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SMR.998d - 28

Research Workshop on Condensed Matter Physics
30 June - 22 August 1997
**MINIWORKSHOP ON
QUANTUM WELLS, DOTS, WIRES
AND SELF-ORGANIZING NANOSTRUCTURES
11 - 22 AUGUST 1997**

**"Transport Spectroscopy
of Artificial Atoms and Molecules"**

PART II

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These are preliminary lecture notes, intended only for distribution to participants.

Transport Spectroscopy of Artificial Atoms and Molecules

in collaboration with:

Sergio E. Ulloa theory

Robert H. Blick experiments
Jürgen Weis

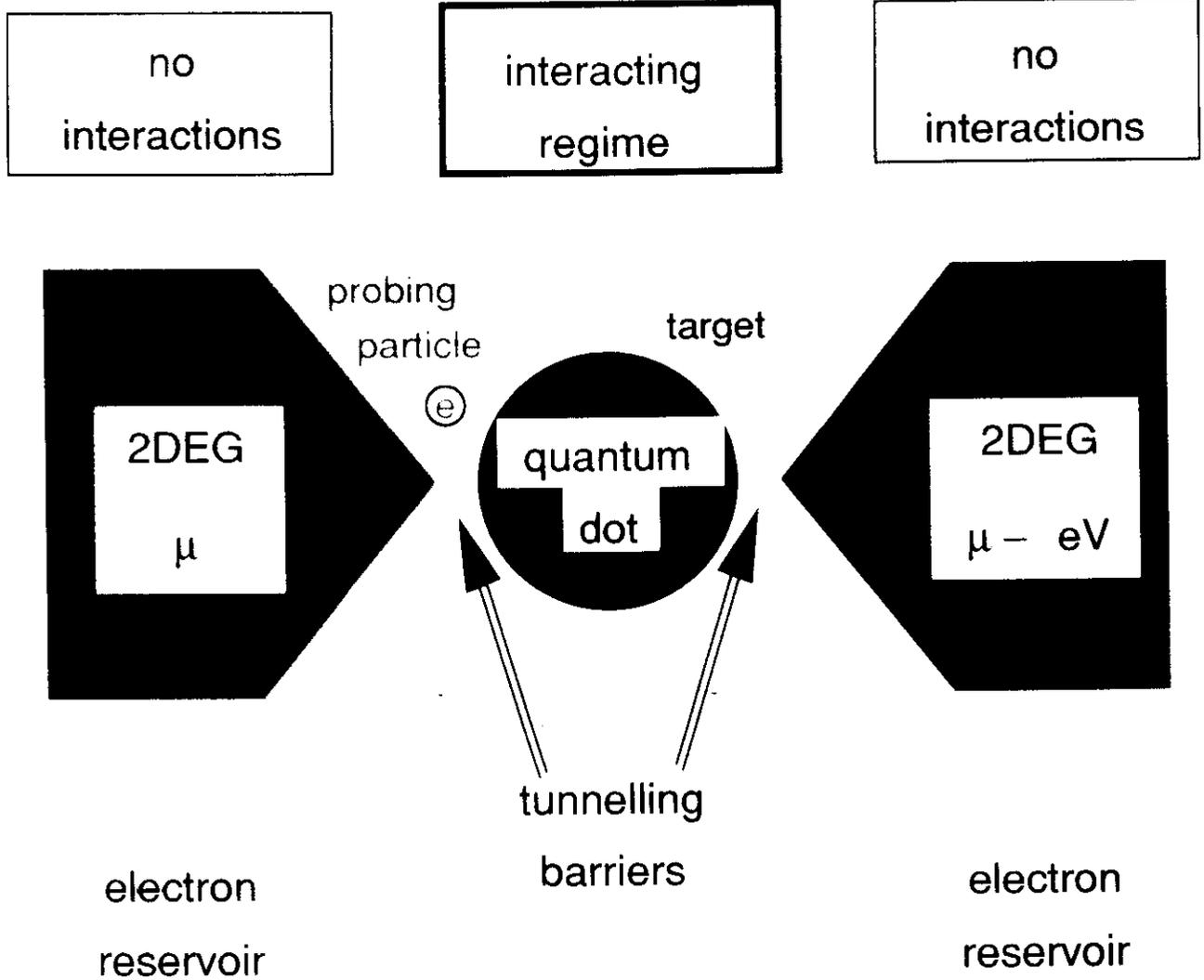
Max Planck Institut für Festkörperforschung, Stuttgart

Outline

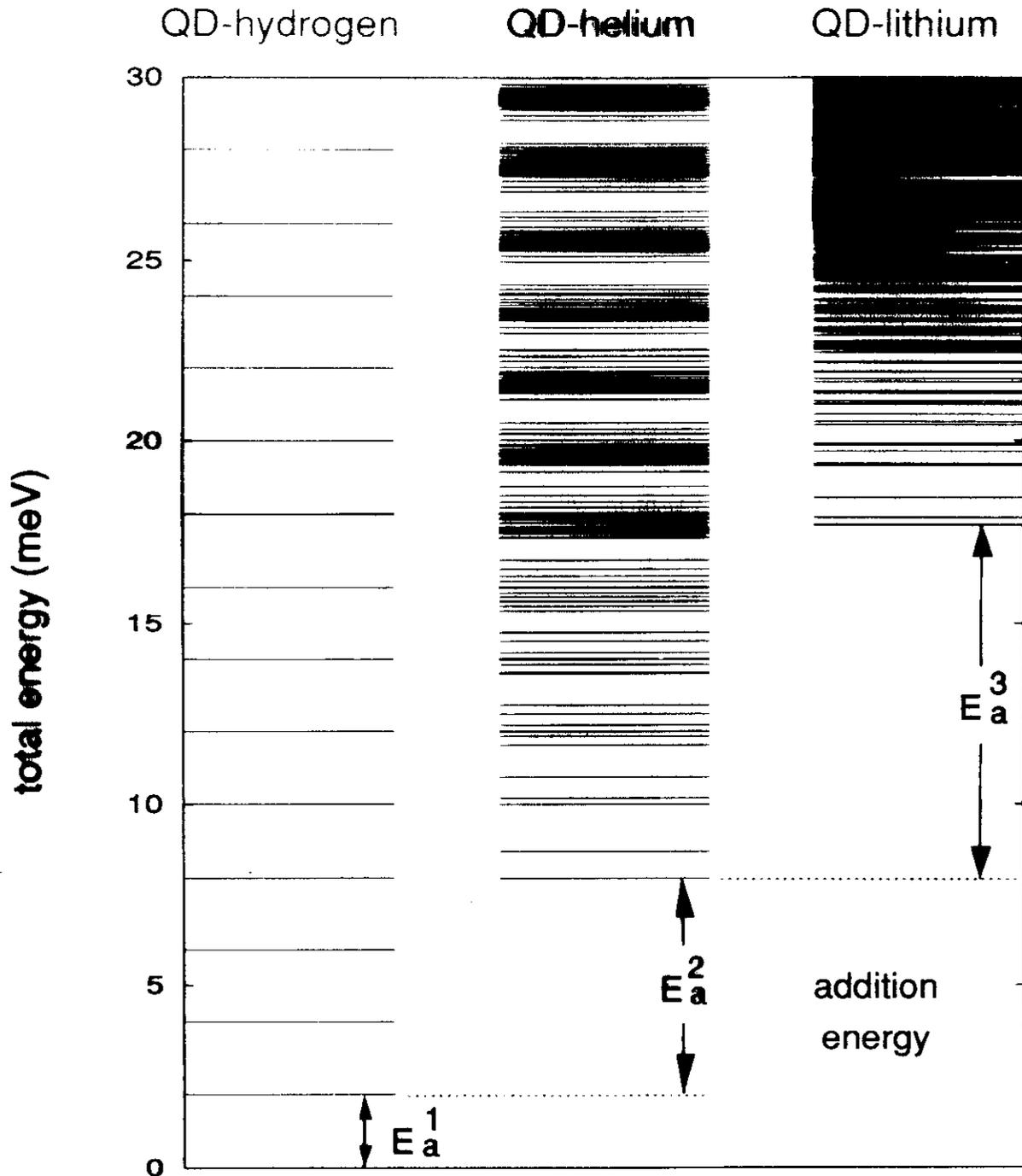
- Transport through Single Quantum Dots:
 - effect of correlations
 - competing channels

- Transport through Double Quantum Dots:
 - electrostatics
 - double-dot eigenstates
 - molecular transport resonances

Transport-Spectroscopy

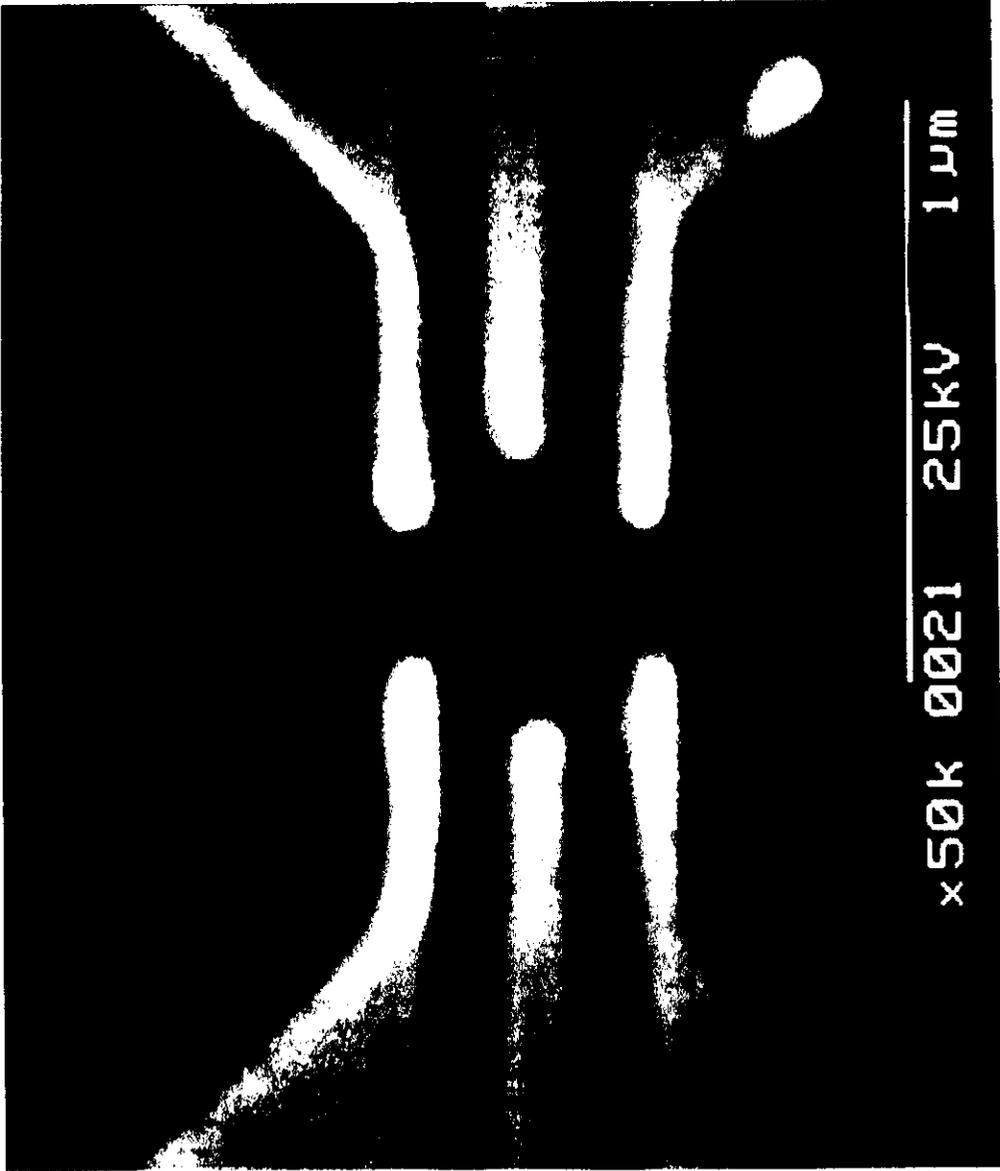


Spectra of different QD-Elements



9316

metallic

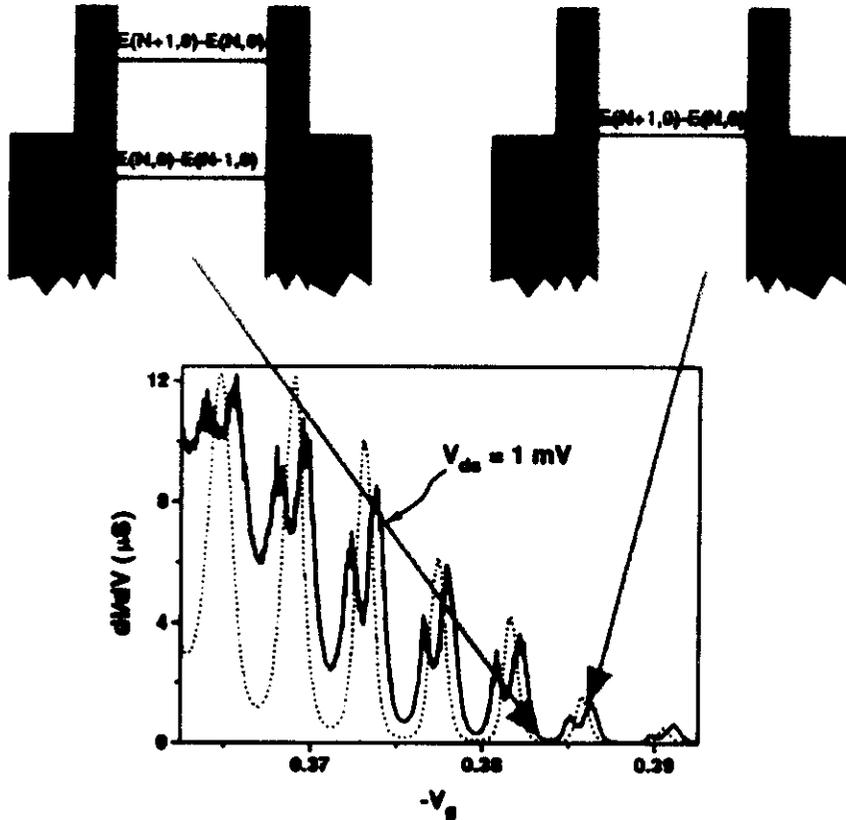


metallic
gates

9316



Transport in Single Quantum Dots



simplification:

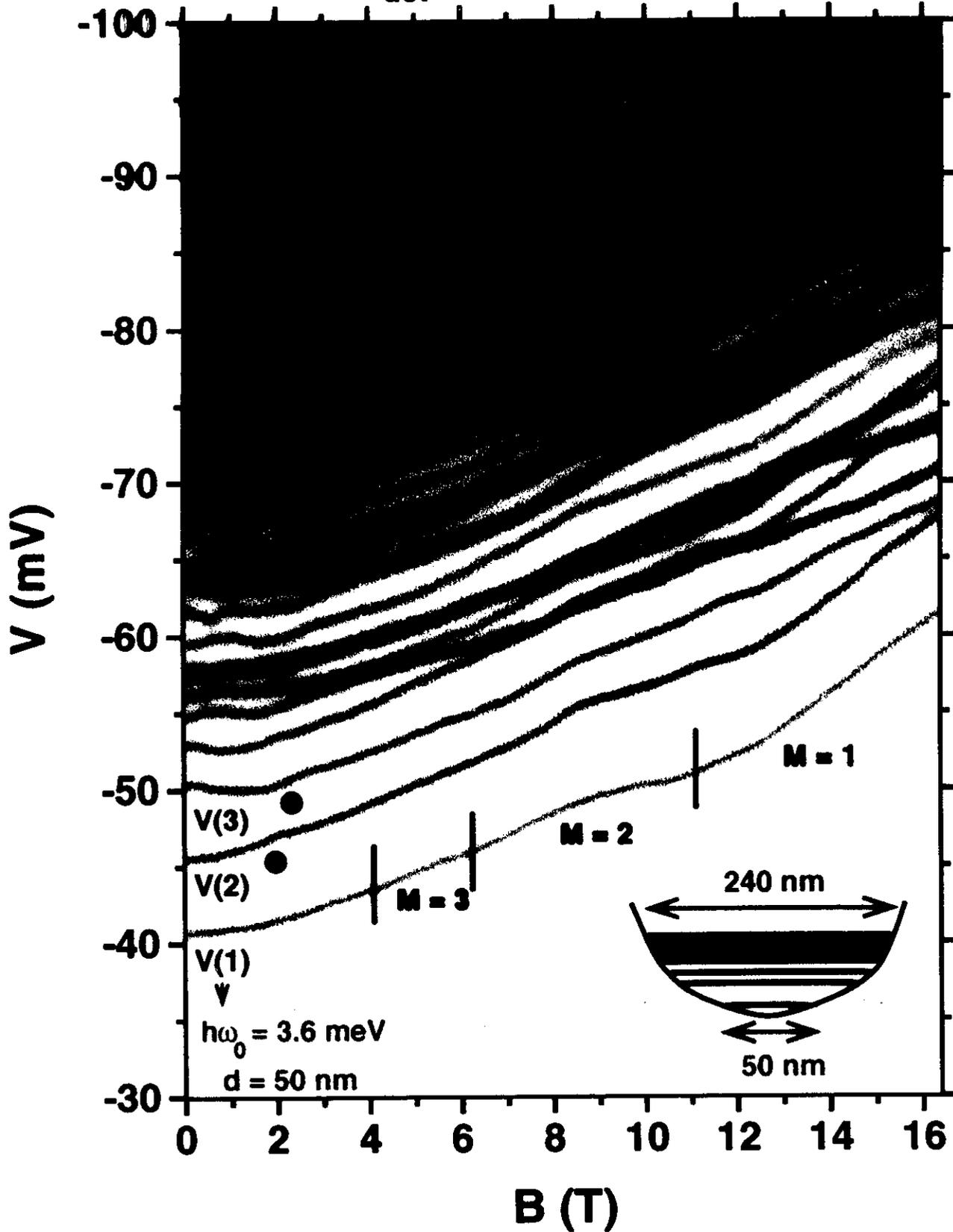
$$E(N, \alpha) = \frac{1}{2C} N^2 e^2 - \lambda_g e N V_g + \sum_k \epsilon_k$$

conductance resonances at:

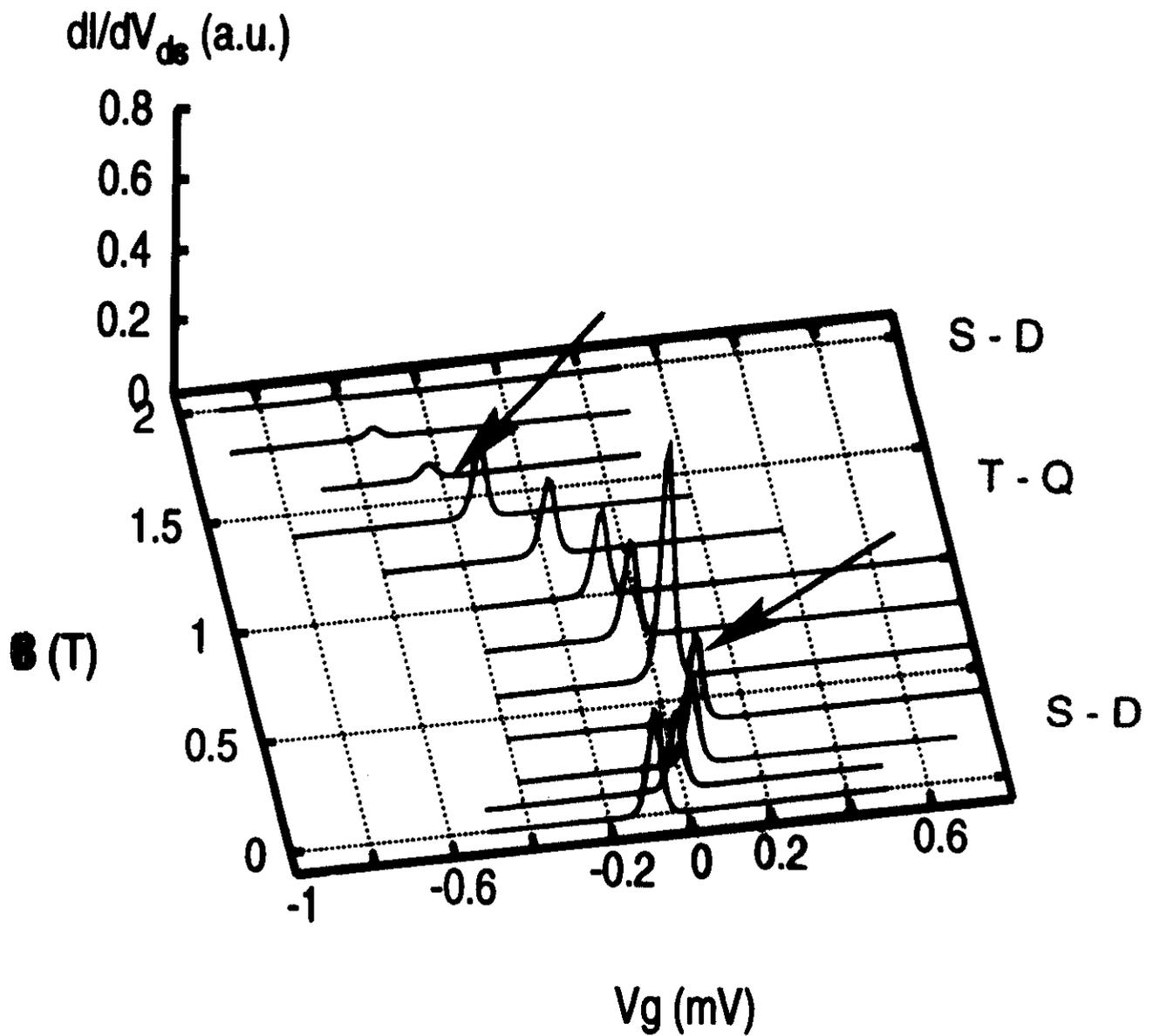
$$\mu = E(N+1, \alpha') - E(N, \alpha) = \frac{e^2}{2C} (2N+1) - \lambda_g e V_g + \epsilon_{k_F}$$

Coulomb Blockade Oscillations

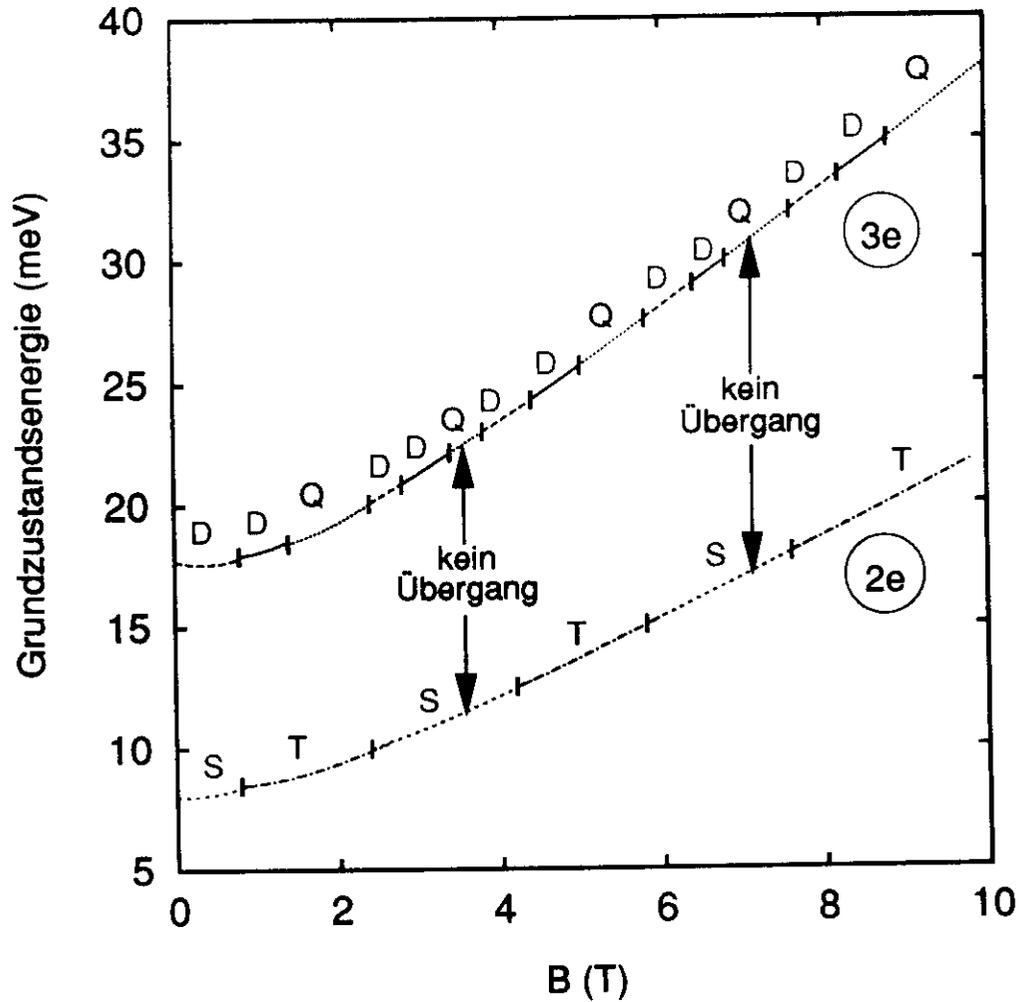
(Palacios et al. 94) $\nu_{\text{dot}} = 1 \rightarrow d = 200 \text{ nm} \sim d_e = 240 \text{ nm}$



Magnetic Field Dependence of Conductance Resonances



Spin-Auswahlregeln



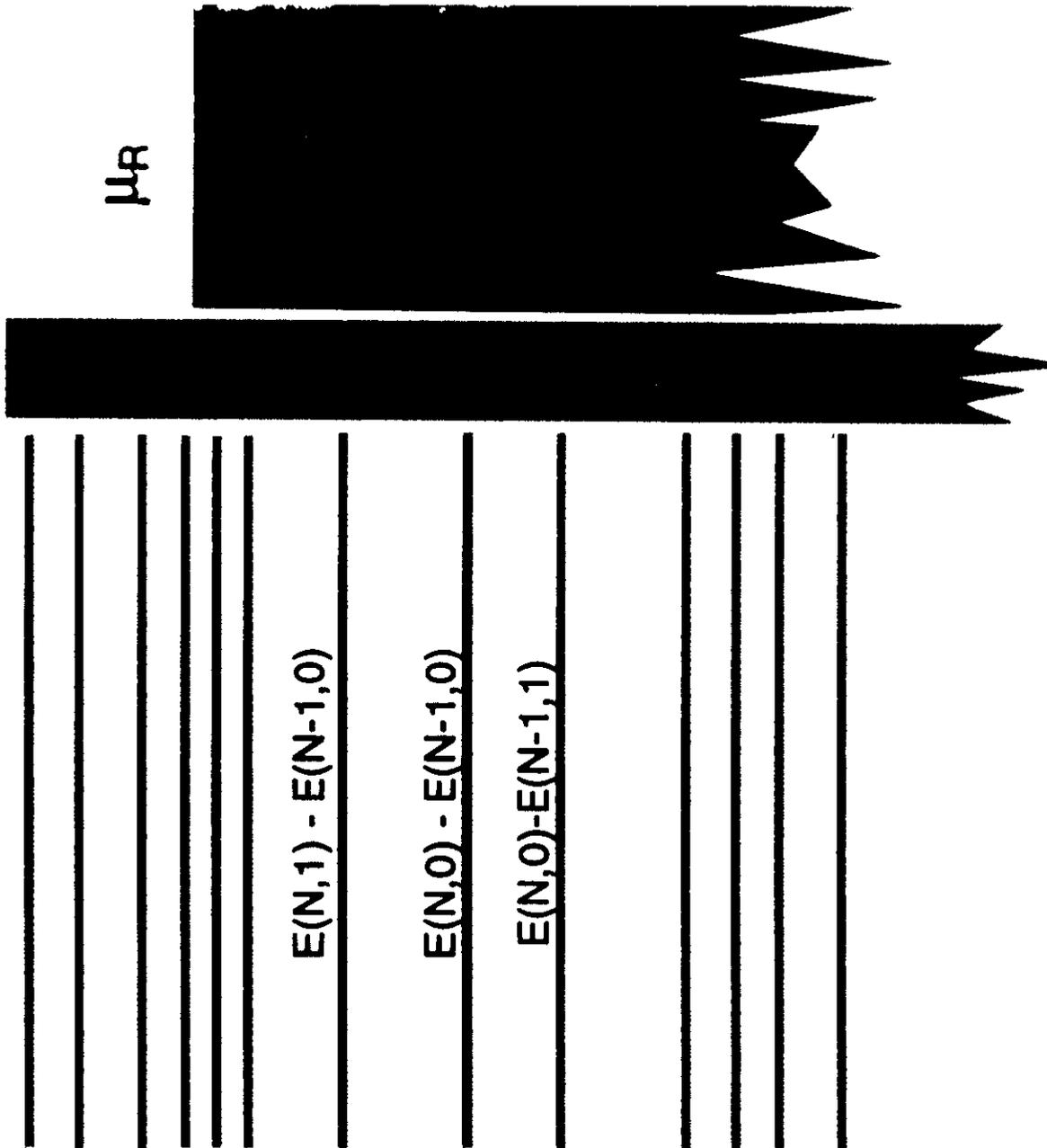
Kein Übergang zwischen Spin-Singulett- und Spin-Quadruplett- Zuständen

Verallgemeinerung auf beliebige Spins:

Weinmann et al., Europhys. Lett., 26, 467 (1994)

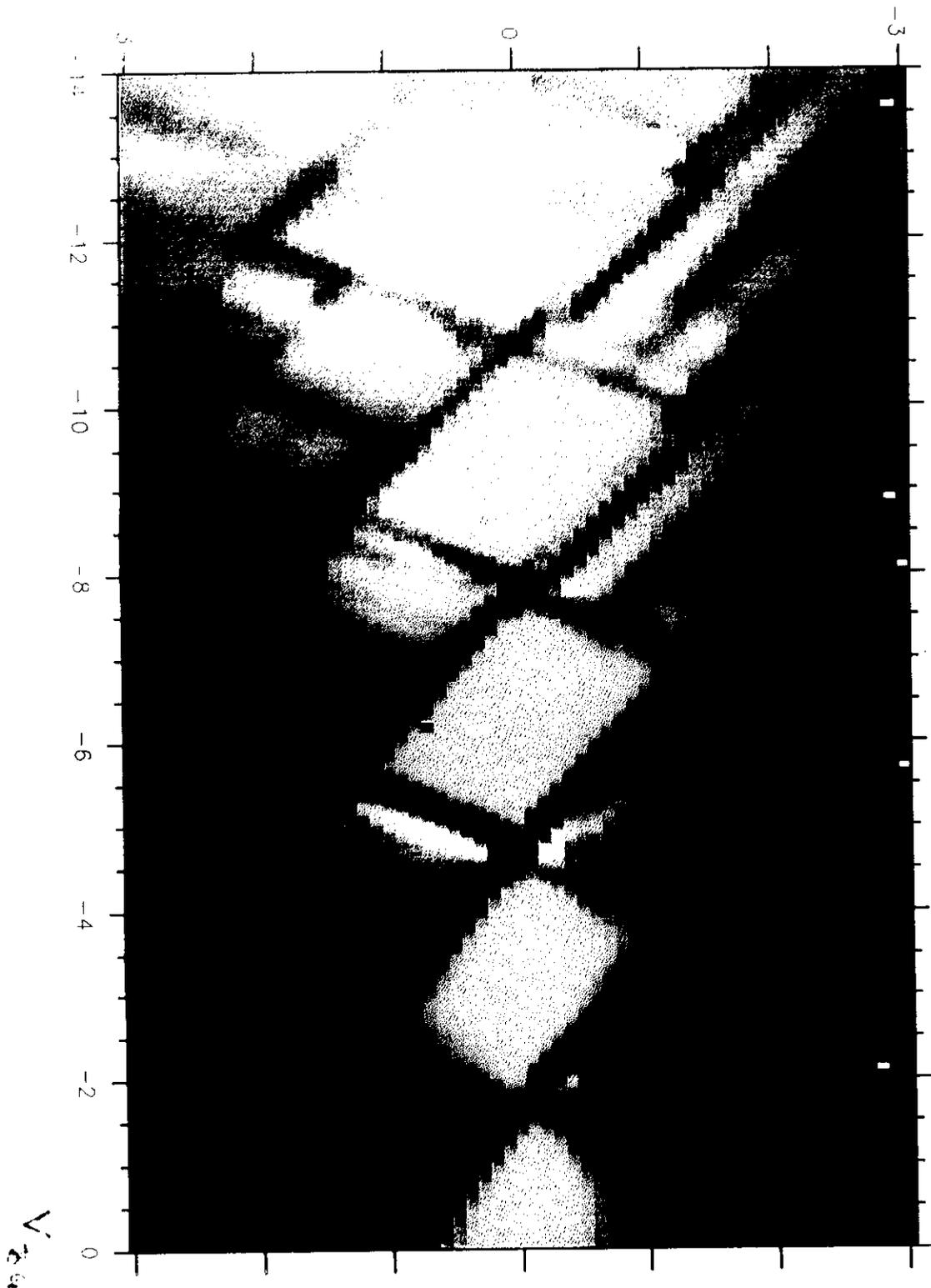
Non-linear Transport

$$E(N+1,0) - E(N,0)$$



Conductance

V_{DS}



100

100

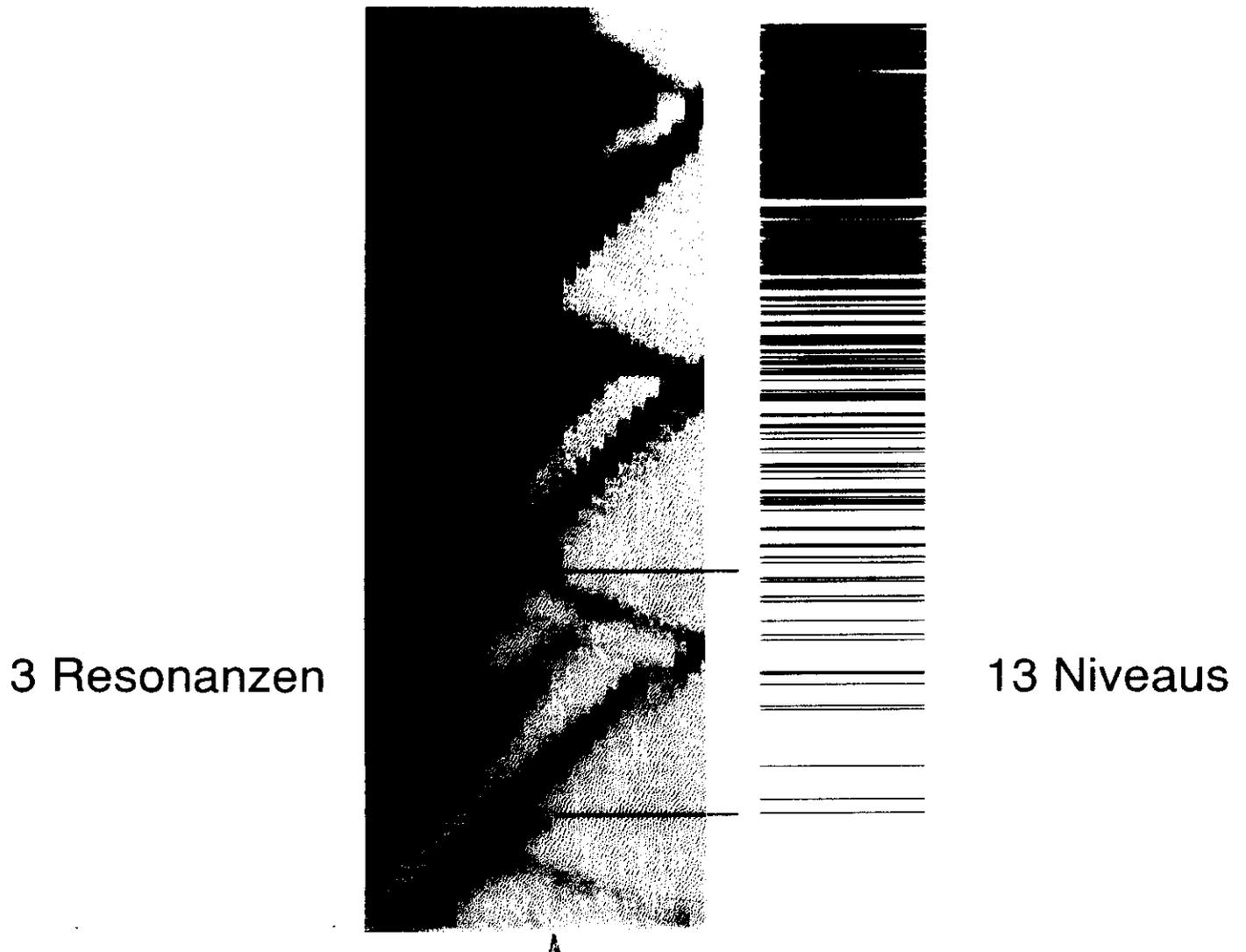
100

111

$B = 0T$

V_{gg}

Vergleich: Experiment - Spektrum (Lithium)



Experiment:

erheblich weniger Resonanzen als erwartet

Sequential Tunneling - Current

Fermi-Distribution of electrons in left reservoir

$$f_{\alpha\alpha'}^L = f_{FD}(E_{N,\alpha} - E_{N-1,\alpha'} - \mu^L)$$

$$I = -e \sum_N \sum_{\alpha\alpha'} \Gamma_{\alpha\alpha'}^L \left[P_{\alpha'} f_{\alpha\alpha'}^L - P_{\alpha} (1 - f_{\alpha\alpha'}^L) \right]$$

probability for dotstate $|N, \alpha\rangle$
 \rightarrow kinetic equations

transition rate

$$\Gamma_{\alpha\alpha'}^L = \frac{2\pi}{\hbar} \sum_{\mathbf{k}} |t_{\mathbf{k}}|^2 \langle N, \alpha | c_n^\dagger | N-1, \alpha' \rangle$$

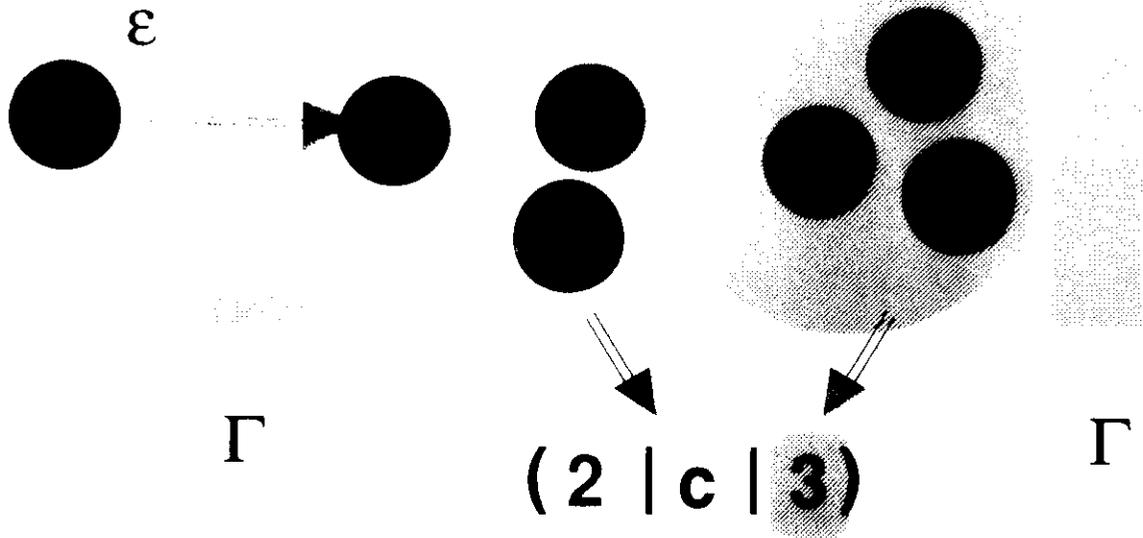
spectral weight \rightarrow overlap

limit: linear response ($\mu^L \simeq \dots$)

$$\frac{dI}{dV_{DS}} = \frac{e^2}{h} \frac{\Gamma^L \Gamma^R}{\Gamma^L + \Gamma^R} \left| \langle N, \alpha | c_n^\dagger | N-1, \alpha' \rangle \right|^2 \left(-\frac{\partial f_{00'}}{\partial E} \right)$$

only ground states thermally occupied

Tunneling Probability



energy conservation:

$$\epsilon + E_2 = E_3$$

tunneling through barrier:

Γ

overlap matrix element:

$$(2 | c | 3)$$

uncorrelated
system:

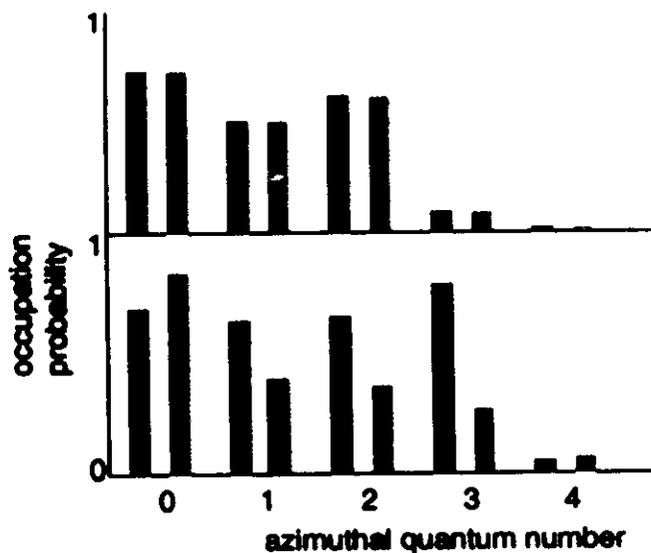
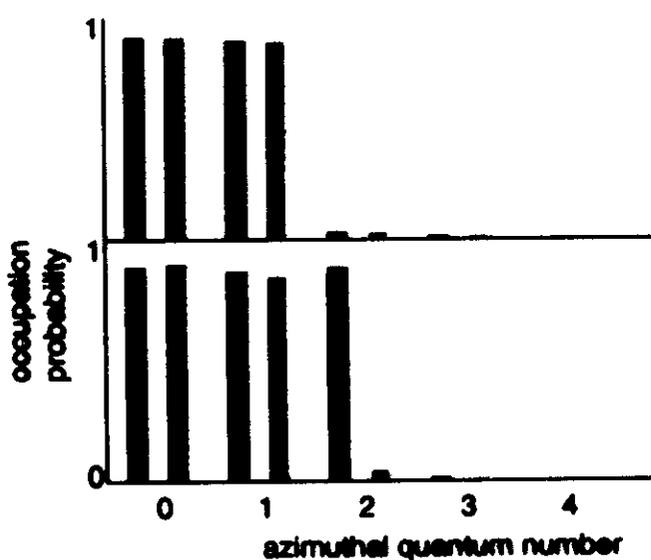
$$\sum_n |(2 | c_n | 3)|^2 = 1$$

Orbital Overlap

uncorrelated

strongly correlated

states

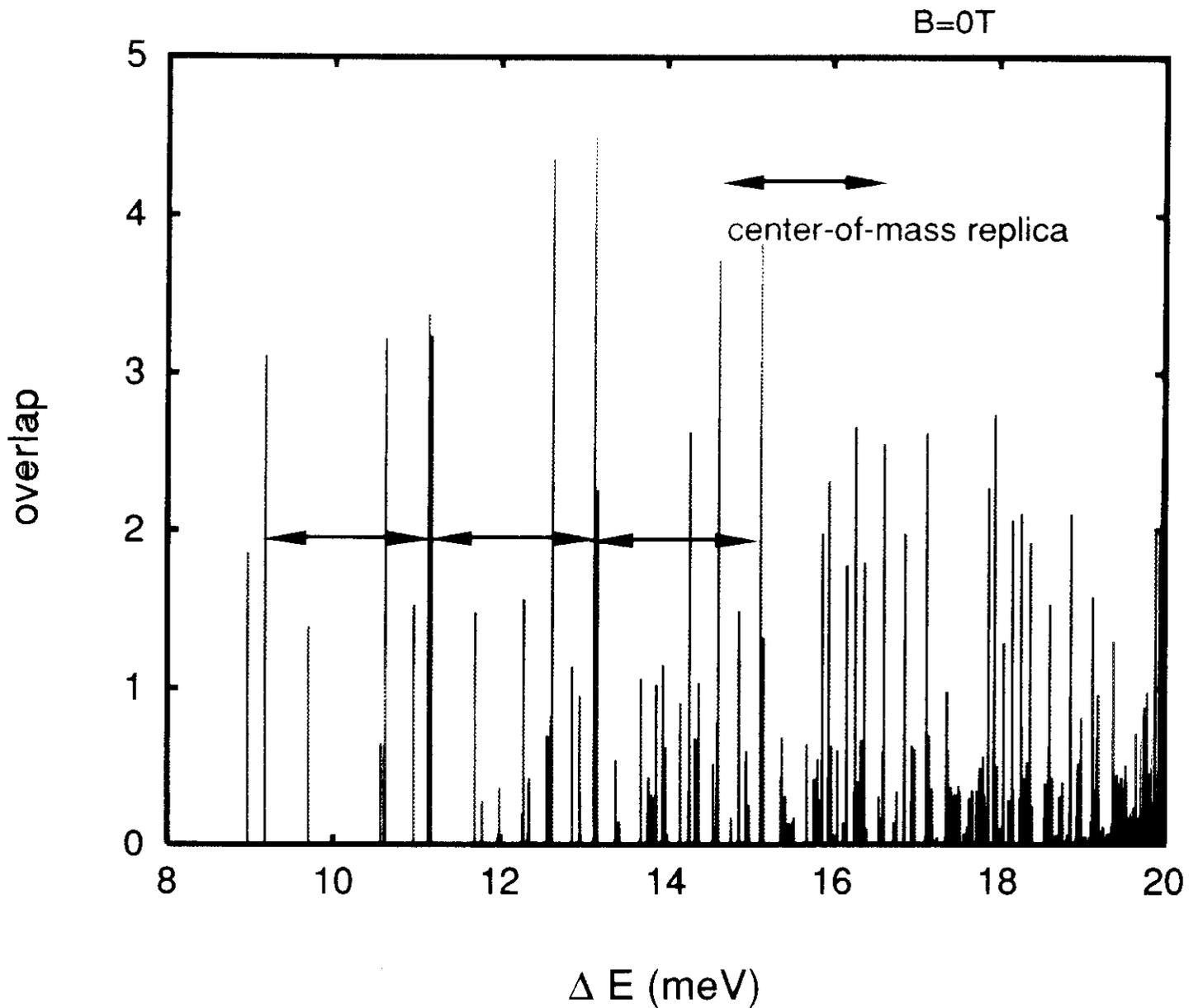


from Palacios et al., Superlattices..., 15, 91,(1994)

$$\sum_n |(4|c_n|6)|^2 = 1$$

$$\sum_n |(4|c_n|5)|^2 \ll 1$$

Overlap

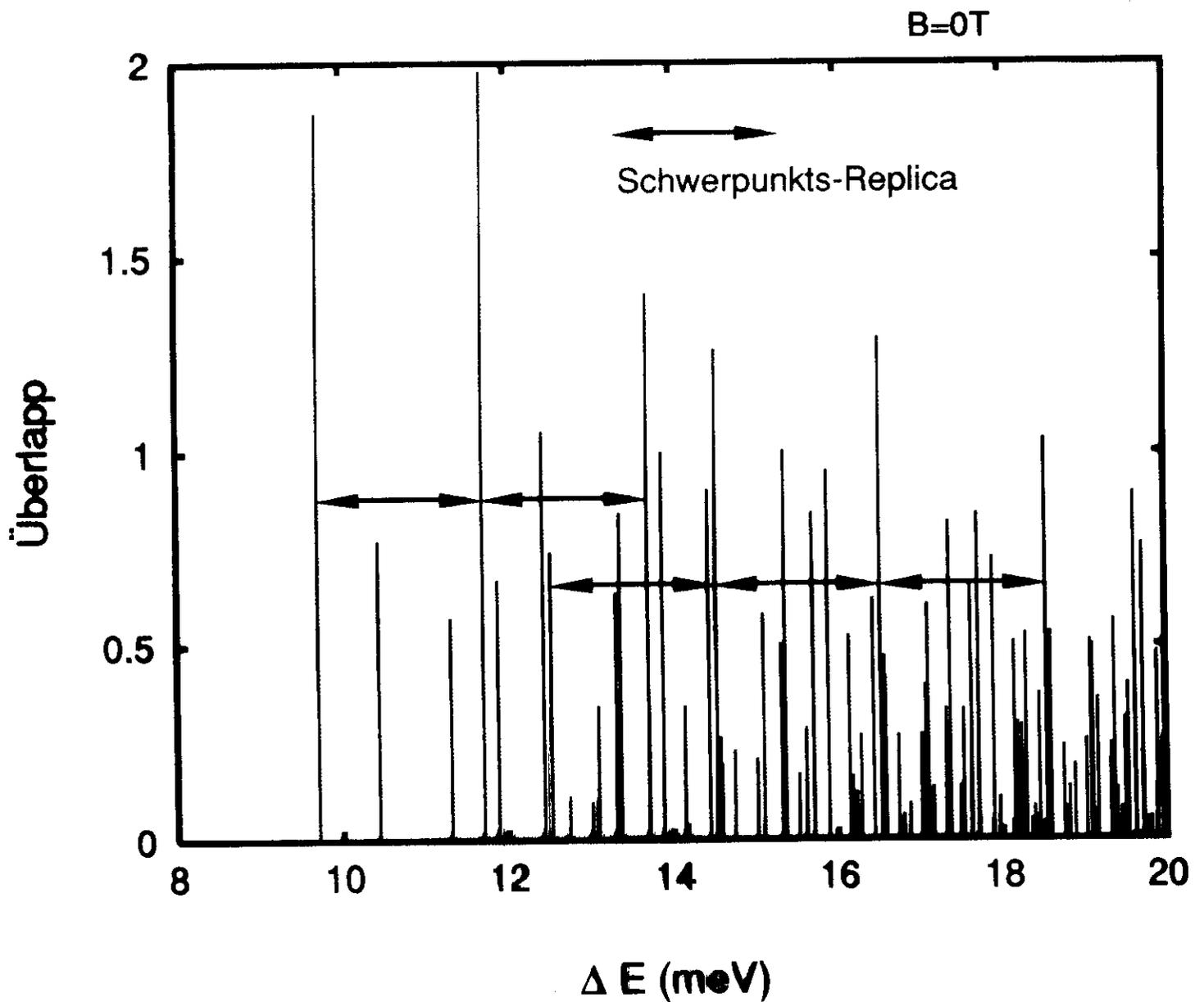


transition:

2-particle lowest triplet to 3-particle state

quasi-selection rules due to correlations

orbitaler Überlapp

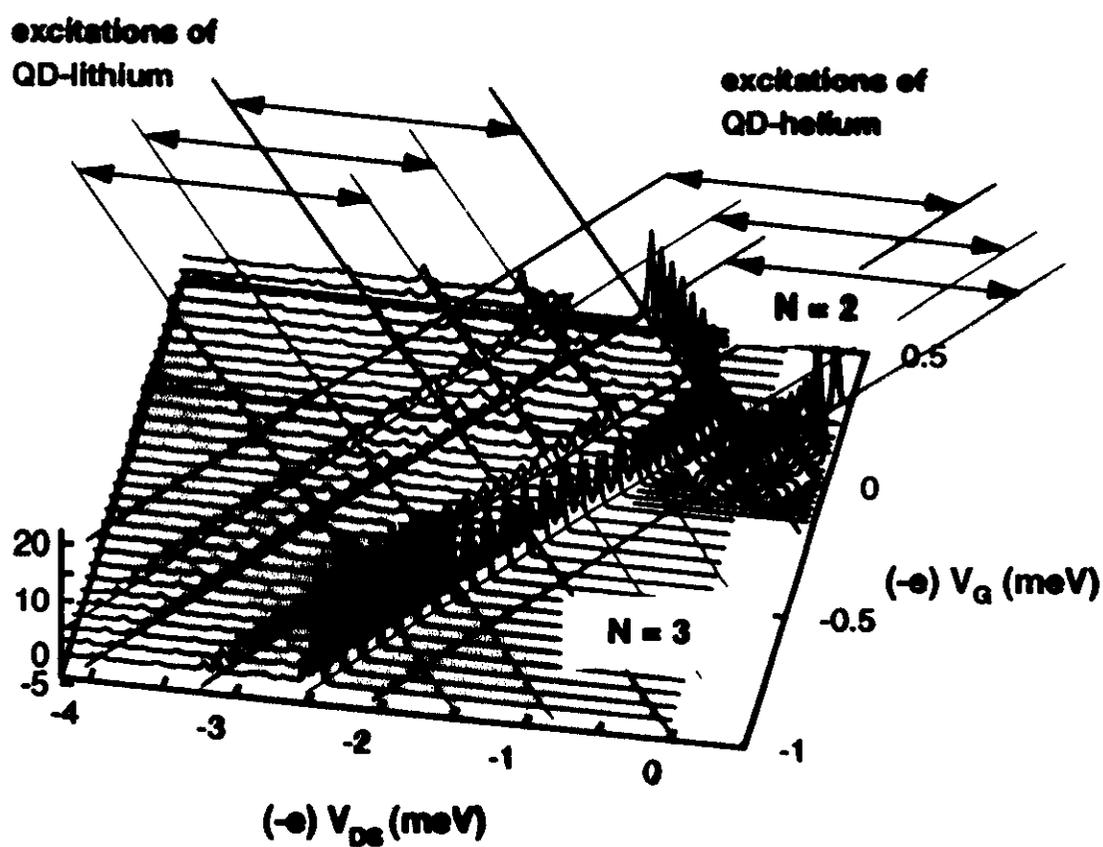


Übergang:

2-Teilchen-Grundzustand in 3-Teilchen-Zustände

Quasi-Auswahlregeln auf Grund von Korrelationen

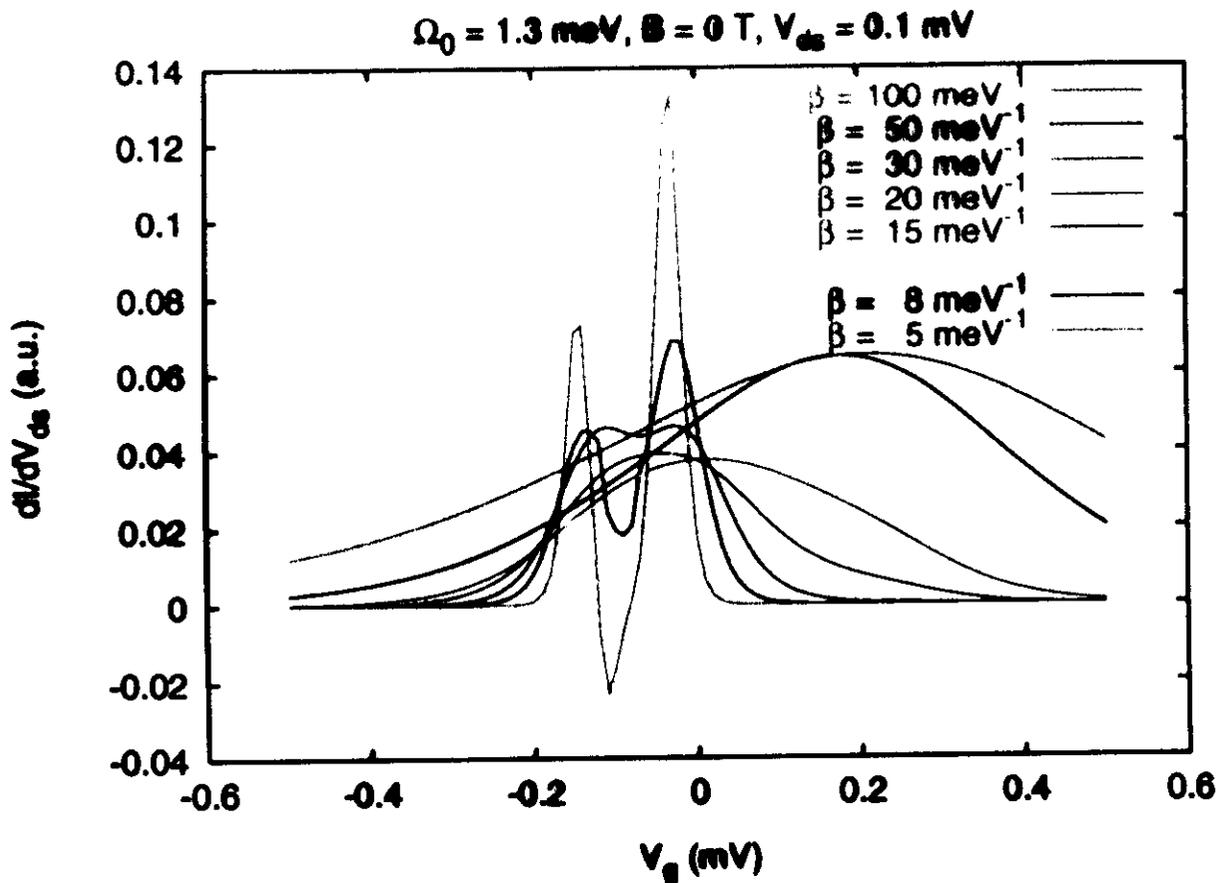
Tunneling spectrum of a Single Quantum Dot



collective excitations

Anomalous Temperature Dependence

single transition: $1/T$ -behavior

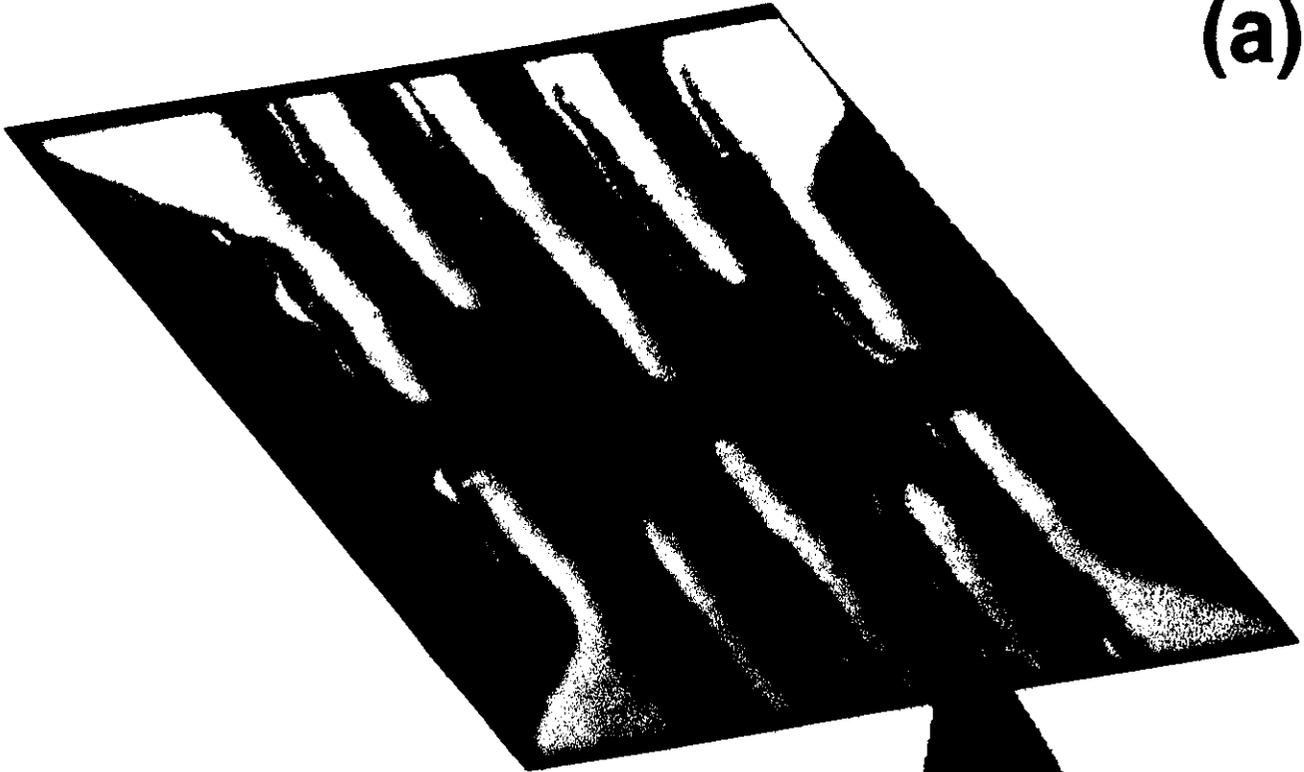


competition between:

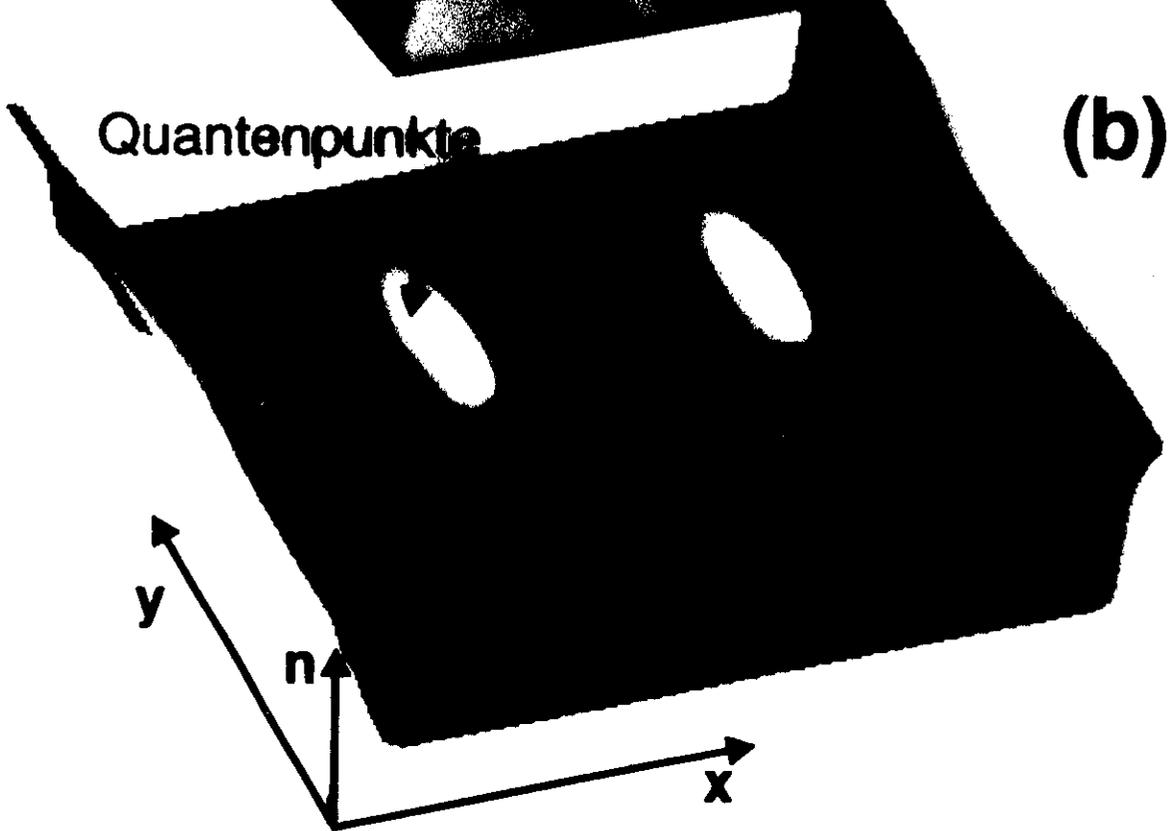
- non-spin polarized transition with small tunneling rate
- spin-polarized transition with large tunneling rate

Doppelquantenpunkte

Gate-Struktur



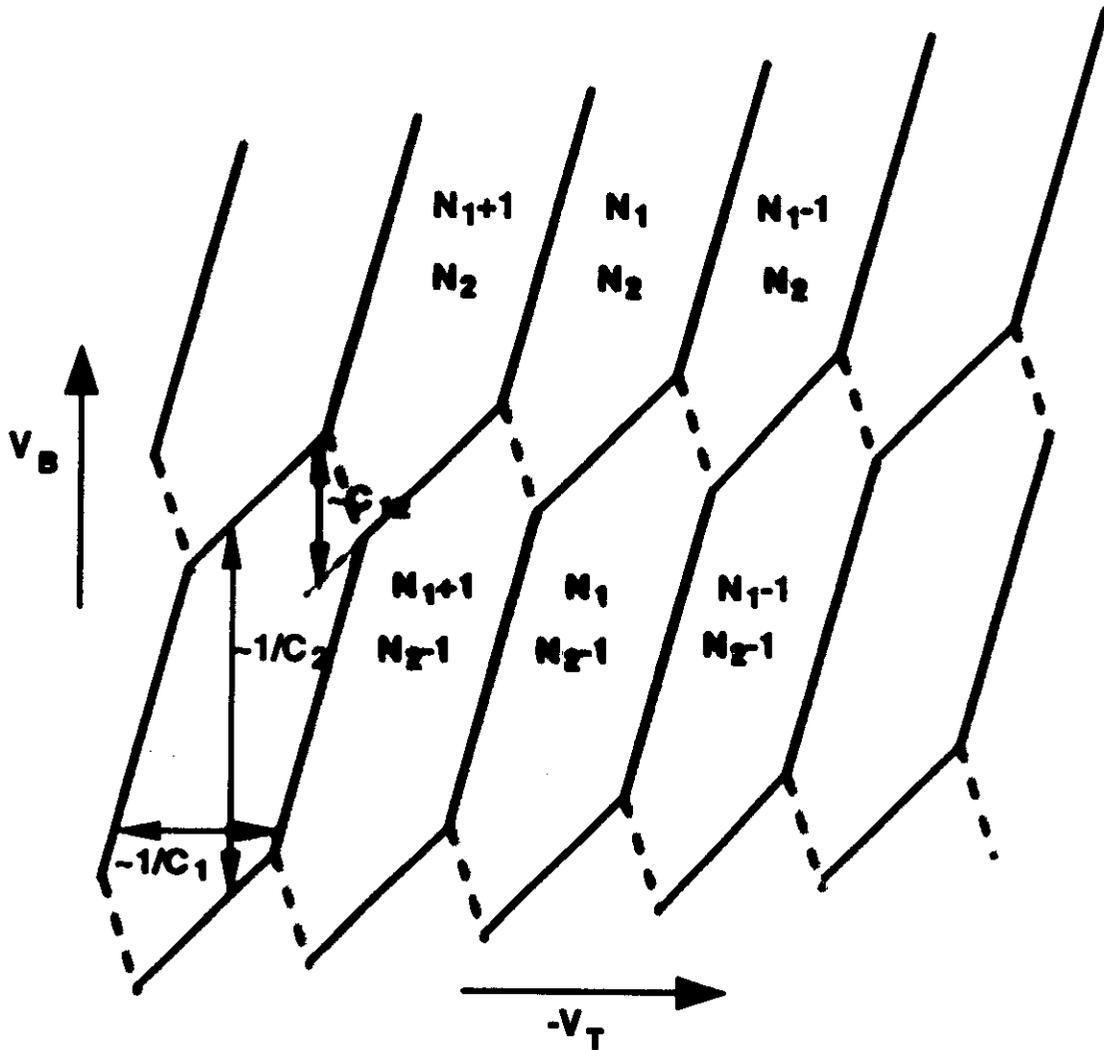
Quantenpunkte



Charging Diagramm

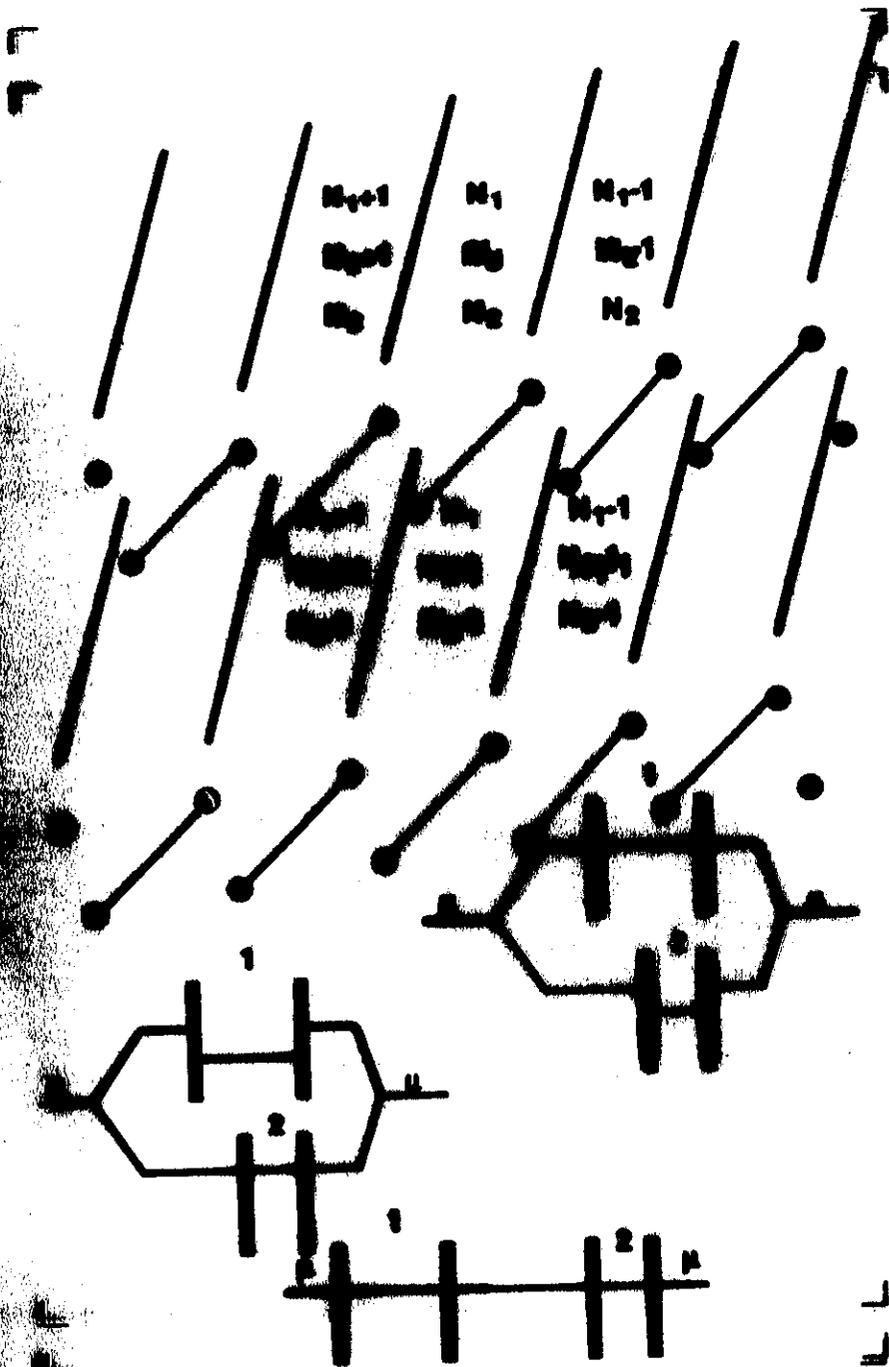
electrostatic energy:

$$E^{el} \simeq \frac{1}{2C_1}(N_1e)^2 + \frac{1}{2C_2}(N_2e)^2 + \frac{C_{12}}{C_1C_2}(N_1e)(N_2e) - (\lambda_{1T}N_1 + \lambda_{2T}N_2)eV_T - (\lambda_{1B}N_1 + \lambda_{2B}N_2)eV_B$$

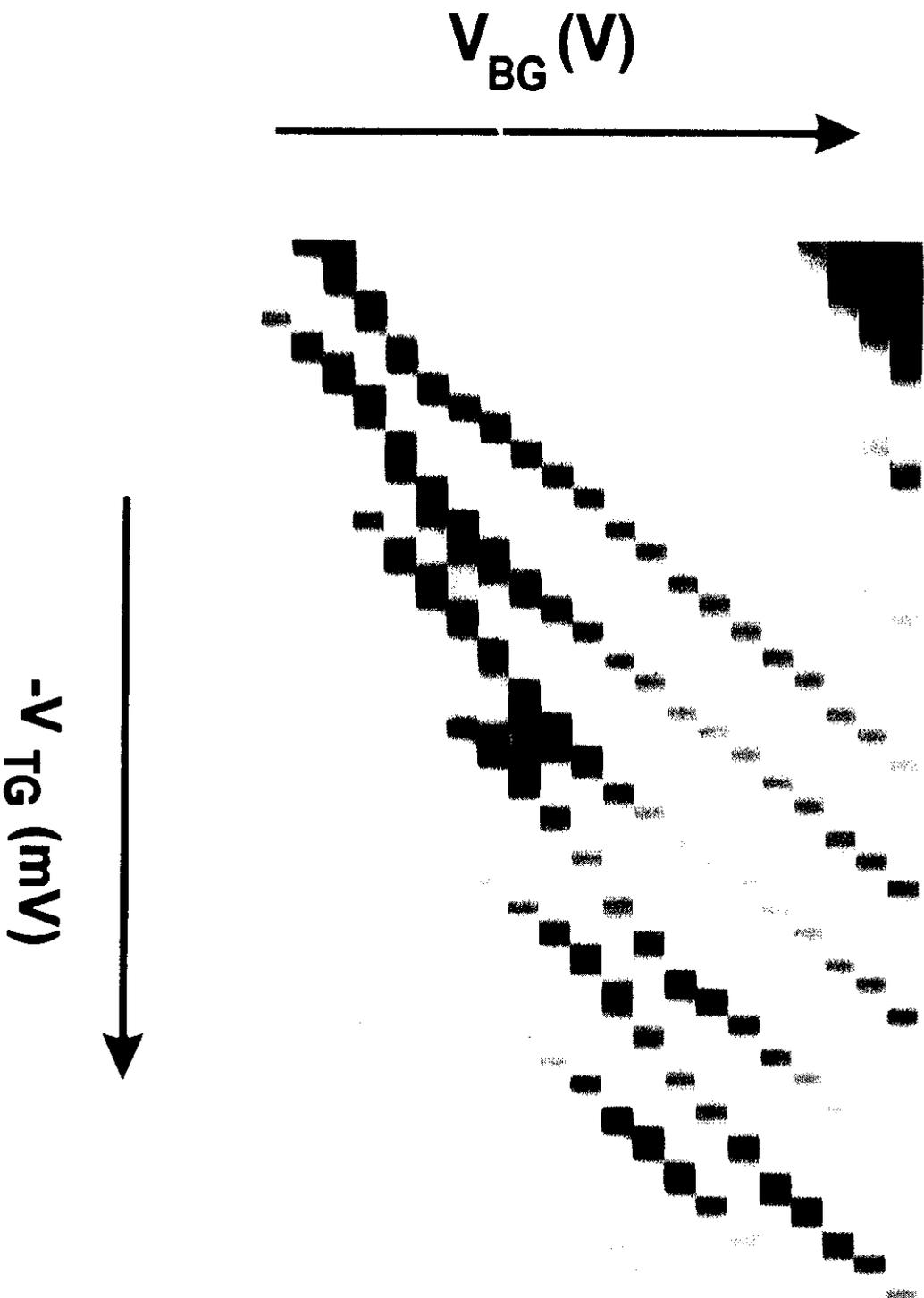


Transport in Double Quantum Dots

sequential



Charging Diagram of the Double Quantum Dot:



Hamilton Operator

$$\begin{aligned} H = & H^e I && \text{electrostat. energy} \\ & + H^L + H^{L \leftrightarrow 1} && \text{left reservoir + tunneling } L \leftrightarrow 1 \\ & + H^{1 \leftrightarrow 2} && \text{interdot tunneling} \\ & + H^{2 \leftrightarrow R} + H^R && \text{tunneling } 2 \leftrightarrow R + \text{right reservoir} \end{aligned}$$

coherent interdot tunneling: $H_{DD} = H^e I + H^{12}$
artificial molecule

Interdot Tunneling

weak coupling between both dots

Double Dot Eigenstates:

$$|N\rangle = \lambda_1 |N_1, N_2\rangle + \lambda_2 |N_1 - 1, N_2 + 1\rangle$$

valence electron shared between both dots

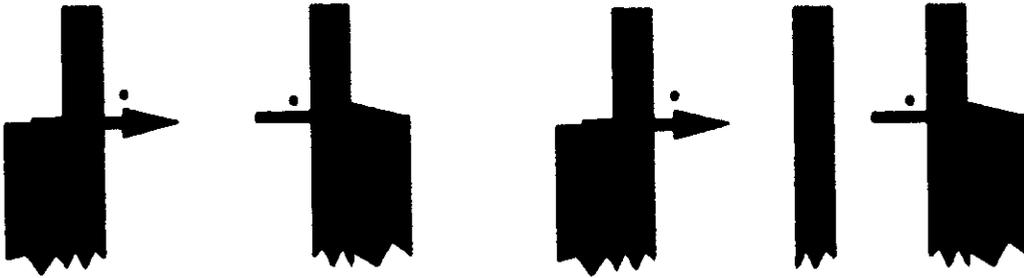
Coefficients depend on:

- interdot barrier transparency t
- $\Delta E = E(N_1, N_2) - E(N_1 - 1, N_2 + 1)$

at triple point:

$$\Delta E = 0, \quad \lambda_1 = \frac{1}{\sqrt{2}} = \lambda_2$$

Coupling to Reservoirs



modified tunneling rates:

$$\Gamma_{a,a'}^L = \Gamma^L |\langle N, a | c_1^\dagger | N-1, a' \rangle|^2$$

$$\Gamma_{a,a'}^R = \Gamma^R |\langle N, a | c_2^\dagger | N-1, a' \rangle|^2$$

intrinsic asymmetry of outer barriers

for single product state:

$$\langle N_1, \alpha; N_2, \beta | c_1^\dagger | N'_1, \alpha; N'_2, \beta \rangle \propto \delta_{N_1, N'_1+1} \delta_{N_2, N'_2}$$

$$\langle N_1, \alpha; N_2, \beta | c_2^\dagger | N'_1, \alpha; N'_2, \beta \rangle \propto \delta_{N_1, N'_1} \delta_{N_2, N'_2+1}$$

never simultaneously $\neq 0$

Differential Conductance of artificial molecules

for energetically isolated transitions between ground states:

$$\sigma = \frac{e^2}{h} 2\pi \Gamma_{0,0'}^{eff} \left(-\frac{\partial f_{0,0'}}{\partial \epsilon} \right)$$

energy conservation

$$\frac{1}{\Gamma_{0,0'}^{eff}} = \frac{1}{\tilde{\Gamma}_{0,0'}^L} + \frac{1}{\tilde{\Gamma}_{0,0'}^R}$$

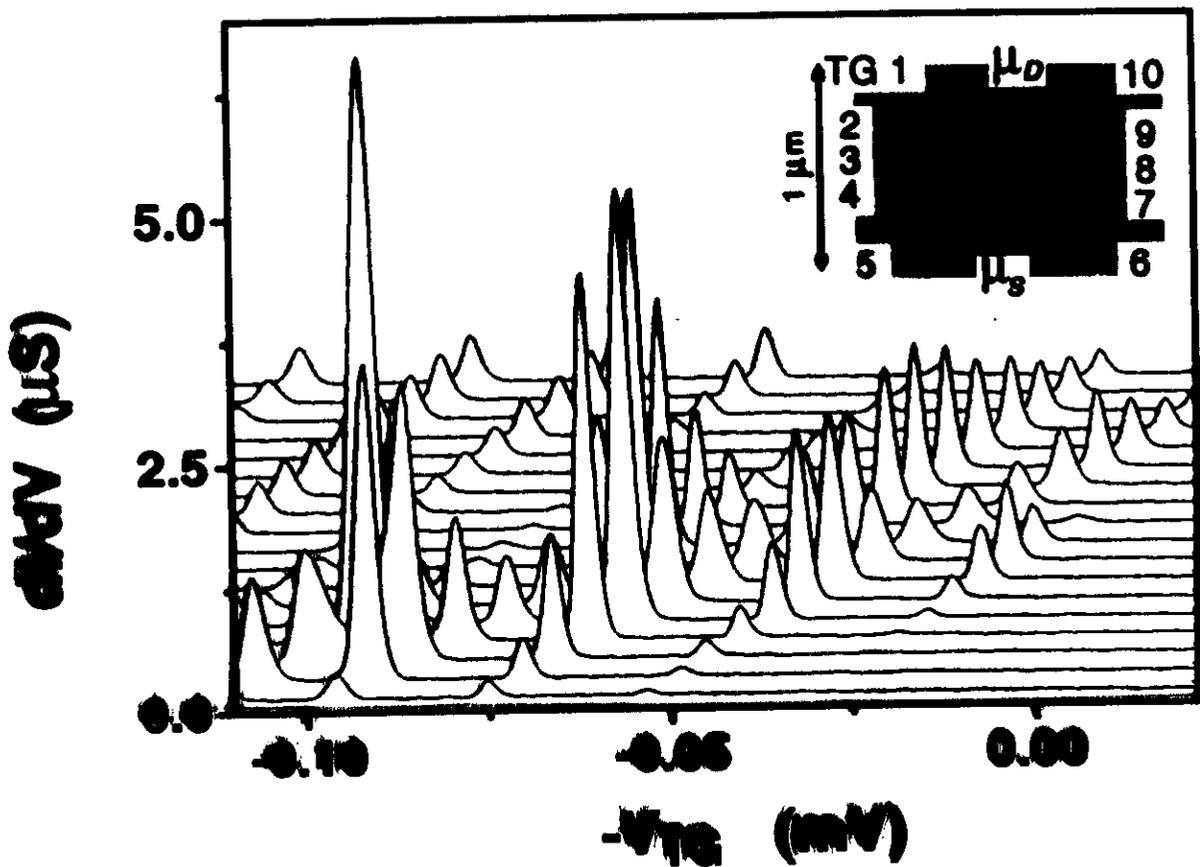
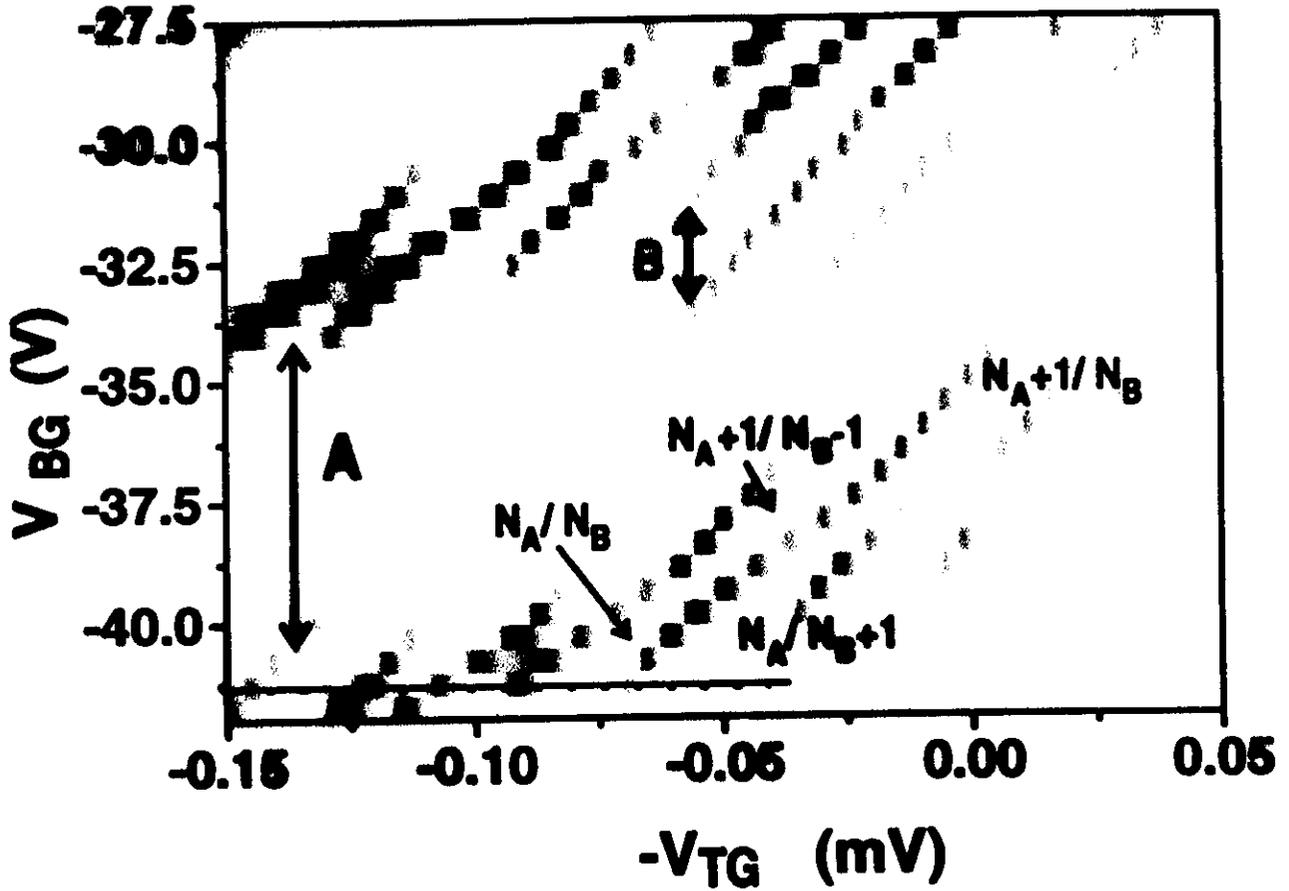
modified tunneling rates

for coherent interdot tunneling:

$$\Gamma_{0,0'}^{eff} = \frac{\lambda_1^2 \lambda_2^2}{\lambda_1^2 + \lambda_2^2} = \Gamma \frac{4|t|^2}{4|t|^2 + (\Delta E)^2}$$

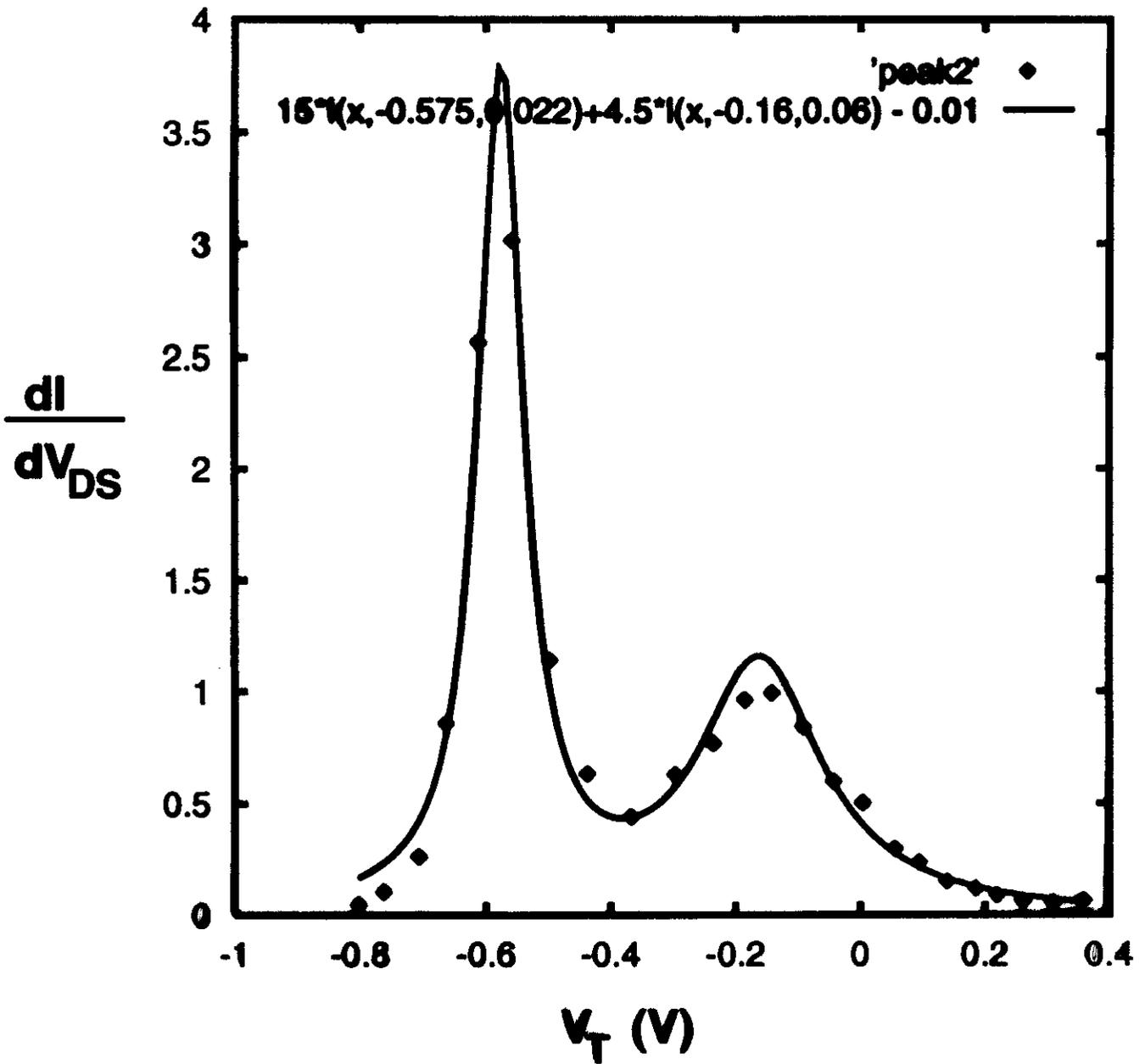
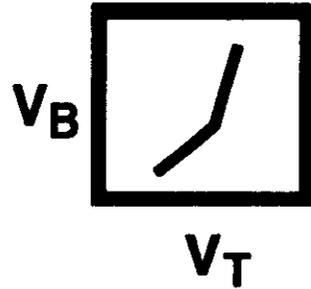
Lorentzian Peakform

Charging Diagram:



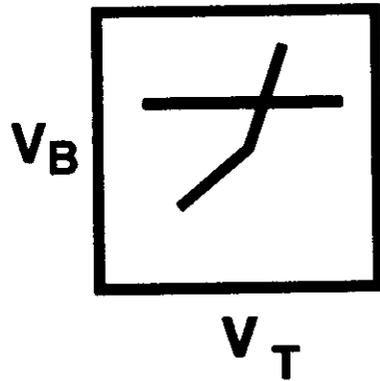
Lorentzian-Lineshape

Theory and Experiment

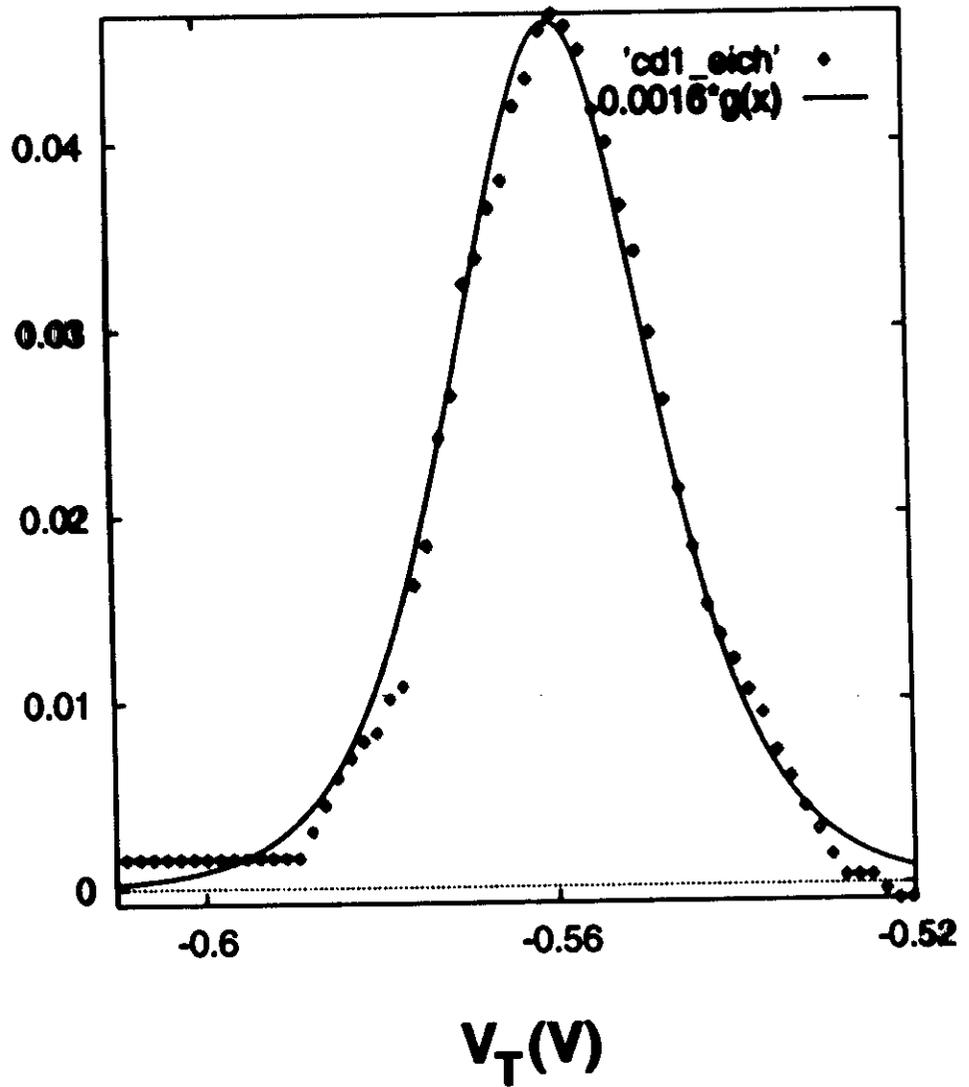


Fermi-Peak

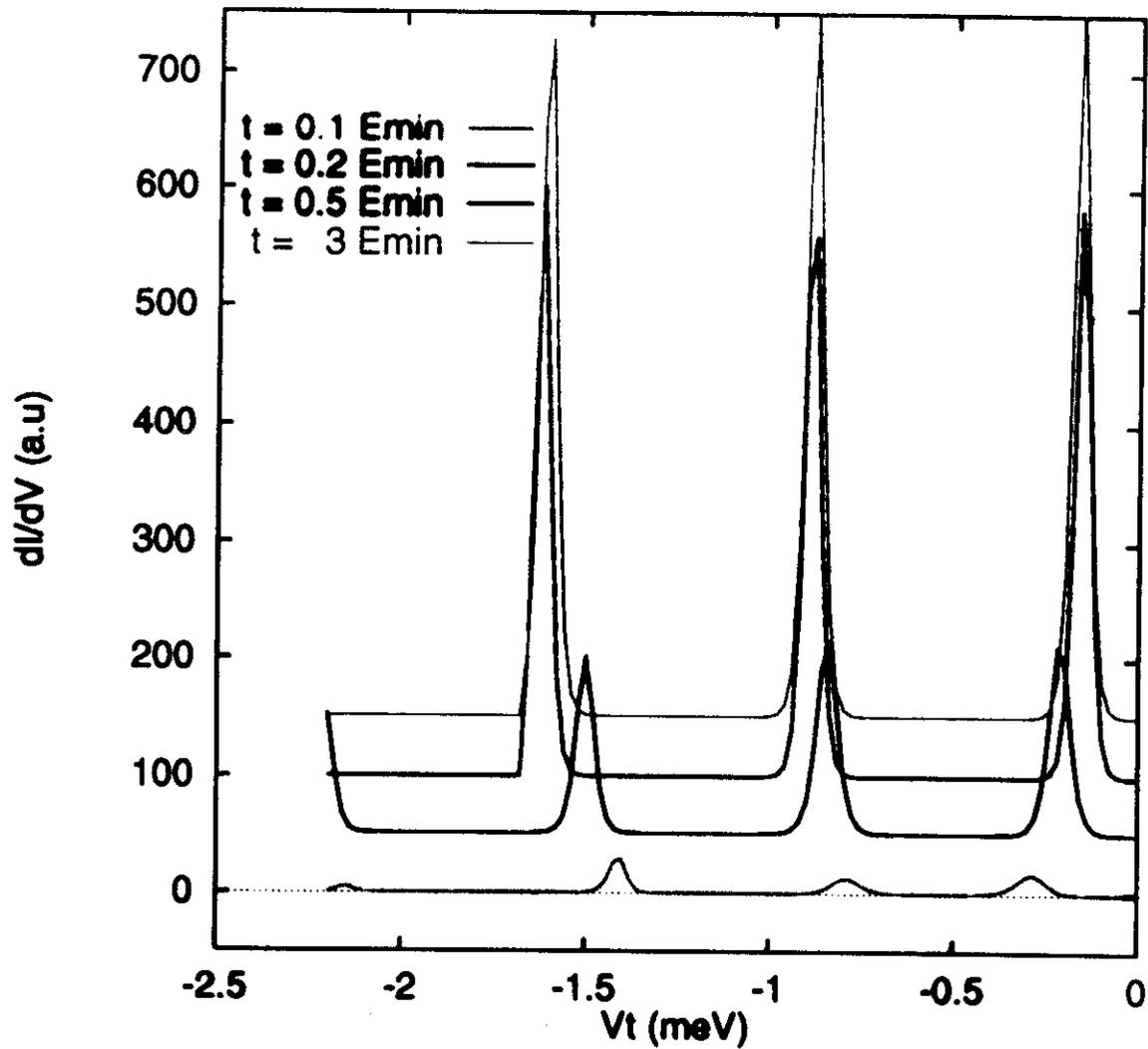
fit: $g(x) \sim (-f_{FD})$



$\frac{dI}{dV_{DS}}$



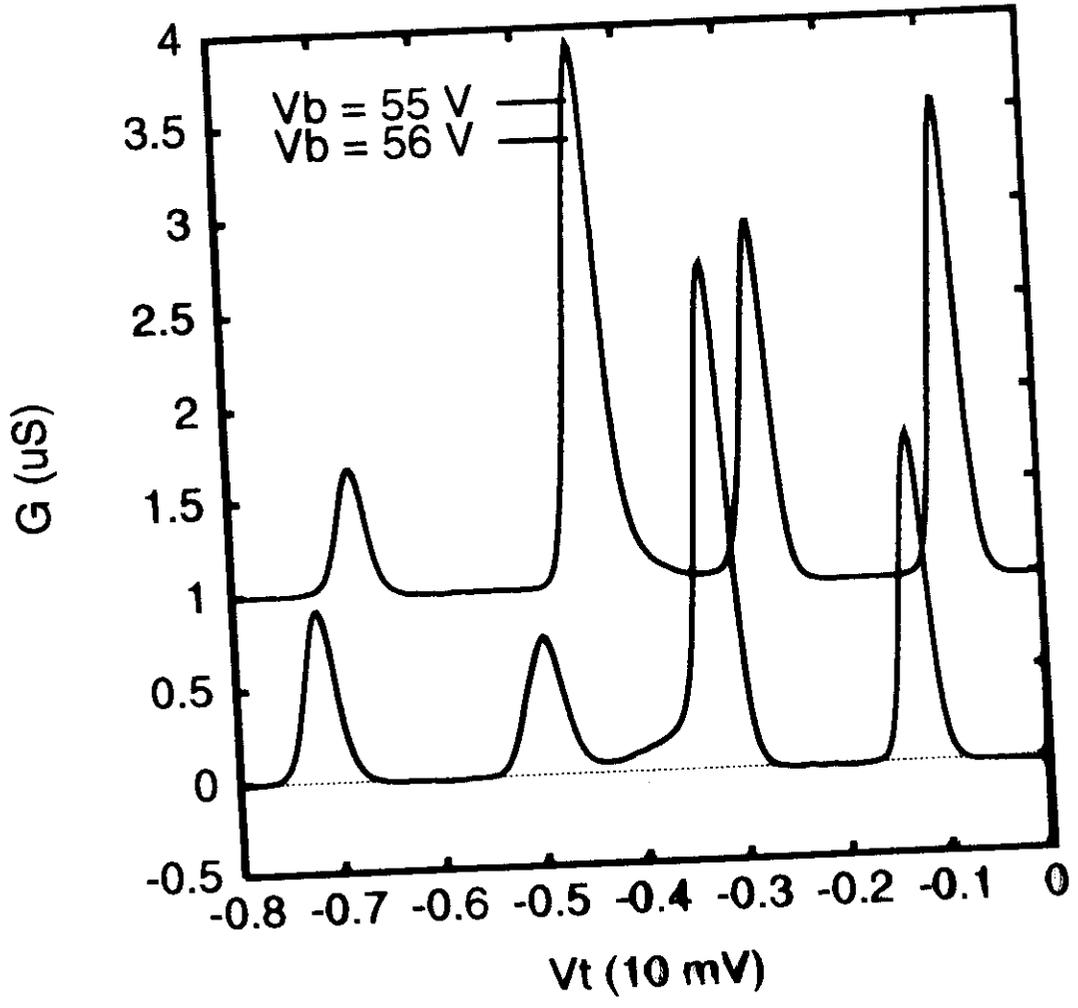
From Double Dot to Single Dot



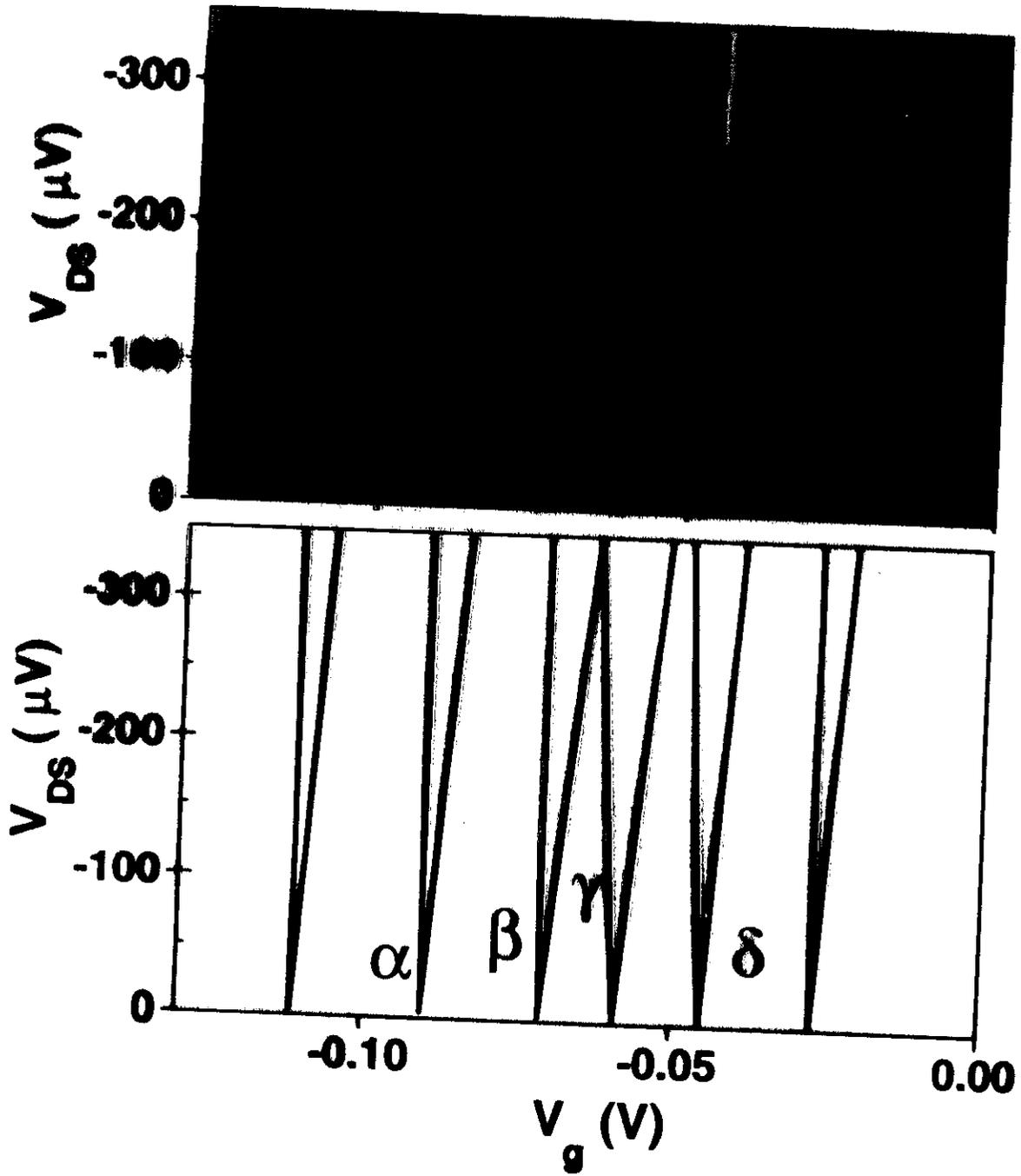
saturation of peak height

vanishing modulation of periodicity

Resonances from Anti-Bonding States



Charging Diagram at Finite Bias



Theory vs Experiment

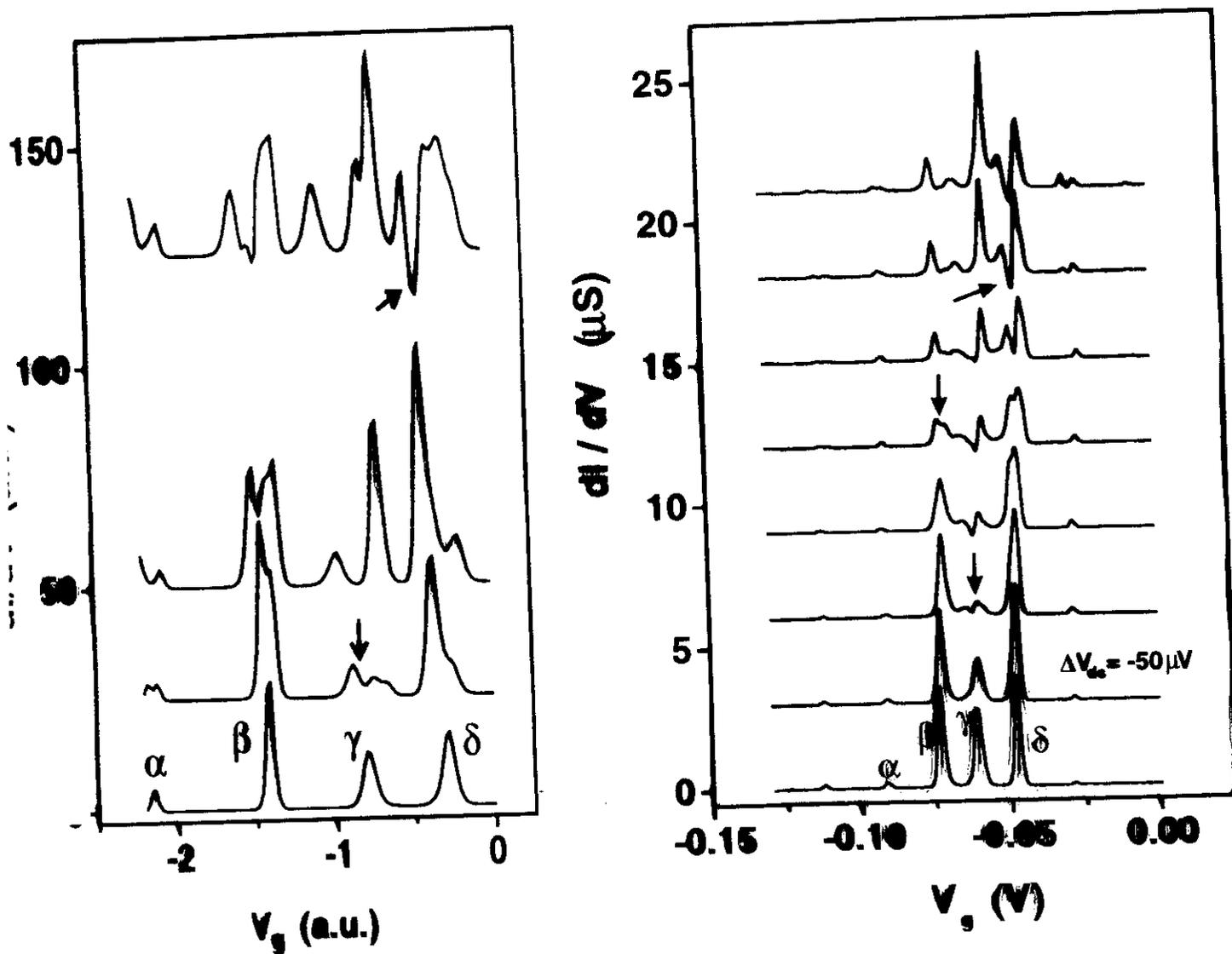


Fig. 4, Blick et al.

Summary

- **Single Quantum Dots:**
sequential tunneling
- **Coulomb interaction:**
correlations → selection rules
- **excitation spectroscopy:**
dominated by collective response
- **linear transport in Double Quantum Dots**
coupled in series
→ **coherent interdot tunneling**
- **spectroscopy of artificial molecular states**
- **resonance shows Lorentzian form**
for electrostatic detuning

