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**SMR. 758 - 32**

**SPRING COLLEGE IN CONDENSED MATTER  
ON QUANTUM PHASES  
(3 May - 10 June 1994)**

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**METAL-INSULATOR TRANSITION**

**"Experimental Highlights"**

**Part II**

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These are preliminary lecture notes, intended only for distribution to participants.

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IV

## HIGHLIGHTS OF THERMODYNAMIC MEASUREMENTS

C = specific heat of electrons

 $\chi$  susceptibility ———

IV 1

3n Fermi liquid:

$$C = \gamma T$$

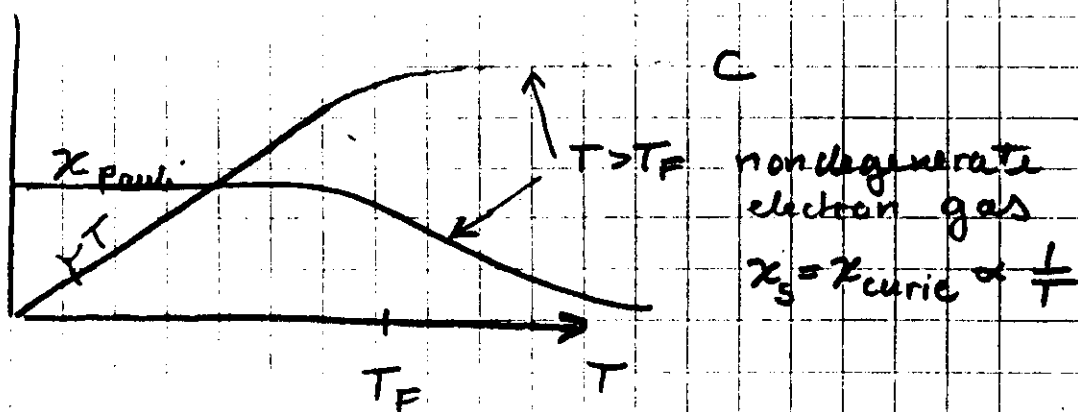
$$\gamma = \frac{1}{2} \pi^2 n k_B / T_F$$

$$\chi_s = \chi_{\text{Pauli}} = \frac{3n \mu_B^2}{2k_B T_F} \quad \text{spin susceptibility}$$

$$\chi_{\text{or}} = - \frac{n \mu_B^2}{2k_B T_F} \quad \text{orbital susceptibility}$$

ESR - measurements probe only  $\chi_s$ 

static magnetization measurements by SQUID or by other devices measure  $\chi_{\text{total}} = \chi_s + \chi_{\text{or}}$ ,  $\chi_s$  &  $\chi_{\text{or}}$  are hard to separate



TV 2 Near MIT

Motivation for  $C$  &  $\chi$  measurements near MIT came from the critical exponent puzzle in Si:P and from the predictions of scaling theories:

- In general universality class the scaling theory predicts quite strong increases of  $\gamma$  &  $\chi_s$  toward lower temperatures near MIT. Also,  $\gamma$  &  $\chi_s$  should behave critically at the transition  $n_c$ .
- On the other hand, in SO-universality class there should be neither  $T$ -increase nor critical behavior in  $\chi_s$ .

Notice: There is no clear prediction for  $\chi_{tot}$  near MIT. It is better to measure  $\chi_s$  by ESR, than  $\chi_{total}$  by SQUID, because the separation of  $\chi_{or}$  and  $\chi_s$  relies on the assumption that  $\chi_{or} = \text{constant}$  thru MIT and as a function of  $T$ .

Notice: In the insulating phase for noninteracting "free" localized spins we expect:

$$C = 0 !$$

$$\chi = \chi_{curie} = \frac{n \mu_B^2}{3k_B T} !$$

#### IV 2.1. Specific heat near MIT

Recent experimental results have been presented on page 45

At lowest temperatures:

$$- C \propto \gamma T \quad \text{and} \quad \gamma_{\text{eff}} = C/T$$

increases toward lower temperatures

-  $\gamma_{\text{eff}}$  increases also toward insulating phase, which has quite large specific heat.

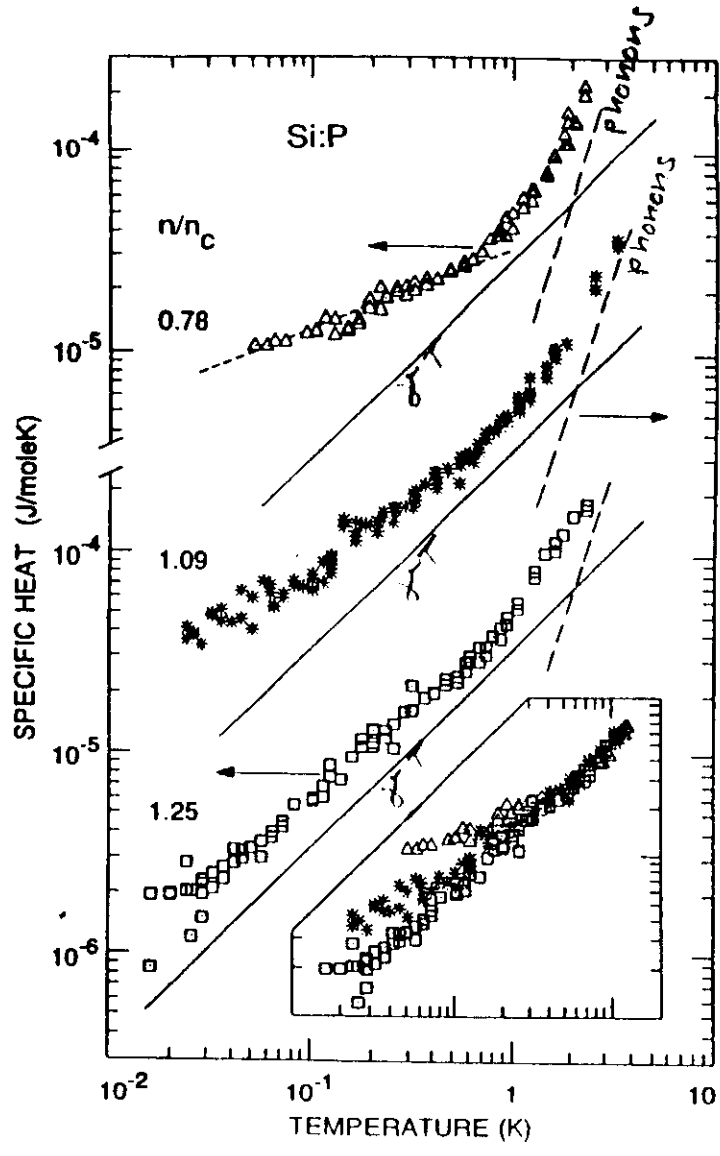
- In the insulating phase  $C \neq 0$

- In the high B-field measurements one can see a Schottky type specific heat peak.

The specific heat measurements are qualitatively in agreement with the scaling predictions of  $\gamma$ -enhancement.

Quantitative comparison is difficult!

Paalonen, Graebner, Bhatt & Sachdev PRL 63, 651 (1984)



- phonon specific heat  $\propto T^3$  appears at higher temperatures
- electron specific heat dominates the low temperature behavior

Lakner & Löhneysen PRL 63, 648 (1989)

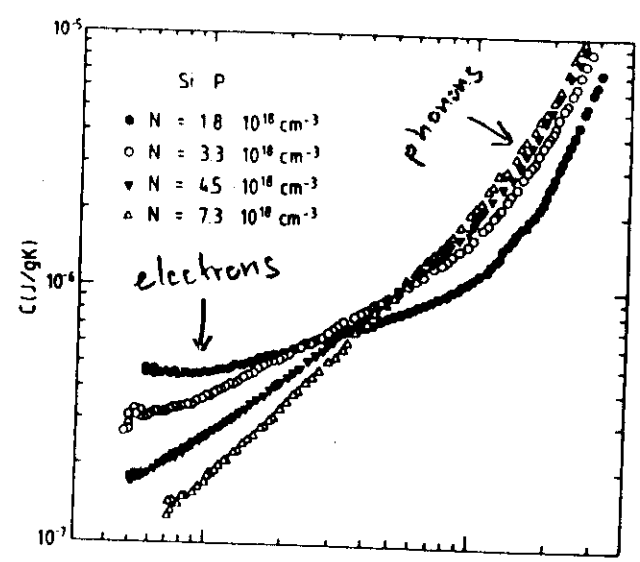
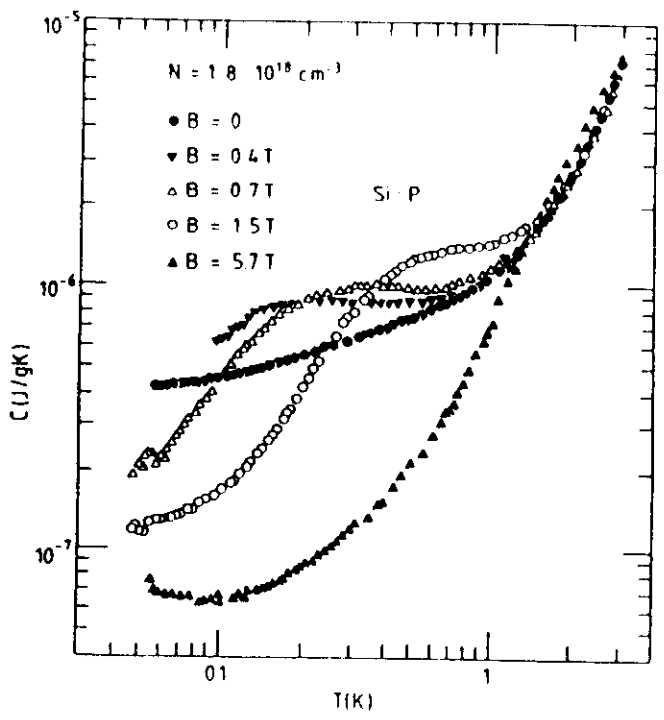


FIG. 3. Specific heat  $C$  in various magnetic fields  $B$  vs temperature  $T$  for one Si:P sample.

## IV 2.2.

Susceptibility measurements

Some of the recent measurements  
 on doped semiconductors (Si:P, Si:PjB,  
 these are  $\chi_s$  measurements by ESR)  
 and in an amorphous metal-semiconductor  
 alloy ( $\text{Nb}_x \text{Si}_{1-x}$ , SQUID measurement  
 of  $\chi_{\text{tot}}$ ,  $\chi_s$  is estimated by subtracting  
 the  $\chi_{\text{or}}$  "background")

— Near MIT, on both sides of  $n_c$ ,  
 the low temperature susceptibility

$$\chi_s(T) \propto T^{-\alpha} \quad \alpha < 1$$

quite universally:

in uncompensated Si:P ( $\mu < 1$ ?, general univ. class)  
 in compensated Si:PjB ( $\mu \approx 1$ , ?)  
 and in  $\text{Nb}_x \text{Si}_{1-x}$  ( $\mu = 1$ , so universality class)

—  $\chi(T=0) \sim \infty$  already for  $n > n_c$   
 $\Rightarrow$  no critical behavior at  $n_c$

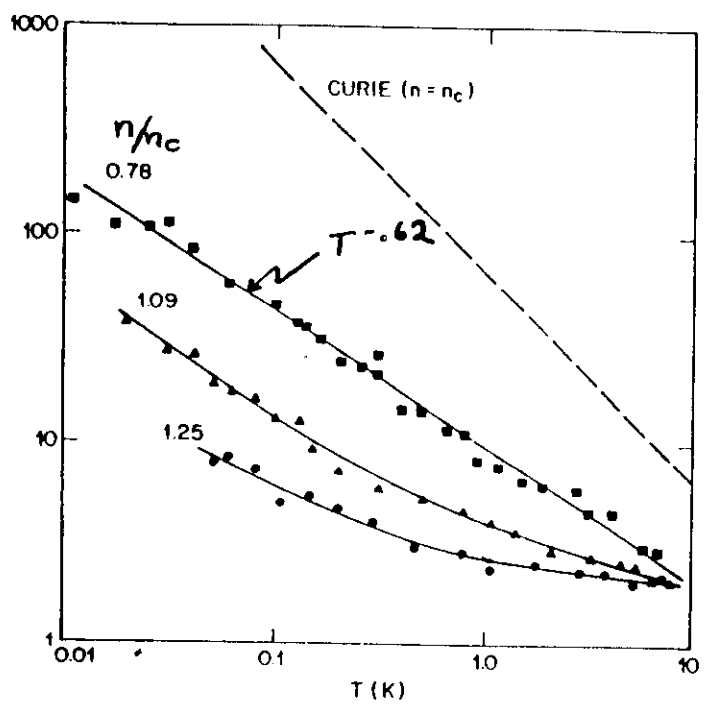
—  $\chi_{\text{comp}} > \chi_{\text{uncomp}}$

This is in contradiction to the  
 predictions of scaling theory

—  $\chi$  of  $\text{Nb}_x \text{Si}_{1-x}$  behaves  
 very similarly to  $\chi$  of Si:P.  
 $\text{Nb}_x \text{Si}_{1-x}$  is in so-universality class.  
 This contradicts also scaling  
 predictions.

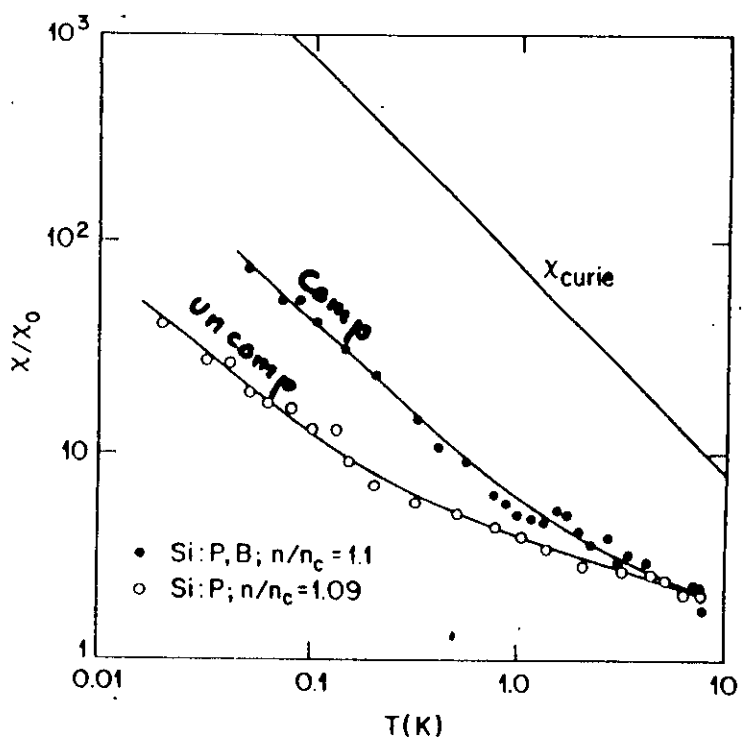
Si:P:

Paalonen, Sachdev, Bhatt & Ruckenstein  
PRL 57, 2061 (1986)



Si:P; B

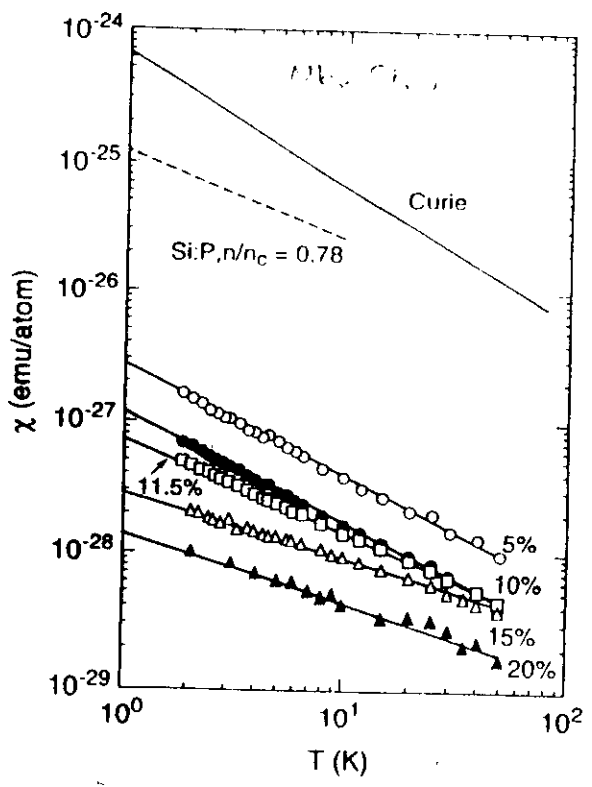
Hirsch, Holcomb, Bhatt & Paalonen, PRL 58, 1418 (1992)



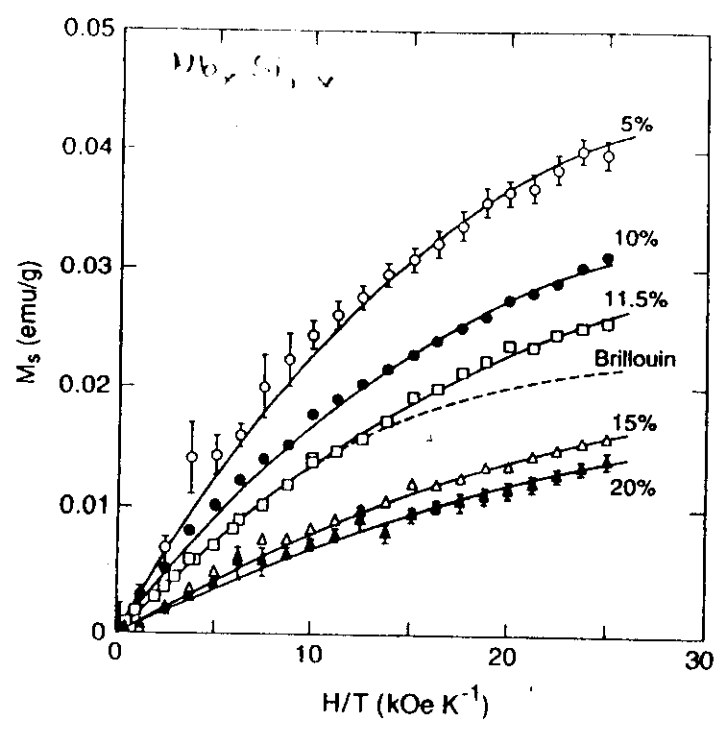
Nb\_x Si\_{1-x}

Allen, Paalonen & Bhatt Europhys Lett. 21, 927 (1973)

χ versus T



Magnetization as a function of magnetic field



### IV 3 INSULATING PHASE OF Si:P

- Random Heisenberg Antiferromagnet

–

$$H = \sum_{i,j} J(r_{ij}) \vec{S}_i \cdot \vec{S}_j$$

–

$$J(r) = 1.636 (r/a_B^*) e^{-2r/a_B^*} R_y^*$$

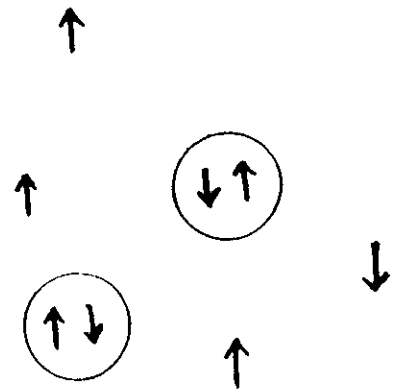
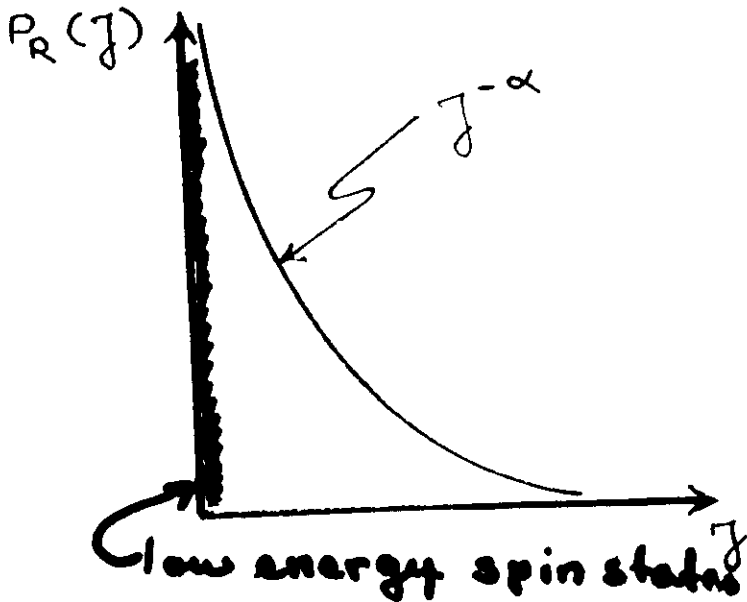
– Not a spin-glass!!

- Elegant solution by BHATT and LEE

– Remove strongest coupled pairs

– Removed pairs renormalize  $J$  of the remaining pairs

- Renormalized J-distribution





## INSULATING PHASE OF Si:P

### Random Heisenberg Antiferromagnet

- Renormalized J-distribution

- $P_R(J) \propto J^{-\alpha}$

- $\alpha \approx .62$  for  $n \lesssim n_c$

- $\chi \propto T^{-\alpha}$

- $\gamma = C/T \propto T^{-\alpha}$

- Wilson ratio

$$\left(\frac{\chi}{\chi_0}\right) / \left(\frac{\gamma}{\gamma_0}\right) = \frac{\pi^2}{3(1-\alpha)/n^2} \approx 10$$

- This model explains in the insulating Si:P:

- Susceptibility; K. Andres et al

- High field magnetization; M. Sarachik et al

- ESR linewidth; Murayama et al Paalanen et al

- $T_1$  of  $^{29}\text{Si}$  NMR; Paalanen et al Holcomb et al

IV 4 Local Moment Formation in Disordered Metal

- Scaling theories fail to produce enough magnetism near MIT
- In the insulating phase, just below  $n_c$ , there are local magnetic moments in the disordered system. The disordered metallic system just above  $n_c$  might also have local moment formation
  - rare sites far away from neighbours
  - Low Kondo Temperature due to low local density of states

Milovanovic, Sachdev & Bhatt PRL 63, 82, 1989  
 Bhatt & Fisher PRL 68, 3072 (1992)  
 Dobrosavljevic et al 69, 1113 (1992)

IV 5Two Fluid Model

The coexistence of local moments and delocalized electrons can be phenomenologically modelled by so called "two fluid model".

## TWO FLUID MODEL

of localized moments and free electrons ( $n > n_c$ )

Interaction between localized moments and itinerant electrons is weak

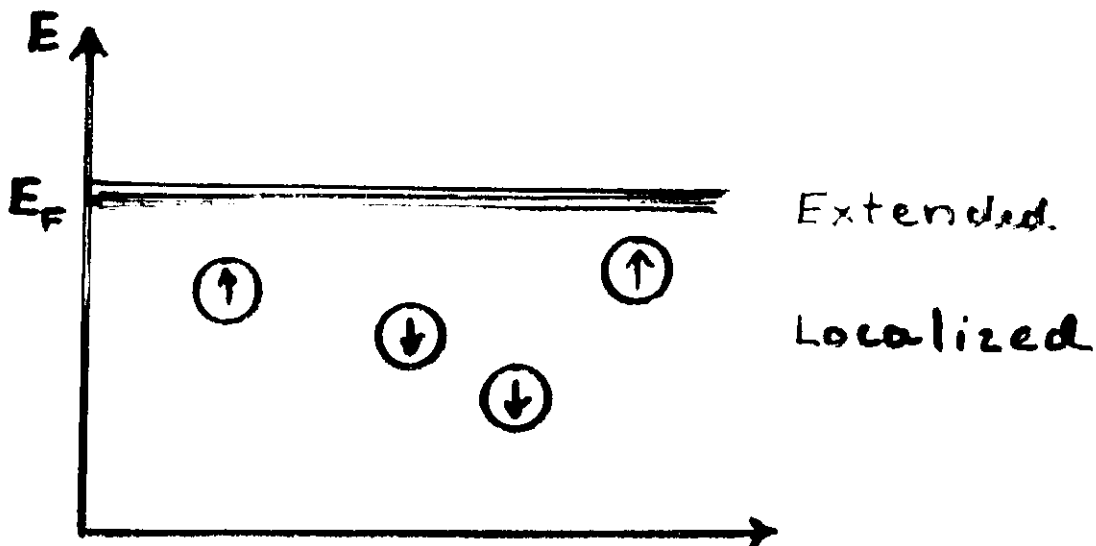
In first order the interactions between local moments described by Bhatt and Lee model

In first order the free electrons described by the Fermi-liquid theory

$$\chi_0 = m^*/m + \frac{\pi^2}{3(1-\alpha)\ln 2} \left(\frac{T}{T_0}\right)^{-\alpha}$$

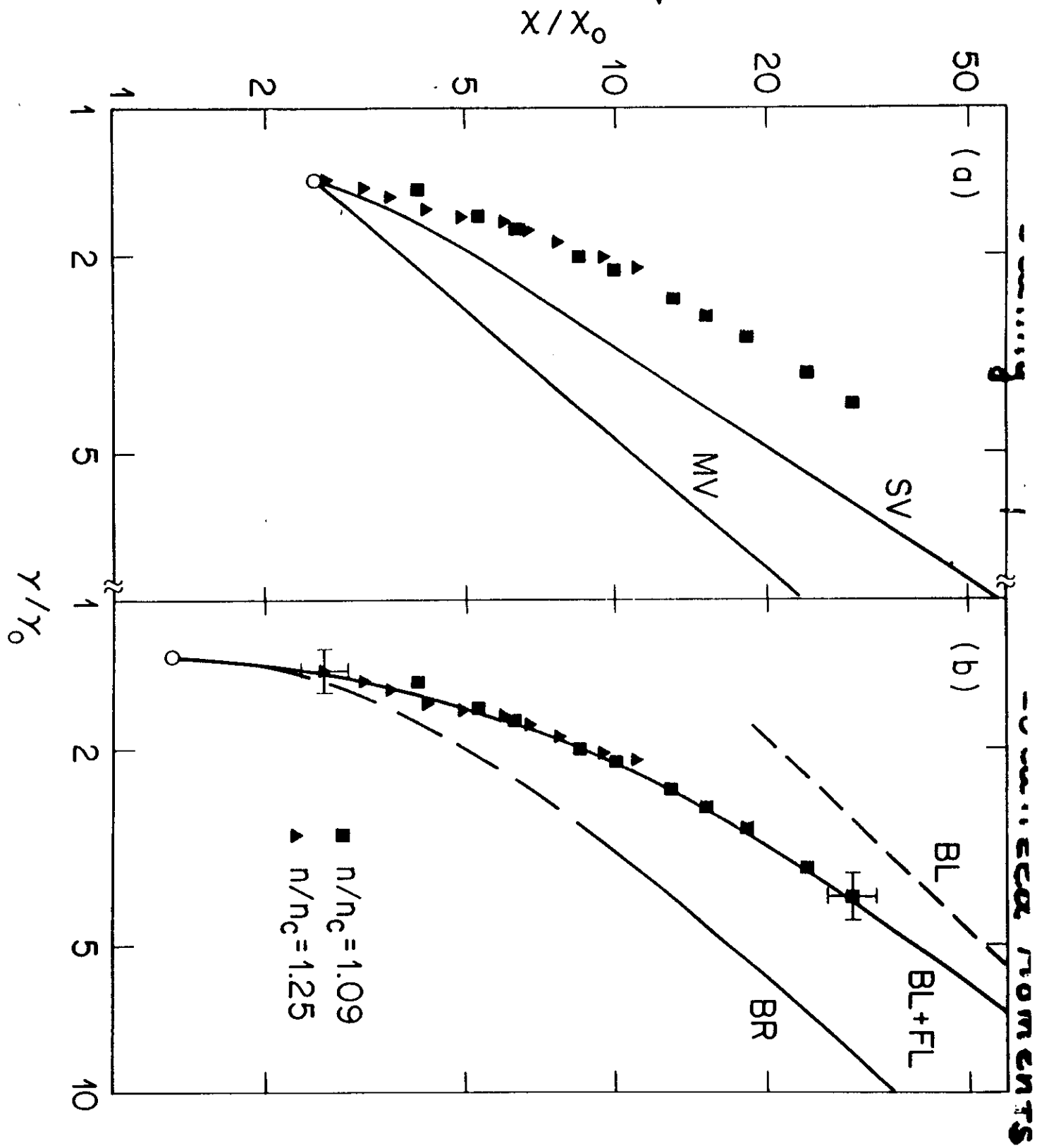
$$\chi_0 = m^*/m + \left(\frac{T}{T_0}\right)^{-\alpha}$$

$T_0$  only adjustable parameter containing the number of localized moments!!



$\chi$  & C measurements in Si:P: PRL 61,597

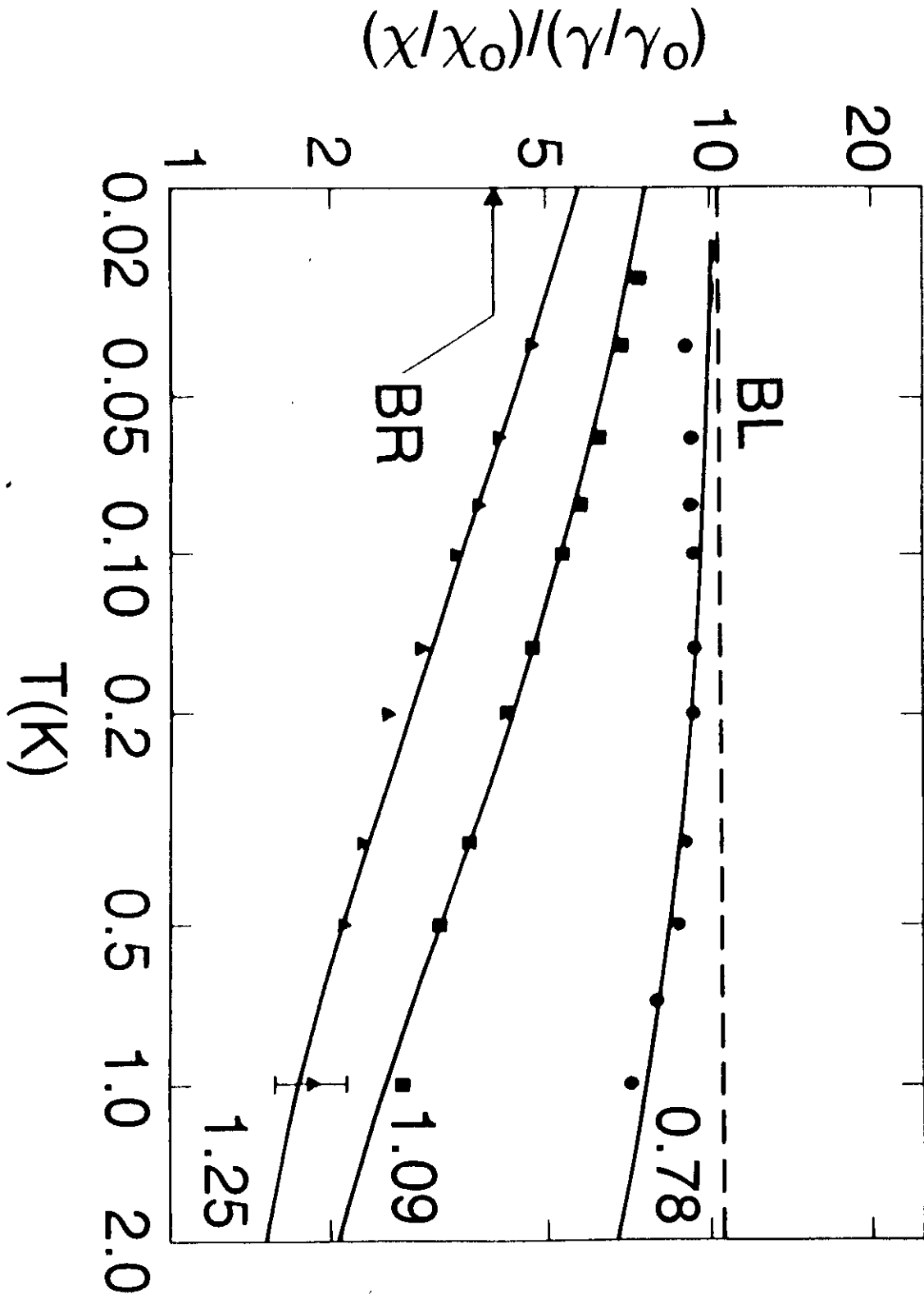
Test of scaling theory and  
two fluid model with local moments near H  
Two fluid model on right is better.



(53)

Wilson ratio for Si:P near MIT  
[PRL 61, 597 (1988)]

The solid lines are from two band  
model with one fitting parameter.



(54)

Two band model, where local moments have wide distribution of  $J$ -couplings following the Blatt & Lee distribution  $P(J) \propto J^{-\alpha}$ , seems to explain the thermodynamic properties of  $SrTi$  and also  $Nb_x Sr_{1-x}$ .

Further confirmation of low lying spin states is given by  $^{29}Si$  NMR measurements.

The spin lattice relaxation time ( $T_1$ ) follows in good Fermi liquids Korringa law

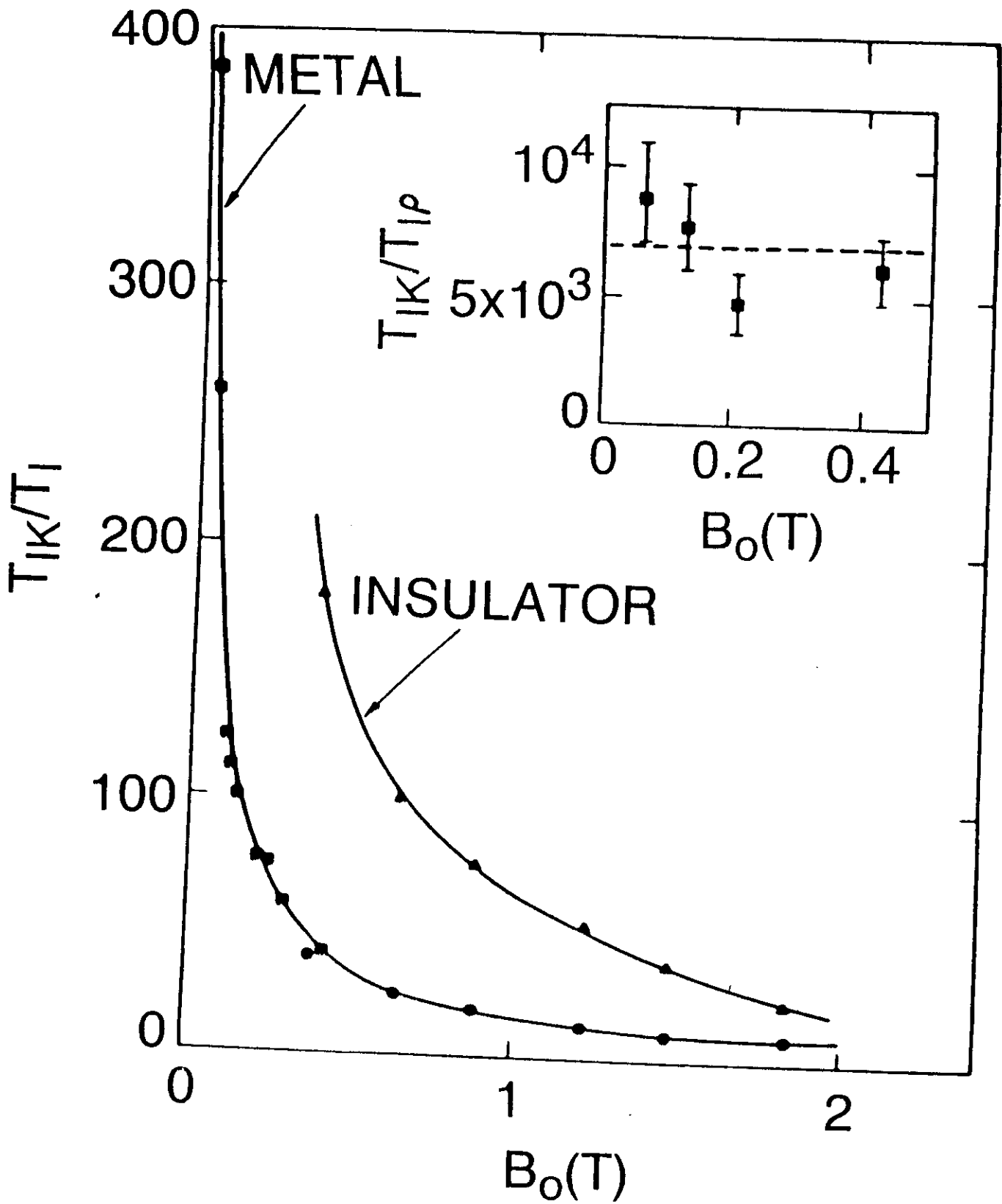
$$T_{1K} \propto \frac{1}{T}$$

and  $T_{1K}$  is independent of magnetic field  $B$ .

On page 55 we have compared the measured  $T_1$  with the predicted  $T_{1K}$  and find huge enhancement in the relaxation rate  $T_1^{-1}$  compared to  $T_{1K}^{-1}$ .

The ratio  $T_{1K}/T_1$  is also  $B$ -dependent.

This all is consistent with the local moment picture.



V CONCLUDING REMARKS

V 1. Critical behavior of  $\beta$  at MIT  
[  $\beta \propto (n-n_c)^\mu$  ]

Theory situation:

- one parameter scaling theory including disorder & e-e interactions exists
- theory predicts 8 universality classes with different critical behaviors. Very rich!
- in some cases we have estimations for  $\mu$  in lowest order  $\epsilon$  (d-2) expansion
  - spin-orbit
  - spin-flip
  - Magnetic field
 } universality classes have  $\mu = 1$
- general universality class  $\mu = ?$  (we don't know)
- in single electron theory without e-e interactions  $\mu \geq 2/3$  (Harris criterion)

Experimental situation:

Si:P (uncompensated):

Shaw et al  
Holcomb et al

- $\mu \approx 0.5$  (?)
- presumably in general univ. class (?)
- T-dependence complicated (?)
- In high B  $\mu \rightarrow 1$  (OK)
- compensation  $\mu \rightarrow 1$  (OK)

Crossover from one univ. class to another ?



Si:B: (uncompensated p-type)  
 - SO - univ. class  
 -  $\mu \approx 0.5$   
 - high B,  $\mu \rightarrow 1$   
 Shroeder et al } (Z)  
 (OK)

AlGaAs:  
 - SO - univ. class  
 -  $\mu \approx 1$   
 -  $\Delta E \propto \sqrt{T}$   
 Katsumoto (OK)  
 (OK)

$\text{In}_x\text{Sb}_{1-x}$   
 - SO - univ. class  
 -  $\mu \approx 1$  (OK)

V 2. Critical behavior of  $R_H$  at MIT

THEORY: Both single electron & interaction calculations are predicting critical behavior for  $R_H$

EXPERIMENTS:  
 -  $R_H$  is hard to measure (harder than  $Z_{xx}$ )  
 - Most experiments show critical  $R_H$  at MIT  
 - Si:As, Si:P, Ar:Ga,  $\text{In}_2\text{O}_3$  show noncritical behavior (?)

V 3

(58)

### Thermodynamic properties

- $C$  &  $\gamma$  don't show critical behaviour at  $n_c$
- $C$  &  $\gamma$  are dominated by the contributions from isolated spins.
- The magnetic fluctuations due to isolated spins are also seen in spin-lattice relaxation time  $T_1$  of the nuclei in the material.  $T_1$  is enhanced over the Korringa prediction for Fermi liquid.