



UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION  
INTERNATIONAL ATOMIC ENERGY AGENCY  
INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS  
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**SMR.998d - 8**

Research Workshop on Condensed Matter Physics  
30 June - 22 August 1997  
**MINIWORKSHOP ON  
QUANTUM WELLS, DOTS, WIRES  
AND SELF-ORGANIZING NANOSTRUCTURES  
11 - 22 AUGUST 1997**

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**"Vertically coupled InGaAs-AlGaAs Quantum Dots:  
Growth, Characterization, High Power Lasers"**

**PART I**

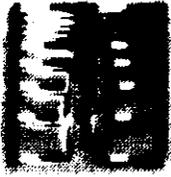
**N.N. LEDENTSOV  
A.F. Ioffe Physico-Technical Institute  
Politekhnikeskaya 26  
194021 St. Petersburg  
Russia**

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**These are preliminary lecture notes, intended only for distribution to participants.**

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ENRICO FERMI BUILDING VIA BEIRUT, 6 (TELEPHONE, FAX AND TELEX THROUGH MAIN BUILDING)

**N.N. Ledentsov**



**Abraham F. Ioffe Institute,  
194021 St. Petersburg, Russia**



**Technische Universität Berlin  
10623 Berlin, Germany**

**QUANTUM DOT  
GROWTH, CHARACTERIZATION,  
HIGH POWER LASERS**

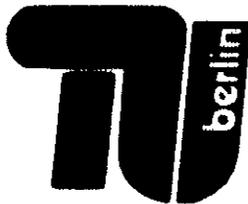
# Cooperation:

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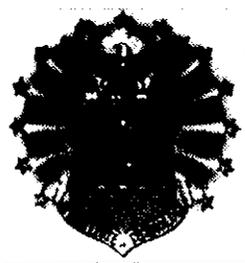
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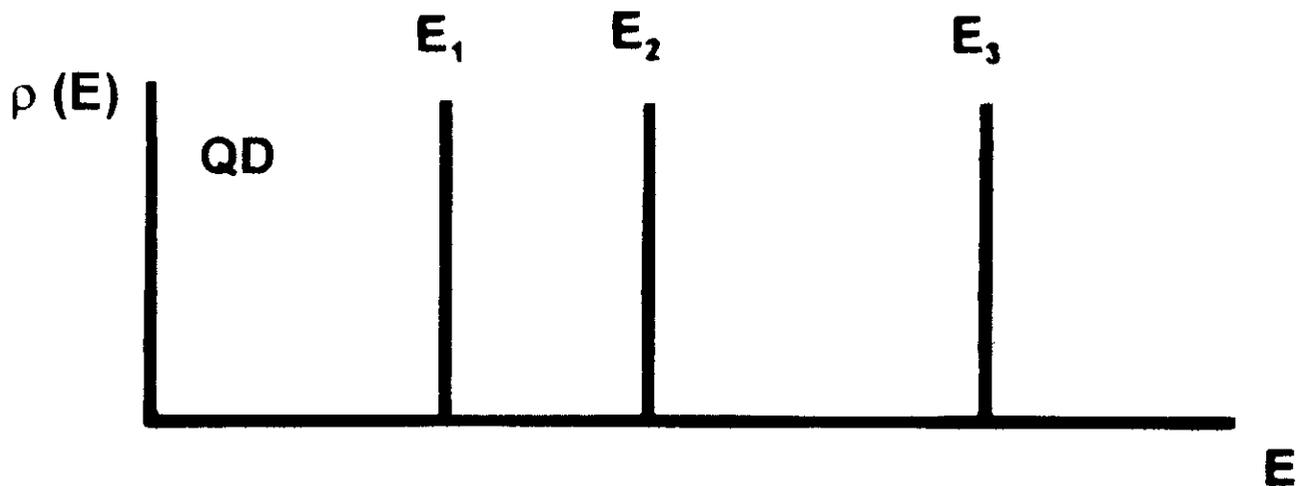
## Acknowledgments

**Volkswagen Stiftung, INTAS-94-1028 grant,  
Russian Foundation of Basic Research,  
Deutsche Forschungsgemeinschaft (Sfb 296)**

# **Contents:**

- ***Advantages and Requirements for QDs***
- ***Self-Organized Growth of QDs  
Ordering Phenomena***
- ***TEM/HRTEM Characterization of QDs***
- ***Energy Spectrum***
- ***Optical Properties***
- ***Shape Transformation Effects  
Vertically Coupled QDs (VCQDs)***
- ***Laterally Associated VCQDs***
- ***Edge Emitting Lasers Based on VCQDs***
- ***Realization of High Power CW Operation***
- ***Vertical Cavity Lasers Based on VCQDs***
  
- ***Future Trends***

# Basic Advantages of Quantum Dots



## ATOM like Energy Spectrum

- **$\delta$ -function like density of states.**

**No thermal broadening.**

**No inhomogeneous broadening for single quantum dot**

- **Giant exciton oscillator strength.**  
**Ultrahigh material gain.**  
**Ultrahigh differential gain**

- **Lifting of  $k$ -selection rule**

- ...

# What Kind of Quantum Dots Do We Need?

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- **At least one electron level should exist in the QD**  
( $\Delta E_c > E_1^{QW}$ )

**Quantum Dot Size**

- **Localization energies for electrons and holes should be larger than 3 kT at RT**

**Temperature Dependent Excitation**

- **Energy separation between QD sublevels should be larger than 3 kT at RT:**  
( $kT < E_1^{QW}$ )

$d^{2D}$  must be smaller than 14 nm (GaAs-QDs)  
 $d^{2D}$  must be smaller than 20 nm (InAs-QDs)

- **Dislocation free, low concentration of nonradiative recombination centers (direct growth methods)**

**Photoluminescence efficiency**

- **Uniformity in shape and in size.**  
**Dense arrays.**

**Requirements for lasers**

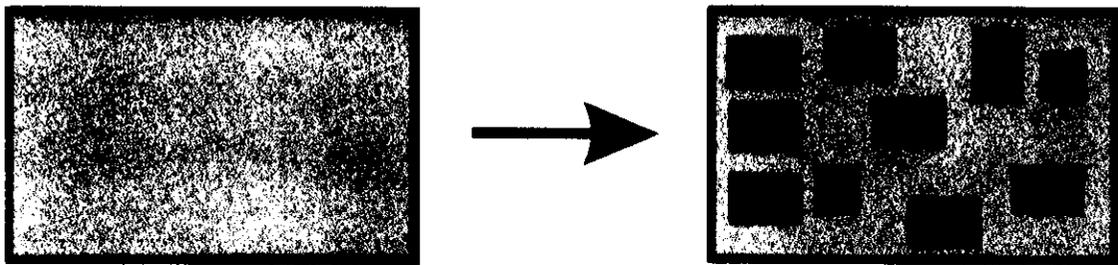
# Selforganization of Quantum Wires and Dots



**Nanofaceting**



**Alloy decomposition during growth**



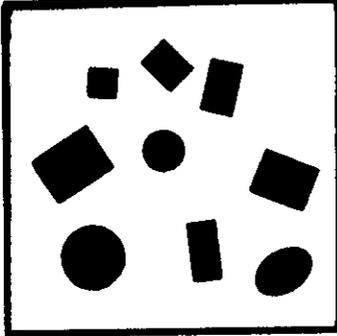
**Alloy decomposition during annealing**



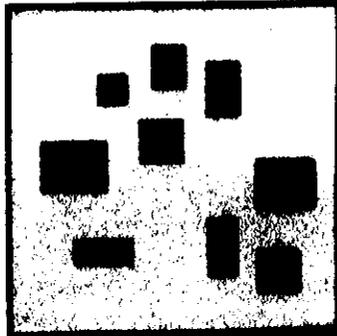
**Islanding**

# Hierarchy of Ordering

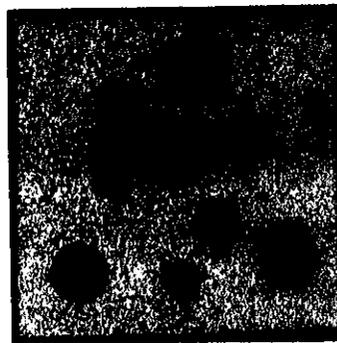
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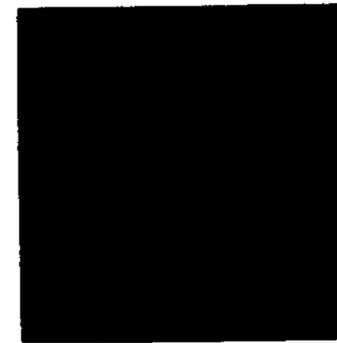
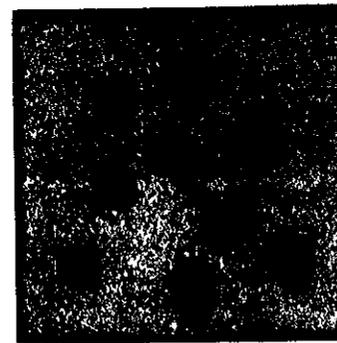
**No Order**



**Orientation**



**Shape**



**Alignment**

# 1985: First Observation of InAs/GaAs Islands and Vertical Ordering

15 periods of  
2.5ML InAs  
30nm GaAs



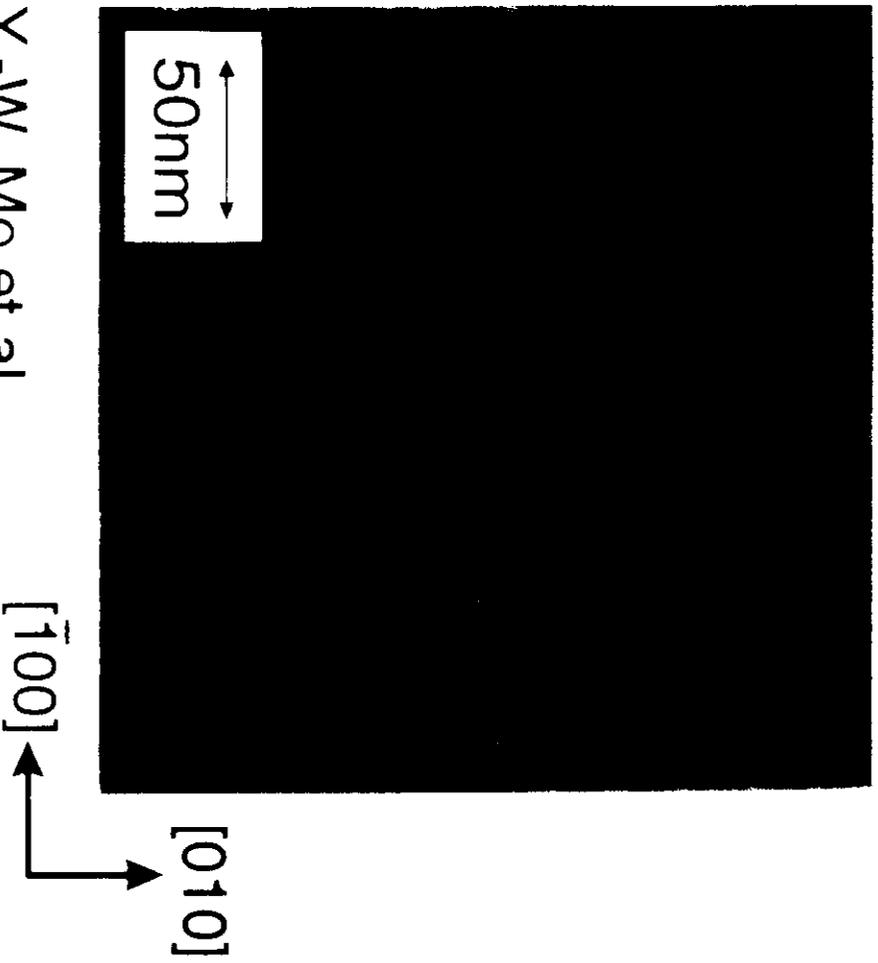
L. Goldstein et al.,  
APL 47, 1099 (1985)

40nm

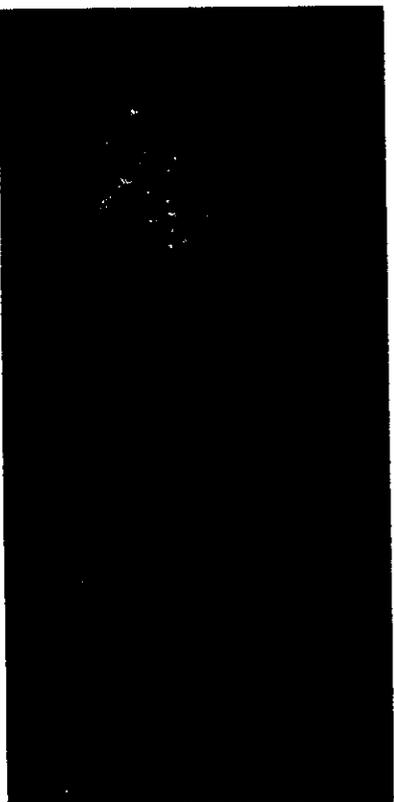
004

"These kind of  
structures are  
thus proved to  
be of interest  
to study  
low-dimensional  
( $<2$ )  
objects showing  
good optical  
properties"

## 1990: Rectangular Ge "Hut" Clusters on Si(001)

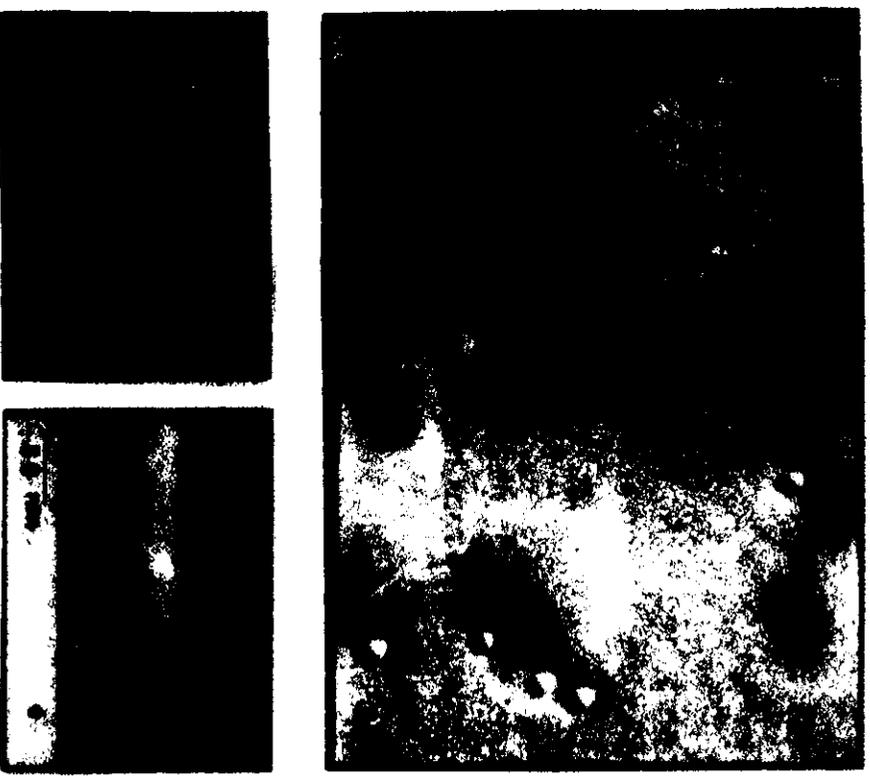


Y.-W. Mo et al.  
PRL 65, 1020 (1990)

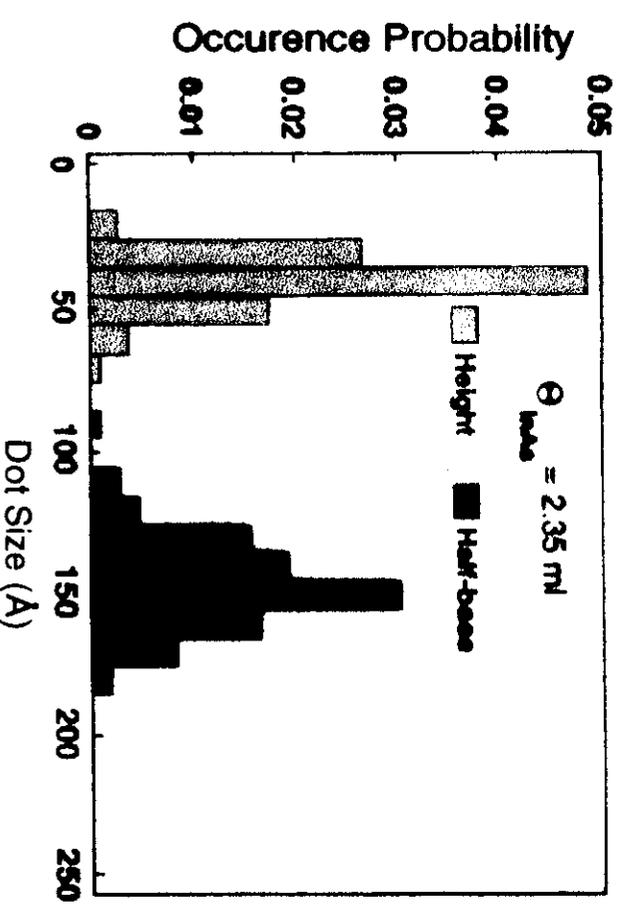


- No size ordering
- No shape ordering

# 19924: Self-ordered InAs/GaAs Quantum Dots



- Size ordering
- Shape ordering



D. Leonard et al.  
APL 63, 3203 (1993)

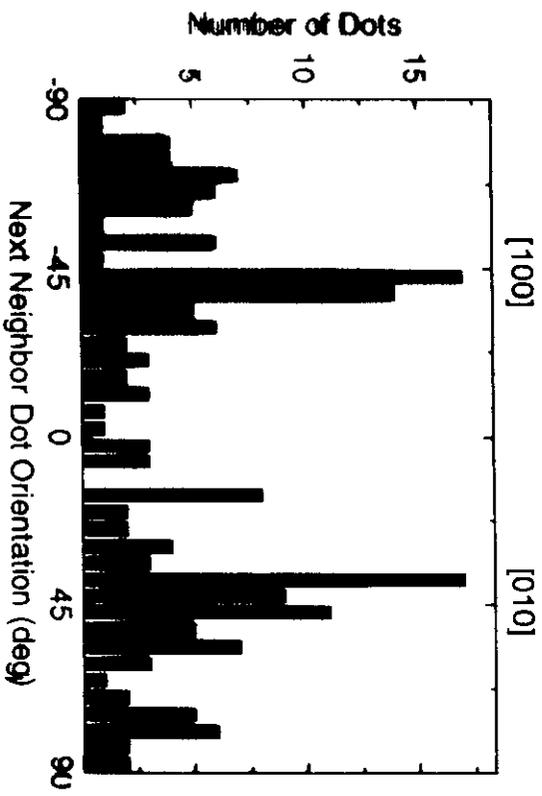
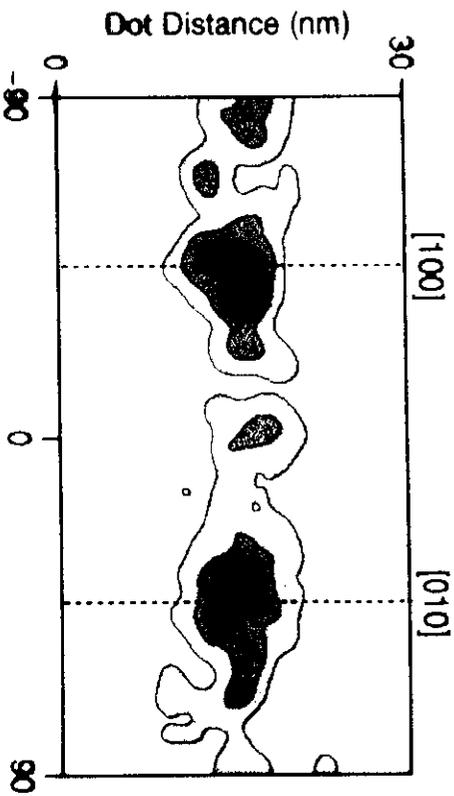
J.M. Moison et al.  
APL 64, 197 (1994)

# Lateral Ordering of Quantum Dots in a 2D Square Lattice

plane-view TEM



Statistical Evaluation

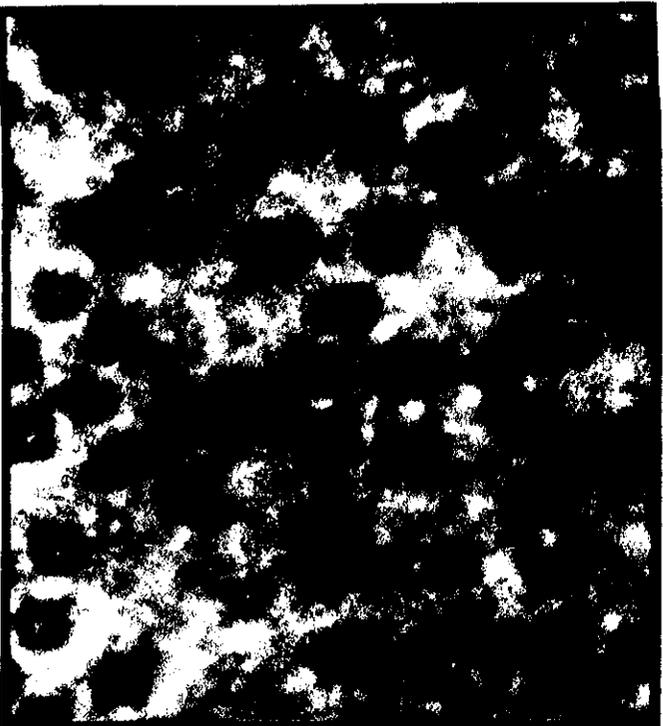


# Self-Organized Growth of Quantum Dots

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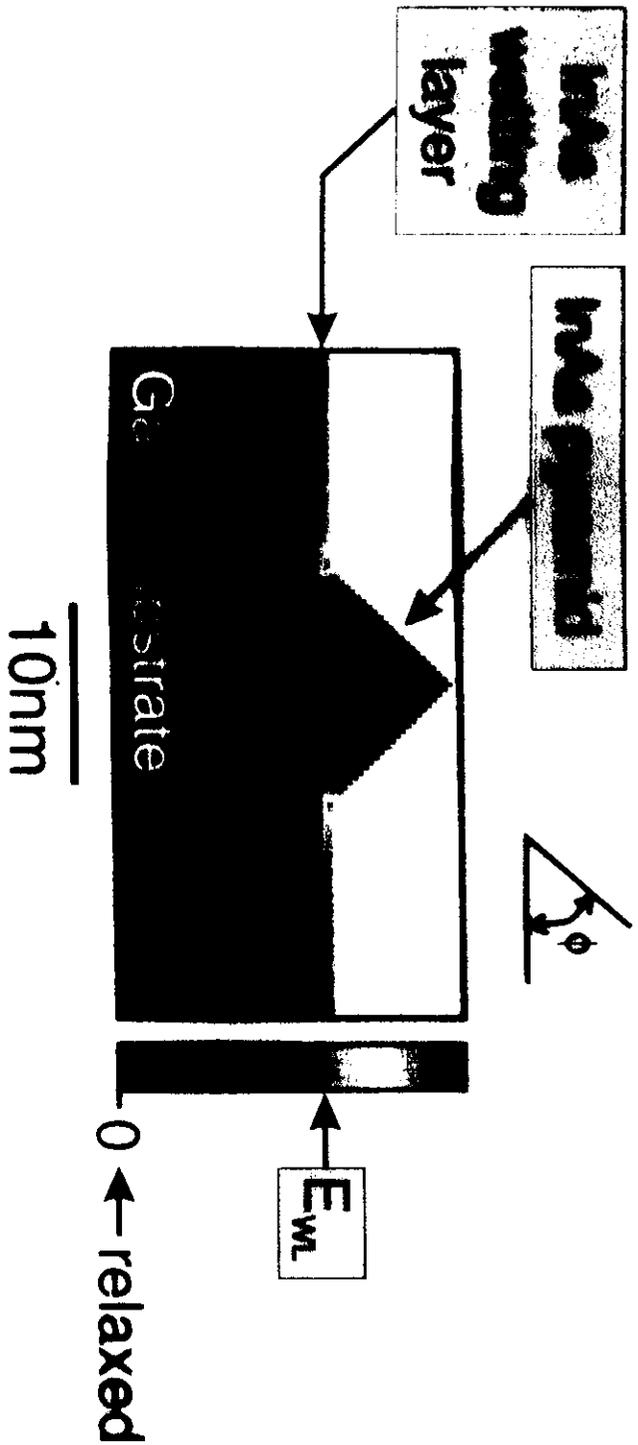
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Plan view TEM of ordered  
array of InAs/GaAs quantum  
dots grown using MBE



- Why do 3D objects of similar size and shape develop ?
- What is their shape?
- Why are they ordered ?
- What are the optimal growth conditions ?

# Relaxation of Elastic Energy



$\phi=45^\circ$	:	$\Delta E = -$	$0.07\%$	$E_{wL}$
$\phi=5^\circ$	:	$\Delta E = -$	$0.8\%$	$E_{wL}$

● Top of pyramid is strain free

M. Grundmann, V.A. Shchukin, 1995

# Energetics of 3D Islanding

Energy Decrease due to the  
Island Elastic Relaxation ( $-\Delta E_v$ )

and

Increase in Surface Area

Change of surface energy  $\Delta E_s$

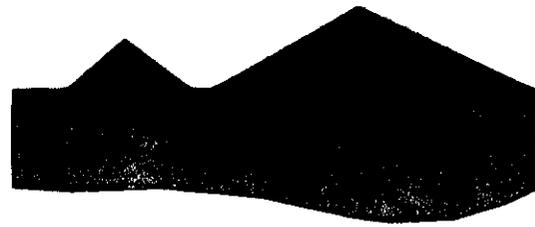
**Positive and large**



Critical island size ( $\Delta E_v > \Delta E_s$ ) is large

Dislocations are formed before islands appear

**Positive and small**



Islands of critical size appear and undergo ripening

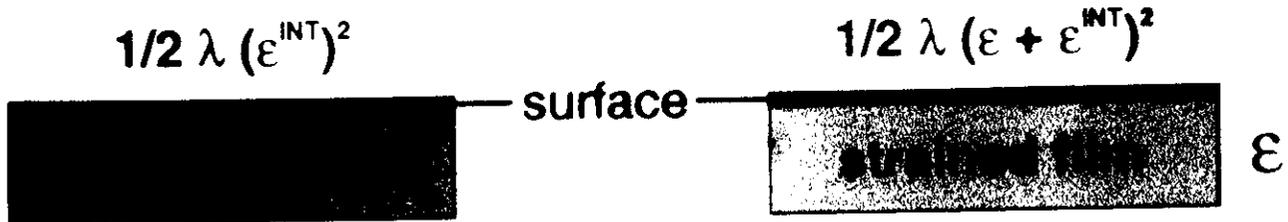
**Negative**

At some size ripening is energetically unfavorable

# Strain-induced Renormalization of Surface Energy

Concept of intrinsic surface strain ( $\epsilon^{INT}$ )

V.I. Marchenko, A.Ya. Parshin, 1980



Change of surface energy per unit area

$$\Delta E_{\text{SURFACE}} = -\tau \epsilon + S \epsilon^2$$

Intrinsic surface stress ( $\tau$ ) can be positive or negative ( $\sim 100 \text{ meV / \AA}$ )

Surface energy ( $S$ ) is always positive ( $\sim 2000 \text{ meV / \AA}^2$ )

**Surface energy of a strained wetting layer can be larger than that of the relaxed island**

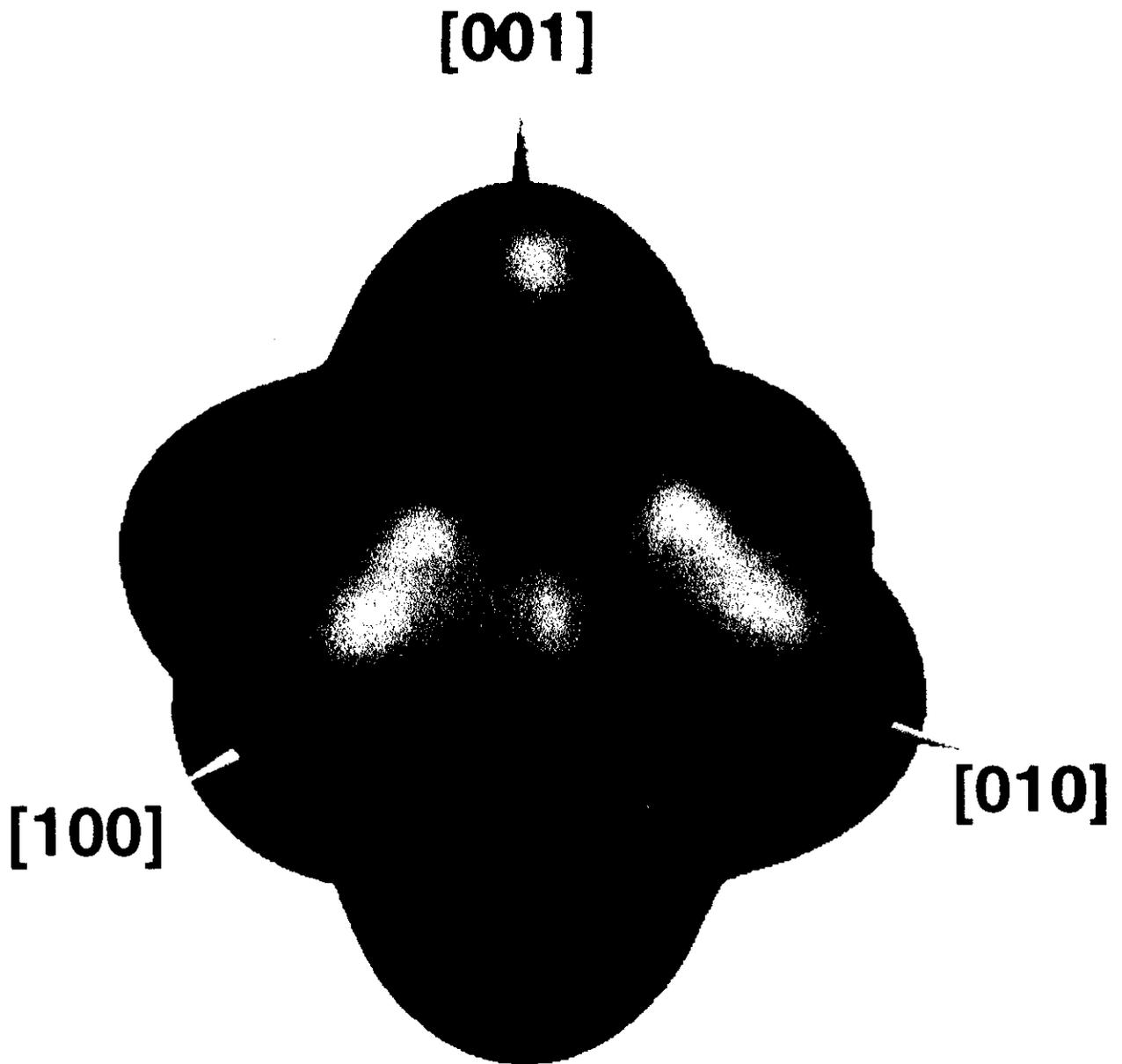
**Coverage of surface with islands of optimal size, no ripening**

# ***Anisotropy of Young's Modulus in GaAs***

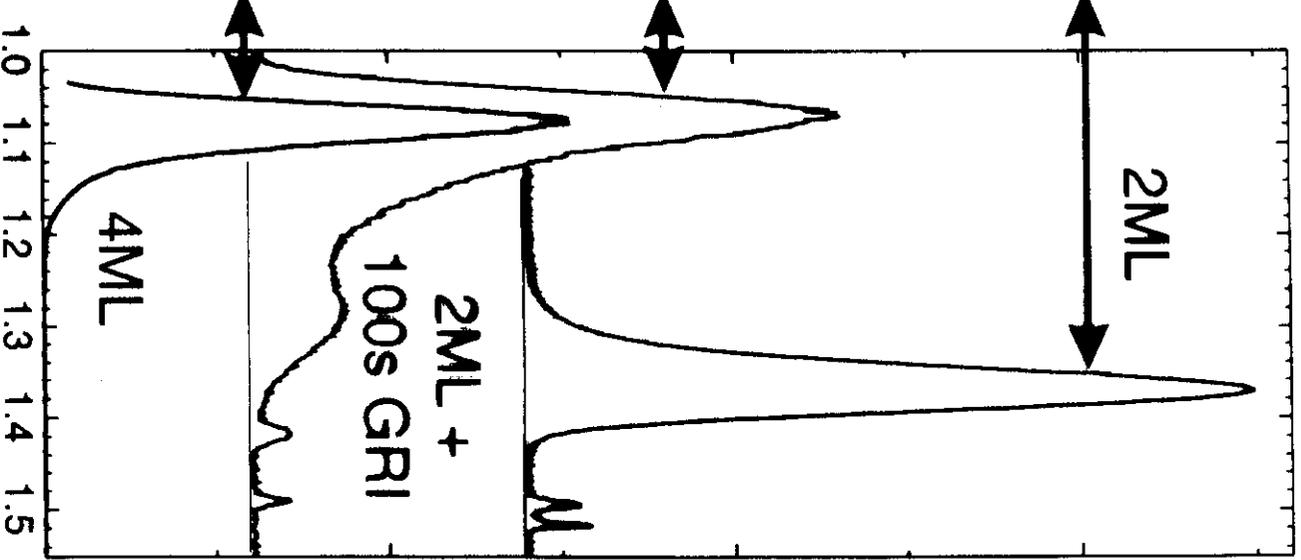
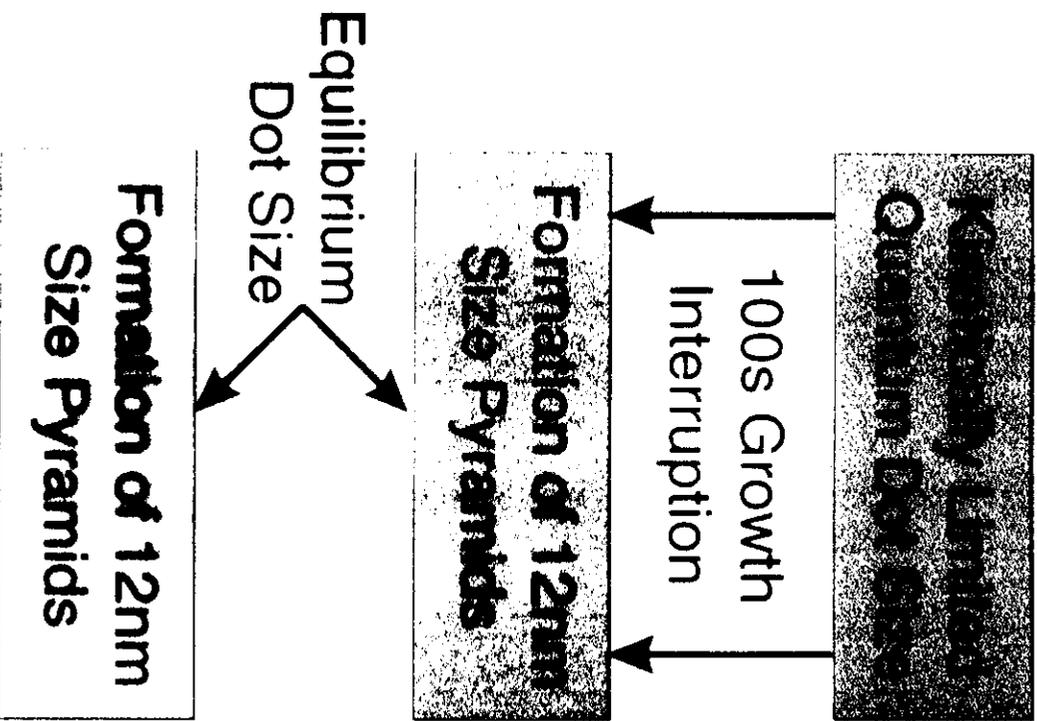
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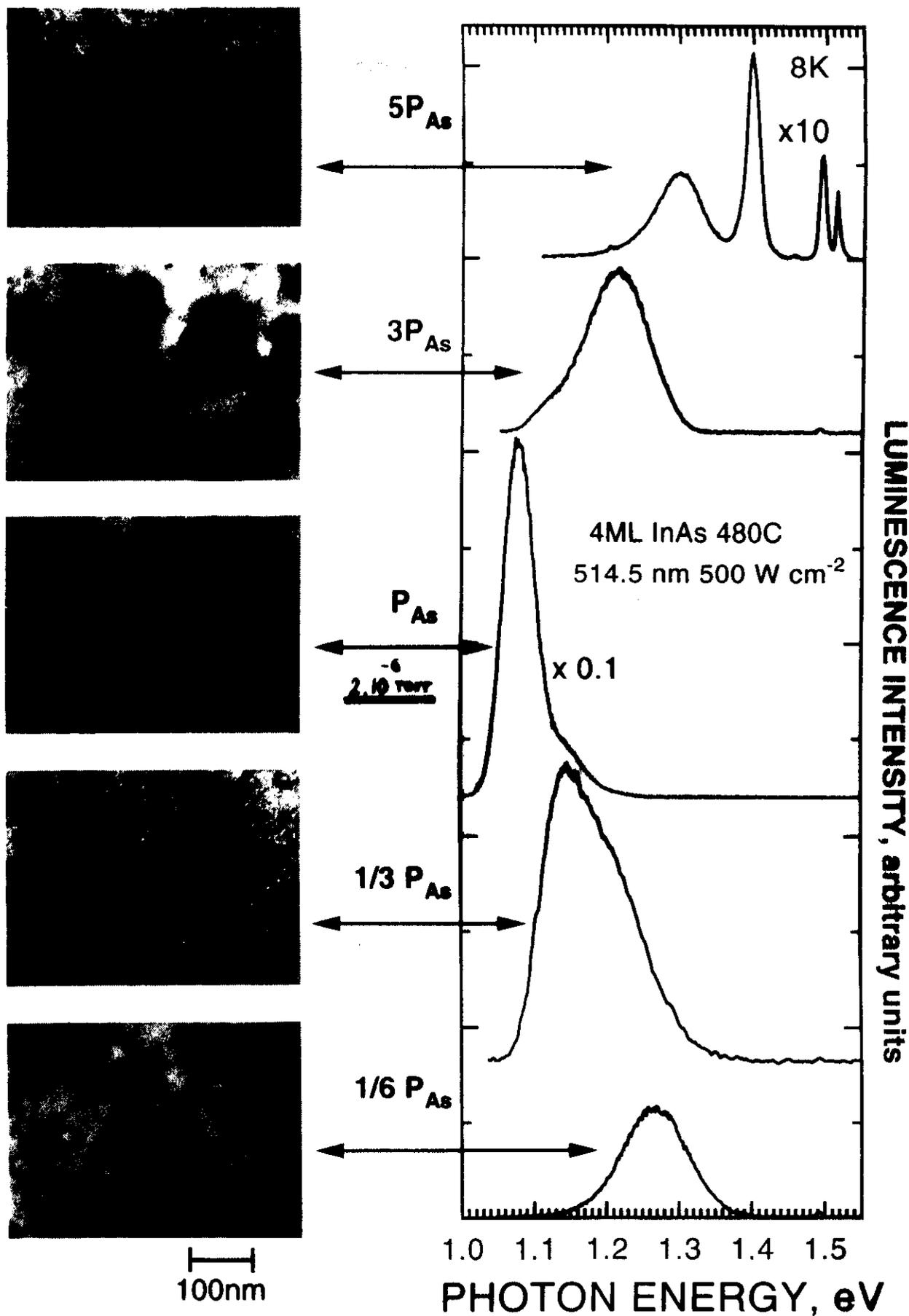
$$\epsilon_{\vec{n}\vec{n}} = \frac{1}{Y(\vec{n})} \sigma_{\vec{n}\vec{n}}$$



# Kinetically Limited and Equilibrium Size Islands

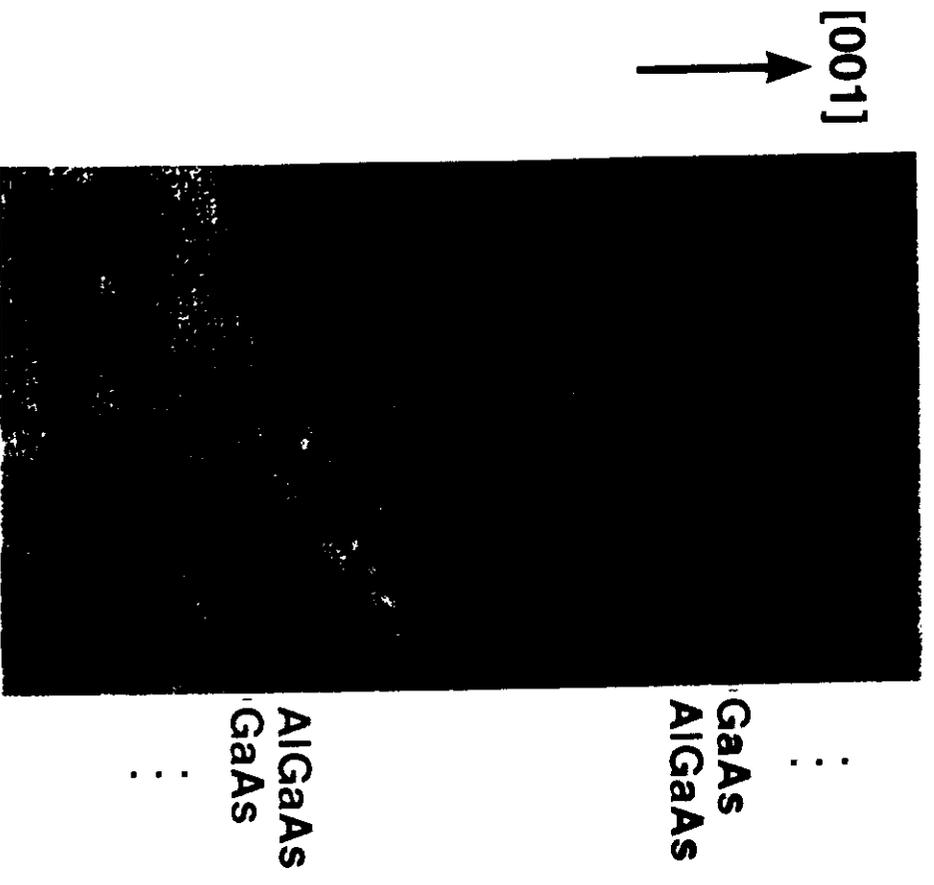


# Arsenic Pressure Dependence of Dot Formation

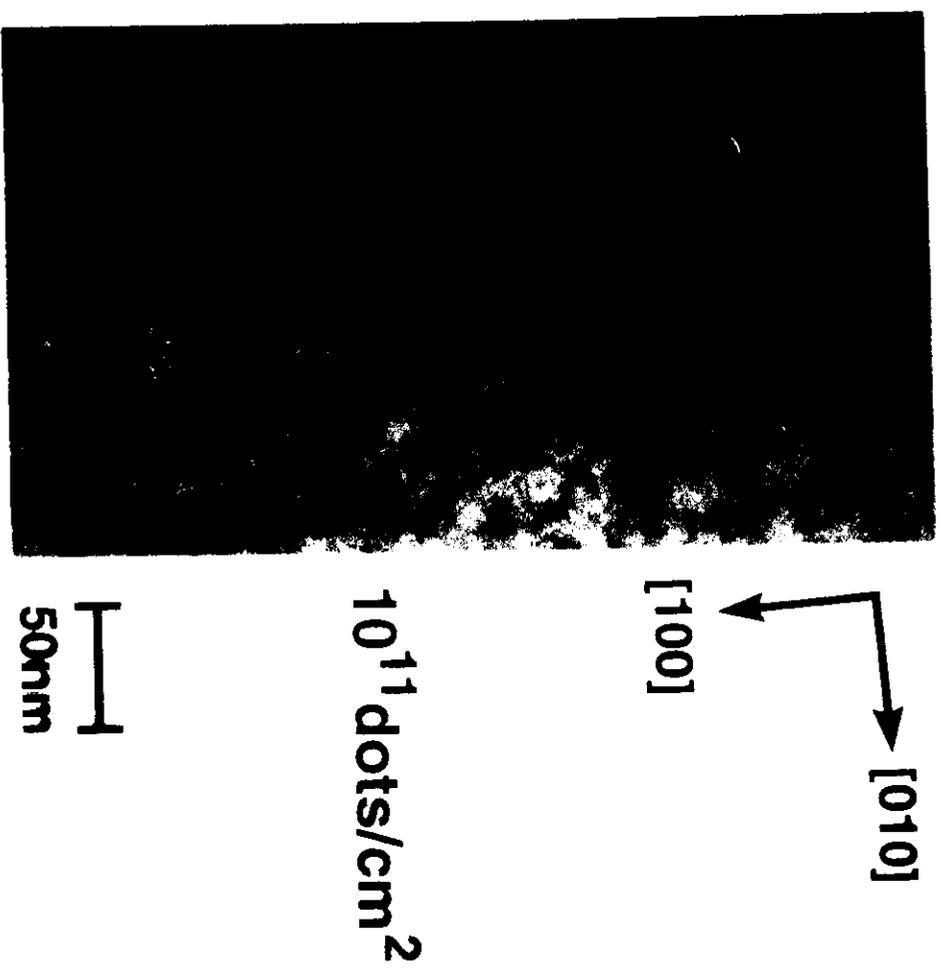


# Transmission Electron Microscopy of InAs/GaAs Quantum Pyramids

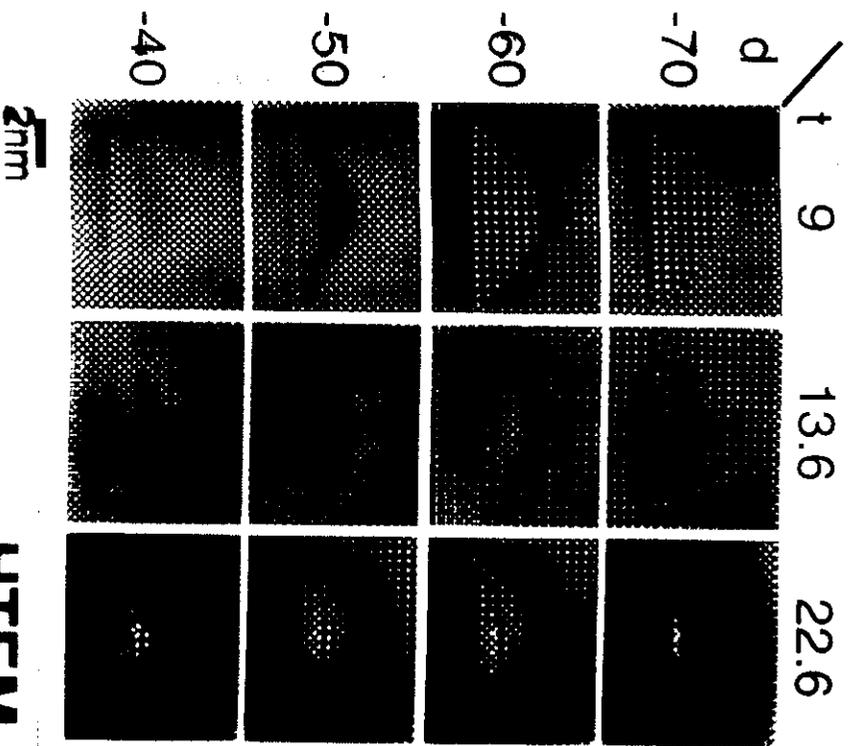
**Cross section**



**Plan view**



# Simulation of TEM of InAs/GaAs Pyramid



**HTEM**

**Model Geometry**

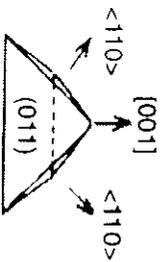
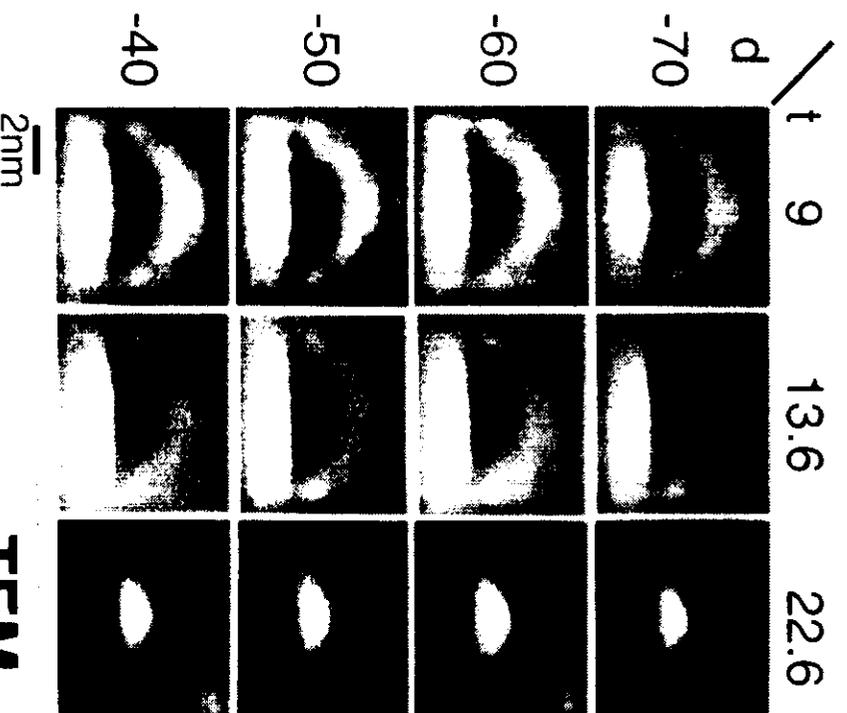


Image plane (010)



**TEM**

- depends strongly on foil thickness and defocus
- optimal defocus ( $d = -60$  nm at  $t = 9$  nm) reveals true shape

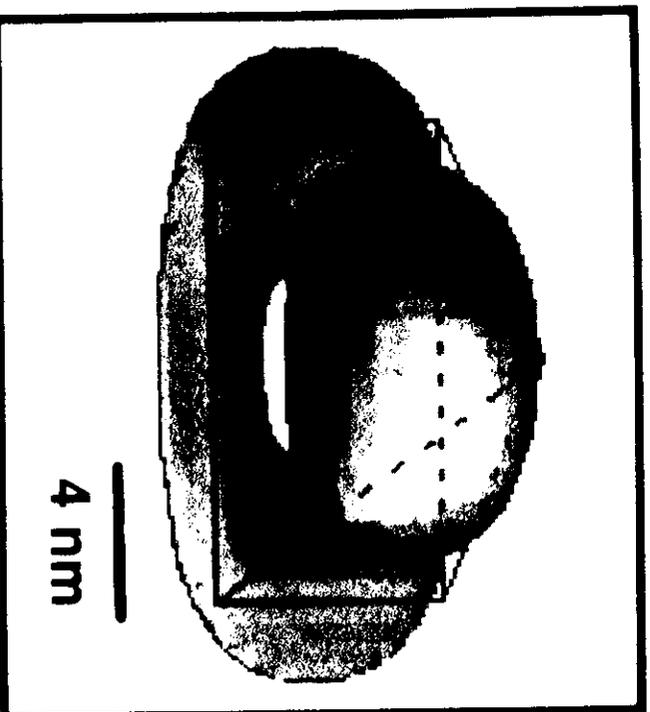
- almost no dependence on defocus
- height is underestimated
- shape appears truncated/lens

# Simulation of Pyramidal Quantum Dots

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Wavefunction of (001) excited  
hole state in pyramidal  
InAs/GaAs quantum dot



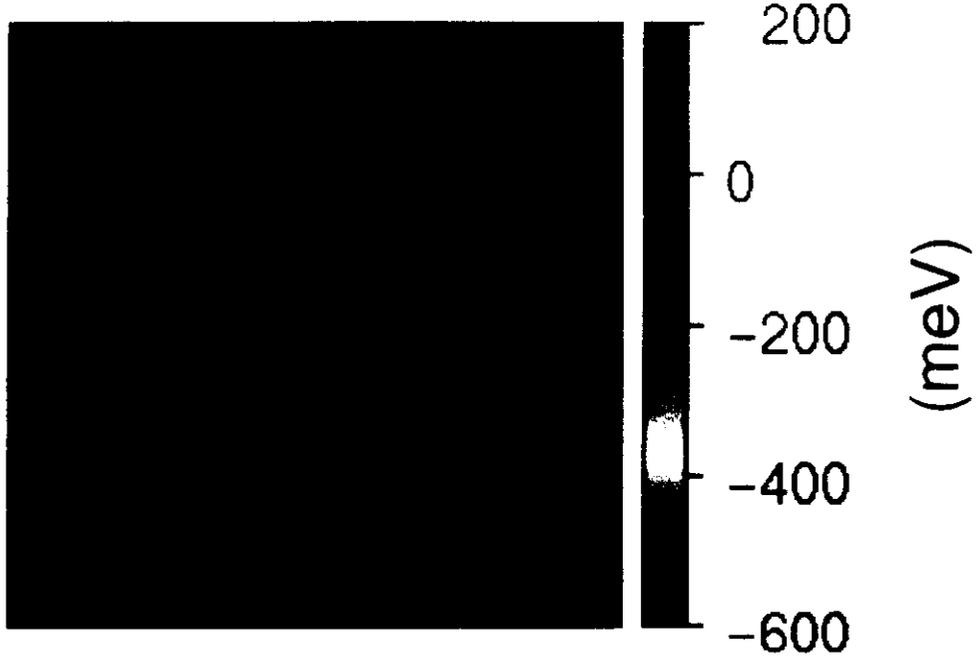
- 3D Strain distribution in dot, wetting layer and surrounding barrier
- Confinement potential
- 3D effective mass Schrödinger equation
- Electron and Hole levels

# Confinement Potentials in Strained InAs/GaAs Pyramid

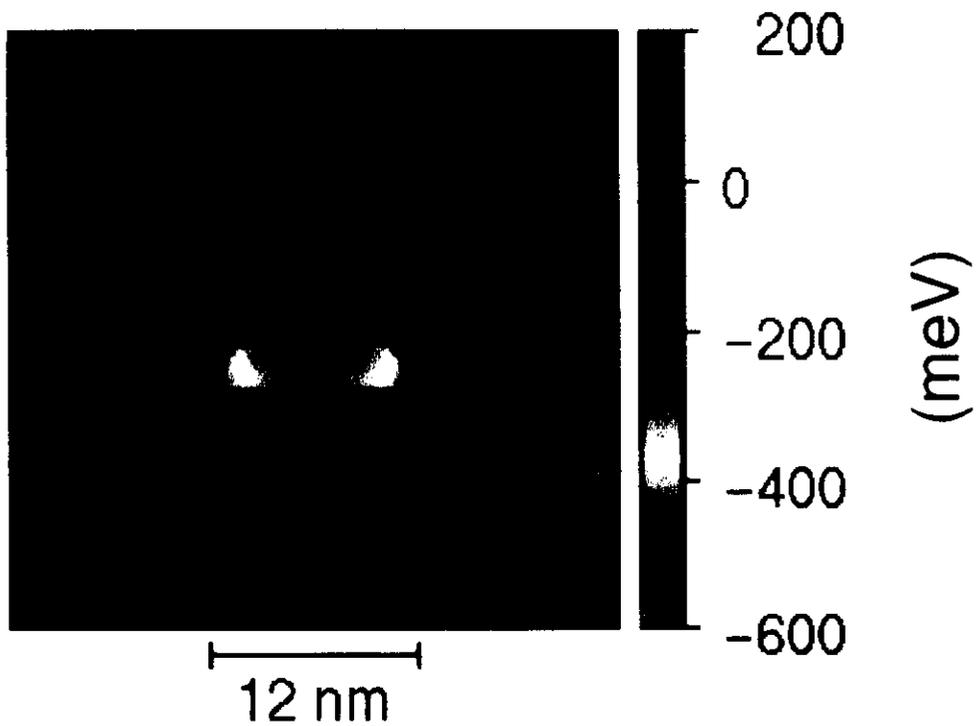
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## Electrons



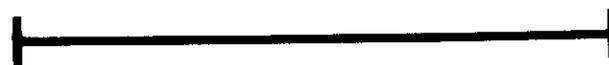
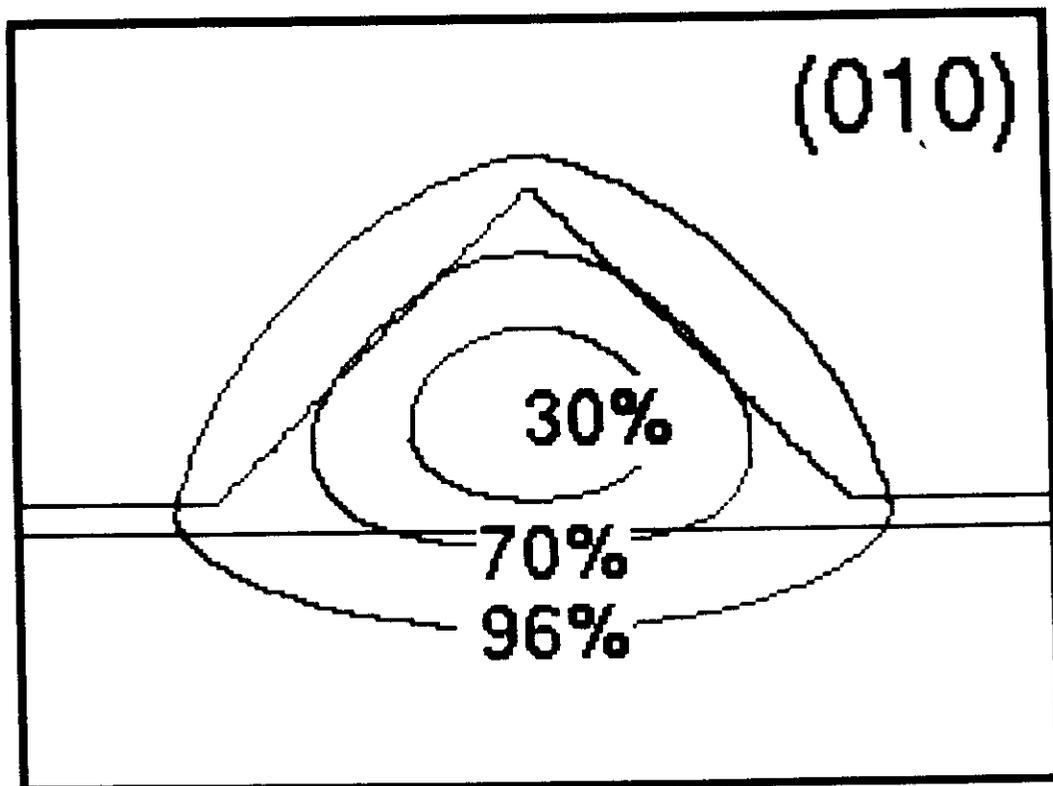
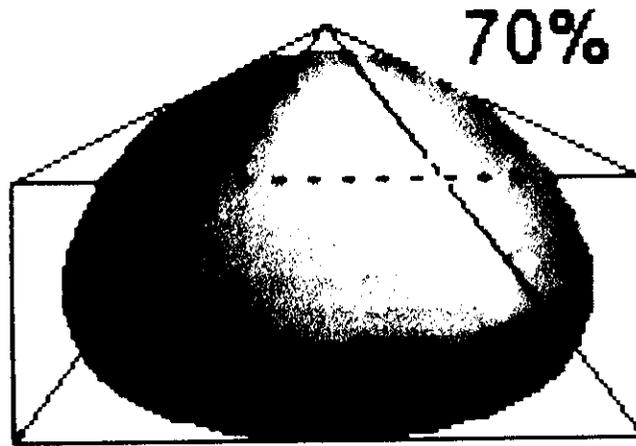
## Holes



# Electron Ground State in InAs/GaAs Quantum Pyramid

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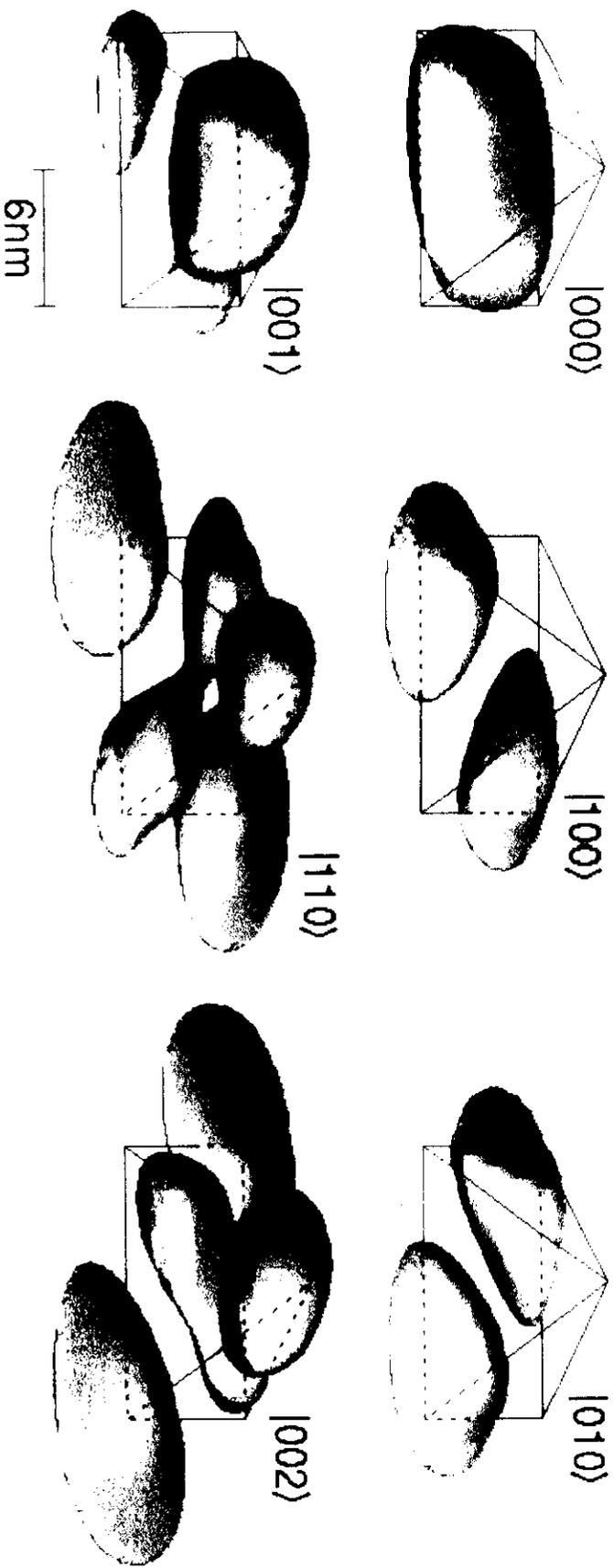


12 nm

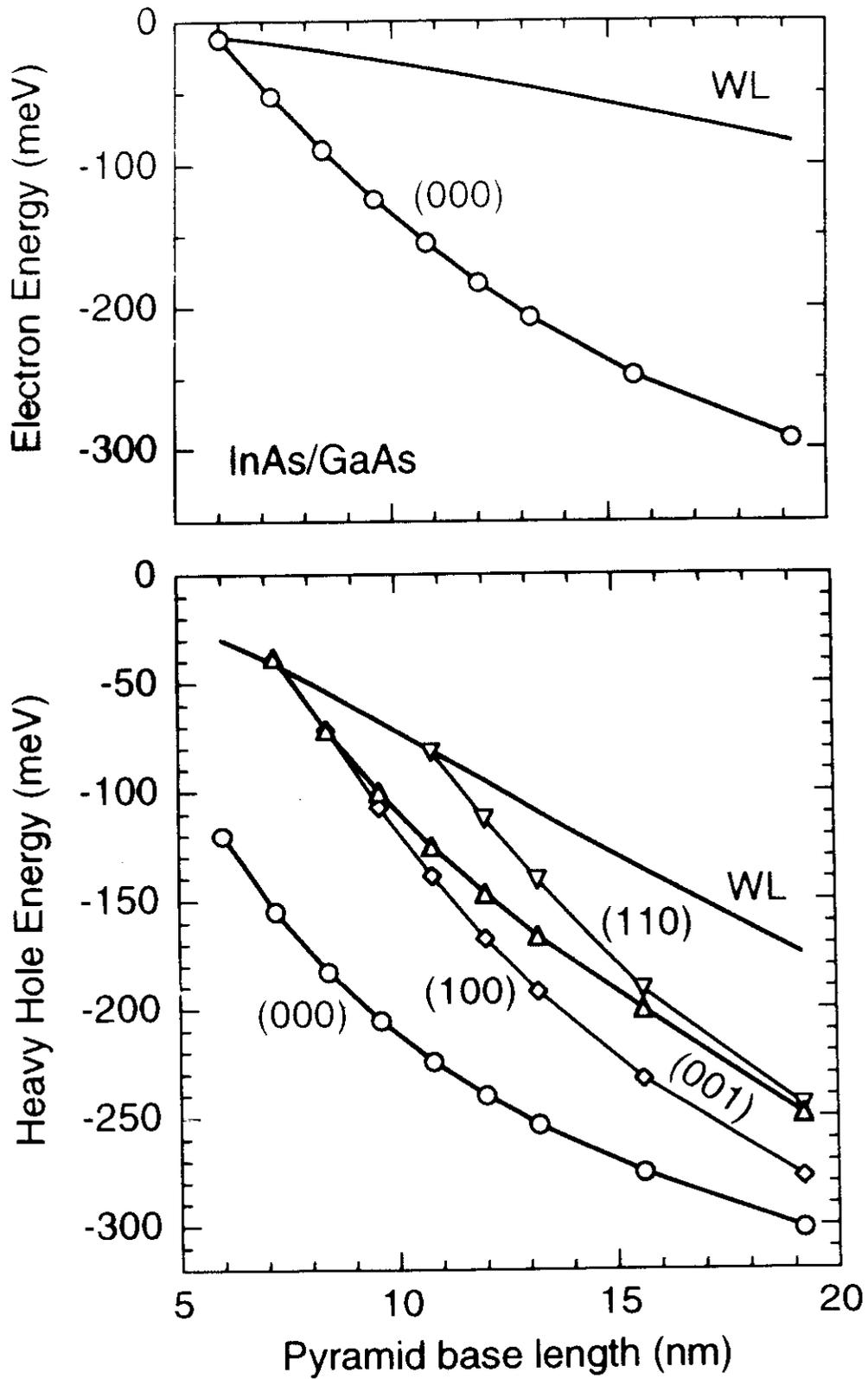
# Hole Wavefunctions in 12nm InAs/GaAs Quantum Pyramid with Piezoelectric Potential

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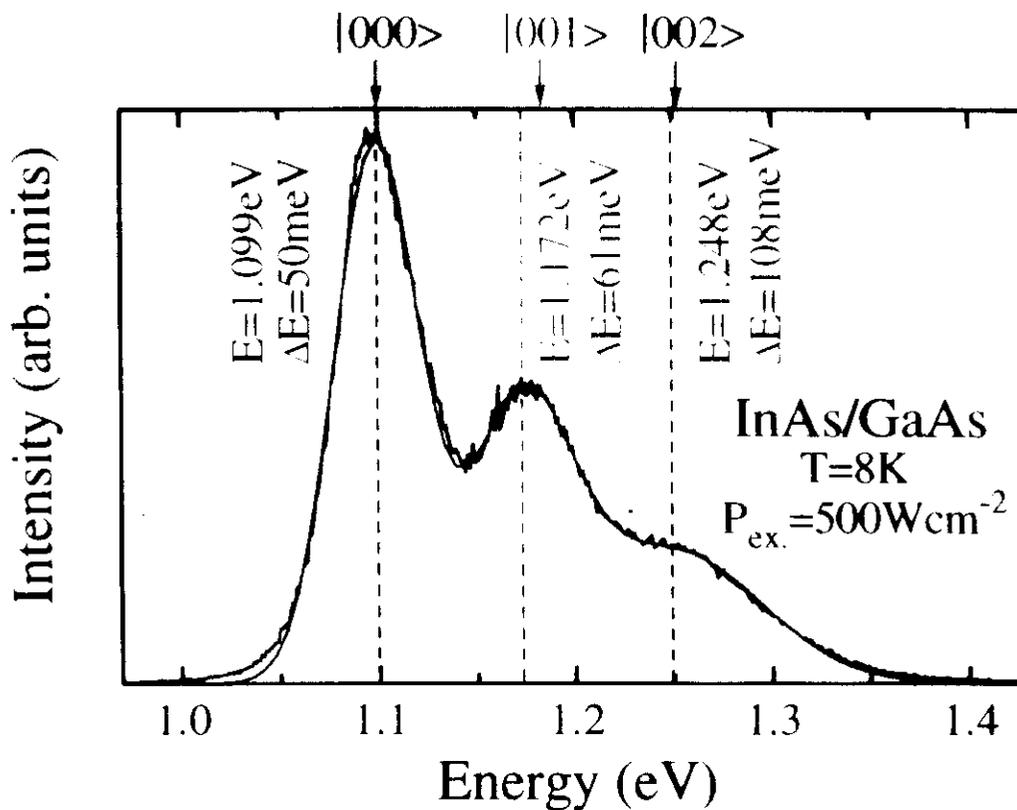
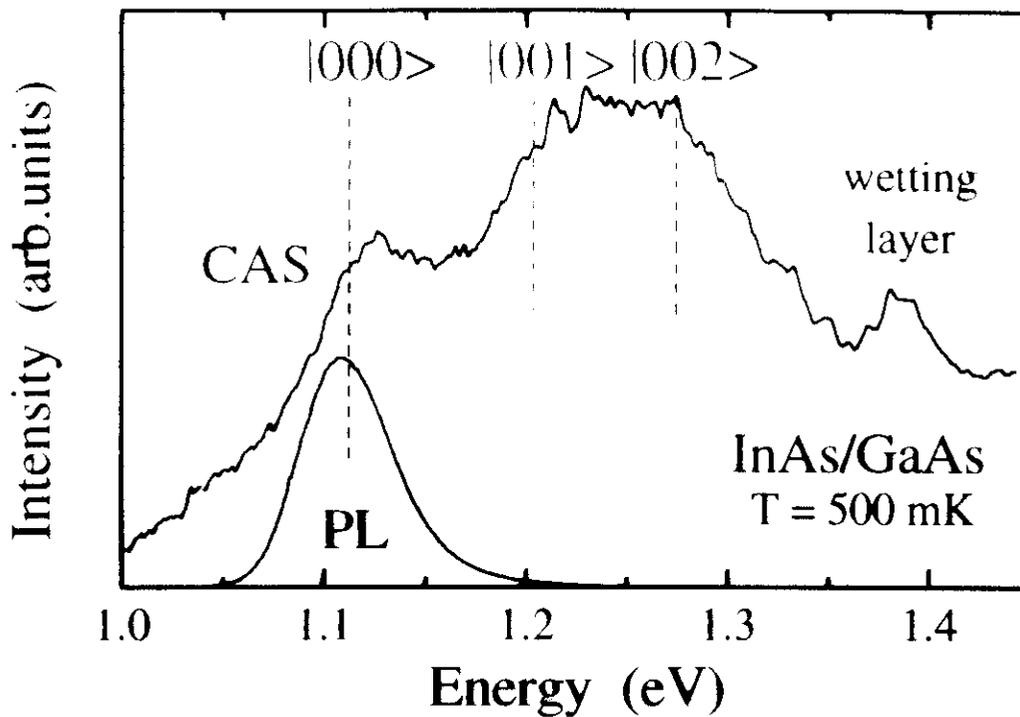
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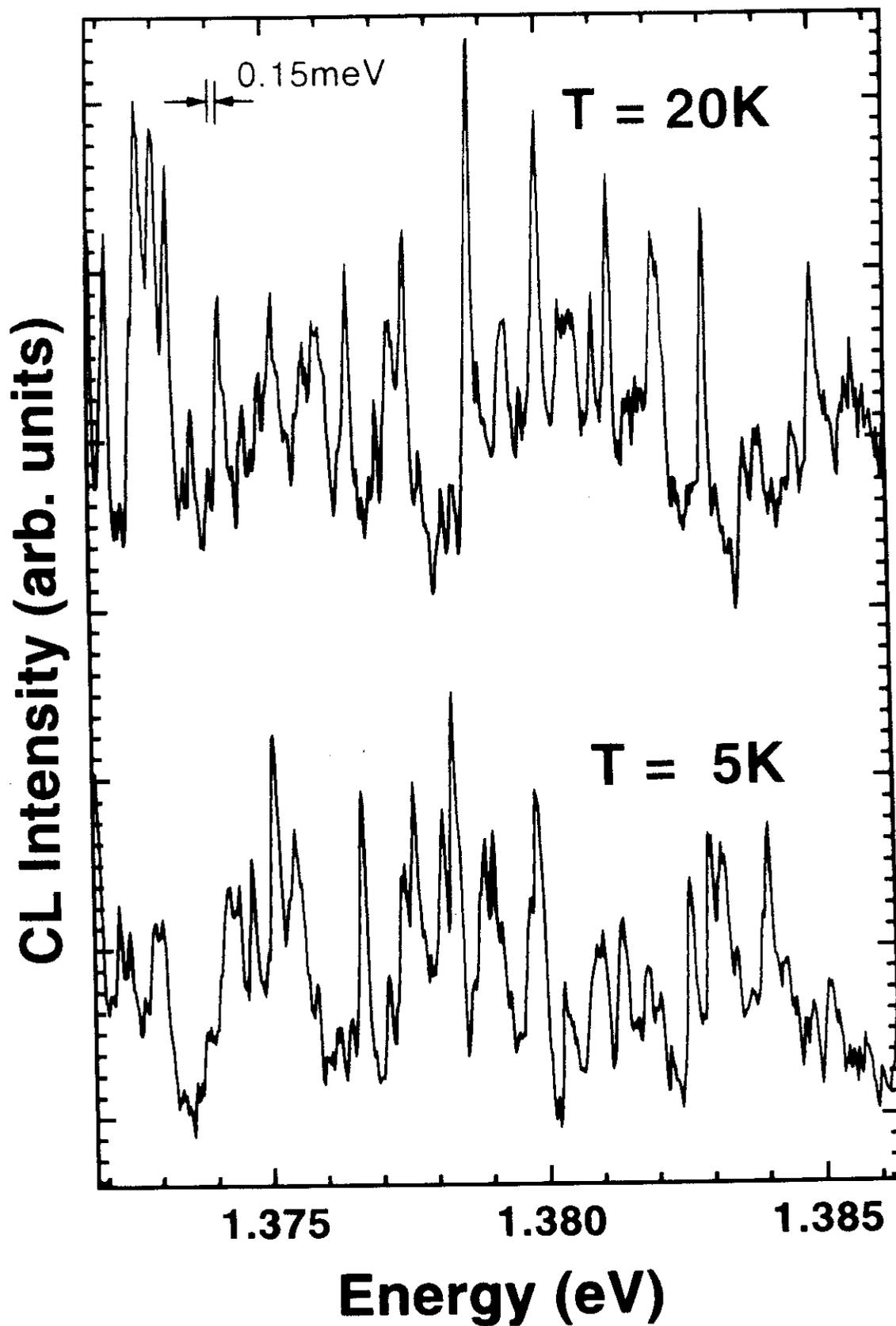
# Quantum Dot Levels as a Function of Size



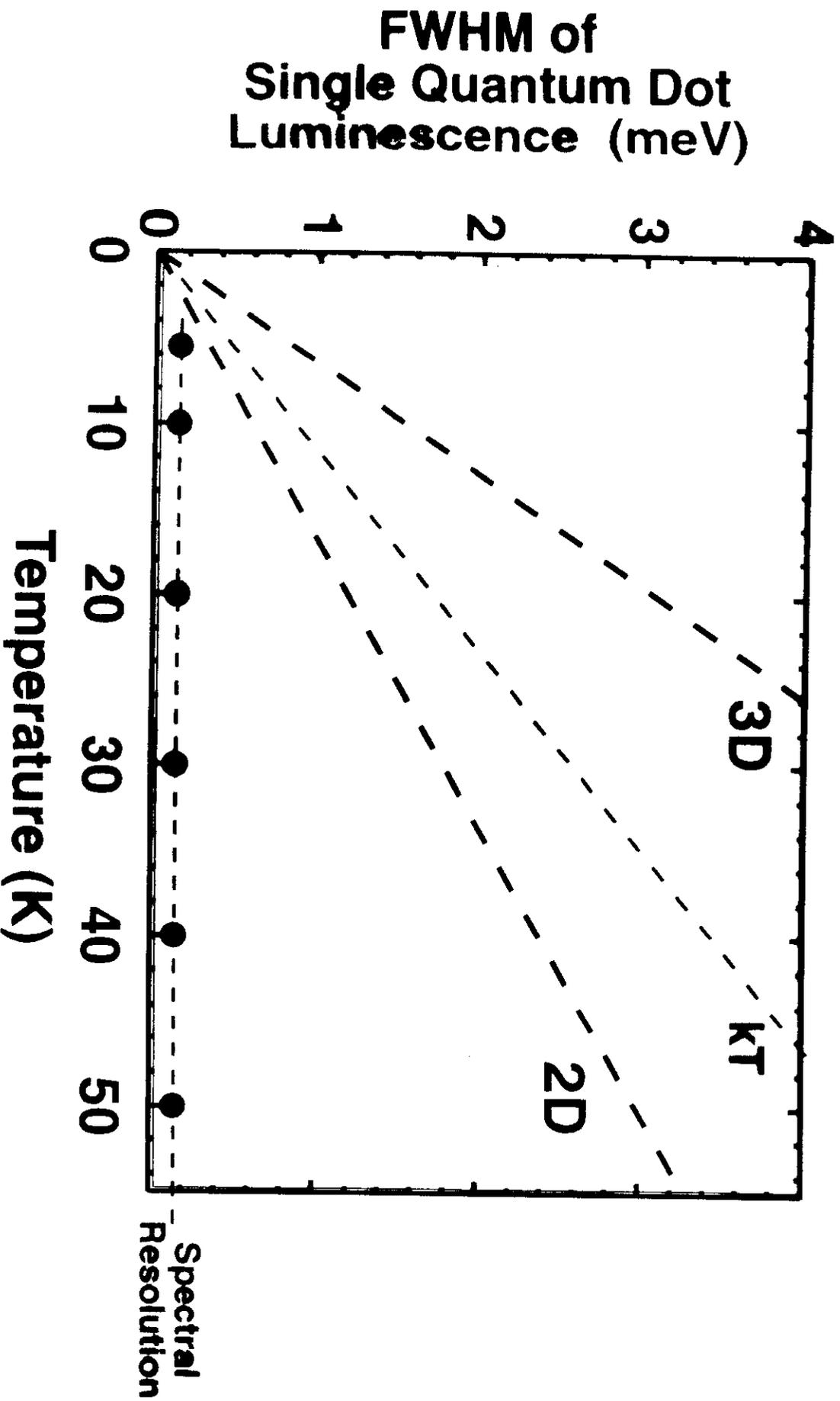
# Excited States of InAs/GaAs Quantum Dots



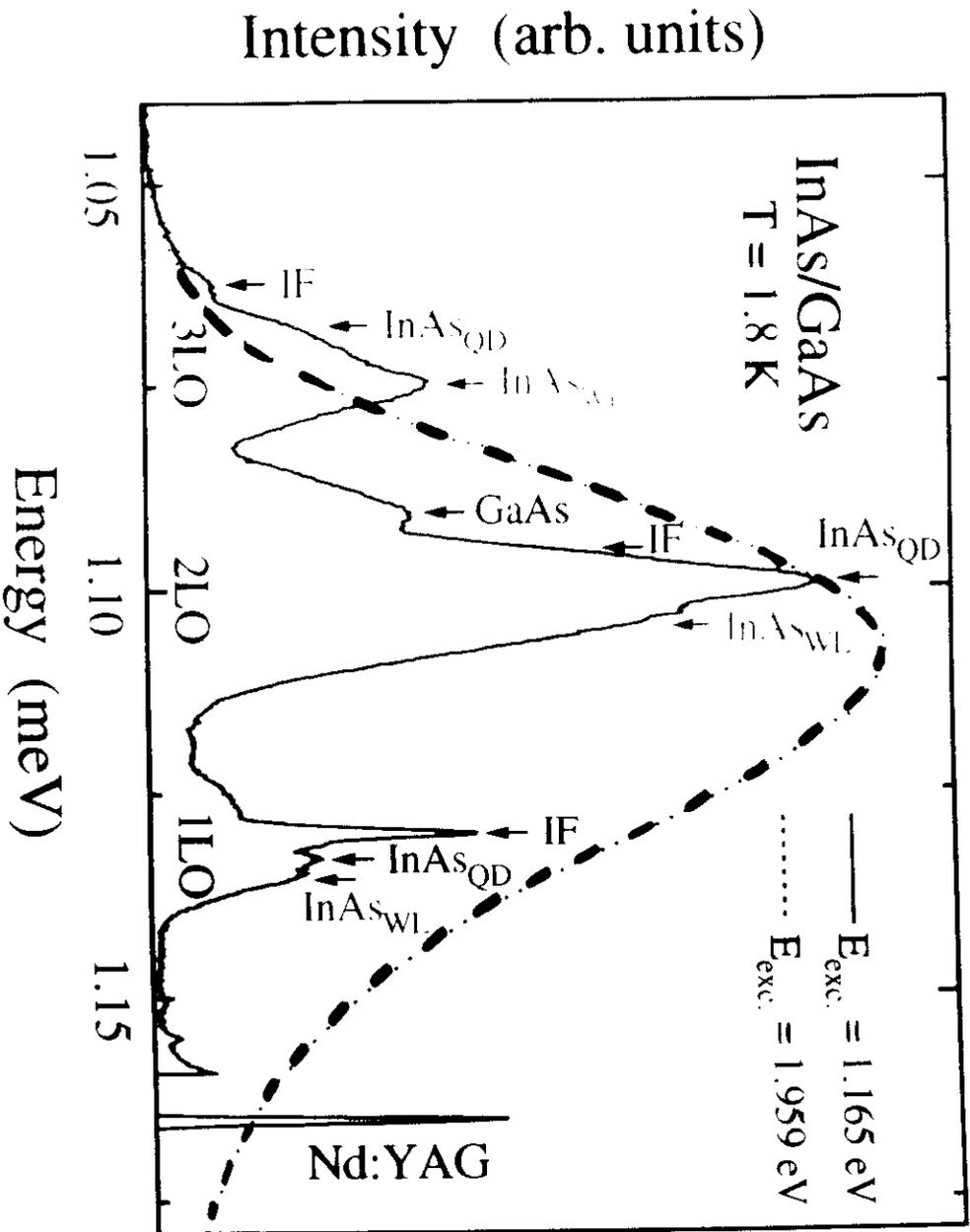
# Spot Focus CL Spectra of InAs/GaAs Dots



# $\delta$ -function-like Density of States



# Selectively Excited Luminescence of InAs/GaAs Dots



—  $E_1$   $\underline{1LO}$   
 —  $E_0$

## Phonon modes:

InAs<sub>WL</sub> = 29.6 meV

InAs<sub>QD</sub> = 31.9 meV

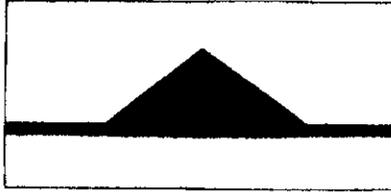
IF = 35.0 meV

GaAs = 36.6 meV

# ***Optical Properties in Quantum Dots***

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**Quantum Dot Phonon**  
 $h\nu_{LO} (\text{InAs}) = 31.9 \text{ meV}$

$\delta$ -function like ( $\Gamma < 0.15 \text{ meV}$ ) ground state  
luminescence is resonant with  $\delta$ -function like absorption.

**NO STOKES SHIFT BETWEEN ABSORPTION AND EMISSION FOR EACH DOT.**

For the same ground state energy there are different energies of excited states for different dots due to shape and strain nonuniformities.

**PLE SPECTRA REPRESENT COMBINATION OF ABSORPTION AND RELAXATION PROCESSES.**

Different LO phonons participate in scattering:  
InAsQD, InAsWL, IF, GaAs.

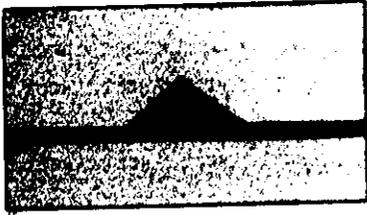
Phonon resonances are broad indicating participation of acoustic phonons.

**EFFICIENT MULTI-PHONON RELAXATION MECHANISM BY PASSES THE PHONON BOTTLENECK EFFECT ( $\tau_{\text{CAPTURE}} < 1 \text{ ps}$ ,  $\tau_{\text{RELAX}} < 40 \text{ ps}$ )**

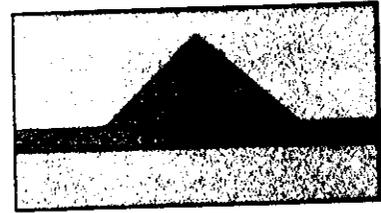
**INCREASED OSCILLATOR STRENGTH AND TUNING OF QD PL AND ABSORPTION PEAKS BY COUPLING OF QDs.**

# Shape Transformation EFFECTS

## Annealing

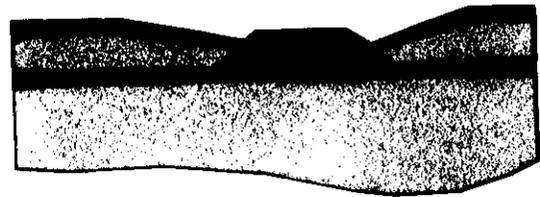
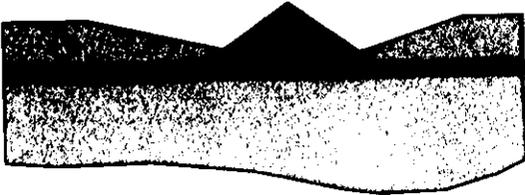


700°C



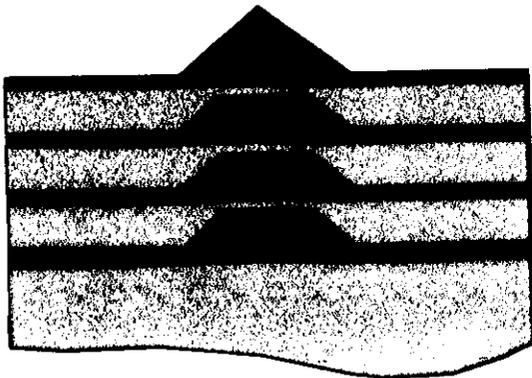
Size increases  
Indium composition decreases  
Pyramid like shape is maintained  
High energy shift of QD luminescence

## Growth Interruption



InAs molecules evaporate  
from pyramids and cover  
free GaAs surface

## Growth of vertical stacks



Formation of  
quantum dot  
superlattice

# Vertically Coupled Quantum Dots

Ledentsov et al. 1995 (Ioffe Inst., TU Berlin, MPI Halle)

Cross section



[001]



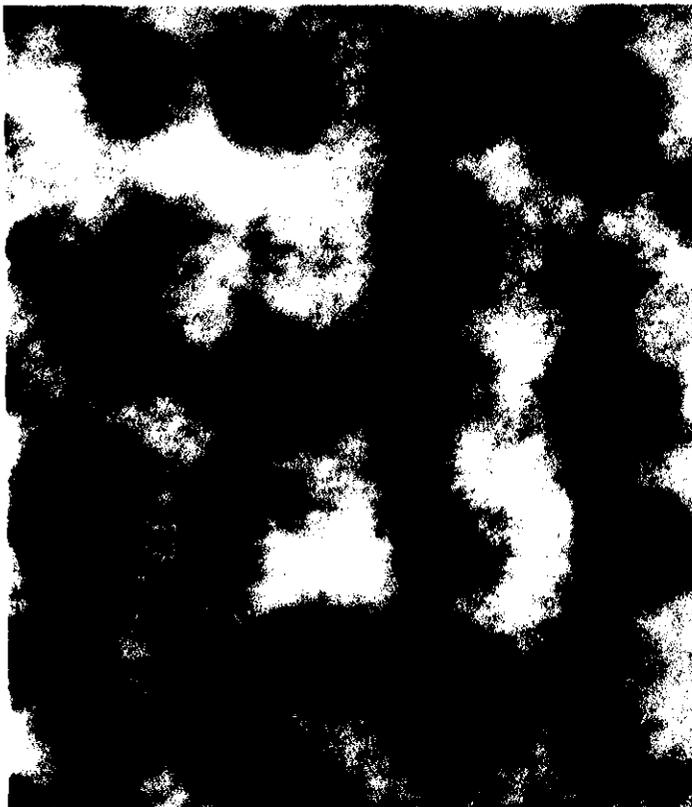
InAs



GaAs



Plan view



Arrangement  
of quantum  
dots in  
3-dimensional  
tetragonal  
lattice

[010]

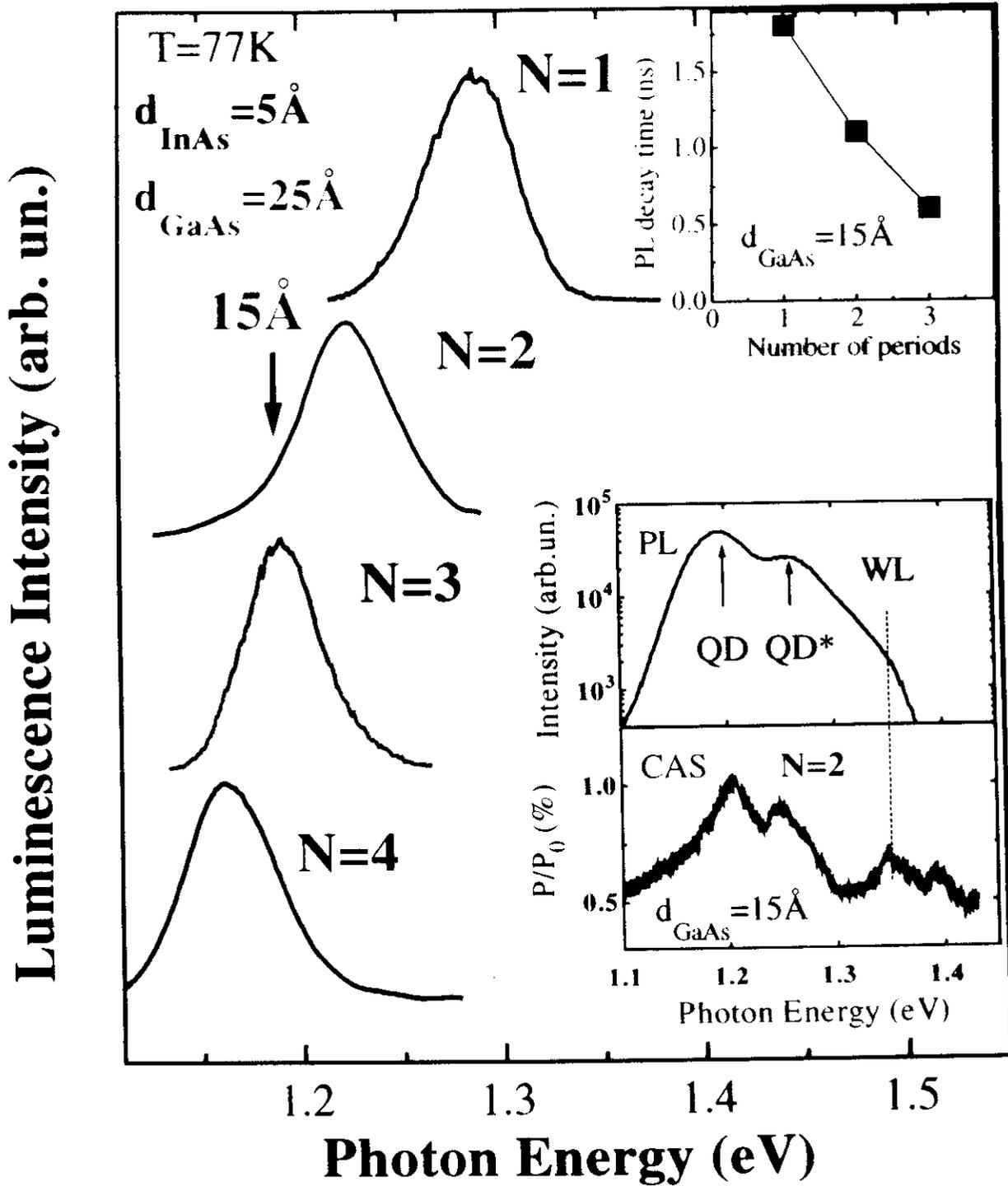


[100]



20 nm

# Electronically Coupled Quantum Dots



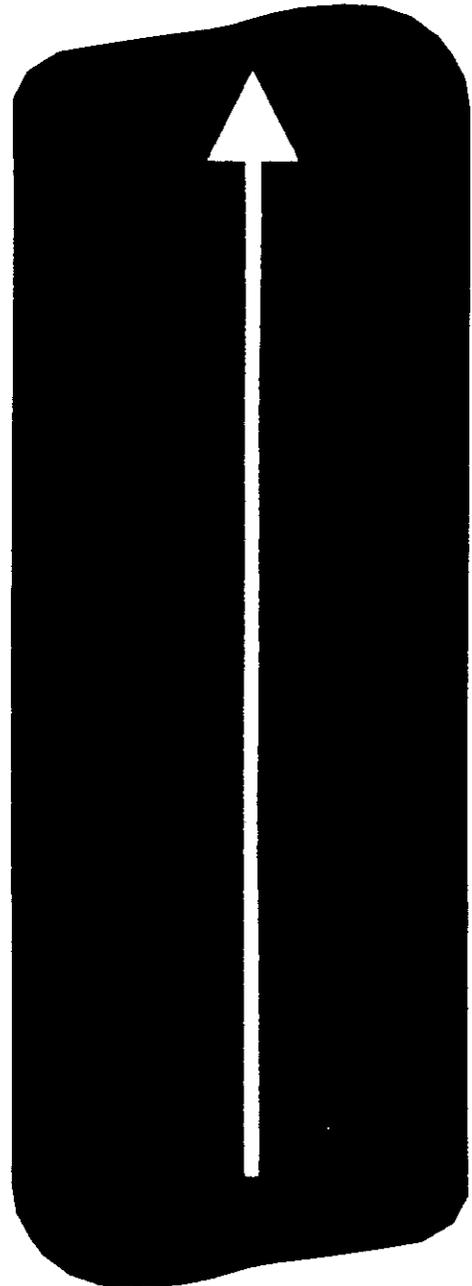
# *Electron Transport in Quantum Dot Superlattices*

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QD SUPERLATTICE

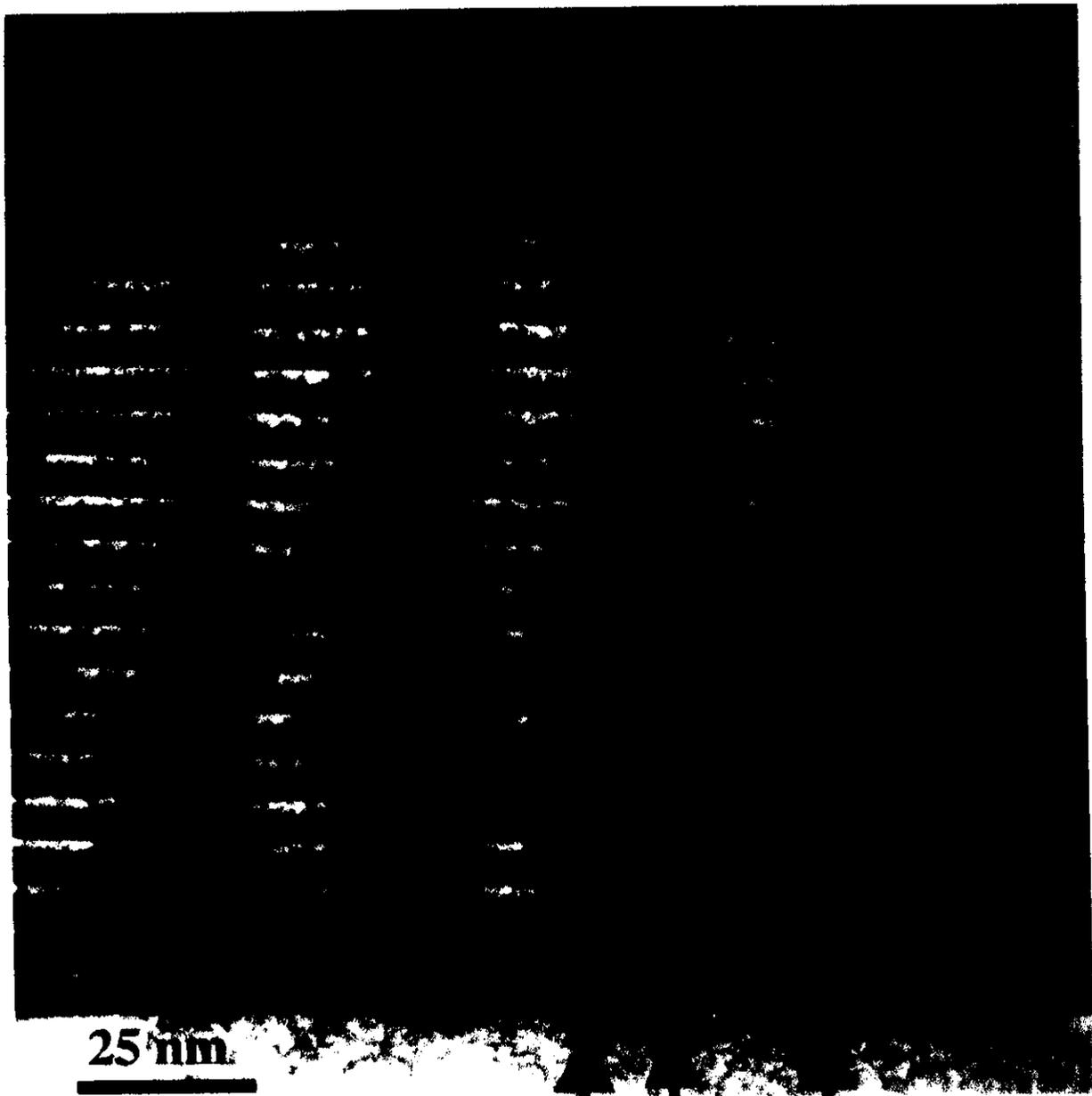
ANTIDOT SUPERLATTICE



# *InGaAs-GaAs Quantum Dot Superlattice*

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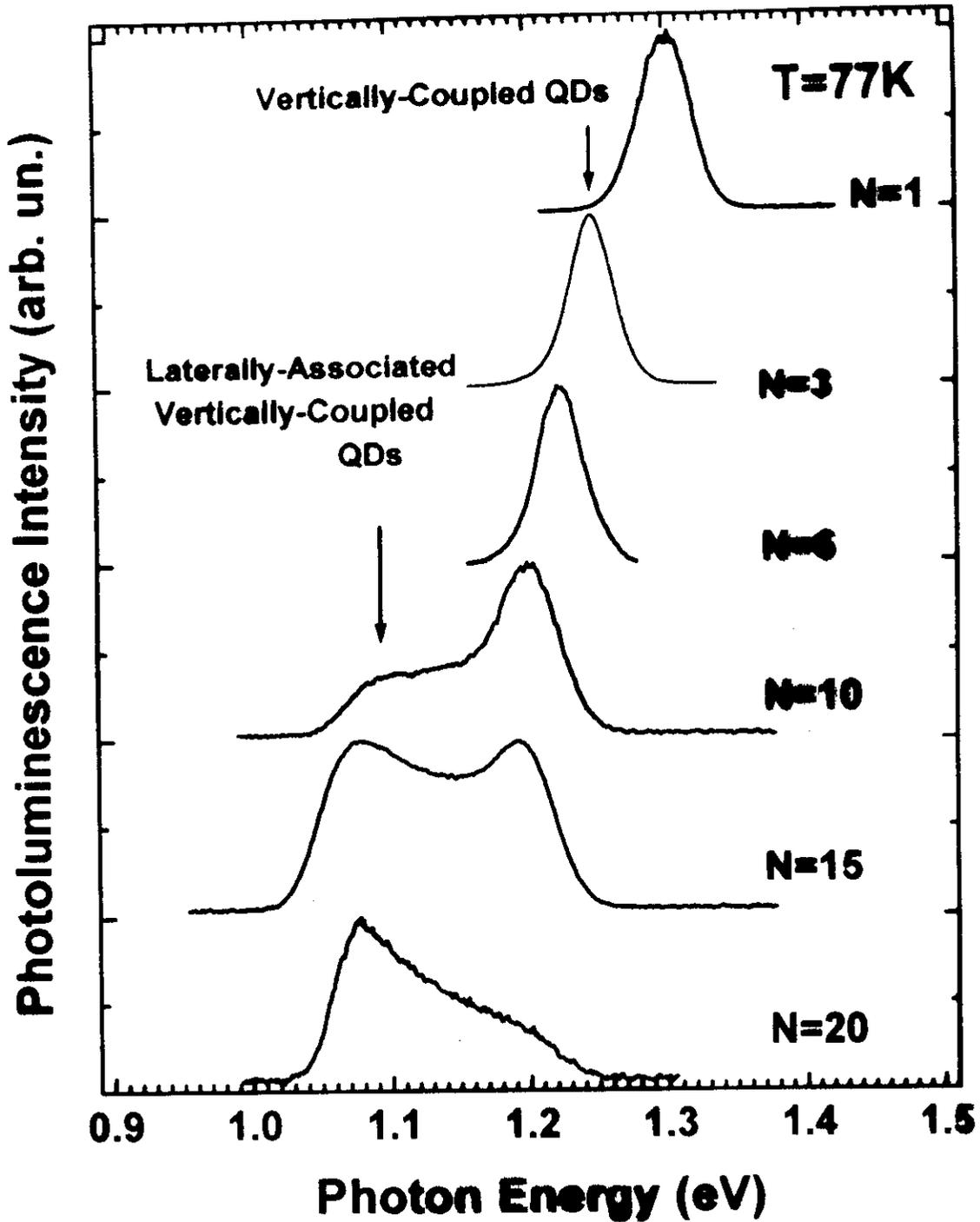
**25 nm**

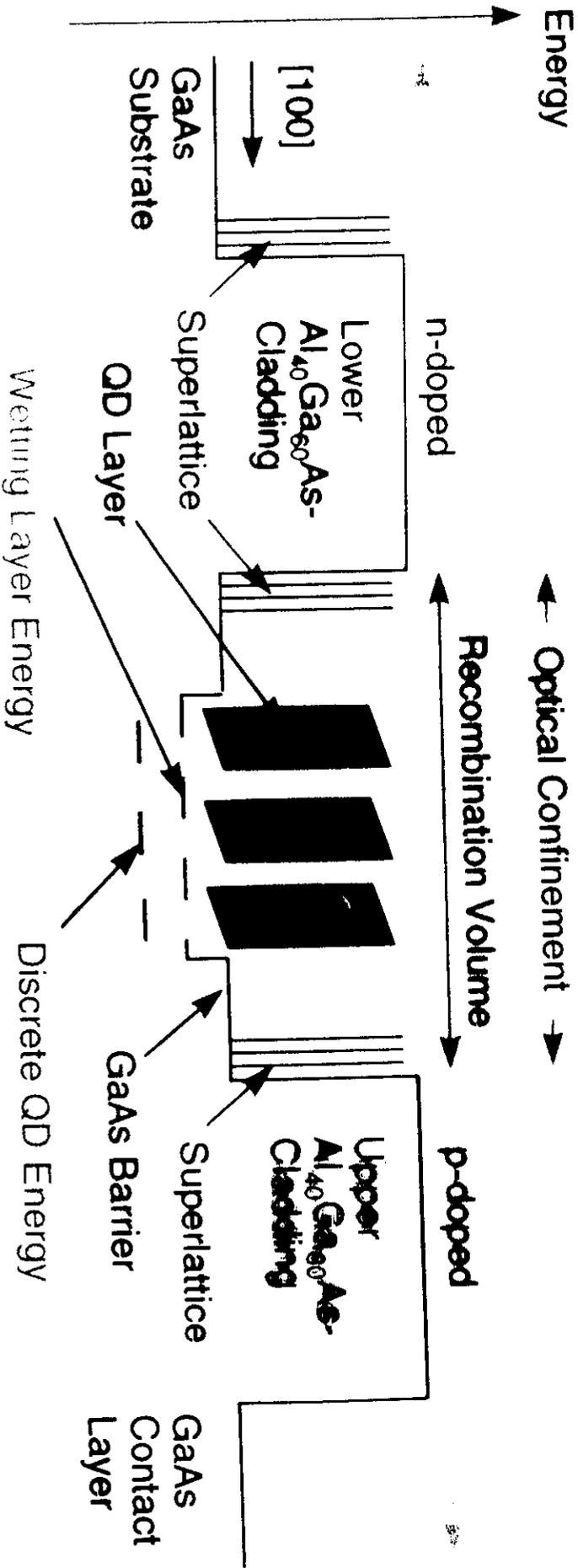
**25x{InGaAs/GaAs}**

**DENSE ARRAY OF COLUMNS**

**CONTINUITY OF COLUMNS THROUGH  
THE STRUCTURE**

# Laterally-Associated Vertically-Coupled Quantum Dots



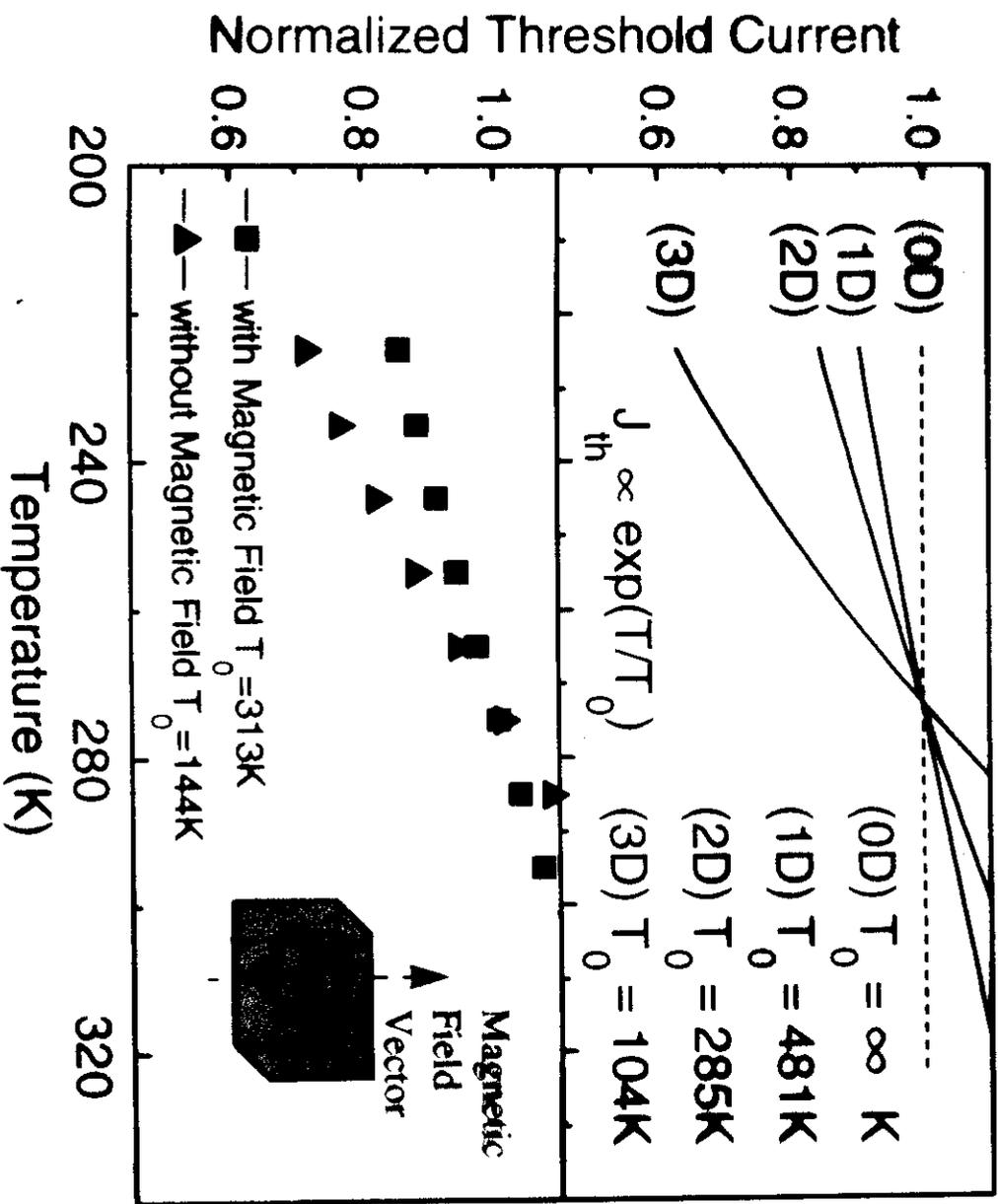




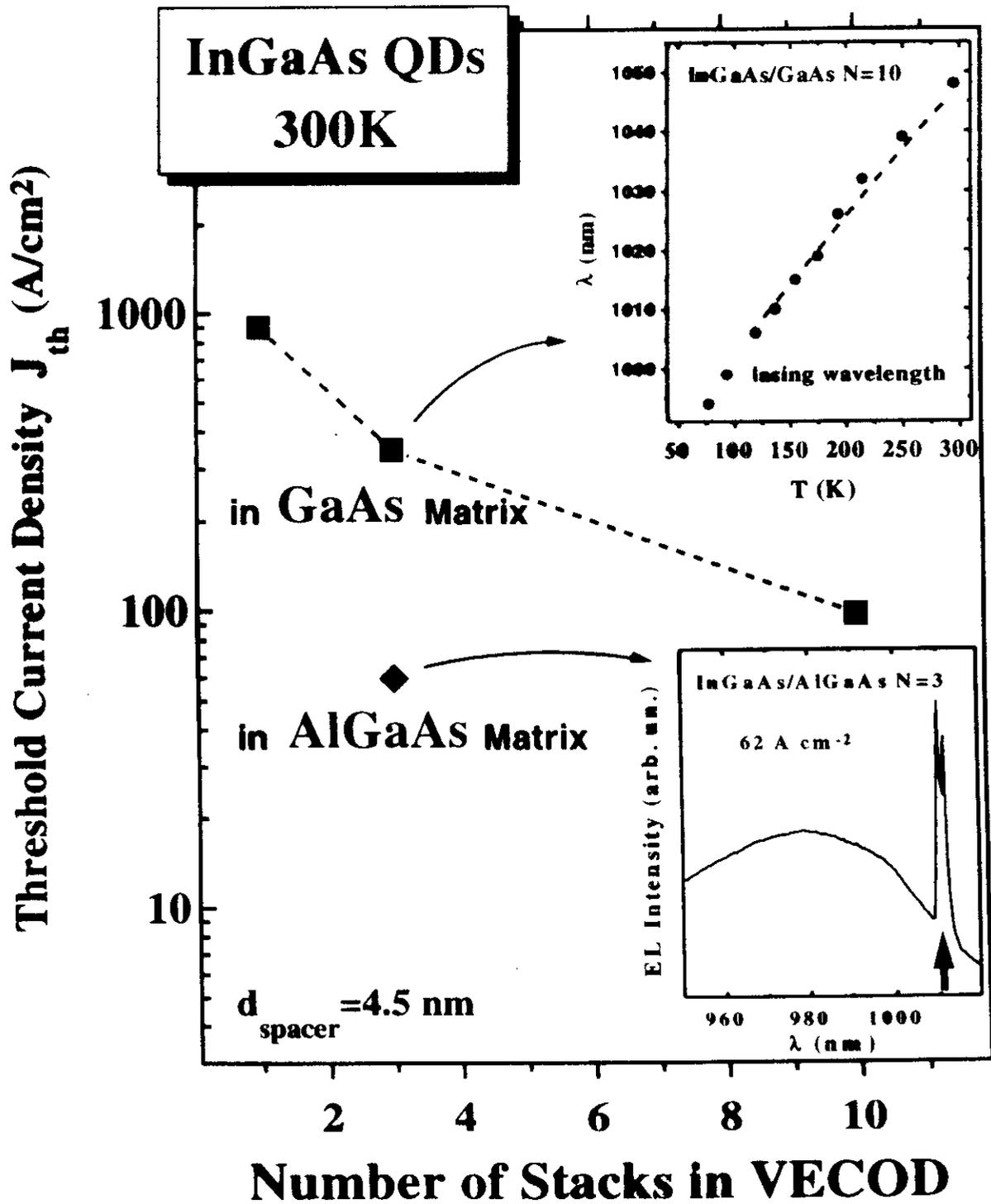
# Prediction

## First Evidence for an Increase of $T_0$ of a Bulk Laser placed in a Magnetic Field

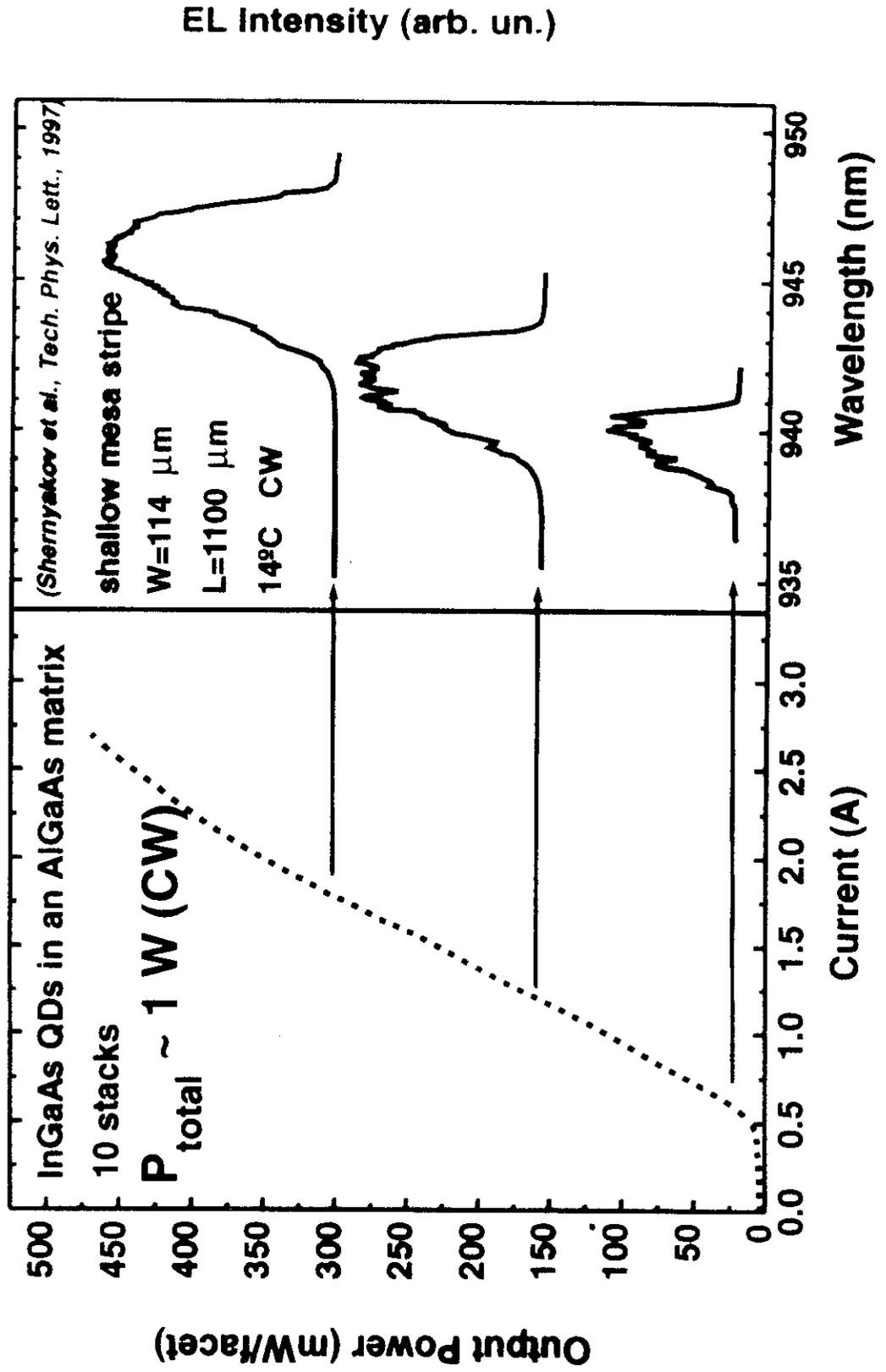
(Arakawa and Sakaki, 1982)



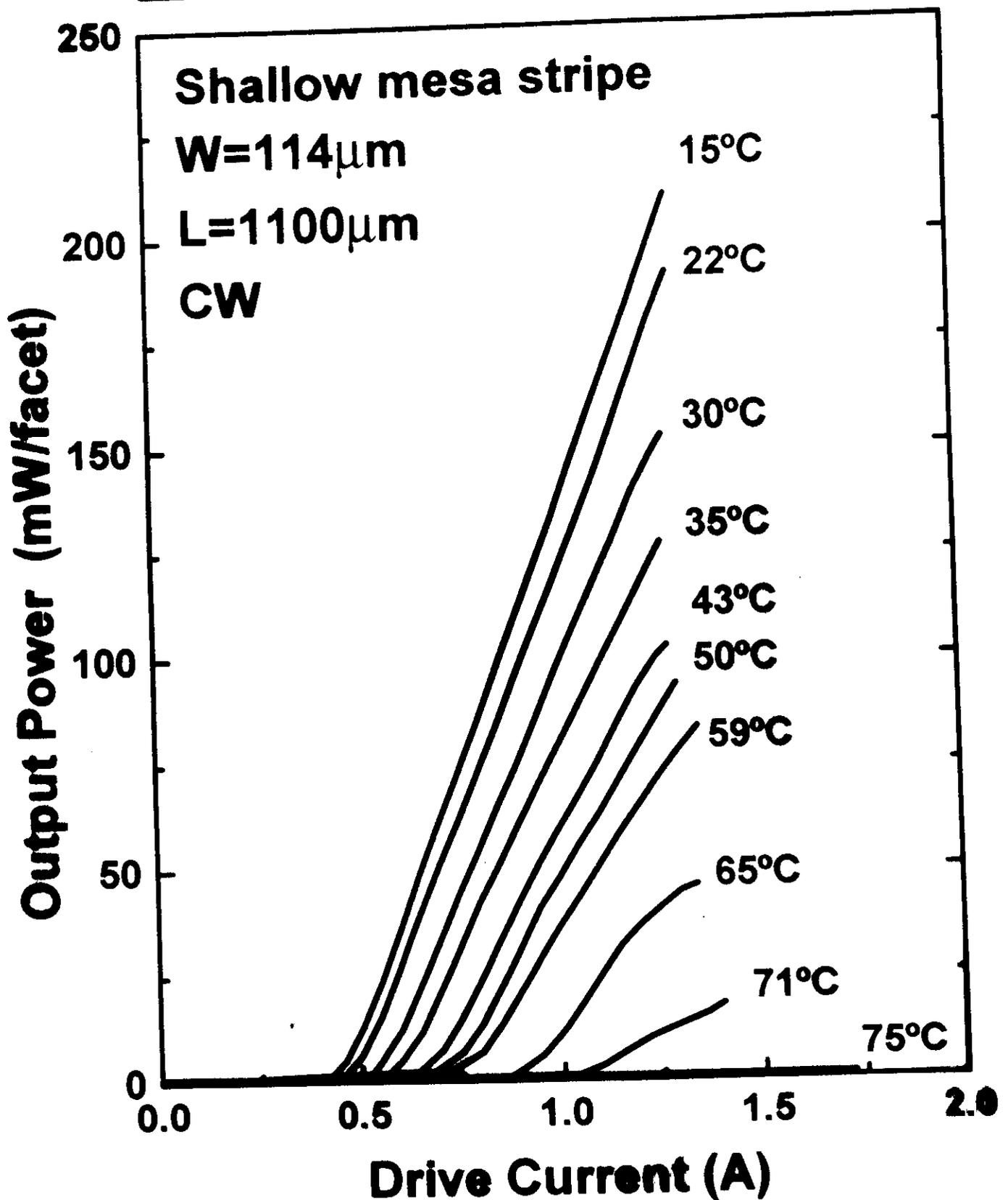
# Lasers Based on Vertically Coupled Quantum Dots



# RT High Power CW Operation of a QD Diode Laser



# High Temperature Operation of a Quantum Dot Laser

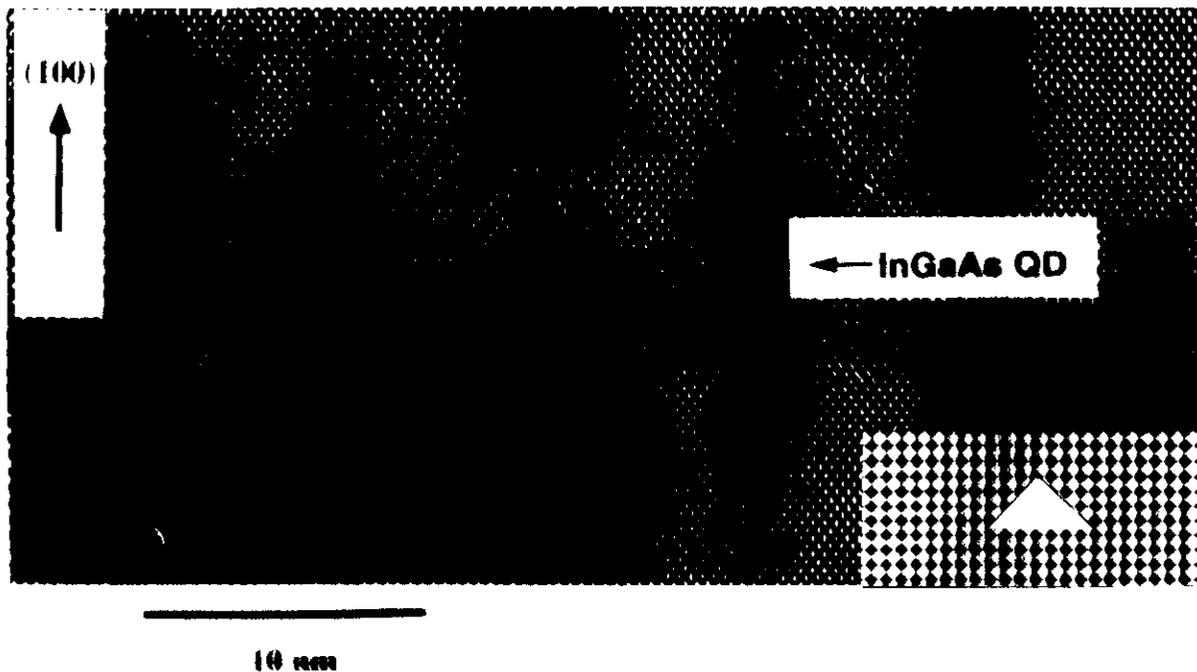


# ***Cross-Section HRTEM Image of MOVPE (In,Ga)As Quantum Dot on GaAs (100)***

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 ***3D Islanding***



- ★ **Pyramidal shape ( 20 nm in base)**
- ★ **Bright PL at 1.36  $\mu\text{m}$  (300 K)**
- ★ **Possibility of Vertical Coupling**

***Ledentsov et al. APL 69, 1095 (1996)***

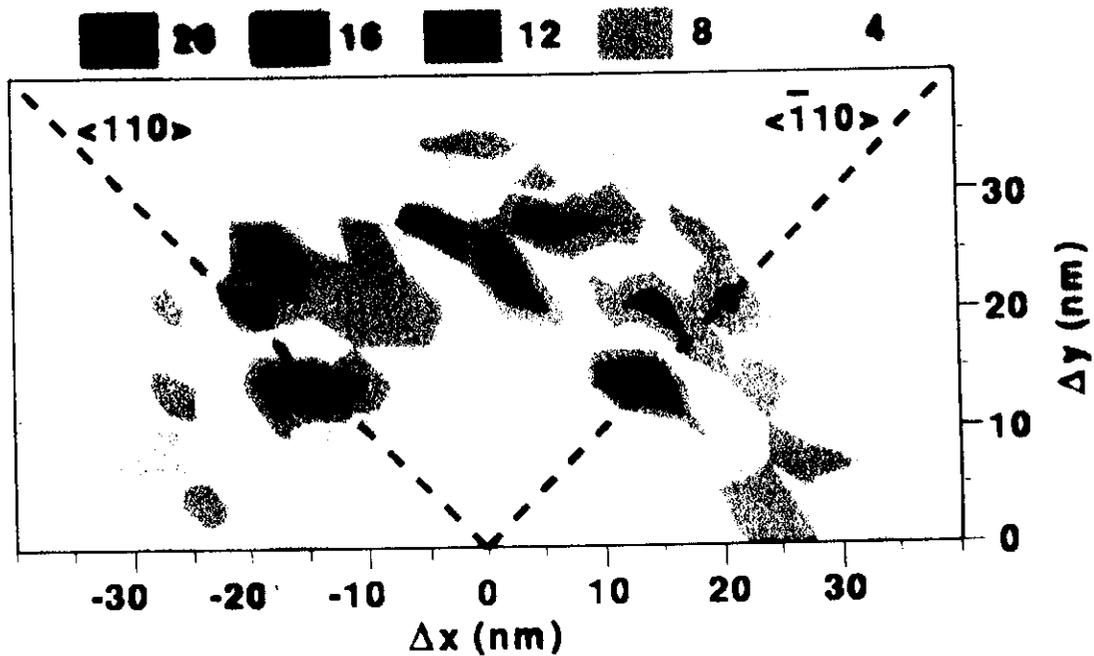
# QD Self Organization in MOCVD



- Chainlike ensemble alignment along  $\langle 110 \rangle$
- (100) oriented square QD base (in larger magnification)



*F. Heinrichsdorff et al.,  
APL 68 (23) 1996*



# MOCVD growth of InAs/GaAs QDs



“Normal”  
growth  
conditions

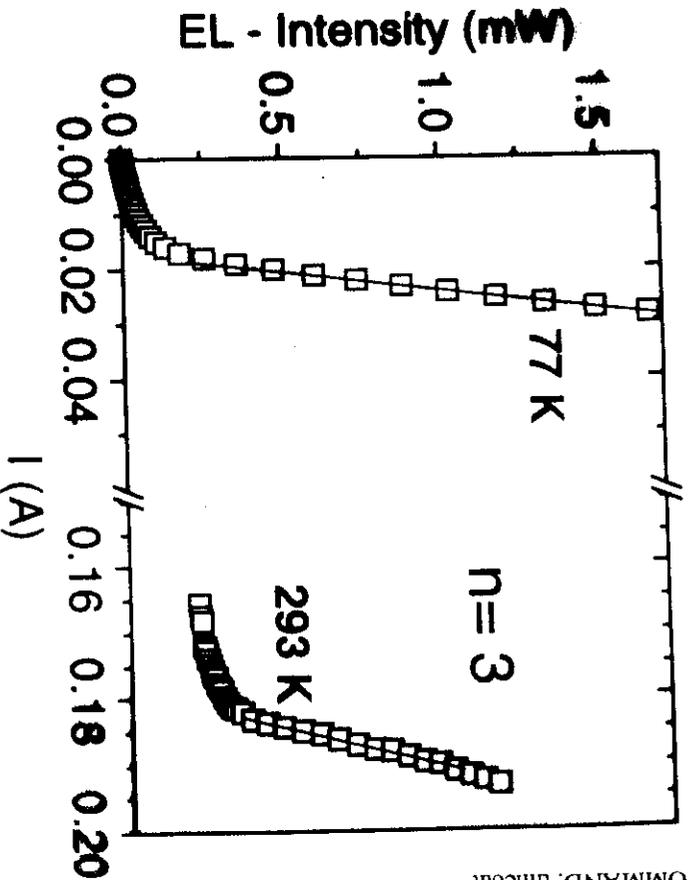
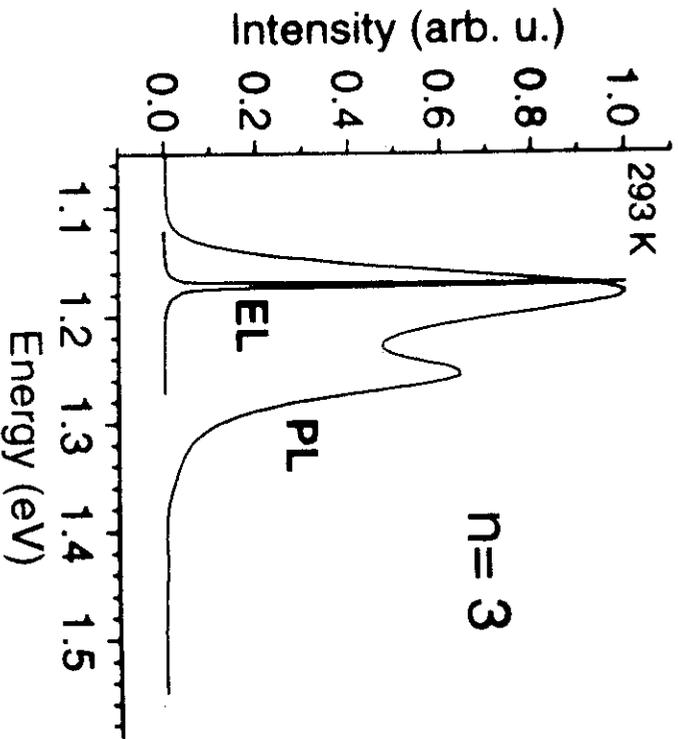


Minimized  
As pressure  
for growth  
and growth  
interruption

- Lateral densities up to  $1.5 \times 10^{11} \text{ cm}^{-2}$
- Coupled and decoupled QD stacks possible

F. Heinrichsdorff et al.,  
*Jpn. J. Appl. Phys.* **36** (1997) in print

# MOCVD InAs/GaAs Quantum Dot Lasers



- Stacked QD laser: Ground state lasing (220 A/cm<sup>2</sup>), cw operation at RT
- Single sheet QD laser: 12.7 A/cm<sup>2</sup> at 100 K (ground state), 181 A/cm<sup>2</sup> at 293 K (excited state)

F. Heinrichsdorff et al.  
*Appl. Phys. Lett.* 71 (27), 1997 in print

ERROR: timeout  
 OFFENDING COMMAND: timeout  
 STACK

# **Quantum Dot Injection Lasers**

## **Room Temperature (300K) Operation**

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### Figures of Merit

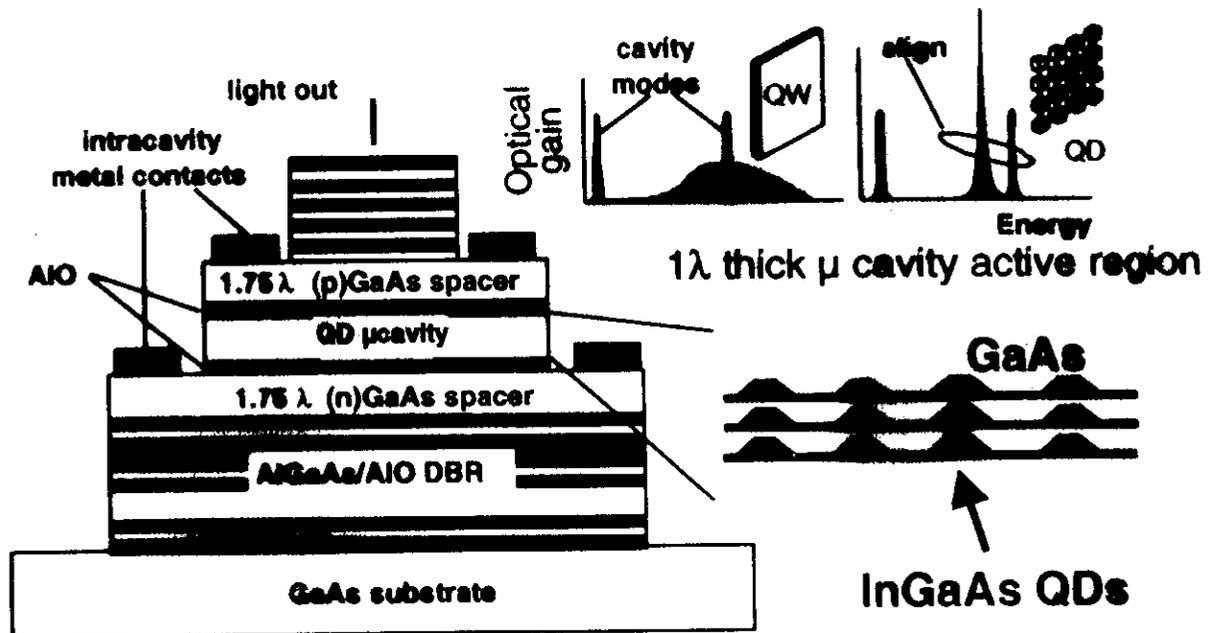
- QD electroluminescence and photoluminescence coincide in energy: Lasing on QD ground state
- High temperature stability ( $T_o=385K$ )
- Low thresholds ( $j_{th}=60A/cm^2$ )
- Differential quantum efficiency up to 70%

### Design Principles

- Stacked sheets of quantum dots,  $N \sim 10$  gain  $\uparrow$
- Increase of barrier height escape rate  $\downarrow$

# Quantum Dots for VCSELs

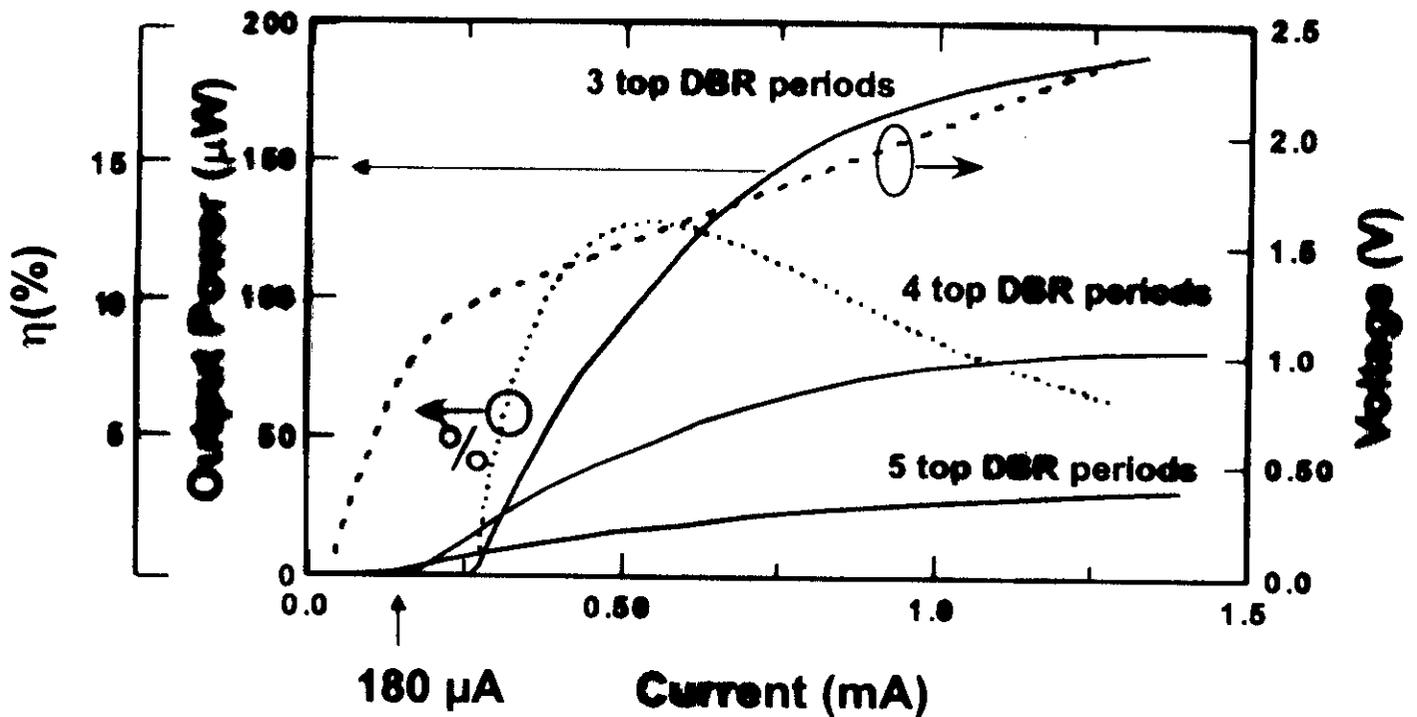
- Basic Advantages of Quantum Dots
- No interface recombination at oxide-defined apertures
- Reduced lateral spreading of carriers out of the aperture region



**Single Quantum Dot Laser at ultralow Threshold Current is possible**

# 3-Fold QD VCSELs at 300 K

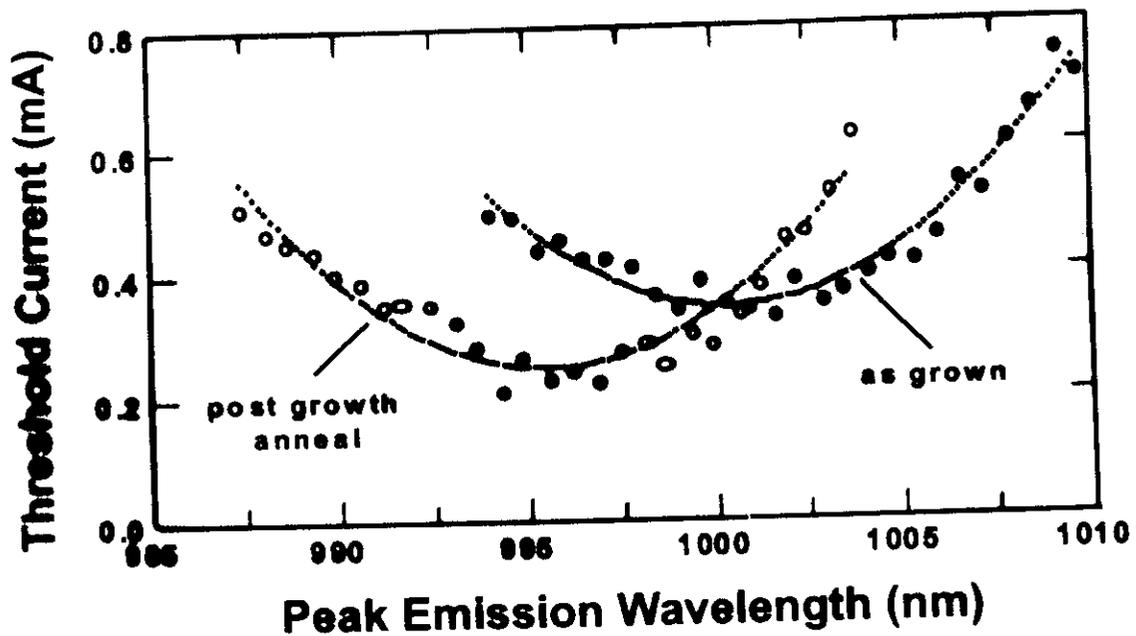
QDs as novel gain medium for oxide-defined aperture VCSELs: threshold,  $I$ - $V$ , light output



Ultralow threshold currents.  
CW output power: 180  $\mu\text{W}$

# Influence of Annealing

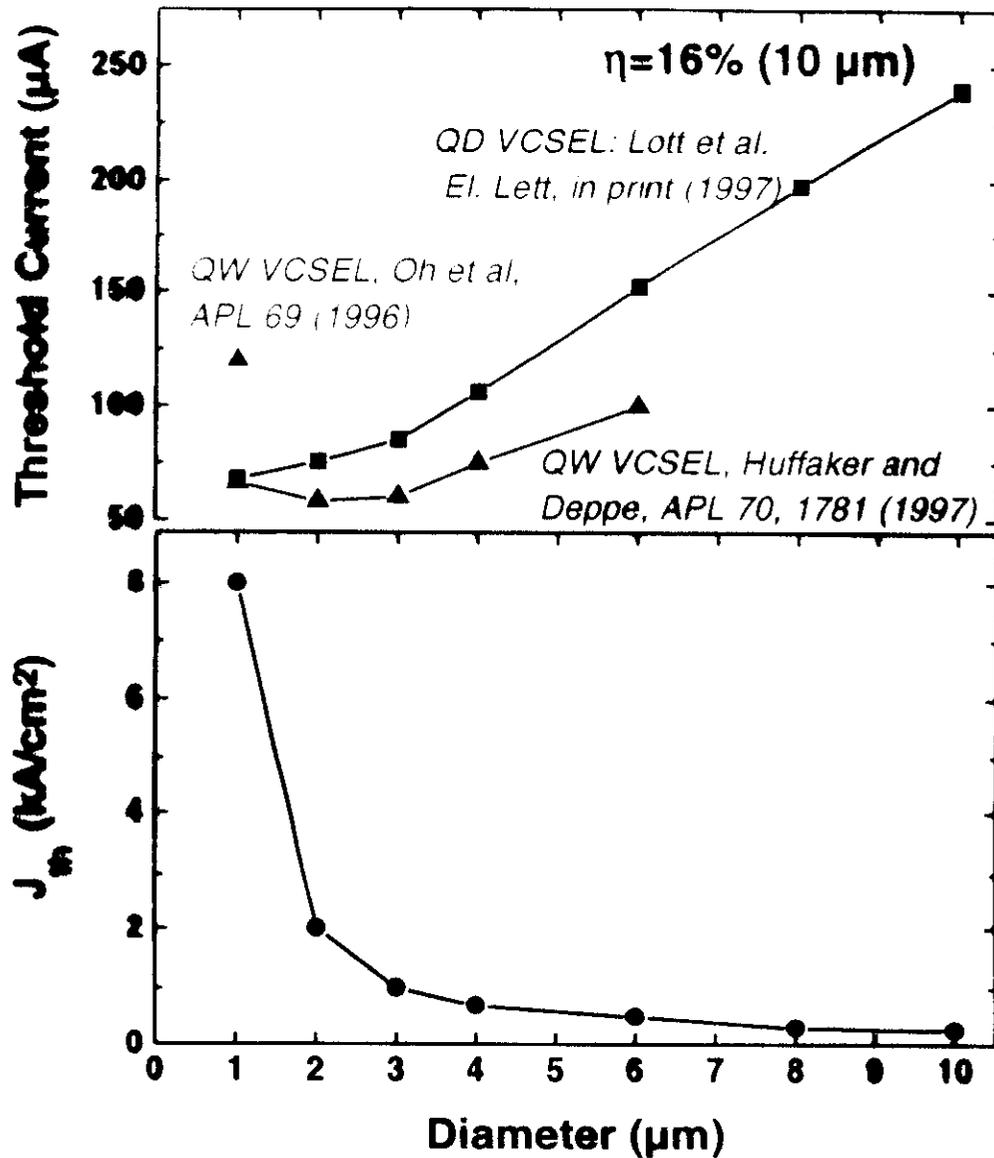
## Tuning of Properties by Post-Growth Processing



**Decrease in threshold current.  
Shorter wavelengths.**

# QD VCSEL:

## Ultrasmall Threshold Currents



**68  $\mu\text{A}$  for 1  $\mu\text{m}$  aperture  
fits to the best QW VCSEL values**

# **Future Trends**

## **Lasers:**

Ultralow threshold current density ( $\sim 10 \text{ A cm}^{-2}$ )  
for reasonable QD size dispersion (10%)  
(Theory: L. Asryan, R. Suris, 1995)

Ultrahigh temperature stability.  
Ultrahigh material gain. Ultrahigh differential gain.

No transport of nonequilibrium carriers:  
reduced surface recombination,  
no overheating of facets, high power lasers,  
lasers in highly dislocated or type-II matrices  
(e.g. InAs QDs in Silicon).

1.3  $\mu\text{m}$  and 1.5  $\mu\text{m}$  wavelength range using GaAs substrates.

QD lasers will replace QW lasers for most  
of the applications.

## **Infrared Detectors:**

Lifting of the  $k$ -selection rule for infrared light.  
No need in surface gratings.

## **Microelectronics:**

Quantum Dot Cellular Automata. Memory Devices.

...

# **Conclusions:**

around 4 years passed since the first report on lasing in self-organized QDs  
Ledentsov et al. *Semiconductors* 28, 832 (1994),  
submitted December 29, 1993

- **QDs and VCQDs Can Be Used in a New Generation of Devices**
- **VCQDs Allow Realization of High Quality Lasers**

## **InGaAs-AlGaAs VCQD Edge-Emitting Lasers:**

- **- Low Threshold Current Density  
(60 A/cm<sup>2</sup>, 300K)**
- **- High Quantum Efficiency (>90%)**
- **- High Differential Efficiency (70%)**

**COMPARABLE WITH THE BEST VALUES FOR  
EDGE EMITTING QW LASERS**

## **InGaAs-GaAs VCQD Vertical Cavity Lasers:**

- **- Low Threshold Current Densities  
(170 A/cm<sup>2</sup>, 300 K)**
- **- Low Total Currents (<70 μA)**

**FITS TO THE BEST VALUES FOR QW  
VERTICAL CAVITY LASERS**

**NEXT STEP: TO OVERCOME BEST QW LASERS**

