



INTERNATIONAL ATOMIC ENERGY AGENCY
UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION



INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS
34100 TRIESTE (ITALY) - P.O.B. 586 - MIRAMARE - STRADA COSTIERA 11 - TELEPHONES: 224281/3/3/4/5/6
CABLE: CENTRATOM - TELEX 460392 I

Page 53

SPRING COLLEGE ON AMORPHOUS SOLIDS
AND THE LIQUID STATE
14 April - 18 June 1982

DEFECTS AND DEFECT MODELS
(Part II)

E.A. DAVIS
Department of Physics
University of Leicester
University Road
Leicester LE1 7RH
UK

These are preliminary lecture notes, intended only for distribution to participants.
Missing or extra copies are available from Room 230.

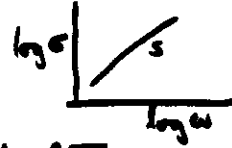
2b) A.C. Conductivity (again)

-1-

QMT (quantum mechanical tunnelling) model

$$\sigma(\omega) \propto T \omega \ln^4\left(\frac{\nu_0}{\omega}\right)$$

$$s = \frac{d \ln \sigma(\omega)}{d \ln \omega} = 1 - \frac{4}{\ln\left(\frac{\nu_0}{\omega}\right)}$$



$$s < 0.8 \quad \Rightarrow \omega \uparrow \quad s \text{ indep of } T$$

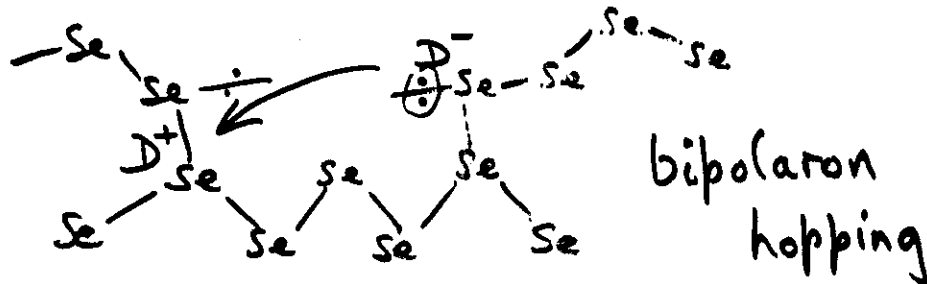
Expt results on chalcogenides (sop. transp. materials)

$$s \approx 0.8-1 \quad s \text{ indep of } \omega \quad s \uparrow T \downarrow$$

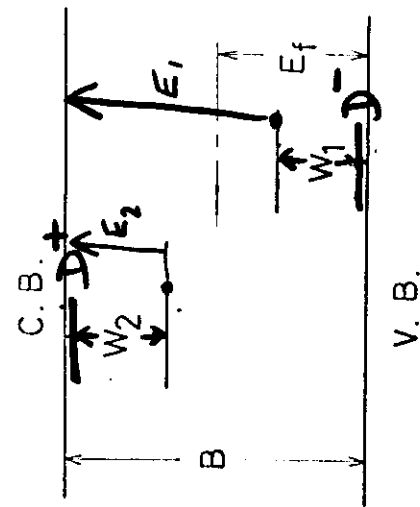
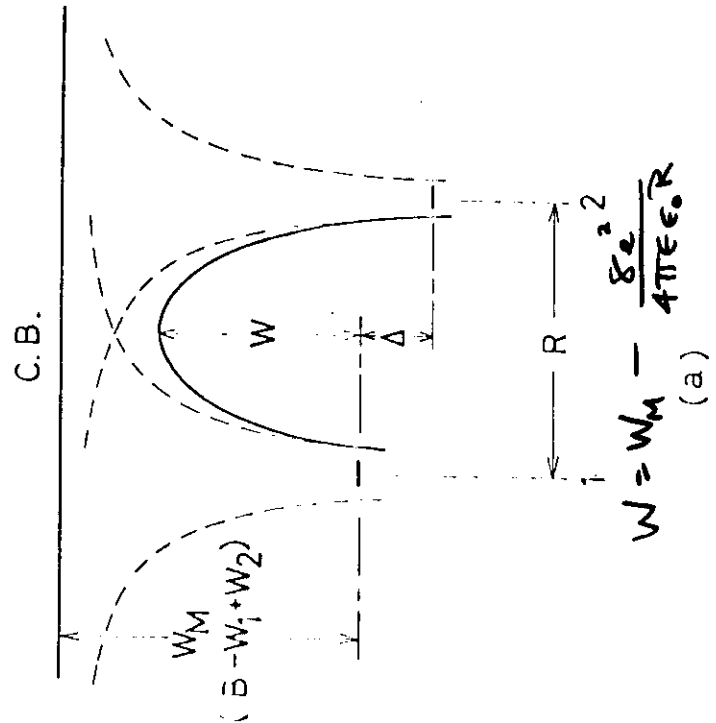
Also s and $\sigma(\omega)$ depend on band gap $\downarrow$

CBH (correlated barrier hopping) model

ELLIOTT, S.R. { Phil Mag 36 1291 (1977)
Solid State Comm 28 939 (1978)
J. Non-Cryst. Sol 35-36 855 (1980)
Phil Mag 43 553 (1978)
Phil Mag 44 507 (1979)
Phil Mag 43 325 (1978)



bipolaron hopping

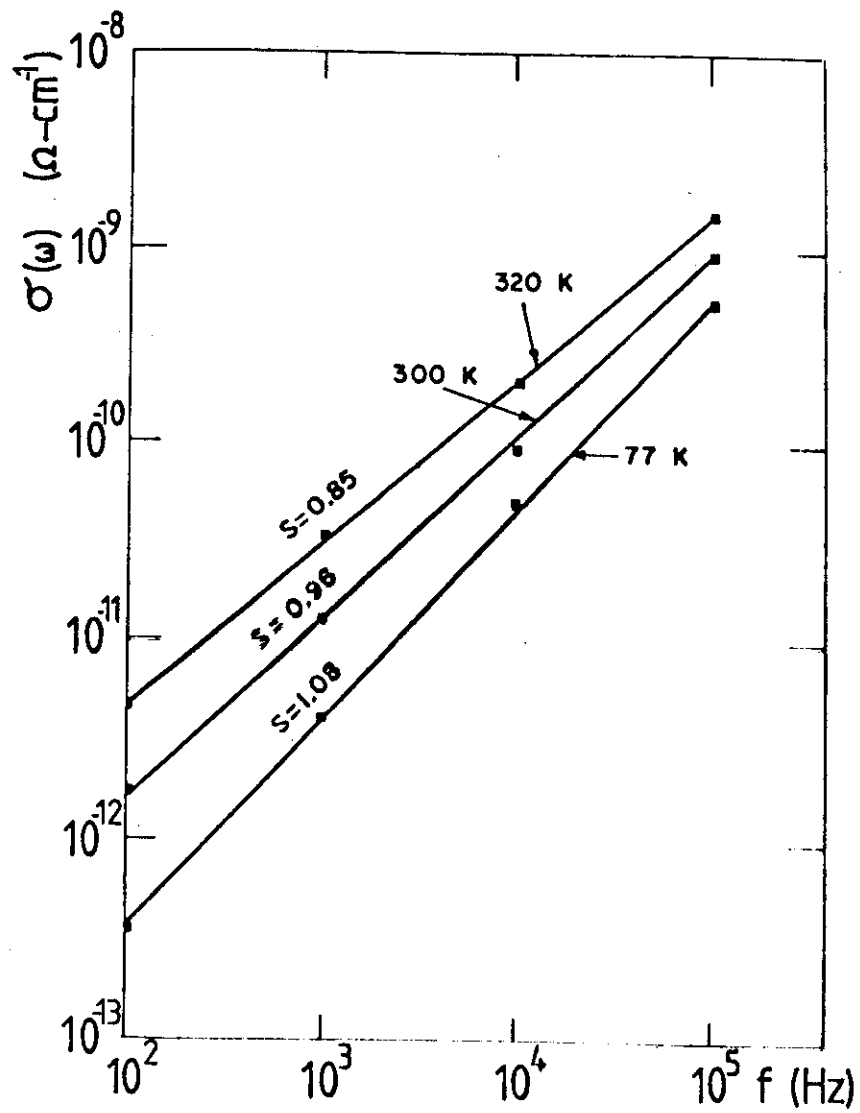


(b)

$$\begin{aligned} E_1 &= B - W_1 - E^- \\ E_2 &= W_2 + E^+ \\ E_1 + E_2 &= B \end{aligned}$$

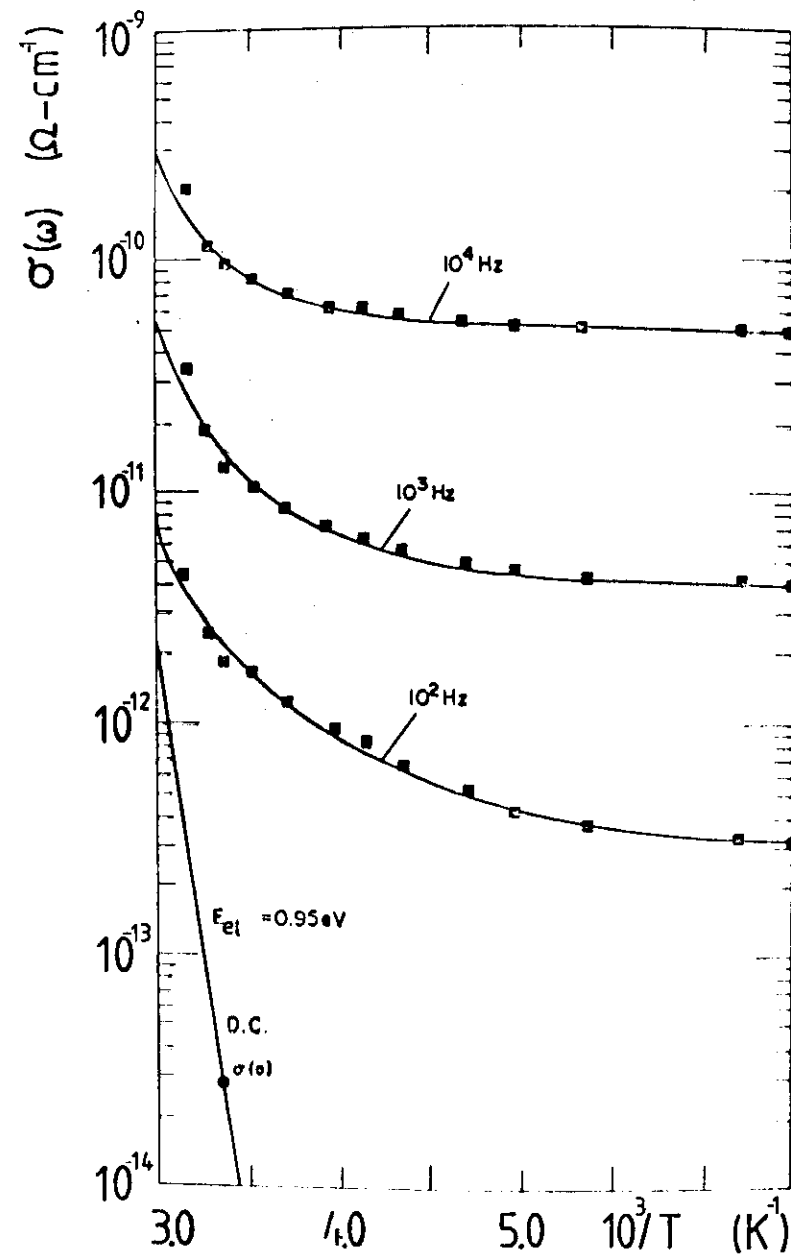
Fig. 1

3

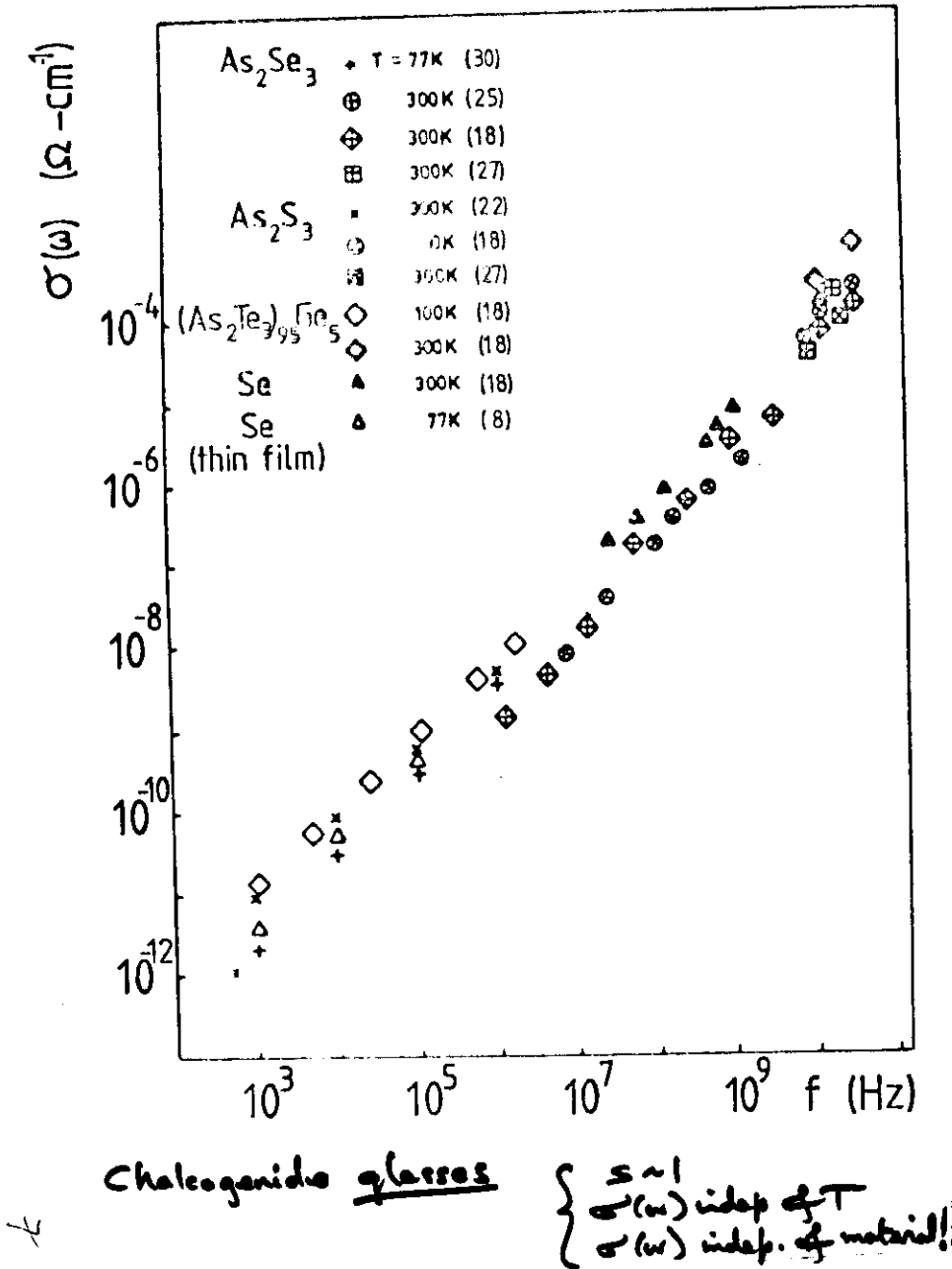
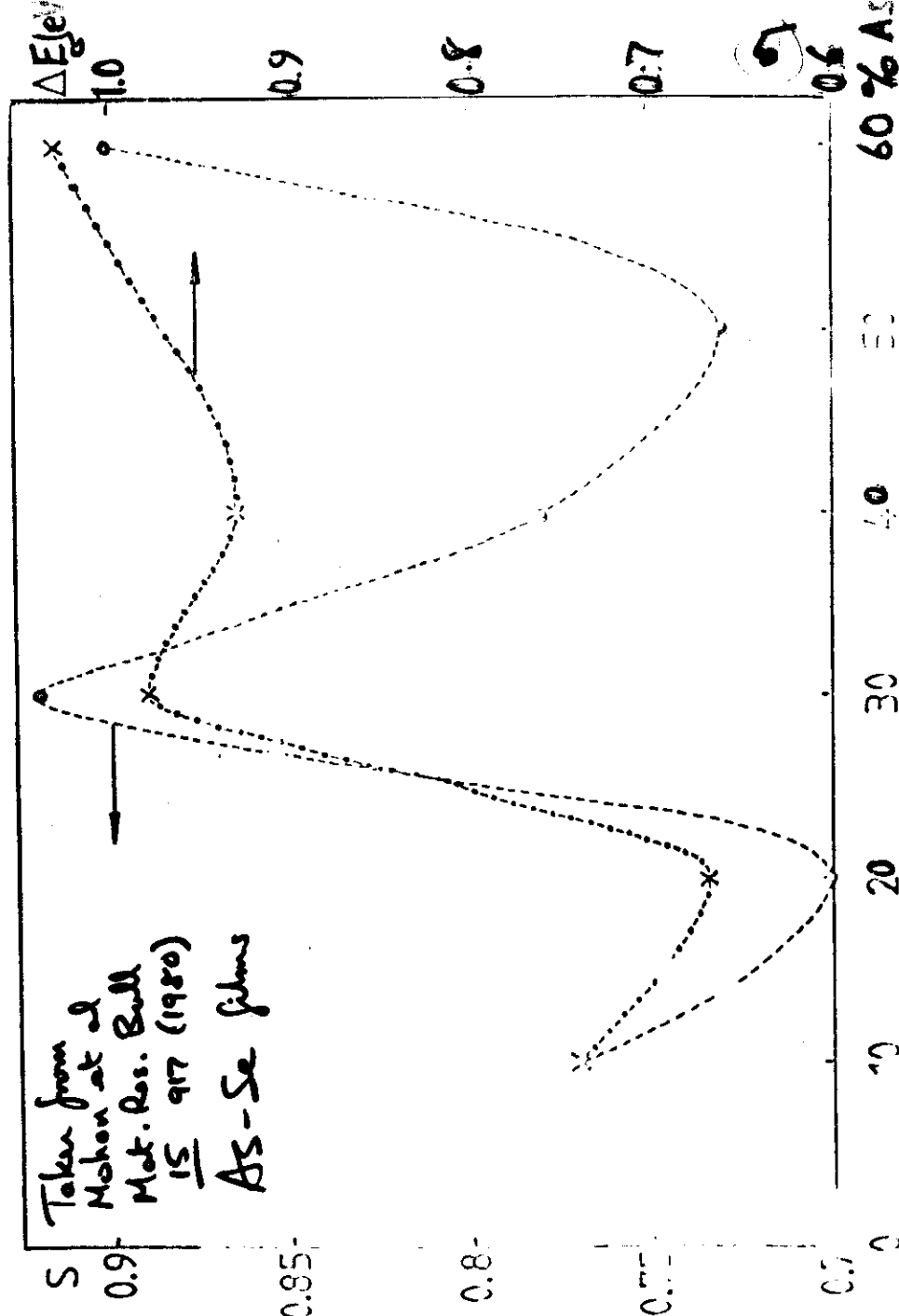


Thin films a-Se
Lakatos + Abkowitz Phys Rev 3 1791 (1971)

4



Lakatos + Abkowitz Phys Rev 3 1791 (1971)



Electric field $E(t) = E \sin \omega t \rightarrow$ polarization $\overset{7}{P(t)}$
 $P(\omega) = \epsilon_0 \chi(\omega) E(\omega)$
 susceptibility $= \chi'(\omega) - i \chi''(\omega)$
 dielectric loss

$$\sigma(\omega) = \epsilon_0 \omega \chi''(\omega)$$

For a Debye response (osc. charge or dipole time constant τ)

$$\chi''(\omega) = \chi(0) \frac{\omega \tau}{1 + \omega^2 \tau^2}$$

For a single τ , loss peak when $\omega \tau = 1$
 and $\sigma(\omega) \propto \omega^2$ for $\omega \tau \ll 1$

In non-cryst. systems there will be a distrⁿ of τ

$$\sigma(\omega) = \int_0^\infty \alpha n(\tau) \frac{\omega^2 \tau}{1 + \omega^2 \tau^2} d\tau$$

In QMT $\tau = \tau_0 \exp 2\alpha r$ with a spread in r (random distrⁿ)

In CBH $\tau = \tau_0 \exp(\frac{W}{kT})$ with W correlated with r

Pair approximation: $\alpha =$ polarisability of a pair of sites

$$\begin{array}{c} \Delta \uparrow \\ \leftarrow r \rightarrow \end{array} = \frac{e^2 r^2}{12 kT \cosh^2(\Delta/2kT)} \text{ for bipolarons}$$

Integrate Δ over the range $0 - \Delta_0$ assuming a flat distribution $\rightarrow$ factor $\frac{2kT}{\Delta_0} \tanh(\frac{\Delta_0}{2kT})$

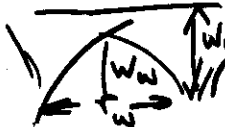
Integrate over a random distrⁿ of r
 $dp(r) = 4\pi N r^2 dr$

$$\sigma(\omega) = \frac{N}{2} \frac{2kT}{\Delta_0} \tanh(\frac{\Delta_0}{2kT}) \omega \int \frac{e^2 r^2}{3kT} \frac{\omega \tau}{1 + \omega^2 \tau^2} 4\pi r^2 dr$$

$\frac{N}{2} =$ no. of hopping pairs of electrons

Change integration variable $r \rightarrow W$
 $dW = \frac{2e^2}{\pi \epsilon_0 r^2} dr$

$$\text{to find } \sigma(\omega) = \frac{\pi}{3} N^2 \epsilon_0 \frac{kT}{\Delta_0} \tanh(\frac{\Delta_0}{2kT}) \omega r_\omega^6$$

$$\text{where } r_\omega = \left(\frac{2e^2}{\pi \epsilon_0} \right) \frac{1}{W_m - W_\omega} \quad \text{and } W_\omega = kT \ln \left(\frac{1}{\omega \tau_0} \right)$$


$$(W_m - W_\omega)^{-6} \rightarrow \frac{1}{W_m^6} \left(\frac{1}{\omega \tau_0} \right)^6 \exp \left[3 \left(\frac{kT}{W_m} \right)^2 \ln^2 \left(\frac{1}{\omega \tau_0} \right) \right]$$

(exact to 2nd order)

$$\sigma(\omega) \approx \frac{\pi}{3} N^2 \epsilon_0 \frac{kT}{\Delta_0} \tanh(\frac{\Delta_0}{2kT}) \left(\frac{2e^2}{\pi \epsilon_0 W_m} \right)^6 \frac{\omega^s}{\tau_0^\beta}$$

$$\text{where } s = 1 - \beta$$

$$\text{and } \beta = \frac{6kT}{W_m}$$

Now $W_m \sim \text{band gap } B$

$$\therefore G(\omega) \propto B^{-6}$$

$$s = 1 - \frac{6kT}{B}$$

$$\left. \begin{aligned} &= 0.85 \text{ for } B = 1 \text{ eV} \\ &= 0.93 \text{ for } B = 2 \text{ eV} \end{aligned} \right\} \text{ at RT}$$

Plot of $\ln[G(\omega) \sqrt{s/N^2}]$ vs $\ln B$ should have slope of -6

(see slide - slope = -6.3)

$G(\omega)$ vs $G(0)$ - see van-graph

RANDOM curve assumes N constant
- data for films

PAIRED curve
- data for glasses

$$G(r) = 4\pi N r^2 \exp\left(-\frac{4\pi N r^3}{3}\right) \exp\left(\frac{e^2}{4\pi\epsilon_0 k T_g r}\right)$$

IVAPs

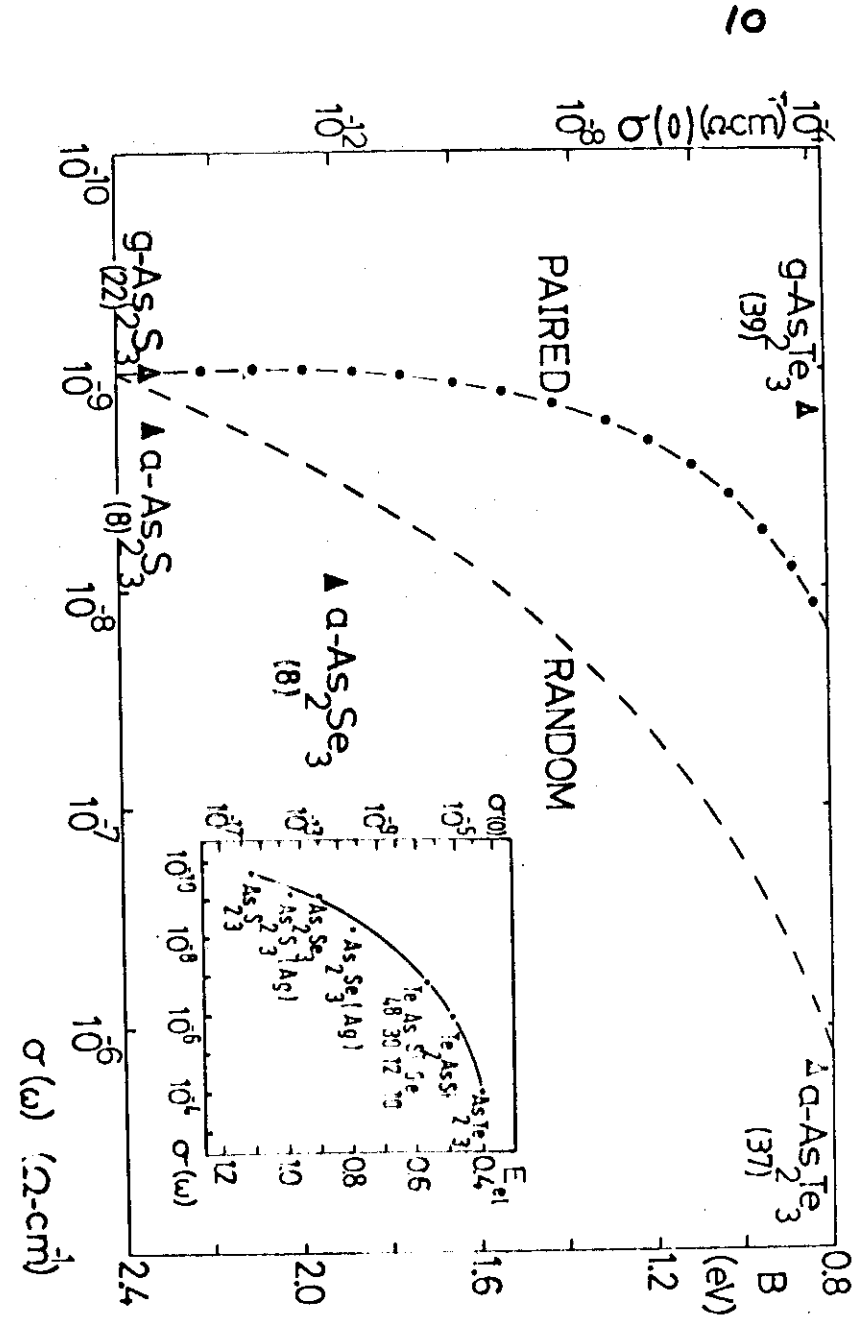
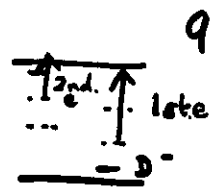
$$T_g = \text{glass transition temp.} \\ (\tau_{\min} = 4.5 \text{ \AA}) \quad S = 1 - \beta + \delta, \quad \delta = \frac{1}{k} \frac{d\ln G}{d\ln \omega}$$

(i) Shimakawa (Grenoble conference) 1981 (1982) $\rightarrow$ de Physique

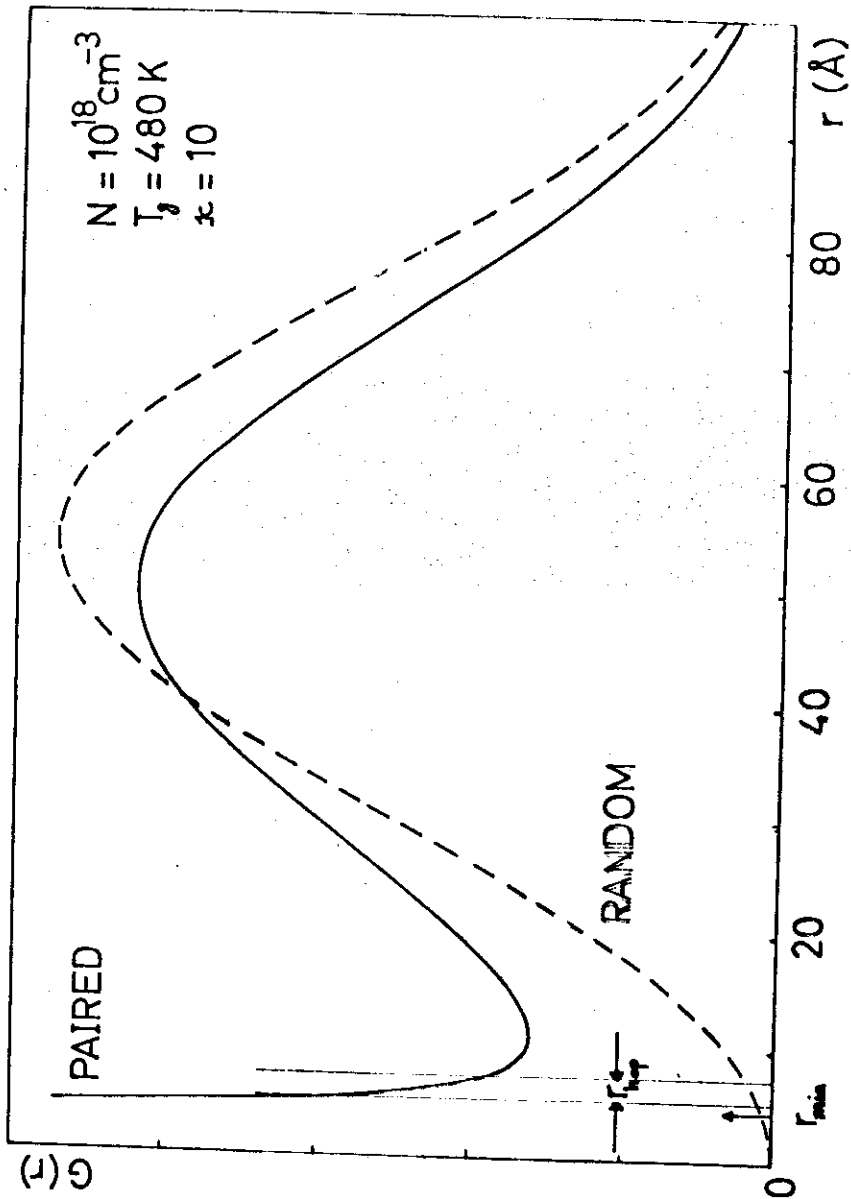
has extended this to case where D 's are thermally created

(ii) Long + Balkan (Phil Mag B41 287 1980)
- a-Ge

- a-Si:H



11



11

12

④ Defects in Group-V materials

As, P, Sb

$\alpha\text{-Ge}$ $\alpha\text{-Si}$ $\alpha\text{-III-V}$ 4-fold rigid v.b. sp^3 bonds defects dangling bonds +ve U $T^{1/4}$ ESR $G(\omega)$ QMT?	$\alpha\text{-Si:H}$ $\geq \text{Si-H}$ $\geq \text{Si-CH}$ → -ve U? No $T^{1/4}$ No ESR $G(\omega)$ CBH	$\alpha\text{-Se}$ $\alpha\text{-As}_2\text{Se}_3$ $\alpha\text{-SiO}_2$ essentially 2-fold flexible lone-pair non-bonding charged paired defects VAP IVAP -ve U No $T^{1/4}$ No ESR $G(\omega)$ CBH
---	---	--

¹³
Defects in Group-V materials

1. Davis in Topics in Applied Physics
Vol 36 "Amorphous Semiconductors"
M.H. Brodsky (Ed) 1979

2. Elliott + Davis J Phys C 12 2577
(1979)

3. Davis J Phys Soc Japan 49
1139 (1980)

4. Davis J de Physique C4-855
42 (1981)

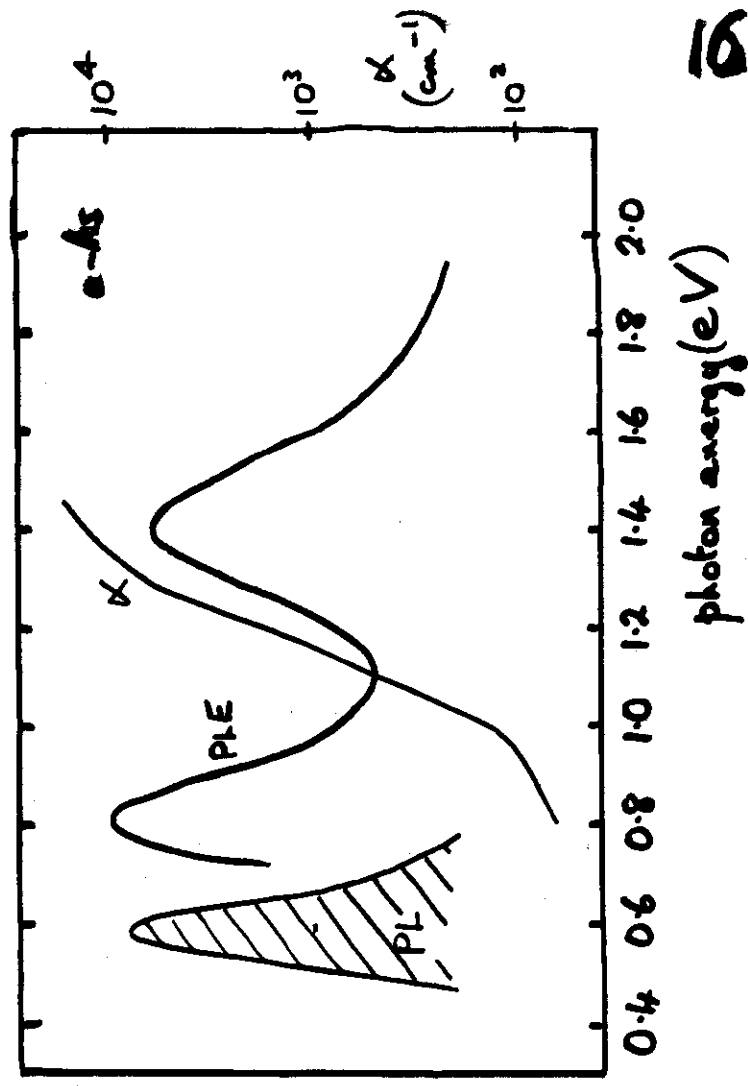
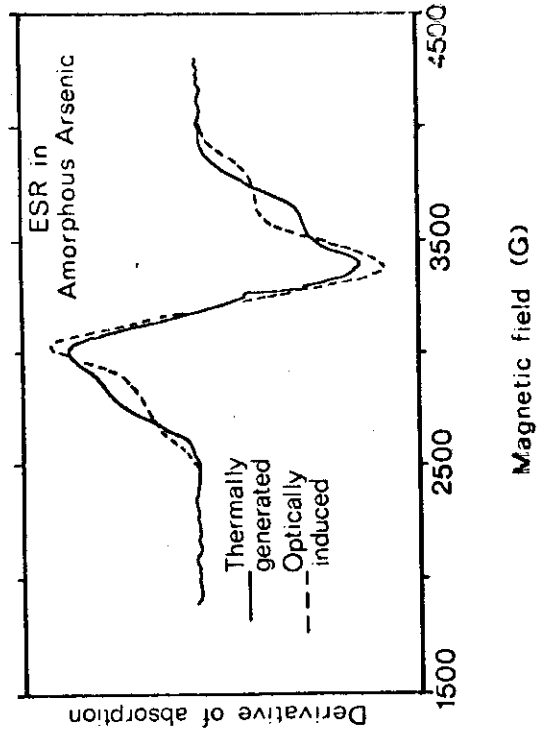
5. Farol + Davis " C4-571

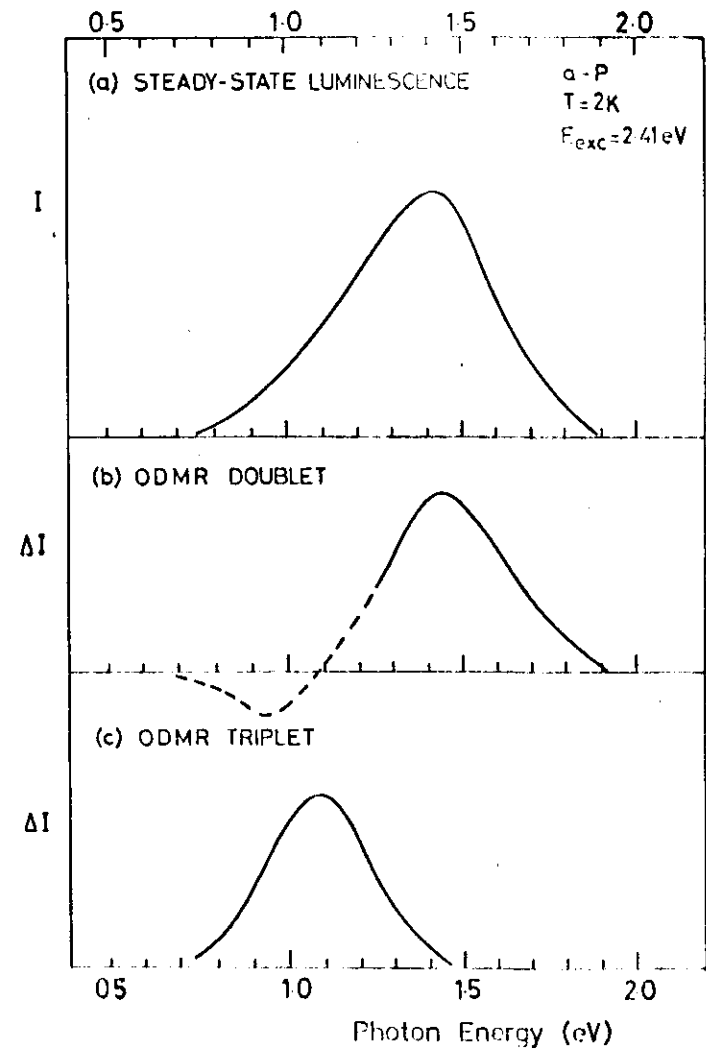
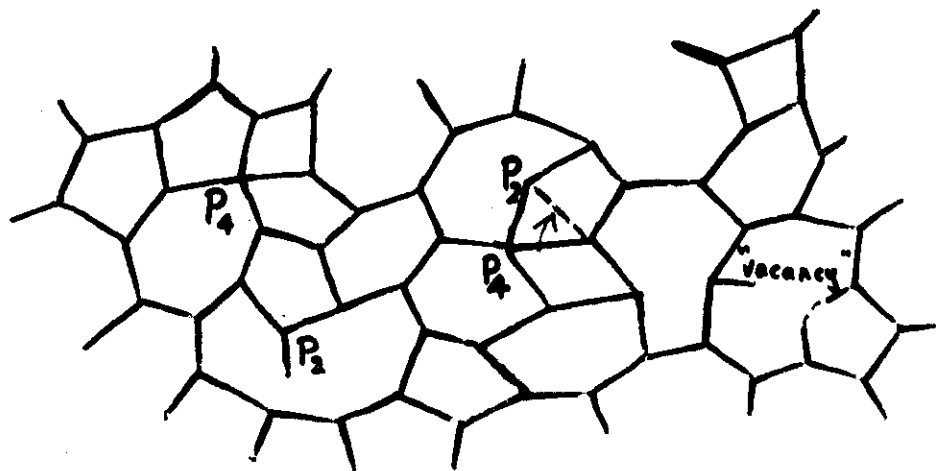
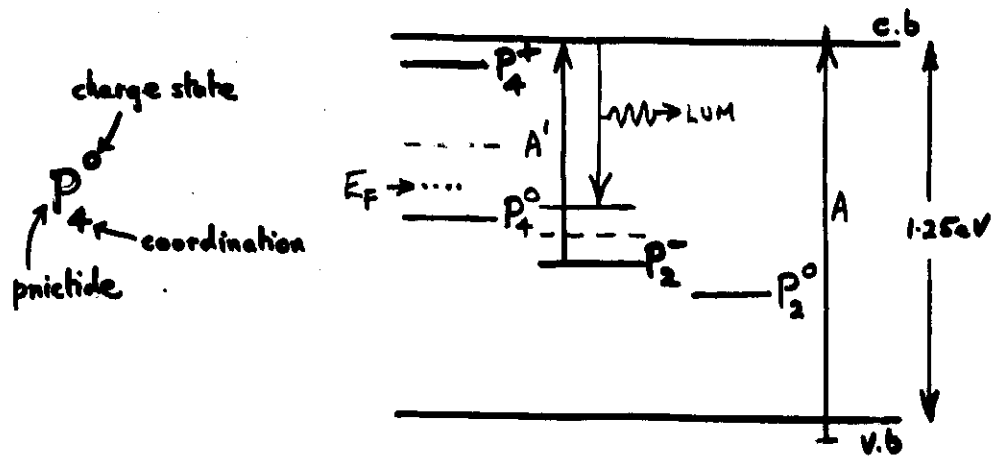
6. Japina + Cavallett Solid State Comm.
40 813 (1981)

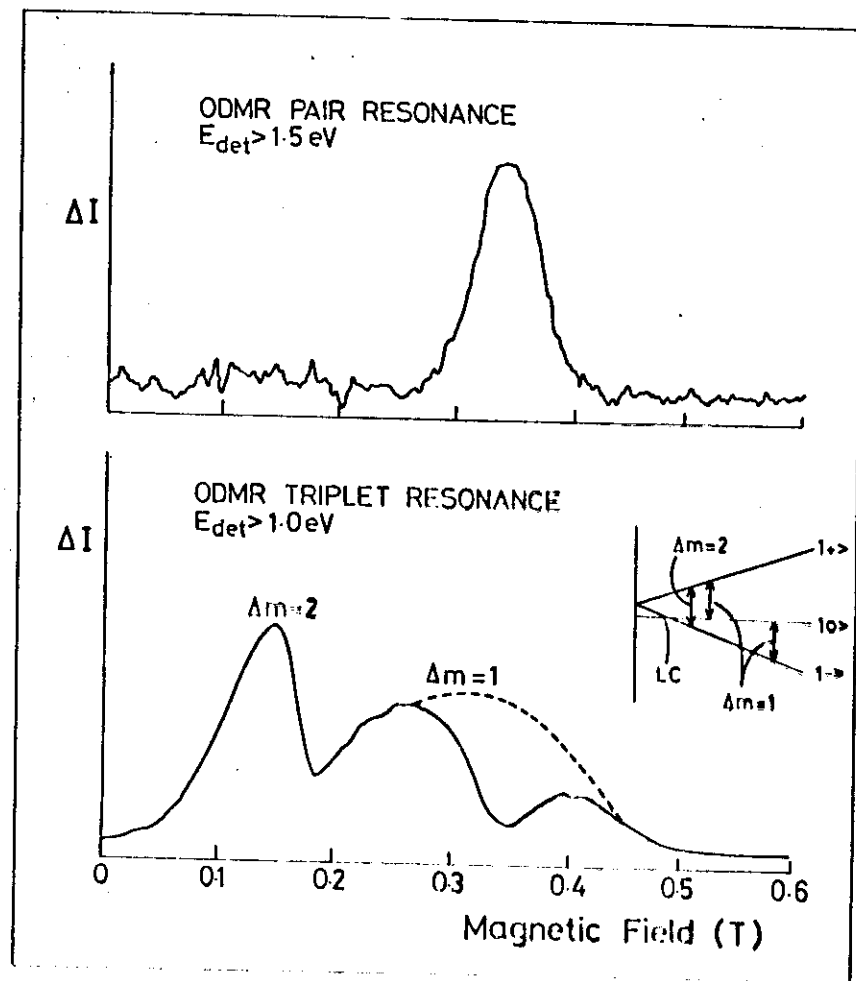
7. Pollard + Ioannopoulos Phys Rev B19
4217 (1979) B21 760 (1980)

¹⁴
8. O'Reilly Phil Mag B43 579
(1981)

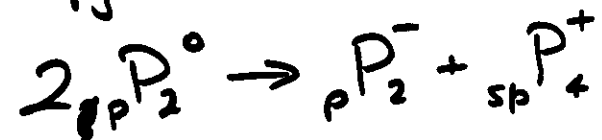
9. Kastner + Fritzsche Phil Mag
B37 199 (1978)







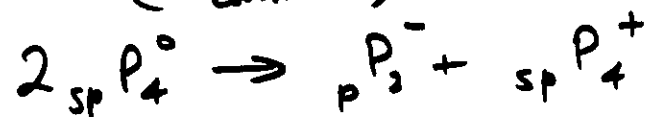
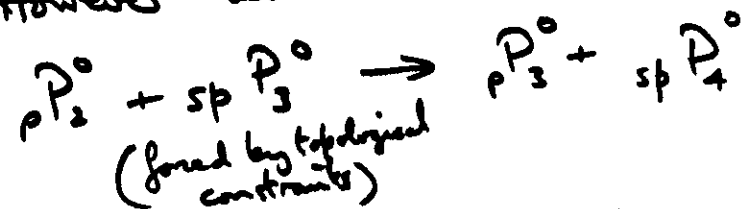
Analogy with chalc

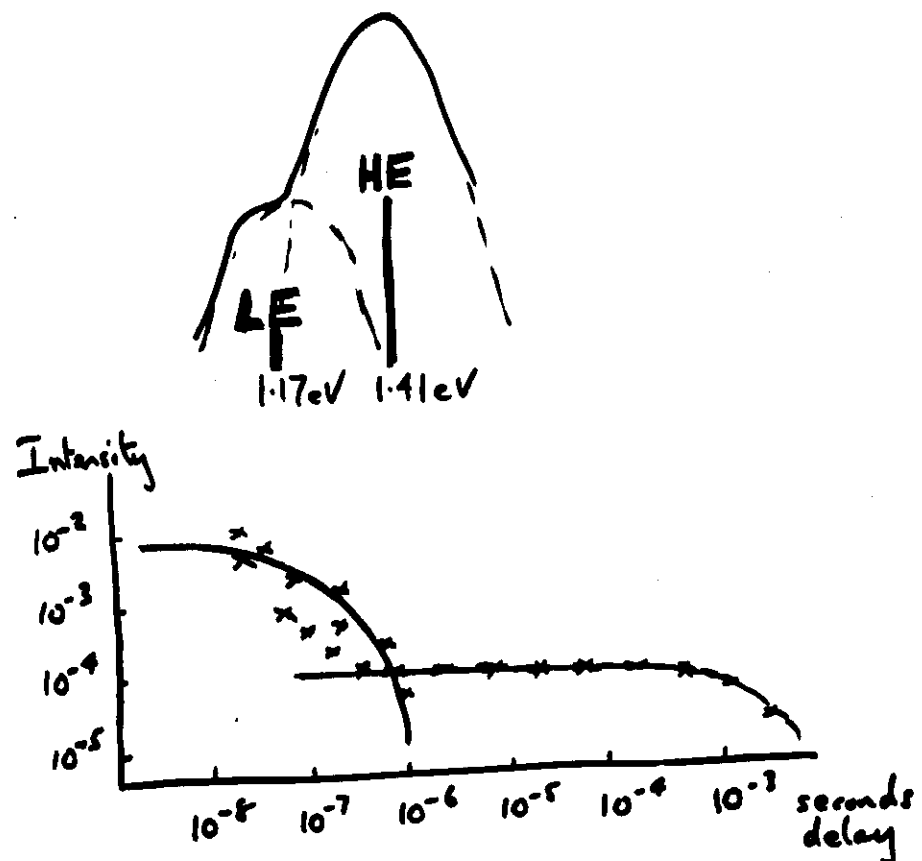


— probably not exothermic
because of large hybridisation
energy ~0.8 eV required

However in certain configurations
might be favourable but
in which case back reaction
easy — weak temp. dependent
dark esr signal (NRL)?

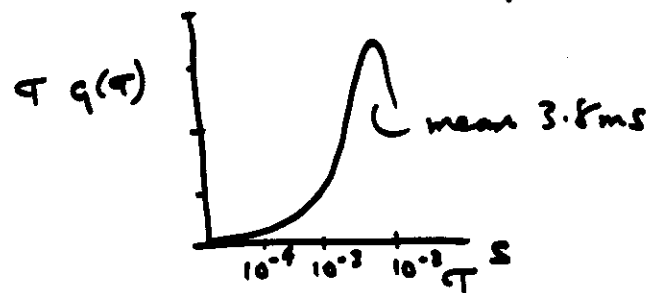
However other route is



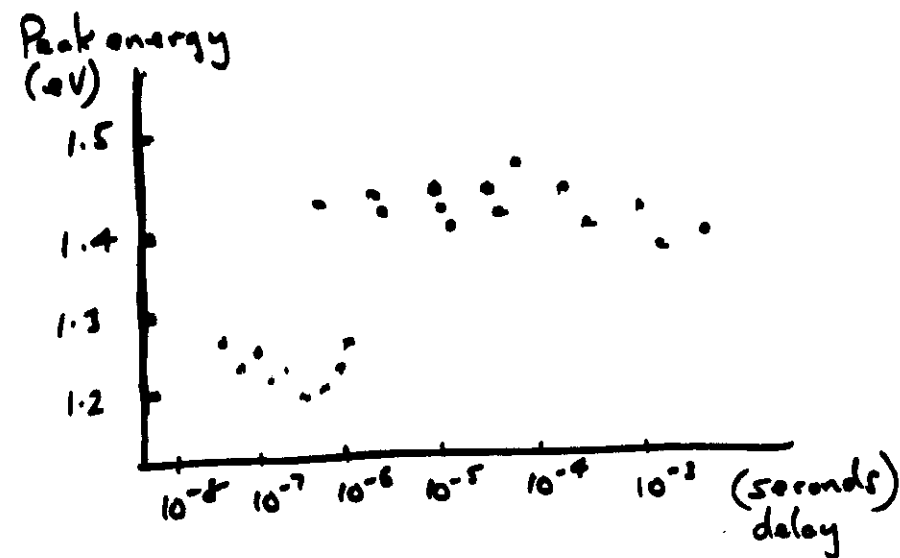


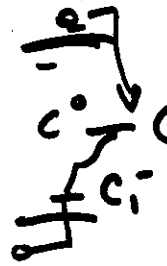
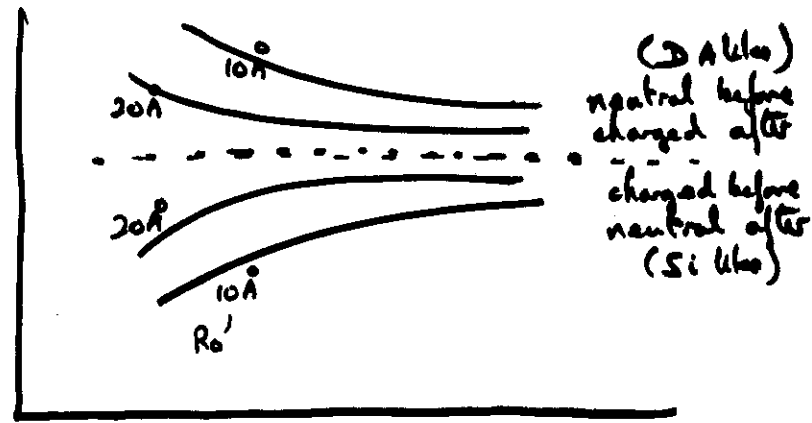
Single exponential
 $\tau = 152 \text{ ns}$

convolution of exponentials
 with distribution of lifetimes



TIME-RESOLVED SPECTROSCOPY ON a-P





Coulomb terms

$$E = \frac{e^2}{4\pi\epsilon\epsilon_0 r}$$

Radiative tunnelling $\tau = \tau_0 \exp(2r/R_0)$

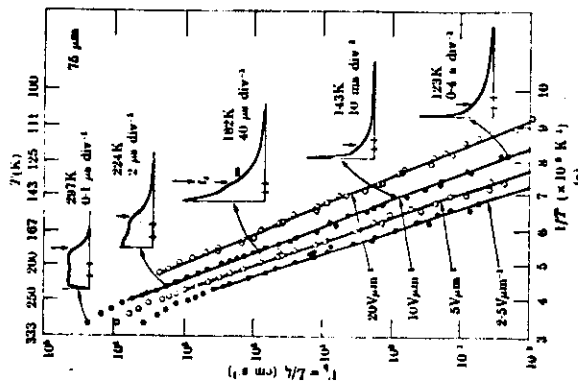
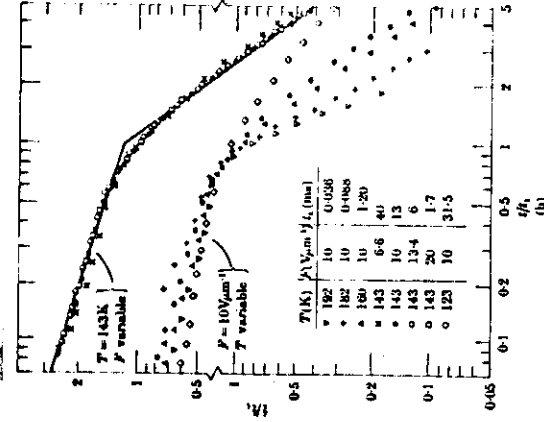
electron



hole

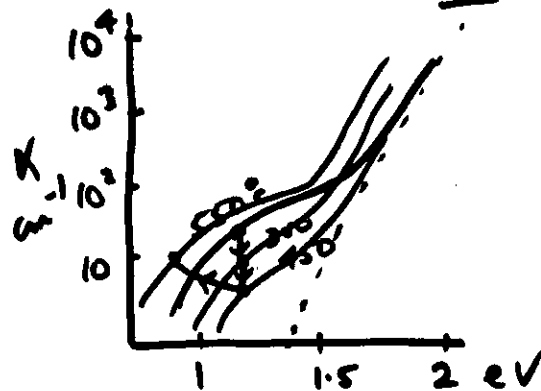
DA recⁿboth neutral before recⁿ

both charged after "

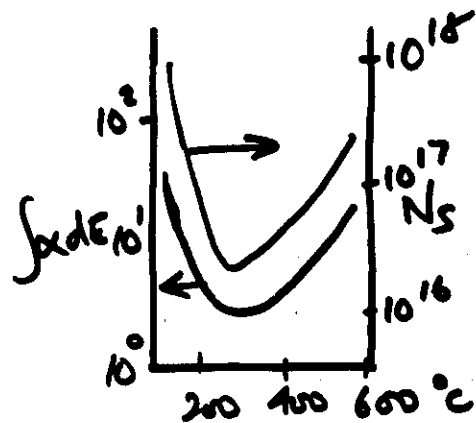


(a) Temperature dependence of hole drift velocity in amorphous selenium at various values of electric field. The shape of the current transients at various temperatures are illustrated; the arrows indicate transit times. (b) (p. 252) Current transients plotted on a log-log basis for various values of temperature and electric field F . The scales have been normalized to illustrate the scaling with respect to the transit time. (From Phila 1976.)

Yamasaki et al ²⁵ J. de Physique
42 C4-297 (1981)

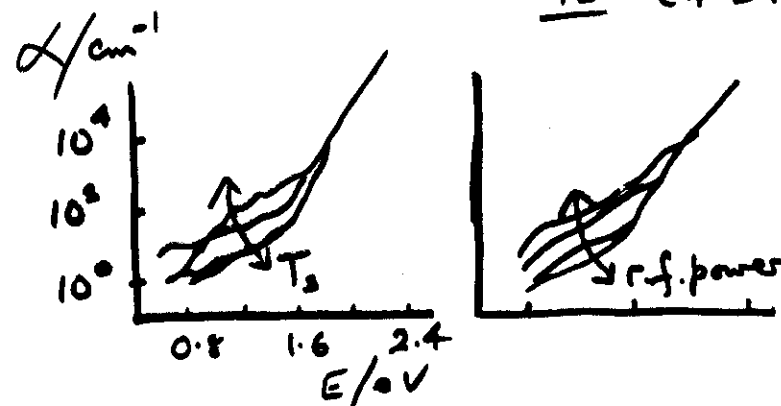


a-Si:H

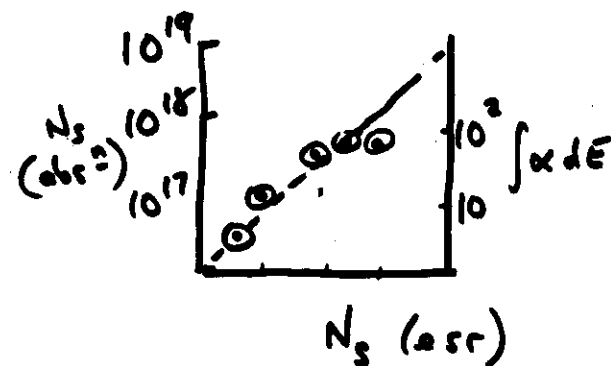


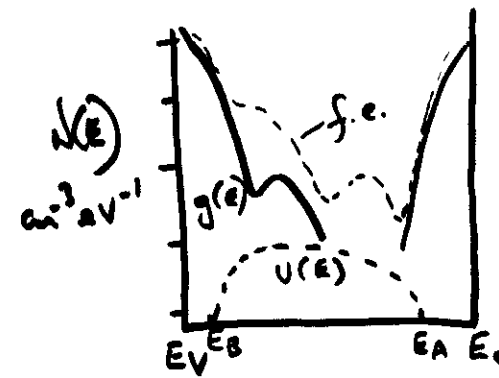
Photoacoustic spectroscopy

Jackson Amer ²⁶ J. de Physique
42 C4-293 (1981)



Photothermal deflection spectroscopy PDS
(Abs. $\Rightarrow$ heating $\Rightarrow$ change of n of adjacent
thin layer of liquid - detected by probe beam)





Schweitzer et al
 J. de Physique
42 c4-827
 (1981)