



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
I.C.T.P., P.O. BOX 586, 34100 TRIESTE, ITALY, CABLE: CENTRATOM TRIESTE



SMR.858 - 35

I

SUMMER SCHOOL IN HIGH ENERGY PHYSICS AND COSMOLOGY

12 June - 28 July 1995

NEUTRINO PHYSICS

A. SMIRNOV
International Centre For Theoretical Physics
Trieste
ITALY

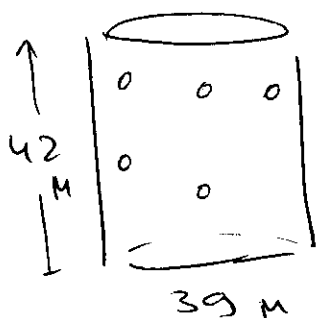
Please note: These are preliminary notes intended for internal distribution only.

NEUTRINO PHYSICS

A. Smirnov

①

- ± In January - February 96, huge steel tank ^{situated} in cavity of Kamioka mine will be filled by water



• 11,200 PMT will look this tank

• 50,000 T. of water

- In April 96 the electronics will turn on and underground detector of new generation will start to operate

→ SUPER KAMIOKANDE

- Also in '96 Sudbury (Canada) detector with 1000 t of heavy ~~wt~~ water is expected to begin to work.

- There is a hope that these detectors will give the answers to the questions we will discuss in ~~the~~ our lectures

2. After top quark discovery, the neutrinos are the only known fermions with unknown masses.

ν -masses & mixing
are main issues
of these lectures

$$\begin{bmatrix} m_\nu \\ \theta_\nu \end{bmatrix}$$

Why the knowledge of ν -masses and mixing is so important?

- ①. Important implications to Cosmology and astrophysics:

- $\Omega_\nu \sim O(1)$
- structure formation in the Universe
- Nucleosynthesis

↙
primordial

↘
in stars

- Stars evolution

relation to

- Baryon ~~as~~ asymmetry of the Universe

- ② Knowledge of $\boxed{m_\nu, \theta_\nu}$ may shed some light on

- fermions mass problem
- quark-lepton symmetry
- L - and B -violation

③

③: Via neutrino masses we can get some information on very large scales:

$$\mu \sim \frac{v_{ew}^2}{m_\nu}$$

v_{ew} - is the electroweak scale

m_ν - neutrino mass

$\mu = ?$

10^{10} GeV

10^{12} -

10^{16} -

10^{18} - ?

M_{pl} - ?

Plan of lectures:

N - mass mixing

EFFECTS

- oscillations
- resonance conversion

Bounds & hints

- solar ν
- atmospheric neutrinos
- $\mu \oplus H$
- LSND
- Karmen
- NS.

implications

- Scenarios
- pattern
- mechanisms

NEUTRINO FLAVOURS

$$\nu_e, \nu_\mu, \nu_\tau$$

states with definite flavours

phenomenological definition:

ν_e — is the state which interacts with electron: (positron)

$$\pi \rightarrow e^+ \nu_e$$

ν_μ — " — with muon

ν_τ — " — τ - lepton

In the Standard Model:

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$$

→ they form the doublets

→ enter the corresponding charge currents.

In general — these two definitions may not coincide:

ν_e state which is produced in β -decay

$\neq$

ν_e - state which enter the same doublet with electron

- This situation is realized in quite probable case of existence of heavy neutral leptons (= or heavy "Rt. neutrinos")
 - it is realized in the see-saw mechanism

Example:

$$\approx 1 \begin{pmatrix} \nu'_e + \epsilon_e N \\ e \end{pmatrix}_L \quad \approx 1 \begin{pmatrix} \nu'_\mu + \epsilon_\mu N \\ \mu \end{pmatrix}_L$$

Let $M_N \geq \frac{M_Z}{2}$ (to avoid LEP bound)

➡ N can not be produced in β -decay or in π decay (for kinematic reasons)

➡ the state which enters the same doublet with e is

$$\nu_e \equiv \nu'_e + \epsilon_e N$$

the state, which is produced in β -decay is ν'_e

ν_e and ν_μ are orthogonal, but not ν'_e, ν'_μ

$$\langle \nu_e | \nu_\mu \rangle = \langle \nu'_e | \nu'_\mu \rangle + \epsilon_e \epsilon_\mu = 0$$

➡

$$\boxed{\langle \nu'_e | \nu'_\mu \rangle = -\epsilon_e \epsilon_\mu}$$

↖ violation of lepton number

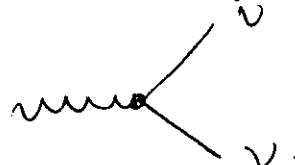
(6)

The bounds on ϵ : $\epsilon \leq 10^{-2}$

(Breaking of the universality etc.)

• Number of neutrino flavours ($\equiv$ species)

Γ_{inv} - invisible width of Z^0 decay:



$$N_\nu = \frac{\Gamma_{inv}}{\Gamma_\nu}$$

$$\Gamma_{inv} = \Gamma_{tot} - \underbrace{\Gamma_e}_{\text{leptonic}} - \underbrace{\Gamma_h}_{\text{hadronic}}$$

LEP:

$$\Gamma_{inv} = 499.5 \pm 2.7 \text{ MeV}$$

Γ_ν is the $Z \rightarrow \nu\bar{\nu}$ width in SM:

$$N_\nu = 2.987 \pm 0.016$$

→ strong bounds on new physics

e.g. - new neutrino species
- ~~or~~ couplings of new light scalars etc.

one subtle point:

what is the neutrino state produced in Z^0 decay?

If L -number is conserved, then one has independent (incoherent) production of pairs $\nu_e \bar{\nu}_e$, $\nu_\mu \bar{\nu}_\mu$, $\nu_\tau \bar{\nu}_\tau$. However, if lepton numbers are broken these pairs can be

L_e, L_μ, L_τ

mixed. May be more natural in this case

to consider the production ~~is~~ of the mass states:

$$\nu_1 \bar{\nu}_1, \nu_2 \bar{\nu}_2, \nu_3 \bar{\nu}_3.$$

In fact, ~~the~~ as follows from the Lagrangian the state which is produced in Z^0 decay is

$$|\nu_Z\rangle = \frac{1}{\sqrt{3}} \left[|\bar{\nu}_1\rangle |\nu_1\rangle + |\bar{\nu}_2\rangle |\nu_2\rangle + |\bar{\nu}_3\rangle |\nu_3\rangle \right]$$

One can easily check that this state gives the same invisible width of Z^0 as three pairs $\bar{\nu}_i \nu_i$:

$$\Gamma^{\text{inv}} \sim |\langle \nu_Z | h | Z^0 \rangle|^2 = 3 \left(\frac{g}{2} \right)^2.$$

According to recent reanalyses of the
the ~~the~~ effective Primordial Nucleosynthesis, the bound on
number of neutrino species ~~is~~ in
the time of Nucleosynthesis ($\sim 1 \text{ sec}$): is

$$N_\nu < 2.5 \quad (95\%) \text{ C.L.}$$

This could imply that ~~some~~ some of
neutrinos are unstable, e.g. ν_τ ,
having the mass $\sim$

$$m \sim 10 - 20 \text{ MeV}$$

and the lifetime: τ

$$\tau < 10 \text{ sec.}$$

$$\nu_\tau \rightarrow \phi + \nu_\mu$$

where ϕ is the Majorana-like particle.

NEUTRINO MASSES

(1). In the Standard Model:

$$m_\nu = 0.$$

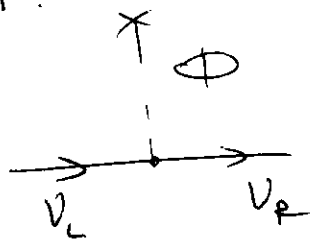
(2). If there are right handed neutrino components, one can introduce Dirac

ν_R

mass term:

$$\mathcal{L}_D = -m_D (\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L) \quad (*)$$

it has the weak isospin $1/2$ and can be generated by Yukawa couplings with Higgs & doublet:



3) In the mass term (*) instead of ν_R one can use $(\bar{\nu}_L)^c$: charge conjugated state.

$$\mathcal{L}_m = \frac{1}{2} m (\bar{\nu}_L \nu_R^c + \bar{\nu}_R^c \nu_L)$$

$$[\nu_L]^c = C(\bar{\nu})^T \quad C = i\gamma^2 \gamma^0$$

This term can be rewritten as:

$$\frac{1}{2} m (\bar{\nu}_\mu \nu_\mu)$$

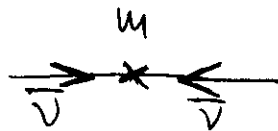
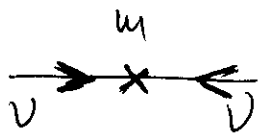
where

$$\nu_\mu = \nu_L + (\nu_L)^c$$

and ν_μ has evident property:

$$(\nu_\mu)^c = \nu_\mu$$

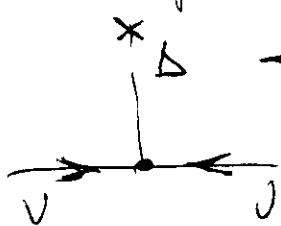
→ Majorana neutrinos



Majorana mass terms.

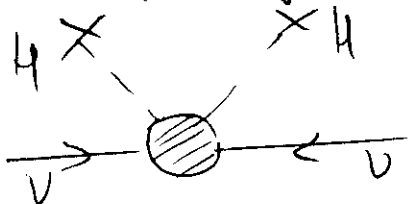
$\Delta L = 2$ - violate lepton number
 $I = 1$ - weak isospin

How to produce them?

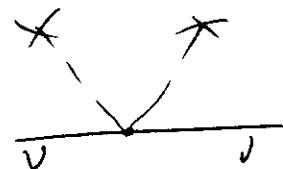


~~electroweak~~
 triplet of Higgses

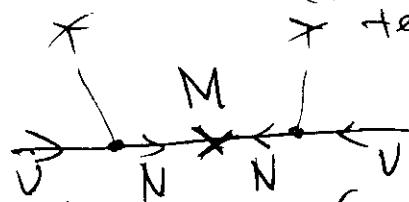
or effectively



: gravity(?)



(non renormalizable)
 term



(see-saw)

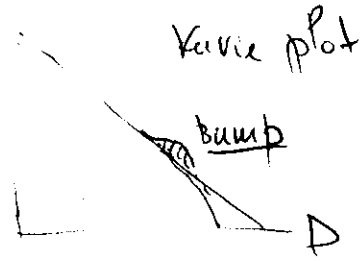
Bands on V-marks

kinematics.
(Best).

Summary:

$\nu_e: 3H \rightarrow He + e^- + \bar{\nu}_e$

end point of the energy spectrum:



INR: RAS: integral electrostatic spectrometers

$m < 4.5 \text{ eV}$ 95% cl.

Mainly:

6. eV
7.2 eV

look
②

①

PSI

$\pi \rightarrow \mu \nu_\mu$

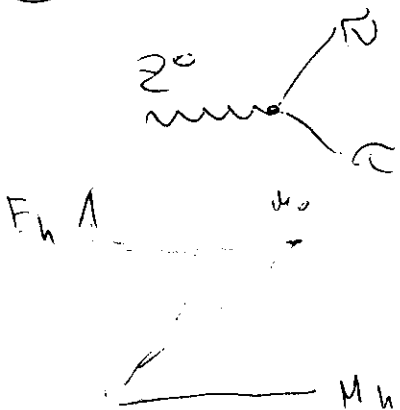
$M(\nu_\mu) < 160 \text{ keV}$ (B)

②

ALEPH CERN

152000 τ -decays.

$\tau \rightarrow 5\pi(\pi^0)\nu_\tau$



• $\text{Recoil: } \left(\frac{E_{had}}{E_{beam}} \right)$

$M_h > 1.626$

• $M_{had}(\text{GeV})$
invariant mass of hadrons

$$m(\nu_e) < 24 \text{ MeV} \quad (95\% \text{ CL}).$$

$$m_h < m_\tau - m_{\nu_\tau} \quad \Leftrightarrow \text{one dimension } \text{Pare}$$

but if there is a mixing? with light neutrinos.

→ there is some probability that we detect some event

• but the mixture should be very small.

$$\nu_e - \nu_\tau \quad (\text{if } \text{majorana} \dots)$$

$$\bullet \quad \nu_s = \nu_s'$$

$$\bullet \quad \nu_\mu = \textcircled{?}$$

Cosmological bound:

$$\Omega_\nu \cdot h^2 = \sum_i \frac{m_{\nu_i}}{92 \text{ eV}}$$

$$t > 1.3 \cdot 10^{10} \text{ yr} \Rightarrow \Omega_\nu h^2 < 0.4$$

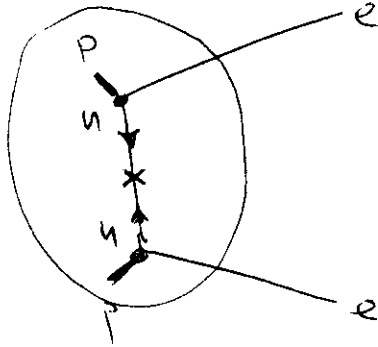
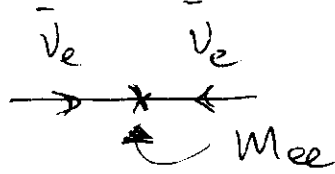
$$\sum m < 37 \text{ eV}$$

$$< 23 \text{ eV}$$

$$h = 0.5$$

Double beta decay

If neutrinos have Majorana masses.



$$Z \rightarrow (Z+2) + 2e^-$$

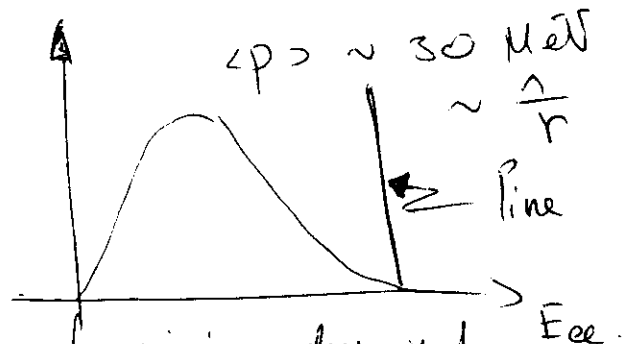
NEUTRINOS double β -decay

$$A \propto \left(\frac{M_{ee}}{P^2} \right)_{\text{nuc.}}$$

for $M_\nu \ll 30 \text{ MeV}$

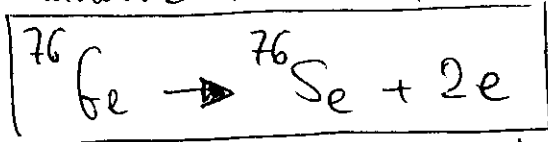
$$A \propto M_{ee}$$

↑ in the case of mixing does not coincide with mass states (see later).



Best limit:

Heidelberg-Moscow (Gran-Sasso)



$$Q = 2038.56 \text{ MeV}$$

$$T_{1/2} > 5.1 \cdot 10^{24} \text{ s}$$

(8.6)

$$|M_{ee}| < 0.68 \text{ eV}$$

$$< 0.52 \text{ eV}$$

unriched
isotopes (80%)
(3 detectors)

$$8.6 \text{ kg} \cdot \text{s} \rightarrow 76$$

$$(16.9 \text{ g})$$

$$\rightarrow 10^{25} \text{ in future!}$$

90% Cl
68% Cl

for heavy
neutrinos.

$$\frac{E}{M_\nu} < \frac{1}{10^6}$$

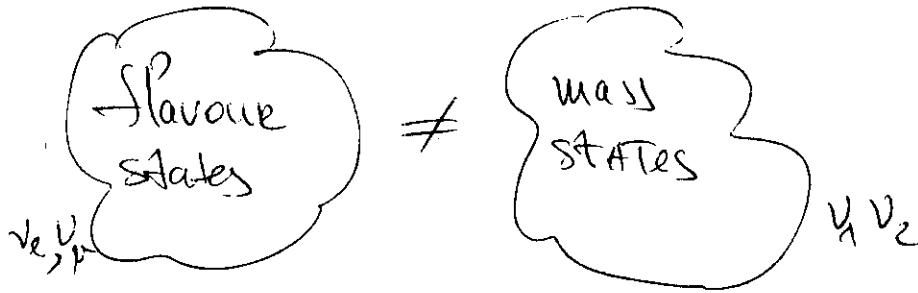
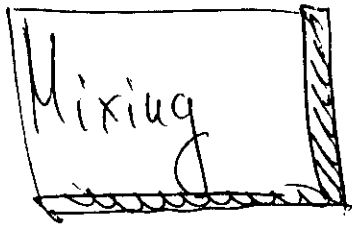
more important!

Matrix elements:

Staud Muto Klaydor (1990)
Mirsch.

Vogel: $\rightarrow \times 2$

$$\rightarrow \boxed{m \lesssim 1.5 \text{ eV}} \quad (90\%)$$



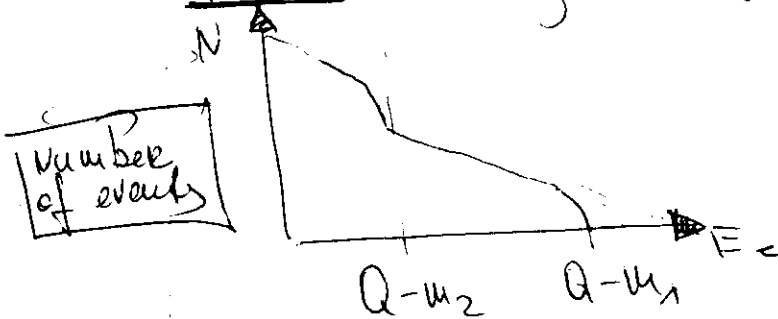
simple 2D case:

$$\begin{aligned} \nu_e &= \cos\theta \nu_1 + \sin\theta \nu_2 \\ \nu_\mu &= \cos\theta \nu_2 - \sin\theta \nu_1 \end{aligned}$$

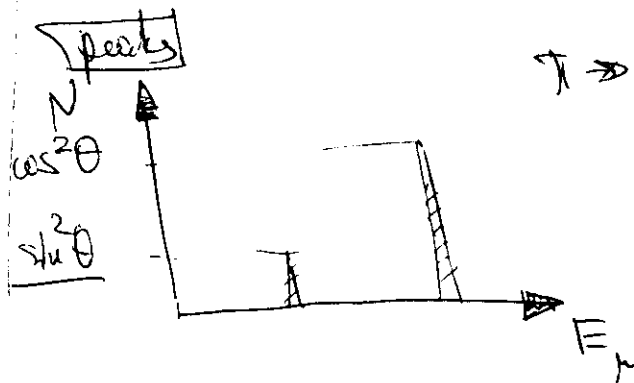
θ is the mixing angle

Kinematical consequences:

kinks in π -decay spectrum:



Q is the end point of spectrum.



$\pi \rightarrow \nu_\mu \mu$

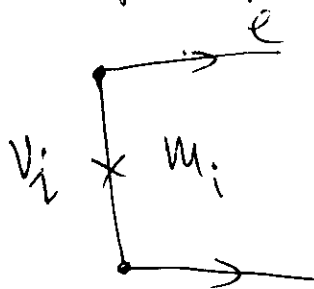
$\pi \rightarrow e \nu$

$$|\mu_{e\nu}|^2 < 5 \cdot 10^{-6}$$

ν -decay:

$$\nu_2 \rightarrow \nu_1 \bar{\nu}_1 \nu_1$$

Double β -decay and mixing,



$$\nu_e = U_{ei} \nu_i$$

$$M_{ee} = \sum_i U_{ei}^2 \cdot M_i$$

effective majorana mass of the electron neutrino

For $M_3 = 20 \text{ MeV}$

$$U_{ei} \leq \sqrt{\frac{M_{ee}}{M_i}} \rightarrow \text{bound on mixing}$$

$$U_{e3} \sim 0.5 \quad M_3 = 20 \text{ MeV}$$

$$\underline{U_{e3} < 1.6 \cdot 10^{-4}} \ll U_{ub}, U_{td}$$

$$\begin{aligned} 0.5 \\ 2 \cdot 10^7 \\ 2.5 \cdot 10^{-8} \end{aligned}$$

is much smaller than cross/funding mixing element in quark sector.

Effects of propagation of mixed states

1) Oscillations: in vacuum and in medium with constant parameters (density etc)

2) Resonance conversion: in the case of medium with variable parameters.

Resonance conversion $\neq$ enhanced oscillations

another effect.

Oscillations

is the effect related to phases which acquire the neutrino mass states during the propagation:

- Suppose ν_e is produced:

$$\nu(0) = \nu_e = \cos\theta \nu_1 + \sin\theta \nu_2$$

ν_1 and ν_2 are the eigenstates of the Hamiltonian in vacuum:

This means that ν_1 and ν_2 propagate independently: there is no transitions

$$\boxed{\nu_1 \leftrightarrow \nu_2}$$

the only what happens is
the phase which acquires v_i .

(18)

$$v_1 \rightarrow v_1 e^{i\phi_1}$$

$$v_2 \rightarrow v_2 e^{i\phi_2}$$

$$S_i \equiv E_i t - p_i x$$

$$S_1 \neq S_2 \quad \left[\begin{array}{l} \text{due to} \\ \text{mass} \\ \text{difference} \end{array} \right]$$

correspondingly the wavefunction state
can be written as

$$\psi(t) = \cos \theta v_1 + \sin \theta v_2 \cdot e^{i\Delta S}$$

$$\boxed{\Delta S = S_2 - S_1}$$

(common factor $e^{i\phi_1}$ is removed; the
phase difference important only)

$$\Delta S?$$

if $p_1 = p_2$ (one can in general take different
 p_1, p_2)

then

$$\boxed{\Delta S = (E_2 - E_1)t}$$

or in ultrarelativistic case:

$$E_i \sim p + \frac{m_i^2}{2E}$$

$$\Delta E = \frac{\Delta m^2}{2E}$$

$$\boxed{\Delta S = \frac{\Delta m^2}{2E} L}$$

(5)

there is a monotonous increase of phase difference in time

~~oscillations~~ oscillations.

$\Delta\varphi = \pi$: (maximal deviation from the initial state)

$\Delta\varphi = 2\pi$: the state returns in the initial (flavour) state.

1) $\Delta\varphi = \pi$:

$$V(\pi) = \cos\theta v_1 - \sin\theta v_2$$

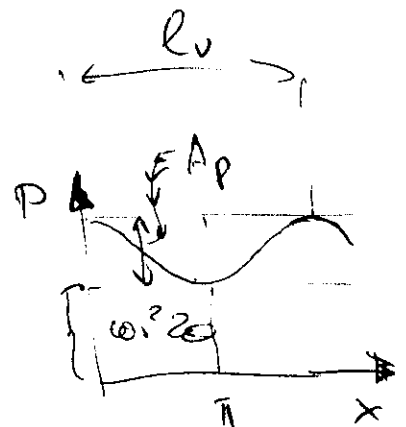
$$\langle v_e | V(\pi) \rangle = \cos^2\theta - \sin^2\theta = \cos 2\theta$$

the probability to find v_e :

$$P_\pi = |\langle v_e | V(\pi) \rangle|^2 = \cos^2 2\theta$$

the depth of oscillations:

$$A = 1 - P_\pi = \sin^2 2\theta$$



2) $\Delta\varphi = 2\pi$

the distance where $\Delta\varphi = 2\pi$:

$$\frac{\Delta m^2}{2E} t = 2\pi$$

$$t = \frac{4\pi E}{\Delta m^2}$$

$= l_v$ — oscillation length.
 $c=1$

Now we can write the oscillation probability:

$$P_{\nu_e \rightarrow \nu_\mu} = \sin^2 2\theta \cdot \left(1 - \cos \frac{2\pi x}{l_\nu}\right) \cdot \frac{1}{2}$$

$\uparrow$ depth of oscillations $\uparrow$ oscillating phase factor

OR:

$$P_{\nu_e \rightarrow \nu_\mu} = \sin^2 2\theta \cdot \sin^2 \frac{\pi x}{l_\nu}$$

To have $\sin^2 2\theta$
for $x = \frac{l_\nu}{2}$

