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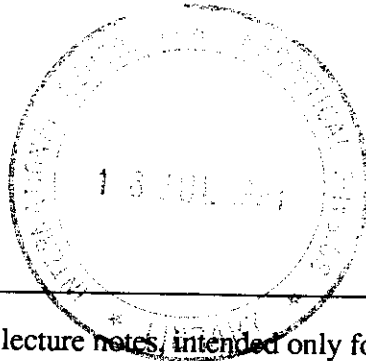
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Workshop on Fluid Mechanics

(7 - 25 March 1994)

**Scaling, turbidite deposition,
and the morphology of the continental slope**

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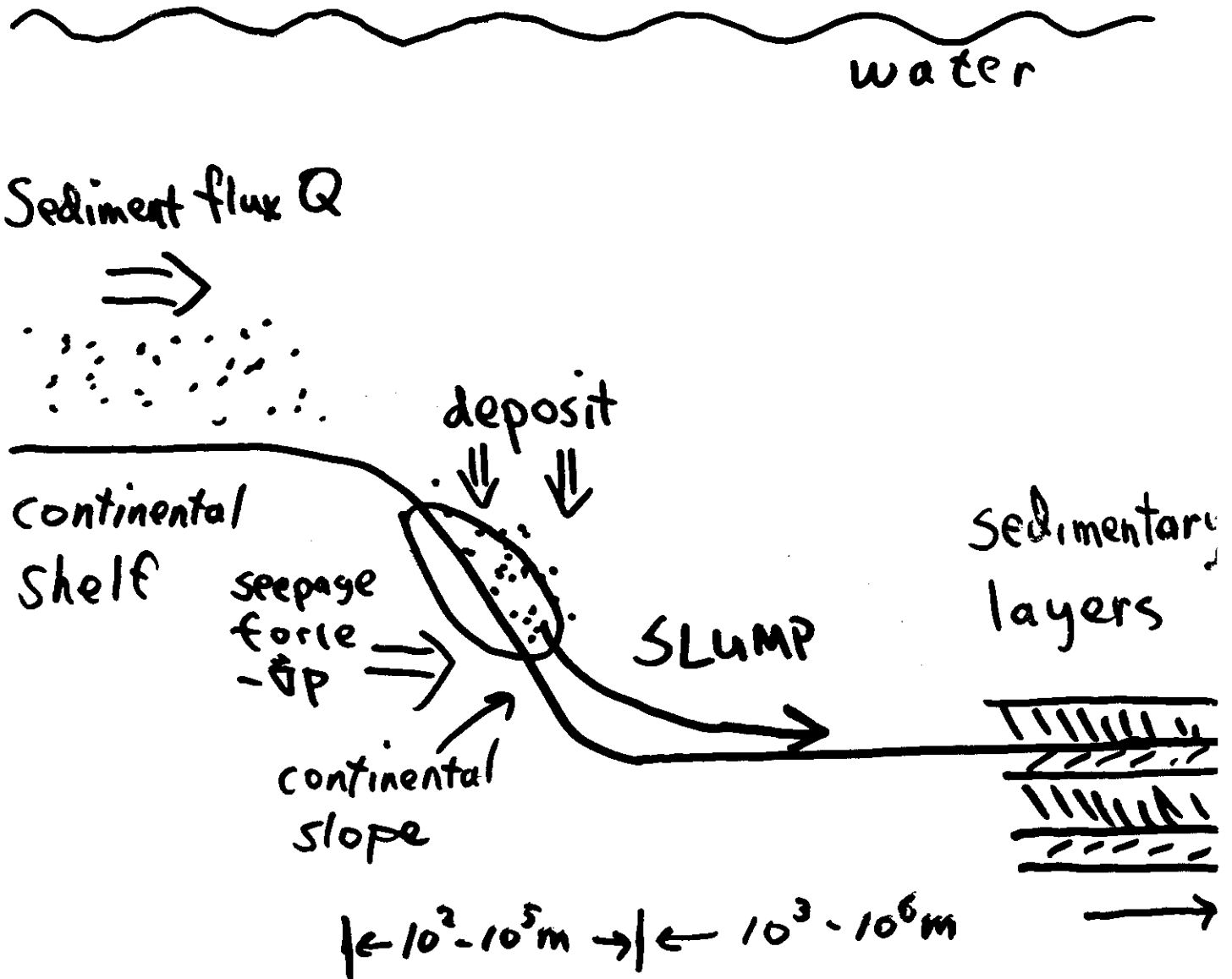
These are preliminary lecture notes, intended only for distribution to participants

Scaling, turbidite deposition, and the morphology of the continental slope

D. Rothman, MIT
w/ John Grotzinger

and P. Flemings, J. Carlson, O. Mikhaïlov

Turbidite sedimentation



Duration of slumping "event": 1 minute - 1 day

Time between events: $10^0 - 10^3$ years



Figure 10-35
 An artist's representation of the floor of the North Atlantic Ocean based on bathymetric studies of Bruce C. Heezen and Marie Tharp of the Lamont-Doherty Geological Observatory. Depths shown in feet below sea level. [Painted by Heinrich C. Berann; copyright © 1968 National Geographic Society.]

Press & Steven

material at the bottom, grading upward to fine

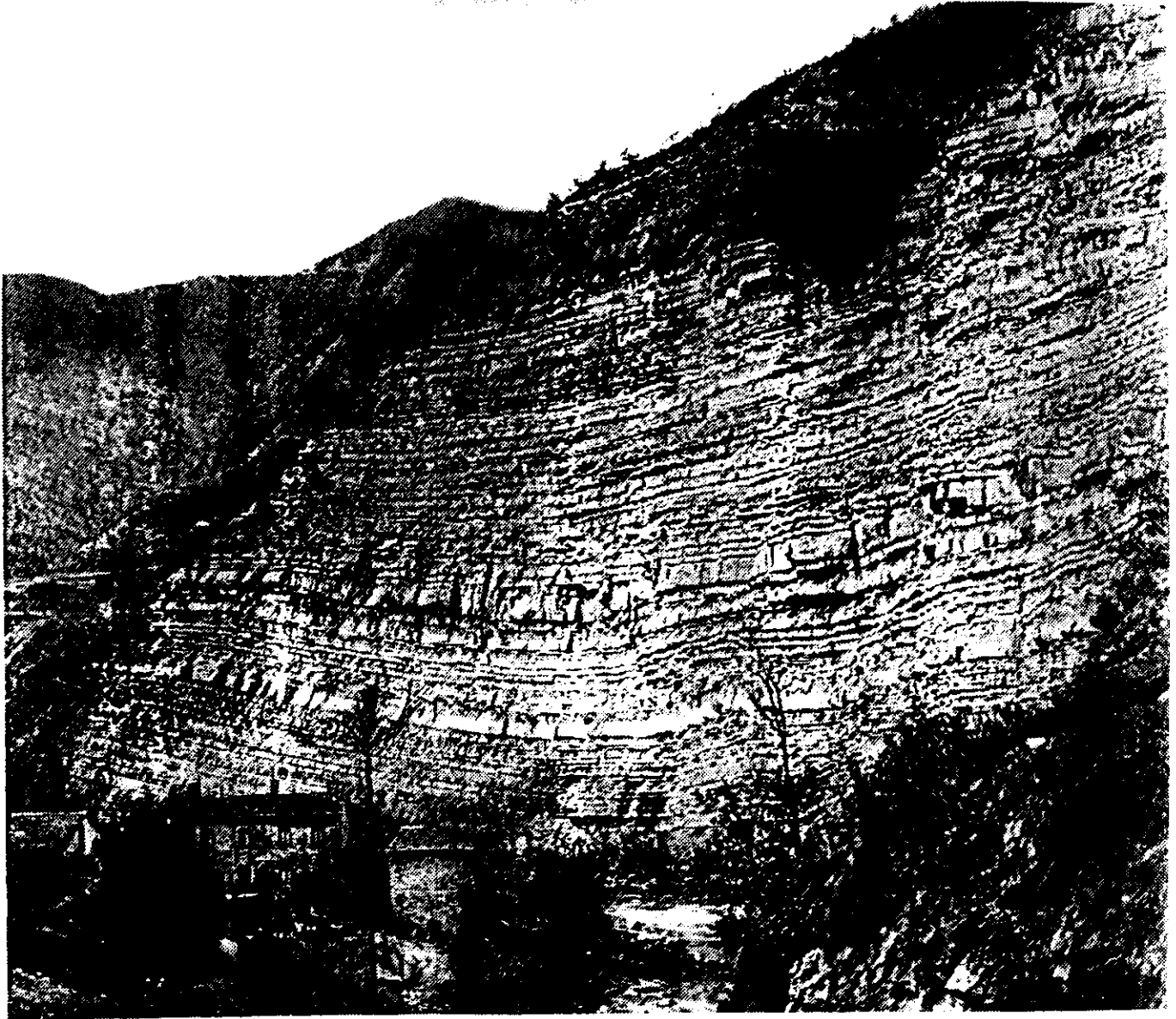
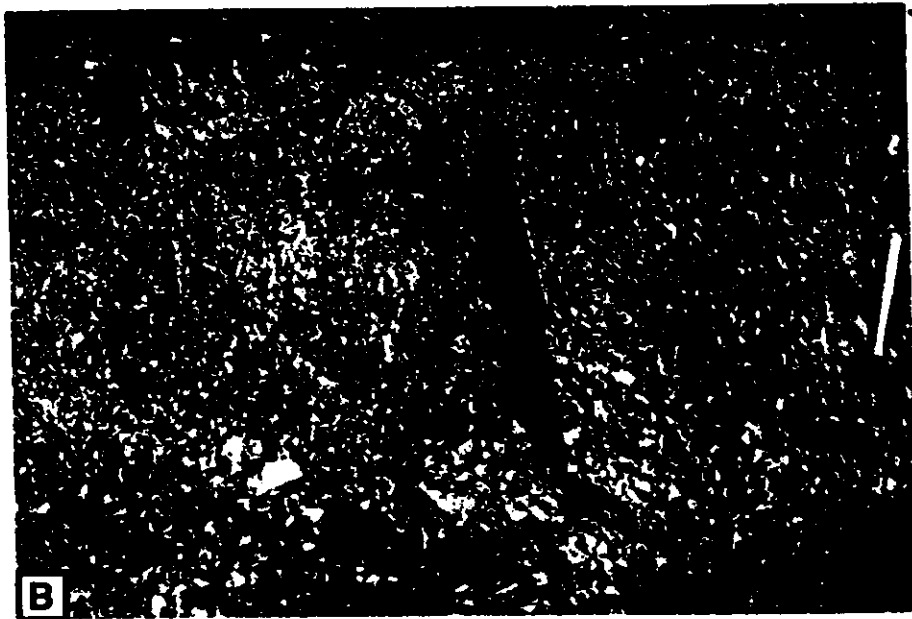


Figure 10-32 *Press & Siever*
A thick sequence of graded Miocene turbidite beds in the Apennines. The lighter, thicker units are sandstones that are coarsest at an abrupt base and grade upward through finer grain sizes into the darker shale beds. Each pair of sandstone-shale units represents one turbidity flow in a deep marine basin. [Photo by P. E. Potter. From F. J. Pettijohn, P. E. Potter, and R. Siever, *Sand and Sandstone*. Copyright 1972 by Springer-Verlag New York, Inc.]

SE California

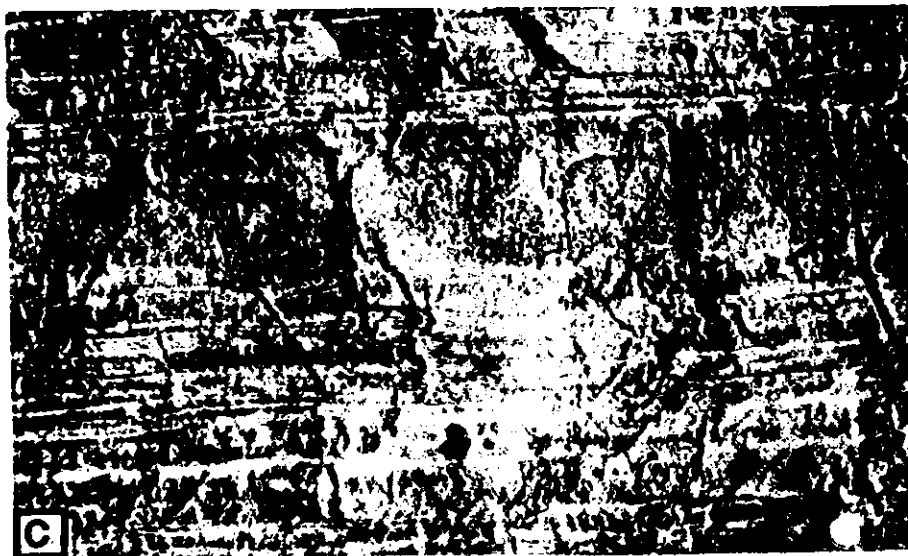


"macro"
scale



Single
layer

"meso"
scale



"micro"
scale

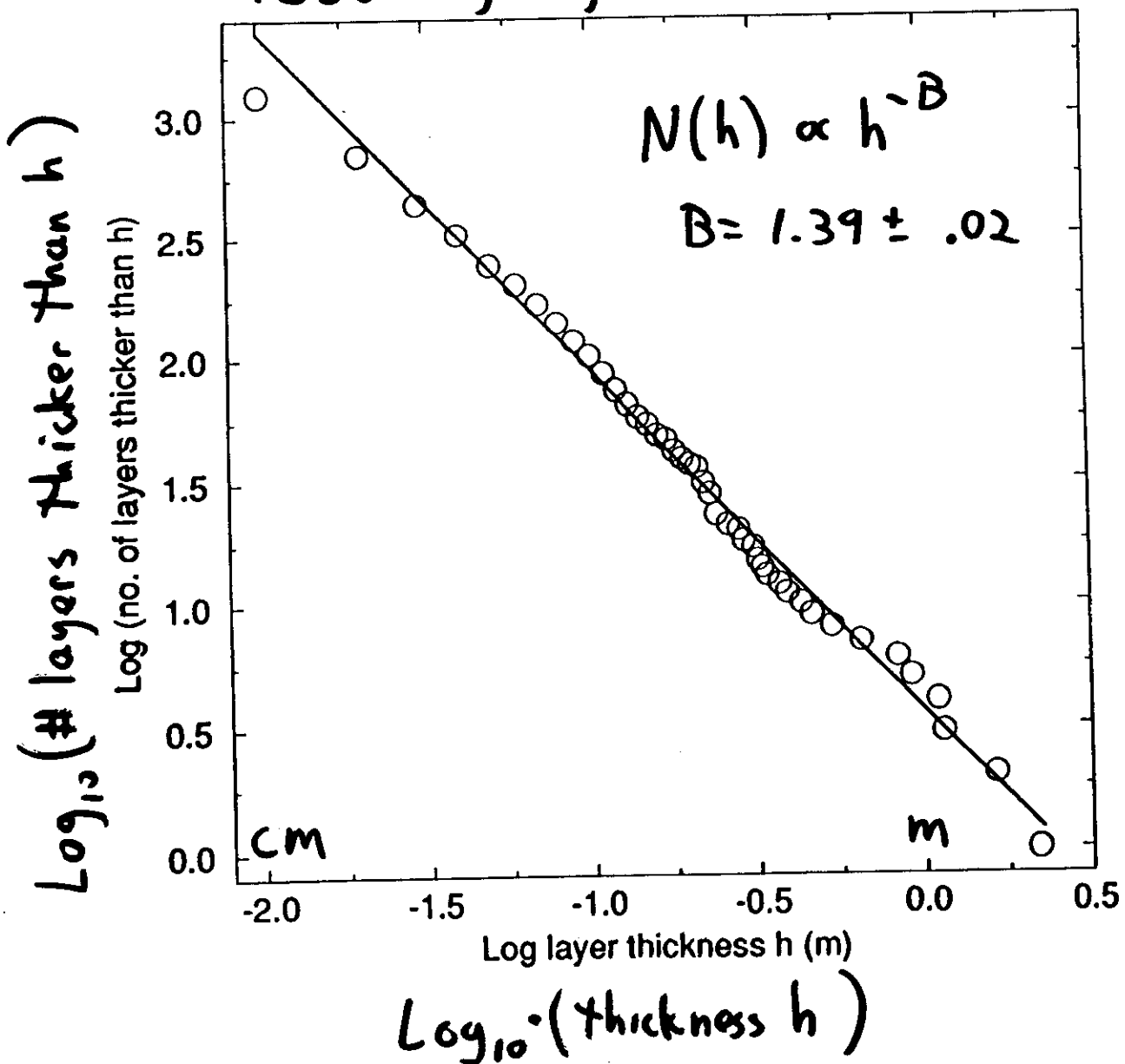
coin

$h = \text{layer thickness}$

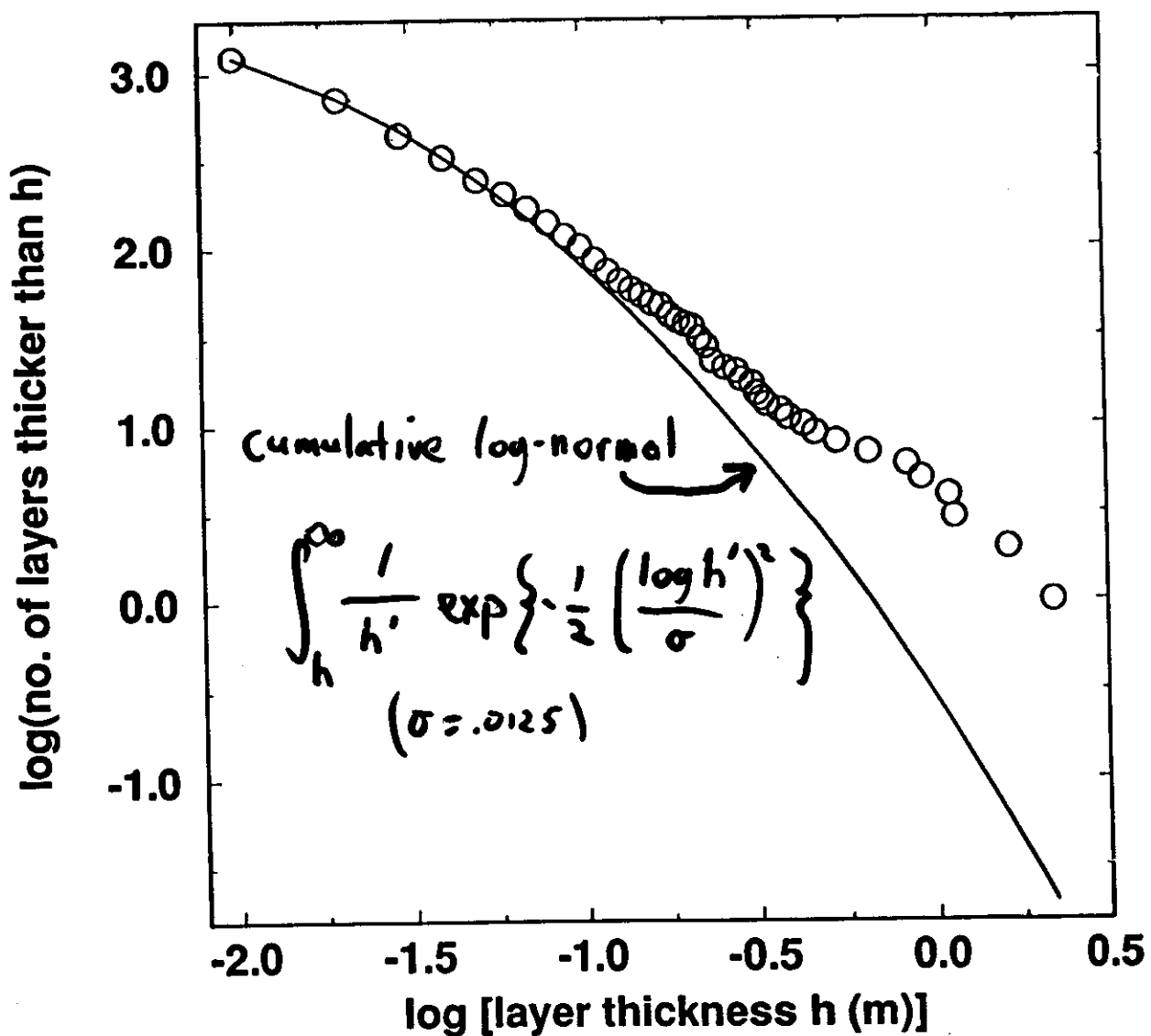
$N(h) = \# \text{ layers thicker than } h$

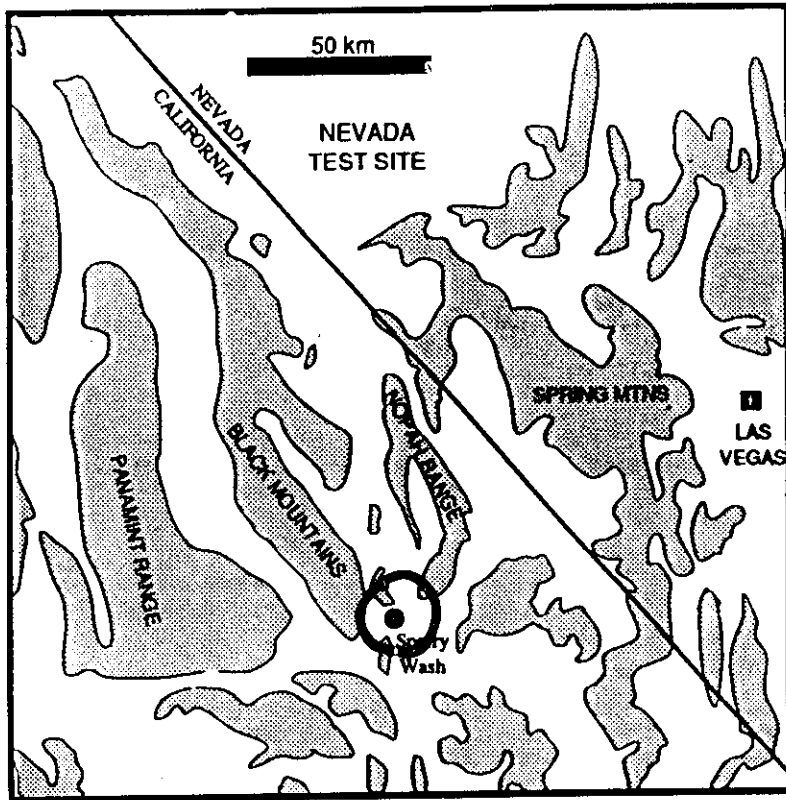
"Direct measurement"

1235 layers, SE California



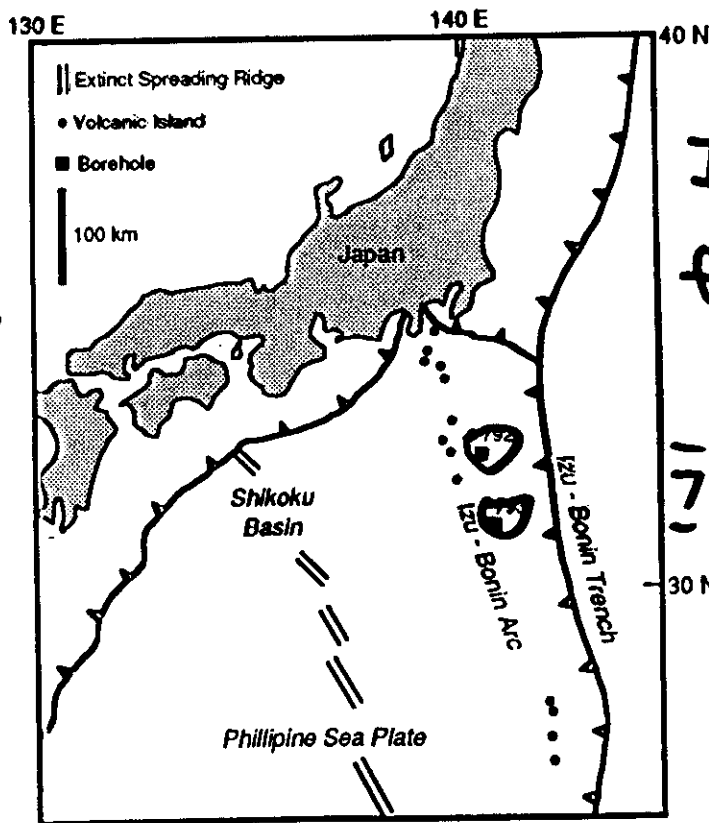
A log-normal distribution
does not fit!





SE Calif
 ~675 Ma

A



Izu-Bonin
 forearc basin

75 km

~30 Ma

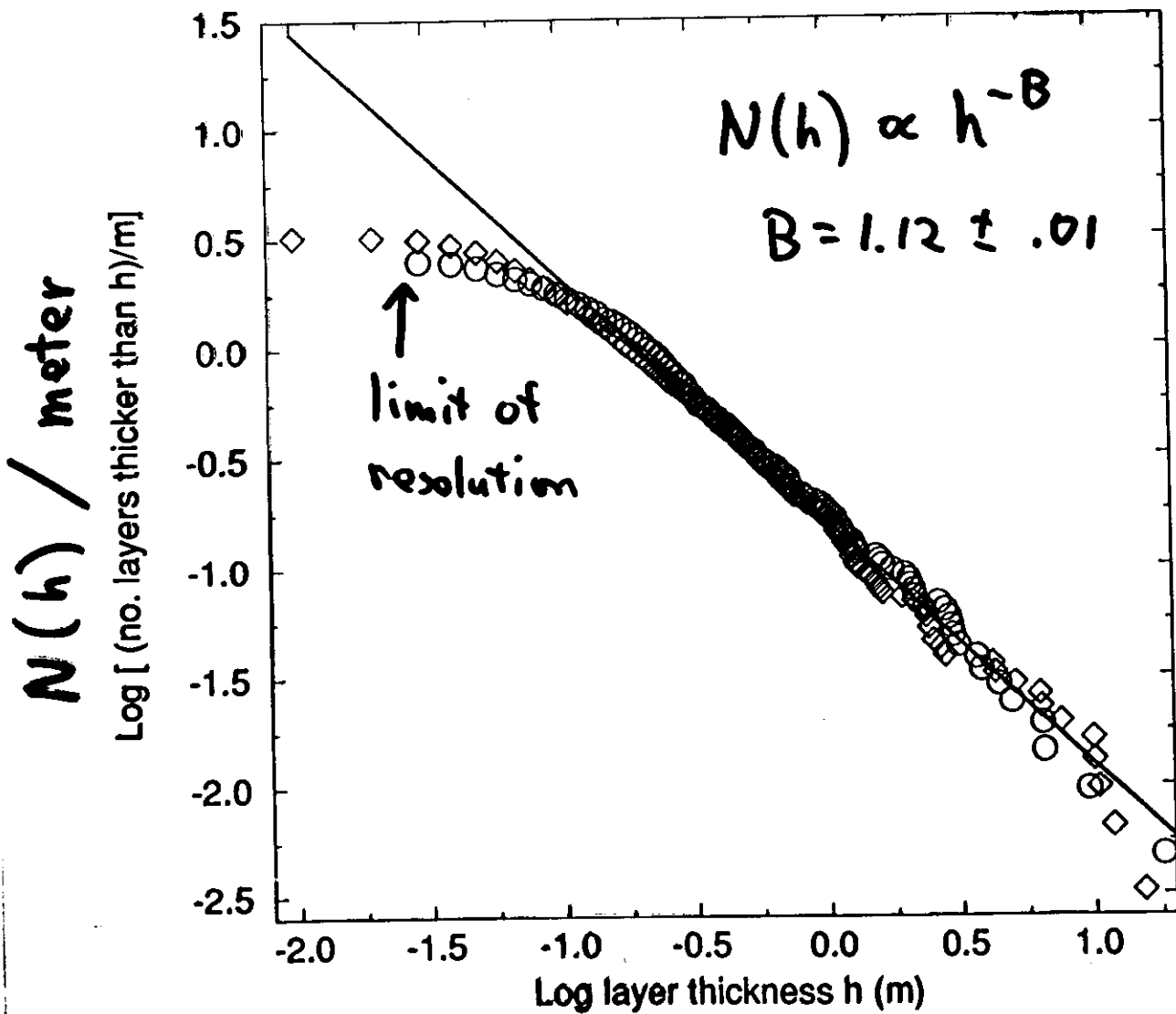
Hiscott et al,
 1992

B

Offshore Japan, FMS images

Hiscott, Collela, Pezard, Lovell, & Malinverno, 1992

O : Hole "792" } ~ 75 km apart
◊ : Hole "793" } Different ages
Different depths

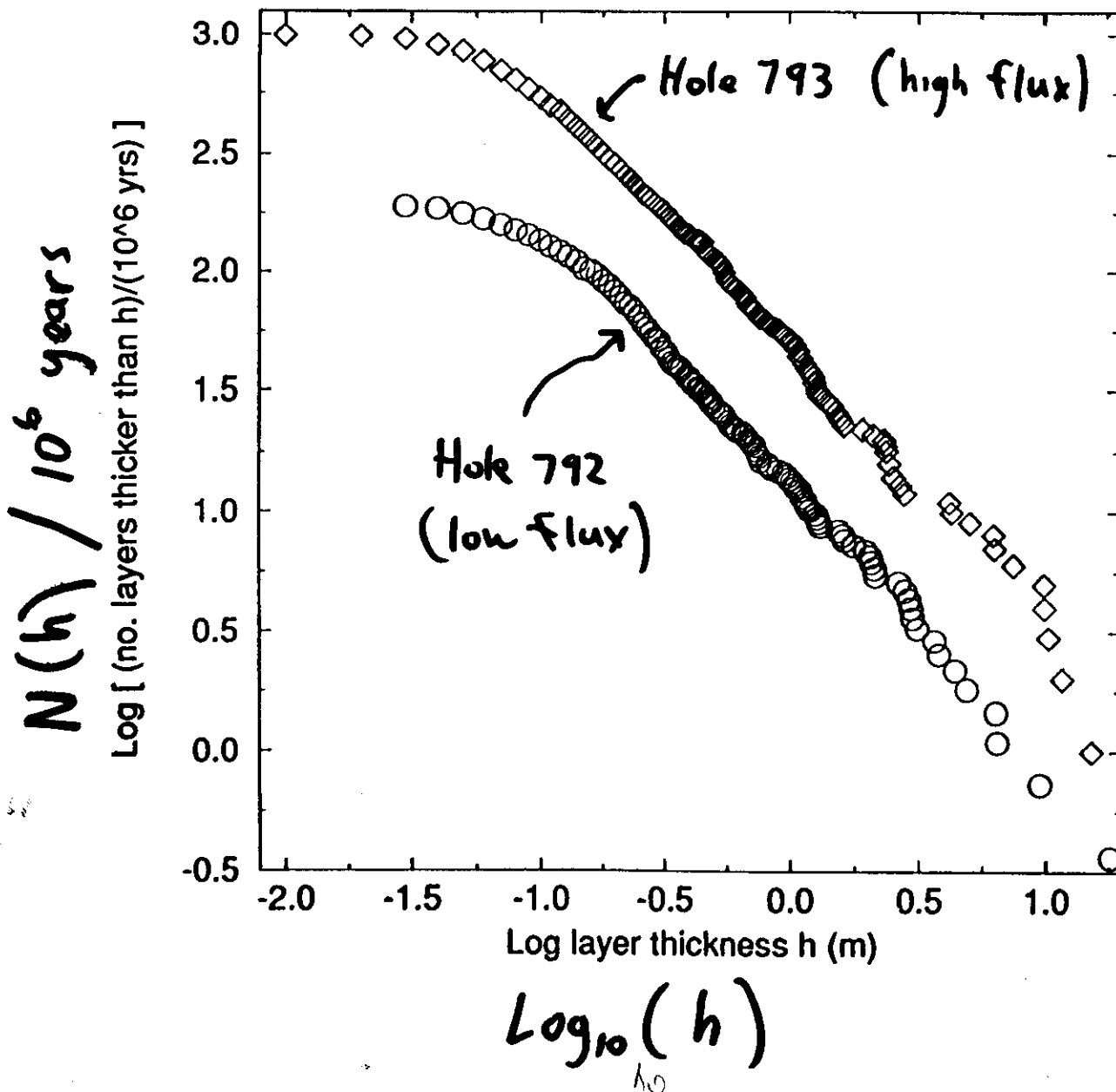


$1 \propto (\text{thickness } h)^B$

Differential flux: avg. sediment accumulation rate is $\sim 4\times$ greater in Hole 793 than Hole 792.

But: dynamics + system size are \sim same
distance from shelf break \sim same

\Rightarrow Turbidite deposition is slaved to flux,
not earthquakes (?)



Implications

- 1.) Dynamics of turbidite deposition may be scale invariant.
(e.g., nonlinear diffusion)

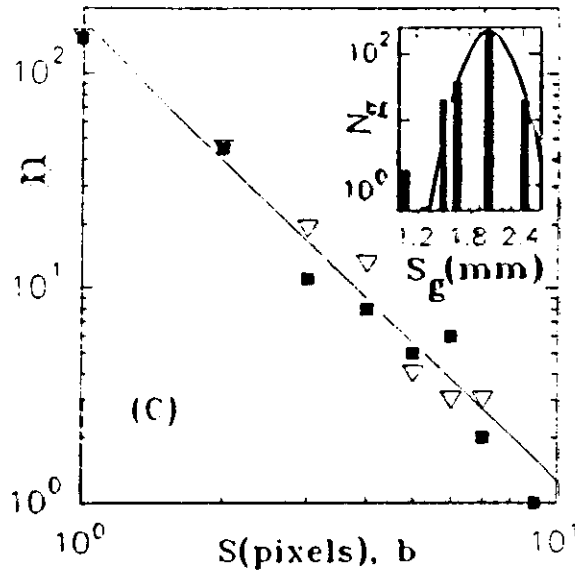
- 2.) Possible connection with "self-organized criticality" (Bak et al, 1988):
Shelf break may be permanently marginally stable;
fluctuations (slump events) occur at all scales.

- 3.) Unlike many laboratory sandpiles
(Evesque + Rajchenbach, 1988; Jaeger + Nagel, 1989;
Held et al, 1990; Bretz et al, 1992; Rosendahl et al, 1993)
turbidite deposition may be an example of a
real (underwater) sandpile that does exhibit
scale invariance.

Bretz et al, 1992

Flat sandpile

$$N(>s) \sim s^{-1.1}$$

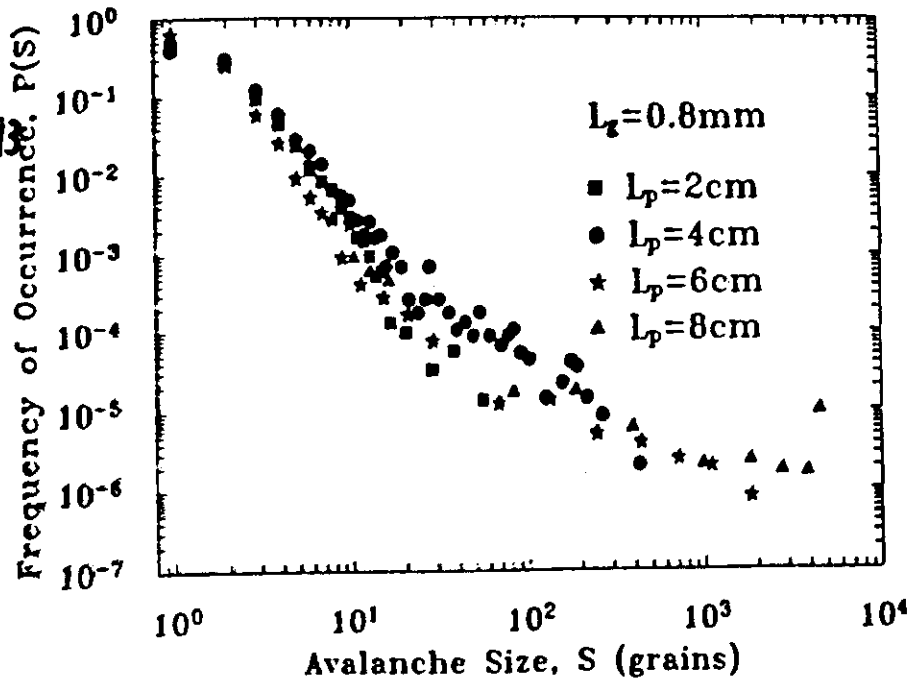


Rosendahl et al, 1993

Conical sandpile

$$N(>s) \sim s^{-1.1}$$

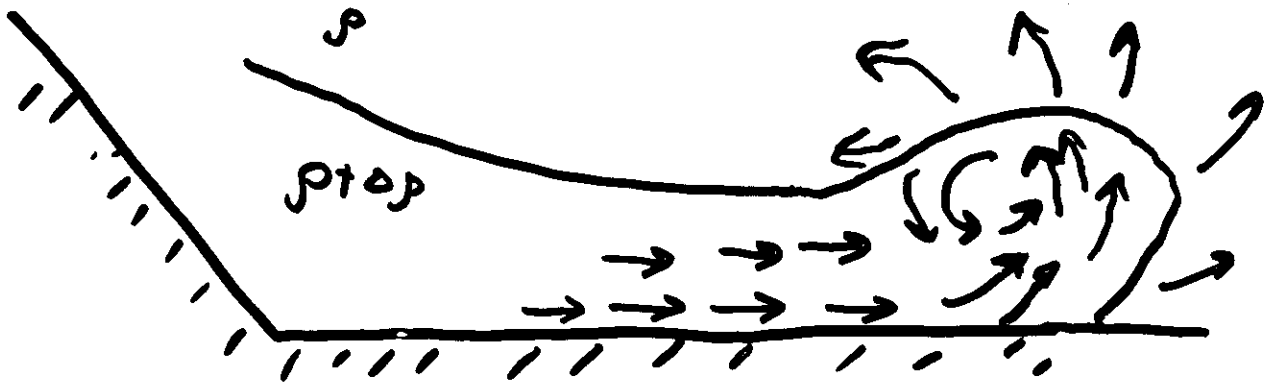
s small



There are, however, large periodic avalanches (relaxation oscillations, i.e., Jaeger et al, 1989)

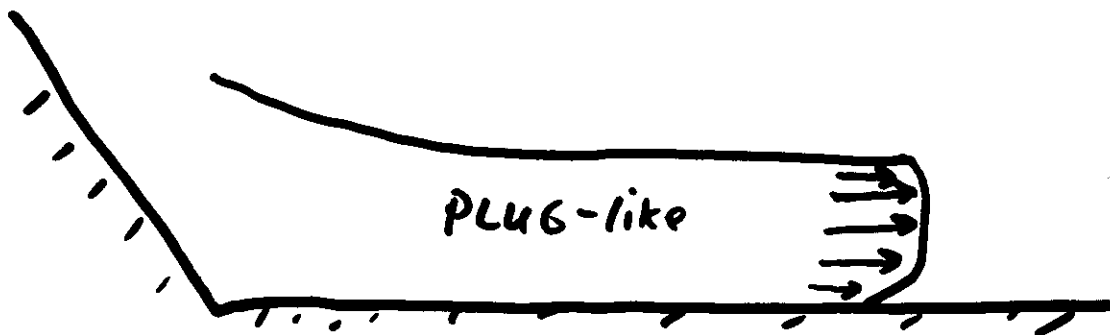
Two types of sediment gravity flows

Turbidity currents

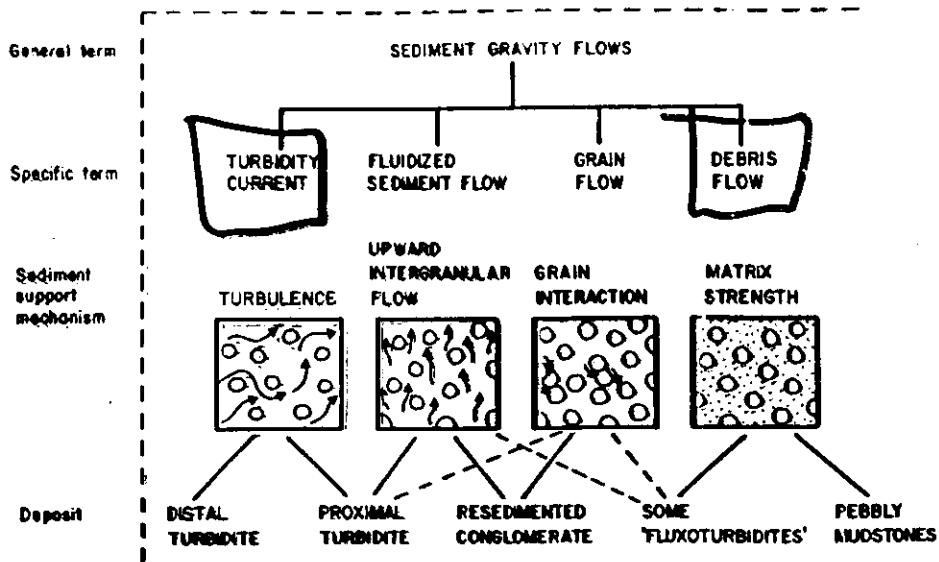


Turbulent vortices at head are sufficiently fast to "lift" or mobilize granular material.

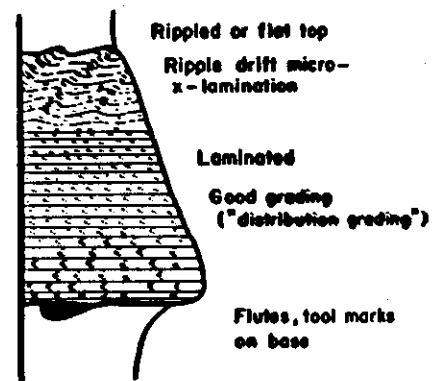
Debris flows



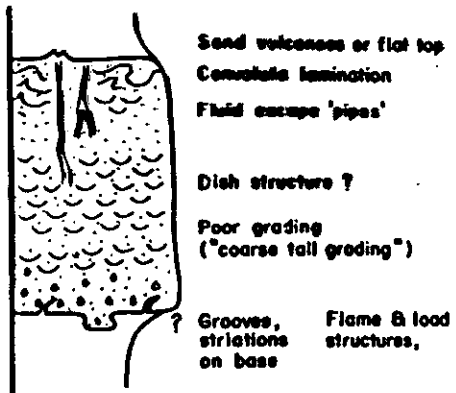
Slow (possibly shear-thinning) flow of dense mud + debris
Mud can be sufficiently dense to almost "float" boulders.



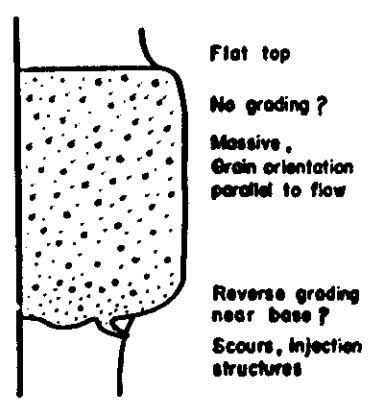
Turbidity Current



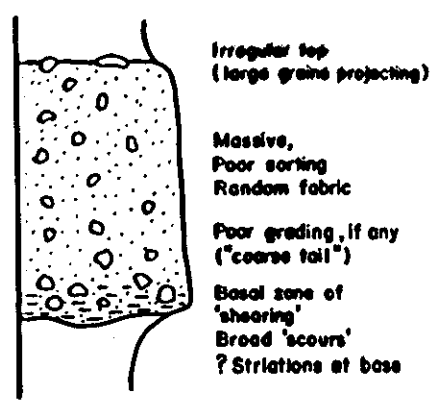
Fluidized Flow



Grain Flow



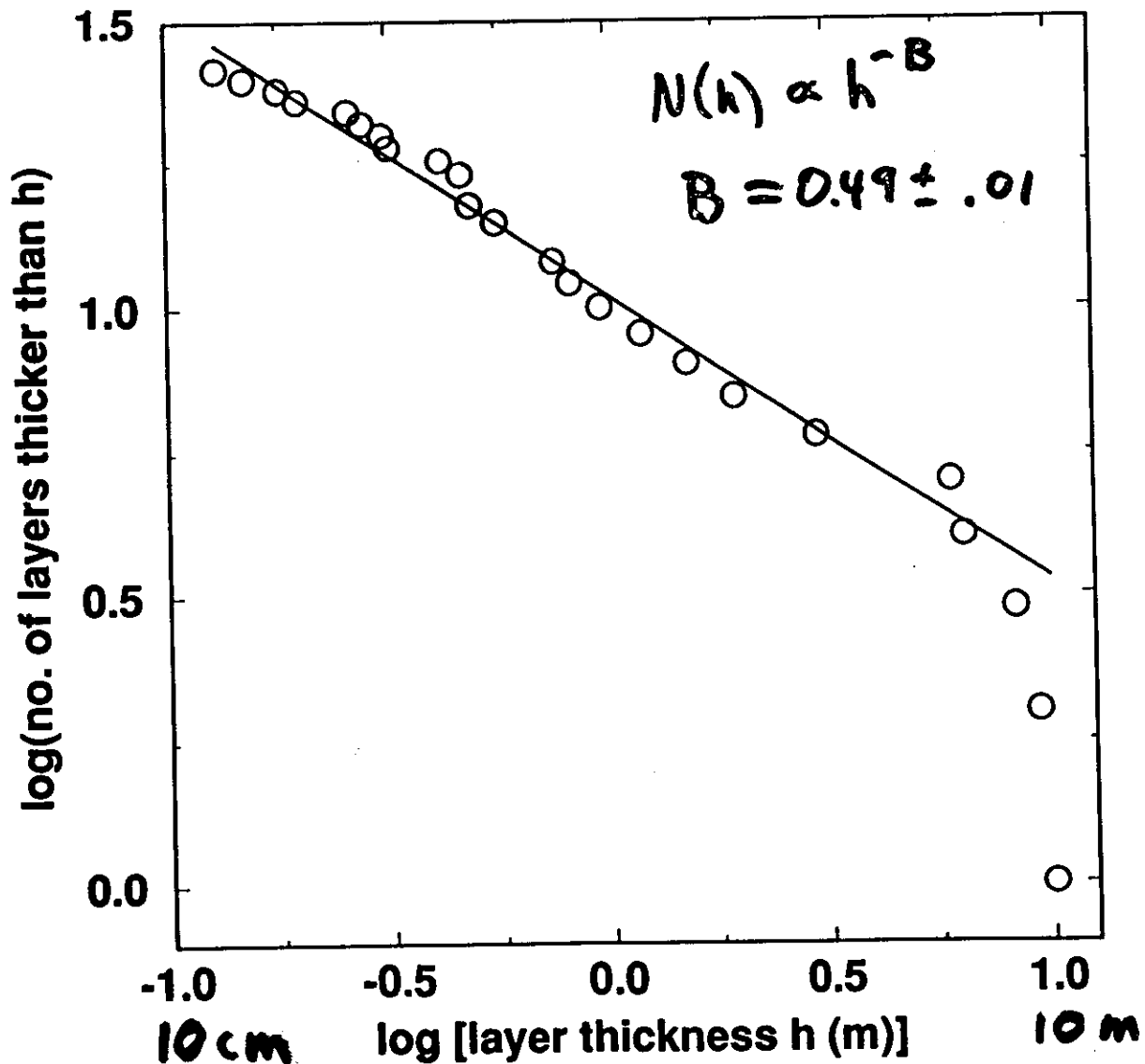
Debris Flow



Middleton & Hampton, 1976

In the same sedimentary sequence
where $B_{\text{turb}} = 1.39$, we find...

24 Debris flows, SE Calif

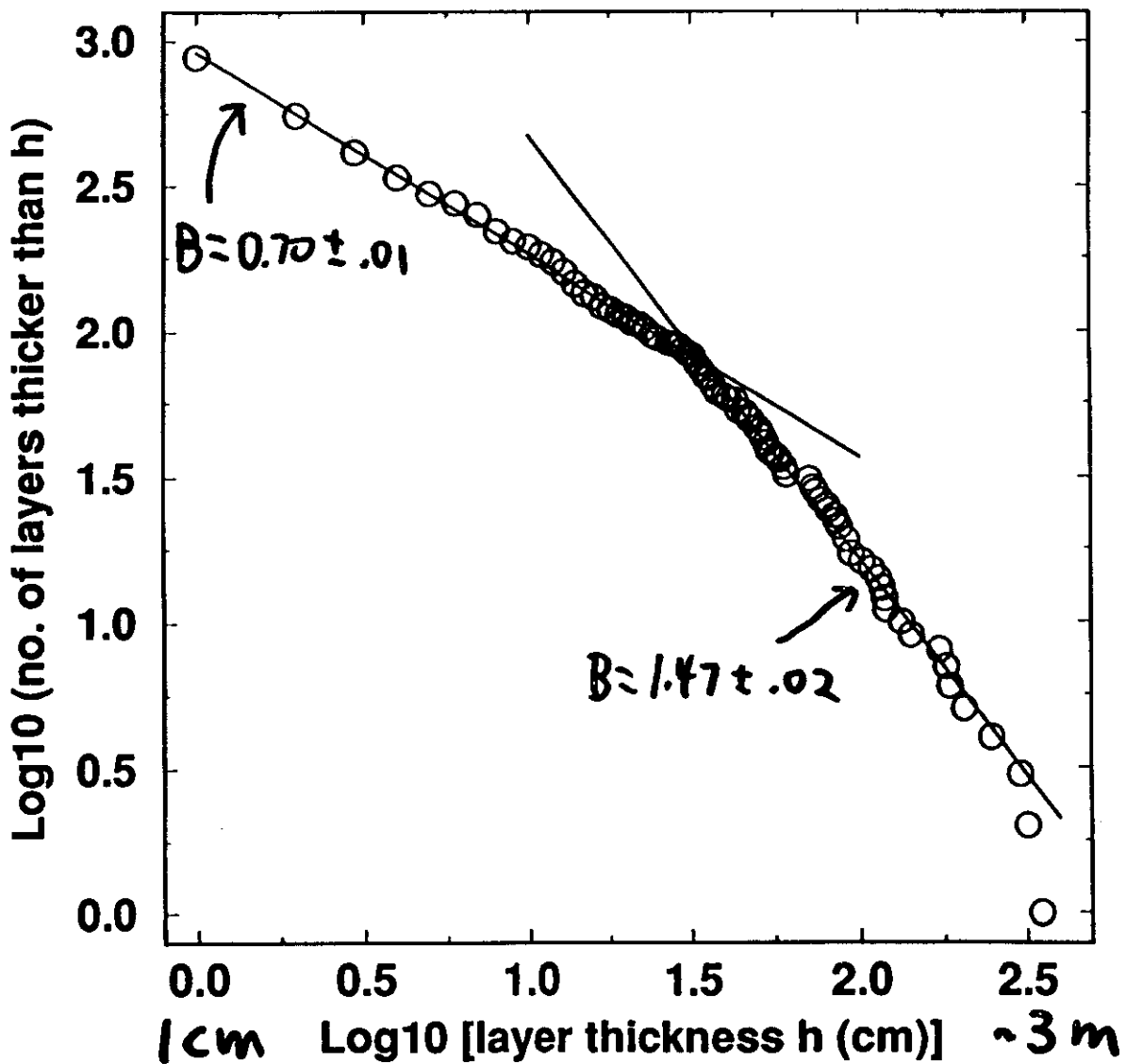


878 layers

Cape fold belt (Karoo), South Africa

Continental subduction zone, ~.25 billion years old.

Karoo turbidites (878)

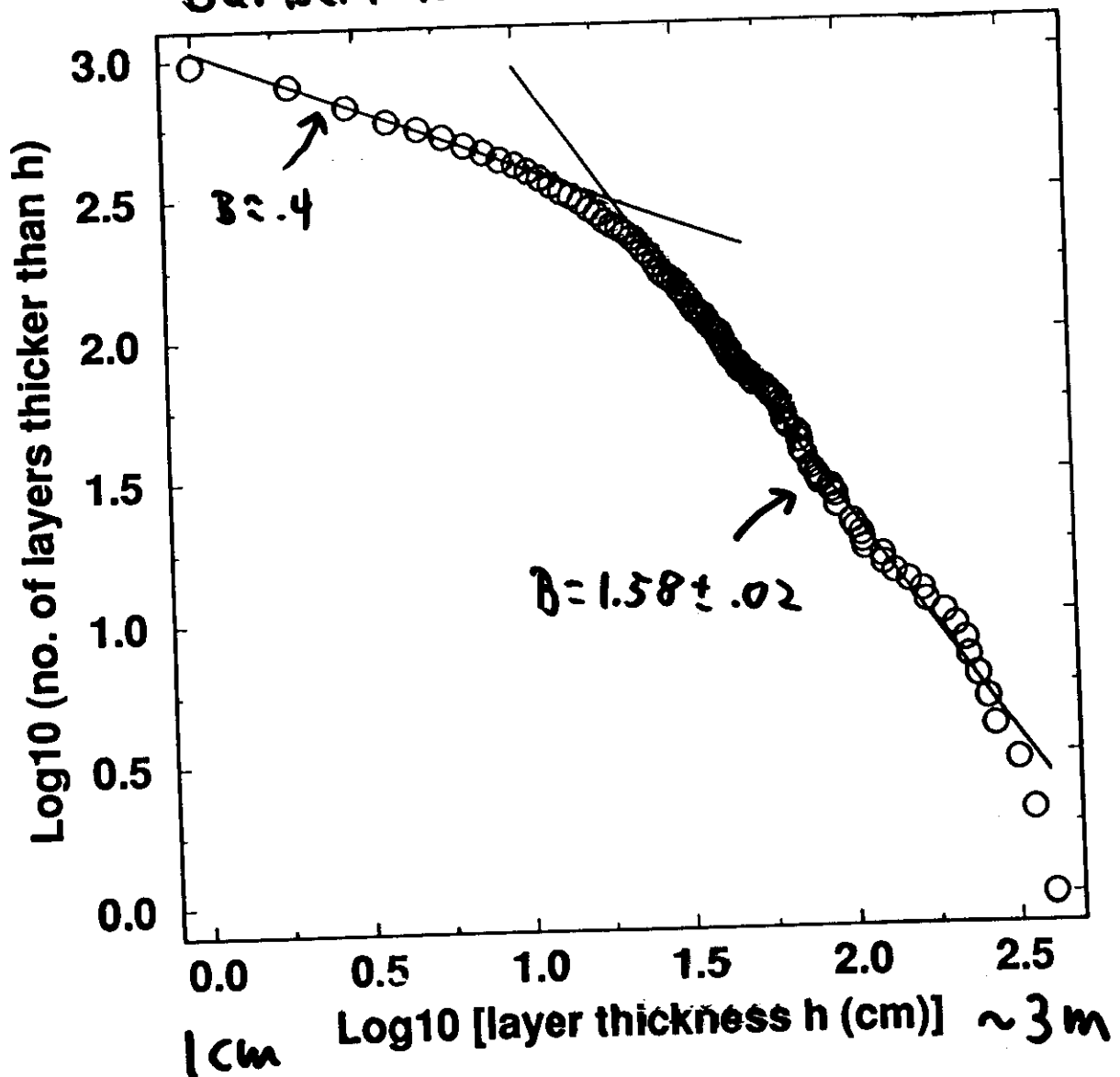


962 layers

Northern South Africa (Barberton)

rift basin, 3.5 billion years old

Barberton turbidites (962)



Some scaling and dimensional analysis

Since $N(h) \propto h^{-B}$

we may define the frequency distribution

$$p_h(h) \propto h^{-B-1}$$

Define

Volume of sedimentation event = V

deposition area = S

$$V = Sh$$

Assume $h \propto V^\alpha$ or $S \propto V^{1-\alpha}$

$\alpha = 1/3 \Rightarrow$ self-similar areal spreading

$\alpha = 2/3 \Rightarrow$ self-similar channelized flow

$\alpha = 1 \Rightarrow$ no spreading

The use of the apparent coefficient of friction H/L_T to characterise sturzstrom behaviour has invariably resulted in a great deal of data scatter (see e. g. Fig. 6, after Scheidegger, 1973; Hsü, 1975), as has the use of the potential energy expended in the event (Howard, 1973; Lucchitta, 1978). This is not unexpected when measurements of the physical quantities involved are necessarily rather approximate, but it may also indicate that friction coefficients and energy expenditure may not, at this stage, be appropriate variables for characterising and understanding sturzstroms.

The ingenious "simulation" by Hsü (1975) of the Elm sturzstrom suggests an alternative approach to the mechanics of debris streams. Hsü found that by using a bentonite — clay suspension, which can resist low shear stresses but flows as a fluid at higher shear stresses, he was able to reproduce, to kinematic model scales, the geometry and motion of the Elm event. This suggests that sturzstroms may flow at high shear stresses and become rigid when shear stresses reduce. Hsü (1975) also found that the height of the initial fall of his clay suspension did not affect the motion or extent of the

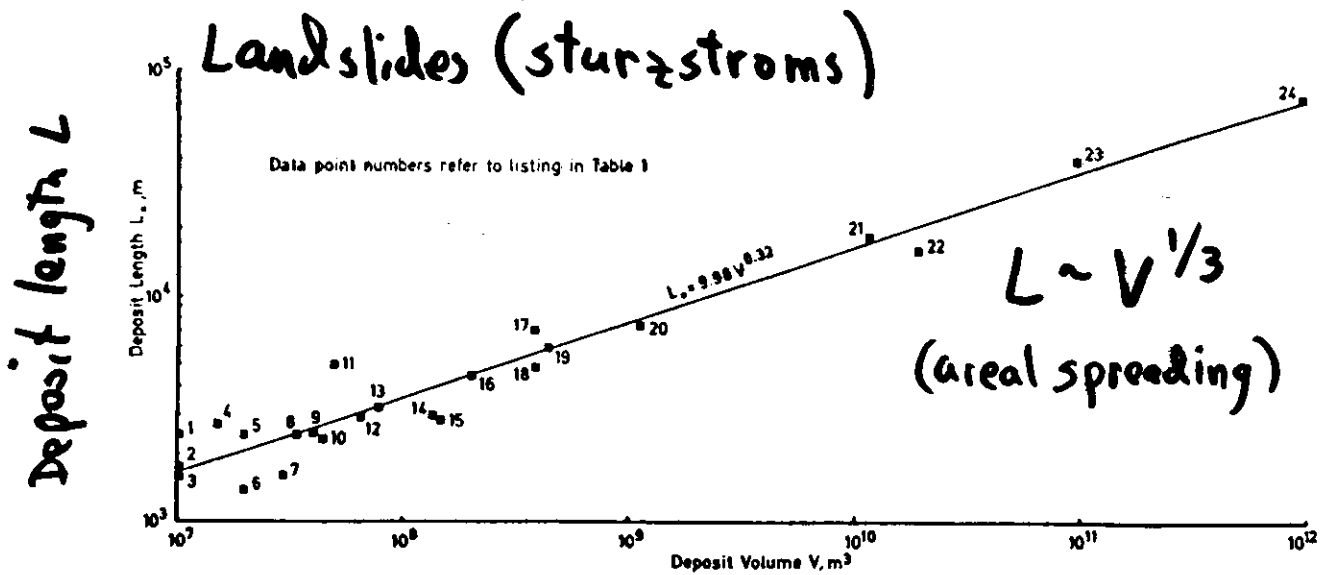


Fig. 1. Deposit length L_s (m) plotted against deposit volume V (m^3)

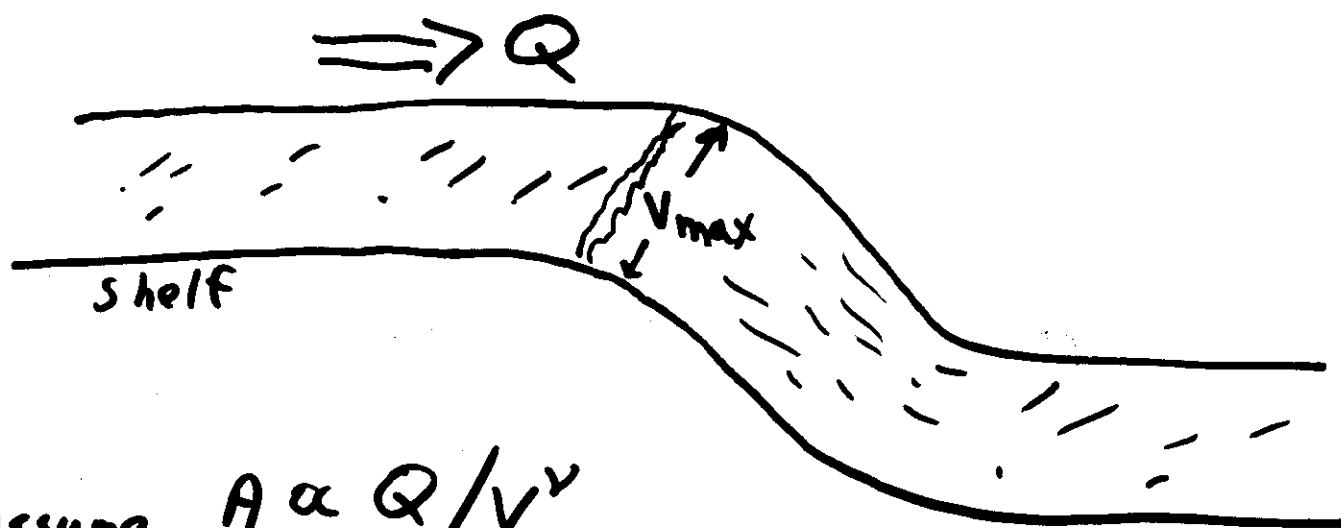
model deposit; this suggests that the areal extent of the deposit was related only to the volume of material involved, provided that the stresses were high enough to fluidise it, and that the height and kinetic energy of the fall did not significantly affect the final deposit characteristics. If this were also true for sturzstroms, then the inclusion of fall height in behaviour plots would merely cause data to scatter, rather than giving any insight into processes;

Davies, 1982

From $h \propto V^\alpha$, the volume frequency distribution is

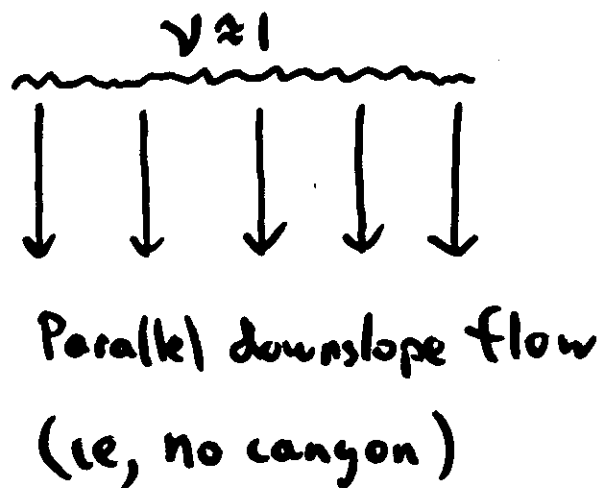
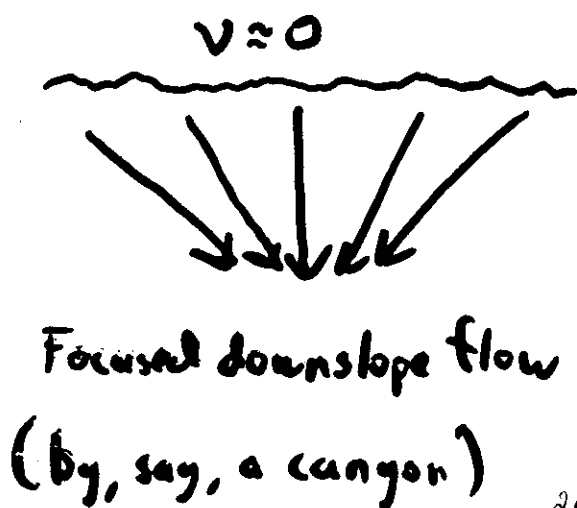
$$\rho_V(V) = A V^{-\alpha B - 1}$$

The prefactor A depends on the total volume flux Q to a shelf break of system size V_{\max} .



Assume $A \propto Q / V_{\max}^\nu$

- c.e. 1.) (Frequency of events of size V) $\propto Q$
2.) V specifies geometry of transport downslope



The flux Q is related to the event-size distribution by

$$Q = \int_{V_{\min}}^{V_{\max}} V f_V(V) dV$$

$$\propto A V_{\max}^{1-\alpha B}, \quad V_{\min} \rightarrow 0, \quad \alpha B < 1$$

$$\propto Q V_{\max}^{1-\gamma-\alpha B}$$

Thus $1-\gamma-\alpha B = 0$

OR

$$\boxed{B = \frac{1-\gamma}{\alpha}}$$

$$(\gamma > 0)$$

For SE Calif turbidites and debris flows:

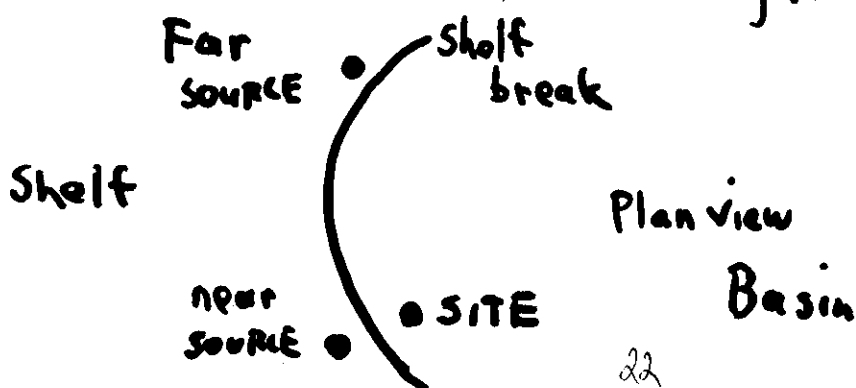
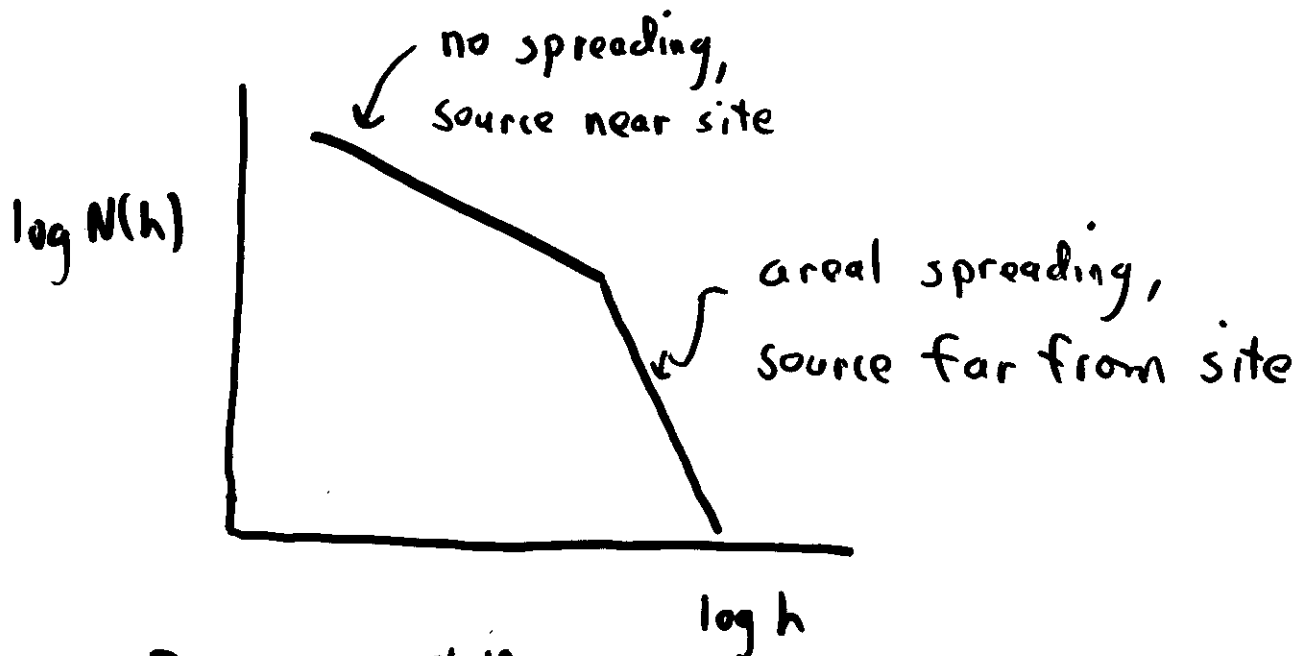
Assume $\nu \approx 1/2$, say. Then

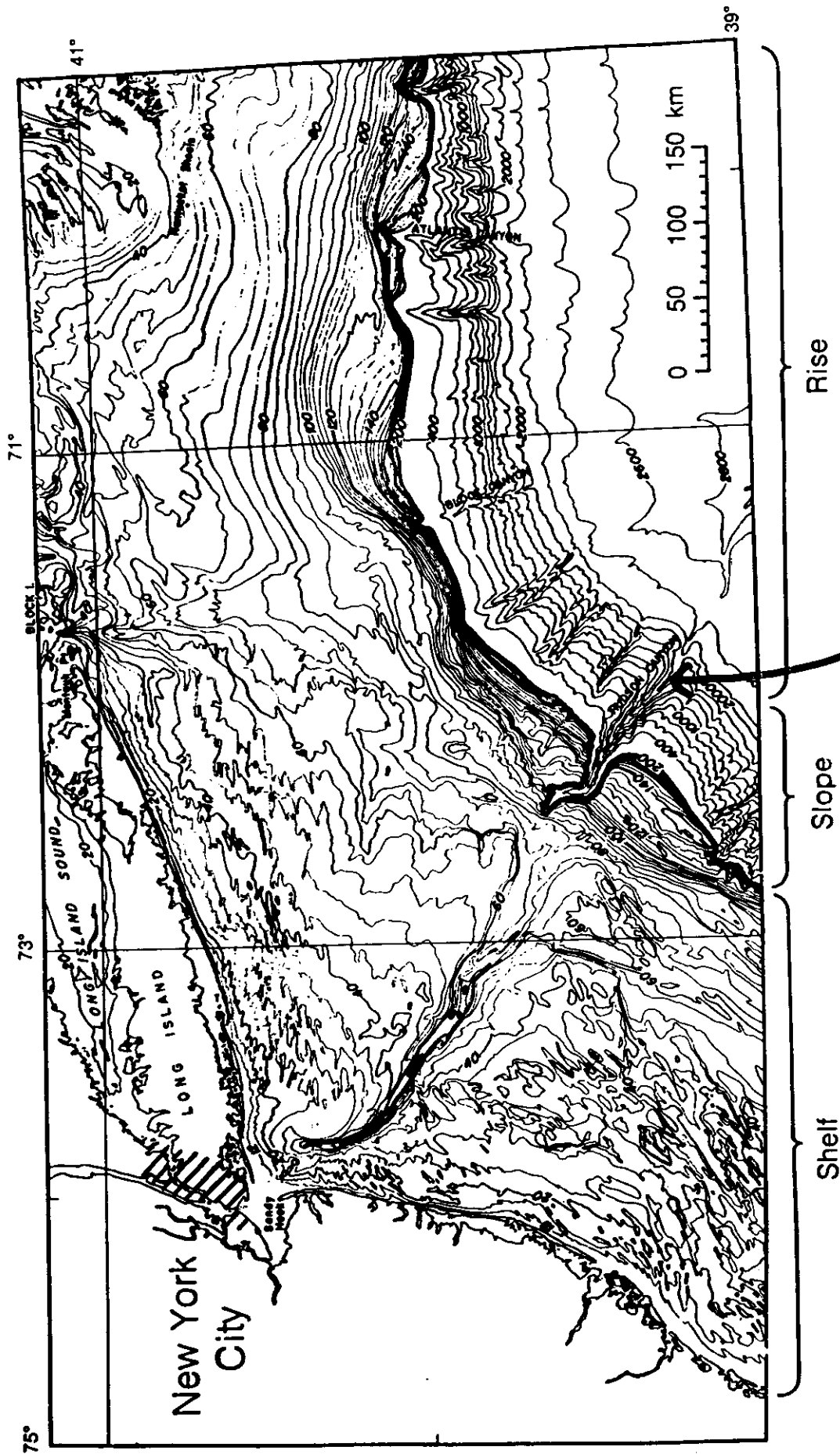
$B_{\text{turb}} \approx 1.4 \Rightarrow \alpha_{\text{turb}} \approx 1/3 \Rightarrow$ areal spreading

$B_{\text{debris}} \approx 1/2 \Rightarrow \alpha_{\text{debris}} \approx 1 \Rightarrow$ no spreading

For the crossover turbidites:

One possible interpretation is constant $\nu \approx 1/2$, and





Submarine canyon

Figure 10-31
Map of continental shelf, slope, rise, and Hudson Canyon off New York City.
[From K. O. Emery, Woods Hole Oceanographic Institution.]

Q. Can the power-law distribution of avalanche sizes be related to the morphological features of the continental slope?

A. Maybe. Some possible approaches:

1. Ask if the topography is fractally rough.

If so, perhaps the power law in avalanches is related to topographic "roughness".

2. Do "drainage" features on the slope satisfy power-law scaling?

3. Quantify force(s) that cause slope failure. Do these imply power-law avalanches?

Orange, Anderson, & Breen, 1994

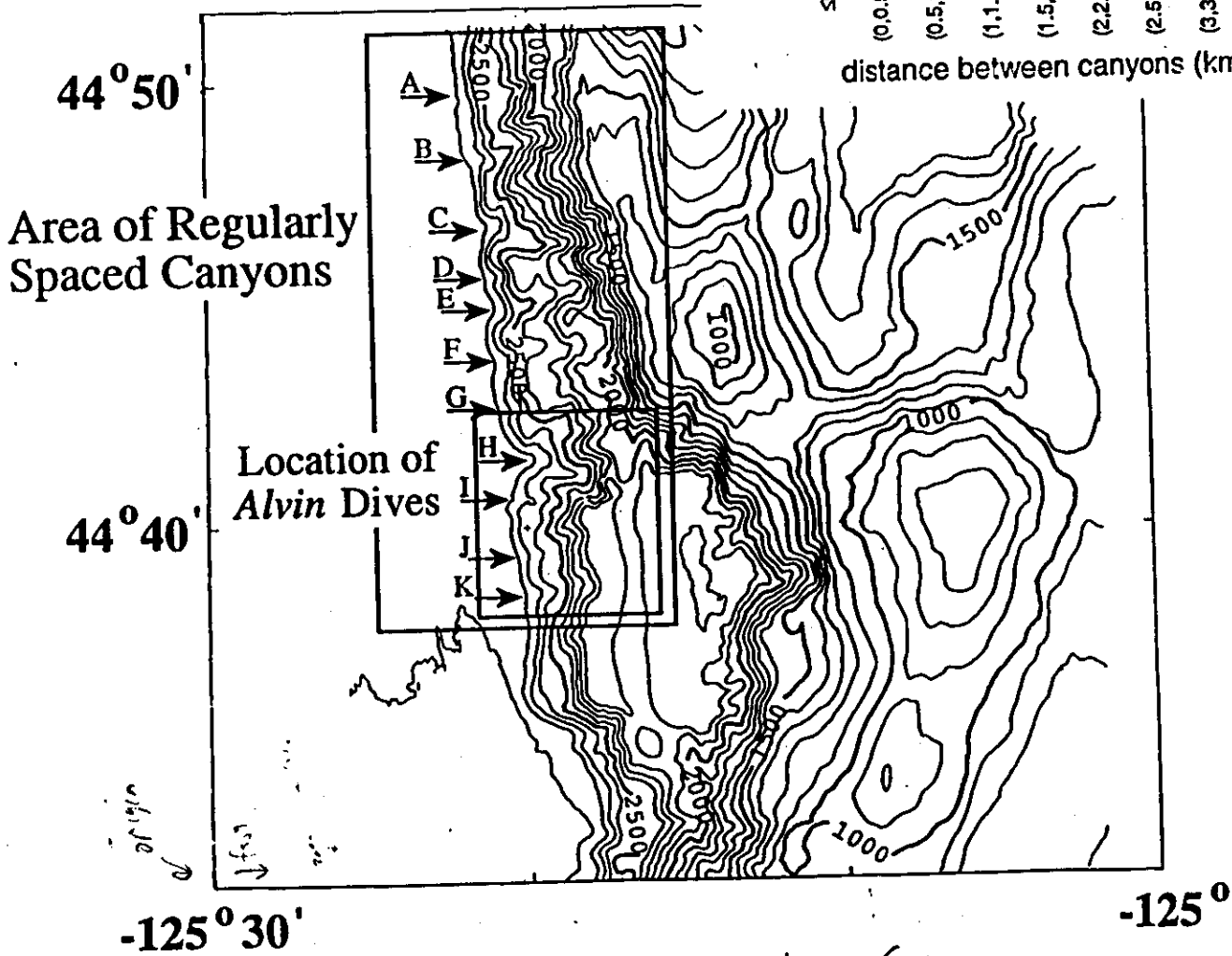
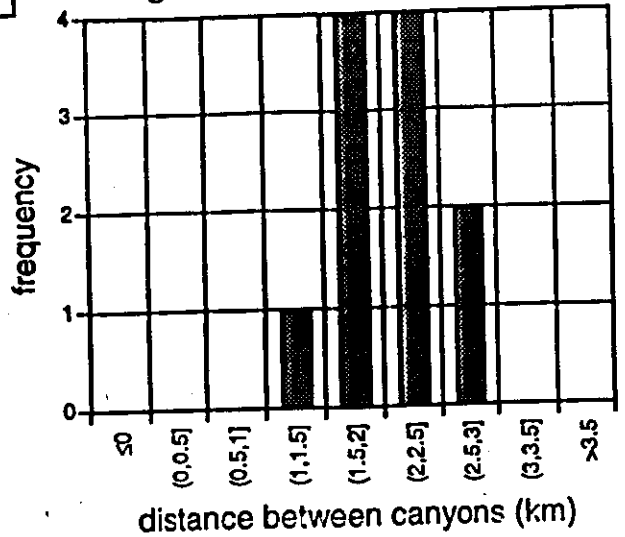
b

Offshore Oregon
Cascadia accretionary complex

a "Headless" canyons

-125° 30'

Oregon Canyon Spacing (n=12)

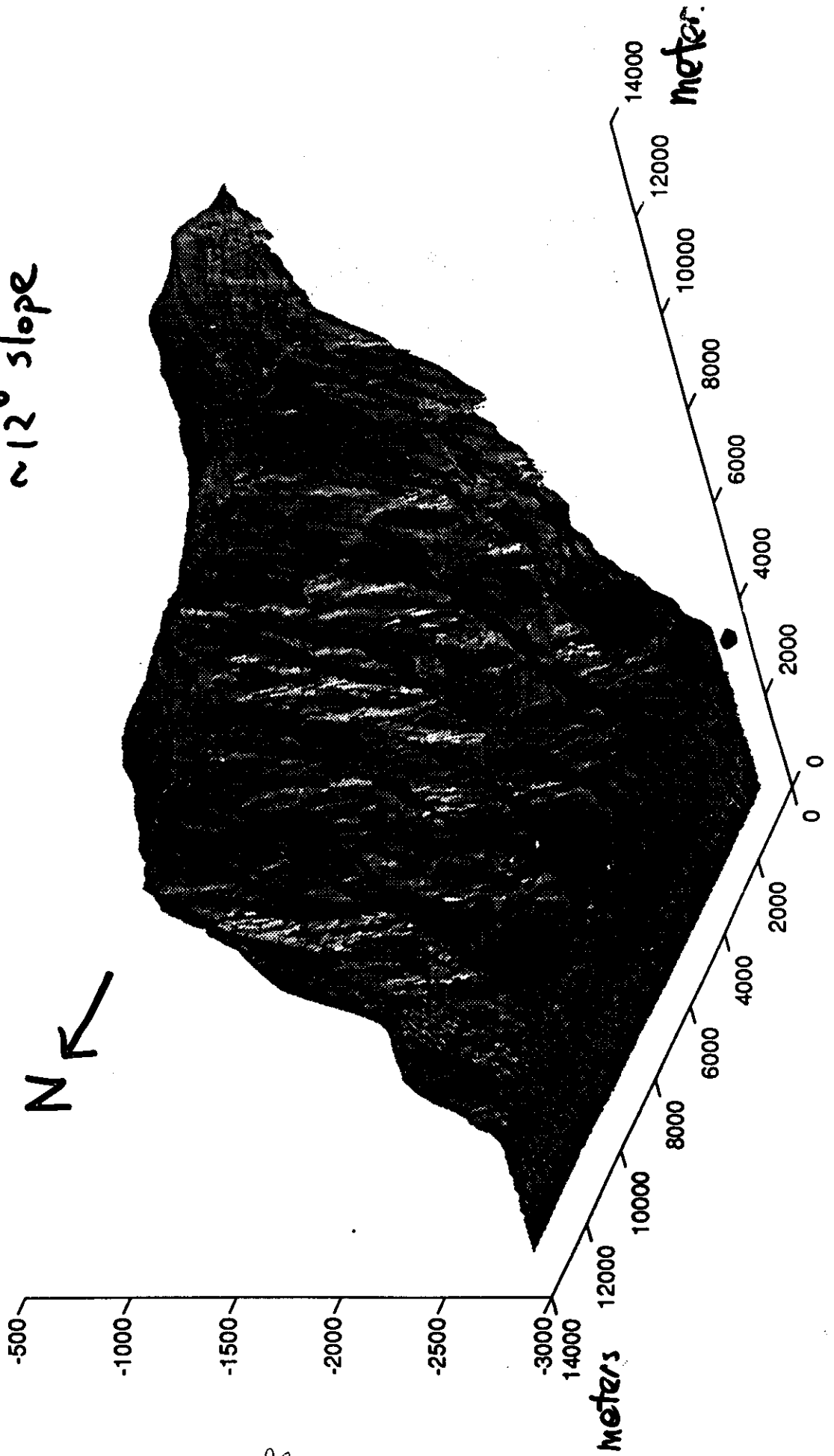


A scale would be helpful.

10 min lat = 10 nmi!

Orange
Fig 10, b.

$\sim 12^\circ$ slope



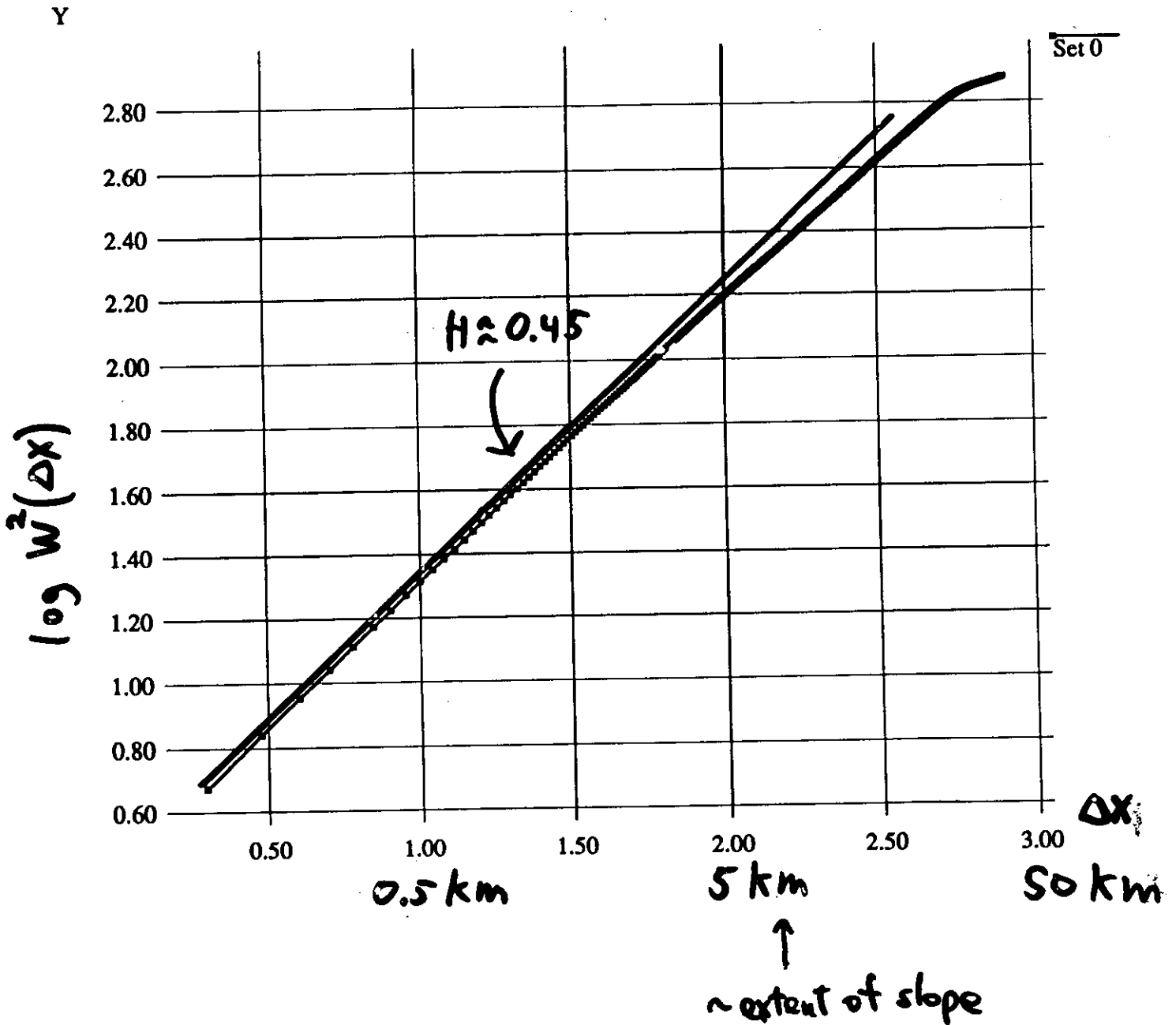
26

Average upslope width as function of i, j th

$$W(\Delta x) = \left\langle \left(\langle z^2 \rangle - \langle z \rangle^2 \right)^{1/2} \right\rangle_{[x, x+\Delta x]}$$

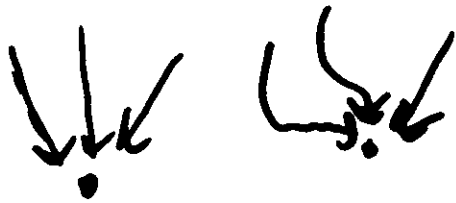
$$\sim (\Delta x)^H$$

whole_grid_upslope



"Drainage" features of the slope (à la Brice et al.)

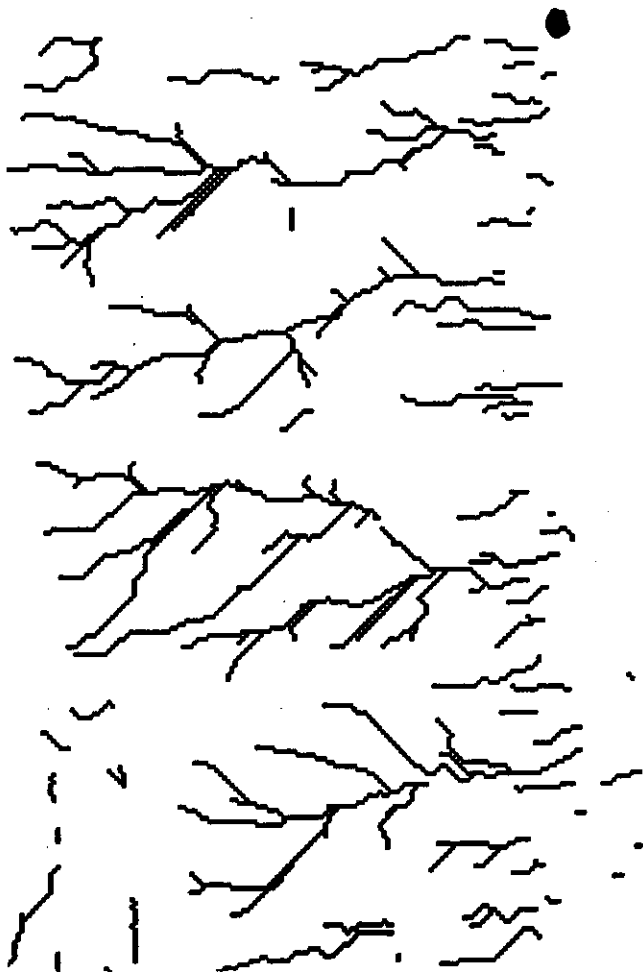
Imagine that each "pixel" of the bathymetric map collects any sand that would fall into it if the slope above were unstable.



Each pixel may then be assigned a drainage area, or "avalanche potential".

A map showing only those pixels with the greatest avalanche potentials forms a dendritic network.

And the avalanche potentials satisfy a power-law distribution.

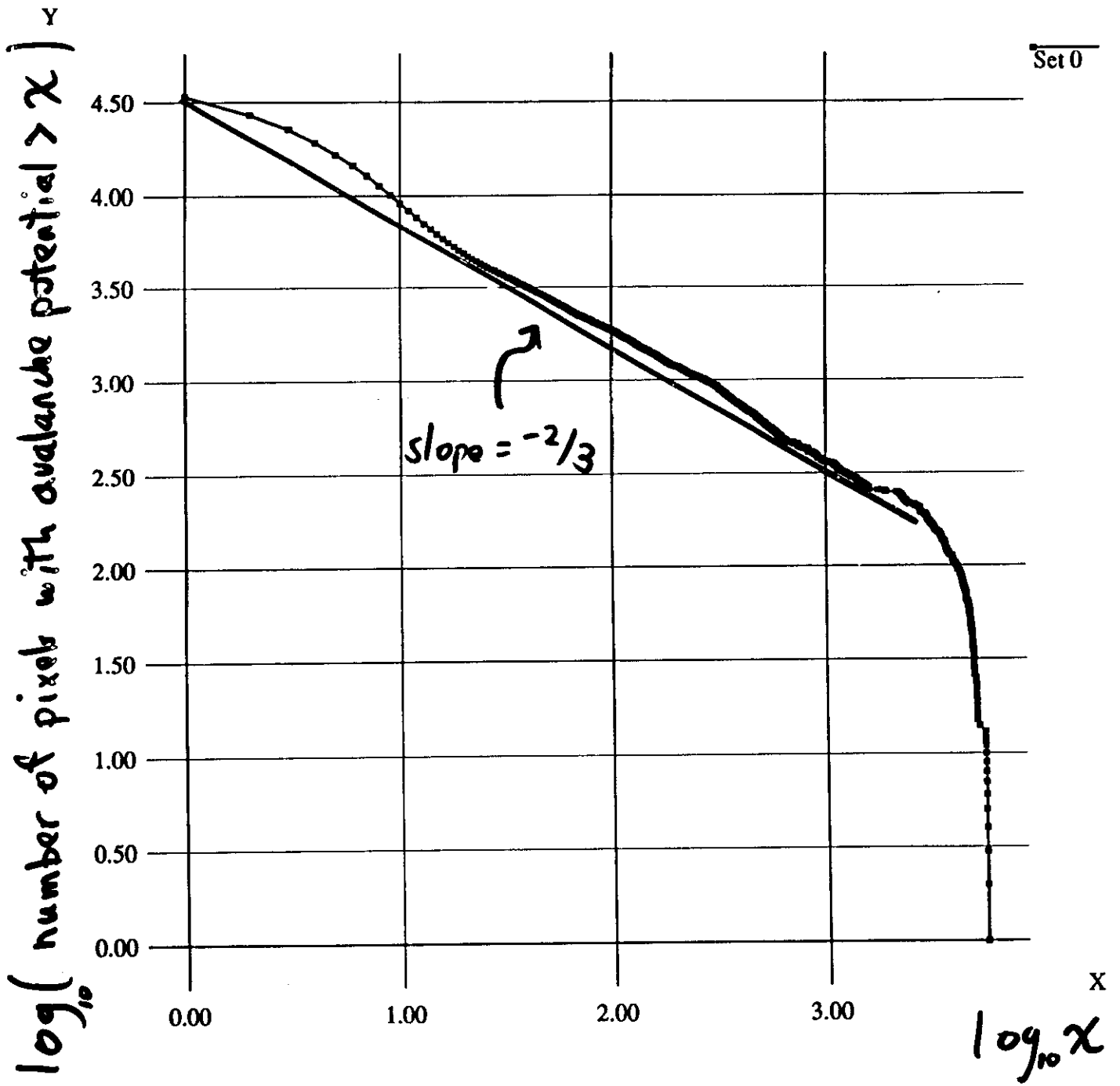


DOWN
SLOPE

SIZE: 13 km x 9 km

N ←

Cumulative distribution of avalanche potentials

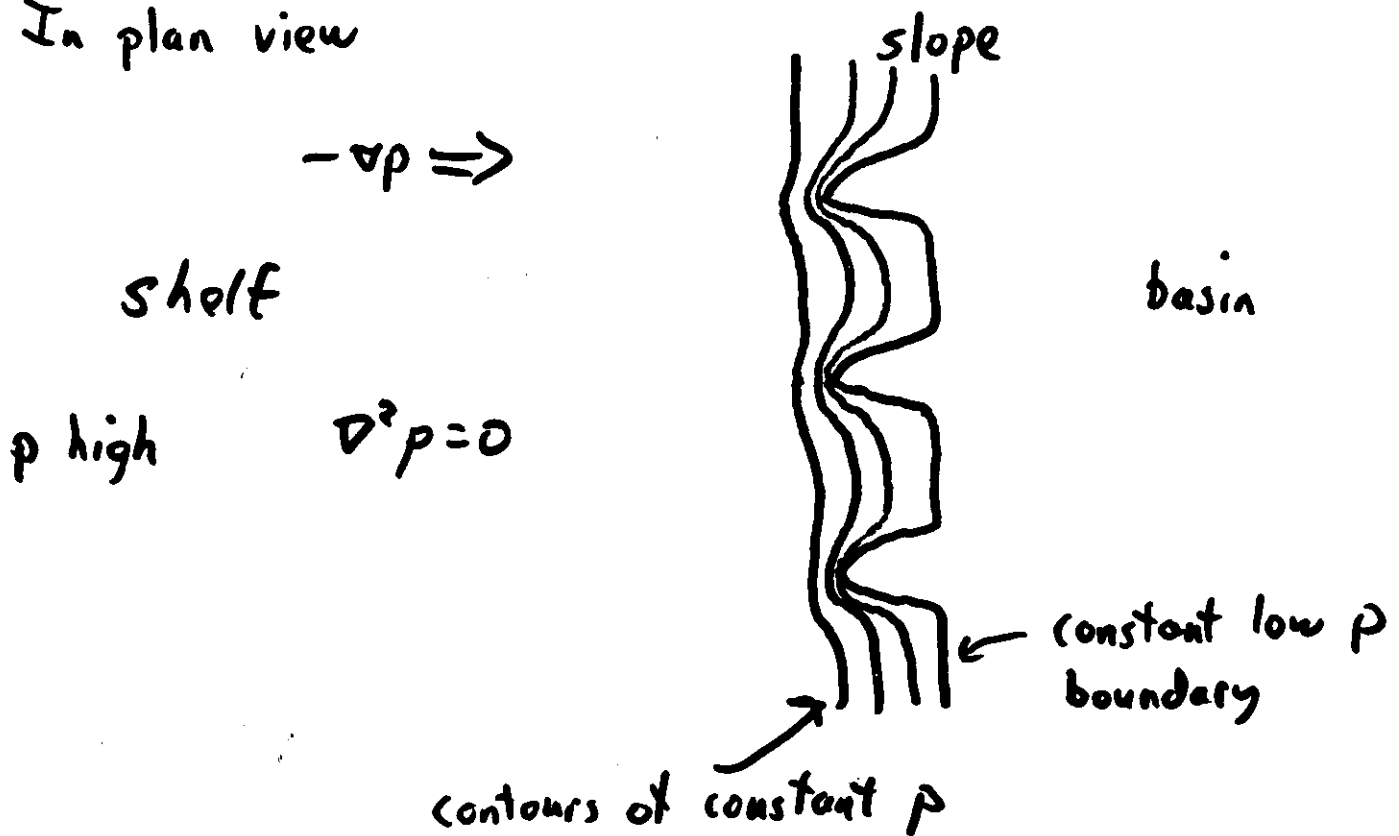


A dynamical model

Assume that the primary destabilizing force is the seepage force $-\vec{\nabla}p$.

i.e., when $|\hat{\nabla}p| > |\hat{\sigma}p|_c$, The slope fails.

In plan view



- Solve $\nabla^2 p = 0$ in bulk
- Evaluate $\vec{\nabla}p|_{\text{boundary}}$
- What is the distribution of $\vec{\nabla}p|_{\text{boundary}}$

Conclusions

1. There are lots of power-law turbidite deposits.
2. We have the beginnings of some testable scaling laws. (by 3-D seismic imaging)
3. The shelf-slope-turbidite system provides nice opportunities to
 - relate dynamics to geometry
 - better understand slowly forced, rapidly relaxing systems

