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INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS

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WORKING PARTY

ON

"PHYSICS OF CONDENSED MATTER AT PLANETARY PRESSURES"

(20 August - 7 September 1984)

SOLID STATE CREEP

(Part II)

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These are preliminary lecture notes, intended only for distribution to participants.
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DEFECT CHEMISTRY AND CREEP

Defect concentration within neutrality range

$$2[V_O^{\bullet\bullet}] \approx n \quad \text{for pure quartz}$$

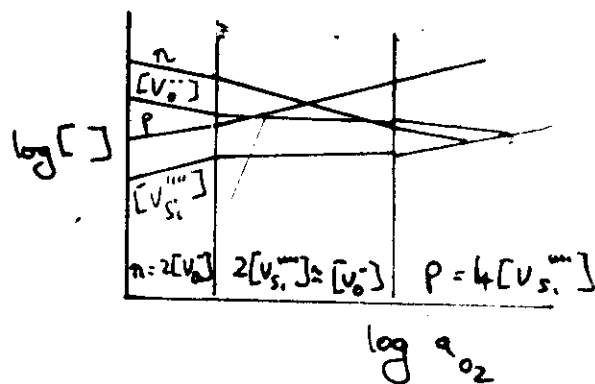
dominance of charged oxygen vacancies in controlling charge on crystal is balanced by free electrons.

Thus, for example

$$n(\text{free electrons}) = 2^{1/3} K_{Si}^{1/6} K_O^{1/3} K_{SiO_2}^{1/6} a_{SiO_2}^{1/6} a_{O_2}^{-1/6}$$

$$[V_O^{\bullet\bullet}] = 2^{-1/3} K_{Si}^{1/6} K_O^{1/3} K_{SiO_2}^{1/6} a_{SiO_2}^{1/6} a_{O_2}^{-1/6}$$

Can construct diagrams:-



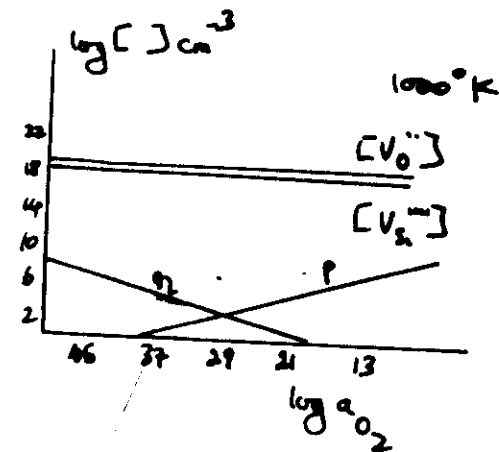
$\log a_{O_2}$

DEFECT CHEMISTRY AND CREEP

Realistic scale can be added to defect diagram for pure quartz

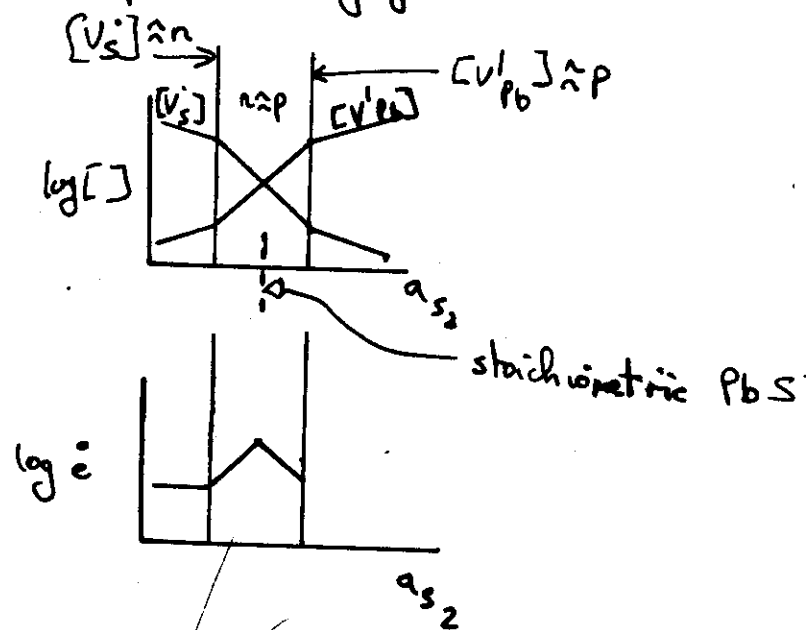
By following way in which a_{O_2} change effect properties believed to be dependent on defect concentration eg creep rates
We can estimate which defects are important.

Pure quartz



DEFECT CHEMISTRY AND CREEP

1. At low sulphur activities, creep controlled by neutral species, eg $(V'_{Pb} V'_S)$ whose concentration is independent of a_{S_2} .
2. At higher activities V'_{Pb} and V'_S control creep rate.
3. Impurities, such as Bi or Ag, act to increase or decrease $[]$ of rate controlling defects and hence their influence can be gauged.



GENERAL CONCLUSIONS ON POINT DEFECTS

1. Under reducing conditions hydrogen incorporated interstitially in most silicates.
2. Under oxidizing conditions, main hydrogen defect seems to be 'hydrogarnet' defect.
 $(SiO_4)^{4-}$ replaced by $(H_3O_4)^{5-}$
3. Analysis of defect structure of 'dry' quartz where Al substitutes for silicon and is charge compensated by interstitial alkalis indicates a strong dependence of defect conc on f_{O_2} . Natural, impure, 'dry' quartz should thus have creep rate dependent on f_{O_2} .

However, Rate at which dry quartz equilibrates with dry oxygen atmosphere is so slow that the influence of f_{O_2} changes would never be observed.

4. Introduction of 'hydrogarnet' defect in large concentrations leads to strong dependence of defect conc. on f_{O_2} and f_{H_2O} but in opposite senses.

The strong dependence on f_{H_2O} is enough to explain hydrolytic weakening effect but f_{O_2} is also worth considering in view of small changes in f_{H_2O} that can be expected in lab + in nature.

FORSTERITE OLIVINE

TABLE 3. Dependence of Charged Defect Concentrations Upon Activities of Chemical Components for $[(\text{Fe})_{\text{Fe}}] = [\text{Mg}]$

Defect	a_{Fe}	f_{O_2}	$f_{\text{H}_2\text{O}}$
$\text{V}^{\bullet\bullet}$	-1	- $\frac{1}{2}$	0
$\text{O}_2^{\bullet\bullet}$	+1	0	- $\frac{1}{2}$
$\text{Fe}_2^{\bullet\bullet}$	+2	0	-1
$\text{Fe}_2^{\bullet\bullet\bullet}$	-2	- $\frac{1}{2}$	0
Fe^{\bullet}	- $\frac{1}{2}$	- $\frac{1}{4}$	0
Fe^{\bullet}	0	0	- $\frac{1}{2}$
Fe_2^{\bullet}	-1	- $\frac{1}{2}$	0
$(\text{Fe})_{\text{Fe}}^{\bullet}$	0	- $\frac{1}{2}$	0

TABLE 4. Dependence of Charged Defect Concentrations Upon Activities of Chemical Components for $[\text{Fe}] = [\text{Al}]_{\text{Fe}}$ in Quartz

Defect	a_{Al}	f_{O_2}	$f_{\text{H}_2\text{O}}$
$\text{V}^{\bullet\bullet}$	0	0	-1
$\text{O}_2^{\bullet\bullet}$	-1	- $\frac{1}{2}$	0
$\text{Al}_2^{\bullet\bullet}$	+2	0	-1
$\text{Al}_2^{\bullet\bullet\bullet}$	-2	- $\frac{1}{2}$	0
Al^{\bullet}	-1	- $\frac{1}{4}$	0
Al^{\bullet}	0	0	- $\frac{1}{2}$
Al_2^{\bullet}	-1	- $\frac{1}{2}$	0
$(\text{Al})_{\text{Fe}}^{\bullet}$	0	- $\frac{1}{2}$	0

TABLE 5. Defect Chemistry of Forsterite, Incorporating Hydrogen and the "Hydrogarnet" Defect

Reaction	Equilibrium Constant	Law of Mass Action
Incorporation of Hydrogen Interstitials		
$\text{H}_2 = 2\text{H}_i^{\bullet}$	K_1	$[\text{H}_2] = K_1 [\text{H}_i^{\bullet}]^2$
Ionization of Hydrogen Interstitials		
$\text{H}_i^{\bullet} = \text{H}_i^{\bullet} + \text{e}^-$	K_2	$[\text{H}_i^{\bullet}] = K_2 [\text{H}_i^{\bullet}] [\text{e}^-]$
Incorporation of the Hydrogarnet Defect		
$\text{H}_2 = 2(\text{H})_{\text{Fe}} + \text{O}_2 + \text{H}_2\text{O}$	K_3	$[\text{H}_2] = K_3 [\text{H}_2\text{O}] [\text{O}_2] [\text{H}]_{\text{Fe}}^2$
Ionization of the Hydrogarnet Defect		
$(\text{H})_{\text{Fe}} = (\text{H})_{\text{Fe}} + \text{e}^-$	K_4	$[(\text{H})_{\text{Fe}}] = K_4 [\text{H}]_{\text{Fe}} [\text{e}^-]$

TABLE 6. Defect Chemistry of Forsterite for the Homogeneity Field $[(\text{Fe})_{\text{Fe}}] = [\text{Mg}]$

Defect	f_{O_2}	$f_{\text{H}_2\text{O}}$	f_{Fe}
$\text{V}^{\bullet\bullet}$	0	-1	0
$\text{O}_2^{\bullet\bullet}$	0	0	0
$\text{Fe}_2^{\bullet\bullet}$	0	-1	0
$\text{Fe}_2^{\bullet\bullet\bullet}$	0	0	0
Fe^{\bullet}	0	- $\frac{1}{2}$	0
Fe^{\bullet}	0	0	- $\frac{1}{2}$
Fe_2^{\bullet}	0	- $\frac{1}{2}$	0
$(\text{Fe})_{\text{Fe}}^{\bullet}$	0	- $\frac{1}{2}$	0

TABLE 7. Defect Chemistry of Forsterite for the Homogeneity Field $[\text{Fe}] = [\text{Al}]_{\text{Fe}}$

Defect	f_{O_2}	$f_{\text{H}_2\text{O}}$	f_{Fe}
$\text{V}^{\bullet\bullet}$	0	-1	0
$\text{O}_2^{\bullet\bullet}$	0	0	0
$\text{Al}_2^{\bullet\bullet}$	0	-1	0
$\text{Al}_2^{\bullet\bullet\bullet}$	0	0	0
Al^{\bullet}	0	- $\frac{1}{2}$	0
Al^{\bullet}	0	0	- $\frac{1}{2}$
Al_2^{\bullet}	0	- $\frac{1}{2}$	0
$(\text{Al})_{\text{Fe}}^{\bullet}$	0	- $\frac{1}{2}$	0

Dependence of defect concentrations upon activities of chemical components for the homogeneity field $[\text{Fe}] = [\text{Al}]_{\text{Fe}}$

Albite Feldspar

4504

Table: Point Defect Chemistry in a Hydrothermal Environment

Table 1. Point Defect Chemistry of Albite

Defect	Equilibrium Constant	Law of Mass Action
Interpenetration of cations	K_1	$[Na^+][H_2O] = K_1 [NaOH]$
Interpenetration of anions	K_2	$[OH^-][H_2O] = K_2 [H_2O]$
Interpenetration of cations	K_3	$[Na^+][H_2O] = K_3 [NaOH]$
Interpenetration of anions	K_4	$[OH^-][H_2O] = K_4 [H_2O]$
Interpenetration of cations	K_5	$[Na^+][H_2O] = K_5 [NaOH]$
Interpenetration of anions	K_6	$[OH^-][H_2O] = K_6 [H_2O]$

Table 2. Concentrations of Point Defects in Albite

Defect	Na^+	H_2O	OH^-	$NaOH$
1	1	1	1	1
2	1	1	1	1
3	1	1	1	1
4	1	1	1	1
5	1	1	1	1
6	1	1	1	1

Table 3. Concentrations of Charged Defects in Albite for the Reactivity Range $10^{-10} < [H_2O] < 10^{-1}$

Defect	Na^+	H_2O	OH^-	$NaOH$
1	1	1	1	1
2	1	1	1	1
3	1	1	1	1
4	1	1	1	1
5	1	1	1	1
6	1	1	1	1

DIFFUSION DATA FOR QUARTZ

(Dennis)

1. Water fugacity dependence at 700°C

$$D_{Ox} \propto f(H_2O)^m$$

$$m = -0.11 \pm 0.29 (11\sigma)$$

$$n = 0.01 \pm 0.51 (1\sigma)$$

i.e. essentially independent over $f(H_2O)$ 11-77 MPa

2. $D_{Ox} \propto f(H_2O)^{1.1}$

(Gibbs/Yund)

a marked dependence over $f(H_2O) = 22.5-225 MPa$

3. Why differences?

PROBLEMS: Both studies used restricted $f(H_2O)$ range and even quite large. This within experimental error, both studies are compatible.

At high total pressure (350 MPa) used by Gibbs/Yund quartz shows significant solubility in water.

Possible influence of solution effects on diffusion profile must be considered.

Body ^a	Wavelength ^b	W ₀	Orientation	D_{gr} , $\mu^2 \text{ s}^{-1}$	SH , hJ mol^{-1}	Conditions ^c	Reference
1	SiO ₂	700-950	n c	2.1×10^{-11}	120.26	SiO ₂	This study
2	SiO ₂	700-950	n c (SiO ₂)	3.9×10^{-10}	120.26	SiO ₂	This study
3	SiO ₂	950-1300	n c	5.0×10^{-11}	120.26	SiO ₂	This study
4	SiO ₂	950-1300	l (SiO ₂)	3.9×10^{-10}	120.26	SiO ₂	Giletti and Yund [this issue]
5	SiO ₂	950-1300	n c	5.0×10^{-11}	172.1	SiO ₂	Giletti and Yund [this issue]
6	SiO ₂	950-1300	n c	1.1×10^{-10}	133	SiO ₂	Prosser and Summels [1982]
7	Si	667	n c	$D_{\text{Si}} = 4.1 \times 10^{-16} \text{ m}^2 \text{ s}^{-1}$			Chevalier et al. [1965]
8	Si	667	n c (SiO ₂)	$D_{\text{Si}} = 0.1 \times 10^{-16} \text{ m}^2 \text{ s}^{-1}$			Chevalier et al. [1965]
9	Si	1000-1300	Isotropic	3.7×10^{-13}	120.23	$1 \times 10^6 \text{ Pa}$	Roul and Vanhous [1962]
10	Si	950-1300	Isotropic	2.1×10^{-14}	106	$2 \times 10^6 \text{ Pa}$	Schachtner and Sobel [1977]

2 (by R. H. H.)

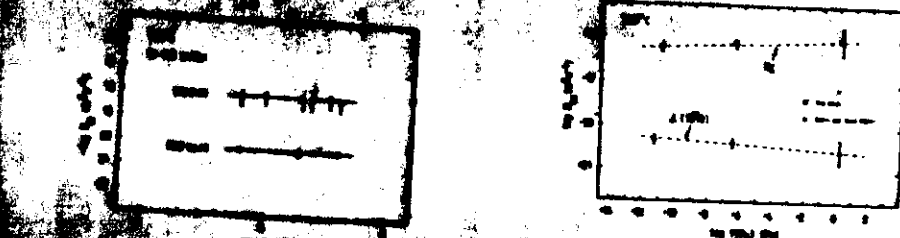


Fig. 5. Measured values of log η_{sp} as a function of log $\phi(q)$ at 70°C. The closed symbols represent data from this study (Table 3) and the open symbols are data taken from Giiletti and Vand [10] (squares). The $\phi(q)$ for the latter results are calculated from the equilibrium constant for transport of water at 70°C (Muller et al., 1978) and the work procedure, $P = 300$ MPa. The slopes for both orientations closely indicate $\phi(q)$ -independent behavior for water diffusion.

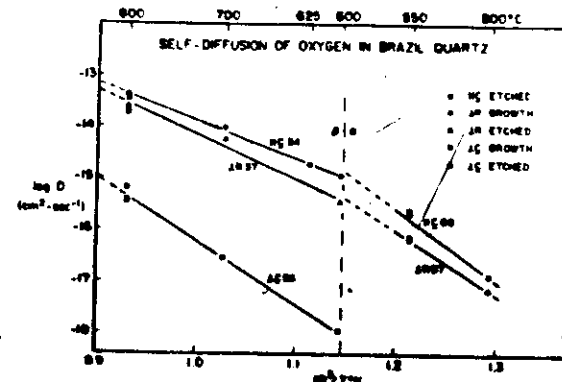
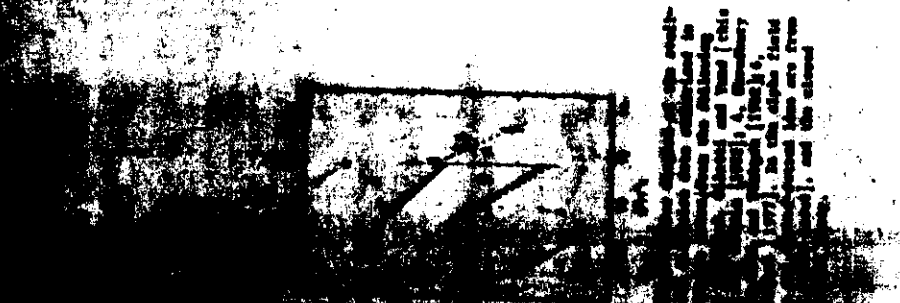


Fig. 3. Activation plot of self-diffusion coefficient D for natural quartz crystal versus $1/TK$ at 100-MPa water pressure. Each point represents the average of all measurements made for that temperature, crystallographic direction, and surface condition. The α - β transition temperature at 100 MPa is shown by the vertical dashed line. Solid lines are least squares fits of data at α or β field. Numbers next to lines are activation energies in kilocalories per mole. The dashed line shows a least squares calculation (transport) parallel to c combining the data from the α and β fields. It should be compared with the two separate solid lines, which show the best fit to the data.

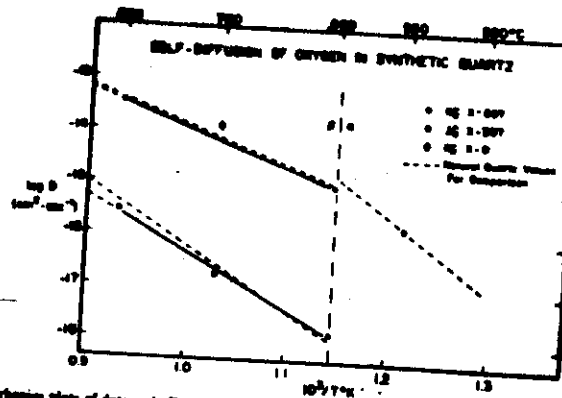


Fig. 4. Arrhenius plots of data as in Figure 1, but for synthetic crystals X-307 and X-2. Solid lines are fitted to the data, while dashed lines are from the natural quartz data shown in Figure 1.

TABLE 4. Preexponential Factor (D_0) and Activation Barriers for Arrhenius Relation

Parameter	# Quartz 500-550°C	# Quartz 600-650°C	# Quartz 650-700°C
D_0 , cm ² /s	140	4.7 × 10 ⁴	1.7 × 10 ⁵
Q , kJ/mol	214 ± 92	142 ± 4	171 ± 41
Q , kcal/mol	64 ± 22	34 ± 1	41 ± 10
D_0 , cm ² /s	3.2 × 10 ⁻¹	9.7 × 10 ⁻¹	2.7 × 10 ⁻¹
Q , kJ/mol	2.0 ± 12	1.5 ± 8	1.6 ± 10
Q , kcal/mol	57 ± 3	37 ± 2	44 ± 3
D_0 , cm ² /s	...	1.7 × 10 ⁻⁴	...
Q , kJ/mol	...	234 ± 8	...
Q , kcal/mol	...	56 ± 2	...
D_0 , cm ² /s	2.7 × 10 ⁻⁴
Q , kJ/mol	205 ± 12
Q , kcal/mol	49 ± 3

See text for discussion of how uncertainties were calculated.

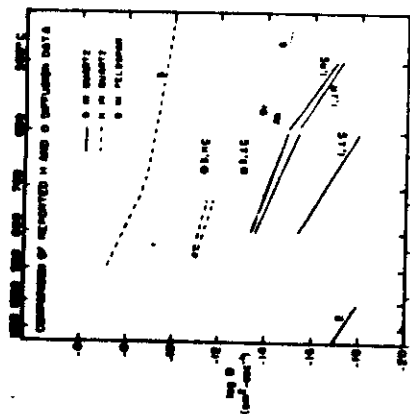
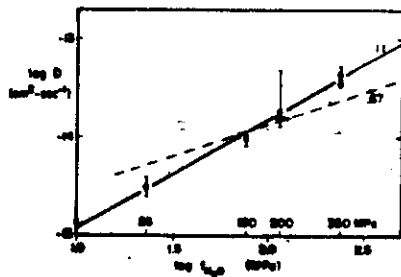


Fig. 4. Comparison of published diffusion data for hydrogen and oxygen. Key to reference numbers next to curves: 1. this work; 2. Head and Doremus (1962) dry experiments; 3. Condliffe et al. (1965) at 120-hr water pressure; 4. Shaffer et al. (1974) hydrogen; 5. Kato et al. (1982) hydrogen; and 6. Gilotti et al. (1978) oxygen diffusion in albite and orthoclase feldspars.

Fig. 5. Effect of water pressure on diffusion in quartz. Plotted as log diffusion coefficient D versus log water fugacity. Lower data show change of observed values. Triangle is data for synthetic quartz X-307; circles are for natural quartz. All for transport parallel to c axis. Numbers on lines are data slopes.

DEFECT CHEMISTRY AND DIFFUSION MECHANISMS

After Dennis data.

1. Independence of D_{Ox} with $f(H_2O)$ and $f(O_2)$ is not consistent with dissolved structural water in the lattice assisting oxygen transport.
2. All models of water incorporation in quartz and influence on diffusion of oxygen predict $D_{Ox} \propto f(H_2O)^n$ where n is >0.5 or <-0.5
3. Results are consistent with material whose point defect structure is controlled by either
 - (a) thermal ionic disorder or
 - (b) non-volatile aliovalent impurity
 - (c) transport system must involve a charged defect
4. Most probable thermal defect is Schottky one with conc. of 10^{-3} mol % at $1000^\circ K$. But defect conc. in Dennis work are at least 10^{-2} mol %, so some sort of impurity disorder is likely to be dominant.

5. Due to high conc. of Al (2.5×10^{18} Al cm⁻³) in test specimens - data accounted for by

Main defects are: divalent vacancies of oxygen, created by incorporation of Al atoms into Si lattice sites.

BUTTER/RAWPRICE MODEL

FOR LOW STRESSES

$$\dot{\epsilon} = 32 w D_b C_0 \sigma / \rho R T d^3$$

w = grain boundary film width

D_b = thin film diffusion coefficient

C_0 = solubility of mobile phase in unstressed sink solution (depends on pore pressure and temperature)

σ = applied stress difference

ρ = density of solid, R = gas constant, T = °K

d = grain size

FOR A SINUSOIDAL GRAIN BOUNDARY

$$\dot{u} = (8 \tau C_0(p, T) w D_b / h^2 \rho) (\partial \ln C_0 / \partial p)_T$$

\uparrow sliding rate \uparrow shear stress \uparrow amplitude of g.b. asperities

$$\dot{\epsilon} = X \dot{u} / d$$

\leftarrow grain size in fault zone
 \nwarrow fraction of grain sliding

PROBLEMS WITH BUTTER/RAWPRICE MODEL

Major uncertainties lie in choice of w , C_0 , D_b

\uparrow thin film width \uparrow solubility \uparrow diffusion coefficient

w - assumed constant + uniform at low stress
But must be squeezed out of region of compression precisely where it is most needed.

Even if polar layers of high viscosity in fluid maintain a layer with finite thickness then the linear dependence of strain rate on stress is likely to be lost.

w assumed $\approx 10^{-9}$ m

If high viscosity is reason fluid remains between grains then it must have different properties to bulk fluid

D_b - bounded initially by diffusivities in aqueous sol^{ns}
($10^{-8} - 10^{-9}$ m².s⁻¹)
and in common minerals - ($\ll 10^{-20}$ m².s⁻¹ at low T/T_m)

② Estimate from Stokes/Einstein/Sutherland relation
But include retardation factor (10^{-5}) because of thin film effect

$$D = kT / m \pi \eta (a/2) \quad k \leq m \leq 6$$

\nwarrow diff. coeff. of solute diffusion in bulk fluid \nwarrow solute particle diameter
 \nwarrow shear viscosity of solvent

① They used incorrect expression for Stokes/Einstein

Corrected gives

$$D_b = 2 \times 10^{-14} \text{ m}^2 \text{ s}^{-1}$$

(300°C, $P_{H_2O} = 200 \text{ bar}$)

② Viscosity of thin film must be of same order as solid or stressed fluid would be continually expelled from intergrain region.

$$\eta_e = (\Delta\sigma / 3\dot{\epsilon})$$

equivalent viscosity for flow of rock

strain difference

strain rate

$$D_b = 10^{19} \rightarrow 10^{-24} \text{ m}^2 \text{ s}^{-1}$$

③ Experiment (Brady) - estimated maximum D_b for silica through tight grain boundaries in presence of aqueous fluid.

$$D_b = 7 \times 10^{-15} \text{ m}^2 \text{ s}^{-1}$$

CONCLUDE : Question validity of Stokes/Einstein for this situation

Because of uncertainty in parameters not fruitful at present to compare experiment with Putter/Mainprice theory.

⑤

①

1. Liquid has some solubility for solid.

2. Liquid penetrates boundary between grains by coating rock between particles.

3. Strain at eroded neck rears so that plastic flow or creep occurs there.

4. Aggregate deforms and neck grows again.

$$\dot{\gamma} = \frac{3}{2} \dot{\epsilon}_0 (\sigma_1^2 - \sigma_1 \sigma_2 + \sigma_2^2 / \sigma_y^2) (\sigma_1 - \sigma_2 / (\sigma_1 + \sigma_2))$$

shear strain rate

σ_1, σ_2 principal stresses at distance

σ_y = yield stress

$$\dot{\epsilon}_0 = 8 D_L C_L \Gamma \Omega / \pi k T r^3$$

D_L = diffusivity of solid in liquid

C_L = solubility of solid in liquid

Γ = surface energy of solid/liquid interface

Ω = atomic/molar volume of diffusing species

k = Boltzmann's constant

$2r = d$ = grain size

Incorporate third power stress dependence of strain rate as yield stress is not a constant but is found experimentally to have the dependence in hydrolytically weakened state.

NON-EQUILIBRIUM THERMODYNAMICS OF PRESSURE SOLUTION

Lehner / Bataille 1984

1. Essential feature of Rutter (and others) p. solnⁿ theories is that there exists an adsorbed intergranular film of fluid that transmits the full intergranular normal stress and supports shear stresses. (Follows earlier work by Weyl).
2. These models use Gibbs fundamental equilibrium condition for a stressed solid in contact with its aqueous solution. Local chemical potential of solid component in the solution film is then LINEARLY related to the local intergranular normal stress. Rapid creep in presence of fluid is explained by essentially stress enhanced solubility along grain to grain contacts, providing driving force for diffusive mass transfer.

PROBLEM: Use of Gibbs' equilibrium condition cannot be reconciled with existence of large shear stresses in the film, which are needed to maintain mechanical equilibrium if the film is to maintain the total grain to grain contact force.

NEED TO REPLACE GIBBS CONDITION WITH EQUILIBRIUM CONDITION FOR FIRST ORDER TRANSITION OF PHASE UNDER NON-HYDROSTATIC STRESS IN EASY CRYSTALS -17-

PATERSON'S "INERT LOADING FRAME"

Useful notion of inert loading frame

1. Fluid-permeated
2. Capable of transmitting arbitrary tractions across grain boundary
3. Permits contact between hydrostatically stressed grain boundary fluid and a dissolving ~~of~~ solid.
4. Can be given clear physical interpretation of a fluid permeated contact zone at grain to grain contact ~~rate~~ fluid permeated gouge layer of fluid ~~fluid~~

PROBLEM: Paterson's generalization of Gibbs equilibrium condition does not hold true when loading frame given interpretation is above.

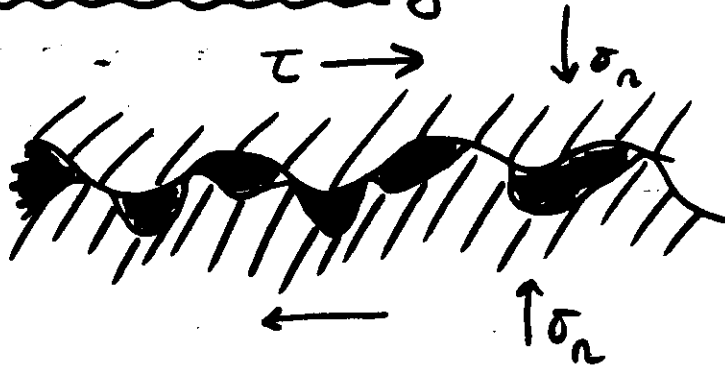
It is only valid as an approximation when interpretation is above replaced with adsorbed solution film supporting full contact stresses.

PROBLEM: Widdly held that pressure solution rates of creep are diffusion controlled.

However, examination of silica-water reaction kinetics shows that below 300 °C solution/precipitation processes are interface reaction controlled.

LENNER / BATAILLE

Pressure solution sliding



Solid portion of boundary 'strong'

For pressure solution creep, strain rates must be slow enough so that fast fracture does not occur and dry friction results for all asperity sizes.

Temps. must be low enough so that creep in solid does not occur in PARALLEL to pressure solution to relax back on asperities

Then pressure solution creep viewed as operating in SERIES with processes responsible for final crushing of asperities e.g. fast fracture - but also ~~stress~~ stress corrosion

Rate of sliding then controlled by slowest of
1. Mechanical failure of asperities 2. Interface mass transfer 3. Solute diffusion

LENNER / BATAILLE

For diffusion-controlled slip of gouge layer containing loosely packed particles (spherical)

$$\dot{\gamma} = \frac{120 \bar{V}_p^s C_p \rho^f D \tau}{\rho^s R T \bar{\delta} r}$$

where $\dot{\gamma} = \dot{u}/h$ = shear rate, \dot{u} = slip rate.

\bar{V}_p^s = molar volume of solid under hydrostatic stress
 C_p = equilibrium solute concentration at precipitation site
 ρ^f = fluid density
 ρ^s = solid density
 D = diffusion rate of species in solution
 τ = shear stress
 $\bar{\delta}$ = mean diffusion path length
 r = ($1/r$ = specific surface area of particles - approximate to $1/r_c$ where r_c is the mean particle radius)

For interface reaction controlled slip

$$\dot{\gamma} = \frac{60 k \bar{V}_p^s \rho^f \tau}{\rho^s R T r}$$

where

k = transfer coefficient

If $k \bar{\delta} / 2 C_p D \ll 1$ process will be interface reaction controlled.

LENER / BATAILLE

Comparing shear strain rates for
interface reaction control
and diffusion control

$$\dot{\gamma}_I$$

$$\dot{\gamma}_D$$

$$\dot{\gamma}_I / \dot{\gamma}_D = k \bar{S} / 2 C_p D$$

$$\dot{\gamma}_I \approx 10^{-18} \tau / r \quad \text{from quartz/water data}$$

$$\text{If } r = 10^{-4} \text{ m (grain size)}$$

and

$$\tau = 10^7 \text{ Pa (100 bars)}$$

then

$$\dot{\gamma}_I = 10^{-7} \text{ s}^{-1}$$

This is about the experimentally determined
point at which
pressure solution weakening
is observed.

CONCLUSIONS:

Pressure solution slip rates should, in
general, depend on an effective normal stress.
However, this effect may be negligible in many cases.

Interface reaction controlled slip rates are expected to be
independent of pore fluid pressure.
Sometimes accords with experiment - sometimes does not.

CALCITE

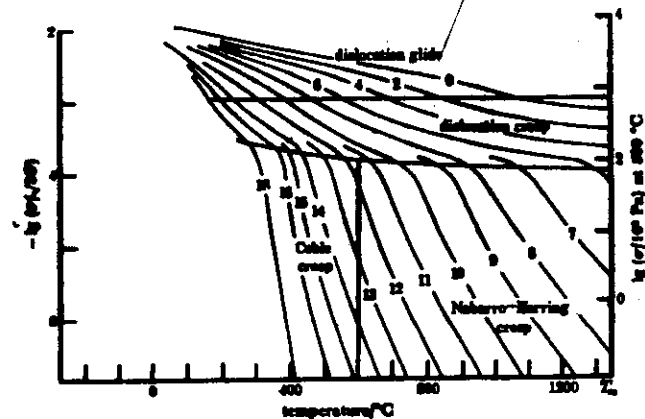


Figure 6. Deformation mechanism map for calcite without pressure solution. Contours of $-\lg$ strain rate are shown. σ is differential stress ($\sigma_1 - \sigma_3$). $d = 100 \mu\text{m}$; $V = 37 \text{ cm}^3$.

QUARTZ

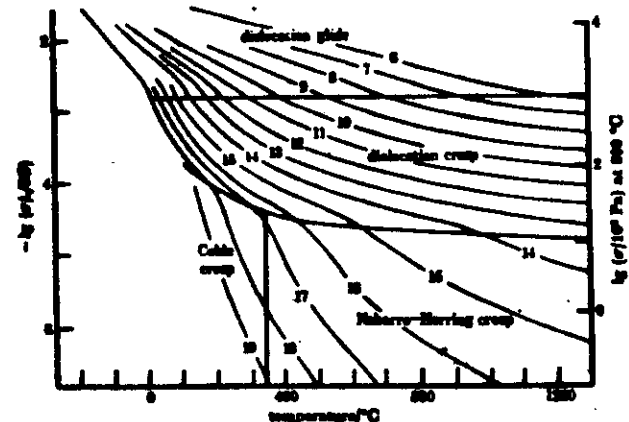


Figure 7. Deformation mechanism map for quartz without pressure solution. Contours of $-\lg$ strain rate are shown. σ is differential stress ($\sigma_1 - \sigma_3$). $d = 100 \mu\text{m}$; $V = 37 \text{ cm}^3$.

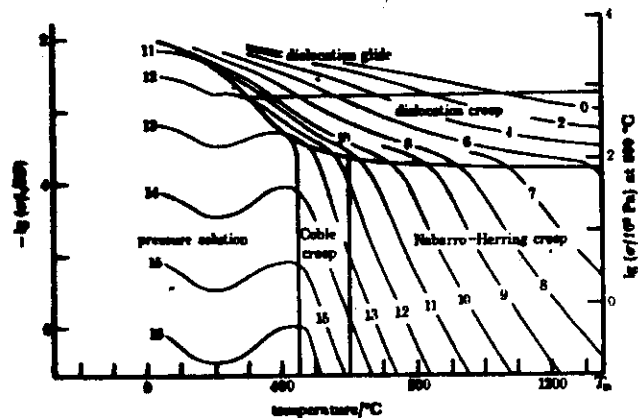


FIGURE 8. Deformation mechanism map for calcite modified by the addition of a pressure solution field. $d = 100 \mu\text{m}$; $V = 57 \text{ cm}^3$.

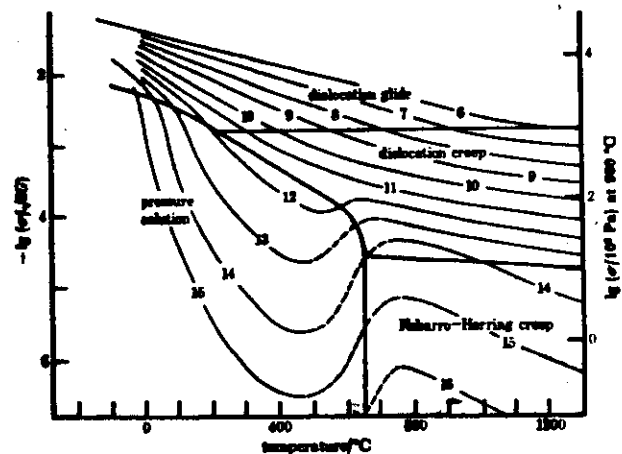
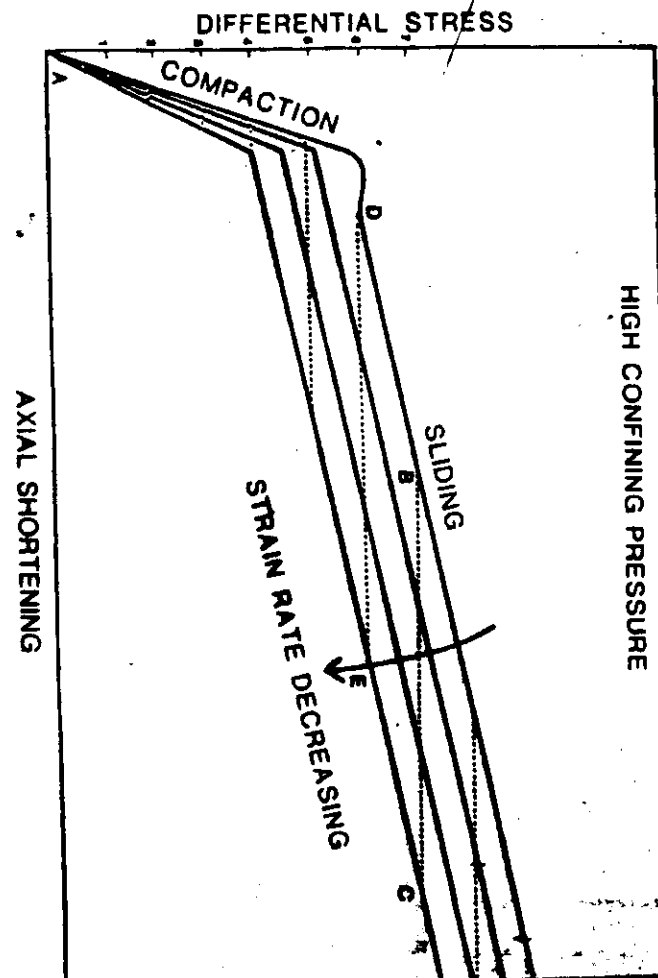


FIGURE 9. Deformation mechanism map for quartz modified by the addition of a pressure solution field. The region of dashed strain rate contours represents the inhibition of pressure solution through decrease in pore water concentration. $d = 100 \mu\text{m}$; $V = 25 \text{ cm}^3$.



SUBCRITICAL CRACKING OF ROCKS

EXTRAPOLATION TO EARTH'S CRUST

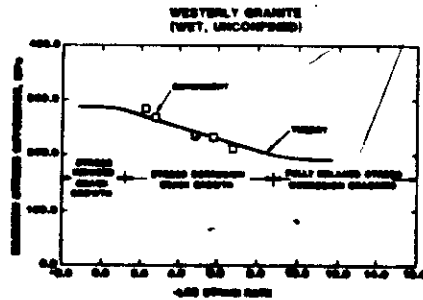


Fig. 7. Comparison of model prediction with experimental results for potential failure strength of Westerly granite over a range of strain rates.

$$1. \quad v = A_1 (k_I / k_{Ic})^{n_1} \quad \text{Charles}$$

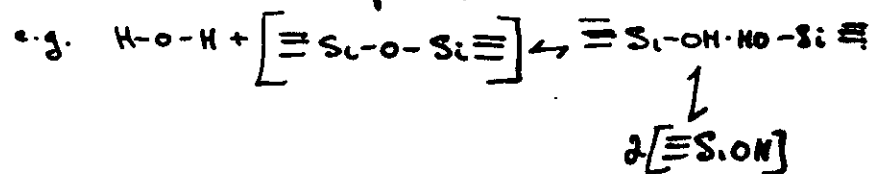
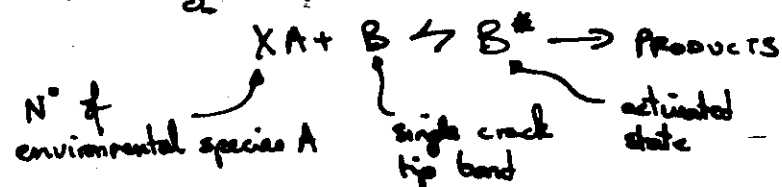
$$2. \quad v = A_2 \exp [n_2 (k_I / k_{Ic})] \quad \text{Wiederhorn-Bily}$$

$$3. \quad v = A_3 \exp [n_3 (k_I / k_{Ic})^2] \quad \text{Lawn}$$

MECHANISMS OF SUBCRITICAL CRACKING IN ROCKS/MINERALS

1. STRESS CORROSION

(a) Quartz (and other silicates)



(b) More complex minerals (biotite, hornblende)
may have constant volume complex chemical
reactions catalyzed by stress intensity concentration

2. DIFFUSION

e.g. boundary, surface
volume, vapour

3. DISSOLUTION

Concentrated at crack tip by stress assisted
removal of dissolution products.

4. ION-EXCHANGE

+ local chemical changes in minerals
involving volume changes

5. MICROPLASTICITY

inhomogeneous plastic deformation leading
to stress concentrations, crack nucleation and
growth by coalescence of microcracks

Table 1. Tensile crack growth rates in quartzite controlled by
boundary diffusion.

Grain size (micrometres)	Temperature (°C)	K_I (MPa.m ^{1/2})	Crack velocity (m.s ⁻¹)
10	200	1	7×10^{-13}
10	200	0.5	5.5×10^{-14}
10	400	1	2.2×10^{-10}
10	400	0.5	2.2×10^{-11}
1000	200	1	7×10^{-15}
1000	200	0.5	5.5×10^{-16}
1000	400	1	2.2×10^{-12}
1000	400	0.5	2.2×10^{-13}

$$\frac{da}{dt} = \frac{\Omega D_b S}{4 l^2 d k T} \left[B \sigma^2 c - \gamma + \sigma l \right]$$

Ω = molecular vol.

D_b = grain boundary diffusion

S = grain boundary width

l = crack tip radius

d = $\frac{1}{2}$ grain diameter

γ = specific grain boundary surface energy

σ = applied stress

c = $\frac{1}{2}$ crack length

$$B = \pi(1-\nu^2)/2E$$

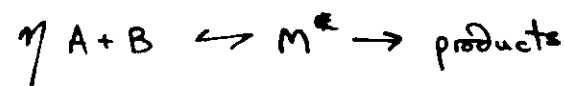
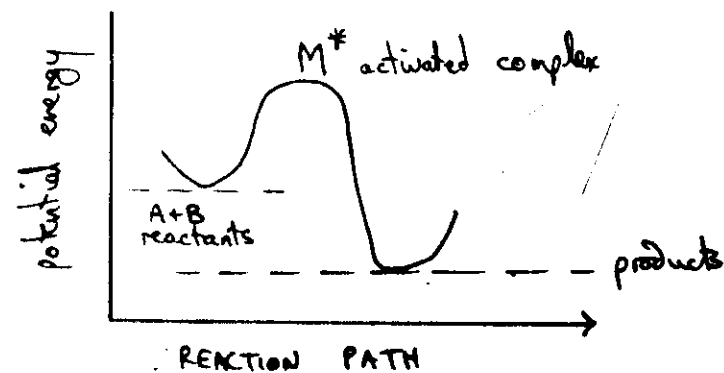
Poisson's ratio

Young's modulus

ACTIVATION ENTHALPY VALUES FOR SUBCRITICAL CRACKING IN GEOLOGICAL MATERIALS

	$\Delta T (^{\circ}\text{C})$	$\Delta H (\text{kJ} \cdot \text{mole}^{-1})$	
QUARTZ			
a plane \perp z	20-200	67	} air H_2O vap. press. 0.1-0.5 Pa
	200-300	99	
	20-100	65	} H_2O vap. 300 Pa
	100-200	73	
	20-80	52.5	H_2O liq.
5° to $[0110]$	90-240	108	} H_2O vap. H_2O vap.
	20-250	63	
$\langle c \rangle$	20-50	46-100	H_2O vap.
QUARTZITE	20-80	70	H_2O liq.
BASIC ROCKS	20-75	30-46	H_2O liq.
CALCITE ROCKS	20-85	63-147	H_2O liq.
GRANITIC ROCKS	20-300	ca. 80-100	H_2O vap.

REACTION RATE THEORY OF CRACK GROWTH



η = N^2 environmental species A reacting with a single each tip bond B to give activated (weakened) state of bond (M^*).



Weakened state assumed to be



Order of reaction

$$-dc/dt = k c^n$$

decrease in concentration (rate of transformation) = $-dc/dt$
untransformed concentration of reactant = c

n = exponent or ORDER

k = rate constant

-30-

on creep/glide ΔH : 163
Diffusion ΔH : 80-180
-29-
proton
0.1 eV

SUBCRITICAL CRACKING OF ROCKS

FRACTURE MECHANICS OF ROCKS

INFLUENCE OF PRESSURE

For surface cracks or blunt internal cracks

1. If pore fluid has access to crack tips, and

$$P_f = P_t \quad \text{ie } P_c = 0$$

$$K_I = Y(\pi c)^{\frac{1}{2}} \sigma$$

applied remote
macroscopic tensile
stress

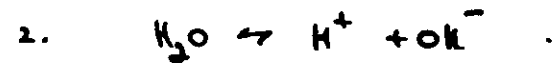
2. If pore fluid has access to crack tips
but $P_f < P_t$ ie $P_c > 0$

$$K_I = Y(\pi c)^{\frac{1}{2}} (\sigma - P_c)$$

SUBCRITICAL CRACKING IN ROCKS

INFLUENCE OF ACTIVITY OF STRESS CORROSION AGENT

1. $a[\text{H}_2\text{O}]$ increases with P_f , T and depth
in crust



$$K_w(\text{in product}) = a_{\text{OH}^-} \cdot a_{\text{H}^+}$$

$a[\text{OH}^-]$ increases with P_f and depth ($\lambda \approx 1$)
but with T goes up (250°C) then decreases



in high-temperature environments expect
neutral or acid conditions to be rare.

SUMMARY OF SUBCRITICAL CRACK GROWTH DATA

1. Slopes of curves in $K-v$ space steep but highly variable.

$$v \propto K_I^n$$

$$n = 12 \rightarrow 100!$$

Generally, the more microstructurally complex the material, the greater is the n value.

Physically, this means the greater the n value the smaller is the extent of subcritical crack growth
i.e. the less important it is for geophysical problems.

2. Activation enthalpies generally low (50-100 kJ/mol) lower than for most intracrystalline plastic deformation processes.
But hard to associate with any particular mechanism.

WHAT DO WE KNOW ABOUT SUBCRITICAL CRACKING IN QUARTZ ROCKS? AND OTHER SILICATES?

1. Stress intensity factor dependence of crack velocity is high
This means can't easily distinguish between theoretical models by lab. expts.
2. Activation enthalpy depends on models + is hard to measure but is generally low.
3. Crack velocities down to ca. 10^{-11} m.s⁻¹ measured experimentally.
4. Ranking of stress corrosion susceptibility (n higher for microstructurally more complex rocks)
5. Crack velocity dependence on water pressure, activity suggests order of reaction involved in subcritical cracking is $= 1$.
6. Increasing concentration of OH^- ions increases the rate of crack propagation
7. Increasing temperature up to 300°C increases rate of crack growth.
8. Influence of pressure?
9. Regions 2 and 3 probably restricted to small range of K values.
10. n depends on $p(H_2O)$. For $p \approx 40$ at 10^{-6} bar
 $p \approx 5-10$ at 1 bar

PHYSICO-CHEMICAL BASIS OF SUBCRITICAL CRACKING

1. Rocks rarely consist of just quartz, however. Multiphase - other silicates → feldspar, mica, pyroxene/amphibole, clinite

DO WEAKENING REACTIONS APPLY TO THESE MINERALS?

2. As crack velocity decreases - crack path tends to become predominantly intergranular.
∴ What controls "stress corrosion" at slower velocities will be details of grain boundary surface chemistry and reaction of g.b.'s/matrix with agent.
???

CONCLUDE: DON'T KNOW WHAT IS MEANT BY 'STRESS CORROSION/SUBCRITICAL CRACKING' AT THE MICROMECHANICAL LEVEL - WHICH IS CRUCIAL FOR GEOPHYSICAL EXTRAPOLATION.

SUBCRITICAL CRACKING OF ROCKS

SUBCRITICAL CRACK GROWTH LIMIT

From Charles-Hillig

$$v = v_0 \exp \left[\underset{\substack{\uparrow \\ \text{stress conc.}}}{\alpha \sigma^*} + \underset{\substack{\uparrow \\ \text{strain energy}}}{\beta \sigma^{*2}} - \underset{\substack{\uparrow \\ \text{interfacial en}}}{(\gamma/r_c)} \right]$$

terms

A: High-order stress terms negligible

$$K_0 = [(QV_n)/2b r_c] + [(E\gamma)/b] \ln(c/2)$$

given by $v = v_0 \exp(bK_1/RT)$

B: Strain energy term dominant

$$K_0 = [(QE\pi/2) + (ERT/V_n)(\pi r_c) \ln(c/2)]^{1/2}$$

Q = interfacial energy

Effect through chemical potential at crack tips

$$\mu_a = \frac{\gamma - \sigma}{l} \quad \text{in absence of stress}$$

γ = specific surface energy
 σ = atomic volume
 l = crack tip radius

$$\mu_a = \frac{\sigma}{l} (B \sigma^2 c - \gamma) \quad \text{when stressed}$$

$B = \pi(1-\nu^2)/E$
 c = crack length

- (1) Because stress enters as σ^2 for long thin cracks both tensile and compressive stress will reduce the driving force for crack spheroidization and sintering.

For small circular cracks compressive stress assists sintering.

- (2) For cracks length a where $a_c < a < a'_c$
 growth limit \rightarrow catastrophic growth
 lengthening by mass transport under tensile or compressive stress will occur.

Tensile stress \rightarrow catastrophic failure

Compressive stress \rightarrow only growth till stress forces crack to

CRACK HEALING

For grain boundary diffusion controlled

$$-dc/dt = [D_g w / 4 r_c d] [1 - \exp(\mu_a N / RT)]$$

$$\mu_a = \gamma_b V_a / r_c$$

chemical potential of atoms at crack tip

if crack stressed

$$\mu_a = (V_a / r_c) [B \sigma^2 c - \gamma_b]$$

Table 9. Subcritical crack growth limits for quartz

Mechanism	Temperature ° (C)	Mode I stress intensity factor at growth limit $K_{Ic}^{1/2}$ (MPa.m ^{1/2})
Stress corrosion		
Case A	20	0.2
	200	0.19
Case B	20	0.39
	200	0.46
Grain boundary diffusion		
Case A	20	0.39
	200	0.22
Case B	20	0.38
	200	0.38

Note: $K_{Ic}^{1/2}$ for quartz is approximately 1 MPa.m^{1/2}.

"Average" crack velocity of $10^{-12} \text{ m.s}^{-1}$
 gives $\approx 1 \text{ cm}$ of crack growth
 in 300 years
 (the recurrence time of some big quakes)

"Average" crack velocity of
 10^{-9} m.s^{-1}
 gives 3 cm/year

Although slow these velocities are
 geophysically significant.

WHAT HAPPENS TO { SUBCRITICAL CRACKING } PROCESS IN GEOLOGICAL ENVIRONMENTS?

- A. Will depend on detailed nature of process.
- B. From what we know of variation of T , P_T , P_f and a [logarithm] with crustal depth - can construct possible patterns of behaviour.

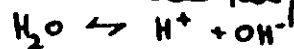
81. If molecular water is the agent.

$a[H_2O]$ increases with increase in P_f , T and depth

\therefore Should get an increase in crack growth rates with depth.

But fugacity $[H_2O]$ changes by only about $1\frac{1}{2}$ orders throughout the crust.

82. If ionized water or hydroxyl involved



$$K_w = a_{OH^-} \cdot a_{H^+}$$

$$K_w = 10^{-14} \text{ @ P.T.}$$

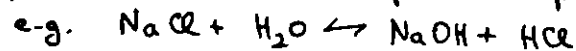
$$= 10^{-8} \text{ at base of crust}$$

$a[OH^-]$ increases with water pressure, increases with depth (if $\lambda=1$) but after slight increase will decrease with temperature.

Substantial changes possible in this variable.

[Is this a way of distinguishing between 2 potential agents?]

83. Because water becomes a stronger acid than most common ones at depth - it will displace them from their salts



Thus neutral or acid conditions should be rare in high-temperature environments

LEVELS OF SHEAR STRESS IN FAULT ZONES

Problem: Current estimates vary by at least 1 order of magnitude. Hence major problems such as

driving mechanism of plate tectonics

energetics of crustal faulting

are entirely unresolved.

Deviatoric

1. Shear stress can only be measured directly very close to the earth's surface by overcoring hydrofracturing wire strain meters etc

2. It becomes necessary to infer from secondary lines of evidence what the level of shear + other stresses might be.

Generally: 2 schools of thought

- ① Shear stress is "high" $\gg 1,000$ bars
- ② Shear stress is "low" ≈ 100 bars

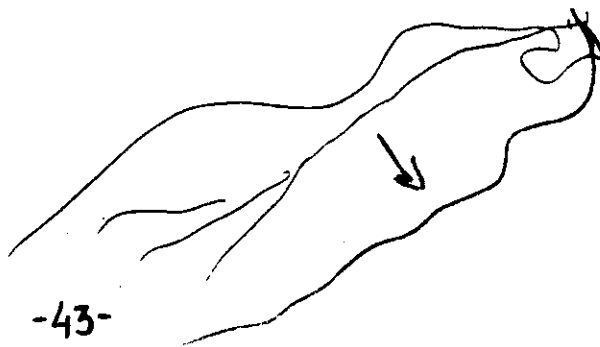
STRESS LEVELS IN FAULT ZONES; SOME

INDIRECT LINES OF EVIDENCE

1. Laboratory studies of rock friction
2. Seismology
3. Heat-flow anomalies around fault zones
4. Geological evidence → fault rock textures
→ hydrothermal veining, etc.
5. Microstructural paleopiezometers
6. Laboratory studies of stress memory effects.

DIRECT LINES OF EVIDENCE

1. Hydrofracturing
2. Overcoring - stress relief
3. Wire stress rods (really strain rods) } surface or near-surface



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THE POTENTIAL GEOPIEZOMETERS

Empirical relations have been established in metals between the dislocation microstructures and deviatoric stress and their applications in the case of rocks discussed by Nicolas & Poirier (1976, p. 137). The main relations tie the dislocation curvature, the dislocation density and the subgrain size to the applied stress.

Durham, Goetze & Blake (1977) have considered the relation between the minimum radius of curvature (R , measured in micrometres) of dislocation loops and the stress (σ , measured in kilobars) in olivine. They observe a fairly good experimental correlation:

$$\sigma \approx 0.6 R^{-1},$$

which when compared with the expected relation

$$\sigma = K \rho b R^{-1},$$

where ρ is the shear modulus and b the Burgers vector, yields a K value of 1.04×10^{-2} kbar cm.

The relation between the free dislocation density (ρ) and the stress has been experimentally investigated by Kohlstedt & Goetze (1974), by Goetze (1975a, b) and by Durham *et al.* (1977) who find a good experimental correlation expressed in the general form:

$$\sigma = K' \rho^{1/2} b,$$

$$\sigma = 9 \times 10^{-2} \rho^{1/2} \text{ (Goetze 1975a, b),}$$

$$\sigma = 2 \times 10^{-2} \rho^{1/2} \text{ (Durham et al. 1977).}$$

The relation between the subgrain size (d , measured in micrometres) and the maximum stress is expected to have the following form:

$$\sigma = K'' \rho^{1/2} d^{-1}.$$

In olivine, the $\{100\}$ tilt wall spacing is principally measured, due to its predominance over any other substructure and to its smallest spacing when compared to the other subboundary systems. The considered subgrains are only those optically visible and not those which subdivide them at the L.C.M. scale (Green & Radcliffe 1972). They are now observed using a new decoration technique (Kohlstedt, Goetze, Durham & Vander Sande 1976) which, making it possible to observe about ten times as many tilt walls than before, can explain the large discrepancy between Raleigh & Kirby's (1970), Goetze's (1975a, b), Mercier's (1976) and Durham *et al.* (1977) relations.

$$\sigma = 17 d^{-1} \text{ (Goetze 1975a, b),}$$

$$\sigma = 115 d^{-1} \text{ (Mercier 1976),}$$

$$\sigma = 10 d^{-1} \text{ (Durham et al. 1977).}$$

The size of dynamically recrystallized olivine grains (neoblasts) has also been considered as a potential geopiezometer for mantle rocks. The following experimental relations have been found:

$$\sigma = 11 d^{-0.5} \text{ (Goetze 1975a, b),}$$

$$\sigma = 10 d^{-0.5} \text{ (Post 1973),}$$

$$\sigma = 60 d^{-0.5} \text{ (Mercier 1976).}$$

Mercier obtains a weak temperature dependence for this relation:

$$d = 1.13 \sigma^{-1.4} \exp(13500/RT).$$

Otherwise, as expected from the metallurgical literature, no temperature dependence is found for all these relations.

-44-

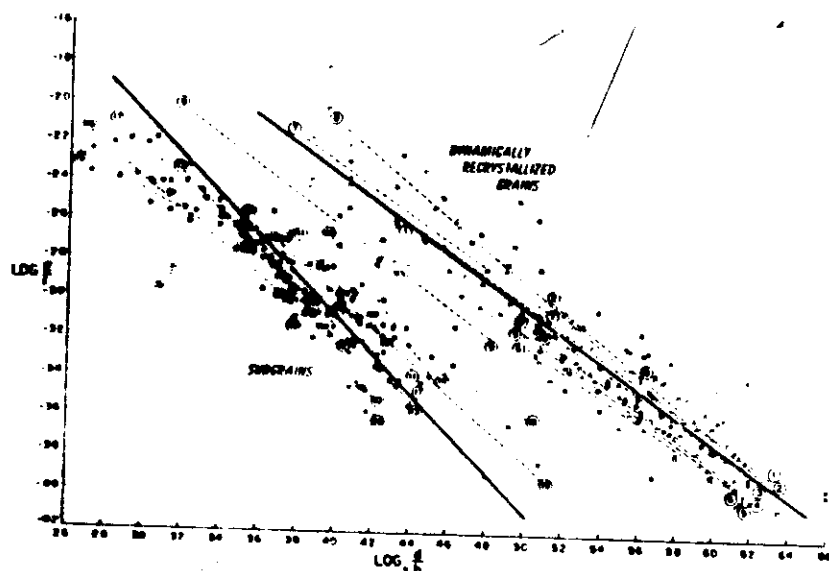


Figure 1

Non-dimensionalized plot of experimentally determined stress vs. subgrain size and recrystallized grain size for steady state creep. The key to the symbols is in Table 1. Data were rendered non-dimensional by constants in Table 2. Dashed lines are unweighted linear regressions to individual data sets. Each solid line is a best fit to the respective group of data for subgrains and recrystallized grains. The slope of the solid line is taken to be the mean of the slopes of the data sets in each group. The theoretical equation fits the solid lines exactly for physically reasonable values of the empirical parameters.

MAXIMUM FRICTION

EXPLANATION
SYMBOL REFERENCE ROCK TYPE

•	2F	Granite, fractured
•	2G	Granite, ground surface
•	3	Limestone, Gabbro, Quartz
•	5	Granite, ground surface
•	6F	Weber Sandstone, faulted
•	6S	Weber Sandstone, saw cut
•	9	Granodiorite
•	13	Gneiss and Mylonite
•	16	Plaster in joint of Quartz Monzonite
•	20	Quartz Monzonite joints
•	25	Westerly Granite, Chlorite, Serpentine, Illite, Kaolinite, Halloysite, Montmorillonite, Vermiculite
•	26	Granite
•	27	Kaolinite, Halloysite, Illite, Montmorillonite, Vermiculite

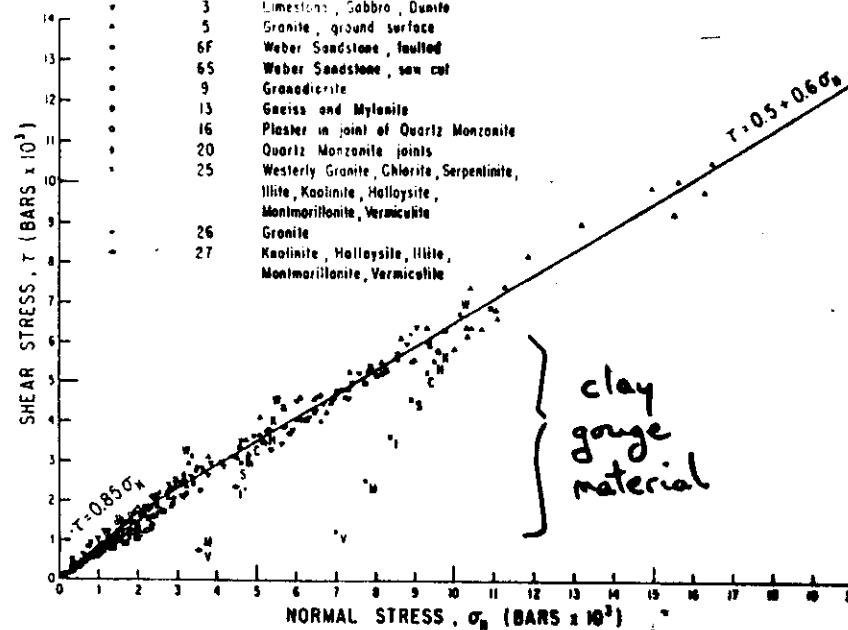


Figure 7

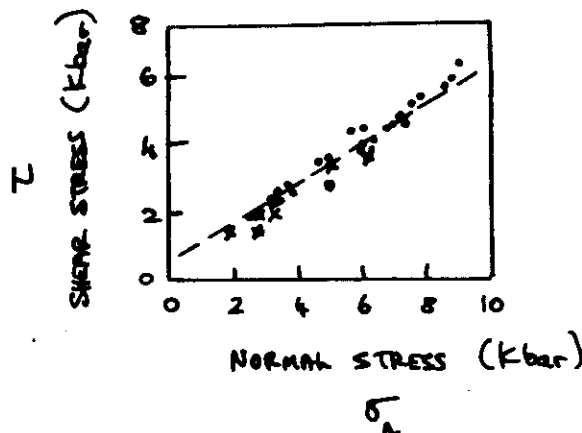
Shear stress plotted as a function of normal stress at the maximum friction for a variety of rock types at normal stresses to 20 kb.

Clay minerals not likely to be stable
below ≈ 10 km.

EFFECT OF TEMPERATURE ON SLIDING STRESS OF WESTERN GRANITE

BRIP
(Saw cuts)

$$\tau = 0.5 + 0.6 \sigma_n$$



- 20°C
- x 100°C
- x 300°C
- 400°C
- x 500°C

①

LABORATORY STUDIES OF ROCK FRICTION

1. Byerlee's law:

For sliding to occur

$$\tau_f = \mu (\sigma_n - P_f)$$

coefficient of static friction

μ is largely independent of rock type.

2. To get low shear stress requires pore fluid pressures \approx lithostatic. from

$$\sigma_{ij} = \sigma_{ij} - P_{fluid}$$

effective stress law. This may occur transiently in earthquake faulting - but permeability data for crust (Brace) suggest that will not be a general condition for earthquake fault zones. Transient increase in P_f due to shear heating - expansion of water in pore space.

Pore fluid pressures are likely to exceed hydrostatic if impermeable cap rocks present. Pore fluids, if not present everywhere, are at least very common in the upper crust.

THUS: LAB DATA SUGGESTS SHEAR STRESSES \approx 1 Kb or less
UNLESS $P_f \approx P_{load}$

GEOPHYSICAL EVIDENCE

1. Stress drops for most earthquakes are low ≈ 100 bars or so for the large ones.

Although exceptions where stress drop is high do occur.

2. Can this be taken to mean that the average ambient shear stress is ≈ 100 bars also?

3. If pore water is present then provided shear strain > 1 near-total stress drops must occur because of seismic shear heating of pore water increasing pore water pressure and decreasing effective stress on fault to near zero. ($\sigma_{eff} = \sigma_t - p$)

4. Only requirement is that hydraulic diffusivity of fault rock is lower than thermal diffusivity so that fluid flow away from fault does not take heat away.

Estimated values for S.A.F. (1 kb, 300°C)

hydraulic diffusivity = $10^{-4} - 10^{-5} \text{ cm}^2 \text{ s}^{-1}$

thermal diffusivity = $10^{-2} \text{ cm}^2 \text{ s}^{-1}$

MAXIMUM INCREASE IN PRESSURE OF WATER IN FAULT DUE TO SEISMOGENIC HEATING AT SLIP VELOCITIES OF METRES/SEC

Average Shear Stress (bars) $\bar{\tau}$	Displacement (cm) u	Width (cm) $2a$	Shear Strain γ	time (s)	change in temperature (°C) ΔT	Pore pressure increase (bars) ΔP
50	10	2	5	0.1	10^{-14}	150
50	10	10	1	0.1	2×10^{-13}	30
50	100	2	50	1.0	10^{-12}	1,500
50	100	10	10	1.0	2×10^{-12}	300
500	10	2	5	0.1	10^{-14}	1,500
500	10	10	1	0.1	2×10^{-13}	300
500	100	2	50	1.0	10^{-12}	15,000
500	100	10	10	1.0	2×10^{-12}	3,000
500	100	100	1	1.0	2×10^{-12}	300

From $\frac{dP}{d\bar{\tau}} = 0.6 \gamma$

change in pressure with shear strain

shear strain

$$\left[\gamma = \frac{u}{2a} \right]$$

HEAT FLOW ANOMALIES

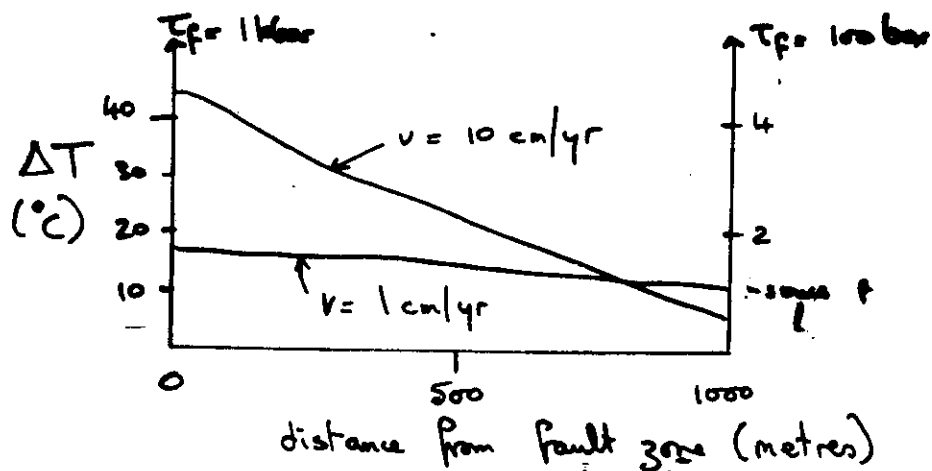
Steady aseismic shearing across fault zone with shear resistance τ_f gives a constant heat flux per unit volume of the zone

$$\dot{H} = (\tau_f \cdot v) / w$$

v = slip rate, w = width of zone

If shear stress high enough over long enough period - can get shear heating leading to heat flow anomalies.

e.g. 10 m wide shear zone, displacement of 1 km at 1-10 cm/yr against shear resistances of 100 bars \rightarrow 1 kbar.



NB: Rise in temperature occurs over a much broader region than fault (10 m wide in this case).

1. Sharpness of thermal gradient increases with slip rate
2. High shear stress is required to generate high energy

ABSENCE OF HEAT FLOW ANOMALY OVER

SAN ANDREAS FAULT

1. Over segment of S.A.F. that is not creeping and ^{which} produced a great earthquake in 1857 no measurable perturbation of the regional value of 1.6 heat flow units occurs.

This is consistent with a low ambient shear stress of \approx 150 bars maximum.

[UNLESS]

Heat generated is dissipated by convective circulation of water, which

Would require a thermal spring flowing at 10,000 litres/hr at 100°C

At every kilometre along fault.

This is not observed -

SAF shows absence of thermal springs except in Geopline Valley where volcanic heat sources exist.

If convection pulls heat away from fault then would get high heat flow over broad region with peak over fault.

This is not observed either.

energy dissipated by other means

e.g. phase change (dehydration or melting)

Creation of new surface area by comminution

Neither of these can absorb enough energy to explain away a shear heating anomaly.

GEOLOGICAL EVIDENCE: HYDROTHERMAL
VEINING, etc.

1. Many faults show en-echelon mineralized hydrofractures and other sorts of hydrothermal veining.
Spatial and textural arrangement suggests they formed at same time as fault.

Condition for their formation is that

$$P_{\text{fluid}} > \sigma_3 \text{ (overburden)}$$

by an amount = tensile strength of rock

\therefore Implies high pore fluid pressures.

2. Other fault zones show no such evidence
 \therefore perhaps "dry".

Remember exhumed fault zones seen at surface represent past state at depth.

Type 1 fault zones (i.e. wet) ones seen most common.

- * No hydrothermal veining in Alpine Fault
- * Hydrothermal veining in San Andreas Fault

IMPLICATIONS OF PRESENCE OF PSEUDO-
TACHYLITE ON FAULTS

1. Field evidence suggests that ^{generation 2} injection of pseudo-tach. melt took place within a few seconds -
implying 'seismic' slip rates of $\sim 10 \text{ cm s}^{-1}$
2. Melting on fault planes is inhibited by presence of pore fluids.
Because frictional heating creates as a transient localized increase in fluid pressure (from P, V, T data for water) that drastically lowers the effective normal stress across the fault plane, and thus the capacity of the fault to generate heat by further slip.
Thus pseudotachylite a product of dry faulting.
3. Because rocks are dry and from τ_f / slip displacement graph - high shear stress of a kilobars is required to initiate pseudotachylite generation
4. As frictional resistance drops with displacement -
One fault is 'lubricated' by presence of melt
then would expect almost total stress relief -
and possibly large earthquakes.

PSEUDO TACHYLITE ON FAULTS

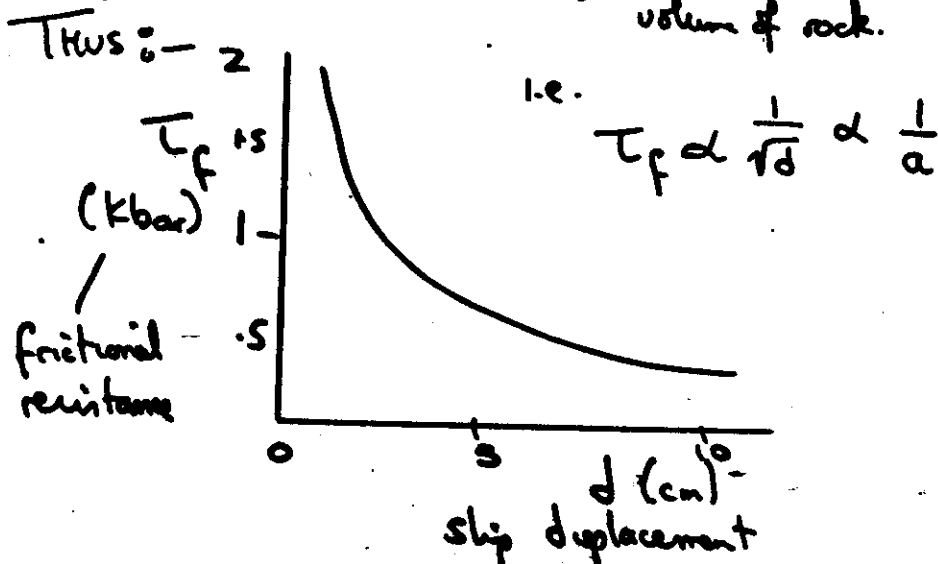
Field observations show that displacement (d) on pseudotachylite faults is related to thickness (a) by

$$d = K a^2 \quad K \approx 500$$

Heat generated per unit area of fault after displacement d \propto thickness of melt layer

$$H = \int_0^d \tau_f \cdot dx = 2 \sqrt{(d/K)}$$

τ_f : frictional resistance, q : heat to melt unit volume of rock.



Frictional resistance falls off with displacement

AS A STRESS INDICATOR

Advantages: Occurs under critical resolved shear stress that is independent of temperature and strain rate and does not appear to be affected by σ_3 or pore fluid pressure.

Most useful: Calcite, Dolomite, Clinopyroxene

Critical shear stresses for twinning in key systems	100 bars	1000 bars	1400 bars
	↓	↓	↓

N.B. Shear stress supported by aggregate varies because not all grains favourably oriented for twinning and some intracrystalline slip must also occur to satisfy Von Mises ductility criterion (5 independent slip systems)

Reduction in shear stress supported by aggregate with T increase or $\dot{\epsilon}$ decrease due to fact that T and $\dot{\epsilon}$ - dependent intracrystalline slip is also occurring.

FROM DEFORMATION MICROSTRUCTURES

Recrystallized grain size: $(\sigma_1 - \sigma_3) = A \cdot D^{-n}$
 diff. stress / grain size
 A, n are constants

e.g. Quartzite
 $(\sigma_1 - \sigma_3) = 381 \cdot D^{-0.71}$
 [MPa] [microns]

Dislocation density: $(\sigma_1 - \sigma_3) = \mu b \sqrt{N}$
 shear modulus (GPa) / Burgers vector (nm) / dislocation density

e.g. Quartz
 $N = 1.6 \times 10^4 (\sigma_1 - \sigma_3)^{1.5}$
 MPa

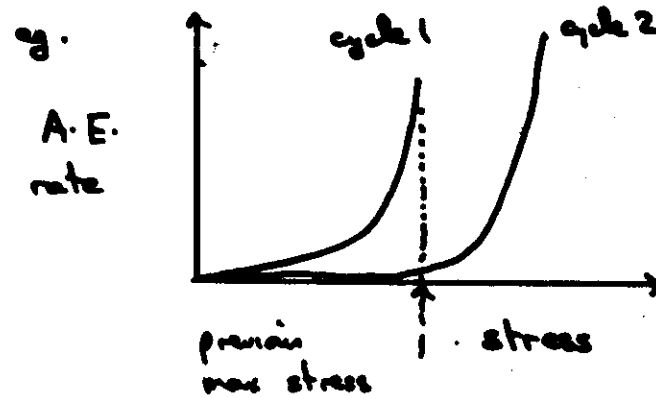
e.g. Coyote Mtn. Mylonite



Problem: Very sensitive to environmental conditions
 ① Based on little experimental data
 ② Affected by post deformation annealing

LAB STUDIES OF STRESS MEMORY EFFECTS

Kaiser effect: Rock subject to cyclic loading only exhibits significant acoustic emission when stressed in the second and subsequent cycles after the maximum stress in previous cycles has been exceeded.



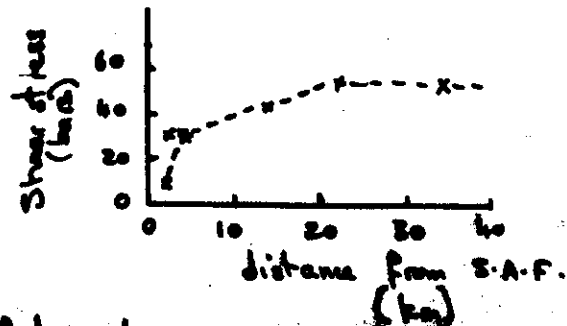
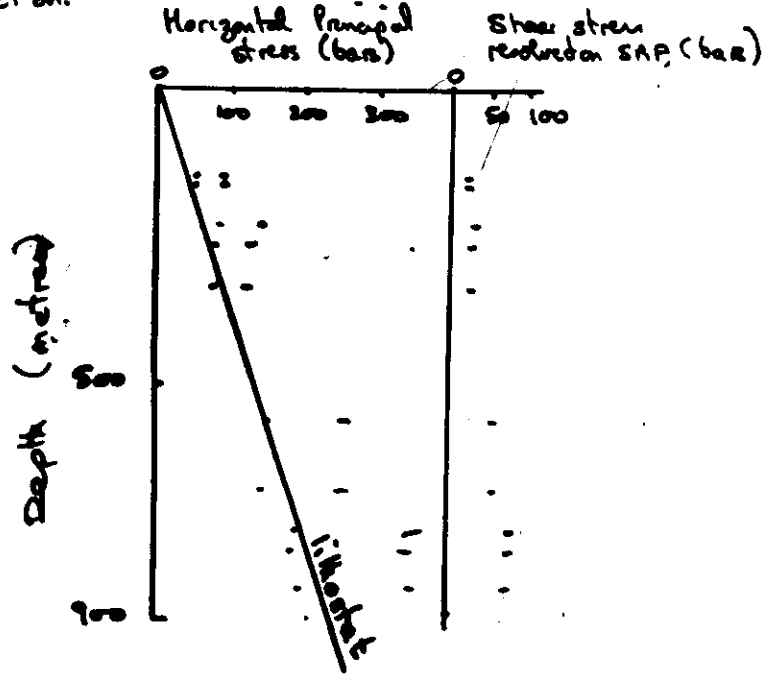
Mogi found sometimes not clear in simple expts - so suggested that the DIFFERENCE in AE activity between cycles is used as an indicator of previous max. stress. This increases markedly once the previous max stress exceeded.

Problems: - ① What about annealing / cavitation / strain rate and memory loss
 ② Kaiser effect not seen in all rocks
 dilatancy associated with failure stress.

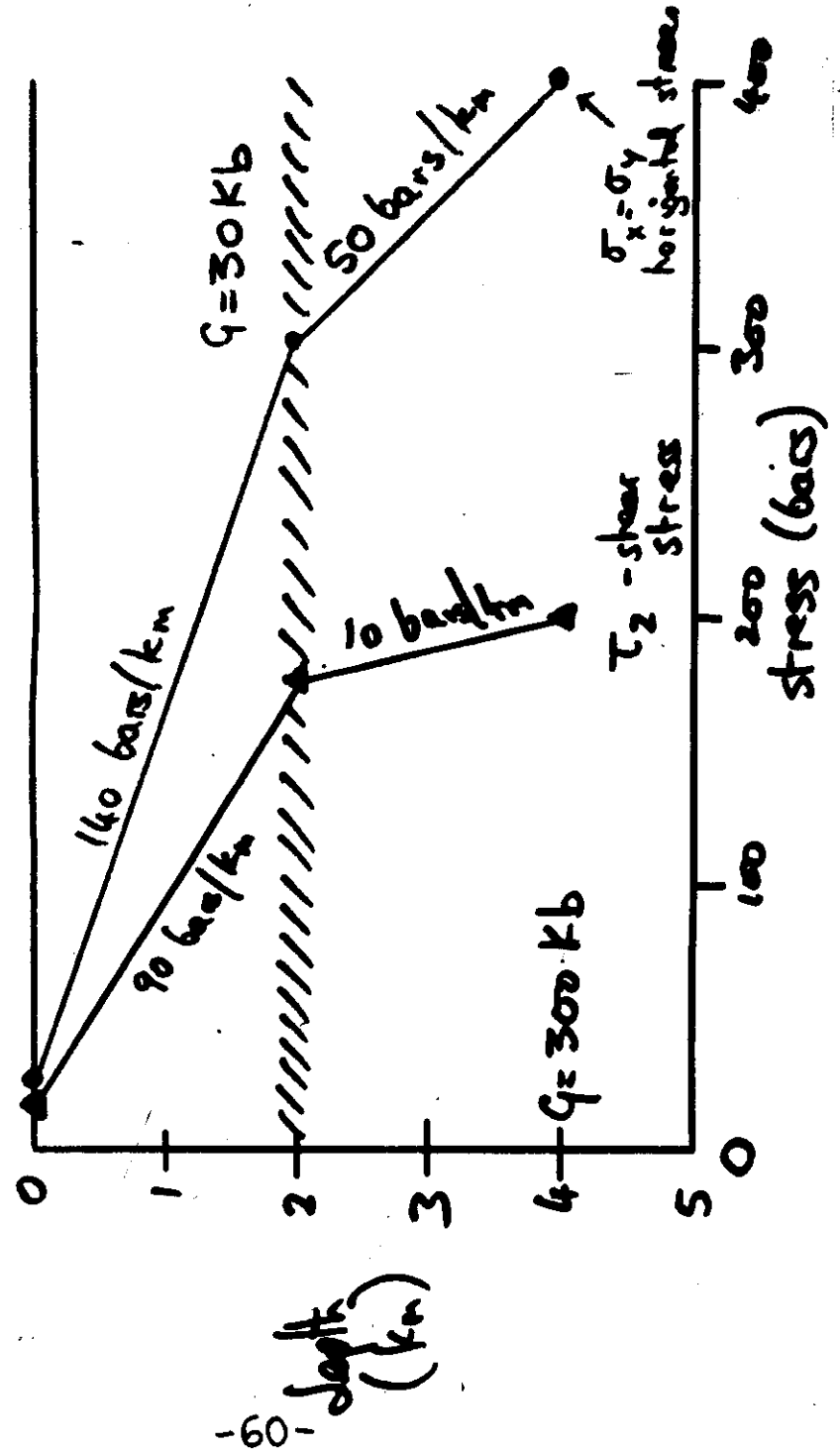
STRESS LEVELS IN VICINITY OF SAN ANDREAS FAULT FROM HYDROFRACTURE

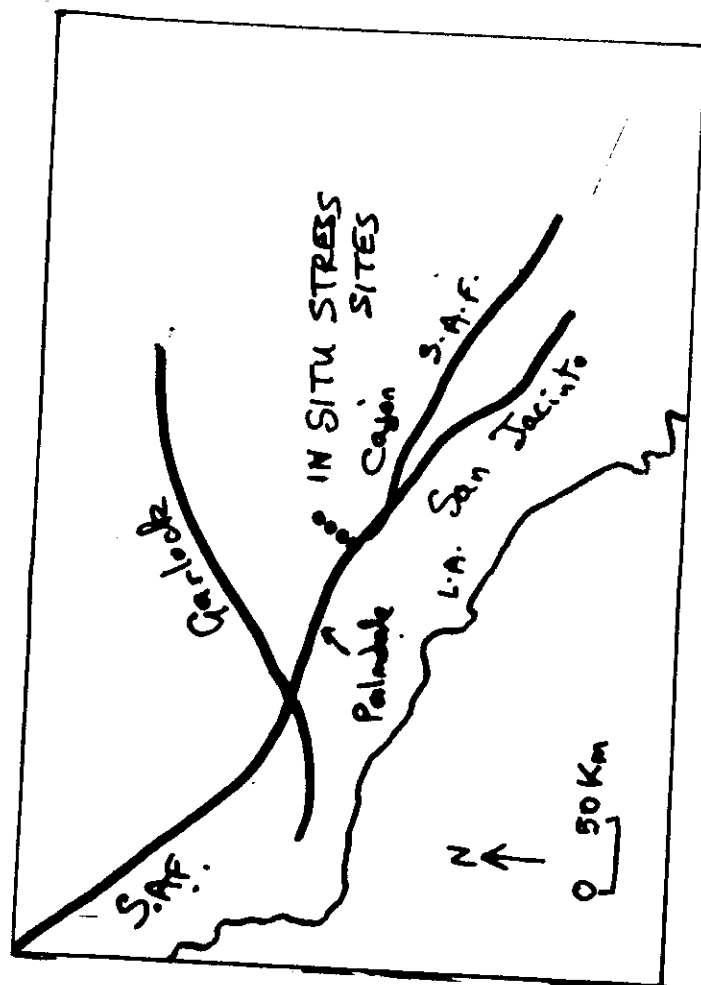
Zoback et al.

DATA



Extrapolation to zero distance from S.A.F. suggests shear stress of several hundred bars - but no increase in step-like Zoback things at a near surface depth and extrapolation not justified. But with ~~step-like~~ things





IN-SITU STRESS

1. Vertical stress gradients are proportional to horizontal gradients of critical surface deformation.
2. Actual displacement measurements around San Andreas Fault. are consistent with a layered crust - not simple model usual used to interpret in-situ stress measurements.
3. Over tectonic time-scale crust has vertically increasing rigidity.
Modelled in figure.
4. In-situ hydrofracturing measurements are very shallow and don't tap deeper trends.
5. Actual shear stress gradient at depth is more likely to be $\sim 10 \text{ bar/km}$
6. Over seismogenic zone - leads to average shear stress of $\leq 225 \text{ bar}$.

ALPINE FAULT

SHEAR HEATING

1. METAMORPHIC ISOGRADS ARE STEEP TO PARALLEL TO FAULT AND VERTICAL. DECREASING IN GRADE AWAY FROM FAULT.
2. HORIZONTAL TEMPERATURE GRADIENT OF $40^{\circ}\text{C}/\text{km}$ INDICATED FROM ISOGRADS.

3. SHEAR STRESS $< 1 \text{ kbar}$ CANNOT PRODUCE THIS HEAT UNLESS SLIP VELOCITIES BETWEEN PLATES ARE $> 10 \text{ cm/yr}$.

4. SCHISTS UP TO 15 km AWAY FROM FAULT ARE DEPLETED IN RADIOGENIC ARGON THAT CANNOT BE EXPLAINED BY SIMPLE UPLIFT.

5. POSSIBLE HEAT FLOW ANOMALY

6. SHEAR STRESS (LONG TERM)

$\sim 1 \text{ kbar}$ at base

SAN ANDREAS FAULT

NO SHEAR HEATING

NO OBVIOUS LINK BETWEEN METAMORPHISM AND FAULT AS IT IS AT PRESENT

SHEAR STRESS OF CA. 100 bars IS CONSISTENT WITH HEAT FLOW DATA.

NO HEAT FLOW ANOMALY

NOT ENOUGH THERMAL SPRINGS
NOT ENOUGH CONJUNCTION
OR DEHYDRATION

SHEAR STRESS (LONG TERM)

$\sim 100 \text{ bars}$

UNLESS ARGILLACEOUS CAP ROCK PRESENT LOCALLY

SUMMARY

1. Some faults 'wet', some 'dry' i.e. have high or low pore fluid pressure 'Wet' are more common
2. Dry faults may support high shear stress $\sim 1000 \text{ bars}$ Wet faults may only support low shear $\sim 100 \text{ bars}$ during seismic and aseismic shearing.

But what is mechanism?

Although transient ^{pore} pressure rise in earthquake faulting due to shear heating may drop effective normal stress on fault

This cannot work for aseismic shearing as pressures dissipated over longer times available.

* Pore fluid pressures are generally not \rightarrow lithostatic but when present may be \rightarrow hydrostatic. Lab. expts to date have shown high frictional resistance under these conditions.

Resolution of dilemma ~~is not possible~~ in recent expts.

\rightarrow unless argillaceous cap rocks present locally

