



UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION
INTERNATIONAL ATOMIC ENERGY AGENCY
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
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SMR.961 - 10

**WORKSHOP ON:
PROTEINS, MEMBRANES and their INTERACTIONS**

22 JULY - 2 AUGUST 1996

**"Structure and thermodynamics of
tethered polymer layers and their ability
to prevent protein adsorption"**

PART II

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These are preliminary lecture notes, intended only for distribution to participants.

Theoretical Studies of PEO tethered layers:

pressure isotherms and prevention of protein adsorption

theoretical "ideas".

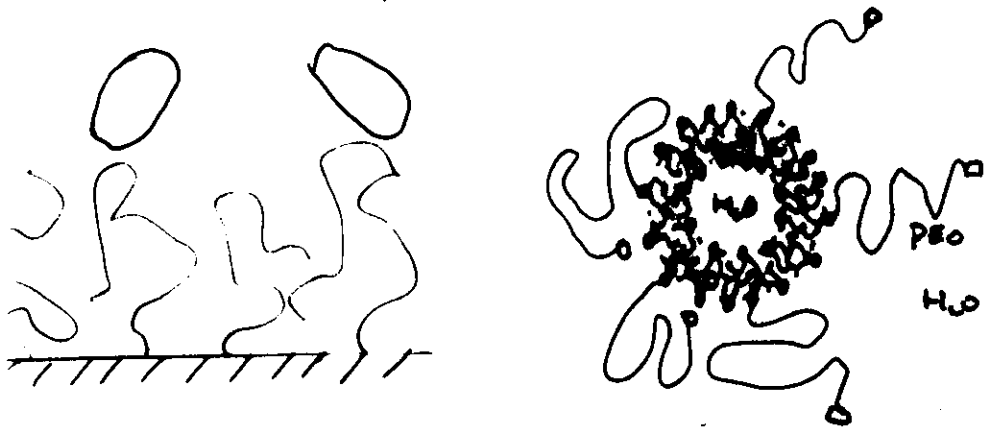
PS-PEO at water-air interface.
comparison with experimental observations

protein adsorption on pluronic modified surfaces.

summary.

Motivation: biocompatible surfaces, surface

modified liposomes, ...



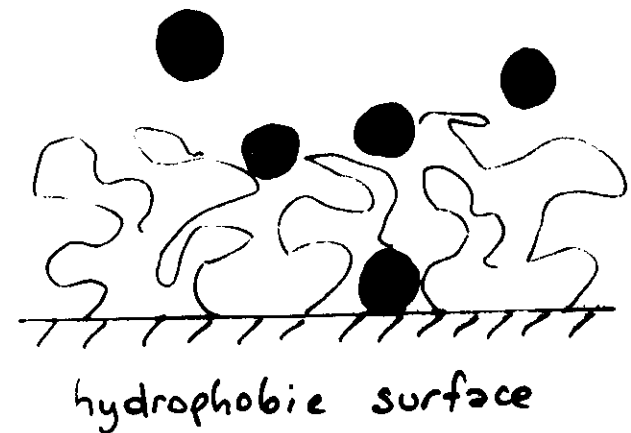
Biocompatible surfaces:

1) Prevention of blood-protein adsorption
(no platelet adhesion to surface).

2) Contact lenses: prevent lysozyme
adsorption (build up).

Grafted polymers can solve the problem!!

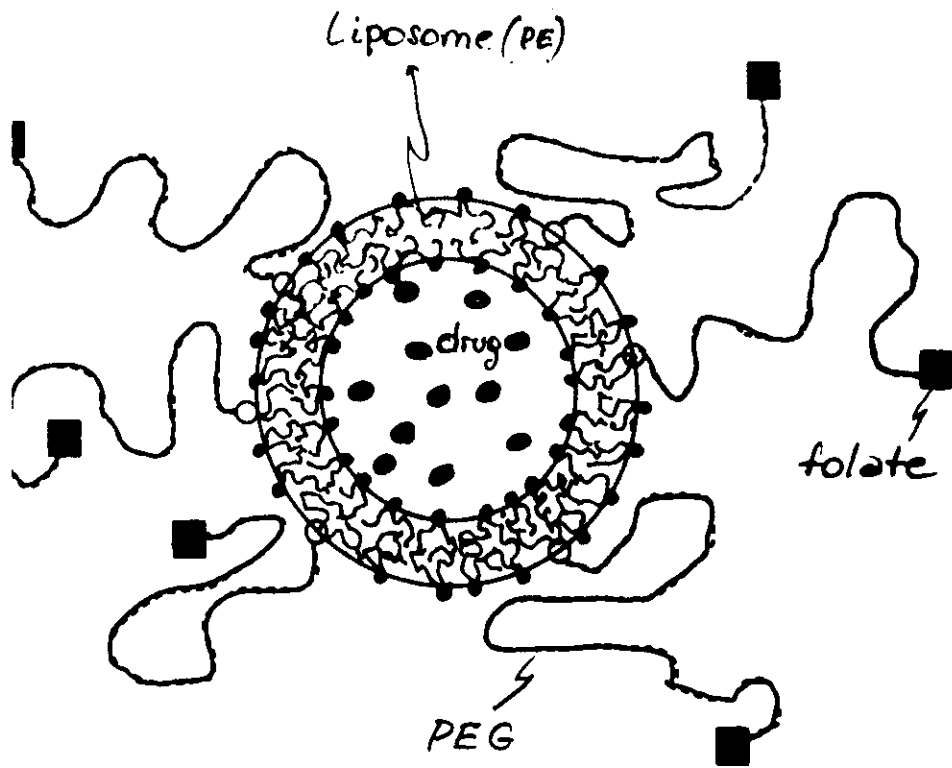
PEO (PEG) $-(CH_2-CH_2-O)_n$ (steric barrier)



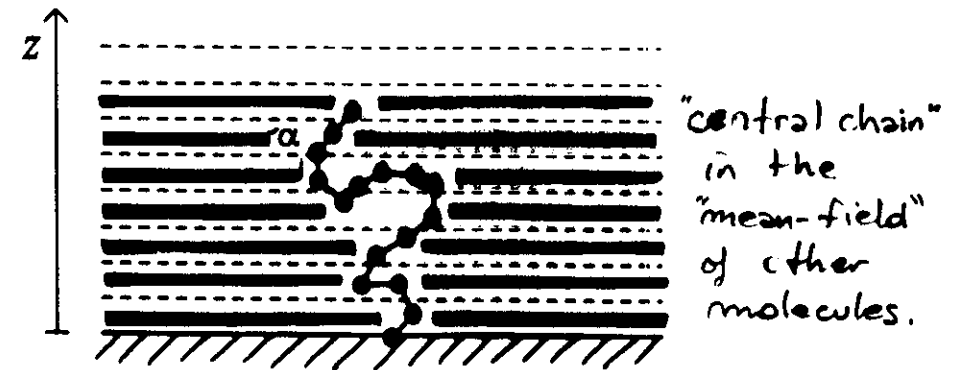
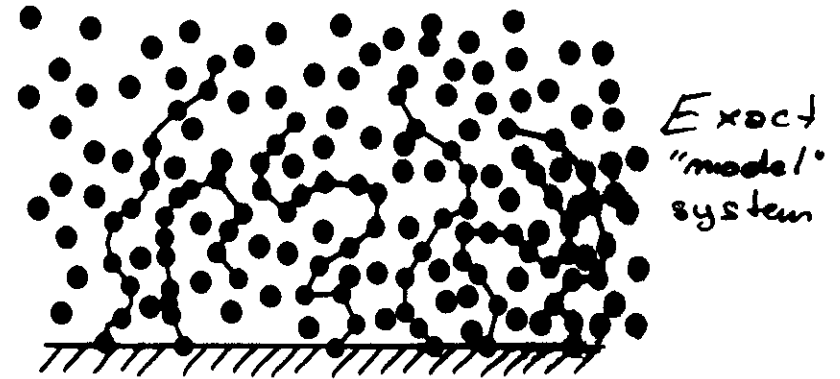
Is this the right picture? nature of PEO,
experimental problems.

Drug delivery:

(Prof. P. Low) specific uptake of liposomes by KB cells.



Theoretical Approach: single-chain mean-field theory.



$P(\alpha)$: probability distribution function of chain conformations.

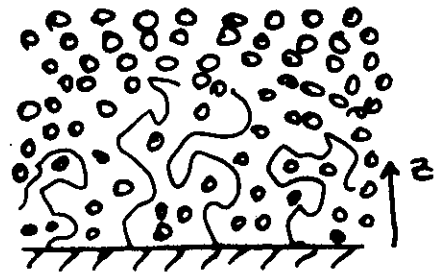
From $P(\alpha)$ any average conformational and thermodynamic property can be calculated. $P(\alpha)$ is a function of surface coverage, quality of solvent, geometry of surface, etc.

Generalization of single-chain mean-field theory

Polymer-solvent mixture \Rightarrow packing constraints

$$\frac{N_P}{A} \langle n_p(z) \rangle v_0 + \phi(z) = 1 \quad z \geq 0$$

free energy density:



$$f = \sigma \int_0^L P(\alpha) \ln P(\alpha) + \int \phi(z) \ln \phi(z) dz - \beta \int \phi(z) \mu_s dz$$

Minimizing subject to constraints:

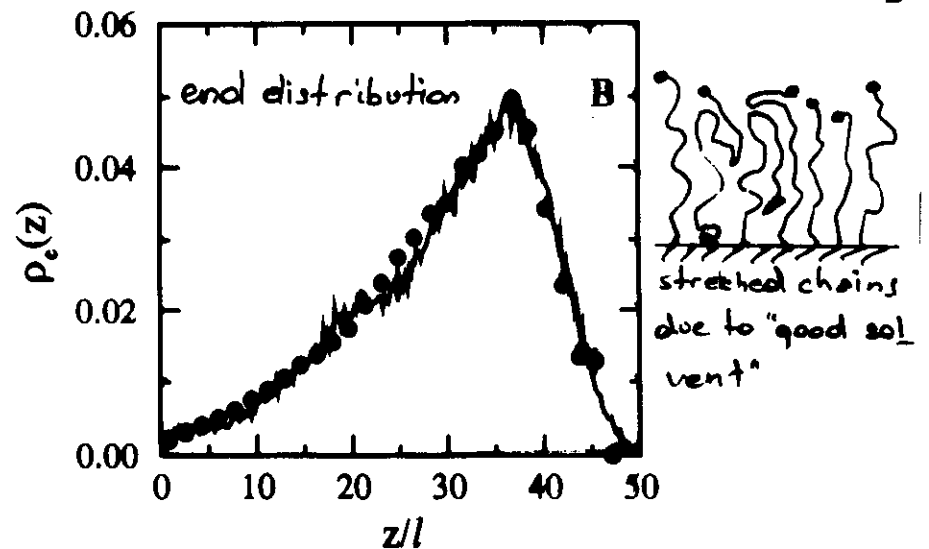
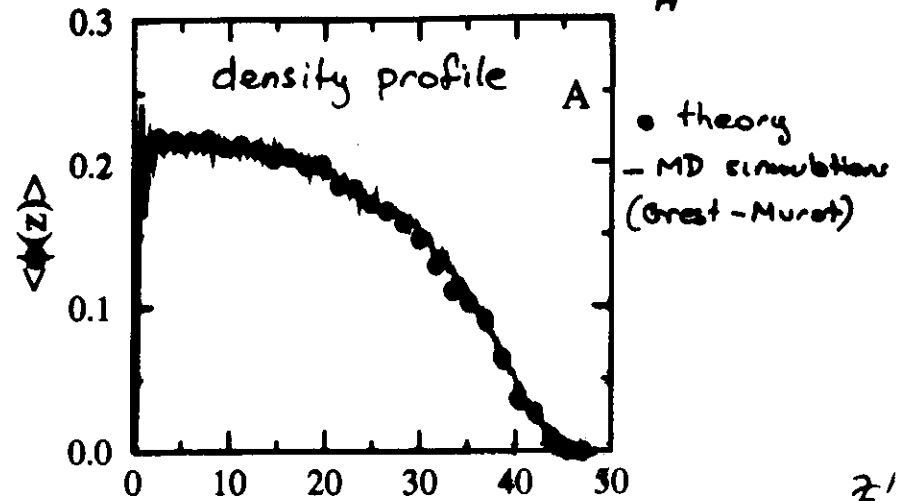
$$P(\alpha) = \frac{1}{\mathcal{Q}} e^{-\int \pi(z) n(z, \alpha) dz}$$

$$\phi(z) = e^{\beta \mu_s - \pi(z)}$$

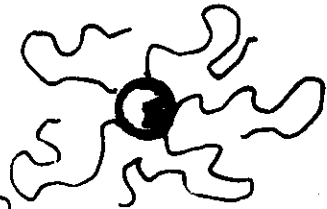
$\pi(z)$: lateral pressures related to osmotic pressure to keep $\mu_s = \text{const.}$ at all z .

$$\beta \frac{f}{A} = -\sigma \ln \mathcal{Q} - \int \pi(z) dz$$

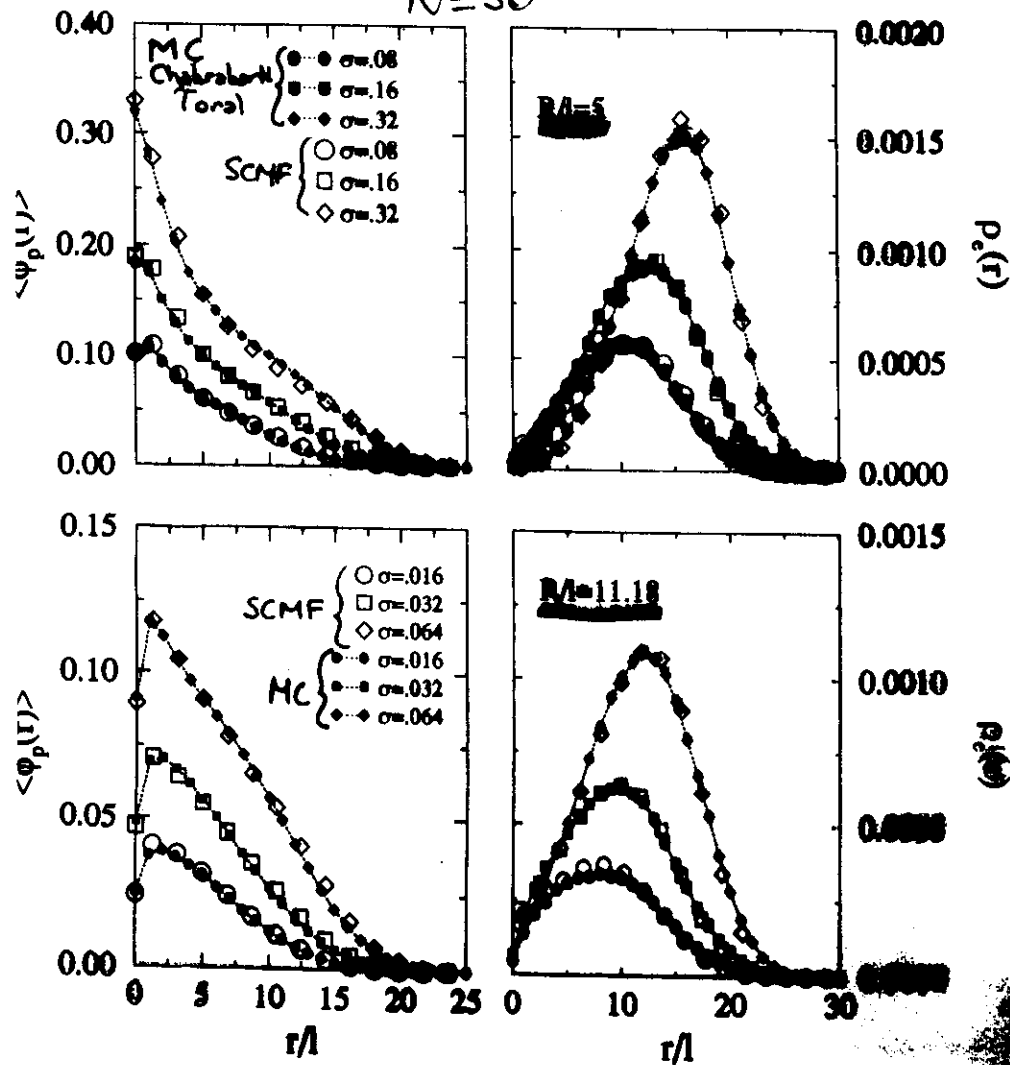
$N=100$ Good solvent $\sigma = \frac{N_P}{A} = 0.07$



Spherical Surfaces
Good Solvent

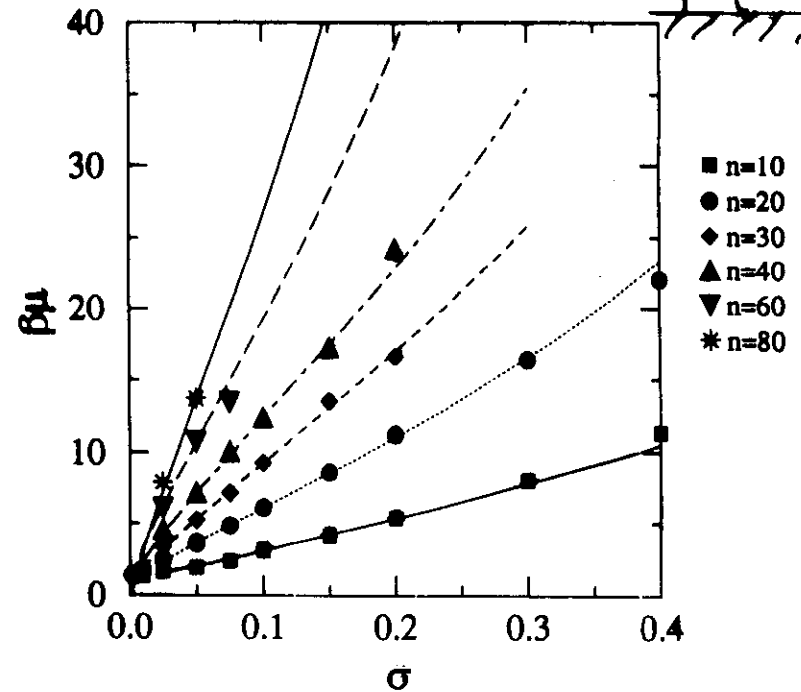
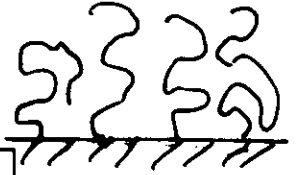


$N=50$



Polymer Chemical Potential.

$$\mu = \left(\frac{\partial F}{\partial N_p} \right)_{N_s, a, T}$$



symbols: MC simulations (S. Shaffer)

lines: SCMF theory

(lattice chain fluctuation band model)

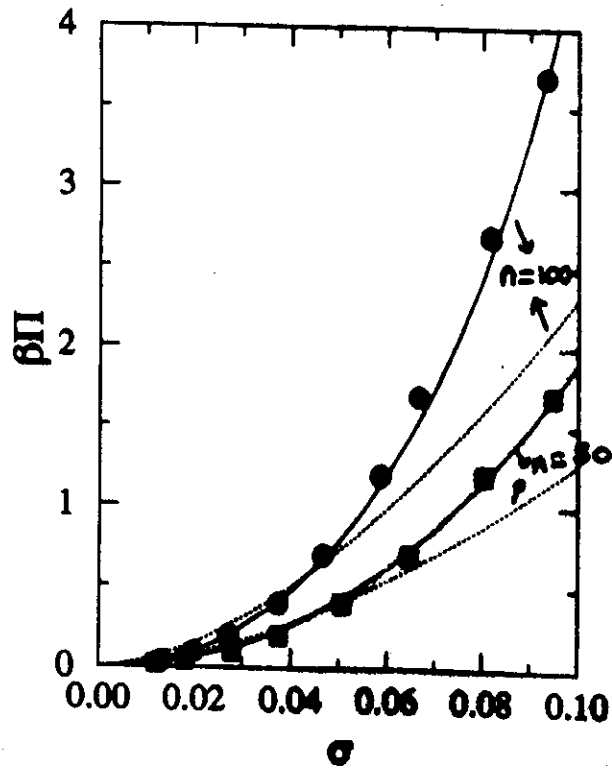
Pressure isotherms $\Pi = \left(\frac{\partial f}{\partial a}\right)$

Good solvent regime

■ ● MD simulations (Grest)

— single chain mean field theory

..... analytical SCF theory

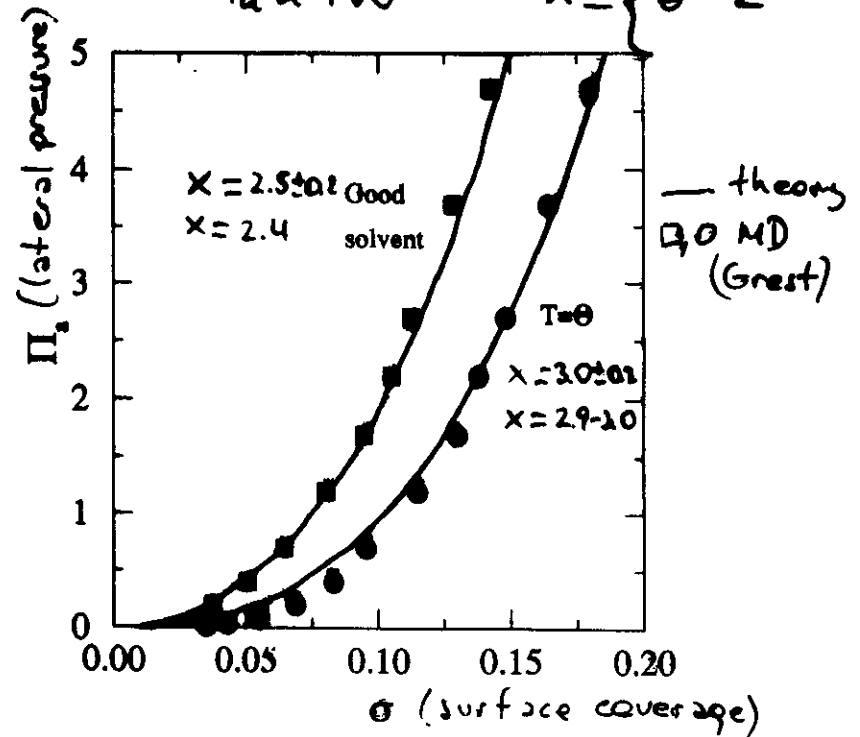


$$\Pi_a = \left(\frac{\partial f}{\partial a}\right)_{N_p, N_s, T}$$

$N = 50$

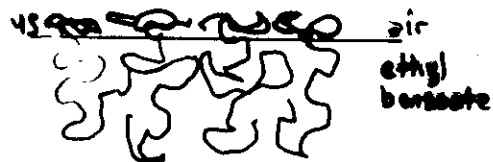
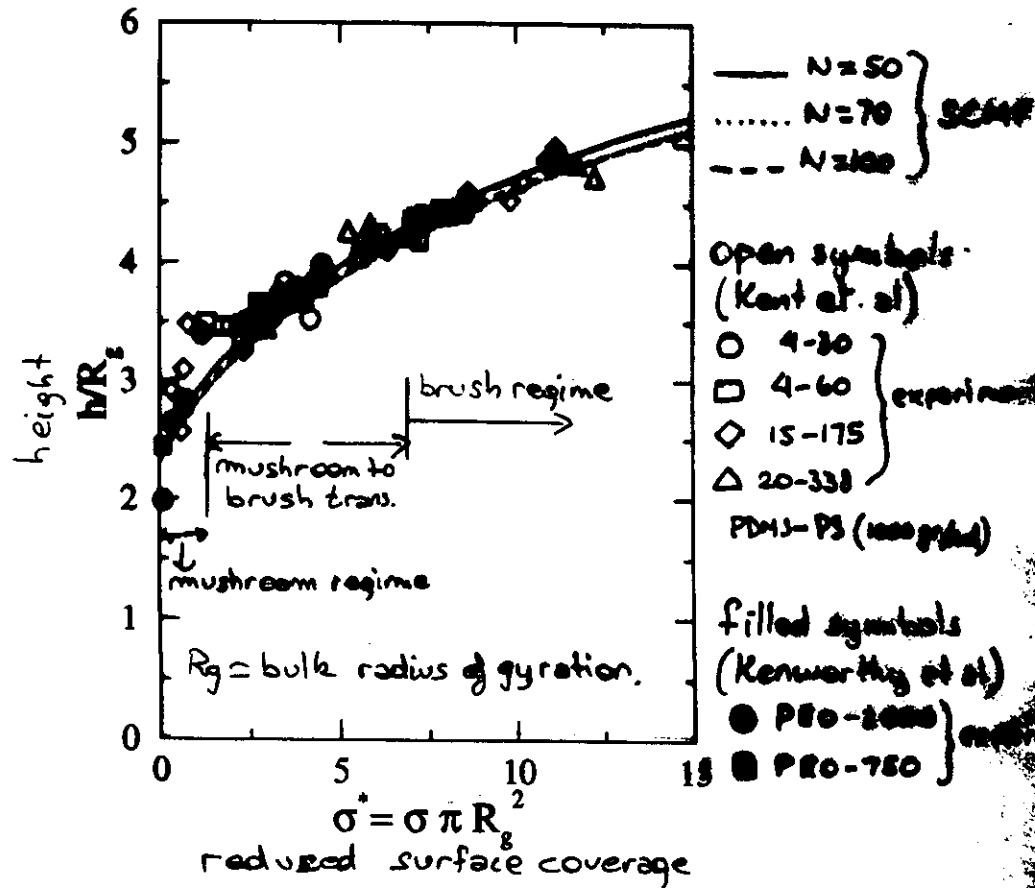
$$\Pi_a \propto N \sigma^x$$

	SCF	scaling
good solvent	5/3	11/6
θ	2	2

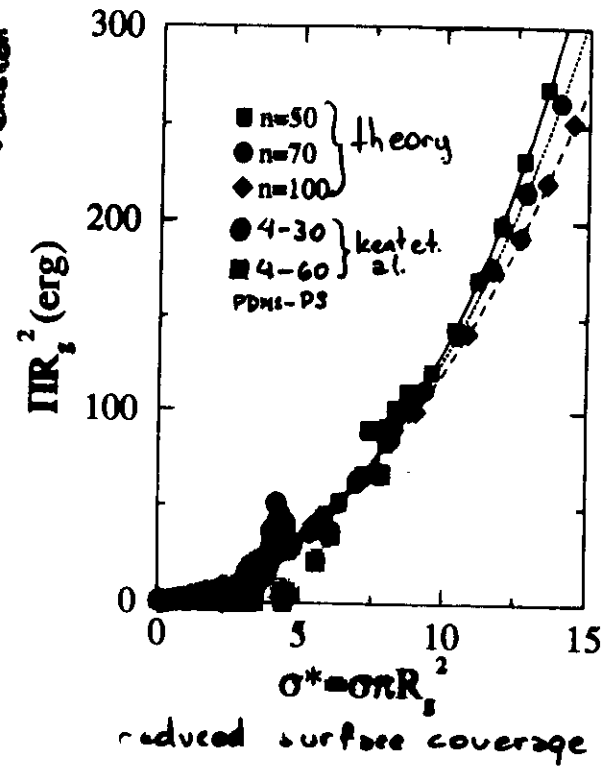


We find virial description better than scaling.

Height of polymer layer



lateral pressure (reduction of surface tension)



Why $T R_g^2$ vs σ^*

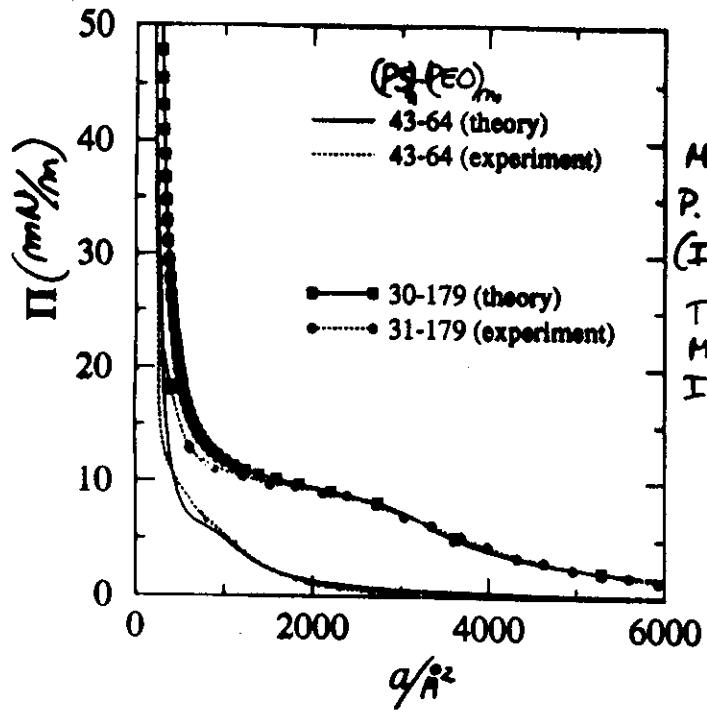
Very low σ we expect $T = A_2 \sigma^2$

$A_2 \propto R_g^2$ (like hard disks, Flory) then

$$T R_g^2 \propto (\sigma R_g^2)^2$$

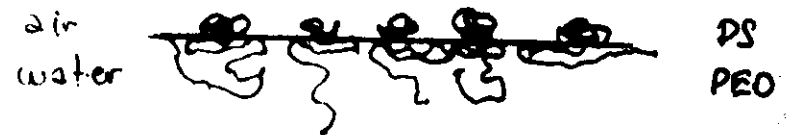
What about the structure?

Pressure-Area Isotherms PS-PEO at water-air interface

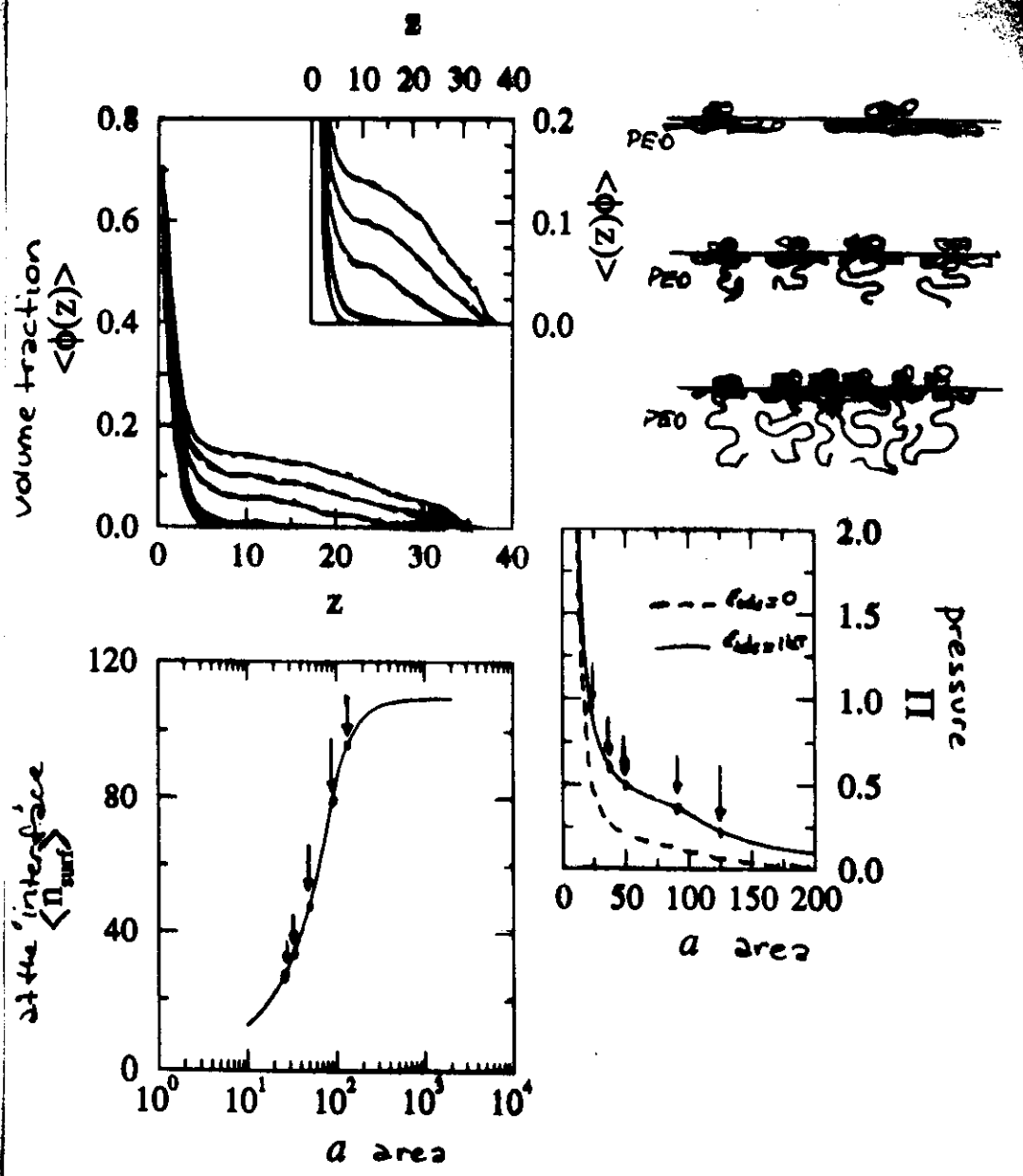


Measurements:
P. Bovey
(Institut Curie)
Theory:
M. A. Carignano,
I. S.

What is the origin of the "plateau".
Preferential adsorption of EO ($\text{CH}_2\text{-CH}_2\text{-O}$) to
water-air interface.



Structure of PEO Layer $N_{EO} \approx 10^3$



Grafted Polymers in contact with protein solution

$$\frac{f}{a} = \sigma f_p + \int_0^{\infty} P_p(z) f_s(z) dz + \int_0^{\infty} P_p(z) f_p(z) dz$$

$$\beta f_p = \sum_i P(\omega) \ln P(\omega) \quad (\text{polymer})$$

$$\beta f_s = \ln P_s(z) - c \quad (\text{solvent})$$

$$\beta f_p = \ln P_p(z) + \int_0^{\infty} P_p(z, \Omega) \left[\ln \frac{P_p(z, \Omega)}{\int \frac{P_p(z, \Omega)}{\pi^2} + U_w(z, \Omega)} \right] dz \quad (\text{protein})$$

Minimization subject to packing constraint:

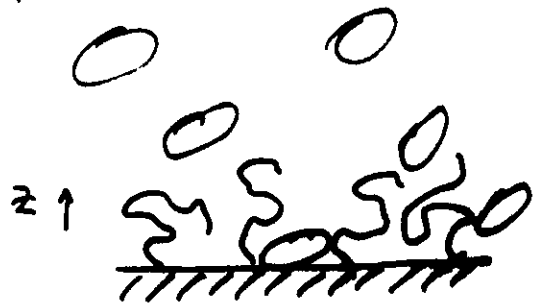
$$0 < \langle n_p(z) \rangle + \int_0^{\infty} P_p(z) \langle n_p(z) \rangle + P_p(z) \leq 1$$

gives:

$$P_p(z) = e^{\beta \mu_p} P_p(z)$$

$$P_p(z, \Omega) = \frac{1}{Z_p(z)} e^{-\int \Pi(z') n_p(z', \Omega) dz' - \beta E_{p-w}(z, \Omega)}$$

(constant μ_p for all z has been taken into account!)



$$P_g(\alpha) = \frac{1}{Q} e^{-\int \Pi(z) n_g(z, \alpha) dz} \quad (\text{grafted po})$$

$$P_s(z) = e^{-\Pi(z) n_s + \beta \mu_s} \quad (\text{solvent})$$

$\Pi(z)$ Lagrange multipliers physical significance
lateral pressures!! (osmotic pressure).

How do we find $\Pi(z)$? insert $P_p(z, \Omega)$, $P_g(\alpha)$
and $P_s(z)$ into const. eq.

Input: set of conformations (α) and prot.; solve
and protein μ , and $U_{p-w}(z)$.

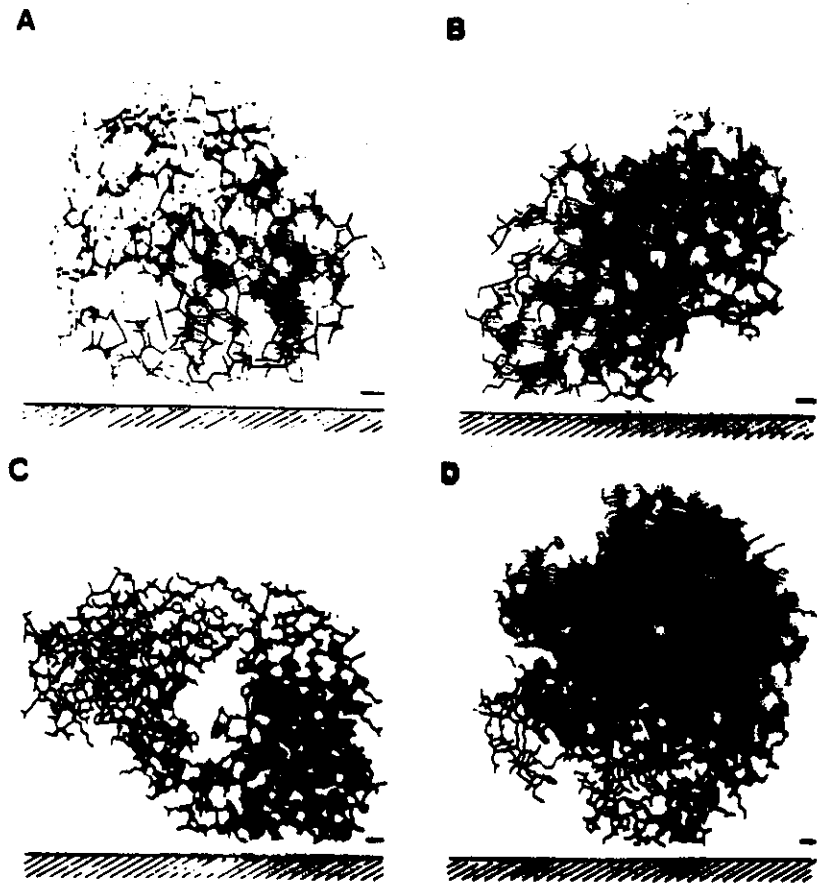
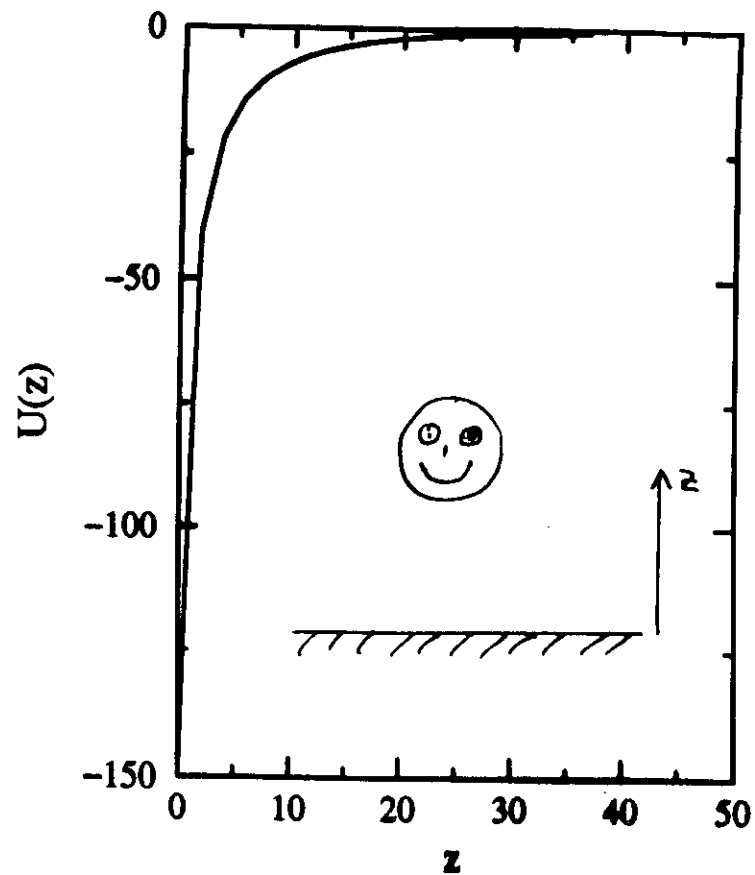
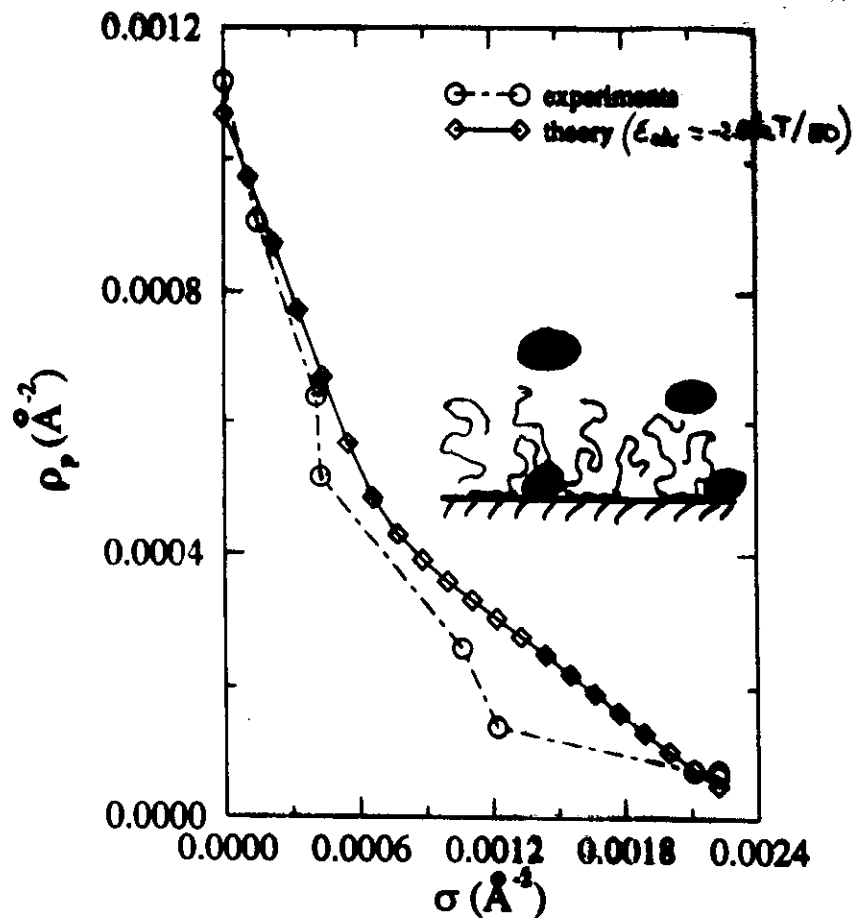


Figure 6. Structures of the four proteins on the polyethylene surface with orientations having the lowest solvation energies. Bar = 2 Å. (A) Lysozyme; (B) trypsin; (C) immunoglobulin F_m ; (D) hemoglobin.

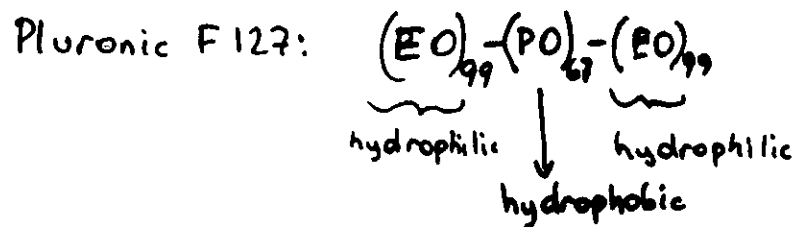
Bare protein-surface potential
Lysozyme (Lee and Park)



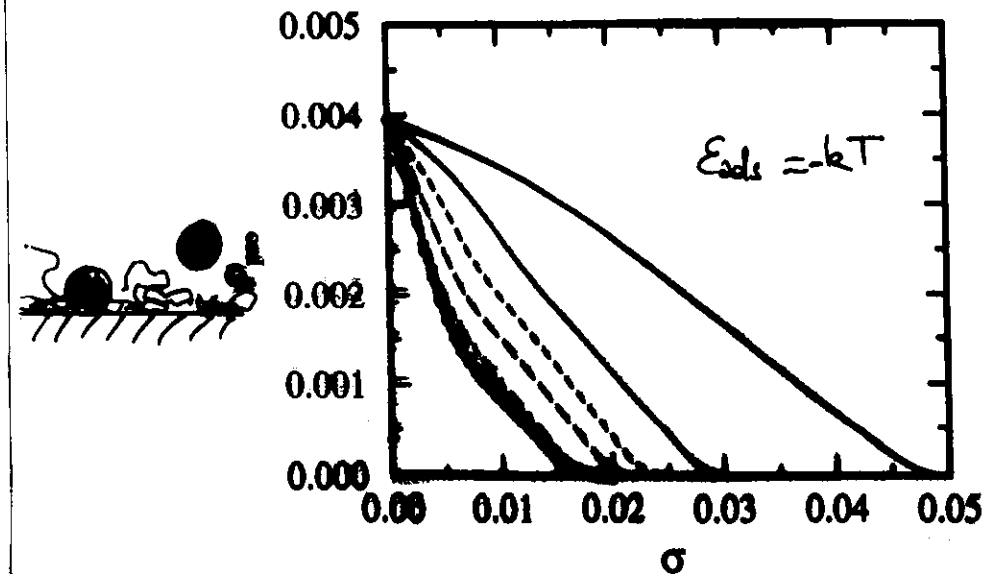
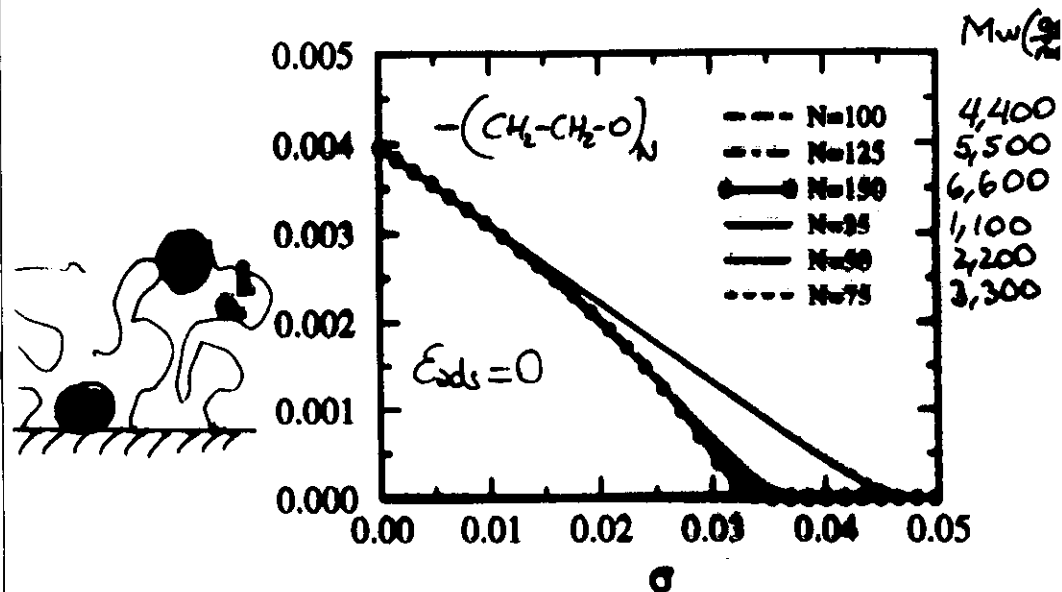
Lysozyme adsorption on Pluronic F127 modified surface



Experimental work: Prof. Kinam Park (Purdue Univ.)

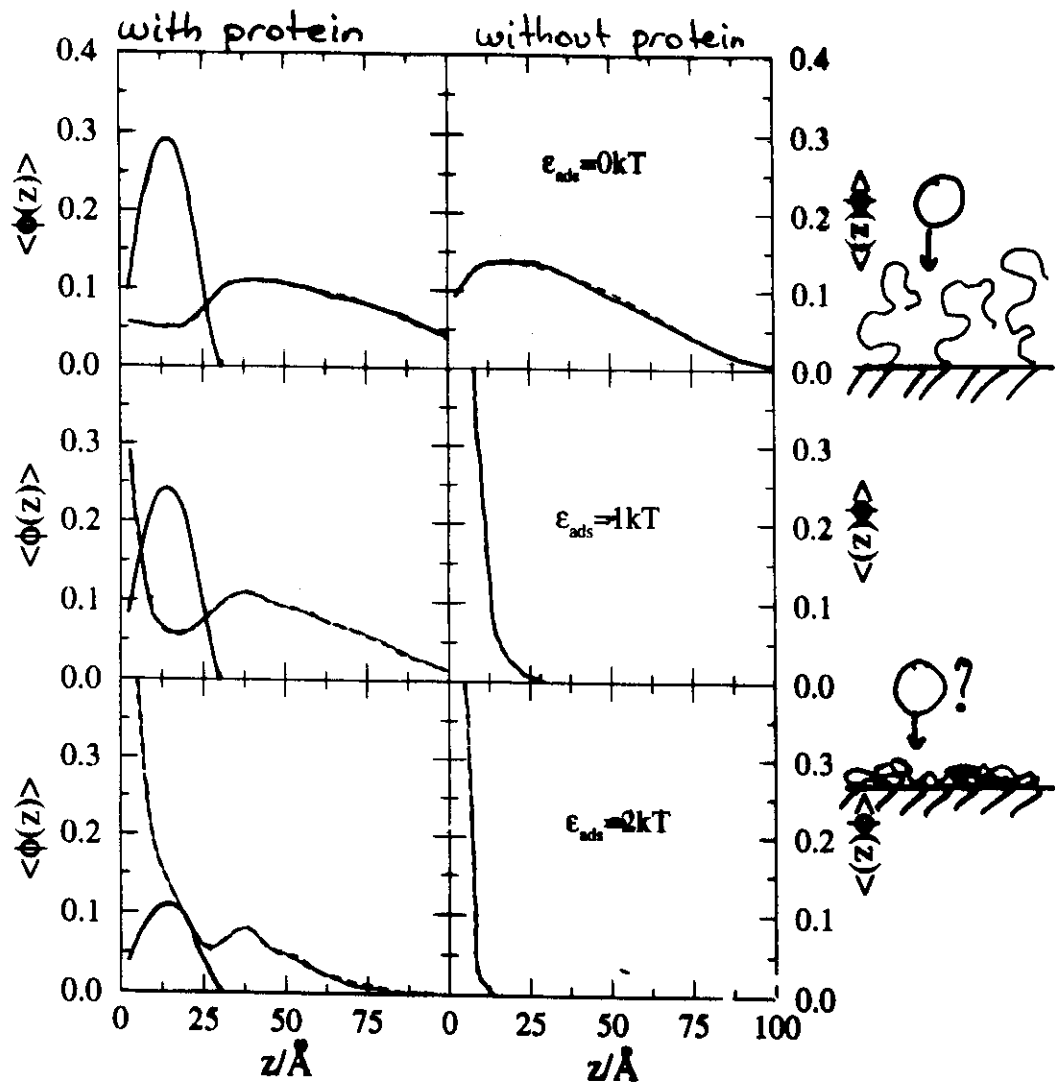


Effect of Molecular Weight

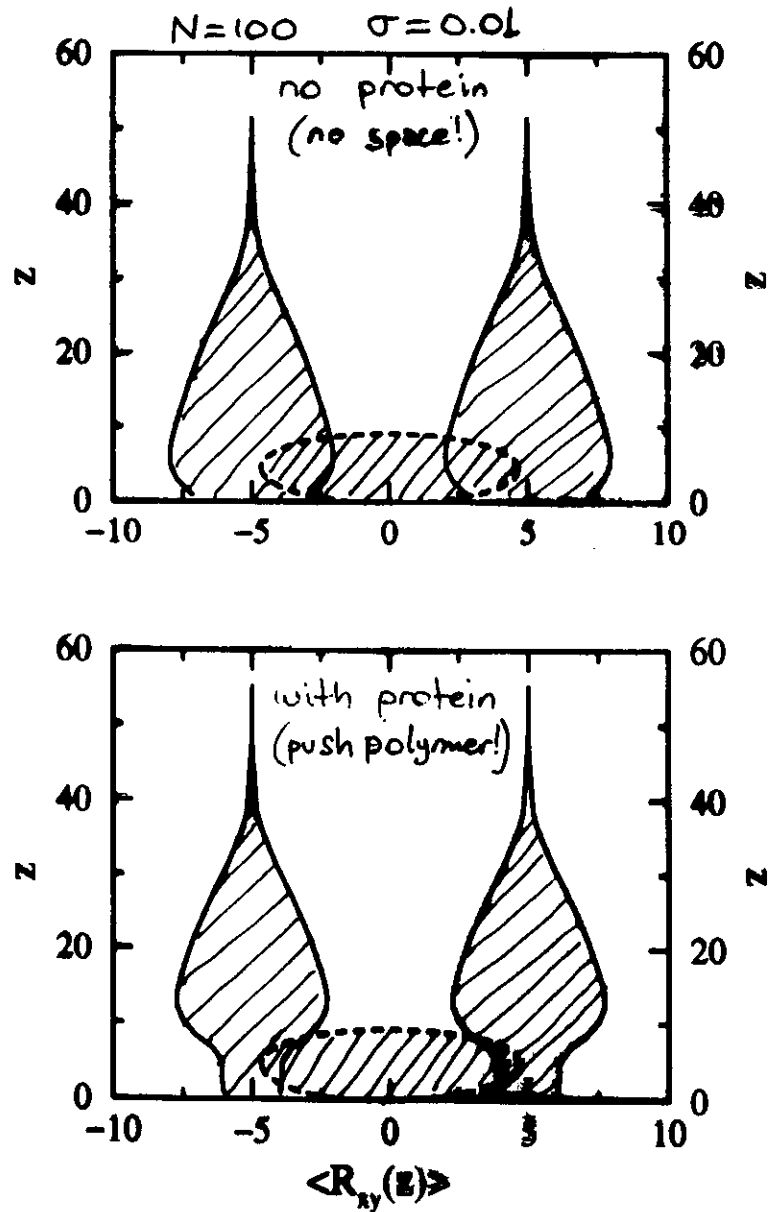


Protein and Pluronic density profiles

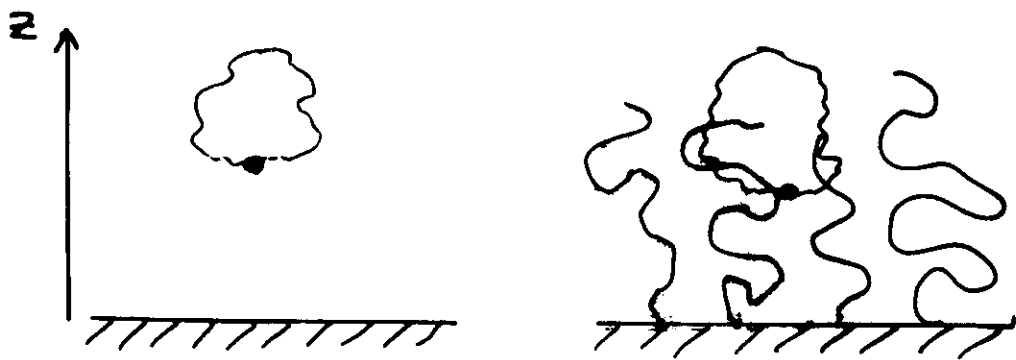
protein "pushes" polymer towards solvent!!



Structure of the polymer layer



Protein adsorption (or lack of it?)



How does $U_{p-s}(z)$ change due to polymer layer?

$$U_{p-s}(z) = U_{p-s}^{attr}(z) + U_{p-s}^{rep}(z)$$

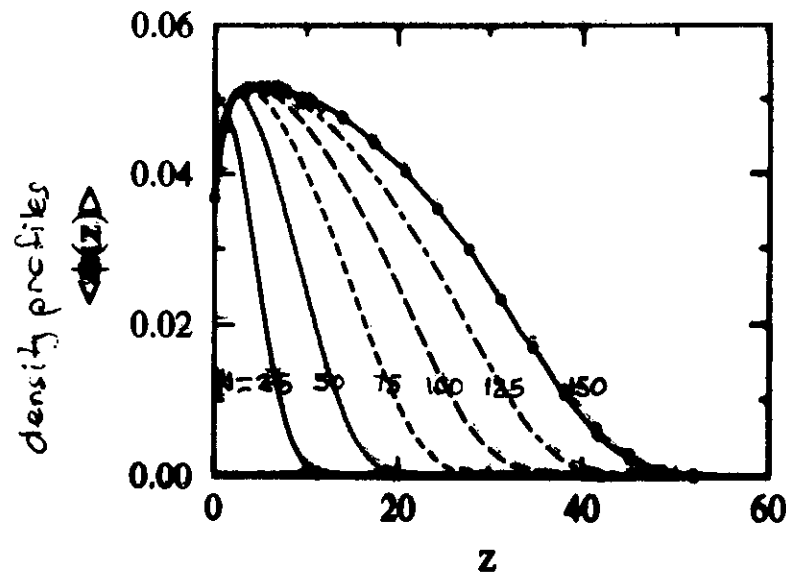
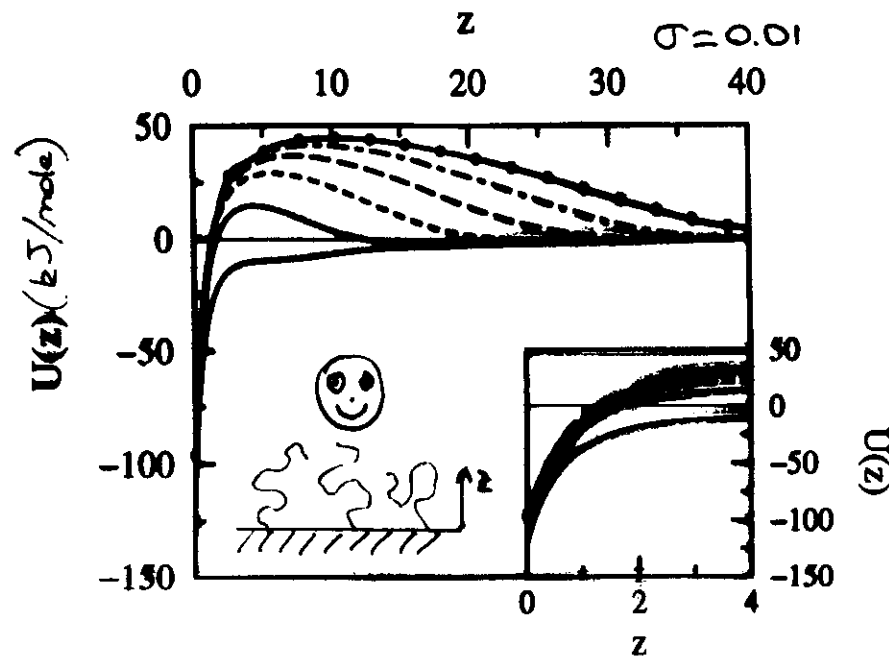
$$U_{p-s}^{rep} = \mu(z) = \int_0^{\infty} \pi(s) N_p(z) ds$$

"Potential of mean-force": averaged over

possible configurations of the polymer

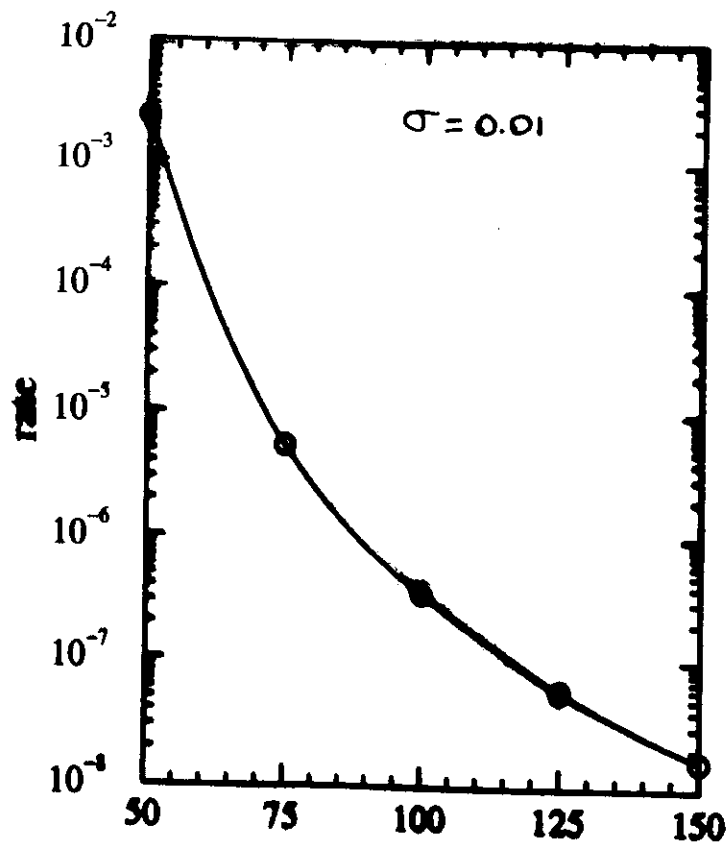
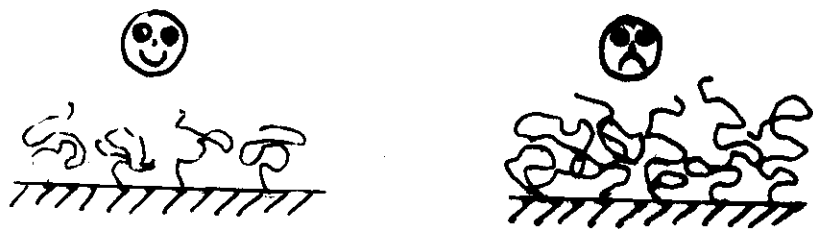
Note that $\pi(s)$ is that of the layer with

Potential of mean force

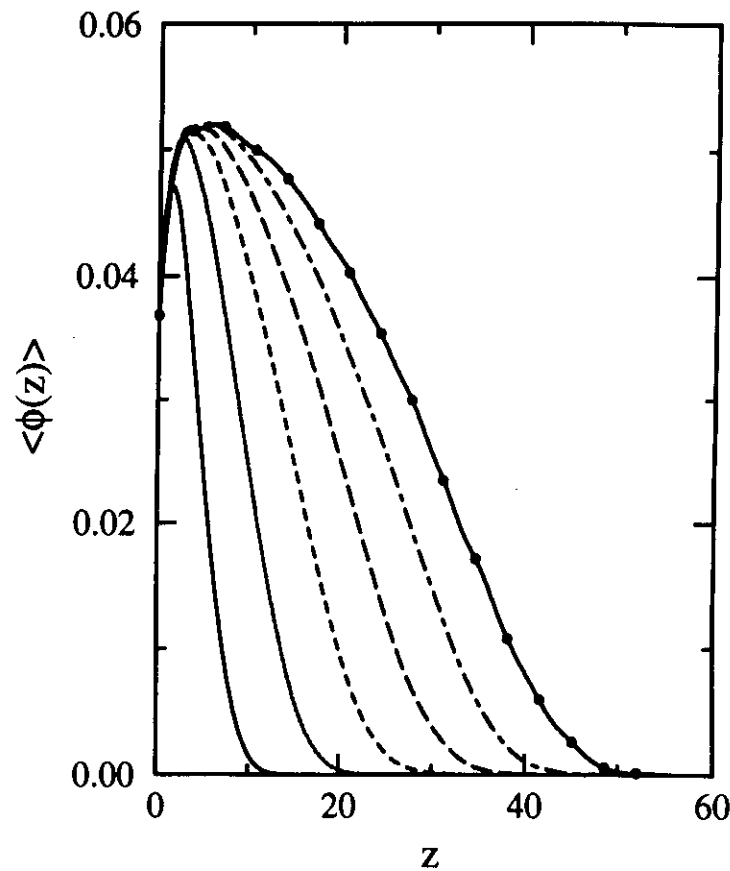


Time scales for adsorption:

$$TST \Rightarrow k = \frac{1}{\tau} \propto e^{-\beta U_{\text{barrier}}}$$



same equil. adsorption ~~orders of magnitude~~



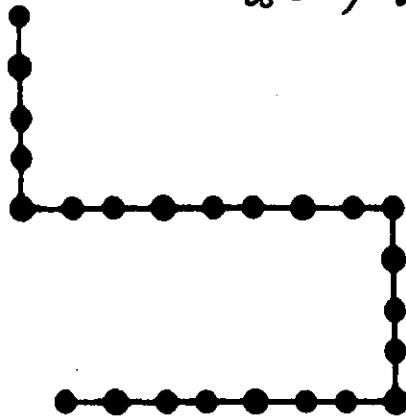
Model Protein:

cubic lattice: $z=6$

blue segments: "hydrophobic"

black segments: "hydrophilic"

$$E_{bb} = E; E_{black, black} = E_{bb} = 0$$



Number of possible configurations $\sim 5^{22} \sim 2 \cdot 10^{15}$

but only ~ 10 "native structure"

and different (~ 10) "surface native structures"

