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international centre for theoretical physics

SMR: 1513/6

**10TH CONFERENCE ON HOPPING  
AND RELATED PHENOMENA**

( 1 - 4 September 2003)

***"Charge Carrier Properties below and above  
the Metal-Insulator Transition in Conjugated  
Polymers - Recent Results"***

presented by:

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University of Leiden  
The Netherlands

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These are preliminary lecture notes, intended only for distribution to participants.



# **Charge carrier properties below and above the MIT in conjugated polymers.**

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**In collaboration with:**

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Iulian Hulea (Leiden), Herman Jan Hupkes (Leiden),  
Frank Pasveer (Eindhoven), Thijs Michels (Eindhoven),  
A.K. Mukerhjee (Bangalore), Reghu Menon (Bangalore)**

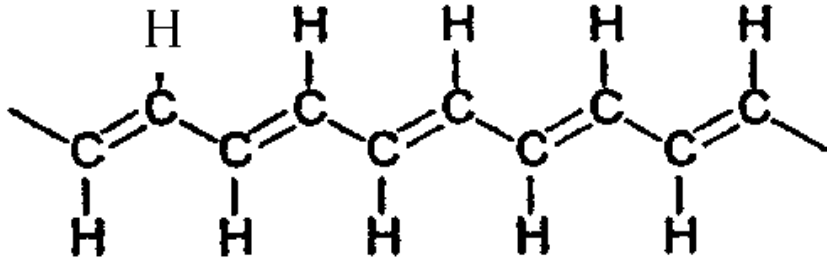
**References:**

**Martens et al., Phys. Rev. B. 67, 121203(R) (2003)**

**Romijn et al., Phys. Rev. Lett. 90, 176602 (2003)**

**HRP10, Trieste, September 4 2003**

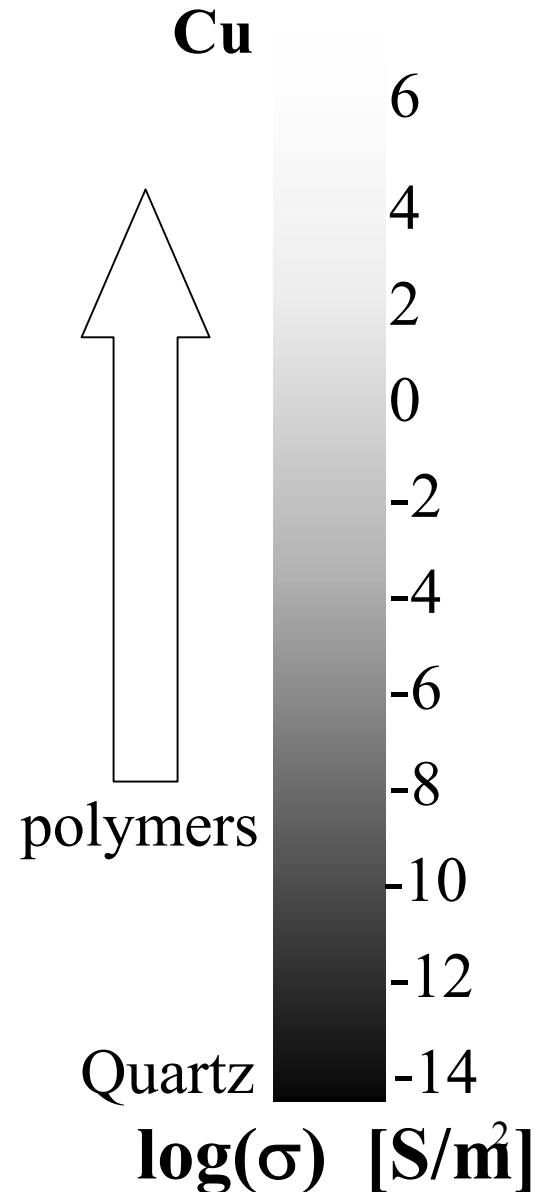
# Conducting polymers



polyacetylene  
doped with iodine

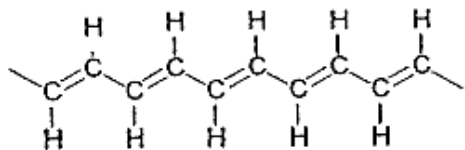
**1977 : Discovery of highly  
conducting polymers**

**2000 : Nobel prize in Chemistry  
A.Heeger, A.MacDiarmid  
and H. Shirakawa**

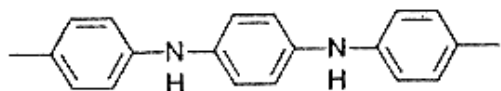


# What causes the conductivity?

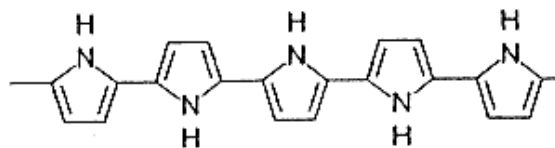
conjugated polymers



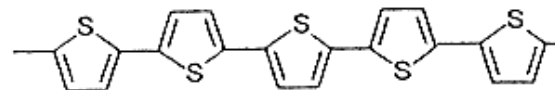
*polyacetylene*



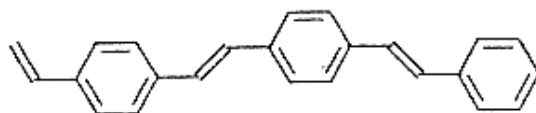
*polyaniline*



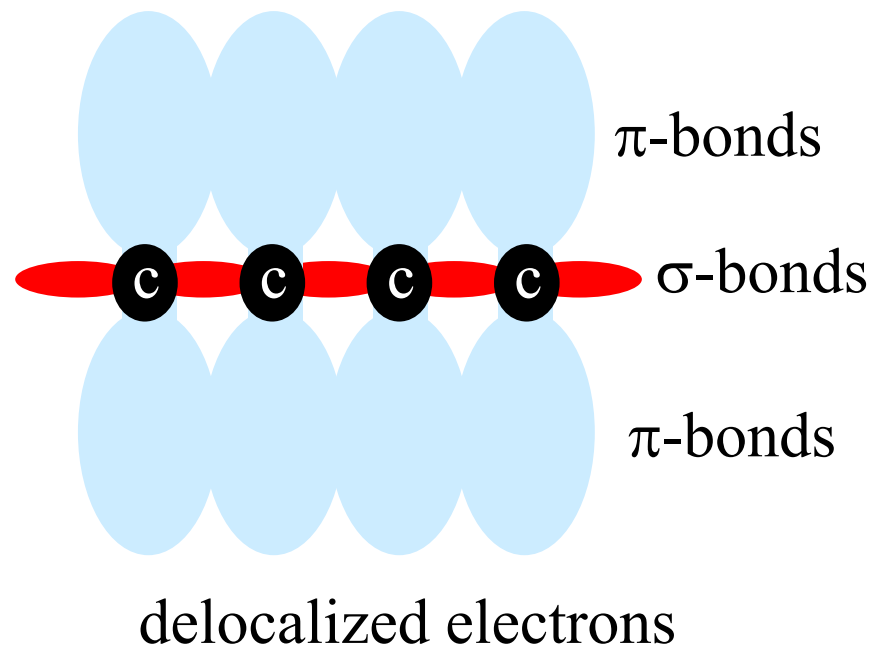
*polypyrrole*



*polythiophene*



*poly(phenylene-vinylene)*

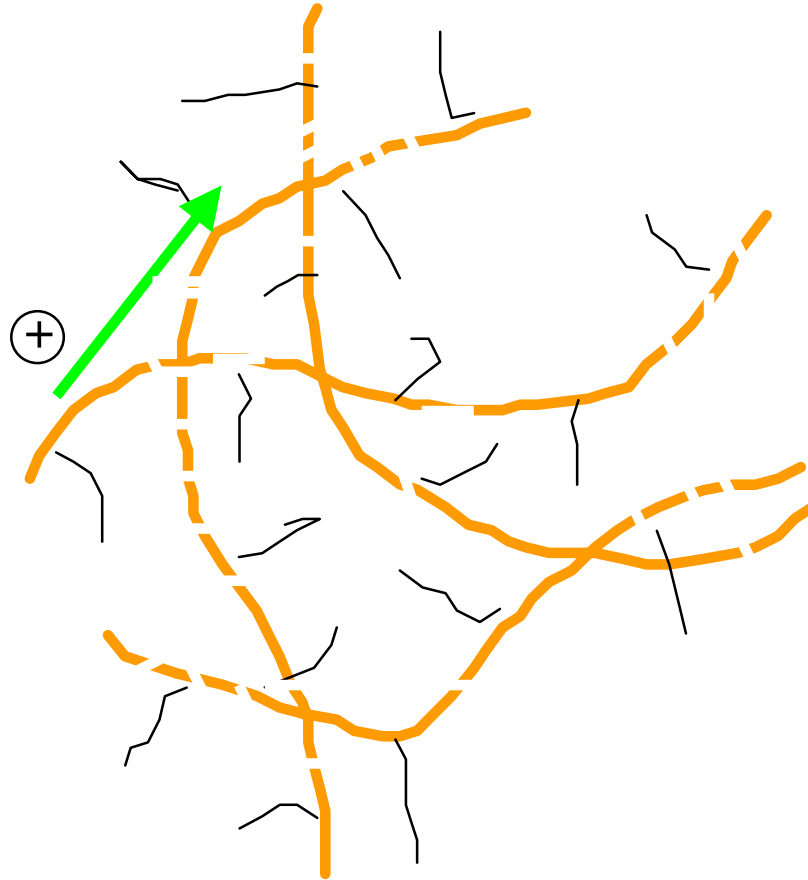


**Chemically doping: introducing charges**

**Charged carriers can move via  $\pi$ -bonds through the polymer**

# Reality conjugated polymers

Conjugation broken by kinks, defects

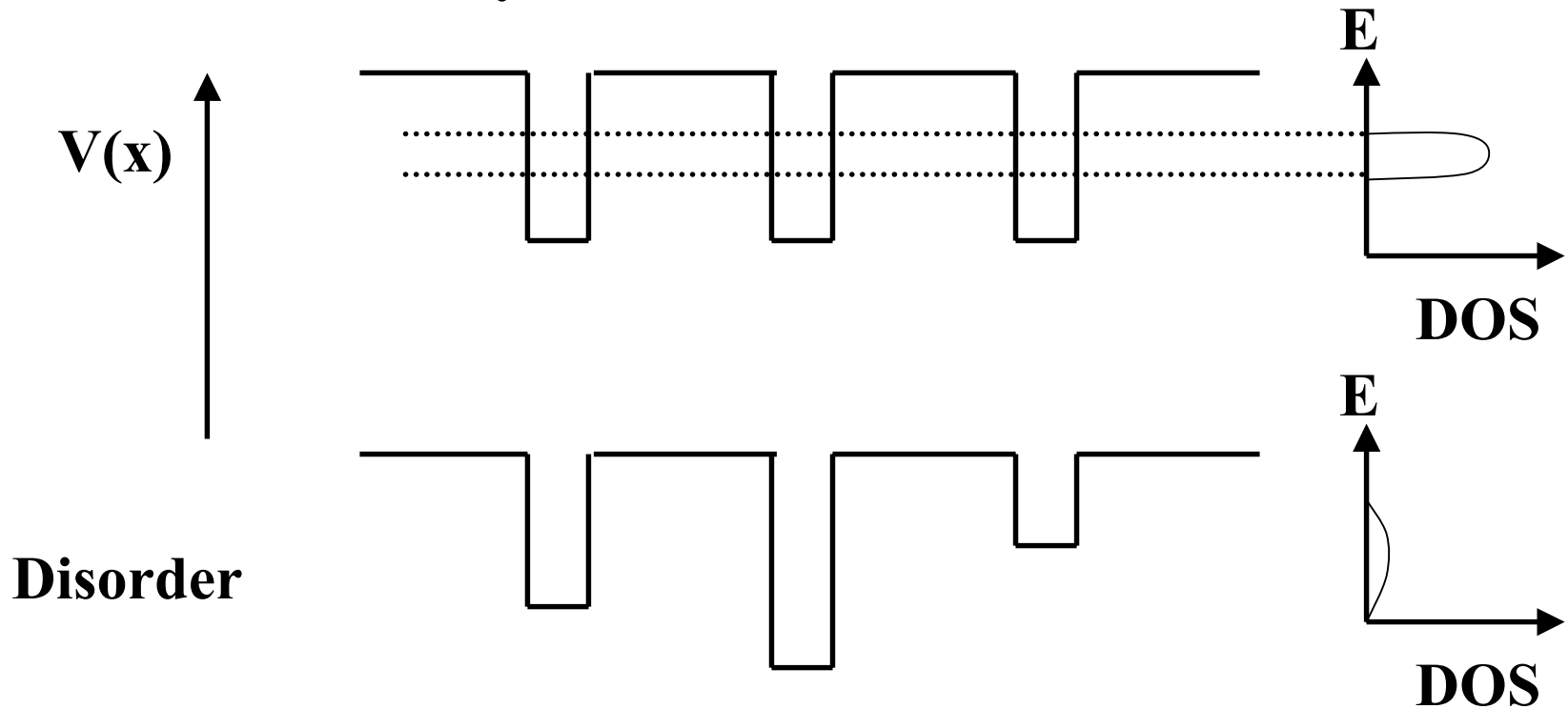


Hopping between conjugated parts – disorder dominant

# Disorder – localized states

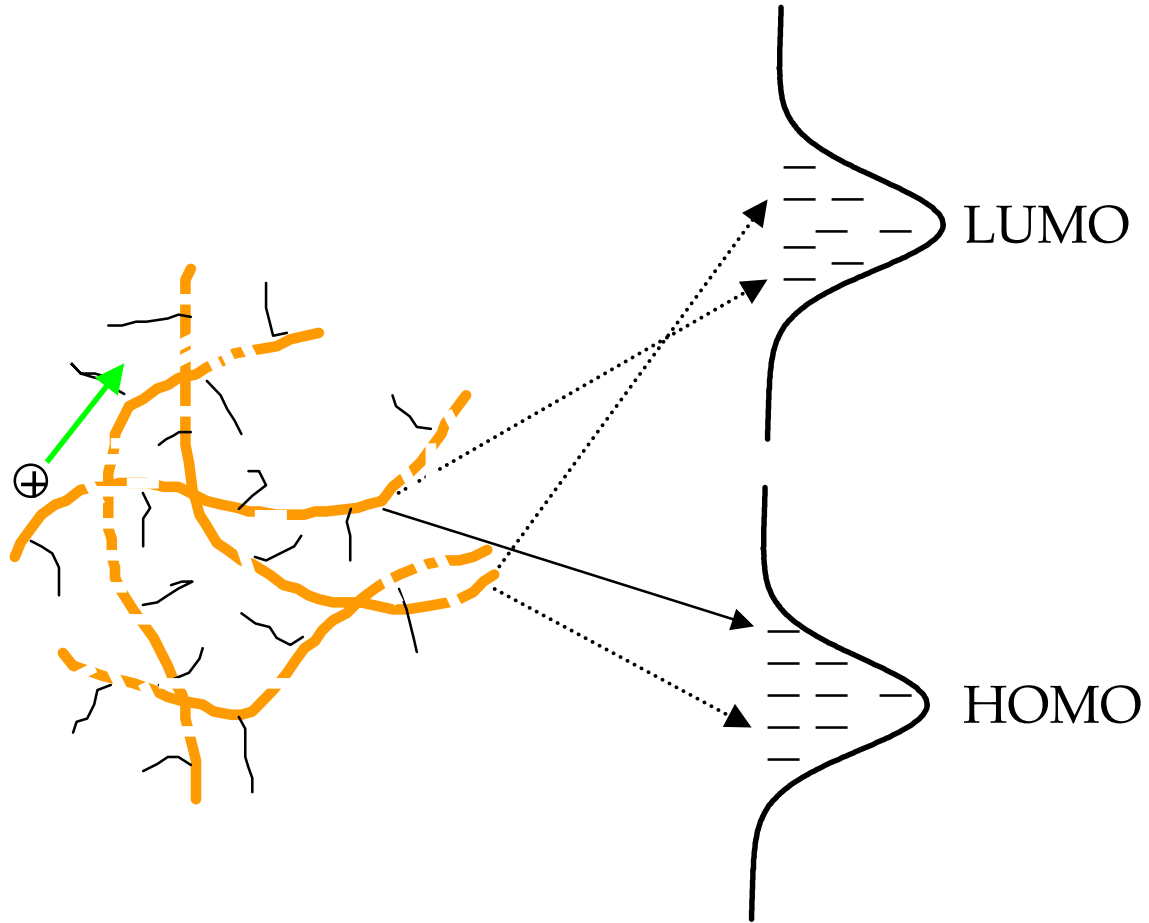
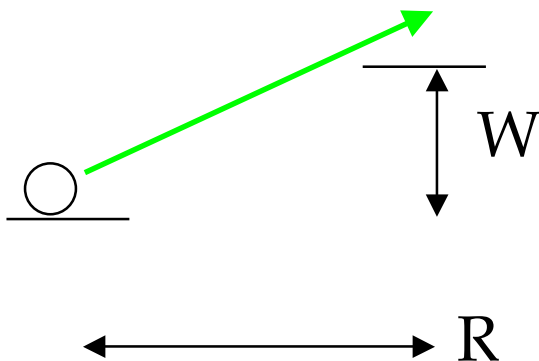
Sufficient disorder produces localized states (Anderson)

Potential Wells for Crystalline Lattice



# Energetic and spatial disorder

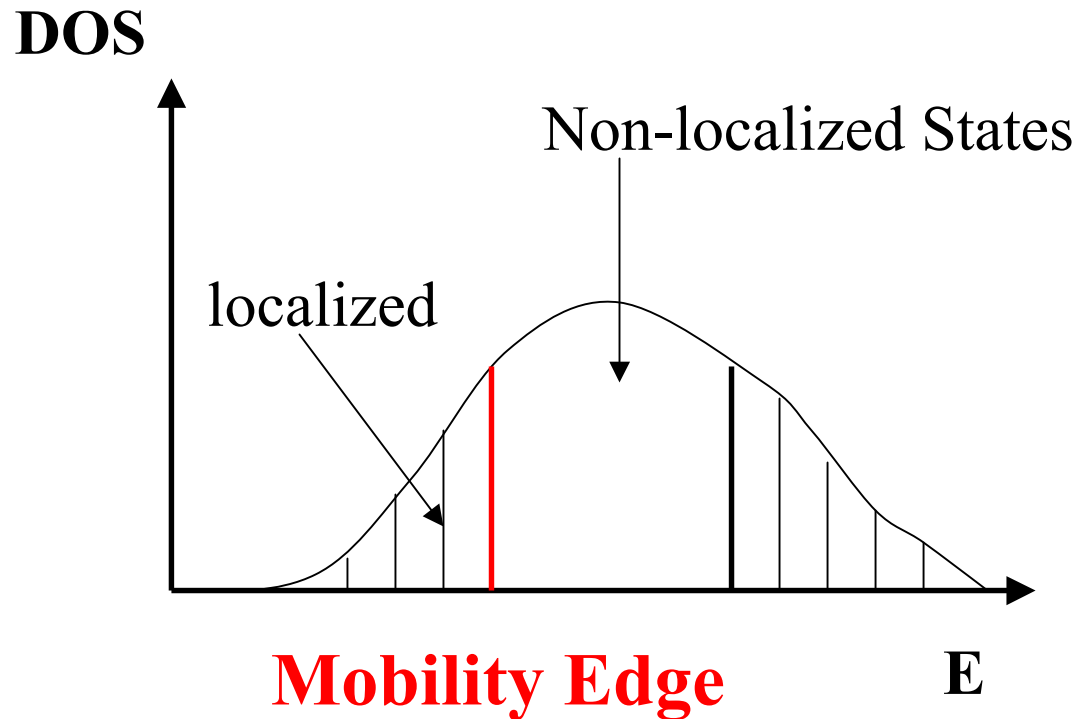
Hopping Process: VRH



$$p_{hop} \approx \exp(-2\gamma R) \exp(-W / kT)$$



# Transport in Disordered Conductors 1

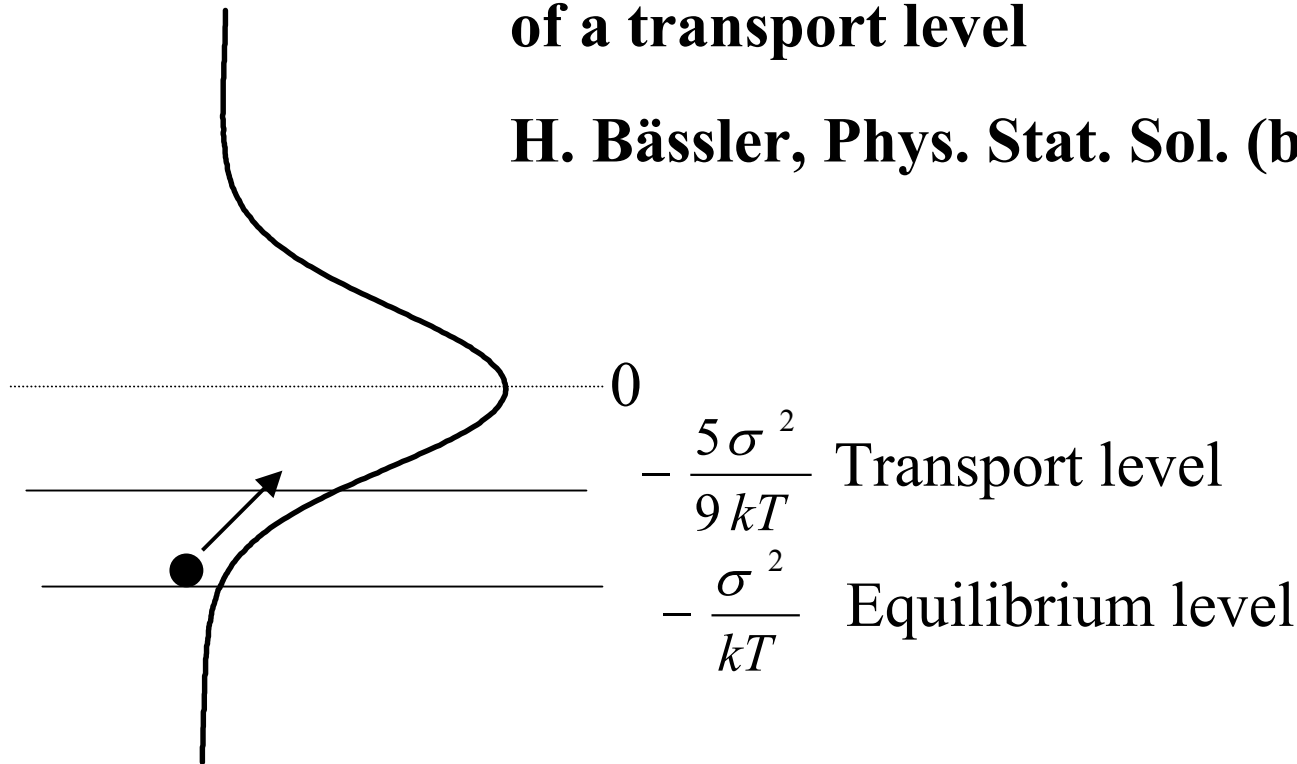


**Fermi-level in localized region gives rise to hopping conduction (Fermi glass) – hopping between localized states or activated**

# Transport in Disordered Conductors 2

**Refinement: Gaussian DOS and the presence of a transport level**

**H. Bässler, Phys. Stat. Sol. (b) 175, 15 (1993)**



# Questions

**How well can the insulating state be described within the framework of variable range hopping (VRH)?**

**How strong are the changes when we cross the MIT – which and how many carriers do contribute to metallic transport?**

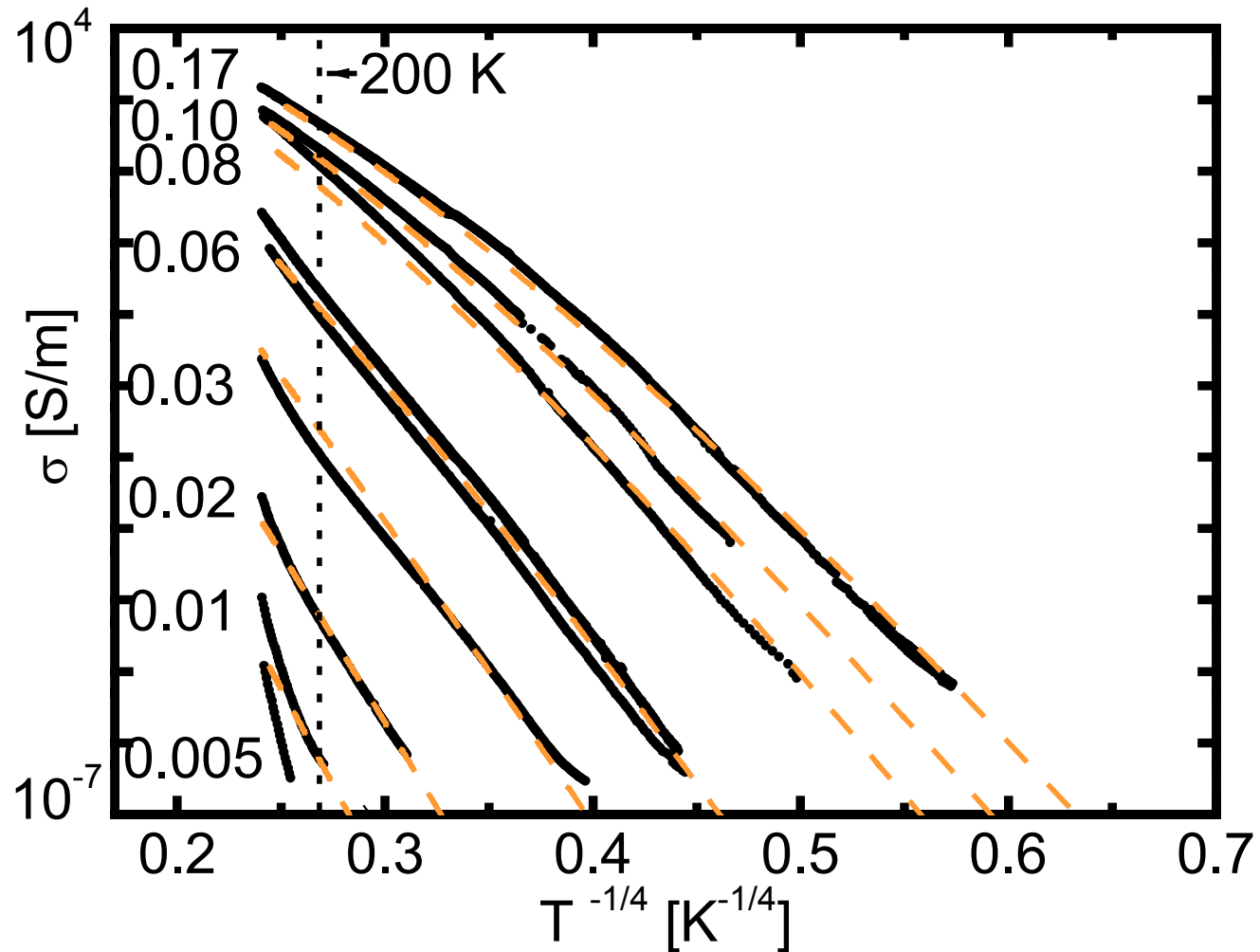
**Can we deduce the density of states vs  $E$ ; is it Gaussian?**

**Two experiments:**

**DC – transport in  $\text{FeCl}_3$  doped PPV (below MIT)**

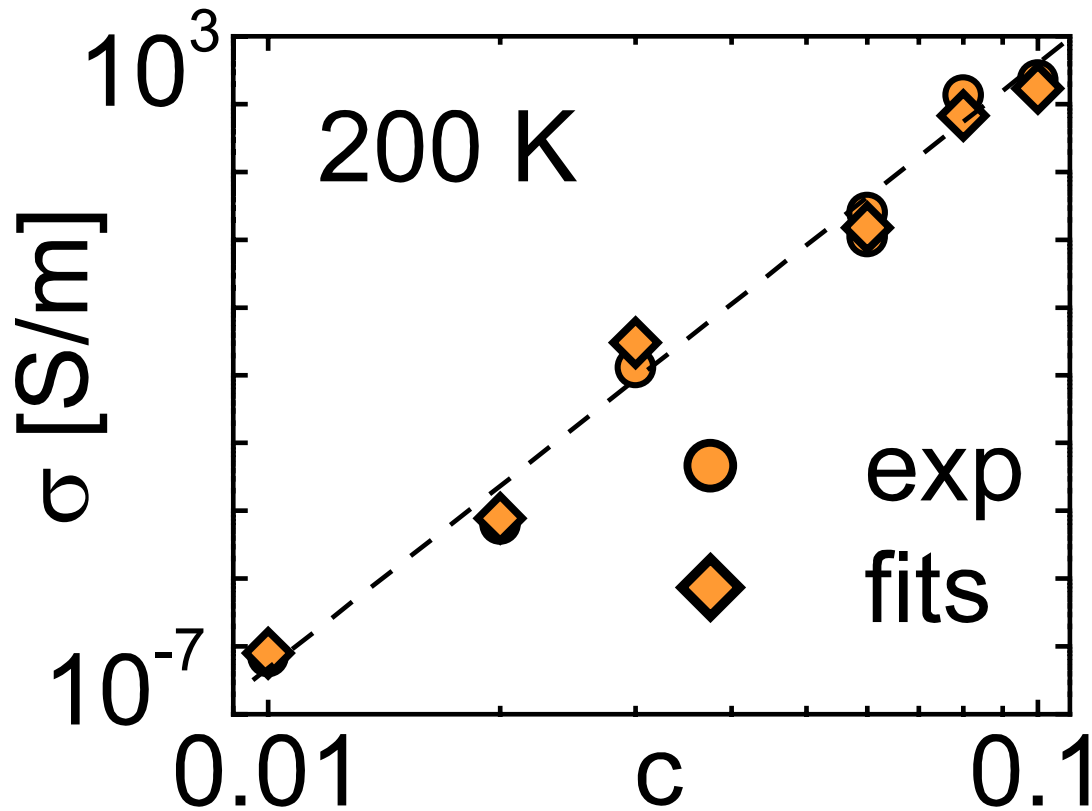
**Dielectric measurements in  $\text{PF}_6$  doped polypyrrole (above MIT)**

# Data $\text{FeCl}_3$ doped PPV vs. T and c



concentration in numbers of carriers per monomer

# Data $\text{FeCl}_3$ doped PPV vs. $c$ at fixed $T$



At fixed  $T$ , 8 orders of magnitude increase in  $\sigma$  with one order increase in  $c$  (more than expected from any previous model).

# Summary experimental observations

**What happens if the doping level is increased:**

**Experimentally**

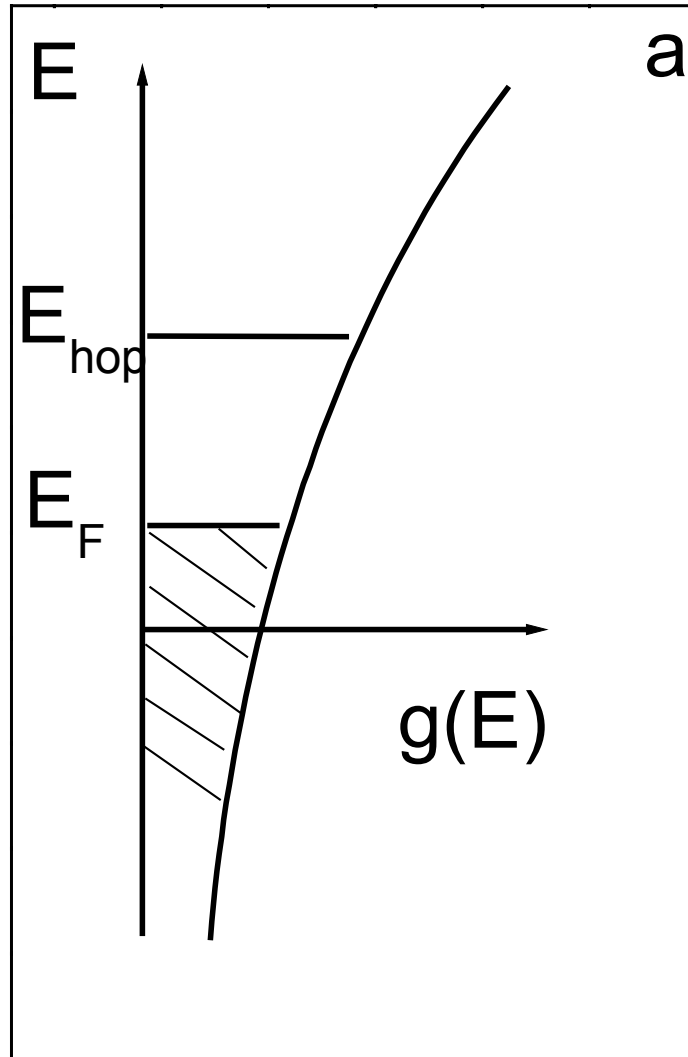
- 1. enormous increase in  $\sigma$  at fixed T (8 orders of magnitude with one order in concentration)**
- 2. Change in slope of  $\sigma$  vs T. At low T  $\sigma \propto \exp(T/T_0)^{1/4}$**
- 3. Flattening of the curves at high c and T**

**How can we model these results?**

**Take into account the variation of the DOS ( $g$ ) and the size of the delocalized volume (radius  $A$ )**

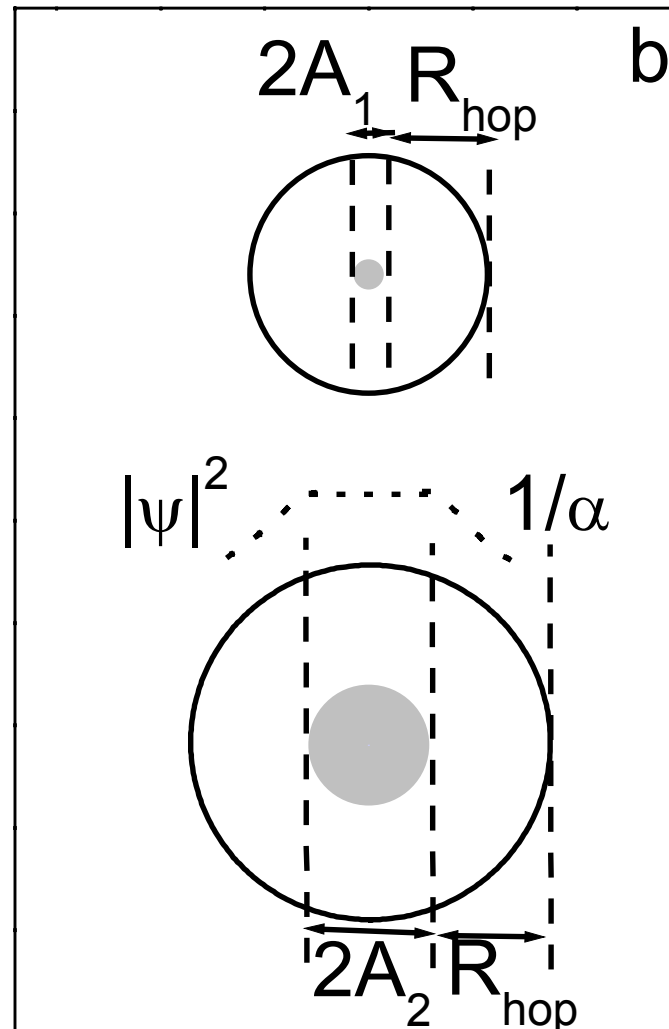
**Ref.: Martens, Hulea, Romijn, Brom, Pasveer and Michels,  
Phys. Rev. B 67, 121203(R) (2003)**

# Density of states



**new carriers will fill up higher energy states given by  $g(E)$  (if doping does not create new states).**

# Extension of states



**Because by doping states with higher energy are filled, the extension of the localized state might grow**



# Results of the model

**Take into account the variation of  $A$  and  $g$  with  $c$  by combined analytic and numerical approach**

**$A$  is a measure for the size of the localized volume.**

**$g$  represents the increasing density of states.**

**(dopant supposed to fill only existing states)**

**Starting relations:**

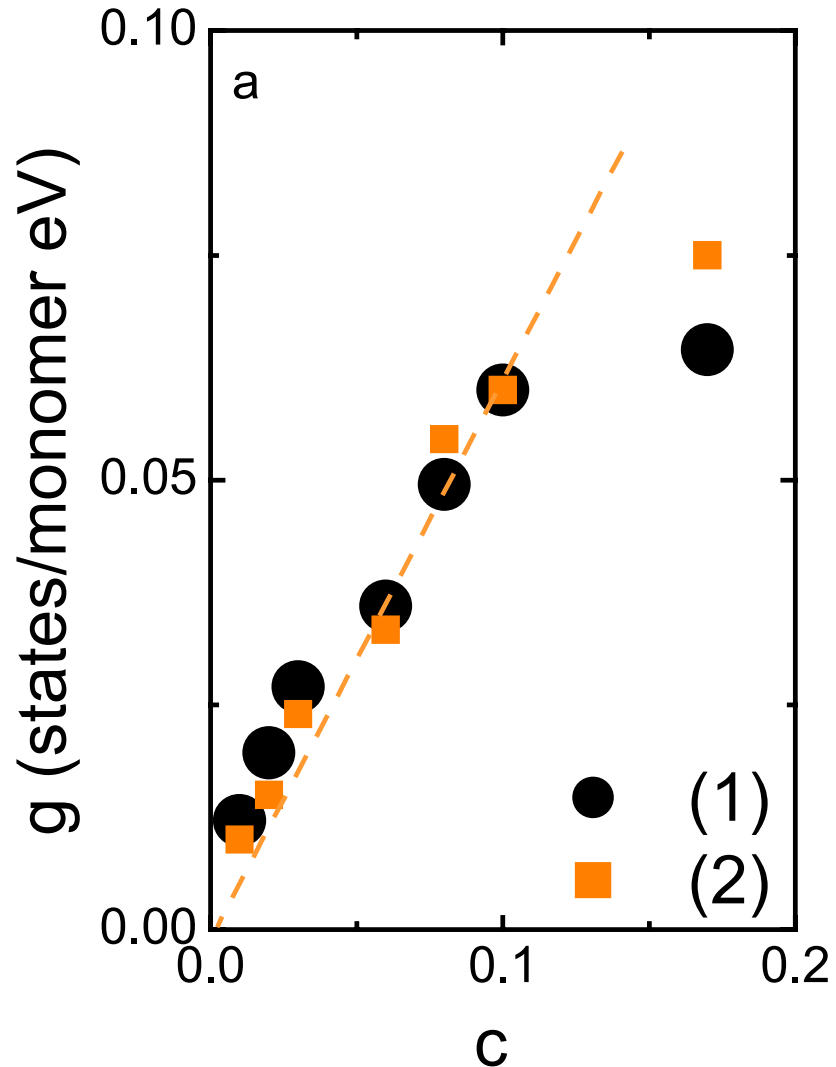
$$\sigma(T,c) = \sigma_0(c) \exp(-\alpha R - \beta(E - E_F)) \text{ and } VN \sim 1$$

**Include the  $c$ -dependence on  $A$  (new) and  $g$  explicitly.**

**One of the results is that 3D Mott's law is recovered for low  $c$  (full eq. is much stronger):**

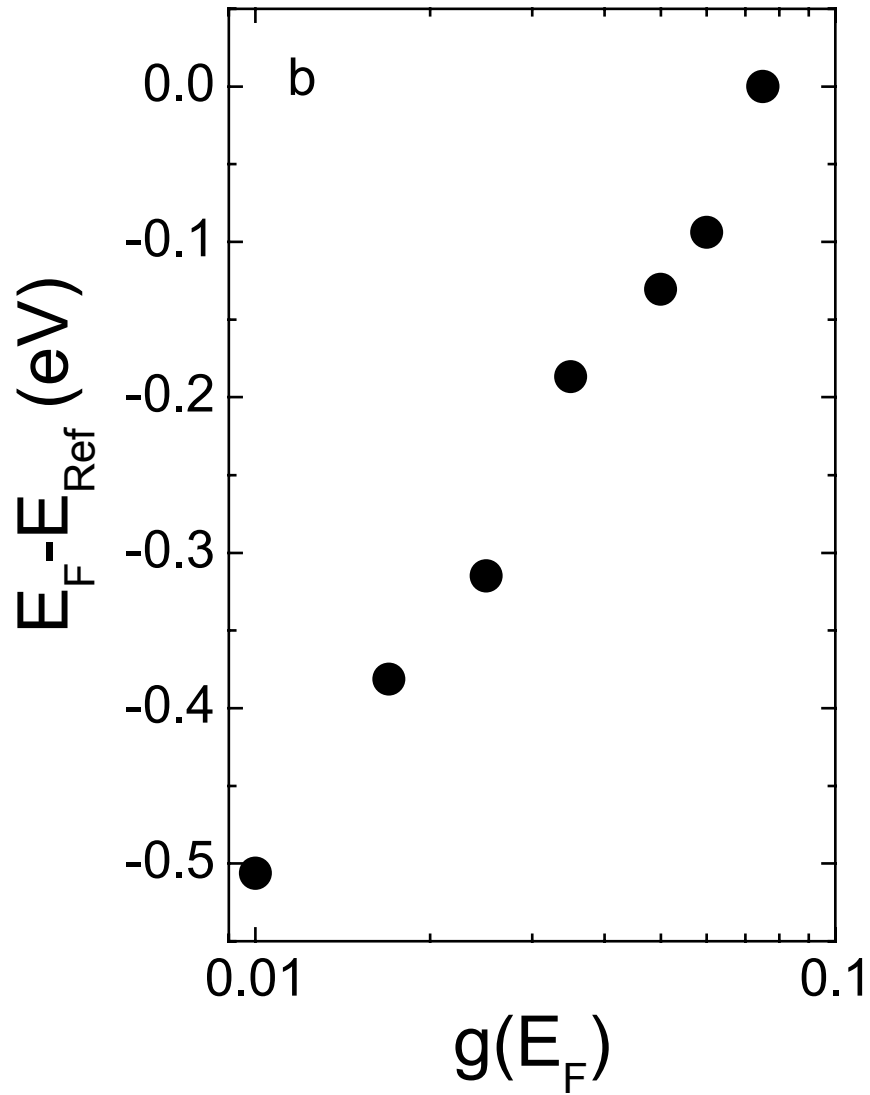
$$\sigma = \sigma_0(c) \exp(\alpha A(c)) \exp(-T_0(c)/T)^{1/4}$$

# Results for $g(c)$



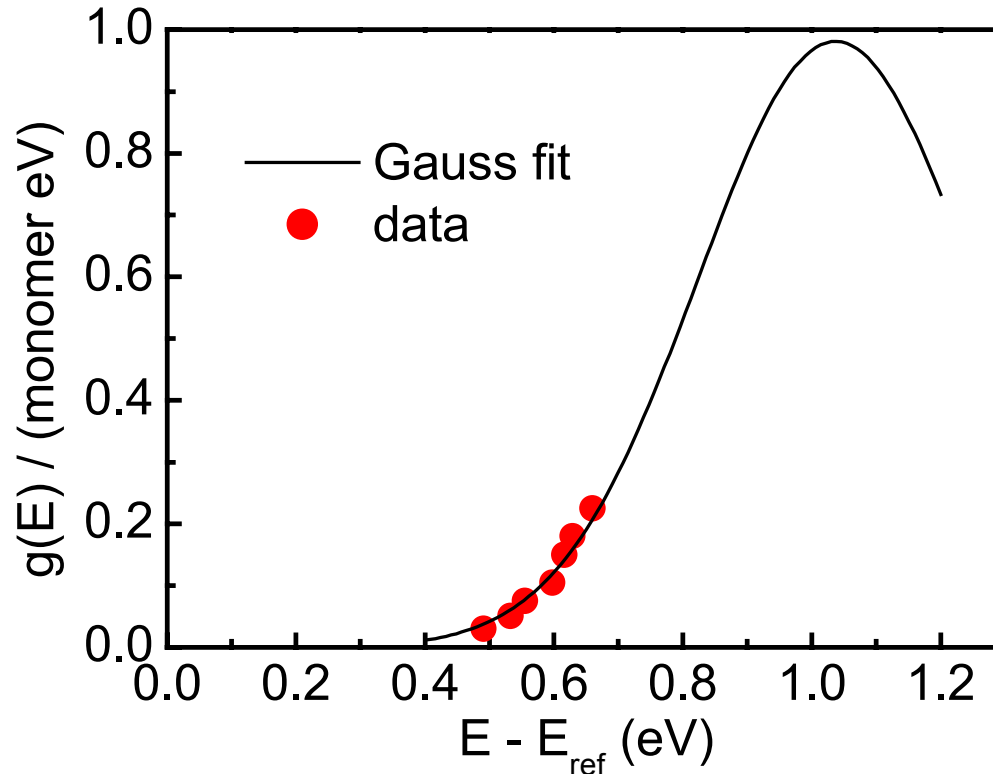
$g$  can be determined in two ways:  
(1) low  $T$  :  $k_B T_0 \sim 1/g$   
(2) fitting based on the numerical approach

# Results for $E_F - E$ vs $g$



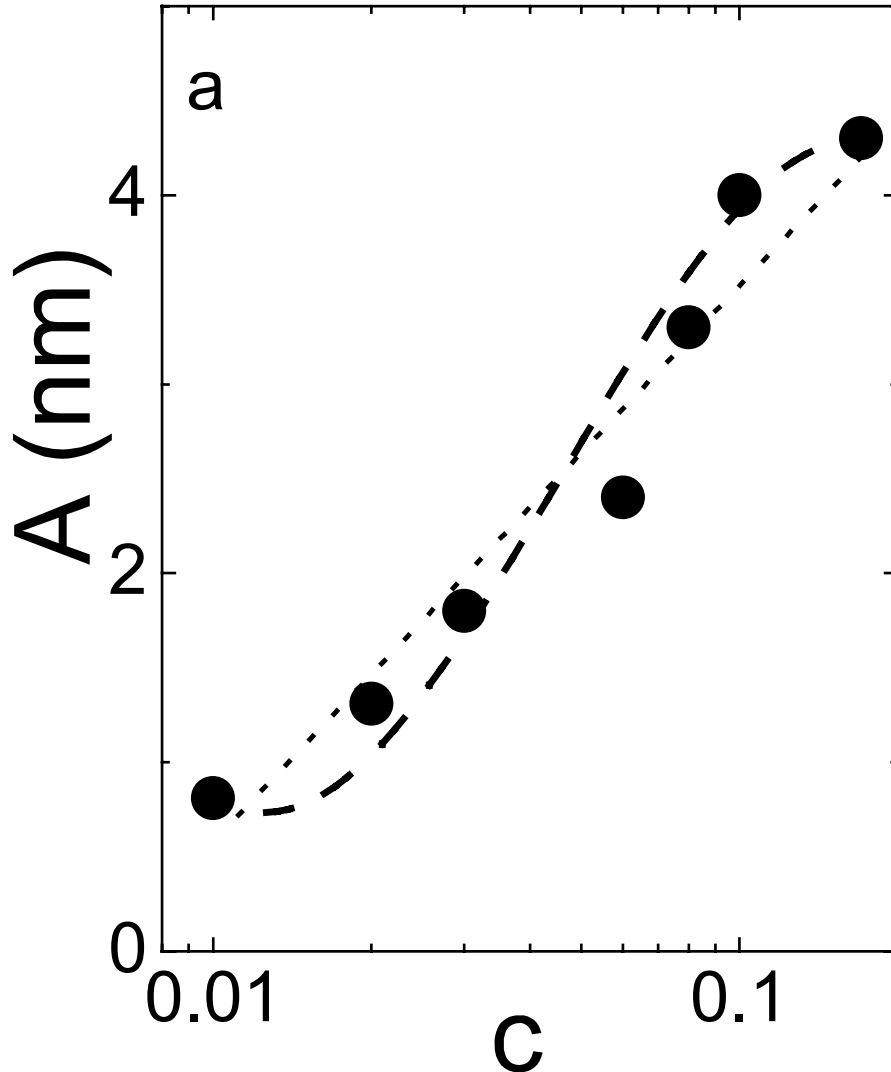
**Scaled to the activation energy  
obtained at high T for  $c=0.01$ .**

# $g(E)$ gaussian?



**Comparison with preliminary data from el. chem. gated transistor confirm gaussian profile  
(Hulea, Brom, Meulenkamp, Vanmaekelbergh et al. , not published)**

# A vs c

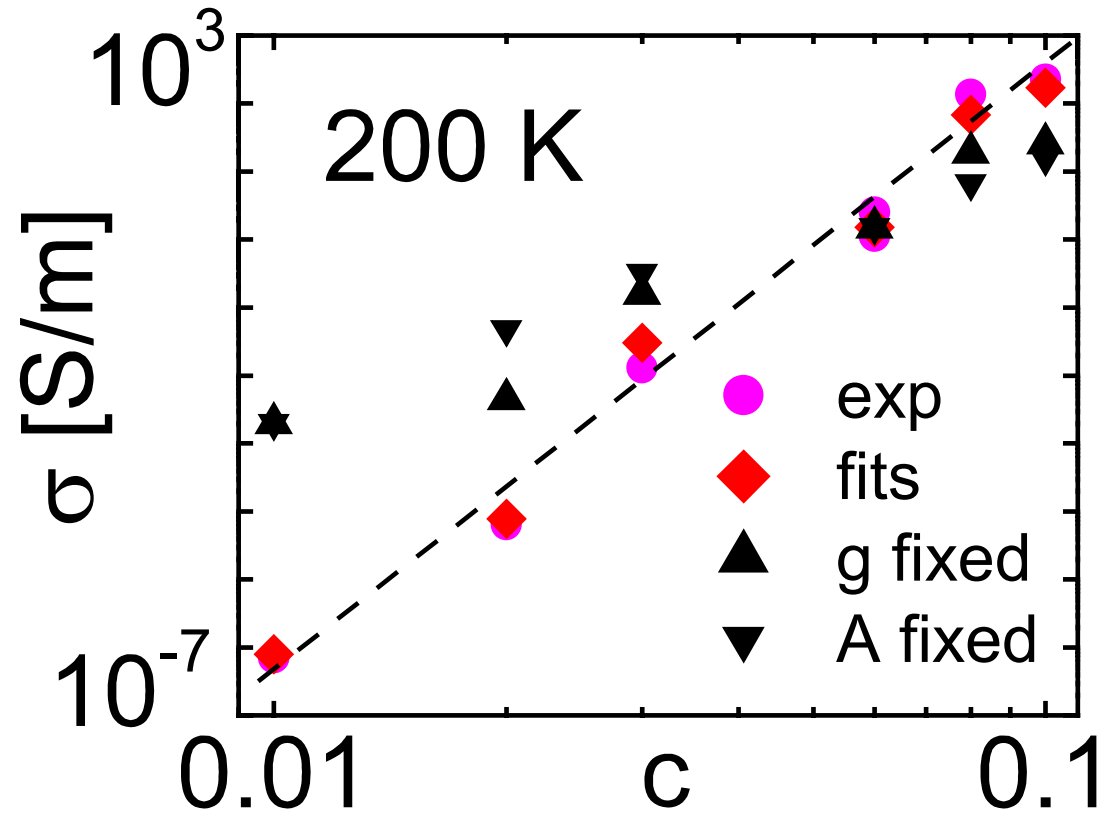


**A is a measure for the size of the localized volume.**

**Dotted line accounts for the logarithmic dependence expected from  $\sigma \sim c^8$ .**

**Dashed line accounts for the saturation at low and high doping. A grows with factor 4**

# A(c) vs g(c)



Approximate:  $\sigma = \sigma_0(c) \exp(\alpha A(c)) \exp(-T_0(c)/T)^{1/4}$   
 Fixed T:  $\sigma \propto \sigma_0(c) \exp(\alpha A(c))$  with  $A(c) \sim \log c$

# Transport below MIT

- the T and c dependence of  $\sigma = \sigma_0(c) \exp(\alpha A(c)) \exp(-T_0(c)/T)^{1/4}$  is a good starting point for the analysis.
- the contributions of both  $g(c)$  and  $A(c)$  are essential to explain the c and T dependence of  $\sigma$ .
- reconstructed dos complies with Gaussian shape

## More references

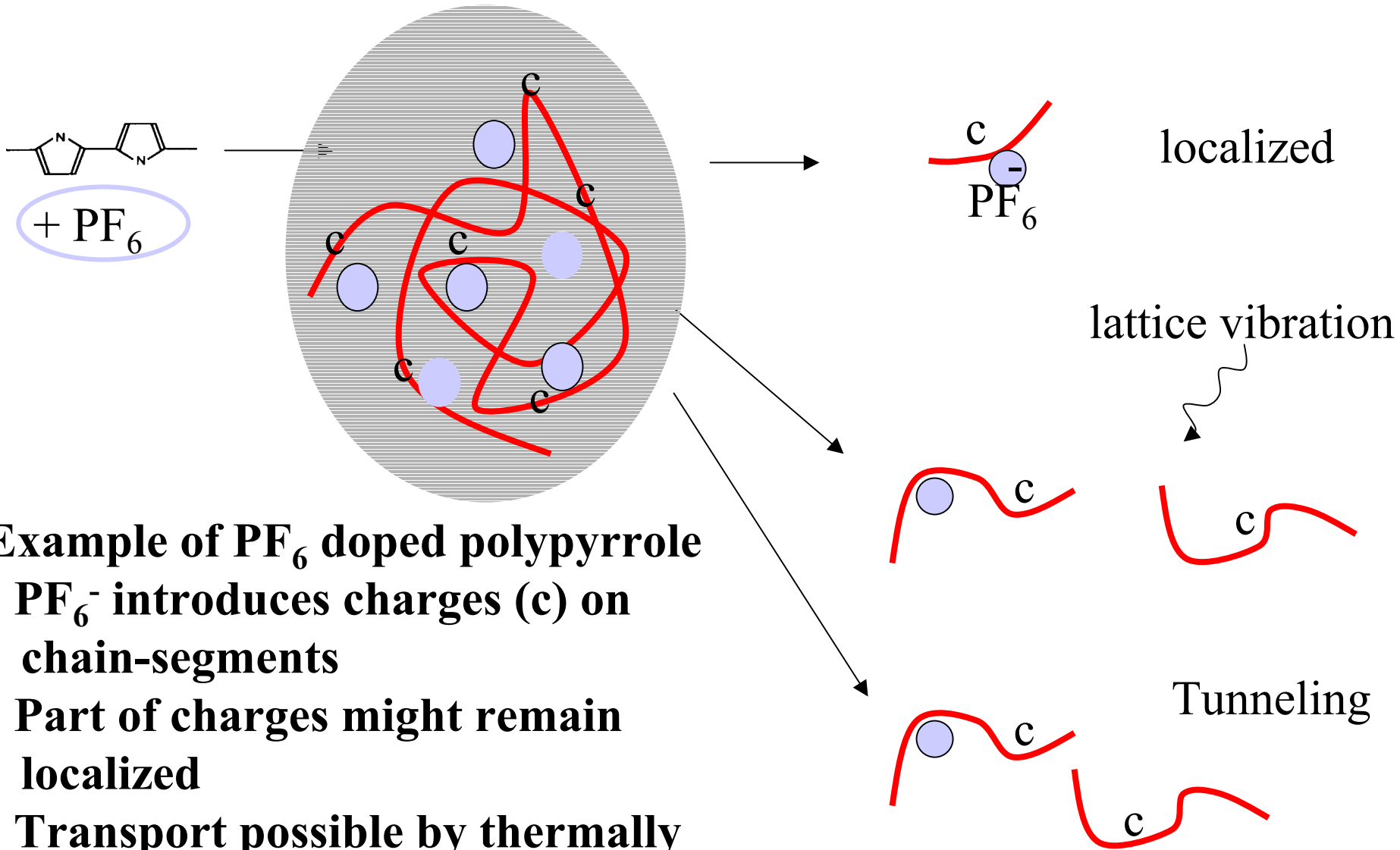
N.F. Mott, *Phil. Mag* 19, 835 (1969).

H. Bässler, *Phys. Stat. Sol. (b)* 175, 15 (1993).

S.D. Baranovskii *et al.*, *PRB* 62, 7934 (2000).

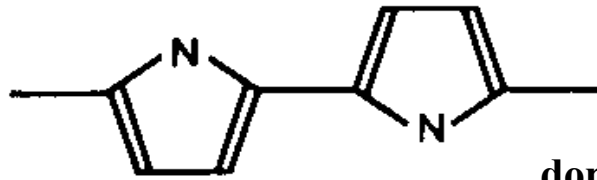
M.C.J.M. Vissenberg and M. Matters, *PRB* 57, 12964 (1998)

# Transport in polymers above MIT





# Test case: PF<sub>6</sub> doped polypyrrole



polypyrrole

doped with hexafluorophosphate

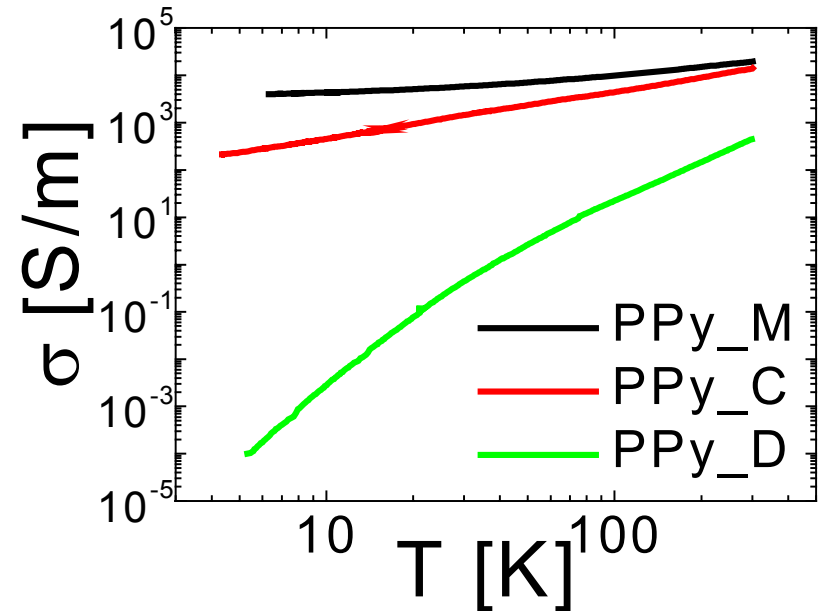
## Why PPy?

PPy is very stable – survives in air for a long time

PPy can be made from deep in the insulating (PPy<sub>D</sub>) to well into the metallic state (PPy<sub>M</sub>)

For PPy<sub>M</sub>:  $\approx 1$  dopant/PPy unit

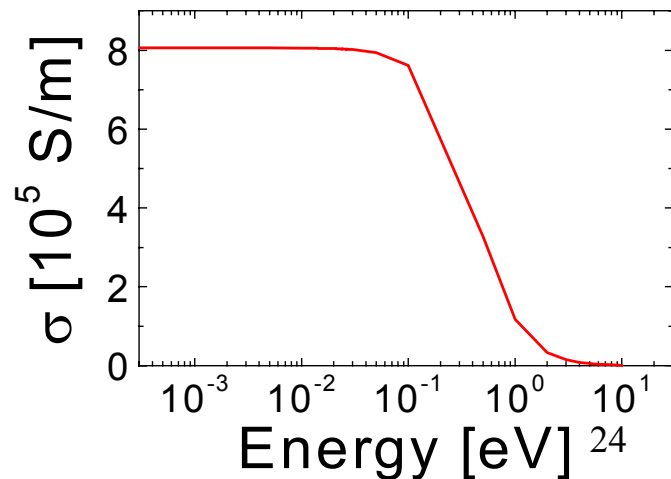
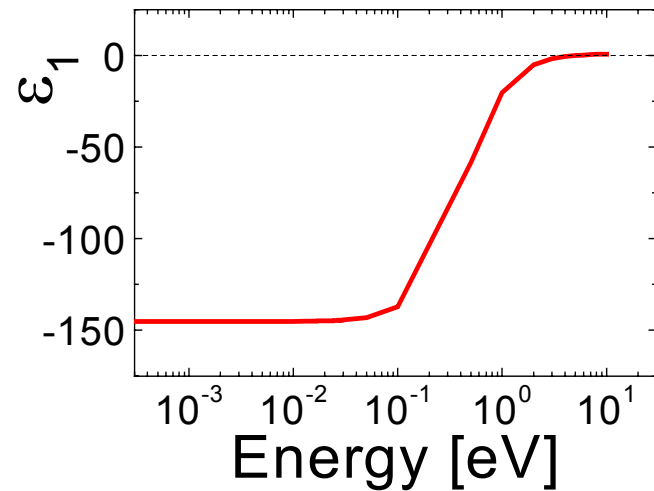
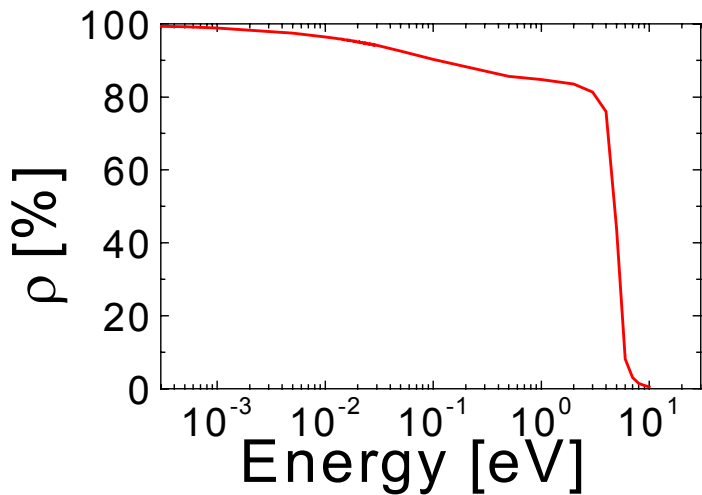
## Metallic? Go to low T



DC conductivity

# Metallic charge transport: high frequency dielectric spectroscopy

## Case of metal

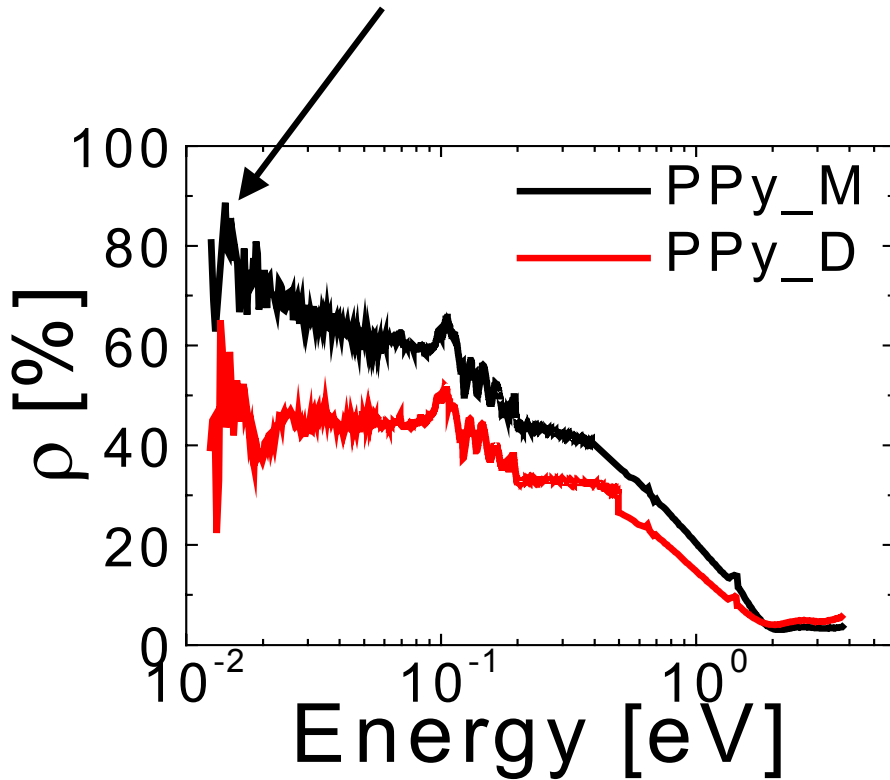


$$R(\omega) = \rho(\omega)e^{i\theta(\omega)}$$

$$\sigma(\omega) = \sigma_1(\omega) + i\sigma_2(\omega)$$

$$\epsilon_1 = i\sigma_2/\epsilon_0\omega$$

# Reflection PPy



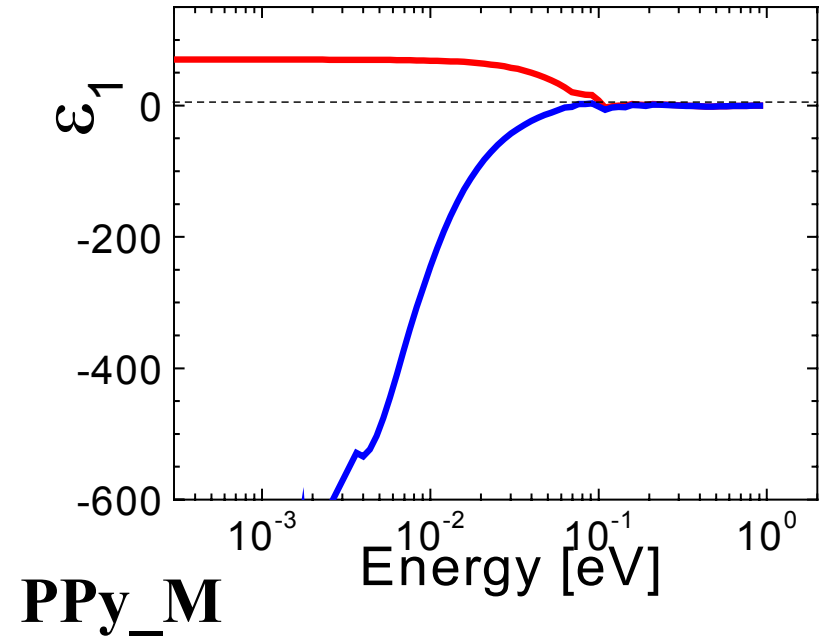
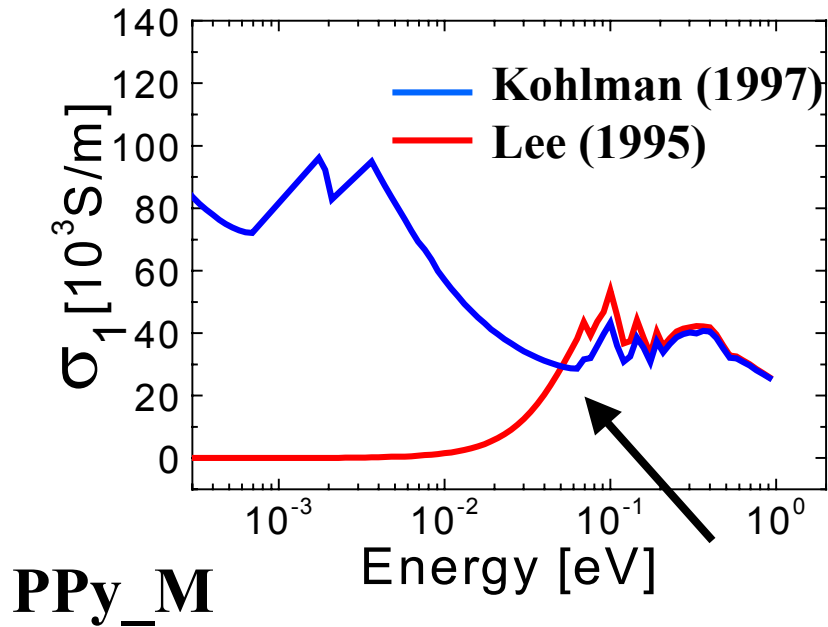
**Bruker FTIR (5 meV – 0.5 eV)**  
**Perkin Elmer UV/VIS (0.5 – 3.5 eV)**

$\rho(\omega)$  and  $\theta(\omega)$ :  $\sigma_1(\omega)$  and  $\epsilon_1(\omega)$   
**Only real part  $\rho(\omega)$  measurable**  
**Calculate imaginary part  $\theta(\omega)$**   
**from  $\rho(\omega)$  by application of**  
**Kramers-Kronig**

$$\theta(\omega) = -\frac{2\omega}{\pi} \int_0^{\infty} \ln \left[ \frac{\rho(\omega')}{\rho(\omega)} \right] \frac{d\omega'}{[(\omega')^2 - \omega^2]}$$

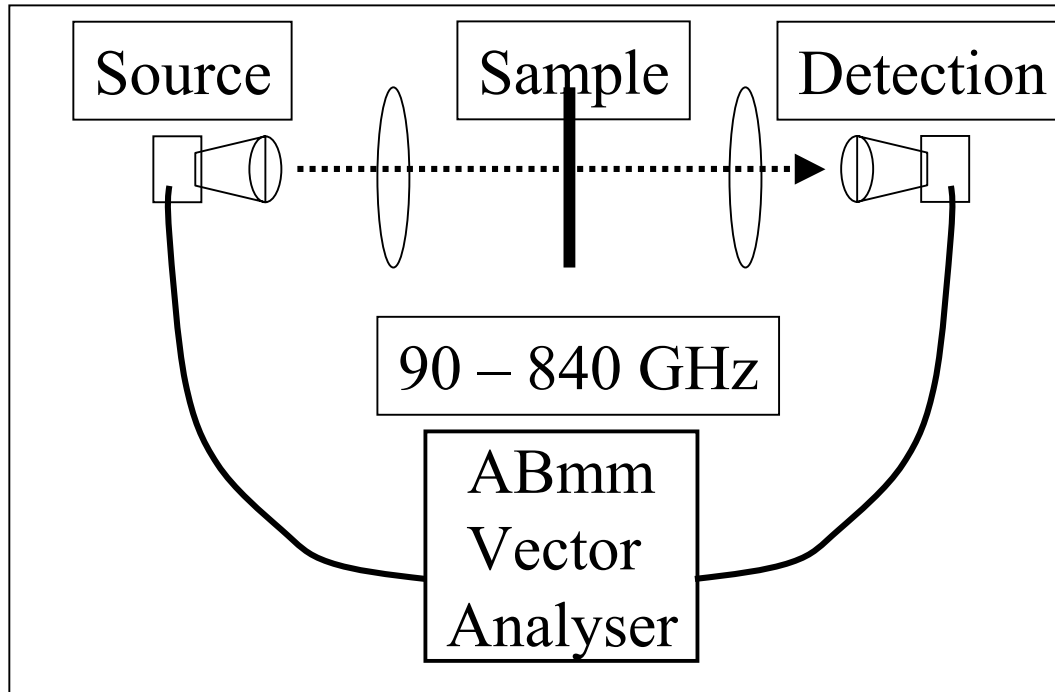
**Extrapolate data  $\rho(\omega)$**

# Old data controversial

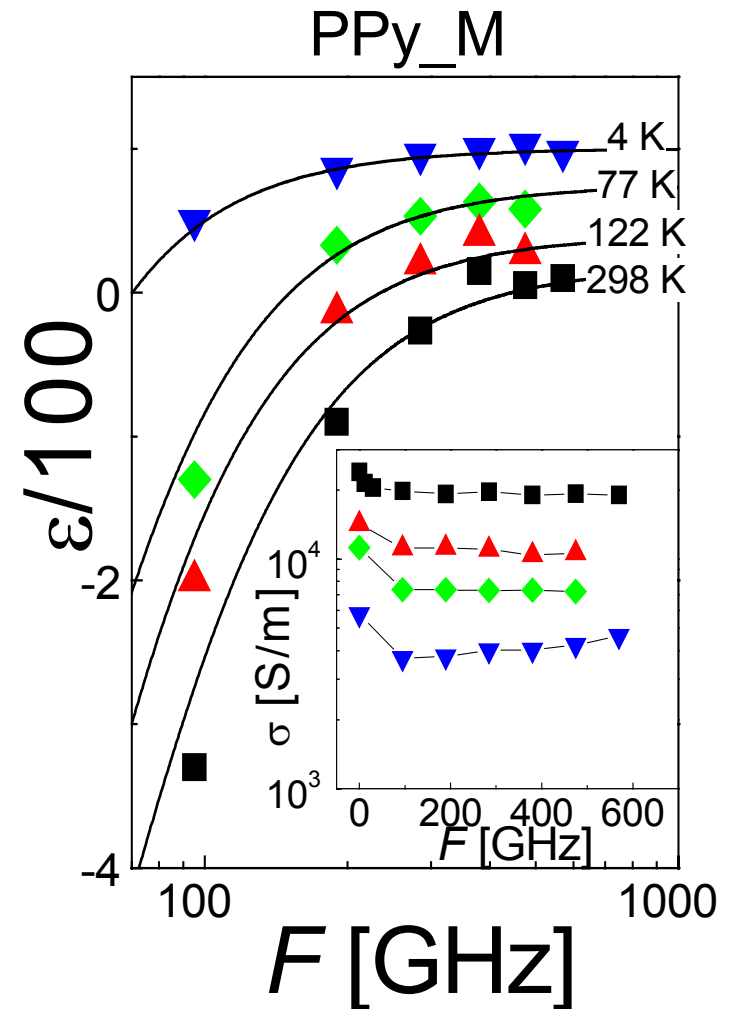


Depending on extrapolation at low energies several groups found completely different conductivity  $\sigma_1$  and dielectric constant  $\epsilon_1$  ( $\epsilon_1 = i\sigma_2/\epsilon_0\omega$ )

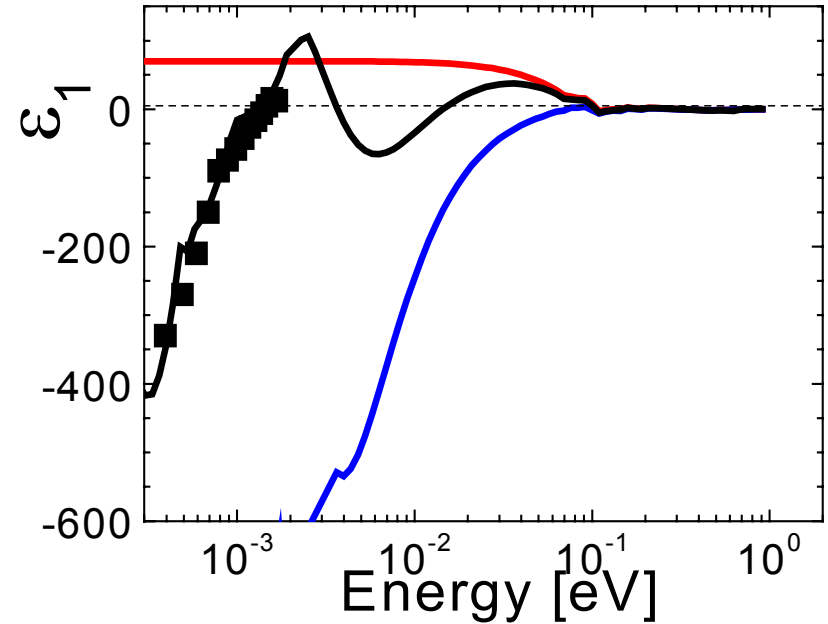
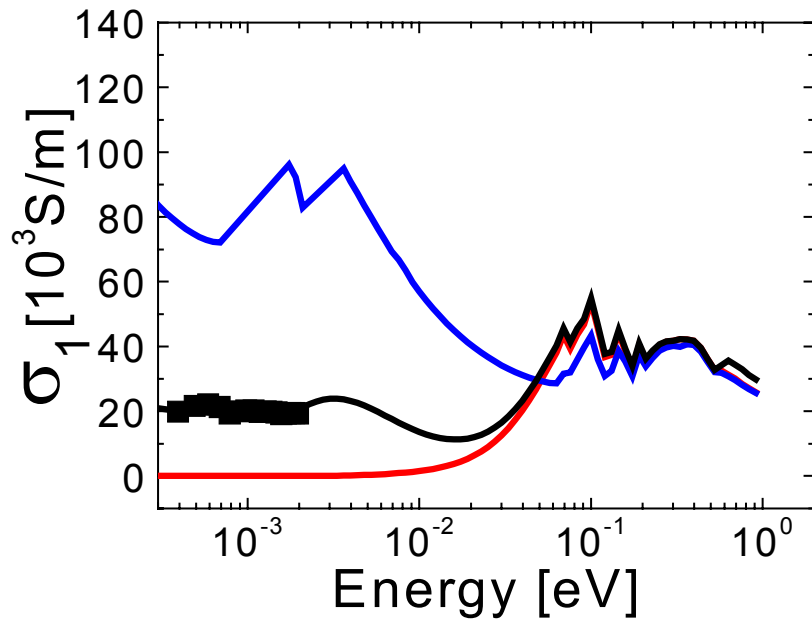
# Additional data below 1 THz



**Complex transmission -  $\epsilon_1$  and  $\sigma_1$  can be determined simultaneously down to 4 K**



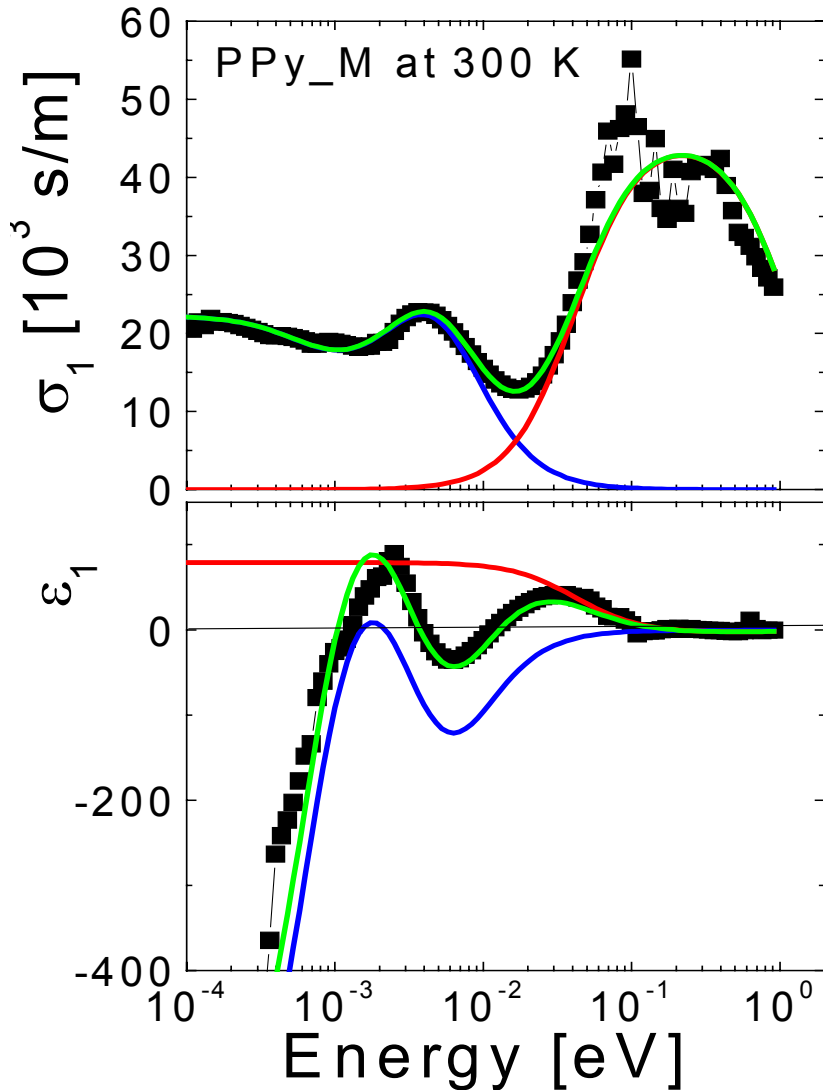
# KK analysis



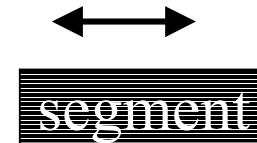
Kohlman et. al., — Lee et. al., ■ GHz data, — our K.K. fit

**The low frequency data give nice boundary conditions for the Kramers-Kronig analysis**

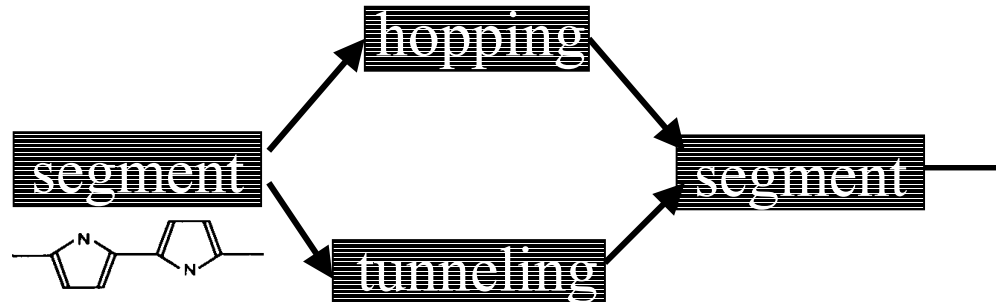
# Model applied to data



99 %: Localized charges:



1%: charges are delocalized:  
transport possible



# Conclusions (conjugated polymers)

- **By doping the number of levels increases as does the delocalization radius (factor of 4)**
- **Map of density of states supports Gaussian model**
- **At the MIT 99% of the introduced charges are localized and do not contribute to the dc-conductivity**
- **The movement of delocalized charges (1%) is governed by thermally activated hopping and QM tunneling between chain segments**



# More references

**H. Böttger and V.V. Bryksin, Hopping conduction in Solids (Akademie Verlag, Berlin, 1993)**

**G. Grüner et al., e.g. this conference**

**Y. Imry, Introduction to Mesoscopic physics (Oxford University Press, Oxford, 1997)**

**A.B. Kaiser, Adv. Mater. B 52, 4779 (2001); Rep. Prog. Phys. 64, 1 (2001)**

**S.V. Novikov, D.H. Dunlap, V.M. Kenkre, P.E. Parris and A.V. Vannikov, Phys. Rev. Lett. 81, 4472 (1998)**

**V.N. Prigodin and A.J. Epstein, Synth. Met. 125, 43 (2002)**