



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
I.C.T.P., P.O. BOX 586, 34100 TRIESTE, ITALY, CABLE: CENTRATOM TRIESTE



UNITED NATIONS INDUSTRIAL DEVELOPMENT ORGANIZATION



INTERNATIONAL CENTRE FOR SCIENCE AND HIGH TECHNOLOGY

c/o INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS 34100 TRIESTE (ITALY) VIA ORIZZANO, 9 (ADRIATICO PALACE) P.O. BOX 586 TELEPHONE 040-234772 TELEFAX 040-234775 TELEX 000400 APH I

H4.SMR/676-32

**SECOND SCHOOL ON THE USE OF SYNCHROTRON
RADIATION IN SCIENCE AND TECHNOLOGY:
"JOHN FUGGLE MEMORIAL"**

25 October - 19 November 1993

Miramare - Trieste, Italy

ATOMIC AND MOLECULAR SPECTROSCOPY

**Giovanni Stefani
Terza Università di Roma
Rome, Italy.**

Atomic and Molecular Spectroscopy

2nd School on the use of Synchrotron Radiation in Science and Technology: "John Fuggle Memorial"

Giovanni Stefani, Dipartimento di Fisica, Terza Università di Roma

In Atomic and Molecular Physics the relevant potentials are:

Nuclear Potential V_n
electron-electron Potential V_{ee}

Problems will rise in including V_{ee} in the model. Not even the simple 3 charged particle problem is exactly solvable.

Many-body properties of atoms and molecules is one of the main challenges

e-e interactions can be classified as:

Bound State	(short & long range)
Continuous State	(short & long range)

Photoionisation is one of the most used tools (single and double)
Near Threshold , Resonant, Direct

In each of these regimes e-e interactions have different relevance

To focalize attention on a specific form of interaction we need to:

- tune continuously the photon energy
- measure small cross sections
- measure angular distributions
- achieve high energy resolution

This implies Tunability, High Flux, Brightness

Will concentrate on :

e-e-interactions

electron spectroscopy

coincidence spectroscopy

Since the pioneering work of Madden and Codling (Phys. Rev. Lett. 10 (1963) 516) on He photoabsorption, e-e interactions have been of prime relevance. Resonances in the continuum in the 200 Å region. Recently, with a resolving power of 10000 major advances have been done in the field. Domke et al. (Phys. Rev. Lett. 66 (1991) 1306) have observed more than 50 states 0.1 meV narrow in the same region.

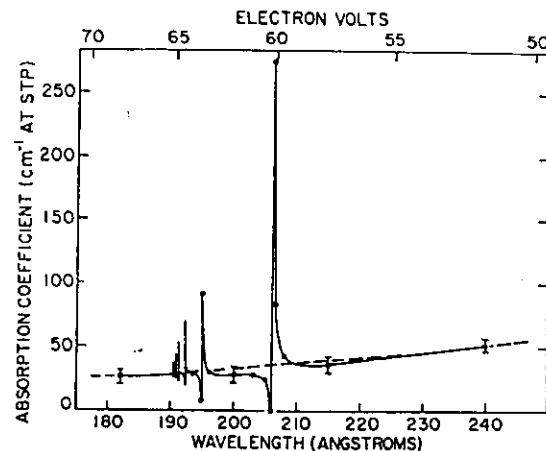


Fig. 1 Autoionization of two-electron excited states in helium converging on the double ionization potential. The data were obtained in an absorption experiment by Madden and Codling.

Photoionization cross-section

$$\hbar\omega + \Psi_i(N) \rightarrow \epsilon + \Psi_f(N-1)$$

Energy conservation

$$\hbar\omega + E_i(N) = \epsilon + E_f(N-1)$$

In single particle scheme

$$\hbar\omega + E_i(N) = \epsilon + E_f(N-1, \bar{\epsilon})$$

single photoionization

$$\sigma(\omega) = \frac{4\pi^2 e^2 \omega}{c} \sum_f |\langle \Psi_f | \hat{e} \cdot \sum_i \underline{z}_i | \Psi_i \rangle|^2 \delta(E_f(\omega) - E_i(\omega) - \hbar\omega)$$

$$T_{if} = \langle \Psi_f | \hat{e} \cdot \sum_i \underline{z}_i | \Psi_i \rangle$$

angular distribution

$$p = \text{polarization} \quad \frac{d\sigma}{d\Omega} = \frac{\sigma}{4\pi} (1 + \beta(1 + 3p \cos 2\theta))$$

Hartree-Fock

$$\Psi_i(N) = A(N) (\psi_1(z) \psi_2(z) \dots \psi_N(z)) \quad ; \quad \phi_i(z) = R_{ne}(z) Y_{lm}(\theta, \phi)$$

$$T_{if} = \langle \Psi_f | \hat{e} \cdot \underline{z} | \Psi_i \rangle S^{ij} + \sum_{j=2}^{j+1} (-1) \langle \Psi_f | \hat{e} \cdot \underline{z} | \Psi_i \rangle S^{ij} + \sum_{j=1}^N (-1)^{j+1} \langle \Psi_f | \psi_j \rangle p^{j+1}$$

ignoring relaxation

$$S^{ij} = \delta_{ij} \quad ; \quad p^{jk} = 0 \quad ; \quad T_{if} = \langle \Psi_f | \hat{e} \cdot \underline{z} | \Psi_i \rangle$$

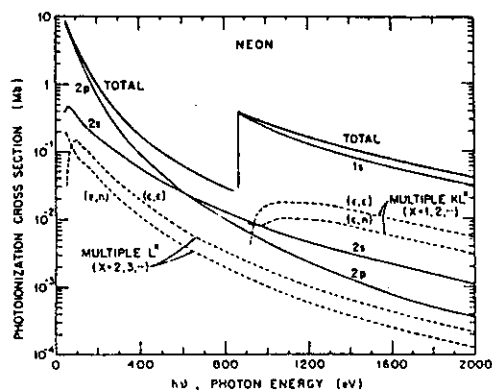
Many-electron Configuration Interaction

$$|\Psi_i(N)\rangle = \sum_m D_{im} |\Phi_m(N)\rangle$$

$\Phi_m(N)$ = Slater det. of given configuration

$$|\Psi_f(N)\rangle = \sum_n D'_{fn} |\Phi'_n(N)\rangle$$

Total photoabsorption cross-section



Typical experimental set up

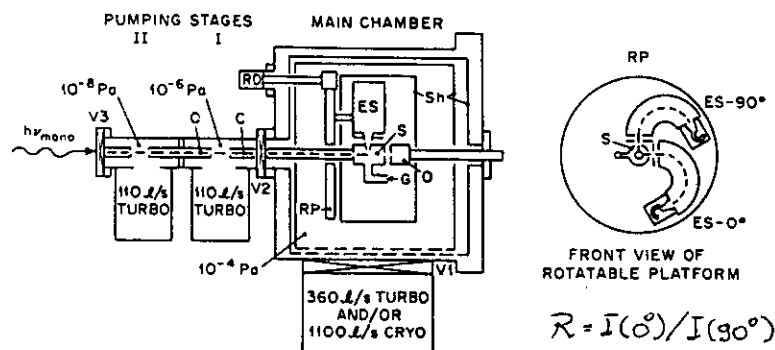


FIG. 1. Sketch of ESSR system, showing two analyzers (ES) mounted on a rotatable platform (RP) with drive (RD) around the electron source (S), which allows the use of a gas (G) or an atomic beam from an oven (O); three magnetic shields (Sh) are used and three valves (V1 to V3) separate components; typical pressures are indicated at an estimated pressure of 10^{-2} Pa in source (S) and the high impedances provided by the capillaries (C).

$$\beta = \frac{4(R-1)}{3p(R+1)-(R-1)}$$

KRAUSE & CARLSON
Phys. Rev. A 24 (1981) 1374

THREE REGIMES

Threshold Direct Resonances

ABSORPTION

Main line Satellites Continuum

ABSOLUTE VALUES & PARTIAL CHANNELS

On Main line

$(nlj) e^-$ ejected $\leftrightarrow$ Independent particle + (correlations)

- o Wrong binding energy : strong relaxation and/or polarization
- o Wrong intensity : continuous or discrete satellites
- o e-e interactions included by 2nd order diagrams and/or relaxed orbitals.

Strong correlation effects in 5s Xe

— ns² —

Coupling between electrons is evident in the asymmetry parameter β vs. energy

- Within LSJ coupling : ns $\rightarrow$ ϵ_p partial wave
 $\hookrightarrow$ hence $\beta = 2$
- Within jjj coupling : Spin orbit coupling in continuum leads to $\epsilon_{p_{3/2}} \neq \epsilon_{p_{1/2}}$ part. waves
 and

$$\beta = \frac{2R_{\epsilon_{p_{3/2}}}^2 + 4R_{\epsilon_{p_{3/2}}}R_{\epsilon_{p_{1/2}}}\cos\Delta}{R_{\epsilon_{p_{1/2}}}^2 + 2R_{\epsilon_{p_{3/2}}}^2}$$

R_i = radial dipole integrals

Δ = relative phase

at high energy $R_{\epsilon_{p_{3/2}}} \approx R_{\epsilon_{p_{1/2}}}$ $\Delta \approx 0 \rightarrow \beta = 2$

near threshold $R_{\epsilon_{p_{3/2}}} \neq R_{\epsilon_{p_{1/2}}}$

Strong correlation effects in 5s Xe

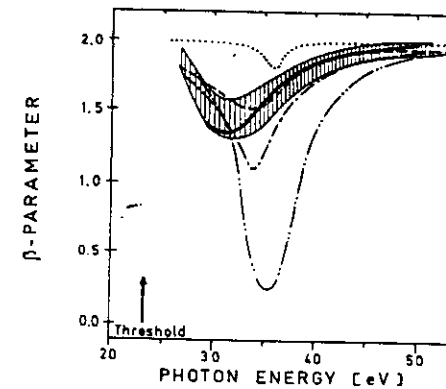


Figure 3.7. Angular distribution parameter β for 5s photoionization in xenon. Hatched region denotes mean experimental data, including error limits (from [WSK79, DSc83, FCK83a, WMS86]). The value at 40.8 eV from the first study of this problem [DDi76] has been omitted because it could not be confirmed by later experiments; for data above 55 eV see [WSK79, FCK83a, SBT83]. Theoretical values: double-dotted chain curve, RRP (4d+5s+5p) calculation [JCh78, JCh79]; dotted curve, K-matrix (5s+5p) (velocity form results [HSi80]); broken and chain curve, RTDLDA with Gunnarsson-Lundqvist and Perdew-Zunger exchange correlation potentials, respectively [PJR84]; full curve, multi-configurational DF (5s+5p) calculation with full account of relaxation [Tul89].

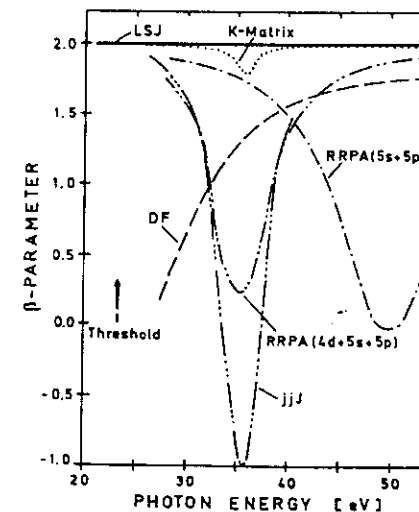
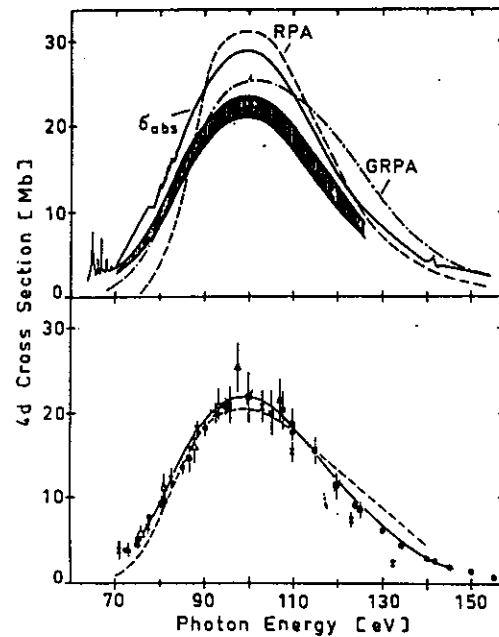


Figure 3.8. Angular distribution parameter β for 5s photoionization in xenon. Compilation of theoretical values: LSJ, Russell-Saunders coupling; jjj coupling [Che78a]; DF calculation ([WWa74, OMa78, OMa79], Coulomb gauge results which correspond in the non-relativistic limit to the velocity form results); K-matrix ([HSi80], velocity form results); RRP (5s+5p) and RRP (4d+5s+5p) calculation [JCh78, JCh79].

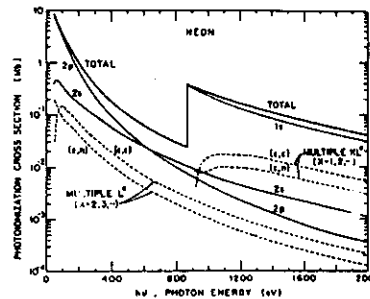
From
 V. Schmidt
 Rep. Prog. Phys.
 55 (1992) 1486

Redistribution of 4d strength in Xe



delayed "onset"

e-e interactions responsible
for O.S. redistribution

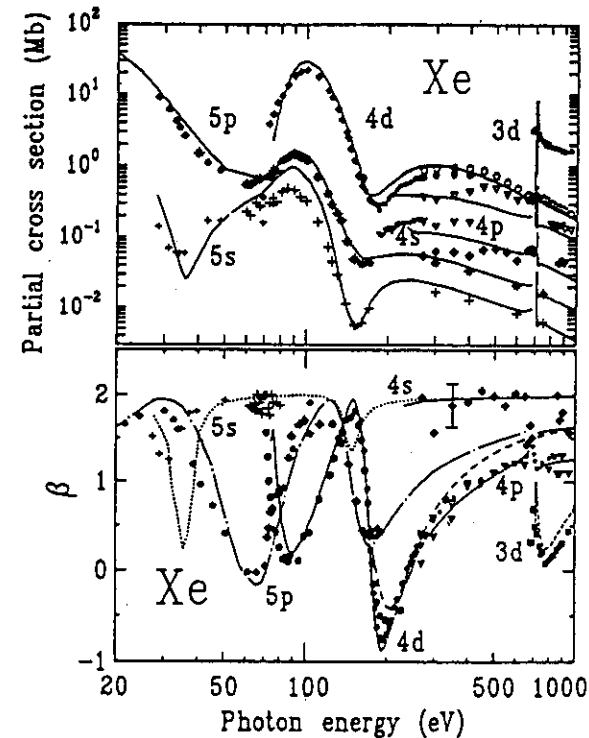


Oscillator Strength $\rightarrow$ Spectral distribution
 $f(\text{excitations}) \propto df/dE (\text{ionisation})$

* ϵf - trapping *

- o Interchannel coupling
- o Interchannel coupling
- o Relaxation processes

Redistribution of 4d strength in Xe



Interchannel coupling
5p-5s

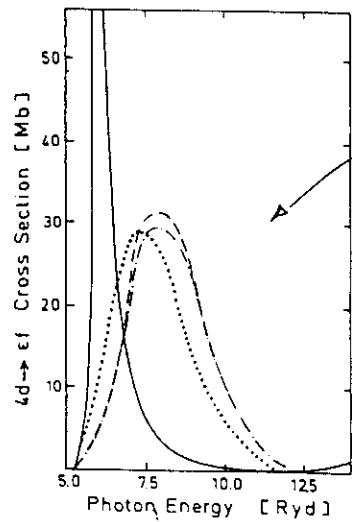
Figure 1: σ and β for the subshell photoionization of Xe up to 1 keV. The different exp. data sets are from:

σ : 5p * [8], * [9]; 5s + [8], + [9]; 4d •, o [9], • [10]; 4p ▼, ▽ [9], ▼ [10]; 4s ♦ [9]; 3d ■ [11];
 β : 5p * [12], * [13]; 5s + [14], + [13]; 4d • [13], • [10], .. [11]; 4p ▼, ▽ [9]; 4s ♦ [9]; 3d ■ [11].

The different theoretical curves represent extended RRPA calculations

FROM: U. BECKER, AIP Conference Proceedings 205 (90) 16

Shape resonance and wavefunction collapse in 4d Xe



Giant Resonance

Intrachannel interaction

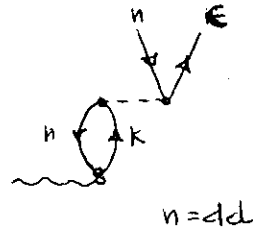
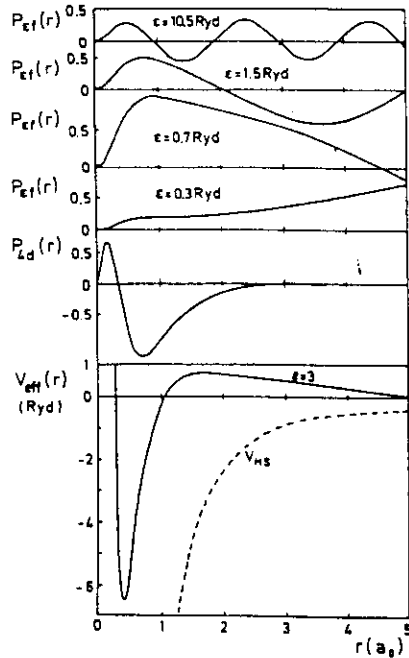


Figure 4.7. 4d $\rightarrow$ ϵf partial photoionization cross-section for xenon;



$$V_{\text{eff}} = V_{\text{Coul}} + \text{Centrif. Barrier}$$

Shape resonance and wavefunction collapse in 4d Xe

Giant resonance $\equiv$ single particle with strong polarisation

$n f$ orbitals located outside the atomic region
orbitals by-passed in Aufbau

4d $\rightarrow$ $n f$ excitation absent
4d $\rightarrow$ $n p$ present



Ionisation makes barrier to collapse

Shape resonance present

Shape resonance and wavefunction collapse in 4d Xe

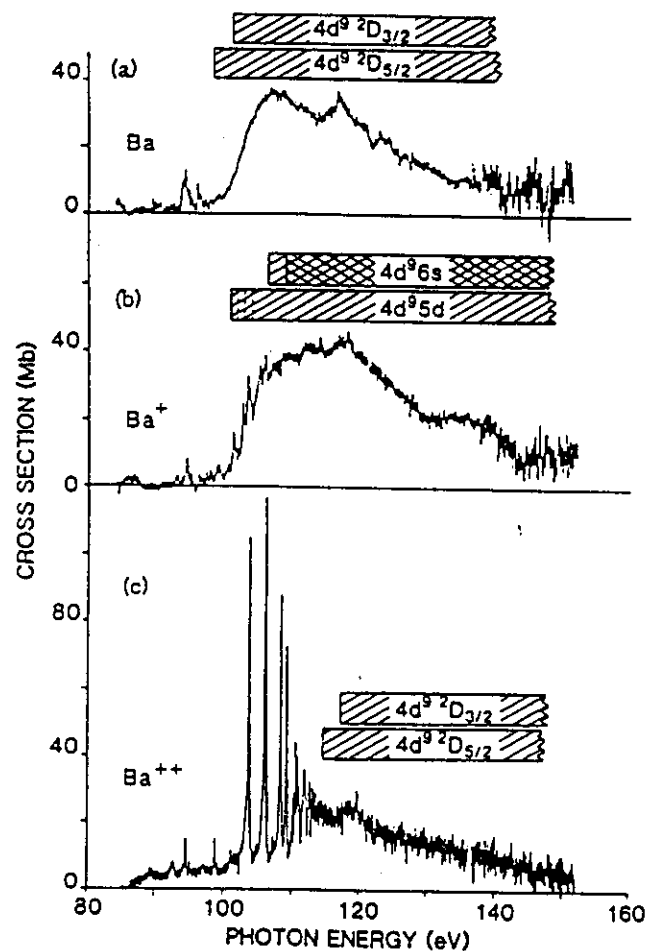
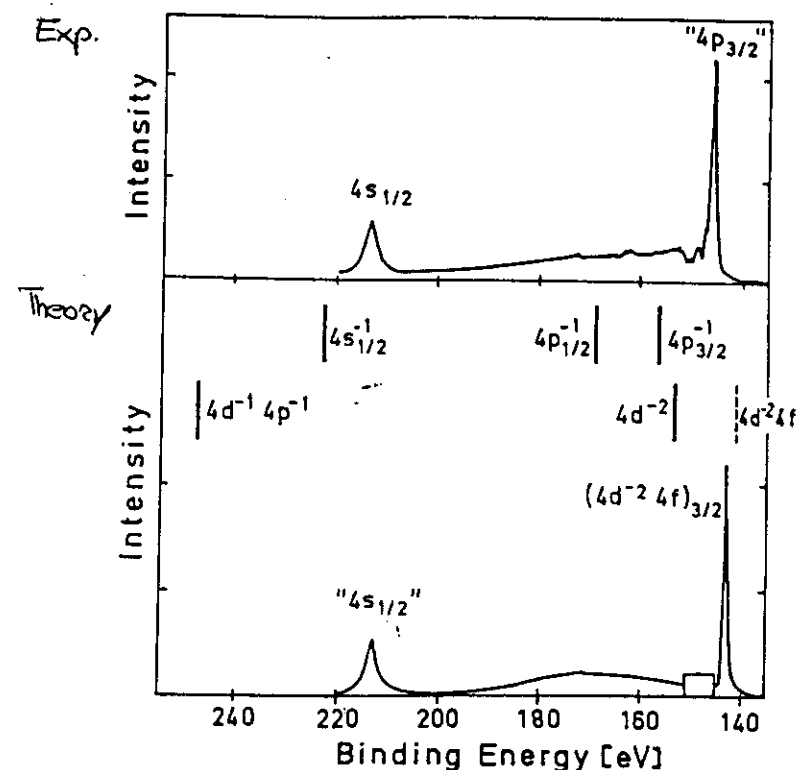
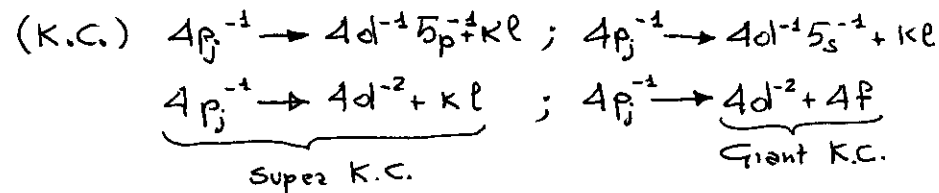


Figure 4.8. Photoabsorption cross-section of (a) Ba, (b) Ba⁺ and (c) Ba²⁺. Peak cross-sections of strong absorption features in Ba²⁺ are underestimated because of saturation and effects of limited resolution. The continua for the respective electron configurations are also included in the figure. From [LMS81].

FROM: LUCATORTO et al. Phys. Rev. Lett. 47 (21)1124

The missing Xe 4p_{1/2} photoline

4s and 4p photoionization in xenon: upper part, experimental spectrum (average curve through the experimental points; from [Gel74, SMB76]); the lines in the middle part indicate theoretically predicted energy positions for the listed electron configurations; lower part, theoretically predicted spectrum from [WOh76].



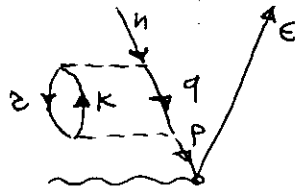
Exp. = Jolus J. Elect. Spect. 5 (1974) 985

Theory = Wendin & Orino Phys. Scripta 1A (1976) 78

The missing Xe 4p_{1/2} photoline

4p⁻¹ & 4d⁻²4f nearly degenerate in energy

Perturb. diagram intensity $\propto \frac{\text{Coulomb Intee.}}{\Delta E}$ ↗ large
↘ small



$$\begin{aligned} n=p=4p & \quad q=4d \\ n=p=4s & \quad q=4p \end{aligned}$$

similar for 4s⁻¹ → 4p⁻¹4d⁻¹4f

4p

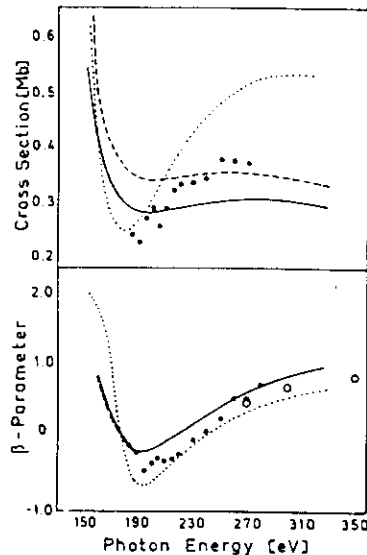


Figure 3.13. Partial cross-section (upper part) and angular distribution parameter β (lower part) for 4p photoionization in xenon. Note that the theoretical data refer to the whole 4p spectral distribution, but the experimental values to the (4d⁻²4f)²P_{3/2} photoline only. Experimental data: solid circles, from [LFH88] (the relative cross-section values have been multiplied by a constant factor in order to place them into the vicinity of the calculated values); open circles, from [BSK89b] (there are additional data for higher energies). Theoretical data [SDe89]: full and broken curves, RPA results including (4p+4d) shell couplings, length and velocity form results, respectively; dotted curves, theoretical values for 4d photoionization, which are in very good agreement with experimental data [LFH88].

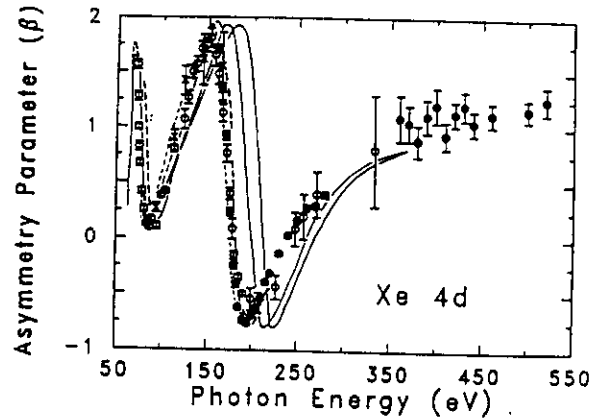
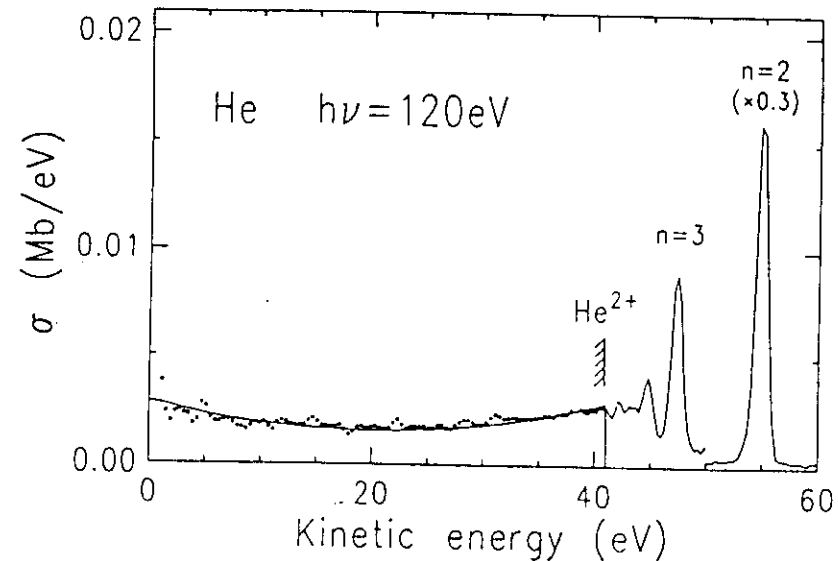


FIG. 3. Asymmetry parameter of the Xe 4d subshell as in the bottom panel of Fig. 2, now including experimental results from Ref. 4 (×), plotted over a wider photon-energy range.

Lindle et al.
 Phys Rev A 37(88)3808

He an example of two electron processes



Photoelectron spectrum of helium satellites at 120 eV photon energy. The 1s main photoline is outside the shown energy range. Discrete satellites are characterized by the principal quantum number n . The double ionization threshold at 79 eV binding energy is marked as He²⁺ and the double ionization continuum for electron emission covers the range from 0 to $E_{exc} = 41$ eV kinetic energy.

Independent particle

$$\sigma^+(1s) = \frac{4\pi^2}{3} \alpha \omega e^2 |\langle 1s | 1s \rangle|^2 R_{ep,1s}^2$$

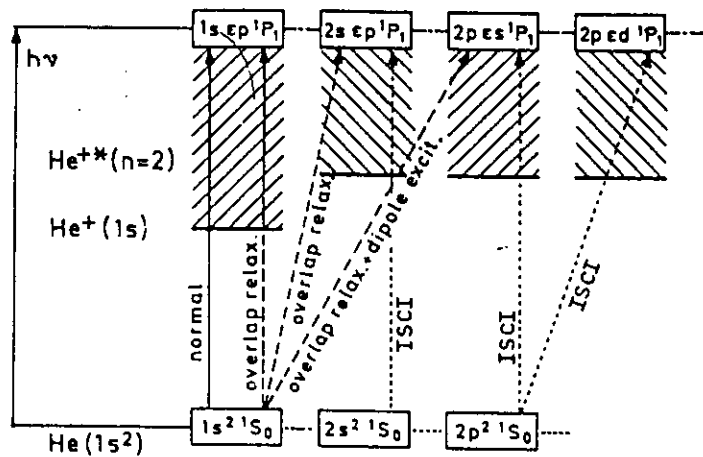
Ionisation with excitation

$$\sigma^{+*}(2s) = \frac{4\pi^2}{3} \alpha \omega e^2 |\langle 2s | 1s \rangle|^2 R_{ep,1s}^2$$

$$\sigma^{+*}(2p) = \frac{4\pi^2}{3} \alpha \omega e^2 |\langle 2p | 1s \rangle|^2 R_{ep,1s}^2$$

FROM: WEHLITZ et al. Phys. Rev. Lett. 67(81) 3764

He an example of two electron processes



Schematic representation of important electron correlations for discrete satellites in helium belonging to ionization and simultaneous excitation to $n=2$ (see

FROM: MANSON J. Electron Spec. 9 (76) 21

He⁺(2s) shake-up; He⁺(2p) conjugate shake-up; He⁺(ε, ε') shake off

⊗ Double ionisation, difficult from single meas.

⊗ Satellite at threshold, interesting

Inner shell satellites, Ne

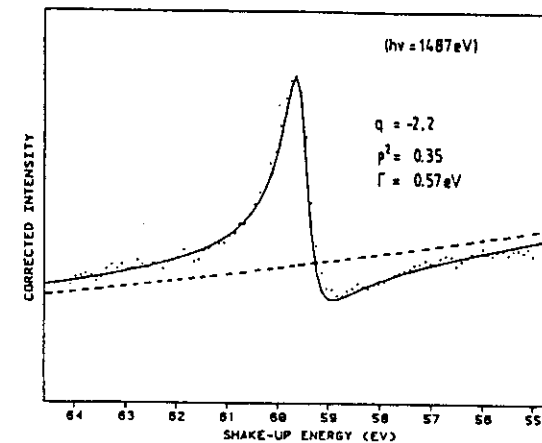


Figure 3.19. The 1s2s2p⁵ lower shake-up satellite of neon observed with 1487 eV photons. If the shake-up energy is added to the 1s ionization energy (870 eV), one obtains the binding energy of this satellite. A small inelastic-scattering and spectrometer background has been subtracted. The dotted curve indicates the unperturbed continuum intensity, the full curve represents a fit of a Fano line profile to the experimental points with the parameters given in the figure. F

$$1s^{-1} + 1s2s^22p^5 \text{ } ^1P \text{ or } 1s2s2p^6 \text{ } ^1P'$$

$$S_{ki} = \langle \psi_k, (N-1) | \psi_i, (N-1) \rangle$$

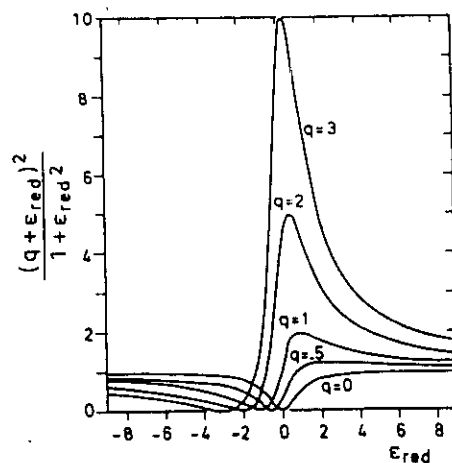
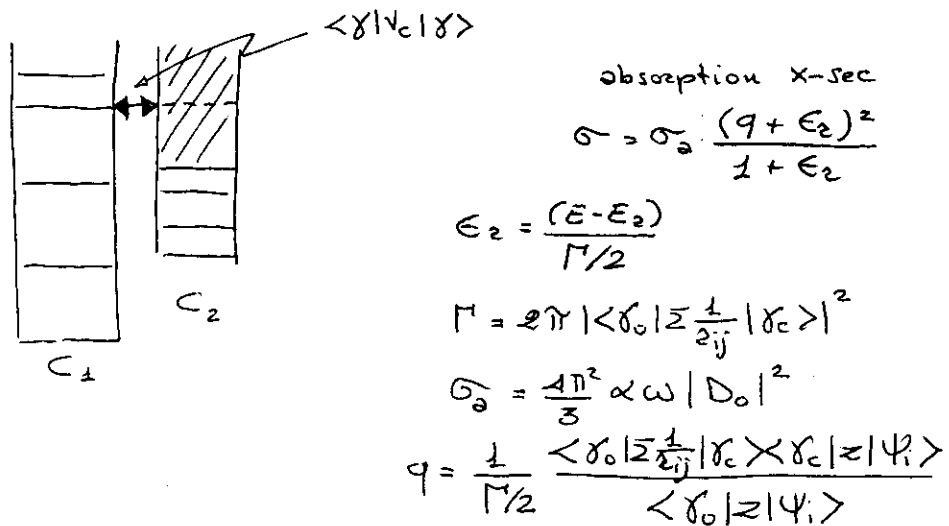
$$\frac{I_k(\epsilon')}{I_0(\epsilon)} = \frac{|\langle \epsilon' | z | i \rangle|^2 S_{ki}^2}{|\langle \epsilon | z | i \rangle|^2 S_{0i}^2}$$

Indistinguishable states reached by two paths

$$\begin{aligned} 1\text{step} &\rightarrow 1s2s^22p^5 (1p/3p) \epsilon_p' (2s^e) \epsilon_p \text{ } ^1P_1 \\ 2\text{step} &\rightarrow 1s2s2p^6 3s \text{ } ^3P^e \epsilon_p \rightarrow 1s2s^22p^5 (1p/2p) \epsilon_p' \epsilon_p \text{ } ^1P_1 \end{aligned}$$

FROM: SVENSSON et al. Phys. Rev. Lett. 58 (87) 2639

Parametrization of resonances



Line profiles of a Fano resonance for different values of the q-parameter. From

From : FANO Rep. Prog. Phys. 46(83) 94

Two electron excited states He

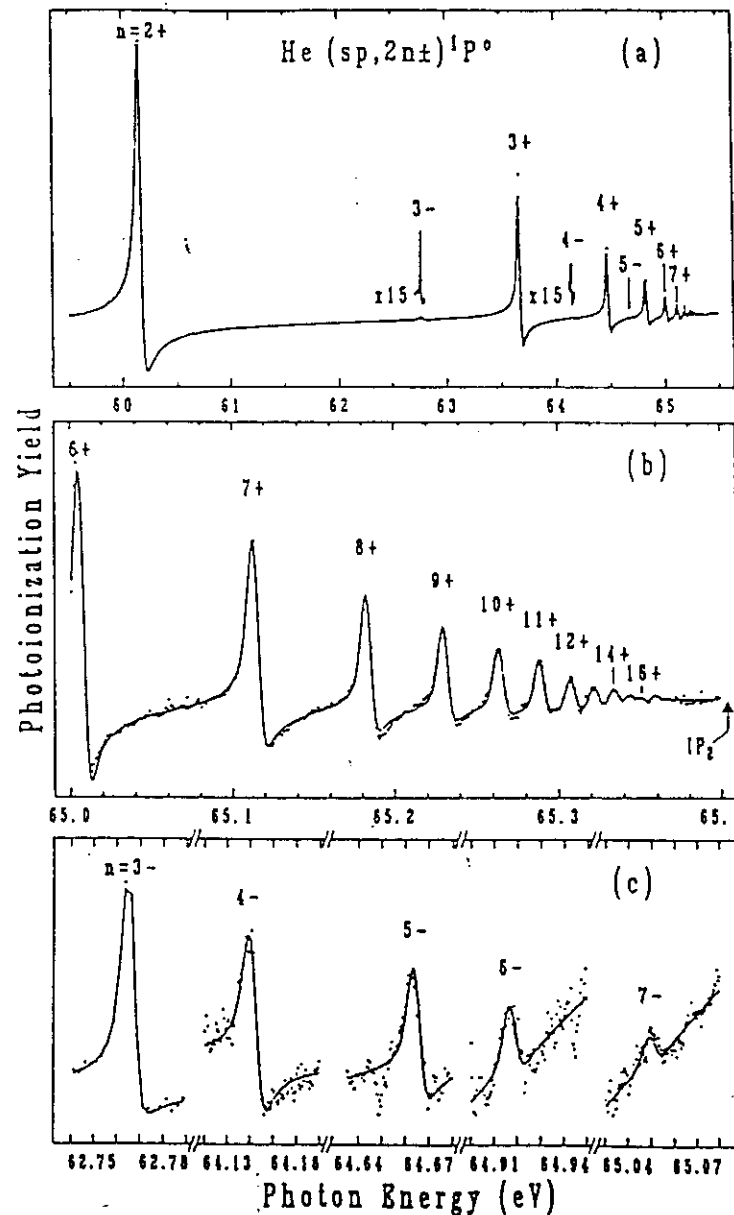
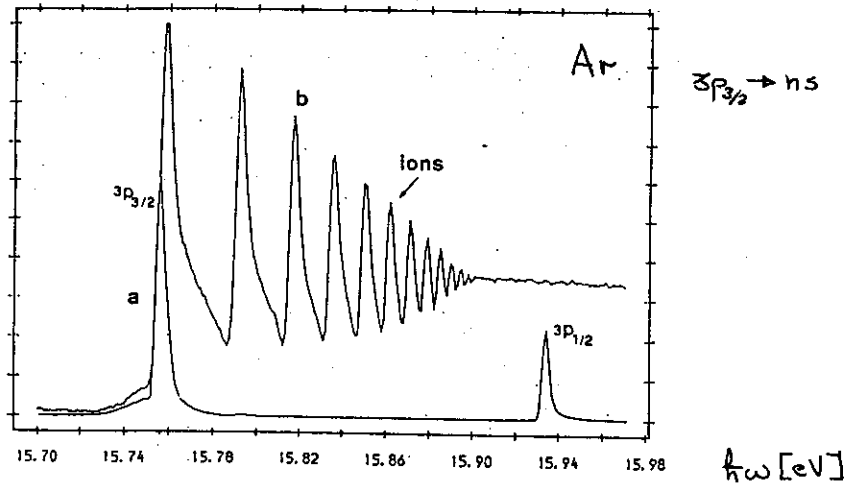
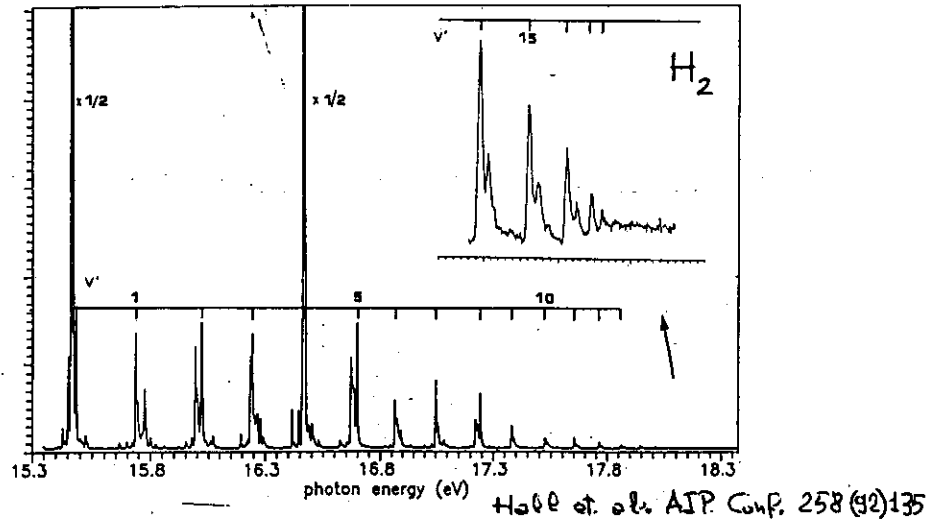


Figure 4.9. Doubly excited states of helium below the threshold for $\text{He}^{++}(n=2)$: overview; (b) magnification of the $n > 6$ region; (c) $sp2n-$ states. From

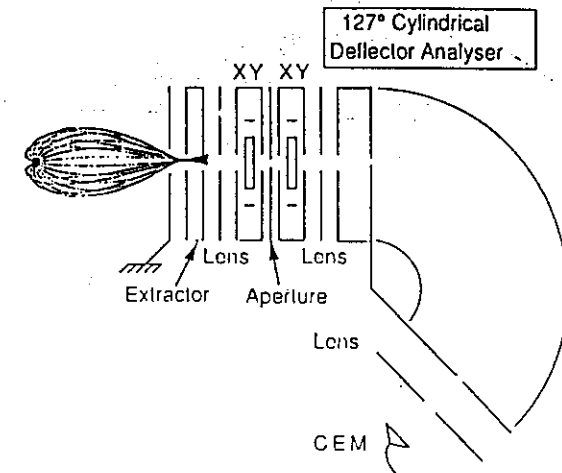
Threshold spectroscopy
ion detection and high energy resolution



Ar threshold photoemission spectrum (a)
and ion Ar^+ spectrum (b) From: Hall et al. Mass. Sci. Technol.
3 (92) 316

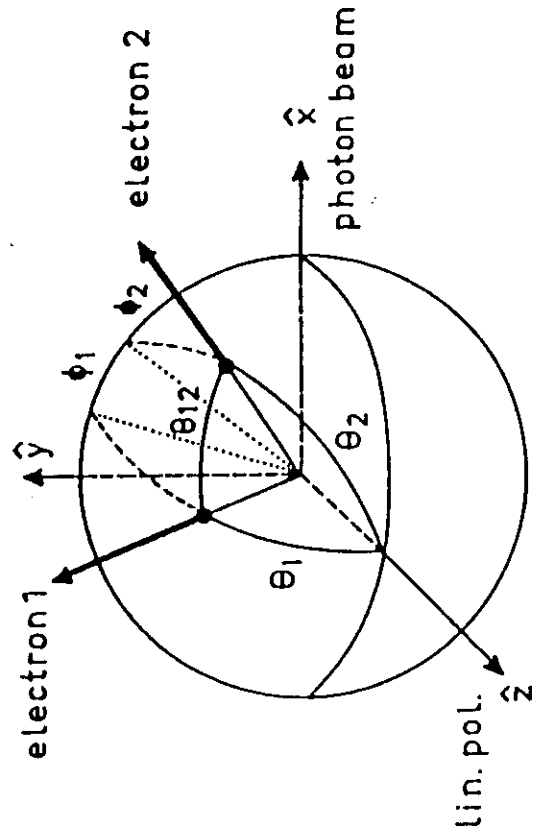


Hall et al. AIP Conf. 258 (92) 135

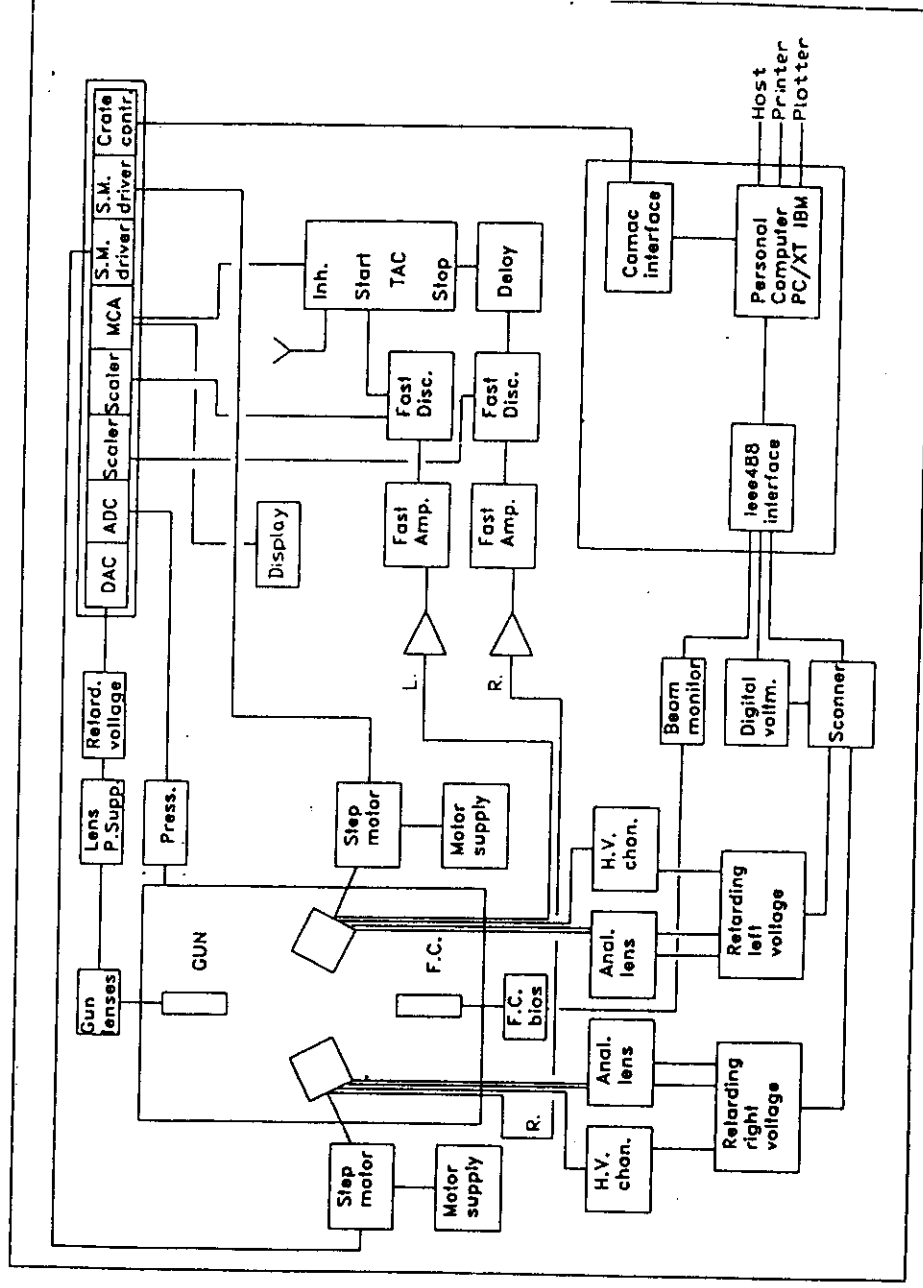


Direct double photoionization DPI

Schematic of DPI experiment

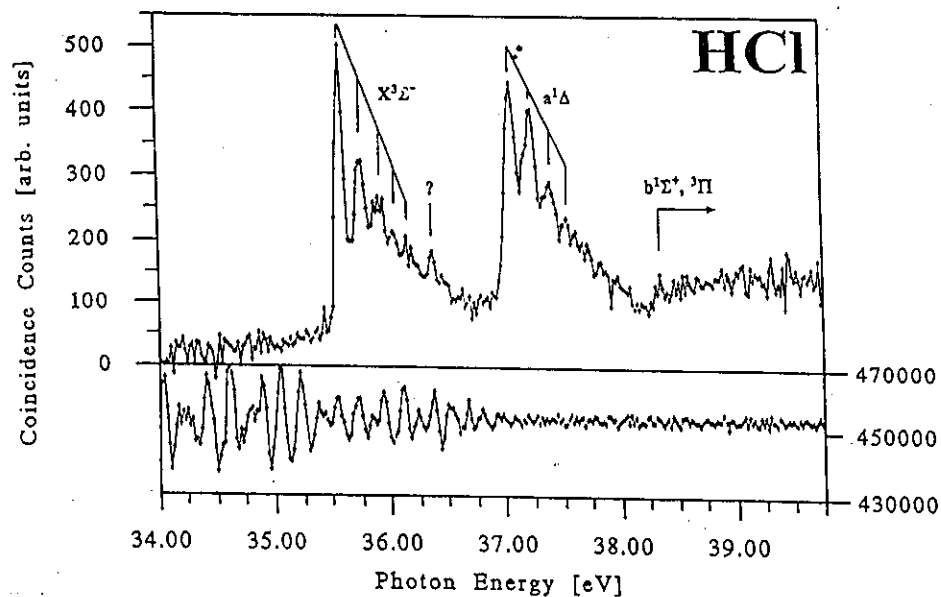


Coincidence set up



DPI

Coincidence experiments started in 1972 with e-ion coincidence
 (Danby and Eland, J. Mass Spectrom. Ion Phys 8, 153)
 e-e coincidence experiments started in 1987
 (Lablanquie et al. Phys. Rev. Lett. 58, 992)



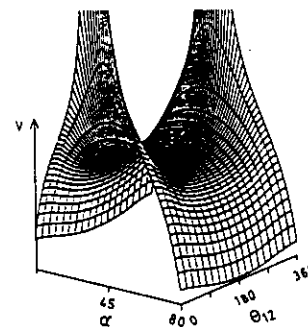
A.G. McConkey et al. (1993)

DPI at threshold, Wannier region

Close to threshold He DPI ideal case for correlated motion of 2 e^- in the continuum.

3 charged particles boundary conditions

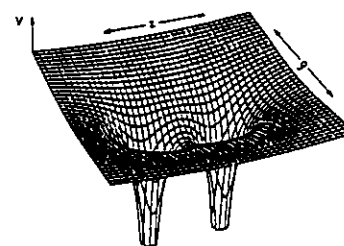
Wannier theory is expected to hold (symmetry in the angular distribution).



$$\frac{d^4\sigma}{dE_1 dE_2 d\Omega_1 d\Omega_2} = |b|^2 (\cos\theta_1 + \cos\theta_2)^2 \exp\{\gamma\} \cdot \delta(E_1 + E_2 - E_{\text{exc}})$$

$$\gamma = -4 \ln 2 (\theta_{12} - 180^\circ)^2 / \theta_{\text{FWHM}}^2$$

$$E_{\text{exc}} = E_1 + E_2 = \hbar\omega - E_{\text{th}}$$

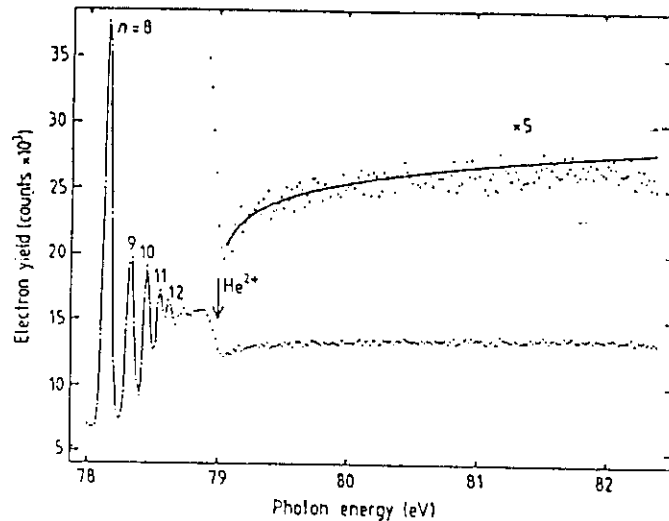


$$\frac{d^3\sigma}{dE_1 d\Omega_1 d\Omega_2} = |a|^2 (\cos\theta_1 + \cos\theta_2)^2 \exp\{\gamma\}$$

$$\theta_{\text{FWHM}} = \theta_0 E_{\text{exc}}^{1/4}$$

$$\frac{d\sigma}{dE} = \text{const} = \frac{\sigma}{E_{\text{exc}}}$$

DPI at threshold, Wannier region



Threshold photoelectron spectrum of helium over an energy range in the region of the double-ionization threshold; photon bandpass 60 meV. The smooth full curve in the expanded inset is a fit to the data of the Wannier threshold law with the exponent $n = 1.056$, equation (4.19). From

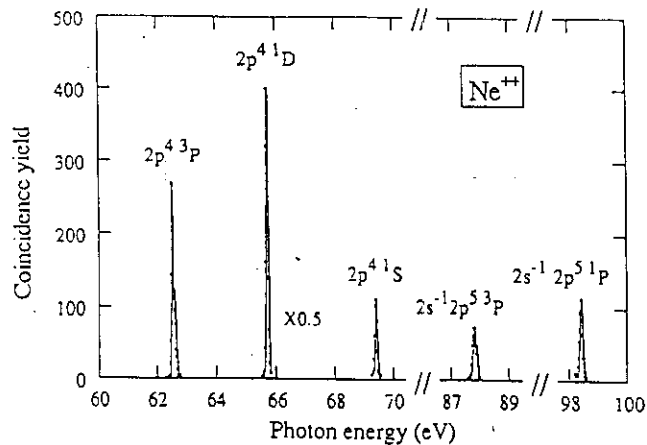


Figure 2a: TPEsCO spectrum of Ne over the photon energy range 62 to 100 eV

DPI at intermediate energies

$$\hbar\omega + \Psi_i(N) \rightarrow \Psi_f(N-2) + \epsilon + \epsilon'$$

a first order approach

Energy conservation

$$\hbar\omega + E_i(N) = \epsilon + \epsilon' + E_f(N-2)$$

In single particle scheme

$$\hbar\omega + E_i(N) = \epsilon + \epsilon' + E_f(N-2, \ell, j)$$

DPI cross section

$$\sigma^{(2)}(\omega) = \frac{4\pi^2 e^2 \omega}{c} \sum_f |T_{if}|^2 \delta(\epsilon + \epsilon' + E_f(N-2) - E_i(N))$$

$$T_{if} = \langle \Psi_f | \hat{e} \cdot \sum_i \underline{e}_i | \Psi_i \rangle$$

Differential cross section

$$\frac{d^6\sigma}{d\underline{k} d\underline{k}'} = \frac{4\pi^2 e^2 \omega}{c} |T_{if}|^2 \delta(\epsilon + \epsilon' + E_f(N-2) - E_i(N))$$

Selection rules

- $d^6\sigma \neq 0$ if $K_z \neq 0, K'_z \neq 0 \quad \hat{z} \parallel \hat{e}$
- $d^6\sigma$ invariant if $\epsilon, \epsilon', K_z, K'_z$ identical
- $d^6\sigma = 0$ if $\epsilon = \epsilon'$ and $K_z = K'_z$
 $T_{if} \propto A(\epsilon, \epsilon') [Y_{10}(\hat{K}) + Y_{10}(\hat{K}')]]$
- $d^6\sigma = \text{Max}$ if $\vec{K} = \vec{K}' \parallel \hat{e}$

DPI DCS the angular distributions

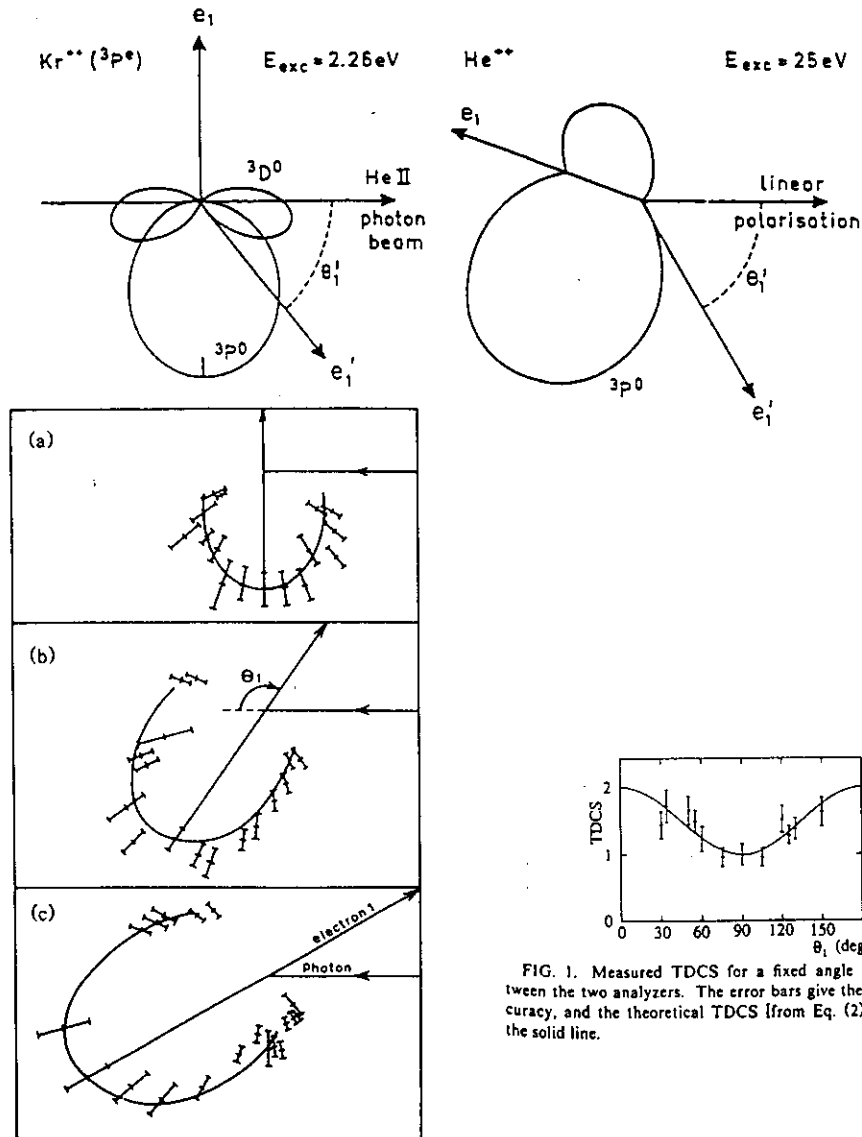


FIG. 2. Measured TDCS for fixed positions of the first electron: (a) $\theta_1 = 90^\circ$, (b) $\theta_1 = 125^\circ$, (c) $\theta_1 = 150^\circ$. The incoming photon beam and first electron are indicated by arrows, and the polar representation with a normalization which is common to (a)-(c) is used.

FROM: MAZEAU et al.
Phys. Rev. Lett. 67 (91) 820

DPI DCS the angular distributions

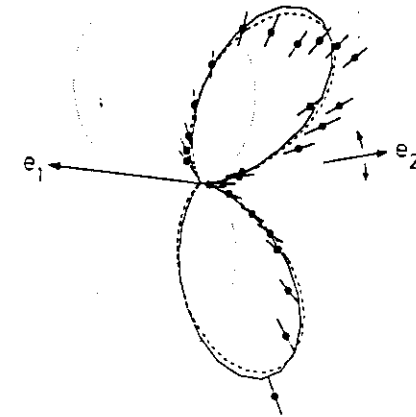


FIG. 2. Relative values of experimental and theoretical TDCS for the double photoionization of helium at $h\nu = 99$ eV in the plane perpendicular to the photon beam: direction of electron e_1 fixed; electron e_2 at different angles. For further details see text.

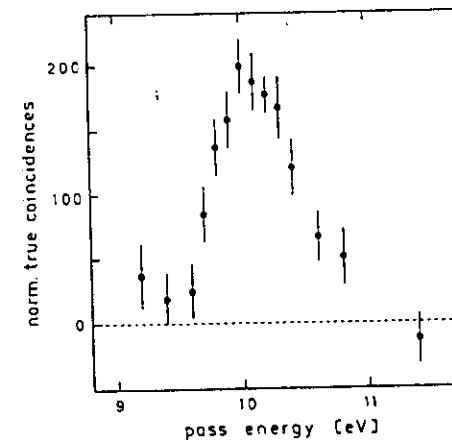


FIG. 1. Coincidence counts as a function of the pass energy E_2 of spectrometer 2 with the pass energy of spectrometer 1 set to $E_1 = E_{exc}/2 = 10$ eV.

FROM: Schwarzkopf
et al.
Phys. Rev. Lett. 20 (93)

DPI in molecules

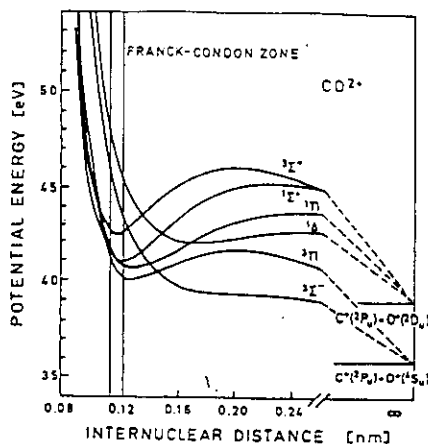
The full fragmentation pattern has been studied for H_2

V. Schmidt and coworkers
Phys. Rev. Lett. 63 (1989) 2040

For larger molecules will be difficult unless results from several experiments are combined or: coincidence of the two electrons with the fragment ions is performed

Various kind of e-ion, ion-ion coincidence experiments have been performed (*)

The CO_2 molecule



PIFICO has shown
 $C^+ O^+$ pairs from
autoionization of
 CO^+

(*) NENNER I. & BESWICH J.A. "Handbook of S.R." 1982

DPI in molecules

TPEsCO Threshold Photoelectron Coincidence Spectra

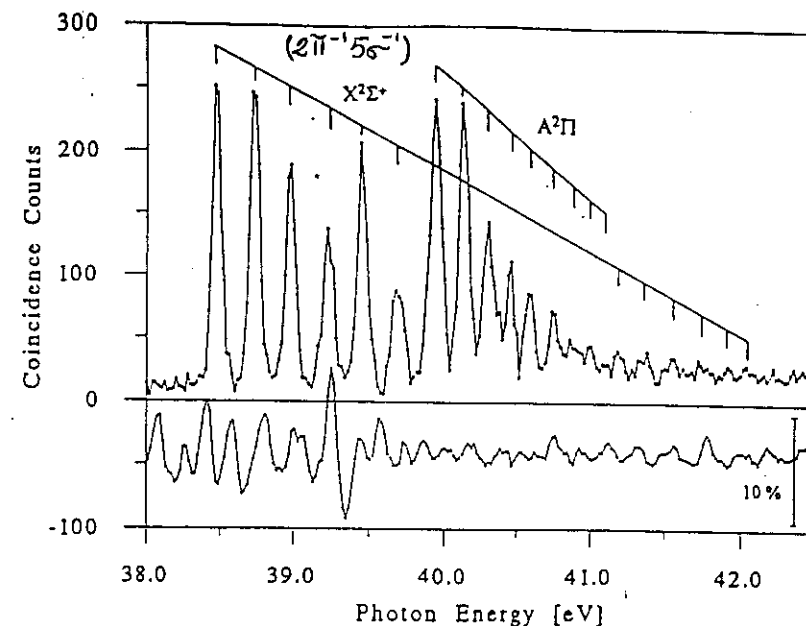


Figure 4a: TPEsCO spectrum of NO_2^+ over the photon energy range 38 to 42.5 eV. The lower spectrum in the figure is the sum of the threshold spectra collected in both analyzers.

$$E(v) = T_0 + \omega_e(v + 1/2) - \omega_e x_e(v + 1/2)^2$$

Table 2: Molecular constants

		exp.	ref. 33	ref. 34
$X^2\Sigma^+$	T_0 (eV)	38.39 ± 0.05	39.42	38.56
	ω_e (meV)	255 ± 19	277	261
	$\omega_e x_e$ (meV)	3 ± 1	4	3
$A^2\Pi$	T_0 (eV)	39.85 ± 0.007	39.96	40.02
	ω_e (meV)	186 ± 4	170	184.
	$\omega_e x_e$ (meV)	4.5 ± 0.4	3	4.6
$B^2\Sigma^+$	T_0 (eV)	43.16 ± 0.015		
	ω_e (meV)	272 ± 18		
	$\omega_e x_e$ (meV)	20 ± 4		

DPI at High energy: Correlation spectroscopy

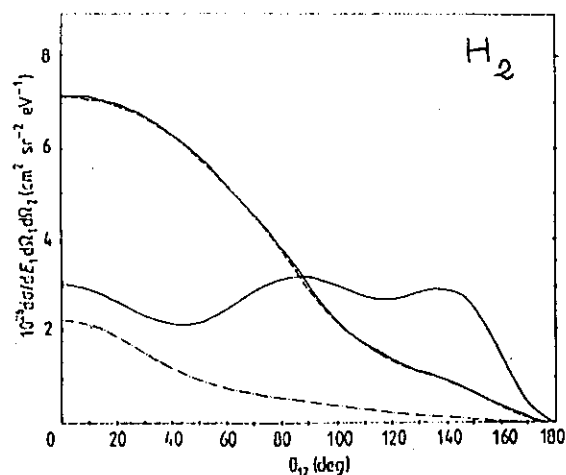
In 1977 Neudatchin et al. () proposed the high energy ($h\nu, 2e$) coincidence experiments to investigate the double ionization of atoms and molecules. These experiments should represent the natural generalization of impulsive ($e, 2e$) experiments. The goal of the proposal () was to develop a spectroscopy of doubly charged ions that would enable the direct determination of the partial two-electron Fourier amplitude

$$\psi_{if}(k_1, k_2) = \frac{1}{2\pi} \int dr_1 dr_2 \psi_{if}(r_1, r_2) e^{i(k_1 \cdot r_1 + k_2 \cdot r_2)}$$

of the many-electron wavefunction $\psi_i(r_1, r_2, \dots, r_N)$ projected on an arbitrarily selected state $\psi_f(r_1, r_2, \dots, r_N)$ of the doubly charged ion

$$\psi_{if}(r_1, r_2) = \int dr_3 \dots dr_N \psi_f^*(r_3, \dots, r_N) \psi_i(r_1, \dots, r_N)$$

The importance of studying these quantities becomes clear when a two electron system is considered. In this case $\psi_{if}(k_1, k_2)$ is merely the wave function of the two electron system in the momentum space representation. It contains all the details of the structure of the system and in particular the momentum distribution of the relative motion of the electrons in the degree of freedom $r_{12} = r_1 - r_2$. This motion is dominated by electron-electron correlations. In many-electron systems if the transition $i \rightarrow f$ involves the knock-out of two electrons from the same orbital then $\psi_{if}(k_1, k_2)$ characterizes the electron-electron correlations in that orbital, viceversa if the transition involves electrons from different orbitals then $\psi_{if}(k_1, k_2)$ enables the study of electron-electron correlations in different orbitals. The sensitivity of the technique can be inferred from a theoretical study of the double photoionization of H_2 molecule



e-e angular distributions

$$h\nu = 296 \text{ eV}$$

$$K_1 = K_2 = 320^{-1}$$

— CI 5 conf.

--- LCAO MO

== Corr. W.F.

LEVIN et al.
J. Phys. B 17 (1984) 1525

DPI at High energy: Correlation spectroscopy

In this approximation the DPJ x-section factorizes as:

$$\frac{d^5\sigma}{d\Omega_1 d\Omega_2 dE} \propto \frac{K_1 K_2}{\omega} |\psi_{if}(k_1, k_2)|^2$$

Experiment Kinematics

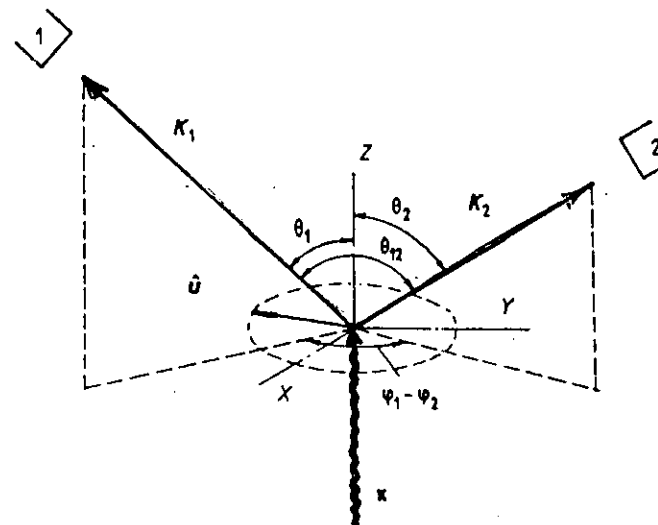
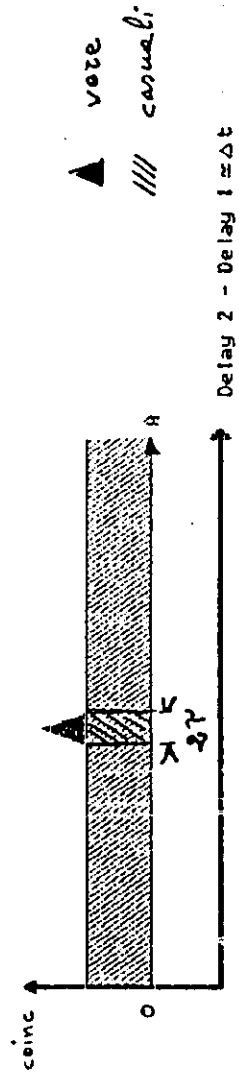
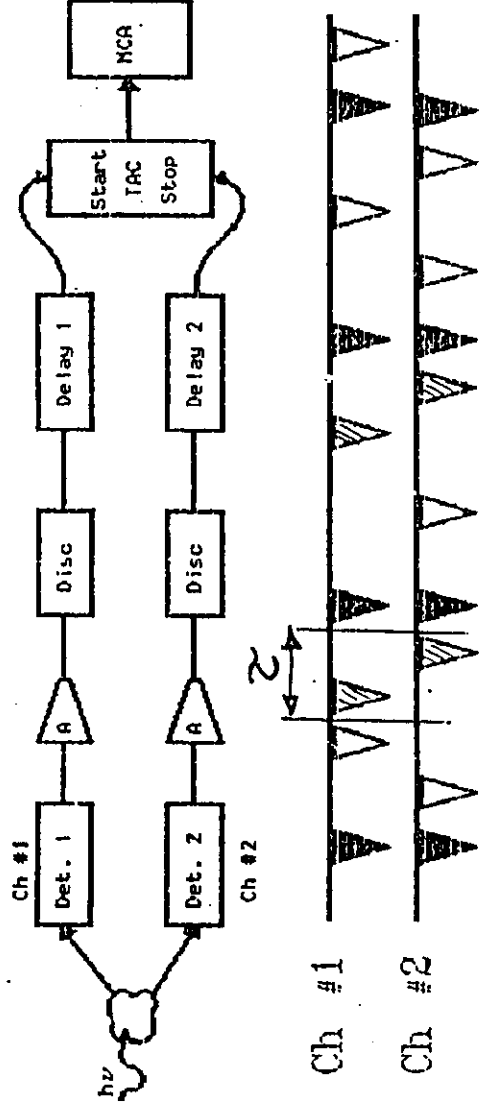


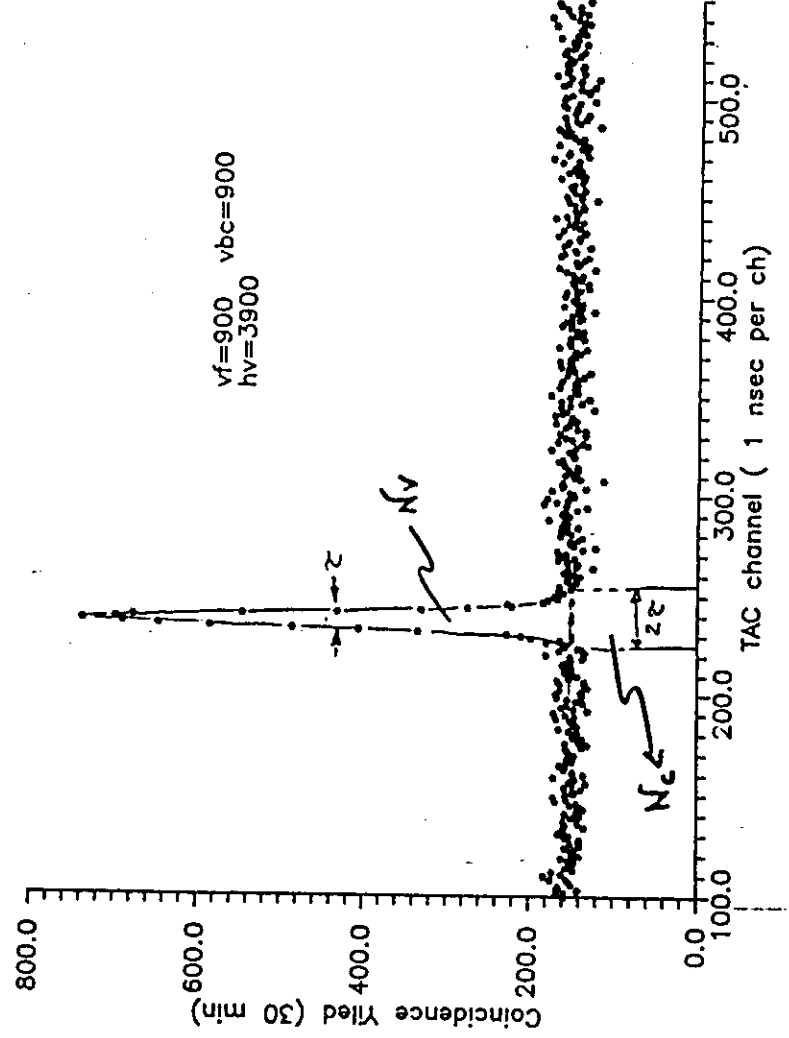
Figure 1. Geometry of a possible experimental set-up for the $(\gamma, 2e)$ process

On the experimental problems in coincidence spectroscopy



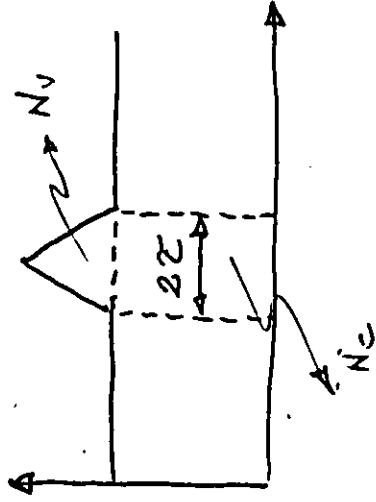
Sorgente "continua" se $\tau > \tau_p$

τ : tempo risolutivo coincid.
 τ_p : durata impulso luce



On the experimental problems in coincidence spectroscopy

COINCIDENCE OPTIMIZATION



To minimize error

$$\epsilon = \frac{N_v}{N_c}$$

as small as possible

Single Rate $R_i = G_i I_{ph}(g_i) \Delta E_i \Delta \Omega_i \rho_i$

Chance C. Rate $R_C = R_1 R_2 \Delta \tau$

True C. Rate $R_V = G_V I_{ph}(g_V) \Delta E_C \Delta \Omega_1 \Delta \Omega_2 \rho_1 \rho_2$

$$\epsilon \propto \left(\frac{G_V}{G_1 G_2} \right) \frac{(2\tau)^{-1} \Delta E_C}{I_{ph}(g_V) \Delta E_1 \Delta E_2}$$

ϵ_{max} for $I_{ph} \rightarrow 0$!

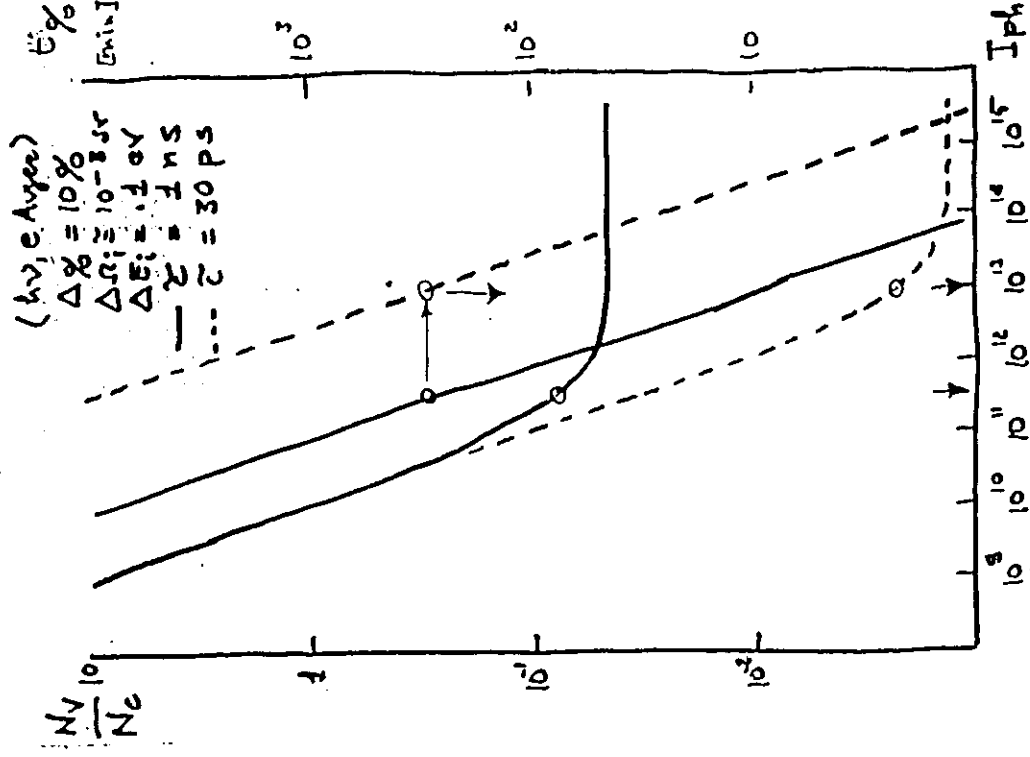
for $g_V \rightarrow 0$!

$\Delta g = \frac{\Delta N_v}{N_v} \leftarrow \text{Acc. time} = t\%$

$$t\% = \frac{\sqrt{2}}{2 \rho_2 \Delta \Omega_1 \Delta \Omega_2} \times \frac{1}{\Delta g^2} \times \frac{1}{G_C} \times \left[\frac{1}{I_{ph} g_V \Delta E_C} + \frac{G_1 G_2}{G_C} \Delta \tau \right]$$

$\Rightarrow t\% \text{ min} \Rightarrow \Delta \Omega_i \text{ large ; } \Delta \tau \text{ short} \leftarrow$

On the experimental problems in coincidence spectroscopy



How to MINIMIZE τ ?

i) Detectors (HCP $\approx 10 \div 100 \text{ ps}$)

ii) Electronics ($\tau_{AC+HCA} \approx 10 \div 100 \text{ ps}$)

iii) Trajectories ($> 200 \text{ ps}$ (e); $\sim 100 \text{ ns}$ (I $^+$))
 After compensation

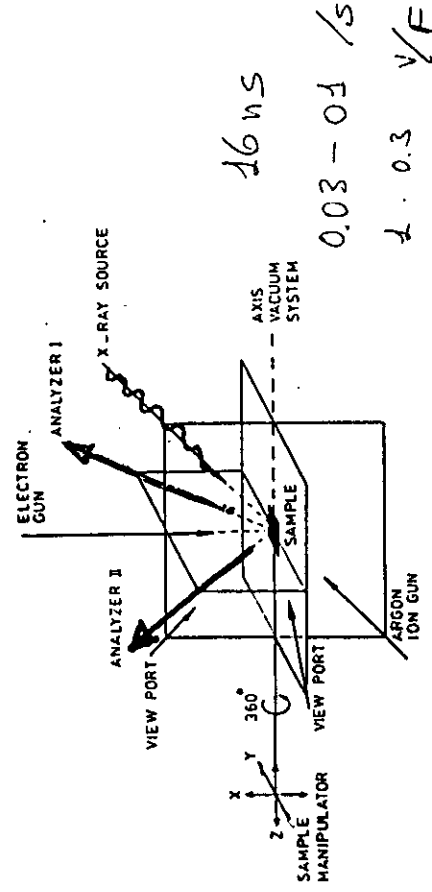
(iii) Host reverse. To reduce:

- a) Hardware or Software Compensation
- b) Reduce $\Delta\Omega_i$!

On the experimental problems in coincidence spectroscopy



H.W. HAAK et al. *Rev. Sci. Instr.* 55 (1984) 696
Phys. Rev. Lett. 41 (1978) 1825



80

Fig. 3.1. Geometric arrangement of various components on the vacuum system.

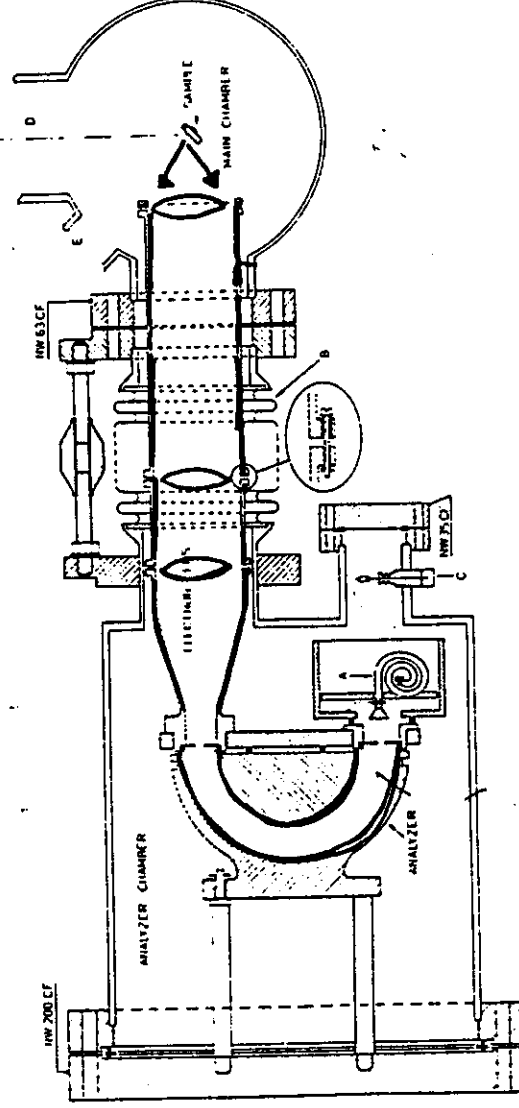
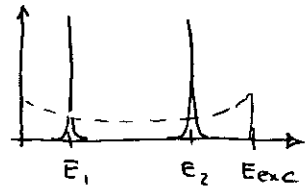


Fig. 3.12. The mechanical construction of the analyzer and electron lens in the vacuum chamber, the magnetic shielding is omitted. The inset shows the electrical insulation between the various lens parts by means of a ceramic ring.

FOR A REVIEW!
 GRANNEMAN & VANDERWIEL
 Handbook of Synchronization
 1982

Inner shell photoionization and coincidence experiments

A two step process
Energy sharing not even



$$E_1 = h\nu - E_B^+$$

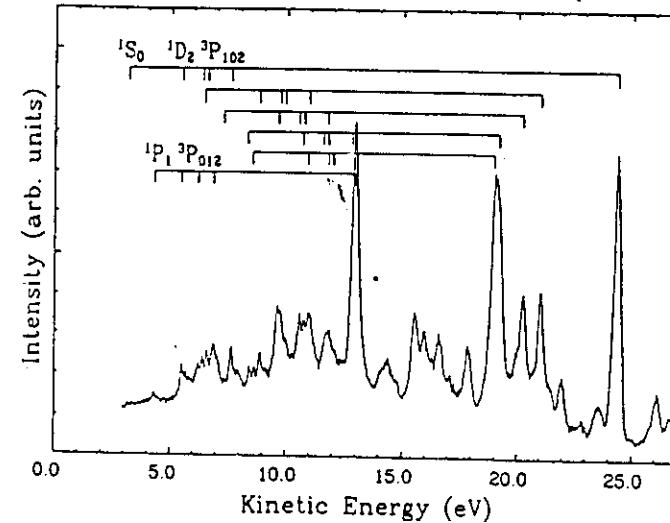
$$E_2 = h\nu - E_B^{++}$$

To establish complete fragmentation pattern only directional dependence is needed.

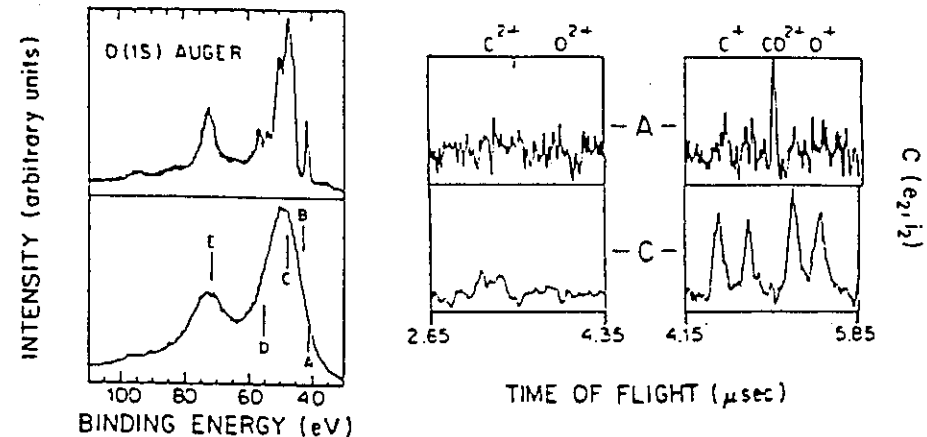
If 2step hold coincidence is not needed.
... $C(e_1, e_2)$ are important if:

- i) LSJ not valid $\rightarrow$ several Auger amplitudes might contribute.
- ii) Complex systems, e.g. $Xe 4d_{5/2} \rightarrow 6p$
 $\begin{matrix} \nearrow Xe^+ + e_1 \\ \searrow Xe^{++} + e_2 \\ \searrow Xe^{++} + e_1 + e_2 \end{matrix}$
- iii) Post collision interactions are present
- iv) In molecules to identify fragmentation patterns associated with given valence-hole configurations.

Inner shell photoionization and coincidence experiments



Low-energy part of the resonant Auger spectrum of xenon taken at the $4d_{5/2} \rightarrow 6p$ resonance (65.1 eV). The first-step decay leads to the following spectator lines: $5s^0 5p^6 (1S_0) 6p$ at 12.96 eV; $5s^2 5p^3 5d 6p$ at 18.98 eV, 19.20 eV and 20.24 eV; $5s^1 5p^5 (1P) 7p$ at 21.05 eV and $5s^1 5p^5 (1P) 6p$ at 24.38 eV. The marks indicate corresponding first and second step Auger lines.



$C(e_2, l_2)$ coincidences in inner-shell photoionization of CO. Left part: O(1s) Auger spectra taken with (bottom) and without (top) the ion extraction field applied across the ionization region; right part: two examples of $C(e_2, l_2)$ coincidence spectra obtained with Auger electrons from the energy regions A and C, respectively.

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