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INTERNATIONAL ATOMIC ENERGY AGENCY
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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SMR.961 - 5

**WORKSHOP ON:
PROTEINS, MEMBRANES and their INTERACTIONS**

22 JULY - 2 AUGUST 1996

***"Modelling lipid membranes by
diblock bilayers"***

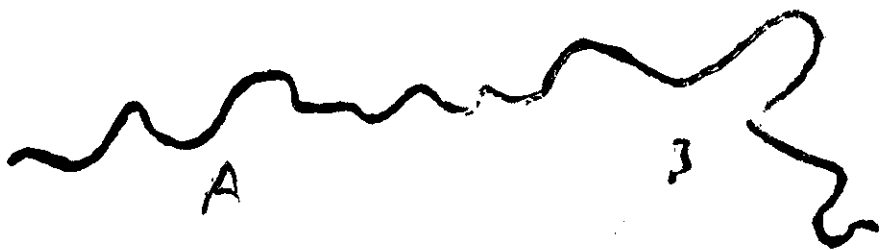
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U.S.A.**

These are preliminary lecture notes, intended only for distribution to participants.

MODELLING LIPID MEMBRANES

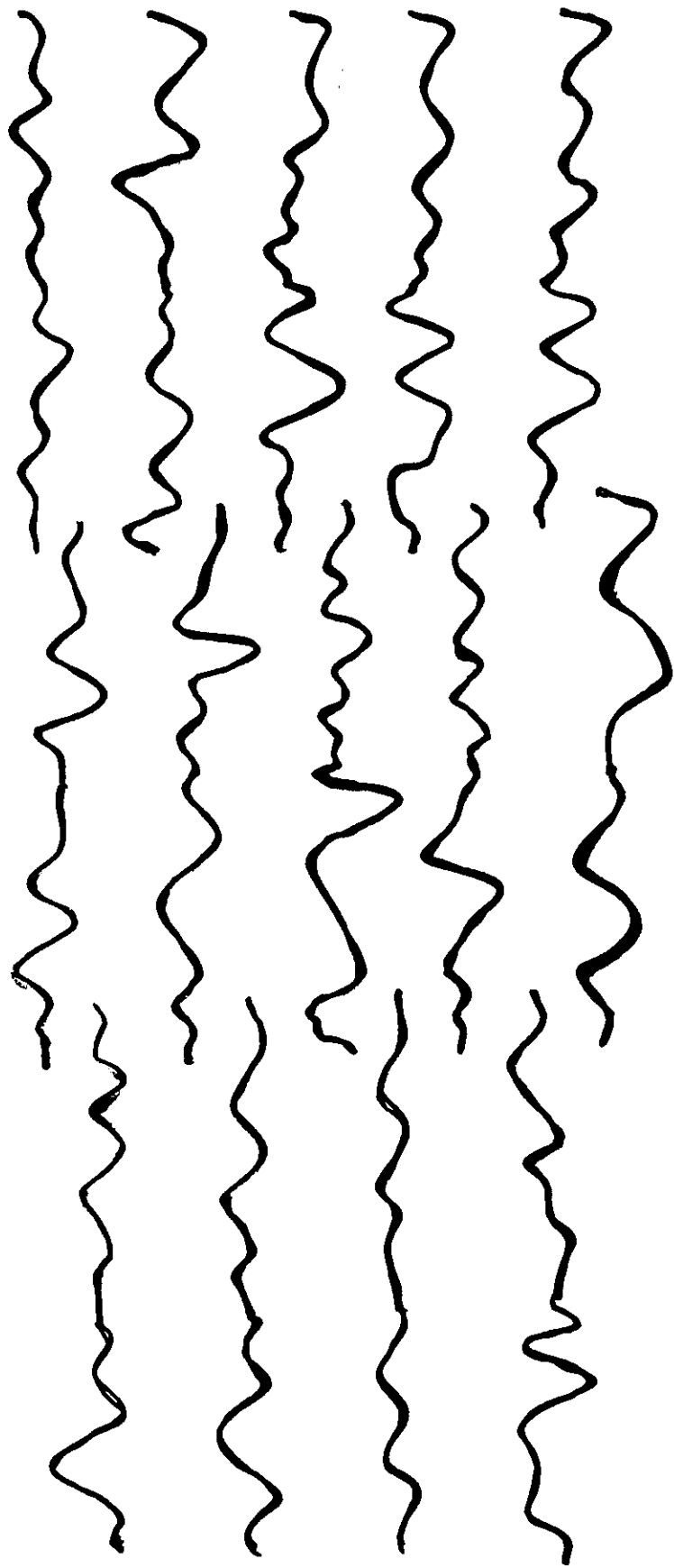
BY DIBLOCK BILAYERS

- I. Diblock Polymorphism
- II. Calculated Diblock Behavior (SCFT)
- III. Addition of Homopolymer
- IV. Rupture of a Bilayer
- V. Pore Formation
 - i Equilibrium Phase of Pores
 - ii Formation of Pores by Fluctuations (Simulation)
- VI. Bilayer of Semiflexible Diblock: Main Transition



A-B	Microstructure
PI-PS	
PE-PEE	
PEP-PEE	
PE-PEP	

LAMELLAR PHASES



LAMELLAR PHASE OF POLYSTYRENE-POLYISOPRENE

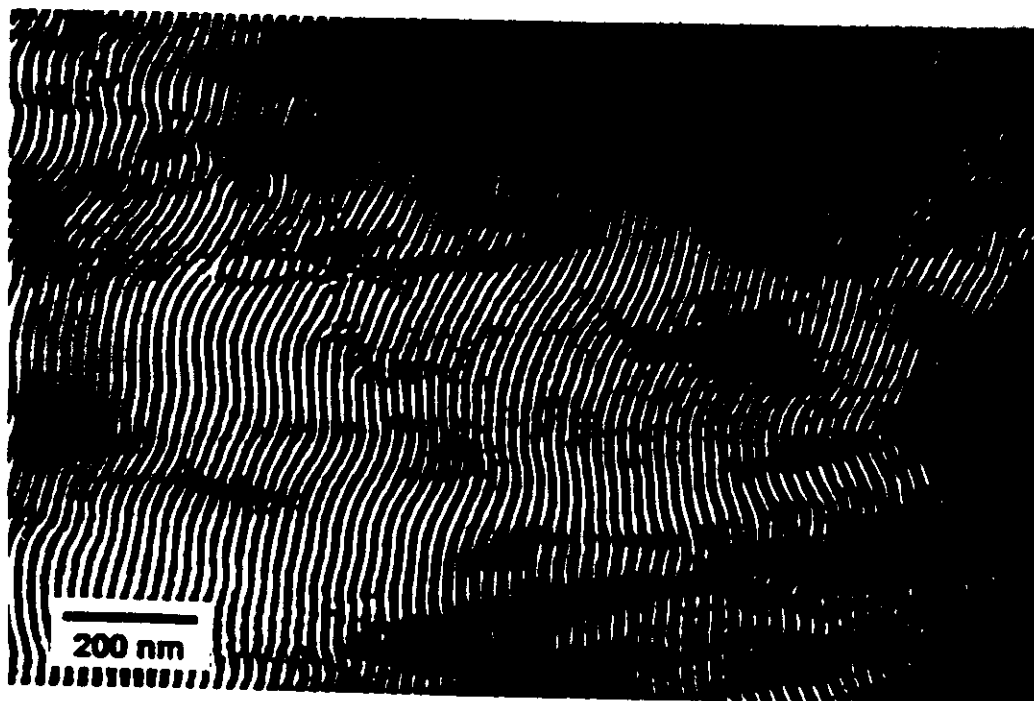
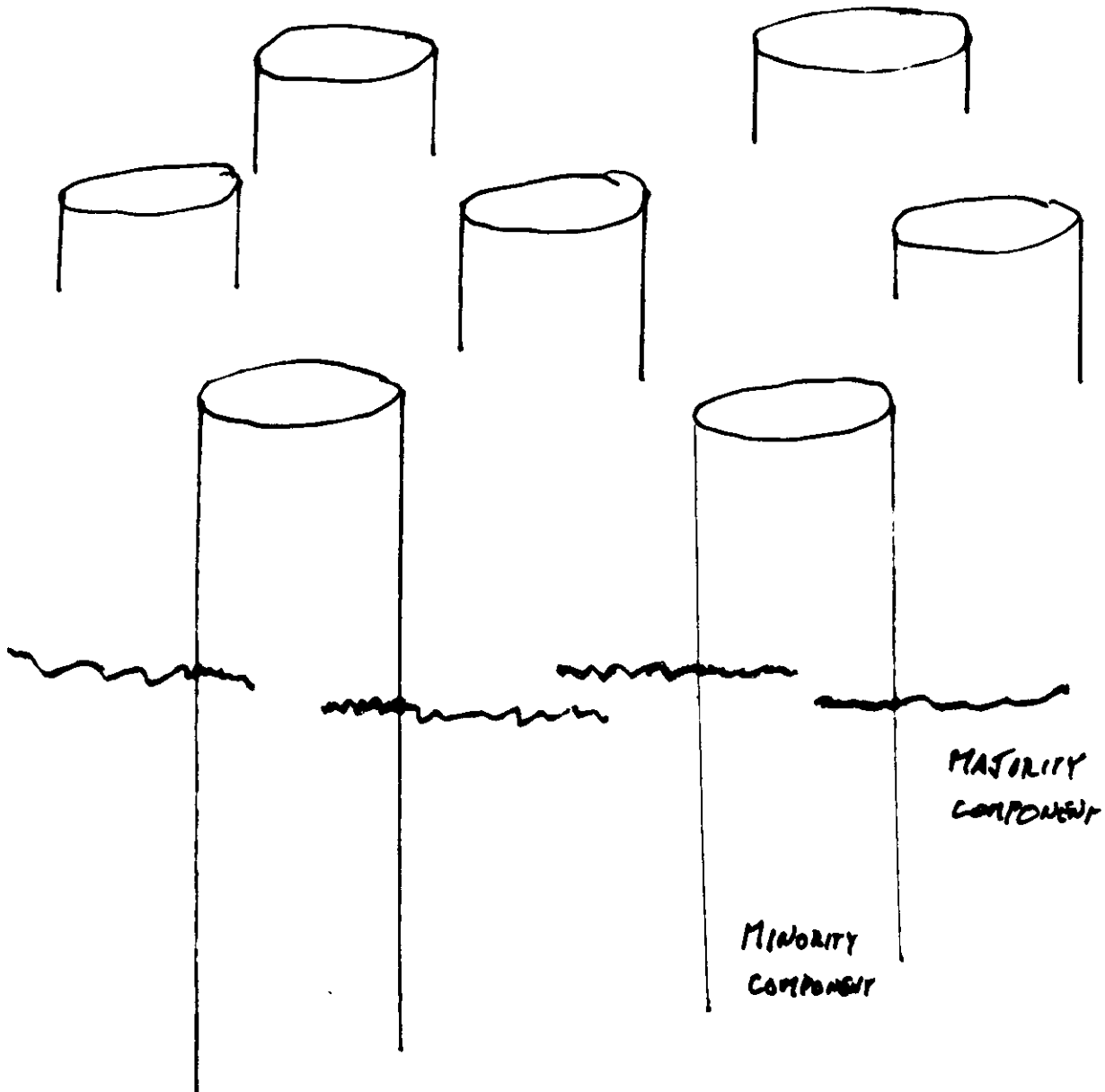


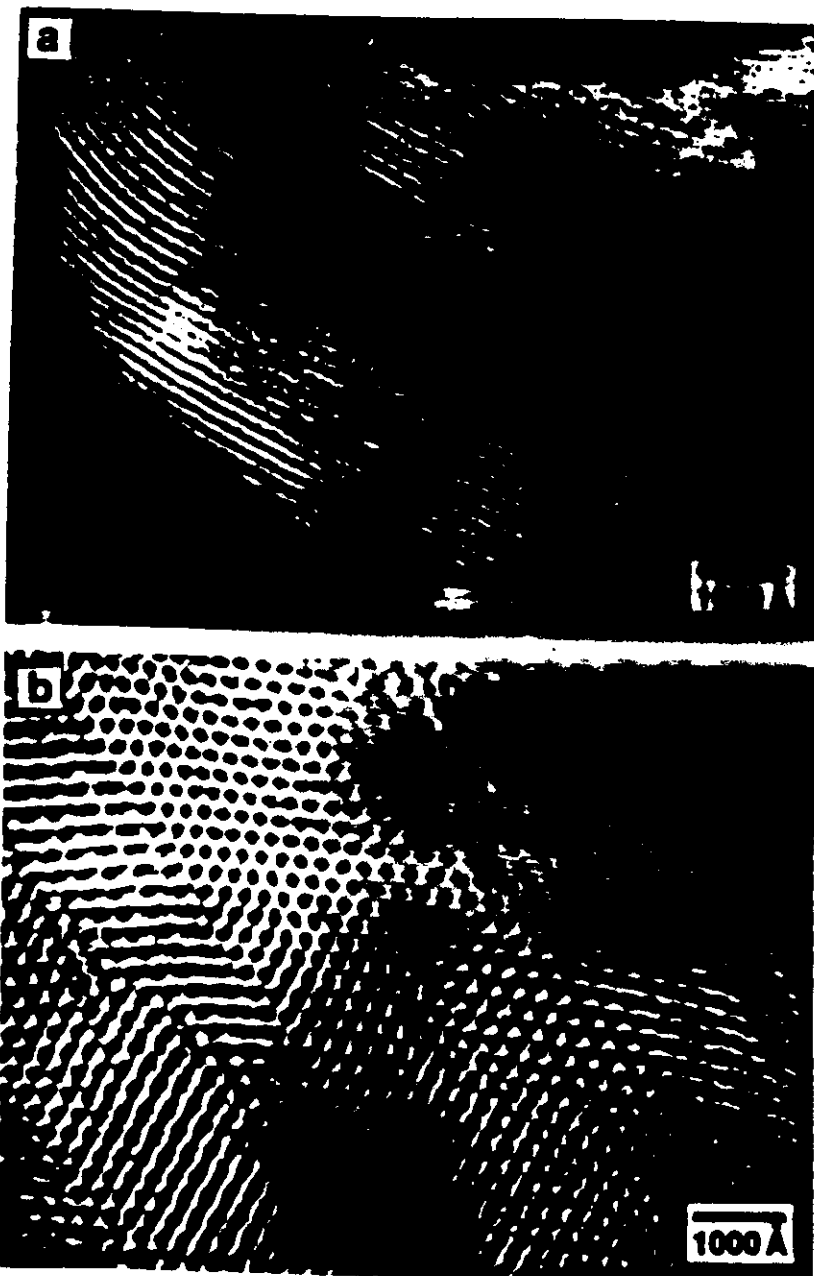
Figure 2. TEM micrograph of a sample of pure diblock cast from toluene and annealed for 1 week at 115 °C. Polyisoprene domains have been stained with OsO₄ to provide contrast and appear dark in the image. A well-ordered lamellar morphology with a repeat period of approximately 210 Å is clearly evident.

HARDUK ET AL. *MACROMOLECULES* **27**, 4063 (1994)

OTHER PHASES

HEXAGONAL



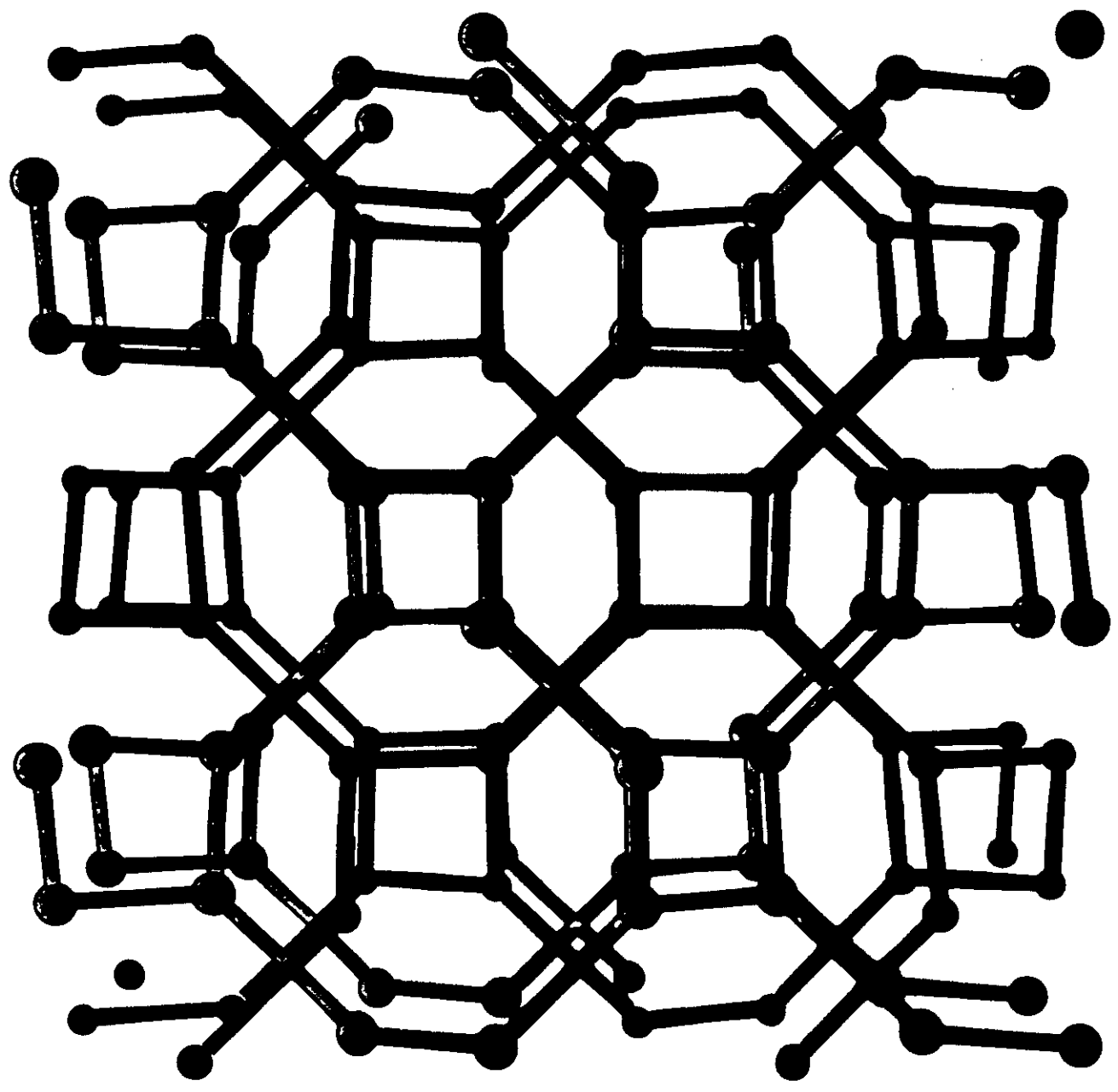
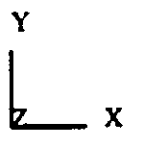


LAM

HEX

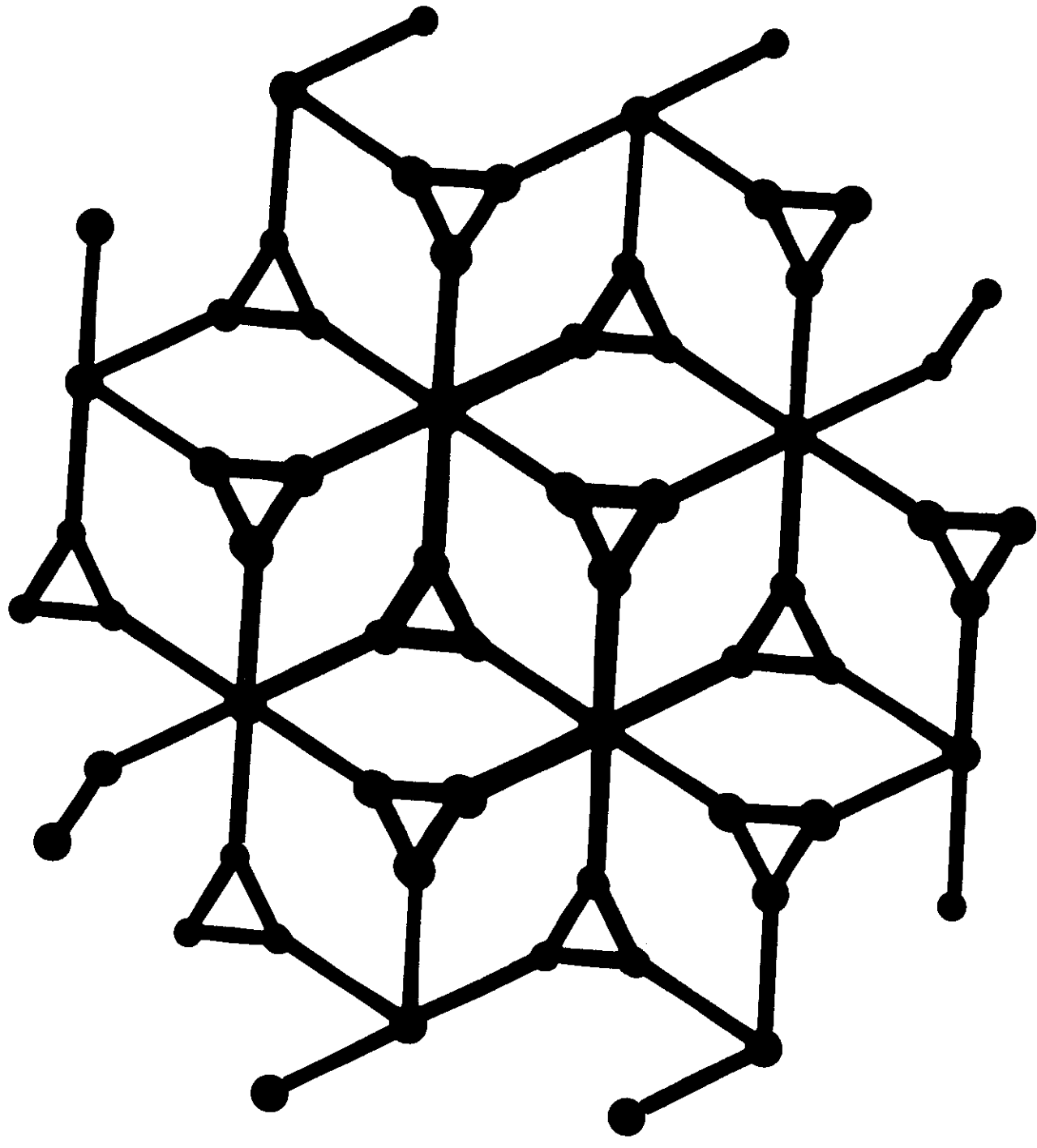
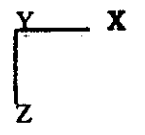
Figure 5. Transmission electron micrographs of (a) IS-42 in phase A (annealed at 145 °C) and (b) IS-33 in phase C (annealed at 145 °C), showing lamellar (LAM) and hexagonally packed cylinder (HEX) structures, respectively.

FÖRSTER ET AL. MACROMOLECULES 27, 6922 (1994)



COURTESY OF A. FRANKEL





SAXS

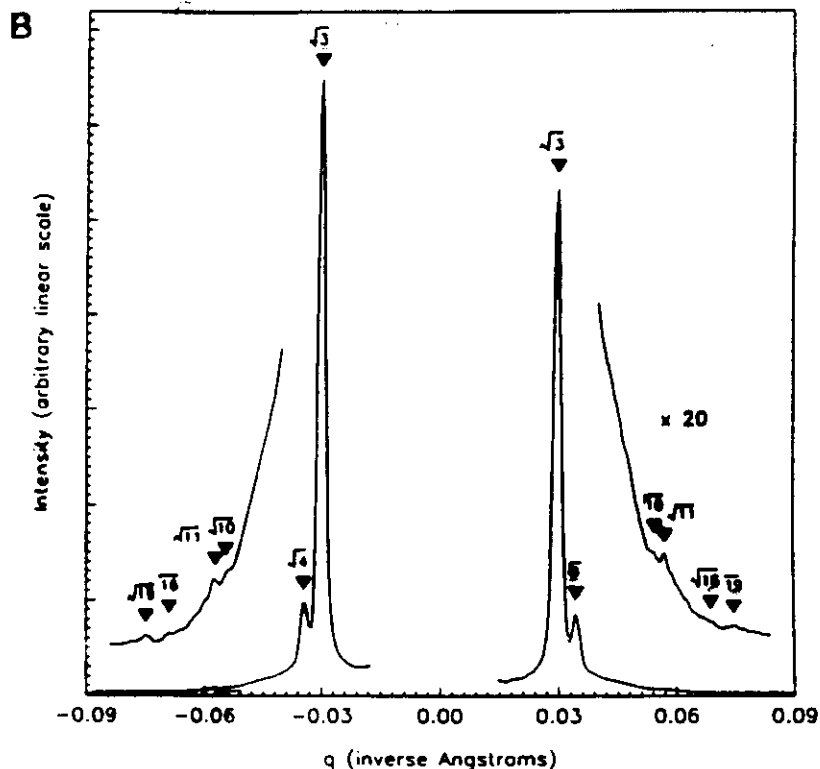


Figure 6. (A) Two-dimensional scattering image obtained from a pure diblock film annealed for 4 h at 150 °C to establish the new morphology, followed by quenching in liquid nitrogen and subsequent annealing at 120 °C for 4 h to eliminate disorder induced by quenching and increase the number of higher order Fourier components in the monomer concentration profile (as described in the text). This image was obtained after integrating for 8 h at 120 °C; comparison of diffraction before and after this period revealed no change in the scattering from the sample. (B) One-dimensional profile prepared from the two-dimensional image. $\sqrt{3}$, $\sqrt{4}$, $\sqrt{10}$, $\sqrt{11}$, $\sqrt{16}$, and $\sqrt{19}$ denote the position ratios of the observed reflections; as discussed in the text, such reflections are most consistent with a structure possessing $Ia3d$ symmetry.

HAJDUK ET AL. *MACROMOLECULES* **27**, 4063 (1994)

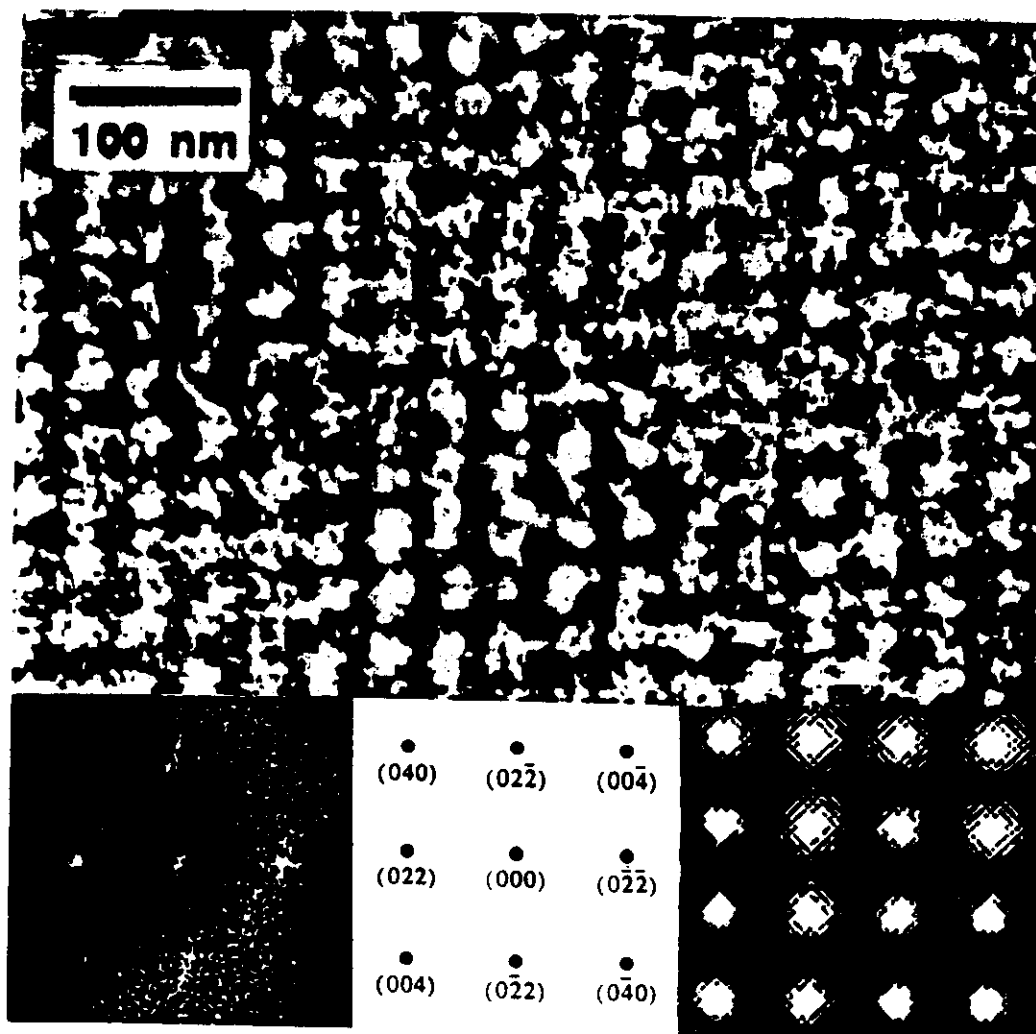


FIGURE 9

HANDUR ET AL. *MACROMOLECULES* 27, 4053 (1994)

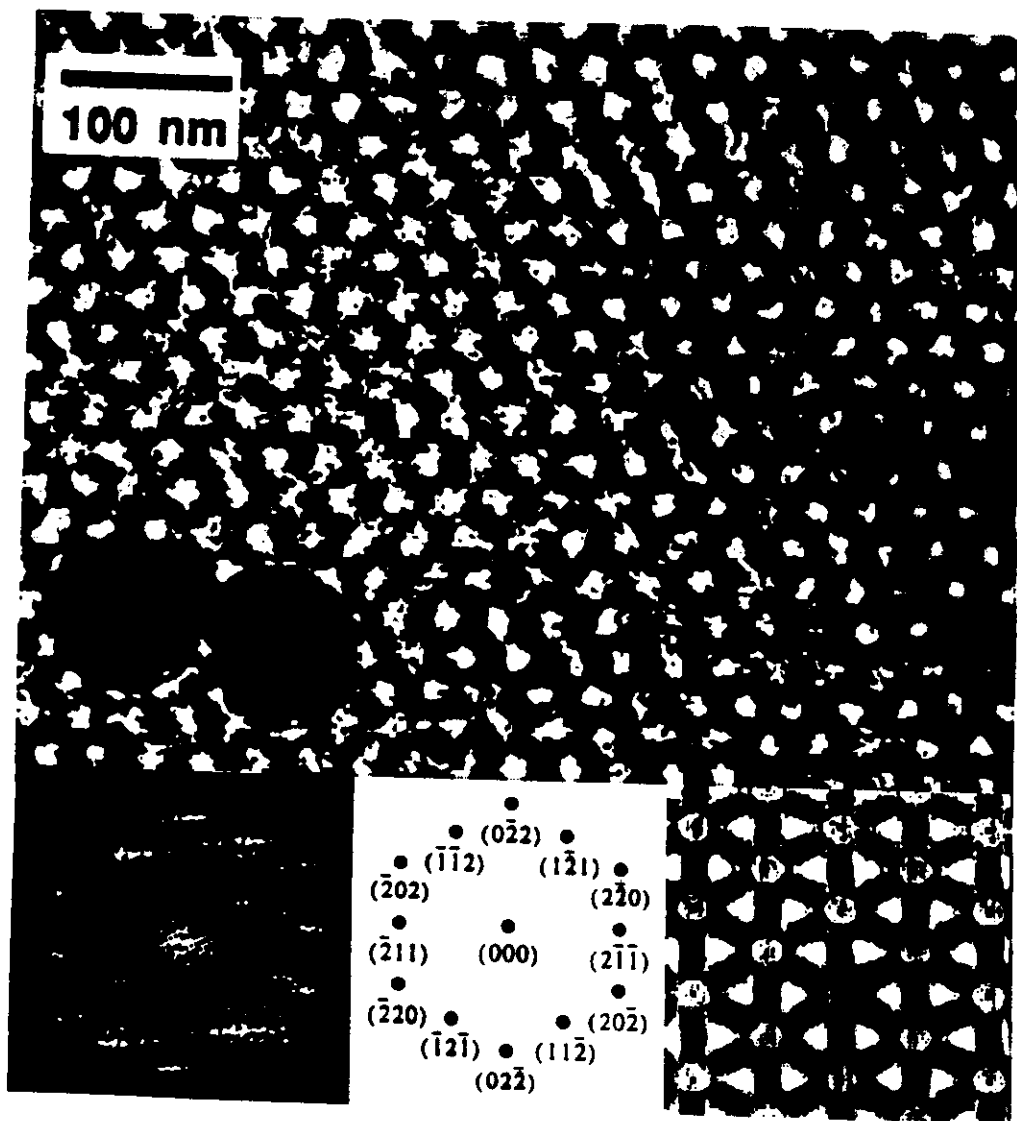


FIGURE 8

HAJDUK ET AL. *MACROMOLECULES* 27, 4063 (1994)

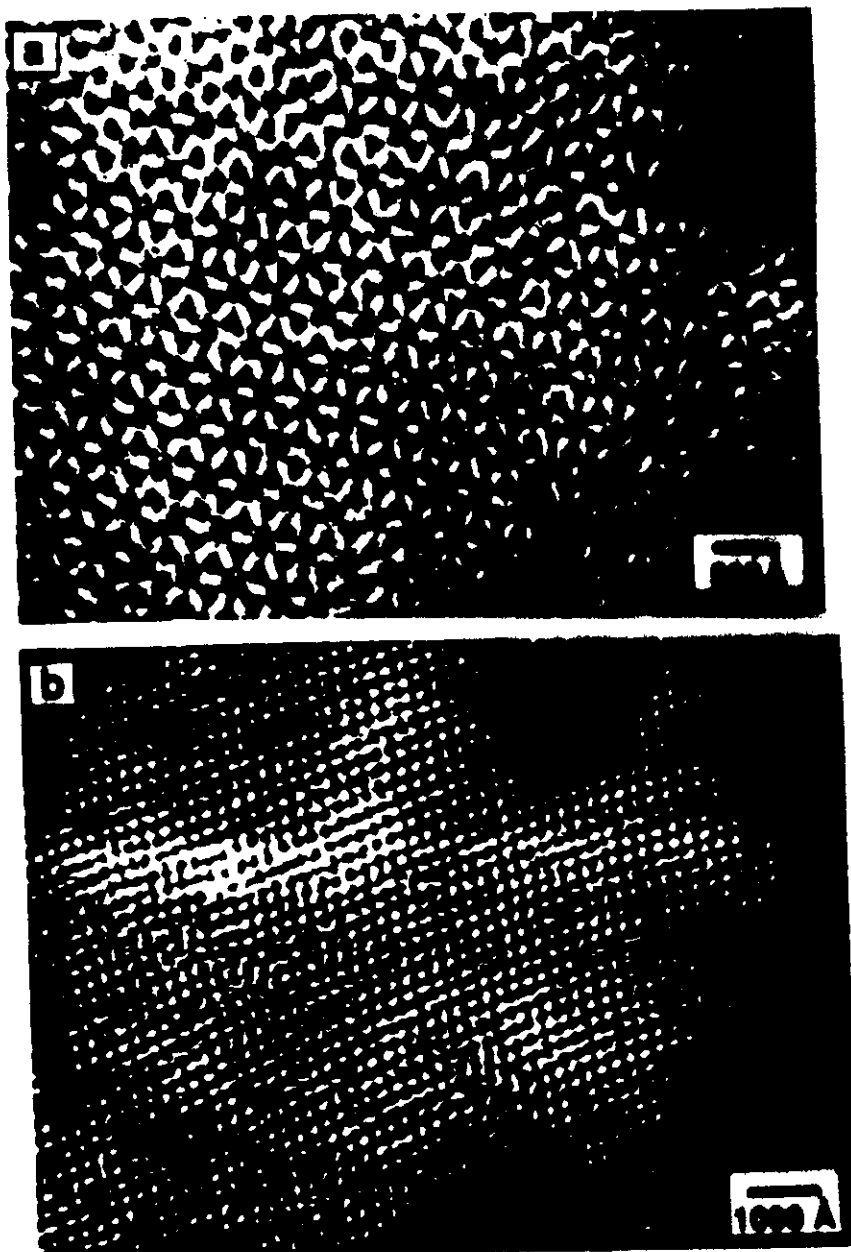
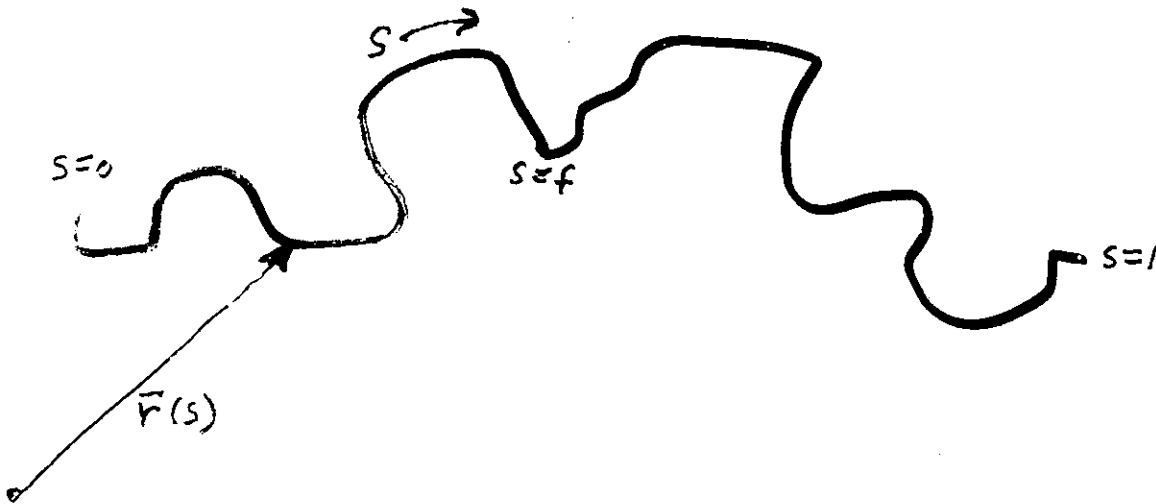


Figure 6. Representative TEM micrographs of IS-30 in phase B (annealed at 205 °C) showing (a) 3-fold and (b) 4-fold projections of the bicontinuous $Ia\bar{3}d$ microstructure.

FÖRSTER ET AL. MACROMOLECULES 27, 6922 (1994)

SINGLE DIBLOCK COPOLYMER IN EXTERNAL FIELDS



$$Q[w_A, w_B] \propto \int \mathcal{D}\mathbf{r} P[\mathbf{r}(s)] \exp - \left(\int_0^f ds w_A(\mathbf{r}(s)) + \int_f^1 ds w_B(\mathbf{r}(s)) \right)$$

where for flexible chains

$$P[\mathbf{r}(s)] = \exp \left\{ -\frac{3}{2Na^2} \int_0^1 ds \left[\frac{d\mathbf{r}(s)}{ds} \right]^2 \right\}$$

and for semi-flexible chains

$$P[\mathbf{r}(s)] = \exp \left\{ -\frac{\kappa}{2N} \int_0^1 ds \left[\frac{d\mathbf{n}(s)}{ds} \right]^2 \right\}$$

where

$$\mathbf{n}(s) \equiv \frac{1}{Na} \left(\frac{d\mathbf{r}(s)}{ds} \right)$$

INTERACTING POLYMER PROBLEM

Density of A monomers

$$\hat{\Phi}_A(\mathbf{r}, \{\mathbf{r}(s)\}) = Nv \sum_{\alpha=1}^n \int_0^f ds \delta[\mathbf{r} - \mathbf{r}_\alpha(s)]$$

Density of B monomers

$$\hat{\Phi}_B(\mathbf{r}, \{\mathbf{r}(s)\}) = Nv \sum_{\alpha=1}^n \int_f^1 ds \delta[\mathbf{r} - \mathbf{r}_\alpha(s)]$$

Interaction

$$+\chi \int \frac{d\mathbf{r}}{v} \hat{\Phi}_A(\mathbf{r}) \hat{\Phi}_B(\mathbf{r})$$

Mean-Field Free Energy per Polymer

$$\frac{F_{mft}}{nkT} = -\ln Q[w_A, w_B] + \frac{1}{V} \int d\mathbf{r} \left(\frac{\chi N}{4} \left[\frac{w_A - w_B}{\chi N} - 1 \right]^2 - w_B \right)$$

where

$$w_A - w_B = \chi N (\phi_B - \phi_A)$$

$$\phi_A = \langle \hat{\Phi}_A \rangle = -V \frac{\delta \ln Q[w_A, w_B]}{\delta w_A}$$

$$\phi_B = \langle \hat{\Phi}_B \rangle = -V \frac{\delta \ln Q[w_A, w_B]}{\delta w_B}$$

$$1 = \phi_A + \phi_B$$

Expand all functions of position in complete set
of eigenfunctions of Laplacian
which have the desired space-group symmetry

$$w_A(\mathbf{r}) = \sum_i w_{Ai} f_i(\mathbf{r})$$

$$w_B(\mathbf{r}) = \sum_i w_{Bi} f_i(\mathbf{r})$$

.....

where

$$\nabla^2 f_i(\mathbf{r}) = \lambda_i D^{-2} f_i(\mathbf{r})$$

Matsen and Schick, PRL72 2660 (1994).

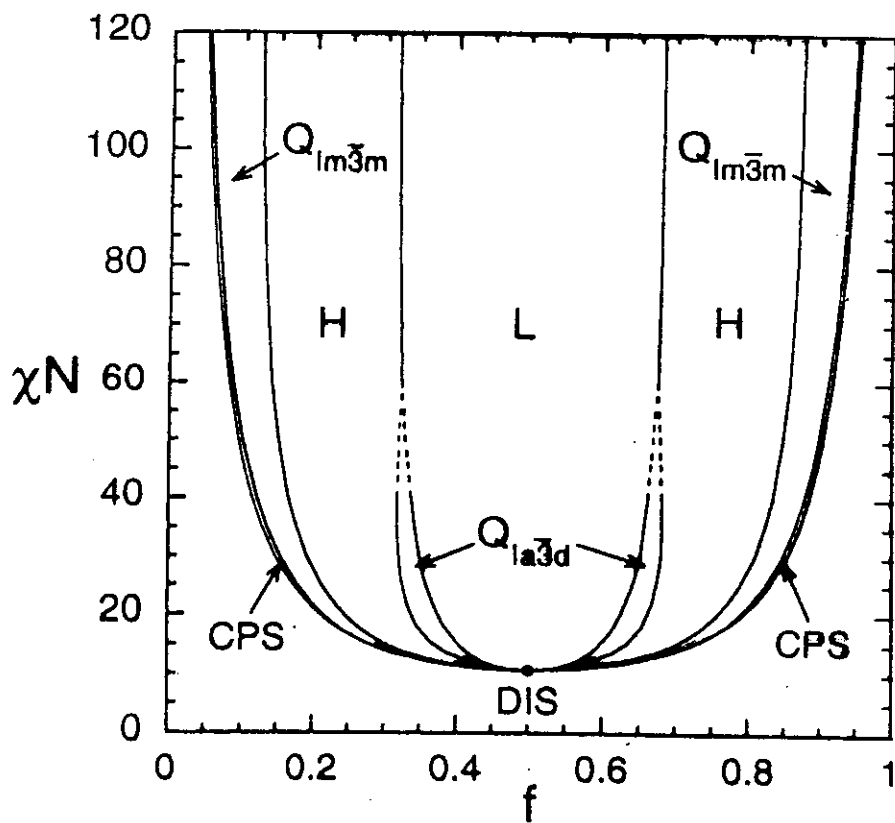


Figure 4, Matsen and Bates, *Macromolecules (Review)*
29, 1091 (1996)

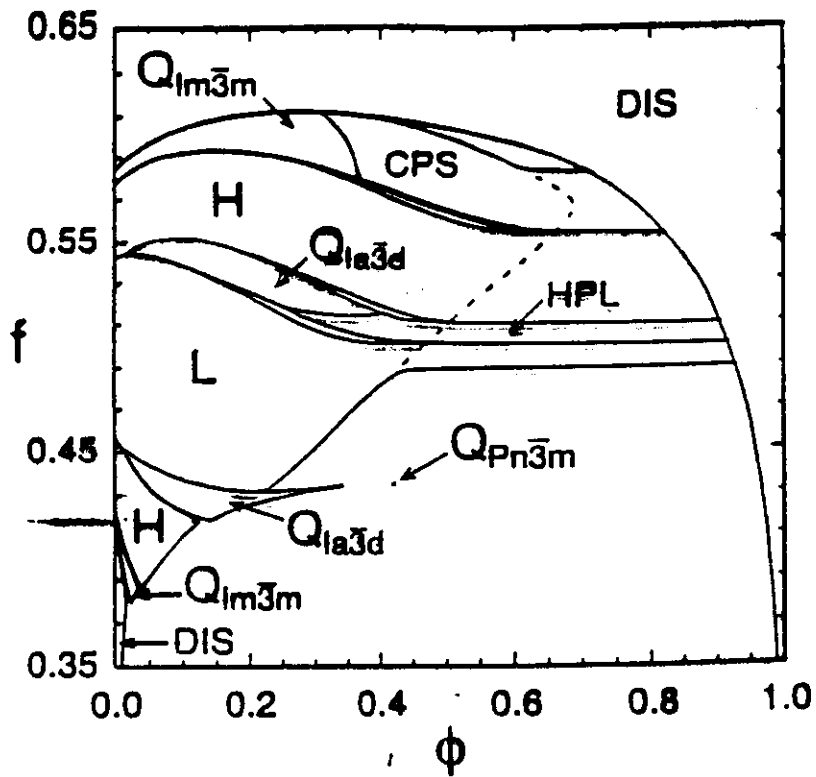
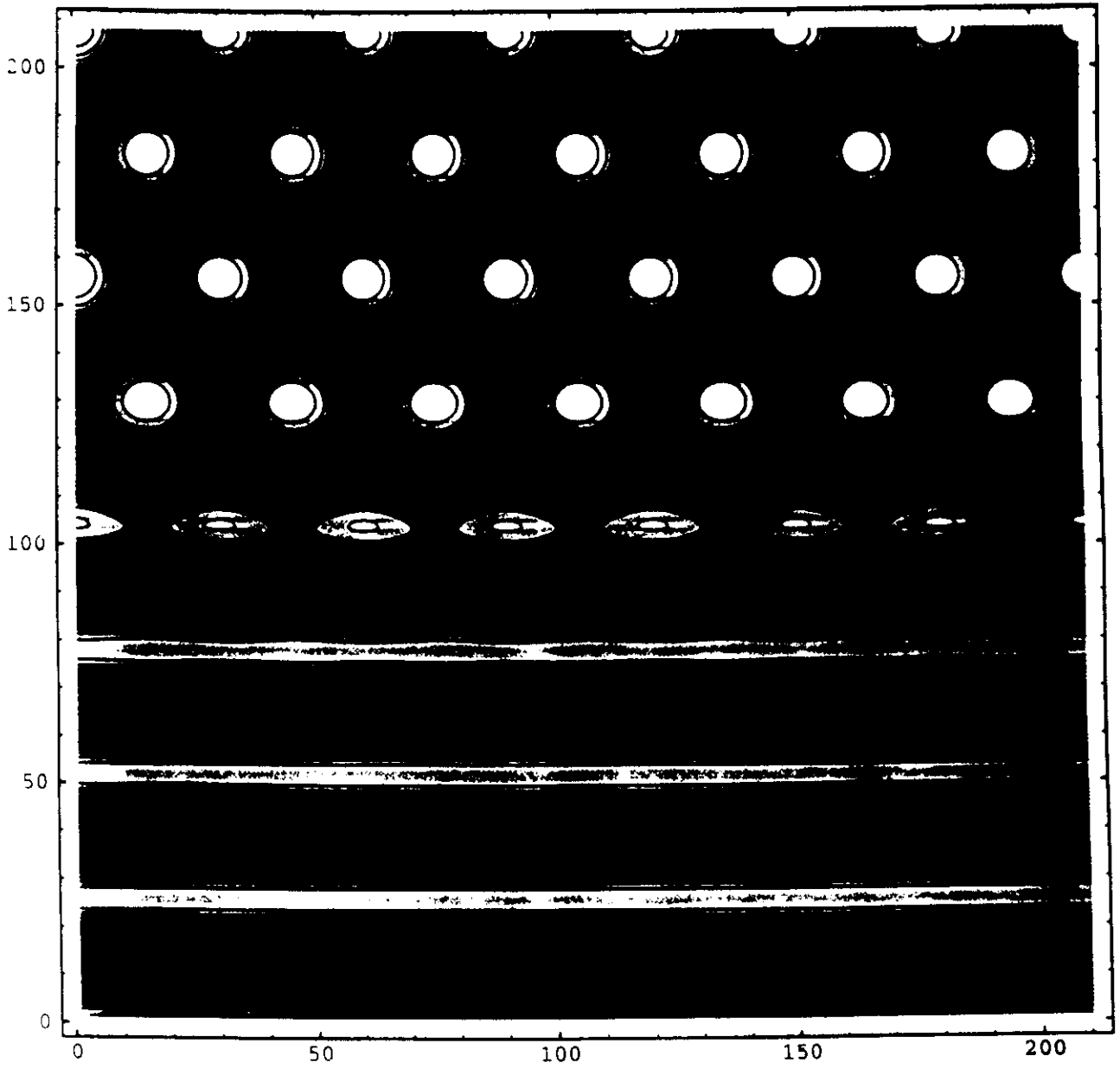


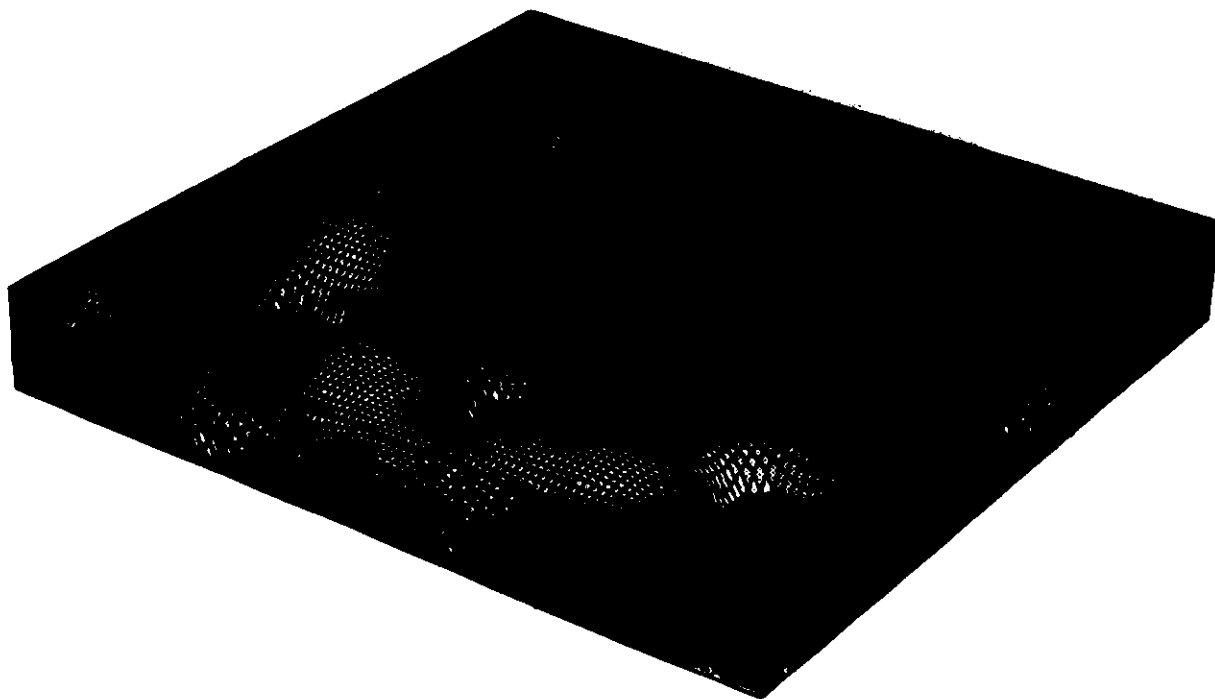
FIG. 1. Phase diagram for blends of AB diblock and A homopolymer at $\chi N = 11$ and equal polymerization indexes ($\alpha = 1$) plotted in terms of the homopolymer volume frac-

MATSEN, PRL 74, 4225 (1995)

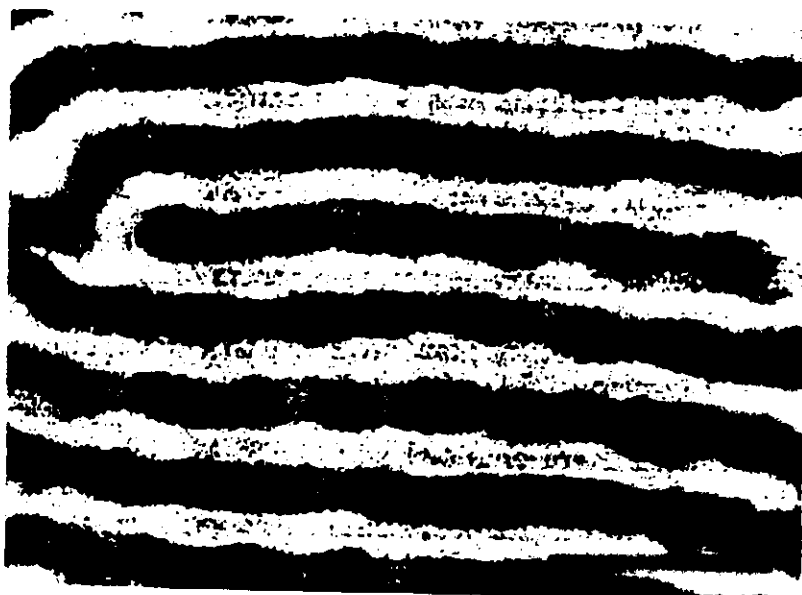
NOW ADD SOLVENT (A HOMOPOLYMER)
TO AB DIBLOCK



CATENOID LAMELLAR



CATENOID LAMELLAR PHASE OBSERVED



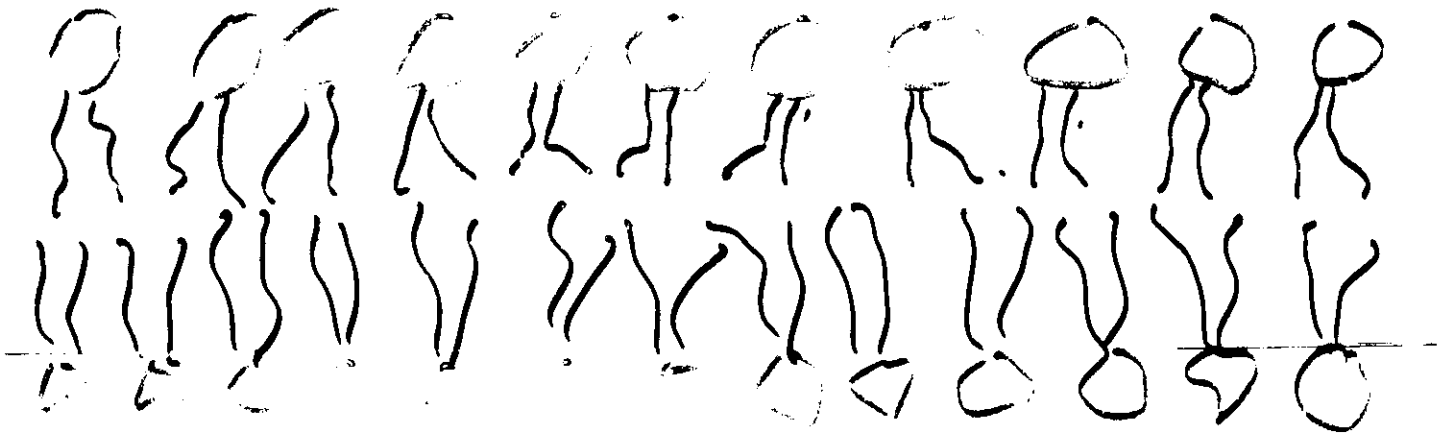
(a)

Figure 2. Transmission electron micrographs of an OsO₄-stained sample prepared from symmetric SB diblock for an edge-on view that is parallel to the lamellas (a) and a view normal to the layers (b). The shapes of punctured butadiene layers suggest a catenoidal shape for the butadiene layers. Scale markers are 100 nm.

STYRENE-BUTADIENE

DISKO ET AL. MACROMOLECULES 26, 2983 (1993)

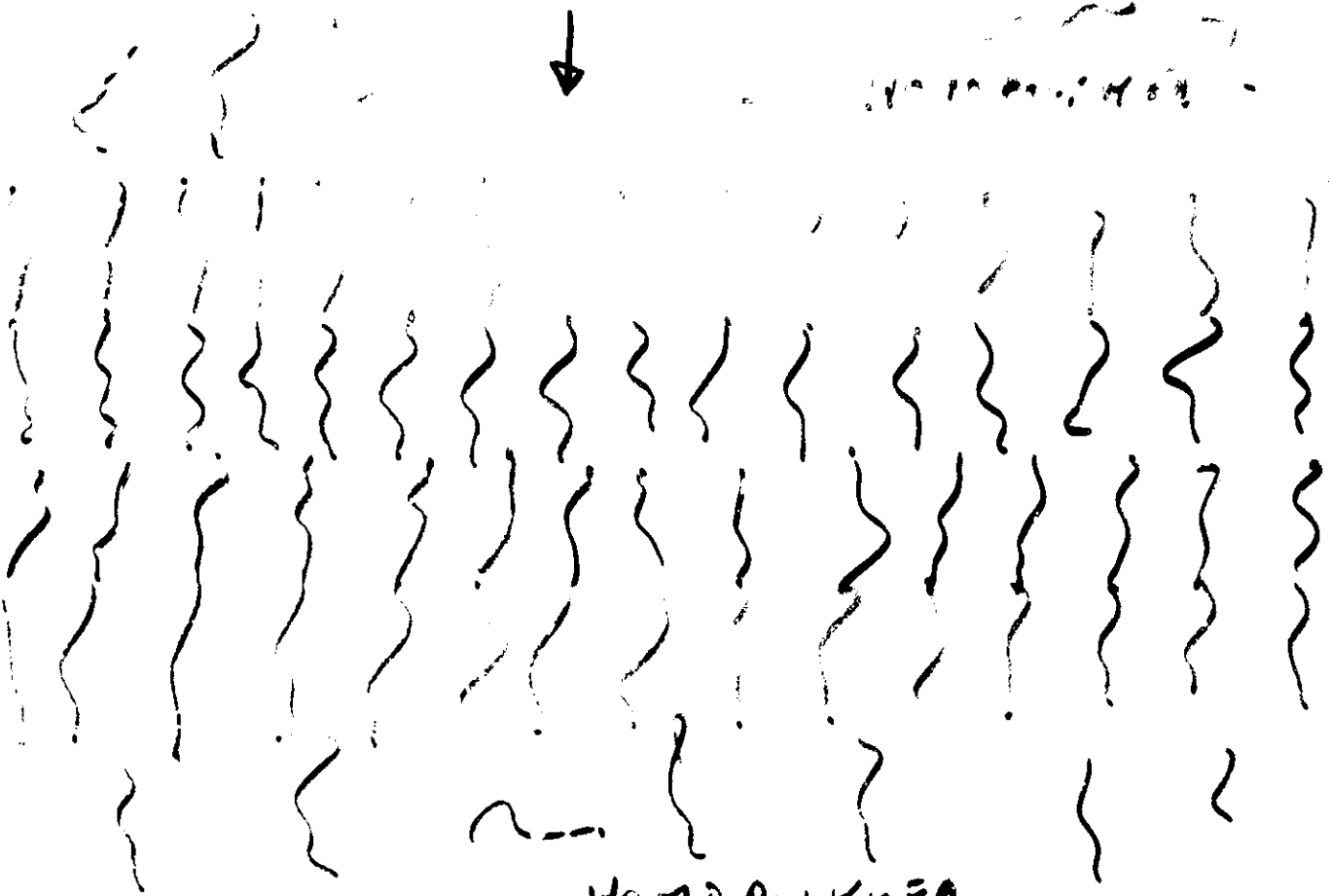
WATER



WATER



WATER

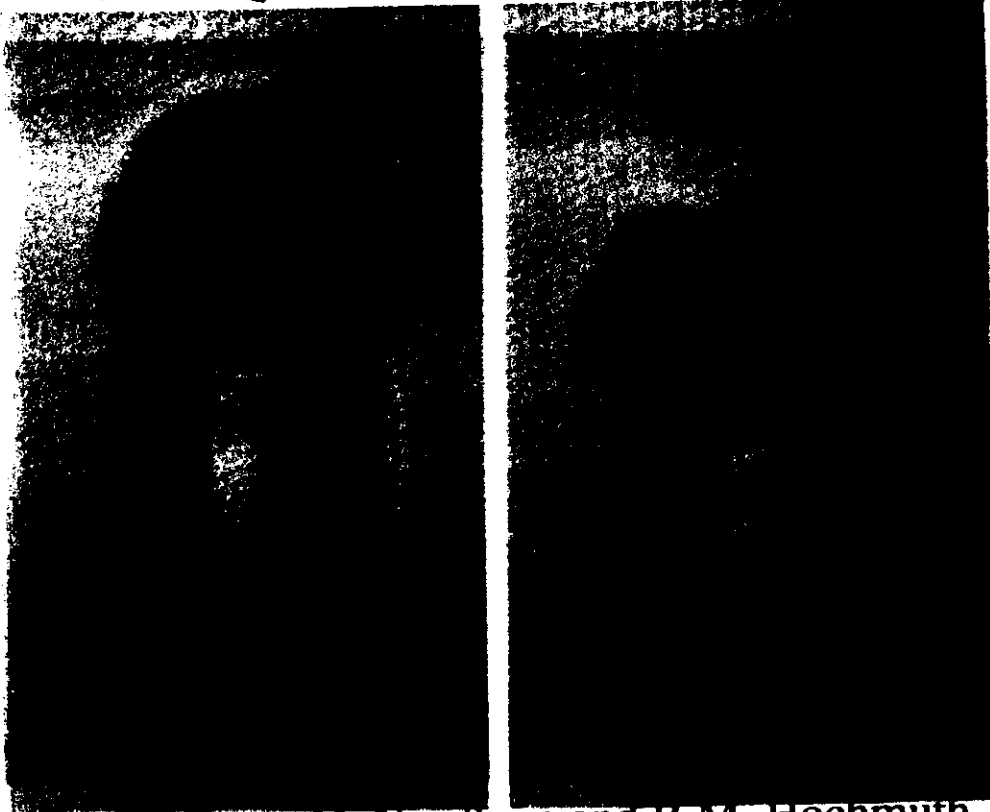
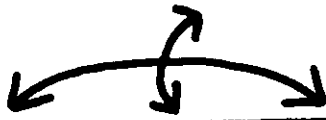


HOMO POLYMER

membrane rupture - vesicle aspiration techniques

E. Evans

surface tension



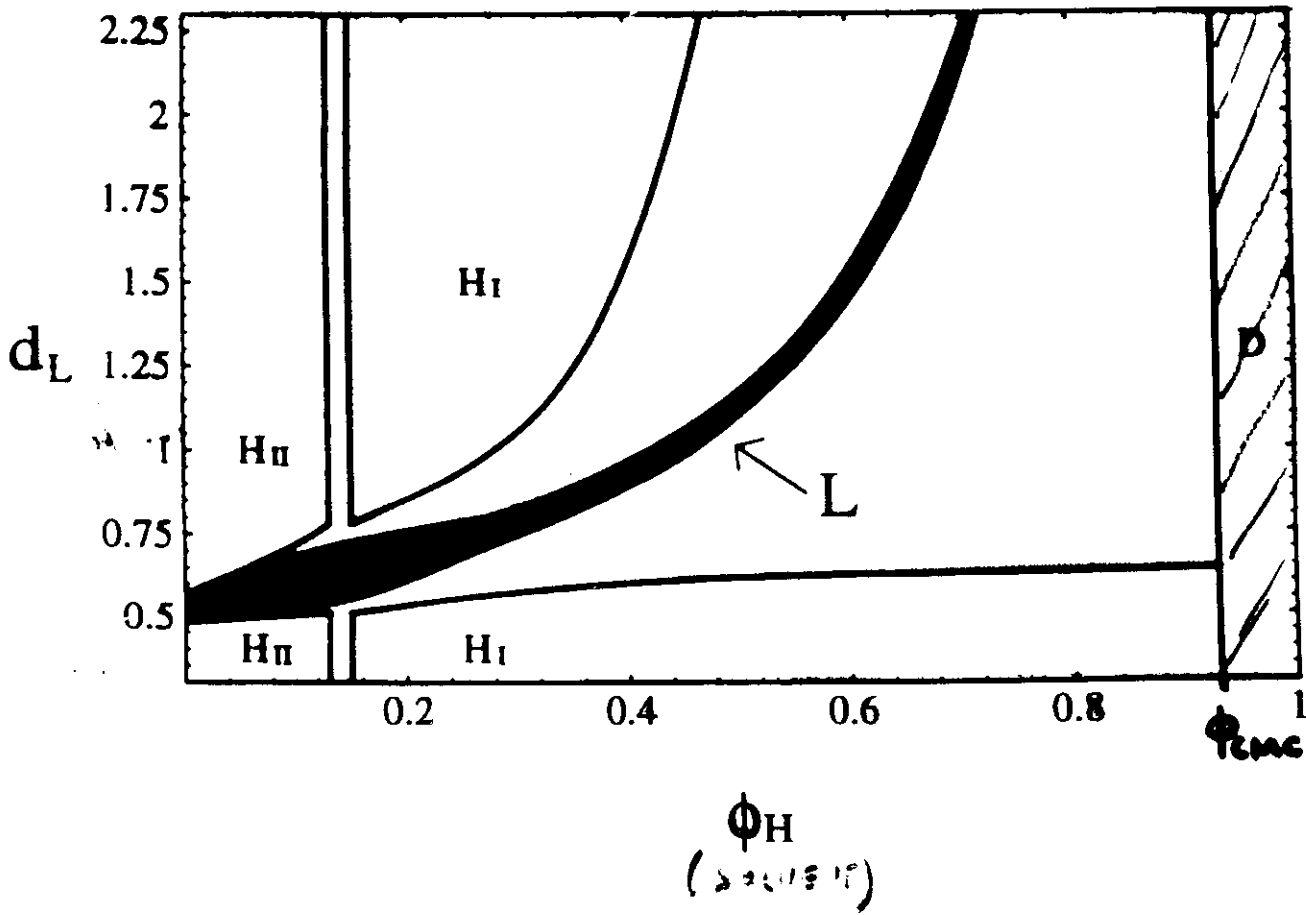
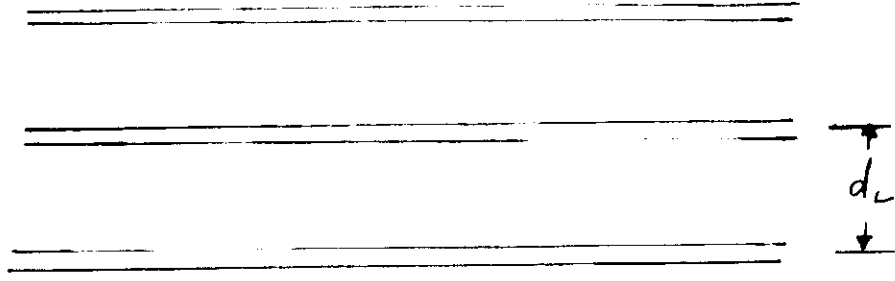
electric
field
pulse

tion
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D. Needham and R.M. Hochmuth
D. Needham and R.M. Hochmuth
Biophysical Journal, 1989
Biophysical Journal, 1989

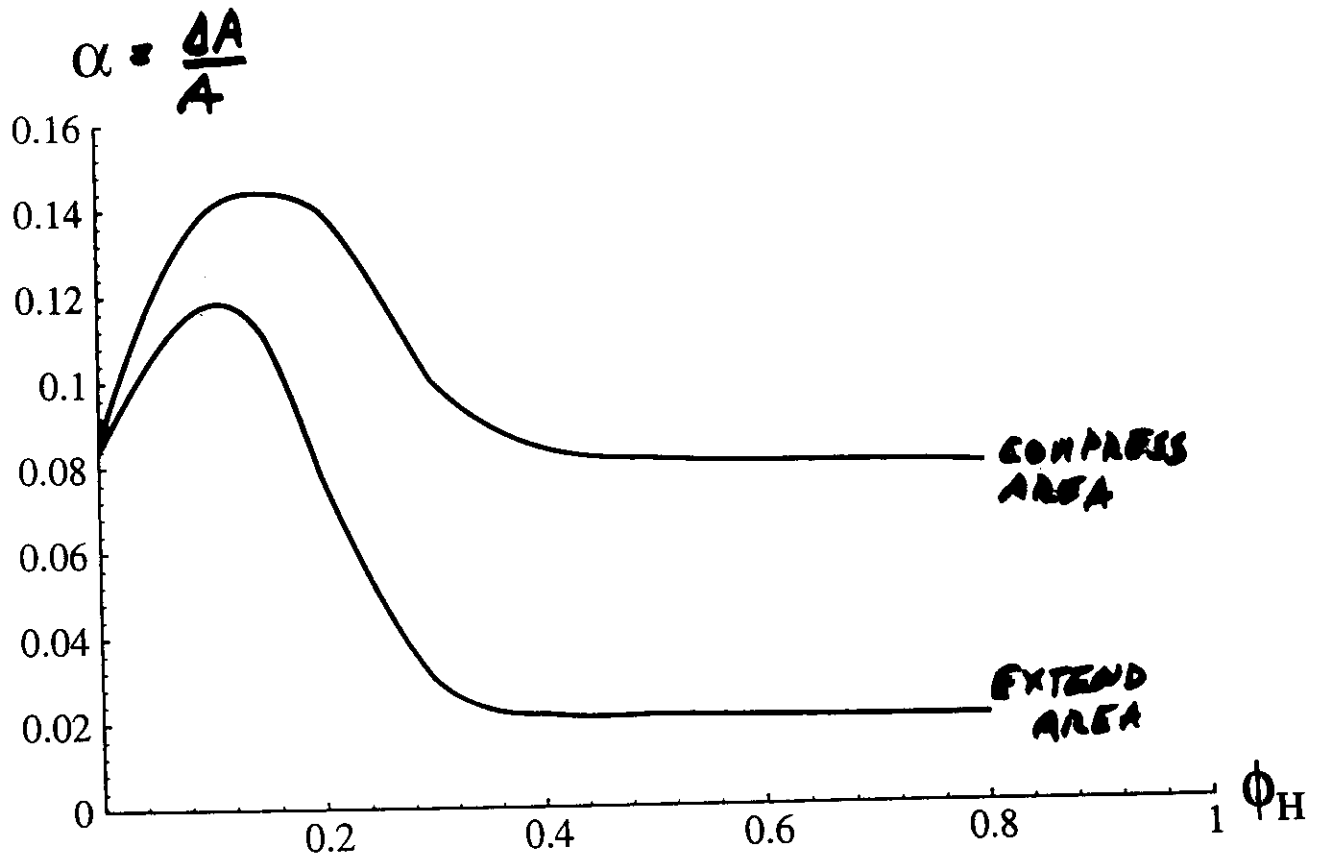
area extension at rupture: 2% - 5%



$f = 0.49$ (BULKY TAILS)

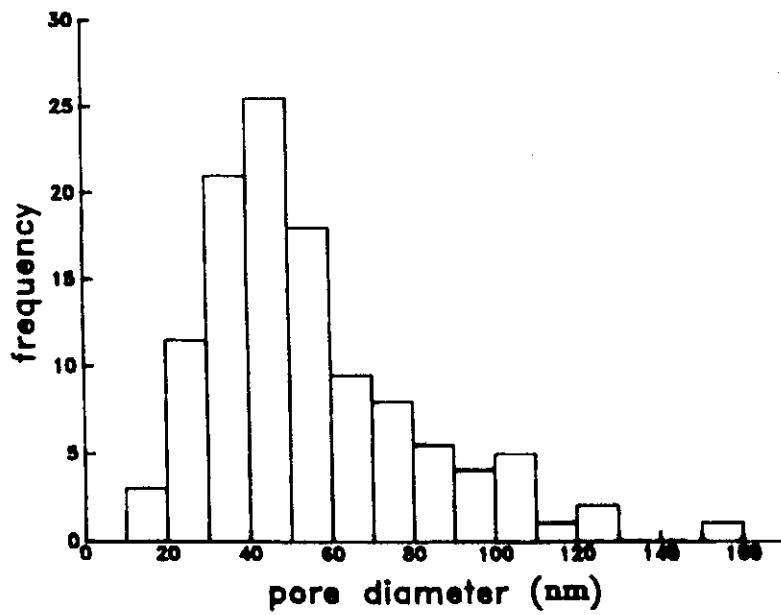
W. DEEZ & M. SCHICK, PRE 53, 3875 (1996)

Netz and Schick, Fig.4



FORMATION OF PORES

D.C. Chang, 1992



GUIDE TO ELECTROPORATION AND ELECTROFUSION, ed by D.C. CHANG ET AL,
(ACADEMIC, SAN DIEGO, 1992)

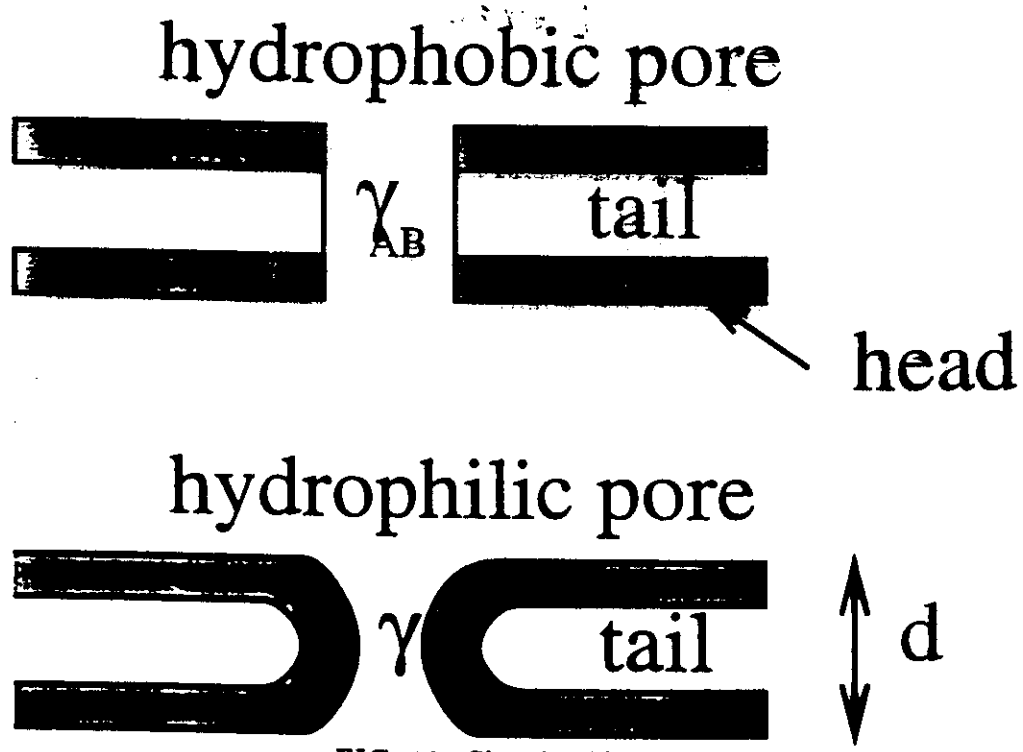
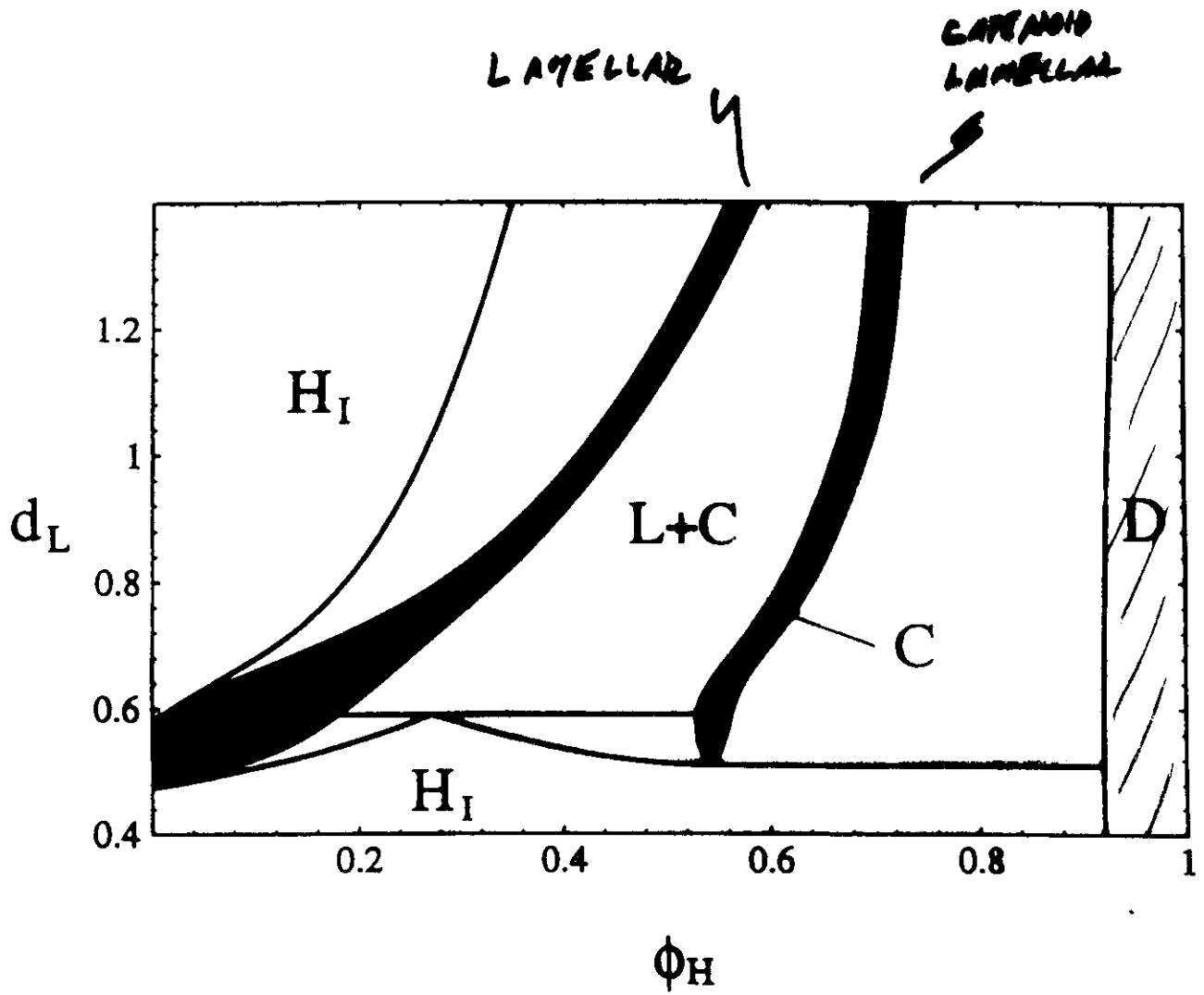
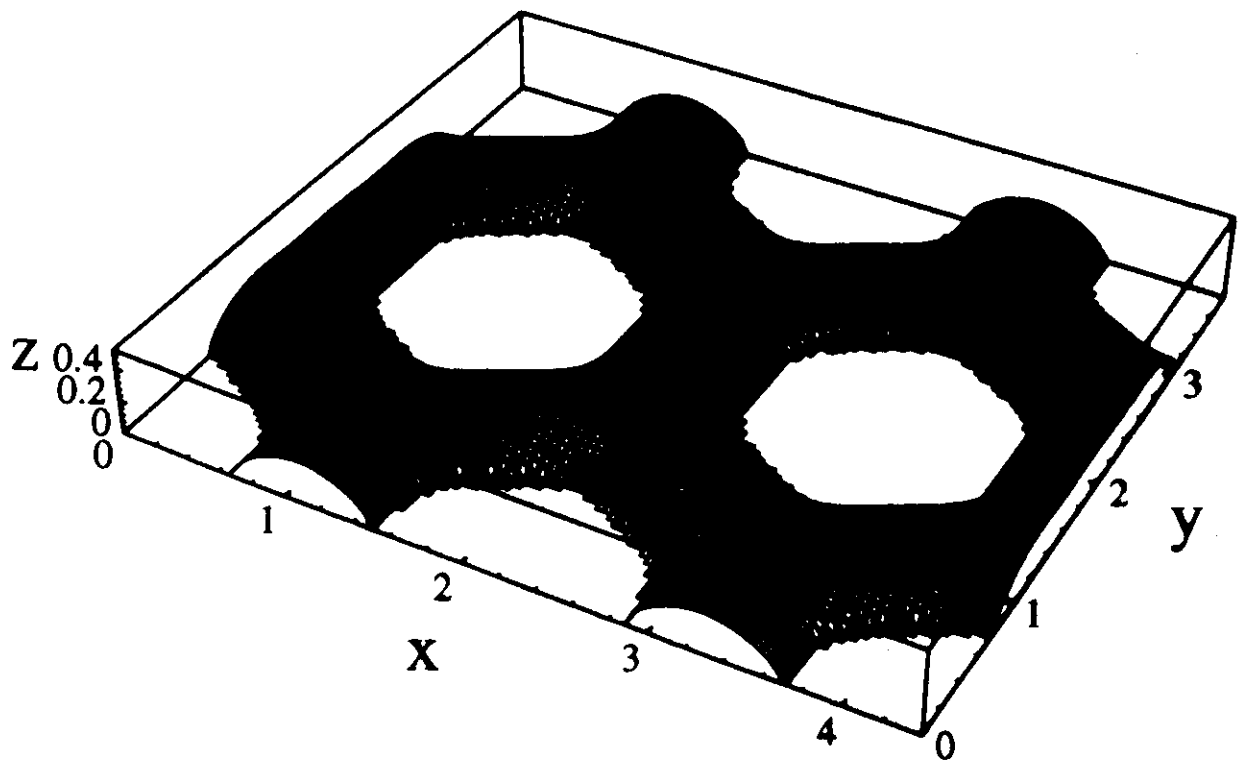


FIG. 18. Sketch of large hydrophobic and hydrophilic pores.

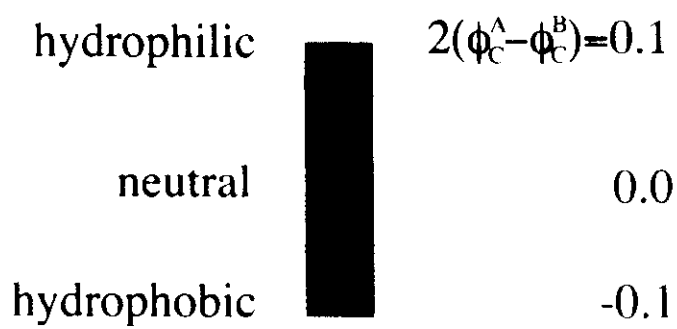
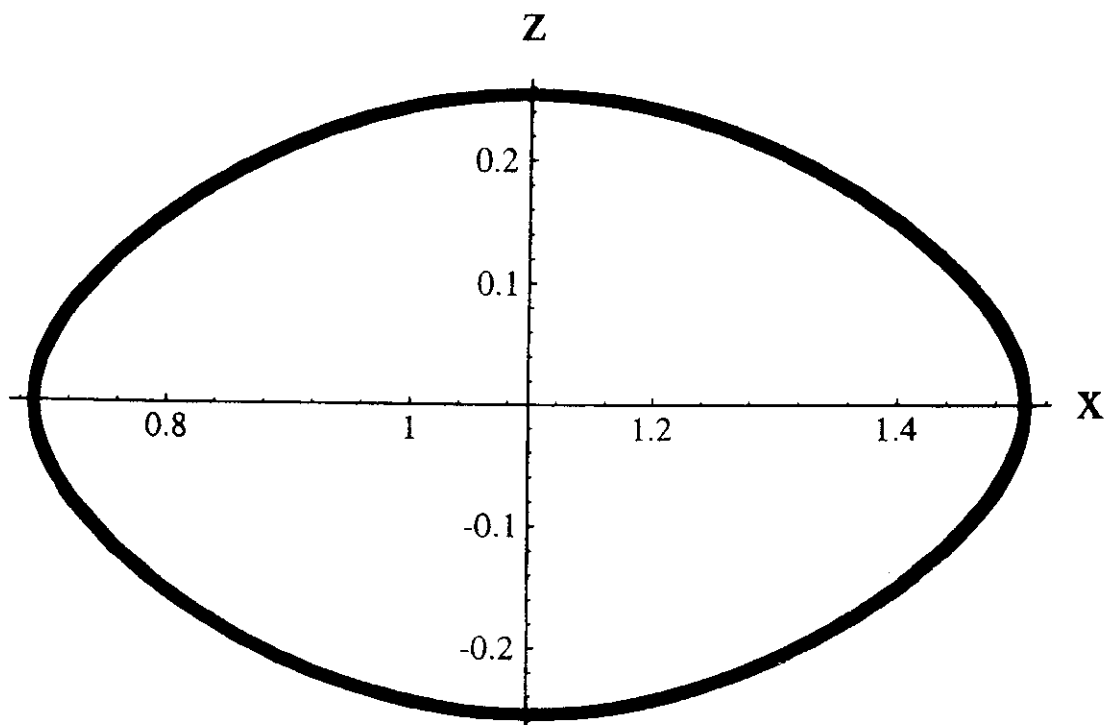
CHANGE ARCHITECTURE OF POLYMER
SLIGHTLY ($f \approx 0.5$)



CLOSE PACKED ARRAY OF PORES IN EQUILIBRIUM



distances in units of
the radius of gyration



MONTE CARLO SIMULATION

Bond Fluctuation Model (Carmesin and Kremer, *Macromolecules* **21**, 2819 (1988).)

Simple cubic lattice $L \times L \times 2L$, $L=64$ or $524,288$ sites, lattice constant u

A monomer is represented by a cube which blocks eight corner sites

Adjacent monomers are connected via one of 108 bonds of length ranging from $2u$ to $\sqrt{10}u$

Chain lengths $N_a = N_{AB} = 32$

Kuhn length $a = 3.05u$

Radius of gyration $R_g = 6.93u$

Monomer volume fraction = 0.5

$\chi N \approx 25$

MARCUS MUELLER

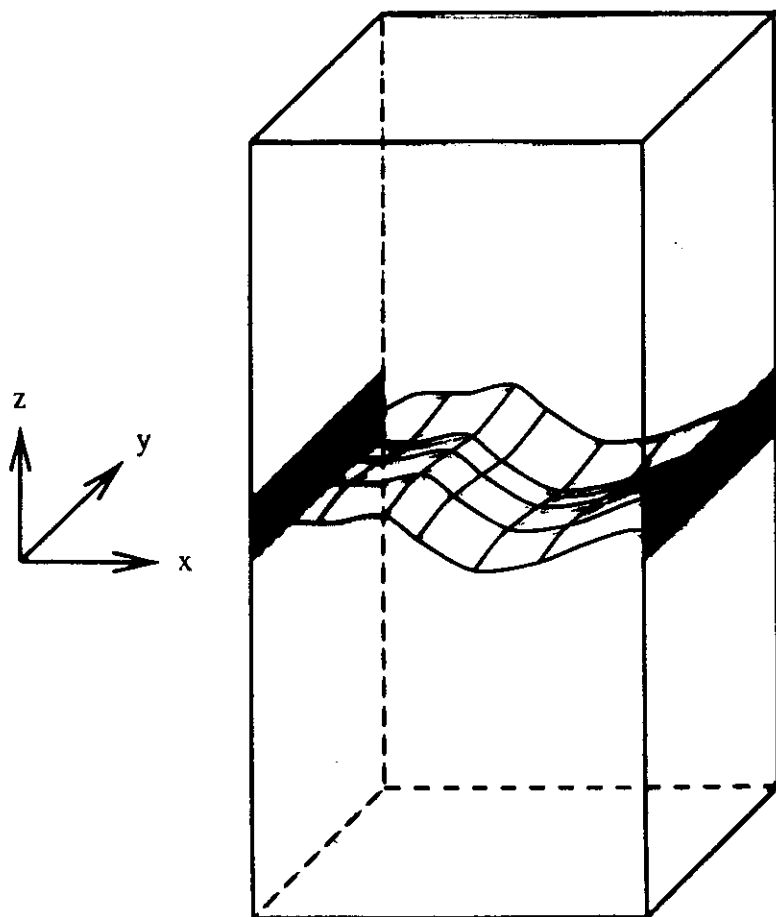


FIG. 1. Sketch of the simulation cell. Periodic boundary conditions are employed in the x and y direction, while there are impenetrable walls in z direction. The light shaded areas of the hard walls attract hydrophobic segments, whereas the dark shaded favor hydrophilic ones. A bilayer forms around $z = 64$ in the xy -plane.

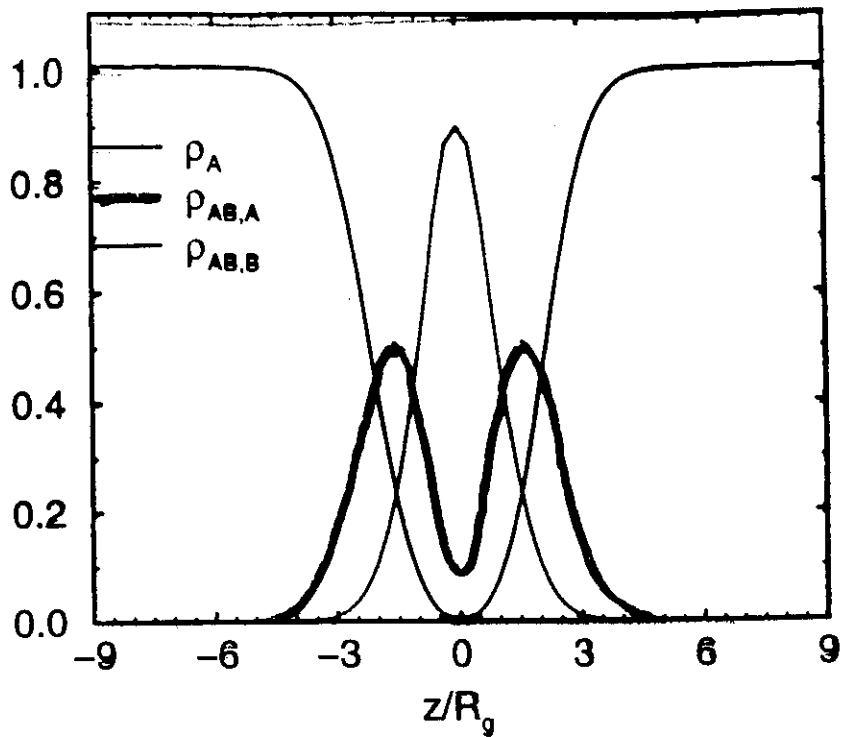
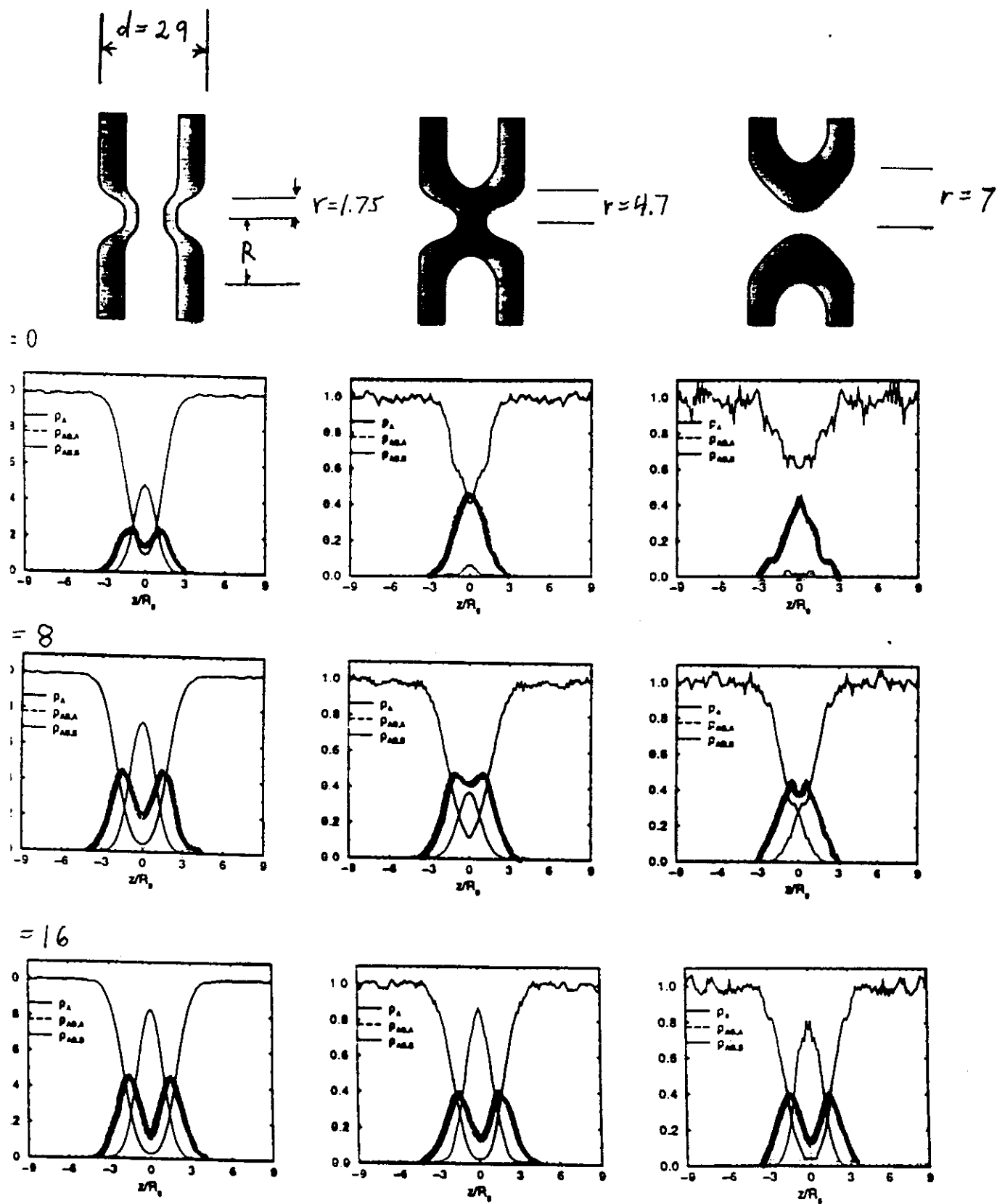
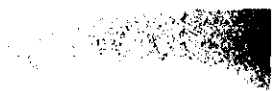
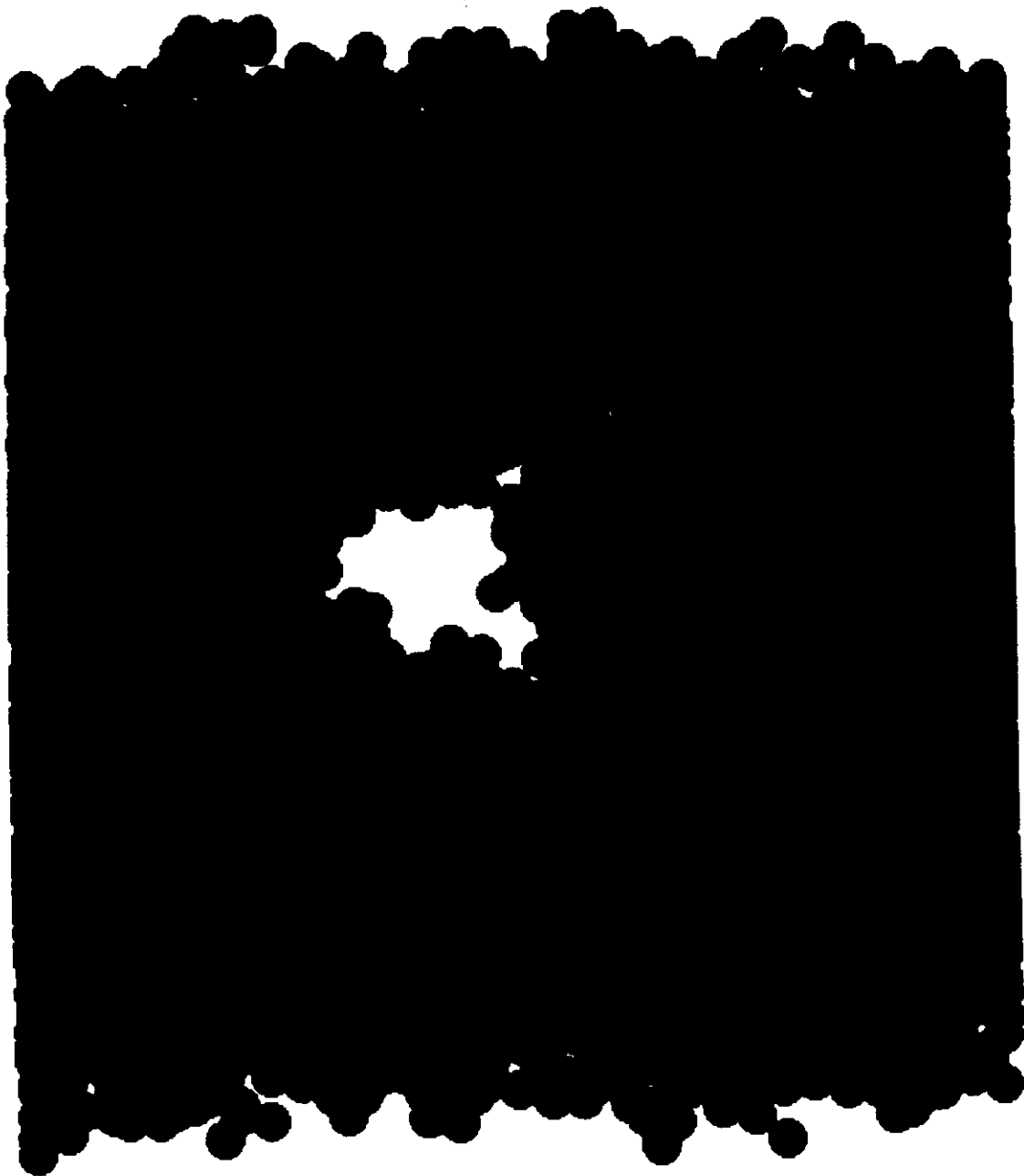


FIG. 4. Composition profile across a bilayer at $\epsilon = 0.15$ and $\Delta\mu = 4.5$. The solid line shows homopolymer, the dashed line corresponds to the head segment density of the amphiphile, and the thin solid line to the tail segment density.





What is the free energy/unit, γ , area of this bilayer?

Obtain it from the fluctuation spectrum

of bilayer position $u(\mathbf{r})$

$$H = \frac{\gamma}{2} \int dx dy (\nabla u)^2$$

From equipartition

$$\frac{2}{L^2 \langle u_q^2 \rangle} = \gamma q^2$$

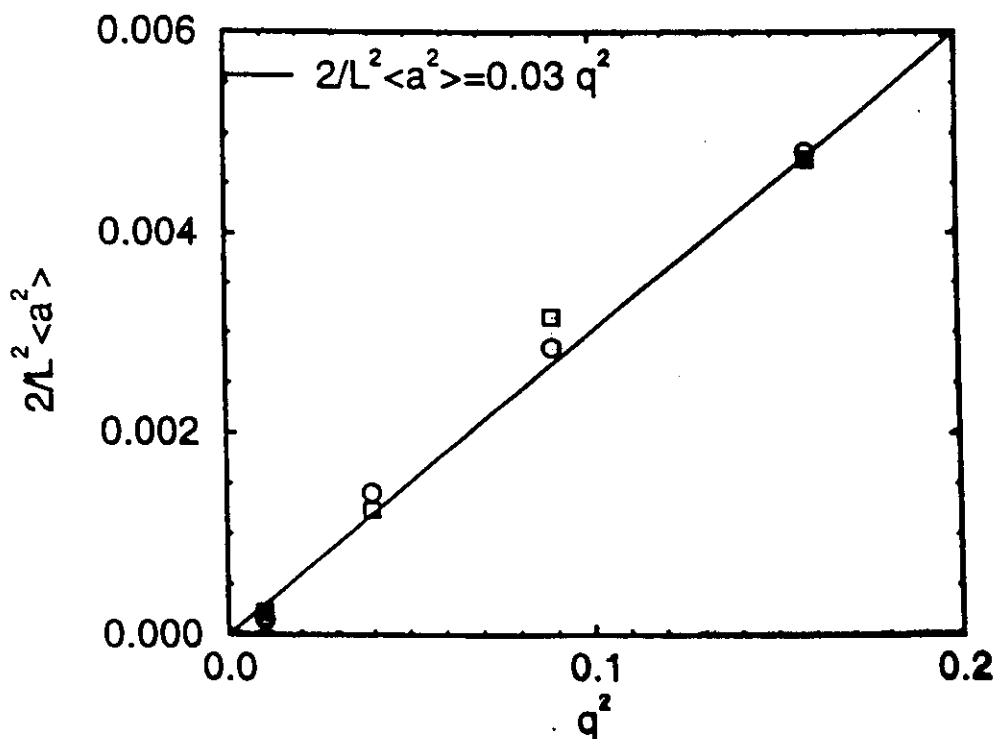


FIG. 8. Low wavevector regime of the bilayer undulation spectrum at $\epsilon = 0.15$ and $\Delta\mu = 0.5$. SOLID LINE corresponds to a tension of $\gamma = 0.030(5)$.

$$\gamma < 2\gamma_{AB} = 0.132$$

What is the line tension of the pore?

Obtain it from the distribution of pore sizes, $P(r)$

$$\ln P(r) = -\delta f = -2\pi r\Gamma + \pi r^2\gamma + \text{constant}$$

Define

$$\Gamma = r\gamma - \frac{1}{2\pi} \frac{d}{dr} \ln P(r)$$

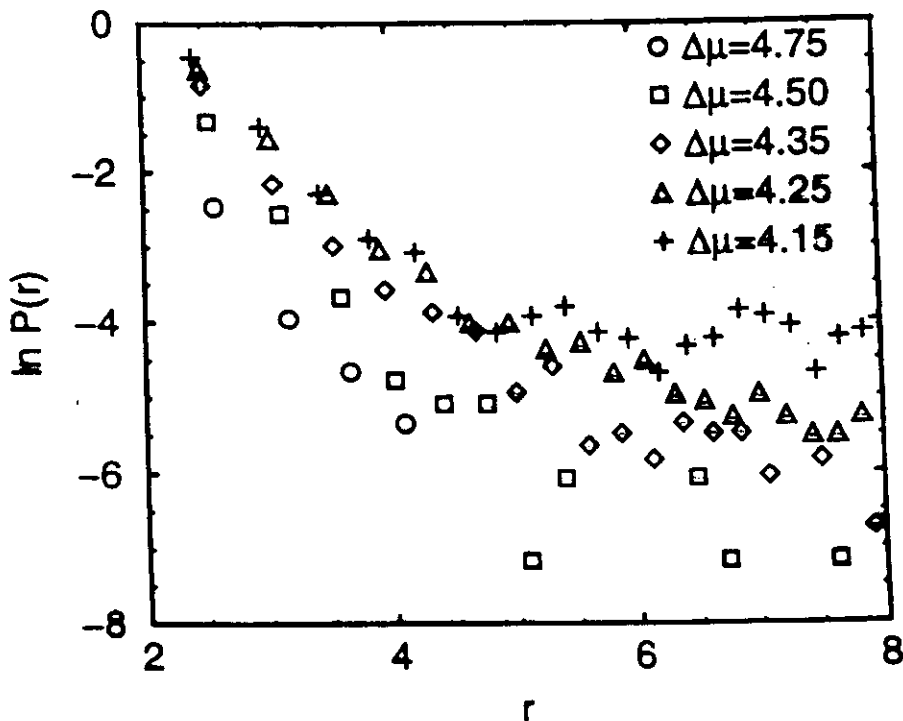
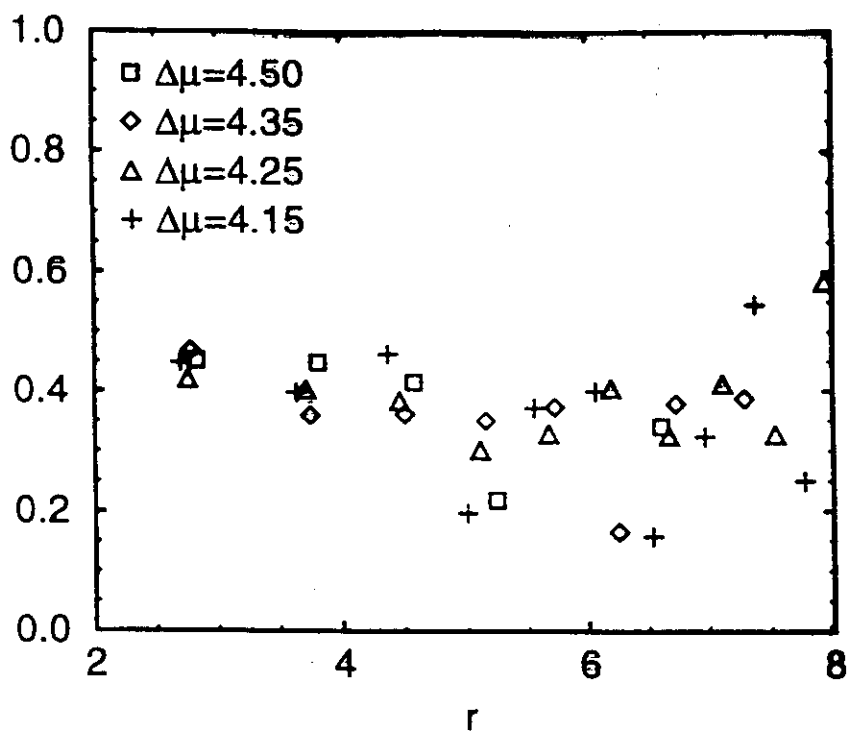


FIG. 15. Probability distribution of pore sizes at various chemical potentials. In the accessible range of pore sizes, no preferred pore size can be observed.



G. 17. Simulation results for the effective edge tension Γ for various chemical potentials. The edge tension is largely independent of the chemical potential of the amphiphile and of the size of the pore.

SUMMARY OF BILAYER PROPERTIES

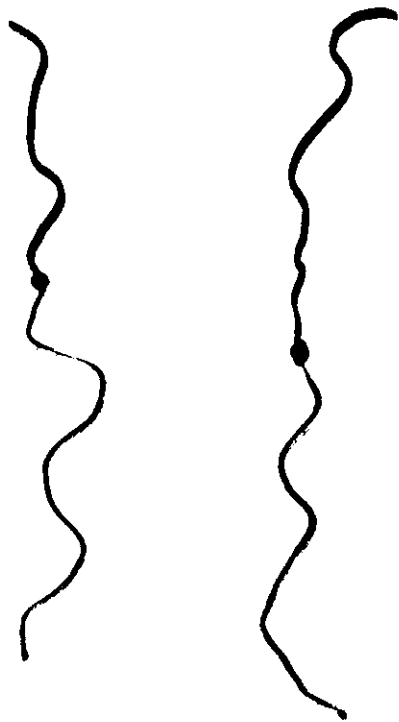
Equate bilayer thickness to 30\AA

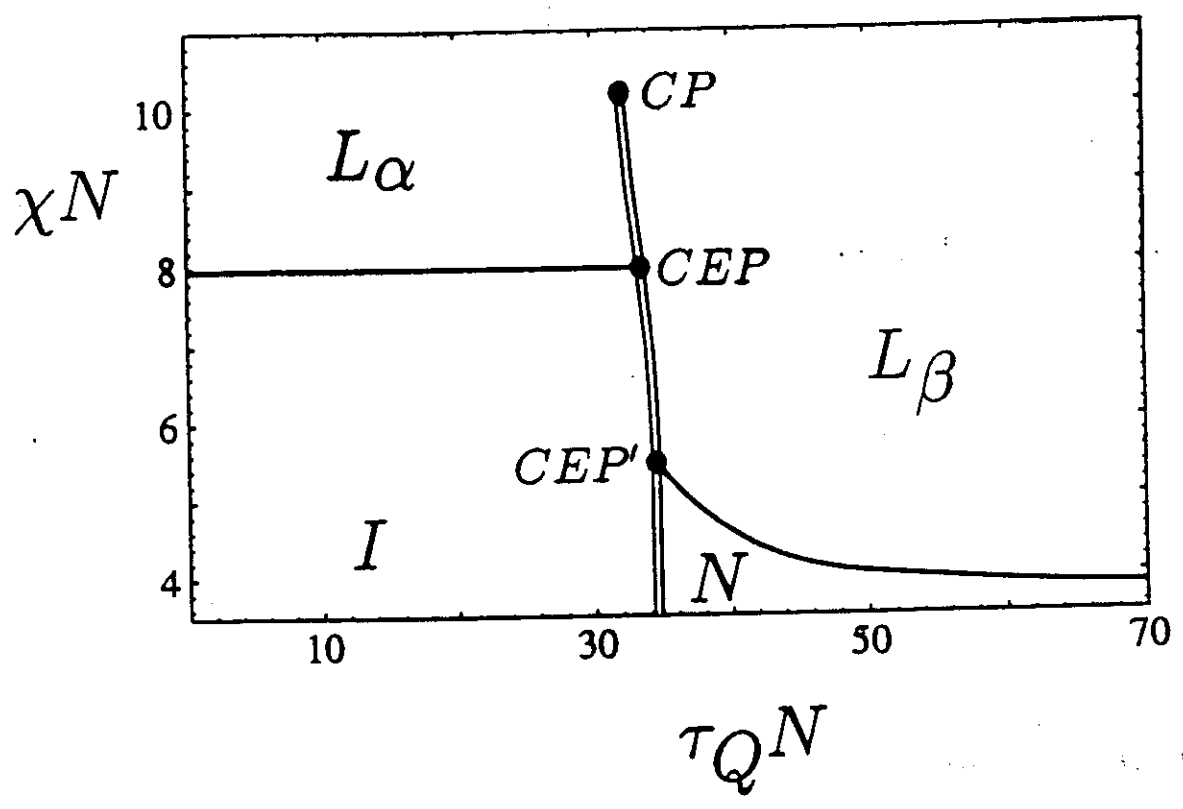
1. γ_{AB} (oil/water tension) $\approx 27 \text{ erg/cm}^2$ (c.f. 50 erg/cm^2)
2. γ (membrane tension) $\approx 12 \text{ erg/cm}^2$ (c.f. 1 erg/cm^2)
3. area per tail $\approx 35\text{\AA}^2$ (good agreement)
4. surface compressibility modulus $\approx 83 \text{ erg/cm}^2$ (120 erg/cm^2 for phosphatidylcholine)
5. line tension $\Gamma \approx 1.7 \cdot 10^{-6} \text{ erg/cm}$ (correct order of magnitude)

Bilayers of Semi-Flexible Copolymer

Interactions

$$\chi \int d\mathbf{r} \hat{\Phi}_A(\mathbf{r}) \hat{\Phi}_B(\mathbf{r}) - \tau_Q \int d\mathbf{r} S^2(\mathbf{r})$$





R. R. NETZ + M. S.

PRL JULY 1996

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PHILIPP JANERT

MICHAEL WIRTH

FRANK JÜLICHNER

PATO

HUMBOLDT STIFTUNG

NSF