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INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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AUTUMN COURSE
ON
VARIATIONAL METHODS IN ANALYSIS AND MATHEMATICAL PHYSICS
20 October - 11 December 1981

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