

*SCHOOL ON SYNCHROTRON RADIATION AND APPLICATIONS*  
*In memory of J.C. Fuggle & L. Fonda*

19 April - 21 May 2004

*Miramare - Trieste, Italy*

1561/17

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**Photoemission from Valence Bands, Dispersion and Fermi  
Surface Mapping**

**Juerg Osterwalder**

# Photoemission from Valence Bands, Dispersion and Fermi Surface Mapping

Jürg Osterwalder

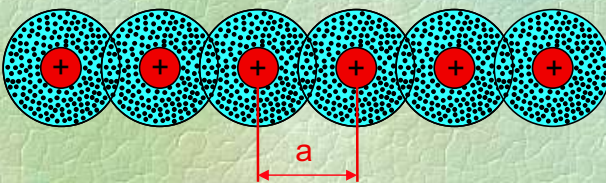
Physik-Institut, Universität Zürich, Winterthurerstr. 190,  
CH-8057 Zürich, Switzerland - [osterwal@physik.unizh.ch](mailto:osterwal@physik.unizh.ch)  
<http://www.physik.unizh.ch/groups/grouposterwalder/>

## Lecture 1

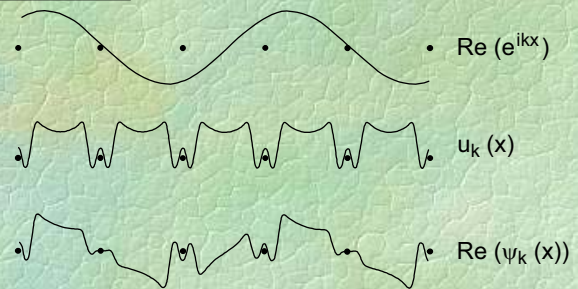
- Electronic Band Structure in 1-3 Dimensions
- Photoemission from a Periodic Potential
- The 3-Step Model
- A 1D Example: p(2x1) O-Cu(110) -> Band Mapping
- A 2D Example: The Shockley Surface State on Cu(111)
- A Few Words about Surface States in General
- Surface States on Stepped Surfaces:  
A Playground for Quantum Mechanics

## Electronic Bandstructure in 1 Dimension

chain of atoms:

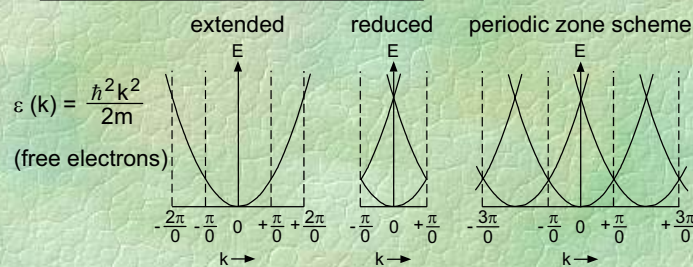


wave functions:



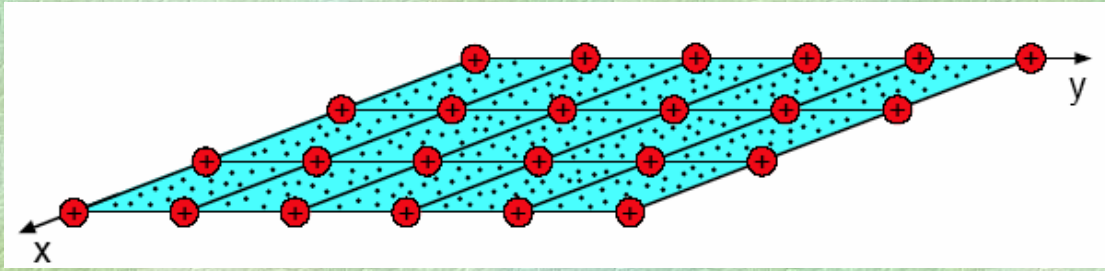
Bloch functions  $\psi_k(x) = u_k(x) e^{ikx}$

dispersion relation (reciprocal space):

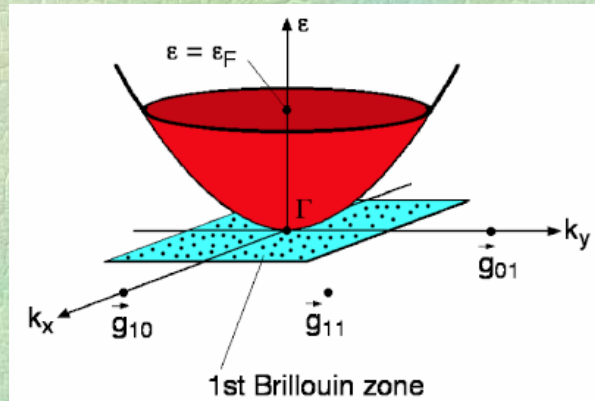


## Electronic Structure in 2 Dimensions

(Plane of atoms)

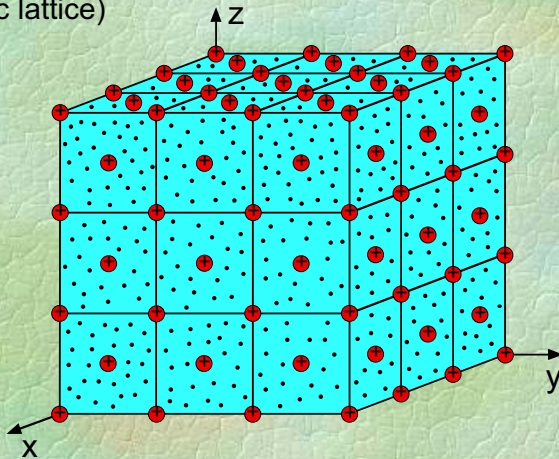


dispersion relation

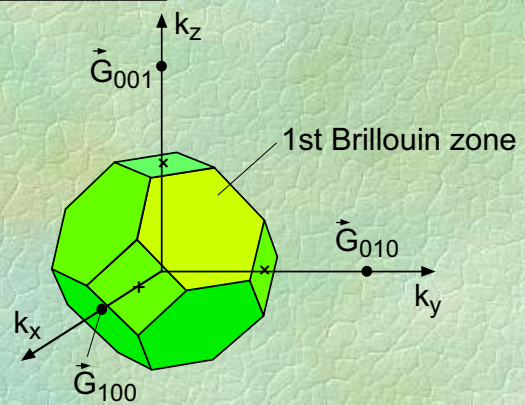


## Electronic Structure in 3 Dimensions

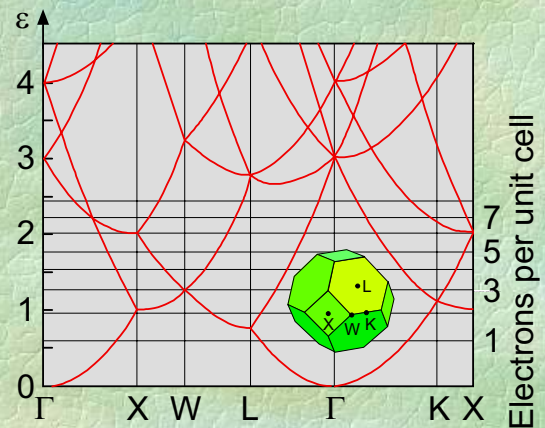
real space:  
(face-centered  
cubic lattice)



reciprocal space:



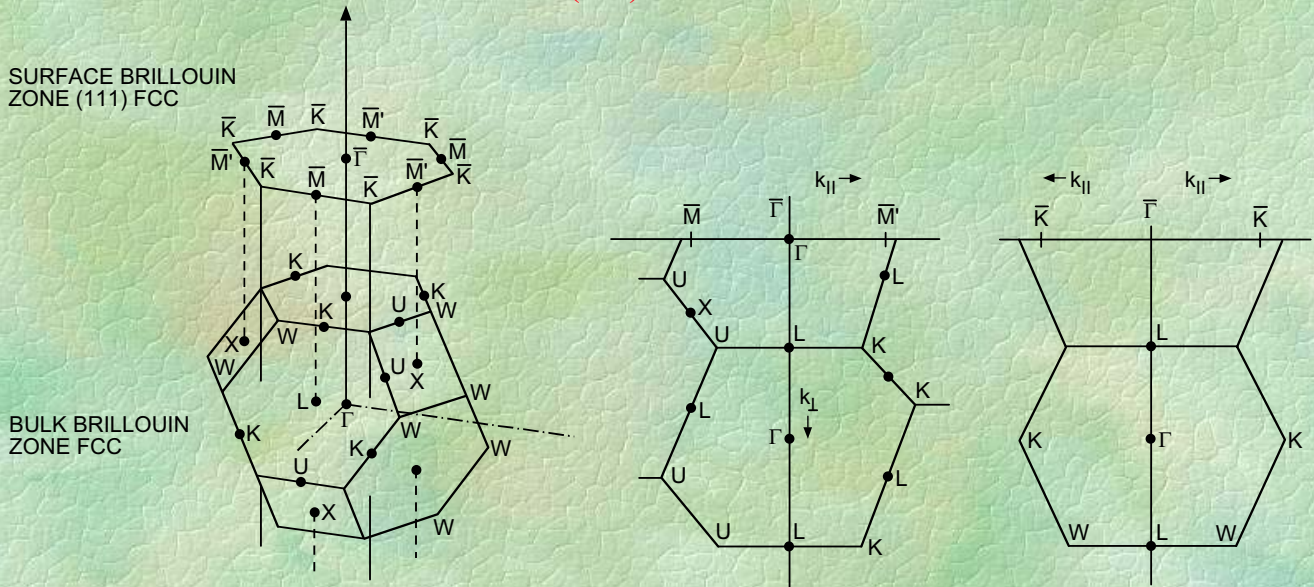
dispersion relation:



# The Geography of Reciprocal Space

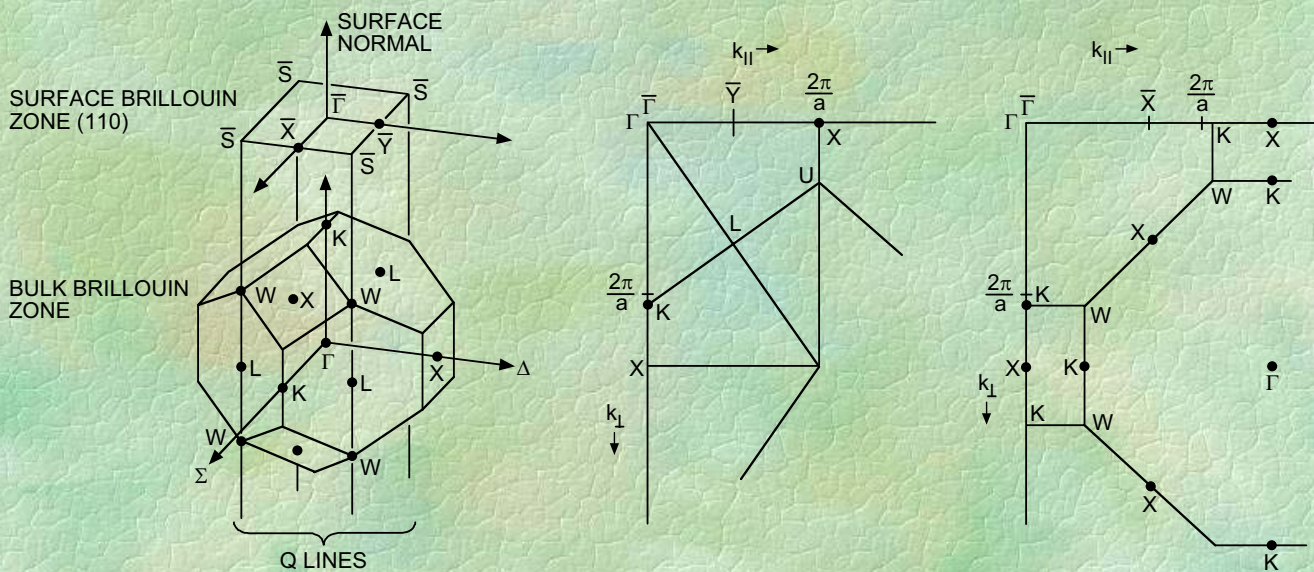
Surface and Bulk Brillouin Zones for face-centered cubic (fcc) Lattices

(111) Surface



Surface and Bulk Brillouin Zones for face-centered cubic (fcc) Lattices

(110) Surface

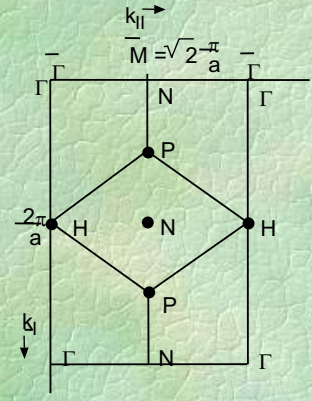
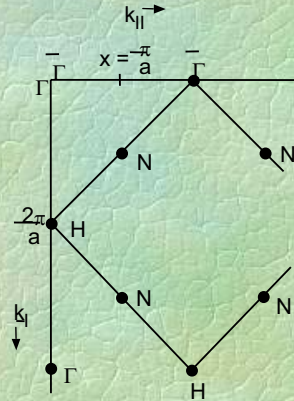
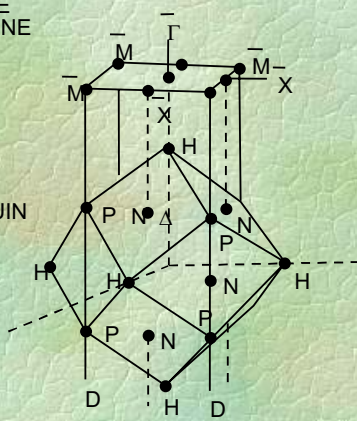


# Surface and Bulk Brillouin Zones for body-centered cubic (bcc) Lattices

## (001) Surface

(001) SURFACE BRILLOUIN ZONE

BULK BRILLOUIN ZONE



From E. W. Plummer, W. Eberhardt  
Adv. Chem. Phys. 49, 533 (1982)

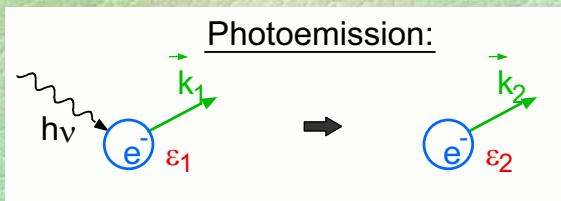
## Photoemission of a free electron

	Energy	Momentum
free electron	$\epsilon(\vec{k}) = \frac{\hbar^2 k^2}{2m}$	$\hbar \vec{k}$
photon ( $h\nu$ )	$\epsilon(\vec{k}) =  \hbar \vec{k} c$	$\hbar \vec{k}$

wave numbers  $k$

$$e^- : k = 0.51 \sqrt{\epsilon [\text{eV}]} \text{ \AA}^{-1}$$

$$h\nu : k = 0.51 \cdot \epsilon [\text{eV}] \cdot 10^{-3} \text{ \AA}^{-1}$$



Conservation Laws:

$$\epsilon_1 + h\nu = \epsilon_2$$

$$\vec{k}_1 + \vec{k}_{h\nu} = \vec{k}_2$$

... cannot be simultaneously fulfilled !  
 $\Rightarrow$  prozess forbidden

Atoms, Molecules: Recoil  
 Solids : Recoil (= reciprocal lattice vector)

## Photoemission from a Periodic Potential

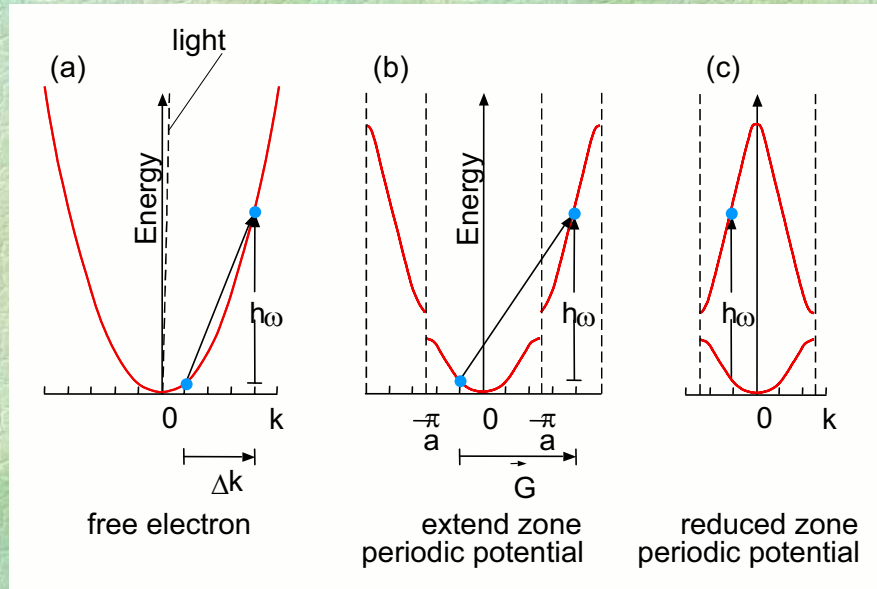
Conservation Laws:

$$\varepsilon_i(\vec{k}_i) + h\nu = \varepsilon_f(\vec{k}_f)$$

$$\vec{k}_i + \vec{k}_{h\nu} + \vec{G} + \vec{g} = \vec{k}_f$$

$$\approx 0$$

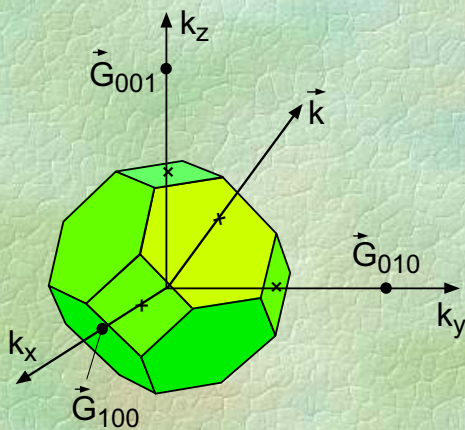
reconstructed surface



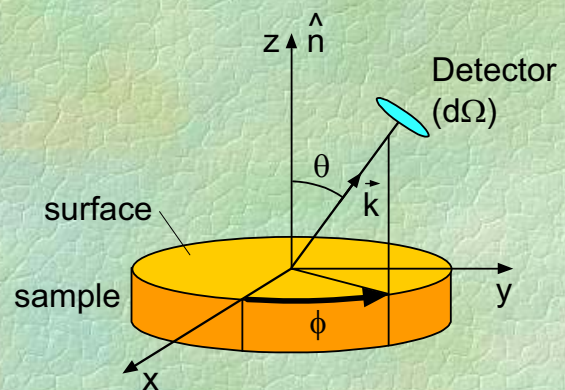
→ Direct Transitions

## Measurement of the Photoelectron Momentum

reciprocal space:



real space:



direction:  $\hat{k} = \theta, \phi$  (watch for refraction)

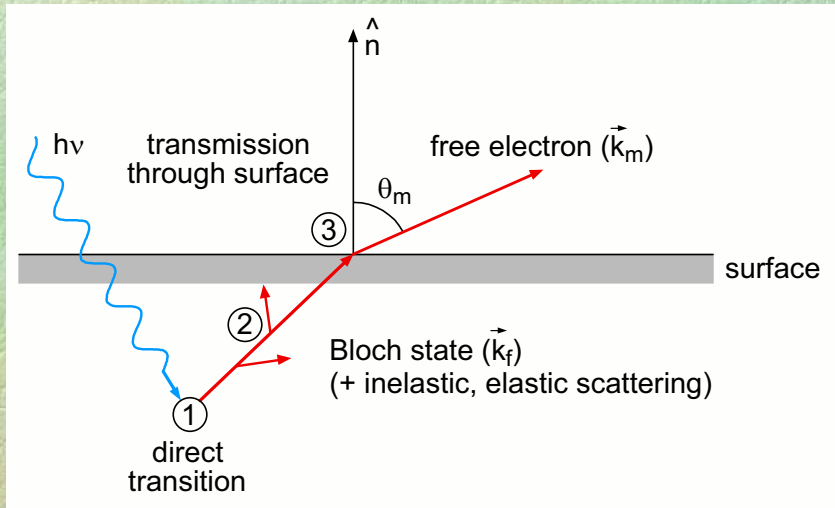
magnitude: from  $\varepsilon_f(\vec{k})$  ( $\varepsilon_f$  is measured)

Problem:  $\varepsilon_f(\vec{k})$  usually not known

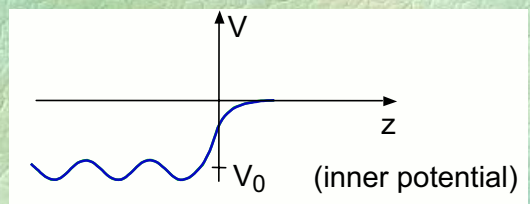
Solution: free electron final state

$$\varepsilon_f(\vec{k}) = \frac{\hbar^2 k^2}{2m}$$

## The 3-Step Model



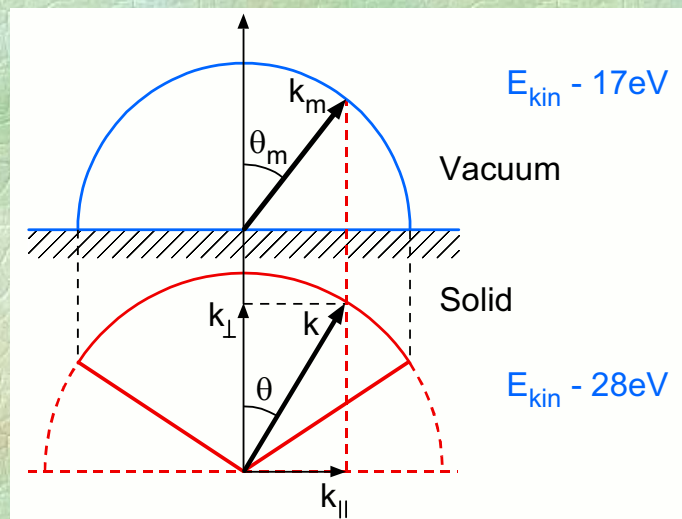
- ① Photoexcitation
- ② Propagation to surface
- ③ surface potential step  $\rightarrow$  Refraction



periodicity within surface  $\rightarrow \vec{k}_{f\parallel} = \vec{k}_{m\parallel}$   
 surface potential step  $\rightarrow \vec{k}_{f\perp} > \vec{k}_{m\perp}$

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## Refraction at the Surface Potential Step

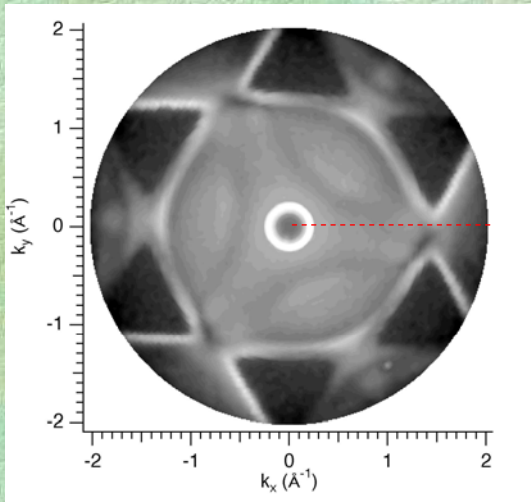
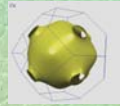


$$\sin \theta = \sin \theta_m \sqrt{\frac{h\nu - \Phi}{h\nu - \Phi + V_0}}$$

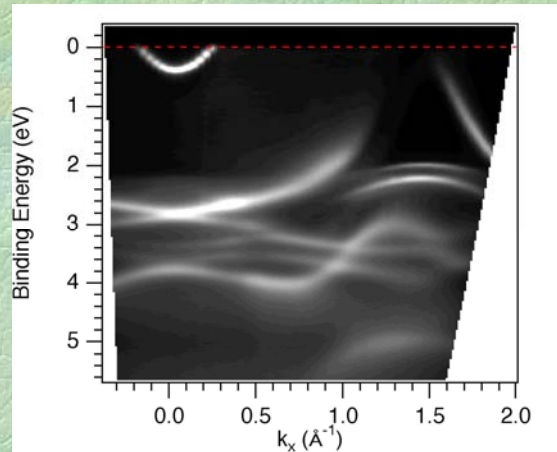
$\Phi$  : work function  
 $V_0$  : inner potential

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# Angle-Resolved Photoemission from Cu(111)

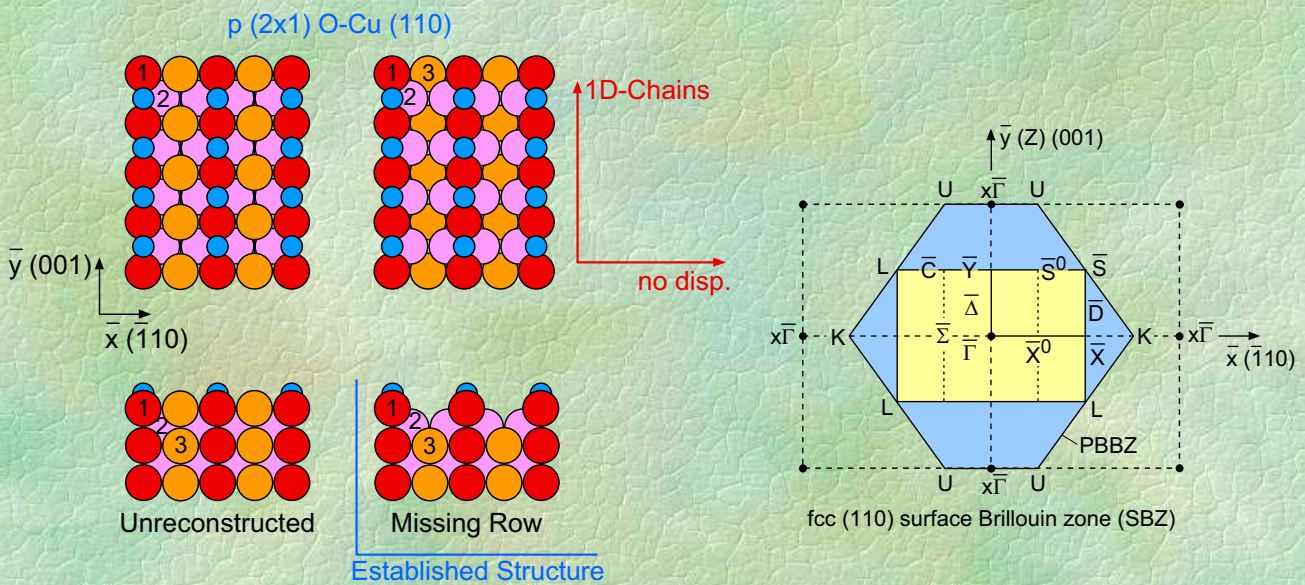


$E_i = E_{fermi}$  scanning of  $(\theta, \phi)$ :  
Cut through the bulk Fermi surface



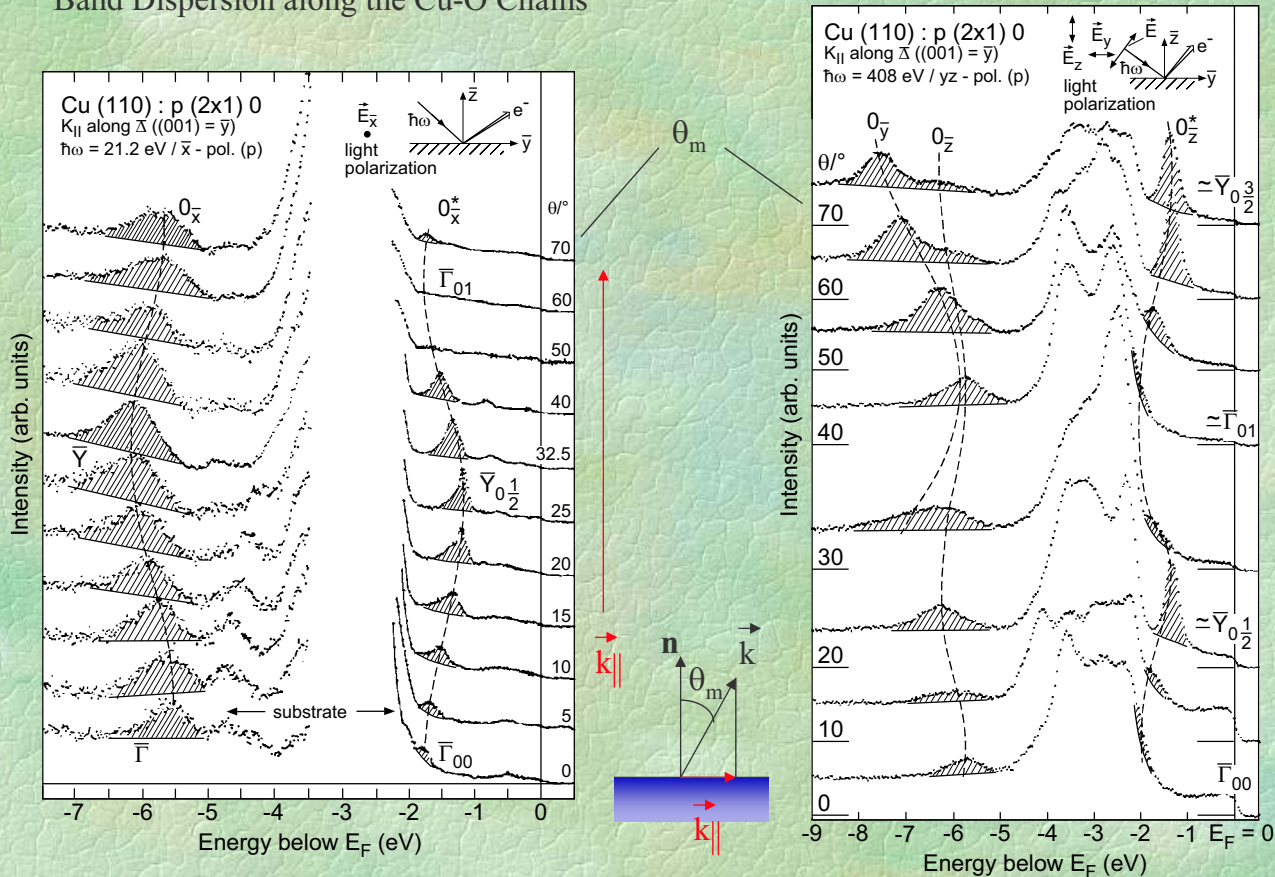
scanning of  $E_i$  and  $\theta$ :  
Band structure along curved line in  
3D k - space

## A One-Dimensional Example:



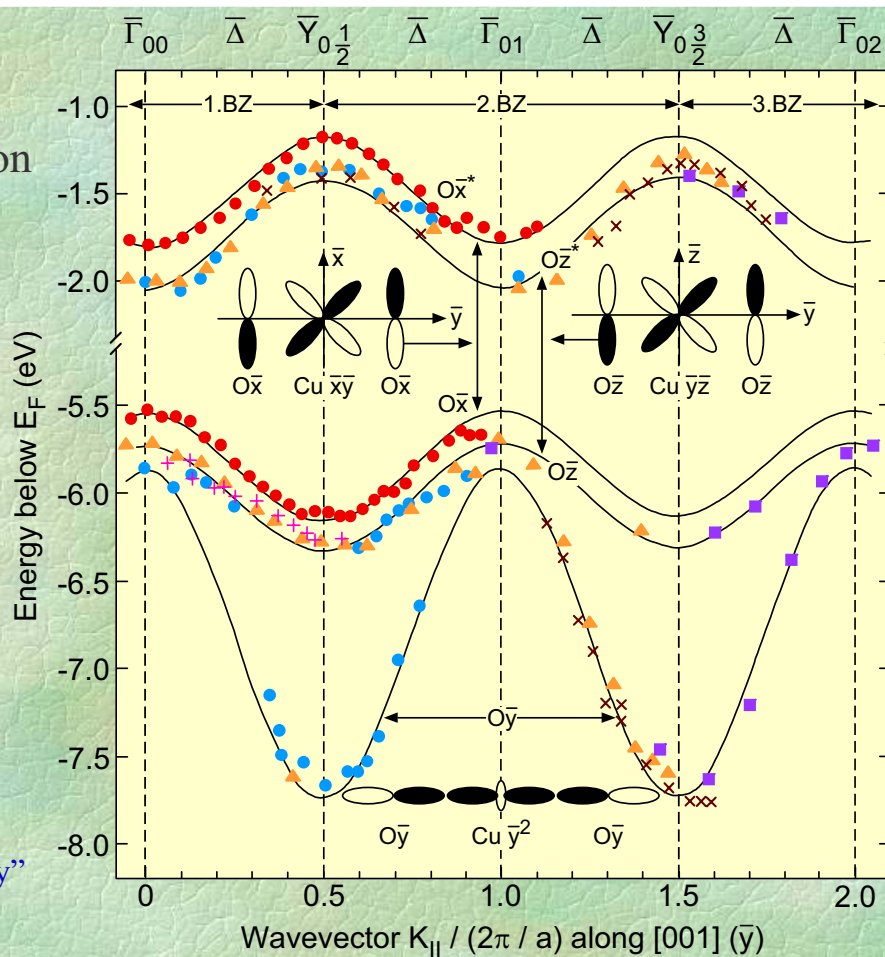


# Band Dispersion along the Cu-O Chains

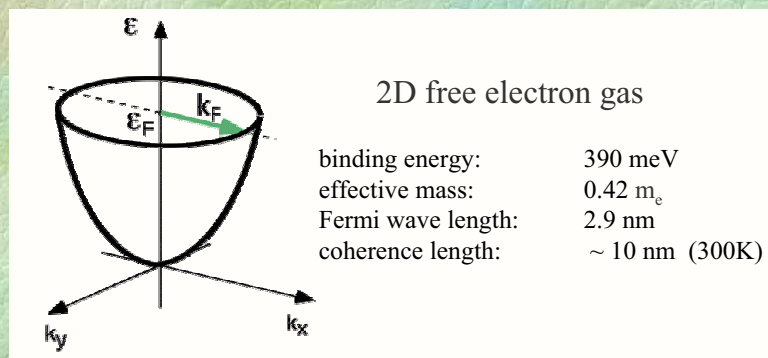
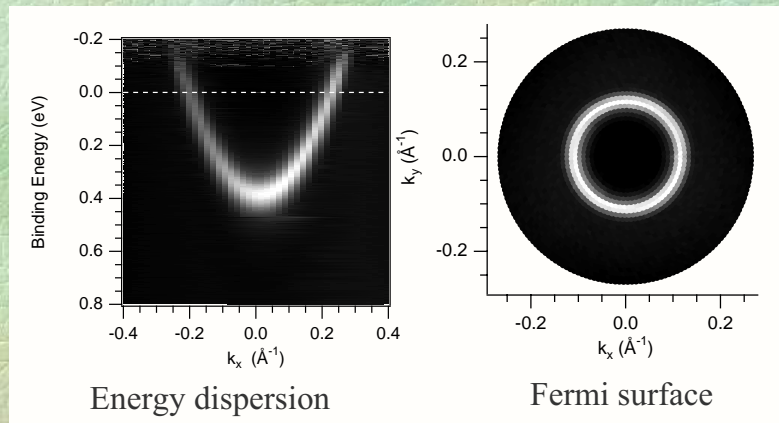


# Finding all the States - Interpretation

Often a simple tight binding model works quite well !

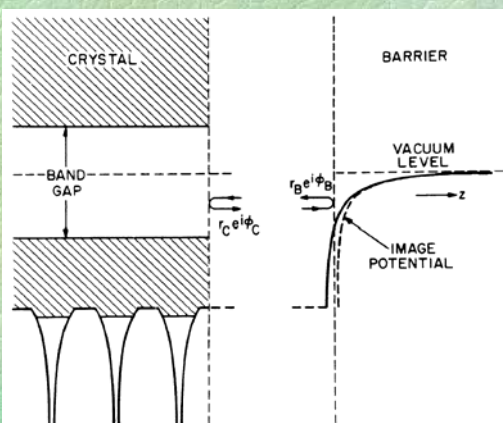


## A 2D Example: The Shockley Surface State on Cu(111)

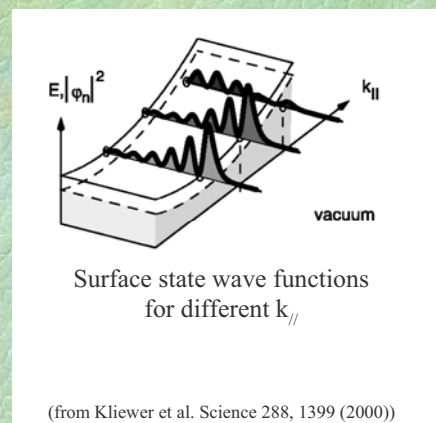


## Multiple reflection model for surface states:

(N.V. Smith, PRB 32, 3549 (1985))



N.V. Smith, PRB 32, 3549 (1985)



$$\phi_c + \phi_b = 2\pi n$$

$$\text{Cu(111), } n = 0: E_B = 0.3\text{eV}, m^* = 0.5m_e$$

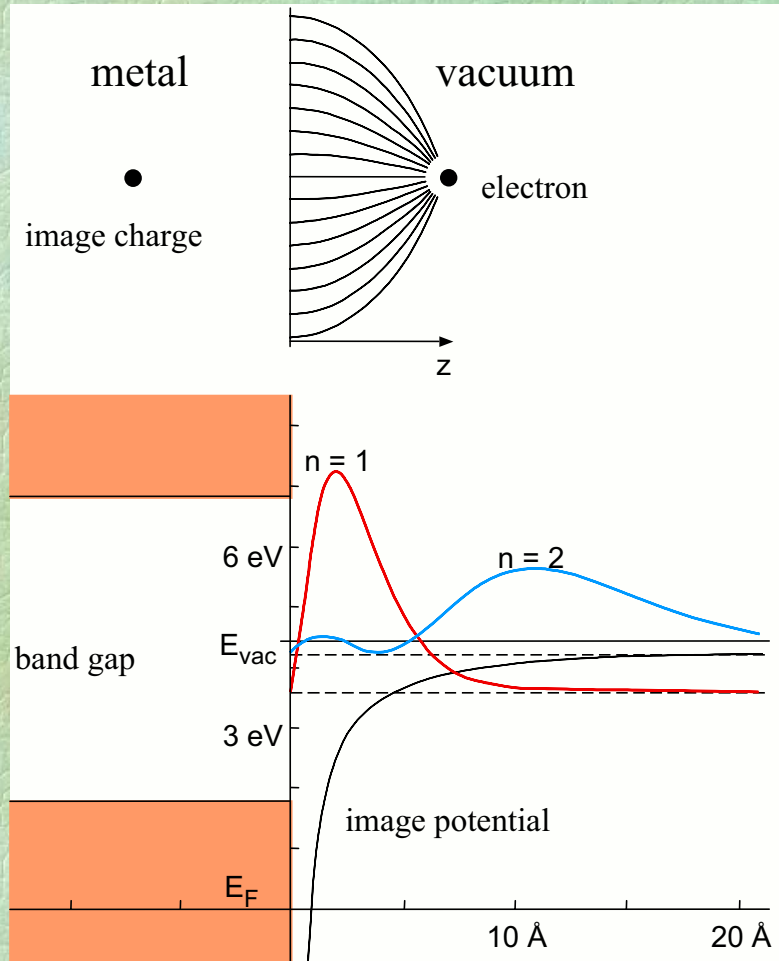
# The Long-Range Image Potential Near a Metal Surface

Image Potential States:

$$E_B = 0.85 \text{ eV} / (n+a)^2$$

(hydrogen-like Rydberg Series, with 'quantum defect' accounting for electron reflectivity at the metal surface)

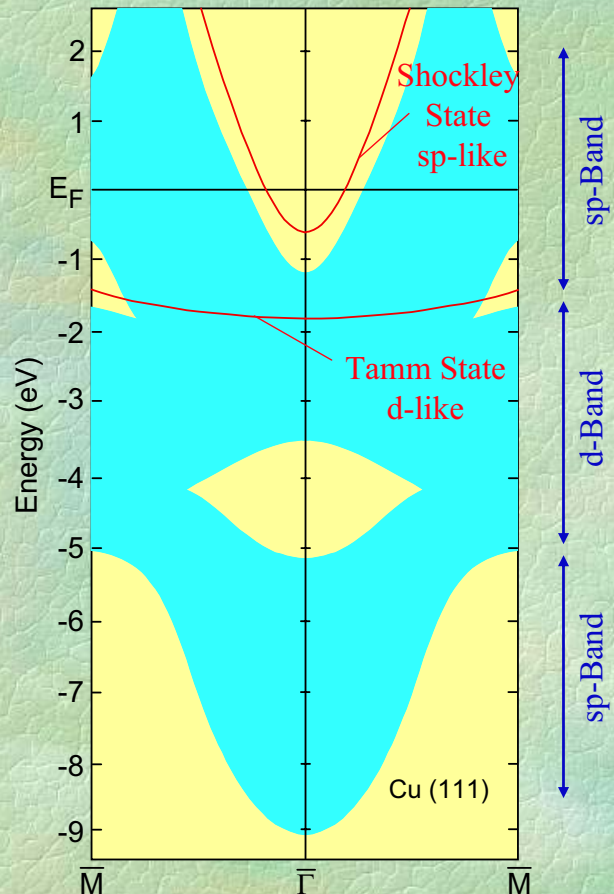
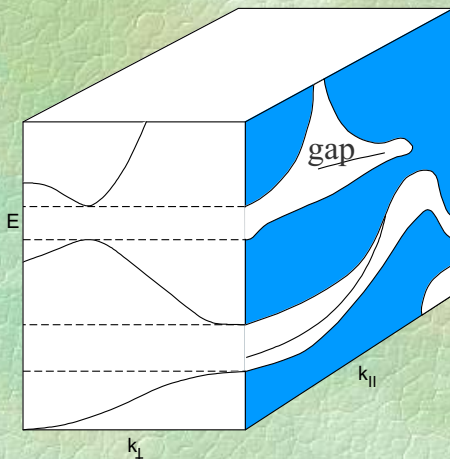
T. Fauster, *Appl. Phys. A* 59, 63 (1994)



# Where do surface states live in k space?

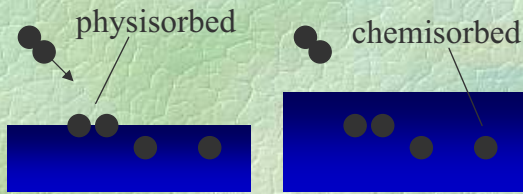
Experimental identification:

- "crud test" (sensitivity to adsorbates)
- no dispersion in  $k_{\text{perp}}$  (use synchrotron rad.)
- lives in projected band gap



## Are Surface States Important at All ?

### Dissociative chemisorption:

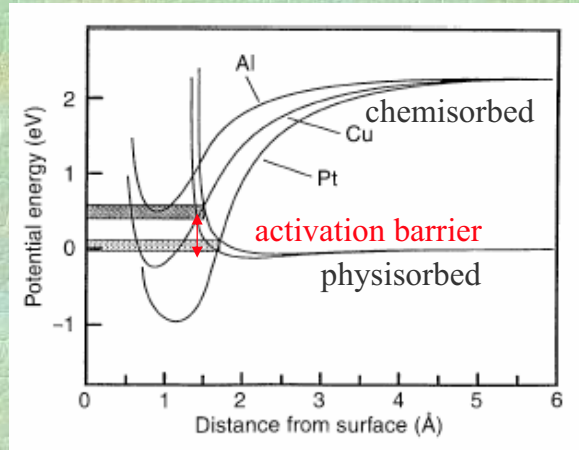


Without S.S.

With S.S.

E. Bertel et al.,

Appl. Phys. A 63, 523 (1996)



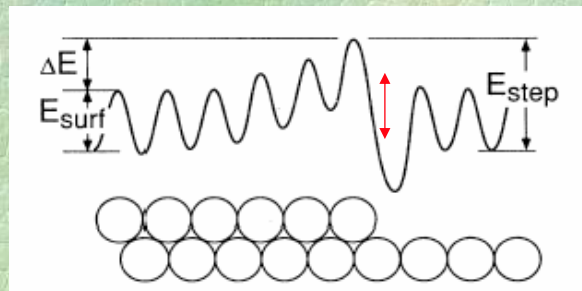
### Surface Diffusion:

**Schwöbl barrier** is reduced by surface state !

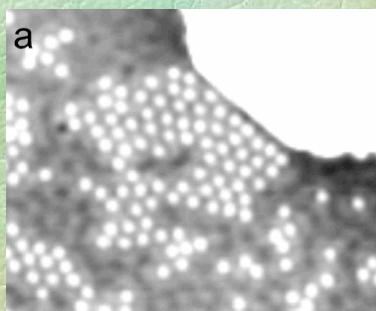
⇒ Adatoms can move across steps.

⇒ Layer-by-layer growth of films

Mommel, Bertel, PRL 75, 485 (1995)



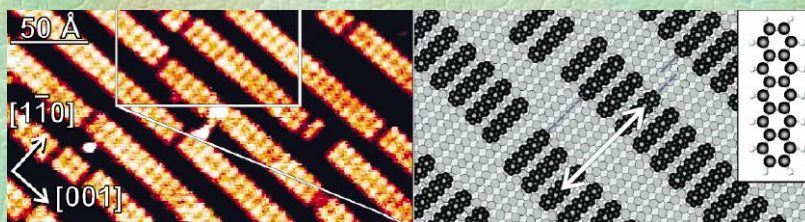
## Surface state mediated long range interactions of adatoms and adsorbates



Cu/Cu(111), T=15K:

Oscillatory interaction with  $\lambda_r/2=14\text{\AA}$

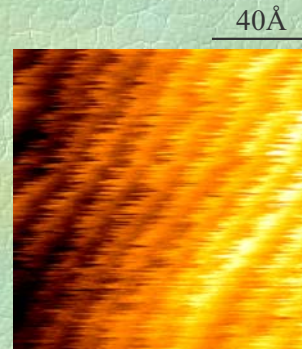
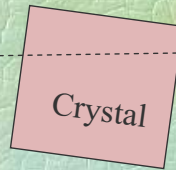
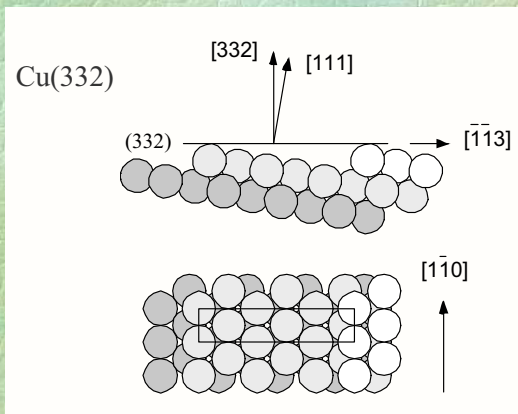
J. Repp et al., PRL 85, 2981 (2000)



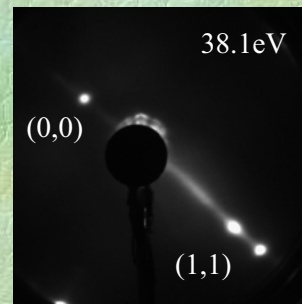
Pentacene, on Cu(110)

S. Lukas et al., PRL 88, 028301 (2002)

# Vicinal Cu(111) Surfaces



Scanning tunneling microscopy (STM), Cu(332)

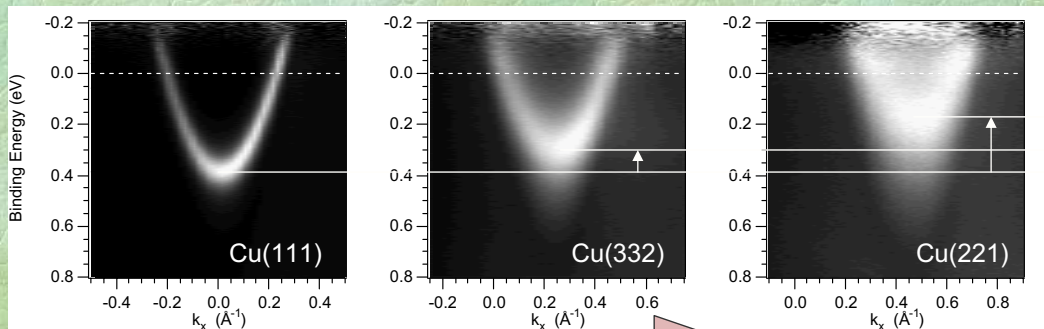


Low energy electron diffraction (LEED), Cu(332)

	Cu(112)	Cu(221)	Cu(332)	Cu(443)
$\alpha$	19.5°	15.8°	10.0°	7.3°
$l$	6.24Å	7.66Å	12Å	16.3Å
$n$	3	4	6	8

Neat way for nanostructuring surfaces !

## How does the electron gas react to the steps ?

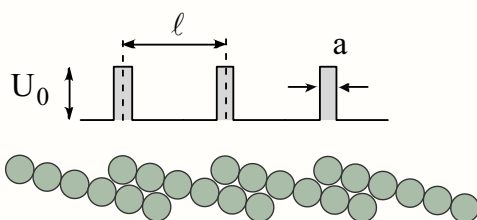


Decreasing terrace width ( $l$ )

1D periodic potential:

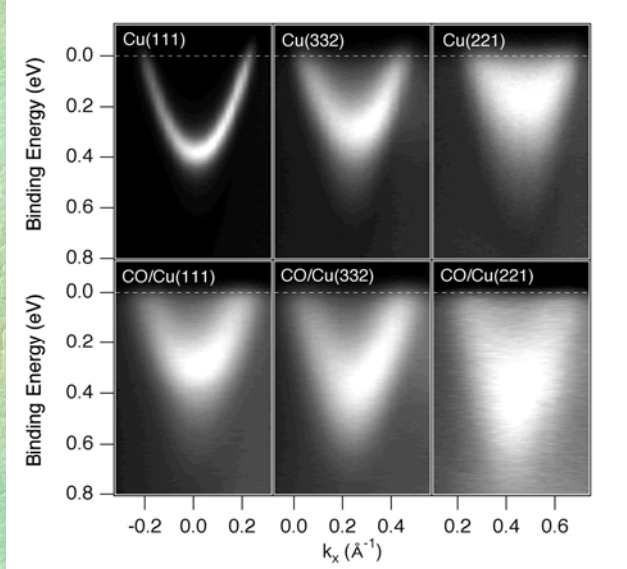
$$\Delta E_B = \frac{U_0 a}{l}$$

$$U_0 a = 1.3 \text{ eV \AA}$$



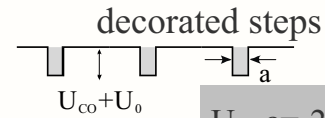
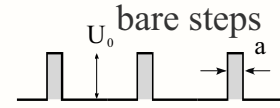
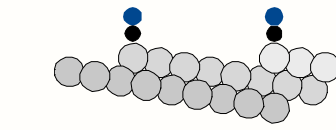
Steps act as potential barriers

# Tailoring confining barriers: CO/vicinal Cu(111)



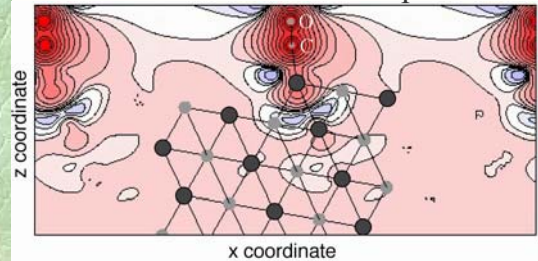
F. Baumberger et al.,  
PRL 88, 237601 (2002)

CO molecules decorate steps

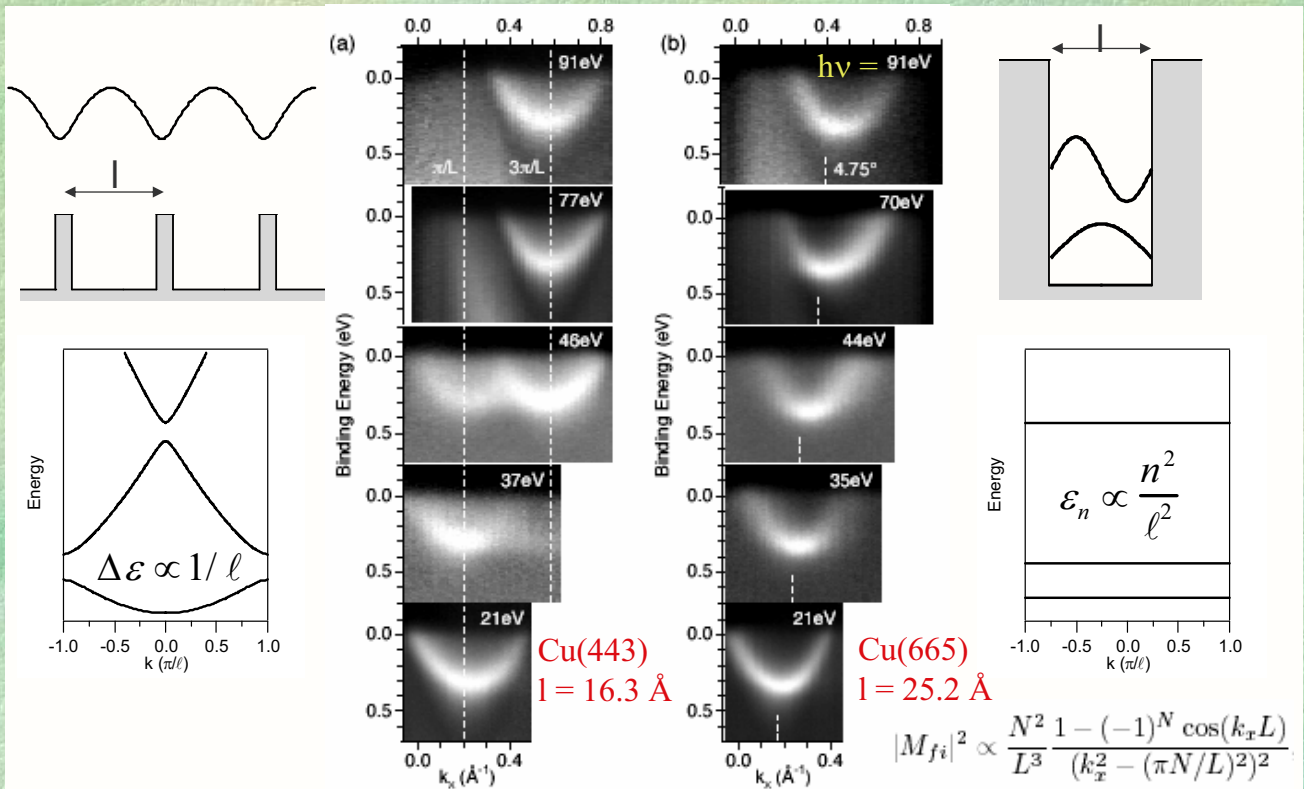


$$U_{CO}a = -2.9\text{eV}\text{\AA}$$

Difference in electrostatic potential



# Periodic potential or decoupled quantum wells?

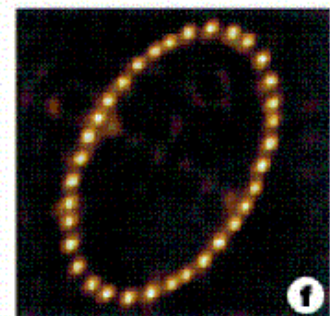
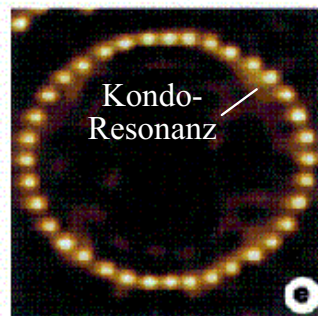
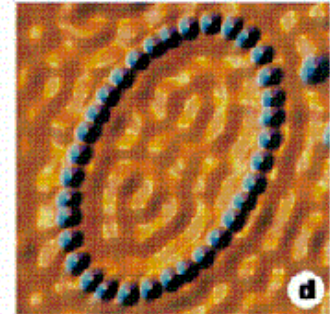
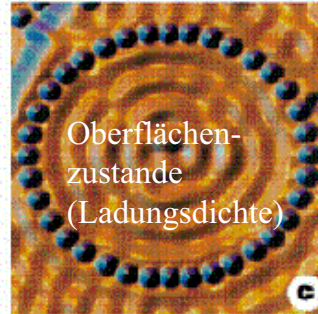
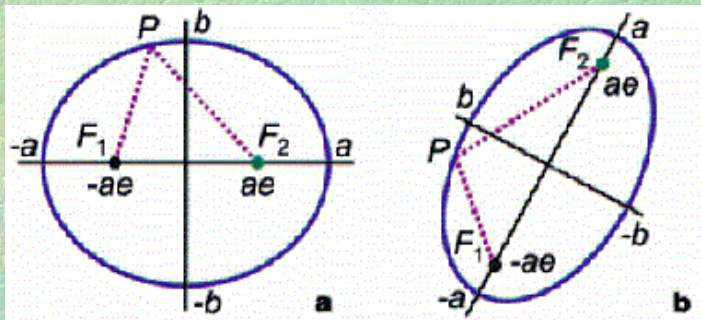


Photon energy ( $k_{\text{perp}}$ ) dependence can unravel the character of the wave functions

Elliptical  
"Quantum Corrals"  
Prepared and Imaged  
by a 4K STM

H. C. Manoharan, C. P. Lutz,  
D. M. Eigler,  
Nature 403 (2000) 512

Valence Bands - Lecture 1



# Photoemission from Valence Bands, Dispersion and Fermi Surface Mapping

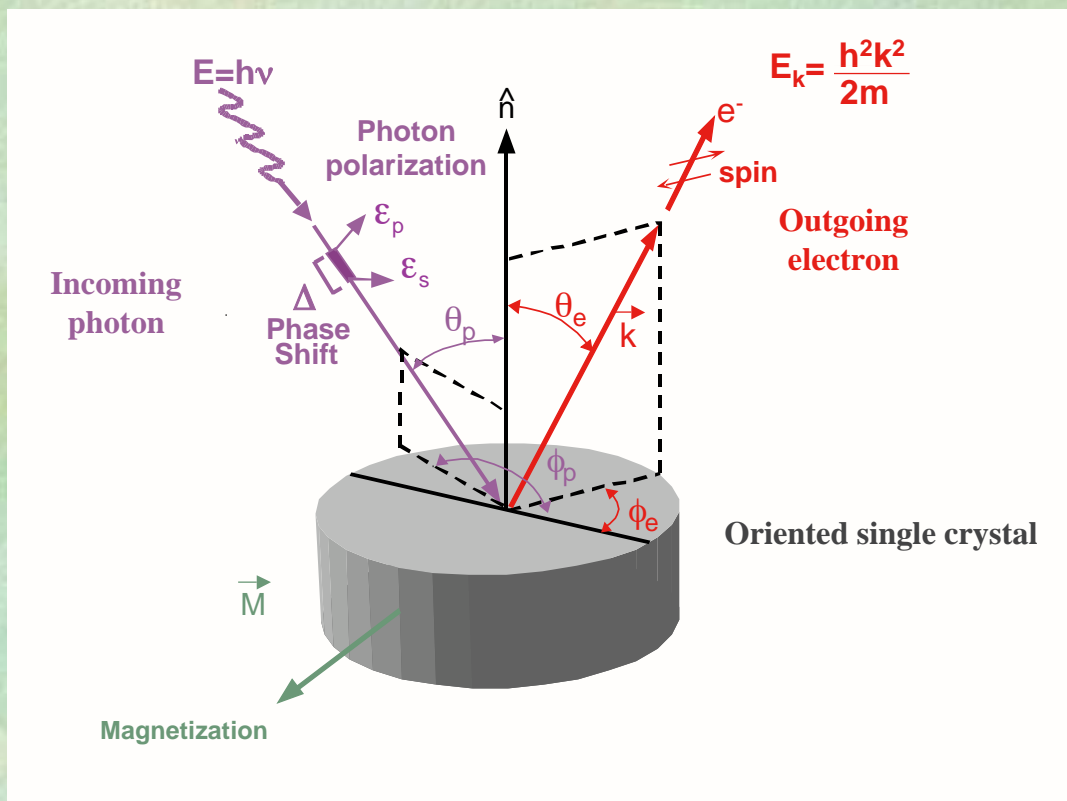
Jürg Osterwalder

Physik-Institut, Universität Zürich, Winterthurerstr. 190,  
CH-8057 Zürich, Switzerland - [osterwal@physik.unizh.ch](mailto:osterwal@physik.unizh.ch)  
<http://www.physik.unizh.ch/groups/grouposterwalder/>

## Lecture 2

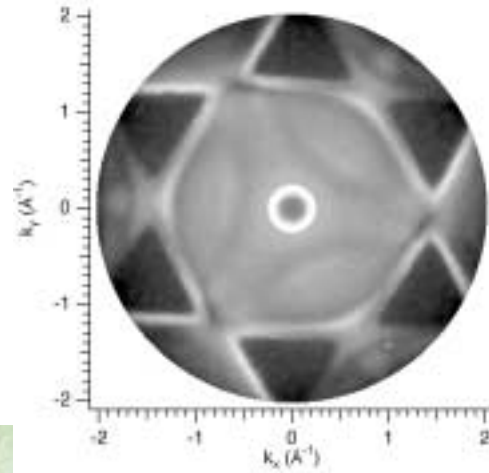
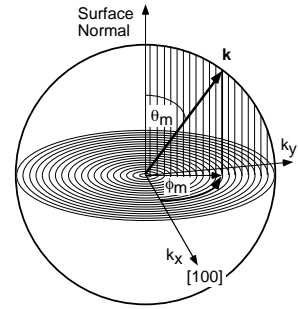
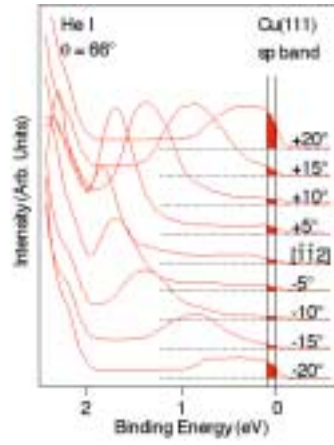
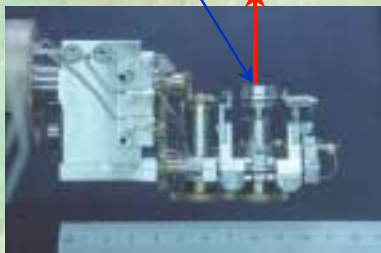
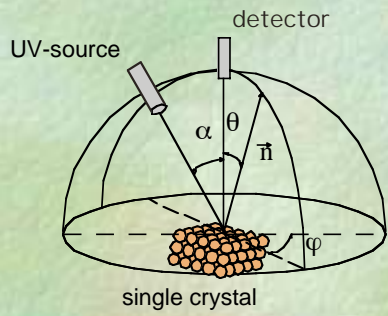
- Constant Energy Mapping in 3D Systems
- A Few Words about the Fermi Surface in General
- 3D Examples for Fermi Surface Mapping: Cu, Al
- The Fermi Surface of Ni: Case of an Itinerant Ferromagnet
- The Magnetic Phase Transition in Ni: More Details

## The photoemission experiment

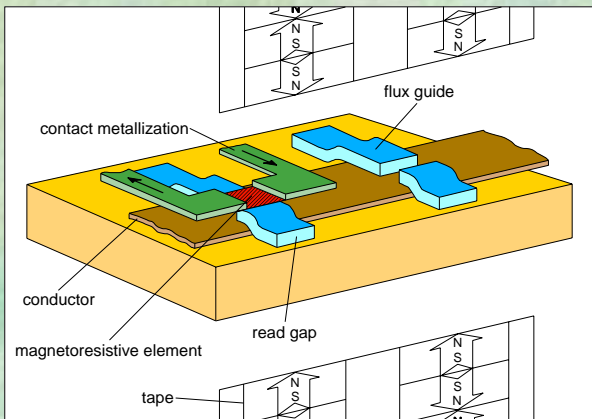




# Fermi Surface Mapping by Photoemission



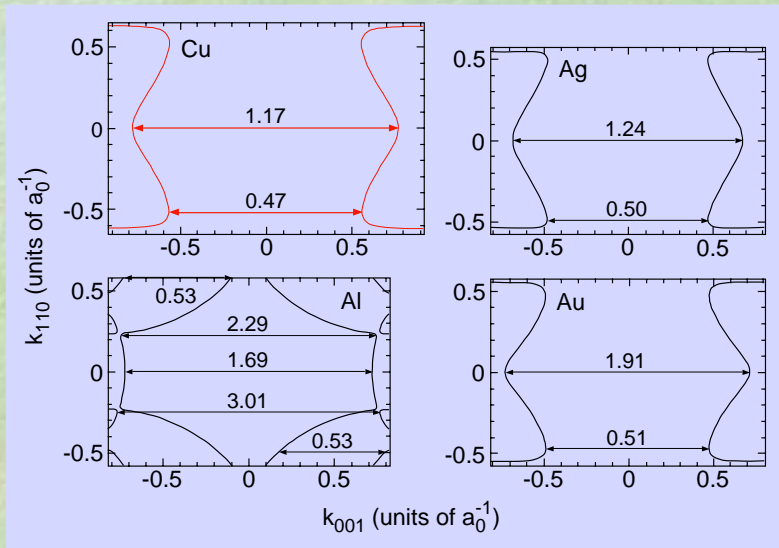
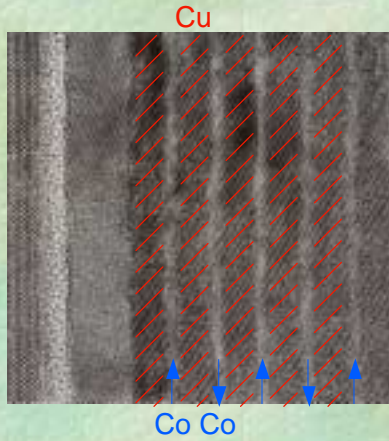
# Magnetic Read Heads Based on Giant Magneto-Resistance in Magnetic Multilayers



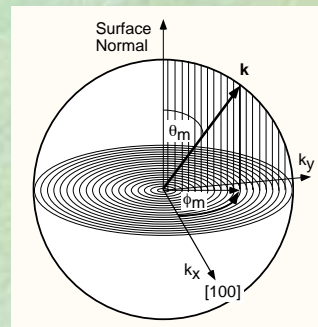
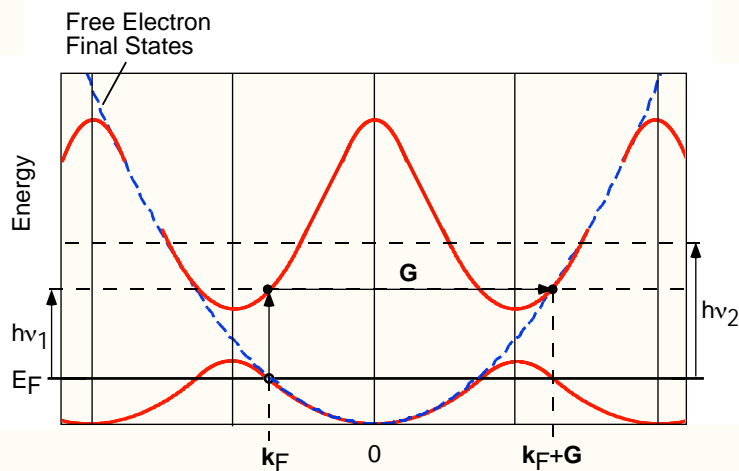
Exchange coupling in magnetic heterostructures

M. D. Stiles

National Institute of Standards and Technology, Gaithersburg, Maryland 20899  
(Received 3 May 1993)



Direct Transitions from the Fermi Surface



$$E_{kin}^m = h\nu - \Phi - E_B$$

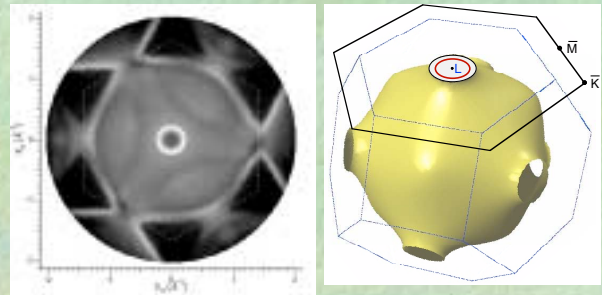
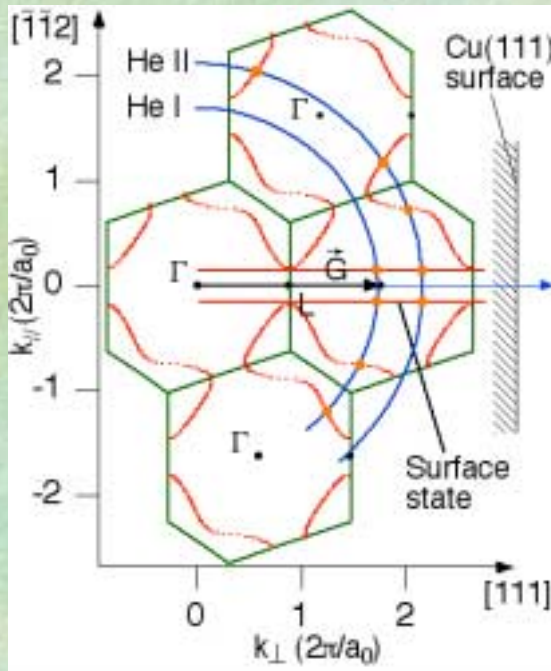
$$|\vec{k}_{||}| = \frac{1}{\hbar} \sqrt{2mE_{kin}^m} \sin \theta_m$$

$$k_{\perp} = \frac{1}{\hbar} \sqrt{2m(E_{kin}^m + V_0)} \cos \theta_m$$

Refraction:  $\sin \theta = \sin \theta_m \sqrt{\frac{E_{kin}^m}{(E_{kin}^m + V_0)}}$

# Fermi surface mapping

Section along  $(1\bar{1}0)$  plane in reciprocal space



In the photoemission process:

Energy conservation:

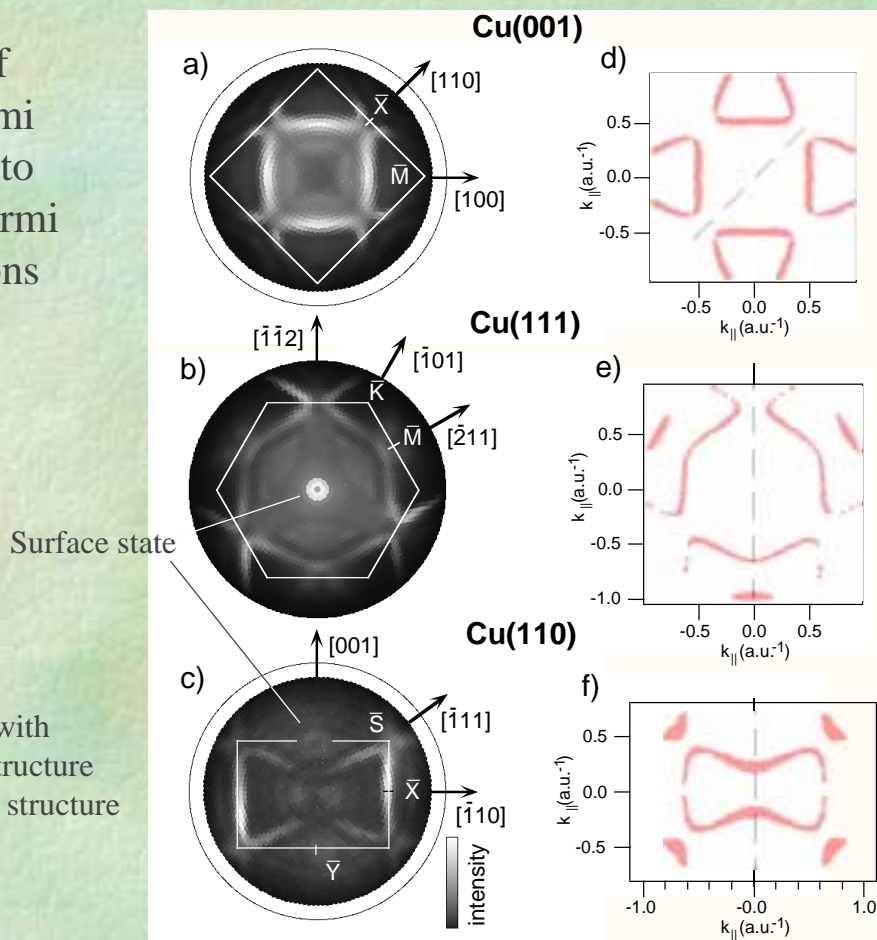
$$E_f = E_i + h\nu$$

Momentum conservation:

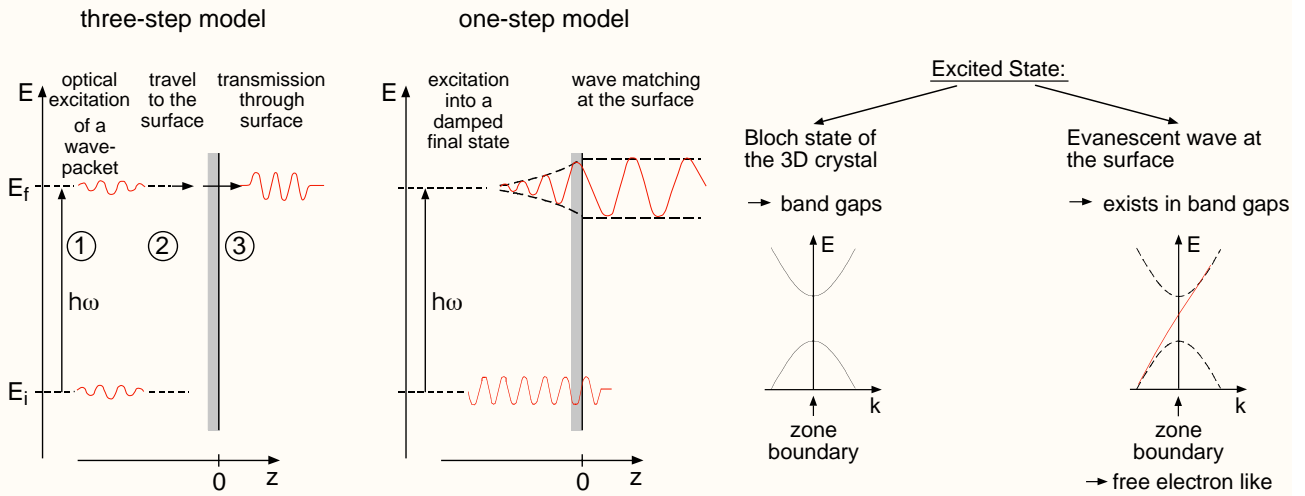
$$\vec{k}_f = \vec{k}_i + \vec{G}$$

## Comparison of Measured Fermi Surface Maps to Calculated Fermi Surface Sections

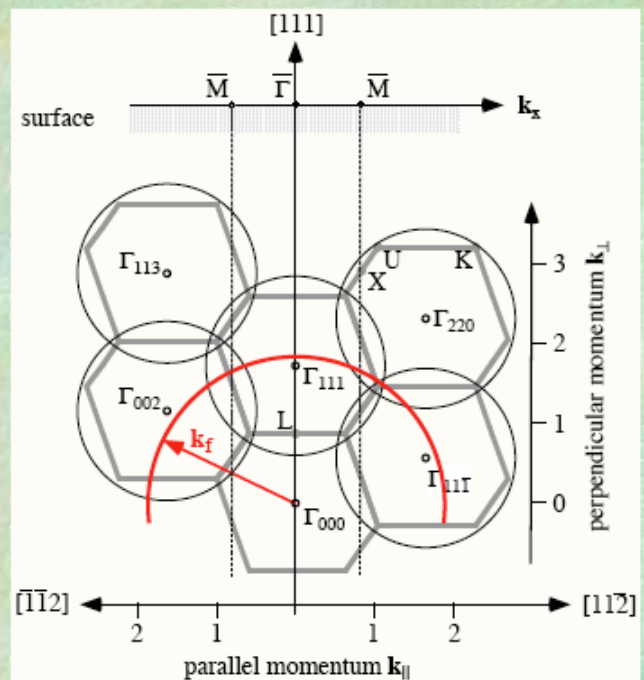
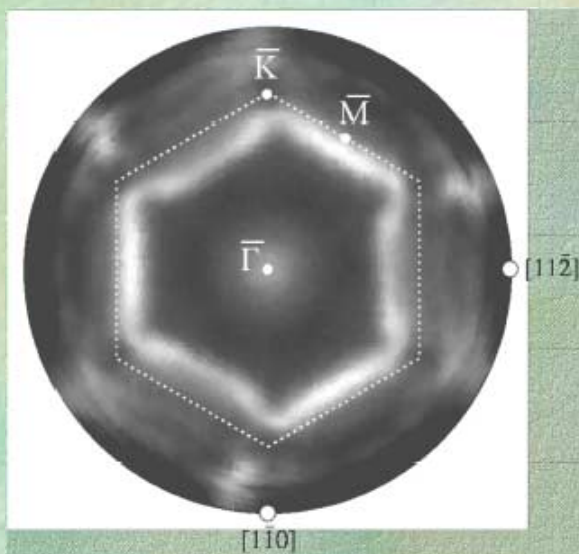
Calculations done with the Wien2k band structure code, assuming the structure of bulk Cu.



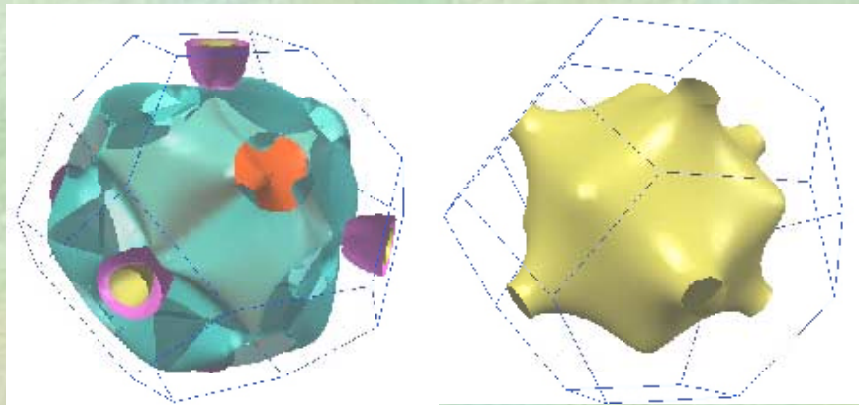
## Comments on the Free Electron Final State



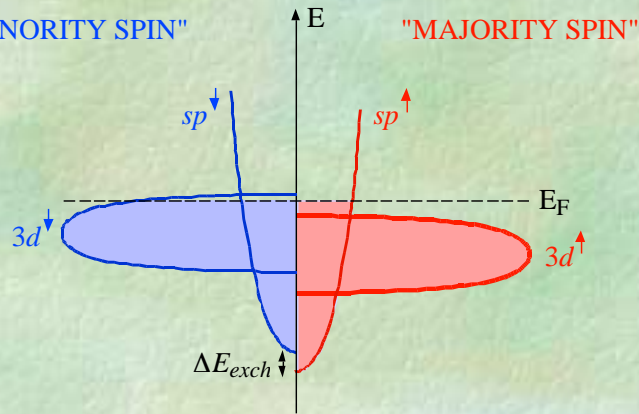
## The Fermi Surface of Aluminium



# The Two Fermi Surfaces of Nickel Metal



Schematic  
Density of States

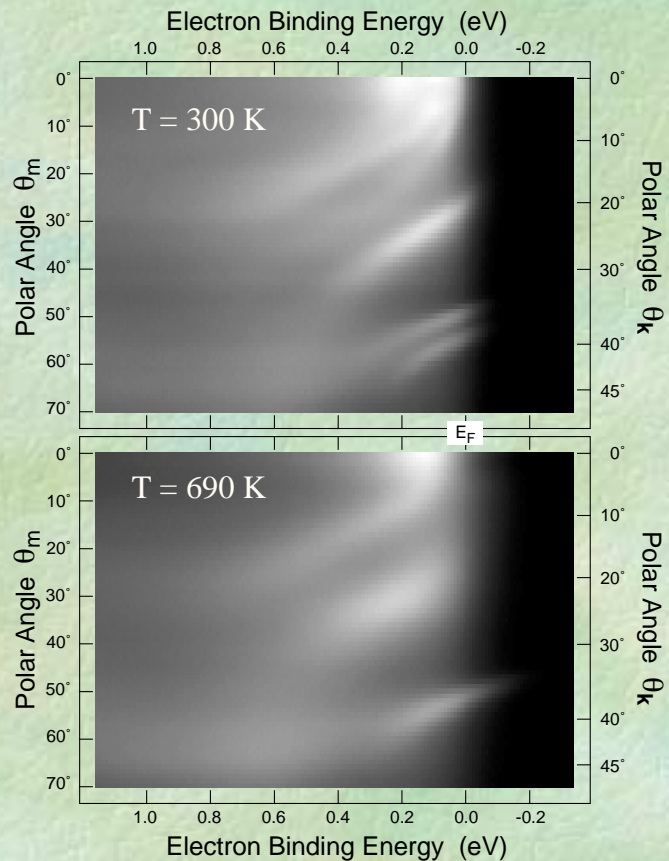


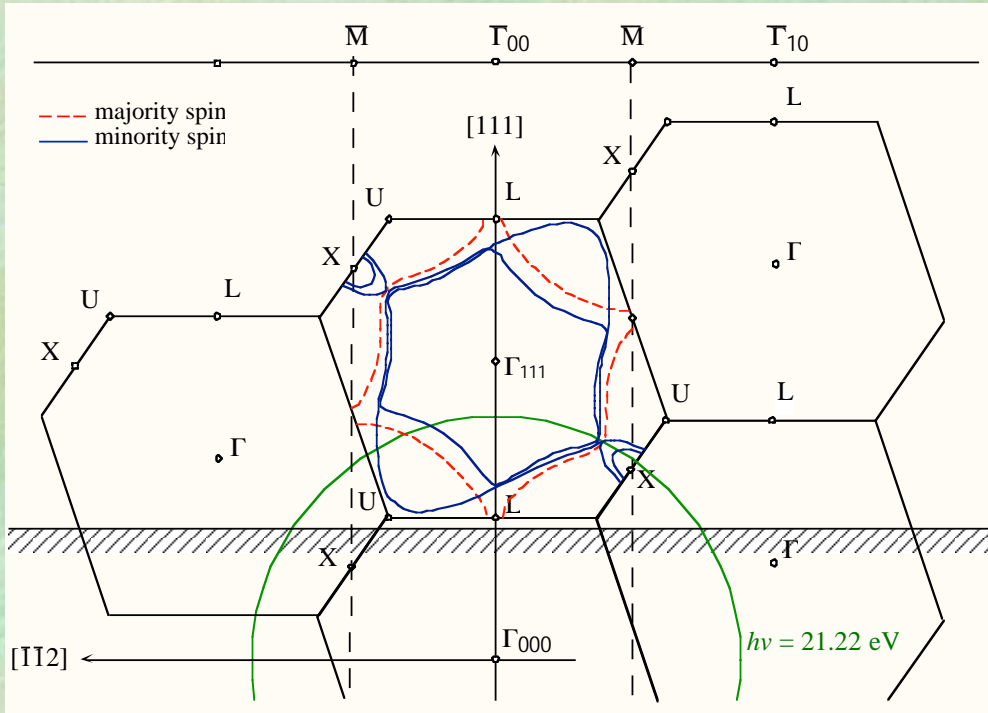
## Monitoring the Magnetic Phase Transition

$$T_c = 631 \text{ K}$$

Question:  
How does the band structure  
change when nickel goes  
from the ferromagnetic to  
the paramagnetic state ?

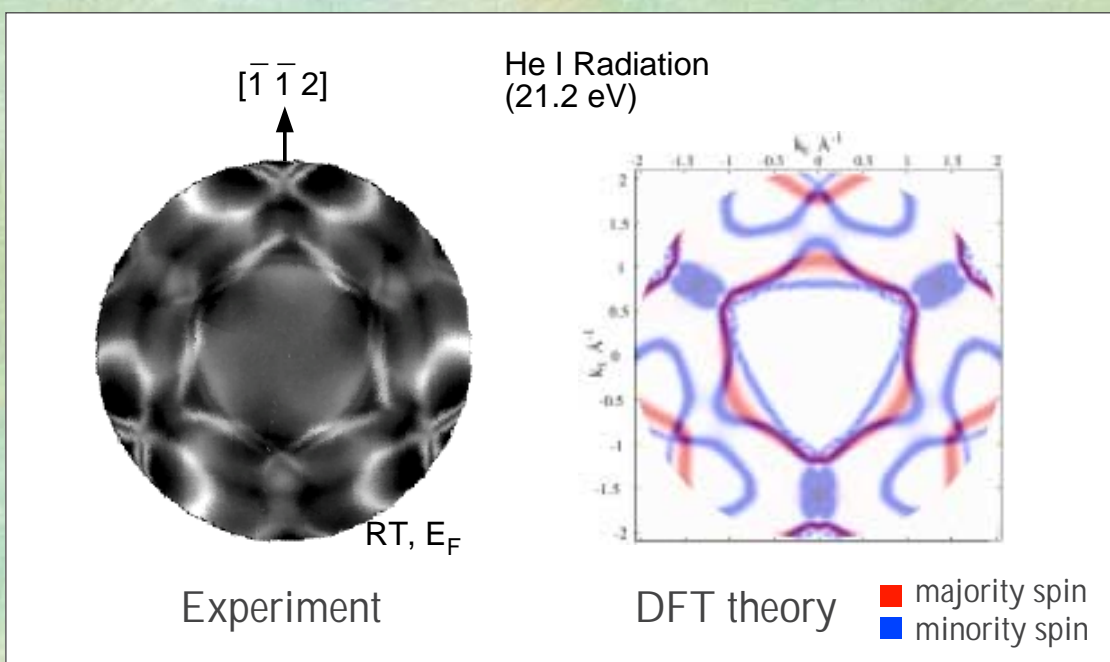
Answer:  
Magnetic exchange  
splittings disappear



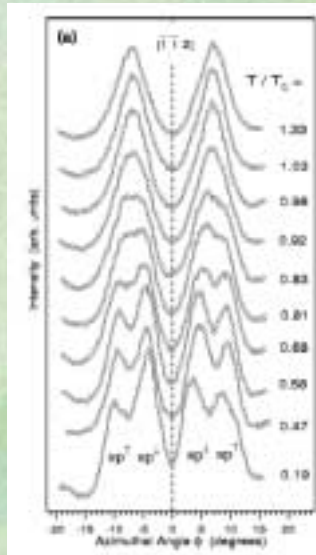
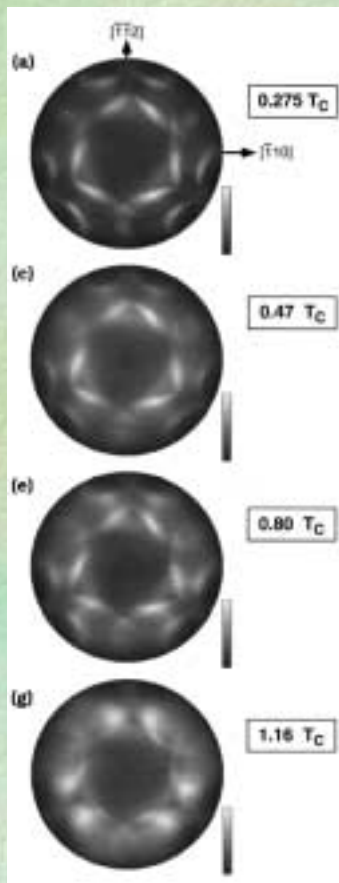


Fermi surface calculation (density functional theory, Wien 97)

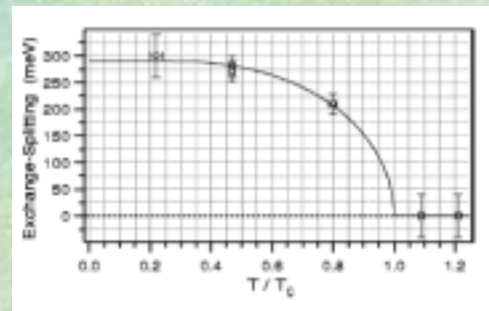
### FermiSurface of Ni as Seen Through the Ni(111) Surface



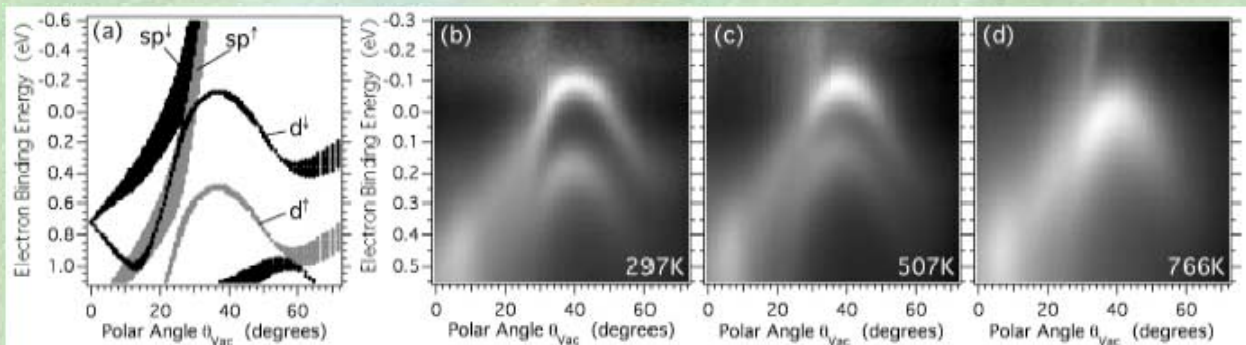
## Evolution of the Fermi Surface During the Phase Transition



... and quantifying the exchange splitting:

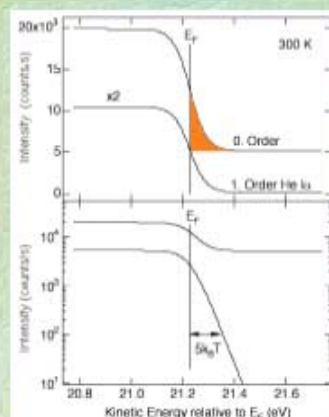


## Observing the Magnetic Exchange Splitting in the d Band



Photoemission above the Fermi Level ?

T. Greber et al., PRL 79, 4465 (1997)

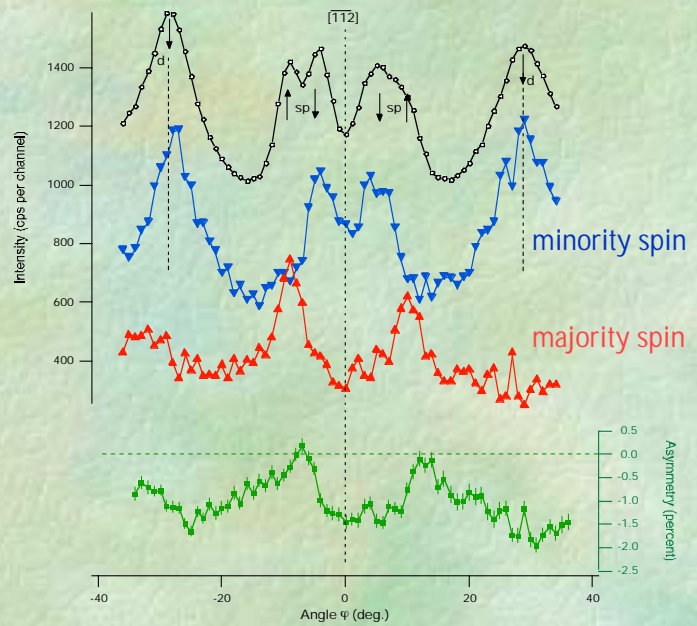
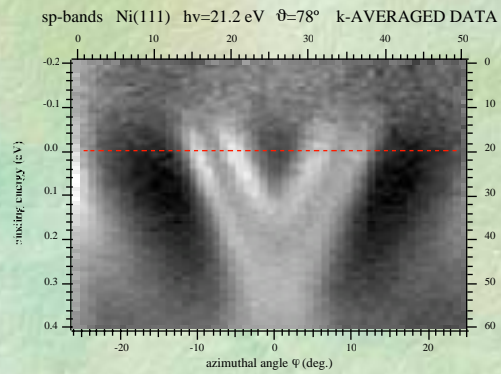
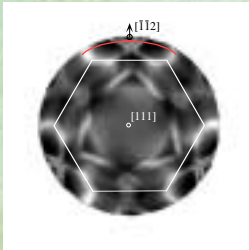


Polar Scan



# Spin-Resolved Fermi Surface Mapping

## Azimuthal Scan



... a new, spin-resolved spectrometer



# Photoemission from Valence Bands, Dispersion and Fermi Surface Mapping

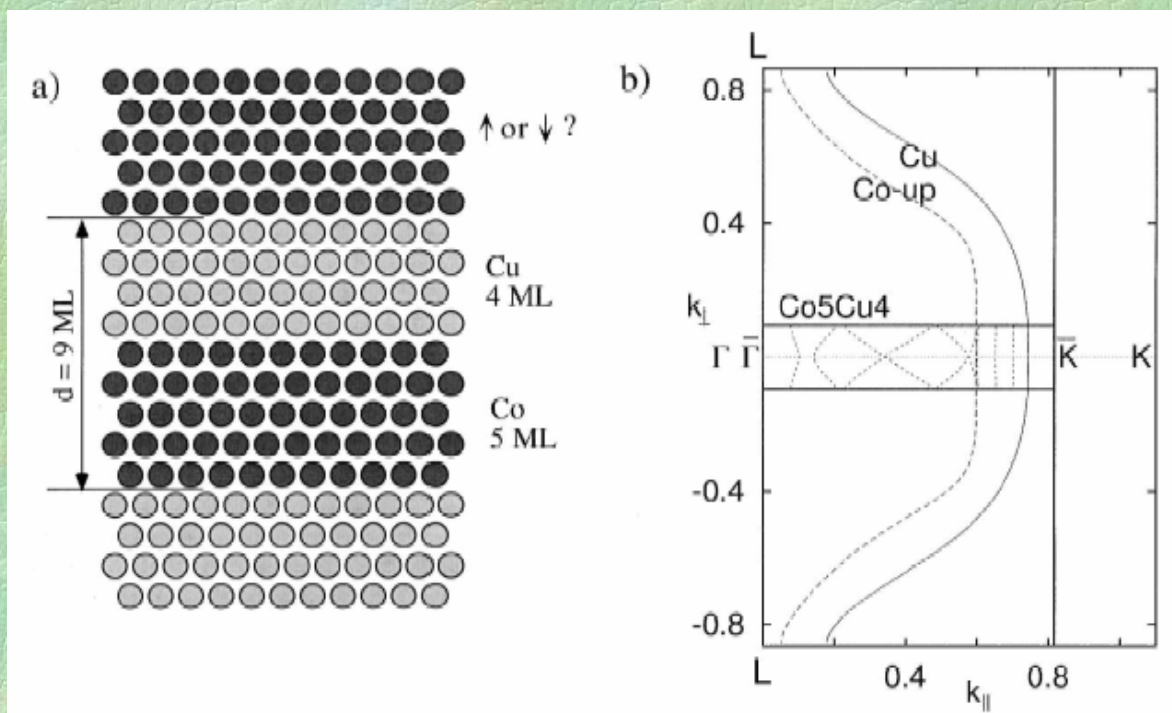
Jürg Osterwalder

Physik-Institut, Universität Zürich, Winterthurerstr. 190,  
CH-8057 Zürich, Switzerland - [osterwal@physik.unizh.ch](mailto:osterwal@physik.unizh.ch)  
<http://www.physik.unizh.ch/groups/grouposterwalder/>

## Lecture 3

- Fermi Surface Mapping with Spin Resolution: Design of a New Spectrometer
- Spin-Resolved Fermi Surface Contours in Nickel
- Spin-Orbit-Split Surface State on Au(111)
- Ultrathin Films of Ni on Cu(001)
- Intensities in Valence Photoemission: Polarization Effects
- Intensities in Valence Photoemission: Atomic Effects
- Intensities in Valence Photoemission: Diffraction Effects

## Magnetic Bandstructure in Multilayered Films



Band folding along  $k_{\text{perp}}$  leads to a multitude of bands!

# Spin-Resolved Fermi Surface Mapping

Problem:

Sample rotation over  $2\pi \Rightarrow$  rotation of the magnetization over  $2\pi$

$\Rightarrow$  need a 3D spin polarimeter !

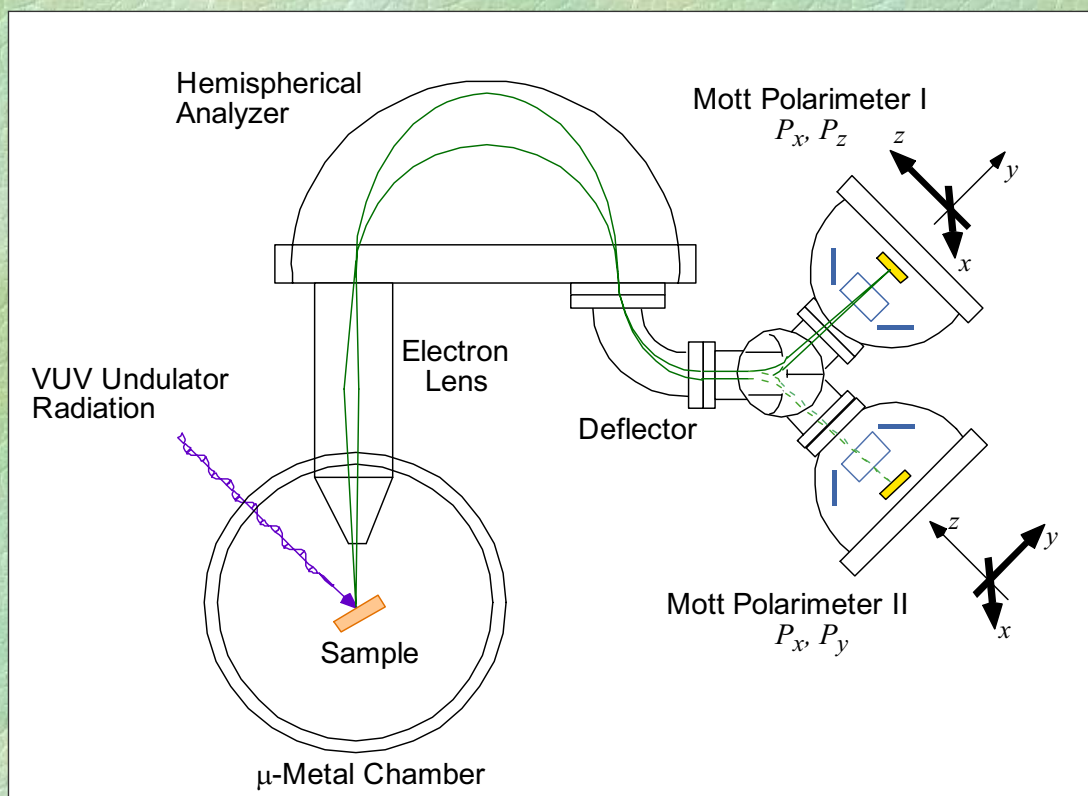
**COPHEE**: the complete photoemission experiment

...measures all properties of the photoelectron:

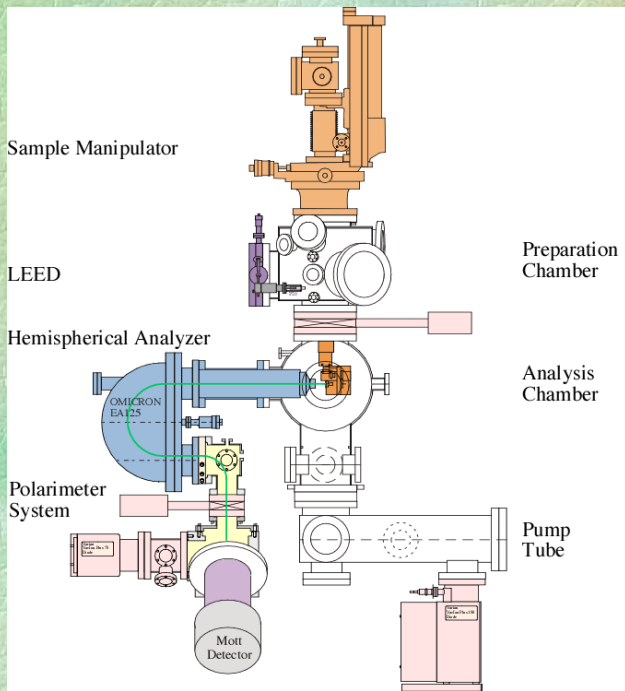
- energy
- momentum ( $\sim$  3D, at the SLS !)
- spin (3D)

... controlled by **CROISSANT** software !

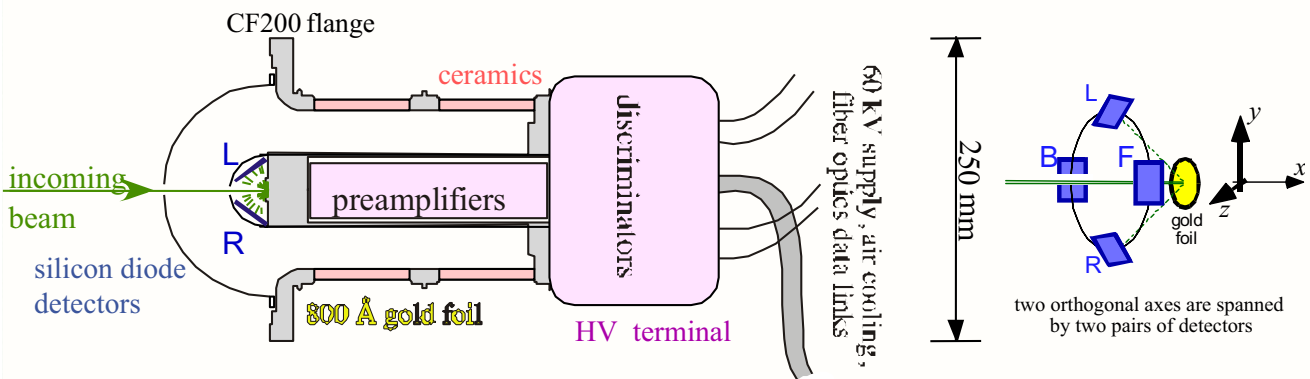
## COPHEE - The Complete Photoemission Experiment



# Setup of COPHEE:



# The 60 keV Mott Detector



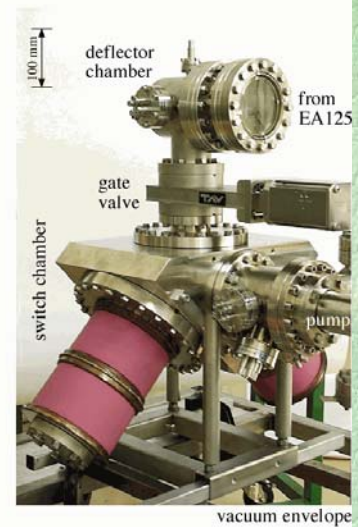
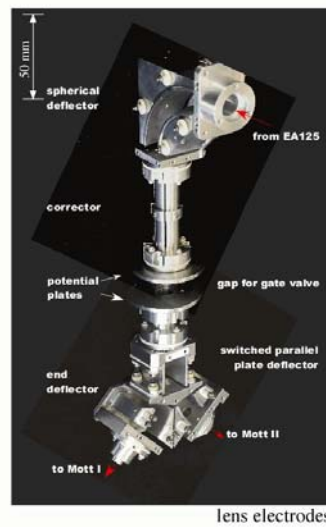
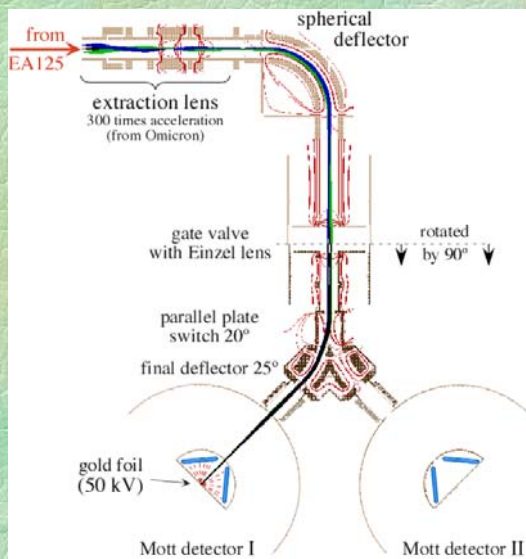
$$\text{asymmetry } A = \frac{(N_L - N_R)}{(N_L + N_R)}$$

$$\text{electron polarization } P = \frac{A}{S}$$

$S$  = "Sherman function"  
(analyzing power)

Backscattering at high energies:  
Very inefficient process ( $\sim 10^{-3}$ )

## The Transfer / Distributor Lens

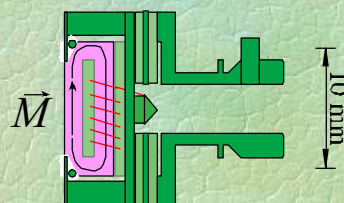
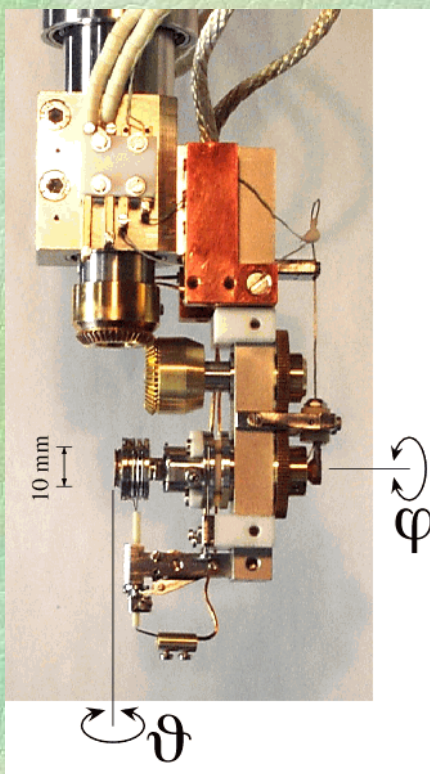


M. Hoesch et al., JES 124, 263 (2002)

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## Goniometer Head of the Sample Manipulator

- 2 axis rotation
- liquid He cooling (60 K)
- contacts for heating and magnetizing
- sample transfer to preparation facilities



Swiss Stub sample holder with picture frame sample



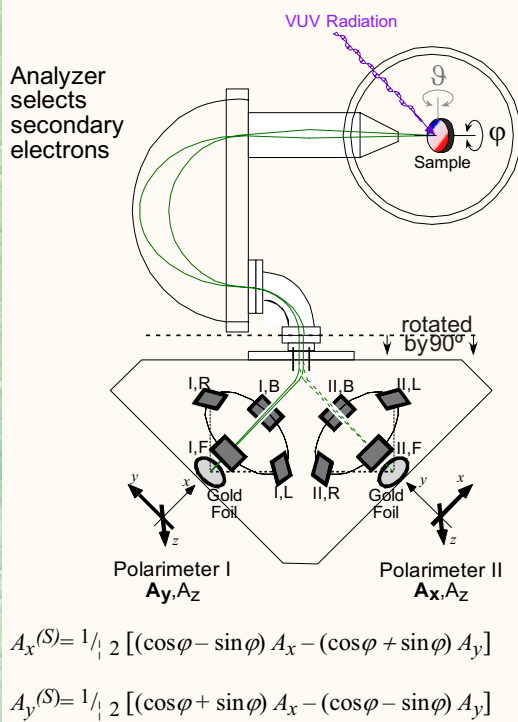
Nickel sample with the filament for DC resistive heating and pulsed current magnetizing remanence ~30%

8

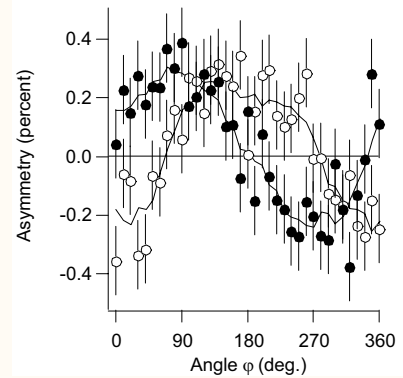
# Secondary electron polarimetry

Courtesy M. Hoesch

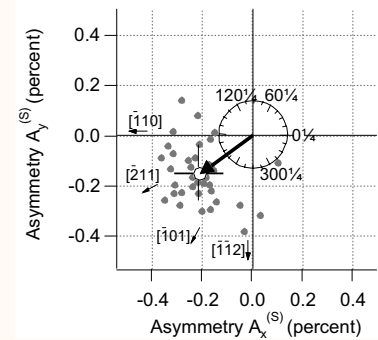
secondary electrons from a magnetized sample are polarized along the magnetization direction (M. Landolt *et al.* 1985)



Measured asymmetries  $A_x, A_y$  (detector coordinates)



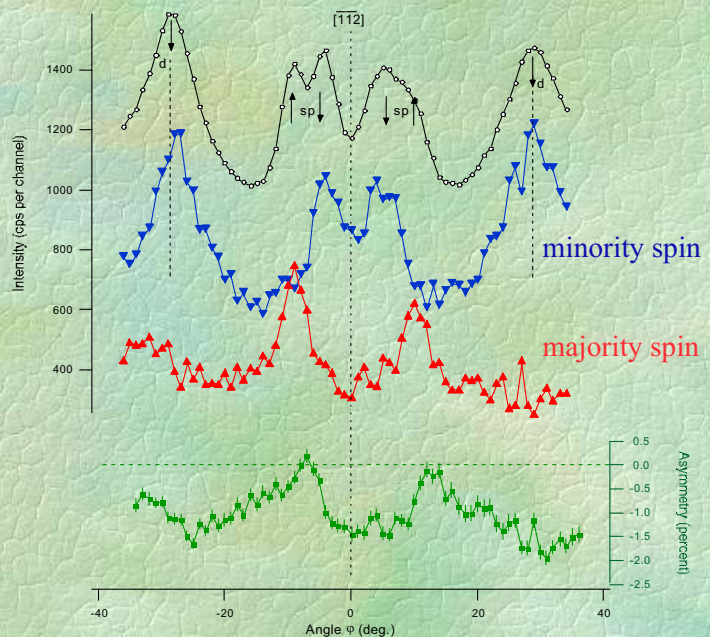
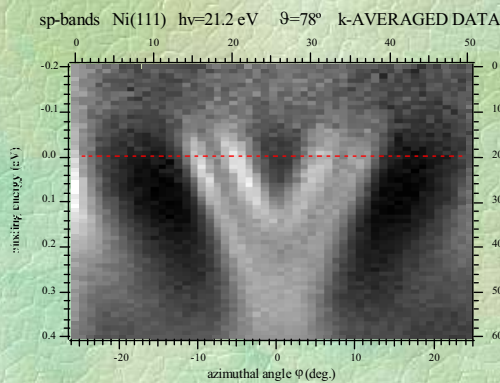
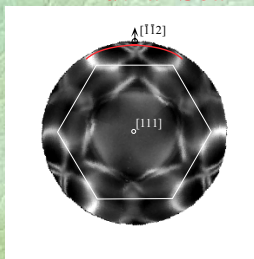
Reconstructed asymmetries  $A_x^{(S)}, A_y^{(S)}$  (sample coordinates)



=> vectorial sensitivity ! 9

# Spin-Resolved Fermi Surface Mapping

## Azimuthal Scan



... a new, spin-resolved spectrometer

## Surfaces/Interfaces: Spectroscopy beamline (SIS) at the Swiss Light Source (SLS)

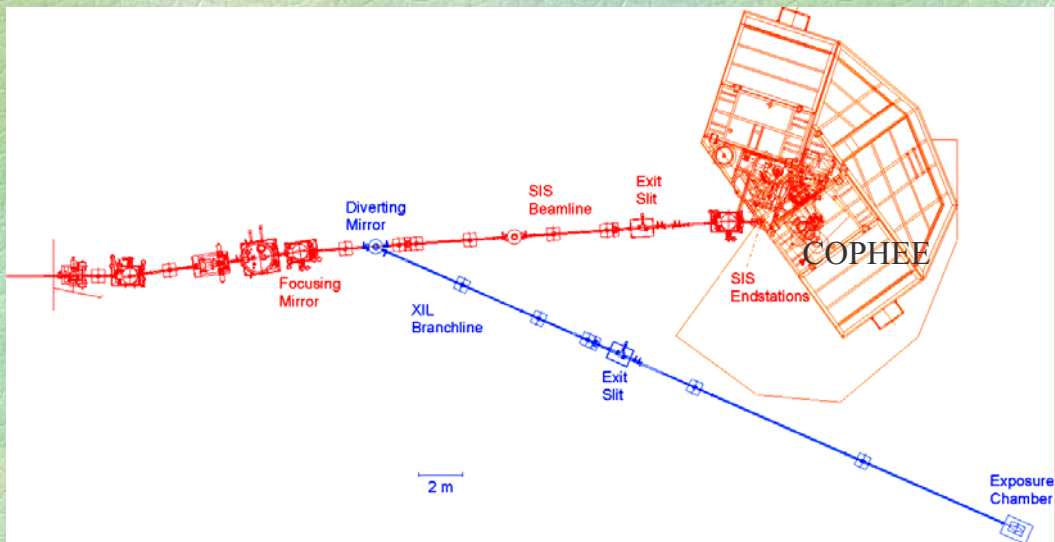
Side view:



Twin UE212

Optics

Spectrometers



## COPHEE at the SIS beamline

⇒ Access to very interesting photon beam properties

- small light spot on sample ⇒ high energy resolution with Omicron EA125 !
- photon energy range: k-space mapping (ARPES) and also core level spectroscopy (incl. XPD)
- fast polarization switching (future) ⇒ dichroism with spin detection
- clean photons (low background in quasiperiodic mode) ⇒ photoemission of thermally excited electrons

First taste: the surface state on Au(111)

# The Spin-Orbit Split Surface State on Au(111)

VOLUME 77, NUMBER 16

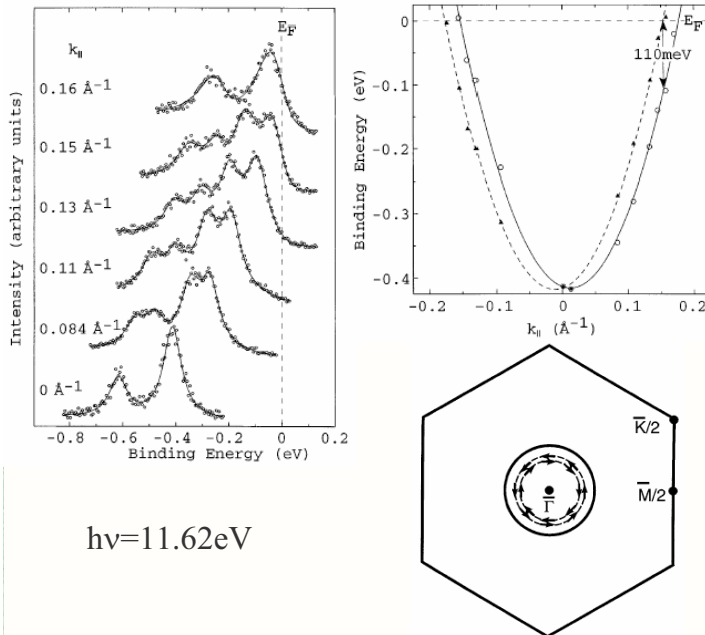
PHYSICAL REVIEW LETTERS

14 OCTOBER 1996

## Spin Splitting of an Au(111) Surface State Band Observed with Angle Resolved Photoelectron Spectroscopy

S. LaShell, B. A. McDougall, and E. Jensen

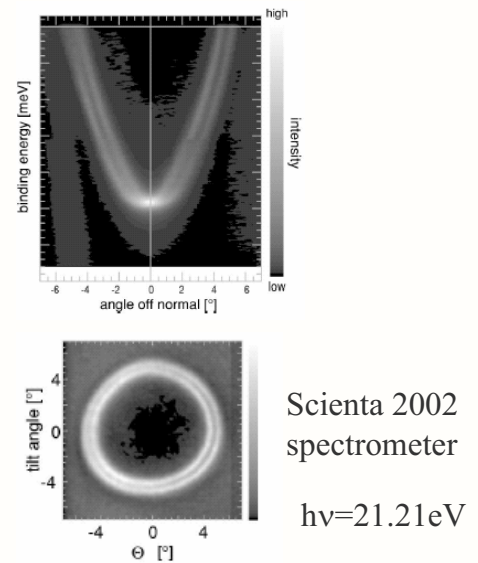
Physics Department, Brandeis University, Waltham, Massachusetts 02254  
(Received 19 July 1996)



PHYSICAL REVIEW B, VOLUME 63, 115415

## Direct measurements of the L-gap surface states on the (111) face of noble metals by photoelectron spectroscopy

F. Reinert,\* G. Nicolay, S. Schmidt, D. Ehm, and S. Hüfner  
Fachrichtung Experimentalphysik, Universität des Saarlandes, 66041 Saarbrücken, Germany  
(Received 6 October 2000; published 1 March 2001)



=> spin-resolution is a challenging task

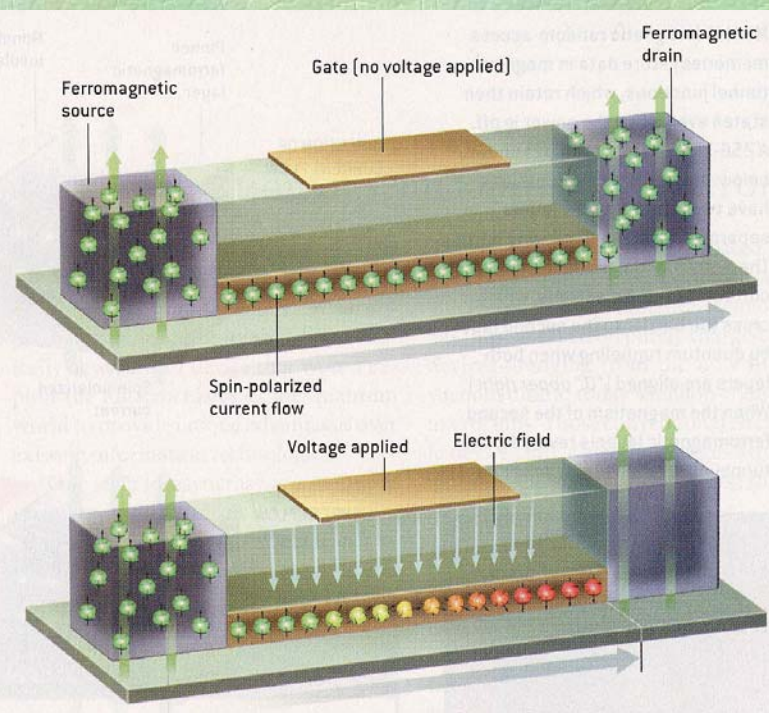
13

# The Spin Field Effect Transistor (spin FET)

**Principle** – electric field from gate causes spins to precess. Channel impedance depends of extent of spin rotation

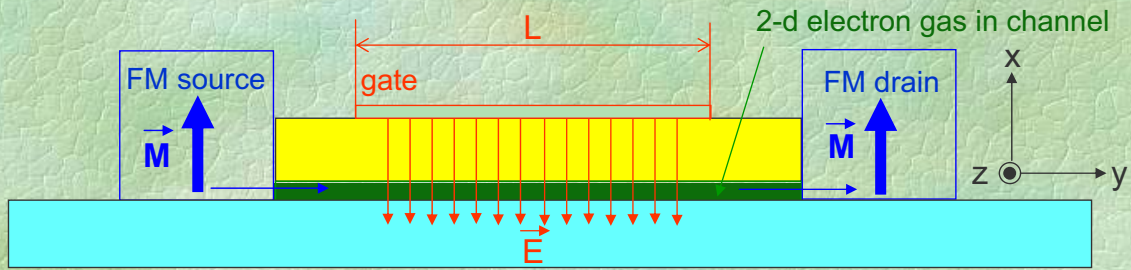
**Advantage** – much less energy and time required to flip spins than to depopulate channel

**Problem** – has yet to be built due to lack of suitable spin injectors for III-Vs and Si. Ferromagnetic semiconductors are best due to conductivity match. Need high  $T_c$  DMS materials!



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# Spin precession in an electric field (?)



Spin-orbit interaction:  $H_{SO} \sim (\vec{E} \times \vec{k}) \cdot \vec{\sigma}$  (Rashba term)

In the channel:  $H_{SO} \sim k_y \sigma_z$

Source: injects spins with  $|s_x\rangle = |-1/2\rangle$

In rotated frame:  $|s_z\rangle = 1/\sqrt{2} |-1/2\rangle + 1/\sqrt{2} |+1/2\rangle$

$$E(|+1/2\rangle) = E_{kin} + \alpha k_y \quad E = E_F \rightarrow k_{F(\uparrow)} - k_{F(\downarrow)} = 2m^*\alpha / \hbar^2$$

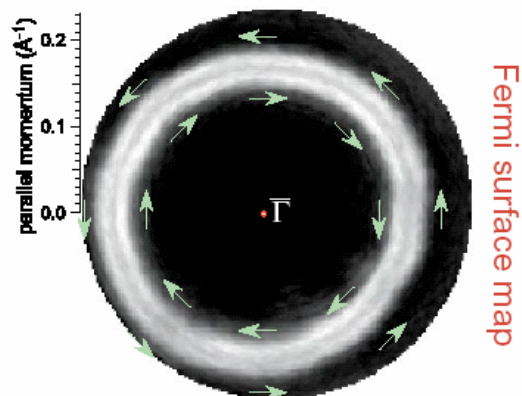
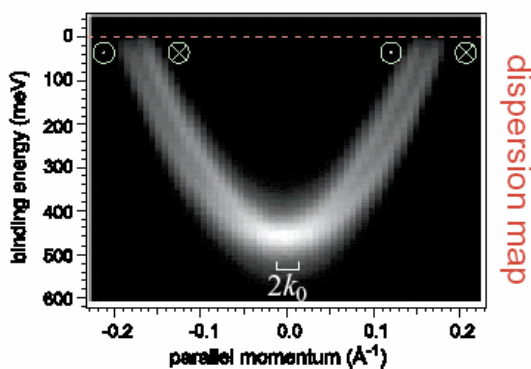
$$E(|-1/2\rangle) = E_{kin} - \alpha k_y$$

$$\rightarrow \text{Phase shift } \Delta\phi = (k_{F(\uparrow)} - k_{F(\downarrow)})L = (2m^*\alpha / \hbar^2)L$$

**→ Spin precession around z axis !**

## The Shockley surface state on Au(111)

spin-integrated photoemission at  $h\nu = 21.1$  eV,  $T = 160$  K instrumental resolution  $\Delta E = 25$  meV,  $\Delta\theta = 0.5^\circ$  (FWHM)



$$2k_0 = 0.026 \text{ \AA}^{-1} \quad E_B = 470 \text{ meV} \quad k_F = 0.173 \text{ \AA}^{-1} \pm k_0 \quad m^* = 0.24 m_e$$

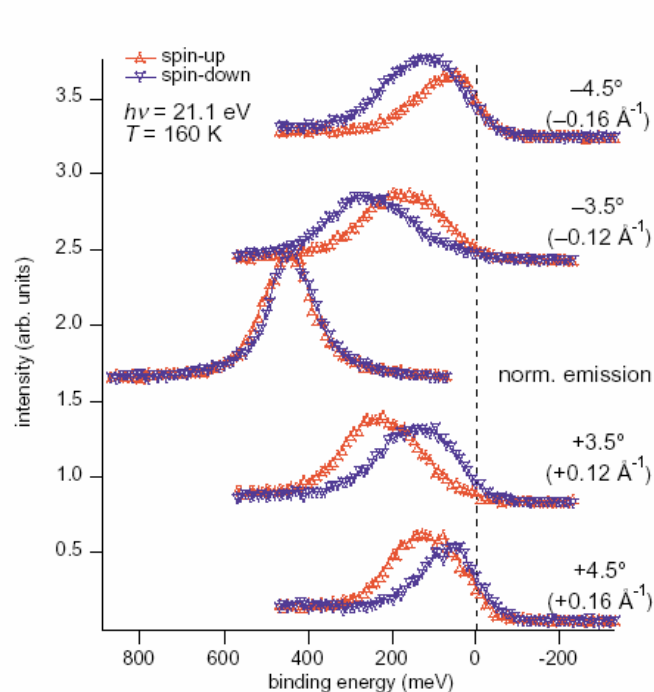
Theory: spin-orbit coupling

$$H_{SOC} = \frac{\mu_B}{2c^2} (\vec{v} \times \vec{E}) \cdot \vec{\sigma}$$

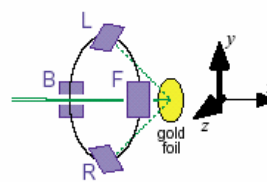
$$E^{\uparrow\downarrow}(k) = E_0 + \frac{(k \pm k_0)^2}{2m^*}$$



# Spin-resolved spectra of the surface state on Au(111)



instrumental resolution  
 $\Delta E = 120$  meV,  $\Delta\theta = 1.8^\circ$  (FWHM)



Mott scattering spin detector

$$\text{asymmetry } A = \frac{(N_L - \eta N_R)}{(N_L + \eta N_R)}$$

$$\text{electron polarization } P = \frac{A}{S}$$

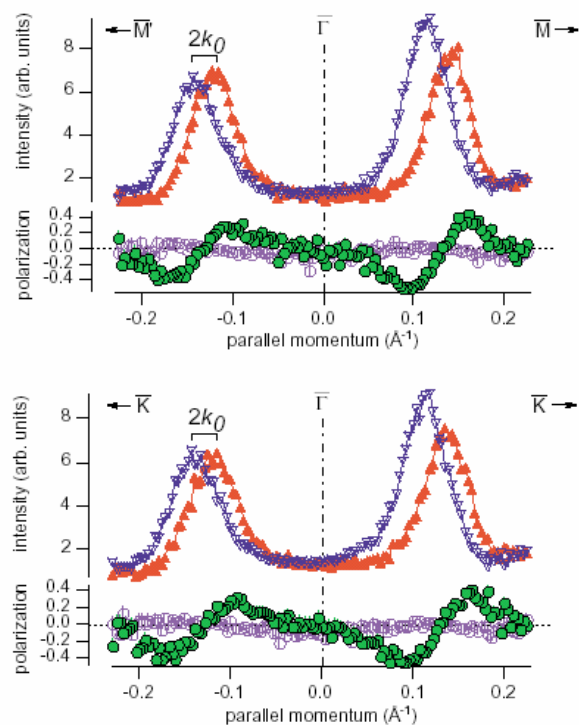
$$\text{Intensities } I^{\pm} = I_0 \cdot (1 \pm P)$$

parameters for analysis:

$\eta$  = Correction of detection efficiency (instrumental asymmetry)

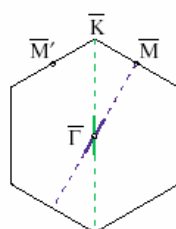
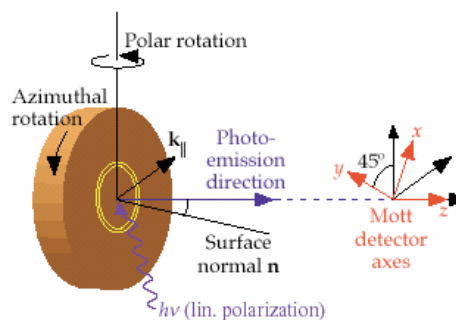
$S$  = "Sherman function" (analyzing power)

# Spin-resolved momentum distribution curves of the surface state on Au(111)



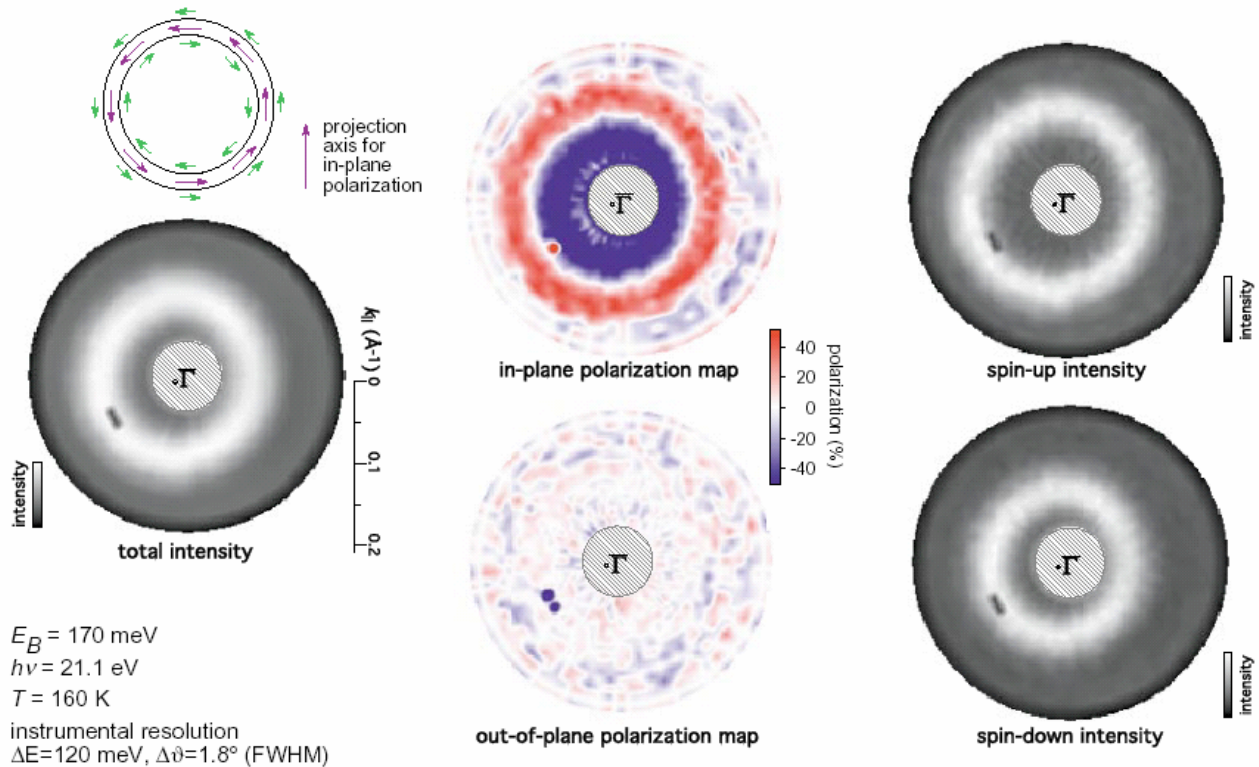
instrumental resolution  
 $\Delta E = 120$  meV,  $\Delta\theta = 1.8^\circ$  (FWHM)

- ▲ spin-up intensity
  - ▼ spin-down intensity
  - in-plane polarization
  - out-of-plane polarization
- $E_B = 170$  meV  
 $h\nu = 21.1$  eV  
 $T = 160$  K



Surface Brillouin zone

## Spin-resolved momentum distribution map of the surface state on Au(111)



=> First spin-resolved "Fermi surface" map

Valence Bands - Lecture 3

## Ultrathin Films of Ni on Cu(001)



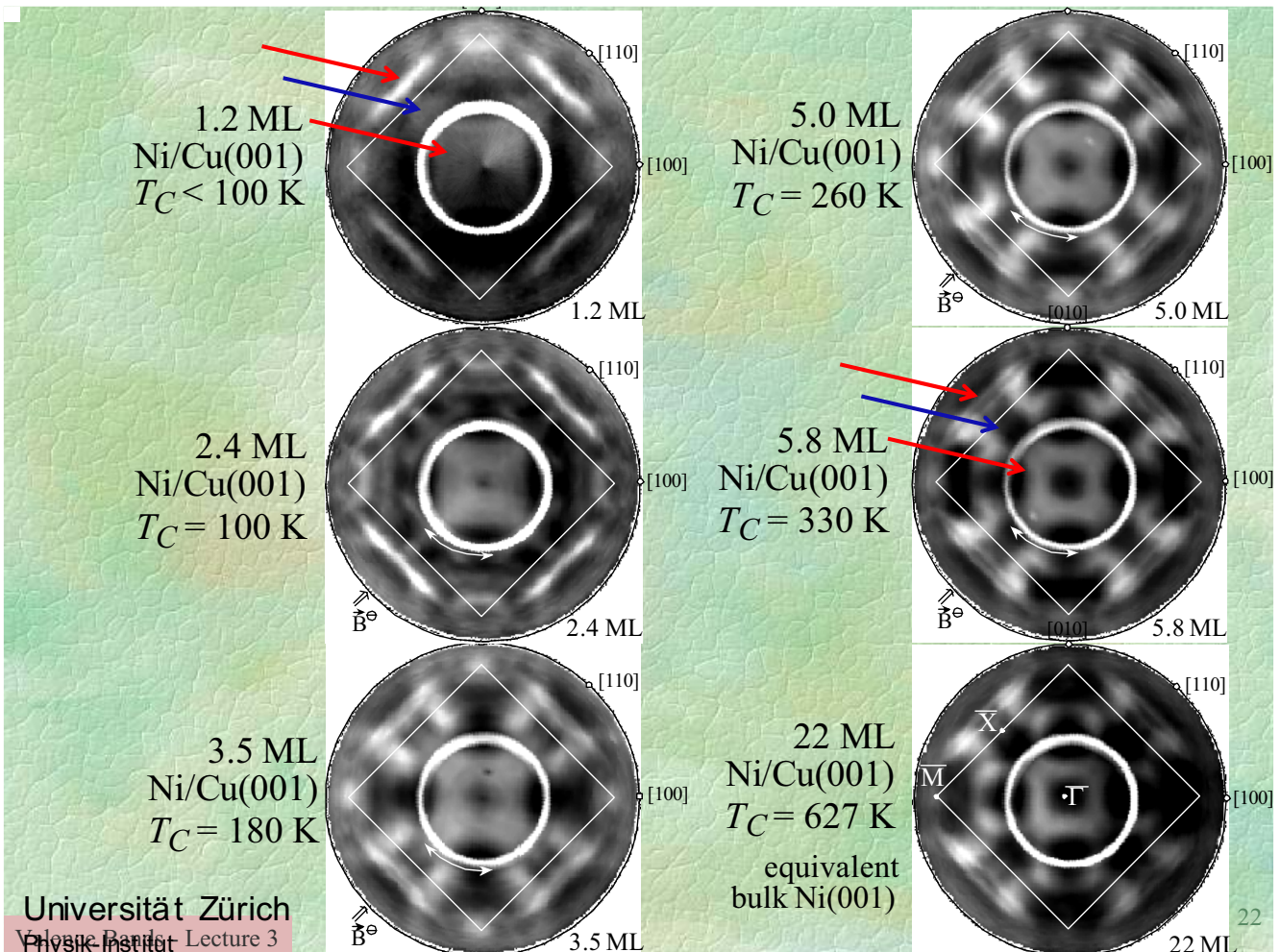
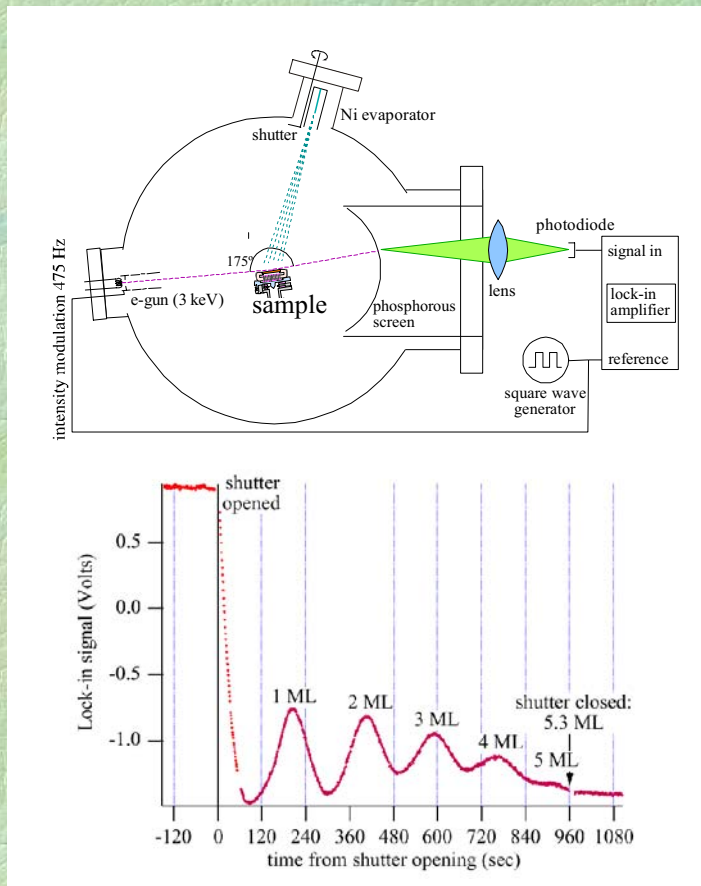
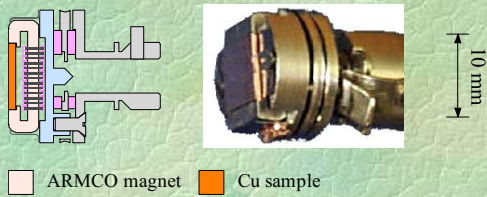
- grows epitaxially
- well ordered films
- $T_c$  depends on film thickness
- bulk-like Fermi surface already at 1 ML (G. J. Mankey et al., PRL 78, 1146 (1997))
- Full 3d magnetic moment reached only at 6 ML (P. Srivastava et al., PRB 56, R4398 (1997))

# Preparation of Monolayer Films of Ni on Cu(001)

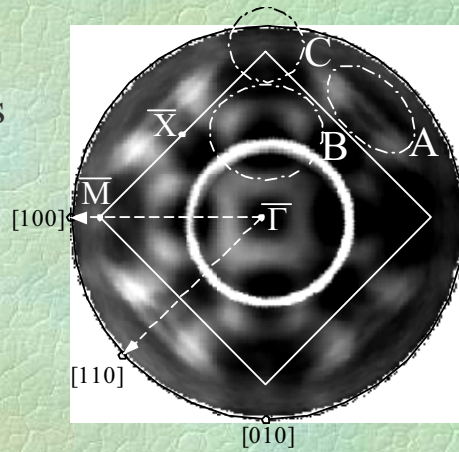
Ni deposited from e-beam heated rod at 0.33 ML/min. onto clean Cu(001)

Annealing to 420 K.

Cooling to 150 K (liquid N<sub>2</sub>).



Band Character of  
Fermi Surface Contours  
(thick film ~ bulk-like)

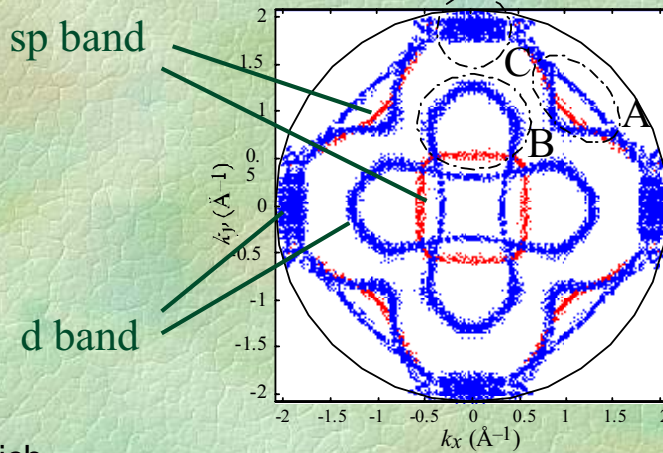


data from  
22 ML  
Ni/Cu(001)  
 $h\nu = 21.22$  eV  
equivalent  
bulk Ni(001)

Fermi surface  
calculation

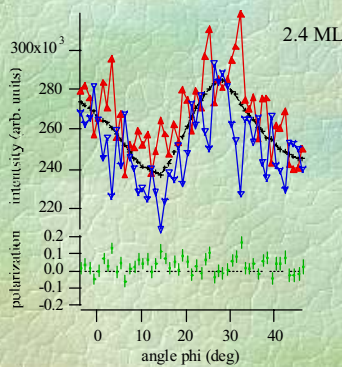
free electron  
final state  
approximation

$h\nu = 21.22$  eV  
 $\Phi = 5.2$  eV  
 $V_0 = 10.2$  eV

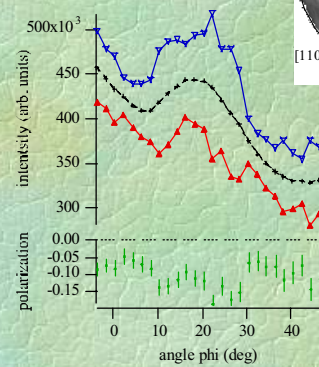


Ni/Cu(001) azimuthal scans at  $E_F$ ,  $\vartheta = 28^\circ$ ,  
 $h\nu = 21.22$  eV,  $T = 150$  K

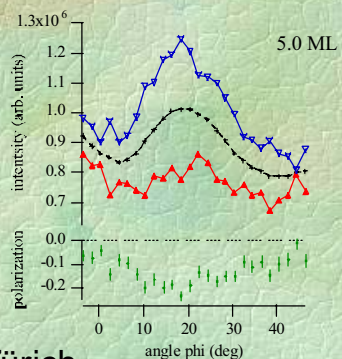
2.4 ML  
Ni/Cu(001)  
 $T_C = 100$  K



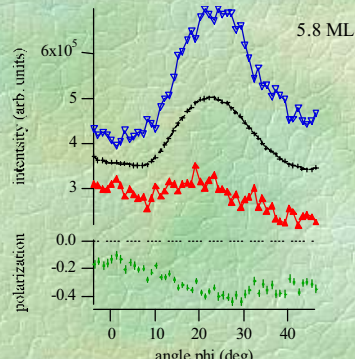
3.5 ML  
Ni/Cu(001)  
 $T_C = 180$  K



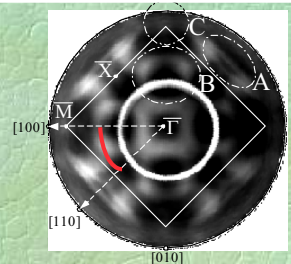
5.0 ML  
Ni/Cu(001)  
 $T_C = 260$  K



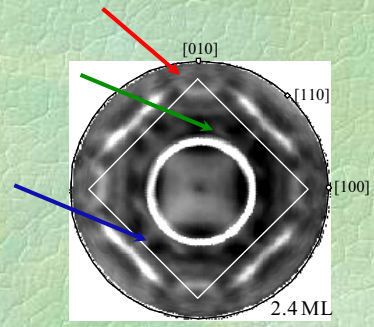
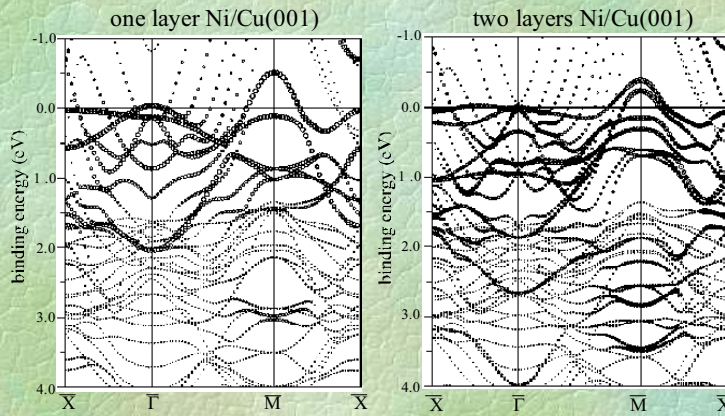
5.8 ML  
Ni/Cu(001)  
 $T_C = 330$  K



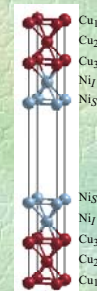
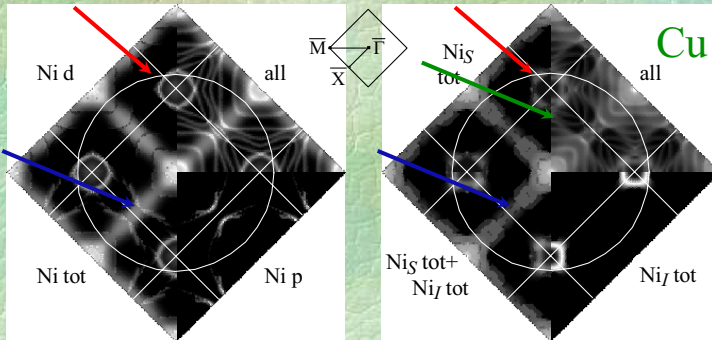
d band



# Ni/Cu(001) Slab Calculations



data from  
2.4 ML Ni/Cu(001)  
 $h\nu = 21.22$  eV

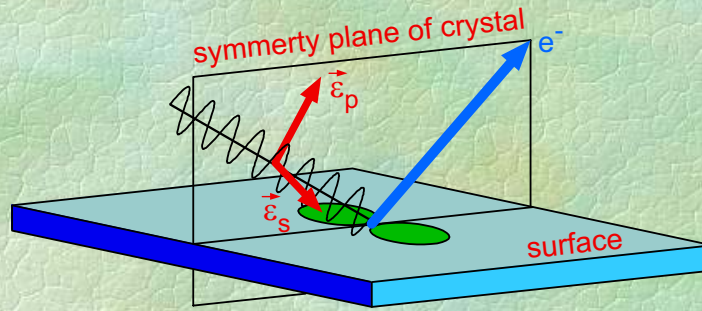


1 ML Ni/5 ML Cu/1 ML Ni    2 ML Ni/5 ML Cu/2 ML Ni

# Ultrathin films of Ni on Cu(001)

- ∞ < 3 ML: paramagnetic interface band structure
- ∞ Around 3 ML two things happen:
  - $T_c > T_{meas} \Rightarrow$  Exchange splitting appears
  - Band structure becomes bulk-like (3D)
- ∞ The sp bands are bulk-like already at ~1 ML
- ∞ The d bands form interface states for < 3 ML

# Intensities in Valence Photoemission - Symmetry Effects



$\vec{\epsilon}_p$  photon polarization in...  
 $\vec{\epsilon}_s$  ...perpendicular ("senkrecht") to...scattering plane

photoemission matrix element:

$$| \langle \phi_{f,kin} | \vec{r}_k \cdot \vec{\epsilon} | \phi_{i,k}(\vec{r}_k) \rangle |^2 \rightarrow \text{Intensity}$$

mirror reflection symmetries:

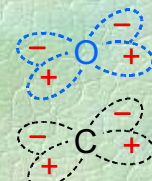
p - pol.	+1	+1	-1	0
	+1	+1	+1	max.
s - pol.	+1	-1	-1	max.
	+1	-1	+1	0

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## CO Molecular Orbitals



$4\sigma$

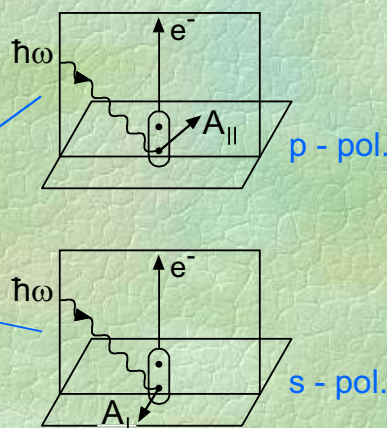
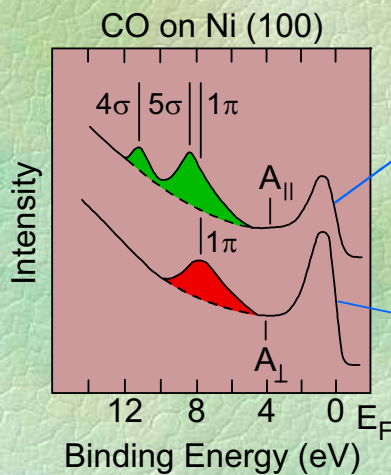
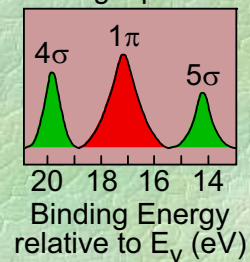


$1\pi$



$5\sigma$

CO gasphase



from Hüfner

28

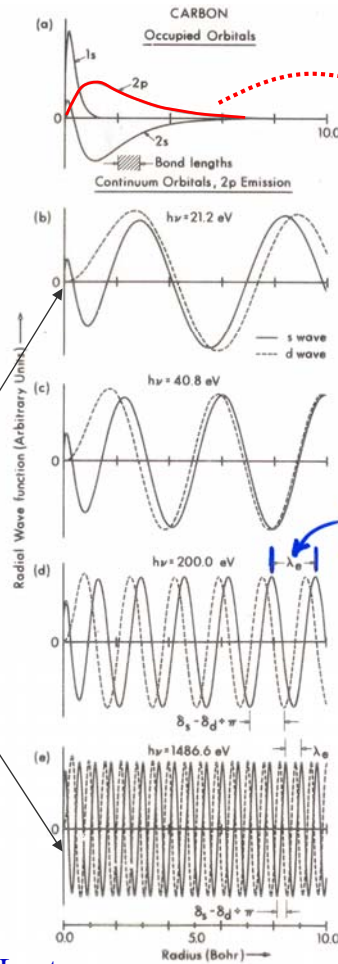
Intensities in  
Valence Photoemission  
- Atomic Effects

$$m_{i,f} \sim \langle \phi_{f,kin} | \vec{r} \cdot \vec{\epsilon} | \phi_{i,k} \rangle$$

as for core levels

**RADIAL MATRIX ELEMENTS TO  $\pm 1 = s$  and  $d$  CHANNELS:**

... for various energies



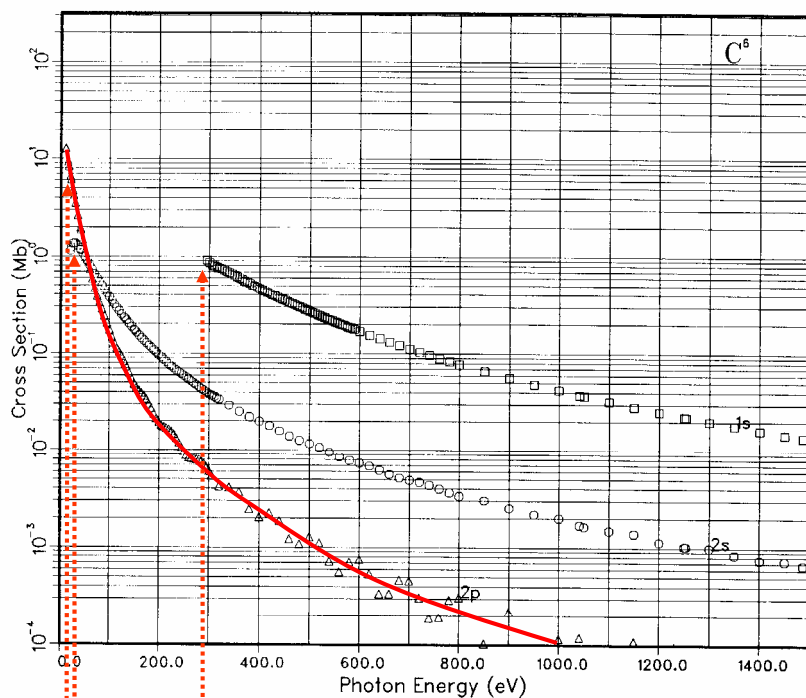
DE BRAGLIE WAVELENGTH =  $\frac{h}{p} = \frac{2\pi}{k}$

PHASE SHIFT DIFFERENCE

Plus other  
Examples  
from Yeh and  
Lindau  
in Sec. 1.5 of  
X-Ray Data  
Booklet, and  
plots for all  
elements at:  
[http://  
ulisse.elettra.  
trieste.it/  
elements/  
WebElements.  
html](http://ulisse.elettra.trieste.it/elements/WebElements.html)

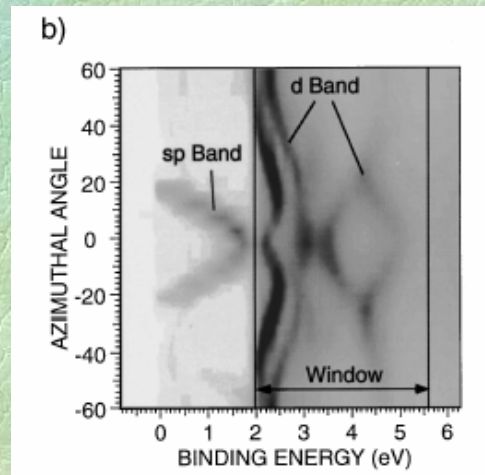
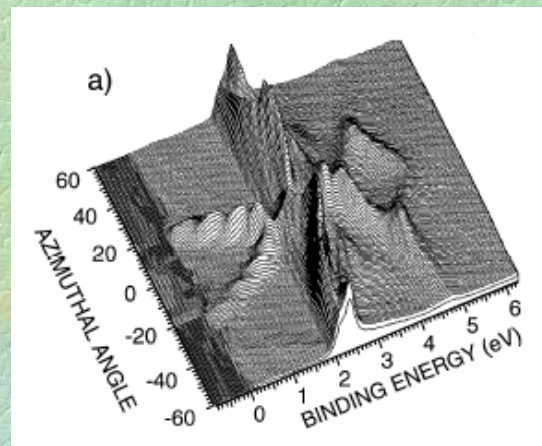
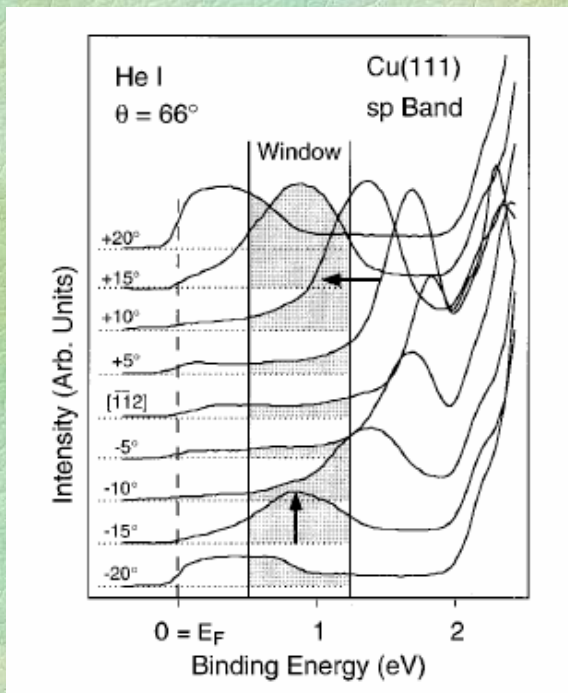
From C. S. Fadley's Lectures

GRAPH 1. Atomic Subshell Photoionization Cross Sections for 0-1500 eV,  $1 \leq Z \leq 103$   
See page 6 for Explanation of Graphs



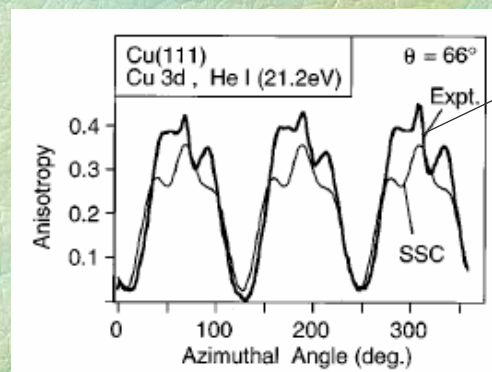
C binding energies(eV) are:  
1s( 2) 290.860    2s( 2) 17.5409    2p( 2) 8.98202

# Intensities in Valence Photoemission - Diffraction Effects



## Integration of Intensities over the Entire d-Band Region

Choose energy window large enough so the d-band peak never leaves the window => the intensity variation of the peaks can be monitored

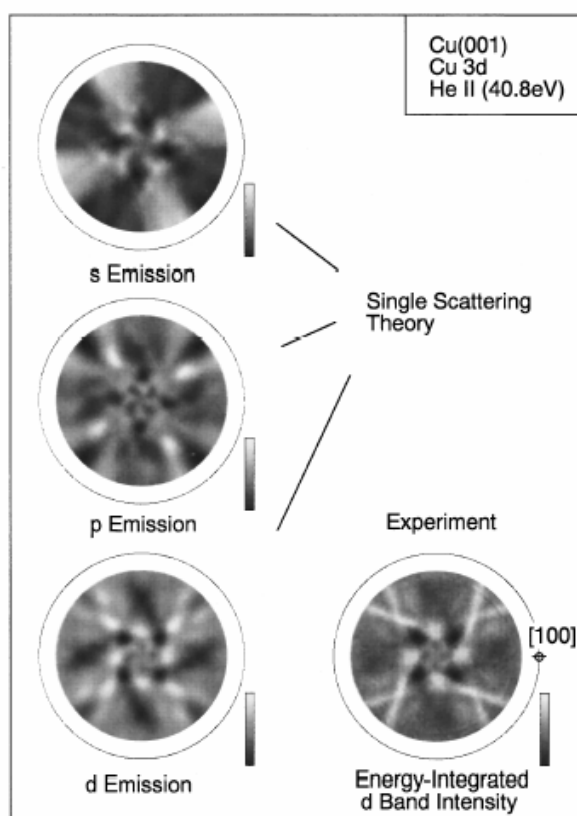
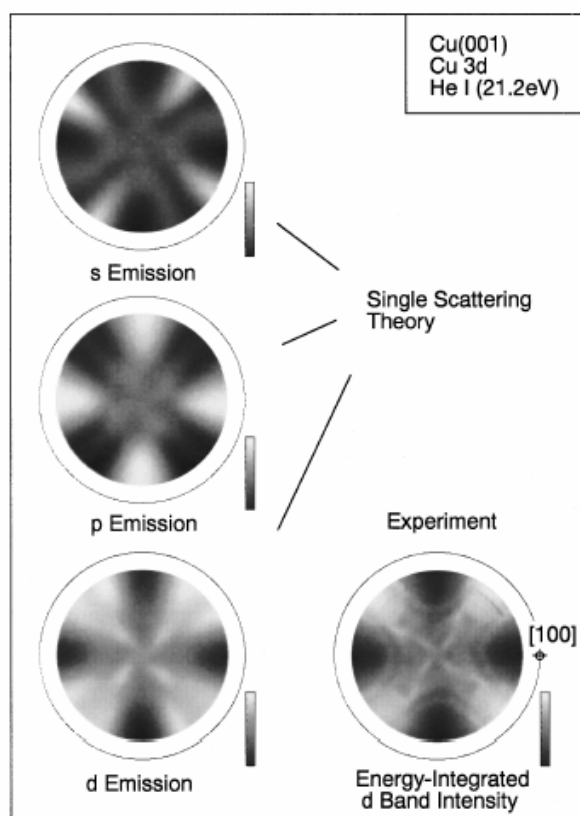
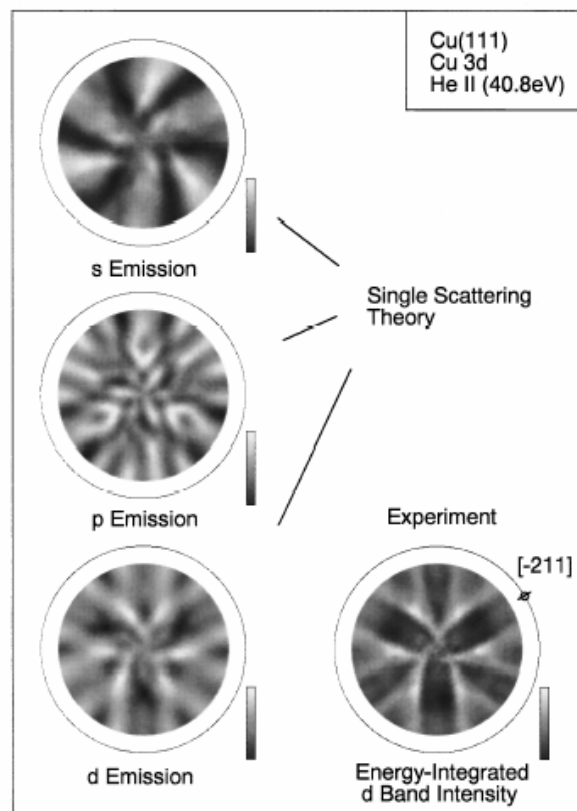
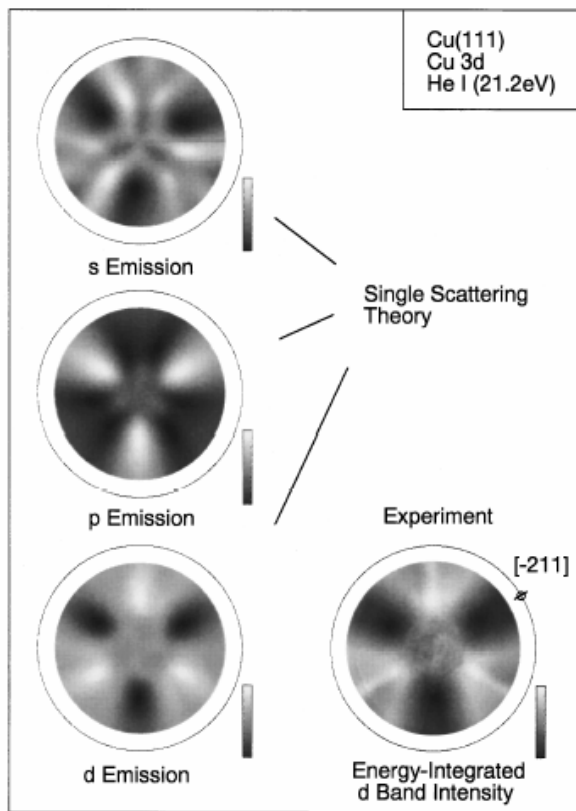


Theoretical curve: Single Scattering Cluster (SSC) calculation for a cluster representing a Cu(111) surface from a localized full d shell (like in x-ray photoelectron diffraction (XPD), hence

ultraviolet photoelectron diffraction (UPD)

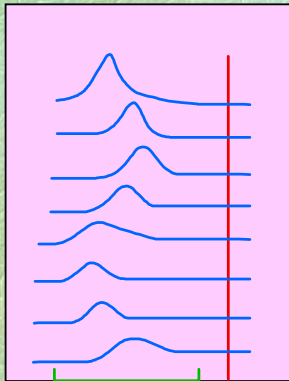
J. Osterwalder et al., PRB 53, 10209 (1996)



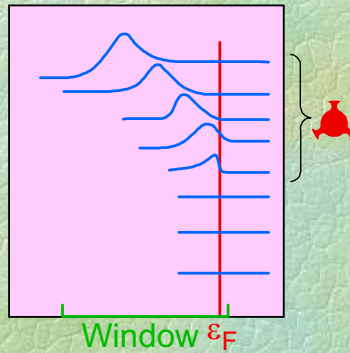


# UPD and Photoemission Intensities

filled shells:



unfilled shells: ?



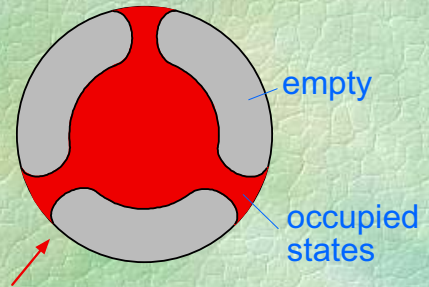
direct transition never disperses out of measurement window (e.g. Cu 3d).



UPD describes overall band intensities !

(sum rule over several subbands)

direct transition is lost at Fermi surface.



But: Must know angular momentum compos. of occupied (crystal field) states !

UPD may describe intens. in occupied k-Region