

*SUMMER SCHOOL ON PARTICLE PHYSICS*

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THE STANDARD MODEL AND HIGGS PHYSICS

Lecture V

W. MARCIANO  
Dept. of Physics  
Brookhaven National Lab.  
Upton, NY  
U.S.A.



## 7.) Higgs Phenomenology

For a nice review, see: S. Dawson hep-ph/9901280  
Trieste Lectures

Basic Parameters of the Standard Model include  $\lambda_0, v_0$   
 and many Yukawa Couplings ( $\sim 72$  parameters).

↓

$m_H, m_W$  or  $m_Z$ , all fermion masses & mixing  
 (modulo neutrino see-saw)

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \omega_1 + i\omega_2 \\ H + v_0 + i\eta \end{pmatrix} \quad \omega_1^+, \eta \text{ isotriplet}$$

$$\mathcal{L}_\phi = \left| \left( \frac{g_2}{2} \sigma^i W^i + i \frac{g_1}{2} B \right) \phi \right|^2 + \frac{1}{2} \mu_0^2 \phi^\dagger \phi - \lambda_0 (\phi^\dagger \phi)^2$$

$$\frac{-G_{ij} \bar{L}_j \phi R_i + \text{h.c.}}{\quad} \quad \frac{-\tilde{G}_{ij} \bar{L}_j \tilde{\phi} R_i + \text{h.c.}}{\quad} \quad \tilde{\phi} = \frac{1}{\sqrt{2}} \begin{pmatrix} H + v_0 - i\eta \\ -\omega_1 + i\omega_2 \end{pmatrix}$$

$$\left. \begin{matrix} e, \mu, \tau \\ d, s, b \end{matrix} \right\} \text{ masses} \quad \left. \begin{matrix} \nu_1, \nu_2, \nu_3 \\ u, c, t \end{matrix} \right\} \text{ masses}$$

$$V(\phi) = -\lambda_0 \left( \phi^\dagger \phi - \frac{\mu_0^2}{2\lambda_0} \right)^2$$

identify as  $\frac{1}{2} v_0^2$  (see later discussion)

$$m_H^2 = 2\lambda_0 v_0^2$$

$$m_W^2 = g_2^2 v_0^2 / 2$$

$$\rightarrow v_0 \simeq 247 \text{ GeV} \rightarrow \underline{m_H \simeq 350\sqrt{2} \text{ GeV}}$$

SM contains 3 massless Goldstone bosons  $w^{\pm}, z$  which become  $W_L^{\pm}, Z_L$  in the unitary gauge & H = Higgs Scalar.

$$\left. \begin{array}{l} \underline{m_H > 114.4 \text{ GeV}} \quad \text{LEP II Bound} \\ \underline{m_H \lesssim 185 \text{ GeV}} \quad \text{Precision Loop Tests} \end{array} \right\} \begin{array}{l} \text{Relatively} \\ \text{Light} \end{array}$$

Other reasons to believe light Higgs?

$\lambda\phi^4$  is a trivial theory (non-interacting) on its own. Given a value of  $\lambda(\mu)$  at high  $\mu$ , it gets screened to zero at low  $\mu$ .

Lattice  $\rightarrow m_H < 640 \text{ GeV}$  avoid triviality

Alternative  $\frac{d\lambda}{dt} = \frac{3\lambda^2}{4\pi^2} \quad t = \ln Q^2/Q_0^2, \quad \lambda = \frac{m_H^2}{2v}$

$$\lambda(Q) = \frac{\lambda(Q_0)}{\left[ 1 - \underbrace{\frac{3\lambda(Q_0)}{4\pi^2} \ln Q^2/Q_0^2}_{\text{Landau Pole}} \right]}$$

Require  $\lambda(\Lambda)$  stay finite up to scale  $\Lambda$  (large)

$$m_H^2 < \frac{8\pi^2 v^2}{3 \ln(\Lambda^2/v^2)}$$

$$\begin{array}{l} \underline{\Lambda \approx 10^{16} \text{ GeV} \rightarrow m_H < 160 \text{ GeV}} \quad (1706 \text{ GeV}) \\ \underline{\Lambda \approx 3 \text{ TeV} \rightarrow m_H < 600 \text{ GeV}} \quad \text{other int.} \end{array}$$

The larger  $m_H$  turns out to be, the closer "new physics"

One scenario,  $\Lambda \sim O(\text{TeV})$ ,  $m_H \sim O(\text{TeV})$  and newphys  $O(\text{TeV})$

Precision Loops Nullified by strong coupling

Vacuum Stability  $\lambda > 0$  (Potential Unbounded Below)  
all the way to  $10^{16}$  validity

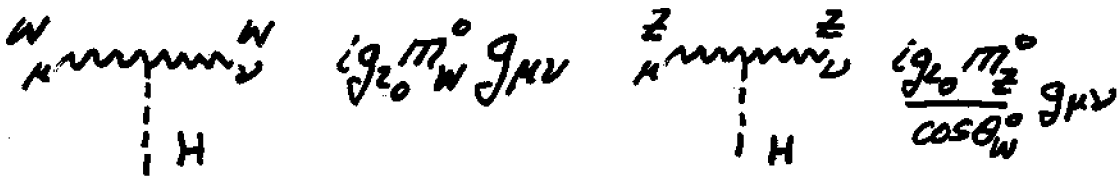
$$\underline{m_H > 130 \text{ GeV} !}$$

This is interesting since in SUSY, the lightest Higgs

$$\underline{m_h \lesssim 130 \text{ GeV}}$$

Higgs Decay Properties Depend on its mass

Heavy Higgs  $m_H > 2m_W$  or  $2m_Z$   $H \rightarrow W^+W^- (ZZ)$   
Dominate



$$\mathcal{M}(H \rightarrow W^+W^-) = ig_2 m_W \epsilon_\mu(k_1) \epsilon^\mu(k_2)$$

$$\sum_{\text{pol}} |\mathcal{M}|^2 = g_2^2 m_W^2 \left( g_{\mu\nu} - \frac{k_{1\mu} k_{1\nu}}{m_W^2} \right) \left( g^{\mu\nu} - \frac{k_2^\mu k_2^\nu}{m_W^2} \right)$$

use  $(k_1 + k_2)^2 = m_H^2$  Integrate over phase-space  
exercise

$$\Gamma(H \rightarrow W^+ W^-) = \frac{g_2^2}{64\pi} \frac{m_H^3}{m_W^2} \left(1 - \frac{4m_W^2}{m_H^2}\right)^{1/2} \left(1 - 4\frac{m_W^2}{m_H^2} + 12\frac{m_W^4}{m_H^4}\right)$$

$$\Gamma(H \rightarrow Z Z) = \frac{g_2^2}{128\pi} \frac{m_H^3}{m_W^2} \left(1 - \frac{4m_Z^2}{m_H^2}\right)^{1/2} \left(1 - 4\frac{m_Z^2}{m_H^2} + 12\frac{m_Z^4}{m_H^4}\right)$$

Note that these decay widths grow as  $m_H^3$ ! (not  $m_H$ )

Leading Term  $\Gamma(H \rightarrow Z Z) = \frac{1}{2} \Gamma(H \rightarrow W^+ W^-)$  isospin rel.

$\Gamma_H(m_H \approx 1 \text{ TeV}) \approx 500 \text{ GeV}$  Very Broad drops fast for lighter Higgs

What if  $m_H < 2m_W$  (160 GeV) But not too light

$H \rightarrow W W^*$  ( $W^* = \text{virtual } W$ ) Dominates



$$\Gamma(H \rightarrow W W^*) \sim \frac{3g^4 m_H}{512\pi^3} \times \mathcal{O}(1)$$

dominant decay for  $m_H \gtrsim 130 \text{ GeV}$

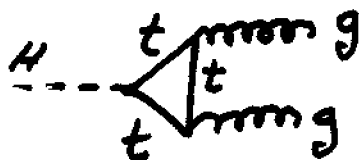
Higgs narrow  $\Gamma_H \sim 10 \text{ MeV}$

For  $m_H \lesssim 130 \text{ GeV}$   $H \rightarrow b\bar{b}$  dominates

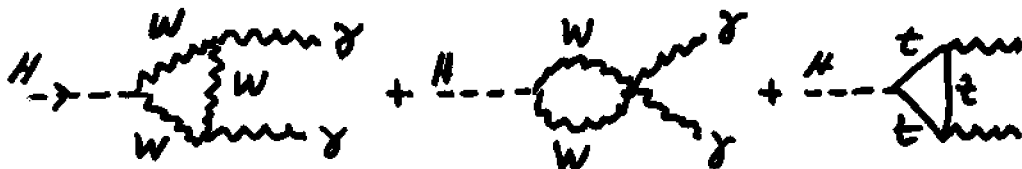
$$\frac{-ig_2 m_F^0}{2m_W^0} \rightarrow \Gamma(H \rightarrow F\bar{F}) = (3) \frac{g_2^2 m_F^2 m_H}{32\pi m_W^2} \left(1 - \frac{4m_F^2}{m_H^2}\right)^2$$

↑  
Color

Interesting loop induced decays

$H \rightarrow gg$    $\sim \alpha_s(m_H)$  suppression

BR  $\sim$  Few % For  $m_H < 150 \text{ GeV}$

$H \rightarrow \gamma\gamma$  

BR  $\sim 10^{-3}$  for  $m_H < 150 \text{ GeV}$

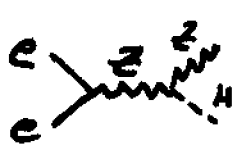
$H \rightarrow \gamma\gamma$  Very Clean but requires high statistics.

$gg \rightarrow H$  Dominant Production Mechanism at LHC

Higgs Discovery and Study Strategy Depends on Mass

Golden Decay  $H \rightarrow ZZ \rightarrow \begin{matrix} \ell^+ \ell^- \\ \ell^+ \ell^- \end{matrix} \} 4 \text{ leptons}$

Past Search:  $e^+e^- \rightarrow ZH \rightarrow b\bar{b}$   $m_H > 114.4 \text{ GeV}$  at LEP II



Current  $p\bar{p} \rightarrow WH + X$  at the Tevatron  
 $ZH$

Need  $\gtrsim 10 \text{ fb}^{-1}$  to cleanly discover expect  $\lesssim 8 \text{ fb}^{-1}$  (borderline)

Future LHC (2007-2008)

For  $m_H \lesssim 200 \text{ GeV}$ , study

Measure some BR.  $\sim \pm 10\%$

$\Gamma_H \sim \pm 10-25\%$

$$gg \rightarrow H \rightarrow \gamma\gamma$$

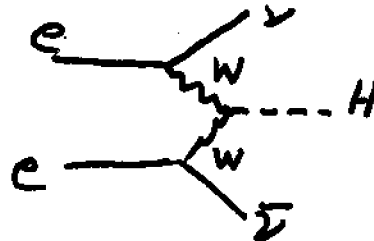
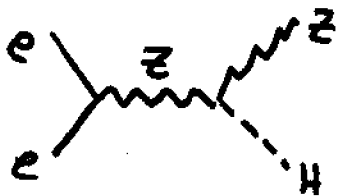
$$gg \rightarrow H \rightarrow WW^*, ZZ^*$$

$$gg \rightarrow t\bar{t}H \rightarrow b\bar{b}, WW^*, \gamma\gamma$$

etc

Precision Higgs Studies

$e^+e^-$  Linear Collider (250-500 GeV)



$\Gamma_H \sim \pm 5\%$ , Coupling  $HWW, HZZ, Ht\bar{t}, Hb\bar{b}, H\tau^+\tau^-, Hgg, H\gamma\gamma$   
 $\pm 5\%$

Higher Energy Study  $HH$  production - Measure  $\lambda$

If the Higgs is narrow, sit at resonance

$$\gamma\gamma \rightarrow H \text{ or } \mu^+\mu^- \rightarrow H$$

use polarization?



## Electroweak Equivalence Theorem

At very high energies,  $W^\pm + Z$  interactions are equivalent to  $\omega^\pm + \gamma$  Goldstone Bosons up to corrections of  $\mathcal{O}(\frac{m_W^2}{s})$ .

Example: Loop Corrections to  $H \rightarrow W^+ W^-$  for  $m_H \gg m_W$

Remember  $\Gamma(H \rightarrow W^+ W^-) = \frac{g_2^2 m_H^3}{64\pi m_W^2} \left\{ 1 + \mathcal{O}\left(\frac{m_W^2}{m_H^2}\right) \right\}$

Consider the Higgs Lagrangian Alone

$$\omega = \frac{\omega_1 + i\omega_2}{\sqrt{2}}$$

$$\mathcal{L}_{\text{Higgs}} = -\lambda_0 \left( \omega^\dagger \omega + \frac{1}{2} g^2 + \frac{1}{2} H^2 + V_0 H + \underbrace{\frac{1}{2} V_0^2 - M_0^2 / 2\lambda_0}_{\text{leave } \neq 0 \text{ mass counter term}} \right)^2 + \text{KE. terms}$$

$$\lambda_0 = \frac{g_2^2 m_H^2}{8 m_W^2}$$

cancel tadpoles + Goldstone masses

Propagators:  $\text{---} \overset{H}{\text{---}} \text{---} \quad \frac{i}{p^2 - m_H^2}$

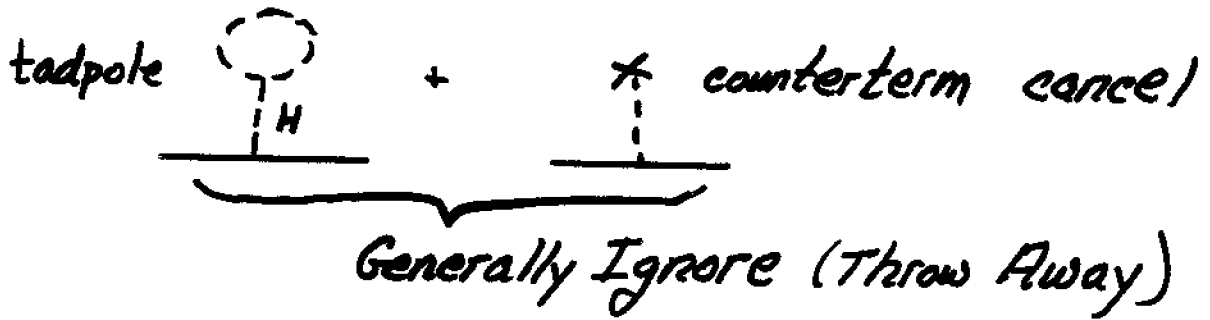
$\text{---} \overset{\omega, \gamma}{\text{---}} \text{---} \quad \frac{i}{p^2}$

$\begin{array}{c} \omega, \gamma \quad \omega, \gamma \\ \text{---} \quad \text{---} \\ | \\ H \end{array} \quad \frac{-i g_2^2 m_H^2}{2 m_W^2} \quad \rightarrow \quad \Gamma(H \rightarrow \omega^+ \omega^-) = \frac{g_2^2 m_H^3}{64\pi m_W^2} \quad \left. \vphantom{\frac{g_2^2 m_H^3}{64\pi m_W^2}} \right\} \text{as above}$

$\begin{array}{c} H \quad H \\ \text{---} \quad \text{---} \\ | \\ H \end{array} = -i \frac{3g_2^2 m_H^2}{2 m_W^2}$

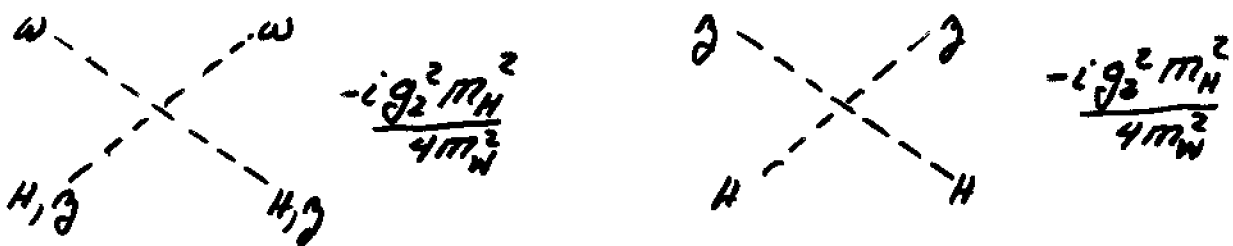
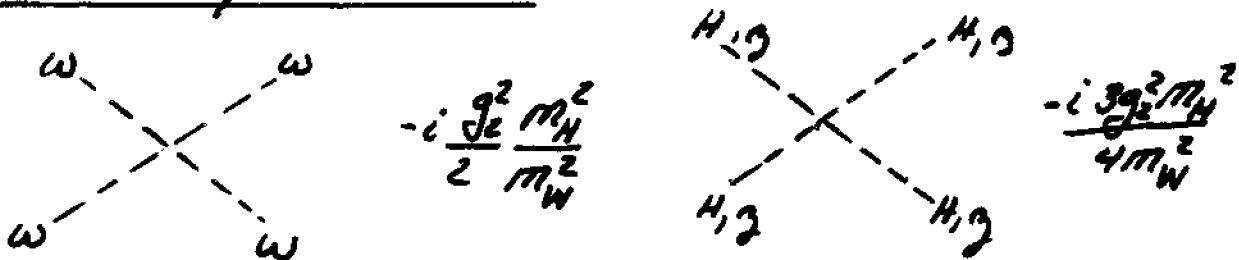
Use  $\mathcal{L} = -\frac{g^2 m_H^0{}^2}{8m_W^0{}^2} \left\{ W^+W + \frac{1}{2} Z^2 + \frac{1}{2} H^2 + \frac{2m_W^0}{g_{20}} H + \frac{2\delta T}{g_{20} m_H^0/m_W^0} \right\}^2$

$\delta T = \lambda_0 v_0 (v_0^2 - \mu_0^2 / \lambda_0)$  Tadpole Counterterm



Must Subtract Mass Counterterm From  $WW, ZZ, HH$

Other Feynman Rules



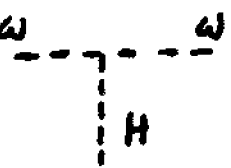
Counterterms

$m_H^0{}^2 = m_H^2 - \delta m_H^2$

$m_W^0{}^2 = m_W^2 - \delta m_W^2$

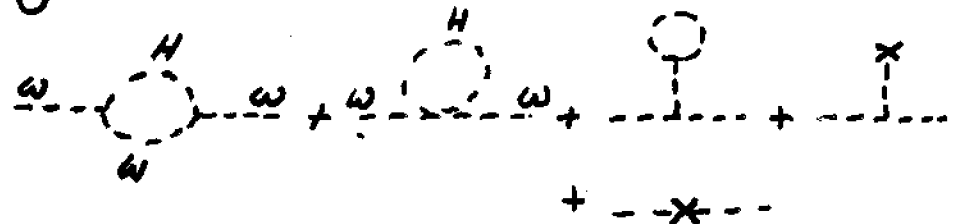
Subtract  $\pi(0)$  Goldstone Boson Self-Energy

Radiative Corrections  $H \rightarrow \omega \omega^-$   $m_H^2 \gg m_W^2$

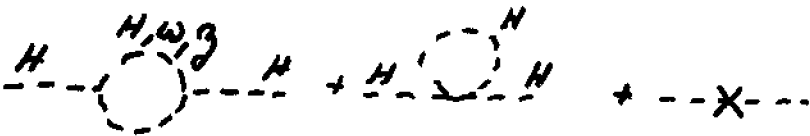
$\omega$    $\omega$   $\frac{i g_2^2 m_H^2}{2 m_W^2} = \frac{i g_2^2 m_H^2}{2 m_W^2} \left\{ 1 - \frac{\delta m_H^2}{m_H^2} + \frac{1}{2} \frac{\delta m_W^2}{m_W^2} \right\}$

$\frac{\delta m_W^2}{m_W^2} = \frac{g_2^2}{16\pi^2} \left( \frac{1}{8} \frac{m_H^2}{m_W^2} \right)$  Finite Mass Counterterm

Scalar Self-Energies

$\omega\omega$   $-i\pi(q^2) =$  

$-i\pi(0) = -i \frac{g_2^2}{16\pi^2} \frac{m_H^4}{m_W^2} \frac{3}{4} \left\{ \frac{1}{\epsilon-4} - \ln \frac{\mu}{m_H} - \frac{1}{2} \right\}$

$HH$   $-i\pi_H(q^2) =$  

$\pi(0)$  counterterm

$\delta m_H^2 = \text{Re} \pi_H(q^2) \Big|_{q^2=m_H^2} = \frac{g_2^2}{16\pi^2} \frac{m_H^2}{m_W^2} \left\{ 3 \left( \frac{1}{\epsilon-4} - \ln \frac{\mu}{m_H} \right) - 3 + \frac{9\pi}{8\sqrt{3}} \right\}$

$Z_W^{1/2} = 1 + \frac{g_2^2}{16\pi^2} \frac{m_H^2}{m_W^2} \left( -\frac{1}{16} \right)$

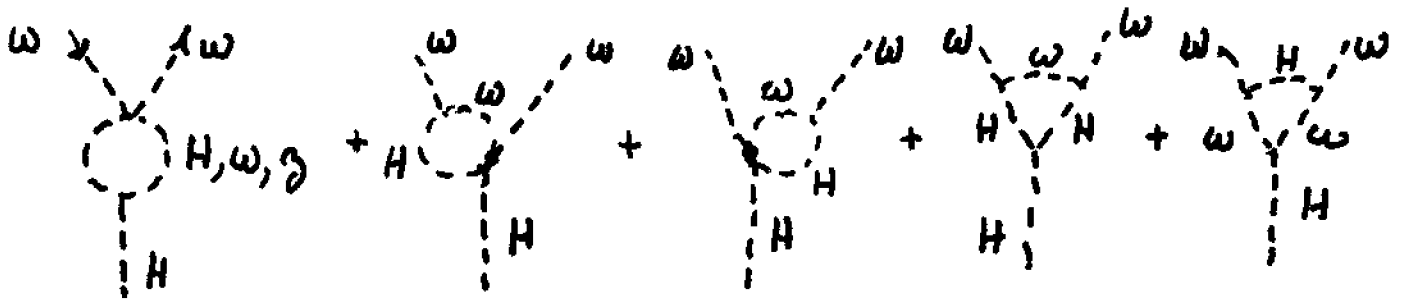
$Z_H^{1/2} = 1 + \frac{g_2^2}{16\pi^2} \frac{m_H^2}{m_W^2} \left( \frac{3}{4} - \frac{3\pi}{8\sqrt{3}} \right)$

$Z_H^{1/2} Z_W = 1 + \frac{g_2^2}{16\pi^2} \frac{m_H^2}{m_W^2} \left( \frac{3}{4} - \frac{3\pi}{8\sqrt{3}} - \frac{1}{8} \right)$   
 $\frac{5}{8} - \frac{3\pi}{8\sqrt{3}}$

Total  $\delta m_W^2, \delta m_H^2, Z_W, Z_H^{1/2}$

$$1 - \frac{g_2^2 m_H^2}{16\pi^2 m_W^2} \left( 3 \left( \frac{1}{\pi-4} - \ln \frac{M}{m_H} \right) - \frac{59}{16} + \frac{3\pi}{2\sqrt{3}} \right)$$

Proper Vertex Diagrams:



$$1 + \frac{g_2^2 m_H^2}{16\pi^2 m_W^2} \left\{ 3 \left( \frac{1}{\pi-4} - \ln \frac{M}{m_H} \right) - \frac{5}{2} + \frac{3\pi}{8\sqrt{3}} + \frac{5\pi^2}{48} \right\} \text{ divergence cancels}$$

$$\text{Total } -i \frac{g_2 m_H^2}{2 m_W^2} \left( 1 + \frac{g_2^2 m_H^2}{16\pi^2 m_W^2} \left( \frac{19}{16} - \frac{3\sqrt{3}\pi}{8} + \frac{5\pi^2}{48} \right) \right)$$

$$\Gamma(H \rightarrow \omega^+ \omega^-) = \frac{g_2^2 m_H^3}{64\pi m_W^2} \left( 1 + \frac{g_2^2 m_H^2}{8\pi^2 m_W^2} \left( \frac{19}{16} - \frac{3\sqrt{3}\pi}{8} + \frac{5\pi^2}{48} \right) \right)$$

0.175 cancellation

Even for  $m_H \approx 1 \text{ TeV}$ , Rad. Corr.  $\sim +15\%$

EW Equivalence Th. useful for strong WW scattering at H.E.

## 9.) Outlook & Conclusion

Standard Model Tested at Tree + Quantum Loop Levels  
Works to  $\pm 0.1\%$  EW Tremendous Success!

No Big Surprises Yet? (Heavy Top, Long  $\tau_b$ , Neutrino Mass + Mixing, ...)

### 3 Prong Exp. Assault

E. Colliders - LHC (pp at 14 TeV)  $\rightarrow$  Higgs (Finally)  
SUSY  
Other?

$e^+e^-$  LC - Precision Studies H,  $W^\pm$ , Z, SUSY  
 $m_t$  ...

Lower Energy:  $e^+e^-$  (?), Atomic P.V., ep,  $\nu_\mu e$  ...  
Precision Measurements

Rare Effects: Proton Decay, e.d.m.s,  $\mu \rightarrow e \gamma$ , ... Dark Matter...  
Revolutionary Neutrinos ...

You Can't Discover If You Don't Look

Good Luck