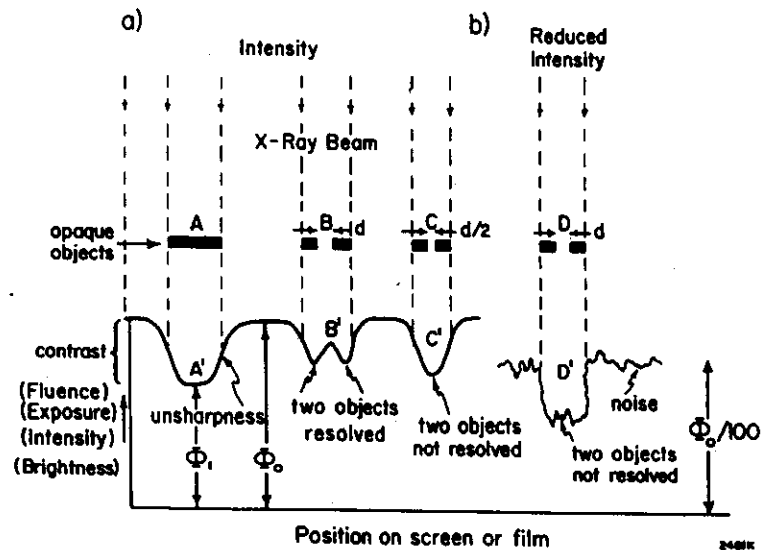
- bootstrap technique
- recording system placed at various distance from the source



SPATIAL RESOLUTION

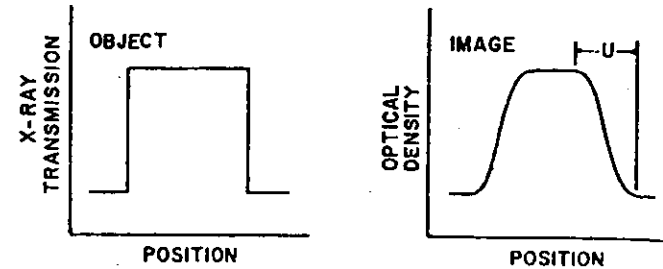
RESOLVING POWER

The ability of a photographic material to maintain in the developed image the separate identity of parallel bars when their relative displacement is small



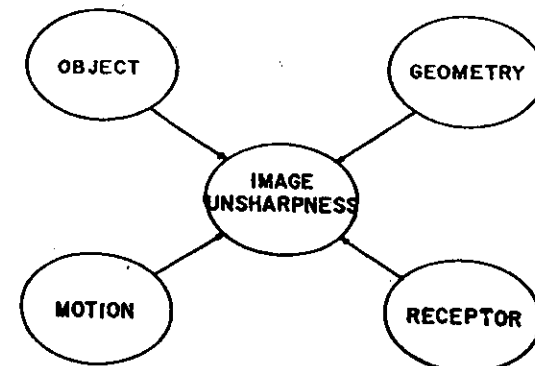
UNSHARPNESS

ONE OBJECT WITH SHARP EDGES PRODUCES AN IMAGE WITH BLURRED EDGE



FACTORS AFFECTING UNSHARPNESS :

- SIZE OF THE FOCAL SPOT
- MOTION OF THE OBJECT DURING EXPOSURE
- GEOMETRIC BLURRING
- BLURRING IN THE SCREEN-FILM COMBINATION

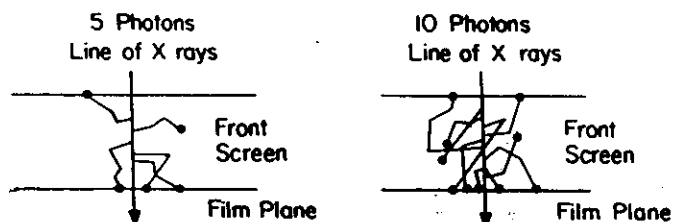


BLURRING IN THE SCREEN-FILM COMBINATION

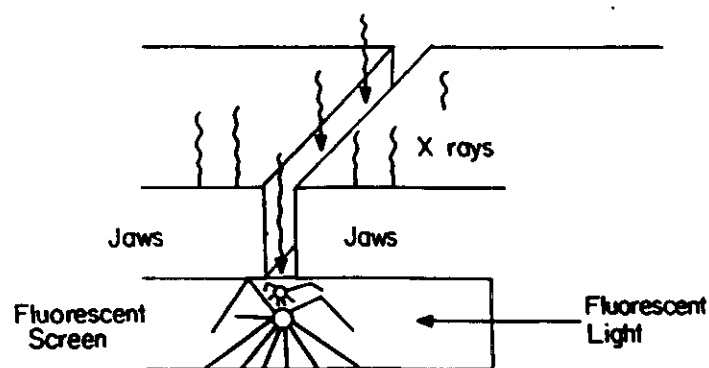
LIGHT SPREAD

When a screen-film combination is exposed to a narrow line of X rays, the resultant fluorescent light diffuses through the screen and "defocusses" the image

LIGHT SPREAD IN A SCREEN
Magnified View

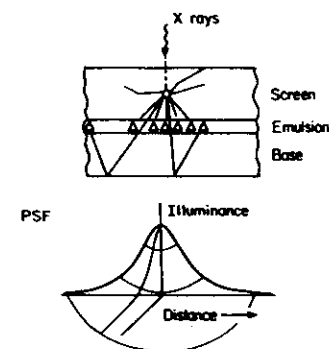


LIGHT SPREAD IN A SCREEN



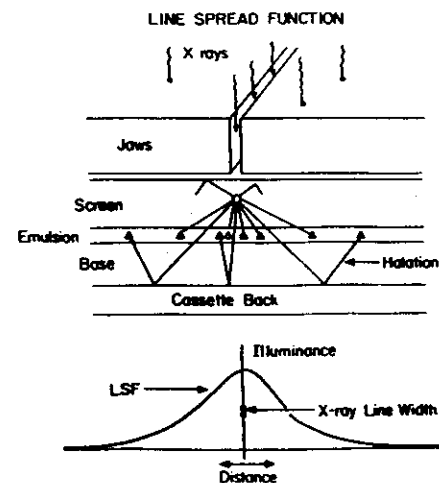
POINT SPREAD FUNCTION (PSF)

Illuminance versus distance function for the light which spreads from a point of X rays absorbed in the screen



LINE SPREAD FUNCTION (LSF)

The spatial distribution of illuminance in the film plane transverse to the X ray line

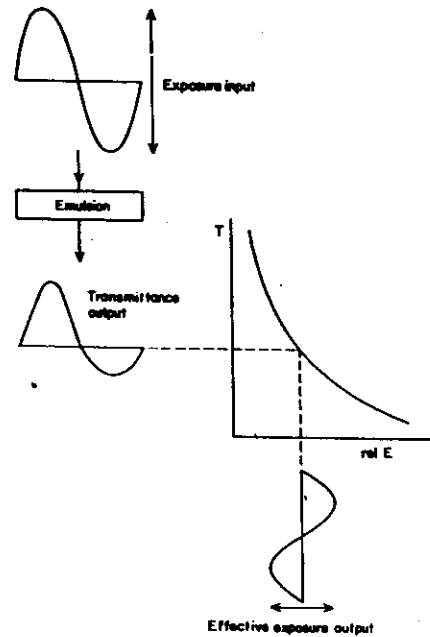


MODULATION TRANSFER FUNCTION (MTF)

MODULATION TRANSFER FACTOR

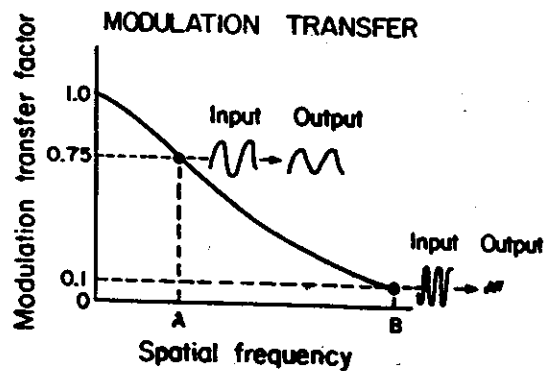
The ratio of the effective exposure modulation to the input exposure modulation

$$MTF = \frac{\text{Modulation of Output Signal } M}{\text{Modulation of Input Signal } M'}$$



In MTF specifies at each spatial frequency the fraction of input modulation which will be imaged

$$MTF(f) = \frac{M(f)}{M(0)}$$



MEASUREMENT OF RESOLVING POWER

SPATIAL DOMAIN

PSF
LSF

FREQUENCY DOMAIN

MTF

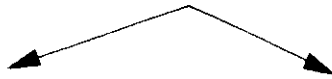
DISADVANTAGES

- Practical difficulties in the measurement
- Function not mathematically additive or multiplicative

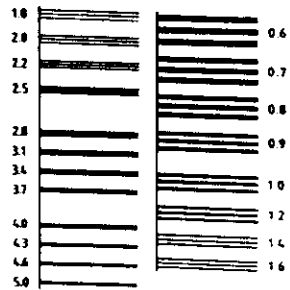
ADVANTAGES

- Provide a complete picture of the resolution.
- Represent the ratio of output amplitude to the input amplitude when a sinusoidal signal of varying frequency is passed through a given transfer system

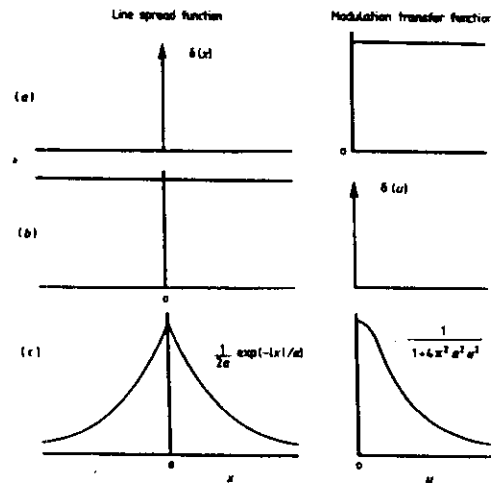
MEASUREMENT OF MTF



DIRECT MEASUREMENT OF PERIODIC PATTERN TEST OBJECT



FOURIER TRANSFORM OF THE MEASURED LSF



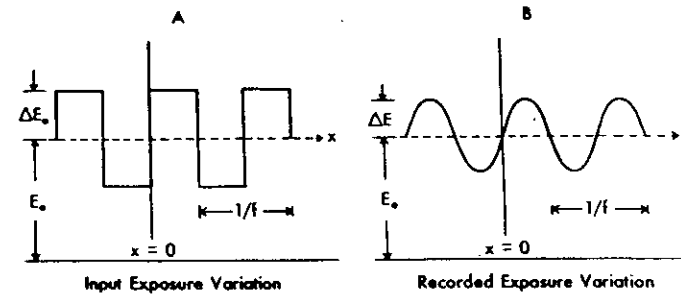
USE OF BAR PATTERN TEST OBJECT

Difficulties to obtain a test object which gives sinusoidal input exposure variation

SQARE-WAVE RESPONSE FUNCTION (SWRF)

Modulation Transfer Factor of a square-wave response

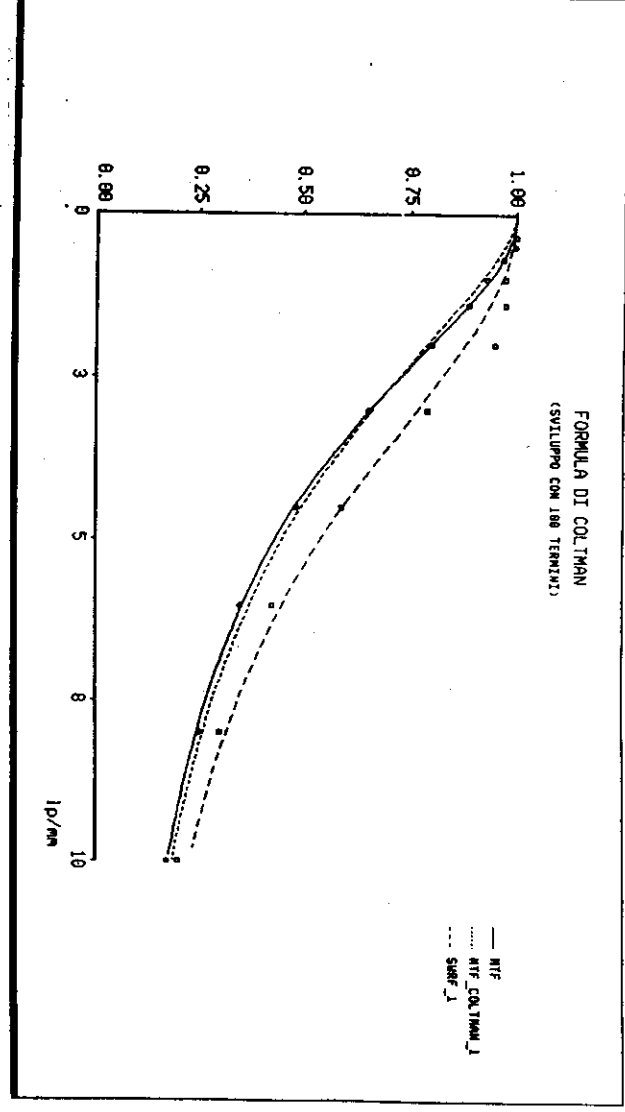
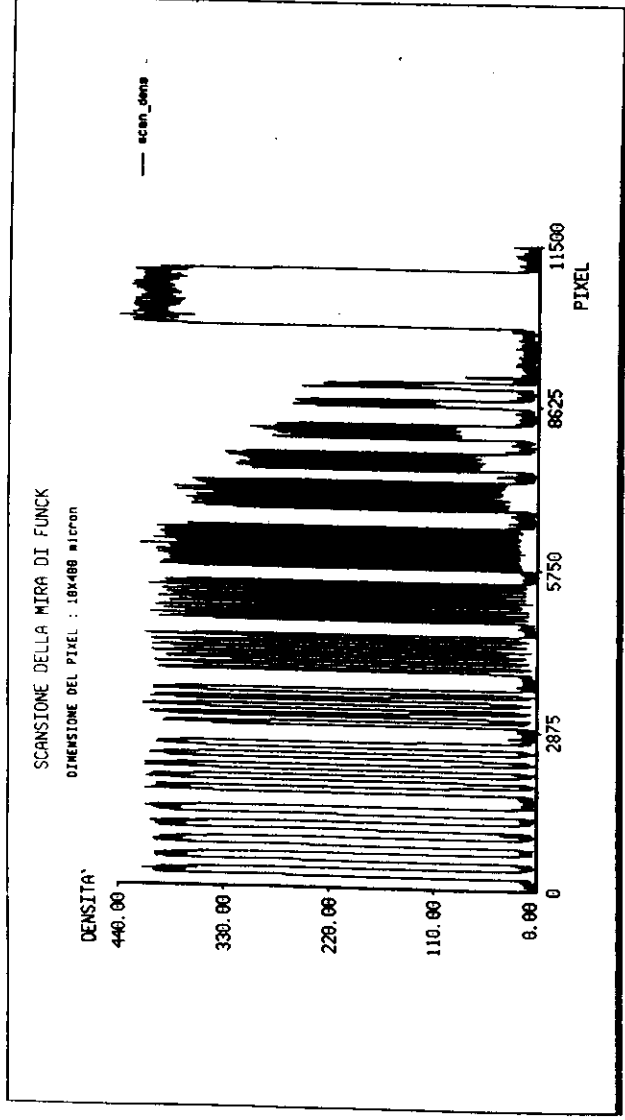
$$S(f) = dE(f) / dE_0$$



COLTMAN EQUATION

Gives the mathematical relationships between the SWRF and MTF

$$MTF(f) = \frac{\pi}{4} \left[S(f) + \frac{S(3 \cdot f)}{3} - \frac{S(5 \cdot f)}{5} + \frac{S(7 \cdot f)}{7} + \frac{S(11 \cdot f)}{11} - \frac{S(13 \cdot f)}{13} - \frac{S(15 \cdot f)}{15} - \frac{S(17 \cdot f)}{17} + \frac{S(19 \cdot f)}{19} \dots \right]$$



NEL LUGLIO
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FOURIER TRANSFORM OF THE LSF

$$MTF(u) = \int_{-\infty}^{\infty} LSF(x) \cos 2\pi ux \, dx / \int_{-\infty}^{\infty} LSF(x) \, dx$$

COMPUTATIONAL METHODS

THE SAMPLING THEOREM

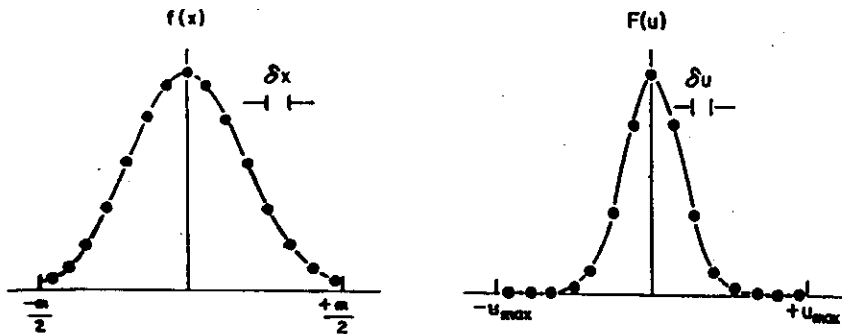
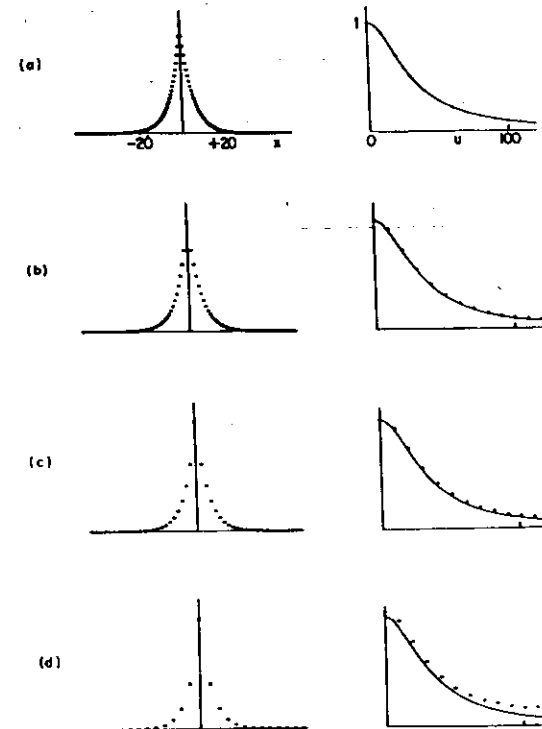


Illustration of the sampling theorem. If $f(x)$ is defined within the range m , then $F(u)$ is fully described by points $\delta u = \frac{1}{m}$ apart. Conversely, if the range of interest of $F(u)$ is $2u_{max}$, then $f(x)$ may be sampled at intervals not greater than $\delta x = \frac{1}{2u_{max}}$.

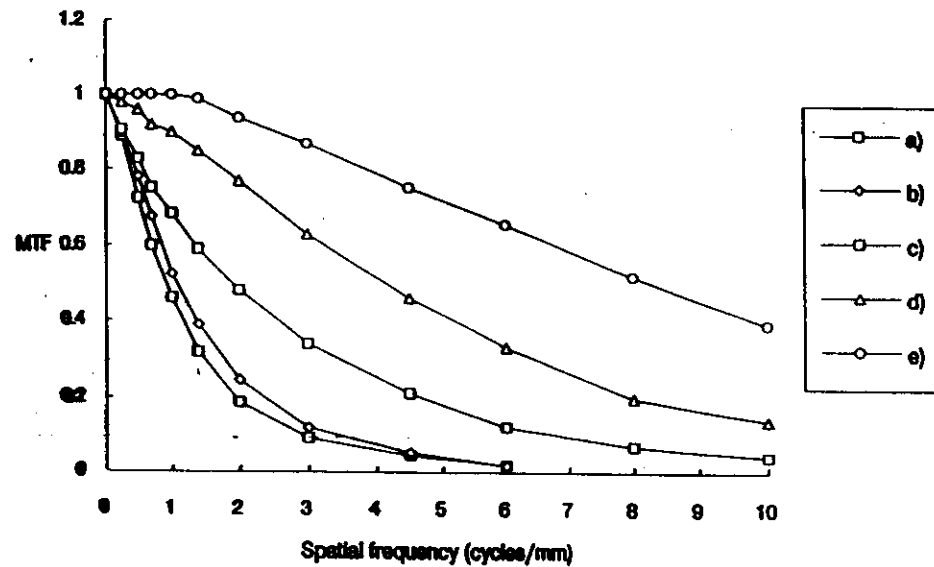
THE EFFECT OF SAMPLING ON COMPUTED MTF



Practical suggestion :

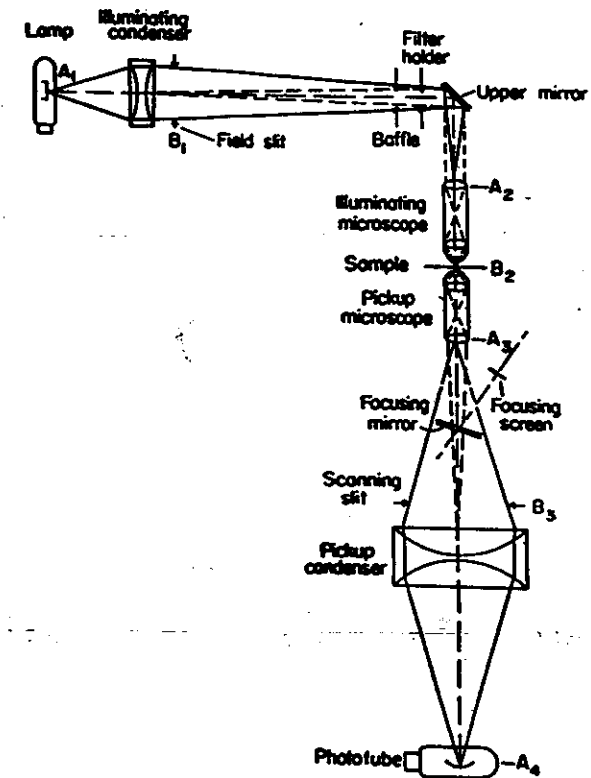
MTF Error < 0.5% \longrightarrow Sampling interval < 25% of the FWHM of the LSF

QUANTITATIVE VALUES (lp/mm)

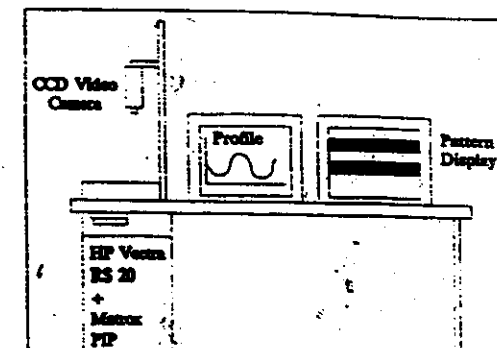


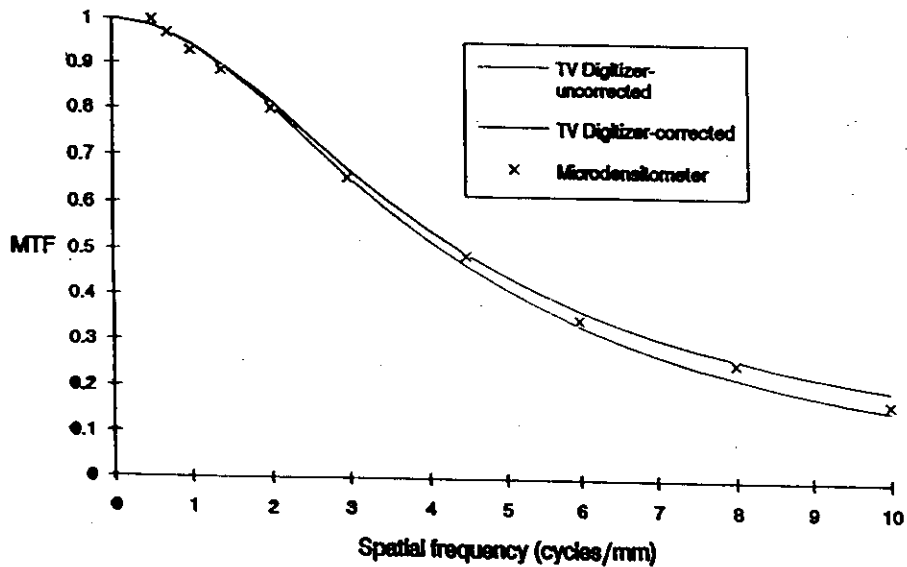
INSTRUMENTATION

MICRODENSITOMETER



TV-CAMERA DIGITIZER





NOISE

The noisy appearance (**RADIOGRAPHIC MOTTLE**) of a uniformly exposed X-Ray film is due to the spatial variation of the film density

A number of studies have demonstrated that the density D_A as measured with an aperture of area A should follow a Gaussian distribution

MEASURE OF RADIOGRAPHIC NOISE

**AUTOCORRELATION
FUNCTION**

WIENER SPECTRUM

AUTOCORRELATION FUNCTION

FIRST ORDER STATISTICS

$$\bar{D} = \frac{1}{A} \iint D(x,y) dx dy \quad \sigma^2 = \frac{1}{A} \iint [D(x,y) - \bar{D}]^2 dx dy$$

While \bar{D} and σ fully describe the statistical character of the noise, they do not tell us whether there is any correlation between density measured at different points

HIGHER ORDER STATISTICS

AUTOCORRELATION FUNCTION

$$C(\zeta, \eta) = \frac{1}{A} \iint \Delta D(x,y) \Delta D(x + \zeta, y + \eta) dx dy$$

It follows that

$$C(0,0) = \sigma^2$$

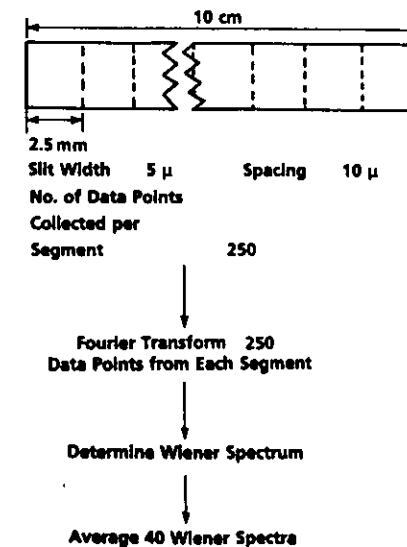
the scale value of the autocorrelation function is simply equal to the variance

WIENER SPECTRUM

$$\phi(f_x, f_y) = \frac{1}{A} \left[\iint \Delta D(x,y) e^{-2\pi i(xf_x + yf_y)} dx dy \right]^2 \quad (6)$$

the Wiener spectrum is the Fourier transform squared of the density fluctuations. While determining $\phi(f_x, f_y)$, an ensemble average should be taken in addition to the space average indicated in Equation

MEASUREMENT



WIENER SPECTRUM

$$\phi(f_x, f_y) = \frac{1}{A} \left[\iint_A \Delta D(x, y) e^{-2\pi i(xf_x + yf_y)} dx dy \right]^2 \quad (6)$$

the Wiener spectrum is the Fourier transform squared of the density fluctuations. While determining $\phi(f_x, f_y)$, an ensemble average should be taken in addition to the space average indicated in Equation

MEASUREMENT

